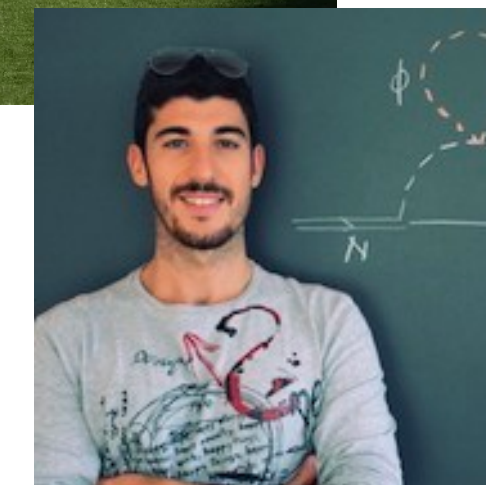


# Dark matter and reheating via dark glueballs

Helena Kolečová (University of Stavanger)

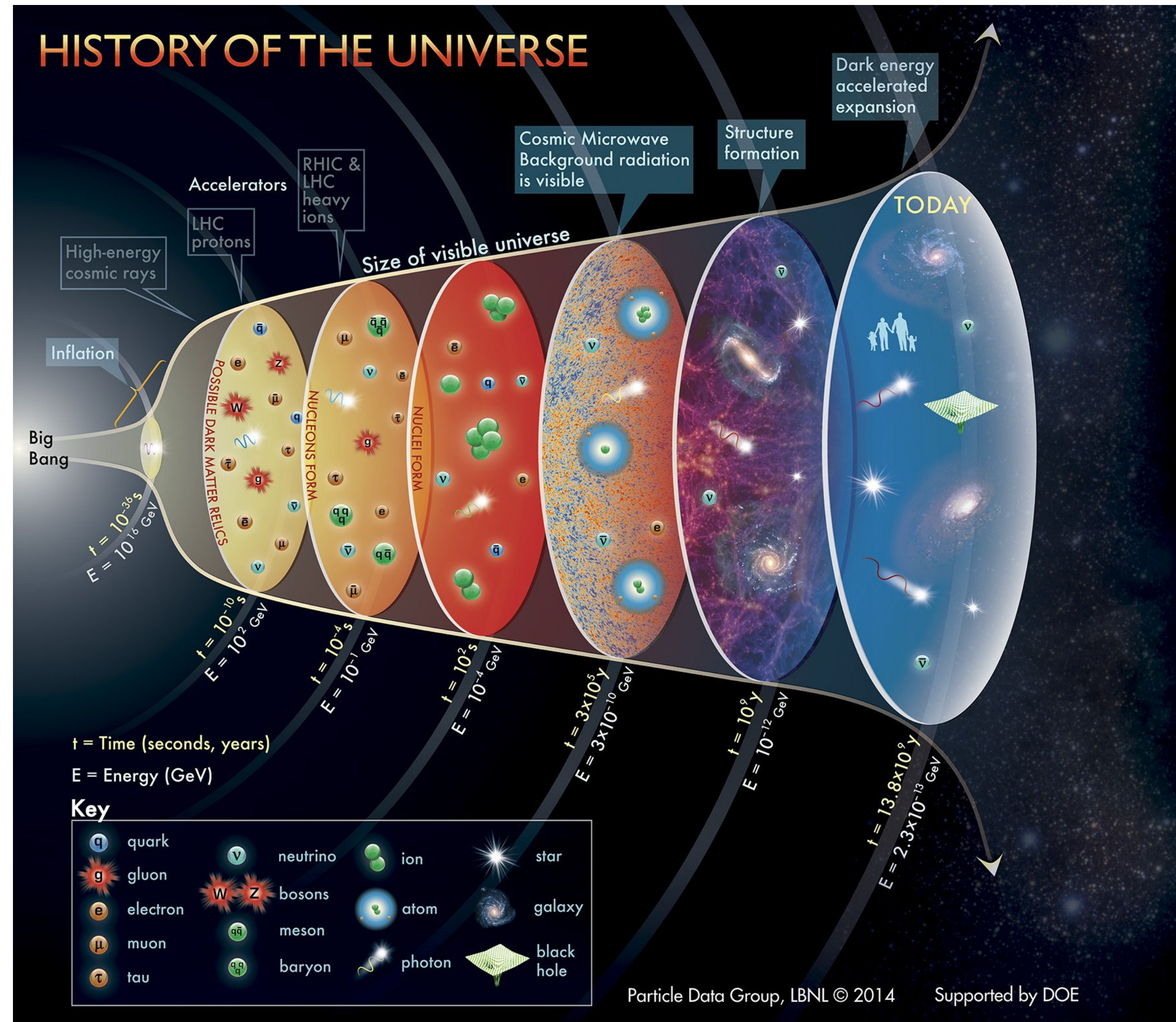


Joint work with Simone Biondini and Simona Procacci  
[arXiv: 2406.10345](https://arxiv.org/abs/2406.10345)

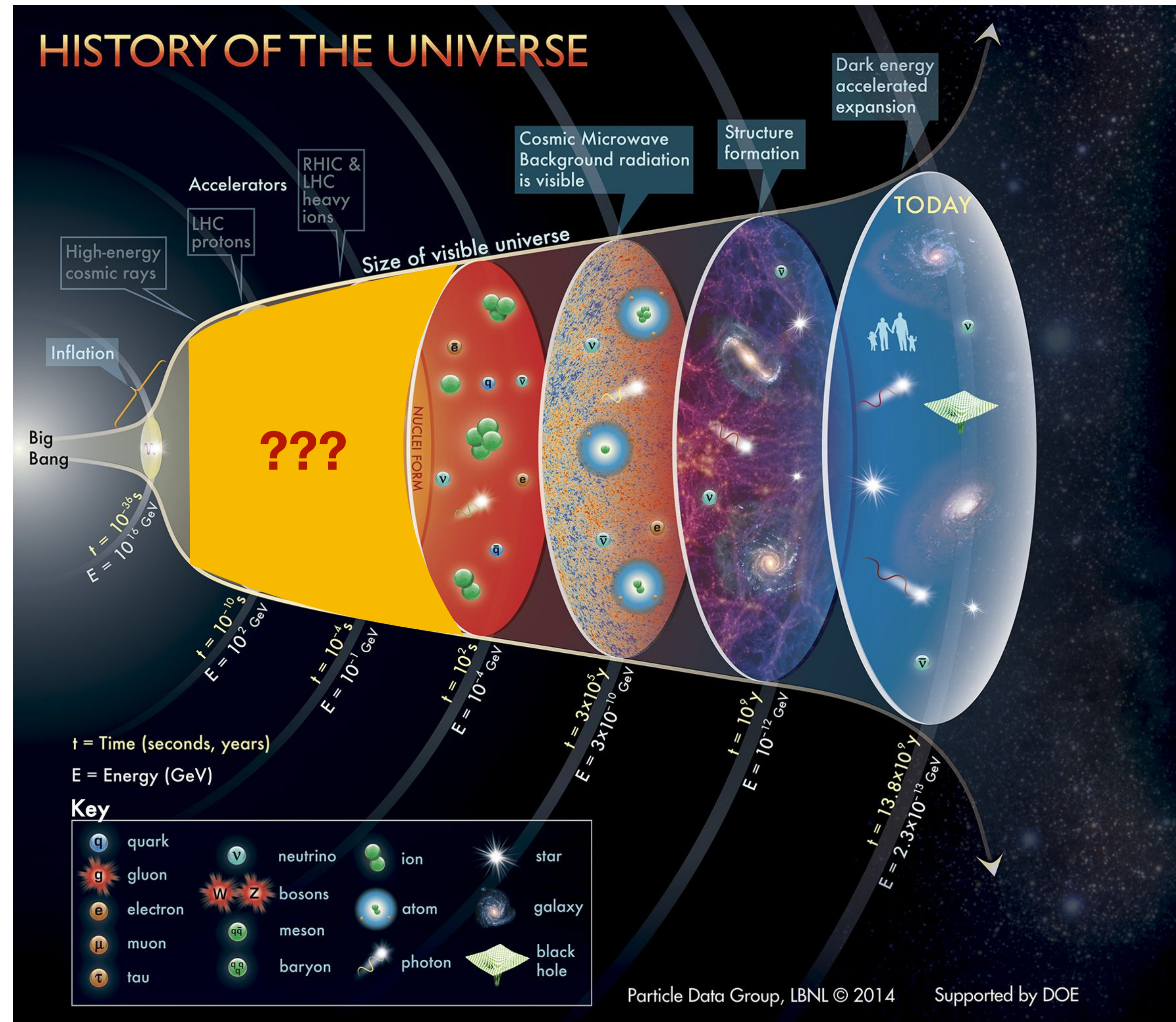


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# Motivation



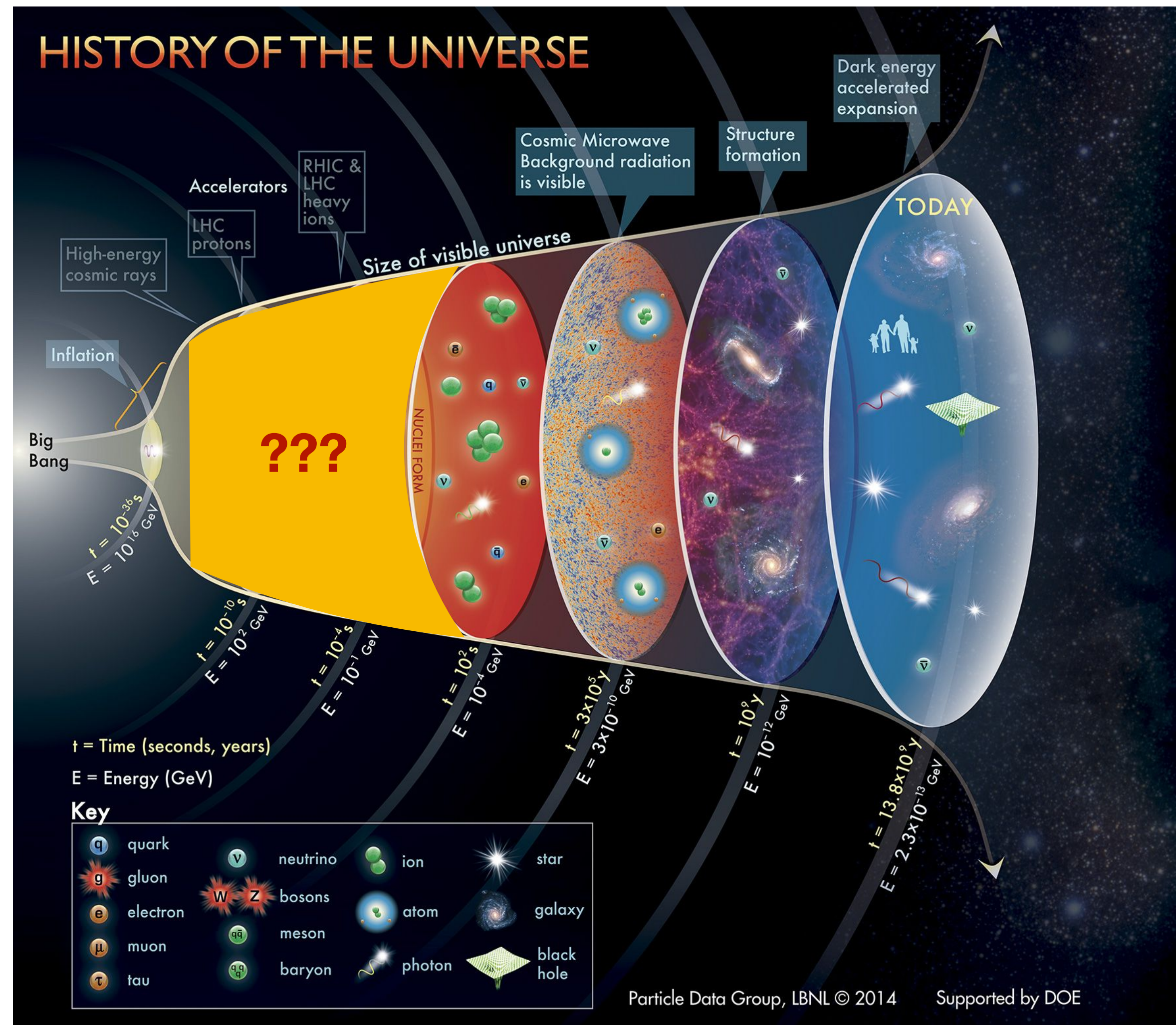
# Motivation



# Motivation

What we “know”:

