

Parton structure from JAM global QCD analysis

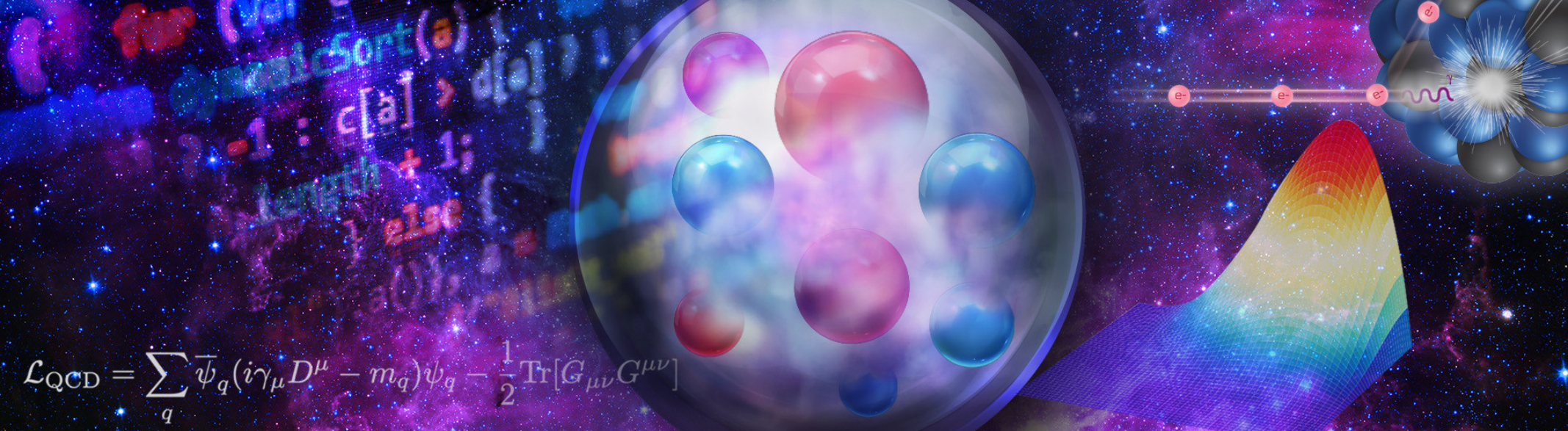
$$\mathcal{L}_{\text{QCD}} = \sum \bar{\psi}_q (i\gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{4} \text{Tr}[G_{\mu\nu} G^{\mu\nu}]$$

Wally Melnitchouk

 **Jefferson Lab**



<http://www.jlab.org/jam>



$$\mathcal{L}_{\text{QCD}} = \sum_q \bar{\psi}_q (i\gamma_\mu D^\mu - m_q) \psi_q - \frac{1}{2} \text{Tr}[G_{\mu\nu} G^{\mu\nu}]$$

■ Jefferson Lab Angular Momentum (JAM) collaboration — an enterprise involving theorists, experimentalists, and computer scientists using QCD to study internal structure of hadrons

→ analyse data using modern Monte Carlo techniques & uncertainty quantification to simultaneously extract various quantum correlation functions

- parton distribution functions (PDFs)
- fragmentation functions (FFs)
- transverse momentum dependent (TMD) distributions
- generalised parton distributions (GPDs)



<http://www.jlab.org/jam>

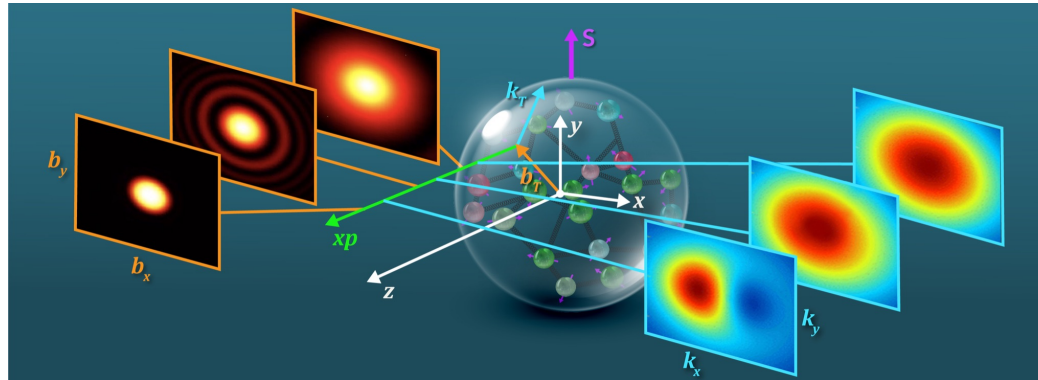
→ inclusion of lattice data and ML algorithms to potentially expand reach and efficacy of JAM analyses and understanding of hadron structure in QCD

■ 3D tomography in terms of quantum correlation functions (QCFs)

→ PDF (x) — 1D (light-front) momentum density

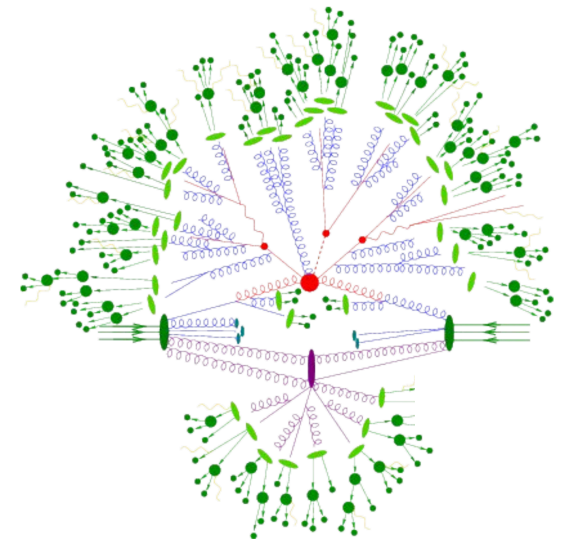
→ TMD (x, k_T) — additional dependence on parton k_T

→ GPD (x, ξ, k_T) — additional dependence on skewness ξ



→ FF (z) — probability for parton to produce hadron with momentum fraction z

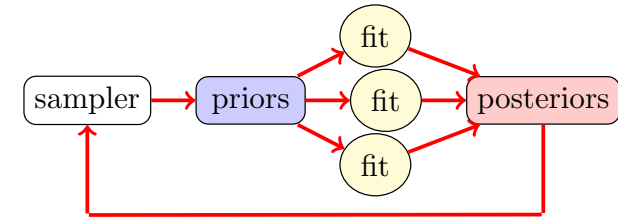
→ TMD FF (z, p_T) — with p_T dependence



JAM global QCD analysis

■ Theoretical framework

- collinear factorization (NLO)
- iterative Monte Carlo
- Bayesian sampling of parameter space



■ Choice of parametrisation, *e.g.*, for PDFs

$$f(x) = N x^\alpha (1-x)^\beta P(x)$$

polynomial, neural net, ...

→ iterate until convergence
(posteriors = priors)

■ “Bayesian master formulas” for expectation values and variances for \mathcal{O} with parameters \vec{a}

$$E[\mathcal{O}] = \int d^n a \mathcal{P}(\vec{a}|\text{data}) \mathcal{O}(\vec{a})$$

probability distribution

$$V[\mathcal{O}] = \int d^n a \mathcal{P}(\vec{a}|\text{data}) [\mathcal{O}(\vec{a}) - E[\mathcal{O}]]^2$$

$$\mathcal{P}(\vec{a}|\text{data}) \propto \mathcal{L}(\text{data}|\vec{a}) \pi(\vec{a})$$

likelihood
function

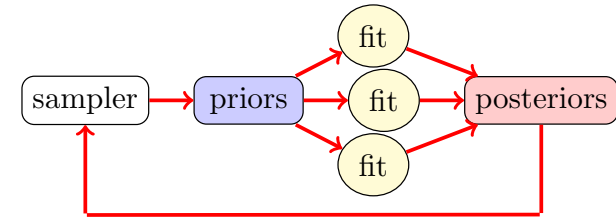
prior
distribution

$$\mathcal{L}(\text{data}|\vec{a}) = \exp \left[-\frac{1}{2} \chi^2(\vec{a}) \right]$$

JAM global QCD analysis

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■ Choice of parametrisation, *e.g.*, for PDFs

$$f(x) = N x^\alpha (1 - x)^\beta P(x)$$

polynomial, neural net, ...

