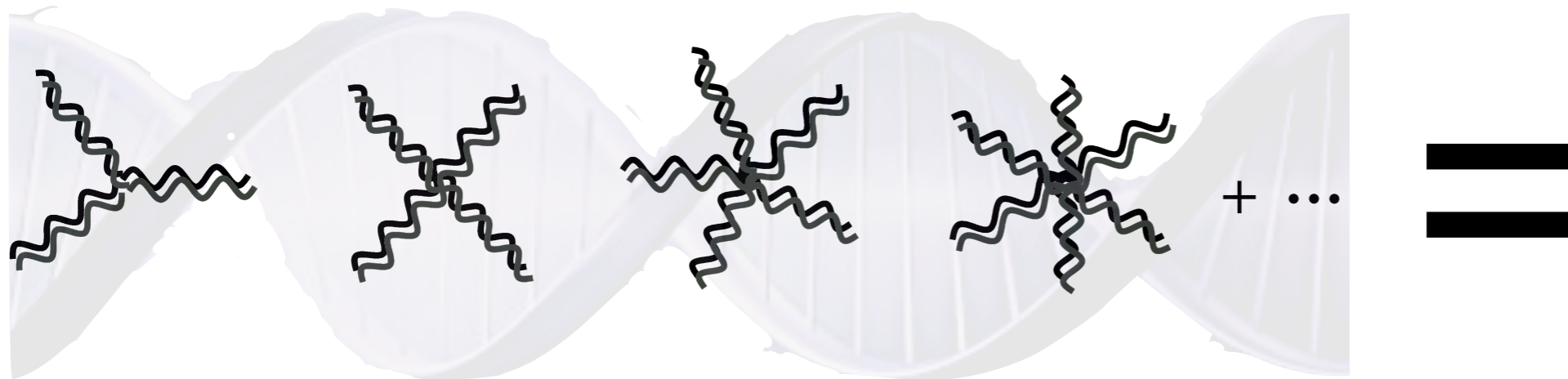
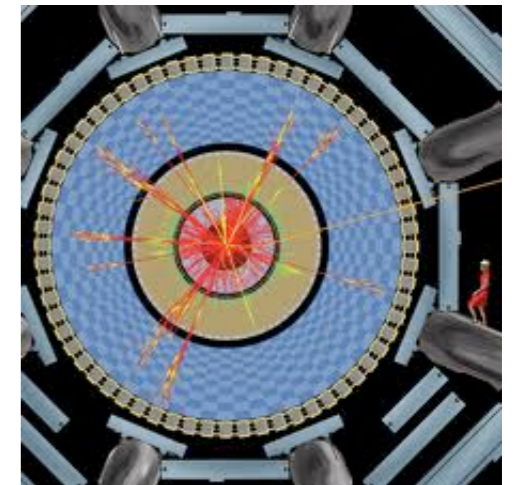
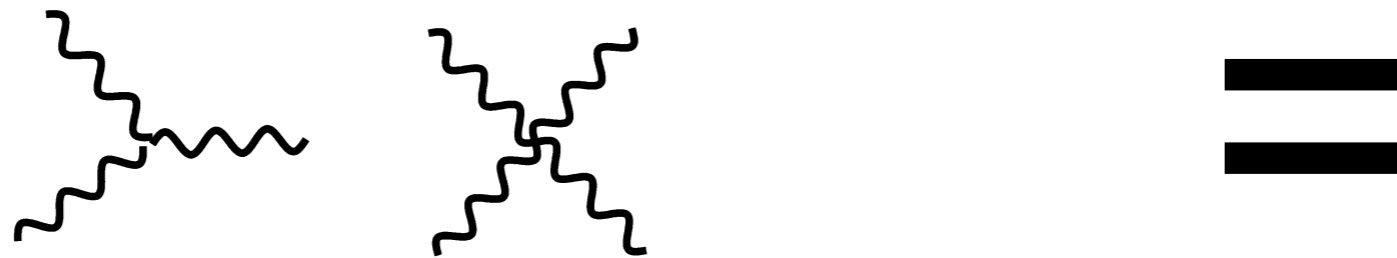


# UV Structure from Double Copy in Effective Field Theory

ICHEP, 20 July 2024



Based on work with Matt Lewandowski and Nic Pavao

Northwestern  
University

Amplitudes &  
Insights

*John Joseph M Carrasco*

Where I'm going:

Mixed HD duality between color and kinematics  
+ factorization consistency induces a TOWER of EFT  
operators to the UV

In case of  $F^3 + \text{YM}$ , double copy lands on so called  
“twisted” string theory amplitudes — with HD freedom  
that lands on e.g. open, closed, heterotic

This has implications for UV completions of N=4 SG

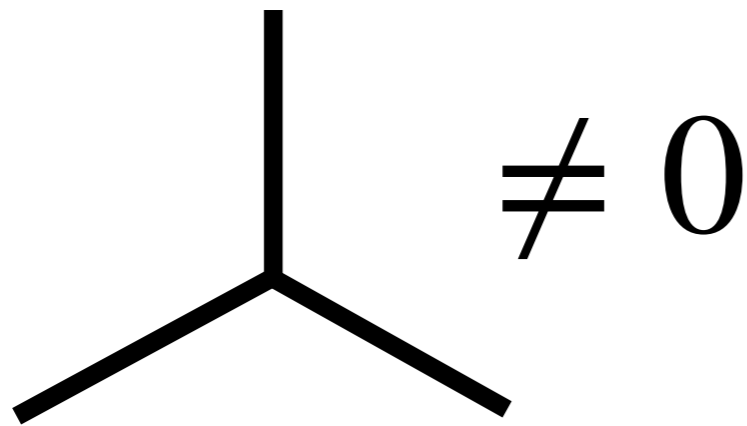
This has applications to inflationary cosmology

Can be easily exploited for bootstrapping encoding of  
massive resonances.

