

QCD Baryogenesis

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SI, T. Tait, PRL (2019), 122, 112001, *arXiv:1811.00559*

D. Croon, J. Howard, SI, T. Tait, PRD 101 (2020) 5, 055042 *arXiv:1911.01432*

S.A.R. Ellis, SI, G. White, JHEP 08 (2019) 002, *arXiv:1905.11994*

D. Berger, SI, T. Tait, M. Waterbury, JHEP 07 (2020) 192

SM QCD cannot explain the matter asymmetry

There can be large CP violation
in the strong sector (axion)



BUT

NO
baryon number
violation!



NO
1st order
phase transition*

*will come back to this soon

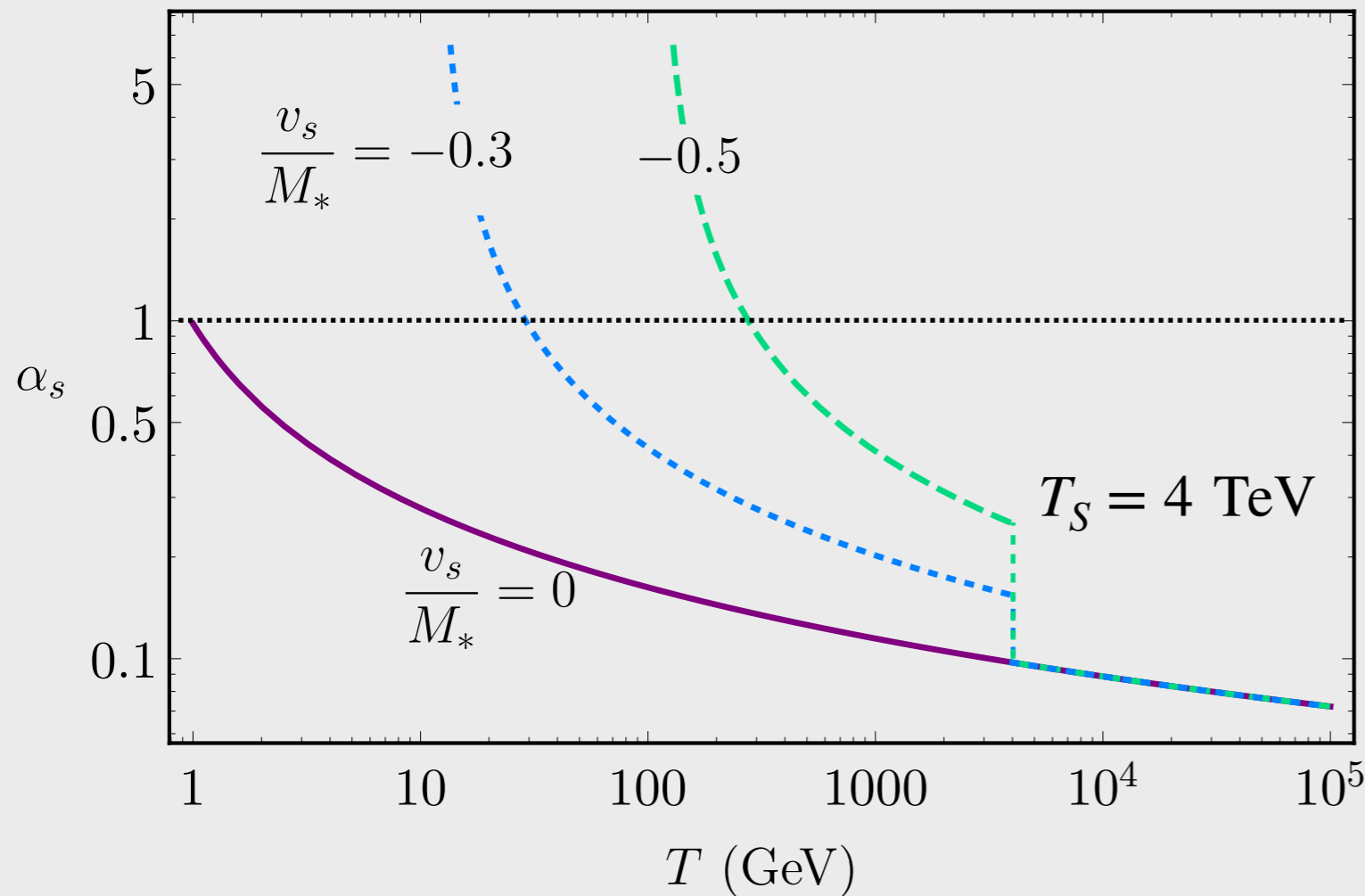
We don't know anything about what happened before Big Bang Nucleosynthesis ($T \sim \text{MeV}$, $t \sim \text{sec}$)

What if QCD was different in the early Universe?

SI, T. Tait, PRL (2019), 122, 112001, *arXiv: 1811.00559*

We can change QCD! - in the early universe

Confinement scale changes with new particles if they interact via strong interactions!



$$\mathcal{L} \supset \left(\frac{1}{g_s^2} + \frac{S}{M_*} \right) G^{\mu\nu} G_{\mu\nu}$$



$$\frac{1}{g_{\text{eff}}^2} = \frac{1}{g_s^2} + \frac{v_S}{M_*}$$

$$\Lambda_{\text{QCD}} \simeq \Lambda_{\text{QCD}}^{\text{SM}} \times \exp \left(\frac{24\pi^2}{2N_f - 33} \frac{v_S}{M_*} \right)$$

currently

$$\Lambda_{\text{QCD}} \sim 400 \text{ MeV}$$



billions of years ago

$$\Lambda_{\text{QCD}} \sim 400 \text{ GeV}$$



Things that depend on the QCD scale will be
different in the early Universe

$$\text{pions} \sim \mathcal{O}(100 \text{ MeV})$$

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If QCD confines before EW symmetry breaking:

Above confinement: 6 massless quarks

Below confinement: quarks are no more! we have mesons

chiral symmetry breaking: $SU(6)_L \times SU(6)_R \rightarrow SU(6)_{\text{diag}}$

$$\mathcal{L}_{\text{ch}} \supset \frac{f_\pi^2}{4} \text{Tr}[\partial_\mu U \partial^\mu U] + \kappa \text{Tr}[U M]$$

the pion matrix $U(x) = e^{2iT^a \Pi^a(x)/f_\pi}$

➔ $\mathcal{L}_{\text{ch}} \supset \sqrt{2} \kappa y_t h - \frac{\kappa}{f_\pi^2} \text{tr}[\{T^a, T^b\} M] \pi^a \pi^b$

$$M = \frac{h}{\sqrt{2}} \text{diag}(y_u, y_d, y_s, y_c, y_b, y_t) \quad \text{quark mass matrix}$$



SM QCD

confinement ~ 400 MeV

mass of up/down quarks $< \Lambda_{\text{QCD}}^{\text{SM}}$

$$\text{pion masses: } m_{\pi^0}^2 = \frac{2\kappa_0(m_u + m_d)}{f_{\pi^0}^2}$$

QCD quantities:

$$\kappa_0 \simeq (225 \text{ MeV})^3$$

$$f_{\pi^0} \simeq 94 \text{ MeV}$$

New physics QCD



confinement ~ 400 GeV

all quarks are lighter than $\Lambda_{\text{QCD}}^{\text{new}}$

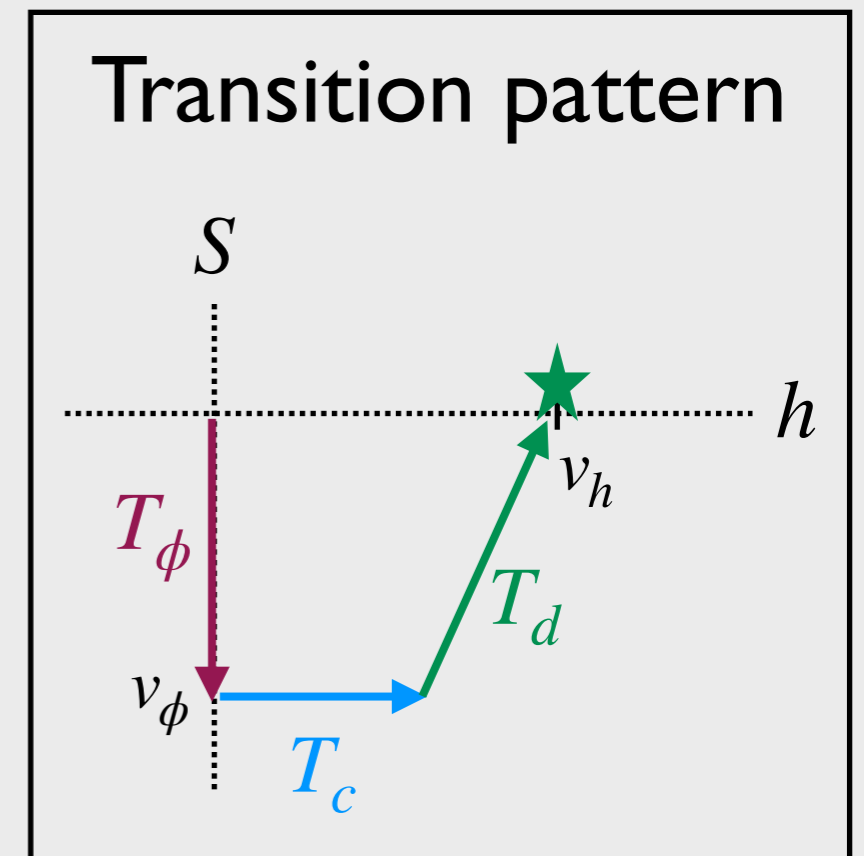
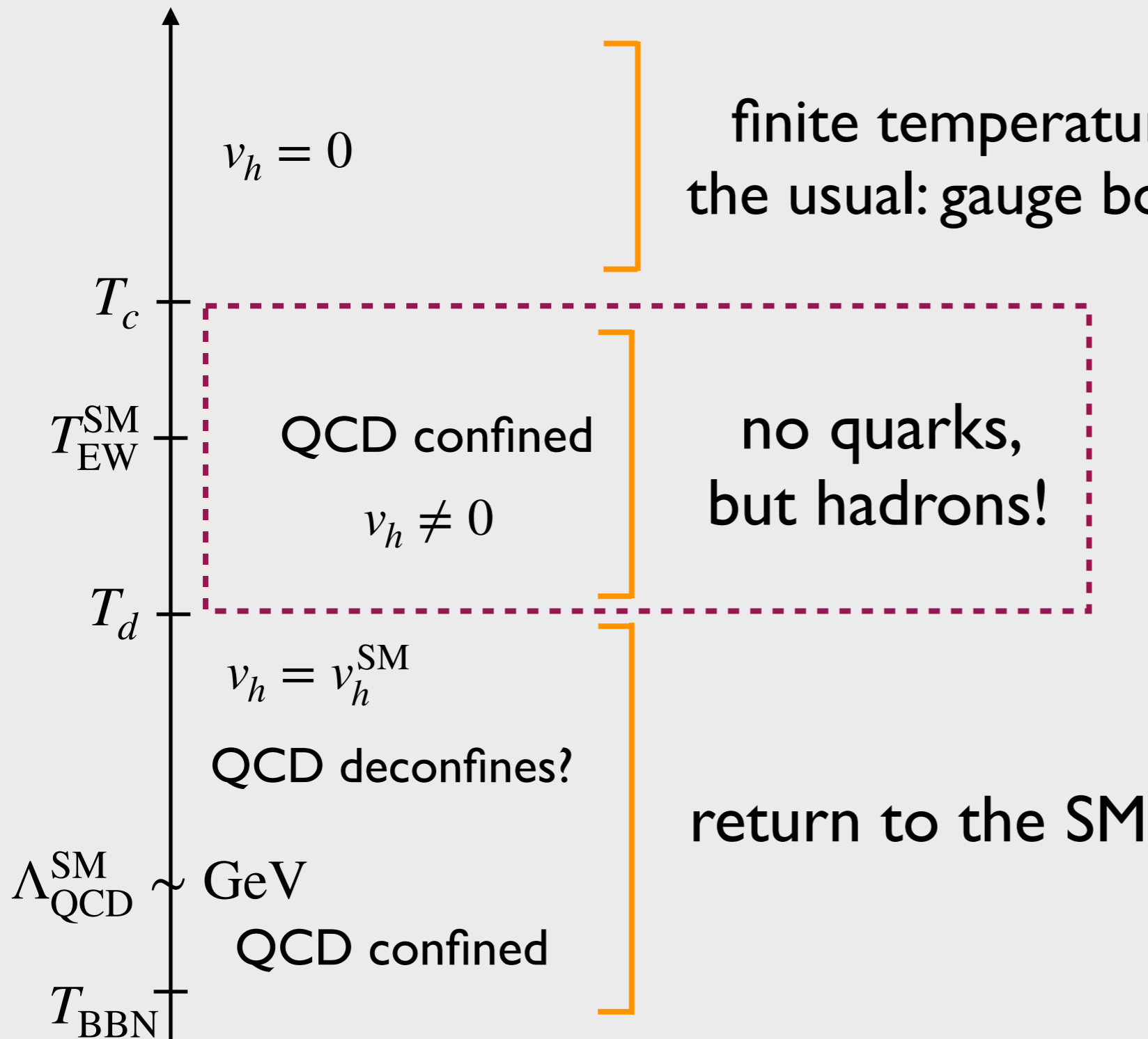
pions are heavier:

$$m_{\pi}^2 \simeq m_{\pi^0}^2 \left(\frac{v_h}{v_h^{\text{SM}}} \right)^{\xi} \quad \text{Higgs vev}$$

$$\kappa \simeq \kappa_0 \xi^3$$

$$f_{\pi} \simeq f_{\pi^0} \xi$$

$$\text{with } \xi \equiv \frac{\Lambda_{\text{QCD}}^{\text{new}}}{\Lambda_{\text{QCD}}^{\text{SM}}}$$