→ iterate until convergence
(posteriors = priors)

■ Extraction of QCFs is challenging because usually there exist multiple solutions — “inverse problem”

- QCFs are not directly measured, but inferred from observables involving convolutions with other functions
- reliable uncertainty quantification is essential

JAM analysis groups

■ Unpolarized PDFs (and FFs)

Global QCD analysis and dark photons

N. T. Hunt-Smith, W. Melnitchouk, N. Sato, A. W. Thomas, X. G. Wang, M. J. White
JHEP 09, 096 (2023), [arXiv:2302.11126 \[hep-ph\]](#)

Bayesian Monte Carlo extraction of the sea asymmetry with SeaQuest and STAR data

C. Cocuzza, W. Melnitchouk, A. Metz, N. Sato
Phys. Rev. D 104, 074031 (2021), [arXiv:2109.00677 \[hep-ph\]](#)

Simultaneous Monte Carlo analysis of parton densities and fragmentation functions

E. Moffat, W. Melnitchouk, T. C. Rogers, N. Sato
Phys. Rev. D 104, 016015 (2021), [arXiv:2101.04664 \[hep-ph\]](#)

Isovector EMC effect from global QCD analysis with MARATHON data

C. Cocuzza, C. E. Keppel, H. Liu, W. Melnitchouk, A. Metz, N. Sato, A. W. Thomas
Phys. Rev. Lett. 127, 242001 (2021), [arXiv:2104.06946 \[hep-ph\]](#)

Strange quark suppression from a simultaneous Monte Carlo analysis of parton distributions and fragmentation functions

N. Sato, C. Andres, J.J. Ethier, W. Melnitchouk
Phys. Rev. D 101, 074020 (2020), [arXiv:1905.03788 \[hep-ph\]](#)

First Monte Carlo analysis of fragmentation functions from e^+e^- annihilation

N. Sato, J. J. Ethier, M. Hirai, S. Kumano, W. Melnitchouk
Phys. Rev. D 94, 114004 (2016), [arXiv:1609.00899 \[hep-ph\]](#)

■ Helicity PDFs

On the resolution of the sign of gluon polarization in the proton

N. T. Hunt-Smith, C. Cocuzza, W. Melnitchouk, N. Sato, A. W. Thomas, M. J. White
[arXiv:2403.08117 \[hep-ph\]](#)

Global analysis of polarized DIS and SIDIS data with improved small-x helicity evolution

D. Adamiak, N. Baldonado, Y. V. Kovchegov, W. Melnitchouk, D. Pitonyak, N. Sato
Phys. Rev. D 108, 114007 (2023), [arXiv:2308.07461 \[hep-ph\]](#)

Accessing gluon polarization with high-PT hadrons in SIDIS

R. M. Whitehill, Y. Zhou, N. Sato, W. Melnitchouk
Phys. Rev. D 107, 034033 (2023), [arXiv:2210.12295 \[hep-ph\]](#)

Polarized antimatter in the proton from global QCD analysis

C. Cocuzza, W. Melnitchouk, A. Metz, N. Sato
Phys. Rev. D 106, L031502 (2022), [arXiv:2202.03372 \[hep-ph\]](#)

How well do we know the gluon polarization in the proton?

Y. Zhou, N. Sato, W. Melnitchouk
Phys. Rev. D 105, 074022 (2022), [arXiv:2201.02075 \[hep-ph\]](#)

First analysis of world polarized DIS data with small-x helicity evolution

D. Adamiak, Y. V. Kovchegov, W. Melnitchouk, D. Pitonyak, N. Sato, M. D. Sievert
Phys. Rev. D 104, L031501 (2021), [arXiv:2102.06159 \[hep-ph\]](#)

First simultaneous extraction of spin-dependent parton distributions and fragmentation functions

J. J. Ethier, N. Sato, W. Melnitchouk
Phys. Rev. Lett. 119, 132001 (2017), [arXiv:1705.05889 \[hep-ph\]](#)

Iterative Monte Carlo analysis of spin-dependent parton distributions

N. Sato, W. Melnitchouk, S. E. Kuhn, J. J. Ethier, A. Accardi
Phys. Rev. D 93, 074005 (2016), [arXiv:1601.07782 \[hep-ph\]](#)

■ Transversity PDFs

First simultaneous global QCD analysis of dihadron fragmentation functions and transversity parton distribution functions

C. Cocuzza, A. Metz, D. Pitonyak, A. Prokudin, N. Sato, R. Seidl
Phys. Rev. D 109, 034024 (2024), [arXiv:2308.14857 \[hep-ph\]](#)

Transversity distributions and tensor charges of the nucleon

C. Cocuzza, A. Metz, D. Pitonyak, A. Prokudin, N. Sato, R. Seidl
Phys. Rev. Lett. 132, 091901 (2024), [arXiv:2306.12998 \[hep-ph\]](#)

First Monte Carlo global analysis of nucleon transversity with lattice QCD constraints

H.-W. Lin, W. Melnitchouk, A. Prokudin, N. Sato, H. Shows
Phys. Rev. Lett. 120, 152502 (2018), [arXiv:1710.09858 \[hep-ph\]](#)

JAM analysis groups

■ Pion distributions

Tomography of pions and protons via transverse momentum dependent distributions

P. C. Barry, L. Gamberg, W. Melnitchouk, E. Moffat, D. Pitonyak, A. Prokudin, N. Sato
Phys. Rev. D **108**, L091504 (2023), [arXiv:2302.01192 \[hep-ph\]](#)

Complementarity of experimental and lattice QCD data on pion parton distributions

P. C. Barry, C. Egerer, J. Karpie, W. Melnitchouk, C. Monahan, K. Orginos, Jian-Wei Qiu, D. Richards, N. Sato, R. S. Sufian, S. Zafeiropoulos
Phys. Rev. D **105**, 114051 (2022), [arXiv:2204.00543 \[hep-ph\]](#)

Global QCD analysis of pion parton distributions with threshold resummation

P. C. Barry, C.-R. Ji, N. Sato, W. Melnitchouk
Phys. Rev. Lett. **127**, 232001 (2021), [arXiv:2108.05822 \[hep-ph\]](#)

Towards the three-dimensional parton structure of the pion: Integrating transverse momentum

N. Y. Cao, P. C. Barry, N. Sato, W. Melnitchouk
Phys. Rev. D **103**, 114014 (2021), [arXiv:2103.02159 \[hep-ph\]](#)

First Monte Carlo global QCD analysis of pion parton distributions

P. C. Barry, N. Sato, W. Melnitchouk, C.-R. Ji
Phys. Rev. Lett. **121**, 152001 (2018), [arXiv:1804.01965 \[hep-ph\]](#)

■ TMDs

Updated QCD global analysis of single transverse-spin asymmetries: Extracting H_T^- , and the role of the Soffer bound and lattice QCD

L. Gamberg, M. Malda, J. A. Miller, D. Pitonyak, A. Prokudin, N. Sato
Phys. Rev. D **106**, 034014 (2022), [arXiv:2205.00999 \[hep-ph\]](#)

New tool for kinematic regime estimation in semi-inclusive deep-inelastic scattering

M. Boglione, M. Dieffenthaler, S. Dolan, L. Gamberg, W. Melnitchouk, D. Pitonyak, A. Prokudin, N. Sato, Z. Scalyer
JHEP **04** (2022) 084, [arXiv:2201.12197 \[hep-ph\]](#)

Origin of single transverse-spin asymmetries in high-energy collisions

J. Cammarota, L. Gamberg, Z.-B. Kang, J.A. Miller, D. Pitonyak, A. Prokudin, T.C. Rogers, N. Sato
Phys. Rev. D **102**, 054002 (2020), [arXiv:2002.08384 \[hep-ph\]](#)

