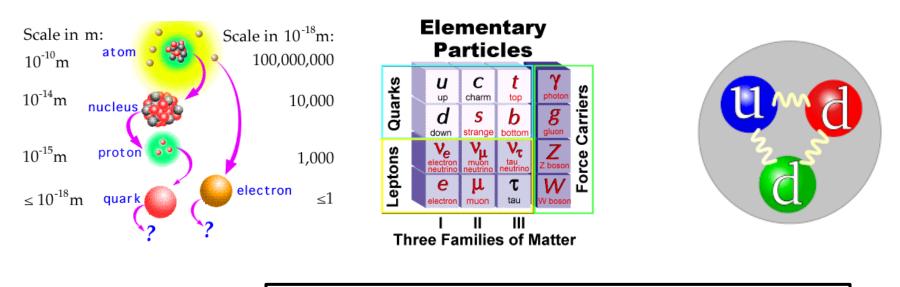
## Nucleon charges from Lattice QCD and their implications for BSM physics

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LA-UR: 23-27930

XVI Quark Confinement, 2024, Cairns, Australia

#### **NME Collaboration:**

#### **Thirteen 2+1-flavor clover ensembles = clover-on-clover formulation**

#### **PNDME and NME members**

- Tanmoy Bhattacharya (T-2)
- Vincenzo Cirigliano (T-2  $\rightarrow$  INT, UW)
- Rajan Gupta (T-2)
- Emanuele Mereghetti (T-2)
- Boram Yoon (CCS-7  $\rightarrow$  **NVIDIA**)
- Junsik Yoo (PD: 2022 May )
- Yong-Chull Jang (PD: 2017-2018)
- Sungwoo Park (PD: 2018-2021)
- Santanu Mondal (PD: 2019-2021)
- Huey-Wen Lin (MSU)
- Balint Joo (NVIDIA)
- Frank Winter (Jlab)

Acknowledgements for Computational Support: MILC for HISQ ensembles. DOE for computer allocations NERSC under ERDCAP OLCF under INCITE hep133 USQCD Institutional Computing at LANL

#### References

- Charges:
- AFF:
- AFF:
- AFF:
- AFF:
- VFF:
- $\sigma_{\pi N}$
- $d_n$  from  $\Theta$ -term
- $d_n$  from qEDM
- $d_n$  from qcEDM
- Moments of PDFs
- Proton spin:

#### NME

- Charges, FF:
- Moments of PDFs

Gupta et al, PRD.98(2018) 034503Gupta et al, PRD 96(2017) 114503

- Jang et al, PRL 124 (2020) 072002
- Jang et al, 11 KL 124 (2020) 072002
- Jang et al, PRD 109 (2024) 014503
- Tomalak et al, PRD 108 (2023) 074514
- Jang et al, PRD 100 (2020) 014507
- Gupta et al, PRL 127 (2021) 242002
- Bhattacharya etal, PRD 103 (2021) 114507
- Gupta et al, PRD 98 (2018) 091501
- Bhattacharya et al, PRD 98 (2018) 091501 Mondal et al, PRD 102 (2020) 054512
- Lin et al, PRD 98 (2018) 094512

Park et al, PRD 105 (2022) 054505 Mondal et al, JHEP 04 (2021) 044





## Outline

- What is Lattice QCD good for?
  - Properties of QCD: spectrum, EoS, ...
  - Matrix elements within hadronic states
- Nucleon charges
  - Isovector axial, scalar, tensor
  - Flavor diagonal axial
  - Flavor diagonal tensor
  - O-Term
  - Flavor diagonal scalar

This talk is will emphasize issues in the Lattice QCD calculations and connections to BSM

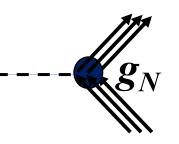
Lattice QCD results for nucleon charges are being reviewed by FLAG: 2019, 2021, 2024

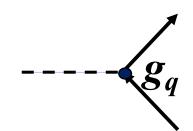
To quote numbers, please use original articles or numbers in the FLAG report

## **Nucleon charges**

- Standard Model specifies the coupling  $g_q$  of electroweak currents with quarks
- Similarly, EFT of BSM at few GeV is in terms of quark and gluon operators
- Experiments measure these interactions on hadrons
- QCD gives significant corrections:  $g_{quark} \rightarrow g_{hadron}$
- Calculation is intrinsically non-perturbative

Example: axial charge of nucleons goes from  $1 \rightarrow 1.276$ 





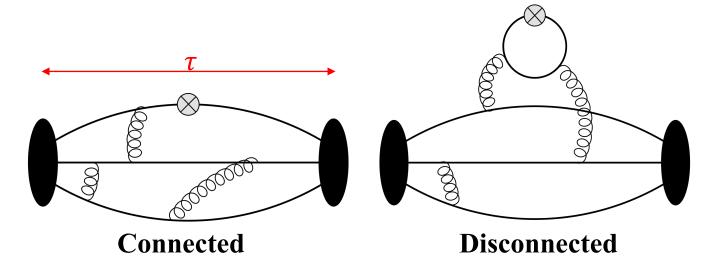
## Nucleon charges: $\langle N | \overline{q} \Gamma q | N \rangle \propto g_{\Gamma}^{q} \Gamma$

- Standard Model
  - Vector charge (CVC)  $g_V^{u-d}$   $1 \rightarrow 1$
  - Axial charge  $g_A^{u-d}$   $1 \to 1.276$
  - Transversity  $g_T^{u,d,s,c,b}$
  - Contribution of quark's spin to nucleon spin  $g_A^{u,d,s,c,b}$
- BSM
  - Novel scalar and tensor interactions via  $g_S^{u-d}$ ,  $g_T^{u-d}$  and precision measurements of neutron decay
  - Coupling to dark matter:  $g_{A,P,S,T,V}^{u,d,s,c,b}$
  - Contribution of quark's EDM to nucleon EDM  $g_T^{u,d,s,c,b}$
  - Contributions of the Θ-Term to nEDM

## Many thanks to

- Raul Briceno:
  - Three-hadron systems
- Andreas Kronfeld:
  - Perturbation theory, power corrections, renormalons and precise evaluation of quark masses and  $\alpha_S$
- Huey-Wen Lin:
  - Parton distributions from lattice QCD and impacts on global QCD analysis
- Finn Stokes:
  - Review of muon g-2
- Andre Walker-Loud:
  - Beta decay as probe of new physics
- Michael Creutz, William Detmold, Xu Feng, Shoji Hashimoto, Martin Hoferichter, David Lin, Ross Young, James Zanotti, ...

