

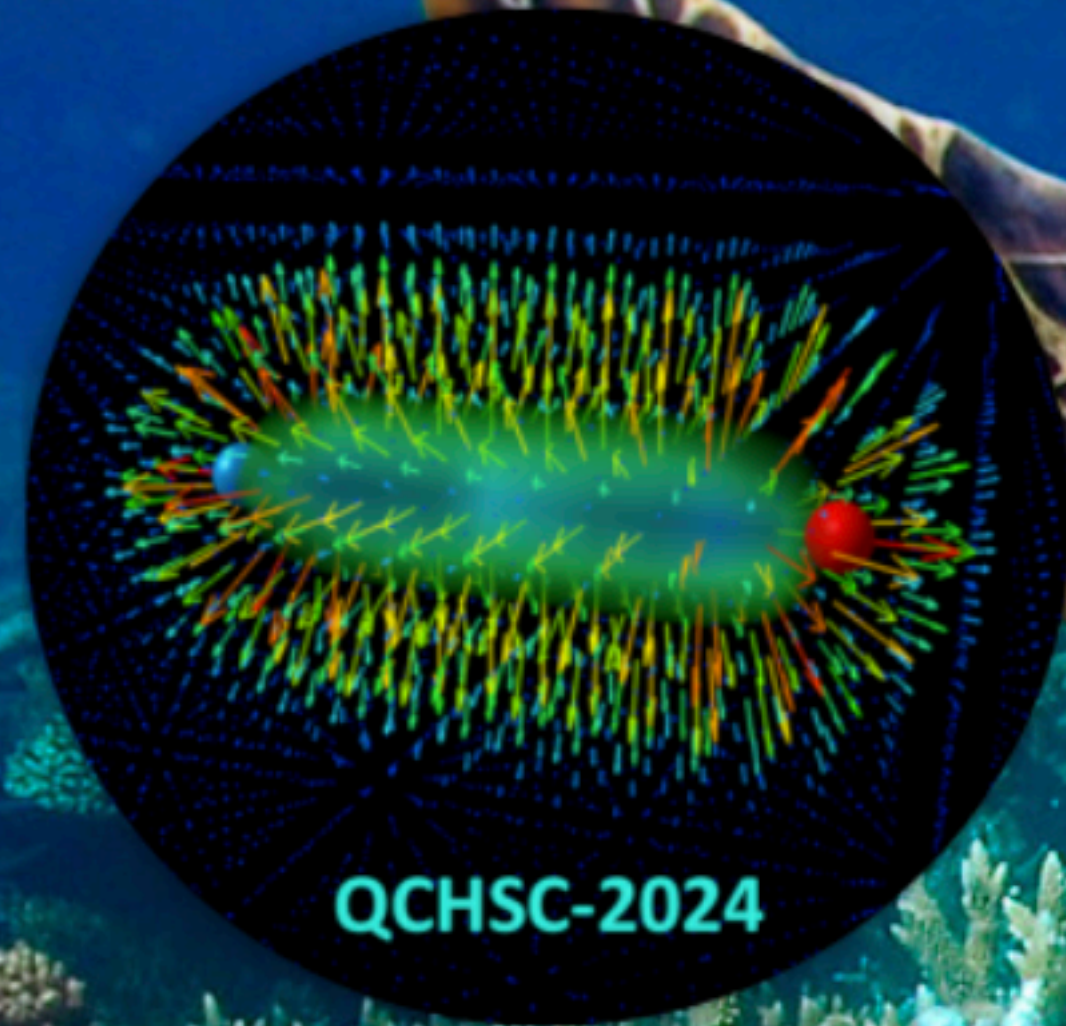
β decay as a probe of new physics

Confinement 2024

Cairns, Australia, August 19 - 24, 2024



André Walker-Loud



QCHSC 2024

The XVth Quark Confinement and the Hadron
Spectrum Conference

β decay as a probe of new physics

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Searches for New Physics in Low Energy Nuclear Physics Environments

Search for BSM (Beyond the Standard Model) physics in low-energy environments offers complimentary and competitive constraints to collider searches:

Precision comparison with experiment

- neutron, nuclear β -decay
- Kaon β -decay

Nuclear Physics is the “background”

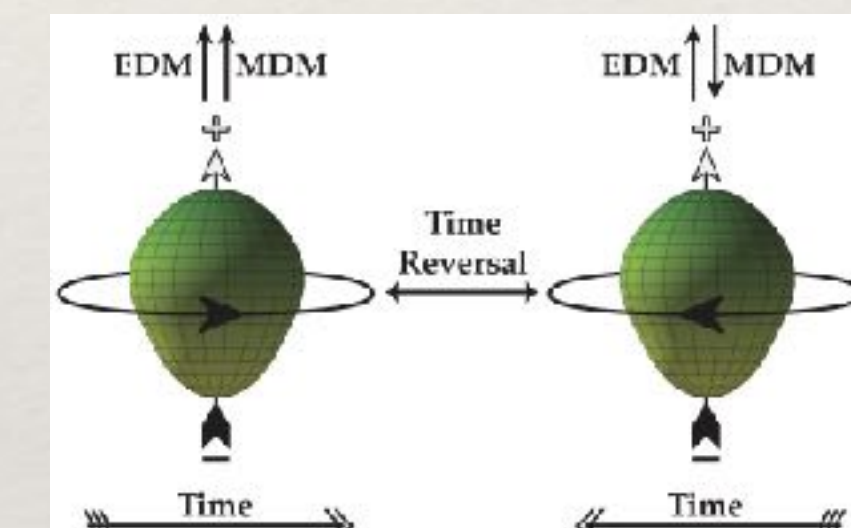
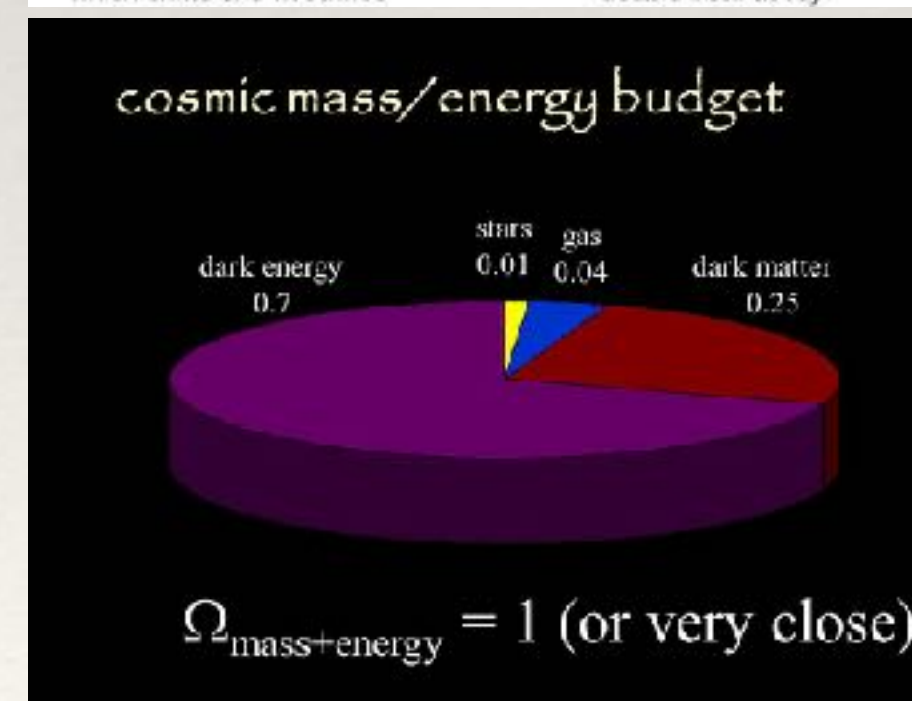
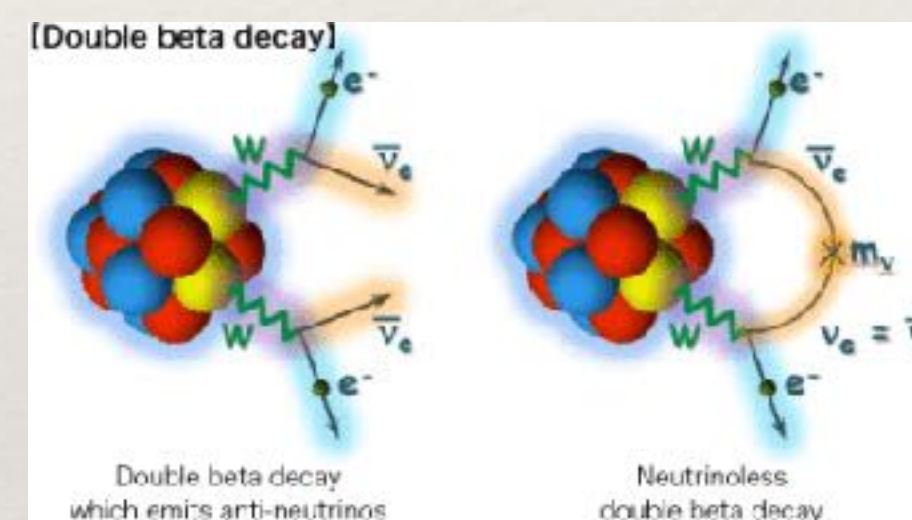
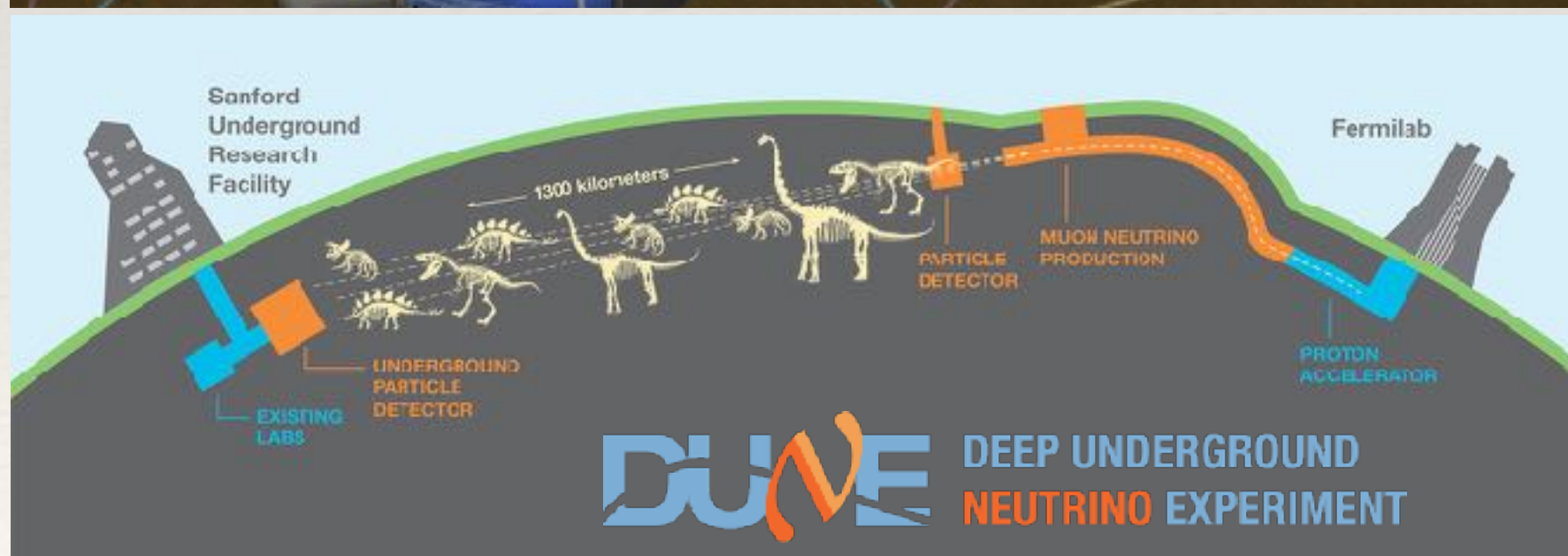
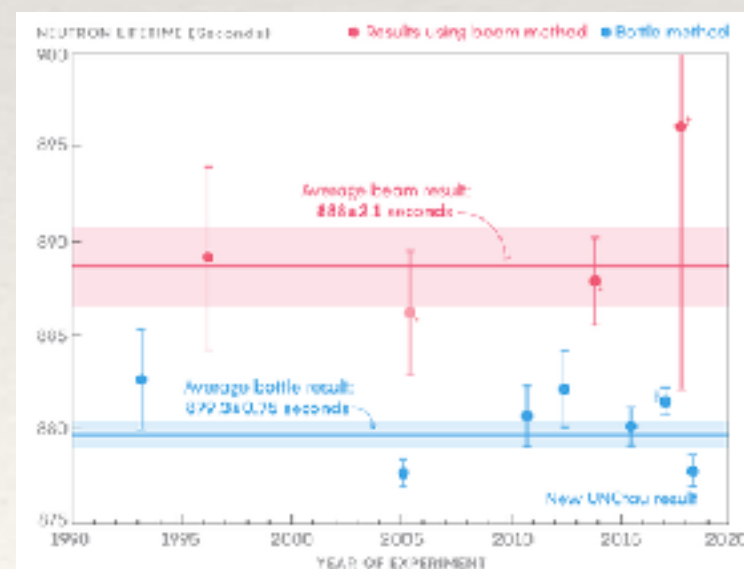
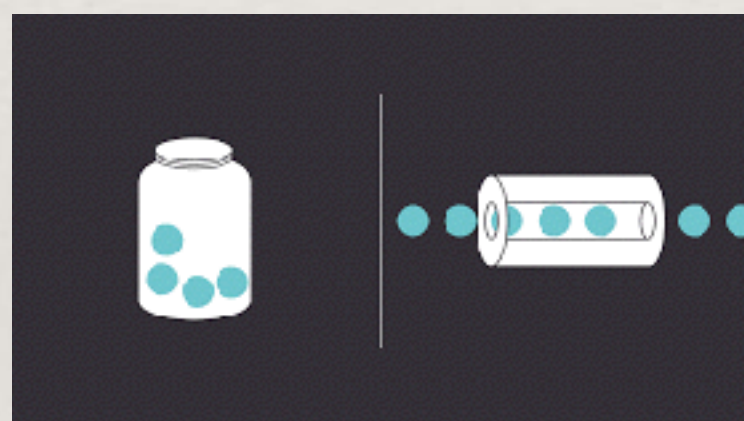
- long-baseline neutrino-nucleus scattering

SM Forbidden

- $0\nu\beta\beta$
- Dark Matter

SM “absent”

- EDMs
- $\mu \rightarrow e$



β -decay — precision tests of the Standard Model (SM)

□ The generic β -decay rate is given by

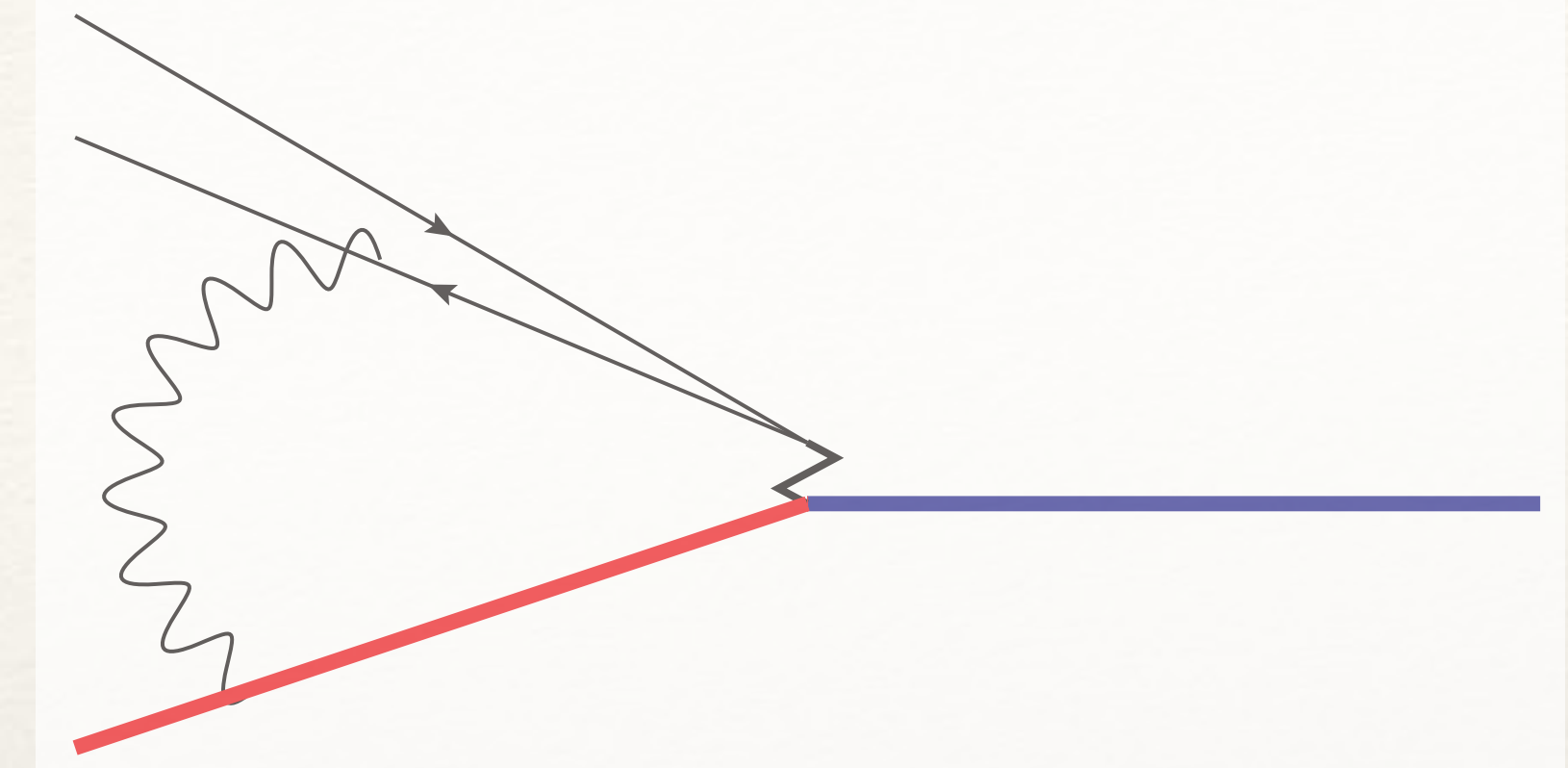
$$\Gamma_k = \left(G_F^{(\mu)} \right)^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{\text{RC}}) \times F_{\text{kin}}$$

Fermi's decay constant
measured with μ -decay

non-perturbative
hadronic matrix elements

radiative QED
corrections

phase space
kinematic factor



Quark mixing matrix elements

V_{CKM} = Cabibbo - Kobayashi - Maskawa matrix

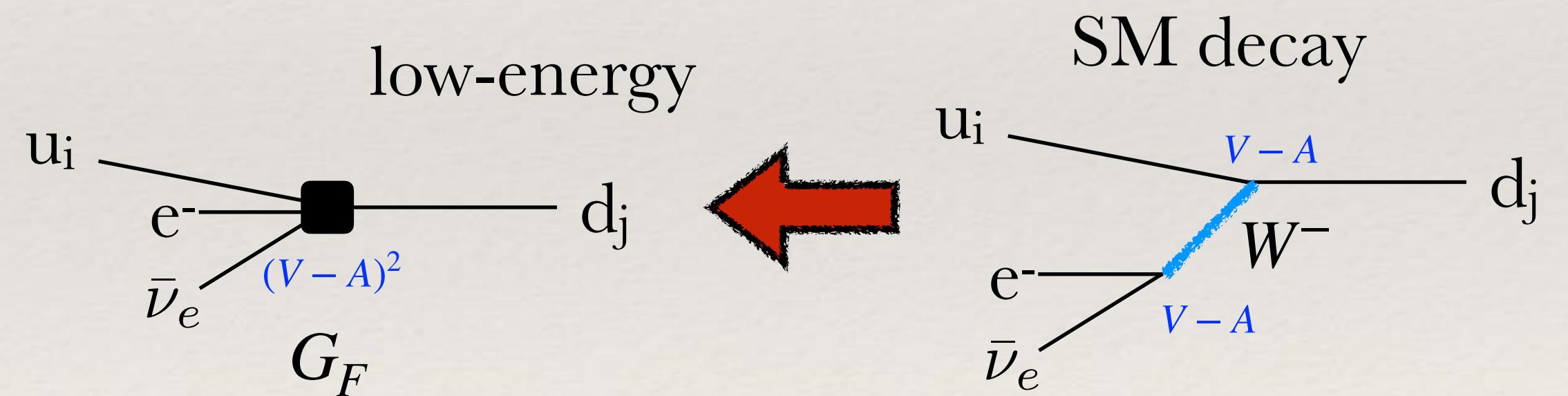
$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{\text{weak}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{QCD}}$$

V_{CKM} is a unitary matrix — if SM only

no new physics: $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$

Determining V_{ij} requires knowledge of $|M_{\text{had}}|$

→ we need LQCD (Lattice QCD)



β -decay — precision tests of the Standard Model (SM)

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$$\Gamma_k = \left(G_F^{(\mu)} \right)^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{\text{RC}}) \times F_{\text{kin}}$$