# Intuition around color-dual and operator constraints:

color-dual kinematics = linearized gauge-invariance

$$\mathcal{L} = (\partial A)^2 + g_1 A^2 (\partial A)$$



Given:

$$k_i \cdot k_j = 0 \quad k_i \cdot \varepsilon_i = 0$$

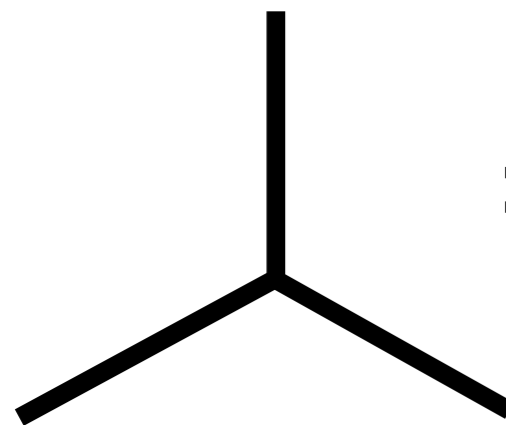
Kinematic building blocks:

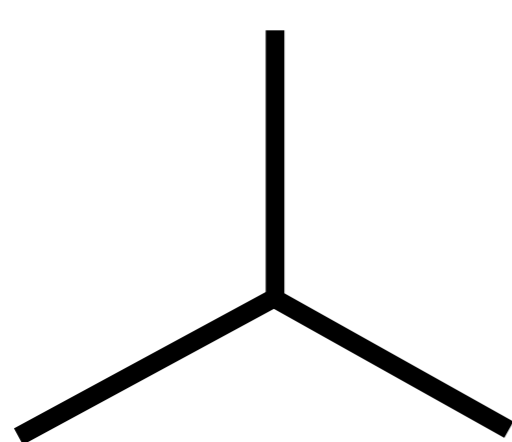
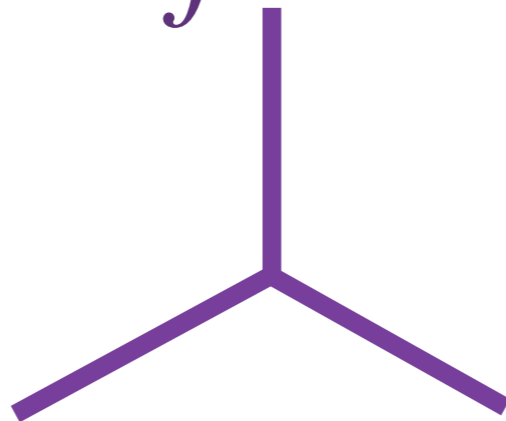
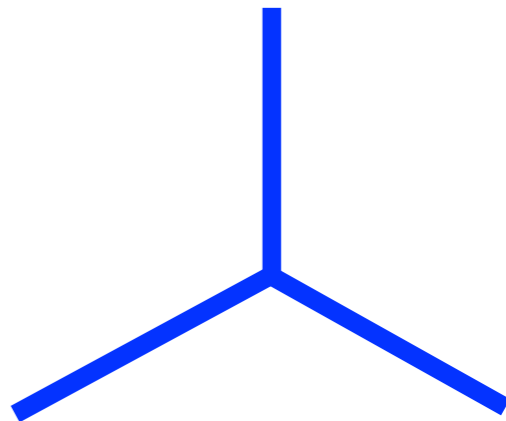
$$\varepsilon_i \cdot \varepsilon_j \quad k_i \cdot \varepsilon_j$$

# Intuition around color-dual and operator constraints:

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$$\mathcal{L} = (\partial A)^2 + g_1 A^2 (\partial A)$$

 $\neq 0$  $\iff$  Fixed by Bose Symmetry

 $=$  $\times$  $(\varepsilon_1 \cdot \varepsilon_2)(k_1 - k_2) \cdot \varepsilon_3 + \dots$

