

# Non-identical particle femtoscopy of pairs containing (anti)deuteron in relativistic heavy-ion collisions with ALICE at the LHC

Wioleta Rzęsa (Warsaw University of Technology)  
on behalf of the ALICE Collaboration



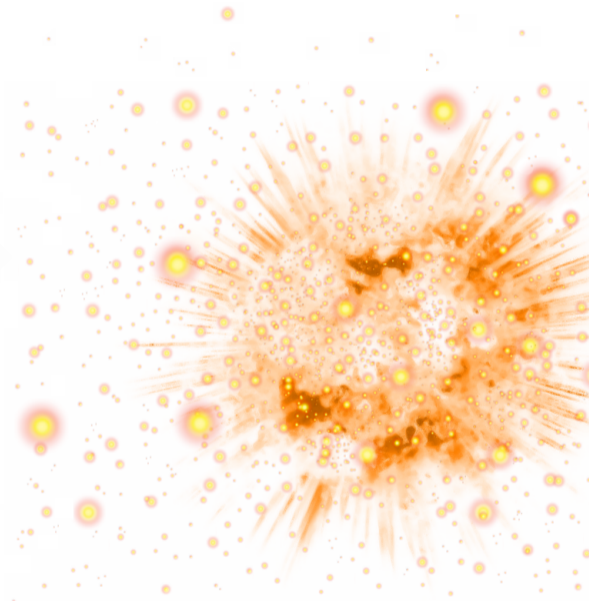
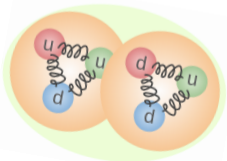
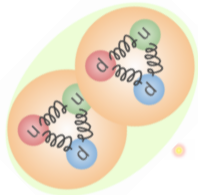
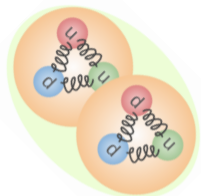
# ALICE



# WUT

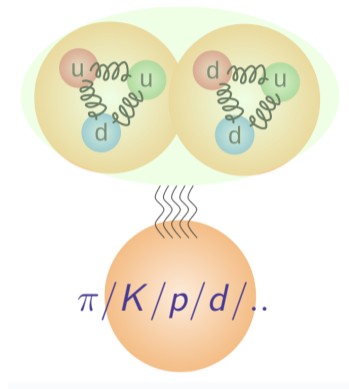


# Why to study deuterons?



# Why to study deuterons? – interactions

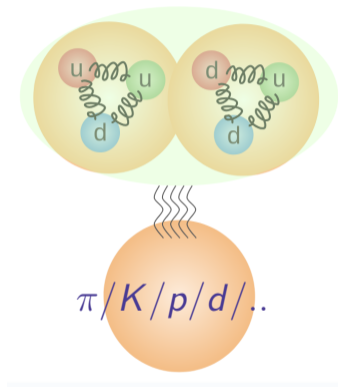
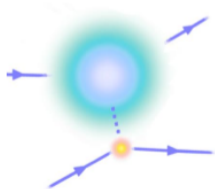
**Kaon-deuteron:** to determine  $K^\pm d$  scattering parameters and obtain the full isospin dependence of the interaction, – a fundamental problem in the strangeness sector in the low-energy regime of QCD.



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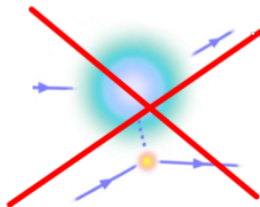
Scattering experiments



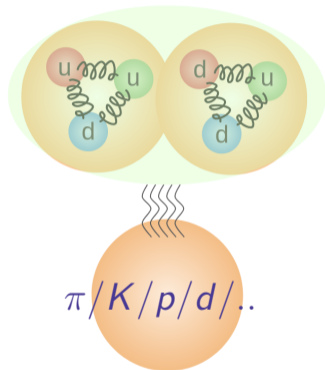
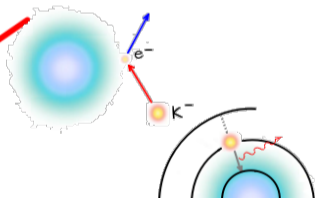
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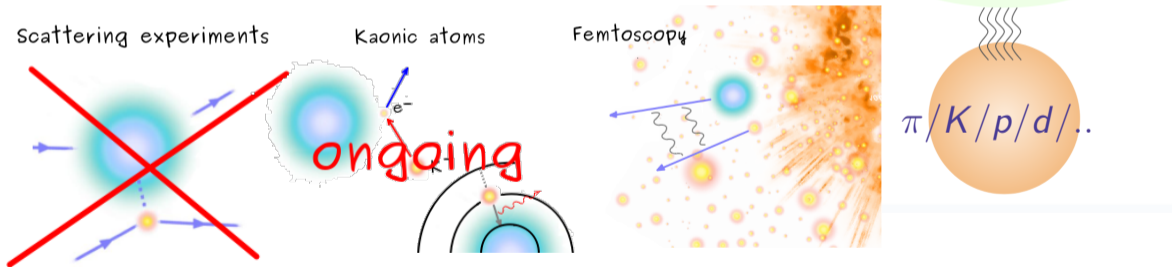