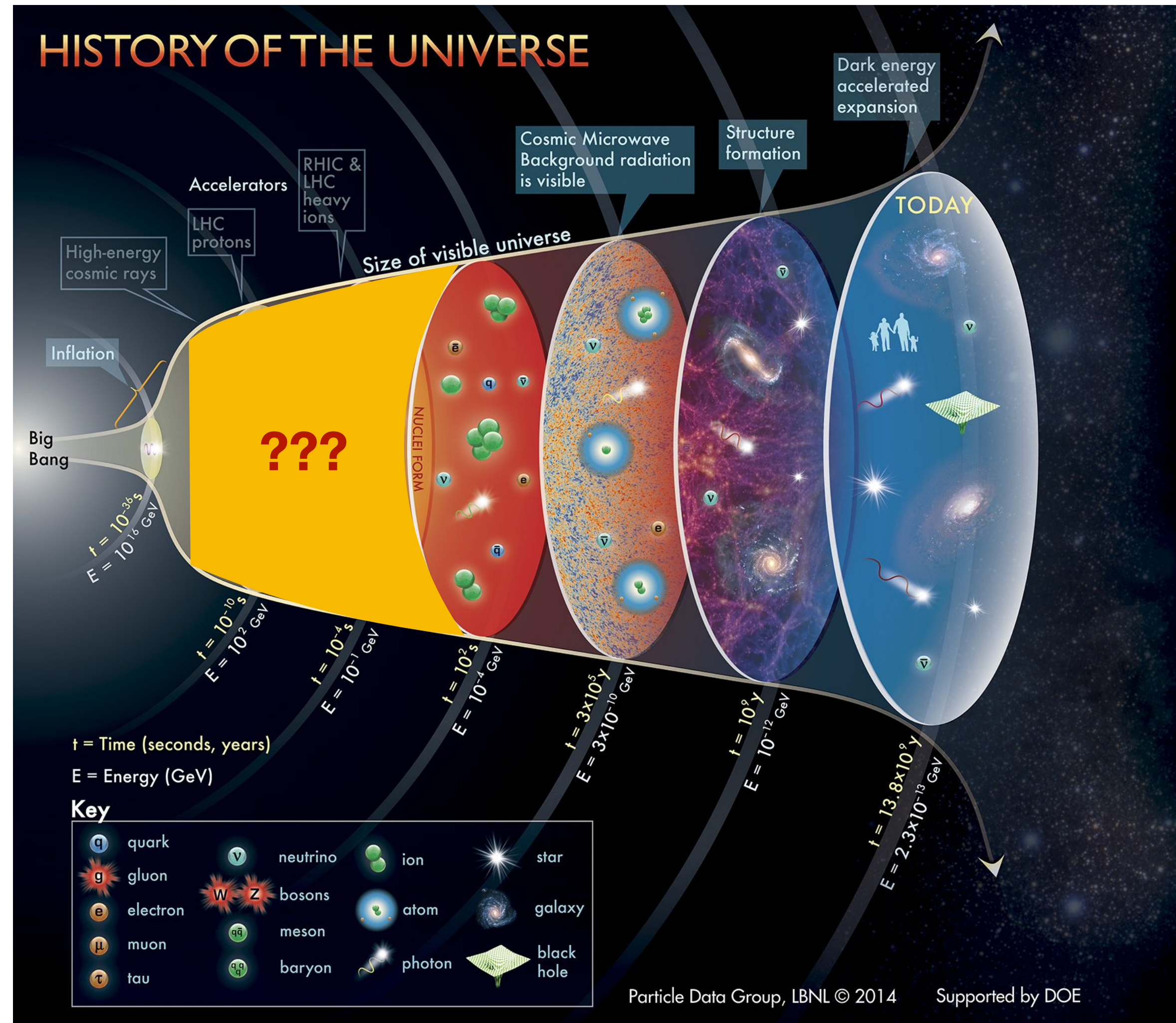
- Standard Model particles had to be reheated at least at temperatures around 4 MeV
- Dark matter had to be produced at some point?
- Perhaps inflation happened very early after Big Bang?



# Motivation

What we “know”:

- Standard Model particles had to be reheated at least at temperatures around 4 MeV
- Dark matter had to be produced at some point?
- Perhaps inflation happened very early after Big Bang?



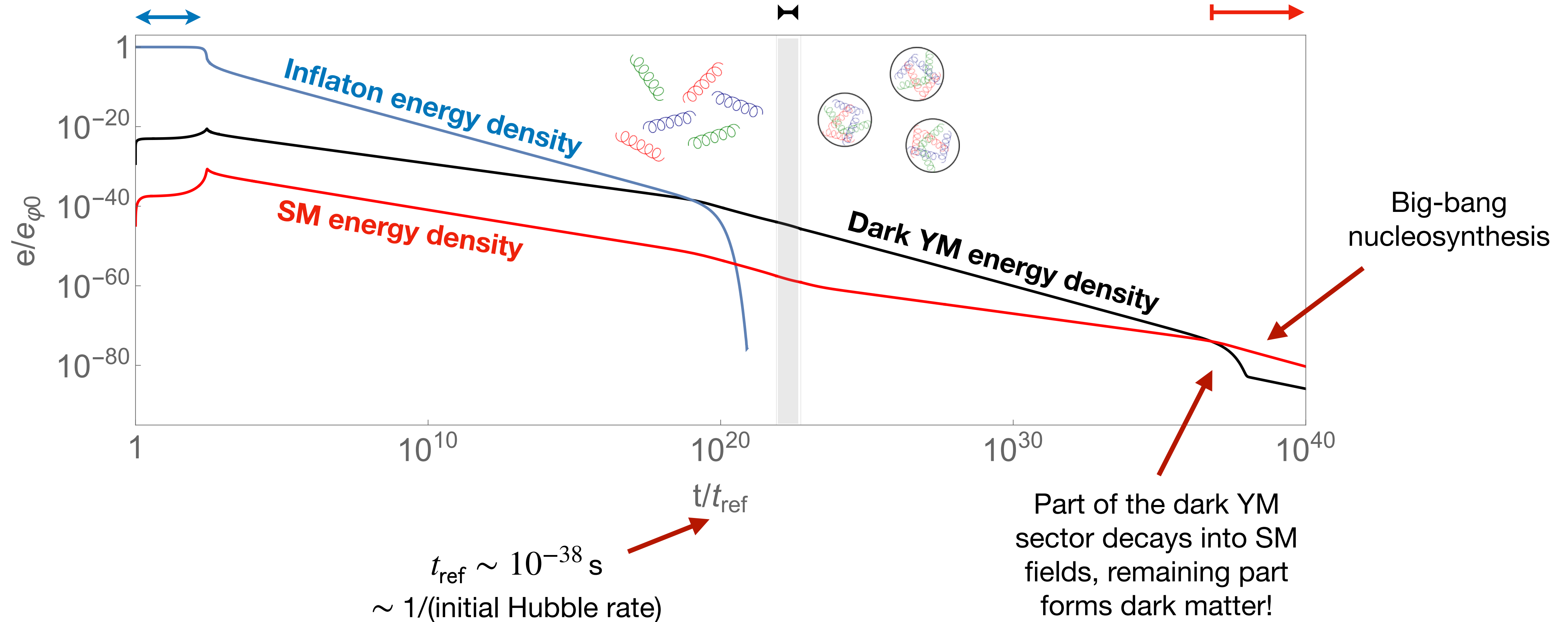
A dark Yang-Mills sector could provide both dark matter and a link between the inflation and SM reheating!

# History of the Universe à la 2406.10345

Slow-roll inflationary phase  
(exponential expansion of  
the Universe)

Dark sector  
phase  
transition

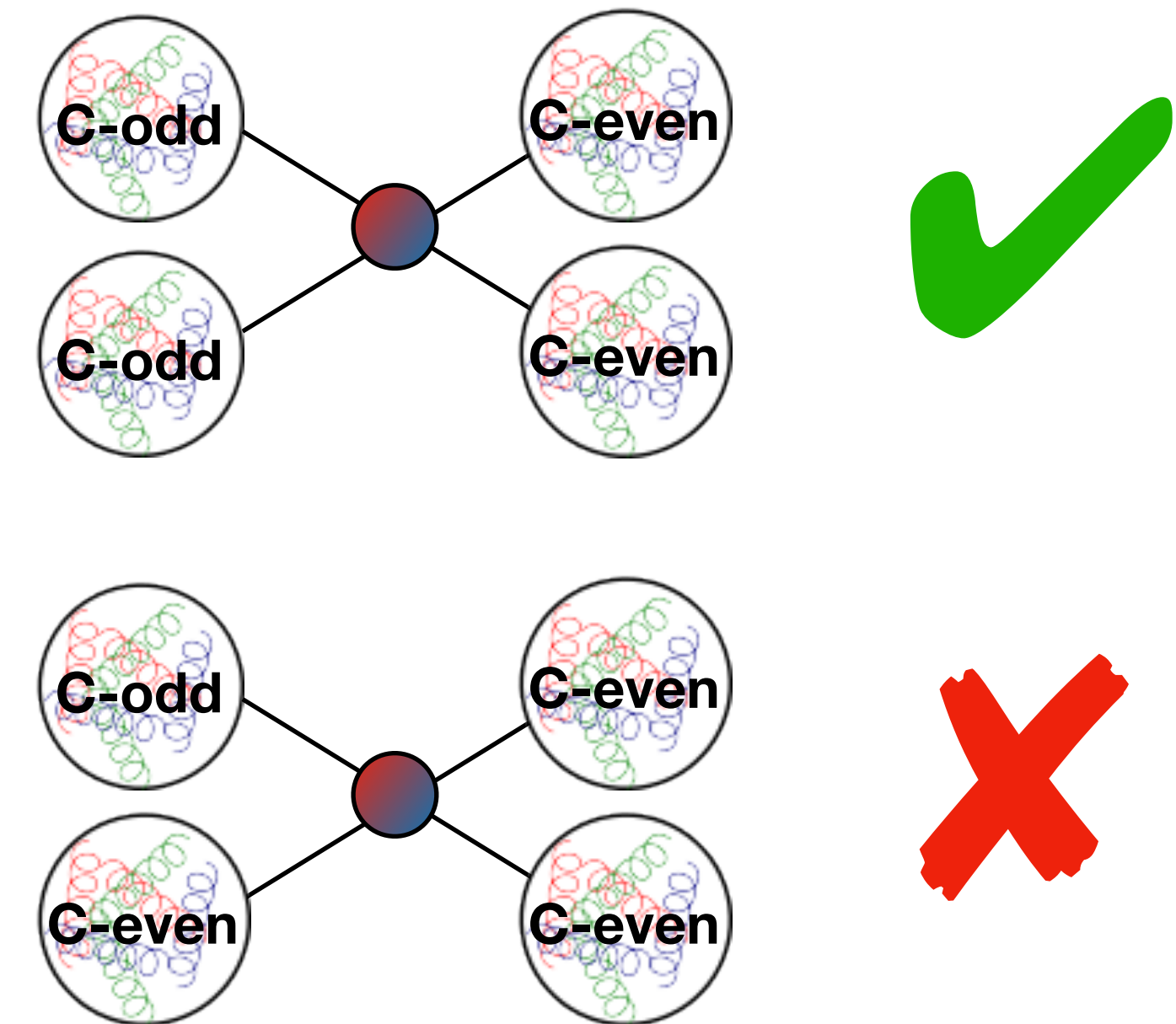
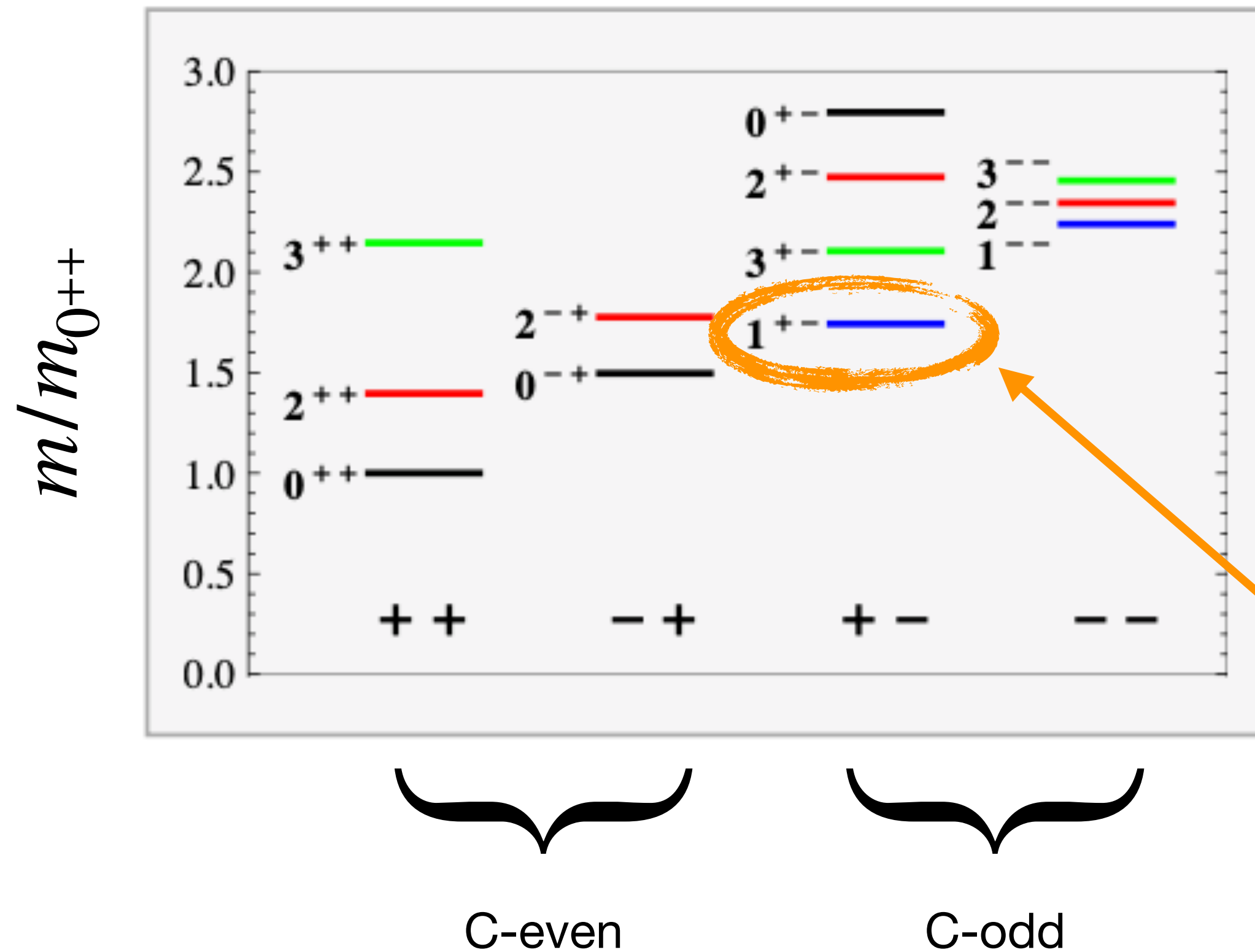
Standard  
radiation  
domination