# Intuition around color-dual and operator constraints:

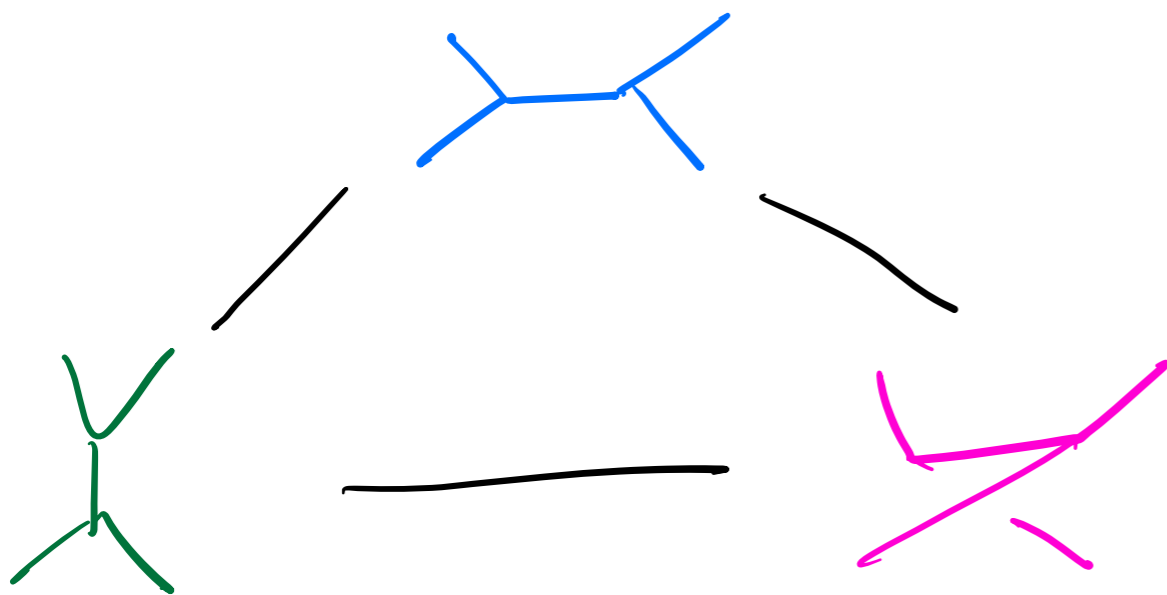
color-dual kinematics = linearized gauge-invariance

$$\mathcal{L} = (\partial A)^2 + g_1 A^2 (\partial A) + g_2 A^4$$

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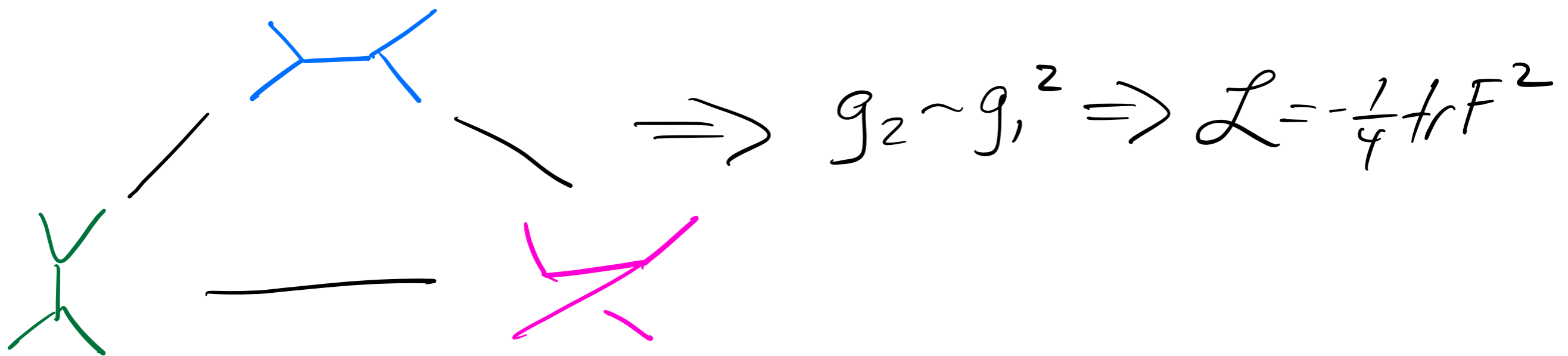
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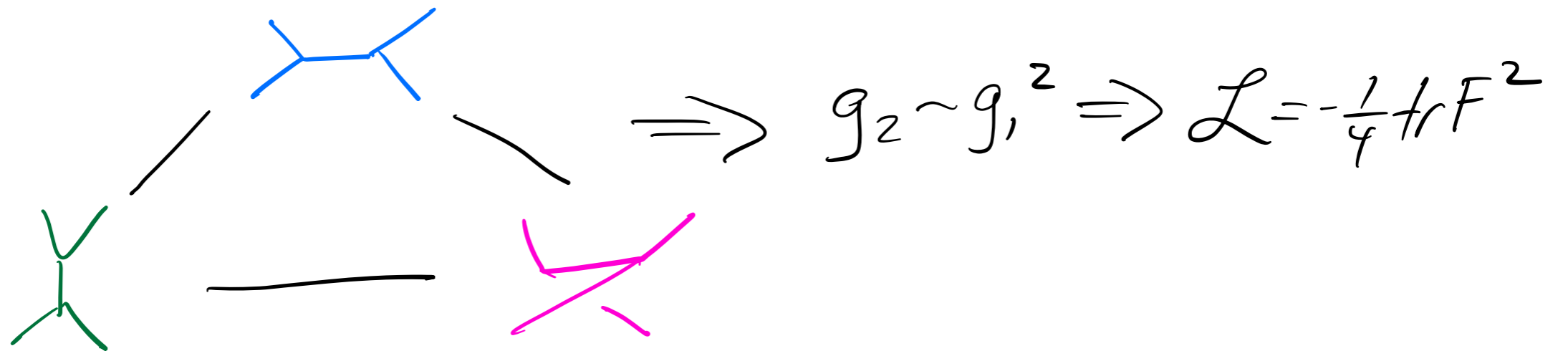
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color-dual kinematics + DC = linear diffeo inv.