Kaonic atoms



# Why to study deuterons? – interactions

**Kaon-deuteron:** to determine  $K^\pm d$  scattering parameters and obtain the full isospin dependence of the interaction, – a fundamental problem in the strangeness sector in the low-energy regime of QCD.



**Not measured so far!**

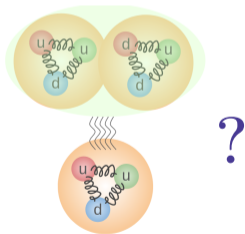
# Why to study deuterons? – interactions

**Proton-deuteron:** deuteron is a composite object consisting of a proton and a neutron. What is the dynamic of the interaction?

?

# Why to study deuterons? – interactions

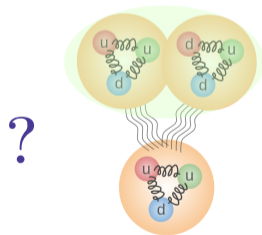
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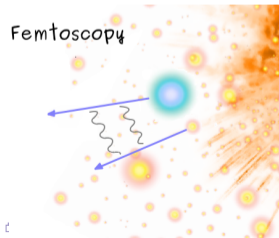
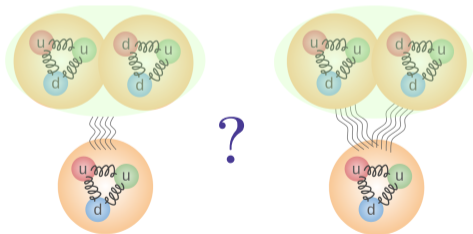
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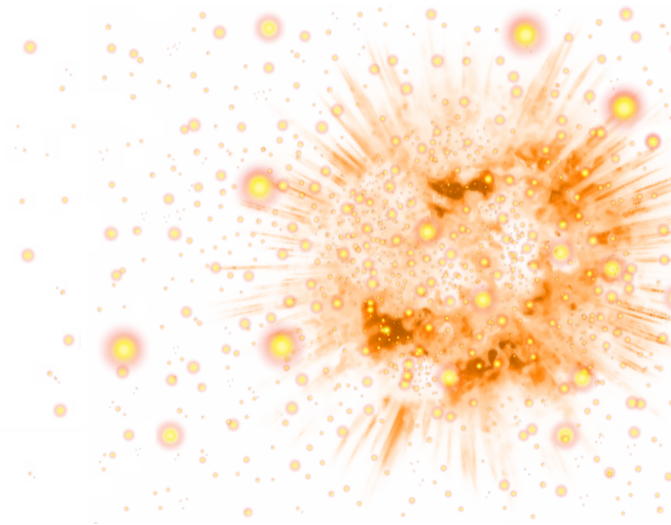
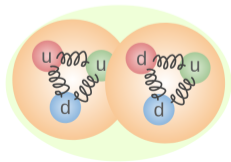


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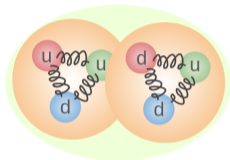


# Why to study deuterons? – production mechanism

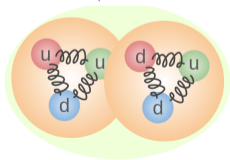


# Why to study deuterons? – production mechanism

"Thermal"



Emission directly from the fireball –  
creation before the chemical freeze-out.

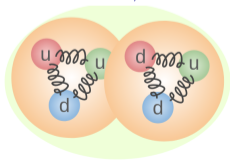


# Why to study deuterons? – production mechanism

"Coalescence"