#### Lattice Methodology well established for "connected" and "disconnected" 3-point correlation functions



stochastic estimates of disconnected contributions are noisier for the same computational cost and smaller in value

Isoscalar 
$$g_{A,S,T}^{u+d} = g_{A,S,T}^{u+d,conn} + 2g_{A,S,T}^{l,disc}$$
  
Isovector  $g_{A,S,T}^{u-d} = g_{A,S,T}^{u-d,conn}$  In the isospin symmetric limit

## Analysis: Spectral decomposition of $\Gamma^2$ and $\Gamma^3$

Three-point function for matrix elements of axial current  $\mathcal{A}_{\mu}$  $\langle \Omega | N(\tau) \mathcal{A}_{\mu}(t) \overline{N}(0) | \Omega \rangle$ 

Insert  $T = e^{-H\Delta t} \sum_i |n_i\rangle \langle n_i|$  at each  $\Delta t$  with  $T |n_i\rangle = e^{-H\Delta t} |n_i\rangle = e^{-E\Delta t} |n_i\rangle$ 

$$\sum_{i,j} \langle \Omega | \overline{N}(\tau) \cdots e^{-H\Delta t} \sum_{j} |n_{j}\rangle \langle n_{j} | \mathcal{A}_{\mu} e^{-H\Delta t} \sum_{i} |n_{i}\rangle \langle n_{i} | \cdots N(0) | \Omega$$

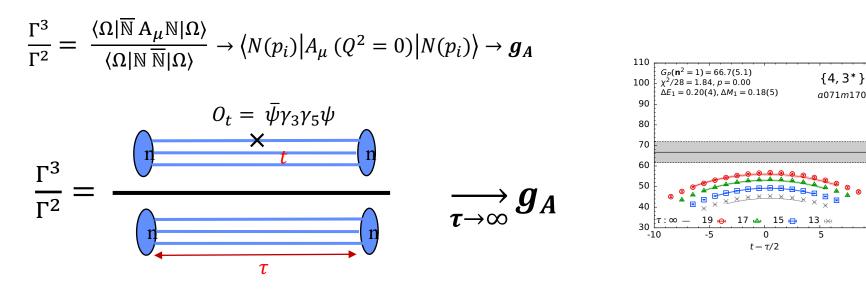
$$\sum_{i,j} \langle \Omega | \overline{N} | n_{j}\rangle e^{-E_{j}(\tau-t)} \langle n_{j} | \mathcal{A}_{\mu} | n_{i}\rangle e^{-E_{i}t} \langle n_{i} | N | \Omega \rangle$$

$$A_{j}^{*} \qquad \text{Matrix Elements} \qquad A_{i}$$

### **Extracting Nucleon Charges**

$$\Gamma^2 = \sum_i A_i^* A_i e^{-E_i \tau} \qquad \Gamma^3 = \sum_{i,j} A_i^* A_j \langle N_i | O | N_j \rangle e^{-E_i t} e^{-E_j (\tau - t)}$$

In the limit  $(\tau \rightarrow \infty)$  only the ground state contributes. Then



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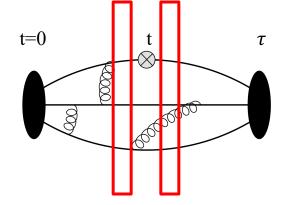
Otherwise, need to make fits to  $\Gamma^3$ . This requires knowing the spectrum (energies  $E_i$ ) and amplitudes ( $A_0$ )

## Spectral decomposition of 3-point function

All states with the same quantum numbers as the nucleon are created by N

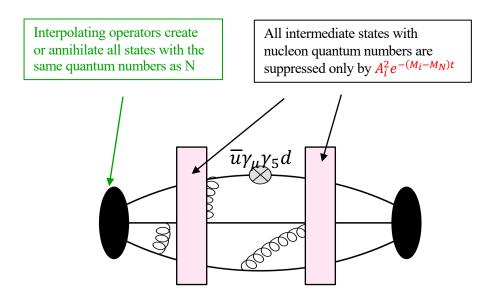
$$\Gamma^{3pt} = \langle 0|\mathcal{O}|0\rangle |A_0|^2 e^{-M_0\tau} \times \left[1 + \frac{\langle 1|\mathcal{O}|1\rangle}{\langle 0|\mathcal{O}|0\rangle} \frac{|A_1|^2}{|A_0|^2} e^{-\Delta M_1\tau} + \frac{\langle 2|\mathcal{O}|2\rangle}{\langle 0|\mathcal{O}|0\rangle} \frac{|A_2|^2}{|A_0|^2} e^{-(\Delta M_2 + \Delta M_1)\tau} + \frac{\langle 0|\mathcal{O}|1\rangle}{\langle 0|\mathcal{O}|0\rangle} \frac{|A_1|}{|A_0|^2} e^{-\Delta M_1\frac{\tau}{2}} \times 2\cosh\left(\Delta M_1(t - \frac{\tau}{2})\right)$$





To isolate  $\langle 0|O|0 \rangle$ , the key quantities needed are  $A_0, M_i$ 

# Which excited states make significant contributions to a given correlation function?

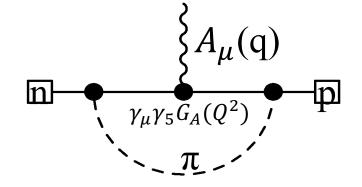


Towers of multihadron states  $N(\vec{p})\pi(-\vec{p})$   $N(0)\pi(\vec{p})\pi(-\vec{p})$   $N(\vec{p})2\pi(-\vec{p})$ ...