$$M_5^{\text{GR}} = \sum \frac{n(\text{H}) n(\text{H})}{dg}$$



**Intuition around color-dual and operator constraints:**  
 color-dual kinematics + DC = linear diffeo inv.

$$M_5^{GR} = \sum \frac{n(\text{H})n(\text{H})}{dg}$$

$$n(\text{H}) = \text{H} + S_{45} \text{H} + S_{12} \text{H}$$

$\Rightarrow$

$$n(\text{H})^2 = \text{H} + S_{12} \text{H} + S_{45} \text{H} + S_{12} S_{45} \text{H}$$

$$+ S_{45} \text{H} + S_{12} S_{45} \text{H}$$

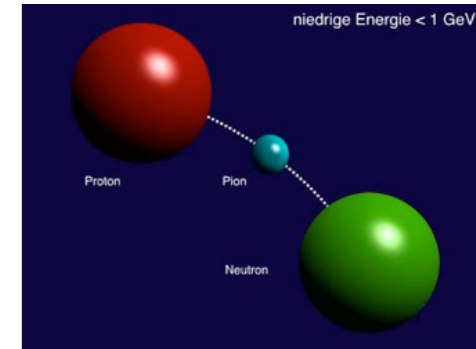
# Intuition around color-dual and operator constraints:

color-dual kinematics = soft bootstrap

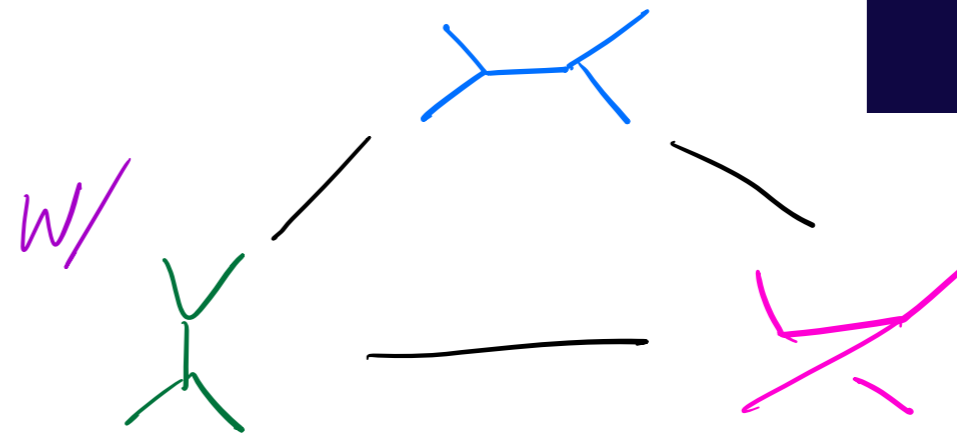
$$\mathcal{L} = (\partial\pi)^2 \sum_{k=0} c_k \pi^{2k}$$

# Intuition around color-dual and operator constraints:

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$$\mathcal{L} = (\partial\pi)^2 \sum_{k=0} c_k \pi^{2k}$$



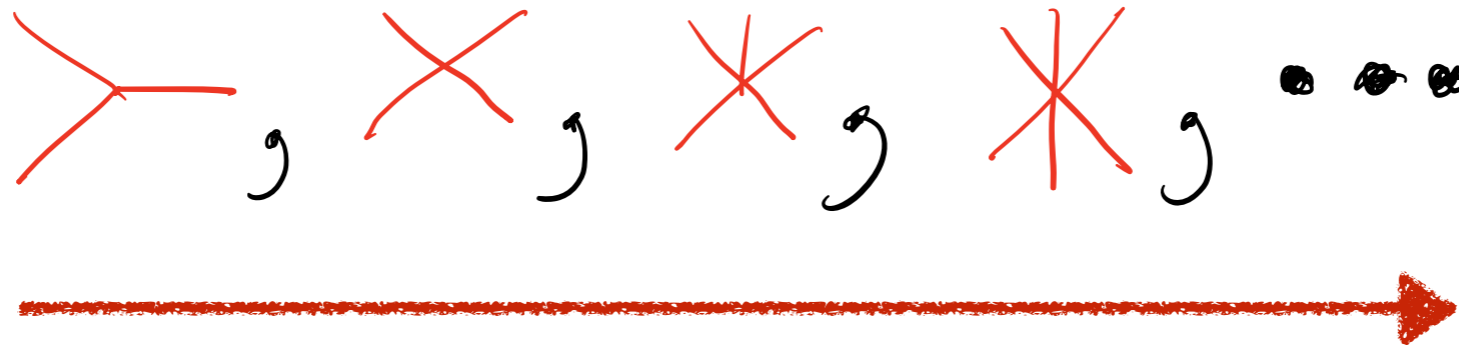
Resums to NLSM:

$$\mathcal{L}^{\text{NLSM}} = \times + * + \dots$$

$$\mathcal{L}^{\text{NLSM}} = (\partial U)^\dagger (\partial U) \quad U = e^{i\pi}$$

# Intuition around color-dual and operator constraints:

Color/kinematics fixes out...