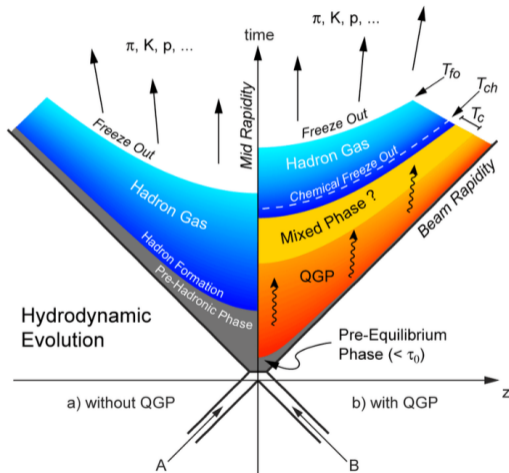
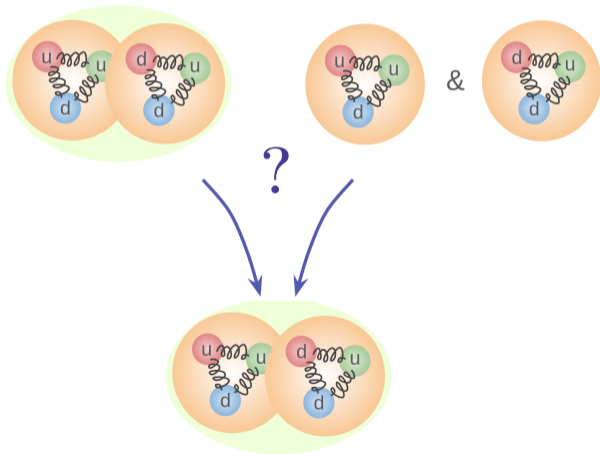
Creation due to the final-state interactions among nucleons after the chemical freeze-out.



# Why to study deuterons? – production mechanism

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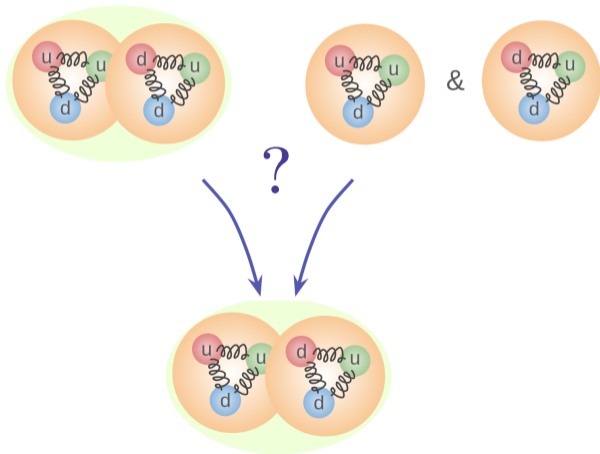
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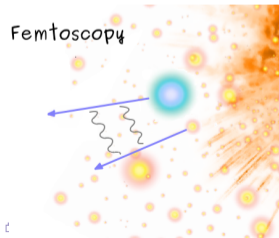
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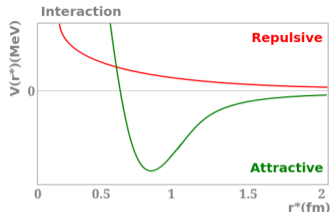
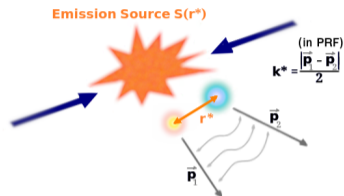
"Coalescence"



**Pion-deuteron, proton-deuteron:**  
to constrain the space-time characteristic  
of emission of deuterons.

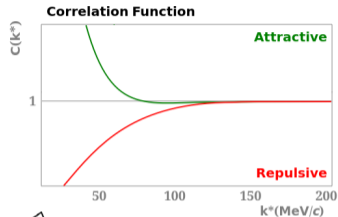


# Femtoscscopy



Two-particle wave function

$$|\Psi(k^*, r^*)|$$



$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3r^* = \xi(k^*) \cdot \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

- **Femtoscscopy**: determination of the space–time characteristics of the particle-emitting source using correlation function (CF) in momentum space.
- **CF**: convolution of the source function and wave function (the latter can combine quantum statistics, as well as strong and Coulomb forces).



# Correlation function

$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3 r^*$$

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- What shape is it?
- What size?
- (Anti-)deuterons' production mechanism?

$$S(r^*) \sim r^{*2} \exp\left(-\frac{r^{*2}}{2R_{AB}^2}\right)$$

# Correlation function

$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3 r^*$$

- What shape is it?
- What size?
- (Anti-)deuterons' production mechanism?
- How to calculate this?
- $f_0$  - scattering length?
- $d_0$  - zero effective-range?

