

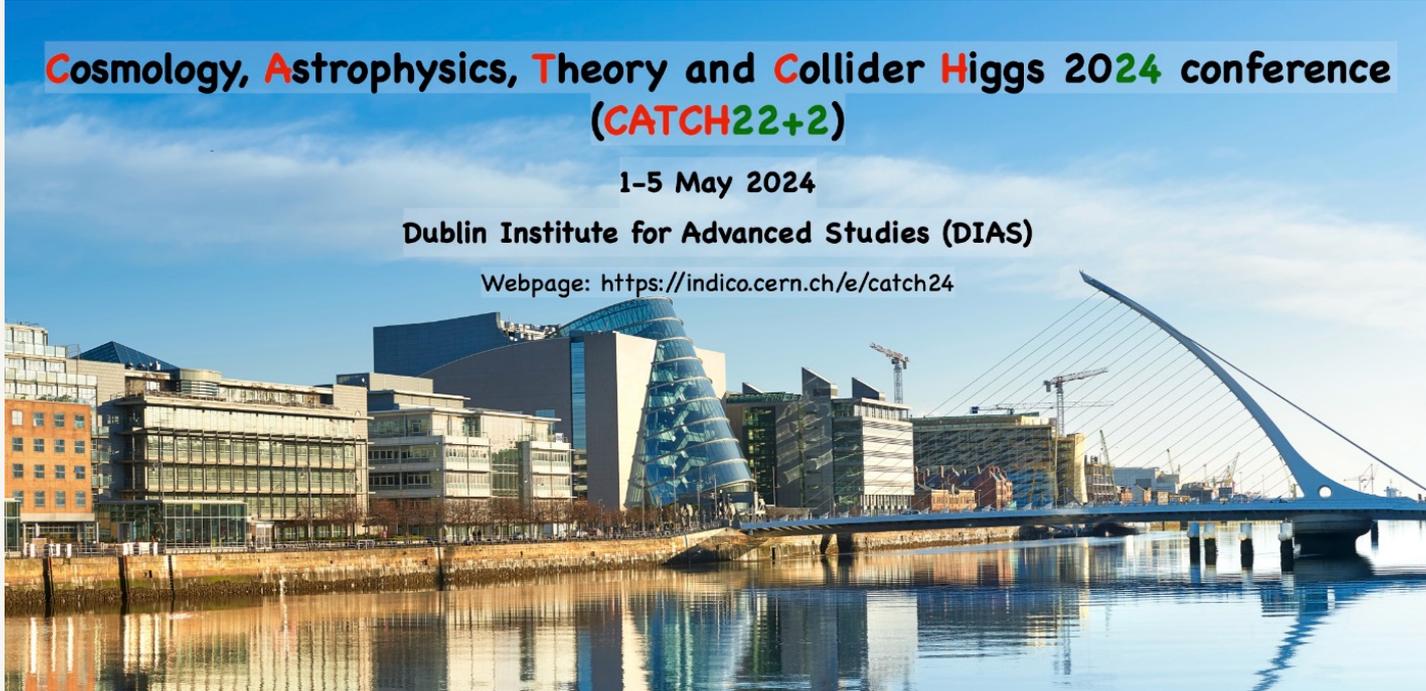
# Deconstructing Flavor: The Privately Democratic Higgs

Cosmology, Astrophysics, Theory and Collider Higgs 2024 conference  
(CATCH22+2)

1-5 May 2024

Dublin Institute for Advanced Studies (DIAS)

Webpage: <https://indico.cern.ch/e/catch24>



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Sat May 4, 2024

**WAYNE STATE**  
UNIVERSITY

# The Beloved *Beautiful* (& Unnatural)



# Standard Model

	three generations of matter (fermions)			interactions / force carriers (bosons)	
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	<b>H</b> higgs
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b><math>\gamma</math></b> photon	
	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau	<b>Z</b> Z boson	
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino	<b>W</b> W boson	

QUARKS

LEPTONS

GAUGE BOSONS  
VECTOR BOSONS

SCALAR BOSONS

3 generations of matter  
 $SU(3)_C \times SU(2)_L \times U(1)_Y$

[https://en.wikipedia.org/wiki/Elementary\\_particle](https://en.wikipedia.org/wiki/Elementary_particle)



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3 generations of matter  
 $SU(3)_C \times SU(2)_L \times U(1)_Y$

WHY?????