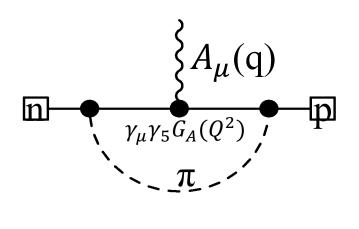
Starting at ~1220 MeV

Radial excitations N(1440) ...

 $\chi$ PT suggests that the contribution of a pion loop could be ~5% in all NME



 $\chi$ PT: In all cases, there is excited-state contribution to nucleon charges from when the pion in pion loop is on shell



This, possibly 5%, contribution from  $N\pi$  excited-state needs to be understood/resolved for each NME

## Need $A_0$ , $M_i$ : but which $M_i$ are significant?

- Mass gaps,  $\Delta M_i$ , of  $N\pi$ ,  $N\pi\pi$ , ... states are smaller than N(1440)
- Their spectrum gets dense as  $\vec{p} \rightarrow 0$
- We approximately know their energies in a finite box
- Creating each extra state ( $\pi$ ) is suppressed by a normalization factor 1/V
- In some cases, the transition ME are large and compensate for the 1/V factor

Issue: With current statistics, fits with  $M_1 = M_{N\pi}$  versus  $M_1 = M_{N(1440)}$  are not distinguished by the  $\chi^2$ !

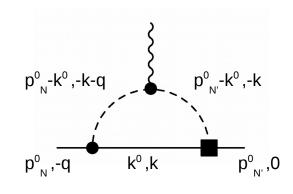
Using priors is not the desired solution

What size statistics are needed to achieve data-driven ( $\chi^2$ ) selection?

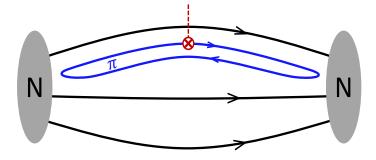
#### **Examples of enhanced excited-state matrix elements**

- Axial Form Factors must satisfy PCAC relation between them
  - Need to include  $N(\vec{p})\pi(-\vec{p})$  states to satisfy PCAC
  - $\langle \Omega | N(\tau) \mathcal{A}_4(t) \overline{N}(0) | \Omega \rangle$  has very large ESC
  - Used  $\langle \Omega | N A_4 \overline{N} | \Omega \rangle$  to include  $N\pi$  state. Data-driven method
  - Enhanced ME: Manifestation of pion-pole dominance hypothesis

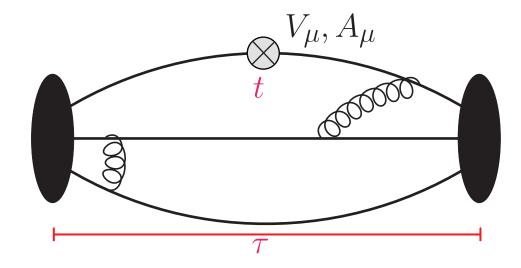
- $\chi$ PT predicts large contributions from  $N\pi$  state in
  - nEDM from  $\Theta$ -term
  - The pion-nucleon sigma term  $\sigma_{\pi N} = m_{ud} g_S^{u+d}$



π



# Isovector charges from forward matrix elements

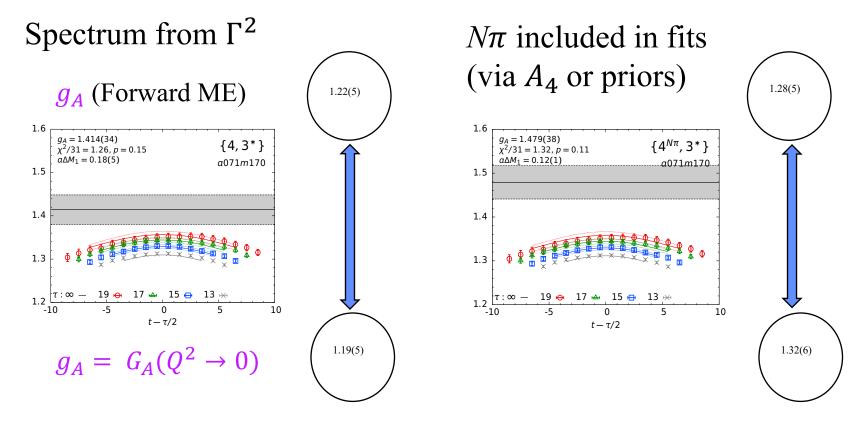


### All (A,P,S,T,V) done at the same time

# Isovector axial charge $g_A^{u-d}$

- Benchmark quantity as it is very well measured  $g_A^{u-d} = 1.276(1)$
- A fundamental parameter in nuclear physics





 $G_A$ ,  $\tilde{G}_P$ ,  $G_P$  do not satisfy PCAC

 $G_A$ ,  $\tilde{G}_P$ ,  $G_P$  satisfy PCAC

## Status

- Current lattice estimates are mostly in the range  $g_A^{u-d} = [1.25 1.31]$
- Precision is improving steadily
- Resolve the possible ~5% excited-state contributions from  $N\pi$  ... states
- Isospin breaking and electromagnetic corrections (talk by Walker-loud)

# Implication for BSM

- Constraints on right-handed currents once Lattice QCD can provide  $g_A^{u-d}$  with few parts per mil precision (see talk by Walker-Loud)
- Neutron decay is a very promising opportunity for extracting V<sub>ud</sub> and testing the unitarity of the first row of the CKM matrix.
   Need τ<sub>n</sub> and g<sup>u-d</sup> from experiments and lattice QCD input in calculating radiative corrections (see talks by Walker-Loud, Xu Feng)

