

Is there a “hyperon puzzle” problem in neutron star study?

Ang LI 李昂

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Xiamen Univ.

Many thanks to
Organizers!

XVIth Quark Confinement and the Hadron Spectrum Conference
19–24 Aug 2024 Cairns, Queensland, Australia

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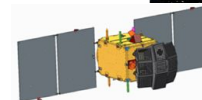
XVIth Quark Confinement and the Hadron Spectrum Conference
19–24 Aug 2024 Cairns, Queensland, Australia



Electromagnetic waves



Insight/
HXMT



Einstein
Probe



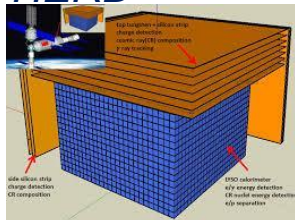
Neutrinos

JUNO

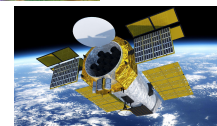


Cosmic Rays

HERD



HUBS



eXTP

web: <https://astro.xmu.edu.cn/>

Our group: Welcome to visit!

[arXiv:2402.02799](https://arxiv.org/abs/2402.02799) PRD
[arXiv:2312.17102](https://arxiv.org/abs/2312.17102) ApJ
[arXiv:2312.12185](https://arxiv.org/abs/2312.12185) ApJ
[arXiv:2312.04305](https://arxiv.org/abs/2312.04305) MNRAS
[arXiv:2305.16058](https://arxiv.org/abs/2305.16058) PRC
[arXiv:2305.08401](https://arxiv.org/abs/2305.08401) ApJ
[arXiv:2304.12050](https://arxiv.org/abs/2304.12050) PRD
[arXiv:2211.04978](https://arxiv.org/abs/2211.04978) PRD
[arXiv:2211.02007](https://arxiv.org/abs/2211.02007) ApJ
[arXiv:2205.10631](https://arxiv.org/abs/2205.10631) ApJ
[arXiv:2204.05560](https://arxiv.org/abs/2204.05560) ApJ
[arXiv:2203.04798](https://arxiv.org/abs/2203.04798) PRD
[arXiv:2201.12053](https://arxiv.org/abs/2201.12053) PRC
[arXiv:2108.00560](https://arxiv.org/abs/2108.00560) ApJ
[arXiv:2107.13997](https://arxiv.org/abs/2107.13997) ApJL
[arXiv:2107.07979](https://arxiv.org/abs/2107.07979) MNRAS
[arXiv:2103.15119](https://arxiv.org/abs/2103.15119) ApJ
[arXiv:2011.11934](https://arxiv.org/abs/2011.11934) ApJ
[arXiv:2009.12571](https://arxiv.org/abs/2009.12571) MNRAS
[arXiv:2007.05116](https://arxiv.org/abs/2007.05116) JHEAp (review)
[arXiv:2006.00839](https://arxiv.org/abs/2006.00839) ApJ
[arXiv:2005.12875](https://arxiv.org/abs/2005.12875) ApJS
[arXiv:2005.02677](https://arxiv.org/abs/2005.02677) PRD
[arXiv:2001.03859](https://arxiv.org/abs/2001.03859) PRC



Wenli Yuan 苑文莉



Quark matter;
QCD phase diagram

**Graduated in 2023;
postdoc in PKU**

Zhenyu Zhu 朱镇宇



Many-body theory;
Merger simulation
Numerical relativity

**Graduated in 2021;
postdoc in CCRG-RIT**

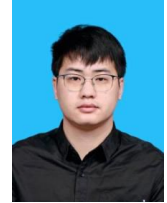
Zhiqiang Miao 缪志强



Hybrid star;
Quark matter;
Bayesian analysis

GR
**Graduated in 2023;
postdoc in TDLee inst.**

Zhonghao Tu 涂中豪



Superfluidity;
Neutron star cooling;
Nuclear pinning force

Peng Liu 刘鹏



Glitch;
Pulsar observation

Xiangdong Sun 孙向东



Nuclear matter;
Hyperon matter;
Many-body theory

Shuochong Han 韩烁冲

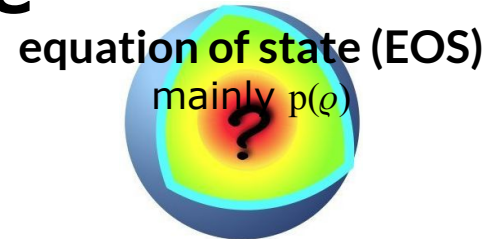


Many-body theory;
Nuclear transport

with 4 undergraduate students

Outline

- **Basic** for neutron star structure and the EOS
- **Recent work** towards the determination of the #(hyper)nuclear force and NS properties from multimessenger astronomy
- **Summary and Exciting future**



What is the nature of the particles that make up neutron stars?



Lev Landau



James Chadwick



Walter Baade



Fritz Zwicky



J. Robert Oppenheimer



Antony Hewish



Dame Jocelyn Bell Burnell

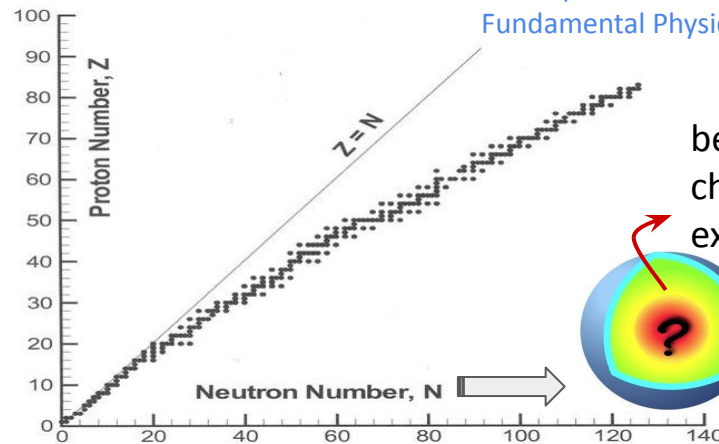
1932-

“the density of matter becomes so great that atomic nuclei come in close contact, forming one gigantic nucleus.”

$A \sim 10^{57}$; For $R=10$ km, $M=1.4 M_{\odot}$,
average density $\sim(2-3)$ nuclear density ρ_0

\sim several hundreds MeV (nonperturbative)

Extreme conditions make it impossible to attain by theo./exp. methods only.