Fermi's decay constant measured with μ -decay



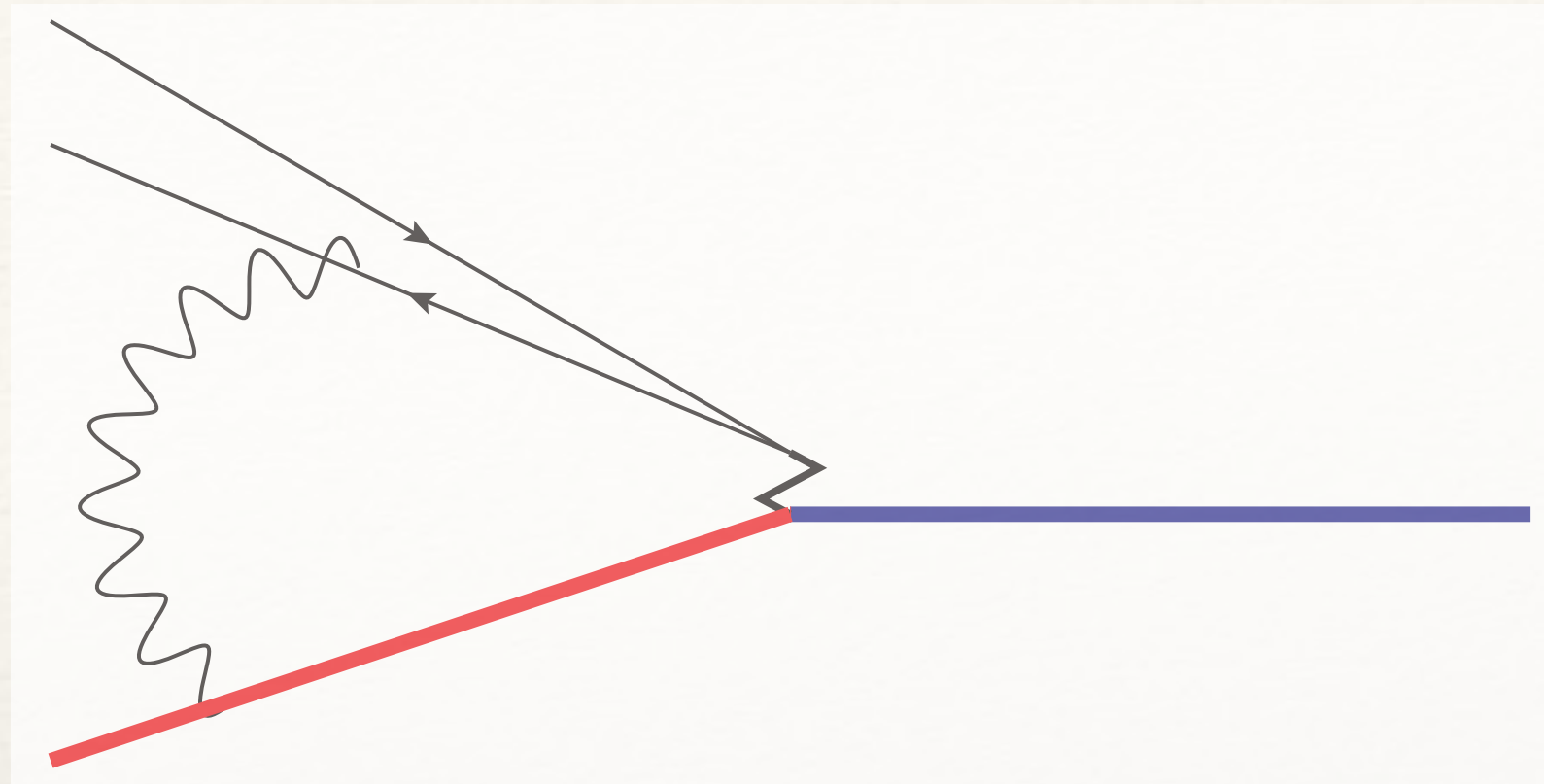
non-perturbative hadronic matrix elements



radiative QED corrections



phase space kinematic factor



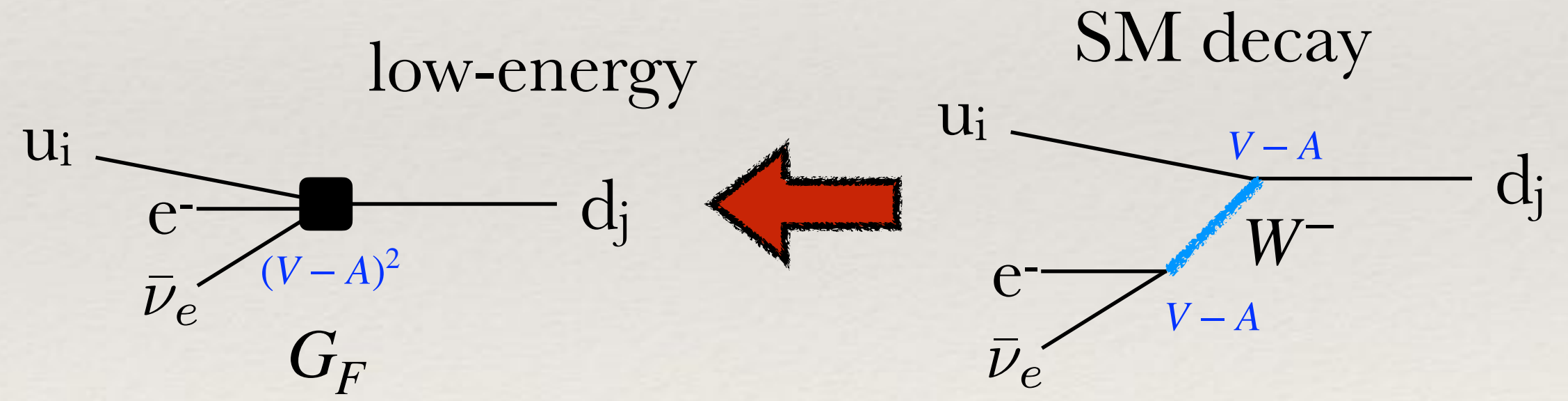
Quark mixing matrix elements

V_{CKM} = Cabibbo - Kobayashi - Maskawa matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{\text{weak}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{\text{QCD}}$$

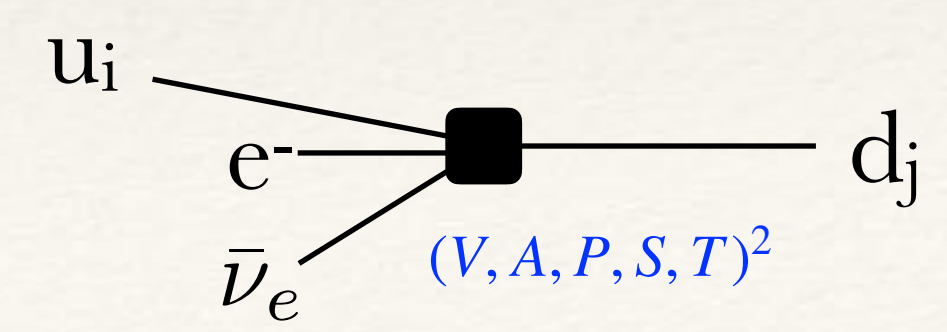
V_{CKM} is a unitary matrix — if SM only
no new physics: $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$

Determining V_{ij} requires knowledge of $|M_{\text{had}}|$
→ we need LQCD (Lattice QCD)



What would heavy BSM contribution look like?

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \neq 1$$



β -decay - determining V_{ij}

$$\Gamma_k = \left(G_F^{(\mu)}\right)^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{\text{RC}}) \times F_{\text{kin}}$$

V_{ud} $\pi^\pm \rightarrow \pi^0 e \bar{\nu}_e$
 theoretically clean
 experimentally noisy

nuclear $0^+ \rightarrow 0^+$
 theoretically messy
 experimentally clean

$n \rightarrow p e \bar{\nu}_e$
 theoretically clean-ish
 experimentally clean-ish

V_{us} $K \rightarrow \pi \mu \bar{\nu}_\mu$
 theoretically clean
 experimentally clean

$$\frac{q^\mu \langle \pi^-(p+q) | \bar{s} \gamma_\mu u | K^0(p) \rangle}{m_K^2 - m_\pi^2} \Big|_{q^2 \rightarrow 0} \rightarrow f_+(0) |V_{us}|$$

$\frac{V_{us}}{V_{ud}}$ $\frac{K \rightarrow \mu \bar{\nu}_\mu}{\pi \rightarrow \mu \bar{\nu}_\mu}$
 theoretically clean
 experimentally clean

$$\frac{\partial^\mu \langle 0 | \bar{s} \gamma_\mu \gamma_5 u | K^+ \rangle}{\partial^\mu \langle 0 | \bar{d} \gamma_\mu \gamma_5 u | \pi^+ \rangle} \rightarrow \frac{m_K^2 F_K |V_{us}|}{m_\pi^2 F_\pi |V_{ud}|}$$

β -decay - determining V_{ij} $\Gamma_k = \left(G_F^{(\mu)}\right)^2 \times |V_{ij}|^2 \times |M_{\text{had}}|^2 \times (1 + \delta_{\text{RC}}) \times F_{\text{kin}}$

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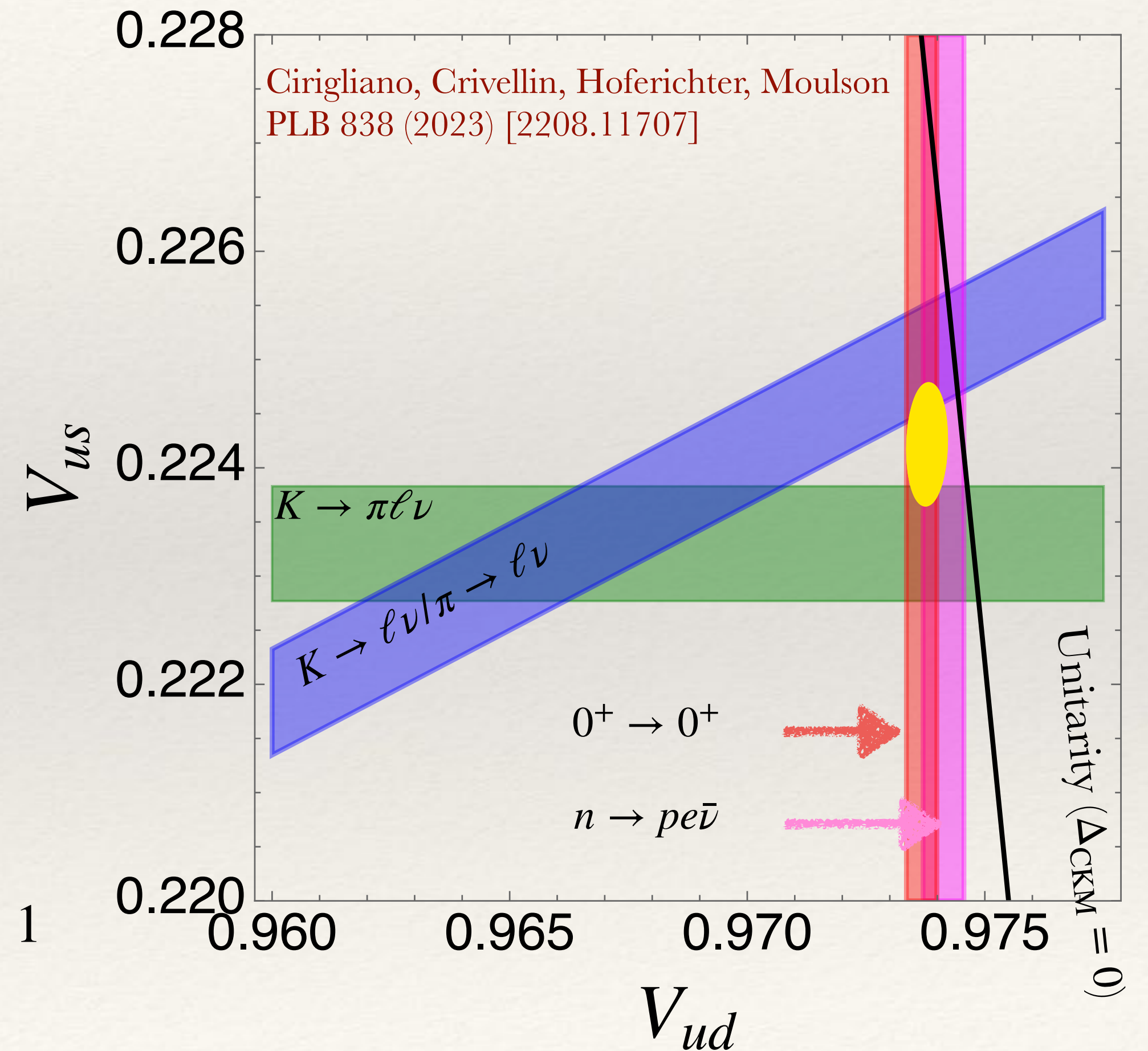
$$\frac{q^\mu \langle \pi^-(p+q) | \bar{s} \gamma_\mu u | K^0(p) \rangle}{m_K^2 - m_\pi^2} \Big|_{q^2 \rightarrow 0} \rightarrow f_+(0) |V_{us}|$$

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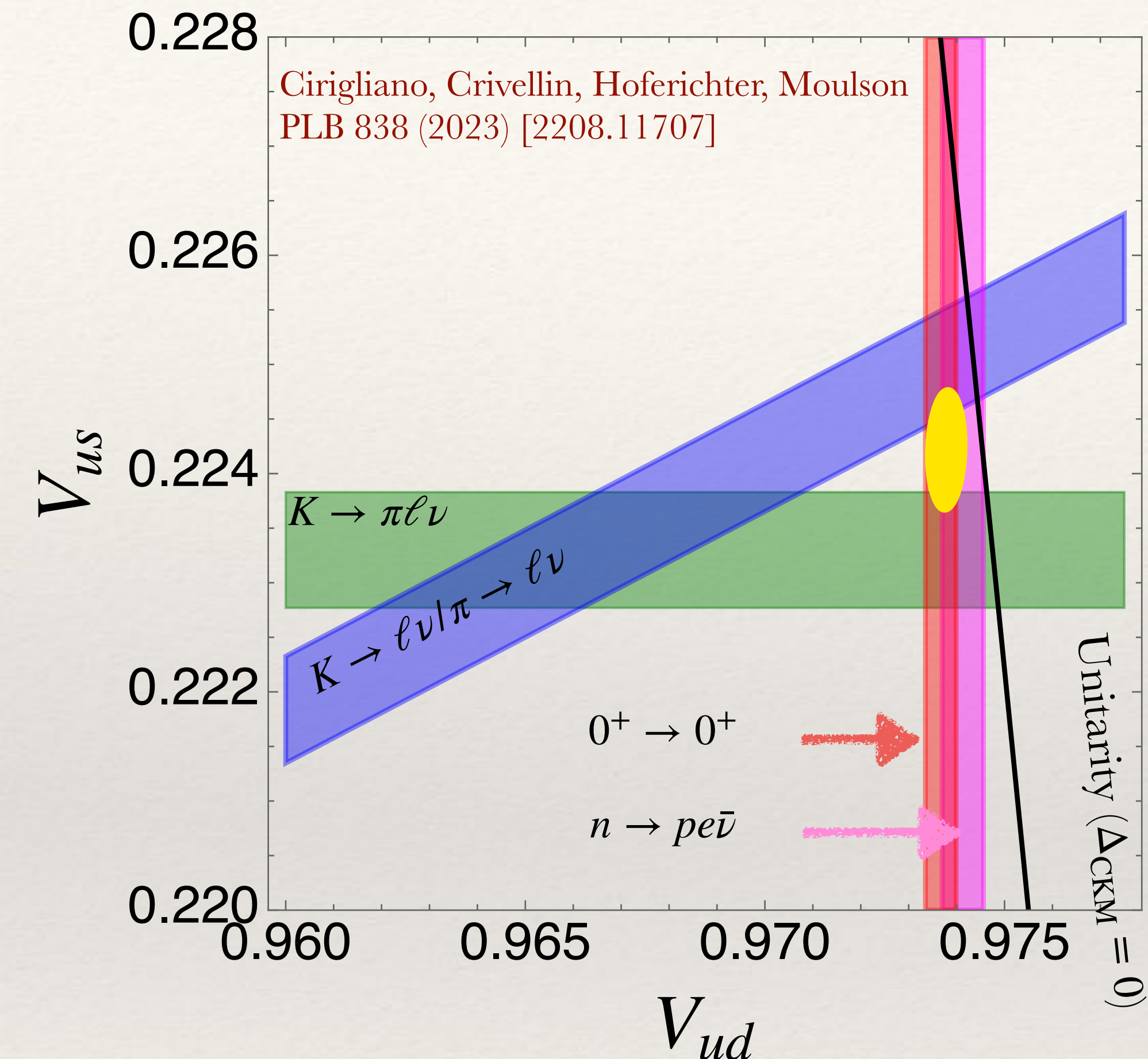
$$\frac{\partial^\mu \langle 0 | \bar{s} \gamma_\mu \gamma_5 u | K^+ \rangle}{\partial^\mu \langle 0 | \bar{d} \gamma_\mu \gamma_5 u | \pi^+ \rangle} \rightarrow \frac{m_K^2 F_K |V_{us}|}{m_\pi^2 F_\pi |V_{ud}|}$$

$$\Delta_{\text{CKM}} = |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = -0.00176(56)$$

Cabibbo Angle Anomaly



β -decay - Tension in the first-row of CKM



$$\begin{aligned} \Delta_{\text{CKM}} &= |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 \\ &= -0.00176(56) \end{aligned}$$

Cabibbo Angle Anomaly

- Most significant tension with unitarity comes from Kaons

$$K \rightarrow \pi \ell \nu \text{ vs } K \rightarrow \ell \nu / \pi \rightarrow \ell \nu$$

$$(K_{\ell 3} \text{ vs } K_{\ell 2} / \pi_{\ell 2})$$

- Some determinations of these CKM elements

$$V_{ud}^{0^+ \rightarrow 0^+} = 0.97367(11)_{\text{exp}}(13)_{\Delta_V^R}(27)_{\text{NS}}[32]_{\text{total}}$$

$$V_{us}^{K_{\ell 3}} = 0.22330(35)_{\text{exp}}(39)_{f_+}(8)_{\text{IB}}[53]_{\text{total}}$$

- At this level of precision, careful treatment of radiative QED corrections has become the frontier

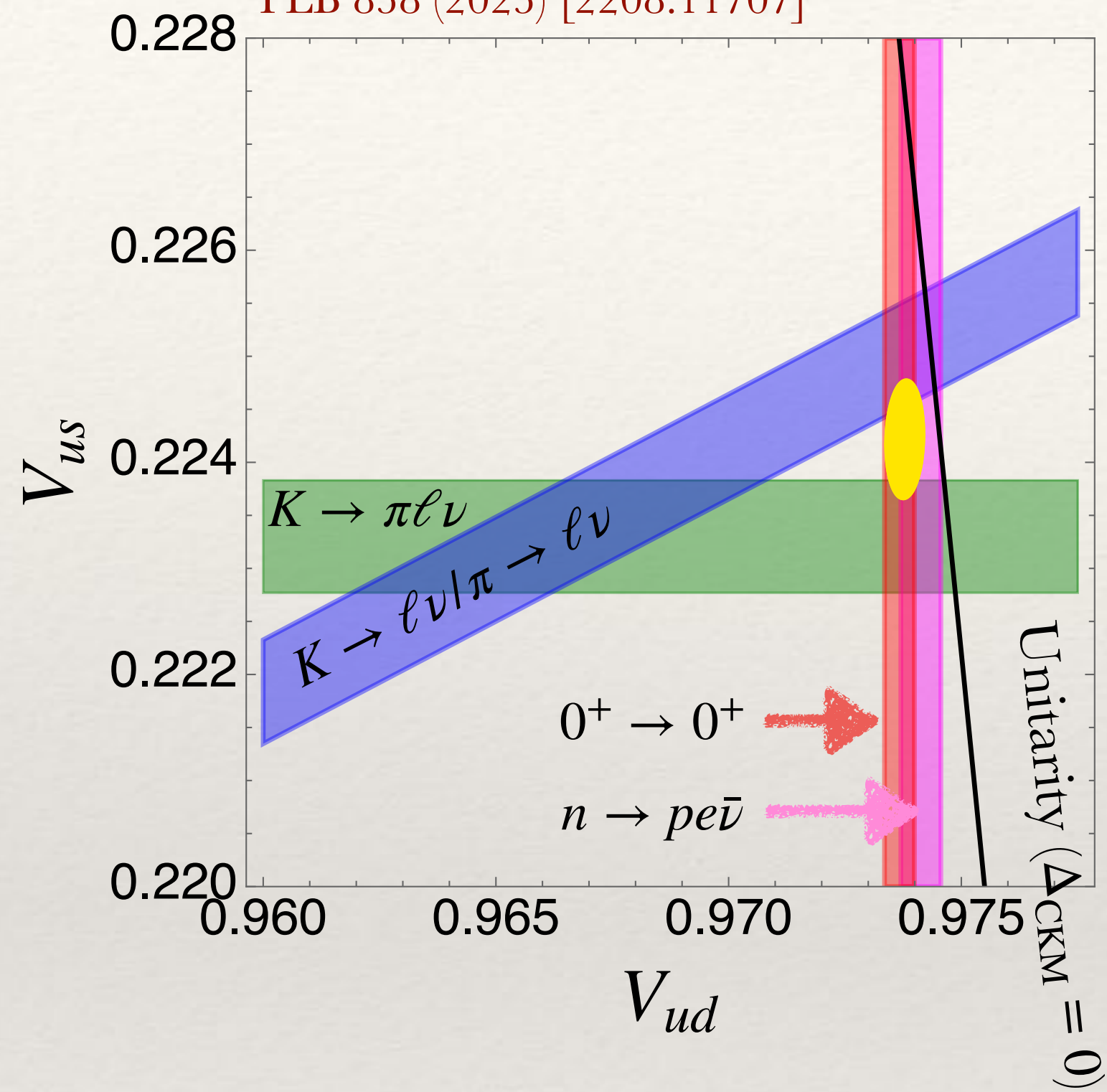
- Original Sirlin & Marciano et al approach (current algebra)

- modern pheno and EFT treatments

- lattice QCD + QED

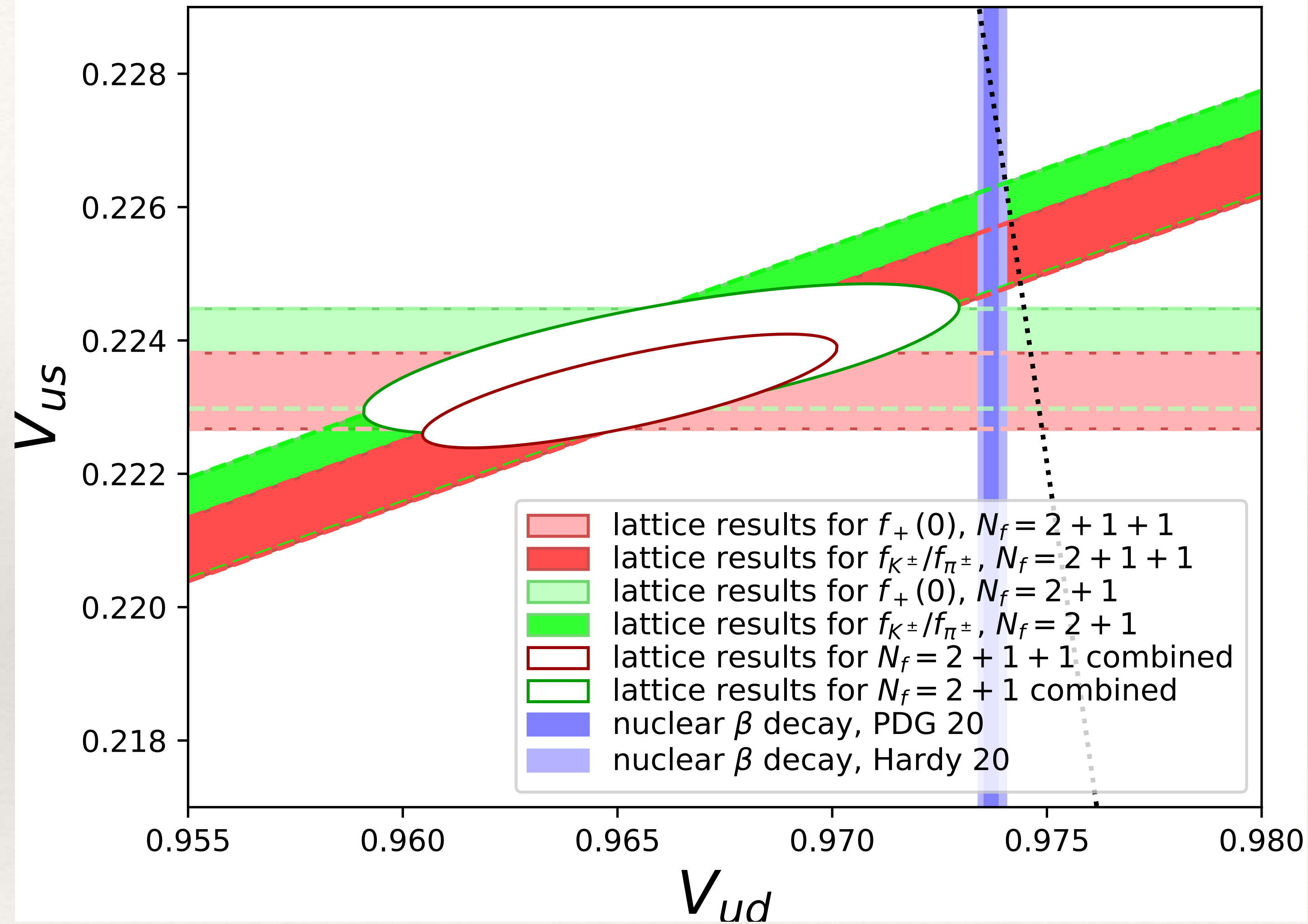
β -decay - Tension in the first-row of CKM