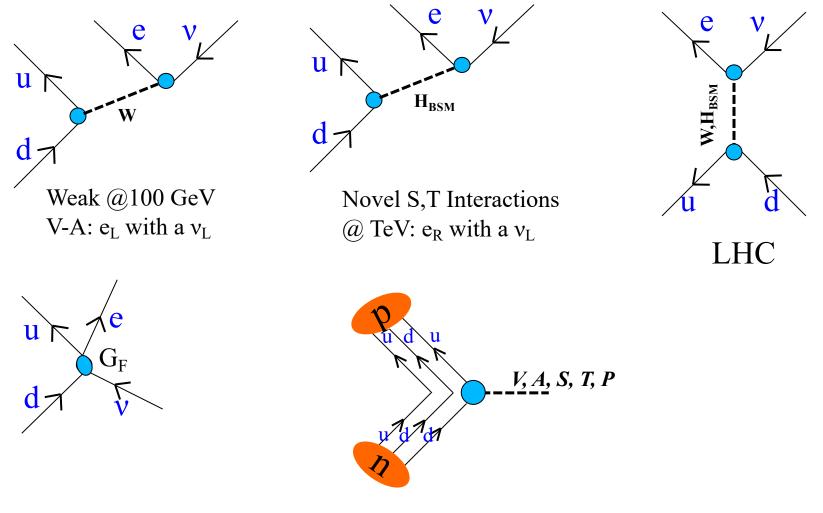
Isovector scalar and tensor charges  $g_S^{u-d}$  and  $g_T^{u-d}$ 

• Combined with high precision measurements of neutron decay, they provide a low energy probe of novel scalar and tensor interactions

Bhattacharya et al, PRD 85, 054512 (2012)

## Probing New Interactions: M<sub>BSM</sub> >> M<sub>W</sub> >> 1 GeV

Many BSM possibilities for novel Scalar & Tensor interactions: Higgs-like, leptoquark, loop effects, ...

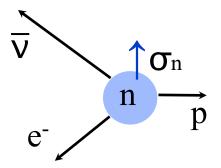


Effective Theory (a)  $\sim 2 \text{ GeV}$ Characterized by  $G_F$ 

New S, T Interactions  $(\varepsilon_S, \varepsilon_T)$ 

## Measure in [Ultra]Cold Neutron Decay: Parameters sensitive to new physics

Neutron decay can be parameterized as



$$d\Gamma \propto F(E_e) \left[ 1 + \frac{b}{E_e} \frac{m_e}{E_e} + \left( B_0 + \frac{B_1}{E_e} \frac{m_e}{E_e} \right) \frac{\vec{\sigma}_n \cdot \vec{p}_\nu}{E_\nu} + \cdots \right]$$

- *b*: Deviations from the leading order electron spectrum: Fierz interference term
- $B_1$ : Energy dependent part of the correlation of antineutrino momentum with the neutron spin

Relating b,  $B_1$  to  $g_{S,T}$  & BSM couplings  $\varepsilon_{S,T}$ 

$$H_{eff} \supset G_{F} \left[ \varepsilon_{S} \overline{u} d \ \overline{e} (1 - \gamma_{5}) v_{e} + \varepsilon_{T} \overline{u} \sigma_{\mu\nu} d \ \overline{e} \sigma^{\mu\nu} (1 - \gamma_{5}) v_{e} \right]$$

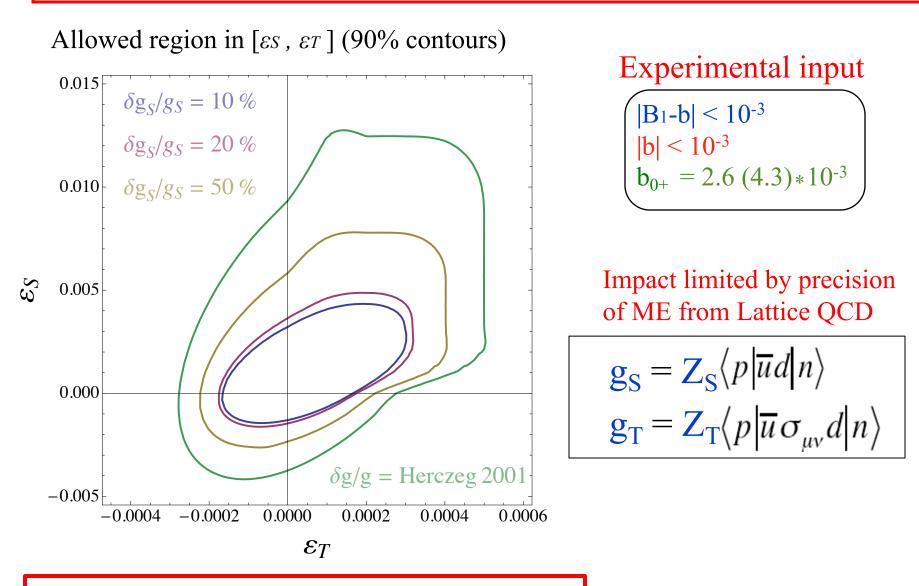
$$g_{S} = Z_{S} \left\langle p \left| \overline{u} d \right| n \right\rangle \quad g_{T} = Z_{T} \left\langle p \left| \overline{u} \sigma_{\mu\nu} d \right| n \right\rangle \quad \begin{bmatrix} \text{Lattice} \\ QCD \end{bmatrix}$$

Analysis of  $n \rightarrow p \ e \ \overline{v}$  decay at leading order in  $\varepsilon_{S,T}$  gives the linear relations

$$b_{v}^{BSM} \approx 0.34 g_{s} \varepsilon_{s} - 5.22 g_{T} \varepsilon_{T}$$
$$b_{v}^{BSM} \equiv B_{1}^{BSM} = E_{e} \frac{\partial B^{BSM} (E_{e})}{\partial m_{e}} \approx 0.44 g_{s} \varepsilon_{s} - 4.85 g_{T} \varepsilon_{T}$$

Bhattacharya et al, PRD 85, 054512 (2012)