$$S(r^*) \sim r^{*2} \exp\left(\frac{r^{*2}}{2R_{AB}^2}\right)$$

$$\Psi = \exp(-ik^*r) + f \frac{\exp(ik^*r)}{r}$$

$$f^{-1}(k^*) = \frac{1}{f_0} + \frac{1}{2}d_0 k^{*2} - ik^*$$

# A magic power of femtoscopy



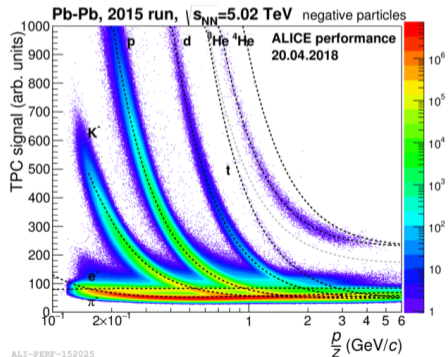
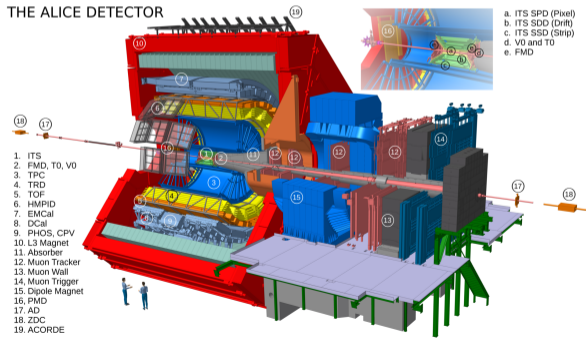
We can compare experimental correlation functions with available models and conclude about their parameterisation, i.e: source and/or interaction parameters.

We need: **experimental data** and **models**.

# Data

- $K^\pm d/K^\pm; \bar{d} \pi^\pm d/\pi^\pm \bar{d}$  CF – Pb–Pb collisions at  $\sqrt{s_{NN}} = 5.02$  TeV  
(3 centrality intervals: 0 – 10%, 10 – 30%, 30 – 50%)
- $pd$  CF – pp collisions at  $\sqrt{s} = 13$  TeV.

THE ALICE DETECTOR



# *Kd* correlation functions

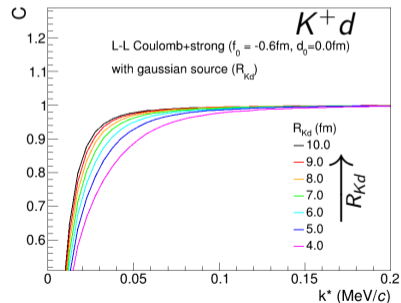
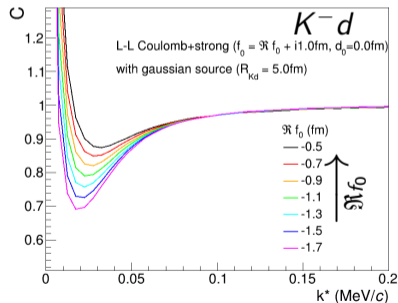
# Modeling correlation functions

- Theoretical CFs modeled with Lednický-Lyuboshits approach [1] with the assumptions:
  - gaussian source,
  - zero effective-range approximation of the interaction,  $d_0 = 0.0$  fm.
- Numerical calculation of theoretical CFs for different fit parameters.

Examples of modeled CFs for different values of fit parameters

Fit parameters:

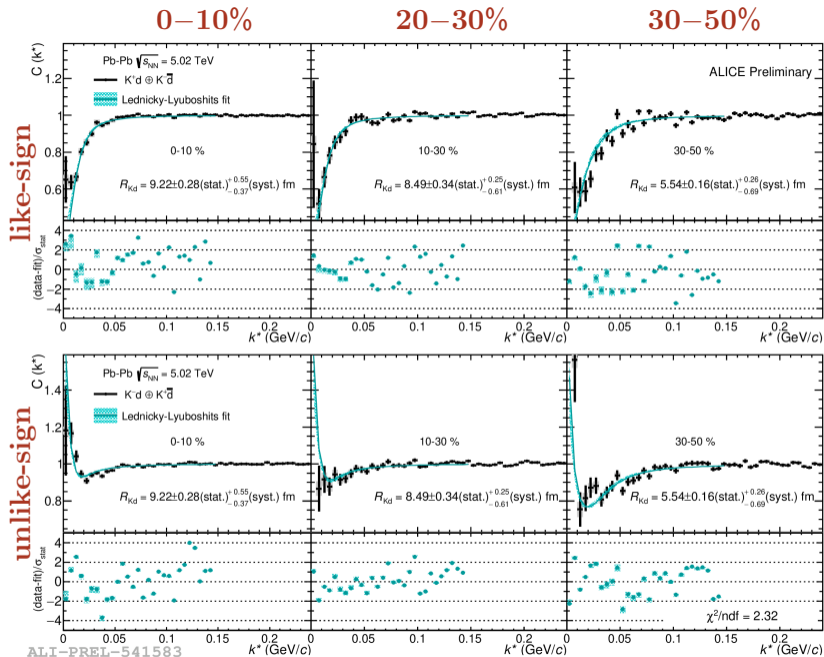
- source radii ( $R_{Kd}$ )
- scattering lengths ( $f_0$ ):
  - $K^-d$  ( $\Re, \Im$ )
  - $K^+d$  ( $\Re$ )



[1] Lednický, R. and Lyuboshits, V. L., Final state interaction effect on pairing correlations between particles with small relative momenta, Yad. Fiz. 35 (1981).