# Glueball dark matter

[Boddy et al.:1402.3629] [Soni, Zhang: 1602.00714] [Forestell, Morrissey, Sigurdson: 1605.08048, 1710.06447]  
 [Carenza, Pasechnik, Wang et al.: 2207.13716, 2306.09510] [Gross, Karamitos, Landini, Strumia: 2012.12087]  
 [McKeen, Mizuta, Morrissey, Shamma: 2406.18635]...

Spectrum of SU(3) glueballs  $J^{PC}$



The lightest C-odd glueball is protected by the discrete symmetry and can be sufficiently stable even if the C-even glueballs decay fast into SM fields!

# Ingredients

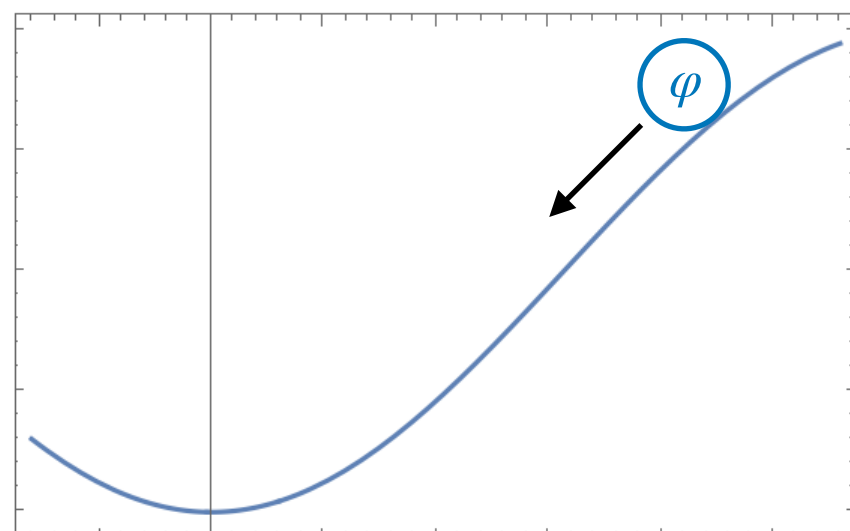
Example of an effective operator either for gravitational interaction (then  $M = m_{pl}$ ) or for interaction via portal particles with large mass  $M$  (e.g. heavy fermions)

Gauge coupling  $\alpha$   $\varphi$   $\epsilon^{\mu\nu\rho\sigma} F_{\mu\nu}^c F_{\rho\sigma}^c$  Yang-Mills field strength

$$\frac{\alpha \varphi \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu}^c F_{\rho\sigma}^c}{16\pi f_a}$$

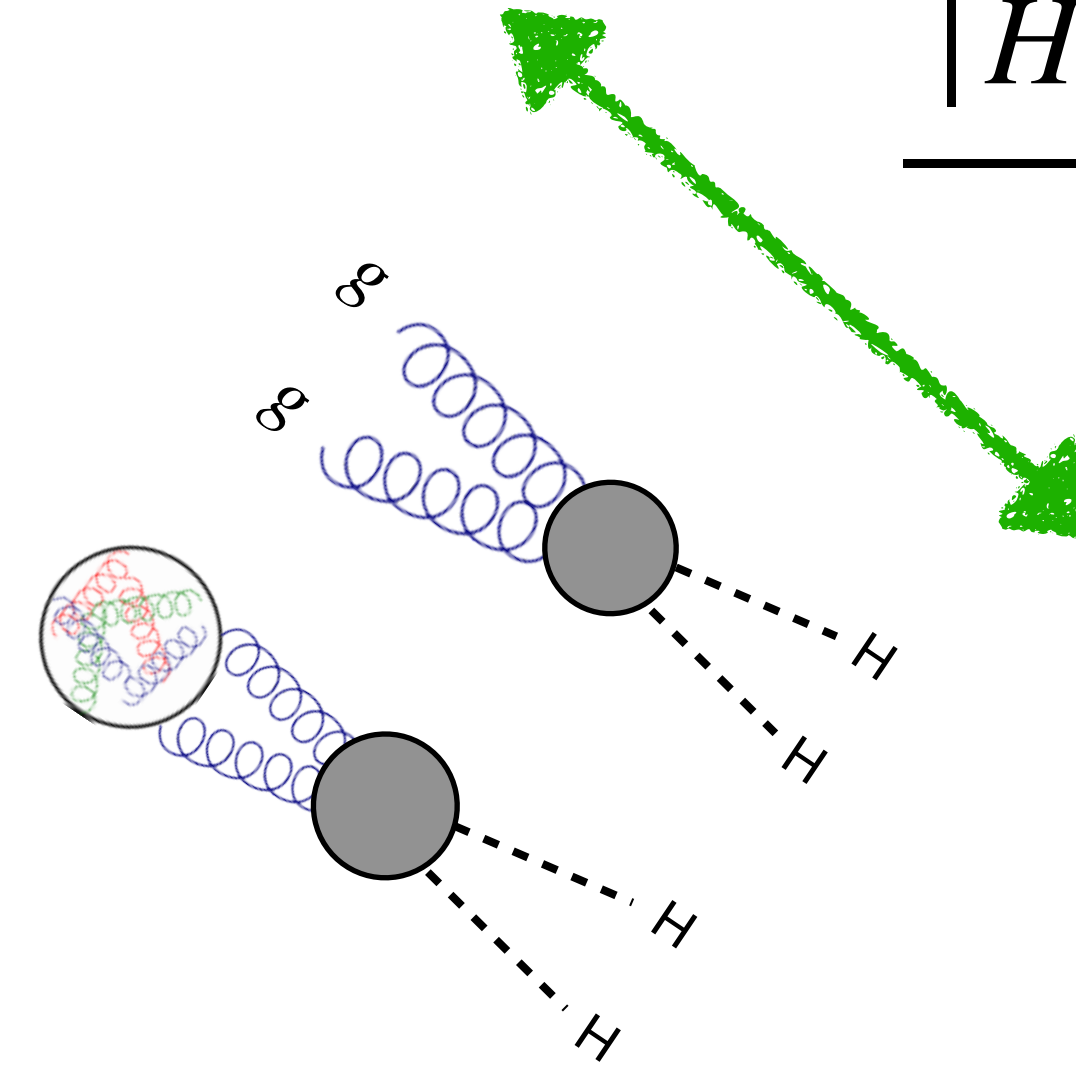
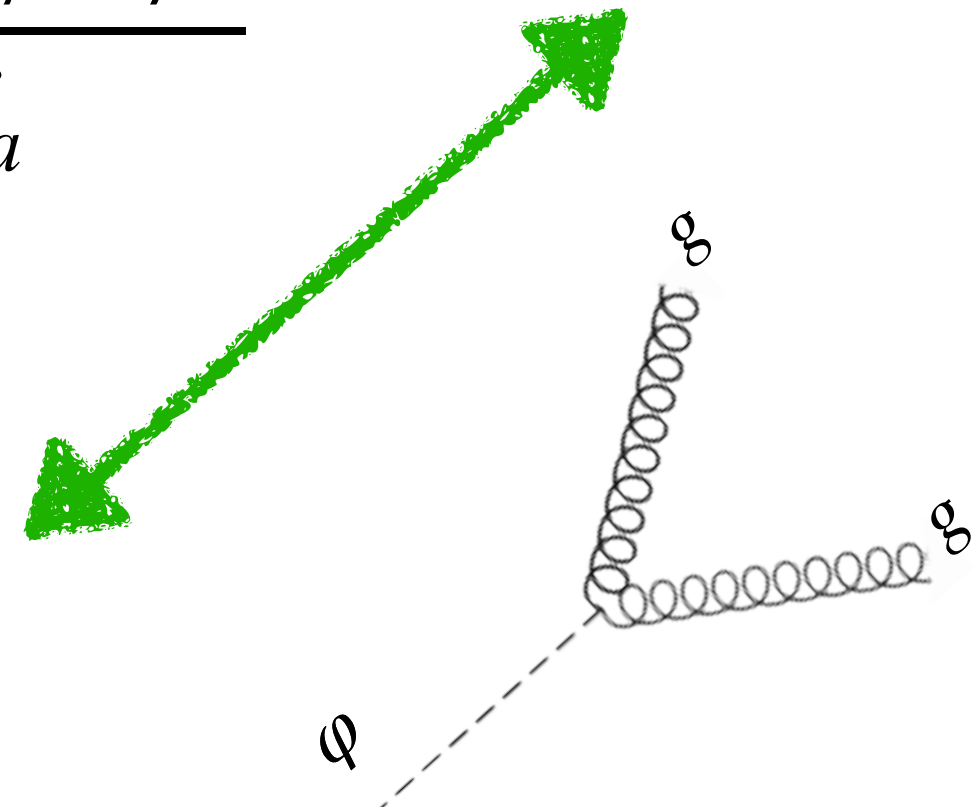
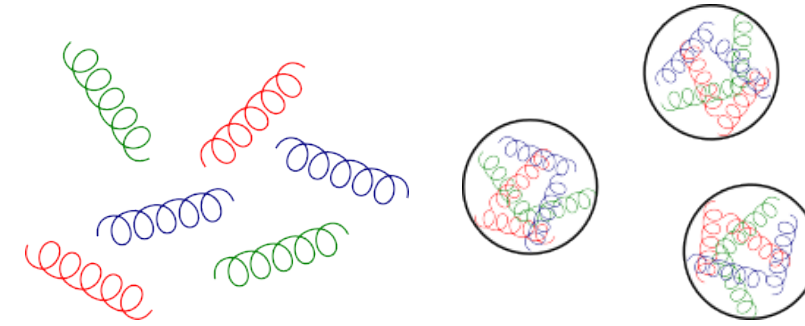
Axion decay constant