Thermal potential in the confined phase

- Higgs gets a tadpole term from the meson mass-term

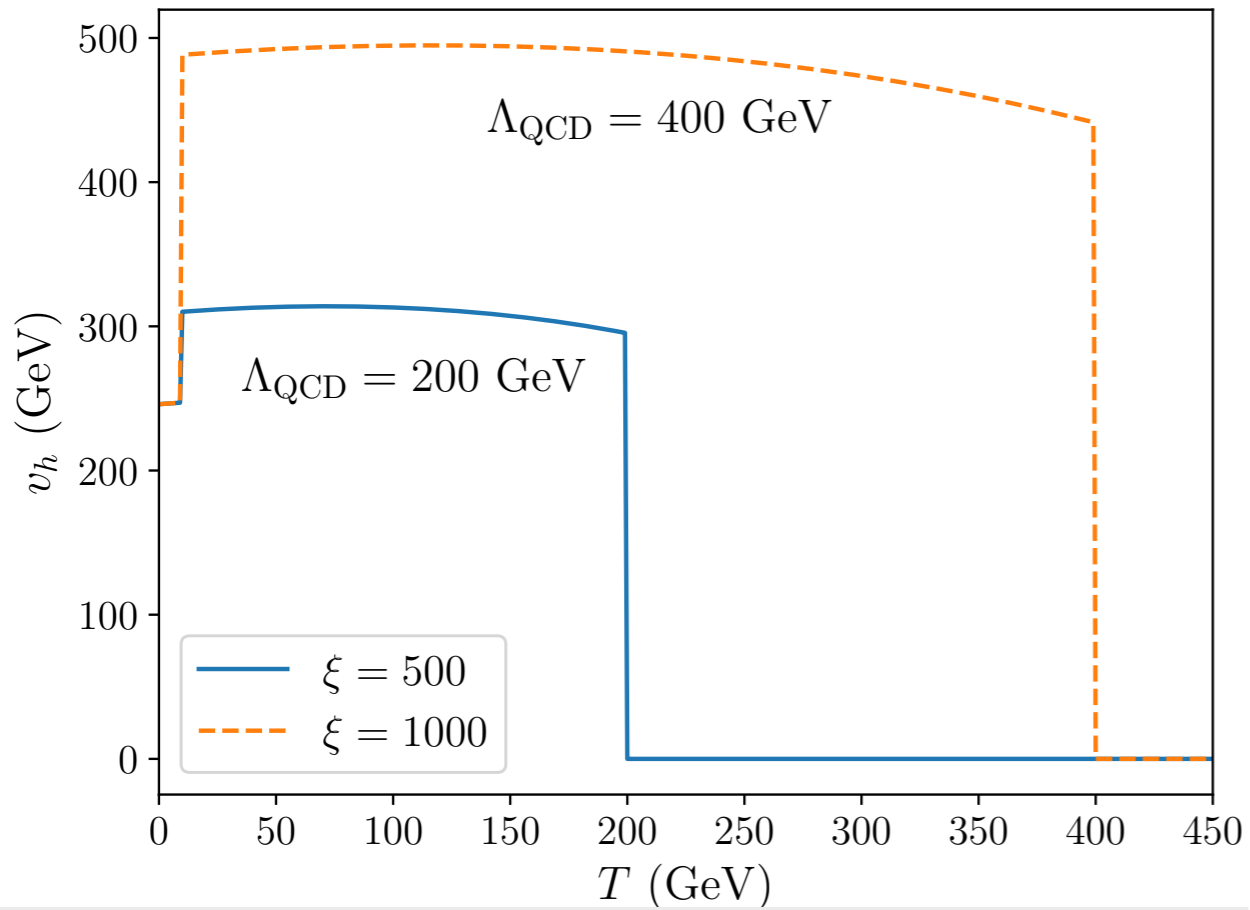
$$V_{\text{tad}}(v_h) \simeq \kappa \frac{y_t}{\sqrt{2}} v_h \simeq -0.0158 \text{ GeV}^3 \left(\frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{QCD}}^{\text{SM}}} \right)^3 v_h$$

- Thermal corrections to the Higgs potential from mesons

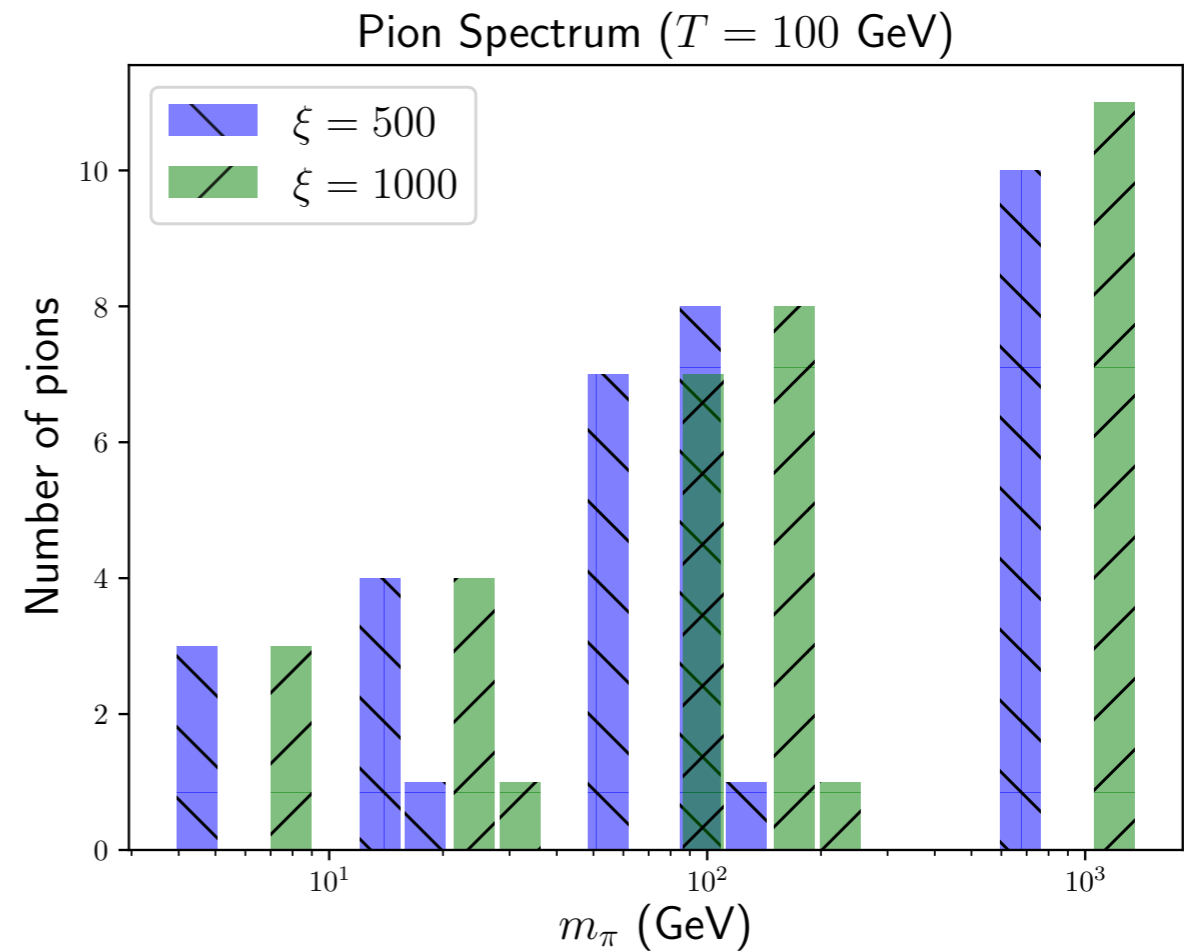
$$V_{\text{meson}}(v_h, T) = \sum_{i=1\dots 35} \frac{T^4}{2\pi^2} J_B \left(\frac{m_i^2}{T^2} \right)$$
$$J_B(m^2) = \int_0^\infty dx x^2 \log \left(1 - e^{-\sqrt{x^2 + m^2}} \right)$$

- The gluon condensate contributes to the singlet potential

$$\frac{S}{M_*} \langle GG \rangle \longrightarrow V_{\text{GC}}(v_S) \simeq \frac{v_S}{4M_*} \Lambda_{\text{QCD}}^4$$



Higgs vev is larger than its SM value!



$$\xi = \frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{QCD}}^{\text{SM}}}$$

$$m_\pi^2 \simeq m_{\pi 0}^2 \left(\frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{QCD}}^{\text{SM}}} \right) \left(\frac{v_h}{v_h^{\text{SM}}} \right)$$

New scalar can interact with the Higgs boson

$$V_{\text{scalar}} = -\mu^2 |H|^2 + \lambda_h |H|^4 + a_2 S^2 + a_3 S^3 + a_4 S^4 - b_1 S |H|^2 + b_2 S^2 |H|^2$$

New QCD cosmology



Baryogenesis!

D. Croon, J. Howard, **SI**, T. Tait, *Phys.Rev.D* 101 (2020) 5, 055042 [arXiv:1911.01432](https://arxiv.org/abs/1911.01432)

$$T = T_c$$

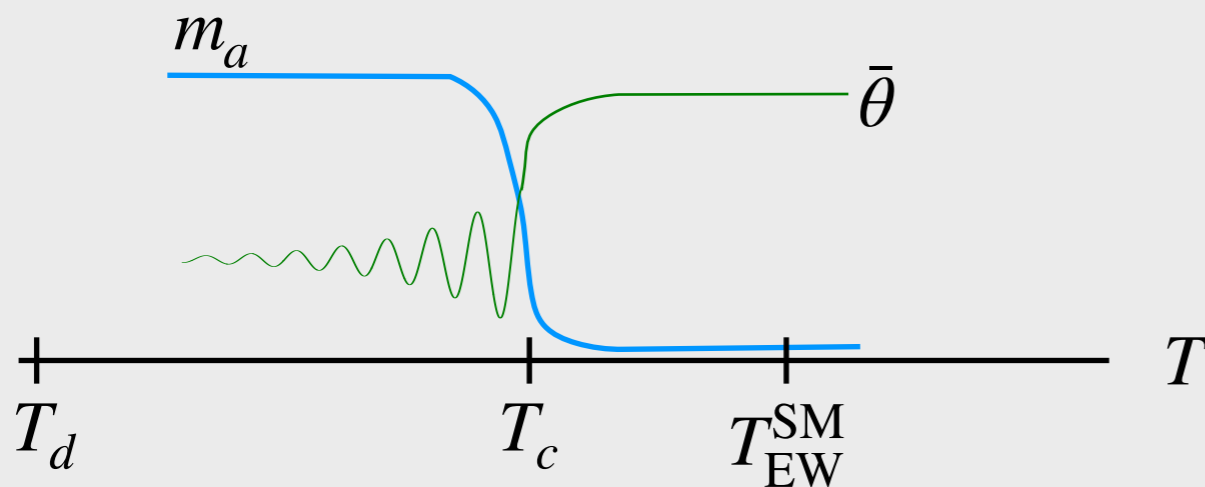
QCD has CP violation!

$$\mathcal{L} \supset \bar{\theta} G^{\mu\nu} \tilde{G}_{\mu\nu}$$

Axions!