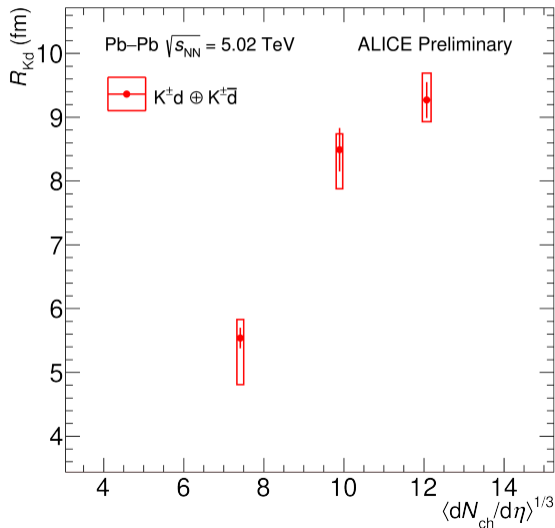
# Kd in Pb-Pb with L-L fit

- Simultaneous fit to 6 CFs.
- Source radii from like- and unlike-sign pairs:
  - one  $R_{Kd}$  per centrality.
- Scattering lengths from three centralities:
  - one  $f_0(\mathcal{R}, \mathcal{S})$  for unlike-sign pairs,
  - one  $f_0(\mathcal{R})$  for like-sign pairs.





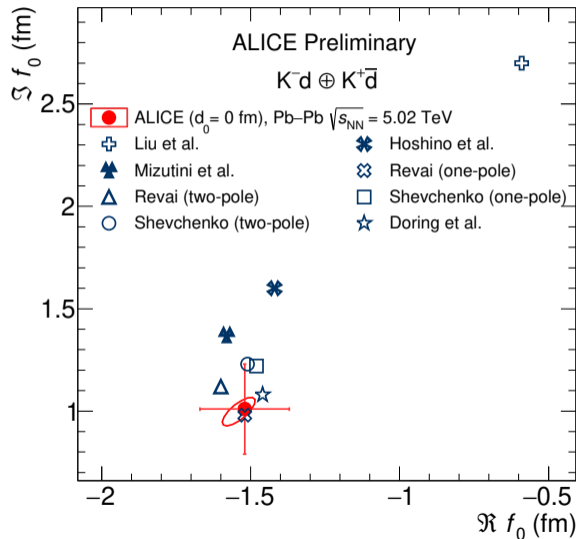
# Kd radii



- 3 radii for 3 centralities (the same radius for all particle pairs).
- Source size increases with multiplicity.

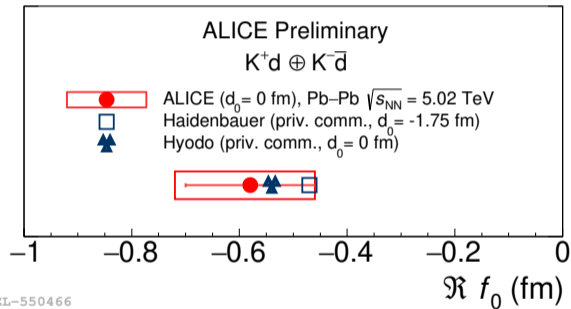
# $K^-d$ scattering length

- $\Re f_0$  and  $\Im f_0$  are in agreement with most of the available calculations.



# $K^+d$ scattering length

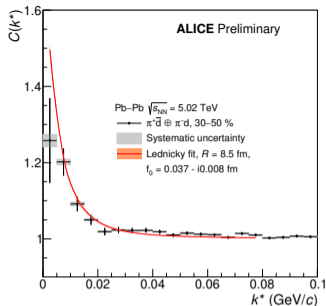
- $\Re f_0$  is in agreement with available calculations.



