

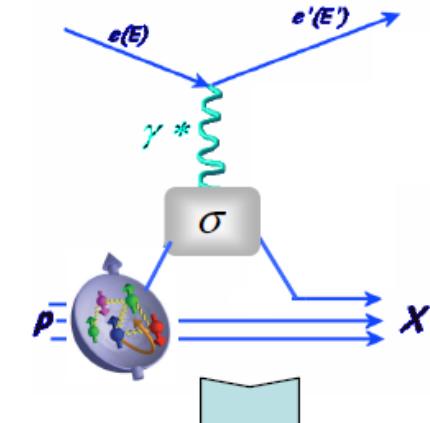
DVCS & hard exclusive meson prod.

-- experimental review --

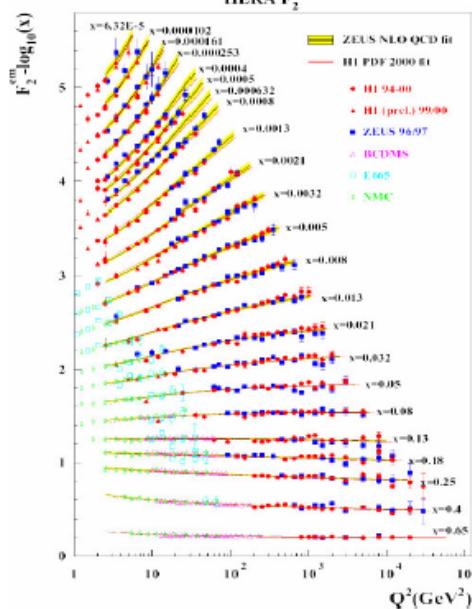
- a very brief introduction
- prerequisites and methods
- from low to high x : selected results
- perspectives

all details tomorrow:
■ F. X. Girod
■ S. Yaschenko
■ N. D'Hose
■ V. Burkert

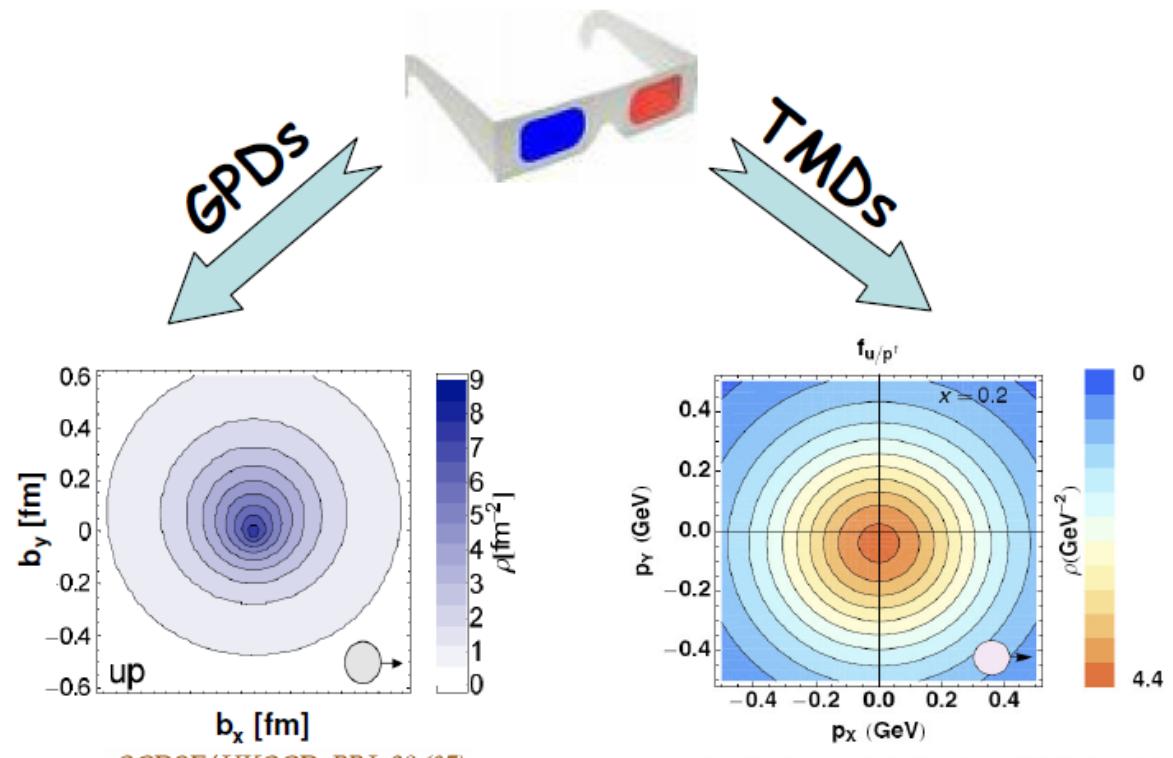
Quantum phase-space tomography of the nucleon



Join the real
3D experience!!



Longitudinal momentum structure of the nucleon



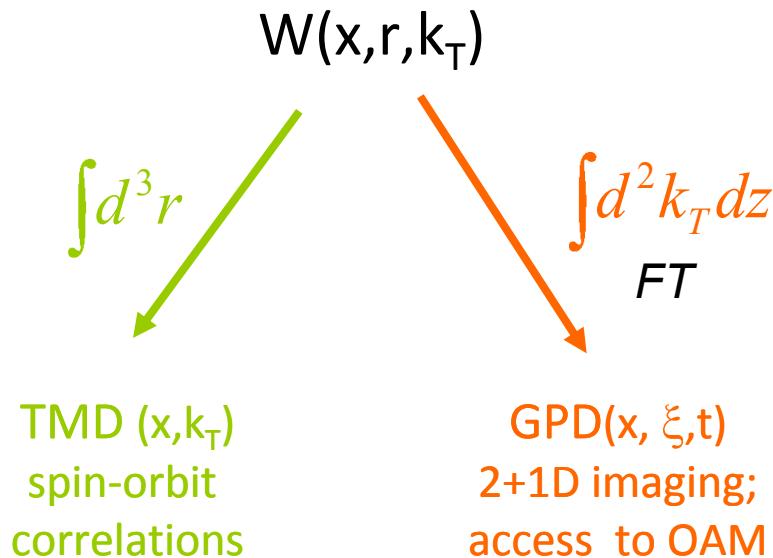
3D picture in coordinate space

A.B., F. Conti, M. Radici, PRD78 (08)

3D picture in momentum space

3D imaging of the nucleon & OAM

Wigner distribution ('mother function'):



C. Lorce [tomorrow]

→ (model dependent) relations between TMDs & GPDs:

$$f_{1T}^{\perp (n)}(x) \sim E^{q(n)}(x, 0, 0)$$

[Burkardt 2002]

[Burkardt, Hwang 2003]

[Diehl, Haegeler 2005]

ecc.