Nobel prize 1974
Fundamental Physics Breakthrough Prize 2018

beta equilibrium;
charge neutrality;
extremely neutron-rich

EOS uncertainty from QCD phase uncertainty and model uncertainty

- **Hyperon puzzle**; $\Delta(1232)$ /hyperon/Kaon/quark complication
- 1) Unified crust-core; 2) High-density extrapolation

Hyperon puzzle: Heavy pulsars larger than $2M_{\odot}$ is a pain

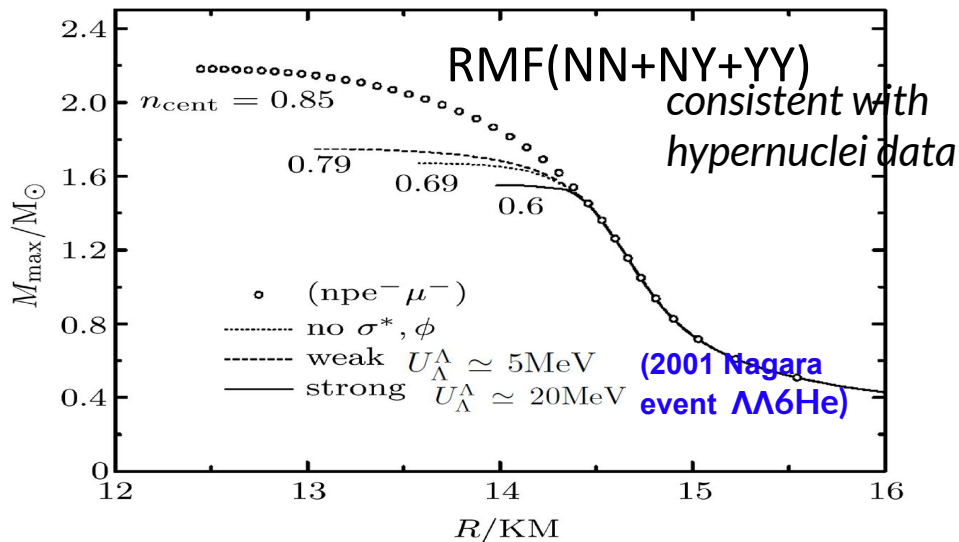
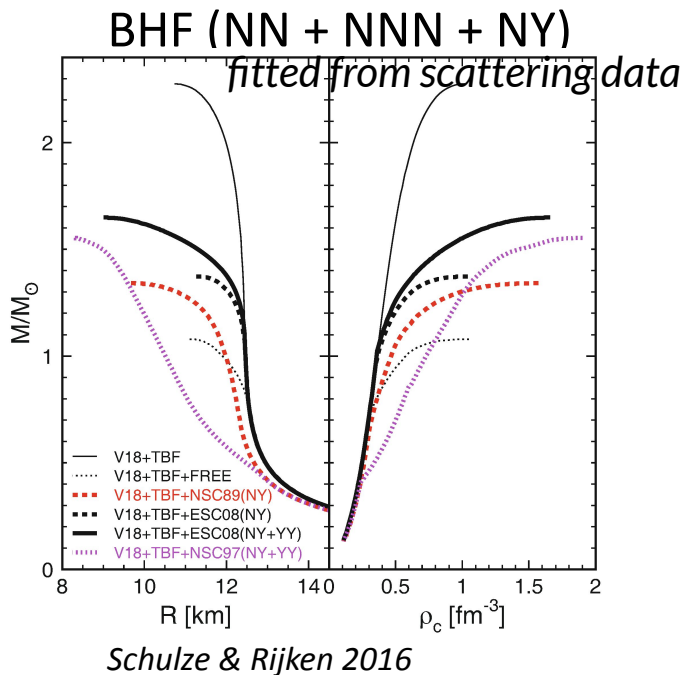


Fig.3. The mass–radius relation calculated for the strong and weak hyperon–hyperon interaction models, in comparison with the one without strange mesons (σ^* , ϕ), and also the results without hyperons. See text for details. *Li et al. 2007*

Is it possible to combine NS multi-messenger (2017-) observations with hypernuclei experiments to understand better the hypernuclear force? **How? What new?**



Astrophysical Implications on Hyperon Couplings and Hyperon Star Properties with Relativistic Equations of States

Xiangdong Sun¹ , Zhiqiang Miao¹ , Baoyuan Sun² , and Ang Li¹ 

¹Department of Astronomy, Xiamen University, Xiamen, Fujian 361005, People's Republic of China; liang@xmu.edu.cn

²Frontiers Science Center for Rare Isotopes, Lanzhou University, Lanzhou 730000, People's Republic of China

From Referee “The present article **addresses a long-standing issue** in neutron star physics, namely the hyperon puzzle. The authors **incorporate new information** from hypernuclei calculations and **treat the hyperon couplings in a more general way** than what exists in the present literature. This is an **interesting work that can have important future implications.**”

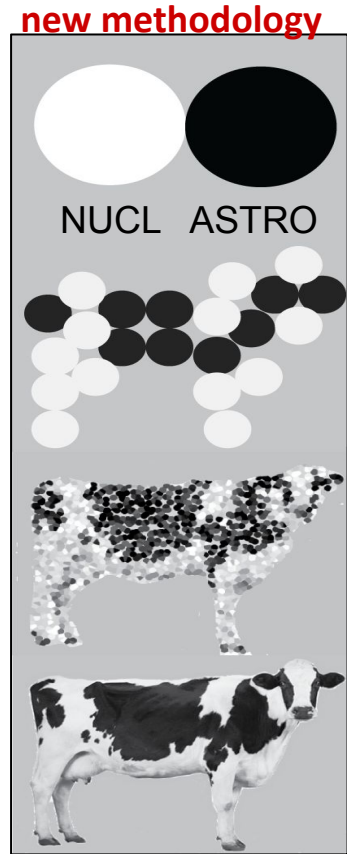
an RMF with density dependent couplings. The authors of Sun et al. (2023) have recently developed a Bayesian inference approach, in the framework of several nuclear RMF, to determine how GW and NICER measurements constrain the $\Lambda - \sigma$ and $\Lambda - \omega$ couplings, while fixing the Σ and Ξ couplings to reasonable values. A major advantage of this methodology is the possibility, once the inference is completed, to discuss the possible composition of matter or the nuclear properties. In the present study, we will base our approach

A major advantage of this methodology is the possibility, once the inference is completed, to discuss the possible composition of matter or the nuclear properties.

Huang, Raaijmakers, Watts,
Tolos, & Providência, 2303.17518
MNRAS

Outline

- **Basic** for neutron star structure and the EOS
- **Recent work** towards the determination of the **#hypernuclear** force and NS properties from multimessenger astronomy
- **Summary and Exciting future**



Combining (binary) NS observations with hypernuclei experiments

$$p(\theta, D) \propto \pi(\theta) \times L(D|\theta, \mathbb{M})$$

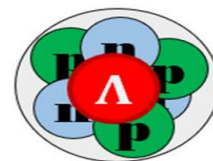
Assuming the sources are hyperon stars:

Formerly:
GW + X-ray



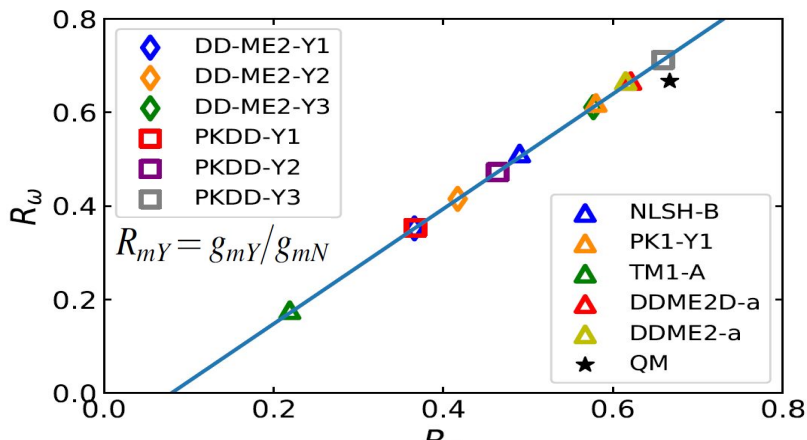
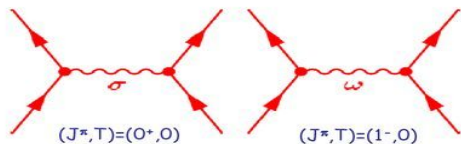
Presently: GW + X-ray + NUCL

$$\mathcal{L}_{\text{NUCL}}(d_{\text{NUCL}}|\theta_{\text{EOS}}) \propto \exp \left[-\frac{1}{2} \frac{(R_{\sigma\Lambda} - \bar{R}_{\sigma\Lambda})^2}{\sigma_{R_{\sigma\Lambda}}^2} \right]$$