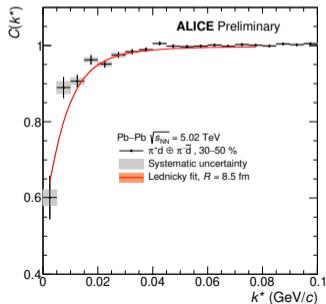
# $\pi d$ correlation functions

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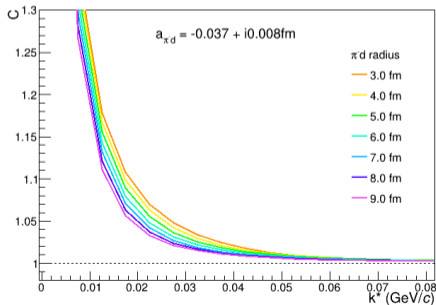
- Lednický-Lyuboshits simultaneous fit to opposite (Coulomb & strong) and same (Coulomb) charges particle pairs.
- Zero effective-range approximation ( $d_0 = 0$ ).



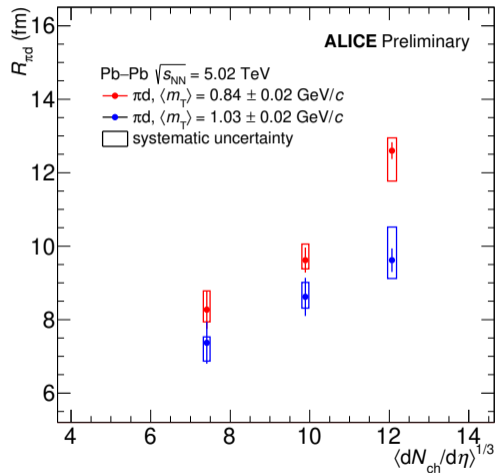
ALI-PREL-504079



ALI-PREL-504079



# $\pi d$ radii



- 6  $\pi d$  radii: 3 centralities, 2  $m_T$  of  $\pi d$  particle pairs.
- $\pi d$  radii depend on  $\langle m_T \rangle$  and multiplicity.

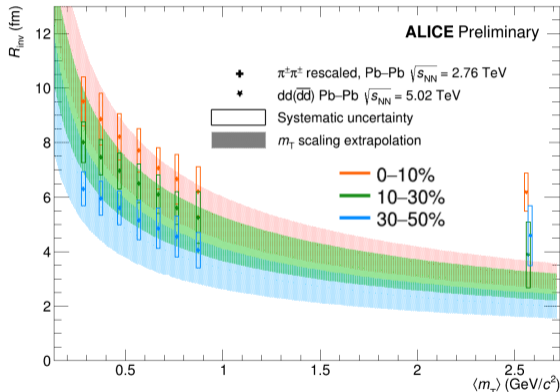
ALI-PREL-504112

# Comparisons with other hadrons

$$R_{\pi d} = \sqrt{R_{\pi}^2 + R_d^2}$$

$$R_d = \sqrt{R_{\pi d}^2 - R_{\pi}^2}$$

- $d(\bar{d})$  source sizes estimated from measured  $\pi d$  radii and single pion radii (measured in Pb–Pb at 2.76 TeV [2] rescaled to 5.02 TeV) are larger than radii expected from  $m_T$  scaling.

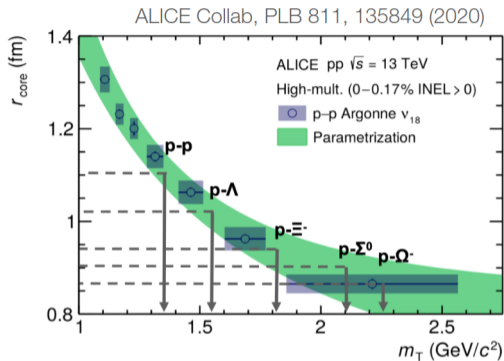


[2] ALICE Collaboration, One-dimensional pion, kaon, and proton femtoscopy in Pb–Pb collisions at  $\sqrt{s_{NN}} = 2.76$  TeV

# $pd$ correlation functions



# Modeling correlation functions

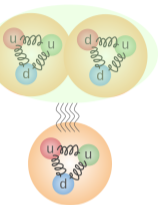


pd source size  $R = 1.08^{+0.06}_{-0.06} \text{ fm}$

$$C(k^*) = \int S(\vec{r}^*) |\Psi(\vec{k}^*, \vec{r}^*)|^2 d^3 \vec{r}^*$$

# Modeling correlation functions – two body

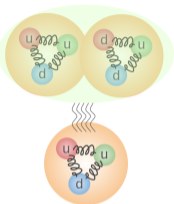
p-d as an effective two body  
Lednický-Lyuboshits approach with  
Strong interaction constrained from  
the scattering measurements [3].



$$C(k^*) = \int S(\vec{r}^*) |\Psi(\vec{k}^*, \vec{r}^*)|^2 d^3 \vec{r}^*$$

[3] In the backup.