Cirigliano, Crivellin, Hoferichter, Moulson
PLB 838 (2023) [2208.11707]



- 3σ tension is seen with $N_f = 2 + 1 + 1$
- less tension with $N_f = 2 + 1$

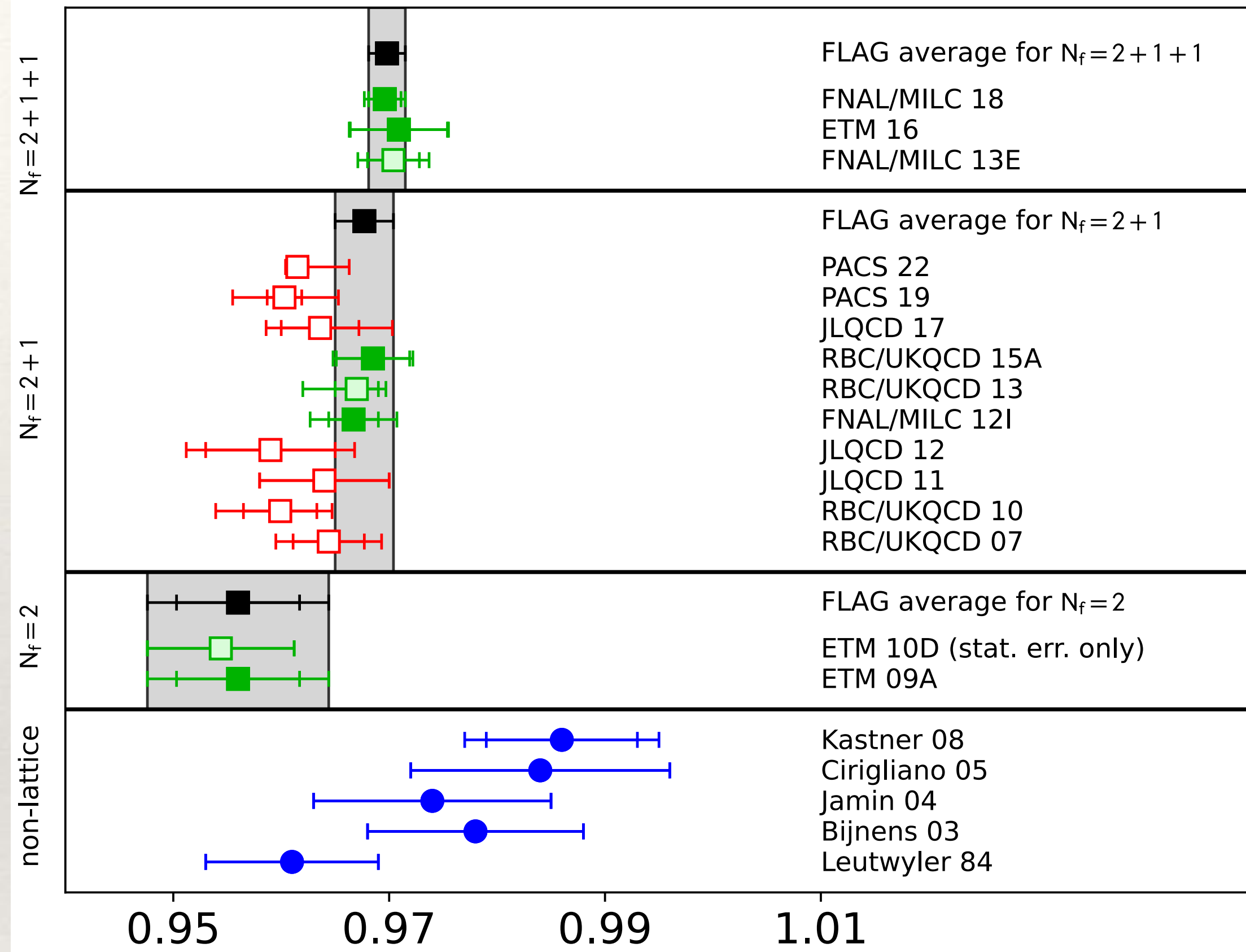
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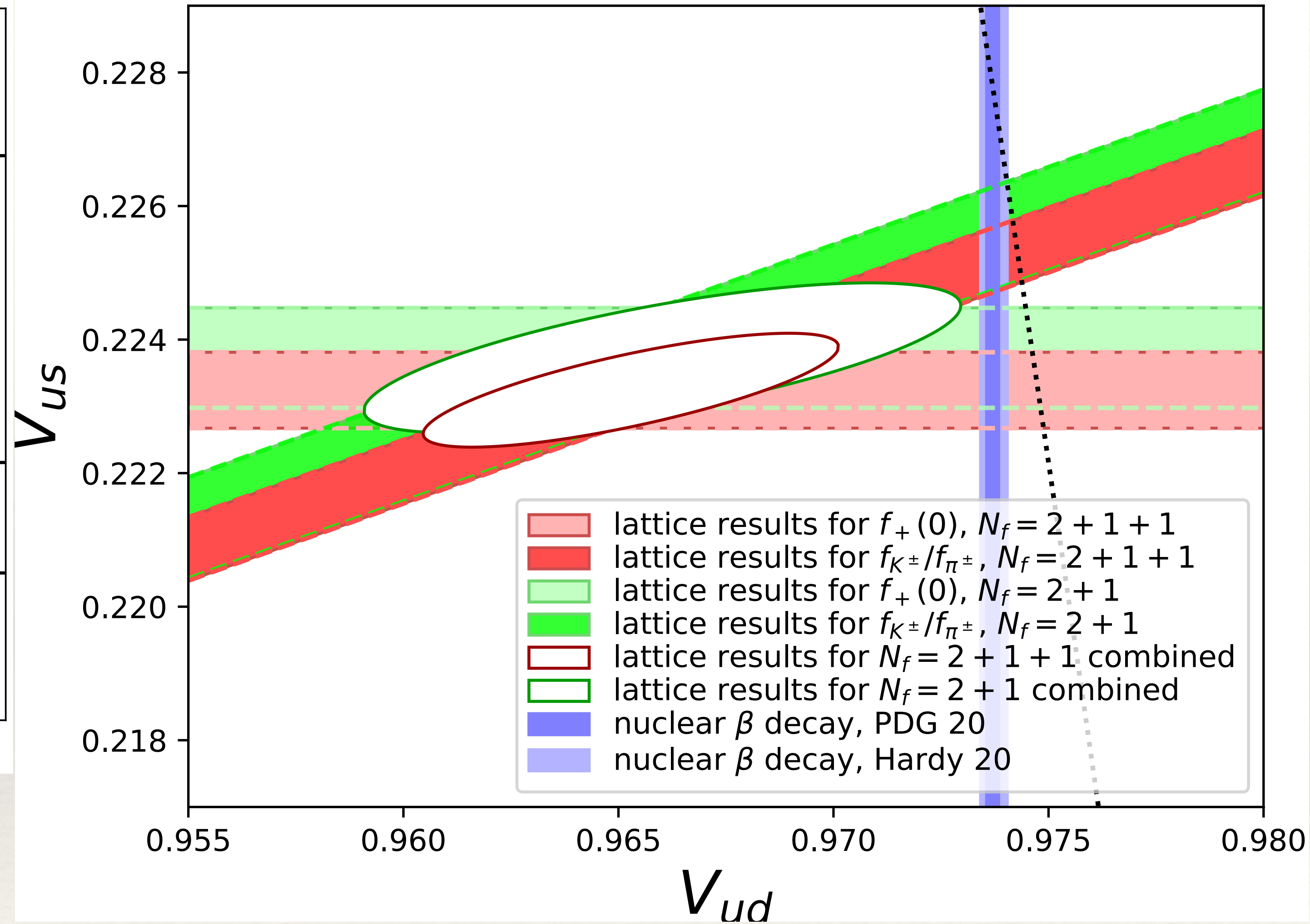
β -decay - Tension in the first-row of CKM

FLAG 2023

$f_+(0)$



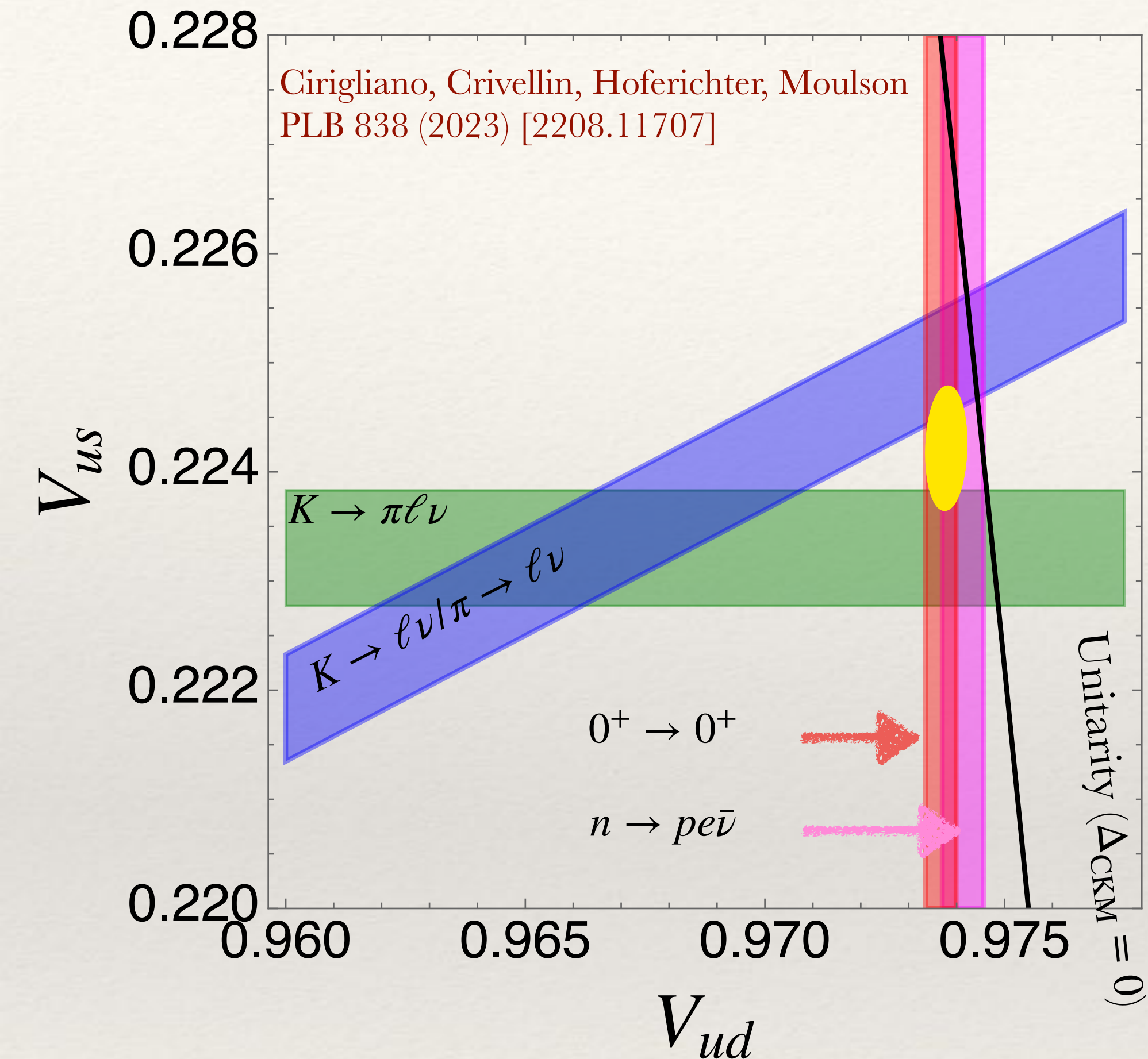
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□ Currently - $> 3\sigma$ tension is driven by a single $N_f=2+1+1$ LQCD result for $f_+(0)$

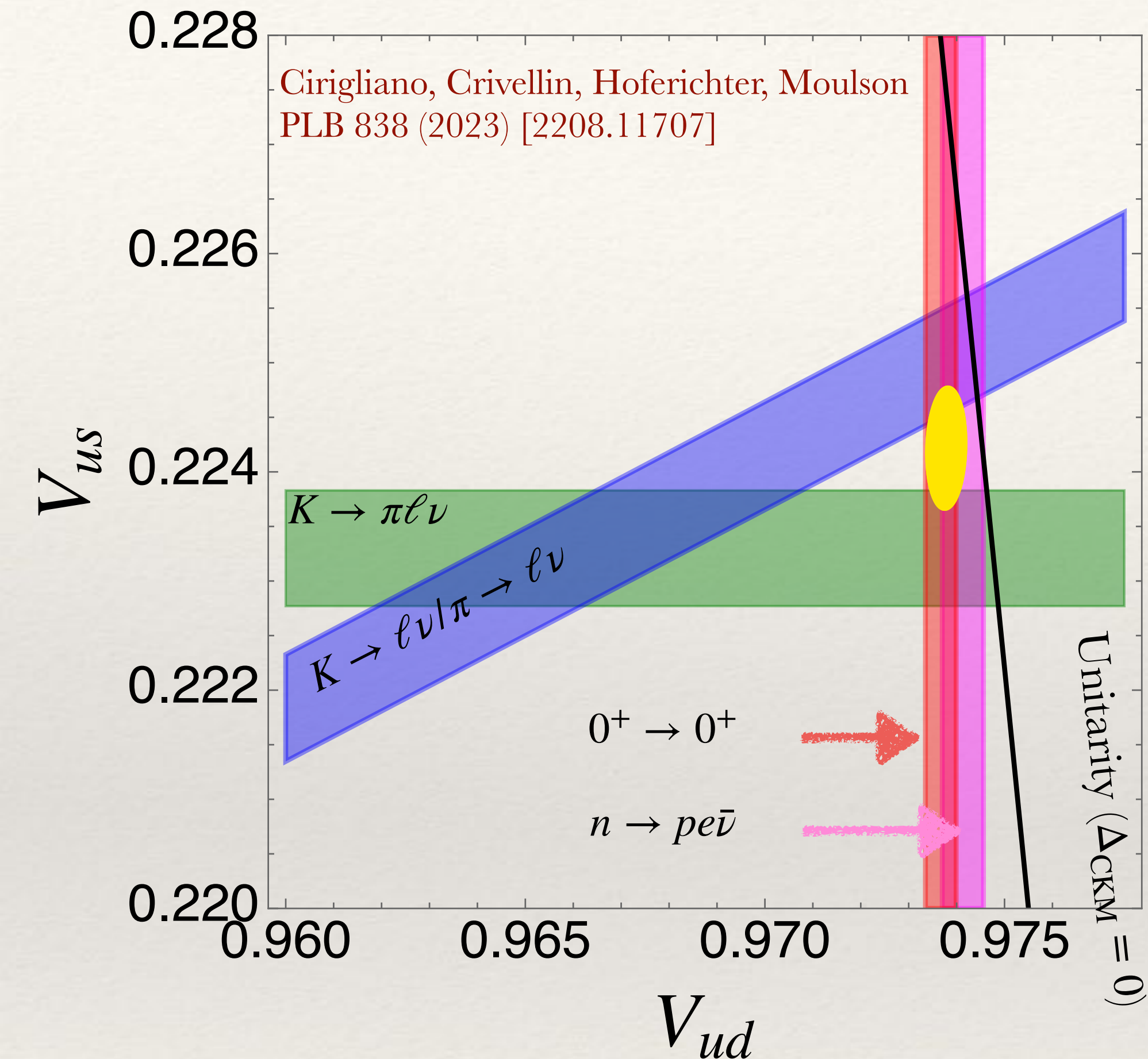
□ It is important for other LQCD results to be pushed to the same precision as FNAL/MILC PACS-CS is getting there with $N_f=2+1$ [Lattice2023, 2311.16755] - we need more

β -decay - Prospects for improving experimental precision



- Current tension in global kaon fits: p-value $< 1\%$ [2208.11707]
 - $K_{\ell 2}$ measurement dominated by single experiment
 - $K_{\mu 3}/K_{\mu 2}$ measurement @ 0.2% will add clarity — NA62
- Tomáš Husek**
Mon. 16:40
- V_{ud} determination dominated by nuclear $0^+ \rightarrow 0^+$ decays
 - challenging to control nuclear structure corrections at 10^{-4} precision
 - $V_{ud}^{0^+ \rightarrow 0^+} = 0.97367(11)_{\text{exp}}(13)_{\Delta_V^R}(27)_{\text{NS}}[32]_{\text{total}}$
 - $V_{ud}^{0^+ \rightarrow 0^+} = 0.97364(10)_{\text{exp}}(12)_{g_V}(22)_{\mu}(12)_{\delta_C}(43)_{g_V^{NN}}(20)_{\delta_{\text{NS}}^E}[56]_{\text{total}}$ [2405.18464]
 - Take best τ_n and $\lambda = g_A/g_V$ measurement from $n \rightarrow p e \bar{\nu}$
 - $V_{ud}^{n, \text{PDG}} = 0.97441(3)_f(13)_{\Delta_V^R}(82)_{\lambda}(28)_{\tau_n}[88]_{\text{total}}$
 - $V_{ud}^{n, \text{best}} = 0.97413(3)_f(13)_{\Delta_V^R}(35)_{\lambda}(20)_{\tau_n}[43]_{\text{total}}$
 - Realistic nuclear structure corrections larger than typically quoted
 - Realistic to expect neutron decay measurements can match precision of nuclear decays
 - one more measurement of τ_n and λ that match best precision make neutron decay extraction competitive
 - **PIONEER** Experiment will measure $\pi \rightarrow e \bar{\nu} / \pi \rightarrow \mu \bar{\nu}$ and $\pi_{\ell 3}$ allowing for independent V_{ud} and V_{us}/V_{ud} determinations

β -decay - Prospects for improving theoretical precision



- SM predictions also need to be controlled at the $O(0.2\%)$ level
 - Significant recent progress in understanding QED corrections beginning with
 - Built upon previous extensive work by Czarnecki, Marciano, Sirlin
 - Seng, Gorchtein, Patel, Ramsey-Musolf, PRL 121 (2018) [1807.10197]
 - Seng, Gorchtein, Ramsey-Mosolf, PRD 100 (2019) [1812.03352]
 - Dispersive methods used to provide more careful treatment of the $\square_{\gamma W}$ arising in β -decay
-
- Inspired new LQCD calculations to determine non-perturbative contributions to $\square_{\gamma W}$
 - Seng, Meissner PRL 122 (2019) [1903.07969]
 - Feng, Gorchtein, Jin, Ma, Seng PRL 124 (2020) [2003.09798]
 - ...
 - Yoo, Bhattacharya, Gupta, Mondal, Yoon, PRD 108 (2023) [2305.03198]
 - Ma, Feng, Gorchtein, Jin, Liu, Seng, Wang, Zhang PRL 132 (2024) [2308.16755]
 - Modern Effective Field Theory Treatments
 - Ando, Fearing Gudkov, Kubodera, Myhrer, Nakamura, Sato PLB 595 (2004) [nucl-th/0402100]
 - Cirigliano, deVries, Hayen, Mereghetti, Walker-Loud PRL 129 (2022) [2202.10439]
 - Cirigliano, Dekens, Mereghetti, Tomalak, PRD 108 (2023) [2306.03188]

NTNP (Nuclear Theory for New Physics)

NTNP

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science ▾

people

meetings ▾

Code of Conduct



U.S. DEPARTMENT OF
ENERGY

Office of
Science

<https://a51.lbl.gov/~ntnp/TC/>

Nuclear Theory for New Physics

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- [Commitment to Diversity](#)
- [Funding Acknowledgement](#)

Nuclear Theory for New Physics
co-chairs: *Vincenzo Cirigliano & Saori Pastore*

DEI Coordinator: *Maria Piarulli*

Lattice QCD

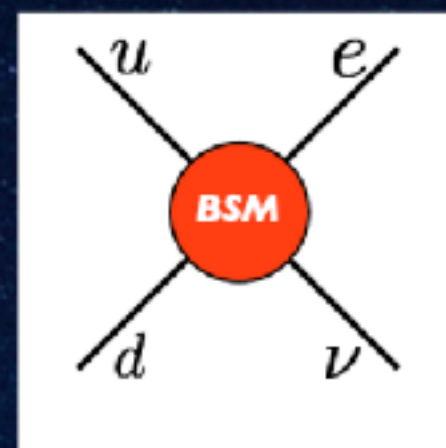
Coordinator:
Andre' Walker-Loud

**EFT /
phenomenology**

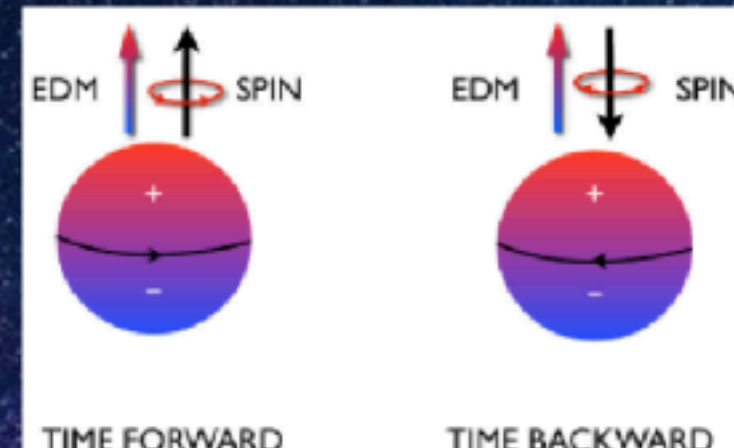
Coordinator:
Emanuele Mereghetti

Nuclear Structure

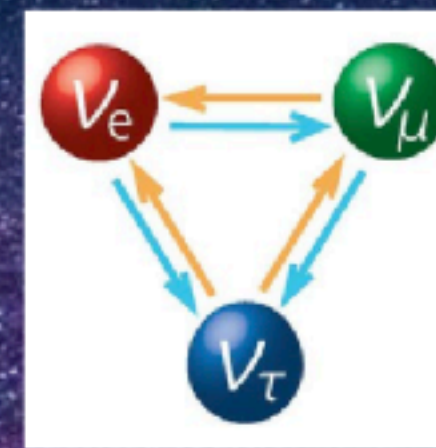
Coordinator:
Heiko Hergert



β decays and new particles



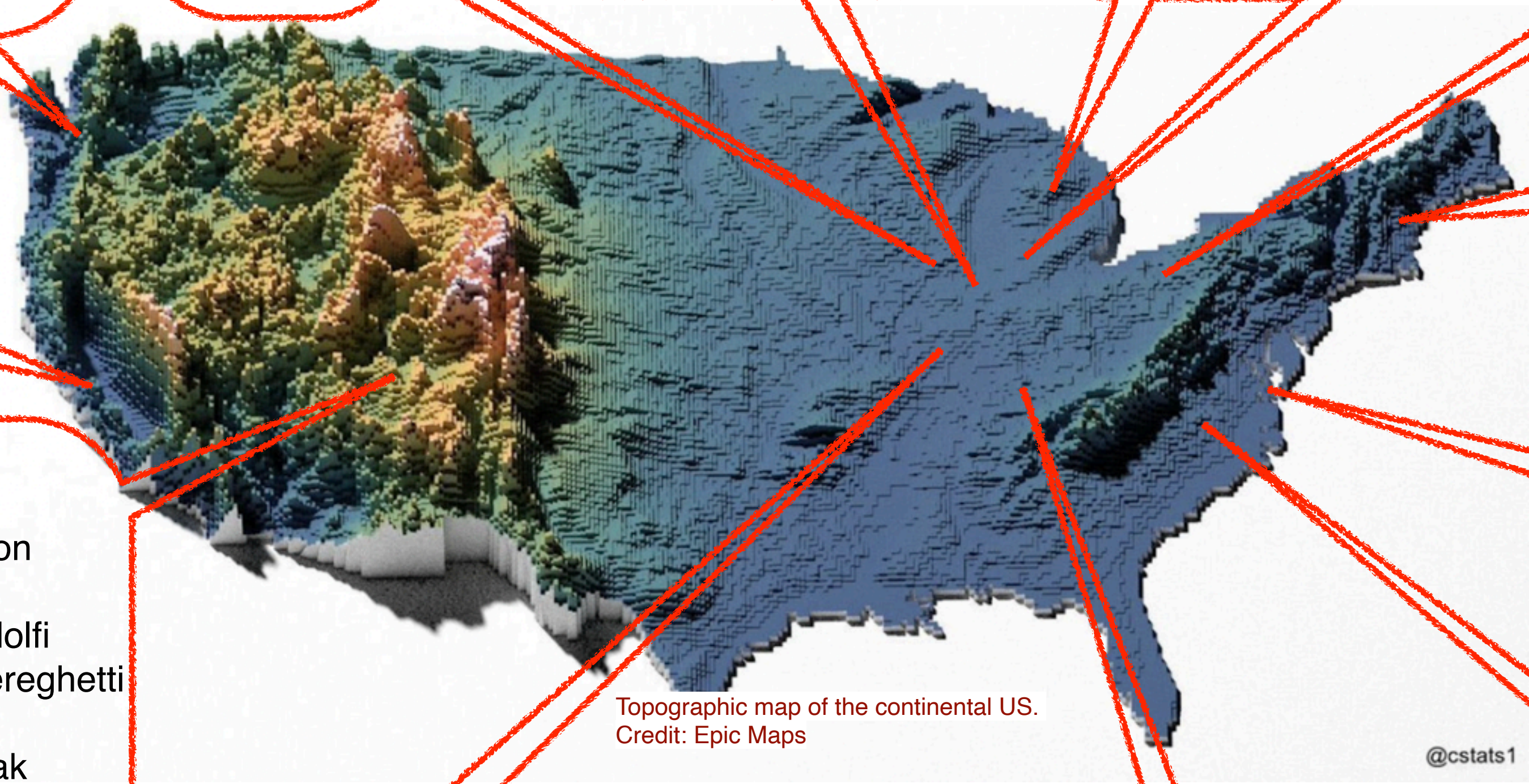
T & CP violation and the Origin of Matter