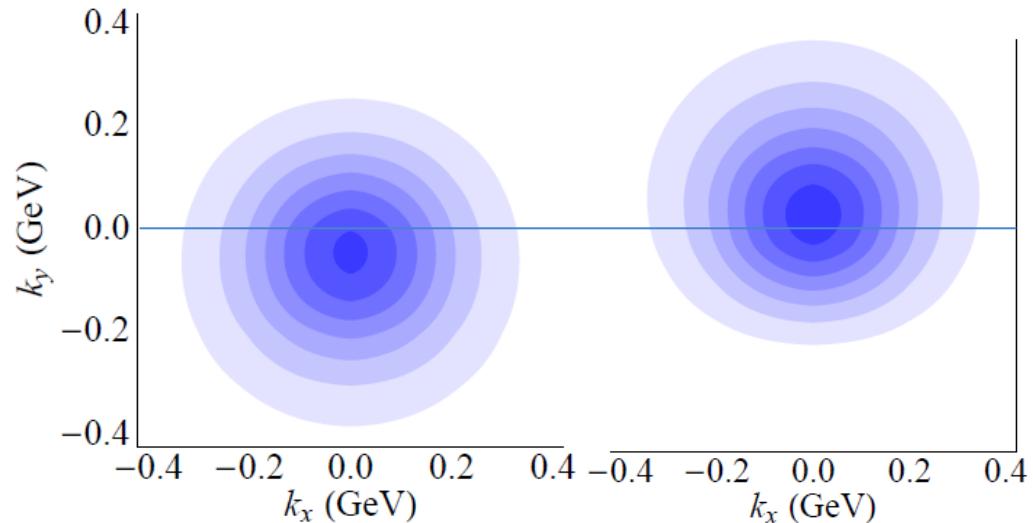
nucleon tomography

[transversely polarised nucleon]



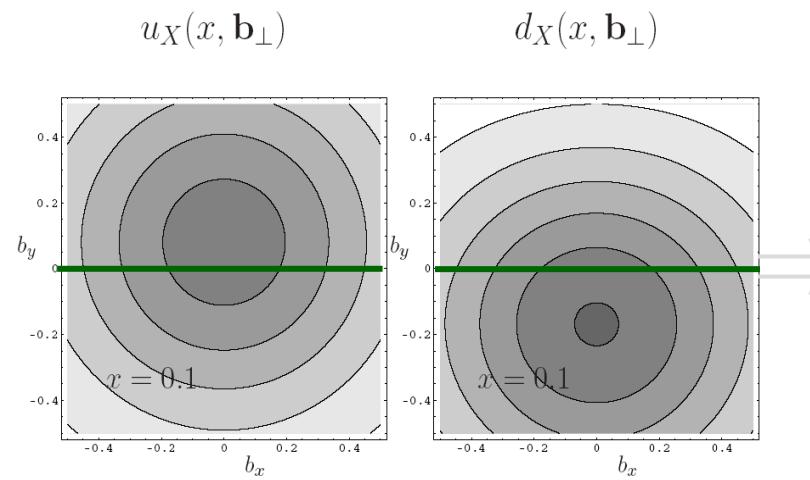
TMDs

[model calculation by B. Pasquini, F. Yuan]



GPDs

[model calculation by M. Burkardt]



Sivers TMD

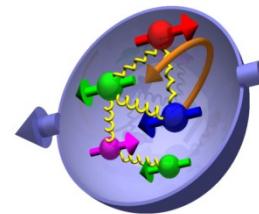
--in transverse momentum coordinates--

← model dependent relation →

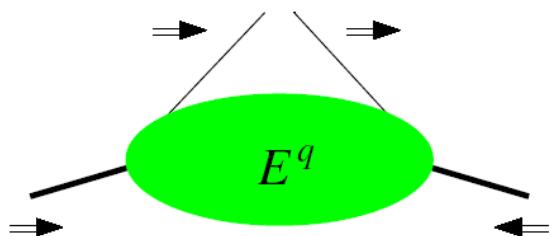
GPD E

--in impact parameter coordinates--

relations to OAM



GPDs



proton helicity flipped while
quark helicity is conserved

$E^q \neq 0$ requires orbital angular
momentum

$$J^q = \frac{1}{2} \int_{-1}^1 dx dx [H^q(x, \xi, t) + E^q(x, \xi, t)]_{t=0}$$

TMDs

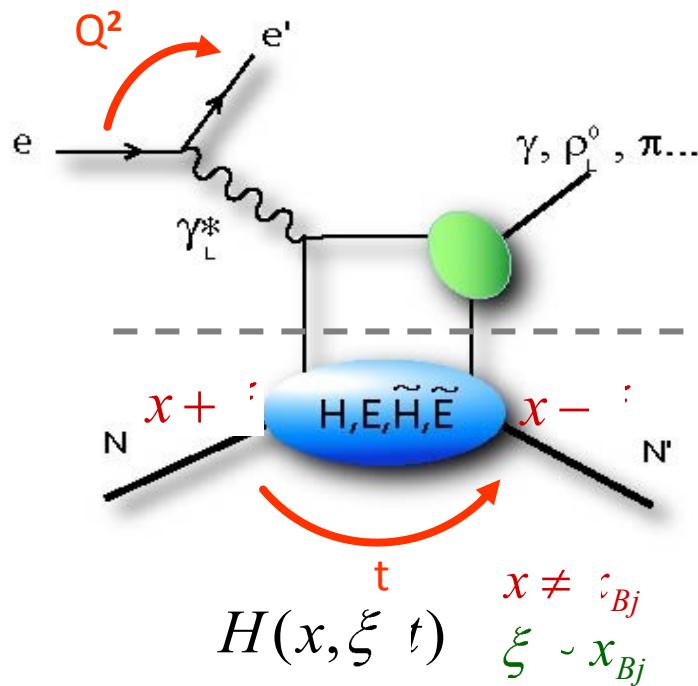
[plot: courtesy B. Musch]

N	U	L	T
U	f_1		h_1^\perp
L		g_1	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1 h_{1T}^\perp

$\Delta L=1$ $\Delta L=1$ $\Delta L=2$

require interference of nucleon wave
fct.s with different units OAM
→ spin-orbit correlation

how to measure GPDs ?

