

# Transition magnetic moments of transition in $\Delta \rightarrow p$ in asymmetric nuclear matter

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- 2 Chiral Mean Field Model.
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  - Impact of Medium on Effective Baryon masses.
- 3 Chiral Constituent Quark Model ( $\chi CQM$ ).
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  - Chiral Symmetry Breaking.
  - Success of  $\chi CQM$ .

# QCD : Present theory of strong interactions

- Quantum Chromodynamics (QCD) provides a fundamental description of hadronic and nuclear structure and their dynamics.
- At high energies, ( $\alpha_s$  is small), QCD can be used perturbatively.
- At low energies, ( $\alpha_s$  becomes large), one has to use other methods such as effective Lagrangian models to describe physics.
- Many fundamental questions have not been resolved. **The most challenging non-perturbative problem in QCD is to determine the structure and spectrum of hadrons in terms of their quark and gluon degrees of freedom.**
- Knowledge has been rather limited because of **confinement** and it is still a big challenge to perform the calculations from first principles of QCD.

Electromagnetic Dirac and Pauli form factors: further related to the static low-energy observables

- **Structure** : Magnetic moments predicted by Dirac theory ( $1.0 \mu N$ ) and experiment ( $2.5 \mu N$ ).  
Proton is not an elementary Dirac particle but has an inner structure.
- **Size**: Spatial extension. Proton charge distribution given by charge radius  $r_p$ .
- **Shape**: Non-spherical charge distribution. Quadrupole moment of the transition  $N \rightarrow \Delta$ .
- **Relation between the properties??**

# QCD : Present theory of strong interactions

- Wide range of applications ranging from the dynamics and structure of hadrons and nuclei to the properties and phases of hadronic matter at the earliest stages of the universe.
- New experimental tools are continually being developed to probe the non- perturbative structure of the theory, for example the hard diffractive reactions, semi-inclusive reactions, deeply virtual Compton scattering etc.

# Proton spin Problem : The driving question

- Year 1988, European Muon Collaboration (EMC) discovered that Valence quarks carry 30% of proton spin.
- Naive Quark Model contradicts this results (Based on Pure valence description:  $proton = 2u + d$ ).  
**“Proton spin crisis”**
- Confirmed by the measurements of polarized structure functions of proton in the deep inelastic scattering (DIS) experiments by SMC, E142-3 and HERMES experiments.
- Provides evidence that the valence quarks of proton carry only a small fraction of its spin suggesting that they should be surrounded by an indistinct sea of  $q\bar{q}$  pairs.

- Year 1991, NMC result: Asymmetric nucleon sea ( $\bar{d} > \bar{u}$ ).  
Results confirmed by E866 and HERMES.
- Measured quark sea asymmetry established that the study of the structure of the nucleon is intrinsically a non-perturbative phenomena.
- **Sum Rules :**
  - Bjorken Sum Rule:  $\Delta_3 = \Delta_u - \Delta_d$
  - Ellis-Jaffe Sum Rule:  $\Delta_8 = \Delta_u + \Delta_d - 2\Delta_s$   
(Reduces to  $\Delta_8 = \Delta\Sigma$  when  $\Delta_s = 0$ )
  - Strange quark fraction:  $f_s \simeq 0.10$
  - Gottfried Sum Rule:  $I_G = \frac{1}{3} + \frac{2}{3} \int_0^1 [\bar{u}(x) - \bar{d}(x)] dx = 0.254 \pm 0.026$

- Recently, a wide variety of accurately measured data have been accumulated for
  - **Static properties of hadrons**: masses, electromagnetic moments, charge-radii etc.
  - **Low energy dynamical properties**: scattering lengths and decay rates etc.
- These lie in the non perturbative range of QCD.
- Flavor and spin structure of the nucleon is not limited to  $u$  and  $d$  quarks only.
- Non-perturbative effects explained only through the generation of “quark sea”.



