

Classes of complete dark photon models constrained by Z-Physics

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5. Constraining dark matter with the electroweak ρ parameter

This talk is based on M.P. Bento, H.E. Haber, and J.P. Silva, Phys. Lett. B **850**, 138501 (2024). See also M.P. Bento, H.E. Haber, and J.P. Silva, JHEP **10** (2023) 083.

Dark sector portals

Models of particle dark matter come in two varieties:

- Particles with electroweak quantum numbers that are very weakly coupled to the Standard Model (SM)
 - example: the lightest neutralino of the MSSM
- Particles that are completely neutral with respect to the SM gauge group (which constitute the dark sector)
 - requires a portal (mediator) that connects the visible (SM) sector to the dark sector

Examples of dark sector portals

- Higgs portal: $H^\dagger H f(\phi_{\text{dark}})$
- right-handed neutrino portal: HLN
- gauge boson kinetic mixing portal: $F_{\mu\nu} F_{\text{dark}}^{\mu\nu}$

In this talk we focus on models of gauge boson kinetic mixing, which necessarily involves the mixing of U(1) gauge bosons. The simplest model of this kind adds a new U(1)' gauge boson that mixes with the hypercharge gauge boson of the SM.

Adding additional matter that is charged under U(1)' but is neutral with respect to the SM provides a plausible model for particle dark matter.

There are many dark photon models in the literature that are based on mixing $U(1)_{\text{EM}}$ with $U(1)'$, under the assumption that the Z boson can be integrated out and is therefore irrelevant.



However, it is dangerous to neglect the effects of the Z due to constraints from precision electroweak data.

Indeed, the precision electroweak data are in good agreement with the SM¹ and thus can be used to constrain beyond the Standard Model (BSM) physics.

¹There are a few intriguing deviations, e.g., $g - 2$ of the muon, the Tevatron W mass measurement, and a few Z -pole observables (A_{LR} and A_{FB}^b), that could potentially be evidence for BSM physics.

Constraining BSM physics with precision electroweak data

- If BSM physics is associated with a new energy scale that lies significantly above the SM, then the physics associated with this scale can be integrated out (resulting in higher-dimensional operators). Typical approaches of this type include SMEFT or HEFT (depending on how the Higgs field is treated).
- In many cases, the corrections to precision electroweak observables arise mainly through gauge boson self-energy corrections, which lead to the introduction of the so-called oblique parameters (e.g., the Peskin-Takeuchi S , T , and U parameters).

Oblique parameters of the $SU(2) \times U(1) \times U(1)'$ model

The current interactions of the SM electroweak gauge bosons are given by:²

$$\begin{aligned} \mathcal{L}_{EW} = & m_W^2 W^{+\mu} W_{\mu}^{-} + \frac{1}{2} \tilde{m}_Z^2 (1 + \Delta_1) Z^{\mu} Z_{\mu} - \frac{g}{\sqrt{2}} (J_{CC}^{\mu} W_{\mu}^{+} + \text{h.c.}) \\ & - e J_{em}^{\mu} A_{\mu} - \frac{g}{2c_W} (1 + \Delta_2) J_{NC}^{\mu} Z_{\mu} - e \Delta_3 J_{em}^{\mu} Z_{\mu}, \end{aligned}$$

where $m_W^2 = \frac{1}{4} g^2 v^2$, $\tilde{m}_Z^2 = \frac{1}{4} (g^2 + g'^2) v^2$, and $e = g s_W = g' c_W$.

Here, $v \simeq 246$ GeV, $s_W \equiv \sin \theta_W$, and $c_W \equiv \cos \theta_W$.

²H. Davoudiasl, K. Enomoto, H.-S. Lee, J. Lee, and W.J. Marciano Phys. Rev. D **108**, 115018 (2023). See also B. Holdom, Phys. Lett. B **166**, 196 (1986).

The corresponding oblique parameters are:

$$\alpha_{\text{EM}} S = 8s_W^2 c_W^2 \Delta_2 - 4s_W c_W (c_W^2 - s_W^2) \Delta_3 ,$$

$$\alpha_{\text{EM}} T = -\Delta_1 + 2\Delta_2 ,$$

$$\alpha_{\text{EM}} U = -8s_W^2 c_W (c_W \Delta_2 + s_W \Delta_3) ,$$

where $\alpha_{\text{EM}} \equiv e^2/(4\pi)$. The precision electroweak data yield:³

$$S = -0.02 \pm 0.10 ,$$

$$T = 0.03 \pm 0.12 ,$$

$$U = 0.01 \pm 0.11 ,$$

where $S = T = U = 0$ corresponds to the SM.