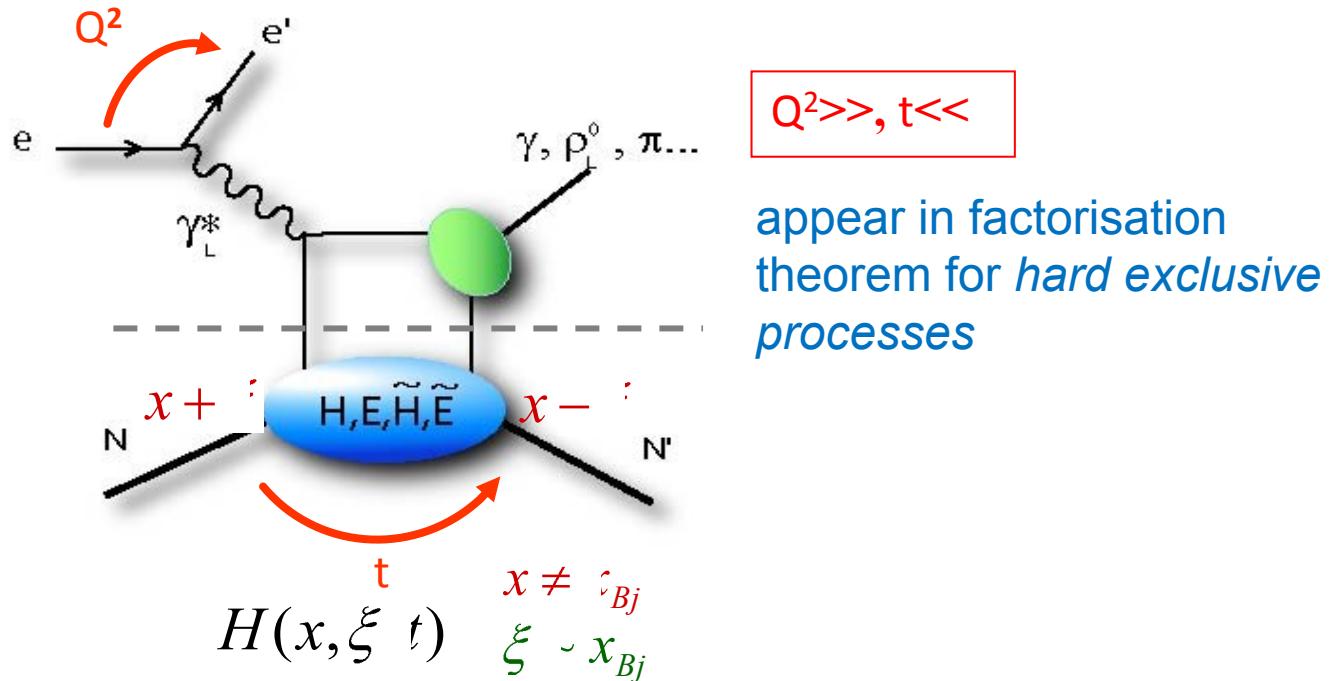


$Q^2 \gg, t \ll$

appear in factorisation
theorem for *hard exclusive
processes*

$$H(x, \xi, t) \quad x \neq x_{Bj} \quad \xi \sim x_{Bj}$$

how to measure GPDs ?

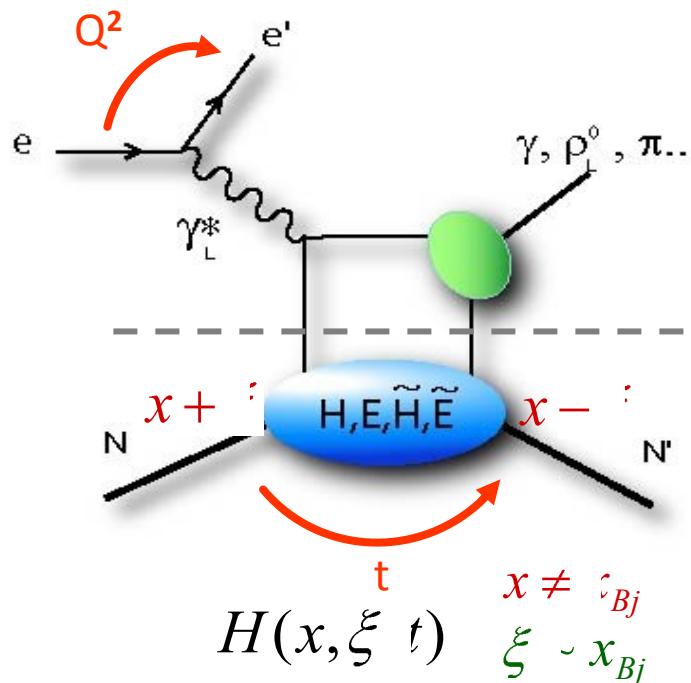


- spin $1/2$ target:

4 leading-tw, chiral even q & g GPDs: H, \tilde{H} conserve nucleon helicity
 E, \tilde{E} involve nucleon helicity flip

+ 4 chiral odd GPDs → connection to transversity

how to measure GPDs ?



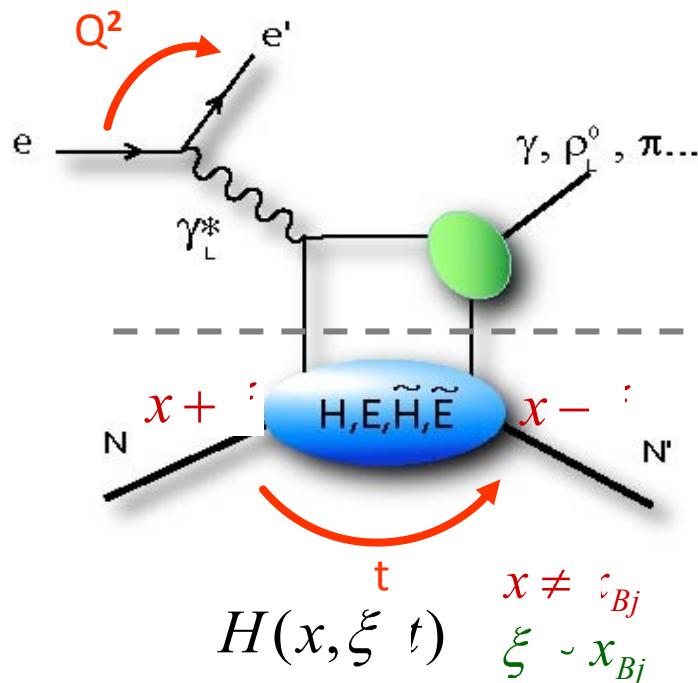
$Q^2 \gg, t \ll$

appear in factorisation theorem for *hard exclusive processes*

- DVCS: most clean process, (some) flavour dependent info from p & n target

$\rightarrow H, \tilde{H}, E, \tilde{E}$

how to measure GPDs ?