**Axion-like inflaton**



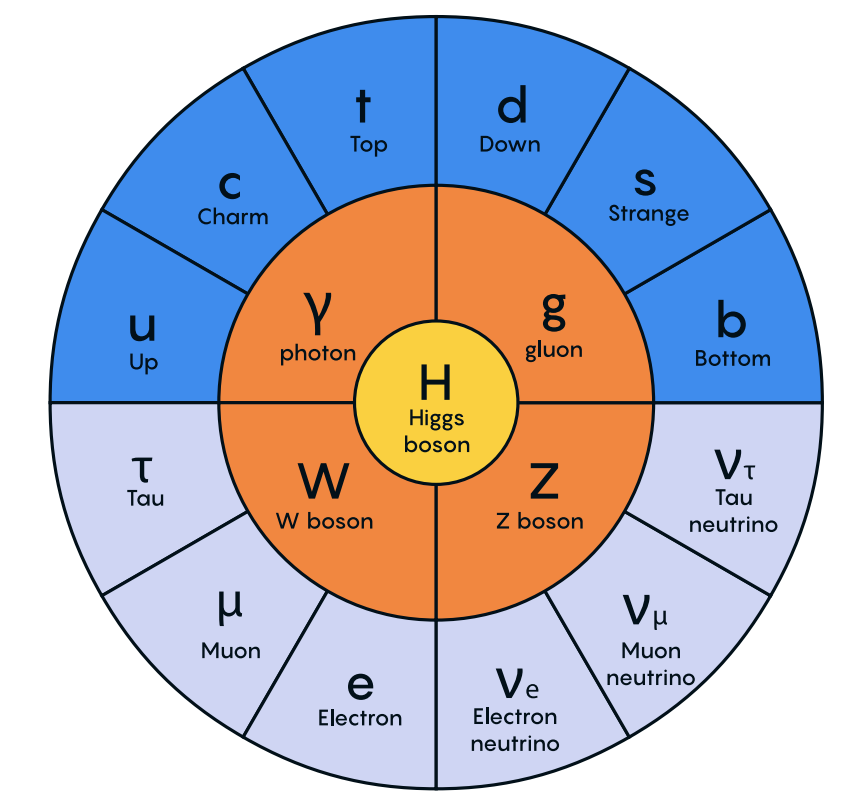
- [Berghaus, Graham, Kaplan: 1910.07525]
- [Laine, Procacci: 2102.09913]
- [Klose, Laine, Procacci: 2201.02317]
- [Klose, Laine, Procacci: 2210.11710]
- [HK, Laine, Procacci: 2303.17973]

**Dark Yang-Mills sector**



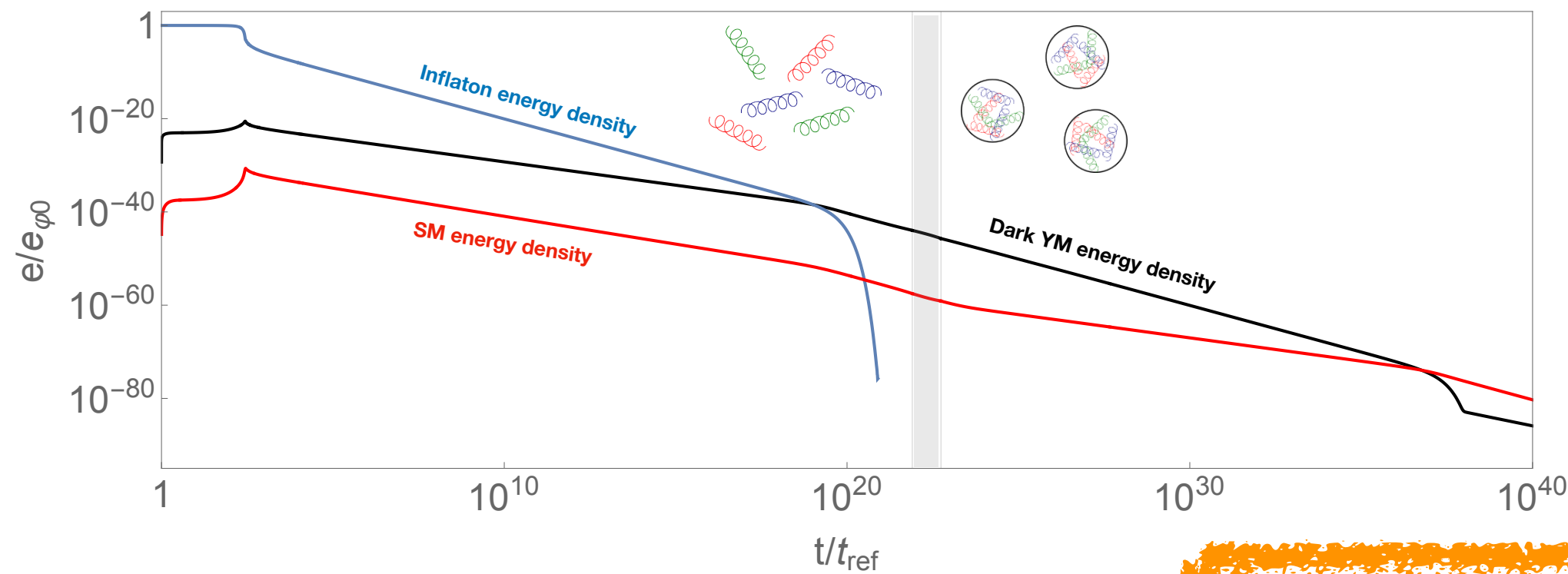
$$\frac{|H|^2 \text{Tr} F_{\mu\nu} F^{\mu\nu}}{M^2}$$

**Standard Model**





# Evolution equations



Inflaton decay rate:  $\Upsilon \simeq \alpha^2 m_\phi^3 / (32\pi^3 f_a^2)$  if  $T_{\text{DS}} \ll m_\phi$ ,

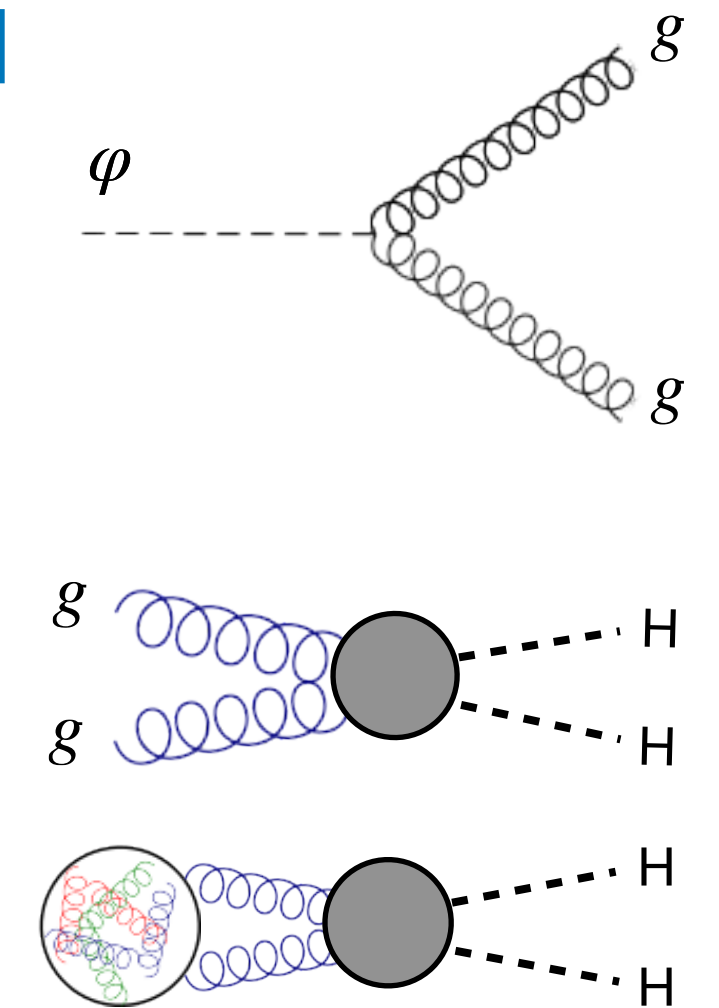
lattice input available for SU(3)

[Moore, Tassler: 1011.1167] [Laine, Niemi, Procacci, Rummukainen: 2209.13804]

$$\dot{e}_\phi + 3He_\phi = -\Upsilon e_\phi$$

$$\dot{e}_{\text{DS}} + 3H(e_{\text{DS}} + p_{\text{DS}}) = \Upsilon e_\phi - \Gamma e_{\text{DS}}$$

$$\dot{e}_{\text{SM}} + 4He_{\text{SM}} = \Gamma e_{\text{DS}}$$



Dark sector energy and pressure densities parameterised by temperature.

SU(3) equation of state:  
[Giusti, Pepe: 1612.00265]  
[Meyer: 0905.422]

Hubble rate:

$$H = \sqrt{\frac{8\pi}{3m_{\text{pl}}^2} (e_\phi + e_{\text{SM}} + e_{\text{YM}})}$$

Gluon annihilation rate:

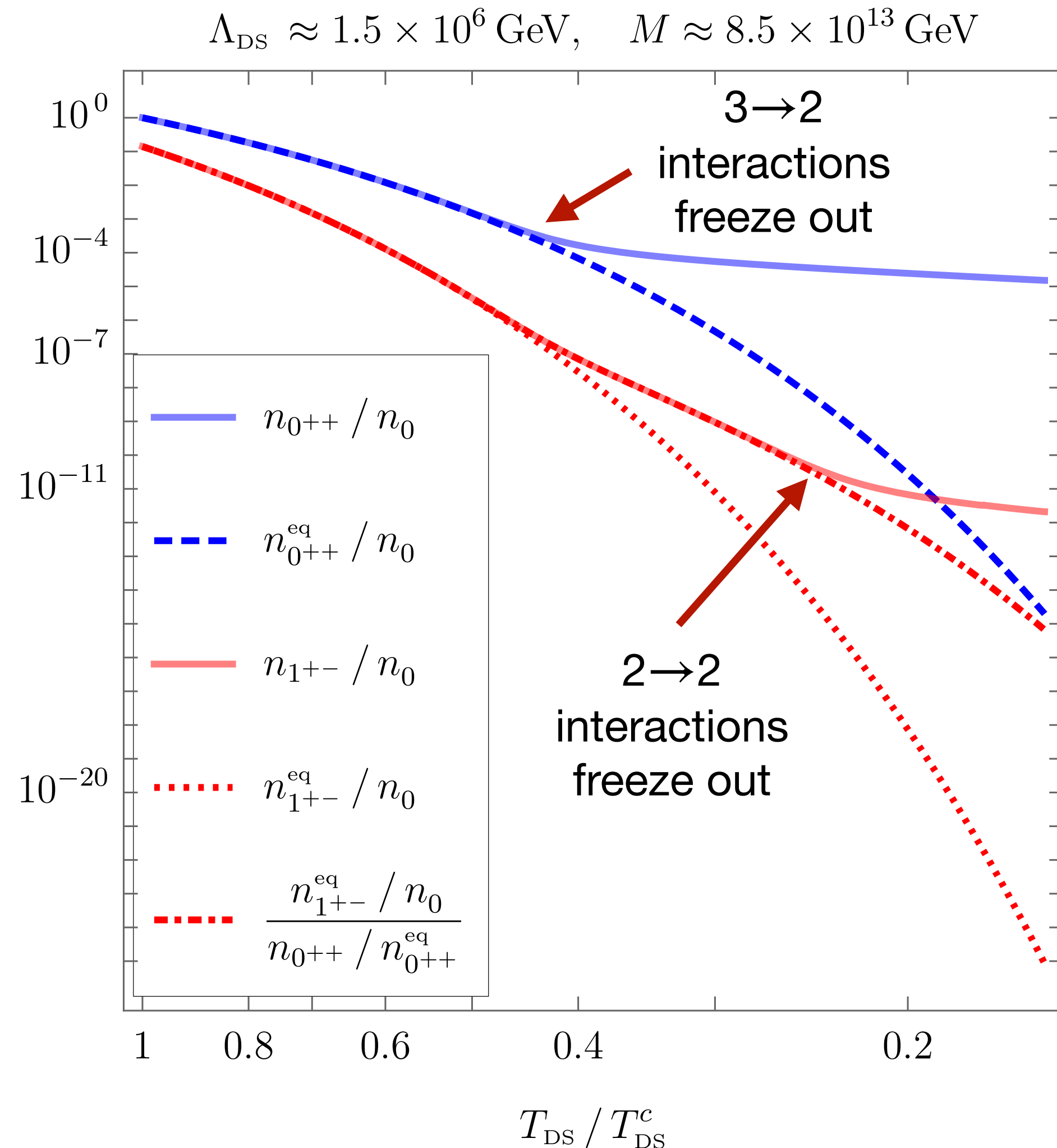
$$\Gamma \propto T_{\text{DS}}^5 / M^4$$