³J. Erler and A. Freitas, in R.L. Workman et al. (Particle Data Group), *Review of Particle Physics*, Prog. Theor. Exp. Phys. 2022, 083C01 (2022).

The parameter ρ_0

In the SM, $\rho \equiv m_W^2/(m_Z^2 c_W^2) = 1$ at tree-level. Erler and Freitas (in their Review of Particle Physics review) introduce

$$\rho_0 \equiv \frac{m_W^2}{m_Z^2 \hat{c}_Z^2 \hat{\rho}} = 1.00038 \pm 0.00020,$$

where $\hat{c}_Z^2 = 1 - \sin^2 \hat{\theta}_W(m_Z)$ is defined in the $\overline{\text{MS}}$ scheme, and $\hat{\rho} \equiv m_W^2/(m_Z^2 \hat{c}_Z^2)$ is computed assuming the validity of the SM.

That is, $\rho_0 = 1$ in the SM, and a deviation from $\rho_0 = 1$ can be interpreted as a consequence of tree-level BSM physics (under the assumption that the latter is a small perturbation that does not significantly modify the SM electroweak radiative corrections).

A generic $SU(2) \times U(1) \times U(1)'$ model

Kinetic mixing of the hypercharge gauge boson \hat{B} and the $U(1)'$ gauge boson \hat{X} is governed by the mixing parameter ϵ ,

$$\mathcal{L} \supset -\frac{1}{4}\hat{B}_{\mu\nu}\hat{B}^{\mu\nu} - \frac{1}{4}\hat{X}_{\mu\nu}\hat{X}^{\mu\nu} + \frac{\epsilon}{2c_W}\hat{X}_{\mu\nu}\hat{B}^{\mu\nu}.$$

To obtain a canonical form of the kinetic Lagrangian, we transform the \hat{B} and \hat{X} fields such that

$$\hat{X} = \eta X, \quad \hat{B} = B + \frac{\epsilon}{c_W}\eta X,$$

where

$$\eta \equiv \frac{1}{\sqrt{1 - \epsilon^2/c_W^2}}.$$

Scalar fields and their vacuum expectation values (vevs)

Φ : SM-like complex scalar doublet with weak isospin $t_1 = \frac{1}{2}$, U(1) and U(1)' charges $Y = \frac{1}{2}$ and $Y' = 0$, and vev $\langle \Phi^0 \rangle = v_1/\sqrt{2}$.

φ_i ($i = 2, 3, \dots, N$): with weak isospins t_i , U(1) and U(1)' charges y_i and y'_i , and vevs $\langle \varphi_i^0 \rangle = v_i/\sqrt{2}$.

The resulting W^\pm mass is

$$m_W^2 = \frac{g^2 v^2}{4} = \frac{g^2 \left[v_1^2 + \sum_{i=2}^N 2(C_{R_i} - y_i^2) v_i^2 c_i \right]}{4},$$

where $C_{R_i} = t_i(t_i+1)$ for a complex [real] φ_i multiplet, with $c_i = 1$ [$c_i = 1/2$]. Scalar field multiplets are chosen such $C_{R_i} = 3y_i^2$ (to reproduce the observed value of m_W/m_Z).

The squared-mass matrix of the massive neutral gauge bosons with respect to the $\{Z^0, X\}$ basis, where $Z^0 \equiv W^3 c_W - B s_W$ is orthogonal to the photon field A , is given by

$$\mathcal{M}^2 = \begin{bmatrix} \tilde{m}_Z^2 & (\mathcal{M}^2)_{12} \\ (\mathcal{M}^2)_{12} & (\mathcal{M}^2)_{22} \end{bmatrix}.$$

An explicit expression for the off-diagonal element of \mathcal{M}^2 is

$$(\mathcal{M}^2)_{12} = -\frac{\tilde{m}_Z^2}{v^2} \left[4\eta t_W \epsilon \sum_{i=1}^N v_i^2 y_i^2 + 4\eta \tau c_W \sum_{i=2}^N v_i^2 y_i y'_i \right],$$

where $t_W \equiv s_W/c_W$, $\tau \equiv g_X/g$ and $\eta \equiv 1/\sqrt{1 - \epsilon^2/c_W^2}$.