Strong linear $R_{\sigma\Lambda}$ - $R_{\omega\Lambda}$ relations from fitting (with some statistical error) calculated Λ separation energies of **eleven** $A \geq 12$ single Λ hypernuclei

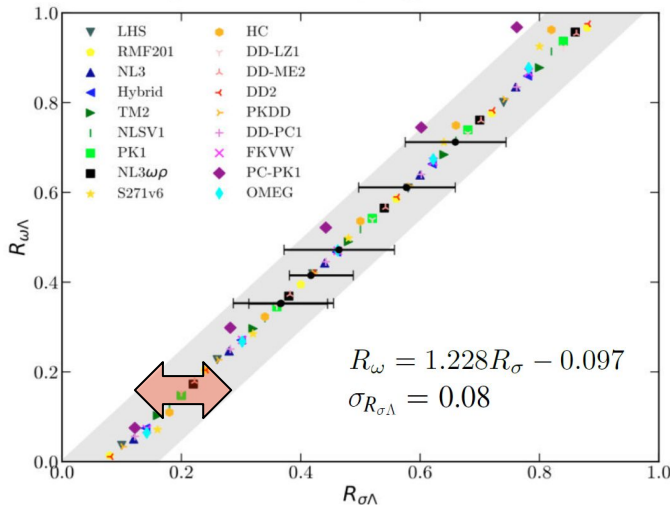
(Rong, Tu & Zhou, 2021): $R_{\omega} = 1.228R_{\sigma} - 0.097$



Hypernuclei	Exp.
$^{12}_{\Lambda}\text{C}$	11.36 ± 0.20
$^{13}_{\Lambda}\text{C}$	12.0 ± 0.2
$^{16}_{\Lambda}\text{O}$	13.0 ± 0.2
$^{28}_{\Lambda}\text{Si}$	17.2 ± 0.2
$^{32}_{\Lambda}\text{S}$	17.5 ± 0.5
$^{40}_{\Lambda}\text{Ca}$	18.7 ± 1.1
$^{51}_{\Lambda}\text{V}$	21.5 ± 0.6
$^{52}_{\Lambda}\text{V}$	21.8 ± 0.3
$^{89}_{\Lambda}\text{Y}$	23.6 ± 0.5
$^{139}_{\Lambda}\text{La}$	25.1 ± 1.2
$^{208}_{\Lambda}\text{Pb}$	26.9 ± 0.8

Linear $R_{\sigma\Lambda}$ - $R_{\omega\Lambda}$ relations consistent with both finite-range meson-exchange and zero-range PC models

$$U_N = -70 \text{ MeV}, U_\Lambda = -30 \text{ MeV}$$



- Meson-exchange

$$\mathcal{L} = \mathcal{L}_{\text{free}}^B + \mathcal{L}_{\text{int}}^B + \mathcal{L}_m + \mathcal{L}_{\text{NL}}$$

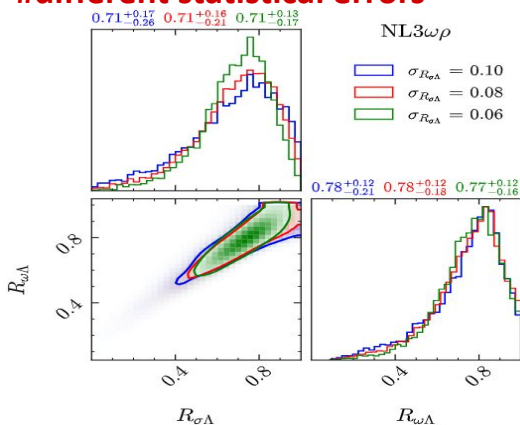
$$\begin{aligned} \mathcal{L}_{\text{free}}^B &= \sum_B \bar{\psi}_B [i\gamma_\mu \partial^\mu - m_B] \psi_B \\ \mathcal{L}_{\text{int}}^B &= \sum_B \bar{\psi}_B [-g_{\sigma B} \sigma - g_{\omega B} \gamma_\mu \omega^\mu - g_{\rho B} \gamma_\mu \vec{\rho}^\mu \cdot \vec{\tau}] \psi_B \\ \mathcal{L}_m &= -\frac{1}{2} m_\sigma^2 \sigma^2 + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu + \frac{1}{2} m_\rho^2 \vec{\rho}_\mu \cdot \vec{\rho}^\mu \\ &\quad + \frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma - \frac{1}{4} \Omega_{\mu\nu} \Omega^{\mu\nu} - \frac{1}{4} \vec{R}_{\mu\nu} \cdot \vec{R}^{\mu\nu} \\ \mathcal{L}_{\text{NL}} &= -\frac{1}{3} g_2 \sigma^3 - \frac{1}{4} g_3 \sigma^4 + \frac{1}{4} c_3 (\omega_\mu \omega^\mu)^2 \\ &\quad + \Lambda_V (g_{\omega B}^2 \omega_\mu \omega^\mu) (g_{\rho B}^2 \rho_\mu \rho^\mu); \end{aligned}$$

- Point-coupling

$$\mathcal{L}_{\text{PC}} = \mathcal{L}_{\text{free}}^B + \mathcal{L}_{4f}^B + \mathcal{L}_{\text{hot}}^B$$

$$\begin{aligned} \mathcal{L}_{\text{free}}^B &= \sum_B \bar{\psi}_B [i\gamma_\mu \partial^\mu - m_B] \psi_B \\ \mathcal{L}_{4f}^B &= -\frac{1}{2} \sum_B \alpha_S^{NB}(\rho) (\bar{\psi}_N \psi_N) (\bar{\psi}_B \psi_B) \\ &\quad - \frac{1}{2} \sum_B \alpha_V^{NB}(\rho) (\bar{\psi}_N \gamma_\mu \psi_N) (\bar{\psi}_B \gamma_\mu \psi_B) \\ &\quad - \frac{1}{2} \sum_B \alpha_{TS}^{NB}(\rho) (\bar{\psi}_N \vec{\tau} \psi_N) (\bar{\psi}_B \vec{\tau} \psi_B) \\ &\quad - \frac{1}{2} \sum_B \alpha_{TV}^{NB}(\rho) (\bar{\psi}_N \vec{\tau} \gamma_\mu \psi_N) (\bar{\psi}_B \vec{\tau} \gamma_\mu \psi_B) \\ \mathcal{L}_{\text{hot}}^B &= -\frac{1}{3} \beta_S^{NN} (\bar{\psi}_N \psi_N)^3 - \frac{1}{4} \gamma_S^{NN} (\bar{\psi}_N \psi_N)^4 \\ &\quad - \frac{1}{4} \gamma_V^{NN} [(\bar{\psi}_N \gamma_\mu \psi_N)] [(\bar{\psi}_N \gamma^\mu \psi_N)]^2, \end{aligned}$$

#different statistical errors



For finite-range interactions:

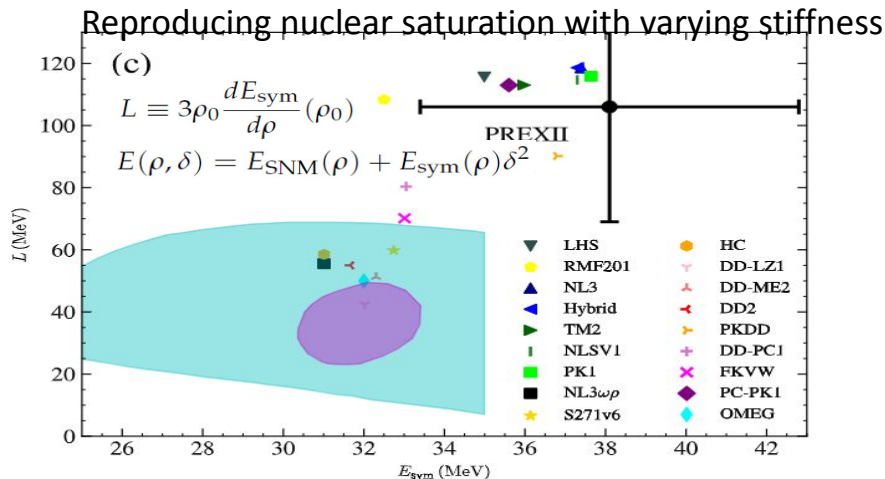
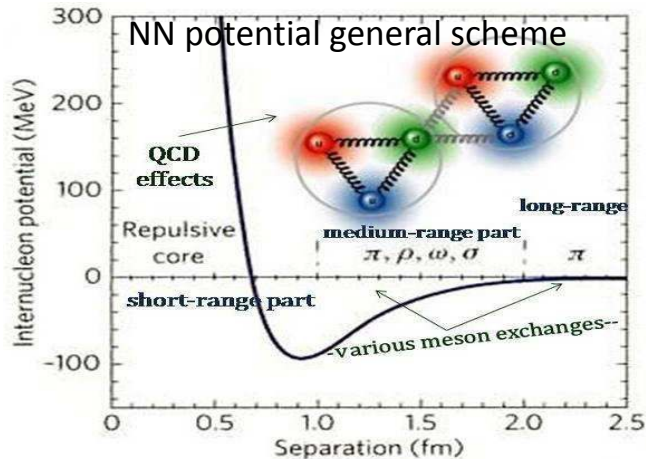
$$R_{\omega\Lambda} \approx \frac{-g_{\sigma N} \sigma}{U_N - g_{\sigma N} \sigma} R_{\sigma\Lambda} + \frac{U_\Lambda}{U_N - g_{\sigma N} \sigma}$$

For zero-range PC

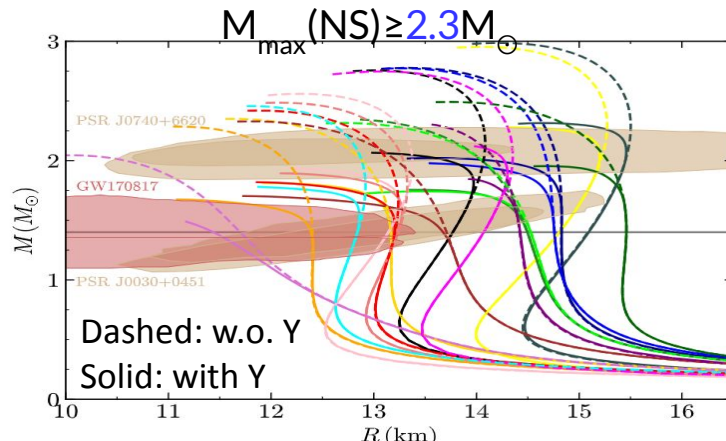
$$\begin{aligned} R_{\omega\Lambda} &\approx \frac{-\alpha_S^{NN} \rho_S}{U_N - \alpha_S^{NN} \rho_S - \beta_S^{NN} \rho_S^2 - \gamma_S^{NN} \rho_S^3 - \gamma_V^{NN} \rho_V^3} R_{\sigma\Lambda} \\ &\quad + \frac{U_\Lambda}{U_N - \alpha_S^{NN} \rho_S - \beta_S^{NN} \rho_S^2 - \gamma_S^{NN} \rho_S^3 - \gamma_V^{NN} \rho_V^3}. \end{aligned}$$

Hyperon star properties do NOT rely sensitively on the choice of the statistical error.

Employed 18 stiff relativistic EOSs with 7 types of variation of the RMF effective interactions

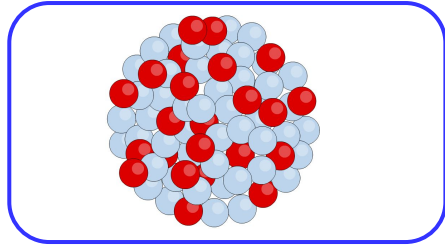


- 1) Original linear Walecka model,
- 2) Nonlinear Walecka model with σ **self-interacting** mesons
- 3) Nonlinear Walecka model with σ, ω **self-interacting** mesons,
- 4) Nonlinear Walecka model with σ, ω **self-interacting** mesons and possible mesonic **cross** terms,
- 5) Models in which the parameters that couple the baryons with the mesons are **density-dependent**,
- 6) Models with the inclusion of δ mesons, i.e., $a_0(980)$,
- 7) **Point-coupling (PC)** models without exchanging mesons.



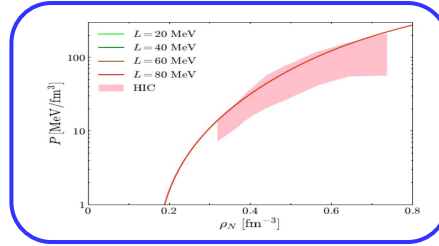
Prepare EoS prior starting for a RMF parameter set

1. Model for interaction between particles



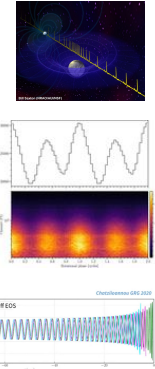
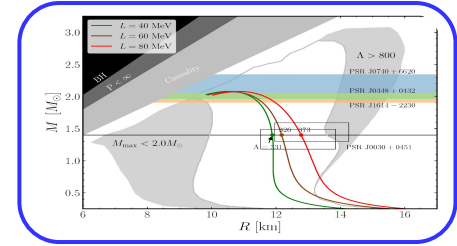
$$\hat{H}\Psi = E\Psi$$

2. the EOS



$$G_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

3. NS observations (M-R relation, Lambda)



(P, I, J symmetry)

$$\mathcal{L} = \bar{\psi} (i\gamma_\mu \partial^\mu - M_N^* - g_{\omega N} \omega \gamma^0 - g_{\rho N} \rho \tau_3 \gamma^0) \psi - \frac{1}{2} (\nabla \sigma)^2 - \frac{1}{2} m_\sigma^2 \sigma^2 - \frac{1}{3} g_2 \sigma^3 - \frac{1}{4} g_3 \sigma^4 + \frac{1}{2} (\nabla \rho)^2 + \frac{1}{2} m_\rho^2 \rho^2 + \frac{1}{2} (\nabla \omega)^2 + \frac{1}{2} m_\omega^2 \omega^2 + \frac{1}{2} g_{\rho N}^2 \rho^2 \Lambda_v g_{\omega N}^2 \omega^2,$$

Eqs. of motion of baryons and mesons can be generated by the Euler-Lagrangian eq. from the Lagrangian:

$$\begin{aligned} \left[i\gamma^\mu \partial_\mu - M_B^* - \gamma^0 \left(g_{\omega B} \omega + g_{\phi B} \phi + \frac{g_{\rho B}}{2} \rho \tau_3 \right) \right] \psi_B &= 0, \\ m_\sigma^2 \sigma + g_2 \sigma^2 + g_3 \sigma^3 &= \sum_B g_{\sigma B} \rho_B^s, \\ m_\omega^2 \omega + c_3 \omega^3 + 2\Lambda_v (g_{\omega N}^2 \omega) (g_{\rho N}^2 \rho^2) &= \sum_B g_{\omega B} \rho_B^v, \\ m_\rho^2 \rho + 2\Lambda_v (g_{\omega N}^2 \omega^2) (g_{\rho N}^2 \rho) &= \sum_B \frac{g_{\rho B}}{2} \rho_B^v, \end{aligned}$$

Then, \mathbf{p} & $\boldsymbol{\varepsilon}$ (with arbitrary isospin asymmetry) from nuclear part can be generated by the energy-momentum tensor.