or glueball decay rate

$$\Gamma \propto \Lambda_{\text{DS}}^5 / M^4,$$

$\Lambda_{\text{DS}}$ : Dark YM confinement scale

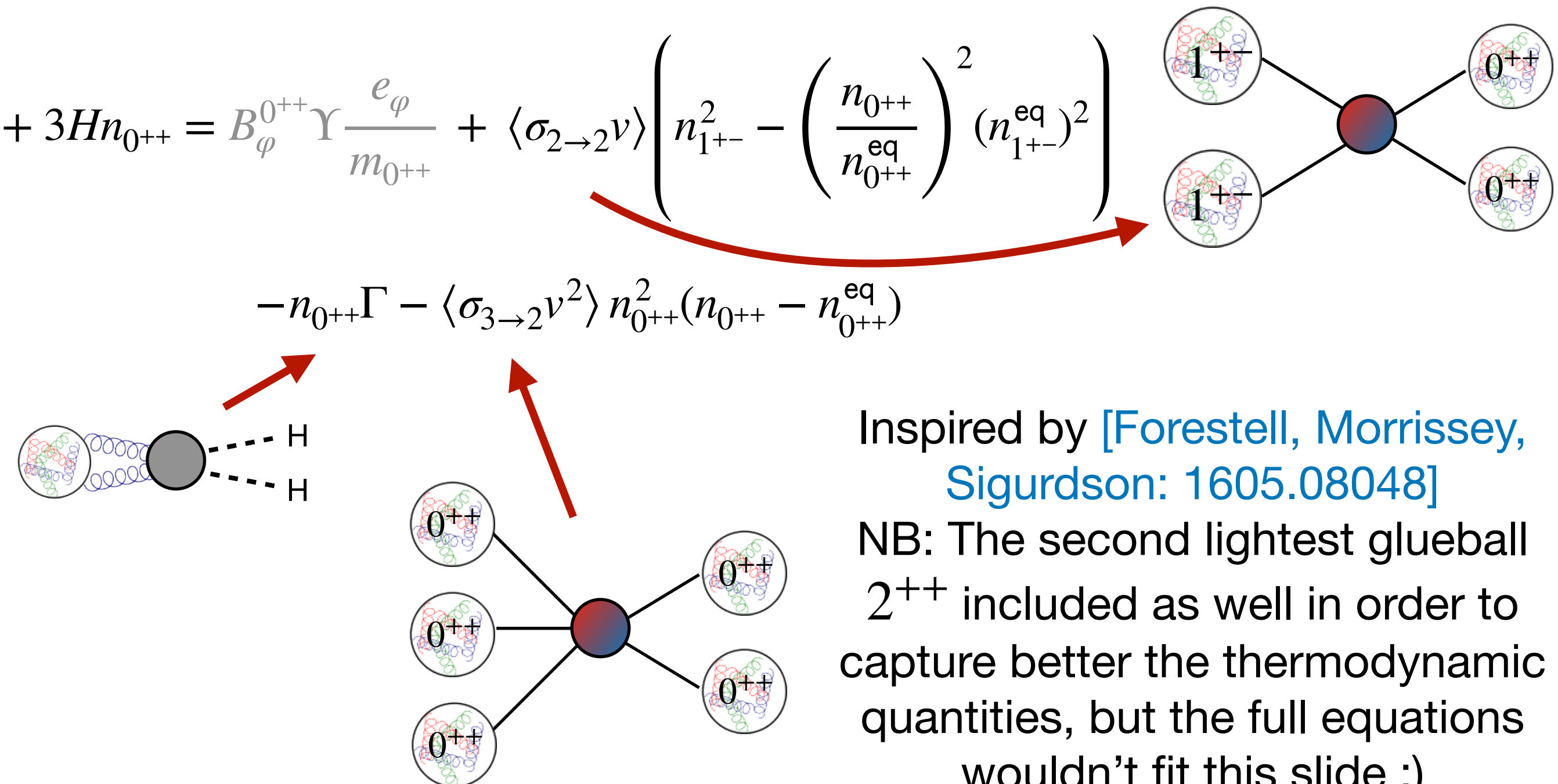
# Dark matter relic abundance?



**Boltzmann equations for the number densities of the lightest C-even and lightest C-odd glueballs:**

$$\dot{n}_{1^{+-}} + 3Hn_{1^{+-}} = B_{\varphi}^{1^{+-}} \Upsilon \frac{e_{\varphi}}{m_{1^{+-}}} - \langle \sigma_{2 \rightarrow 2} v \rangle \left( n_{1^{+-}}^2 - \left( \frac{n_{0^{++}}}{n_{0^{++}}^{\text{eq}}} \right)^2 (n_{1^{+-}}^{\text{eq}})^2 \right)$$

$$\dot{n}_{0^{++}} + 3Hn_{0^{++}} = B_{\varphi}^{0^{++}} \Upsilon \frac{e_{\varphi}}{m_{0^{++}}} + \langle \sigma_{2 \rightarrow 2} v \rangle \left( n_{1^{+-}}^2 - \left( \frac{n_{0^{++}}}{n_{0^{++}}^{\text{eq}}} \right)^2 (n_{1^{+-}}^{\text{eq}})^2 \right)$$



# Results: open parameter space

---  $0^{++}$  and  $1^{+-}$ , —  $0^{++}$ ,  $2^{++}$  and  $1^{+-}$

NB: Inflaton parameters fixed based on CMB constraints

[Klose, Laine, Procacci: 2201.02317]:

$$m_\phi = 1.09 \times 10^{-6} m_{\text{pl}},$$

$$f_a = 1.25 m_{\text{pl}}$$

Too much dark matter

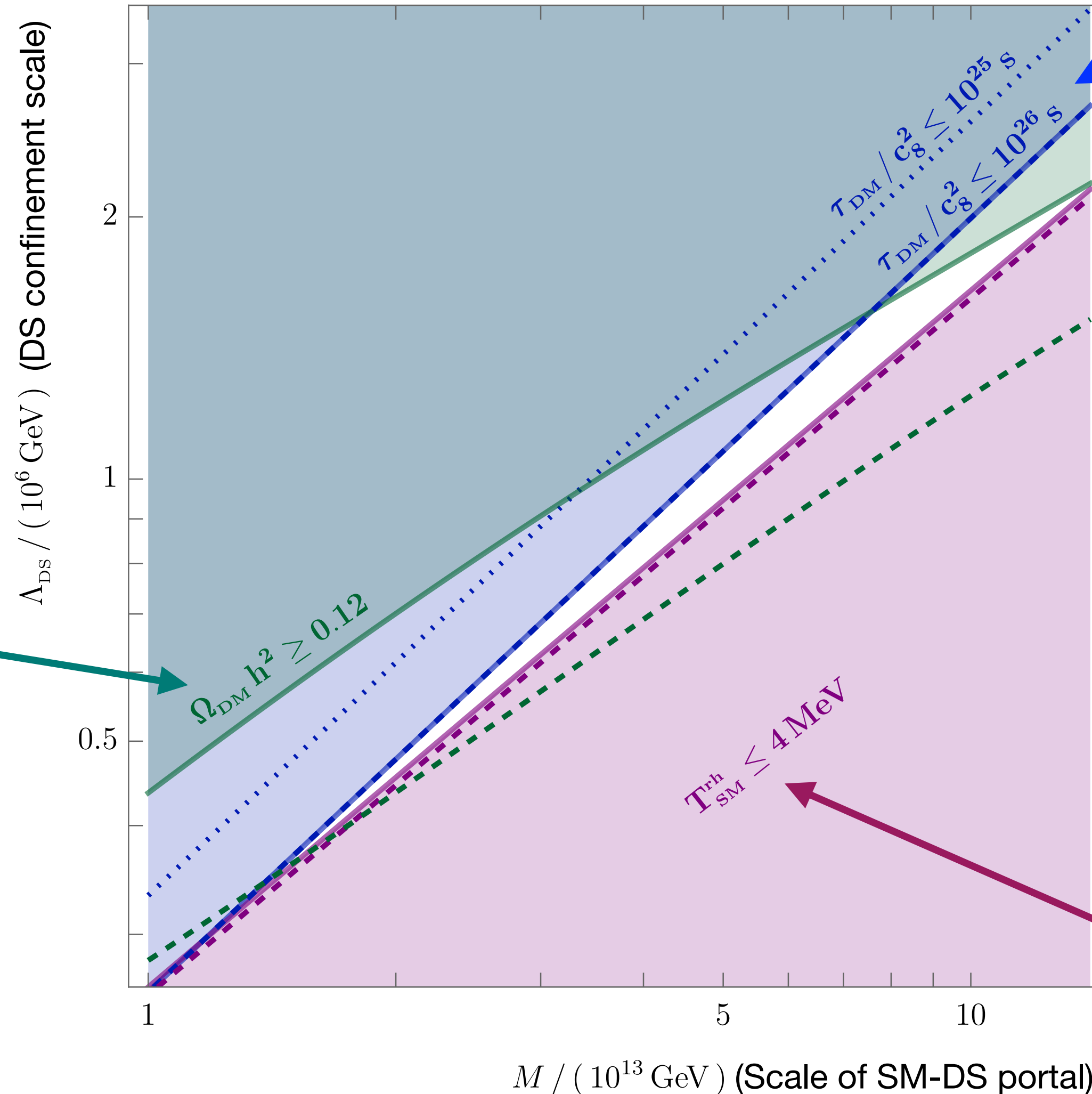
$\Leftrightarrow$

Too early freeze-out

$\Leftrightarrow$

Too weak interactions:

$$\langle \sigma_{2 \rightarrow 2\nu} \rangle \propto 1/\Lambda_{\text{DS}}^2$$

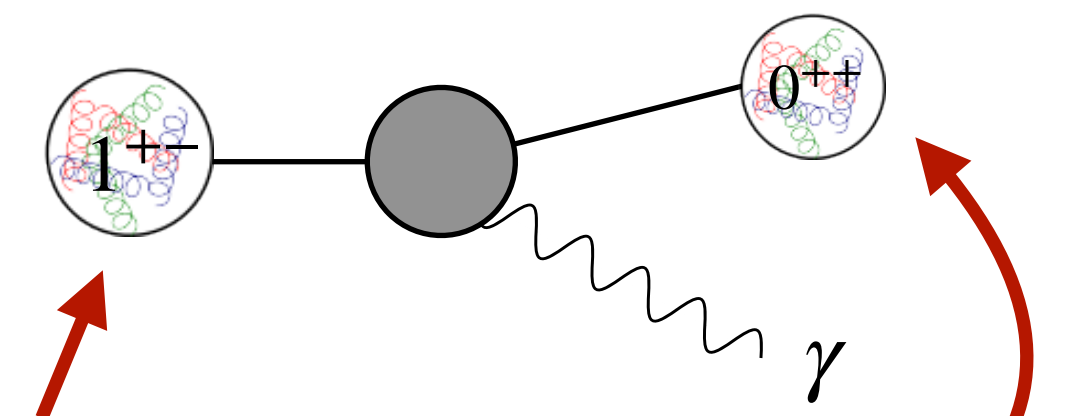


Too large DM decay rate

$$\Gamma_{\text{DM}} \propto \Lambda_{\text{DS}}^9 / M^8$$

NB: C-odd glueballs decay through operators like

$$c_8 \frac{B_{\mu\nu} \text{Tr} G^{\mu\nu} G_{\alpha\beta} G^{\alpha\beta}}{M^4}$$