Neutrino properties & CP violation

- We are a new DOE Topical Collaboration
- We are **jointly funded** by the Offices of Nuclear and High Energy Physics
- A main goals of our collaboration:
 - improve the theoretical understanding of
 - neutron β -decay
 - nuclear β -decay
- Expertise in
 - Phenomenology
 - Lattice QCD
 - Effective Field Theory
 - Many-body nuclear methods
- We are happy to collaborate with others
 - **Get in touch!**

NTNP



Topographic map of the continental US.
Credit: Epic Maps

@cstats1



UW/INT
Vincenzo Cirigliano
Wouter Dekens
Chien-Yeah Seng
Ayala Glick-Magid
Maria Dawid



FNAL
Noemi Rocco



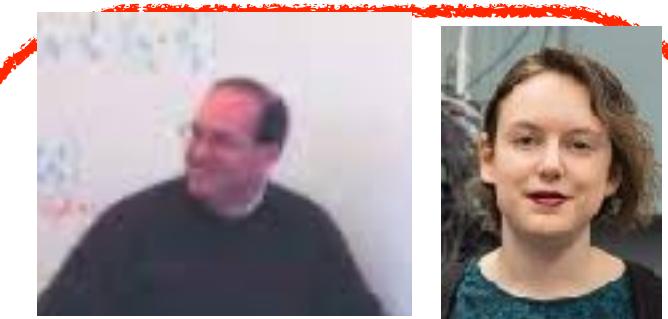
ANL
Alessandro Lovato
Anna McCoy
Robert Wiringa



MSU (& FRIB)
Scott Bogner
Heiko Hergert



Notre Dame
Ragnar Stroberg



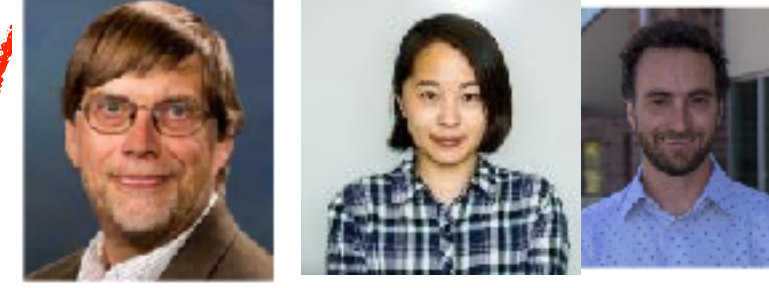
Carnegie Mellon University
Colin Morningstar
Sarah Skinner



UC Berkeley/LBNL
Wick Haxton
André Walker-Loud
Andrea Shindler
Lukáš Gráf
Zack Hall



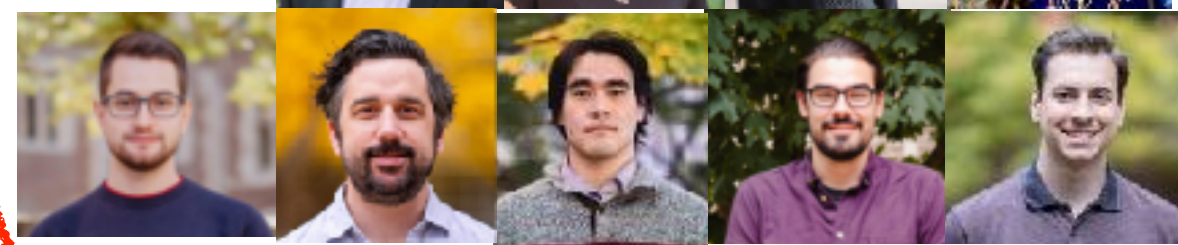
UMass Amherst
Michael Ramsey-Musolf
Leon Friedrich



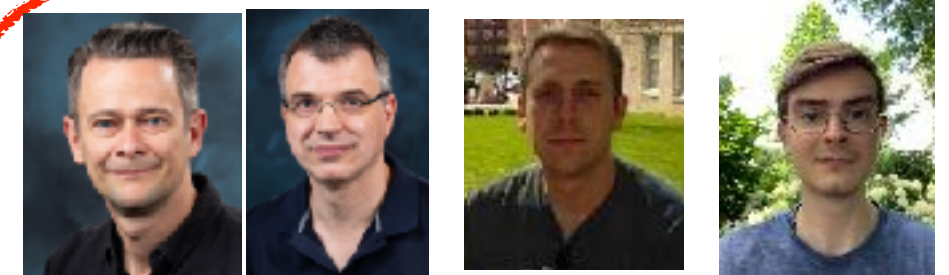
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Joseph Carlson
Kaori Fuyuto
Stefano Gandolfi
Emanuele Mereghetti
Ingo Tews
Sasha Tomalak
Jacky Kumar



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Alex Gnech
Rocco Schiavilla



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Sam Novario
Jason Bub
Garrett King



ORNL / University of Tennessee
Gaute Hagen
Thomas Papenbrock
Lucas Platter
Evan Combes



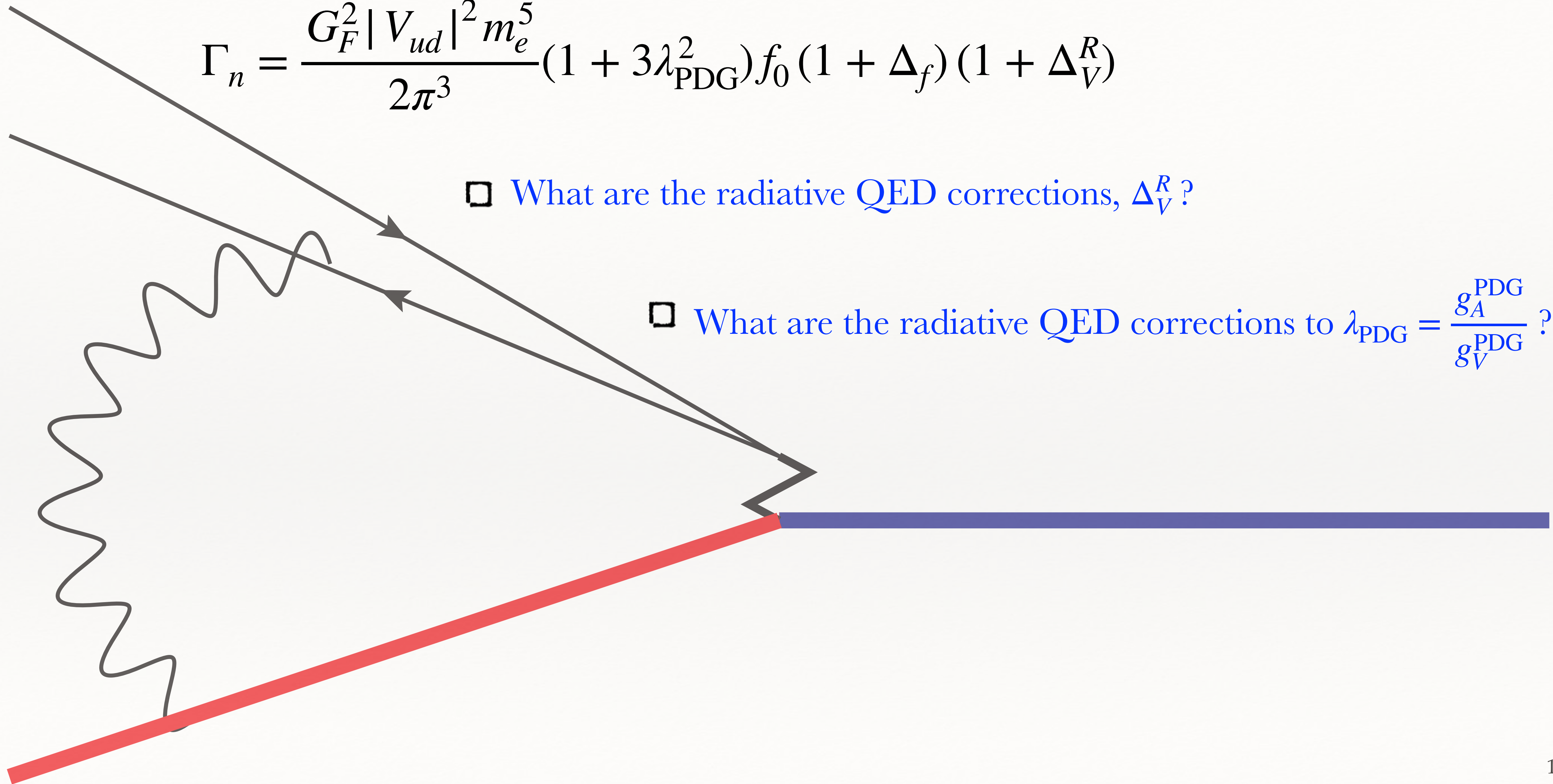
UNC Chapel Hill
Jon Engel
Amy Nicholson
Zack Hall
Joeseeph Moscose

β -decay - Two theoretical opportunities for $n \rightarrow pe\bar{\nu}$

$$\Gamma_n = \frac{G_F^2 |V_{ud}|^2 m_e^5}{2\pi^3} (1 + 3\lambda_{\text{PDG}}^2) f_0 (1 + \Delta_f) (1 + \Delta_V^R)$$

□ What are the radiative QED corrections, Δ_V^R ?

□ What are the radiative QED corrections to $\lambda_{\text{PDG}} = \frac{g_A^{\text{PDG}}}{g_V^{\text{PDG}}}$?



β -decay - QED corrections, Δ_V^R

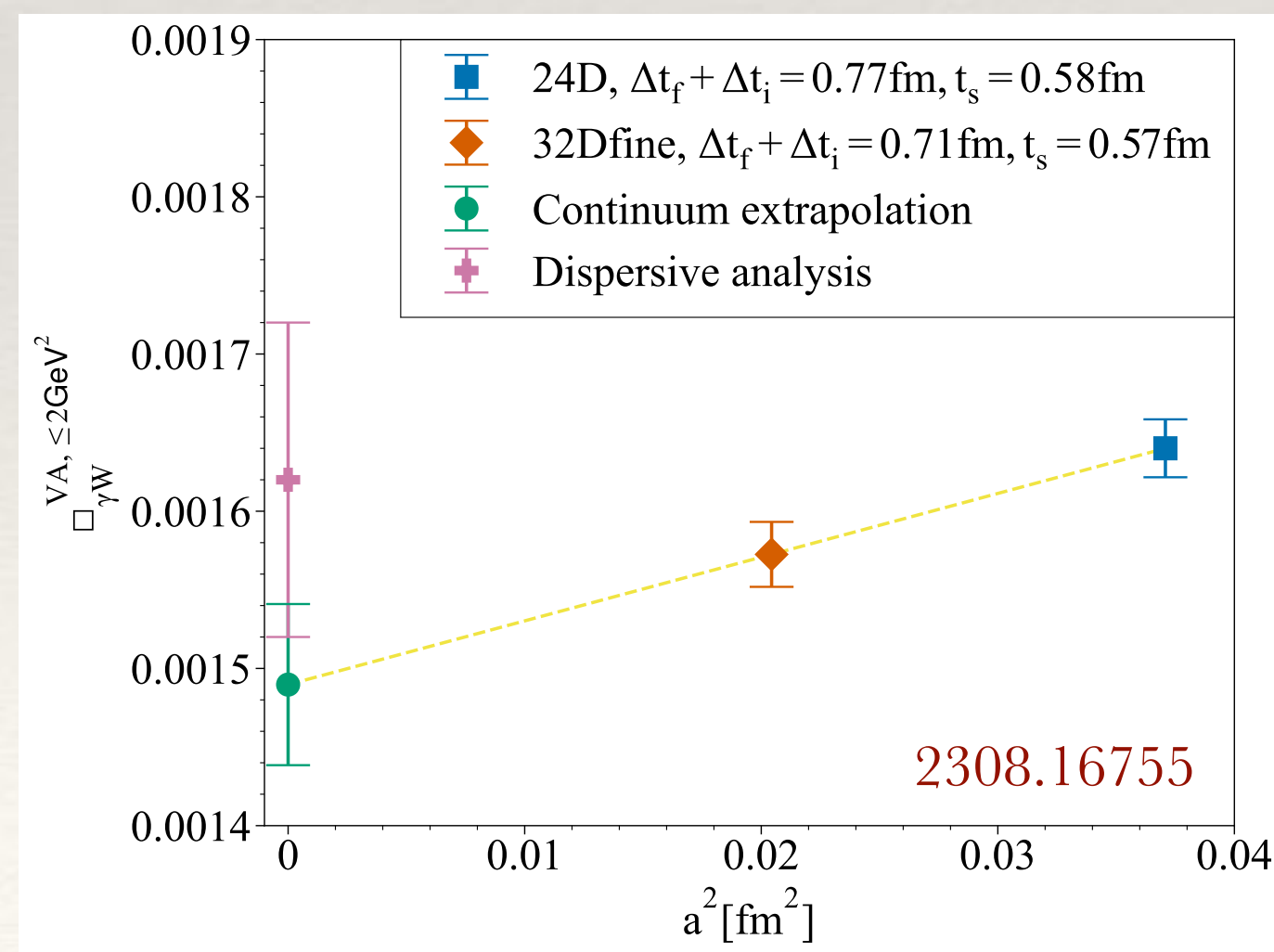
$$\Gamma_n = \frac{G_F^2 |V_{ud}|^2 m_e^5}{2\pi^3} (1 + 3\lambda_{\text{PDG}}^2) f_0 (1 + \Delta_f) (1 + \Delta_V^R)$$

$$\Delta_V^R = \frac{\alpha}{2\pi} \left[3 \ln \frac{M_Z}{m_p} + \ln \frac{M_Z}{M_W} + \tilde{a}_g \right] + \delta_{\text{HO}}^{\text{QED}} + 2 \square_{\gamma W}^{\text{VA}}$$

$$\square_{\gamma W}^{\text{VA}} = \frac{ie^2}{2M_N^2} \int \frac{d^4q}{(2\pi)^4} \frac{m_W^2}{m_W^2 - q^2} \frac{\epsilon^{\mu\nu\alpha\lambda} q_\alpha p_\lambda}{(q^2)^2} T_{\mu\nu}^{\gamma W}$$

$$T_{\mu\nu}^{\gamma W} = \int d^4x e^{iq \cdot x} \langle p(p, S) | T \{ J_\mu^{em}(x) J_\nu^W(0) \} | n(p, S) \rangle$$

Xu Feng
Mon. 17:00



- π Feng, Gorchtein, Jin, Ma, Seng PRL 124 (2020) [2003.09798]
- K Seng, Feng, Gorchhtein, Jin, Meissner JHEP 10 (2020) [2009.00459]
- K Ma, Feng, Gorchtein, Jin, Seng PRD 103 (2021) [2102.12048]
- πK Yoo, Bhattacharya, Gupta, Mondal, Yoon PRD 108 (2023) [2305.03198]
- n Ma, Feng, Gorchtein, Jin, Liu, Seng, Wang, Zhang PRL 132 (2024) [2308.16755]

Challenging calculations — particularly for the neutron
these are **State-of-the-art LQCD** results

- requires an integral over two-current insertions between ground-state neutron and proton
- many systematics need to be controlled
 - excited state contamination
 - separation between perturbative/non-perturbative Q^2 contributions
 - continuum limit
 - infinite volume limit
 - 2308.16755 was performed @ m_π^{phys} !

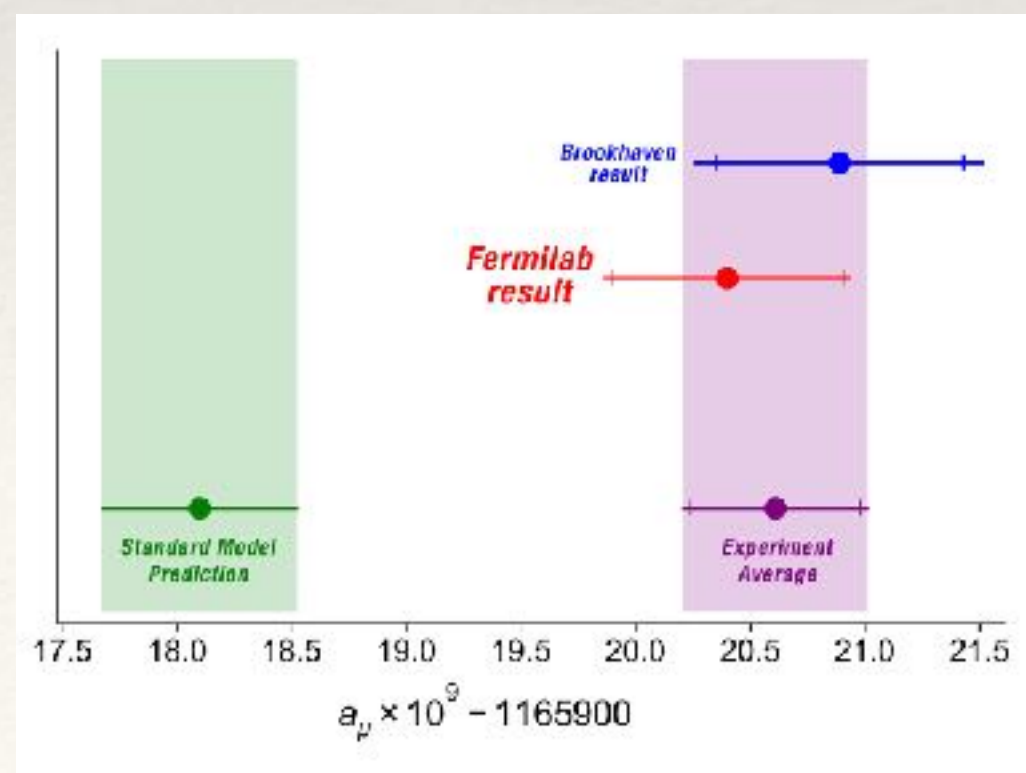
I suspect the full systematic uncertainty is larger than currently quoted
[don't let me take anything away from this very impressive work]

It will be great to see more LQCD results to compare with

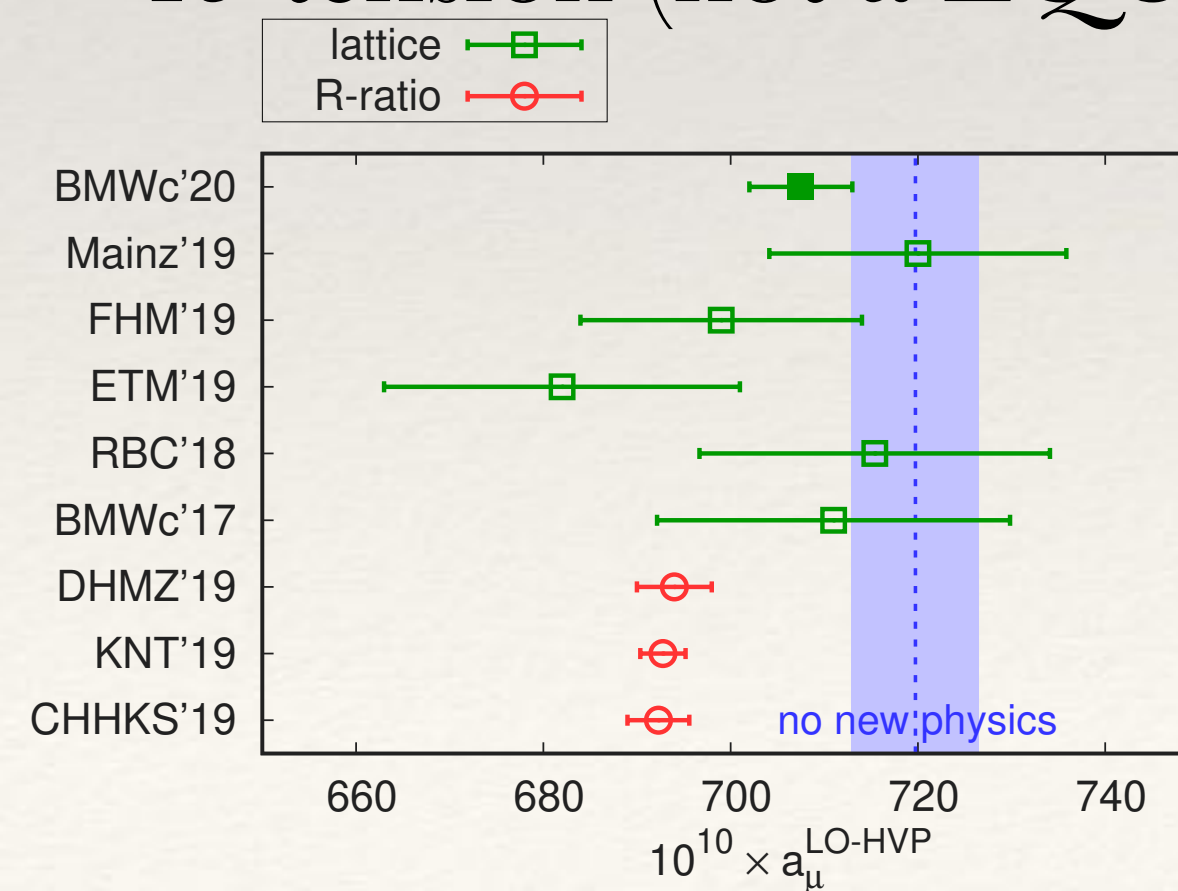
β -decay - QED corrections, Δ_V^R

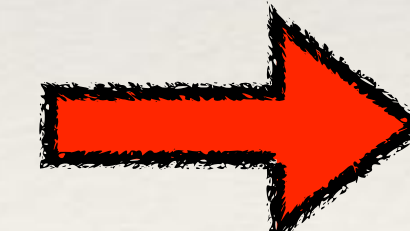
$$\Gamma_n = \frac{G_F^2 |V_{ud}|^2 m_e^5}{2\pi^3} (1 + 3\lambda_{\text{PDG}}^2) f_0 (1 + \Delta_f) (1 + \Delta_V^R)$$