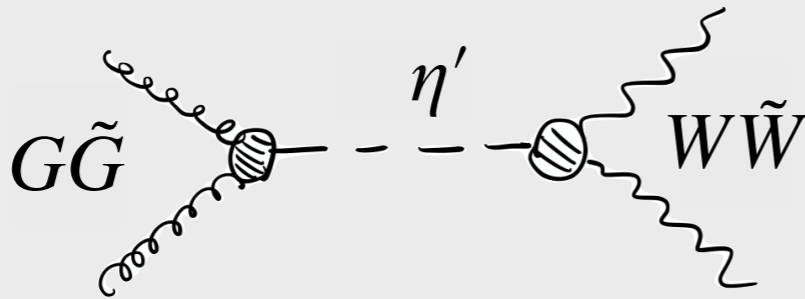
$$m_a^2(T) f_a^2 \simeq \begin{cases} m_\pi^2 f_\pi^2 \zeta \left(\frac{\Lambda_{\text{QCD}}}{T} \right)^n & T > T_c \\ m_\pi^2 f_\pi^2 & T < T_c \end{cases}$$

has small mass at high T
T-dependence given by number of light flavors, etc



How about B violation?

$$T = T_c$$



$$\partial_\mu j_B^\mu = \frac{\alpha_W}{8\pi} \text{Tr}[W\tilde{W}]$$

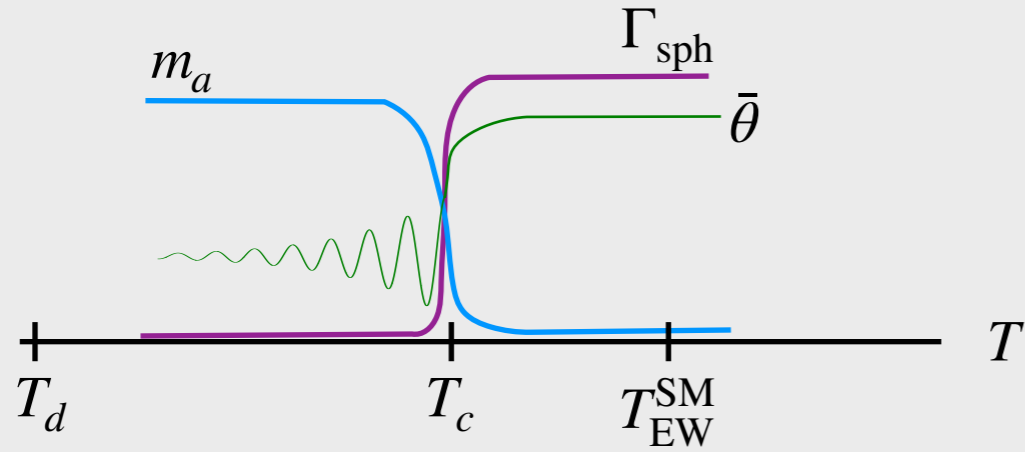
$$\Gamma_B \sim 25\alpha_W^5 T^4$$

$$\mathcal{L}_{\text{eff}} = \frac{10}{f_\pi^2 m_{\eta'}^2} \left[\frac{\alpha_s}{8\pi} \langle G\tilde{G} \rangle \right] \left[\frac{\alpha_W}{8\pi} W\tilde{W} \right]$$

anomalous baryon current

generates a chemical potential

$$\frac{\alpha_s}{8\pi} \langle G\tilde{G} \rangle = m_a^2(T) f_a^2 \sin \bar{\theta} \quad \longrightarrow \quad \mu = \frac{10}{f_\pi^2 m_{\eta'}^2} \frac{d}{dt} \left[m_a^2(T) f_a^2 \sin \bar{\theta}(T) \right]$$



Spontaneous baryogenesis

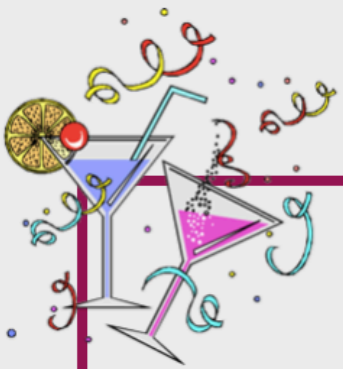
A. Cohen, D. Kaplan, Nucl. Phys. B308 (1988) 913–928

Baryon asymmetry of the universe

Number of baryons: $n_B = \int_{t_i}^{t_f} dt \frac{\Gamma_B}{T} \mu$

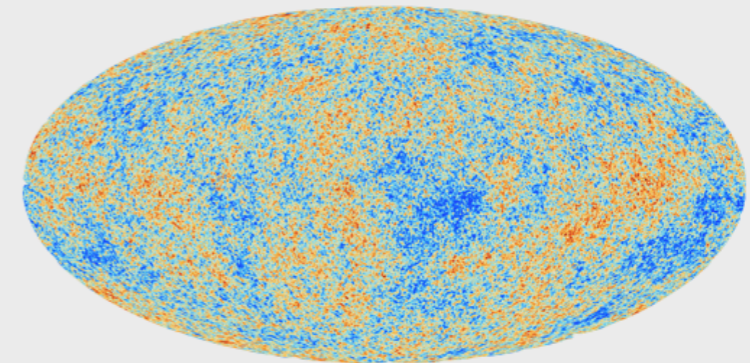
Baryon-to-entropy ratio $\eta = \frac{n_B}{s} \simeq \frac{5625}{2\pi^2 \underbrace{g_*(T_{\text{reh}})}_{\sim 45}} \alpha_w^5 \sin \bar{\theta} \frac{\overbrace{\Delta [m_a^2(T) f_a^2]}^{\sim m_\pi^2 f_\pi^2}}{f_\pi^2 m_{\eta'}^2} \left(\frac{T_{\text{sph}}}{T_{\text{reh}}} \right)^3$

$$4.4 \times 10^{-9} \sin \bar{\theta} \left(\frac{v_h}{v_h^0} \right) \left(\frac{\Lambda_{\text{QCD}}^{\text{SM}}}{\Lambda_{\text{QCD}}} \right)$$



$$\eta \sim 10^{-11} \overbrace{\sin \bar{\theta}}^{\sim 1} \frac{\overbrace{v_h}^{\sim 4}}{\Lambda_{\text{QCD}}} \left(\frac{\overbrace{T_{\text{sph}}}{> 1}}{T_{\text{reh}}} \right)^3$$

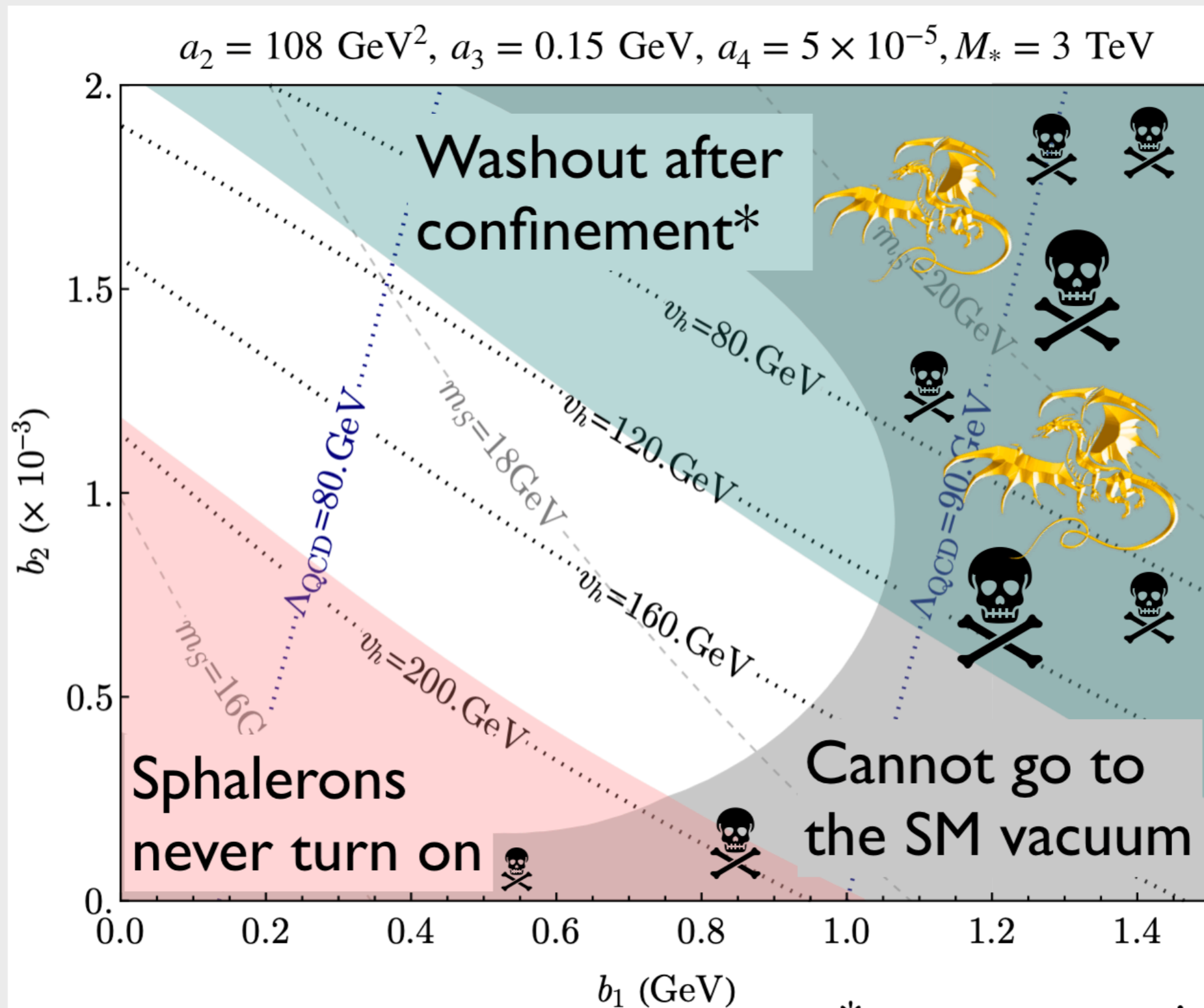
$$\eta_{\text{obs}} \simeq 8.5 \times 10^{-11}$$



fix (6 benchmark scenarios)

vary

$$V_0 = -\mu^2 |H|^2 + \lambda_h |H|^4 + a_2 S^2 + a_3 S^3 + a_4 S^4 - b_1 S |H|^2 + b_2 S^2 |H|^2$$

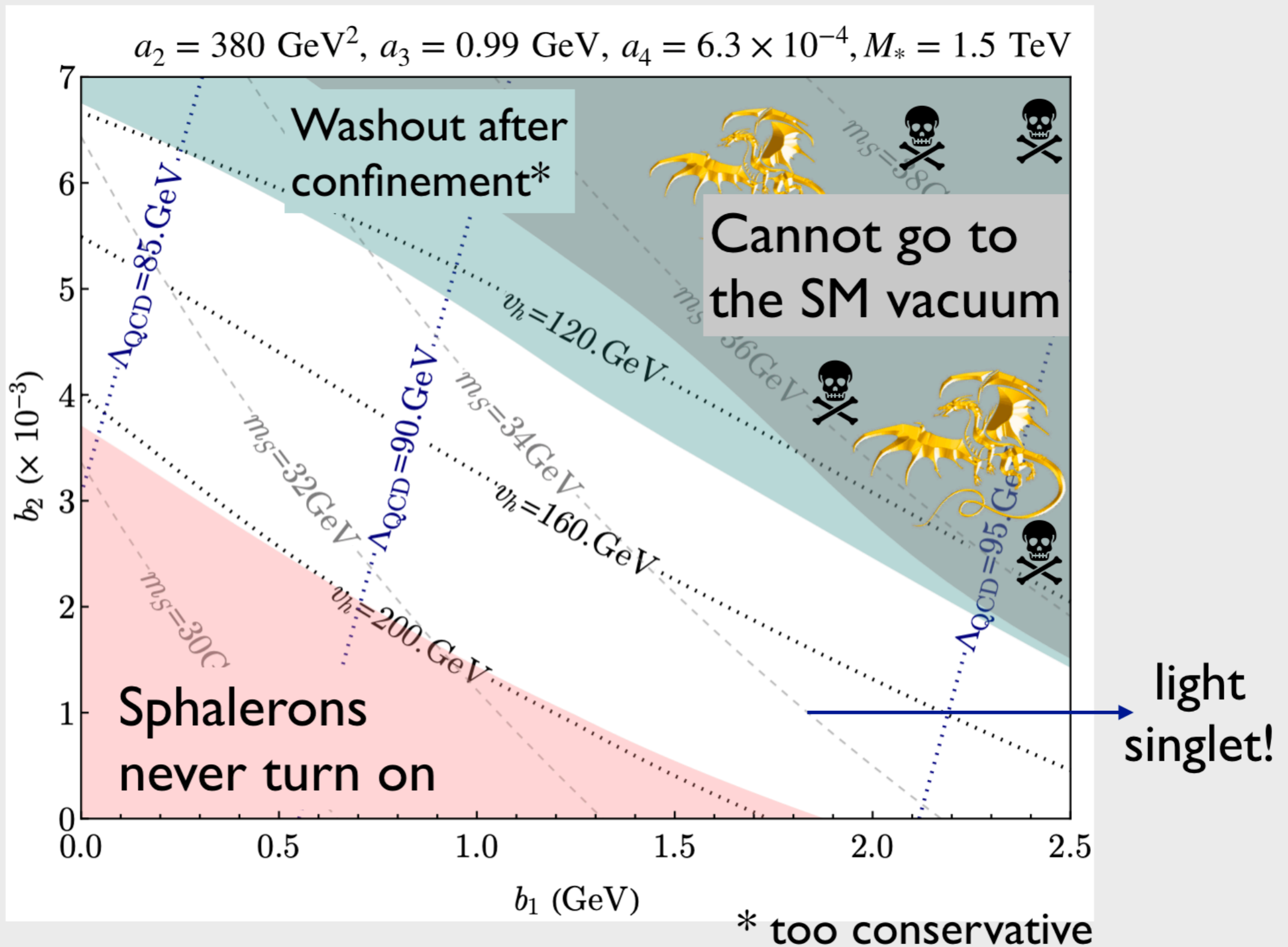


* too conservative

fix (6 benchmark scenarios)

vary

$$V_0 = -\mu^2 |H|^2 + \lambda_h |H|^4 + a_2 S^2 + a_3 S^3 + a_4 S^4 - b_1 S |H|^2 + b_2 S^2 |H|^2$$