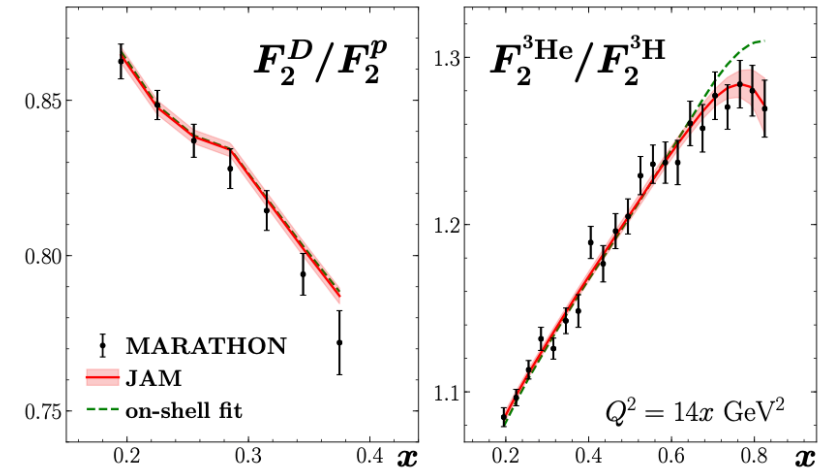
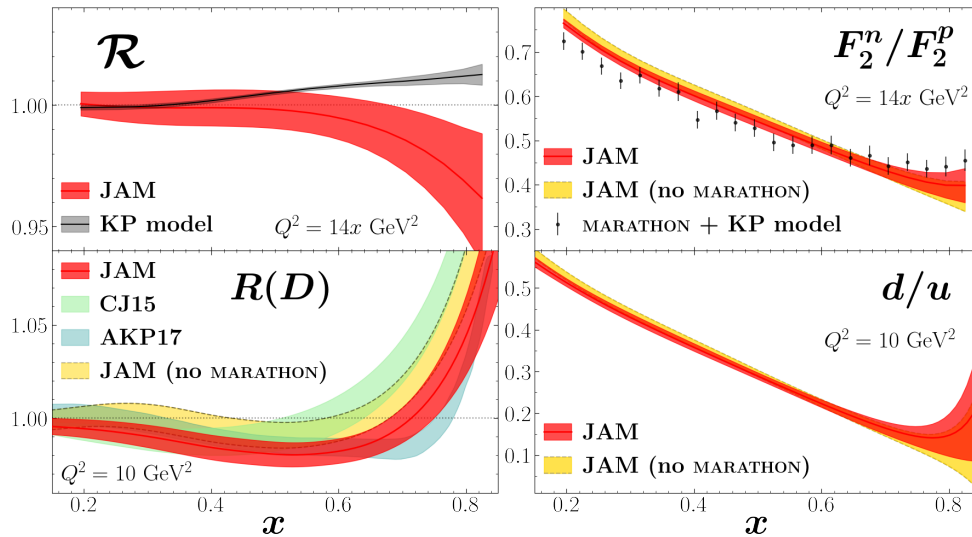
■ GPDs

Shedding light on shadow generalized parton distributions

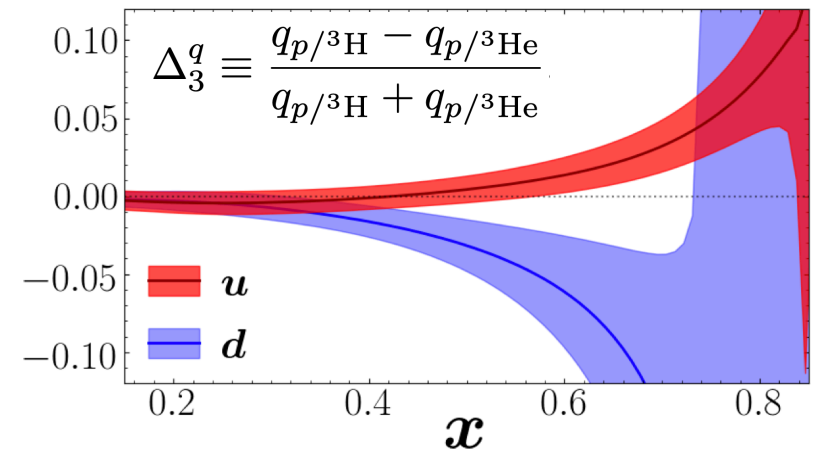
E. Moffat, A. Freese, I. Cloët, T. Donohoe, L. Gamberg, W. Melnitchouk, A. Metz, A. Prokudin, N. Sato
Phys. Rev. D **108**, 036027 (2023), [arXiv:2303.12006 \[hep-ph\]](#)

Isovector nuclear EMC effect

- Global analysis including MARATHON DIS data on D/p , tritium / helium



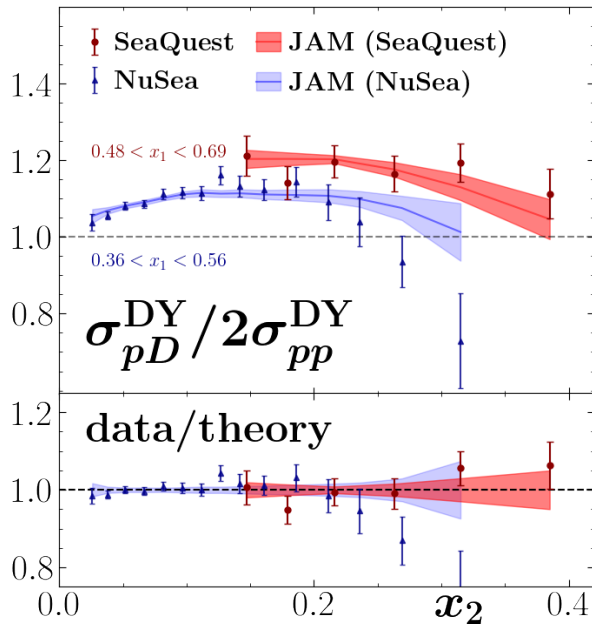
- evidence for different medium modifications for u and d quarks
- naive modeling of nuclear PDFs (*e.g.*, $u/p/A = d/n/A$) violates isospin symmetry for isospin-asymmetric nuclei



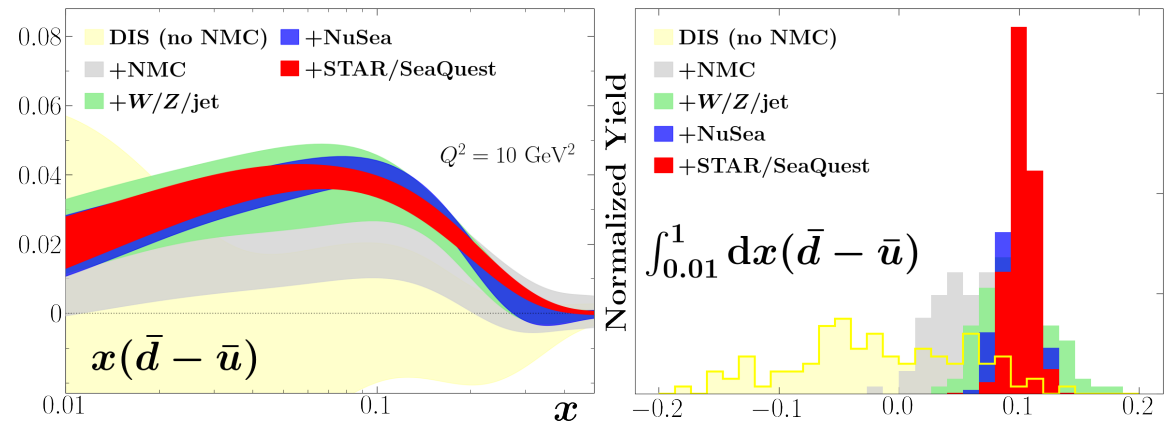
Cocuzza, Keppel, Liu, WM, Metz, Sato, Thomas
PRL 127, 242001 (2021)

Sea quark asymmetries — unpolarised

Impact of SeaQuest & RHIC W-production data

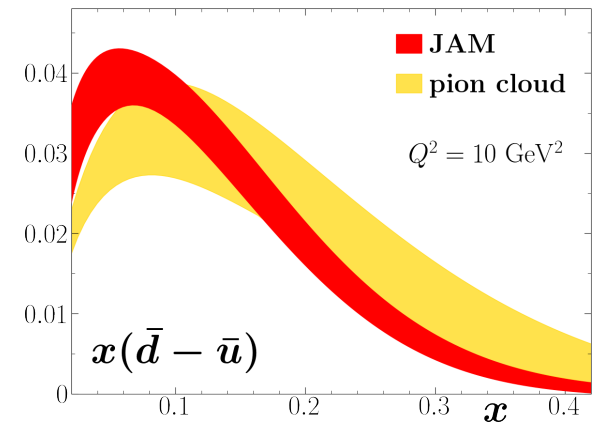


$$\frac{\sigma^{pd}}{\sigma^{pp}} \approx 1 + \frac{\bar{d}(x_2)}{\bar{u}(x_2)} \quad \text{for } x_1 \gg x_2$$