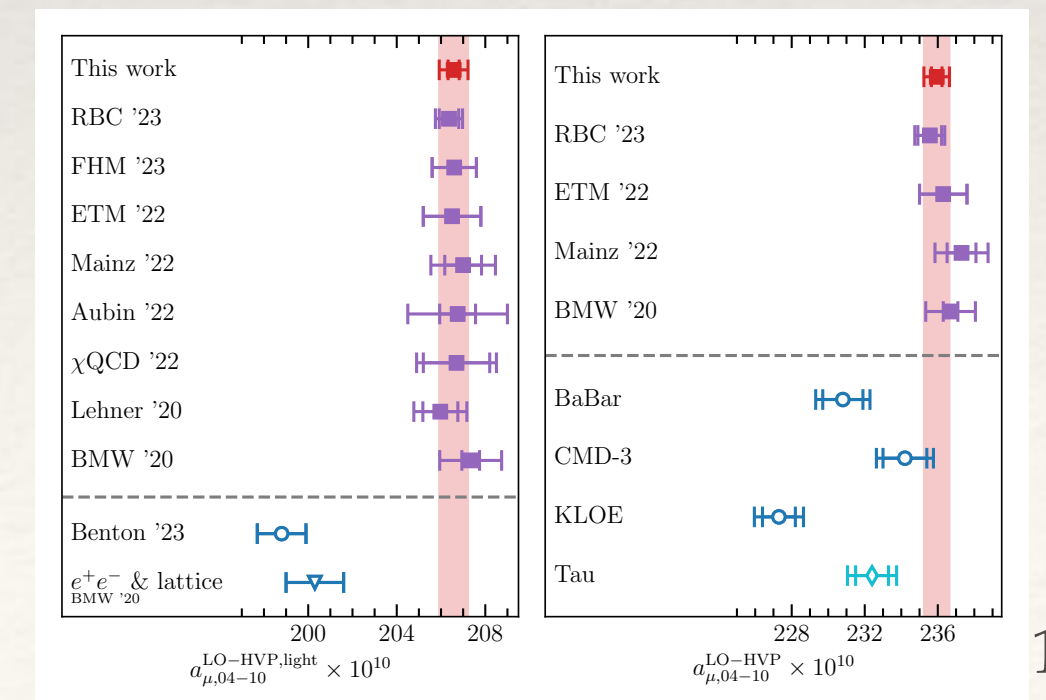
- It is worth considering a full LQCD+QED calculation of $n \rightarrow pe\bar{\nu}$
- This would be a challenging calculation
 - but possible on the time scale of new neutron τ_n and $\lambda = g_A/g_V$ measurements
- If first-row CKM approaches 5-sigma tension, we should have 2 or more methods
 - Look to muon $g - 2$ as an example —
 - dispersion theory to determine hadronic vacuum polarization (HVP): $\approx 4\sigma$ tension
 - LQCD determination of HVP: $\approx 1\sigma$ tension (not a LQCD consensus yet, but moving this way)




 precise LQCD
2020




 LQCD consensus
on pieces of calc
2024

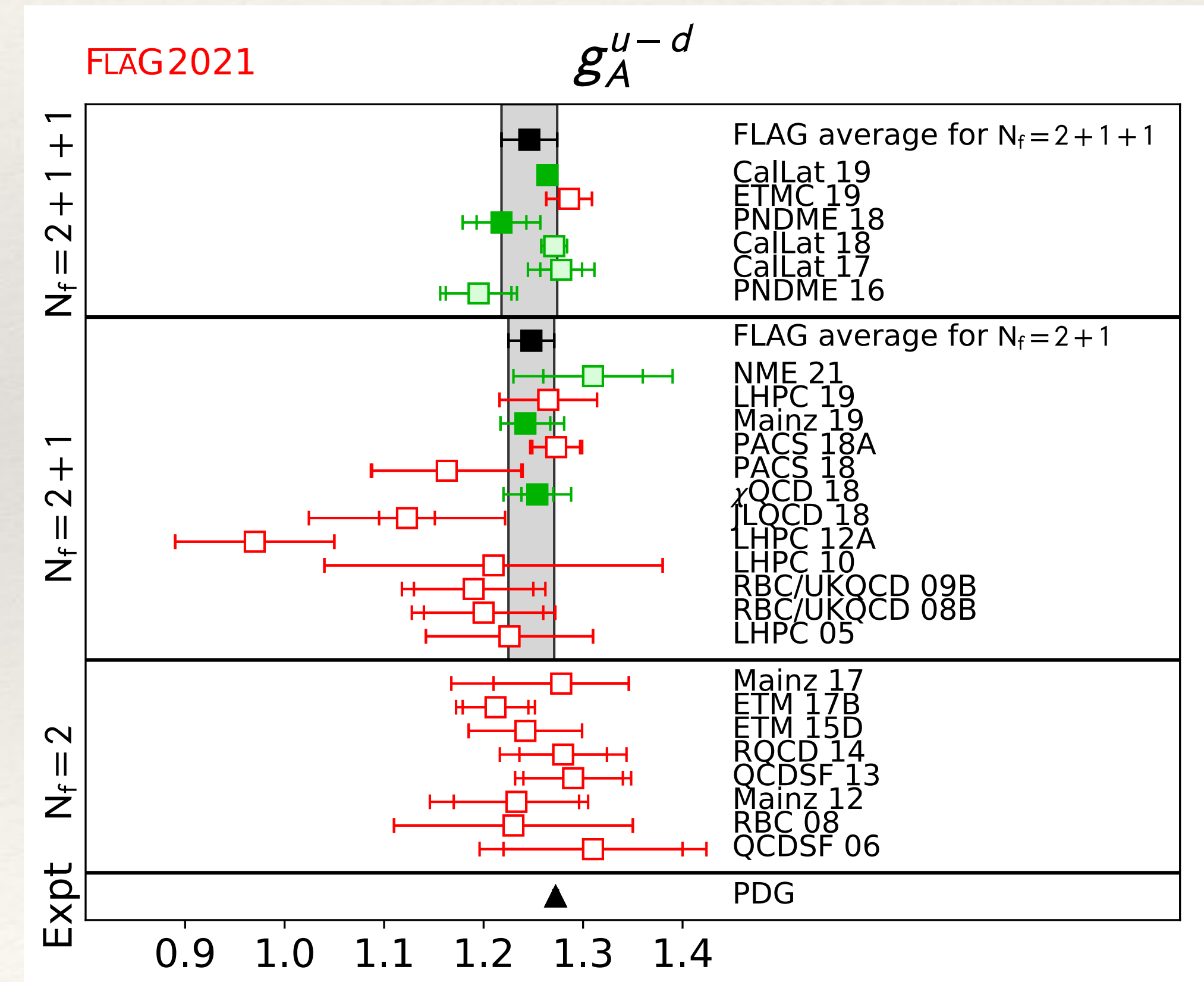


β -decay - QED corrections to $\lambda_{\text{PDG}} = g_A^{\text{PDG}} / g_V^{\text{PDG}}$

$$\Gamma_n = \frac{G_F^2 |V_{ud}|^2 m_e^5}{2\pi^3} (1 + 3\lambda_{\text{PDG}}^2) f_0 (1 + \Delta_f) (1 + \Delta_V^R)$$

$$\lambda_{\text{PDG}} \approx \lambda^{\text{"exp"}} - \Delta_A^{R, \text{Sirlin, analytic}} = \lambda_{\text{QCD-iso}} + \Delta_A^{R, \text{other}}$$

- λ_{PDG} is determined with *some* QED corrections subtracted
- Additional QED corrections to g_A^{PDG} ($\Delta_A^{R, \text{other}}$) do not impact V_{ud} extraction — the $(1 + \Delta_A^R)$ cancels in Γ_n and λ_{PDG}
- Comparing LQCD calculations of $g_A^{\text{QCD-iso}}$ to g_A^{PDG} can constrain BSM right-handed currents
- Previously, we thought $\Delta_A^{R, \text{other}} \approx \text{O}(0.2\%)$
- Potentially significant low-energy nucleon structure corrections may spoil this comparison, $\Delta_A^{R, \text{other}} \simeq \text{O}(2\%)$
 Cirigliano, de Vries, Hayen, Mereghetti, Walker-Loud
 PRL 129 (2022) [2202.10439]



β -decay - QED corrections to $\lambda_{\text{PDG}} = g_A^{\text{PDG}} / g_V^{\text{PDG}}$

While QED corrections to λ_{PDG} do not directly impact V_{ud}

Global analysis of first-row CKM constraints

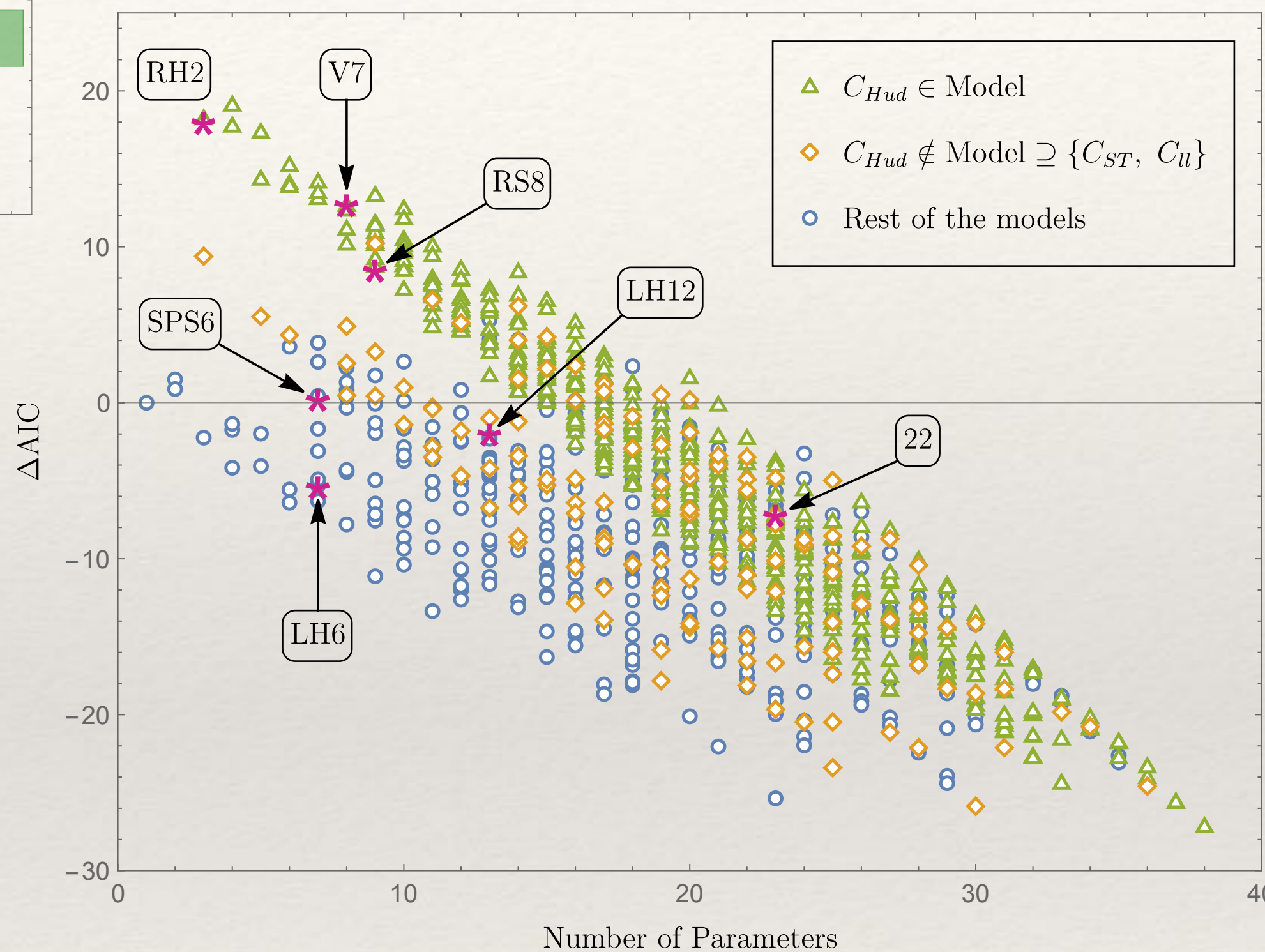
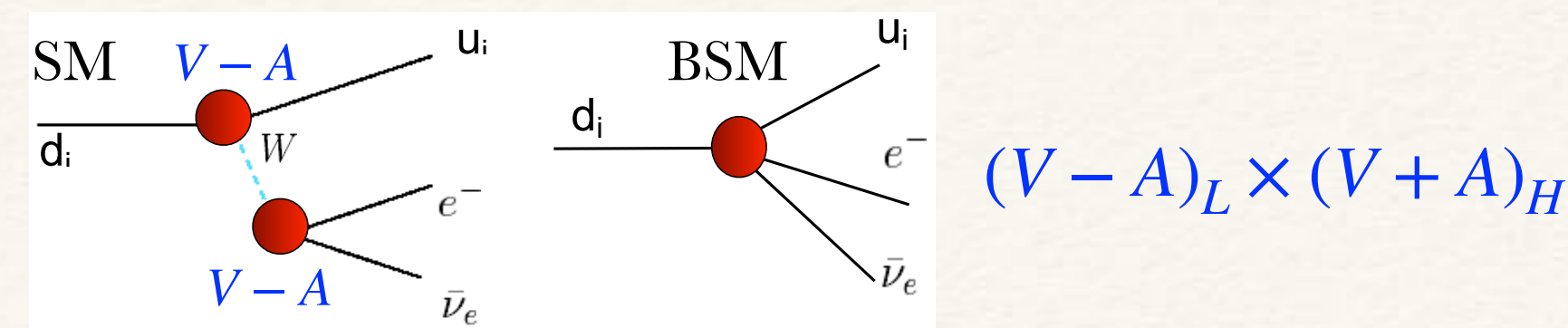
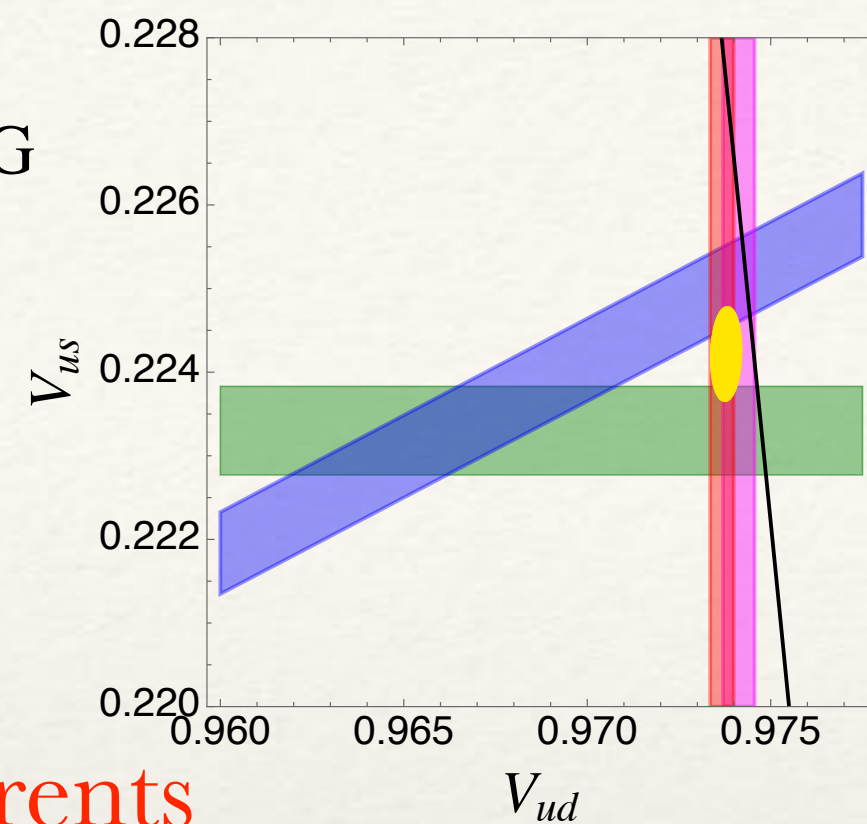
including collider constraints,

favours BSM Right-handed currents

Cirigliano, Dekens, de Vries, Mereghetti, Tong, JHEP 03 (2024) [2311.00021]

see also:

Belfatto, Trifinopoulos, PRD 108 (2023) [2302.14097]



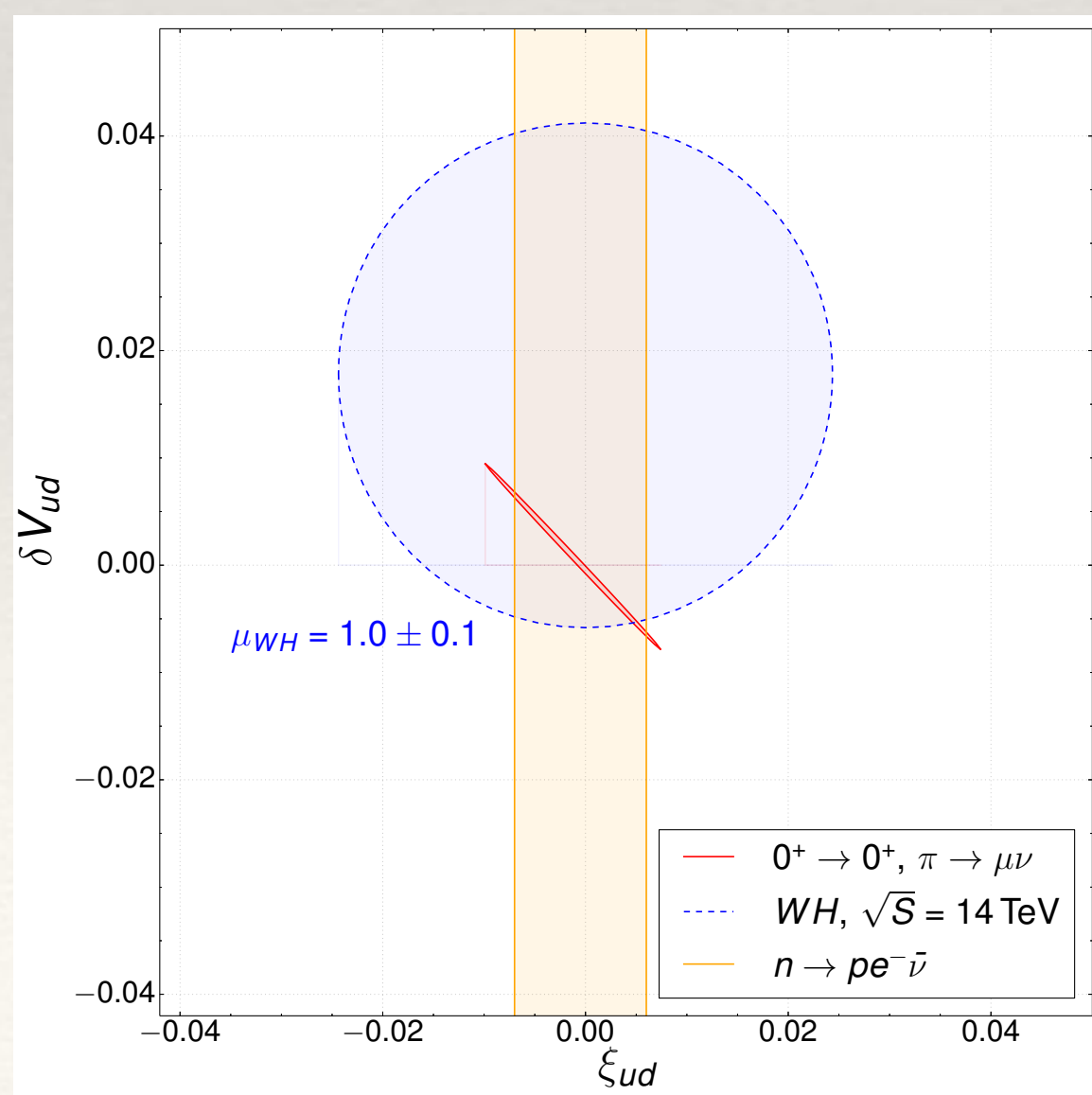
More favored (by AIC)



Standard Model



Less favored (by AIC)



If we can quantitatively understand QED corrections to λ_{PDG} Particularly in a correlated way with isospin symmetric LQCD results

We can turn this into the most precise constraint on BSM Right-Handed currents

Pion-induced radiative corrections to neutron beta-decay

Cirigliano, de Vries, Hayen, Mereghetti & Walker-Loud, PRL 129 (2022) [2202.10439]

□ Systematic, EFT treatment of neutron β -decay

$$\frac{d\Gamma}{dE_e d\Omega_e d\Omega_\nu} = \frac{(G_F V_{ud})^2}{(2\pi)^5} (1 + 3\lambda^2) w(E_e) \times \left[1 + \bar{a}(\lambda) \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + \bar{A}(\lambda) \frac{\vec{\sigma}_n \cdot \vec{p}_e}{E_e} + \dots \right]$$