Interested in $m_S \sim O(10 \text{ GeV})$

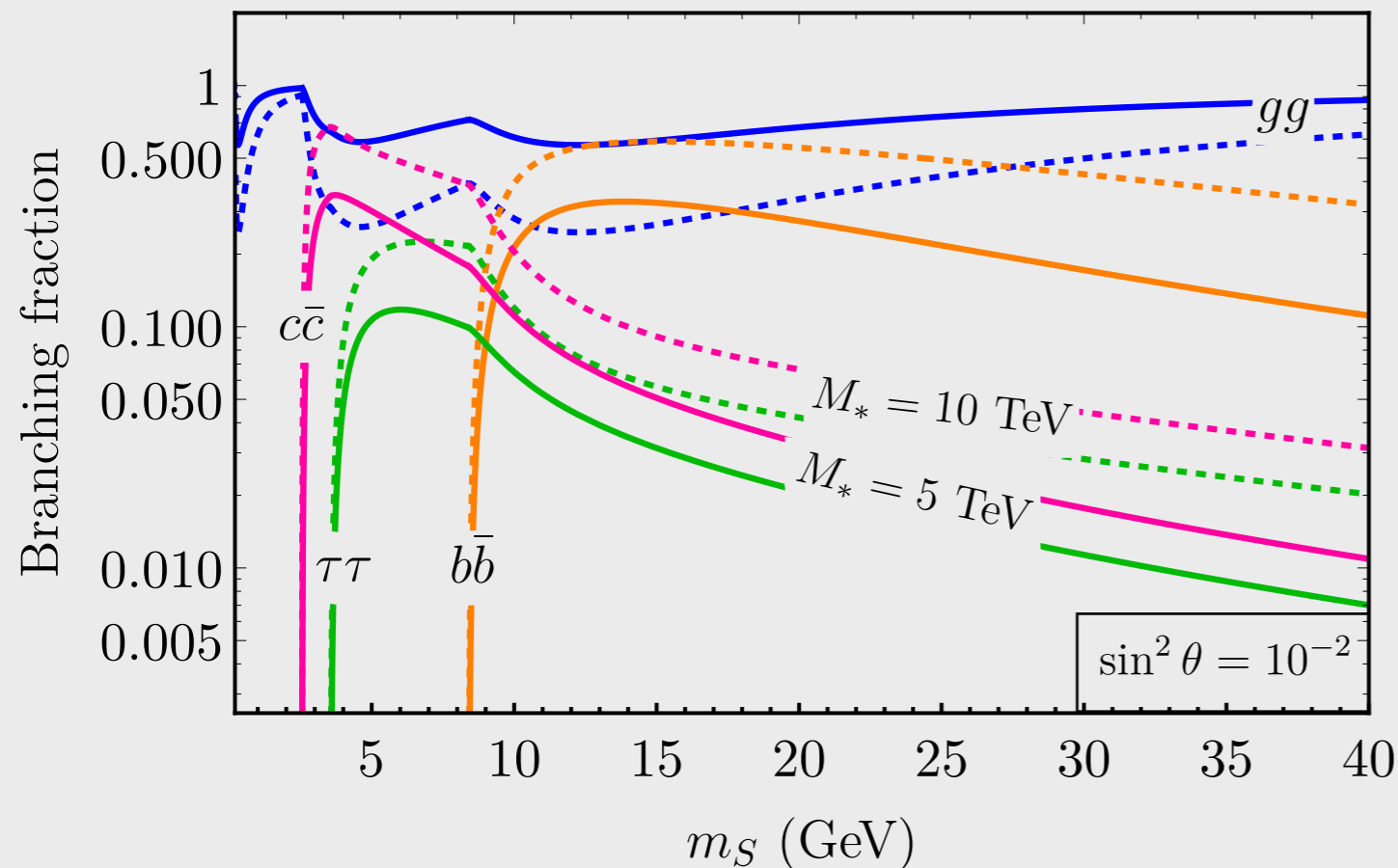
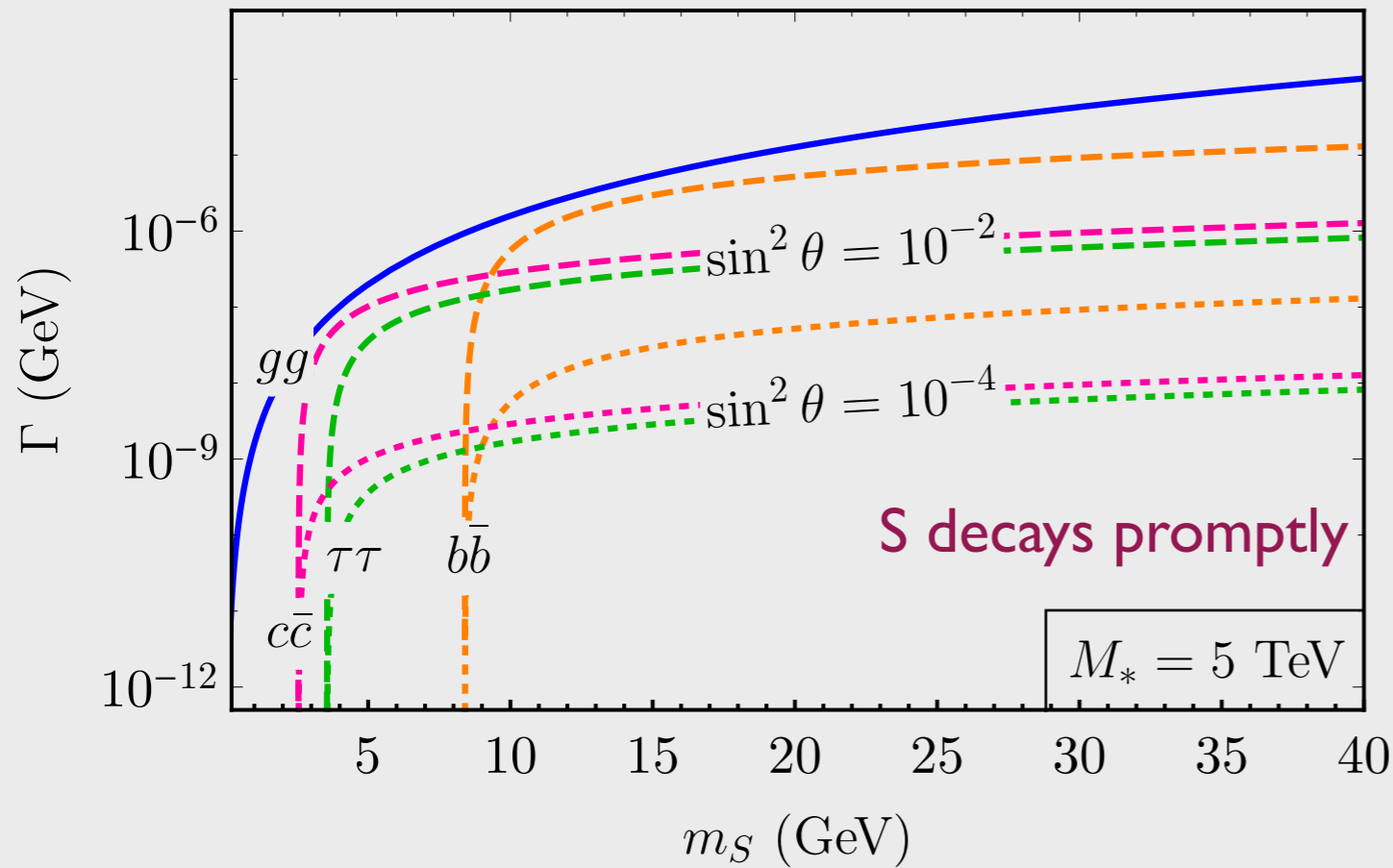
Singlet decays

1) gluons via $(S/M_*)GG$

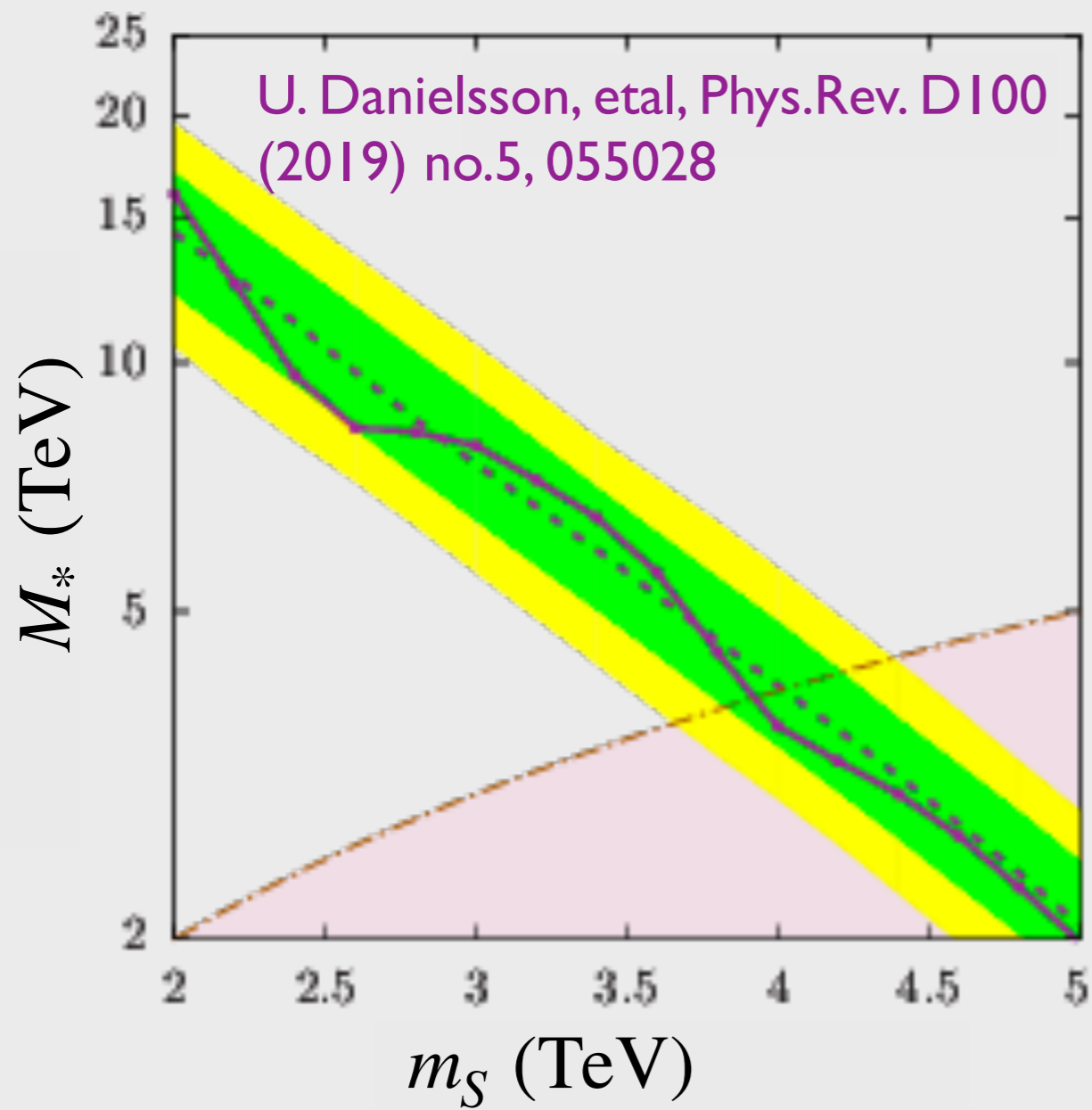
$$\Gamma(S \rightarrow gg) \simeq \frac{m_S^3}{8\pi M_*^2}$$