Static approximation considered in the Lagrangian on mesons so that their time components are neglected;

Spatial part of $\boldsymbol{\omega}$ meson disappears for the **time reversal symmetry**;

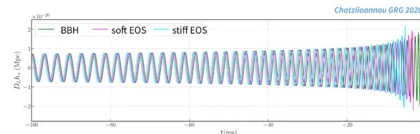
Infinite nuclear matter has **translational invariance**, removing the partial part of the coordinate space.

Bayesian inference of hyperon-nucleon interaction strengths from combining (binary) NS observations with hypernuclei experiments

- Finite size effects of the merging star alter late inspiral GW signal:

$$\mathcal{L}_{\text{GW}}(d_{\text{GW}}|\boldsymbol{\theta}_{\text{GW}}, \mathbb{M}) \propto \exp \left[-2 \int_0^\infty \frac{|\tilde{d}(f) - \tilde{h}(f, \boldsymbol{\theta}_{\text{GW}})|^2}{S_n(f)} df \right],$$

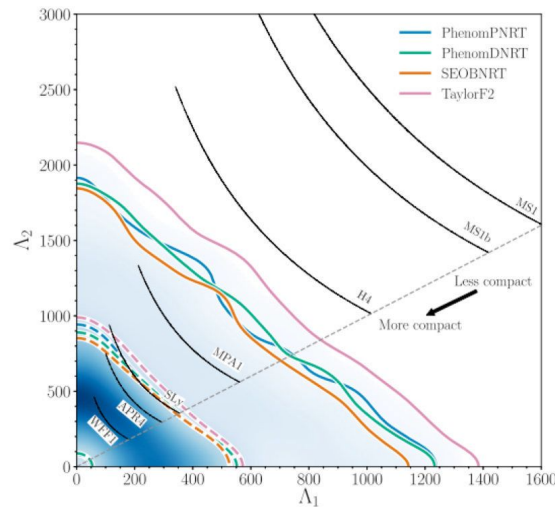
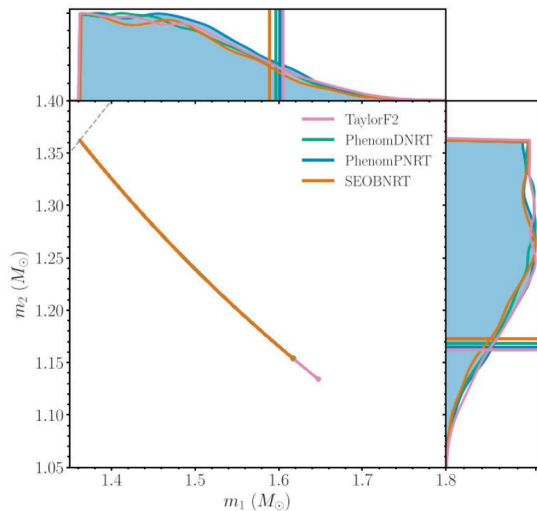
$$\boldsymbol{\theta}_{\text{GW}} = \{M_1, M_2, \Lambda_1, \Lambda_2, \chi_{1z}, \chi_{2z}, \varphi, \Psi, \theta_{\text{jn}}, t_c, d_L, \text{R.A.}, \text{Decl.}\}$$



waveform depending on 17(4) parameters



$(1.36, 1.60) M_\odot$
 $(1.16, 1.36) M_\odot$



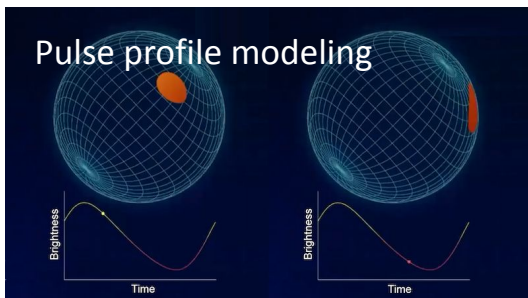
$$Q_{ij} = -\Lambda(\text{EOS}, m) m^5 \varepsilon_{ij}$$

Bayesian inference of hyperon-nucleon interaction strengths from combining (binary) NS observations with hypernuclei experiments

- $\mathcal{L}_{\text{NICER}}(M, R | \theta_{\text{EOS}} \cup \{\varepsilon_c\}, \mathbb{M}) = P_{\text{KDE}}(M(\theta_{\text{EOS}}; \varepsilon_c), R(\theta_{\text{EOS}}; \varepsilon_c)),$

Kernel density

Trace rays from hot spots on NS surface: estimation



PSR J0030+0451

Miller et al, ApJL, 2019

$$M = 1.44^{+0.15}_{-0.14} M_{\odot} \quad R = 13.02^{+1.24}_{-1.06} \text{ km}$$

Riley et al, ApJL, 2019

$$M = 1.34^{+0.15}_{-0.16} M_{\odot} \quad R = 12.71^{+1.14}_{-1.19} \text{ km}$$

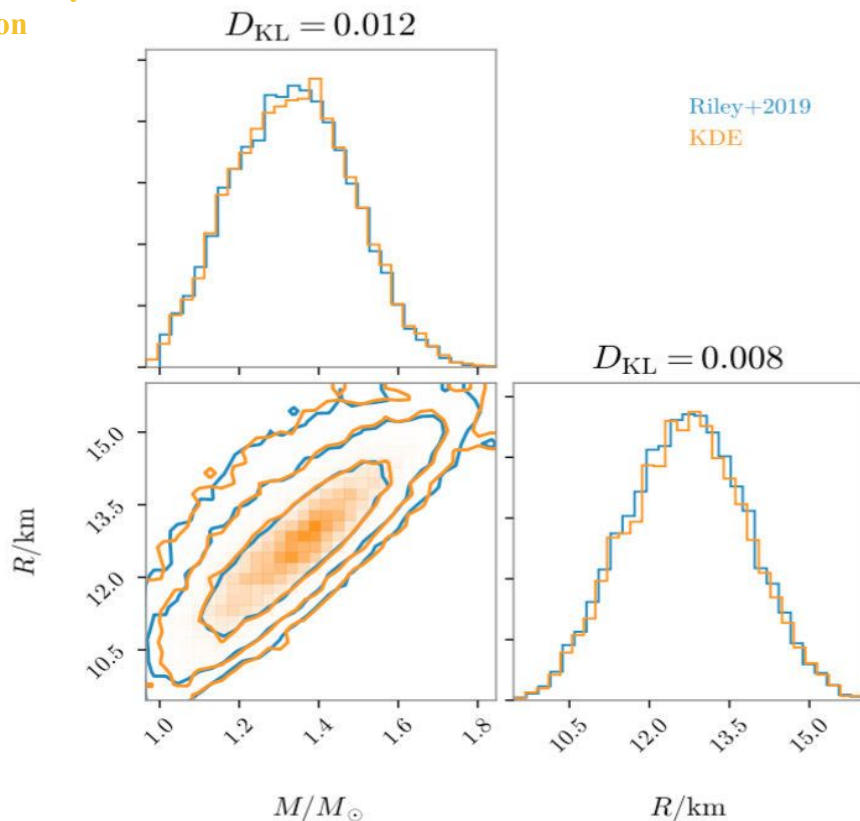
PSR J0740+6620

Miller et al, ApJL, 2021

$$M = 2.062^{+0.090}_{-0.091} M_{\odot} \quad R = 13.71^{+2.61}_{-1.50} \text{ km}$$