$Q^2 \gg, t \ll$

appear in factorisation theorem for *hard exclusive processes*

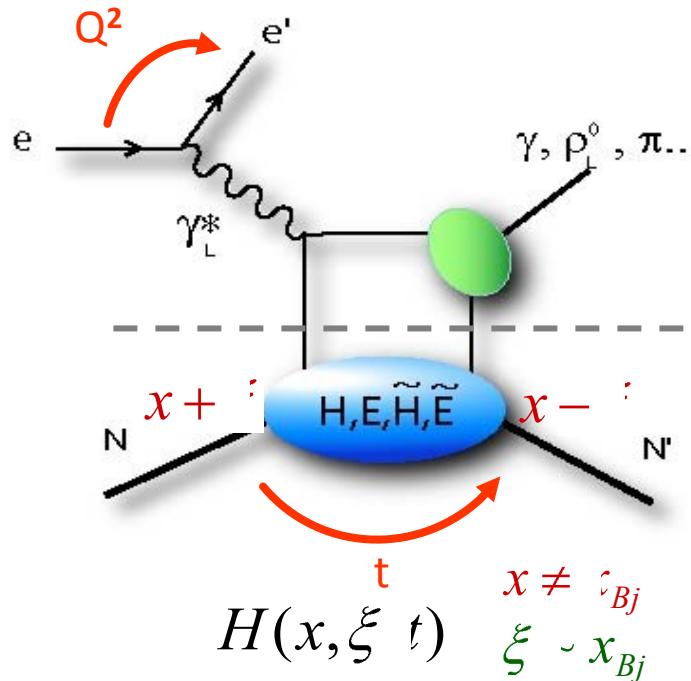
- DVCS: most clean process, (some) flavour dependent info from p & n target
- DVMP: flavour decomposition; gluons:

$\rightarrow H, \tilde{H}, E, \tilde{E}$

VM $\rightarrow H, E$

PS $\rightarrow \tilde{H}, \tilde{E}$

how to measure GPDs ?



$Q^2 \gg, t \ll$

appear in factorisation theorem for *hard exclusive processes*

- DVCS: most clean process, (some) flavour dependent info from p & n target

- DVMP: flavour decomposition; gluons:

BUT:

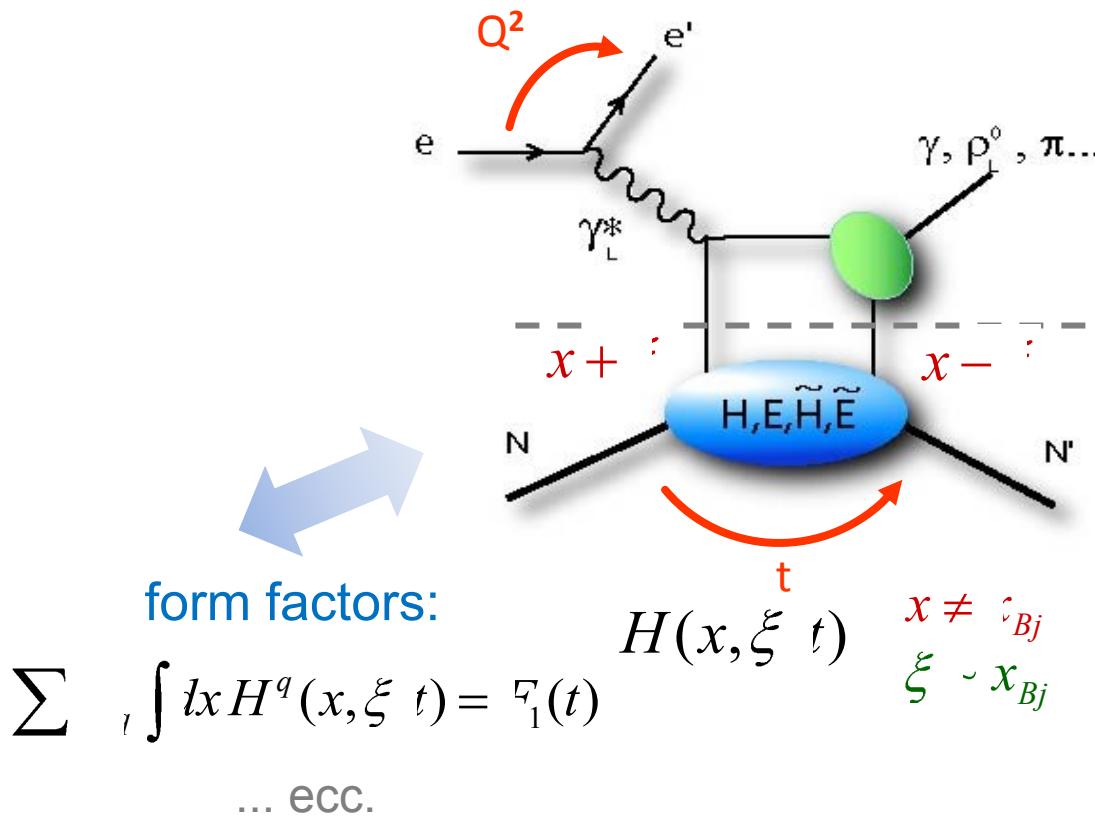
- factorisation only for σ_L
- meson distribution amplitude needed
- large NLO & power corrections

$\rightarrow H, \tilde{H}, E, \tilde{\bar{E}}$

VM $\rightarrow H, E$

PS $\rightarrow \tilde{H}, \tilde{E}$

constraints of GPDs



$Q^2 \gg, t \ll$

appear in factorisation theorem for hard exclusive processes

PDFs :

$$H^{q,g}(x,0,0) = q(x)$$

$$\tilde{H}^{q,g}(x,0,0) = \Lambda(x)$$

$$H_T^q(x,0,0) = h_l(x)$$

E, \tilde{E} : nucleon helicity flip \rightarrow don't appear in DIS

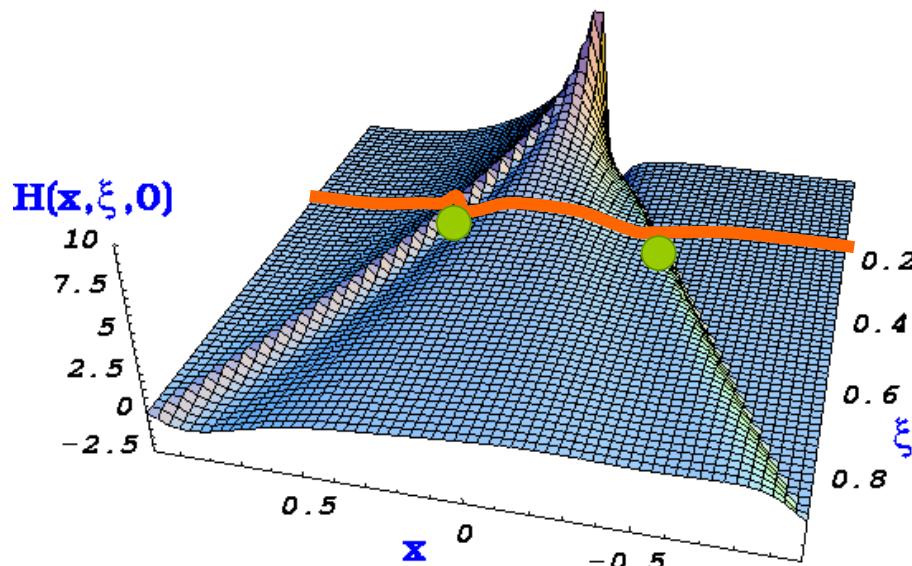
- + Lorentz invariance: polynomiality
- + lattice calculations