[https://en.wikipedia.org/wiki/Elementary\\_particle](https://en.wikipedia.org/wiki/Elementary_particle)



# The Beloved *Beautiful* (& Unnatural)

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QUARKS

LEPTONS

GAUGE BOSONS  
VECTOR BOSONS

SCALAR BOSONS

Non-Minimal  
Unnatural

Arbitrary Content  
Arbitrary Masses  
Arbitrary Mixings

Arbitrary Higgs Mechanism

[https://en.wikipedia.org/wiki/Elementary\\_particle](https://en.wikipedia.org/wiki/Elementary_particle)





*A PLETHORA*

**OF HIGGS**



mass  
charge  
spin

$\approx 2.2 \text{ MeV}/c^2$   
 $\frac{2}{3}$   
 $\frac{1}{2}$   
**u**  
**up**

$\approx 1.28 \text{ GeV}/c^2$   
 $\frac{2}{3}$   
 $\frac{1}{2}$   
**c**  
**charm**

$\approx 173.1 \text{ GeV}/c^2$   
 $\frac{2}{3}$   
 $\frac{1}{2}$   
**t**  
**top**

$\approx 4.7 \text{ MeV}/c^2$   
 $-\frac{1}{3}$   
 $\frac{1}{2}$   
**d**  
**down**

$\approx 96 \text{ MeV}/c^2$   
 $-\frac{1}{3}$   
 $\frac{1}{2}$   
**s**  
**strange**

$\approx 4.18 \text{ GeV}/c^2$   
 $-\frac{1}{3}$   
 $\frac{1}{2}$   
**b**  
**bottom**



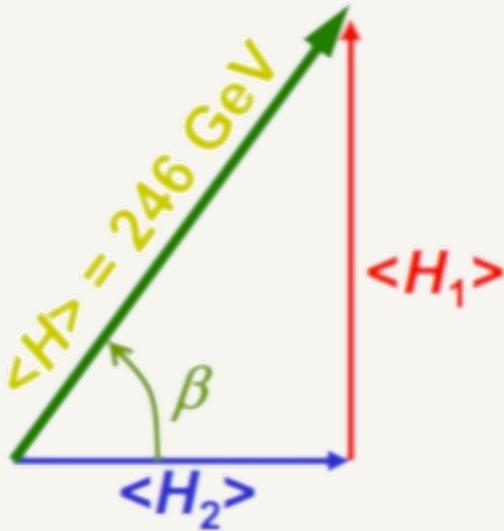
QUARKS

$$\langle H_f \rangle \sim m_f$$

$$y_f \sim 1$$

But we  
**SEE**  
a SM-like Higgs!

# 2 Higgs Doublet Model (2HDM).



$$\langle H_1 \rangle, \langle H_2 \rangle \rightarrow \langle H \rangle, \tan \beta$$