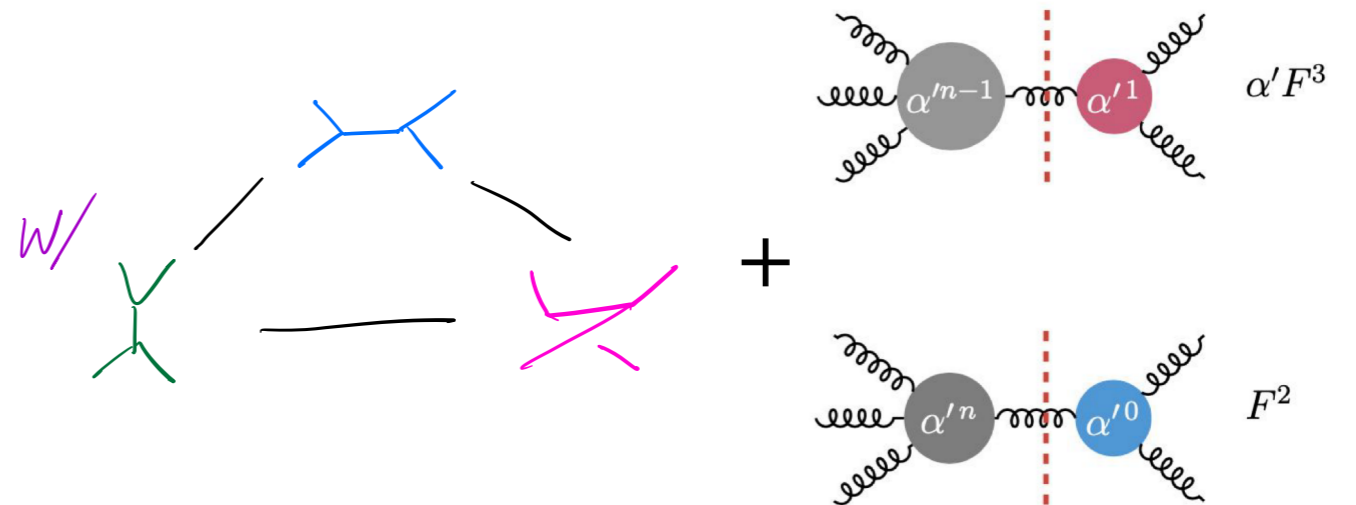


# **New story in the UV!**

# New story in the UV!

Color/Kinematics + EFT (mixed HD contacts)  
constraints **UP!**

$$\mathcal{L}^{YM+F^3} = -\frac{1}{4}F^2 + \frac{\alpha'}{3}F^3 + \alpha'^2 F^4 + \alpha'^2 \sum_n c_{(n)} \alpha'^n D^{2n} F^4$$