Diagonalizing \mathcal{M}^2 yields the mass eigenstate fields Z and Z' .

$$\begin{pmatrix} Z^0 \\ X \end{pmatrix} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} Z \\ Z' \end{pmatrix}$$

defines the mixing angle α , and $\tilde{m}_Z^2 = m_Z^2 \cos^2 \alpha + m_{Z'}^2 \sin^2 \alpha$, where m_Z [$m_{Z'}$] is the mass of the physical Z [dark Z'] boson.

Having chosen scalar multiplets such that $C_{R_i} = 3y_i^2$, it follows that

$$\frac{m_W^2}{\tilde{m}_Z^2 c_W^2} = 1,$$

at tree level. Hence,

$$\rho - 1 = (r - 1) \sin^2 \alpha,$$

with $r \equiv m_{Z'}^2/m_Z^2$, and the value of $\sin \alpha$ is controlled by $(\mathcal{M}^2)_{12}$.

In particular,

$$\sin^2 2\alpha = \frac{4[(\mathcal{M}^2)_{12}]^2}{(m_Z^2 - m_{Z'}^2)^2}.$$

It is useful to eliminate $\sin \alpha$ in favor of the parameter r_{12}^2 ,

$$r_{12}^2 \equiv \left(\frac{(\mathcal{M}^2)_{12}}{\tilde{m}_Z^2} \right)^2 = \frac{(1-r)^2 \sin^2 \alpha \cos^2 \alpha}{[1 - (1-r) \sin^2 \alpha]^2}.$$

As before, $r \equiv m_{Z'}^2/m_Z^2$. The end result is:

$$\rho - 1 = \frac{-1 + r - 2r_{12}^2 + \sqrt{(1-r)^2 - 4r r_{12}^2}}{2(1 + r_{12}^2)},$$

which is a monotonically decreasing function of r_{12} . Equivalently,

$$r_{12}^2 = \frac{(1-\rho)(\rho-r)}{\rho^2}.$$

A dark matter (DM) candidate

Consider the dark Z' model with an additional an $SU(2) \times U(1)$ singlet Dirac fermion with a nonzero $U(1)'$ charge, denoted by χ . Then, the dark Lagrangian is given by

$$\mathcal{L}_{\text{DM}} = i\bar{\chi}\not{D}\chi - m_\chi\bar{\chi}\chi,$$

where the covariant derivative can be expanded as

$$D_\mu = \partial_\mu + ig_X Y' \eta (s_\alpha Z_\mu + c_\alpha Z'_\mu),$$

with $s_\alpha \equiv \sin \alpha$ and $c_\alpha \equiv \cos \alpha$.

In the following, we assume that the DM candidate χ is in thermal equilibrium in the early Universe.

The velocity averaged cross section for $\bar{\chi}\chi$ annihilation is given by

$$\langle\sigma_{\chi\chi}v\rangle \simeq 2 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1} \simeq 1.7 \times 10^{-9} \text{ GeV}^{-2},$$

for values of $m_\chi \gtrsim 10 \text{ GeV}$, under the assumption that χ particles saturate the observed DM abundance today. As the Universe evolves and the temperature drops, a point is reached where the DM decouples from the thermal bath and it freezes out.

We consider models where $m_{Z'} < m_Z$ (or equivalently, $r < 1$), omitting the regime where r is close to 1. Two scenarios emerge:

1. $m_{Z'} > m_\chi > m_e$

2. $m_\chi > m_{Z'} > m_e$

1. The characteristic regime: $m_{Z'} > m_\chi > m_e$.⁴

The dominant annihilation mechanism is the s -channel scattering process $\bar{\chi}\chi \rightarrow Z'^* \rightarrow \bar{f}f$. It then follows that

$$\langle \sigma_{\chi\chi} v \rangle \approx \frac{m_\chi^2}{\pi m_{Z'}^4} (\epsilon e g_X Y')^2 ,$$

under the assumption that $m_\chi \gg m_e$ and $m_{Z'} \gg m_\chi$. By assuming $Y' = 1$, we obtain the observed DM abundance with

$$\frac{1.7 \times 10^{-9}}{\text{GeV}^2} \approx \frac{0.038}{\text{GeV}^2} \left(\frac{m_\chi}{0.01 \text{ GeV}} \right)^2 \left(\frac{0.1 \text{ GeV}}{m_{Z'}} \right)^4 (\epsilon g_X)^2 ,$$

which, after fixing the masses, yields a value for ϵg_X .