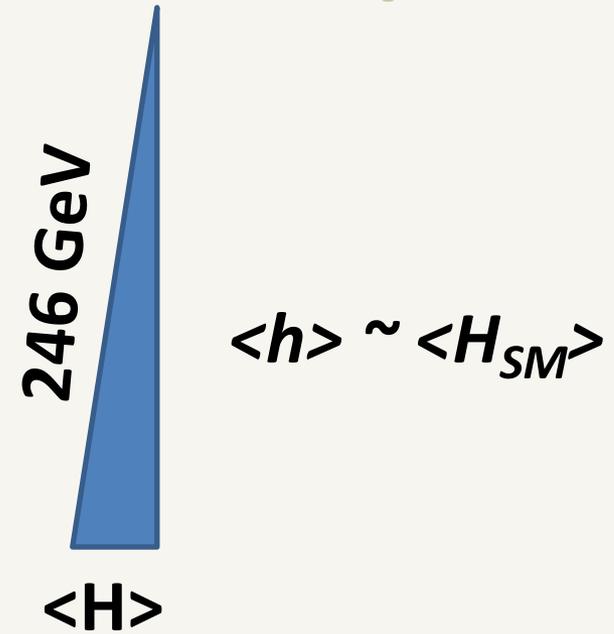
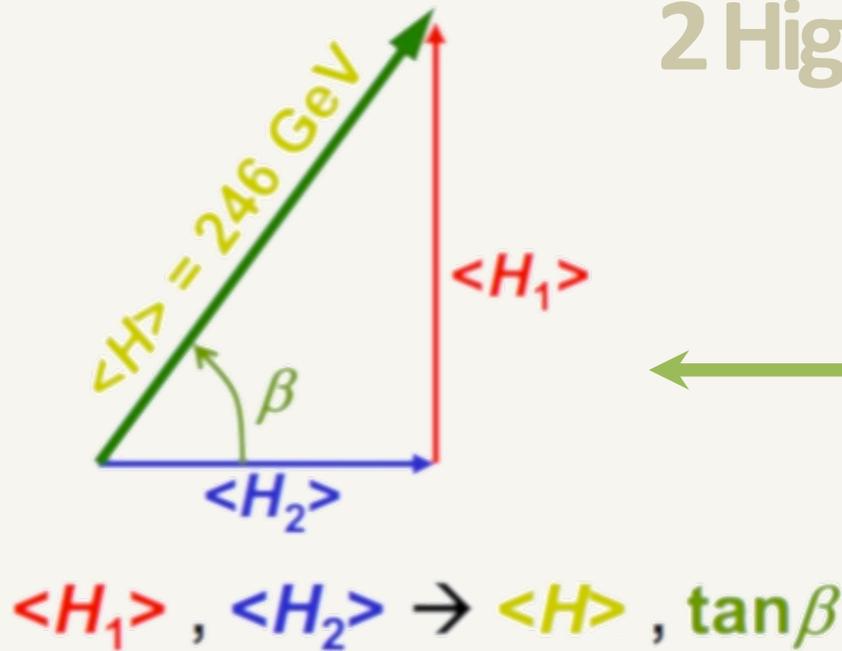
5 Physical Higgs bosons:

CP-Even: **h, H**

CP-Odd: **A**

Charged Higgs: **H<sup>±</sup>**

# 2 Higgs Doublet Model (2HDM).



5 Physical Higgs bosons:  
 CP-Even:  $h, H$   
 CP-Odd:  $A$   
 Charged Higgs:  $H^{\pm}$

SM: Only 1 Higgs which then acquires a vev and leads to EWSB.

This is what we want!

**ALIGNMENT**

# Recipe: SM-Like Higgs.



$$v \sin^2 \beta$$



$$H_{SM} = \sin \beta H_u + \cos \beta H_d \leftarrow v \cos^2 \beta$$

$$H_{NSM} = -\cos \beta H_u + \sin \beta H_d$$

**SM: Only 1 Higgs which then acquires a vev and leads to EWSB.**

**This is what we want!**

**Lighter ( $h$ ) is 125 GeV SM-like Higgs.**

**Additional states can exist!**

**Additional States can be light!**

Haber and Gunion, '03, M. Carena, I. Low, N.R.S. & C. Wagner, '13, A. Delgado, G. Nardini & M. Quiros, '13, N. Craig, J. Galloway & S. Thomas, '13, P. Dev, A. Pilaftsis '14, M. Carena, H. Haber, I. Low, N.R.S. & C. Wagner '14 & '15 etc....