- strong constraints on integrated $\bar{d} - \bar{u}$ in measured region
- shape and magnitude consistent with models based on pion cloud of nucleon

Thomas, PLB 126, 97 (1983)



Cocuzza, WM, Metz, Sato
PRD 104, 074031 (2021)

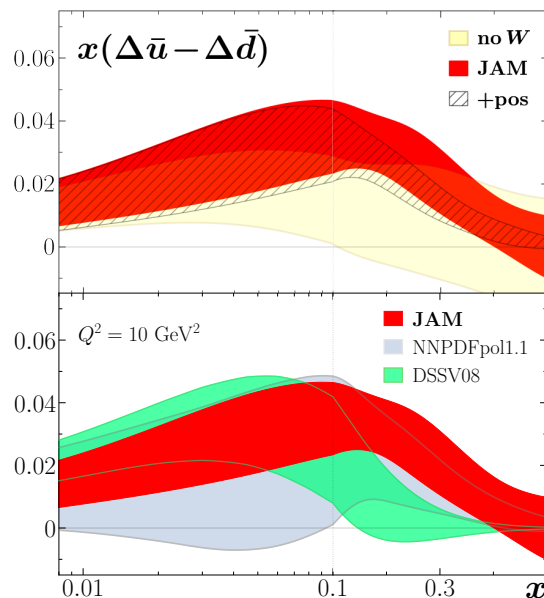
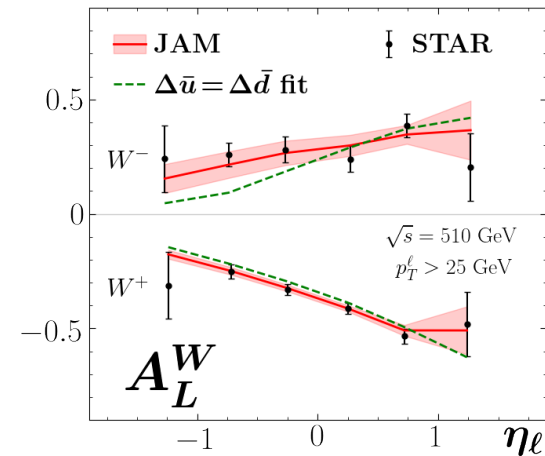
Sea quark asymmetries — polarised

■ Flavour asymmetries in spin PDFs expected from antisymmetrisation

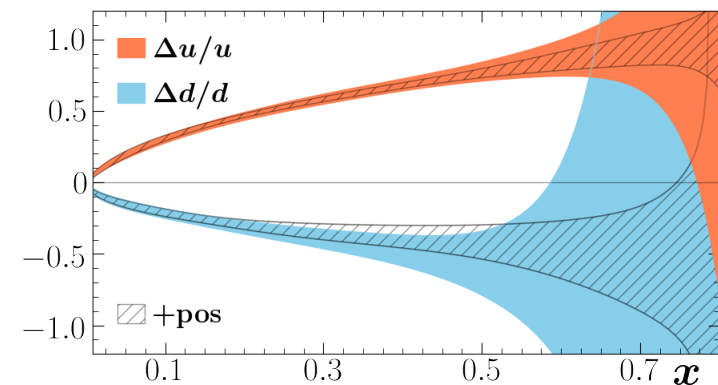
→ tested in W production
in polarised pp collisions

$$A_L^{W^+} \sim \Delta\bar{d}(x_1)u(x_2) - \Delta u(x_1)\bar{d}(x_2)$$

$$A_L^{W^-} \sim \Delta\bar{u}(x_1)d(x_2) - \Delta d(x_1)\bar{u}(x_2)$$



*Cocuzza, WM, Metz, Sato
PRD 106, L031502 (2022)*



→ excess of $\Delta\bar{u}$ over $\Delta\bar{d}$
at intermediate x

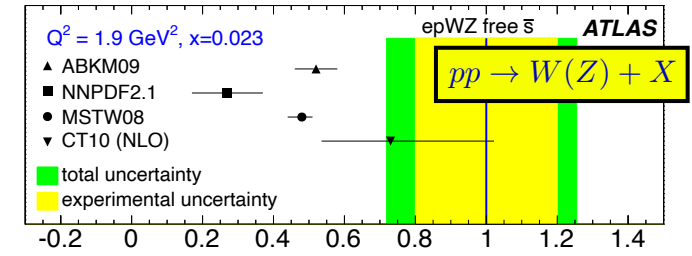
→ first consistent (simultaneous)
extraction of ratios $\Delta q/q$

Strange quark sea

■ Shape and magnitude of strange quark PDF is controversial

→ historically, strange to nonstrange ratio $R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}} \sim 0.4$