2) quarks and leptons via Higgs mixing

$$\Gamma(S \rightarrow ff) \simeq \frac{N_c y_f^2 \sin^2 \theta m_S}{8\pi} \left(1 - \frac{4m_f^2}{m_S^2}\right)^{3/2}$$

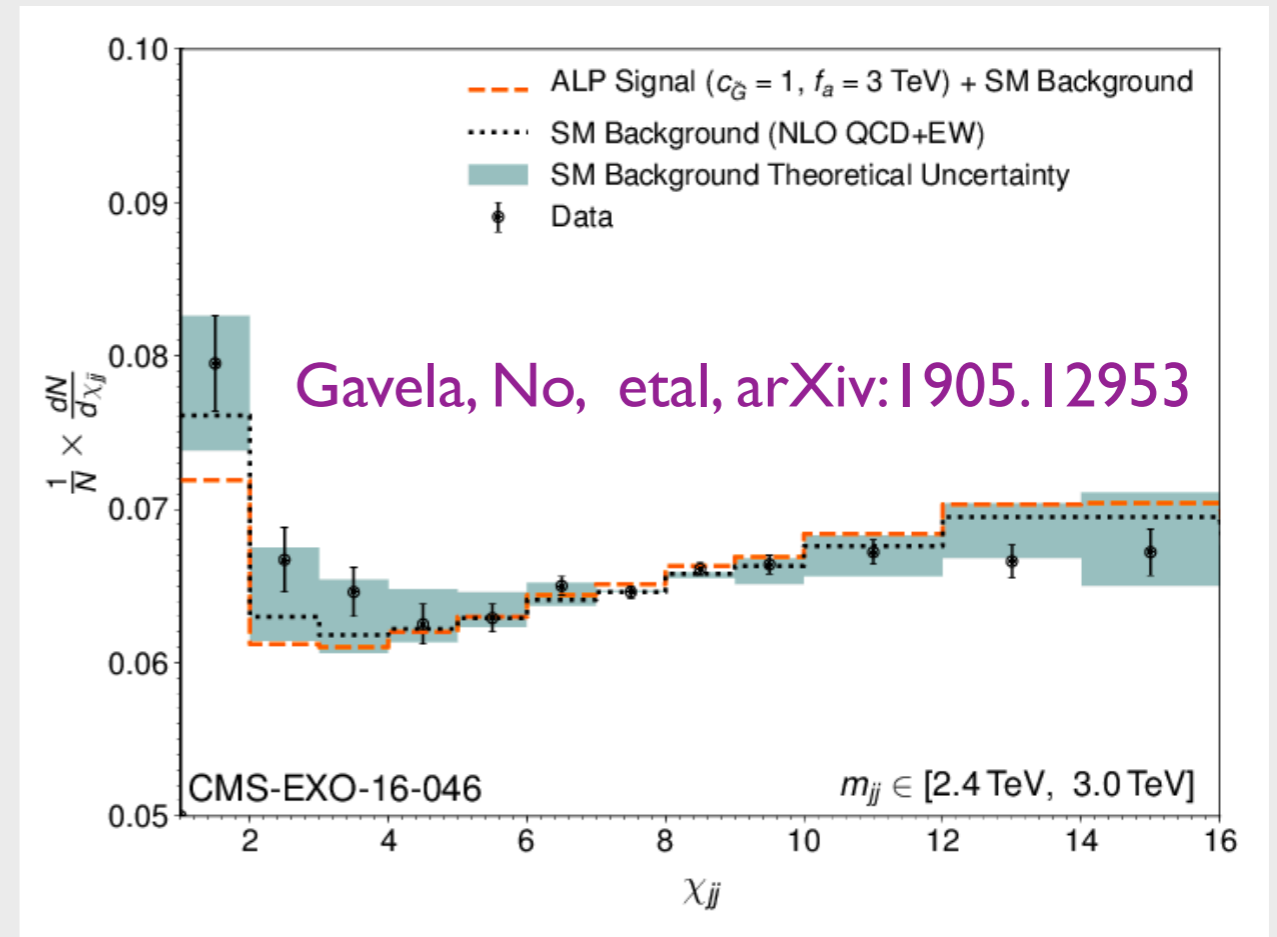


ATLAS dijet resonant searches



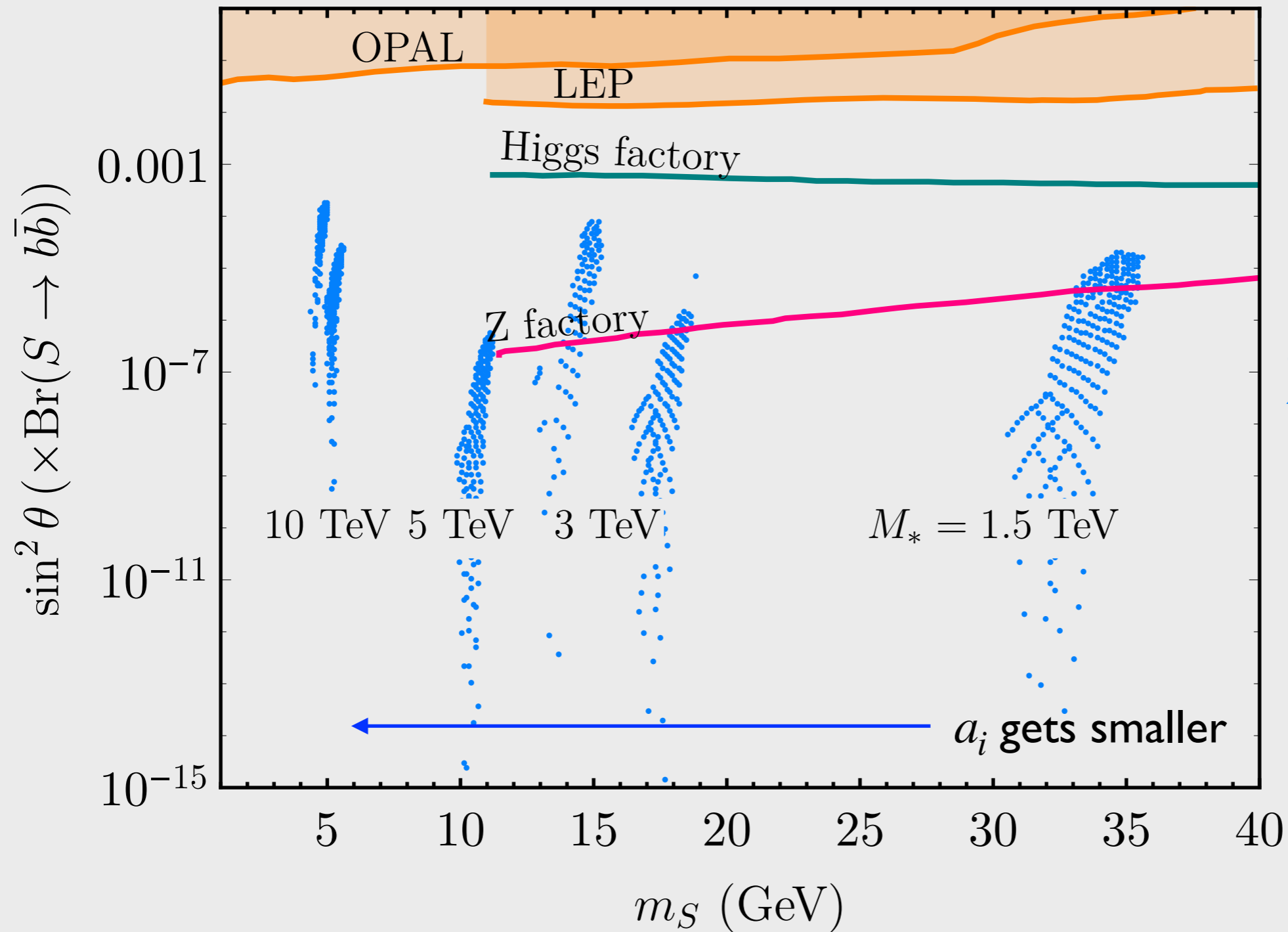
Only for very heavy S!

CMS dijet angular distribution



$M_* > 3$ TeV

This is for ALPs!
Not clear for a scalar



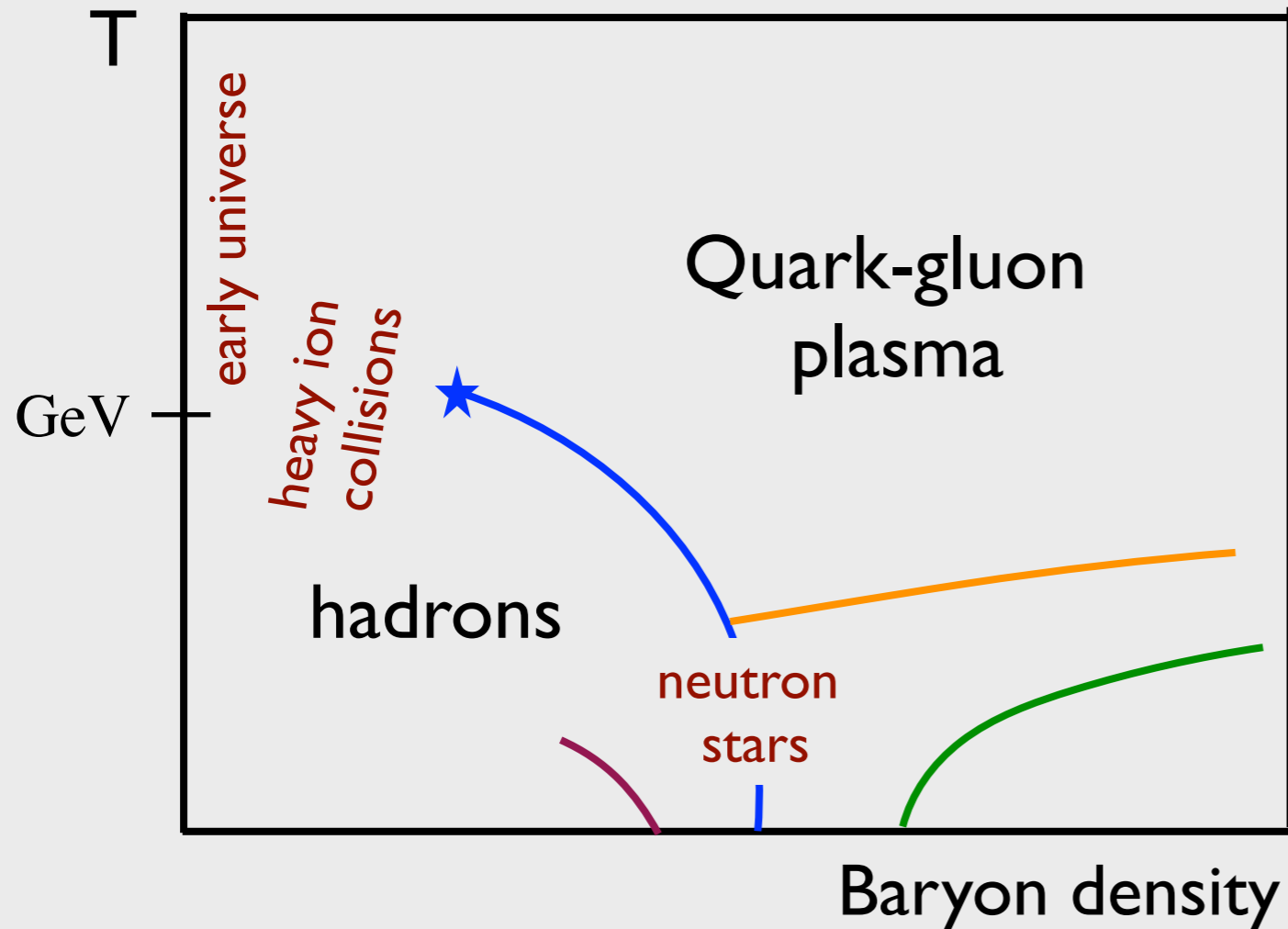
6 benchmark scenarios,
there should be more!