#### Impact of reducing errors in $g_S$ and $g_T$ from 50 $\rightarrow$ 10%



**Goal: 10% accuracy in**  $g_S$  and  $g_T$ 

PRD 85, 054512 (2012)

### **Constraints on** $[\varepsilon_S, \varepsilon_T]$ : $\beta$ -decay versus LHC

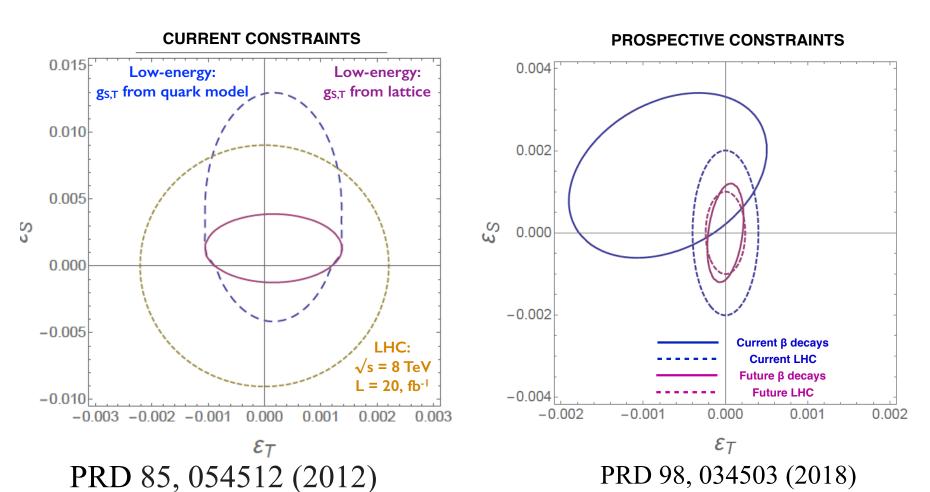
• LHC:  $(u+d \rightarrow e+v)$  look for events with an electron and missing energy at high transverse mass

W,H<sub>BSM</sub>

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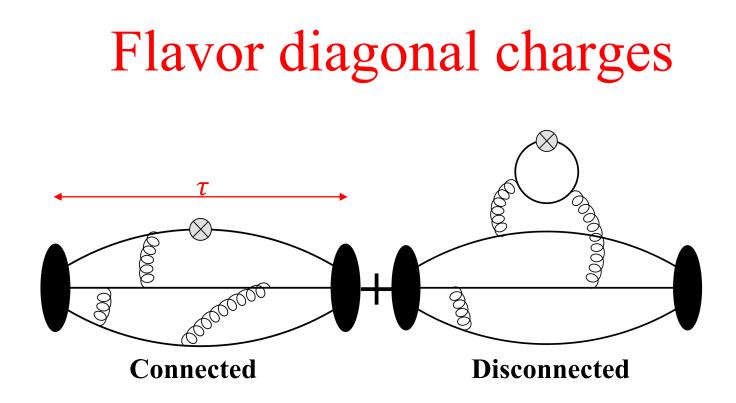
LHC

• low-energy experiments + lattice with  $\delta g_S/g_S \sim 10\%$ 



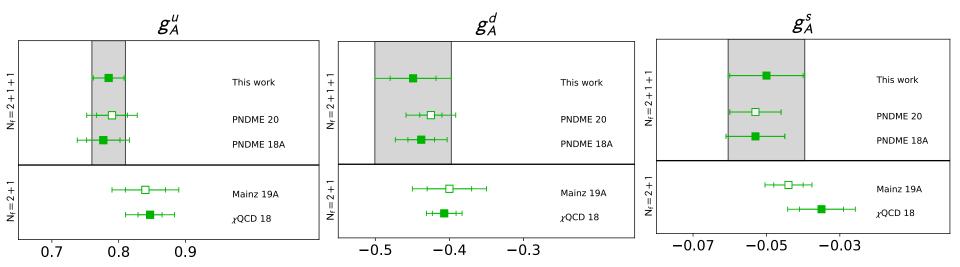
# Implication for BSM

- For next generation low energy search for novel scalar and tensor interactions, the main improvement needed is in neutron decay experiments to get *b* and  $B_1$  to  $10^{-4}$  precision.
- Need  $g_S^{u-d}$  and  $g_T^{u-d}$  to within a few percent, which is on track
- LHC constraints are currently stronger



- All (A,P,S,T,V) done at the same time
- Calculation of disconnected contributions is more costly and noisy

## FD axial charges $g_A^{u,d,s,c}$



## Issues

- Disconnected contribution is small,  $\sim 5\%$
- Need much higher statistics to reduce uncertainty to ~1%

#### **FD** axial charges Intrinsic quark spin contribution to proton spin

gauge invariant decomposition of the proton spin is given by

$$\frac{1}{2} = \sum_{\{u,d,s,c\}} \left(\frac{1}{2}\Delta q + L_q\right) + J_g$$

$$\frac{1}{2} = \sum_{\{u,d,s,c\}} \left( \frac{1}{2} \Delta q + L_q \right) + J_g$$

$$S_P^q = \sum_q S_q \equiv \sum_q \frac{\Delta q}{2} \equiv 0.5 \sum_q g_A^q$$

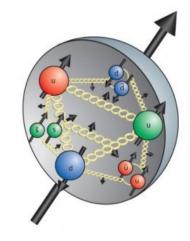
[X. Ji, PRL 78 (1997) 610]

$$g_A^q = \langle N(p_i) | Z_A A_\mu^q(0) | N(p_i) \rangle$$

LANL (PNDME) result (PRD 98 (2018) 094512):