extracting GPDs: caveats

$$T_{\mu\nu} = [\mathcal{H}, \mathcal{E}, \tilde{\mathcal{H}}, \tilde{\mathcal{E}}](\xi, t, Q^2), \quad \mathcal{F}(\xi, t, Q^2) = \int_{-1}^1 dx C^-(\xi, x) F(x, \xi, t, Q^2),$$

Compton Form Factor (CFF)

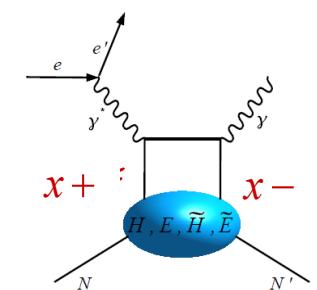
- x is mute variable (integrated over), needs deconvolution
→ apart from ‘cross over’ trajectory ($x = \xi$) GPDs not directly accessible
- extrapolation $t \rightarrow 0$ model dependent



cross section & beam charge asymmetry $\sim \text{Re}(T^{\text{DVCS}})$

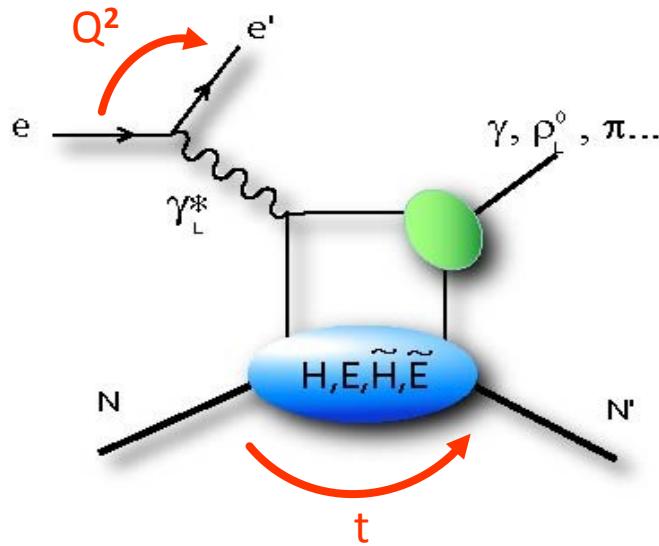
beam or target spin asymmetries $\sim \text{Im}(T^{\text{DVCS}})$

→ x scan of GPDs from Q^2 evolution: *EIC*



the ideal experiment for measuring hard exclusive processes

$Q^2 \gg, t \ll$



- high & variable beam energy
 - ensure hard regime
 - wide kinematic range
 - L/T separation for ps meson prod.
- high luminosity
 - small cross sections
 - fully differential analysis
- hermetic detectors
 - ensure exclusivity

... doesn't exist (yet)...

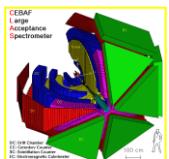
experimental prerequisites



- polarised 27GeV e+/e-
 - unpolarised 920GeV p
 - ≈full event reconstruction
-
- polarised 27GeV e+/e-
 - long+transv polarised p, d targets
 - unpolarised nuclear targets
 - missing mass technique
 - 2006/7 data taken with recoil det.



experimental prerequisites



Hall-A

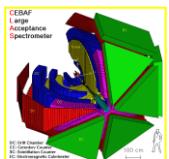
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- highly polarised, high lumi 6GeV e-
- long polarised effective p, n targets
- missing mass/energie technique



experimental prerequisites



Hall-A



- polarised 27GeV e+/e-
- unpolarised 920GeV p
- ≈full event reconstruction

- polarised 27GeV e+/e-
- long+transv polarised p, d targets
- unpolarised nuclear targets
- missing mass/energie technique
- 2006/7 data taken with recoil det.

- highly polarised, high lumi 6GeV e-
- long polarised effective p, n targets
- missing mass/energie technique

- highly polarised, 160GeV μ
- long+transv polarised effective p, d targets
- missing mass/energie technique



COMPASS-II with recoil det.

low → high x



HERA collider

$10^{-4} < x_B < 0.02$

sea quarks & gluons

HERMES / JLab

$0.02 < x_B < 0.4$ / $0.1 < x_B < 0.6$

(gluons) (valence) quarks

low → high x



HERA collider

COMPASS

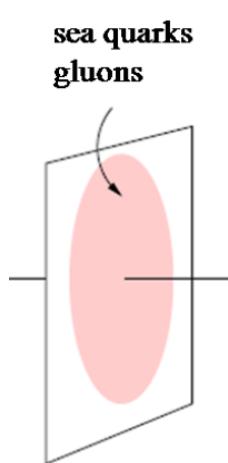
HERMES / JLab

$$10^{-4} < x_B < 0.02$$

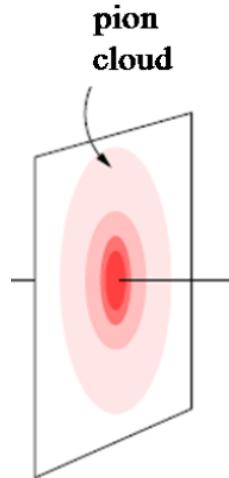
$$0.02 < x_B < 0.4 \quad / \quad 0.1 < x_B < 0.6$$