→ larger than expected strangeness extracted from ATLAS W/Z data

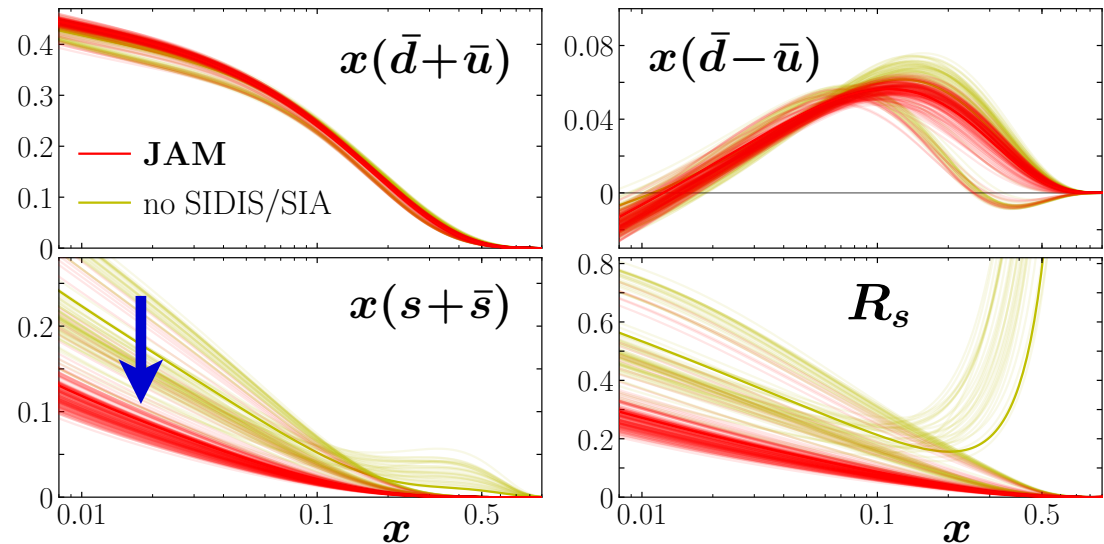


■ Impact of SIDIS & SIA data on unpolarised PDFs

→ SIA data at large z disfavor small $s \rightarrow K$ FF

→ larger $s \rightarrow K$ FF requires smaller strange PDF

→ suppression of strange PDF compared to ATLAS extraction



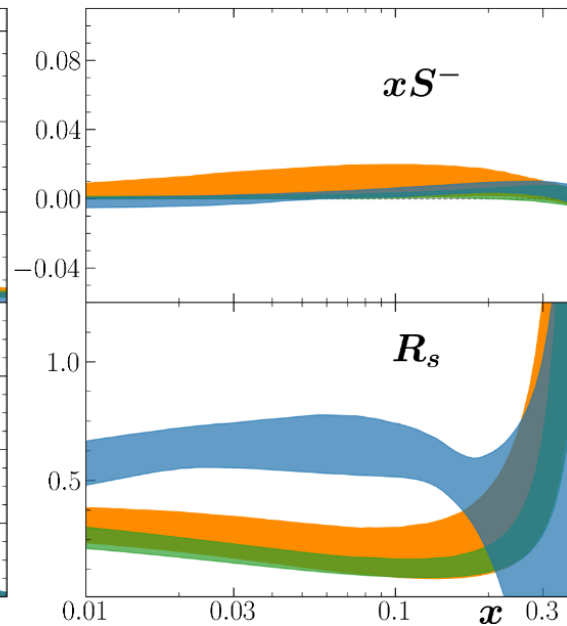
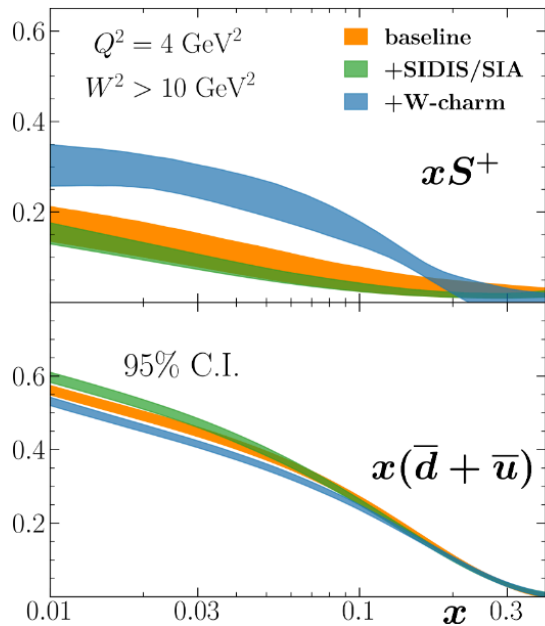
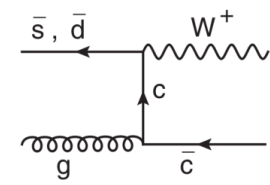
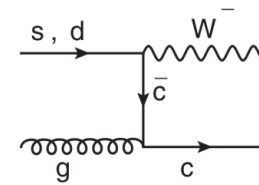
Sato, Andres, Ethier, WM
PRD **101**, 074020 (2020)

Strange quark sea

■ $W+c$ production in pp collisions

→ sensitive to s and \bar{s} distributions

→ ATLAS and CMS data indicate larger strange content



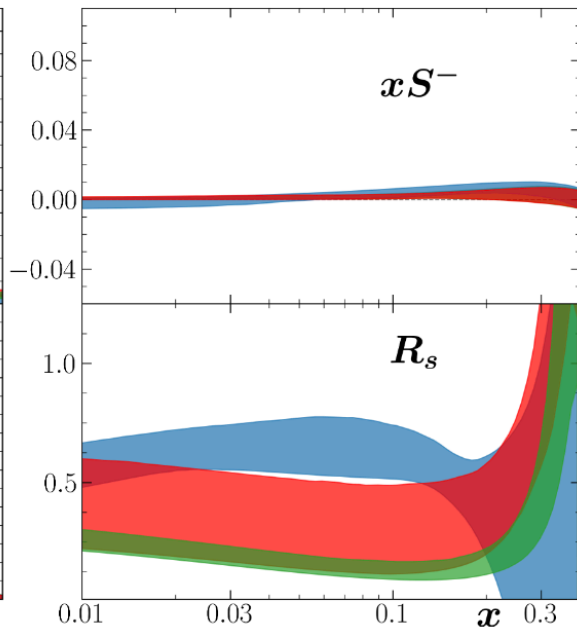
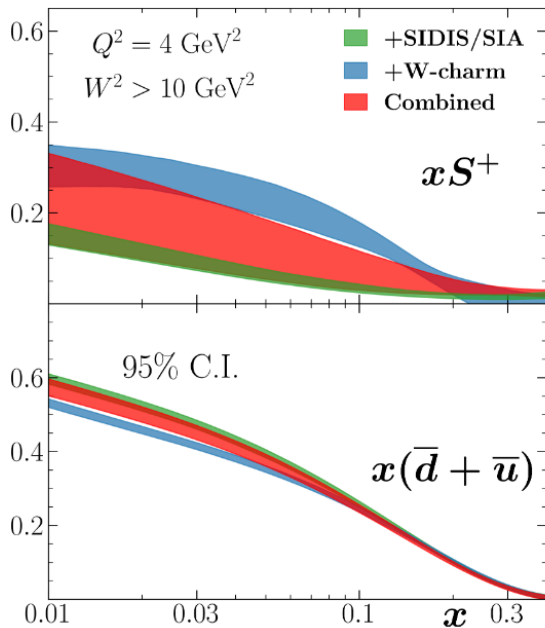
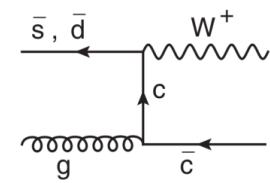
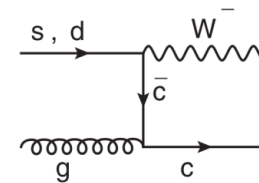
*Anderson, WM, Sato,
in preparation (2024)*

Strange quark sea

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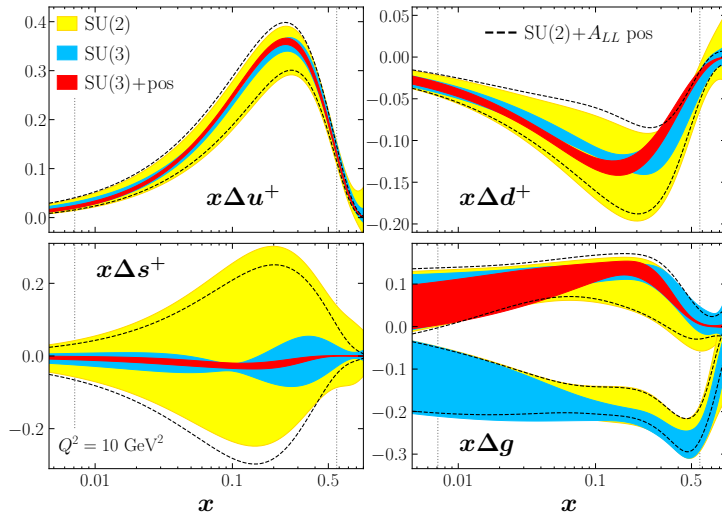


Anderson, WM, Sato,
 in preparation (2024)

→ combined analysis gives $R_s \approx 0.2 - 0.5$ for $0.01 \lesssim x \lesssim 0.25$ with larger overall uncertainty

Polarised glue

- First simultaneous analysis including polarised *and* unpolarised jets in proton-proton and proton-antiproton collisions



Zhou, Sato, WM, PRD 105, 074022 (2022)

SU(2):

$$\int_0^1 dx [\Delta u^+ - \Delta d^+](x, Q^2) = g_A \quad \checkmark$$

SU(3):

$$\int_0^1 dx [\Delta u^+ + \Delta d^+ - 2\Delta s^+](x, Q^2) = a_8 \quad ?$$

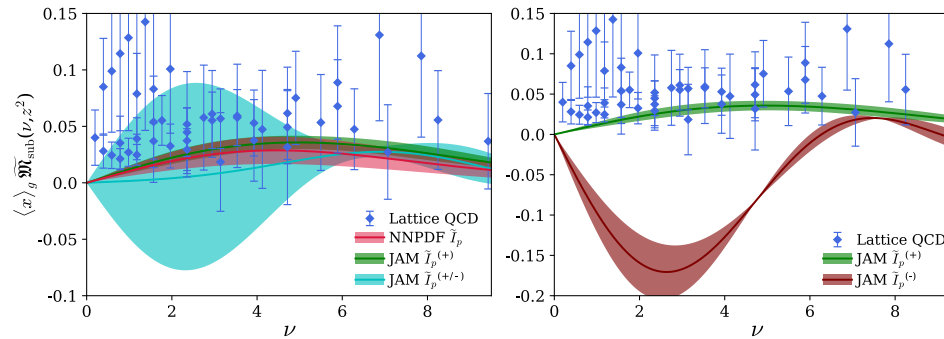
PDF positivity:

$$|\Delta f_i(x, Q^2)| \leq f_i(x, Q^2) \quad \times$$

- polarised strange and gluon spin PDFs depend strongly on theoretical assumptions, especially positivity of (unpolarised) PDFs
- cannot rule out negative gluon polarisation from experiment alone!