# Modeling correlation functions – two body



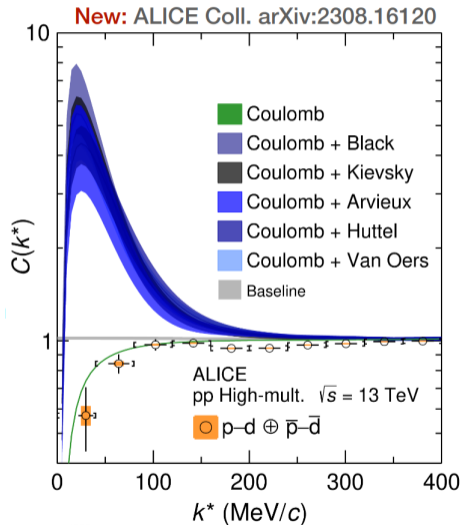
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$$\text{pd source size } R = 1.08^{+0.06}_{-0.06} \text{ fm}$$

**Failed to reproduce experimental data.**

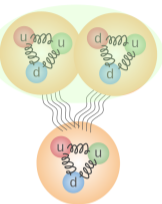
- Asymptotic strong interaction: not sufficient for distances  $\sim 1$  fm?
- Pauli blocking at short distances?

[3] In the backup.



ALI-PUB-556039

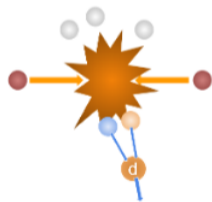
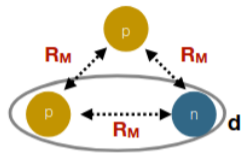
# Modeling correlation functions – three body



A three-nucleon dynamics of p-(pn)[4]

$R_M = 1.43 \pm 0.16 \text{ fm}$ , nucleon-nucleon source size in pd

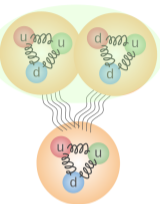
Assumption: coalescence production,  
 $A_d$  - formation probability of d



$$C(k^*) = \frac{1}{16A_d} \sum_{m_2, m_1} \int \rho^5 d\rho d\Omega |\Psi_{m_2, m_1}(\vec{k}^*)|^2 \frac{e^{-\rho/4R_M^2}}{(4\pi R_M^2)^3}$$

[4] M. Viviani, et al. Role of three-body dynamics in nucleon-deuteron correlation functions

# Modeling correlation functions – three body



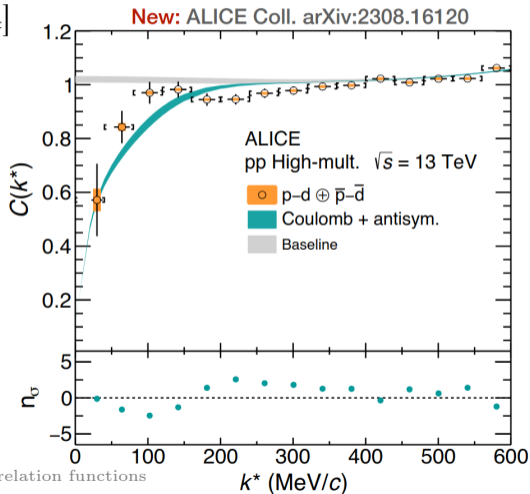
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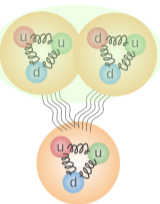
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**Coulomb only cannot reproduce  
the experimental data.**



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# Modeling correlation functions – three body



A three-nucleon dynamics of  $p$ -( $pn$ ) [4]

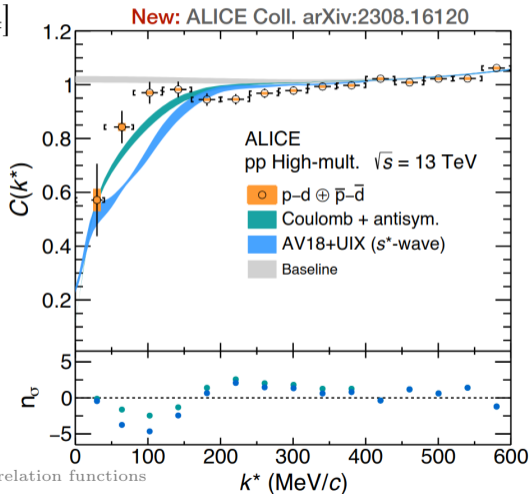
$$R_M = 1.43 \pm 0.16 \text{ fm},$$

nucleon-nucleon source size in  $pd$

Assumption: coalescence production,

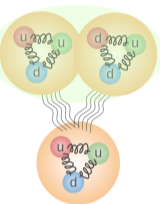
$A_d$  - formation probability of  $d$

**EFT NLO (s-wave) cannot describe the experimental data.**



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# Modeling correlation functions – three body