sea quarks & gluons

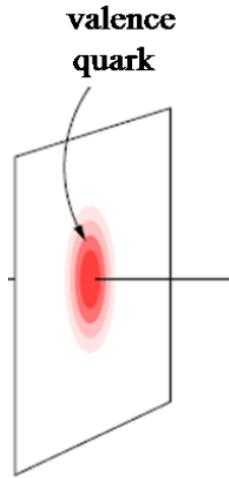
(gluons) (valence) quarks



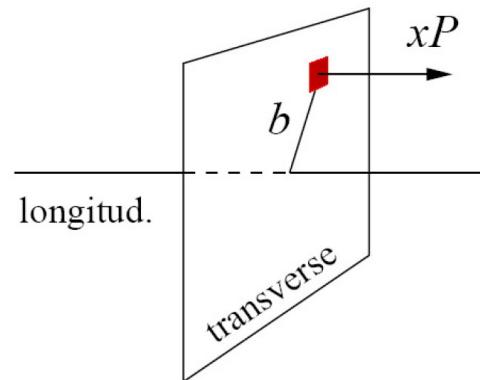
$$x \sim 0.003$$



$$x \sim 0.03$$



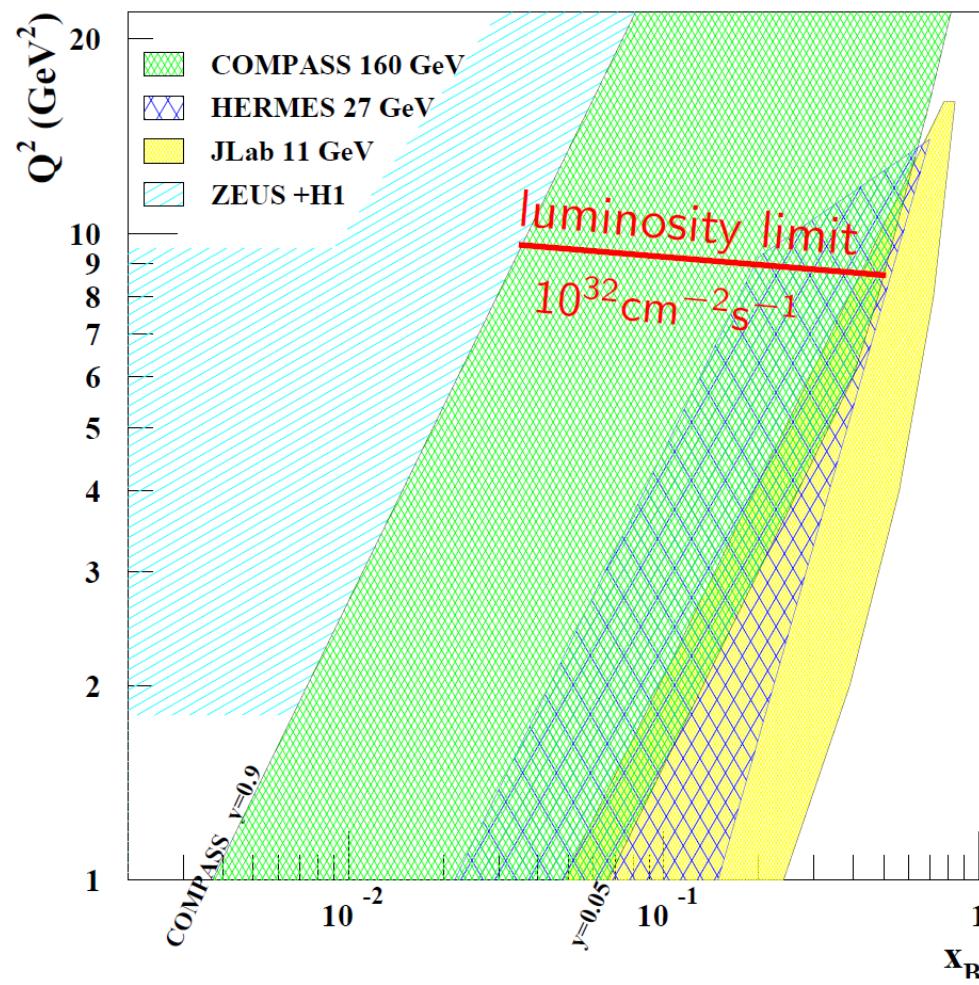
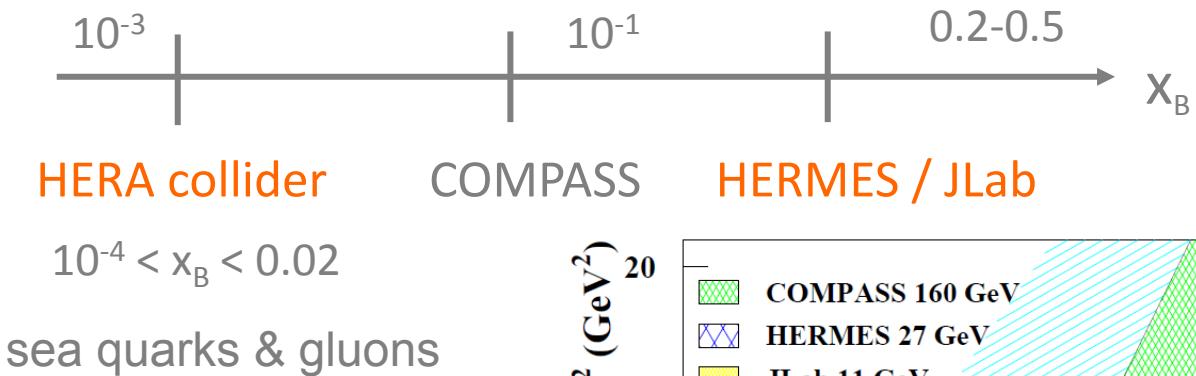
$$x \sim 0.3$$



longitud.

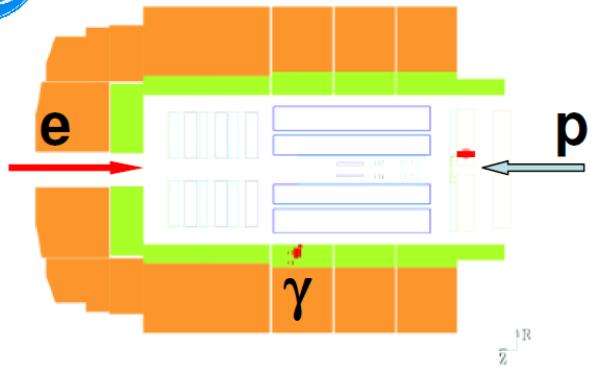
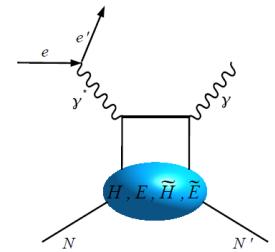
transverse