Polarised glue

■ New lattice QCD calculations of Ioffe-time pseudo-distributions



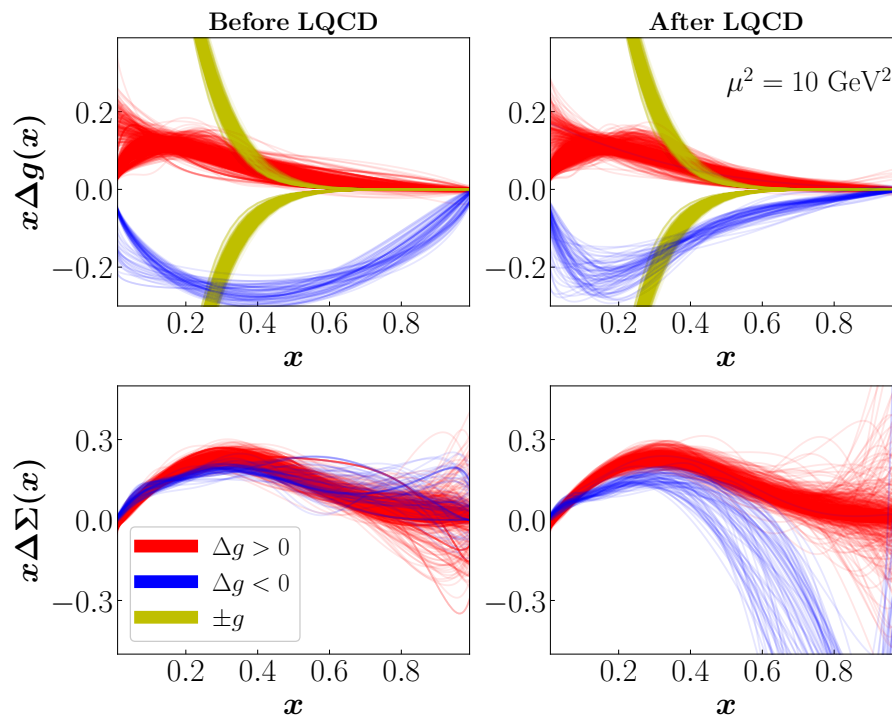
$\widetilde{\mathcal{M}}(\nu, z^2)$ depends on

$$\tilde{\mathcal{I}}_p(\nu) = \frac{i}{2} \int_{-1}^1 dx e^{-ix\nu} x \Delta g(x).$$

Egerer et al. [HadStruc Collaboration]
PRD **106**, 094511 (2022)

→ favours positive gluon polarisation?

→ fit experimental + lattice data simultaneously



→ good description of data after inclusion of LQCD for both solutions for Δg

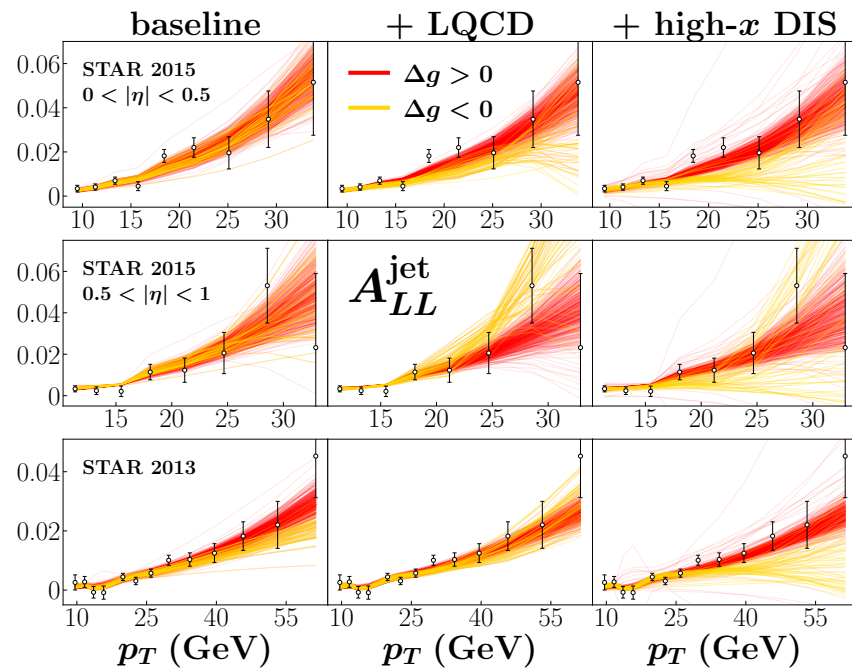
→ from χ^2 alone, LQCD cannot discriminate sign of Δg

but ... negative Δg gives rise to negative $\Delta\Sigma$ at large x

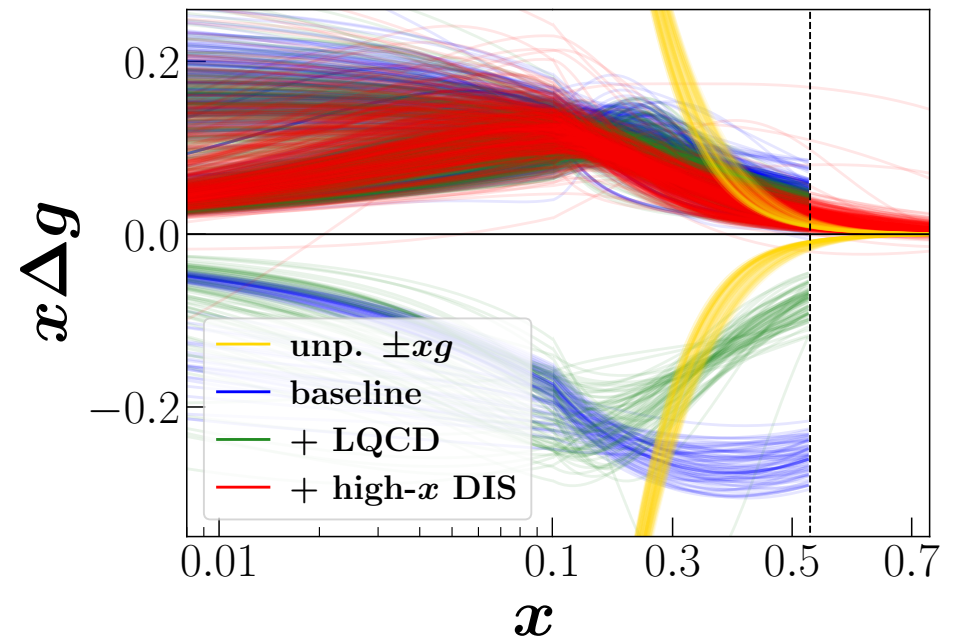


Polarised glue

- Lower W^2 cut from 10 GeV^2 to 4 GeV^2 to include high- x region



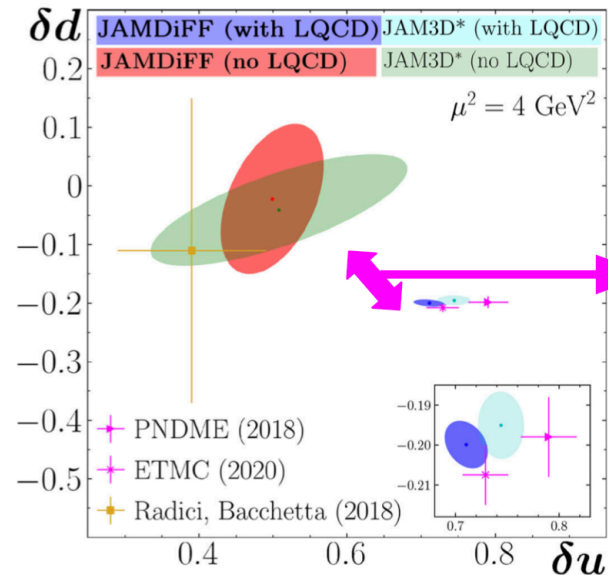
Hunt-Smith, Cocuzza, WM, Sato, Thomas, White, arXiv:2403.08117



- including high- x DIS data (CLAS, Hall A, SANE), LQCD strongly disfavours negative $\Delta\Sigma$ solutions at $x > 0.5$
- in data-driven approach, $\Delta g < 0$ can be ruled out only with inclusion of polarised jet, lattice, and high- x DIS data!