$$\langle H_d \rangle = v \cos \beta$$

$$\langle H_u \rangle = v \sin \beta$$

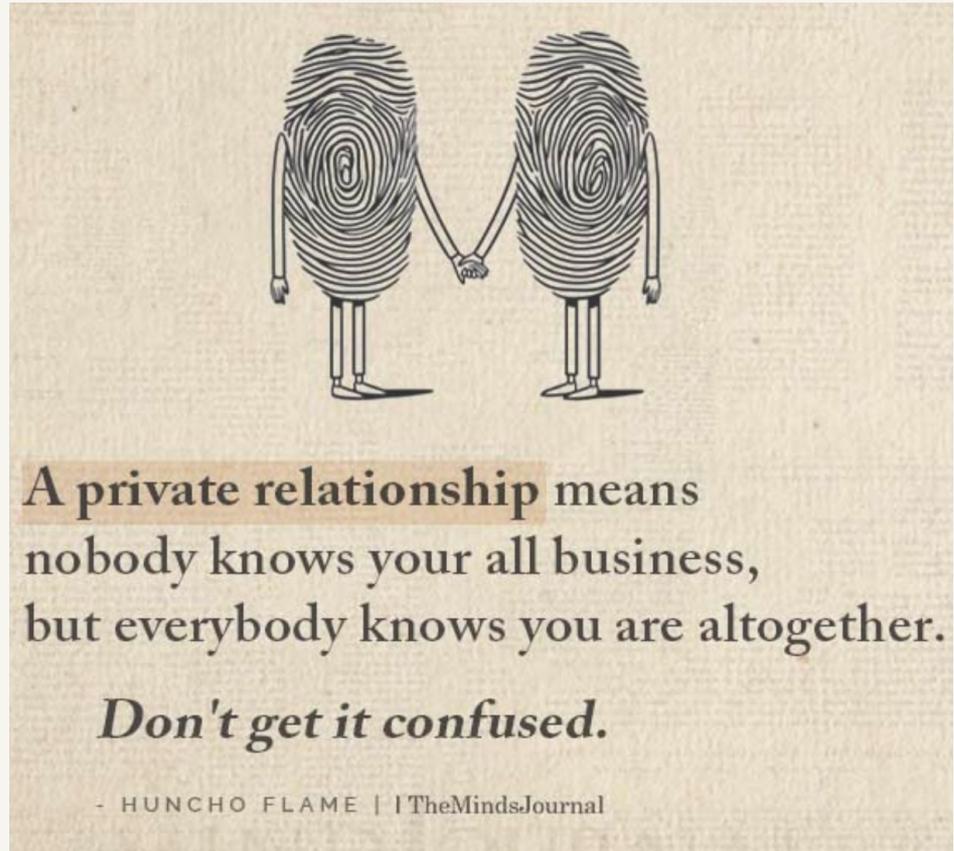
$$\Rightarrow \langle H_{SM} \rangle = v$$

$$\langle H_{NSM} \rangle = 0$$

**SM-like HIGGS**

**ALIGNMENT**

$$\sum m_f^2 \approx m_t^2 \approx v_{SM}^2$$



# PRIVATE HIGGS

Or is it SECRET instead !?!

# Private Higgs

R. Porto & A. Zee '07 + follow ups

A private Higgs for every SM fermion!  
Plus additional singlets  
Impose Symmetries

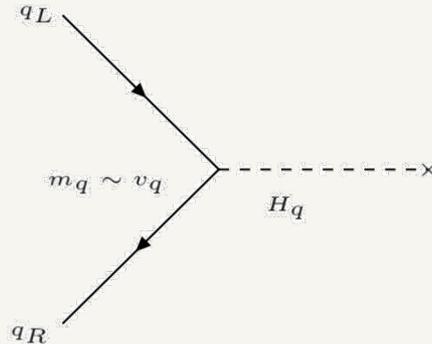
$$\langle H_f \rangle \sim m_f$$

$$y_f \sim 1$$

$$v_t \sim v_{SM}, \quad H_t \sim H_{SM} = H_{125},$$

Usual negative mass squared terms to induce EWSB  
Additional singlets w/ masses and vevs  $\sim v_t$ .

$$\mathcal{L} \supset \sum_j \left( \bar{Q}'^j_L H_d^j d_R^j + \bar{Q}'^j_L \tilde{H}_u^j u_R^j \right) + \text{h.c.}$$



$$\mathcal{L}_{H_f} \sim M_f^2 H_f^\dagger H_f - \lambda S S H_f^\dagger H_t$$

$$v_f^2 \ll v_t^2, f \neq t,$$

Assume  $M_f \gg m_t$

“Scalar see-saw” mechanism:

$$\text{Hierarchy: } y_f \rightarrow v_f \sim \frac{v_t^3}{M_f^2}$$

COMPLETELY diagonal structure.  
No CKM!