Riley et al, ApJL, 2021

$$M = 2.072^{+0.067}_{-0.066} M_{\odot} \quad R = 12.39^{+1.30}_{-0.98} \text{ km}$$



Bayesian inference of #hyperon-nucleon interaction strengths from combining (binary) NS observations with hypernuclei experiments

Likelihood Prior

$$p(\boldsymbol{\theta} | D, \mathbb{M}) = \frac{\mathcal{L}(D | \boldsymbol{\theta}, \mathbb{M}) \pi(\boldsymbol{\theta})}{\int p(D | \boldsymbol{\theta}, \mathbb{M}) \pi(\boldsymbol{\theta}) d\boldsymbol{\theta}}$$

Posterior

Parameter Data Model

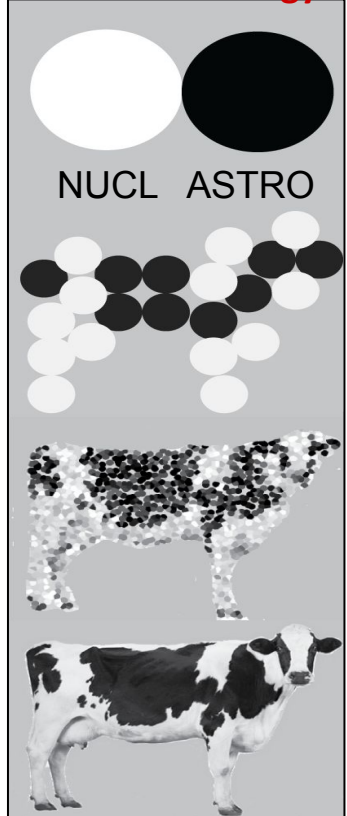
Likelihood

- $\mathcal{L}_{\text{NUCL}}(d_{\text{NUCL}} | \boldsymbol{\theta}_{\text{EOS}}) \propto \exp \left[-\frac{1}{2} \frac{(R_{\sigma\Lambda} - \bar{R}_{\sigma\Lambda})^2}{\sigma_{R_{\sigma\Lambda}}^2} \right]$
- $\mathcal{L}_{\text{GW}}(d_{\text{GW}} | \boldsymbol{\theta}_{\text{GW}}, \mathbb{M}) \propto \exp \left[-2 \int_0^\infty \frac{|\tilde{d}(f) - \tilde{h}(f, \boldsymbol{\theta}_{\text{GW}})|^2}{S_n(f)} df \right],$
- $\mathcal{L}_{\text{NICER}}(M, R | \boldsymbol{\theta}_{\text{EOS}} \cup \{\varepsilon_c\}, \mathbb{M}) = P_{\text{KDE}}(M(\boldsymbol{\theta}_{\text{EOS}}; \varepsilon_c), R(\boldsymbol{\theta}_{\text{EOS}}; \varepsilon_c)),$

Software:

- Bilby** (Ashton et al. 2019, version 0.5.5, <https://git.ligo.org/lscsoft/bilby/>),
- PyMultiNest** (Buchner 2016, version 2.6, <https://github.com/JohannesBuchner/PyMultiNest>),
- Toast** (Hernandez Vivanco et al. 2020, <https://git.ligo.org/francisco.hernandez/toast>),
- Corner** (Foreman-Mackey 2016, <https://github.com/dfm/corner.py>).

new methodology



Span uncertainty in YN interaction

#parameters and priors

$$\theta_{\text{EOS}} = \{R_{\sigma\Lambda}, R_{\omega\Lambda}\}$$

$$R_{\sigma\Lambda} \sim U[0, 1]$$

and $R_{\omega\Lambda} \sim U[0, 1]$

- ONLY explore the couplings of Λ hyperons;
- Keep Σ, Ξ hyperon couplings fixed to their empirical values or based on SU(3) symmetry.

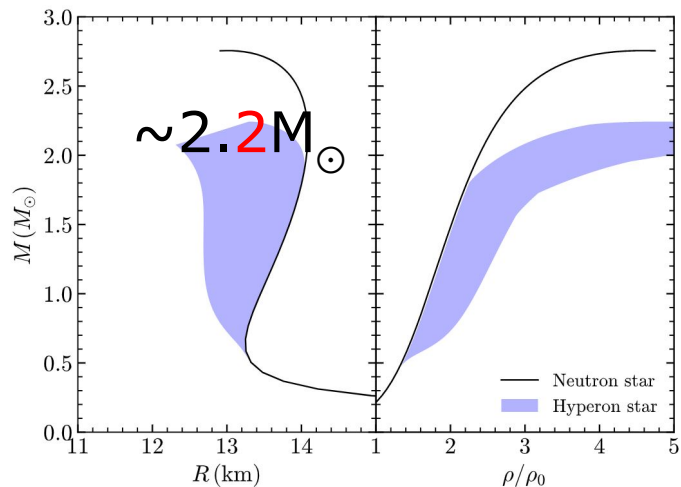
#posteriors

Most Probable Intervals of $R_{\sigma\Lambda}$ and $R_{\omega\Lambda}$ (68% Credible Intervals)