Dark matter particle:

lightest C-odd  
glueball

$$m_{1^{+-}} \simeq 11 \Lambda_{\text{DS}}$$

Lightest glueball  
(unstable):

$$m_{0^{++}} \simeq 7 \Lambda_{\text{DS}}$$

SM not reheated efficiently enough

$$\Leftrightarrow \Gamma \propto \Lambda_{\text{DS}}^5 / M^4 \text{ too small}$$

# Conclusions & Outlook

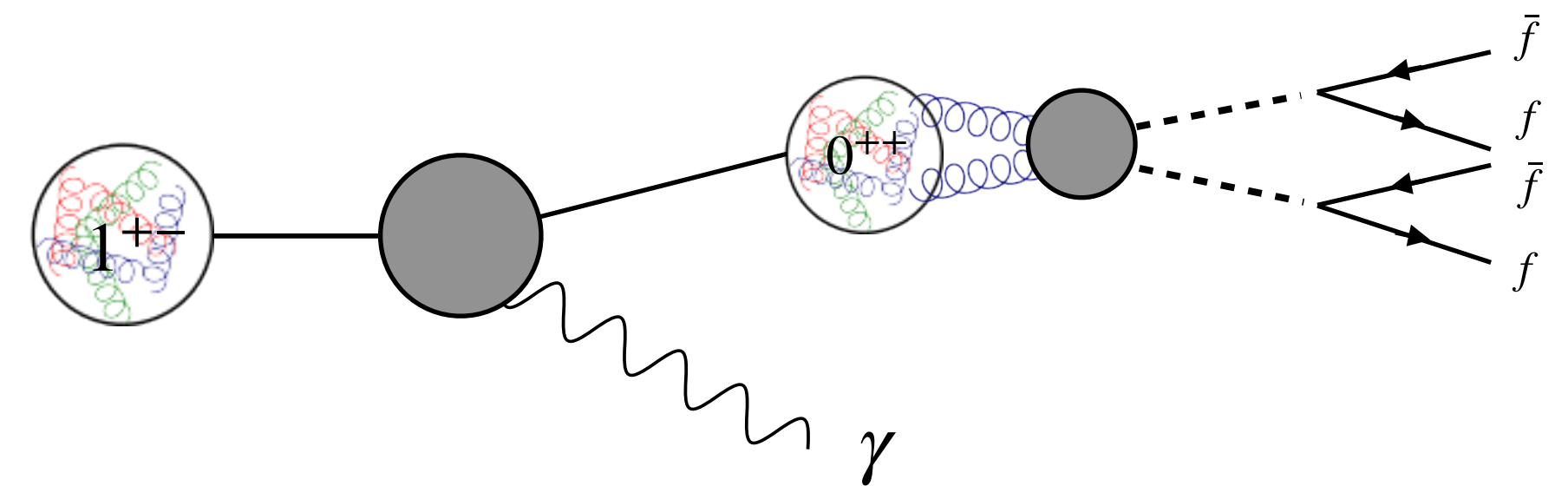
- A general scenario linking dark matter production with inflation and SM reheating provided
- Dark matter relic abundance independent of the details of the inflationary scenario  $\Rightarrow$  generalisations beyond axion-like inflation possible

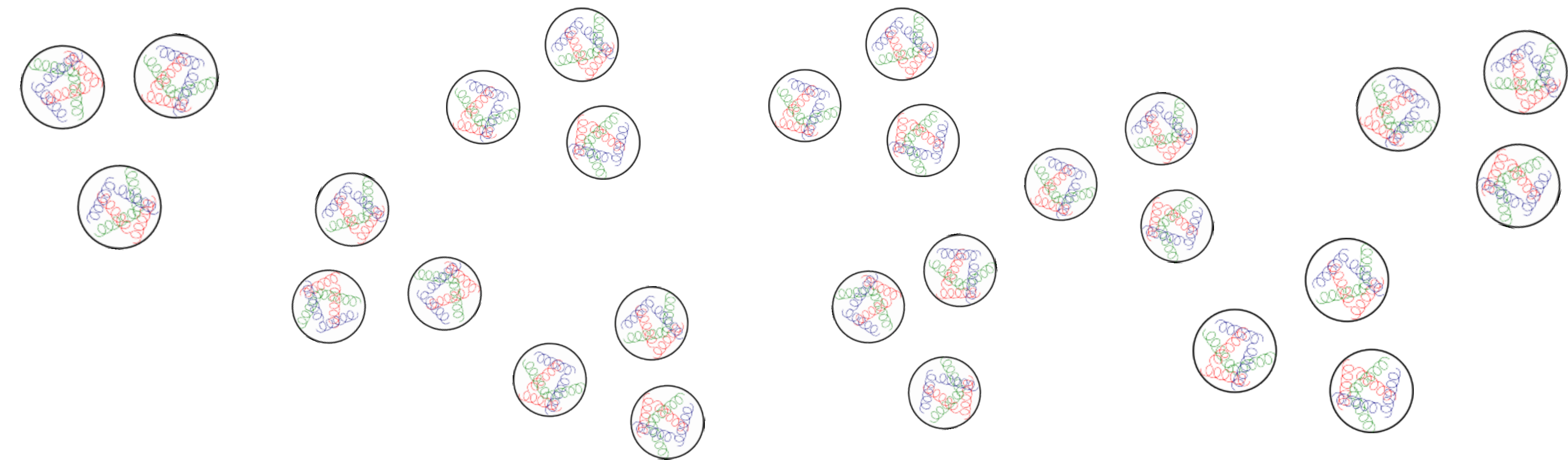
- If SU(3) dark sector chosen, portal to SM at energies  $M \sim 10^{13}$  GeV needed. Connection to other puzzles in high-energy physics?

- Larger open parameter space can be obtained for theories where the “protected” glueballs are more long-lived. E.g., for SO(N) with  $N \geq 8$ :

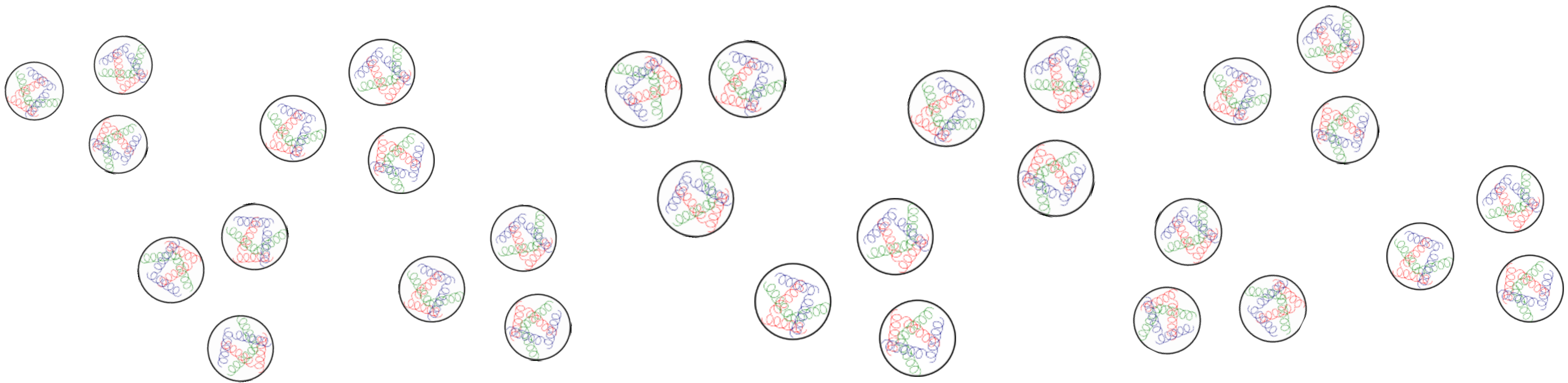
$$\Gamma_{\text{DM}} \propto \Lambda_{\text{DS}}^{2N-3} / M^{2N-4}$$

- Concrete indirect detection signal to be predicted!