- The direct calculations of these quantities form the first principle of QCD are extremely difficult, because they require non-perturbative methods.
- **Naive Quark Model** is able to provide a intuitive picture and successfully accounts for many of the low-energy properties of the hadrons in terms of the valence quarks.
- **Techniques such as lattice gauge theory, QCD sum rules, and a wide variety of models have been developed to study this extremely interesting energy regime.**

# Importance of studying the properties of hadrons in medium

Studying the medium modifications hadron properties is important

- 1 Understanding the Quark Gluon Plasma's (QGP) characteristics and behavior.
- 2 Understand the nuclear matter under extreme conditions such as neutron stars or during heavy-ion collisions.
- 3 To make QCD predictions under the extreme conditions and guide the experimental search.
- 4 MAMI and Jefferson lab experiments found the signatures of medium modification in Electro-magnetic properties of hadrons.
- 5 KEK-E325, sPrings8 facility, ANKE-COSY collaborations observed the modification in mass and decay width of  $\phi$  meson mass.
- 6 Many theoretical studies like QMC model, **Chiral SU(3) mean field model** etc have been used to study the effective masses and magnetic moments of hadrons.

# Chiral Quark Mean Field Model: Introduction

- Based on consideration of quarks and mesons as degrees of freedom.
- Baryons are formed via the confinement of quarks by an effective potential ( $\mathcal{L}_c$ ).
- The interactions between quarks and mesons ( $\mathcal{L}_{qm}$ ) and scalar & vector meson self interactions ( $\mathcal{L}_{VV}, \mathcal{L}_{\Sigma\Sigma}$ ) are based on  $SU(3)$ .
- Constituent quarks and mesons obtain their masses through spontaneous symmetry breaking ( $\mathcal{L}_{\chi SB}$ ).
- The total effective Lagrangian density in chiral  $SU(3)$  model

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{q0} + \mathcal{L}_{qm} + \mathcal{L}_{VV} + \mathcal{L}_{\Sigma\Sigma} + \mathcal{L}_{\chi SB} + \mathcal{L}_{\Delta m} + \mathcal{L}_c$$

- The term  $\mathcal{L}_{q0}$  represents the free part of mass-less quarks.

# Masses of quarks in Chiral Mean Field Model

- Interactions among quarks are mediated through non-strange scalar-isoscalar field ( $\sigma$ ), strange scalar-isoscalar field ( $\zeta$ ) and scalar-isovector field ( $\delta$ ).
- The vector fields ( $\omega, \rho, \phi$ ) are also incorporated which represent repulsive interactions.
- The in-medium constituent quark mass ( $m_i^*$ ) and effective quark energy ( $e_i^*$ ) are defined in terms of above fields

$$m_q^* = -g_\sigma^q \sigma - g_\zeta^q \zeta - g_\delta^q I^{3q} \delta + m_{q0} \quad (1)$$

$$e_q^* = e_q - g_\omega^q \omega - g_\rho^q I^{3q} \rho - g_\phi^q \phi \quad (2)$$

- Here,  $g^q$  are coupling constants of quarks with respective fields while  $I^{3q}$  is the third component of isotopic spin.
- Parameters of the model are fitted to obtain the binding energy value of -16 MeV at the nuclear saturation density ( $\rho_0 = 0.16 \text{ fm}^{-3}$ ).

# Masses of Baryons in Chiral Mean Field Model

- The in-medium mass of a baryon is expressed in terms of its effective energy  $E_i^*$  and spurious center of mass momentum  $p_{icm}$  as,

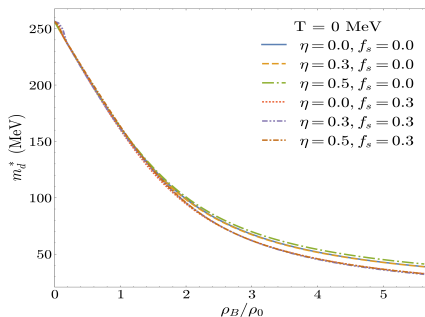
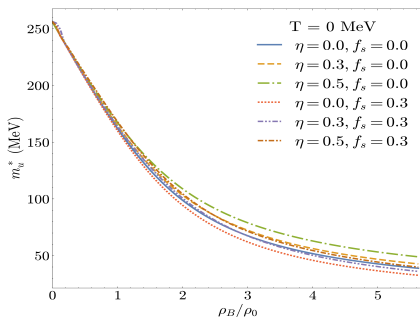
$$M_i^* = \sqrt{E_i^{*2} - \langle p_{icm}^{*2} \rangle}.$$