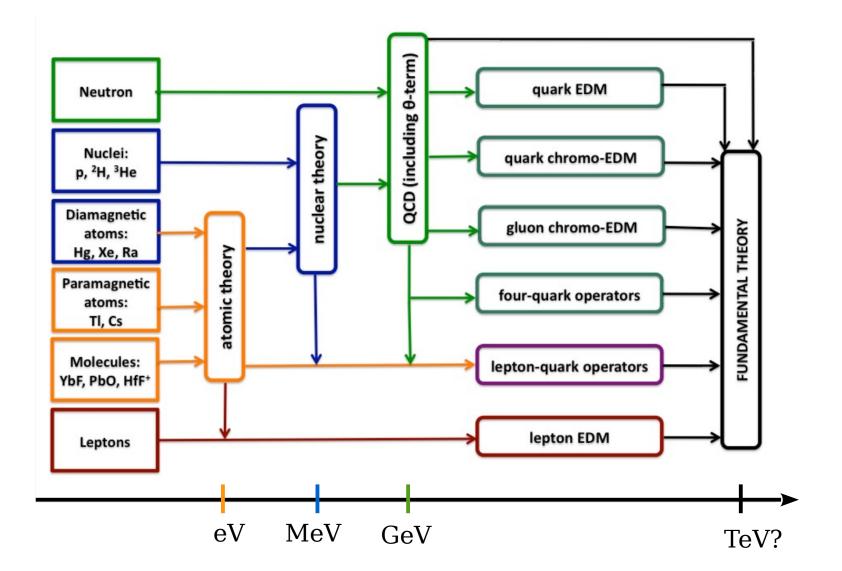
$$0.5\sum_{q} g_{A}^{q} = (0.777(39) - 0.438(35) - 0.053(8))/2 = 0.143(31)(36)$$

COMPASS result:  $0.13 \le \sum_q S_q \equiv 0.5 \sum_q g_A^q \le 0.18$ 

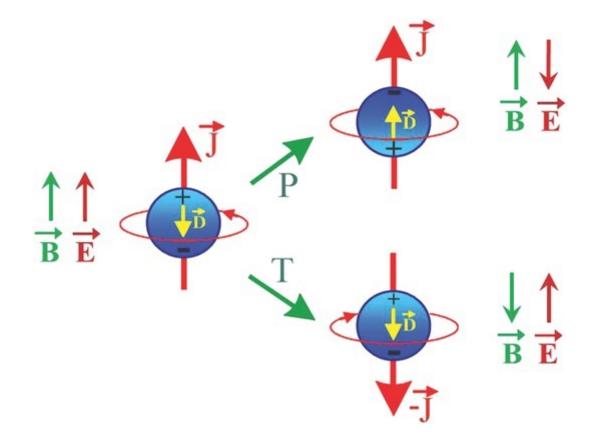


# $g_T^{u,d,s,c}$ Contribution of the quark EDM to neutron EDM

## Novel CP violation in BSM $\rightarrow$ EDMs



## EDMs violate P and T invariance



## CP(T)-violation and EDMs

#### Effective CPV Lagrangian at Hadronic Scale

$$\begin{split} \mathcal{L}_{\text{CPV}}^{d \leq 6} &= -\frac{g_s^2}{32\pi^2} \overline{\theta} G \tilde{G} & \text{dim}{=}4 \text{ QCD } \theta\text{-term} \\ &- \frac{i}{2} \sum_{q=u,d,s,c} d_q \overline{q} (\sigma \cdot F) \gamma_5 q & \text{dim}{=}5 \text{ Quark EDM (qEDM)} \\ &- \frac{i}{2} \sum_{q=u,d,s,c} \tilde{d}_q g_s \overline{q} (\sigma \cdot G) \gamma_5 q & \text{dim}{=}5 \text{ Quark Chromo EDM (CEDM)} \\ &+ d_w \frac{g_s}{6} G \tilde{G} G & \text{dim}{=}6 \text{ Weinberg's 3g operator} \\ &+ \sum_i C_i^{(4q)} O_i^{(4q)} & \text{dim}{=}6 \text{ Four-quark operators} \end{split}$$

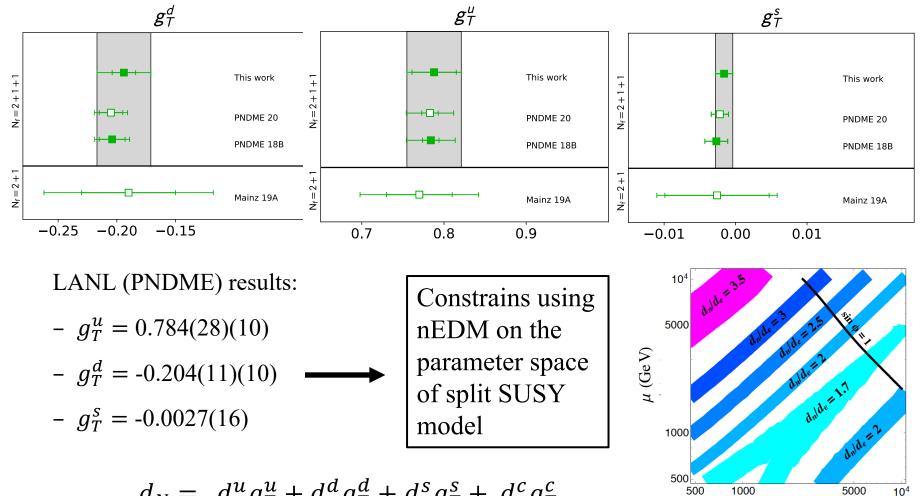
- $\overline{\theta} \leq \mathcal{O}(10^{-8} 10^{-11})$ : Strong CP problem
- Dim=5 terms suppressed by  $d_q \approx \langle v \rangle / \Lambda_{BSM}^2$ ; effectively dim=6
- All terms up to d = 6 are leading order

Each CP violating interaction gives a contribution to neutron EDM

- $\Theta$ -term
- Quark EDM  $\rightarrow$  Flavor diagonal tensor charges  $g_T^{u,d,s,c}$

$$\begin{aligned} d_n &= \overline{\Theta} \langle N \mid J_{EM} \int d^4 x \frac{G_{\mu\nu} \tilde{G}^{\mu\nu}}{32\pi^2} \mid N \rangle |_{CPV} \\ &+ d^u g_T^u + d^d g_T^d + d^s g_T^s + d^c g_T^c \\ &+ \cdots \end{aligned}$$