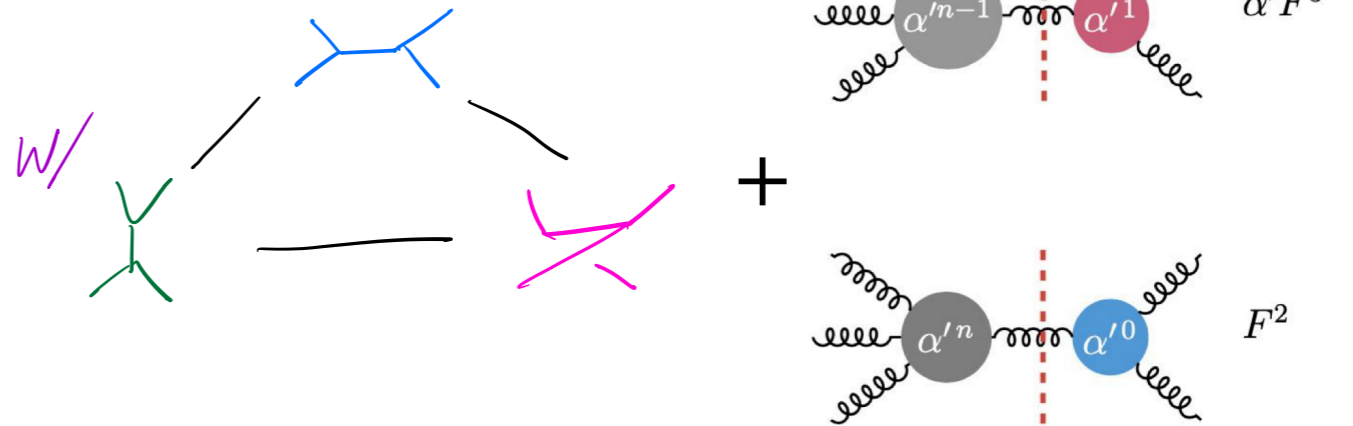


$$\mathcal{L}^{DF^2+YM+HD}$$

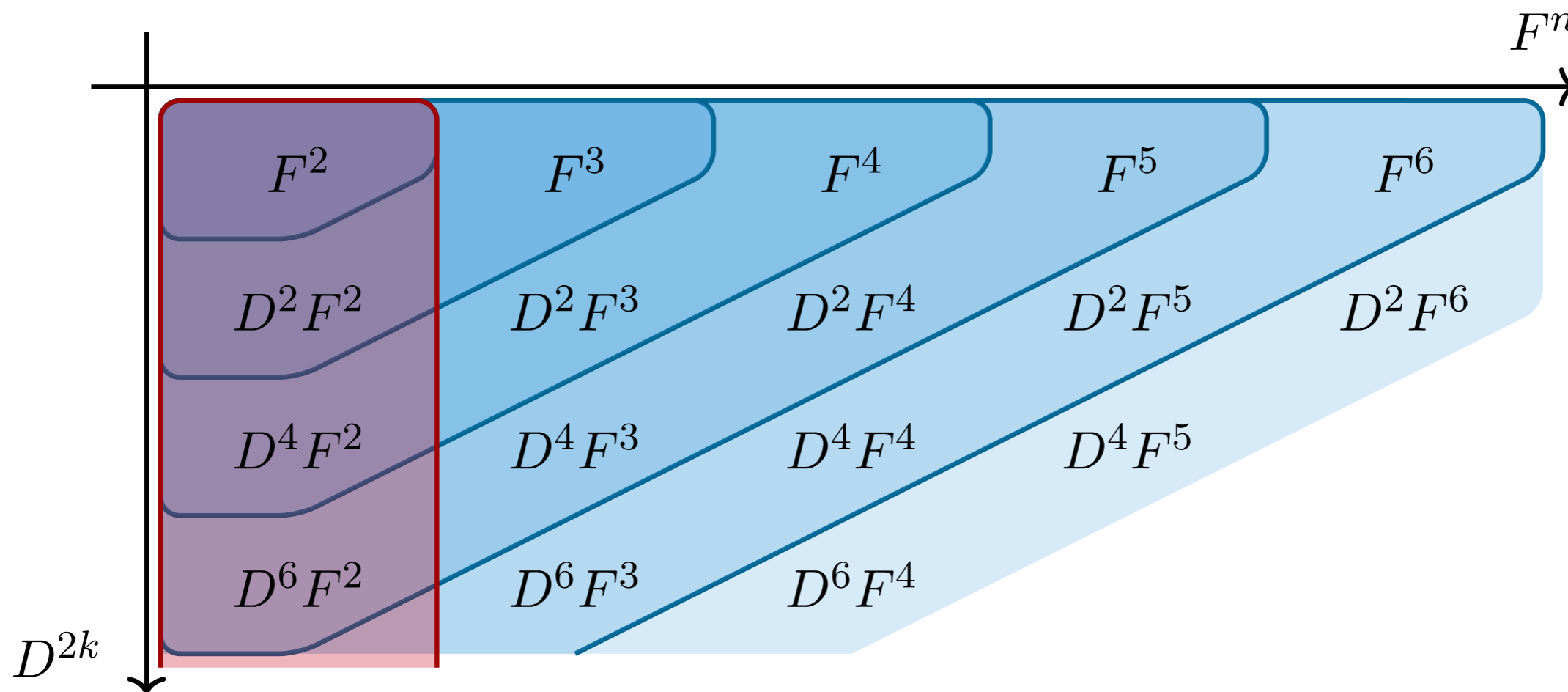
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# Color-dual consistency and EFT





# Natural encoding of massive resonances in a bootstrapped tower of color-dual HD operators

$$\mathcal{A} = \sum_g \frac{c_g n_g}{d_g - m_g^2} \quad \longrightarrow \quad \mathcal{M} = \sum_g \frac{\tilde{n}_g n_g}{d_g - m_g^2}$$

VS

$$\mathcal{A}^{\text{UV}} = \sum_g \frac{c_g N_g}{d_g} \quad \longrightarrow \quad \mathcal{M}^{\text{UV}} = \sum_g \frac{\tilde{n}_g N_g}{d_g}$$

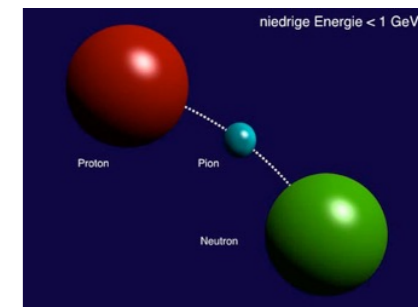
$$N_g = n_g + \sum_k c_k (\alpha')^k n_g^{(k)}$$

From Masses to Wilson Coefficients:

$$\begin{aligned} A_4^{\text{UV}} &= A_4^{\text{IR}} \times \prod_{k=1}^{\infty} \frac{P_k(\sigma_2, \sigma_3)}{(s - \mu_k)(t - \mu_k)(u - \mu_k)} \\ &= A_4^{\text{IR}} \times \prod_{k=1}^{\infty} \exp [c_k \Omega_k(\sigma_2, \sigma_3)] \end{aligned}$$