- $E_i^* = \sum_q n_{qi} e_q^* + E_{ispin}$ : where  $E_{ispin}$  is a correction term in the effective energy of a baryon.
- $\langle p_{icm}^{*2} \rangle = \frac{(11e_q^* + m_q^*)}{6(3e_q^* + m_q^*)} (e_q^{*2} - m_q^{*2})$ ;
- To obtain the density and temperature dependent values of scalar and vector fields, the strange isospin asymmetric thermodynamic potential is minimized with respect to these fields.

$$\frac{\partial \Omega}{\partial \sigma} = \frac{\partial \Omega}{\partial \zeta} = \frac{\partial \Omega}{\partial \delta} = \frac{\partial \Omega}{\partial \omega} = \frac{\partial \Omega}{\partial \rho} = \frac{\partial \Omega}{\partial \phi} = \frac{\partial \Omega}{\partial \chi} = 0$$

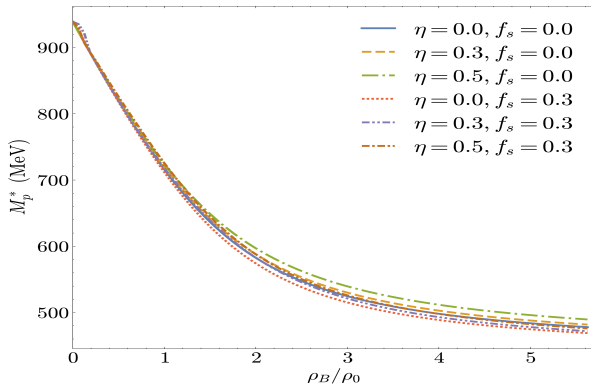
- The above equations are solved for different values of baryonic density ( $\rho_B$ ), temperature, isospin asymmetry ( $\eta$ ) and strangeness fraction ( $f_s$ ) to obtain the values of meson fields and hence the in-medium masses of quarks and baryons.

# In-Medium Masses of Light Quarks



- A decrease in masses is observed with  $\rho_B$  at isospin asymmetry  $\eta = 0$  and strangeness fraction,  $f_s = 0$ .
- At fixed value of  $\rho_B$  and  $\eta$ , there is further decrease in value of mass of light quarks with the increase in strangeness fraction ( $f_s$ ).
- For fixed value of  $\rho_B$  and  $f_s$ , there is an increase in value of mass of light quarks with the increase in isospin asymmetry parameter,  $\eta$ .
- Difference in behavior b/w  $u$ , and  $d$  is attributed to difference in value of third component of isospin appearing in Eq. 1.

# Modification in proton masses



- Using the effective/in-medium quark masses and fitting  $E_{ispin}$  value to vacuum mass of proton, the effective mass of proton ( $M_p^*$ ) is obtained as varying values of  $\rho_B, \eta, f_s$  and T.
- Similar features as discussed for quarks are observed. Values of  $m_u^*, m_d^*$  &  $M_p^*$  are used in the calculations for effective transition magnetic moments

# Chiral Constituent Quark Model

- $\chi$ CQM initiated by Weinberg and developed by Manohar and Georgi to explain the successes of NQM.
- The fluctuation process describing the effective Lagrangian is

$$q \uparrow\downarrow \rightarrow \text{GB} + q' \downarrow\uparrow \rightarrow (q\bar{q}') + q' \downarrow\uparrow$$

$q\bar{q}' + q'$  constitute the sea quarks.

- Incorporates confinement and chiral symmetry breaking.
- “Justifies” the idea of constituent quarks.