Mixing angle is too small for current searches

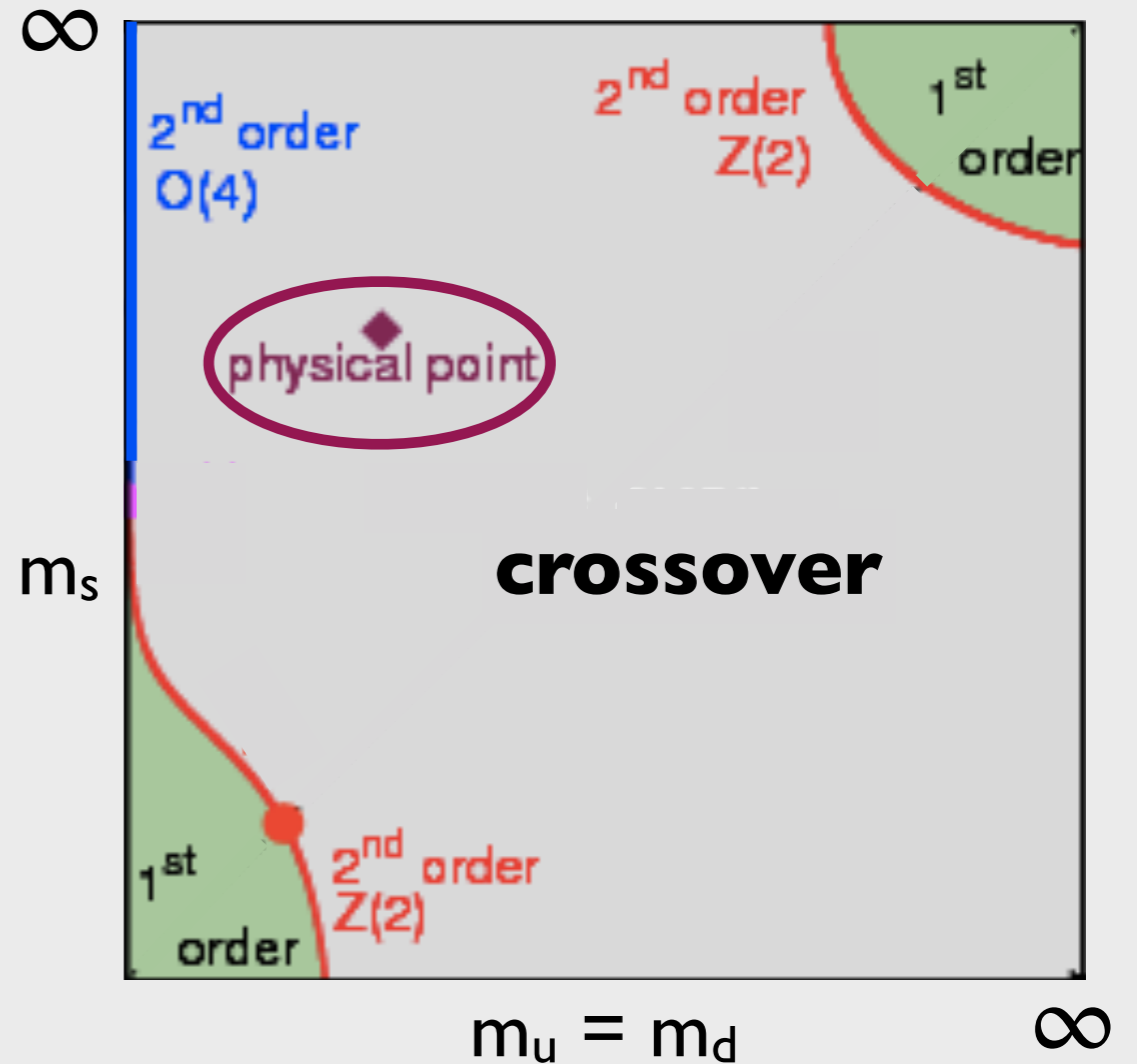
Singlet lighter than $\sim 10 \text{ GeV}$

is hard to constrain since it decays primarily to gluons

QCD Phase Diagram



J. Phys. Conf Ser. 432 012027 (2013)



If 3 or more massless quarks \longrightarrow First order phase transition???

R.D. Pisarski, F.Wilzcek, Phys. Rev. D29 (1984) 338–341

Maybe not :(

F. Cuteri, O. Philipsen, A. Sciarra, *arXiv: 2107.12739*

L. Dini, etal, *arXiv: 2111.12599*

J. Bernhardt, C. Fischer, *arXiv: 2309.06737*

Backup slides

High temperature

$$T > T_{EW} > T_c$$

$$b_1 = 0.7 \text{ GeV}, b_2 = 10^{-3}$$

$$a_2 = 108 \text{ GeV}^2, a_3 = 0.15 \text{ GeV}, a_4 = 5 \times 10^{-5}$$

T = 200 GeV

Finite temperature potential:

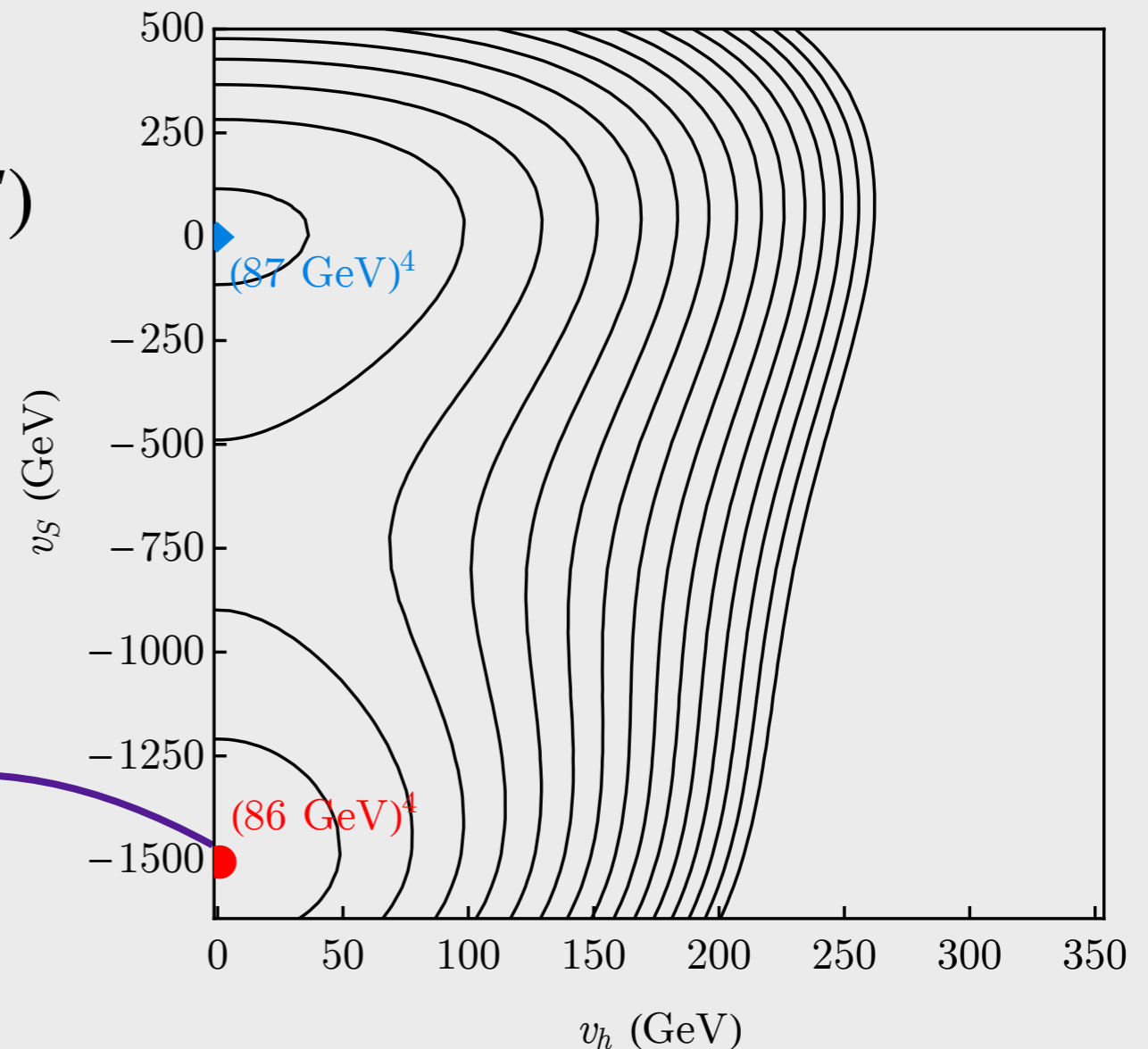
$$V(v_h, v_s, T) = V_0(v_h, v_s) + V_{\text{gauge}}(v_h, T)$$

$$+ V_{\text{top}}(v_h, T)$$

$$V_0 = -\mu^2 |H|^2 + \lambda_h |H|^4$$

$$+ a_2 S^2 + a_3 S^3 + a_4 S^4$$

$$- b_1 S |H|^2 + b_2 S^2 |H|^2$$



vacuum is at $v_s, v_h = 0$

● global minimum

Below EW scale

$$T_{EW} > T > T_c$$

$$b_1 = 0.7 \text{ GeV}, b_2 = 10^{-3}$$

$$a_2 = 108 \text{ GeV}^2, a_3 = 0.15 \text{ GeV}, a_4 = 5 \times 10^{-5}$$

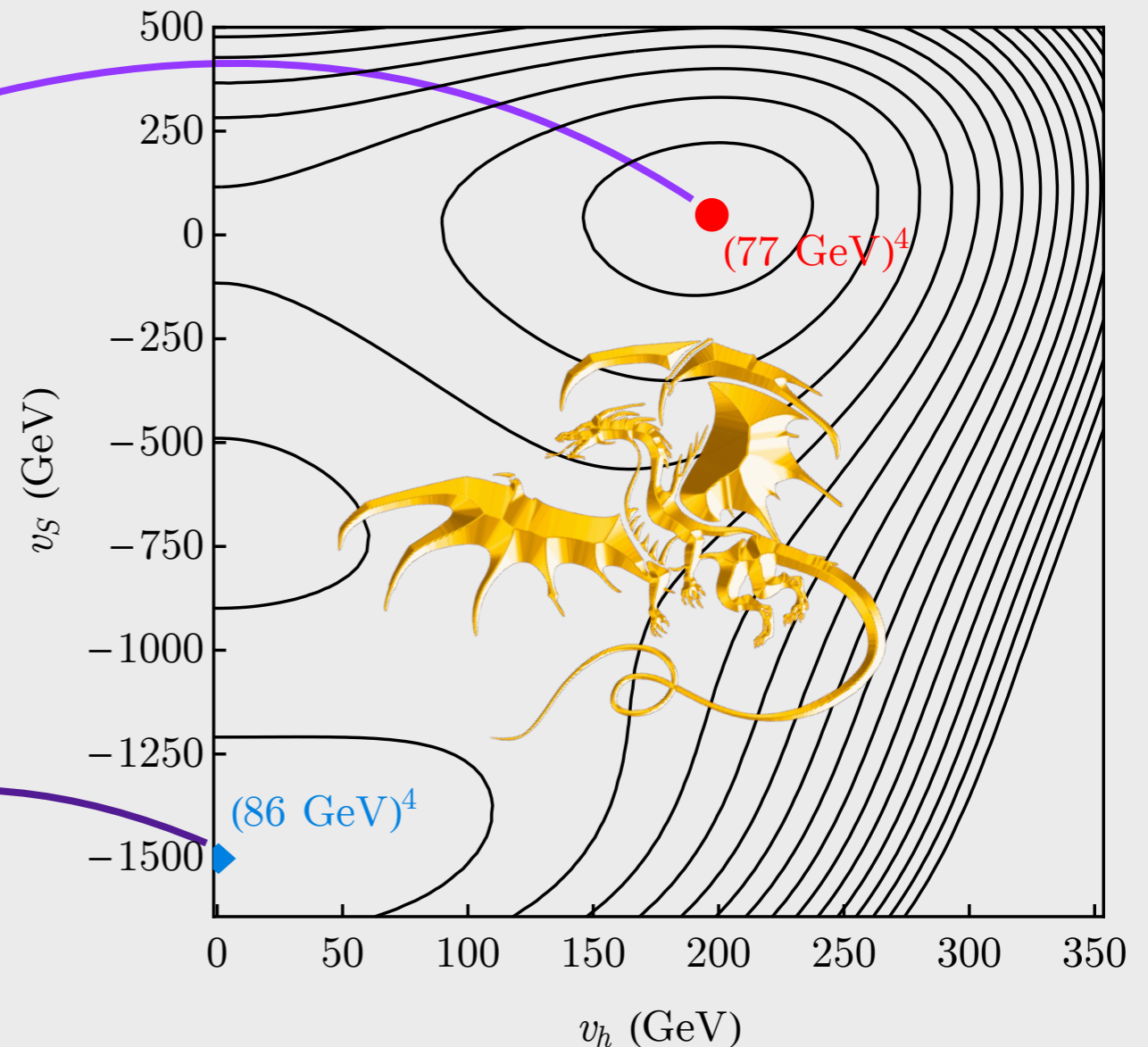
T = 100 GeV

Global minimum is SM-like

There is an impenetrable barrier between the two vacua!