# From Wilson Coefficients to Masses?

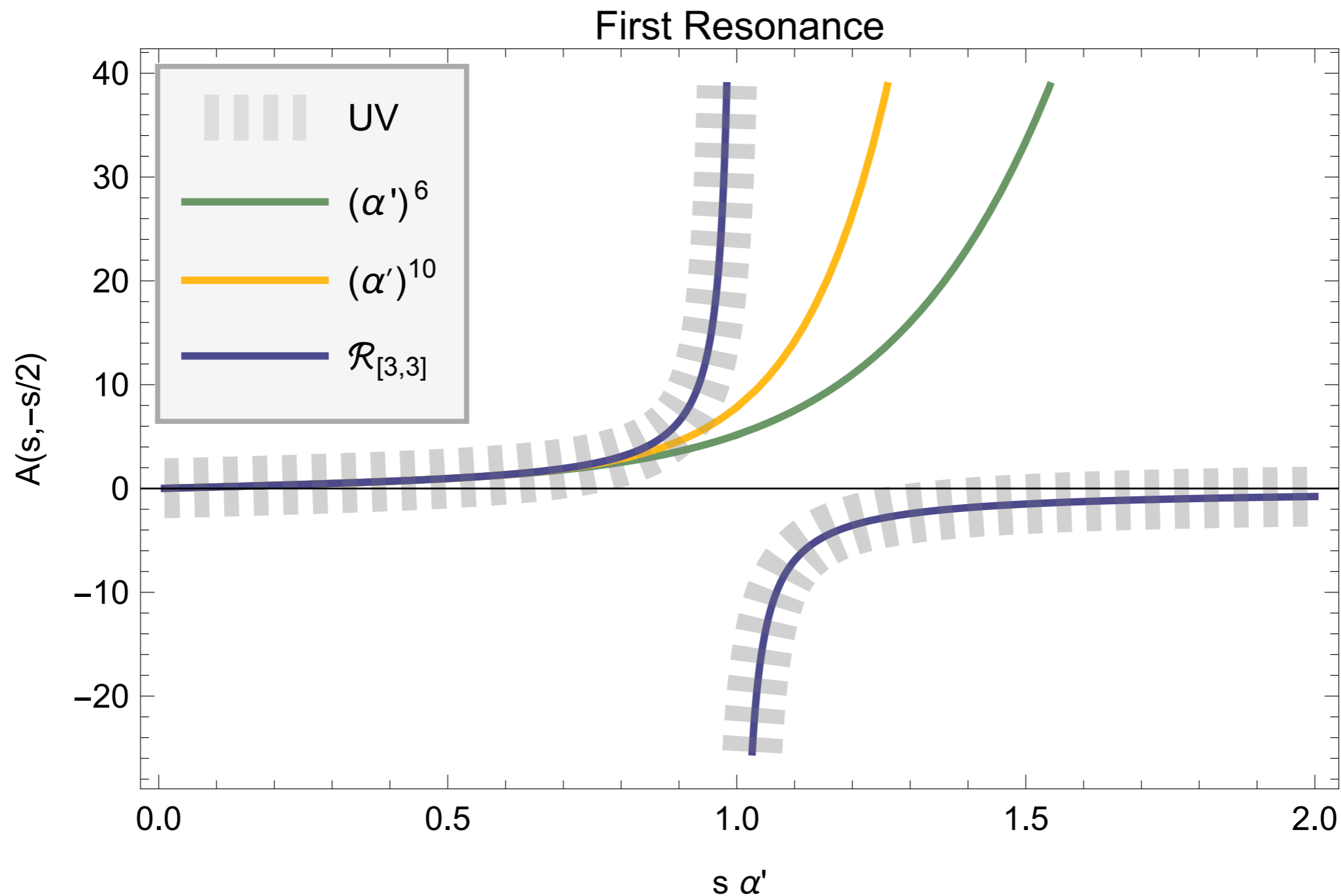
$$\mathcal{A}_{\text{IR}} = f^{a_1 a_2 b} f^{b a_3 a_4} (s_{23} - s_{13}) + f^{a_4 a_1 b} f^{b a_2 a_3} (s_{12} - s_{13}) + f^{a_3 a_1 b} f^{b a_4 a_2} (s_{23} - s_{12})$$



$$M^{2\text{-mode}} = \frac{1 \times 10^3}{(s\alpha' - 1)(t\alpha' - 1)(u\alpha' - 1)(s\alpha' - 10)(t\alpha' - 10)(u\alpha' - 10)}.$$

Consider e.g. 10 Wilson Coefficients w/ fixed precision

$$\begin{aligned} \mathcal{A} = \mathcal{A}^{\text{IR}} \times [ & 1.000 + 1.010(\alpha')^2 \sigma_2 + 1.001(\alpha')^3 \sigma_3 + 1.010(\alpha')^4 \sigma_2^2 + 2.01(\alpha')^5 \sigma_2 \sigma_3 \\ & + (\alpha')^6 (1.010 \sigma_2^3 + 1.001 \sigma_3^2) + 3.02(\alpha')^7 \sigma_2^2 \sigma_3 + (\alpha')^8 (1.010 \sigma_2^4 + 3.01 \sigma_2 \sigma_3^2) \\ & + (\alpha')^9 (4.03 \sigma_2^3 \sigma_3 + 1.001 \sigma_3^3) + (\alpha')^{10} (1.01 \sigma_2^5 + 6.03 \sigma_2^2 \sigma_3^2) + \mathcal{O}(\alpha')^{11} ] . \end{aligned}$$