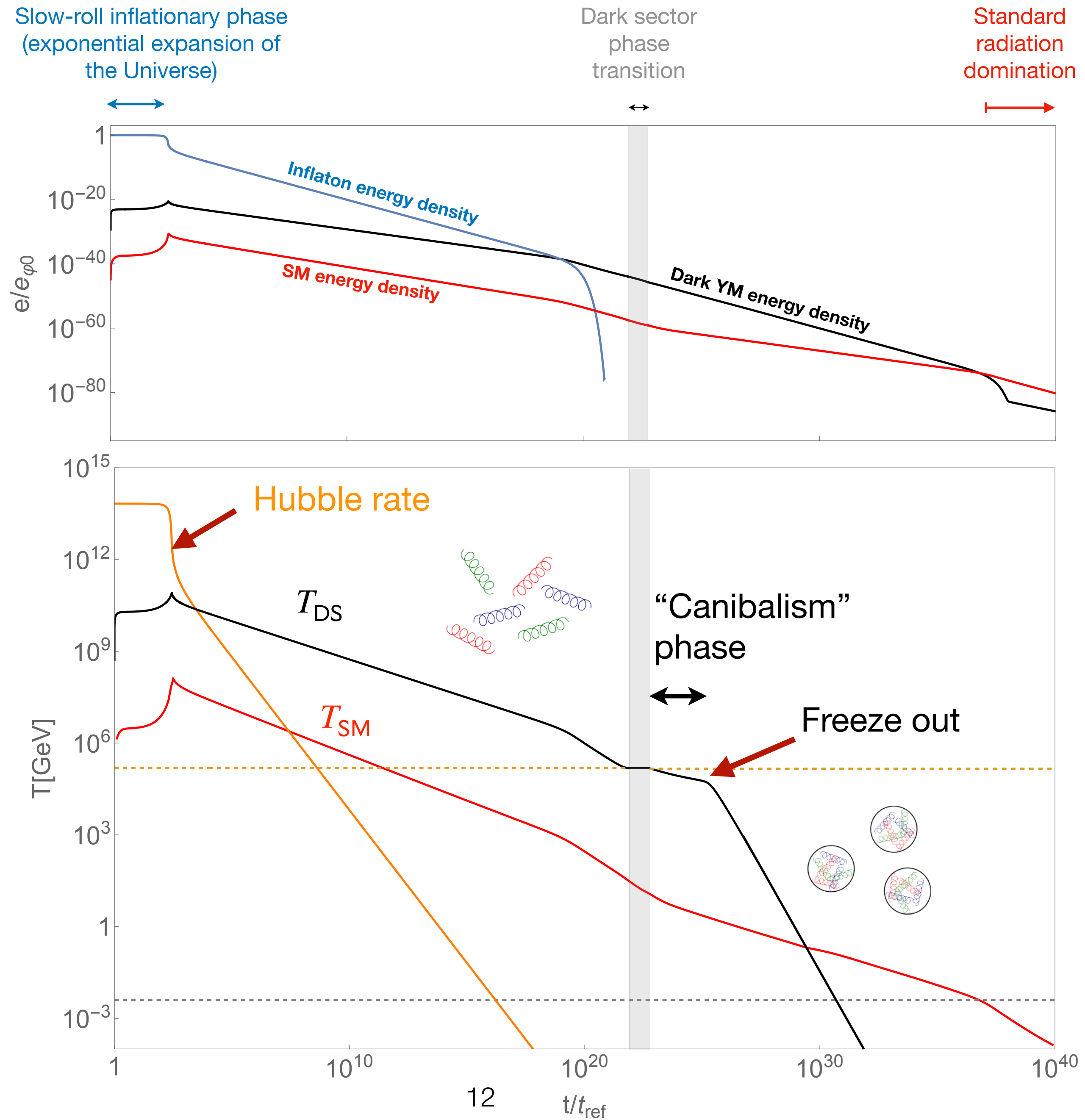


**Thanks for your attention!**



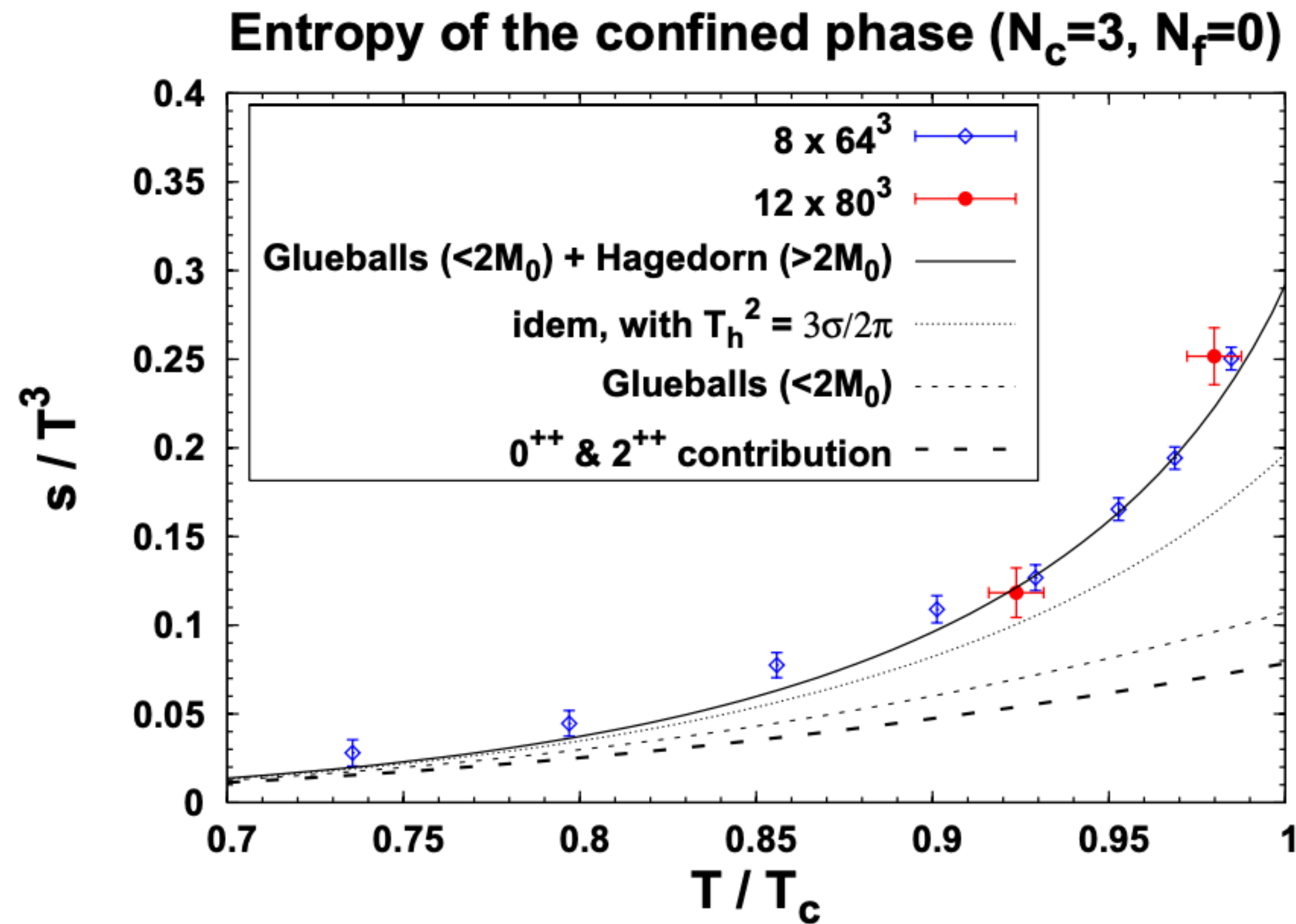
# Backup

# History of the Universe à la 2406.10345



$T_{\text{DS}}^c \simeq 1.24 \Lambda_{\text{DS}}$ :  
 Dark sector  
 confinement  
 temperature

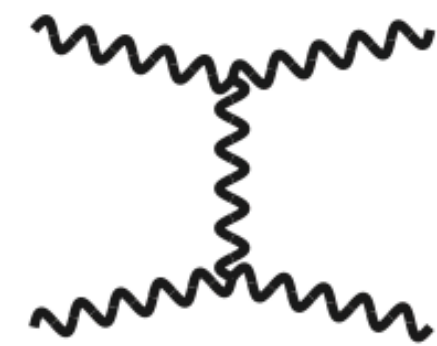
Thermodynamics of a YM theory below confinement scale might be indeed described as an ensemble of glueballs!



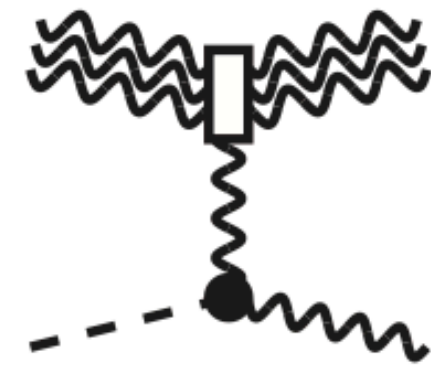
[Meyer: 0905.4229]



# Thermalisation?



(a)



(b)

Thermalisation rate:

$$\Gamma_g \sim \alpha^2 T$$

$$\Gamma_a \sim \Upsilon$$

# Glueball dark matter

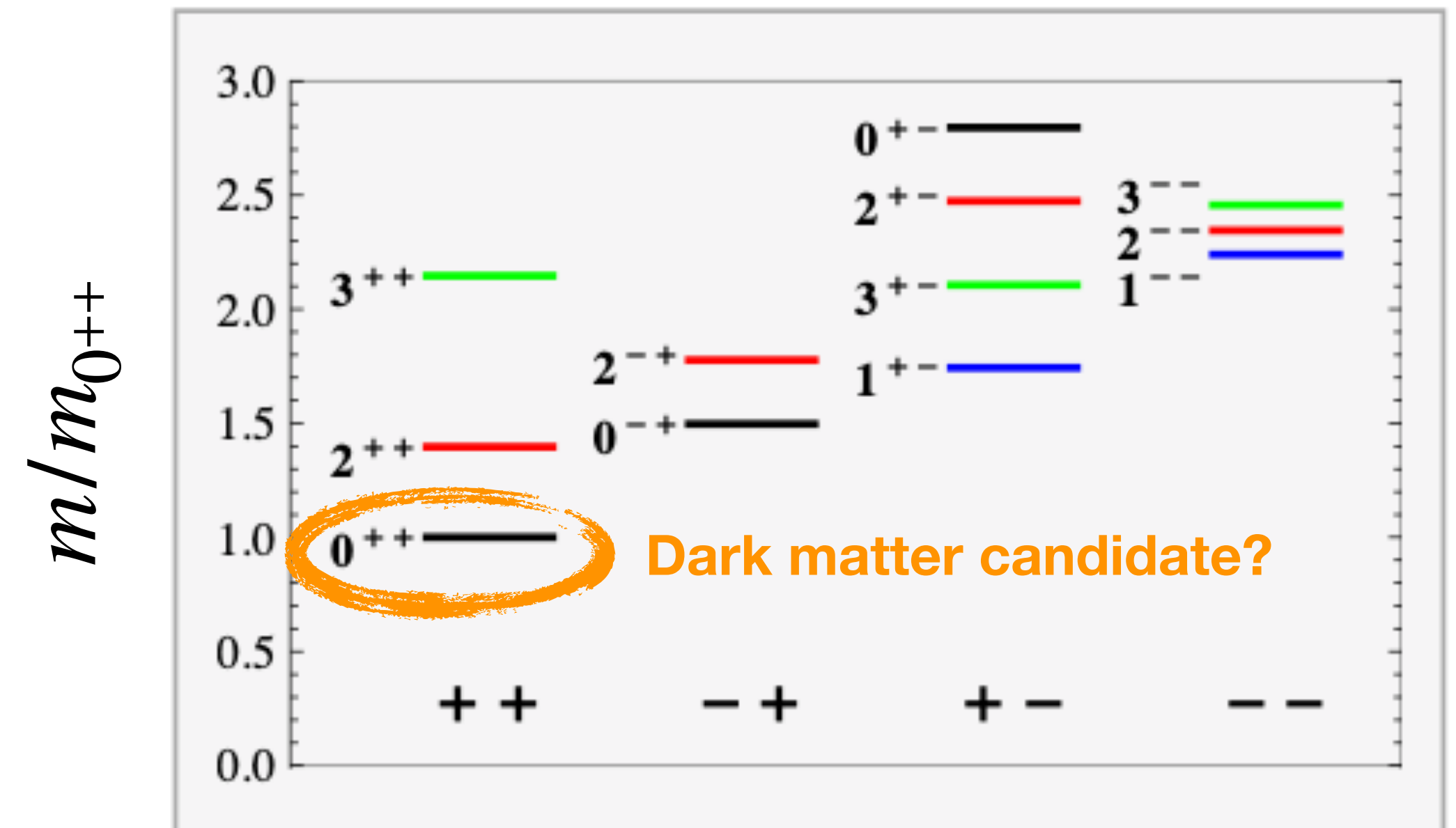
[Boddy et al.:1402.3629] [Soni, Zhang: 1602.00714] [Forestell, Morrissey, Sigurdson: 1605.08048, 1710.06447] [Carenza, Pasechnik, Wang et al.: 2207.13716, 2306.09510]...

- Self-interacting dark matter:  $\sigma_{GB} \propto m_{GB}^{-2}$   
 $\sigma_{GB}/m_{GB} \sim 1 \text{ cm}^2/\text{g}$  if  $\Lambda \sim 100 \text{ MeV}$
- Example of the lowest order effective operator for the decay of the lightest  $0^{++}$  glueball to SM fields:

$$\frac{|H|^2 \text{Tr} G_{\mu\nu} G^{\mu\nu}}{M^2} \Rightarrow \Gamma_{0^{++}} \sim \frac{\Lambda^5}{M^4}$$

- If the lightest glueball forms dark matter:  $1/\Gamma_{0^{++}} \gtrsim 10^{26} \text{ s}$
- Even if  $M \sim m_{pl}$  this translates to  $\Lambda \lesssim 10^6 \text{ GeV}$

Spectrum of SU(3) glueballs  $J^{PC}$



[Juknevich, Melnikov, Strassler: 0903.0883]

# Model setup: Example of a “warm inflation”

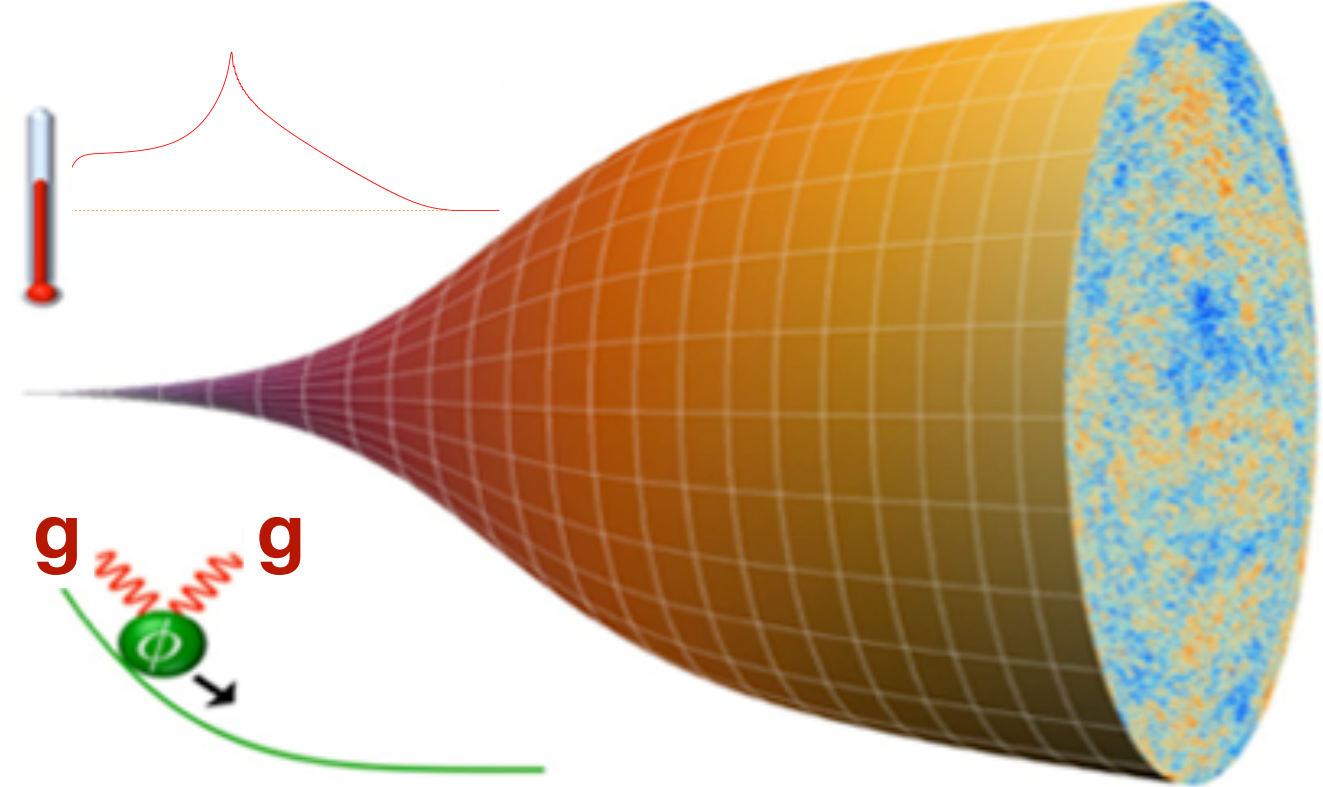
- Axion inflation coupled to non-abelian dark sector