⁴See E. Izaguirre, G. Krnjaic, P. Schuster, and N. Toro, Phys. Rev. D **90**, 014052 (2014), and H. Davoudiasl and W.J. Marciano, Phys. Rev. D **92** 035008 (2015).

2. The secluded regime: $m_\chi > m_{Z'} > m_e$.⁵

The dominant annihilation mechanism is $\bar{\chi}\chi \rightarrow Z'Z'$ via t -channel χ -exchange. It then follows that

$$\langle \sigma_{\chi\chi v} \rangle \approx \frac{g_X^4 \eta^4 c_\alpha^4 Y'^4}{8\pi m_\chi^2},$$

under the assumption that $m_\chi \gg m_{Z'}$. Assuming again that $Y' = 1$, we obtain the observed DM abundance with

$$1.7 \times 10^{-9} \text{ GeV}^{-2} \approx 0.04 \frac{g_X^4 \eta^4 c_\alpha^4}{m_\chi^2}.$$

After fixing m_χ and $m_{Z'}$ (and determining the mixing angle α), we may constrain the values of g_X and ϵ .

⁵See M. Pospelov, A. Ritz, and M.B. Voloshin, Phys. Lett. B **662**, 53 (2008), and J.A. Evans, S. Gori and J. Shelton, Looking for the WIMP Next Door, JHEP **02** (2018) 100.

Dark matter and the electroweak ρ parameter

Example 1: An $SU(2) \times U(1) \times U(1)'$ model with scalar multiplets φ_i beyond the SM Higgs doublet that are non-inert (i.e., $v_i \neq 0$) and charged under both $U(1)$ and $U(1)'$. If we assume a parameter regime where $\epsilon \ll 1$ and $r = m_{Z'}^2/m_Z^2 \ll 1$, then

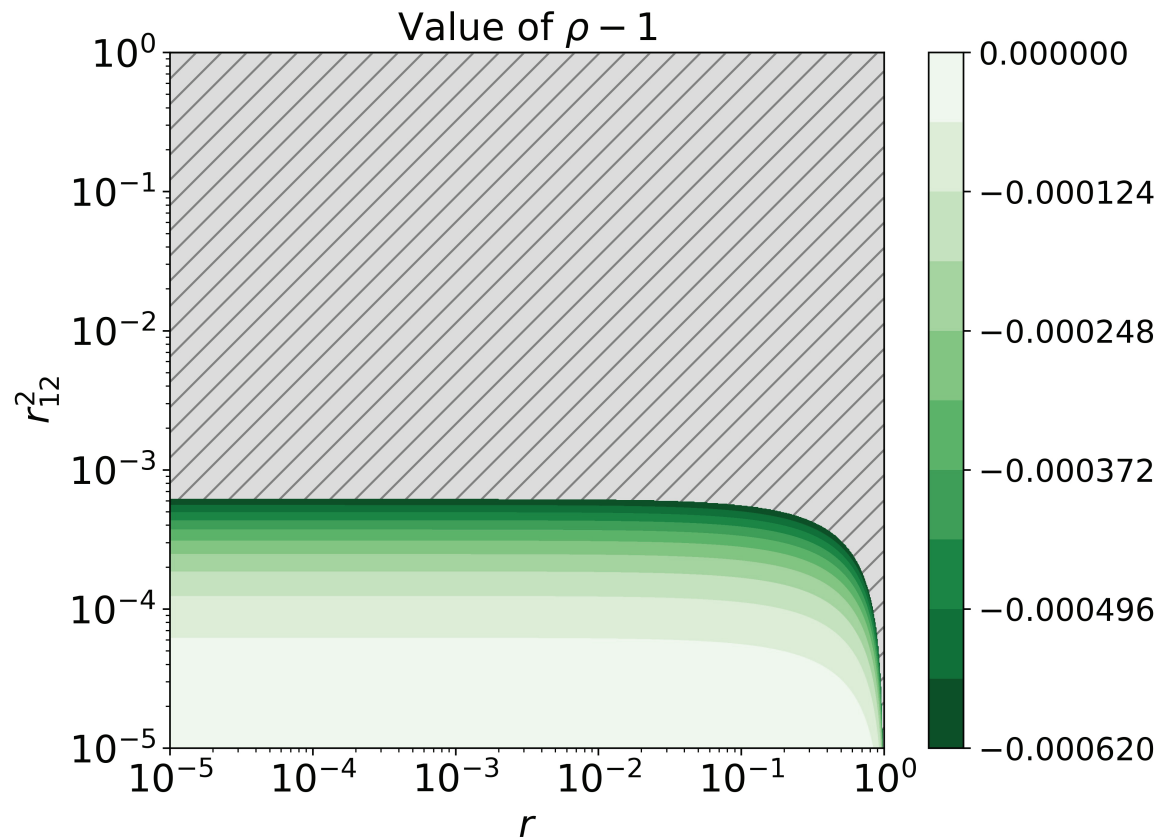
$$c_\alpha^2 = \frac{1}{1 + r_{12}^2} + \mathcal{O}(r).$$