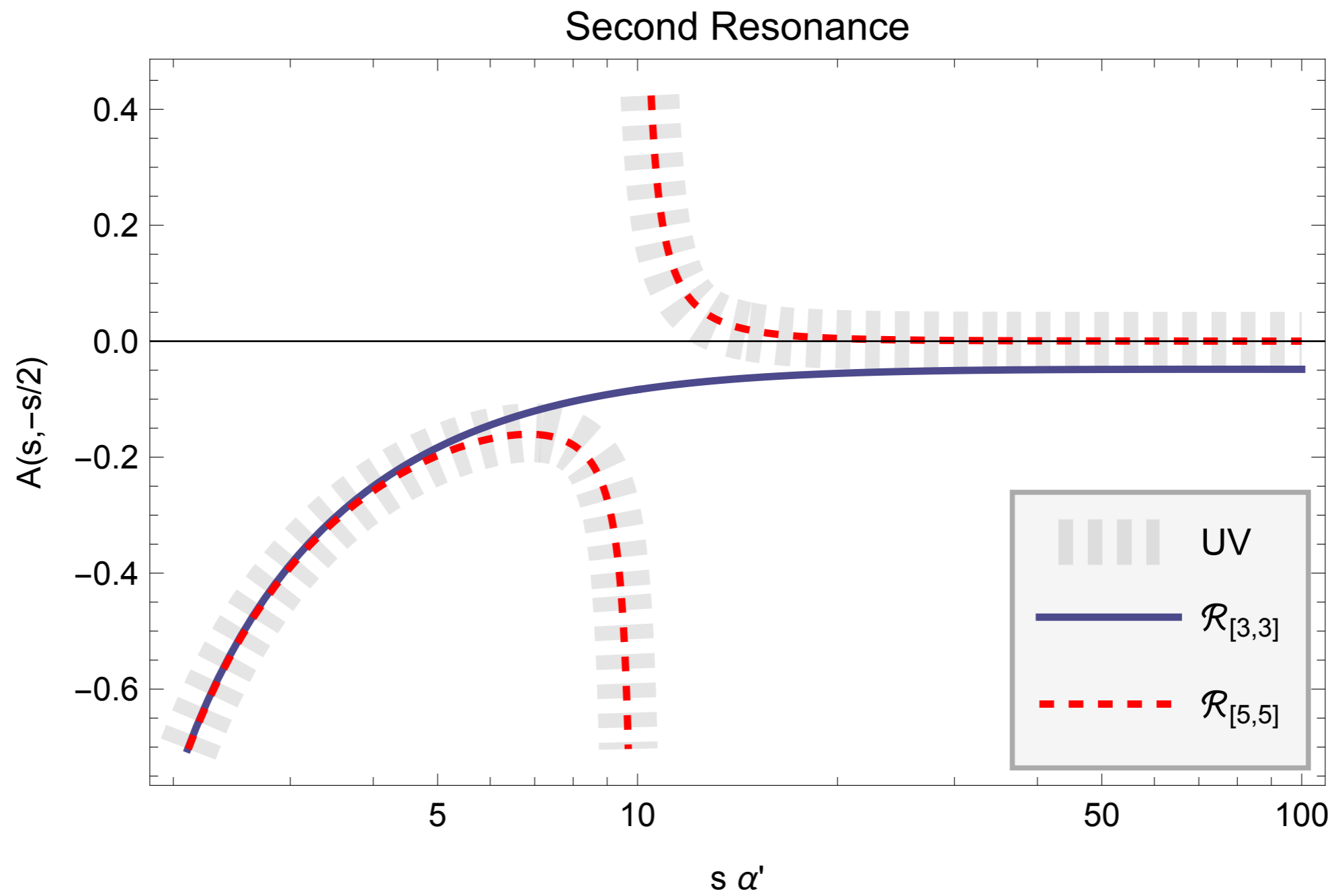


Padé approximants

$$\mathcal{R}_{[m,n]}(x) \equiv \frac{A_m(x)}{B_n(x)},$$

$$A_m(x) = \sum_{j=0}^m a_j x^j, \quad B_n(x) = 1 + \sum_{j=0}^n b_j x^j.$$

Coefficients matched by taking derivatives



## Takeaways:

Mixed HD duality between color and kinematics  
+ factorization consistency induces a TOWER of EFT  
operators to the UV

In case of  $F^3 + \text{YM}$ , double copy lands on so called  
“twisted” string theory amplitudes — with HD freedom  
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This has implications for UV completions of N=4 SG

This has applications to inflationary cosmology

Can be easily exploited for bootstrapping encoding of  
massive resonances.

Consider this talk an invitation, there are many reviews:

Snowmass White Paper: the Double Copy and its Applications, 2204.06547

-gentle overview for broad audience, nice discussion including non-flat backgrounds, classical solns, GW astrophysics, cosmological challenges

Snowmass White Paper: Gravitational Waves and Scattering Amplitudes, 2204.05194

The SAGEX review on scattering amplitudes (chapter 2), 2203.13013

-gentle introduction targeting amplitudes expertise

The Duality Between Color and Kinematics and its Applications, 1909.01358

-technical, overview of literature ~ 2019

Supergravity amplitudes, the double copy and ultraviolet behavior, 2304.07392

-focus on UV behavior of SG