# Higgs Pheno??

$$\mathcal{L}_{H_f} \sim M_f^2 H_f^\dagger H_f - \lambda S S H_f^\dagger H_t$$

$$v_f \sim \frac{v_t^3}{M_f^2}$$

Lightest “Heavy” Higgs  $\rightarrow H_b$   
 $M_b \sim 1$  TeV

Produced via gluon fusion, bottom loops

Decays to  $b\bar{b}$

Can consider low energy theory via either mixing or “integrating out”

Y. BenTov & A. Zee '12

$$\mathcal{L}_{H_t b \bar{b}} = -\frac{m_b}{v_t} \left( 1 - \Gamma_t \frac{v_t^2}{\mathcal{M}_b^2} \right) H_t b \bar{b} + h.c.$$

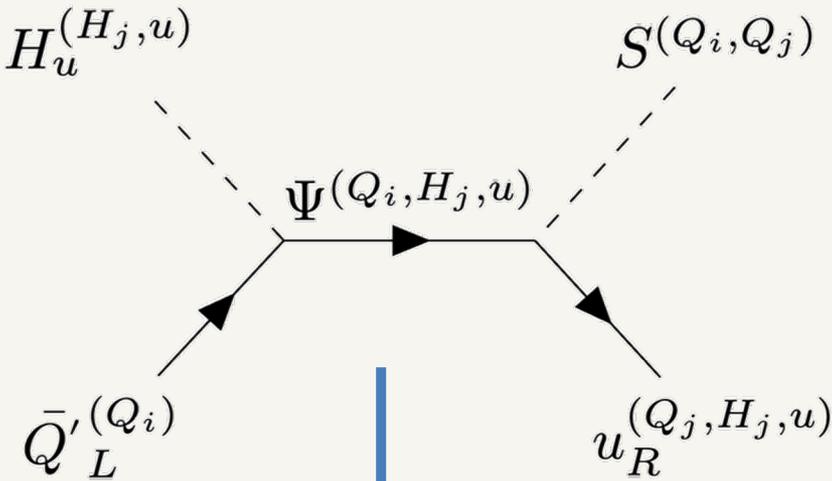
$$H_t \sim H_{SM} = H_{125}$$

## Higgs Precision in the future??

[Many singlets  $\sim \mathcal{O}$  (100 GeV) floating around...]

# CKM??

$$\mathcal{L}_q \supset \sum_{i,j} \left( \bar{Q}'_L{}^j H_q^i \psi_q^{ij} + \bar{\psi}_q^{ij} S^{ij} q_R^i \right) + \text{h.c.}$$



Impose  $Z_2$ s to allow only interactions we want

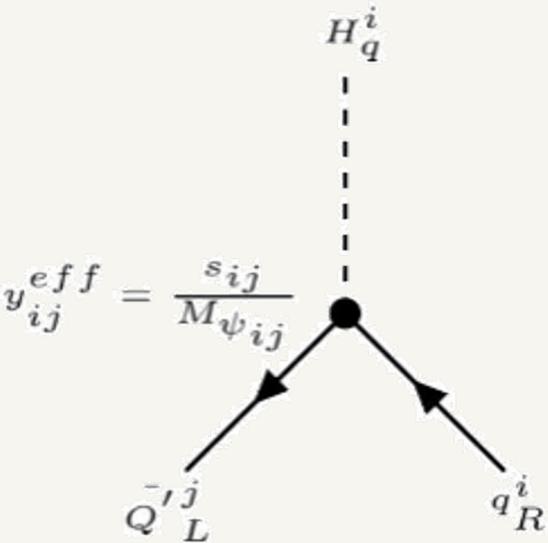
For each  $Q_i$  Quark generation:  $Z_2^{Q_i}$