The parameters can be measured

If we want to connect them to Standard Model (SM) parameters we need to start from a Lagrangian with parameters related to SM parameters

pion-less low-energy EFT

$$\lambda = \frac{g_A}{g_V}$$

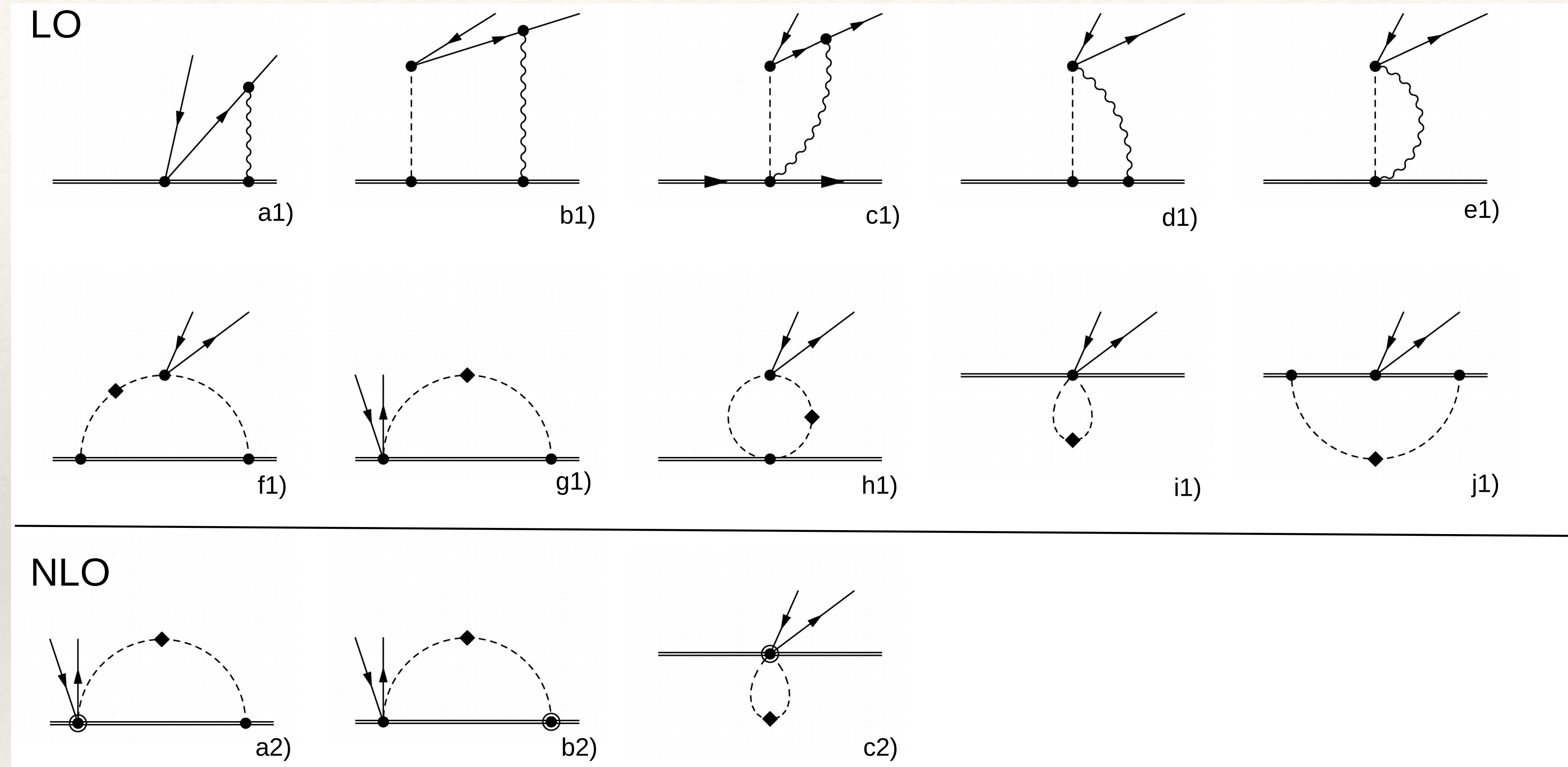
$$\begin{aligned} \mathcal{L}_{\not{\pi}} = & -\sqrt{2}G_F V_{ud} \left[\bar{e} \gamma_\mu P_L \nu_e \left(\bar{N} (g_V v_\mu - 2g_A S_\mu) \tau^+ N \right. \right. \\ & + \frac{i}{2m_N} \bar{N} (v^\mu v^\nu - g^{\mu\nu} - 2g_A v^\mu S^\nu) (\overleftarrow{\partial} - \overrightarrow{\partial})_\nu \tau^+ N \left. \right) \\ & + \frac{ic_T m_e}{m_N} \bar{N} (S^\mu v^\nu - S^\nu v^\mu) \tau^+ N (\bar{e} \sigma_{\mu\nu} P_L \nu) \\ & \left. + \frac{i\mu_{\text{weak}}}{m_N} \bar{N} [S^\mu, S^\nu] \tau^+ N \partial_\nu (\bar{e} \gamma_\mu P_L \nu) \right] + \dots \quad (2) \end{aligned}$$

Perform the calculation with SU(2) heavy-baryon χ PT and match the results to this pion-less EFT whose parameters can be matched to experimentally measured quantities

Pion-induced radiative corrections to neutron beta-decay

Cirigliano, de Vries, Hayen, Mereghetti & Walker-Loud, PRL 129 (2022) [2202.10439]

□ Sub-set of $O(50)$ diagrams



Pion-induced radiative corrections to neutron beta-decay

Cirigliano, de Vries, Hayen, Mereghetti & Walker-Loud, PRL 129 (2022) [2202.10439]

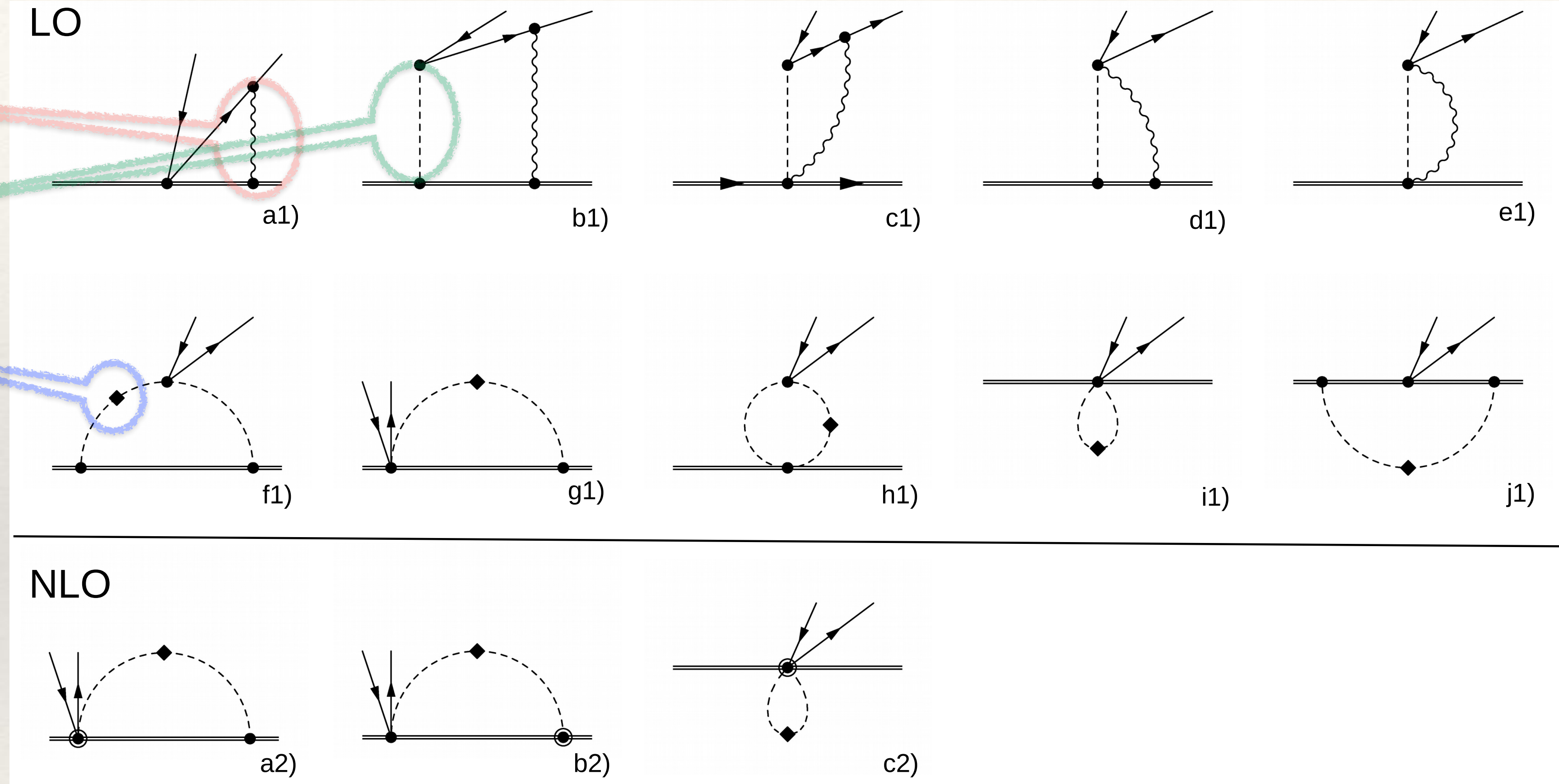
□ Sub-set of O(50) diagrams

photons

pions

pion electromagnetic mass splitting

$$m_{\pi^{\pm}}^2 - m_{\pi^0}^2 = 2e^2 F_{\pi}^2 Z_{\pi}$$



Pion-induced radiative corrections to neutron beta-decay

Cirigliano, de Vries, Hayen, Mereghetti & Walker-Loud, PRL 129 (2022) [2202.10439]

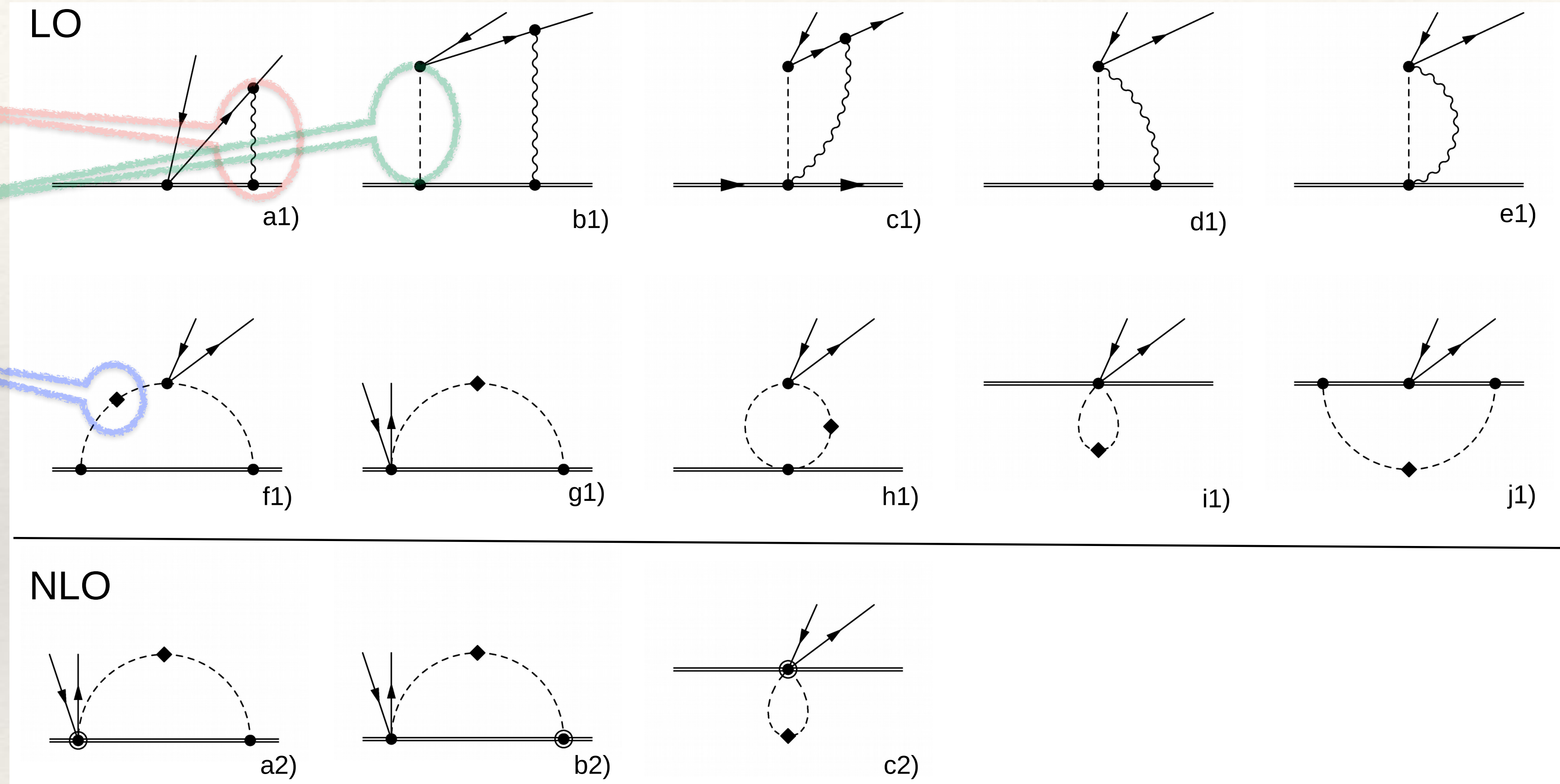
□ Sub-set of $O(50)$ diagrams

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$$m_{\pi^\pm}^2 - m_{\pi^0}^2 = 2e^2 F_\pi^2 Z_\pi$$



NOTE: at this order, we also include QED, $m_d - m_u$ corrections to $M_n - M_p$

- iso-vector contributions to $M_n - M_p$ vanish from symmetry constraints for τ^+ current
- iso-scalar contributions do not vanish - but the sum of all of them does vanish through NLO

Pion-induced radiative corrections to neutron beta-decay

Cirigliano, de Vries, Hayen, Mereghetti & Walker-Loud, PRL 129 (2022) [2202.10439]

□ **Matching** $\lambda_{\text{PDG}} = g_A^{\text{QCD}} \left(1 + \delta_{\text{RC}}^{(\lambda)} - 2\text{Re}(\epsilon_R) \right) \quad \delta_{\text{RC}}^{(\lambda)} = \frac{\alpha}{2\pi} \left(\Delta_{A,em}^{(0)} + \Delta_{A,em}^{(1)} - \Delta_{V,em}^{(0)} \right)$

$$\Delta_{A,em}^{(0)} = Z_\pi \left[\frac{1 + 3g_A^{(0)2}}{2} \left(\ln \frac{\mu^2}{m_\pi^2} - 1 \right) - g_A^{(0)2} \right] + \hat{C}_A(\mu) \quad g_{V/A} = g_{V/A}^{(0)} \left[1 + \sum_{n=2}^{\infty} \Delta_{V/A,\chi}^{(n)} + \frac{\alpha}{2\pi} \sum_{n=0}^{\infty} \Delta_{V/A,em}^{(n)} + \left(\frac{m_u - m_d}{\Lambda_\chi} \right)^{n_{V/A}} \sum_{n=0}^{\infty} \Delta_{V/A,\delta m}^{(n)} \right]$$

$$\Delta_{Z,em}^{(0)} = \hat{C}_V(\mu)$$

$$\Delta_{A,em}^{(1)} = Z_\pi 4\pi m_\pi \left[c_4 - c_3 + \frac{3}{8m_N} + \frac{9}{16m_N} g_A^{(0)2} \right]$$

$$\Delta_{\chi,em,\delta m} \sim \mathcal{O}(\epsilon_\chi^n)$$

$$\epsilon_\chi = \frac{m_\pi}{4\pi F_\pi}$$

CVC $n_V = 2 \quad n_A = 1$

explicit calculation:

$$\Delta_{A,\delta m}^{(0),(1)} = 0$$

$$\Delta_{V,\delta m}^{(0)} = 0$$

Low-Energy-Constants (LECs)

$\hat{C}_{A,V}(\mu)$ - completely unknown

$c_{3,4}$ are estimated from literature (large)

Using Naive Dimensional Analysis (NDA) to estimate $C_A(\mu)$ and $c_{3,4}$ from the literature

$$\delta_{\text{RC}}^{(\lambda)} \in \{1.4, 2.6\} \cdot 10^{-2}$$

an order of magnitude larger than previous estimates

Pion-induced radiative corrections to neutron beta-decay

Cirigliano, de Vries, Hayen, Mereghetti & Walker-Loud, PRL 129 (2022) [2202.10439]

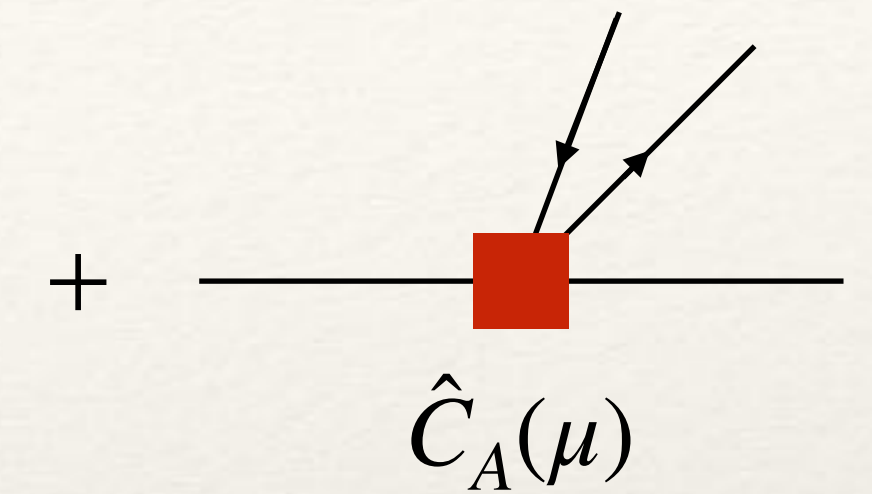
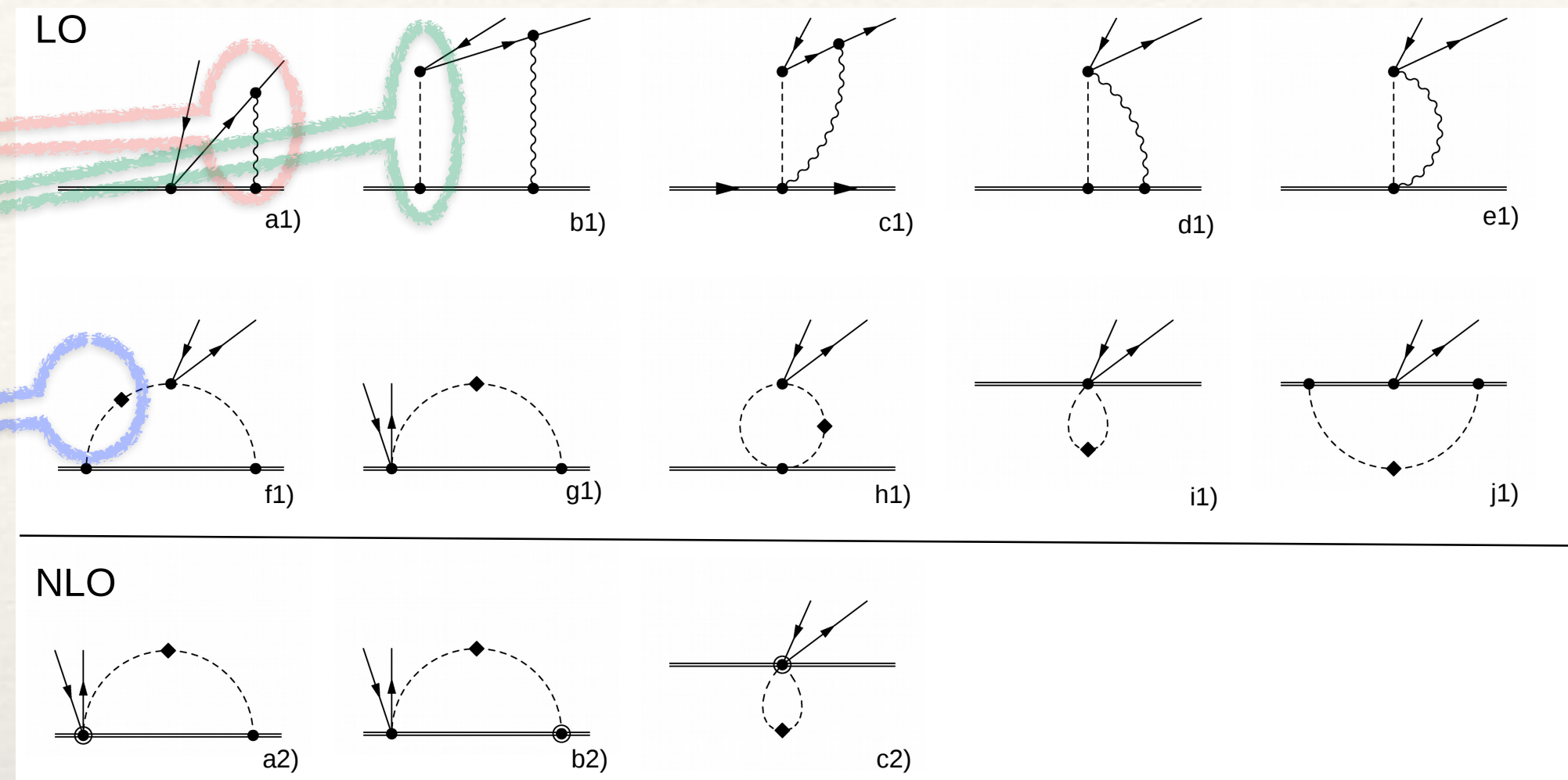
□ Sub-set of O(50) diagrams

photons

pions

pion electromagnetic mass splitting

$$m_{\pi^\pm}^2 - m_{\pi^0}^2 = 2e^2 F_\pi^2 Z_\pi$$



Low-Energy-Constants (LECs)

$$g_A^{\text{PDG}} = g_A^{\text{QCD-iso}} + \delta_{\text{RC}}^{(\lambda)}(\alpha_{fs}, \hat{C}_A(\mu), \dots)$$

$$\delta_{\text{RC}}^{(\lambda)} \in \{1.4, 2.6\} \cdot 10^{-2}$$

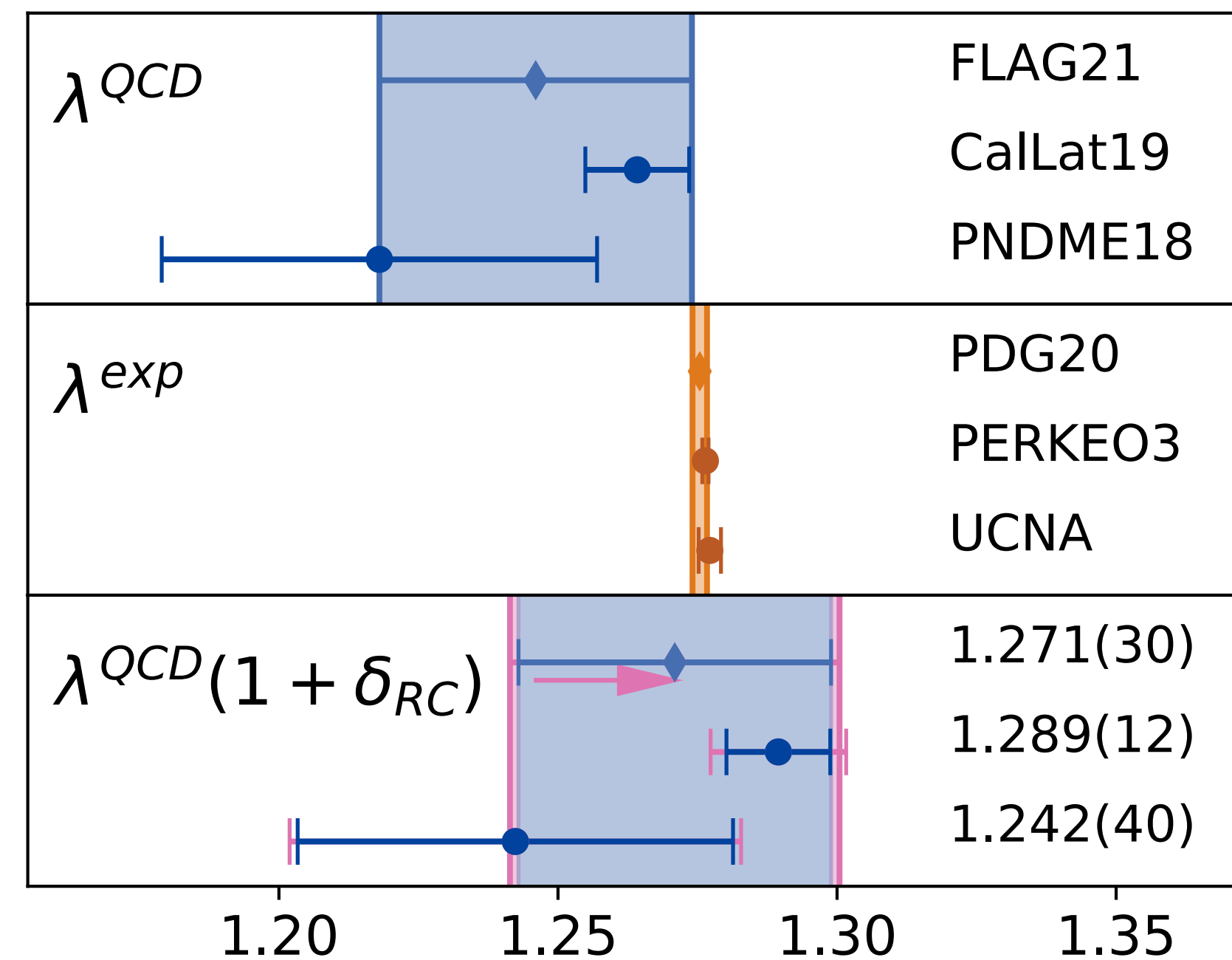
□ seems to move g_A^{QCD} towards g_A^{exp}