# Pion Cloud Mechanism

- Quark sea is believed to originate from process such as virtual pion production.
- It is suggested that in the deep inelastic lepton-nucleon scattering, the lepton probe also scatters off the pion cloud surrounding the target proton. The  $\pi^+(\bar{d}u)$  cloud, dominant in the process  $p \rightarrow \pi^+ n$ , leads to an excess of  $\bar{d}$  sea.
- However, this effect should be significantly reduced by the emissions such as  $p \rightarrow \Delta^{++} + \pi^-$  with  $\pi^-(\bar{u}d)$  cloud. Therefore, the pion cloud idea is not able to explain the significant  $\bar{d} > \bar{u}$  asymmetry.
- This approach can be improved upon by adopting a mechanism which operates in the *interior* of the hadron.

- The effective interaction Lagrangian between GBs and quarks from in the leading order can now be expressed as

$$\mathcal{L}_{\text{int}} = -\frac{g_A}{f_\pi} \bar{\psi} \gamma^\mu \gamma^5 \psi,$$

which using the Dirac equation  $(\gamma^\mu \partial_\mu - m_q)q = 0$  can be reduced to

$$\mathcal{L}_{\text{int}} \approx i \sum_{q=u,d,s} \frac{m_q + m'_q}{f_\pi} \bar{q} \gamma^5 q = i \sum_{q=u,d,s} c_8 \bar{q} \gamma^5 q.$$

- $c_8$  ( $= \frac{m_q + m'_q}{f_\pi}$ ) is the coupling constant for the octet of GBs and  $m_q$  ( $m'_q$ ) is the quark mass parameter.

- The Lagrangian of the quark-GB interaction, suppressing all the space-time structure to the lowest order, can now be expressed as

$$\mathcal{L}_{\text{int}} = c_8 \bar{\psi} \Phi \psi.$$

- The QCD Lagrangian is also invariant under the axial  $U(1)$  symmetry, which would imply the **existence of the ninth GB**. This breaking symmetry picks the  $\eta'$  as the ninth GB.
- The effective Lagrangian describing interaction between quarks and a nonet of GBs, consisting of octet and a singlet, can now be expressed as

$$\mathcal{L}_{\text{int}} = c_8 \bar{\psi} \Phi \psi + c_1 \bar{\psi} \frac{\eta'}{\sqrt{3}} \psi = c_8 \bar{\psi} \left( \Phi + \zeta \frac{\eta'}{\sqrt{3}} I \right) \psi = c_8 \bar{\psi} (\Phi') \psi,$$

where  $\zeta = \frac{c_1}{c_8}$ ,  $c_1$  is the coupling constant for the singlet GB, and  $I$  is the  $3 \times 3$  identity matrix.

- “Proton spin problem” including quark spin polarizations, orbital angular momentum of quarks etc.
- Quark flavor distributions, fraction of a particular quark (antiquark) present in a baryon, flavor structure functions, the Gottfried integral and the meson- baryon sigma terms.
- Magnetic moments of octet and decuplet baryons including their transitions and the Coleman-Glashow sum rule.
- Axial-vector form factors of the low lying octet baryons, singlet ( $g_0^A$ ) and nonsinglet ( $g_3^A$  and  $g_8^A$ ) axial-vector coupling constants.
- The spin independent ( $F_1^N$  and  $F_2^N$ ) and the spin dependent ( $g_1^N$ ) structure functions, longitudinal spin asymmetries of nucleon ( $A_1^N$ ).

- Hyperon  $\beta$  decay parameters including the axial-vector coupling parameters F and D.
- Magnetic moments of octet baryon resonances well as  $\Lambda$  resonances .
- Charge radii and quadrupole moment of the baryons.
- **The model is successfully extended to predict the important role played by the small intrinsic charm content in the nucleon spin in the SU(4)  $\chi$ CQM and to calculate the magnetic moment and charge radii of charm baryons including their radiative decays.**