where $r_{12}^2 = [(\mathcal{M}^2)_{12}]^2 / \tilde{m}_Z^4 \sim g_X^2/g^2 \sim 2.34g_X^2$, assuming that

$$\frac{4c_W}{v^2} \sum_i y_i y_i' v_i^2 \sim \mathcal{O}(1).$$

For example, if $m_\chi = 20 \text{ GeV}$ (corresponding to the secluded regime) then $g_X \sim 0.0645$.

As g_X becomes larger, so does r_{12}^2 . Because the expression obtained for $\rho - 1$ is a monotonically decreasing function with r_{12}^2 , it follows that $\rho - 1$ gets more negative with larger r_{12}^2 . Thus, a large g_X pushes towards a larger negative value of $\rho - 1$.



For $r \ll 1$, the contribution of r to $\rho - 1$ is small. Then, we may approximate

$$\rho - 1 = -\frac{r_{12}^2}{1 + r_{12}^2} + \mathcal{O}(r).$$

Using $r_{12}^2 \sim g_X^2/g^2 \sim 2.34g_X^2$, we end up with

$$\rho - 1 \sim -0.0096,$$

which, is inconsistent with the global electroweak fit value of $\rho_0 = 1.00038 \pm 0.00020$ quoted earlier. That is, we can assume that the deviation from $\rho = 1$, which is due to the tree-level effect exhibited above, can be constrained by the observed value of ρ_0 .

Example 2: An $SU(2) \times U(1) \times U(1)'$ model with an extended Higgs sector that contains an $SU(2) \times U(1)$ singlet scalar φ (dark Higgs) with a $U(1)'$ charge of $y' = 1$. In this case, $r_{12}^2 = \eta^2 t_W^2 \epsilon^2$. Assuming that $|\epsilon| \ll 1$ and $1 - r \sim \mathcal{O}(1)$, it follows that

$$\rho - 1 = \frac{r_{12}^2}{r - 1} + \mathcal{O}(r_{12}^4).$$

We then end up with:

$$\rho - 1 = -\frac{\epsilon^2 t_W^2}{1 - r} + \mathcal{O}(\epsilon^4).$$

For example, assuming that the true value of ρ_0 is no more than 5σ below the central value obtained in the analysis of electroweak data, one can deduce an upper limit of $|\epsilon| \lesssim 0.046$.

Conclusions

- Models of dark matter mediated by a dark photon (or dark Z boson) cannot ignore constraints of precision electroweak data.
- The precision of the parameter ρ_0 obtained in a global fit to electroweak data imposes strong constraints on realistic models of dark matter that communicate with the SM sector via gauge boson kinetic mixing.
- Additional constraints based on the oblique parameters (or more generally, the coefficients of higher dimensional operators in SMEFT or HEFT) should also be taken into account in determining whether a particular dark matter model is viable.