□ need LQCD+QED calculation to determine $\delta_{\text{RC}}^{(\lambda)}$

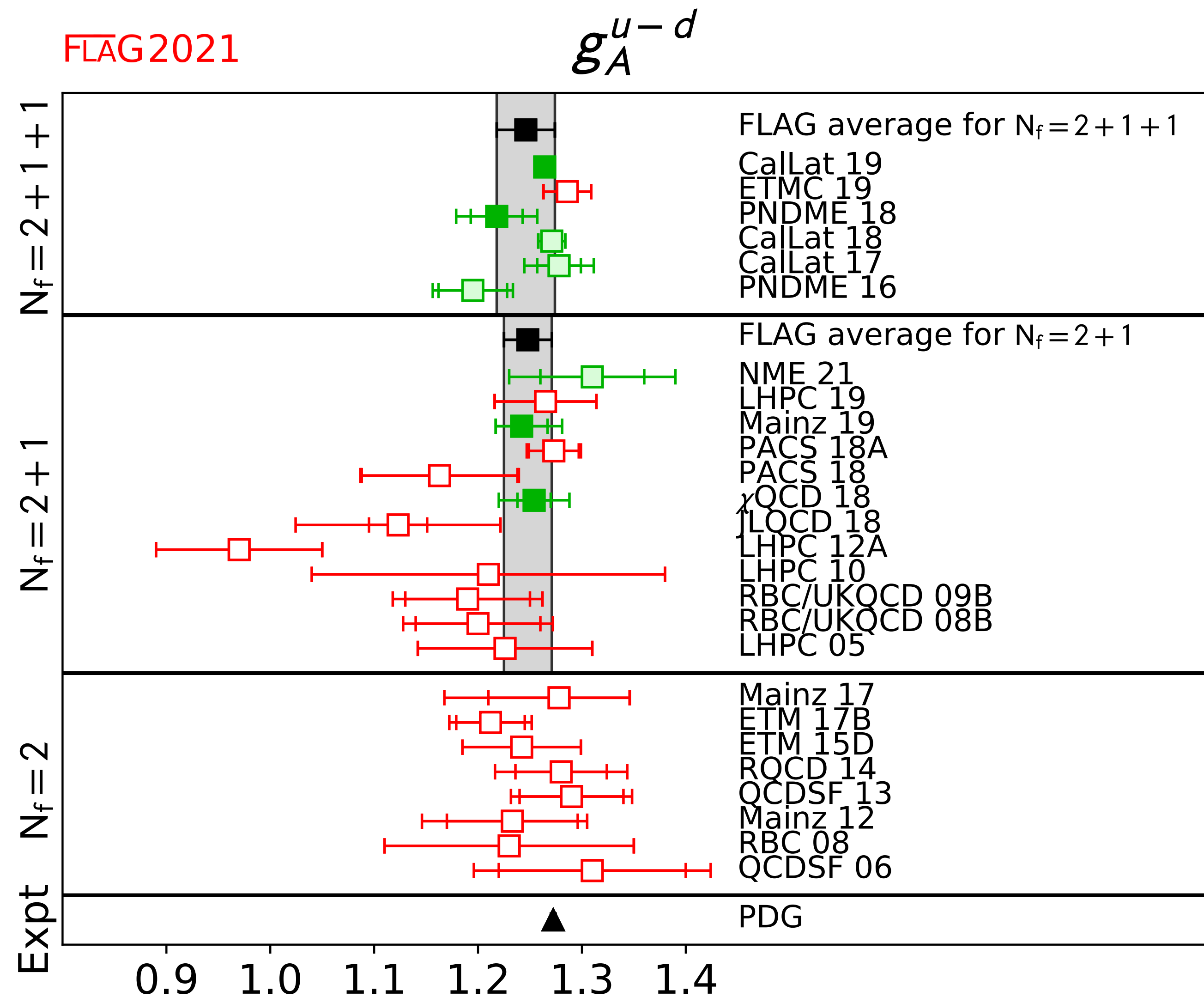
□ requires careful understanding of

□ renormalization

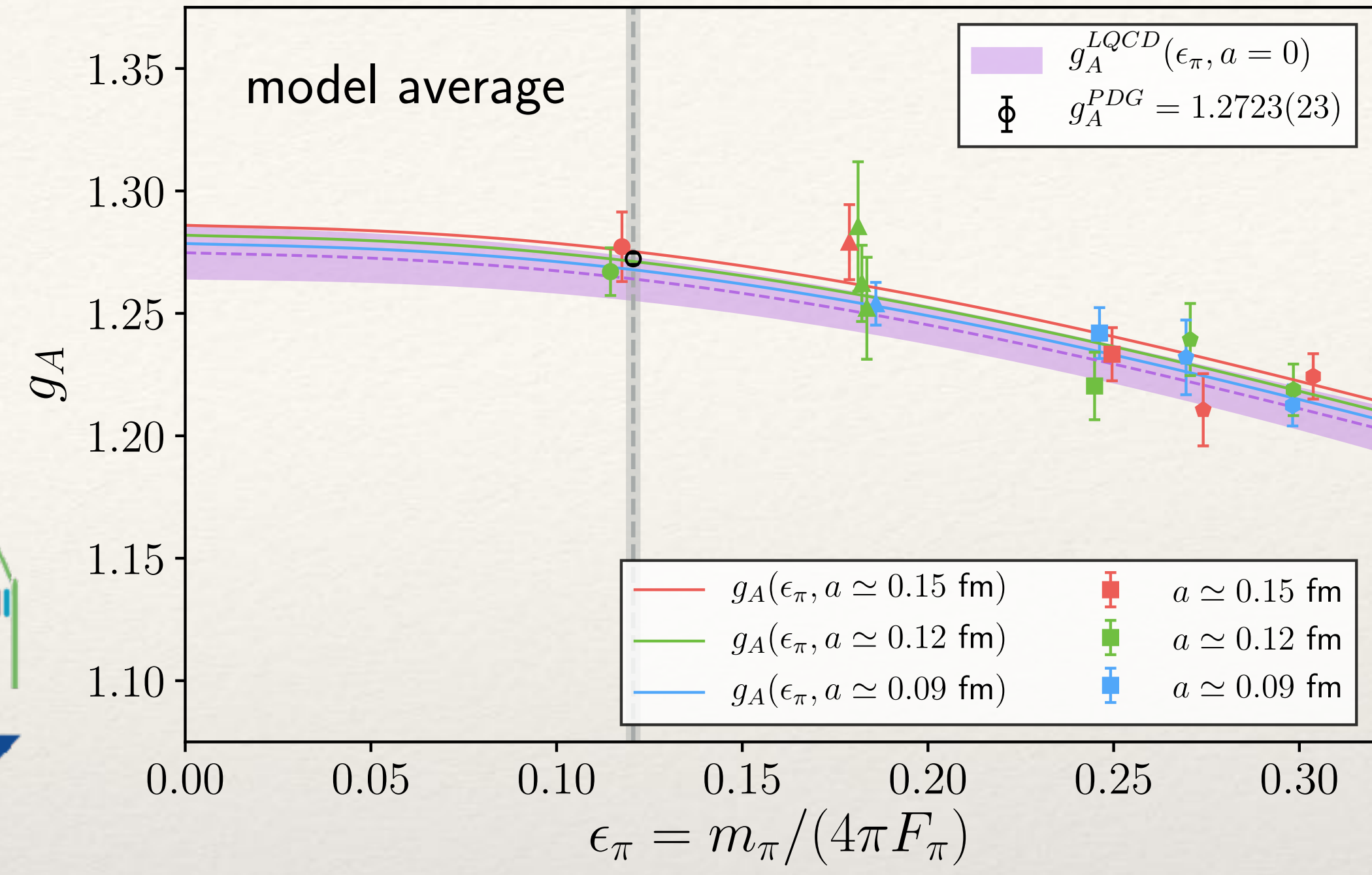
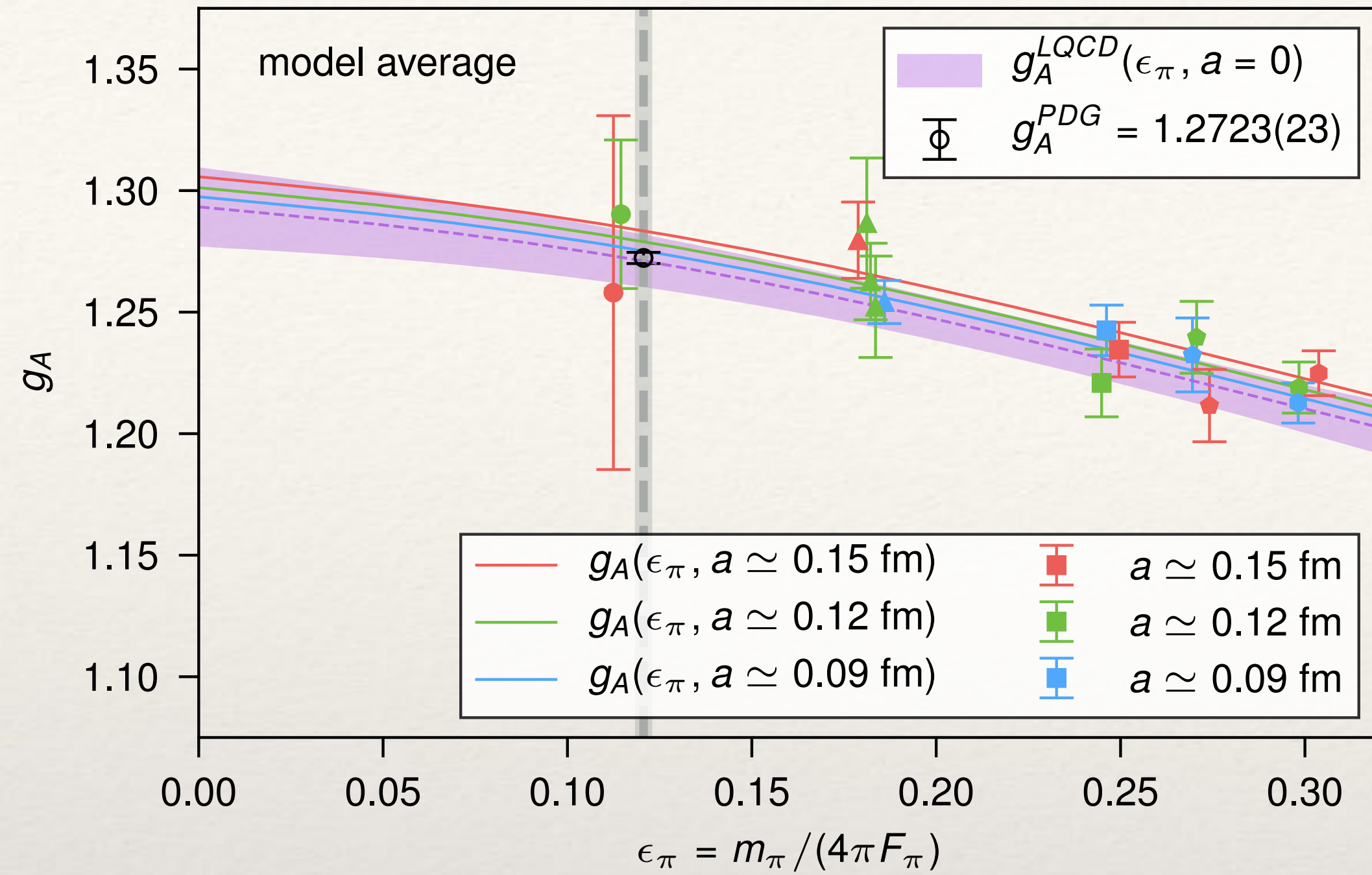
□ QED gauge/scheme choice to handle IR/UV



Status of LQCD results for $g_A^{\text{QCD-isosymmetric}}$

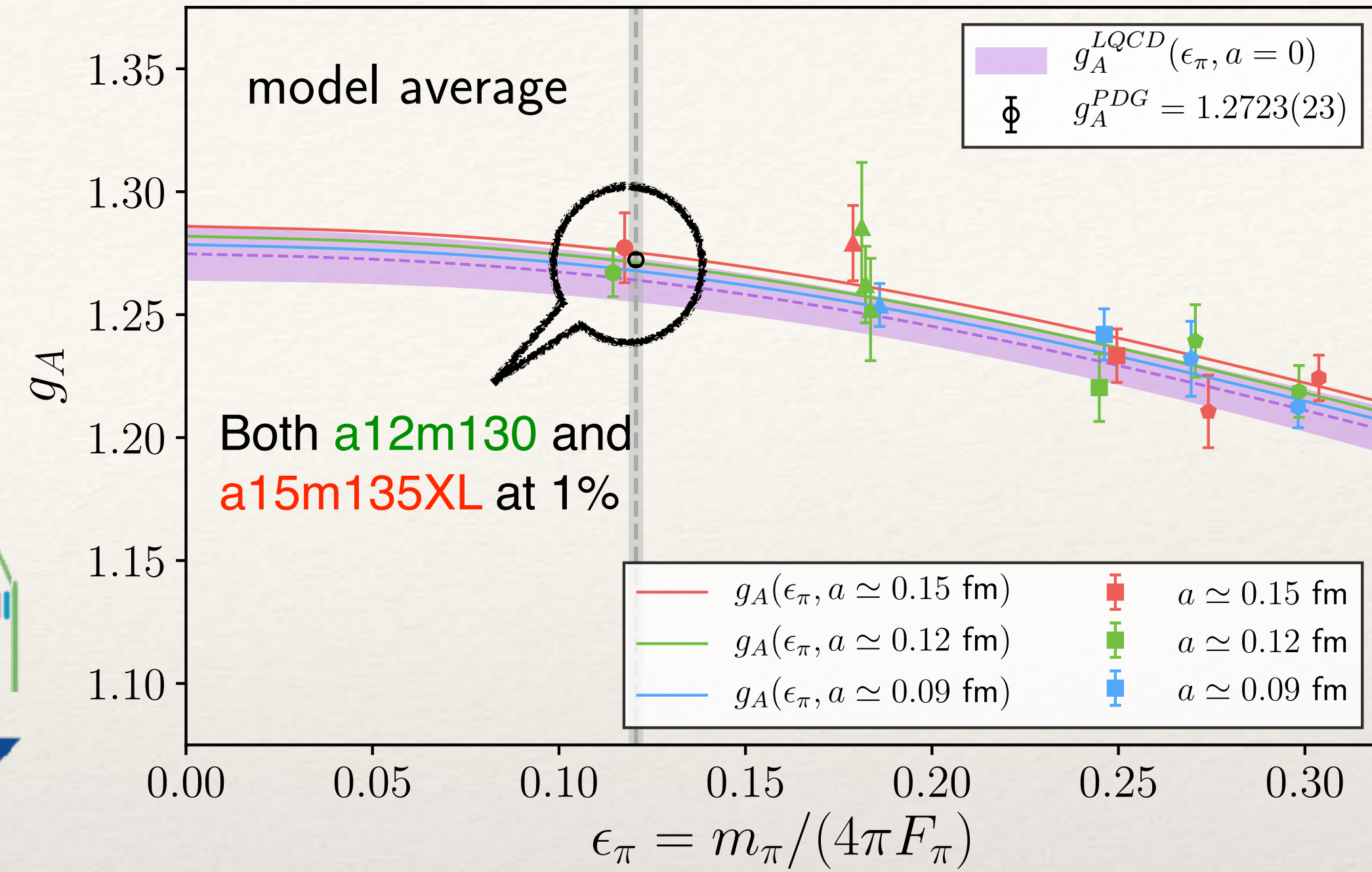
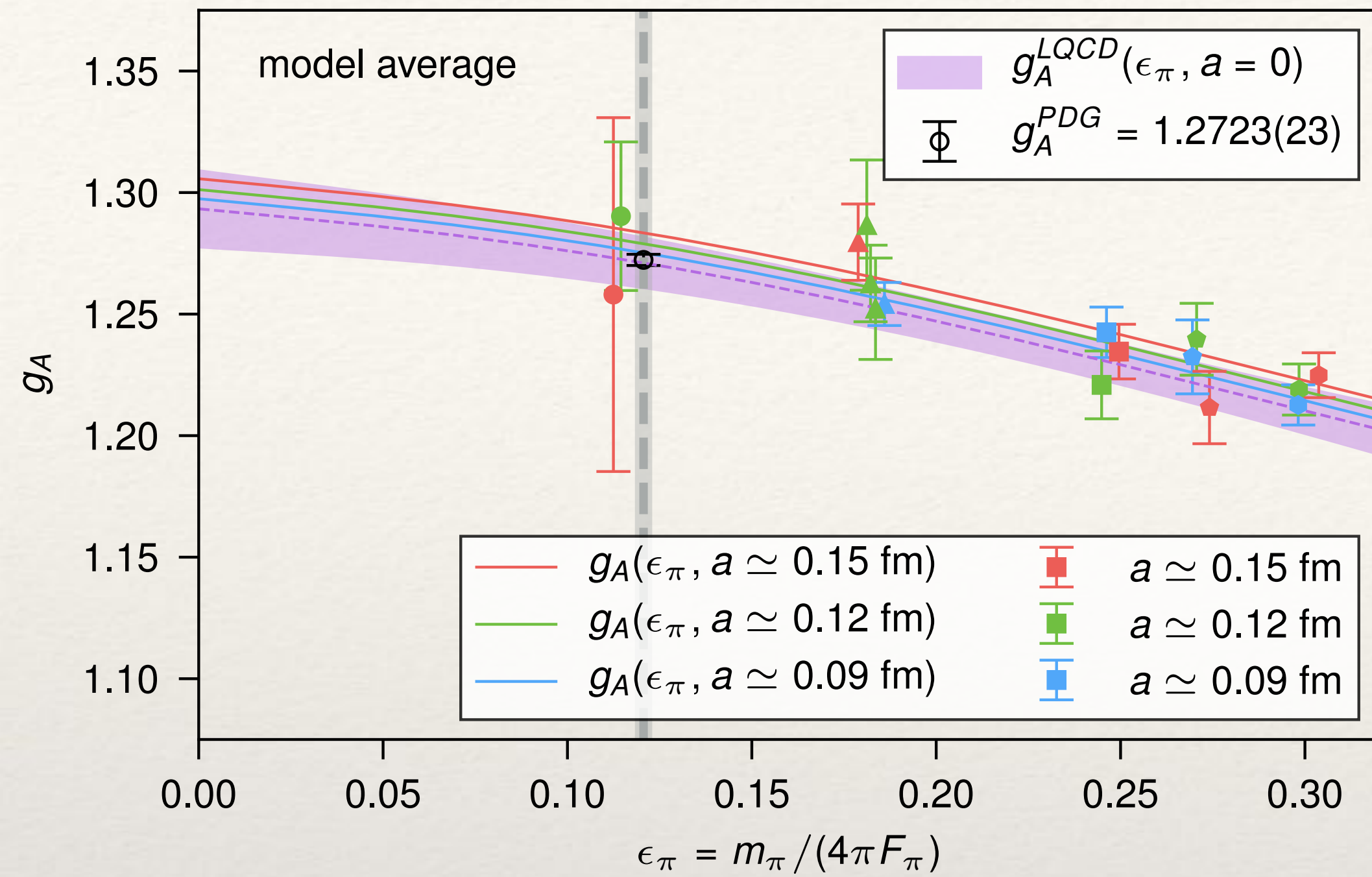


- Many groups obtain values of g_A fully extrapolated to the physical point (green)
 - physical pion mass
 - continuum
 - infinite volume
- Callat results
 - CalLat 18: $g_A = 1.271(13)$ 1%
 - CalLat 19: $g_A = 1.2642(93)$ 0.74%
 - CalLat 24/25: ~0.5%?
- Experiment:
 - $|g_A^{\text{PDG}}| = 1.27540(130)$
 - $|g_A^{\text{PERKEO-III}}| = 1.27641(046)$
- In order to take advantage of these precise results — we must determine QED corrections to g_A !