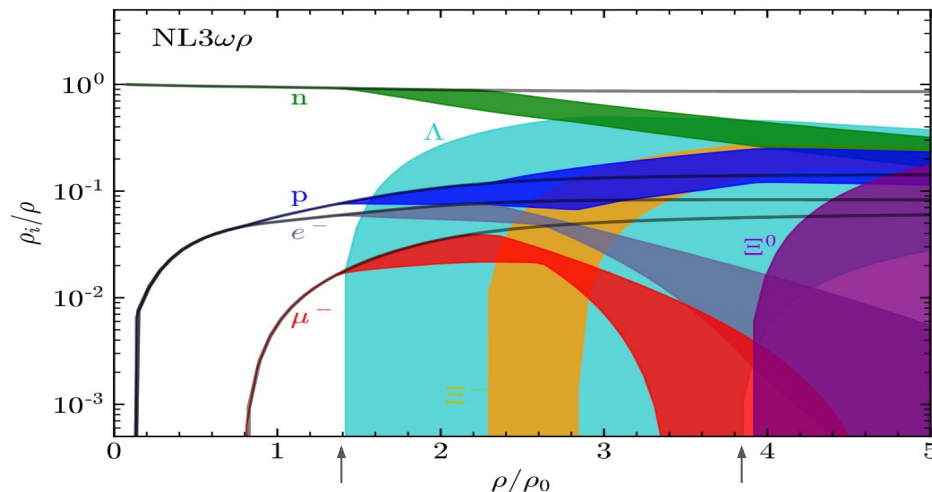
EOS	+NICER		+NICER +NUCL		+NICER +GW170817		+NICER +GW170817 +NUCL	
	$R_{\sigma\Lambda}$	$R_{\omega\Lambda}$	$R_{\sigma\Lambda}$	$R_{\omega\Lambda}$	$R_{\sigma\Lambda}$	$R_{\omega\Lambda}$	$R_{\sigma\Lambda}$	$R_{\omega\Lambda}$
LHS	0.821 ^{+0.125} _{-0.463}	0.755 ^{+0.073} _{-0.155}	0.865 ^{+0.074} _{-0.208}	0.658 ^{+0.130} _{-0.194}	0.941 ^{+0.035} _{-0.048}	0.763 ^{+0.034} _{-0.028}	0.658 ^{+0.163} _{-0.251}	0.752 ^{+0.049} _{-0.095}
RMF201	0.760 ^{+0.186} _{-0.520}	0.759 ^{+0.081} _{-0.224}	0.658 ^{+0.172} _{-0.249}	0.672 ^{+0.138} _{-0.056}	0.949 ^{+0.032} _{-0.028}	0.769 ^{+0.035} _{-0.028}	0.842 ^{+0.090} _{-0.250}	0.754 ^{+0.061} _{-0.136}
NL3	0.424 ^{+0.330} _{-0.293}	0.746 ^{+0.156} _{-0.261}	0.681 ^{+0.171} _{-0.247}	0.768 ^{+0.136} _{-0.214}	0.399 ^{+0.379} _{-0.291}	0.794 ^{+0.128} _{-0.216}	0.765 ^{+0.130} _{-0.191}	0.840 ^{+0.101} _{-0.163}
Hybrid	0.363 ^{+0.381} _{-0.265}	0.807 ^{+0.132} _{-0.276}	0.750 ^{+0.130} _{-0.179}	0.865 ^{+0.096} _{-0.157}	0.305 ^{+0.388} _{-0.217}	0.764 ^{+0.143} _{-0.254}	0.777 ^{+0.118} _{-0.181}	0.869 ^{+0.090} _{-0.147}
TM2	0.311 ^{+0.330} _{-0.221}	0.751 ^{+0.179} _{-0.494}	0.736 ^{+0.145} _{-0.201}	0.856 ^{+0.102} _{-0.193}	0.323 ^{+0.487} _{-0.237}	0.784 ^{+0.158} _{-0.300}	0.772 ^{+0.137} _{-0.239}	0.870 ^{+0.086} _{-0.204}
NLSV1	0.252 ^{+0.285} _{-0.183}	0.756 ^{+0.167} _{-0.281}	0.688 ^{+0.117} _{-0.227}	0.863 ^{+0.100} _{-0.199}	0.247 ^{+0.279} _{-0.177}	0.744 ^{+0.182} _{-0.259}	0.689 ^{+0.122} _{-0.225}	0.866 ^{+0.100} _{-0.206}
PK1	0.254 ^{+0.273} _{-0.185}	0.756 ^{+0.172} _{-0.250}	0.687 ^{+0.139} _{-0.222}	0.869 ^{+0.099} _{-0.216}	0.248 ^{+0.271} _{-0.170}	0.754 ^{+0.176} _{-0.247}	0.683 ^{+0.130} _{-0.220}	0.867 ^{+0.101} _{-0.222}
NL3 $\omega\rho$	0.384 ^{+0.393} _{-0.280}	0.773 ^{+0.147} _{-0.247}	0.690 ^{+0.163} _{-0.208}	0.759 ^{+0.131} _{-0.176}	0.420 ^{+0.448} _{-0.294}	0.777 ^{+0.127} _{-0.269}	0.712 ^{+0.157} _{-0.215}	0.778 ^{+0.121} _{-0.183}
S271v6	0.287 ^{+0.290} _{-0.207}	0.775 ^{+0.158} _{-0.232}	0.750 ^{+0.105} _{-0.144}	0.886 ^{+0.080} _{-0.128}	0.304 ^{+0.286} _{-0.189}	0.782 ^{+0.157} _{-0.147}	0.740 ^{+0.118} _{-0.161}	0.884 ^{+0.083} _{-0.134}
HC	0.266 ^{+0.253} _{-0.192}	0.517 ^{+0.316} _{-0.370}	0.733 ^{+0.110} _{-0.156}	0.902 ^{+0.070} _{-0.134}	0.266 ^{+0.304} _{-0.189}	0.783 ^{+0.157} _{-0.226}	0.737 ^{+0.106} _{-0.160}	0.902 ^{+0.072} _{-0.134}
DD- LZ1	0.298 ^{+0.321} _{-0.218}	0.775 ^{+0.152} _{-0.251}	0.769 ^{+0.122} _{-0.190}	0.871 ^{+0.083} _{-0.148}	0.327 ^{+0.381} _{-0.223}	0.792 ^{+0.142} _{-0.254}	0.772 ^{+0.128} _{-0.177}	0.870 ^{+0.087} _{-0.139}
DD-ME2	0.275 ^{+0.337} _{-0.192}	0.771 ^{+0.167} _{-0.299}	0.770 ^{+0.120} _{-0.172}	0.885 ^{+0.078} _{-0.137}	0.267 ^{+0.345} _{-0.188}	0.776 ^{+0.160} _{-0.237}	0.767 ^{+0.128} _{-0.168}	0.883 ^{+0.079} _{-0.124}
DD2	0.292 ^{+0.346} _{-0.205}	0.775 ^{+0.163} _{-0.252}	0.783 ^{+0.121} _{-0.173}	0.901 ^{+0.071} _{-0.135}	0.305 ^{+0.392} _{-0.221}	0.785 ^{+0.153} _{-0.276}	0.789 ^{+0.119} _{-0.157}	0.900 ^{+0.069} _{-0.120}
PKDD	0.267 ^{+0.347} _{-0.185}	0.806 ^{+0.140} _{-0.244}	0.820 ^{+0.095} _{-0.153}	0.930 ^{+0.051} _{-0.090}	0.282 ^{+0.420} _{-0.240}	0.813 ^{+0.136} _{-0.147}	0.835 ^{+0.102} _{-0.147}	0.932 ^{+0.047} _{-0.083}
FKVW	0.327 ^{+0.343} _{-0.236}	0.677 ^{+0.217} _{-0.260}	0.647 ^{+0.196} _{-0.250}	0.706 ^{+0.171} _{-0.211}	0.353 ^{+0.356} _{-0.240}	0.696 ^{+0.272} _{-0.203}	0.658 ^{+0.177} _{-0.254}	0.716 ^{+0.158} _{-0.217}
PC-PK1	0.283 ^{+0.310} _{-0.210}	0.701 ^{+0.215} _{-0.134}	0.650 ^{+0.150} _{-0.205}	0.770 ^{+0.147} _{-0.214}	0.282 ^{+0.319} _{-0.211}	0.703 ^{+0.212} _{-0.139}	0.651 ^{+0.148} _{-0.208}	0.771 ^{+0.146} _{-0.215}
OMEG	0.272 ^{+0.298} _{-0.194}	0.778 ^{+0.156} _{-0.244}	0.726 ^{+0.117} _{-0.171}	0.880 ^{+0.089} _{-0.153}	0.273 ^{+0.275} _{-0.188}	0.775 ^{+0.163} _{-0.242}	0.731 ^{+0.119} _{-0.167}	0.889 ^{+0.082} _{-0.152}

Current status of the hypernuclear matter and hyperon star properties due to the uncertain YN interaction

- Taking the NL3 $\omega\rho$ one as an exemplary stiffest one;



2205.10631



Due to hyperons, the maximum mass is lowered by $\sim 20\%$: $M_{\max} = 2.176^{+0.085}_{-0.202} M_{\odot}$ (68% credible interval);

And the stellar radius is smaller above $\sim 0.5 M_{\odot}$ and grows with the stellar mass.