Euclidean bounce action

$$\frac{S_E}{T} \sim \left(\frac{\Delta v_s}{\Delta V(v_s)} \right)^4 \sim 10^{-8}$$



Universe is stuck at $v_s, v_h = 0$

We require: $m_h = 125 \text{ GeV}$
 $v_h^0 = 246 \text{ GeV}$

Below QCD confinement

$$T_d < T \lesssim T_c$$

$$b_1 = 0.7 \text{ GeV}, b_2 = 10^{-3}$$

$$a_2 = 108 \text{ GeV}^2, a_3 = 0.15 \text{ GeV}, a_4 = 5 \times 10^{-5}$$

$$T = \Lambda_{\text{QCD}} = 85 \text{ GeV}$$

$$V(v_h, v_s, T) = V_0(v_h, v_s) + V_{\text{gauge}}(v_h, T)$$

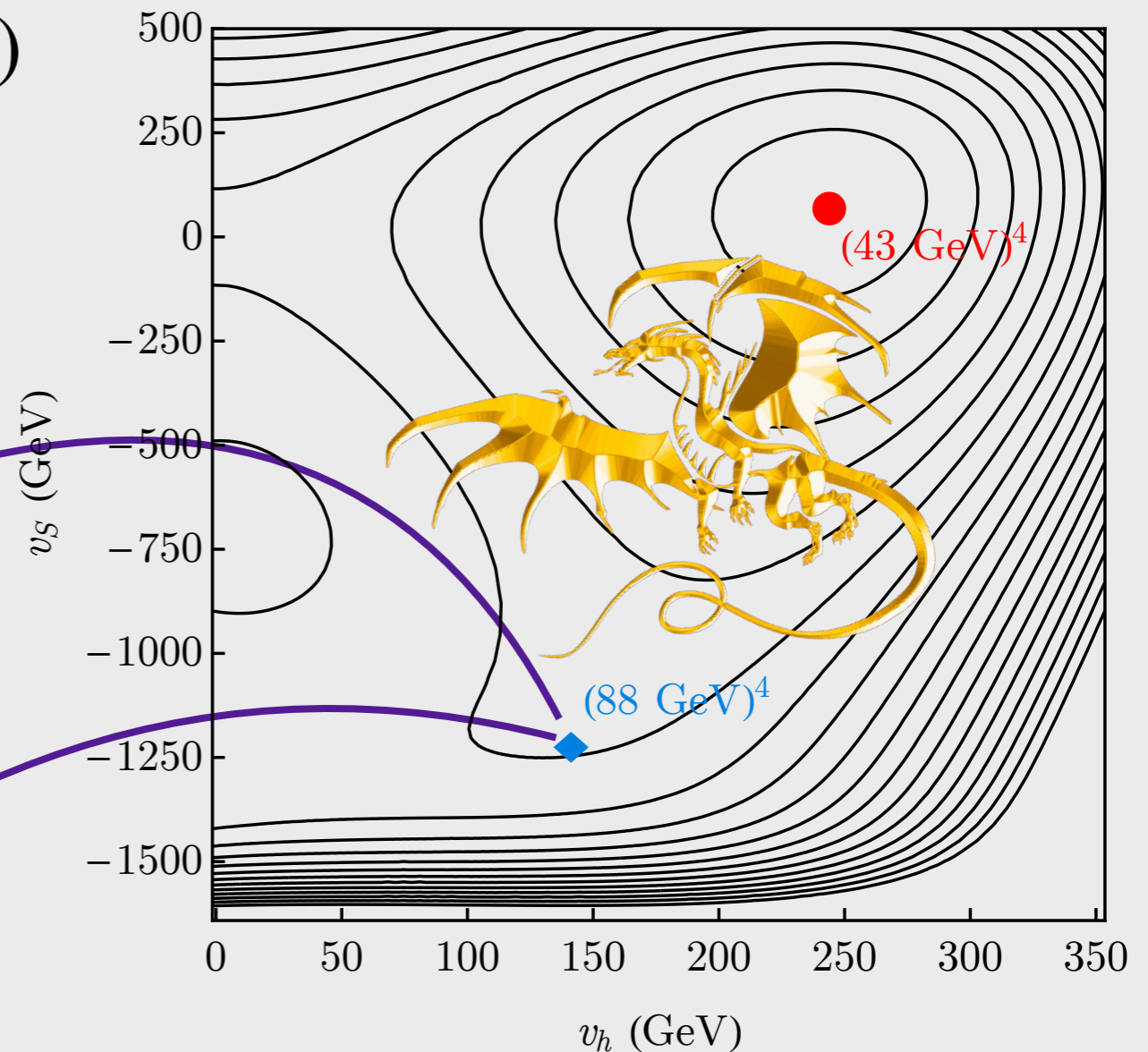
$$+ V_{\text{tad}}(v_h) + V_{\text{GC}}(v_s)$$

$$+ V_{\text{meson}}(v_h, T)$$

QCD confinement tips this vacuum towards finite v_h (but not towards the SM value)

But there is still a barrier between the two vacua!

Universe is stuck at $v_s, v_h < v_h^{\text{SM}}$



Back to the SM

$$T_c > T_d > T$$

Universe has the right Higgs vev and Λ_{QCD}

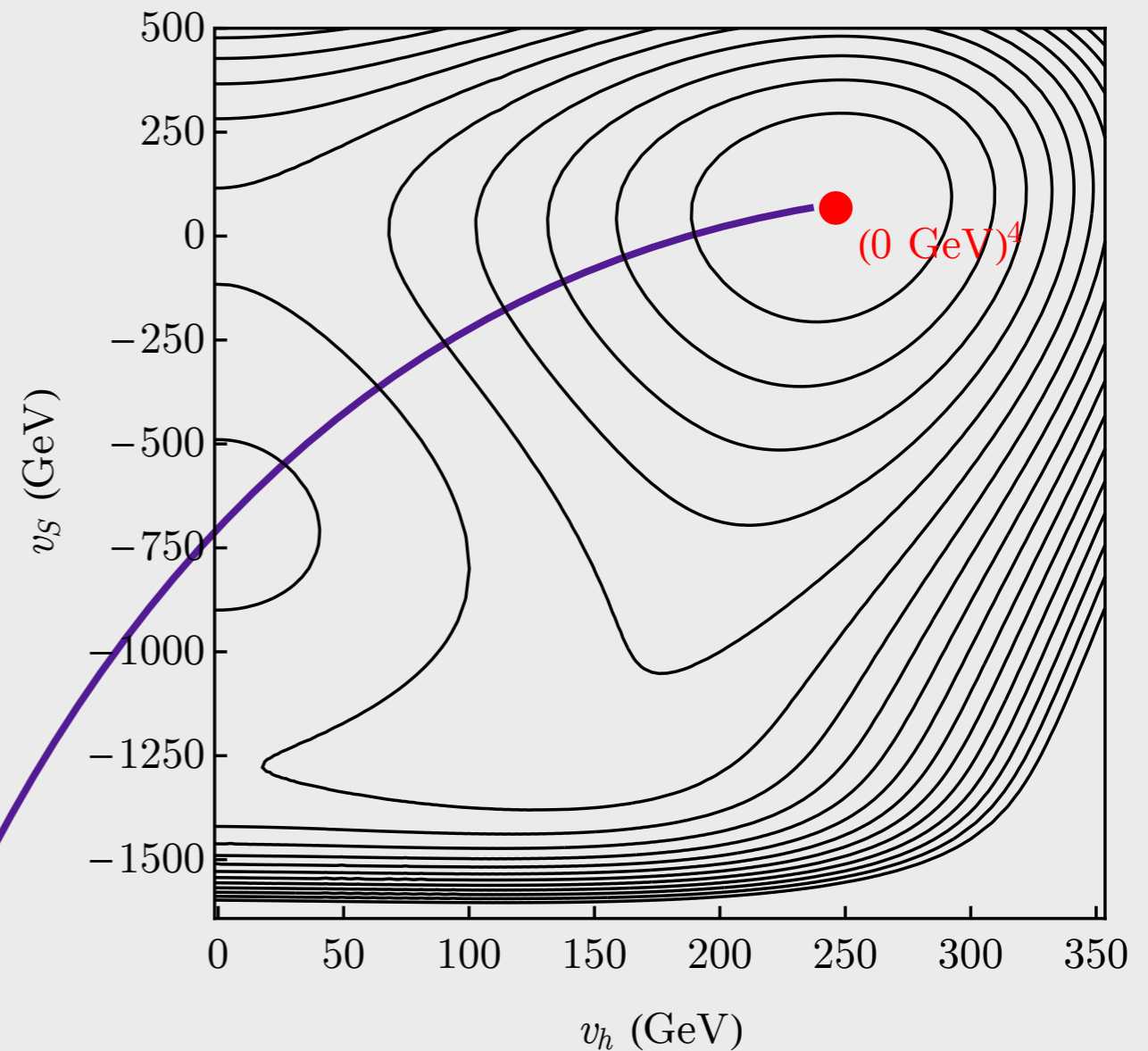
The barrier disappears

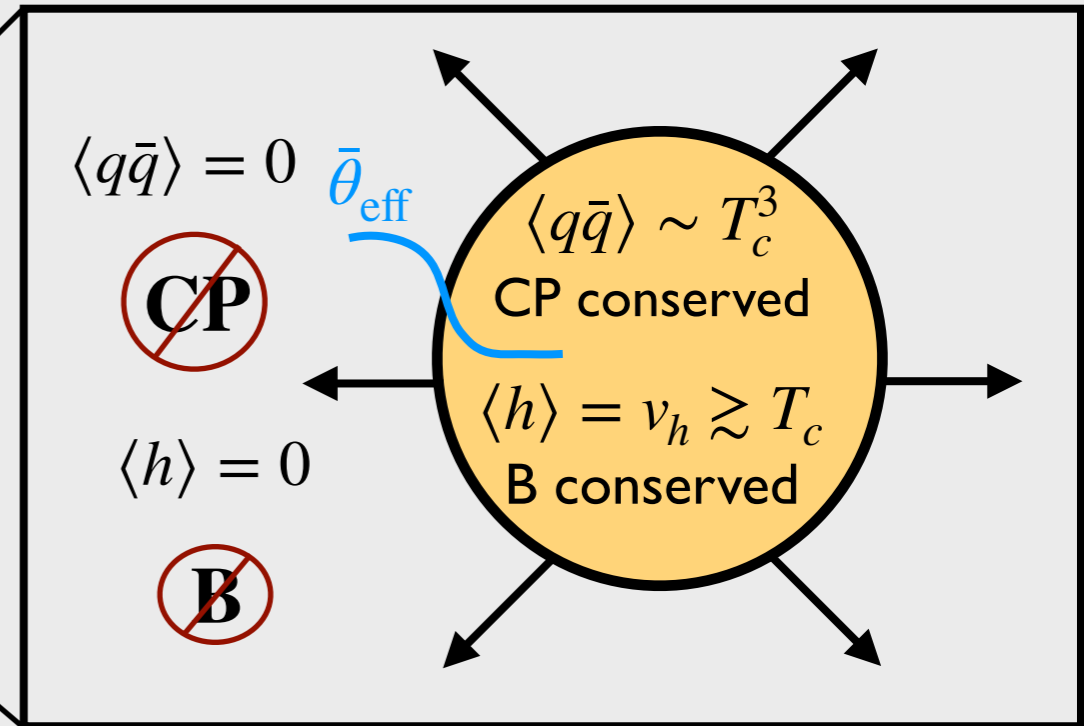
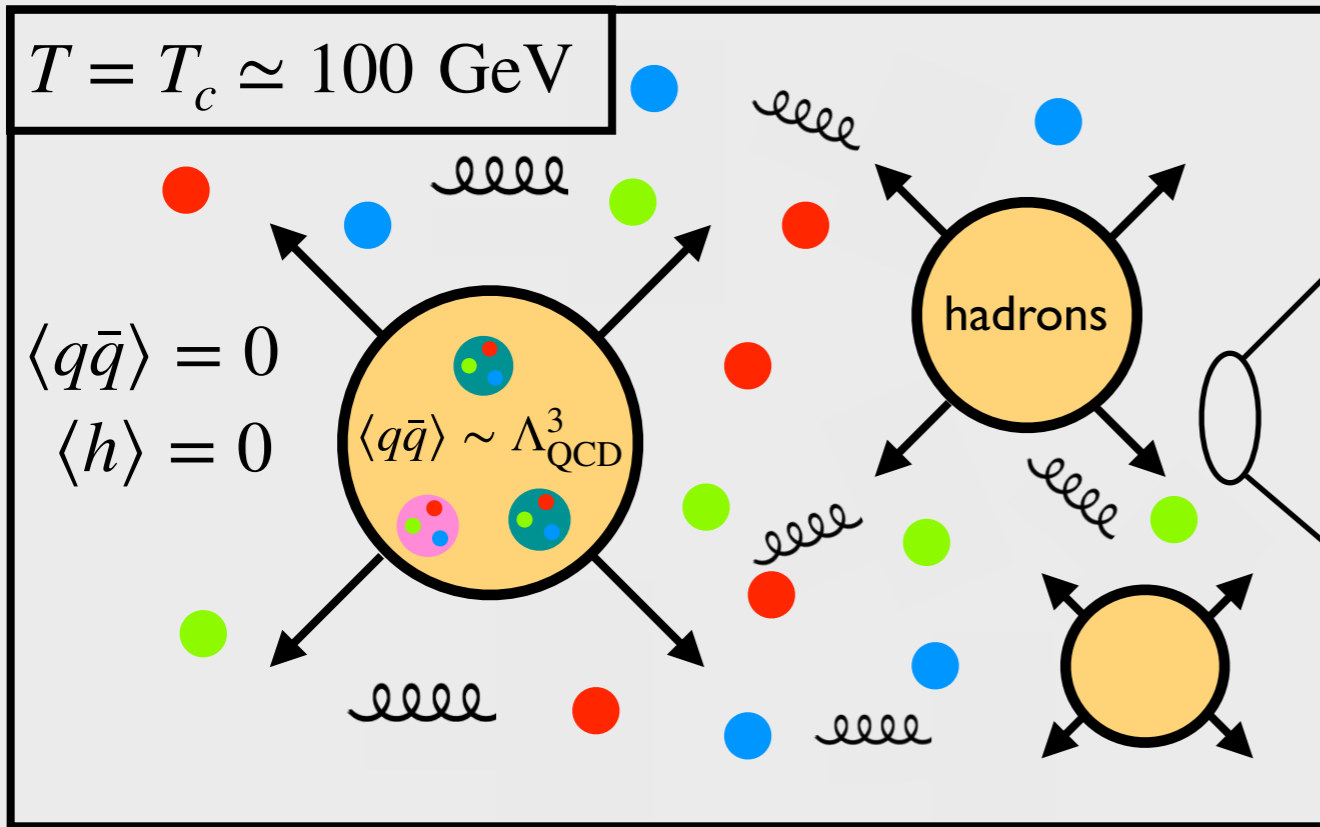
The universe can roll over instead of tunneling