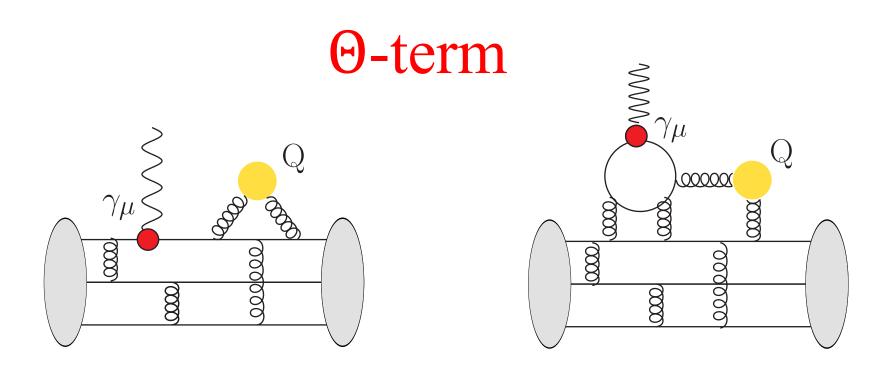
## $J_{T}^{u,d,s,c}$ : Contribution of the quark EDM to neutron EDM



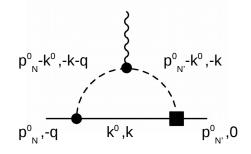
$$d_N = d^u g^u_T + d^d g^d_T + d^s g^s_T + d^c g^c_T$$

PRD 98 (2018) 091501

 $M_2$  (GeV)



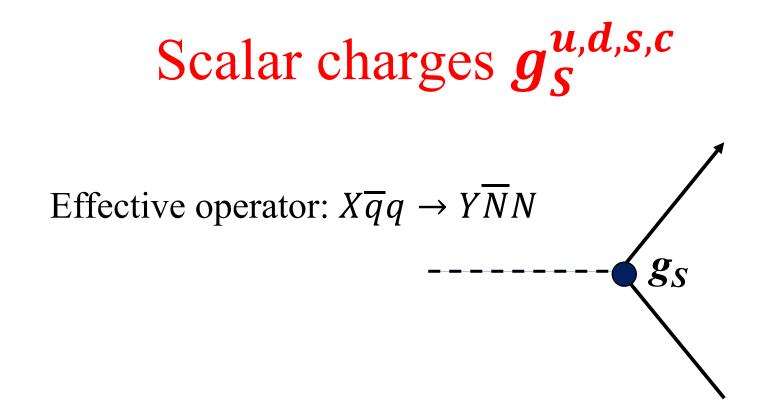
- Weight  $\Gamma^3$  with the topological charge
- Remove excited-state contributions
- Expand ME in terms of form factors
- Extract the contribution to the CP violating FF  $F_3$
- Status
  - Large error in the extraction of  $F_3$  (statistics)
  - Resolving and controlling  $N\pi$  contributions



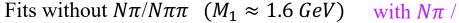
# Implication for BSM

- Knowing the bound [value] on nucleon EDM  $d_n$  and  $g_T^{u,d,s,c}$ , we can constrain BSM models in which quark EDM is the dominant CP violating operator.
- The coupling  $\overline{\Theta}$  is the sum of the SM and BSM. LQCD provides the contribution of the CP violating  $G_{\mu\nu}\tilde{G}^{\mu\nu}$  operator to the nucleon EDM.
  - To disentangle sources of  $\overline{\Theta}$ , need to measure EDMs of many systems

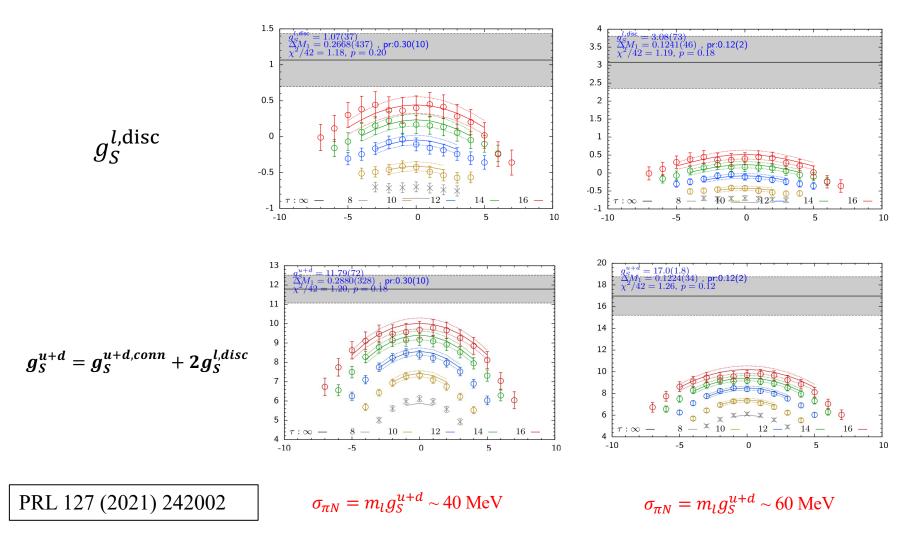
# Flavor diagonal scalar charges $g_{s}^{u,d,s,c}$