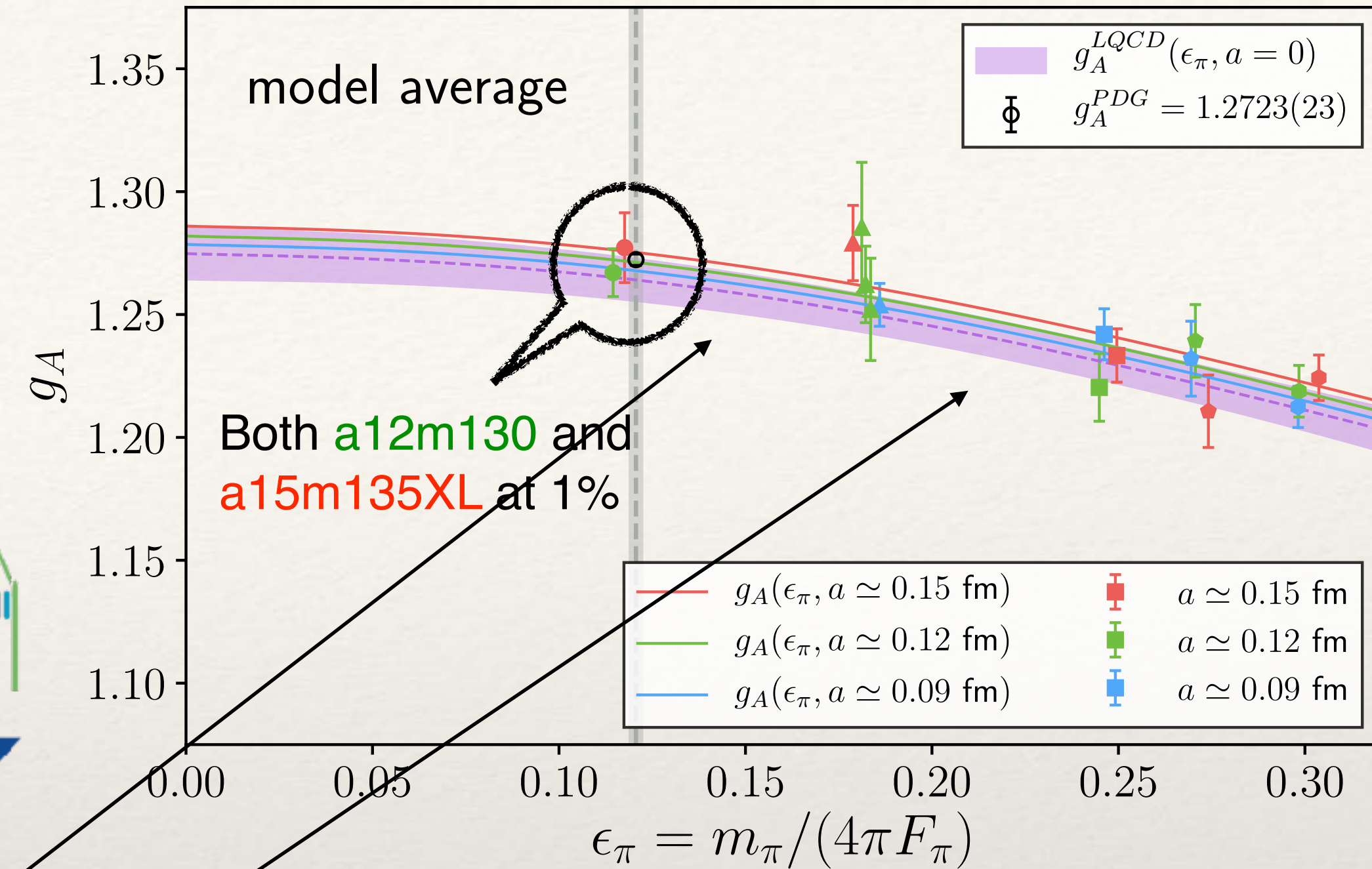
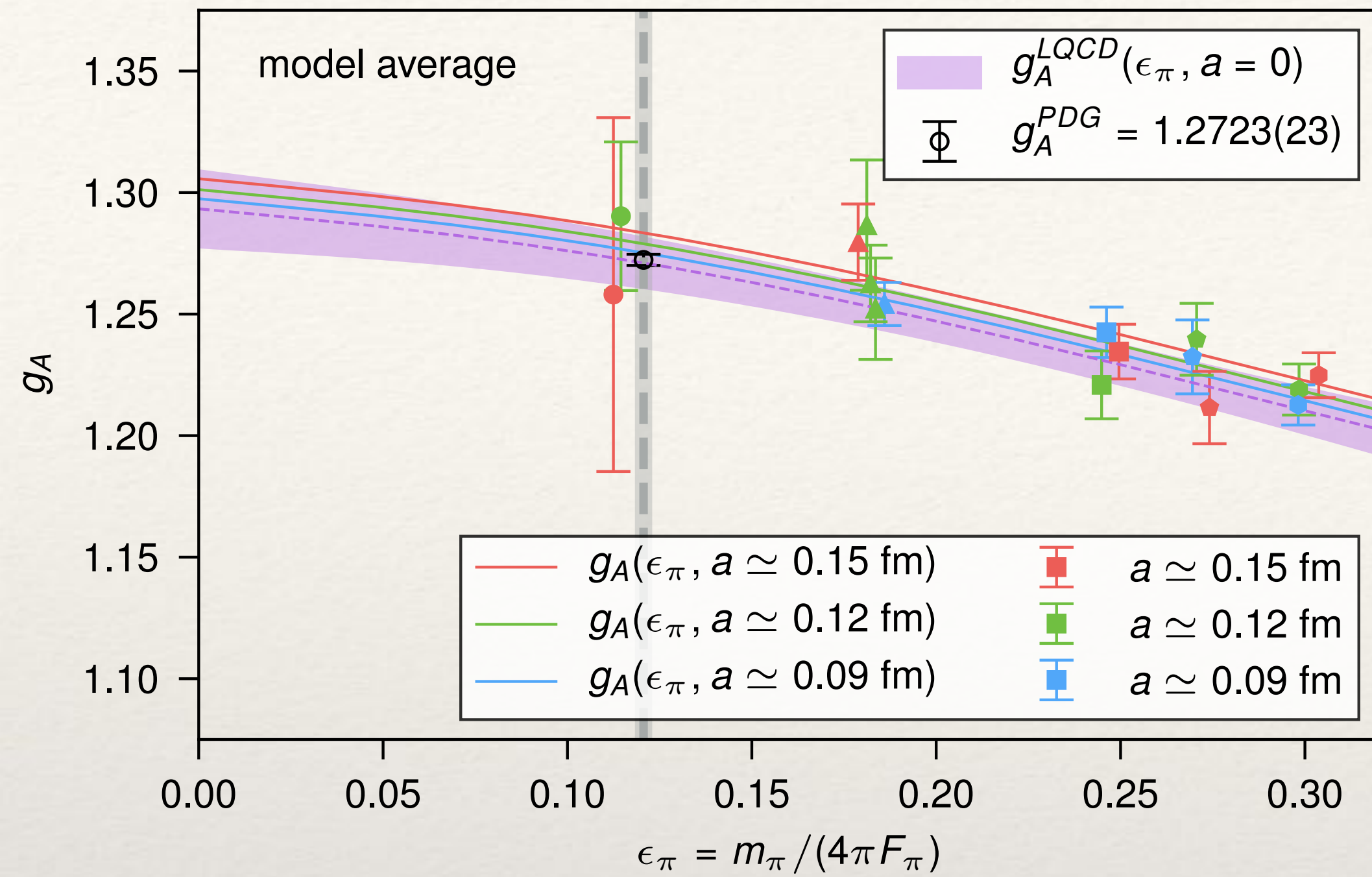
- The **a12m130** ($48^3 \times 64 \times 20$) with 3 sources cost as much as all other ensembles combined
 - 2.5 weekends on Sierra → 16 srcs
 - Now, 32 srcs (un-constrained, 3-state fit)
- We generated a new **a15m135XL** ($48^3 \times 64$) ensemble (old **a15m130** is $32^3 \times 48$)
 - $M\pi L = 4.93$ (old $M\pi L = 3.2$)
 - $L_5 = 24, N_{\text{src}} = 16$

$g_A = 1.2711(125) \rightarrow 1.2641(93) [0.74\%]$



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□ We have 2 additional pion masses (180, 260) and a 4th finer lattice spacing, $a \approx 0.06 \text{ fm}$ @ $M\pi \approx 220, 310 \text{ MeV}$

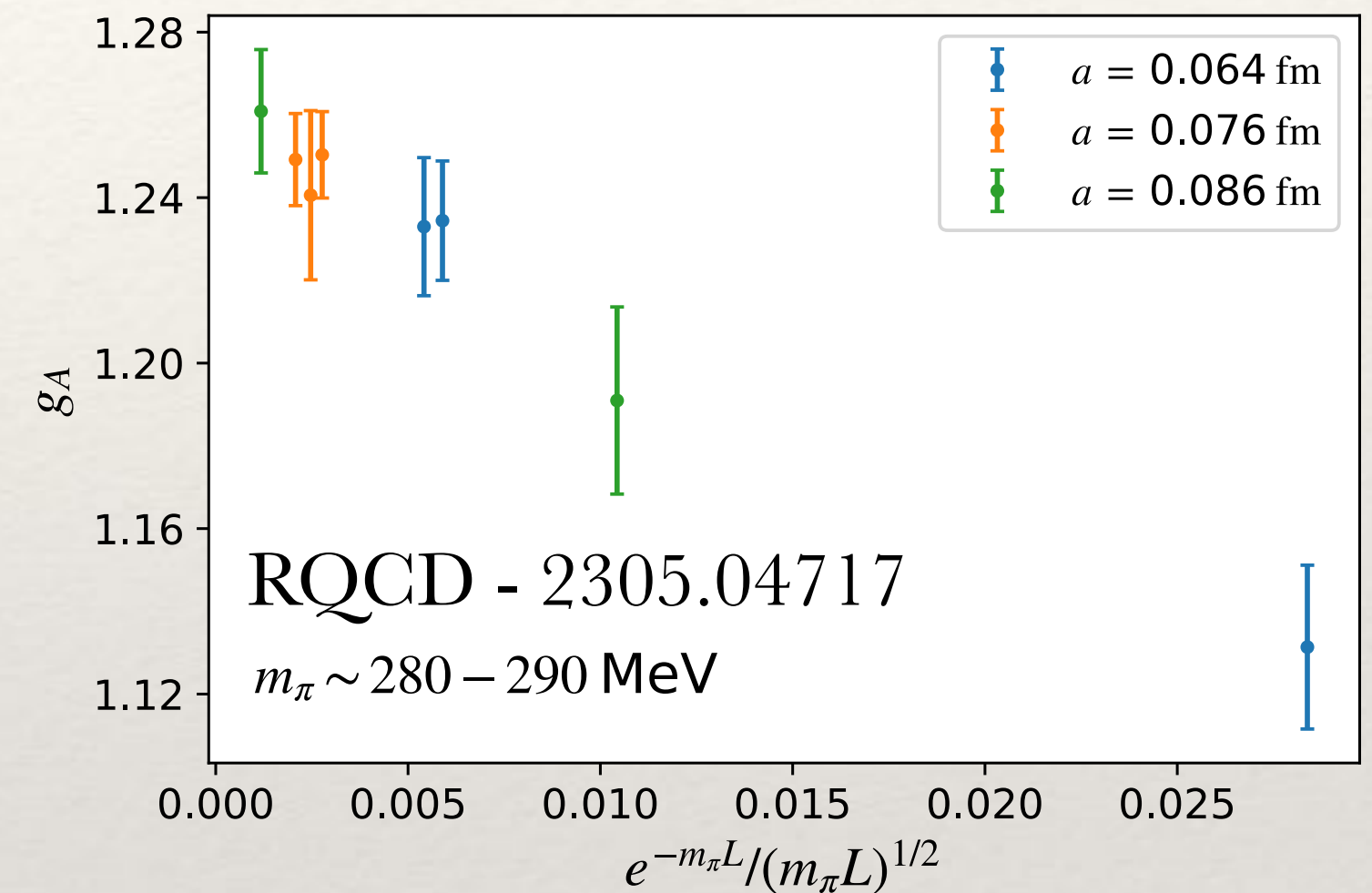
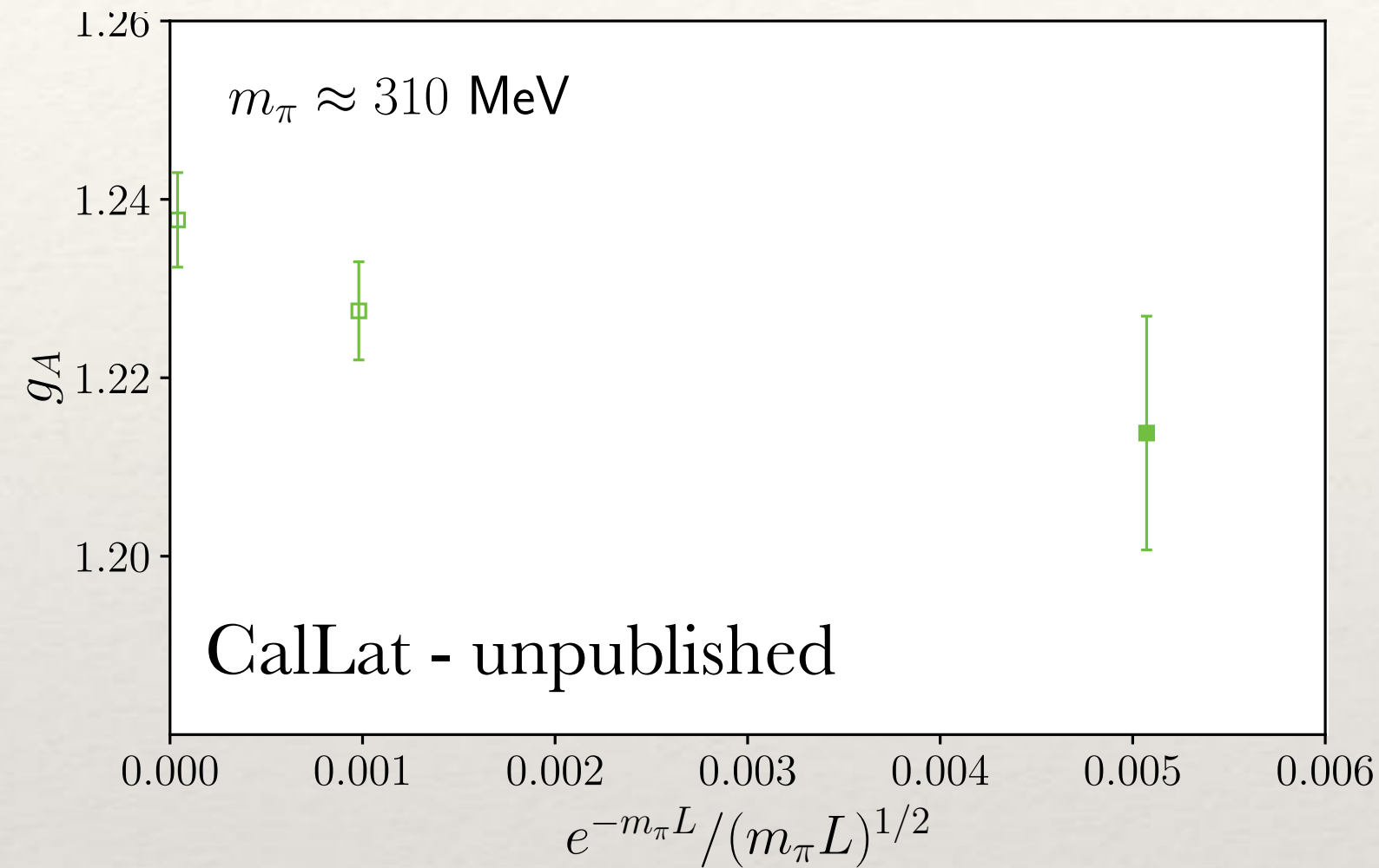
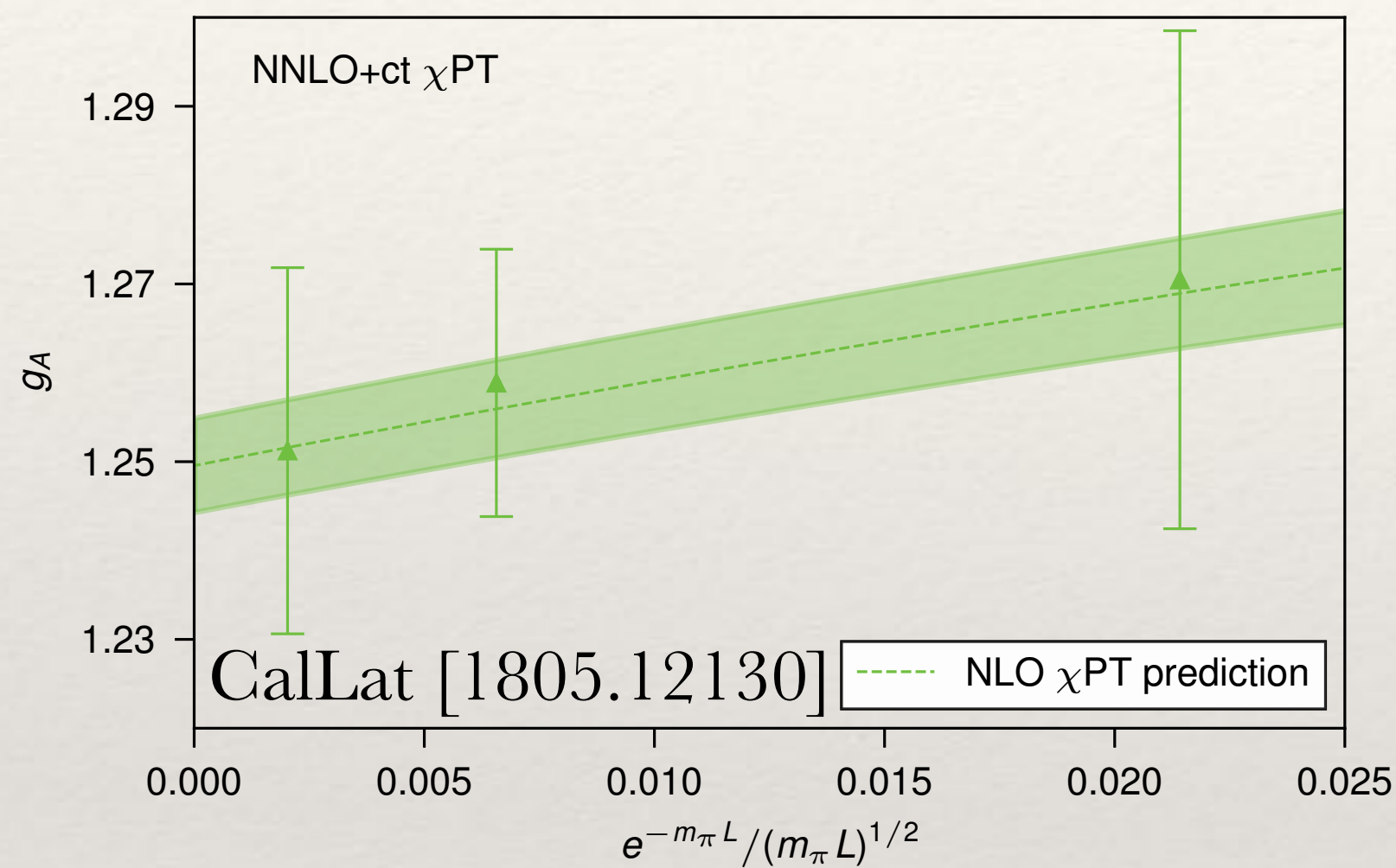
□ We anticipate improving g_A to $\sim 0.5\%$ — we need to address the radiative QED correction to make this useful

Sub-percent determination of $g_A^{\text{QCD-isosymmetric}}$

□ At sub-percent precision — we have to worry about

non-monotonic finite volume corrections to g_A

Z. Hall, D. Pefkou, A.S. Meyer, R. Briceño, M.A. Clark, M. Hoferichter, E. Mereghetti, H. Monge-Camacho, C. Morningstar, A. Nicholson, P. Vranas, A. Walker-Loud — *In preparation*



□ Sign change versus m_π is expected from baryon χ PT

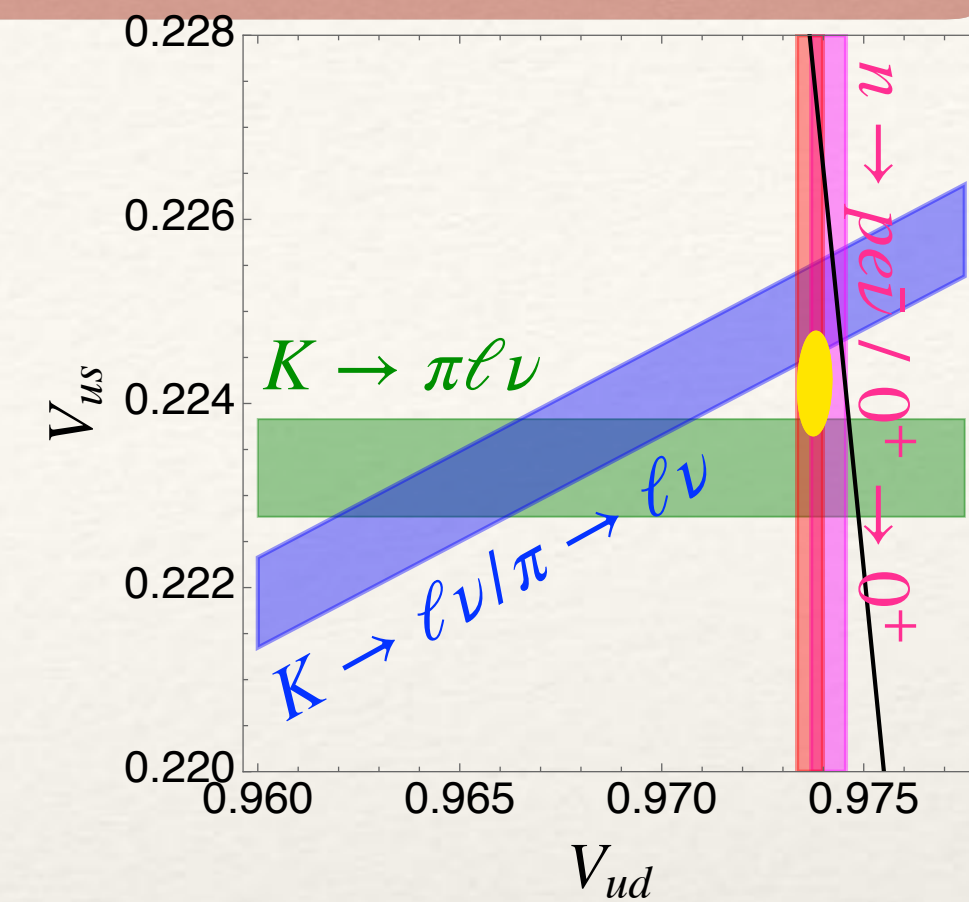
□ Current strategy of most groups: $g_A(L) = g_A + c_2 \frac{m_\pi^2}{(4\pi F_\pi)^2} \frac{e^{-m_\pi L}}{\sqrt{m_\pi L}}$ fit c_2 at heavy m_π , apply to all

□ We need to add sub-leading FV corrections $+ c_3 \frac{m_\pi^3}{(4\pi F_\pi)^3} \frac{e^{-m_\pi L}}{m_\pi L} + \dots$

□ and simultaneously understand discretization errors...

Summary & Outlook

- Interesting $\approx 3\sigma$ tension in the first row CKM unitarity
- Experimental prospects to
 - Improve the precision of $K_{\ell 2}$ (currently dominated by single experiment) and determine $K_{\mu 3}/K_{\mu 2}$ — **NA62**
 - Improve V_{us}/V_{ud} and determine V_{ud} from π^+ decays — **PIONEER**
 - Improve measurements of neutron lifetime and axial coupling to get competitive precision on V_{ud} as compared to superallowed nuclear decay
- In order to take advantage of the anticipated experimental precision — we need to provide SM theory prediction with **O(0.2%)** uncertainty
 - We need more LQCD calculations of $K_{\ell 3}$ — both pure **QCD** and **QCD+QED**
 - Requires understanding radiative **QED** corrections down to O(0.2%)
 - Exciting new LQCD determinations of electroweak $\square_{\gamma W}$ contribution to pion, kaon and now nucleon
Agrees with previous (and recent) dispersive determinations
- BSM Right-Handed currents provide more statistically favored solutions to CKM unitarity tension
 - LQCD calculations of g_A can be compared with $\lambda_{\text{PDG}} = g_A^{\text{PDG}}/g_V^{\text{PDG}}$ to constrain right-handed currents
 - Unexpected O(2%) **QED** correction to g_A spoils this comparison
 - Need LQCD+QED calculation to determine it



Thank You