For each  $H_{ui}$  coupling to u-type quarks:  $Z_2^{H_{ui}}$

For each  $H_{di}$  coupling to d-type quarks:  $Z_2^{H_{di}}$

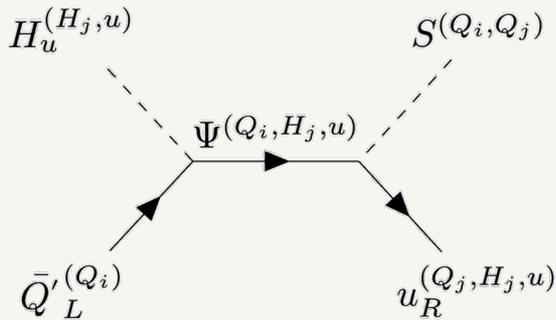


3 Additional Singlets  $S^{i,j}$  with vevs  $s_{i,j} = s_{j,i}$   
 6 singlet Vector-like Quarks  $\Psi^{i,u_j}$  with masses  $M_{i,j} \neq M_{j,i}$   
 $i \neq j$



CKM 😊

# Complexities ...



VLQ heavy  
Mixing effects with SM quarks or integrate them out

Leads to rescaling of SM quarks kinetic terms  
Canonically normalize them

Rescaling of SM quarks –  $W$  couplings absorbed in CKM

SM quarks –  $Z$  couplings leads to NON-UNIVERSAL  $Zqq$  couplings (patience!!)



$$\begin{bmatrix} \frac{\lambda_{11} v_u}{x m_u} & \frac{\lambda_{12} v_c \alpha_{12} s_{12}}{M_{12} y m_c} & \frac{\lambda_{21} v_t \alpha_{21} s_{21}}{M_{21} z m_t} \\ \frac{\lambda_{21} v_u \alpha_{21} s_{21}}{M_{21} x m_u} & \frac{\lambda_{22} v_c}{y m_c} & \frac{\lambda_{23} v_t \alpha_{23} s_{23}}{M_{23} z m_t} \\ \frac{\lambda_{31} v_u \alpha_{31} s_{31}}{M_{31} x m_u} & \frac{\lambda_{32} v_c \alpha_{32} s_{32}}{M_{32} y m_c} & \frac{\lambda_{33} v_t}{z m_t} \end{bmatrix}$$

$$\begin{aligned} x &= \sqrt{1 + \left(\frac{\alpha_{12} s_{12}}{M_{12}}\right)^2 + \left(\frac{\alpha_{13} s_{13}}{M_{13}}\right)^2}, \\ y &= \sqrt{1 + \left(\frac{\alpha_{21} s_{21}}{M_{21}}\right)^2 + \left(\frac{\alpha_{23} s_{23}}{M_{23}}\right)^2}, \\ z &= \sqrt{1 + \left(\frac{\alpha_{31} s_{31}}{M_{31}}\right)^2 + \left(\frac{\alpha_{32} s_{32}}{M_{32}}\right)^2} \end{aligned}$$

# What do we Learn?

(Actually  $V_{CKM}^{-1}$ )

$$\begin{bmatrix} \frac{\lambda_{11}v_u}{xm_u} & \frac{\lambda_{12}v_c\alpha_{12}s_{12}}{M_{12}ym_c} & \frac{\lambda_{21}v_t\alpha_{21}s_{21}}{M_{21}zm_t} \\ \frac{\lambda_{21}v_u\alpha_{21}s_{21}}{M_{21}xm_u} & \frac{\lambda_{22}v_c}{ym_c} & \frac{\lambda_{23}v_t\alpha_{23}s_{23}}{M_{23}zm_t} \\ \frac{\lambda_{31}v_u\alpha_{31}s_{31}}{M_{31}xm_u} & \frac{\lambda_{32}v_c\alpha_{32}s_{32}}{M_{32}ym_c} & \frac{\lambda_{33}v_t}{zm_t} \end{bmatrix}$$

$\lambda, \alpha \sim 1$  couplings

$v_f \sim m_f$

$V_{CKM}$  dictates ratio of  $s_{ij}/M_{ij}$ !