- The GB field can be expressed in terms of the GBs and their transition probabilities as  $\Phi' =$

$$\begin{pmatrix} \frac{P_\pi \pi^0}{\sqrt{2}} + \frac{P_\eta \eta}{\sqrt{6}} + \frac{P_{\eta' \eta'}}{4\sqrt{3}} - \frac{P_D \eta_c}{4} & P_\pi \pi^+ & P_K K^+ & P_D \bar{D}^0 \\ P_\pi \pi^- & -\frac{P_\pi \pi^0}{\sqrt{2}} + \frac{P_\eta \eta}{\sqrt{6}} + \frac{P_{\eta' \eta'}}{\sqrt{3}} - \frac{P_D \eta_c}{4} & P_K K^0 & P_D D^- \\ P_K K^- & P_K \bar{K}^0 & -\frac{2P_\eta \eta}{\sqrt{6}} + \frac{P_{\eta' \eta'}}{4\sqrt{3}} - \frac{P_D \eta_c}{4} & P_D D_s^- \\ P_D D^0 & P_D D^+ & P_D D_s^+ & -\frac{3P_{\eta' \eta'}}{4\sqrt{3}} + \frac{3P_D \eta_c}{4} \end{pmatrix}$$

- The chiral fluctuations  $u(d) \rightarrow d(u) + \pi^{+(-)}$ ,  $u(d) \rightarrow s + K^{+(0)}$ ,  $u(d, s) \rightarrow u(d, s) + \eta$ ,  $u(d, s) \rightarrow u(d, s) + \eta'$  and  $u(d) \rightarrow c + \bar{D}^0 (D^-)$  are given in terms of the transition probabilities  $P_\pi$ ,  $P_K$ ,  $P_\eta$ ,  $P_{\eta'}$  and  $P_D$  respectively.

# Transition Magnetic Moments

- The transition magnetic moments for the the spin  $\frac{3}{2}^+ \rightarrow \frac{1}{2}^+$  transitions from the radiative decays  $B_i \rightarrow B_f + \gamma$ , where  $B_i$  and  $B_f$  are the initial and final baryons.
- The magnetic moment of a given baryon in the  $\chi$ CQM receives contribution from the valence quark spin, sea quark spin and sea quark orbital angular momentum

$$\mu \left( B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+} \right)_{Total} = \mu \left( B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+} \right)_V + \mu \left( B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+} \right)_S + \mu \left( B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+} \right)_O$$

$$\mu \left( B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+} \right)_V = \sum_{q=u,d,s} \Delta q \left( \frac{3^+}{2} \rightarrow \frac{1^+}{2} \right)_V \mu q$$

$$\mu \left( B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+} \right)_S = \sum_{q=u,d,s} \Delta q \left( \frac{3^+}{2} \rightarrow \frac{1^+}{2} \right)_S \mu q$$

$$\mu \left( B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+} \right)_O = \sum_{q=u,d,s} \Delta q \left( \frac{3^+}{2} \rightarrow \frac{1^+}{2} \right)_V \mu(q_+ \rightarrow)$$

- The quark magnetic moments are given as  $\mu_d^* = - \left( 1 - \frac{\Delta M}{M_B^*} \right)$  and  $\mu_u^* = -2\mu_d^*$  in the units of  $\mu_N$  (nuclear magneton).
- $\Delta q \left( \frac{3^+}{2} \rightarrow \frac{1^+}{2} \right)_V$  &  $\Delta q \left( \frac{3^+}{2} \rightarrow \frac{1^+}{2} \right)_S$  represent valance and sea quark spin polarizations respectively.
- $\mu(q_+ \rightarrow)$  is the orbital moment for any chiral fluctuation,  $M_B^*$  is the effective mass of baryon and  $\Delta M = M_B^* - M_{vac}$



- The spin structure of a decuplet to octet transition matrix element is defined as

$$\left\langle B_{\frac{1}{2}^+}, S_z = \frac{1}{2} \left| N(B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+}) \right| B_{\frac{3}{2}^+}, S_z = \frac{1}{2} \right\rangle$$