low → high x



exclusivity

@ the HERA collider experiments

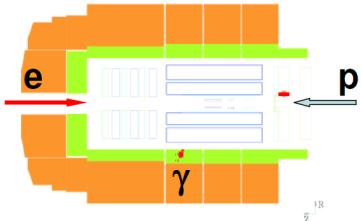


\approx hermetic detector

$\rightarrow p$ escapes through beam pipe

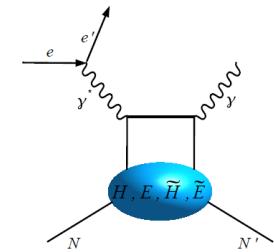


LPS: p tagged control sample

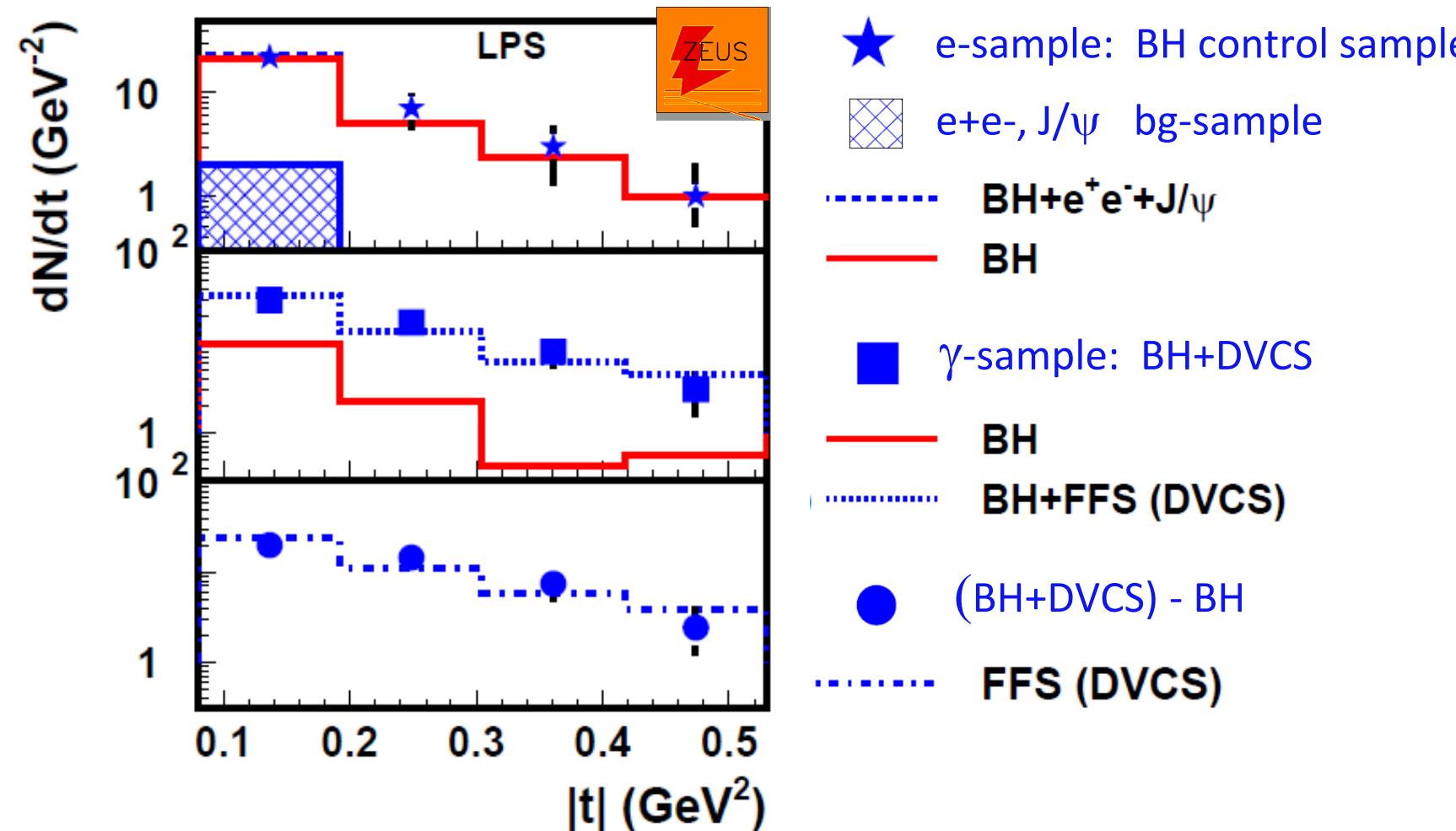


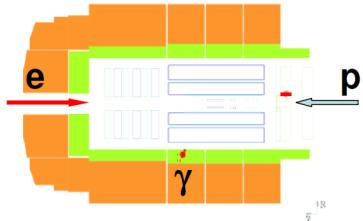
exclusivity

@ the HERA collider experiments



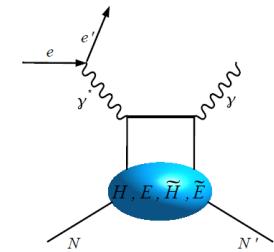