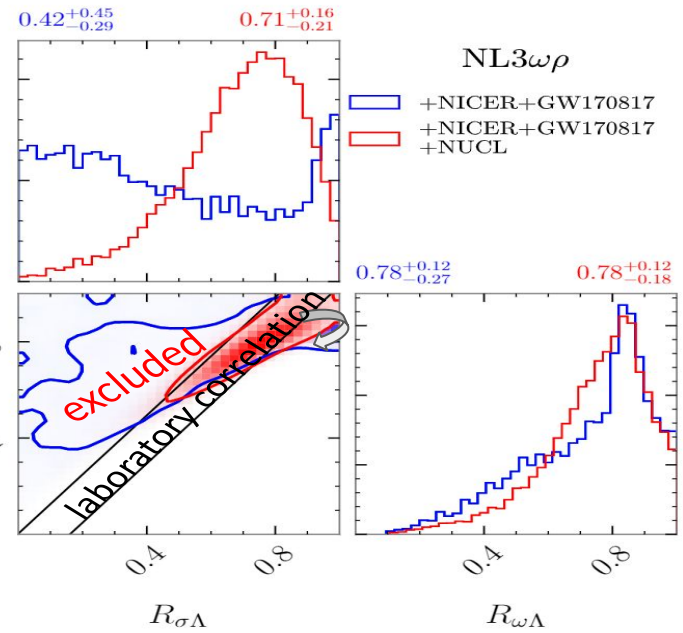
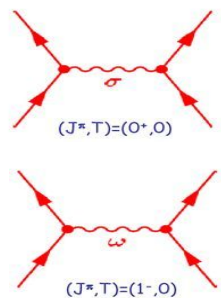
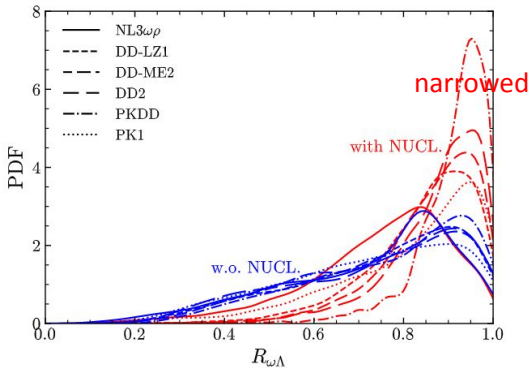
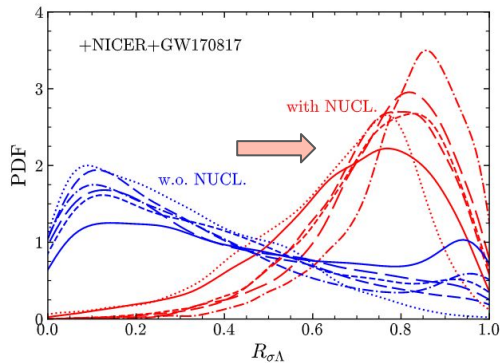
threshold density of Λ hyperons: $1.4\text{--}3.8\rho_0$

Unclear whether Λ or Ξ^- appear first.

future: +a few $\Lambda\Lambda$ hypernuclei, Ξ hypernuclei

Hyperon-nucleon interactions in the relativistic Lagrangian

- Hypernuclei constraint favors large values of $R_{\sigma\Lambda}$ and $R_{\omega\Lambda}$ and disfavors small values of both couplings;
- The addition of astrophysical observational data on top of the laboratory $R_{\sigma\Lambda}$ - $R_{\omega\Lambda}$ correlation rotates the linear correlation **slightly** towards the direction of small values of $R_{\omega\Lambda}$.



No existence of hyperon puzzle?!

Perform Bayesian inference to find the golden EoS (2021-)

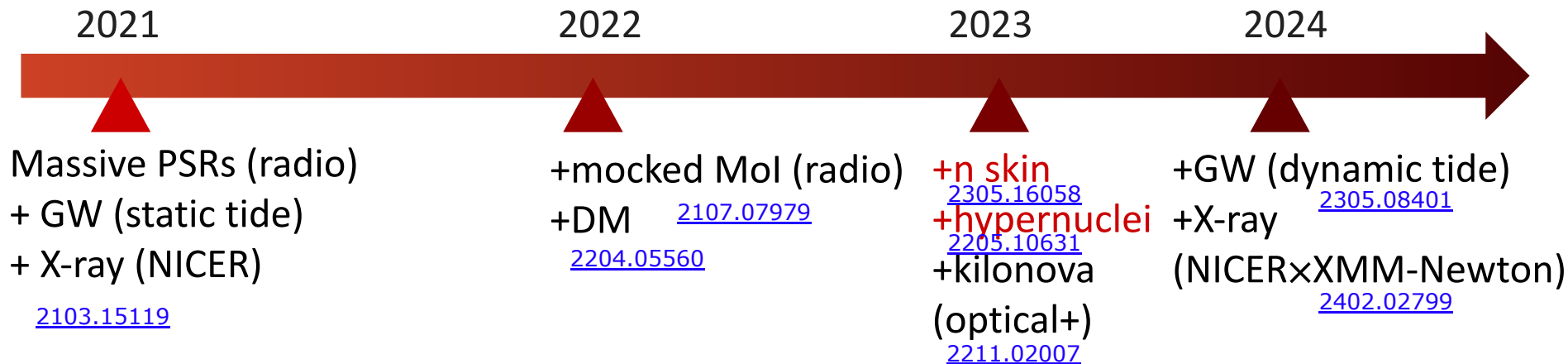
Data:

GW event of GW170817(+GW190425) & **kilonova** light curve of AT2017gfo,

NICERxXMM-Newton's measurement of mass and radius of 2 PSRs,

(Mocked) **SKA**'s moment of inertia measurement on PSR J0737-3039,

Neutron-skin from PREX-II, CREX and the ab initio predictions on ^{208}Pb , ^{48}Ca ;



Black box = EoS microphysics

Procedure used until now

$$\Gamma = (\rho + P)(dP/d\rho)/P$$

- ❑ Piecewise polytrope EoS: Logarithm of the adiabatic index (Γ) of the EoSs are treated as polynomial: **Little to no microphysics;**

Better procedure

- ❑ More physics at the EoS modelling stage;
- ❑ Support quantitative studies of the EoS at **different** density regimes;
- ❑ With prior **explicitly** considering phase transition;
- ❑ Allow for **straightforward** extensions to higher-dimensional models, accommodating the inclusion of additional particles within NSs, even dark matter;
- ❑ **Can discuss the composition of matter and the underlying strong interaction;**
- ❑ Facilitate a **connection** with the ongoing research efforts in the field of relativistic HIC.



Summary and Exciting future

- We incorporate new information from hypernuclei calculations to address a long-standing issue in NS physics;
- We find that the strong correlation between the scalar and vector channel of YN interactions indicated by s.p. separation energy of available Λ hypernuclei **ENSURE** that there is **sufficient (vector) repulsion** and a prediction of hyperon stars with $M_{\max} \sim 2.2M_{\odot}$;
- Comprehensive analysis of multi-messenger, multi-wavelength data ongoing to probe the EOS at **different** density regimes...

Thank you! 🌹

new methodology