$$|V_{CKM}| = \begin{pmatrix} 0.97446 \pm 0.0001 & 0.2245 \pm 0.00044 & 0.00365 \pm 0.00012 \\ 0.22438 \pm 0.00044 & 0.97359^{+0.0001}_{-0.00011} & 0.04214 \pm 0.00076 \\ 0.00896^{+0.00024}_{-0.00023} & 0.04133 \pm 0.00074 & 0.999105 \pm 0.000032 \end{pmatrix}.$$

$$M_{12} \approx M_{21} \approx 4S_{12},$$

$$M_{23} \approx M_{32} \approx 25S_{23}$$

$$M_{31} \approx 265S_{31}, M_{13} \approx 115S_{13}$$

Assumed singlet vevs  $\sim$  SM vev  
Nothing requires it so far...

# Now the Z Couplings ...

## Diagonal matrix C:

$$g_{z\bar{f}_i f_i}^{NP} = g_{z\bar{f} f}^{SM} \times \left( 1 - \frac{\sin^2 \theta_w Q \sum_{j=1,2,3}^{i \neq j} \frac{|\lambda_{ij}^u|^2}{M_{ij}^2} \nu_j^{u2}}{T^3 - \sin^2 \theta_w Q} \right)$$

Non-universal, but still diagonal in original basis

$$Z \bar{q}_i C q_i$$

After rotating to mass basis ...

$$M_{12} \approx M_{21} \approx 4S_{12},$$

$$M_{23} \approx M_{32} \approx 25S_{23}$$

$$M_{31} \approx 265S_{31}, M_{13} \approx 115S_{13}$$

$$g^u = V_{CKM} C V_{CKM}^\dagger \neq \mathbb{I}!!!$$

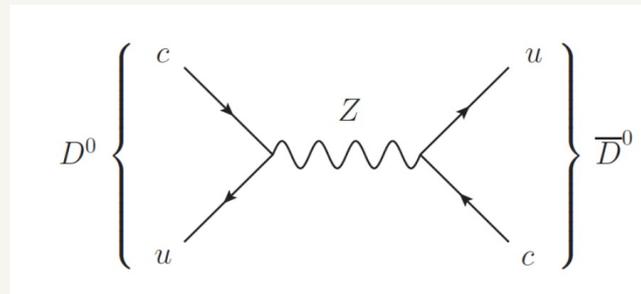
	$u$	$c$	$t$
$\bar{u}$	$\left  -0.2367 + \frac{0.23\text{GeV}^2}{S_{13}^2} + \frac{0.27\text{GeV}^2}{S_{23}^2} \right $	$\left  \frac{-0.05\text{GeV}^2}{S_{13}^2} + \frac{1.15\text{GeV}^2}{S_{23}^2} \right $	$\left  \frac{0.05\text{GeV}^2}{S_{23}^2} \right $
$\bar{c}$	$\left  \frac{-0.05\text{GeV}^2}{S_{13}^2} + \frac{1.15\text{GeV}^2}{S_{23}^2} \right $	$\left  -0.2367 + \frac{0.01\text{GeV}^2}{S_{13}^2} + \frac{5\text{GeV}^2}{S_{23}^2} \right $	$\left  \frac{-0.21}{S_{23}^2} \right $
$\bar{t}$	$\left  \frac{0.05\text{GeV}^2}{S_{23}^2} \right $	$\left  \frac{0.21\text{GeV}^2}{S_{23}^2} \right $	0.2367

# Any more Luck?

	$u$	$c$	$t$
$\bar{u}$	$\left  -0.2367 + \frac{0.23\text{GeV}^2}{S_{13}^2} + \frac{0.27\text{GeV}^2}{S_{23}^2} \right $	$\left  \frac{-0.05\text{GeV}^2}{S_{13}^2} + \frac{1.15\text{GeV}^2}{S_{23}^2} \right $	$\left  \frac{0.05\text{GeV}^2}{S_{23}^2} \right $
$\bar{c}$	$\left  \frac{-0.05\text{GeV}^2}{S_{13}^2} + \frac{1.15\text{GeV}^2}{S_{23}^2} \right $	$\left  -0.2367 + \frac{0.01\text{GeV}^2}{S_{13}^2} + \frac{5\text{GeV}^2}{S_{23}^2} \right $	$\left  \frac{-0.21}{S_{23}^2} \right $
$\bar{t}$	$\left  \frac{0.05\text{GeV}^2}{S_{23}^2} \right $	$\left  \frac{0.21\text{GeV}^2}{S_{23}^2} \right $	0.2367