[Berghaus, Graham, Kaplan: 1910.07525]

[Laine, Procacci: 2102.09913]

[Klose, Laine, Procacci: 2201.02317]

[Klose, Laine, Procacci: 2210.11710]



Credit: João G. Rosa/University of Aveiro; ESA and the Planck collaboration

$$\mathcal{L} \supset \frac{1}{2} \partial^\mu \varphi \partial_\mu \varphi - V_0(\varphi) - \frac{\alpha \varphi \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu}^c F_{\rho\sigma}^c}{16\pi f_a}$$

Inflaton field

Inflaton potential:

$$V_0 \simeq m^2 f_a^2 \left[ 1 - \cos\left(\frac{\bar{\varphi}}{f_a}\right) \right]$$

“Natural/axion inflation”  
[Freese, Frieman, Olinto: Phys.Rev.Lett. 65 (1990)]

Gauge coupling

Yang-Mills field strength

Axion decay constant

Hubble rate

Friction due to inflaton coupling to dark sector

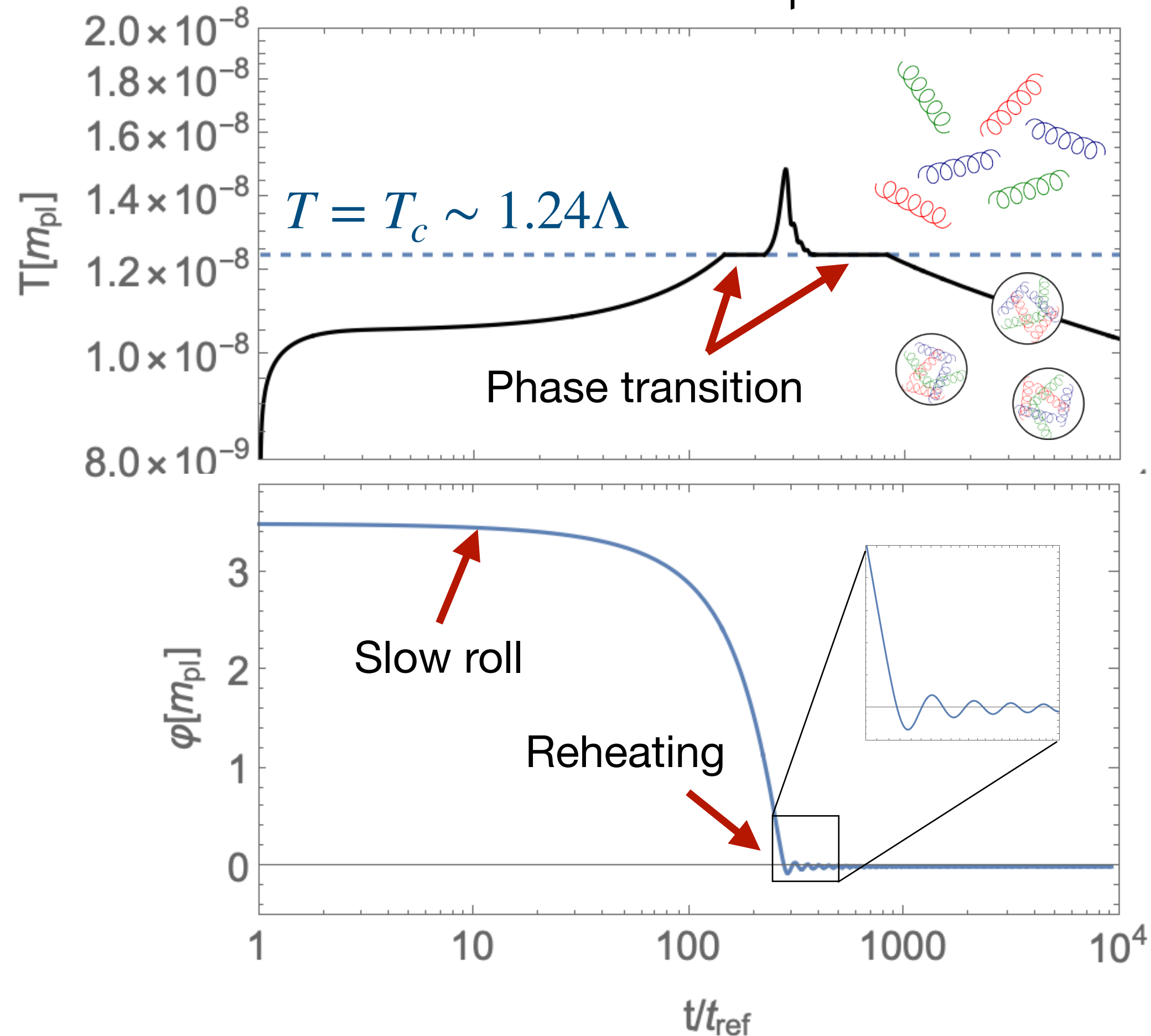
$$\ddot{\bar{\varphi}} + (3H + \Upsilon)\dot{\bar{\varphi}} + V_\varphi \simeq 0$$

$$\dot{\rho}_r + 3H(\rho_r + p_r) \simeq \Upsilon \dot{\bar{\varphi}}^2$$

Dark radiation energy and pressure densities

# Evolution of the dark sector

$$\Lambda = 10^{-8} m_{\text{pl}}$$



$$(m_{\text{pl}} = 1.22 \times 10^{19} \text{ GeV})$$

- Evolution of an SU(3) sector coupled to axion inflation studied for varying confinement scale  $\Lambda$  [HK, Laine, Procacci: 2303.17973]

Friction due to inflaton coupling to dark sector:  
lattice input available for SU(3)  
[Moore, Tassler: 1011.1167] [Laine, Niemi, Procacci, Rummukainen: 2209.13804]

$$\ddot{\phi} + (3H + \Upsilon)\dot{\phi} + V_{\phi} \simeq 0$$

$$\dot{\rho}_r + 3H(\rho_r + p_r) \simeq \Upsilon \dot{\phi}^2$$

Dark radiation energy and pressure densities.  
SU(3) equation of state:  
[Giusti, Pepe: 1612.00265]  
[Meyer: 0905.422]

# NB: abelian vs non-abelian dark sector

- Pseudoscalar inflaton coupled to gauge fields:

$$\mathcal{L} \supset - \frac{\alpha \varphi \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu} F_{\rho\sigma}}{16\pi f_a}$$

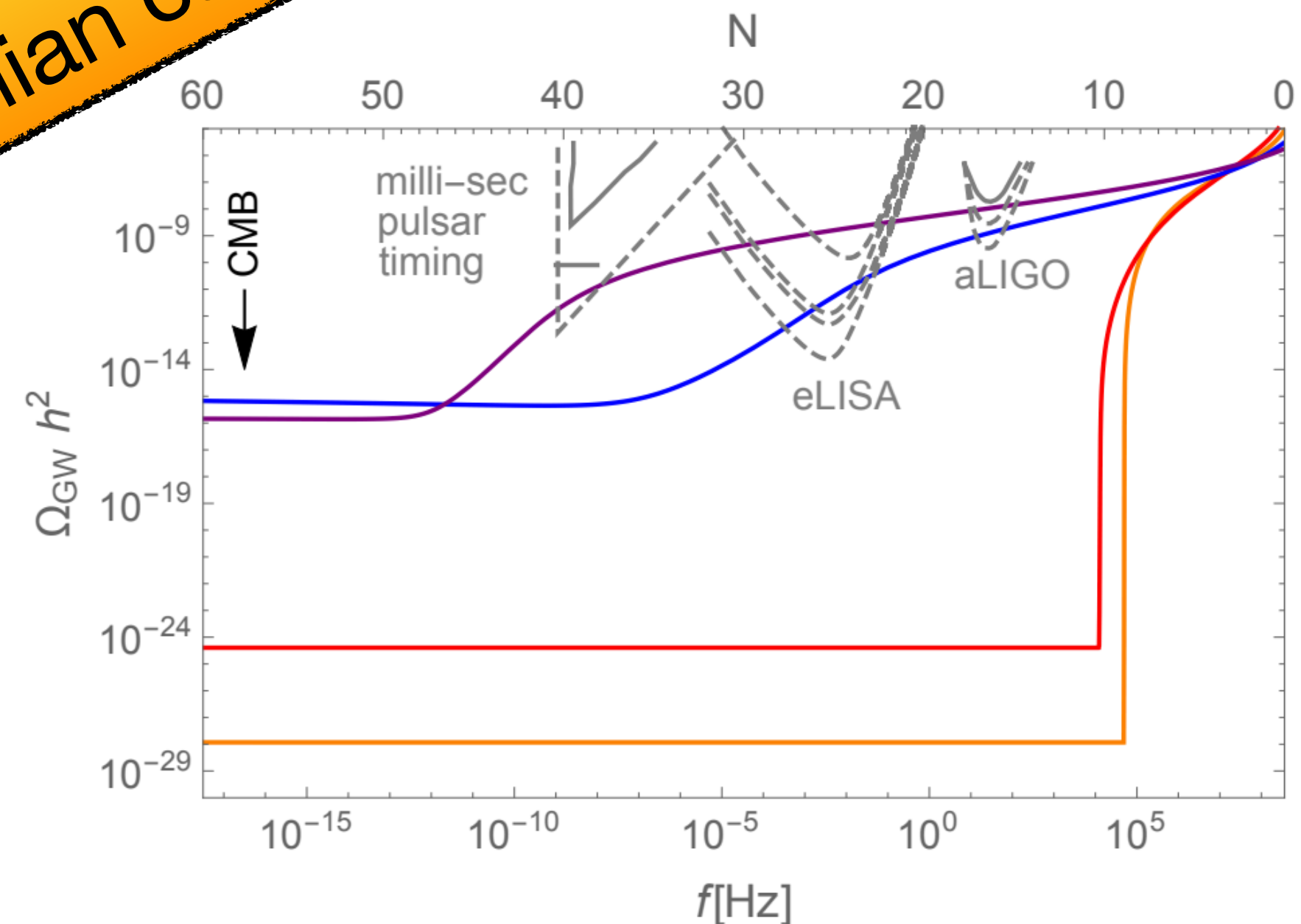
Absent in thermal non-abelian case!

- Abelian case: exponential growth of one helicity mode of the vector field  $\Rightarrow$  GW, PBH, CMB non-gaussianities...

[Sorbo: 1101.1525;  
Cook, Sorbo: 1101.1525;  
Barnaby, Pajer, Peloso: 1110.3327;  
Domcke, Pieroni, Binétruy: 1603.01287...]

- Discussion about back-reaction [... Figuera et al.: 2303.17436]

- Non-Abelian case: thermalisation assumption simplifies the back-reaction modeling!



[Domcke: 1605.06364;  
Domcke, Pieroni, Binétruy: 1603.01287]