- The number operator measures the number of quarks with spin up ( $\uparrow$ ) or down ( $\downarrow$ ) in the transition ( $\frac{3}{2}^+ \rightarrow \frac{1}{2}^+$ )

$$N(B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+}) = \sum_{q=u,d,s} \left( N_{q\uparrow}(B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+}) + N_{q\downarrow}(B_{\frac{3}{2}^+} \rightarrow B_{\frac{1}{2}^+}) \right)$$

- The magnetic moment contribution of the angular momentum of a given sea quark

$$\langle L_q \rangle = \frac{M_{GB}}{M_q + M_{GB}} \quad \text{and} \quad \langle L_{GB} \rangle = \frac{M_q}{M_q + M_{GB}}.$$

- The general orbital moment for any quark (q) is given as

$$\mu(q^\uparrow \rightarrow q'^\downarrow) = \frac{e_{q'}}{2M_q} \langle L_q \rangle + \frac{e_q - e_{q'}}{2M_{GB}} \langle L_{GB} \rangle.$$

- The magnetic moment arising from all the possible transitions of a given valence quark to the GBs is obtained by multiplying the orbital moment of each process to the probability for such a process to take place.

- The orbital moments of  $u$ ,  $d$ ,  $s$  and  $c$  quarks after including the transition probabilities  $P_\pi$ ,  $P_K$ ,  $P_\eta$ ,  $P_{\eta'}$  and  $P_D$  as well as the masses of GBs  $M_\pi$ ,  $M_K$ ,  $M_\eta$ ,  $M_{\eta'}$ ,  $M_D$ ,  $M_{D_s}$ , and  $M_{\eta_c}$  can be expressed as (in the units of  $\mu_N$ )

$$[\mu^* (u_\uparrow \rightarrow)] = a \left[ \frac{3m_u^{*2}}{2M_\pi (m_u^* + M_\pi)} - \frac{P_\pi^2 (M_K^2 - 3m_u^{*2})}{2M_K (m_u^* + M_K)} + \frac{P_\eta^2 M_\eta}{6 (m_u^* + M_\eta)} \right. \\ \left. + \frac{P_{\eta'}^2 M_{\eta'}}{48 (m_u^* + M_{\eta'})} + \frac{P_D^2 M_{\eta_c}}{16 (m_u^* + M_{\eta_c})} + \frac{P_D^2 M_D}{m_u^* + M_D} \right] \mu_N,$$

$$[\mu^* (d_\uparrow \rightarrow)] = a \frac{m_u^*}{m_d^*} \left[ \frac{3 (M_\pi^2 - 2m_d^{*2})}{4M_\pi (m_d^{*2} + M_\pi)} - \frac{P_\pi^2 M_K}{2 (m_d^* + M_K)} + \frac{P_D^2 (2M_D^2 - 3m_d^*)}{2M_D (m_d^* + M_D)} \right. \\ \left. - \frac{P_\eta^2 M_\eta}{12 (m_d^* + M_\eta)} - \frac{P_{\eta'}^2 M_{\eta'}}{96 (m_d^* + M_{\eta'})} + \frac{P_D^2 M_{\eta_c}}{32 (m_d^* + M_D)} \right] \mu_N,$$

$$[\mu^* (s_{\uparrow} \rightarrow)] = a \frac{m_u^*}{m_s^*} \left[ \frac{P_{\pi}^2 (M_K^2 - 3m_s^{*2})}{2M_K (m_s^* + M_K)} - \frac{P_{\eta}^2 M_{\eta}}{3(m_s^* + M_{\eta})} + \frac{P_D^2 (2M_{D_s}^2 - 3m_s^{*2})}{2M_D (m_s^* + M_{D_s}^2)} \right. \\ \left. - \frac{P_{\eta'}^2 M_{\eta'}}{96(m_s^* + M_{\eta'})} - \frac{P_D^2 M_{\eta_c}}{32(m_s^* + M_D)} \right] \mu_N,$$

$$[\mu^* (c_{\uparrow} \rightarrow)] = a \frac{m_u^*}{m_c} \left[ \frac{P_D^2 (M_D^2 + 3m_c^2)}{2M_D (m_c + M_D^2)} - \frac{P_D^2 (M_{D_s}^2 + 3m_c^2)}{2M_d (m_c + M_{D_s}^2)} \right. \\ \left. + \frac{P_{\eta'}^2 M_{\eta'}}{16(m_c + M_{\eta'})} + \frac{9P_D^2 M_{\eta_c}}{16(m_c + M_{\eta_c})} \right] \mu_N$$