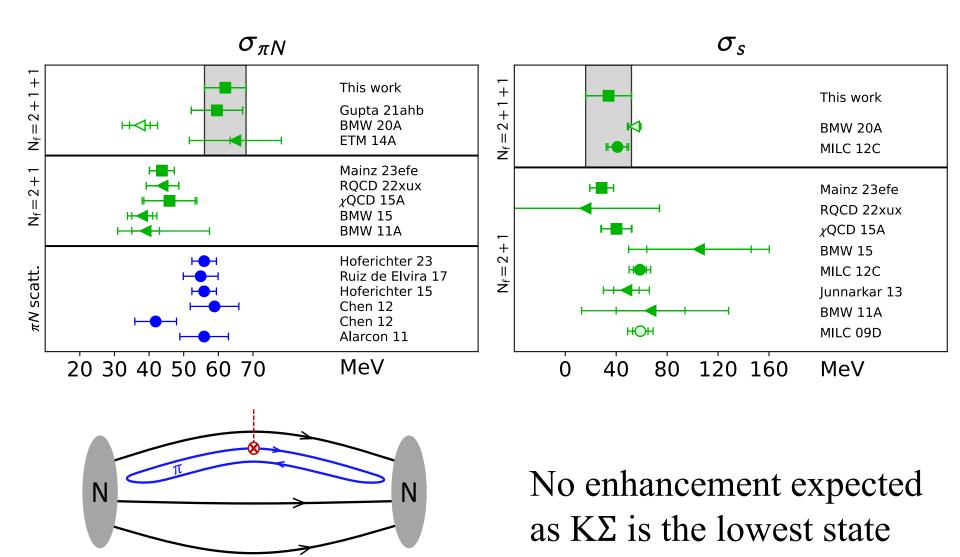
 $g_S^{u-d}$ : novel scalar interaction measured in neutron decay  $g_S^{u,d,s,c}$ : flavor independent interactions (dark matter)  $g_S^{u+d}$ : rate of change of nucleon mass with *u,d* quark mass  $g_S^{u,d}$ : Excited-state effects are large and results very sensitive to  $N\pi / N\pi\pi$  states







# Sigma terms



Enhanced contribution

#### The pion-nucleon sigma term:

Resolving tension between Lattice QCD and Phenomenology

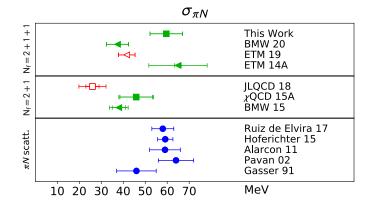
$$\sigma_{\pi N} \equiv m_{ud} g_S^{u+d} \equiv m_{ud} \langle N \big| \bar{u}u + \bar{d}d \big| N \rangle$$

#### FLAG Reports 2019, 2021:

- Lattice results ~40 MeV
- Phenomenology favors ~60 MeV

#### Post FLAG 2021 results

BMW (arXiv:2007.03319)  $\sigma_{\pi N} = 37.4(5.1)$  MeV (FH) RQCD (JHEP 05 (2023) 035)  $\sigma_{\pi N} = 43.9(4.7)$  MeV (FH) Mainz (PRL 131 (2023) 261902)  $\sigma_{\pi N} = 43.7(3.6)$  MeV (FH) ETM (PRD **102**, 054517)  $\sigma_{\pi N} = 41.6(3.8)$  MeV (Direct)



#### LANL Results: PRL 127 (2021) 242002; e-Print: 2105.12095

- Without including  $N(\vec{k})\pi(-\vec{k})$  and  $N(0)\pi(\vec{k})\pi(-\vec{k})$  states: = 41.9 (4.9) MeV
- Including  $N(\vec{k})\pi(-\vec{k})$  and  $N(0)\pi(\vec{k})\pi(-\vec{k})$  states: = 59.6 (7.4) MeV

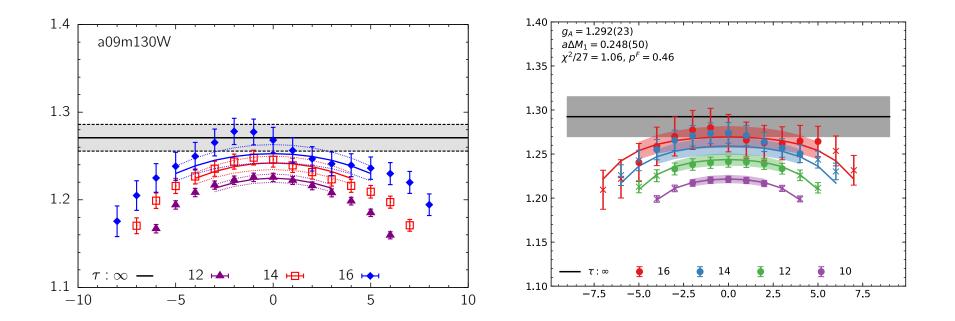
See talk by M. Hoferichter

# Implication for BSM

- Whether  $\sigma_{\pi N} \equiv m_{ud} g_S^{u+d}$  is  $\approx 40$  MeV or 60 MeV comes from whether  $g_S^{u+d}$  is 12 or 18
- This factor of 1.5 in coupling translates to 2.25 in cross-section for the favored scalar channel, and thus the reach of the dark matter direct detection experiments
- Enters in the analysis of  $\mu \rightarrow e$  conversion
- $\sigma_{\pi N}$  is a fundamental parameter in nuclear physics

## Future

- Brute force: increase statistics to get to larger  $\tau$ 
  - Will 5X in statistics yield data-driven fits that resolve excited state contributions?
- Variational basis of interpolating operators including  $N\pi$  to get results from smaller  $\tau$

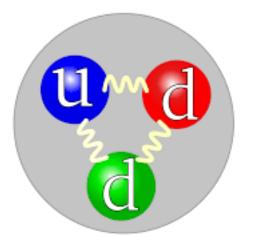


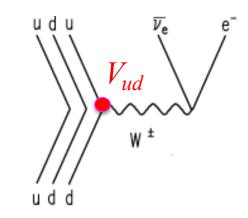
## The neutron is a clean but challenging system

Decays weakly  $\Rightarrow$  a stable bound state of QCD

Properties:

- Charges  $g_A$ ,  $g_P$ ,  $g_S$ ,  $g_T$ ,  $g_V$
- Spin content
  - Quark contribution
  - Gluon contribution
- Contributions to nEDM
- Form factors
  - Electric, Magnetic
  - Axial
- Distribution functions, moments
  - PDF
  - GPD
- Radiative corrections to n-decay  $\rightarrow V_{ud}$





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