Transversity

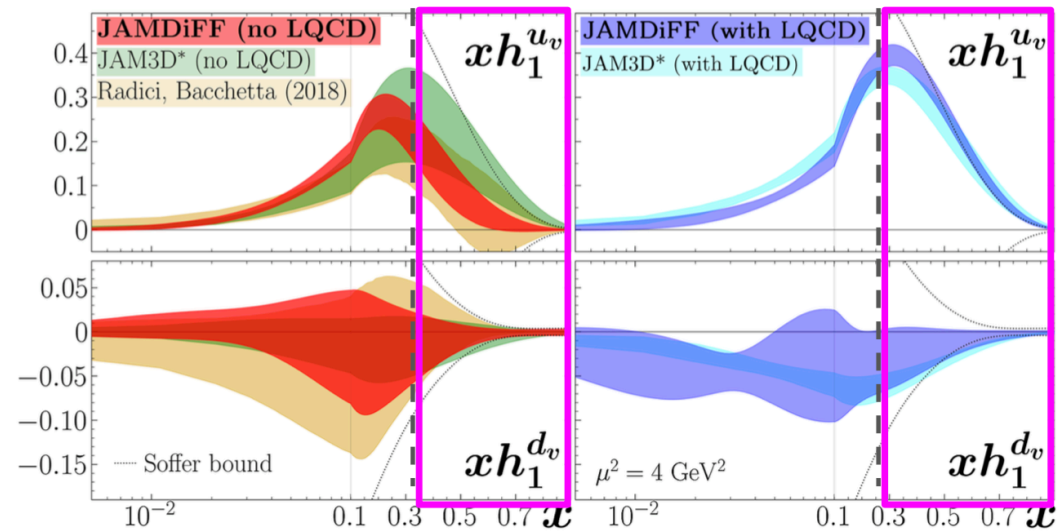
- Reconstruct transversity h_1 PDFs from
 - single spin asymmetries (SIDIS, pp) within TMD+CT3 framework
 - “JAM3D”
 - dihadron production in SIDIS, pp and e^+e^- data
 - “JAMDiFF”



tension between LQCD & experiment removed by adjusting h_1 in (extrapolated) large- x region

- Tension between experiment and lattice QCD data?

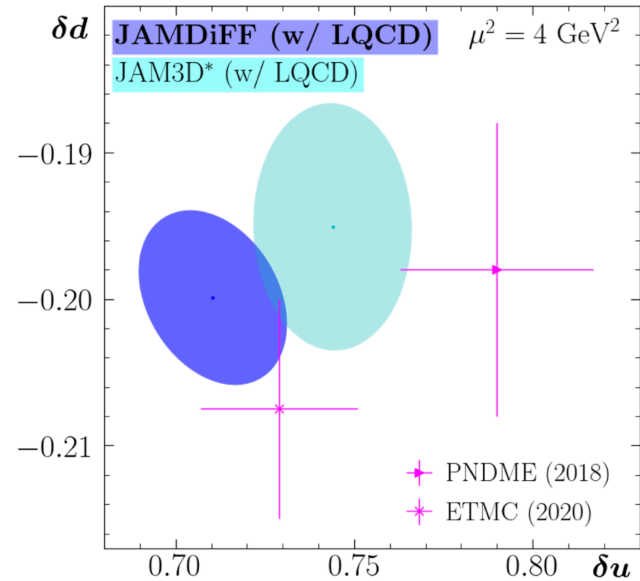
- weak constraints on h_1 from experiment at $x > 0.3$
- LQCD moments suggest large contributions at high x
- more high- x data needed to test compatibility



Cocuzza, Metz, Pitonyak, Prokudin, Sato, Seidl
 PRD **109**, 034024 (2024)
 PRL **132**, 091901 (2024)

Transversity

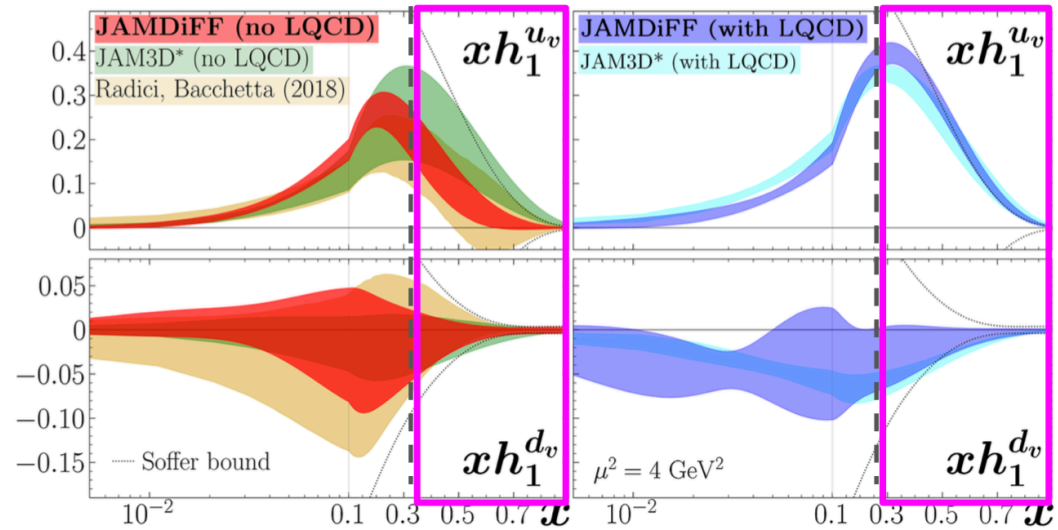
- Reconstruct transversity h_1 PDFs from
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Cocuzza, Metz, Pitonyak, Prokudin, Sato, Seidl
 PRD **109**, 034024 (2024)
 PRL **132**, 091901 (2024)

Generalised parton distributions

■ JAM's GPD efforts moving towards ML-based analysis

- GPDs more complicated, traditional methods require more modeling
- capitalise on tools developed for imaging in ML
- model GPDs as pixels instead of assuming functional forms
... address resolution with which images can be reconstructed

■ JAM participating in multi-institutional projects

- Quark-Gluon Tomography (QGT) Topical Collaboration
— global analysis of GPDs from DVCS & DVMP data with LQCD



- LDRD

- SDHEPS to reconstruct x dependence: photoproduction in Hall D

- QuantOm

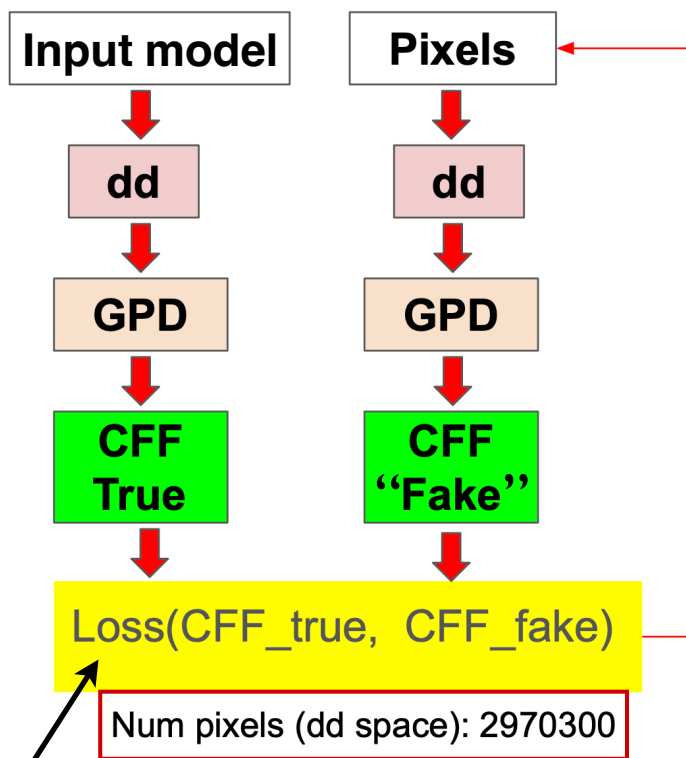
- integrated experiment and theory event-level analysis framework for hadron structure studies: fold detector effects with QCD reaction

- ML-enabled framework requires differentiable programming libraries (PyTorch)

- develop data analysis framework for simultaneous extractions of QCFs
— capitalise on JAM PDF/TMD machinery