# Valence and sea transition magnetic moments for $\Delta \rightarrow p$ transitions

- Valence contribution is given as

$$\mu(\Delta \rightarrow p)_V = \frac{2\sqrt{2}}{3}\mu_u^* - \frac{2\sqrt{2}}{3}\mu_d^*$$

- Sea contribution is given as

$$-\frac{2\sqrt{2}}{3}a \left[ 1 + P_\pi^2 + \frac{P_\eta^2}{3} + \frac{P_{\eta'}^2}{24} + \frac{17P_D^2}{16} \right] \mu_u^*$$
$$+\frac{2\sqrt{2}}{3}a \left[ 1 + P_\pi^2 + \frac{P_\eta^2}{3} + \frac{P_{\eta'}^2}{24} + \frac{17P_D^2}{16} \right] \mu_d^*$$

- The orbital contribution to the magnetic moment of the decuplet to octet transition  $\mu \left( B_{\frac{3}{2}}^+ \rightarrow B_{\frac{1}{2}}^+ \right)$  for the baryon of the type  $B(Q_1 Q_2 Q_3)$  is

$$\begin{aligned}
 B(Q_1 Q_2 Q_3) = & \Delta Q_1 \left( \frac{3^+}{2} \rightarrow \frac{1^+}{2} \right)_V \mu(Q_1^\uparrow \rightarrow) \\
 & + \Delta Q_2 \left( \frac{3^+}{2} \rightarrow \frac{1^+}{2} \right)_V \mu(Q_2^\uparrow \rightarrow) \\
 & + \Delta Q_3 \left( \frac{3^+}{2} \rightarrow \frac{1^+}{2} \right)_V \mu(Q_3^\uparrow \rightarrow).
 \end{aligned}$$

Orbital Contribution is given as

$$\frac{2\sqrt{2}}{3} [\mu_u^* (u^\uparrow \rightarrow) - \mu_d^* (d^\uparrow \rightarrow)]$$

- Input parameters: transition probabilities  $P_\pi$ ,  $P_K$ ,  $P_\eta$ ,  $P_{\eta'}$ ,  $P_D$  and masses of GBs  $M_\pi$ ,  $M_K$ ,  $M_\eta$ ,  $M_{\eta'}$ ,  $M_{\eta_c}$ .
- Hierarchy followed by the probabilities of fluctuations of a constituent quark into pions,  $K$ ,  $\eta$ ,  $\eta'$  and  $D$  mesons.

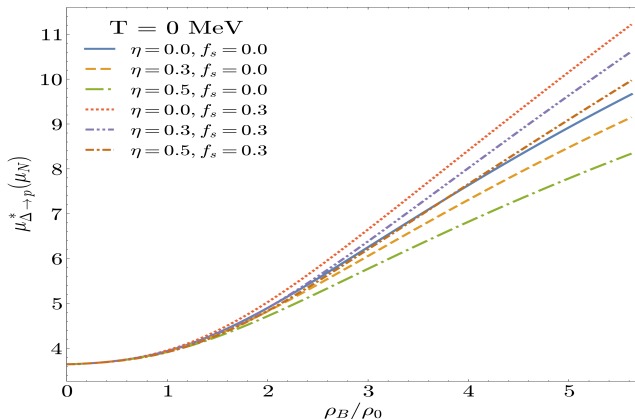
$$P_D < P_{\eta'} < P_\eta < P_K < P_\pi$$

- The transition probabilities are fixed by the experimentally known spin and flavor distribution functions measured from the DIS experiments. A detailed analysis leads to the following probabilities:

$$P_D = 0.01, P_{\eta'} = 0.03, P_\eta = 0.04, P_K = 0.06, P_\pi = 0.12$$

- The on mass shell mass values can be used for the orbital angular momentum contributions characterized by the masses of quarks and GBs ( $M_q$  and  $M_{GB}$ ).