A three-nucleon dynamics of p-(pn)[4]

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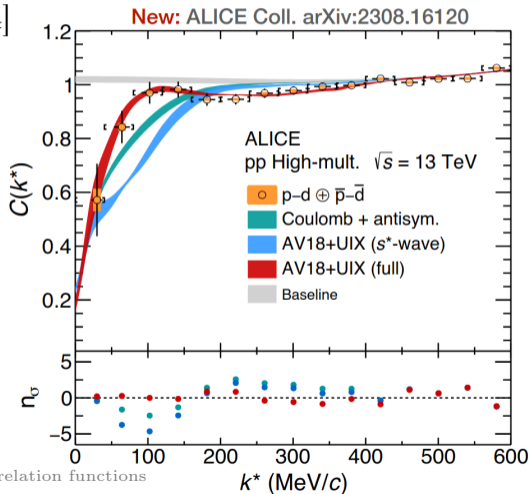
nucleon-nucleon source size in pd

Assumption: coalescence production,  
 $A_d$  - formation probability of d

**EFT NLO (s+p+d waves) can describe the experimental data.**

- Three-body dynamics at short distances
- Higher partial wave up to d-waves are necessary (s-wave only is not sufficient)

[4] M. Viviani, et al. Role of three-body dynamics in nucleon-deuteron correlation functions



# Summary

- First ever measurements of:

- femtoscopic correlations with deuterons in relativistic heavy-ion collisions,

- the scattering parameters of the strong interaction,

- of  $K^\pm d$  pairs,

- $d$  source sizes,

- $\pi d$  and  $Kd$  source sizes.

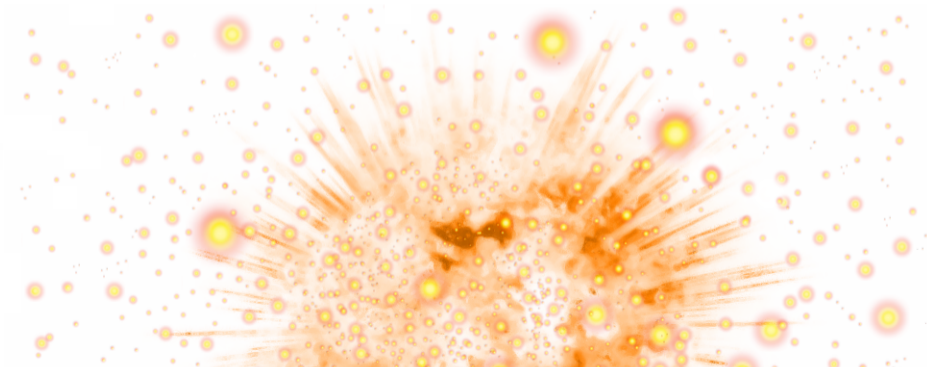


# Summary

- First ever measurements of:

- femtoscopic correlations with deuterons in relativistic heavy-ion collisions,
- the scattering parameters of the strong interaction, of  $K^\pm d$  pairs,
- $d$  source sizes,
- $\pi d$  and  $Kd$  source sizes,
- femtoscopic correlations with deuterons in pp collisions,
- Revealing the importance of three-body interactions and higher order partial waves at small distances.

Thank you for your attention!



[3]

$S = 1/2$		$S = 3/2$		
$a_0(\text{fm})$	$d_0(\text{fm})$	$a_0(\text{fm})$	$d_0(\text{fm})$	
$1.30^{+0.20}_{-0.20}$	—	$11.40^{+1.80}_{-1.20}$	$2.05^{+0.25}_{-0.25}$	<i>Van Oers, Brockmann et al. Nucl. Phys. A 561-583 (196)</i>
$2.73^{+0.10}_{-0.10}$	$2.27^{+0.12}_{-0.12}$	$11.88^{+0.10}_{-0.40}$	$2.63^{+0.01}_{-0.02}$	<i>J.Arviex et al. Nucl. Phys. A 221 253-268 (1973)</i>
4.0	—	11.1	—	<i>E.Huttel et al. Nucl. Phys. A 406 443-455 (1983)</i>
0.024	—	13.8	—	<i>A.Kievsky et al. PLB 406 292-296 (1997)</i>
$-0.13^{+0.04}_{-0.04}$	—	$14.70^{+2.30}_{-2.30}$	—	<i>T.C.Black et al. PLB 471 103-107 (1999)</i>