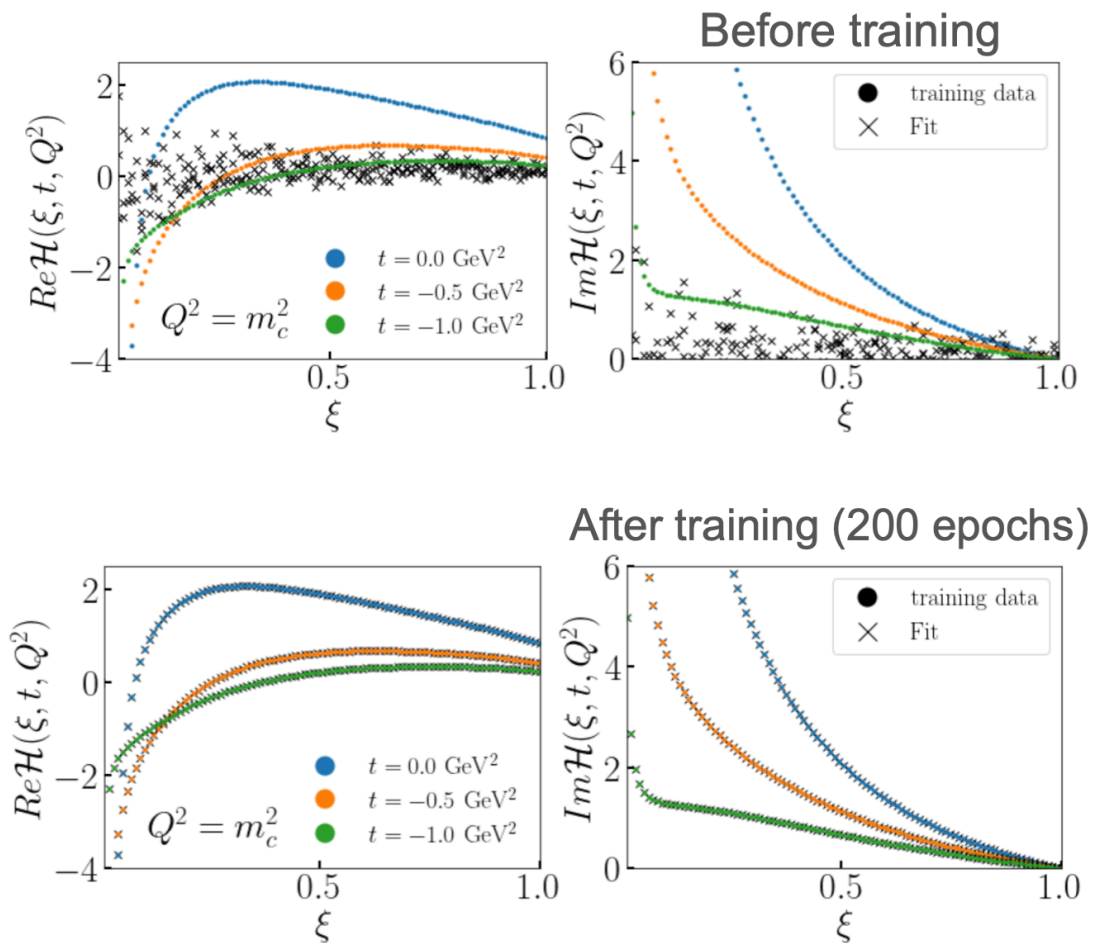
QGT: GPDs from Compton form factors

■ Closure test analysis



χ^2 between true & fake

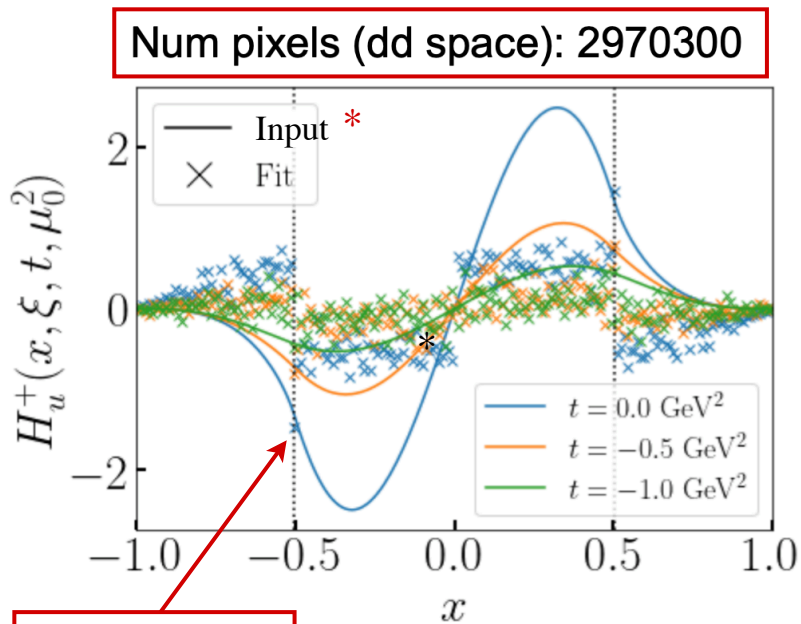
→ differential programming essential!



- fit and data coincide after training
- can tune 3M parameters to reproduce original “data”
- can use setup to reconstruct CFFs from DVCS observables

QGT: GPDs from Compton form factors

Are GPDs reconstructed from CFFs unique?

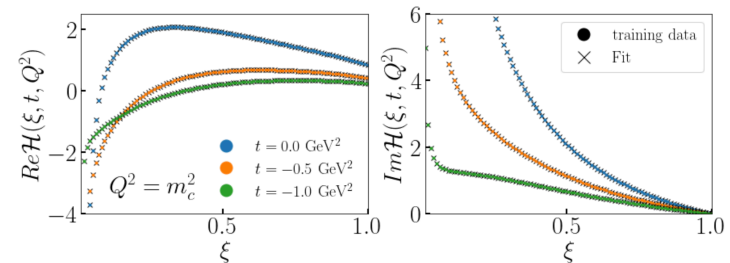


$x = \xi$ “ridge”

Moffat et al.,
in preparation (2024)

*“toy analysis”: no evolution, only u -quark flavor, CFFs only sensitive to charge-even combination, no uncertainty quantifications

→ both “input” and “fit” GPDs give same CFFs!



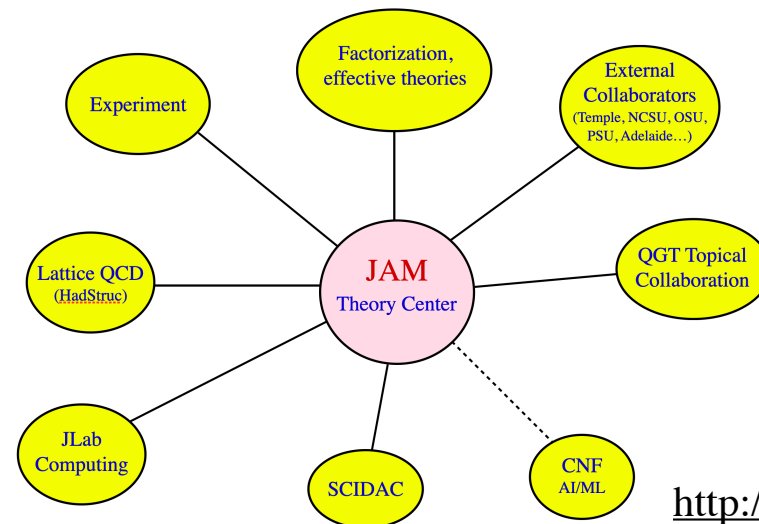
→ pixel-based reconstruction shows clear demonstration of shadow GPDs

→ more inputs needed (models and/or lattice and/or experiment) to reconstruct x dependence of GPDs

→ **future of GPD reconstruction**
— use lattice QCD input (QGT)
— use double DVCS, SDHEPS data (LDRD)

Outlook

- Progress made by JAM Collaboration towards simultaneous QCD analysis of all observables sensitive to collinear (spin-averaged and spin-dependent) PDFs and FFs, as well as TMD PDFs and TMD FFs
- Incorporation of lattice QCD data into global analysis (with caution)
- Increasing utilization of AI/ML tools to meet complexity challenge
- JAM machinery being leveraged in development of ML-based analysis framework for GPDs → 3-D structure of hadrons



<http://www.jlab.org/jam>