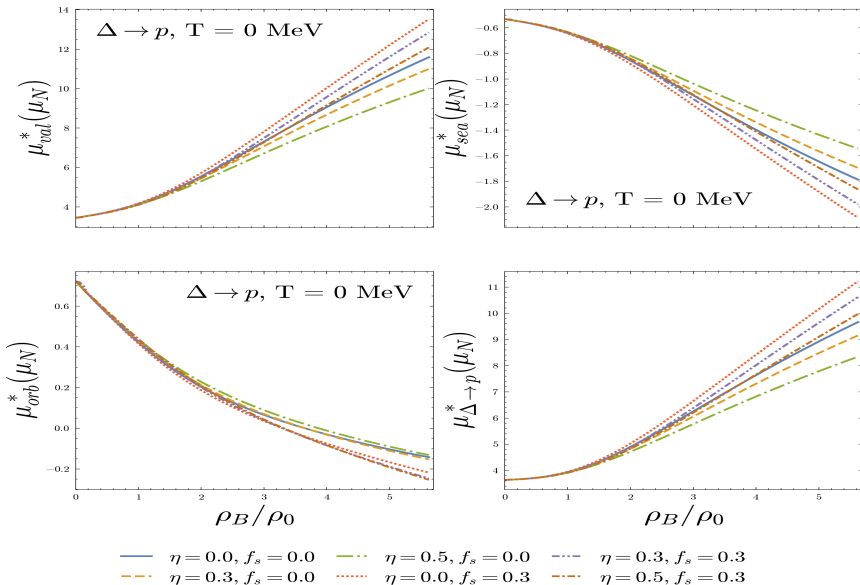
# Magnetic moments in for $\Delta \rightarrow p$ transitions



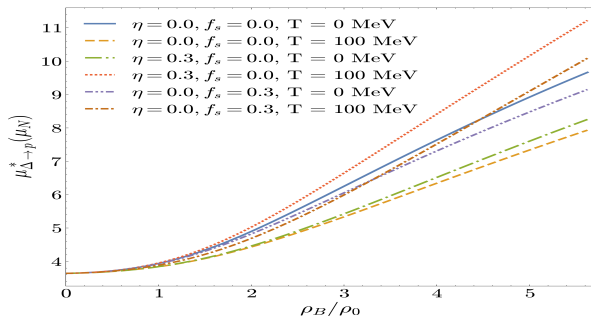
- Value of  $\mu^*$  increases with the increase in  $\rho_B$  at  $\eta$  and  $f_s$ .
- The increase in  $f_s$  shows an increase in  $\mu^*$  at same values of  $\rho_B$  and  $\eta$ .
- The increase in  $\eta$  shows a decrease in  $\mu^*$  at same values of  $\rho_B$  and  $f_s$ .



# Valence, Sea and Orbital Magnetic moments



# Magnetic moments in for $\Delta \rightarrow p$ transitions at High Temperature



- For symmetric nuclear matter ( $\eta = 0, f_s = 0$ ),  $\mu^*$  decreases with increase in temperature.
- For isospin asymmetric nuclear matter ( $\eta \neq 0$ ), large increase is observed with increase in temperature for all values of  $\rho_B$ .
- For symmetric strange matter,  $\mu^*$  increases with increase in temperature

# Summary

- Variation of Effective masses of quarks and hadrons with density studied for symmetric and asymmetric nuclear matter along-with in the asymmetric strange matter.
- Masses are found to decrease with density with sharp rate of decrease at lower density values.
- The increase in strangeness fraction decreases the mass while enhancement in the isospin asymmetry increases the mass at fixed density.
- The transition magnetic moment for  $\Delta \rightarrow p$  transition also studied under the same conditions.
- The effective transition magnetic moments increase with the increase in density. At the fixed density, with  $\eta$  magnetic moments decrease while with  $f_s$  an increase is observed.
- The temperature also has a significant impact on the magnetic moment.

# Thank You!