SM-like vacuum!

$$b_1 = 0.7 \text{ GeV}, b_2 = 10^{-3}$$
$$a_2 = 108 \text{ GeV}^2, a_3 = 0.15 \text{ GeV}, a_4 = 5 \times 10^{-5}$$

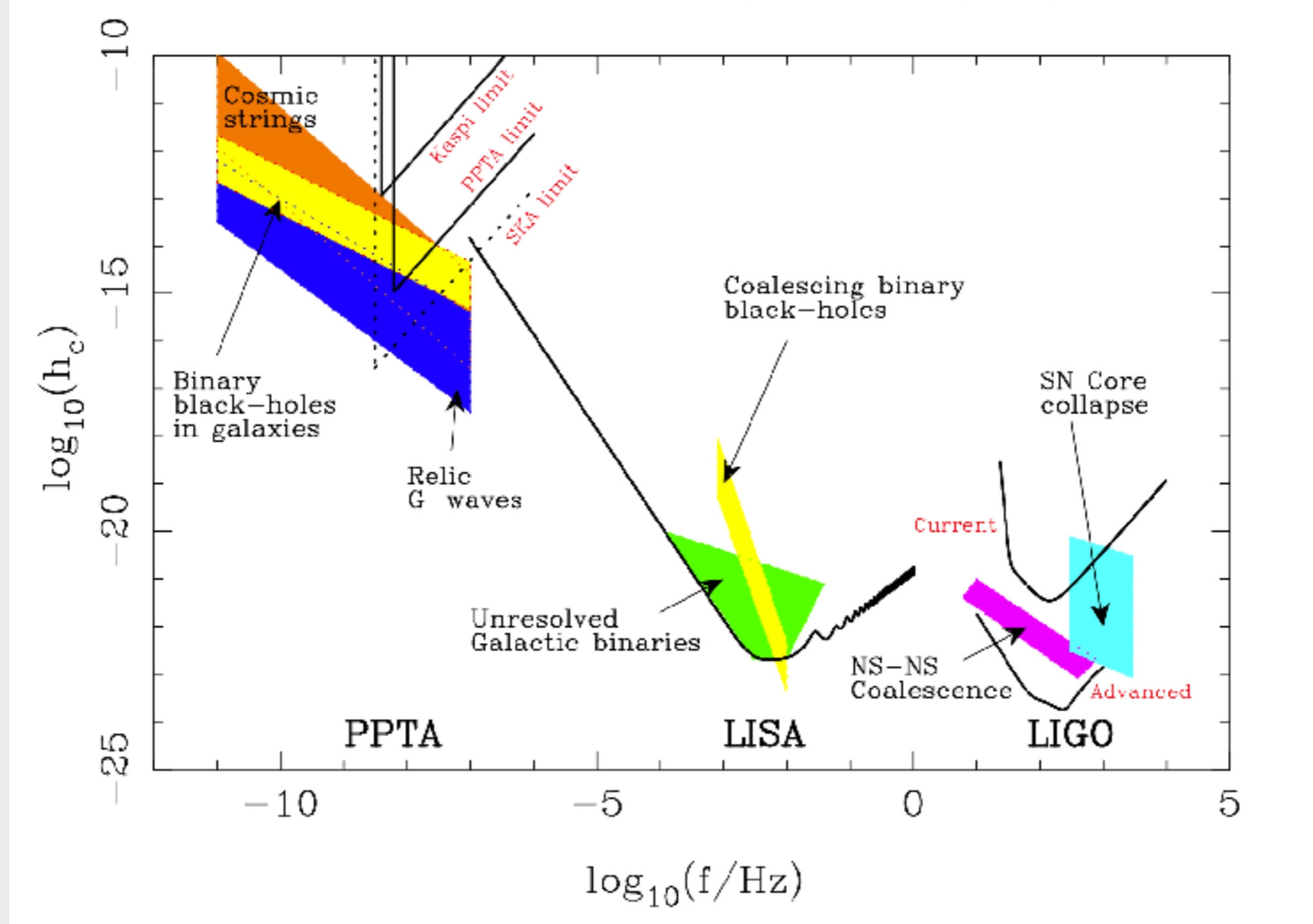
T = 2 MeV





$$\eta \sim 10^{-11} \overbrace{\sin \bar{\theta}}^{\sim 1} \overbrace{\frac{v_h}{\Lambda_{\text{QCD}}}}^{\sim 4} \left(\overbrace{\frac{T_c}{T_{\text{reh}}}}^{> 1} \right)^3$$

$$\eta_{\text{obs}} \simeq 8.5 \times 10^{-11}$$



Benchmark scenarios

	M_*	a_2/GeV^2	a_3/GeV	a_4
1.	1.5 TeV	380	9.9×10^{-1}	6.3×10^{-4}
2.	3 TeV	108	1.5×10^{-1}	5.1×10^{-5}
3.	3 TeV	44.2	6.14×10^{-2}	2.1×10^{-5}
4.	5 TeV	38.9	3.24×10^{-2}	6.6×10^{-6}
5.	10 TeV	9.72	4.05×10^{-3}	4.1×10^{-7}
6.	10 TeV	4.92	2.27×10^{-3}	2.6×10^{-7}

What is κ ? We can find by matching to the SM QCD!

OLD

$$m_{\pi 0}^2 = \frac{2\kappa_0(m_u + m_d)}{f_{\pi 0}^2}$$

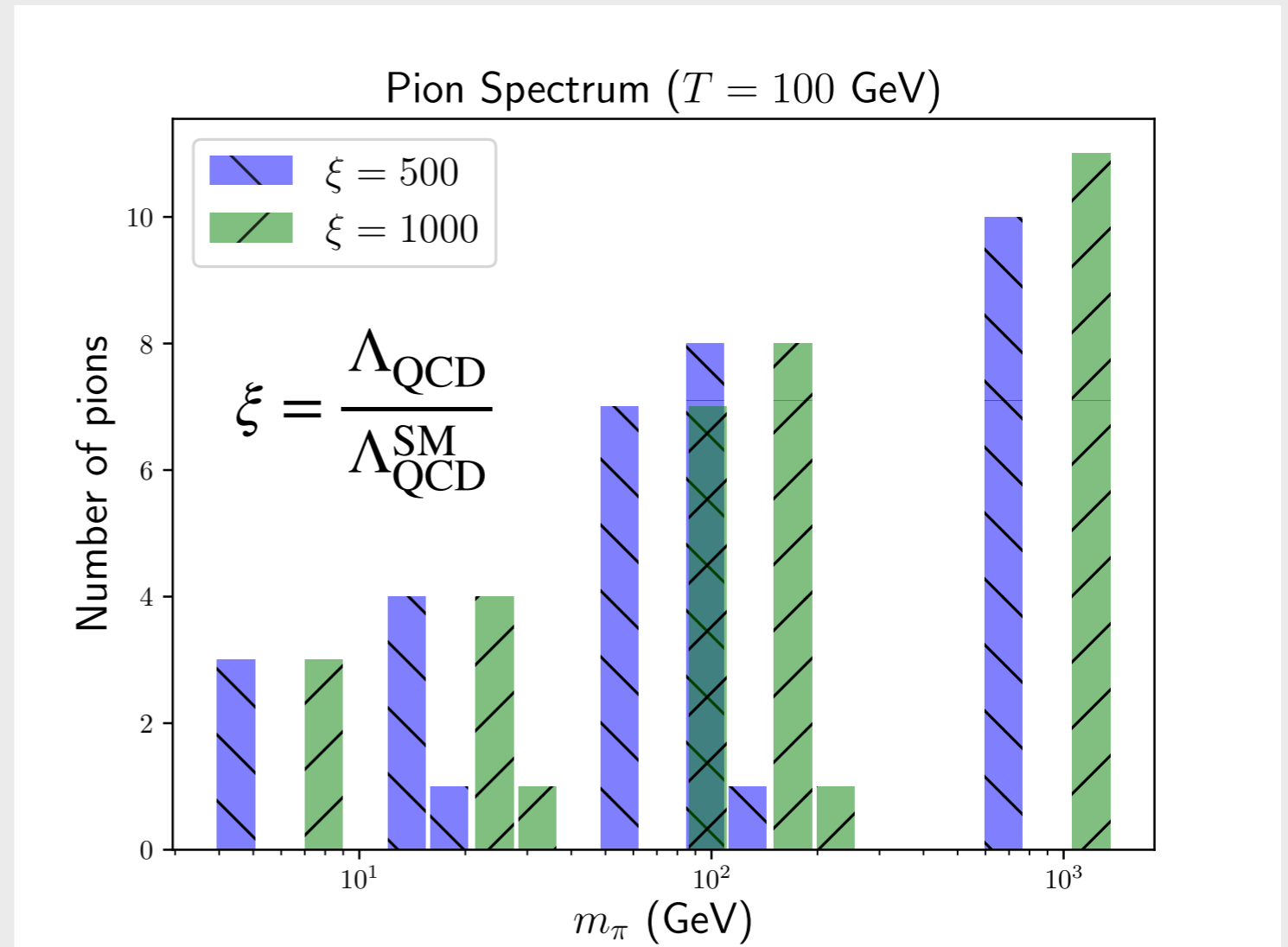
$$\kappa_0 = \frac{m_{\pi 0}^2 f_{\pi 0}^2}{\sqrt{2} v_h^0 (y_u + y_d)} \simeq (224 \text{ MeV})^3$$

NEW

$$\kappa \simeq \kappa_0 \left(\frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{QCD}}^{\text{SM}}} \right)^3$$

$$f_{\pi} \simeq f_{\pi 0} \left(\frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{QCD}}^{\text{SM}}} \right)$$

$$m_{\pi}^2 \simeq m_{\pi 0}^2 \left(\frac{\Lambda_{\text{QCD}}}{\Lambda_{\text{QCD}}^{\text{SM}}} \right) \left(\frac{v_h}{v_h^{\text{SM}}} \right)$$



How about other gauge couplings?

S.A.R. Ellis, **SI**, G.White, *JHEP* 08 (2019) 002, *arXiv:1905.11994*

$$\mathcal{L} \supset \left(\frac{1}{g_Y^2} + \frac{\phi}{M_{\text{Pl}}} \right) B^{\mu\nu} B_{\mu\nu} + \left(\frac{1}{g_2^2} + \frac{\phi}{M_{\text{Pl}}} \right) W^{\mu\nu} W_{\mu\nu}$$