For  $s \sim 100$  GeV, corrections  $\lesssim 10^{-4}$  to diagonal couplings

FCNC: D-D mixing



Not constrained by  
current  
measurements if  
 $s_{ij} \gtrsim 150$  GeV

FCNC:  $t \rightarrow Zu, Zc$

Only constrains  $\lesssim 10^{-2}$  for off-diagonal couplings...

Rich phenomenology:

Many new particles expected

LHC signatures?

Precision Higgs/SM physics?

Dark Matter connections?

Cosmology +  
Gravitational Waves...

# Many Avenues to Explore

$$M_{12} \approx M_{21} \approx 4S_{12},$$

$$\Psi_{ij}$$

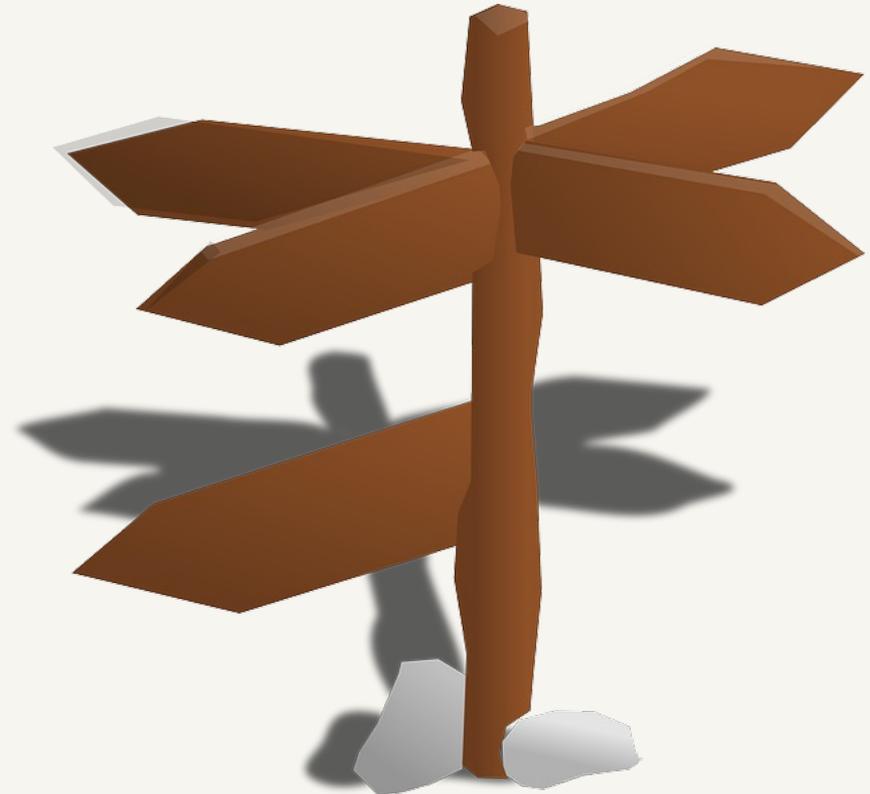
$$M_{23} \approx M_{32} \approx 25S_{23}$$

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$$s_{ij} \sim 100 \text{ GeV}$$

$$M_{H_f} \gg \text{TeV (except } b)$$

$$M_{S_{ij}} ??$$



Thank You!



SM works beautifully...

But it's a pretty **RIDICULOUS** model!!

What are the right questions?

Hypothesize an at-least-as-ridiculous(!!!) BSM model.  
Seems rather difficult to probe...

Data + Theory:  
Where to look next!

???

**Absence of Evidence != Evidence of Absence**

Data driven age: Collider + Precision + Astrophysical Probes ...

**HOPE blooms ETERNAL!!!**