LPS: p tagged data sample



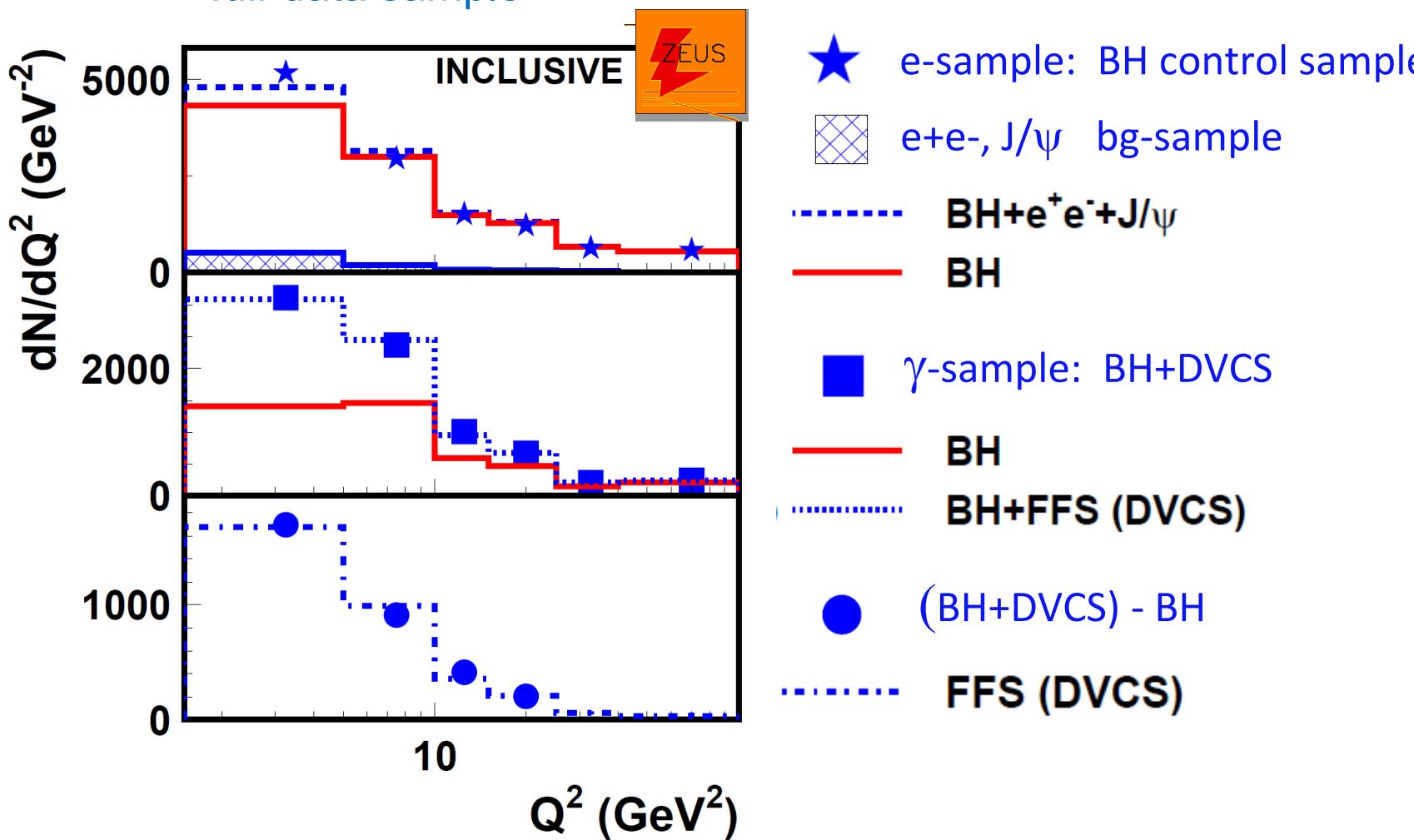


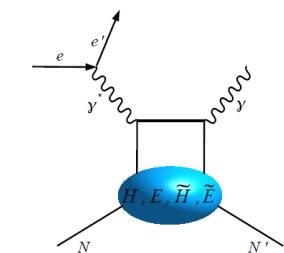
exclusivity

@ the HERA collider experiments



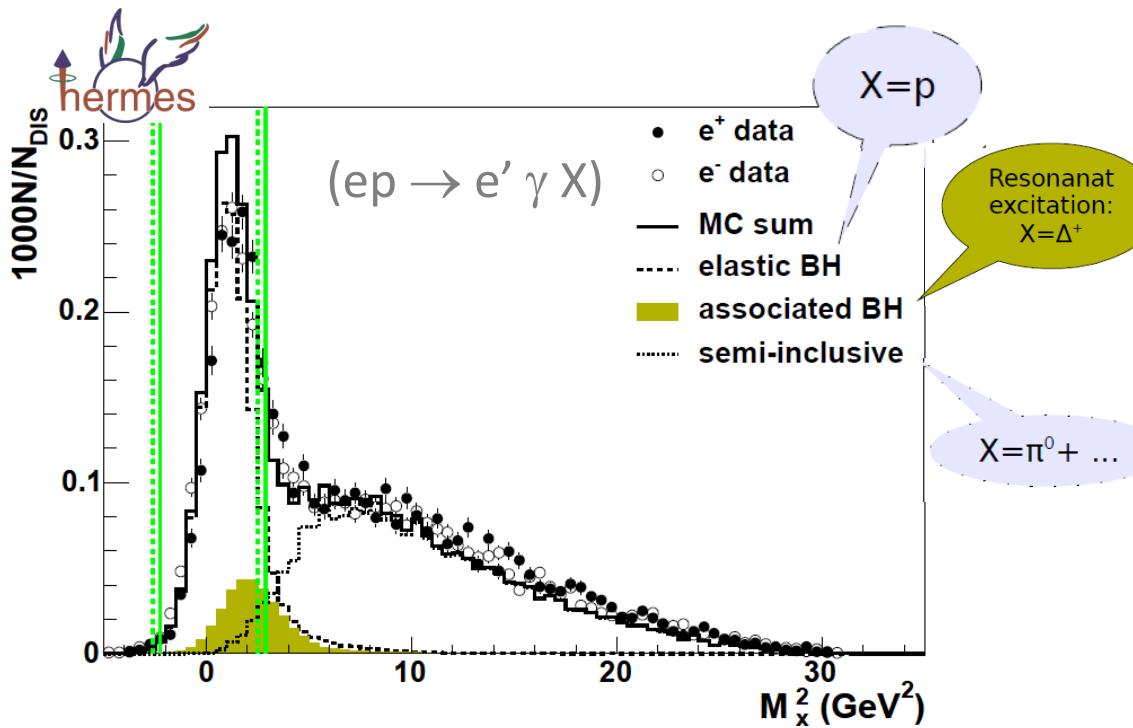
full data sample





exclusivity

fixed target: via missing mass / energy

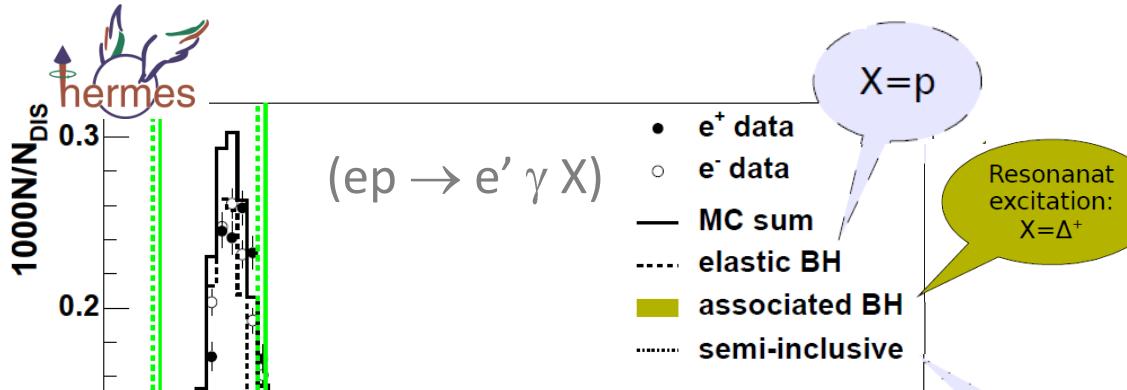
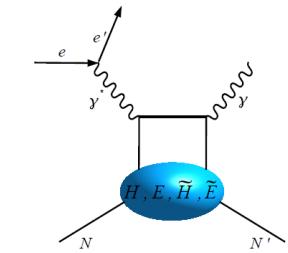


part of the signal

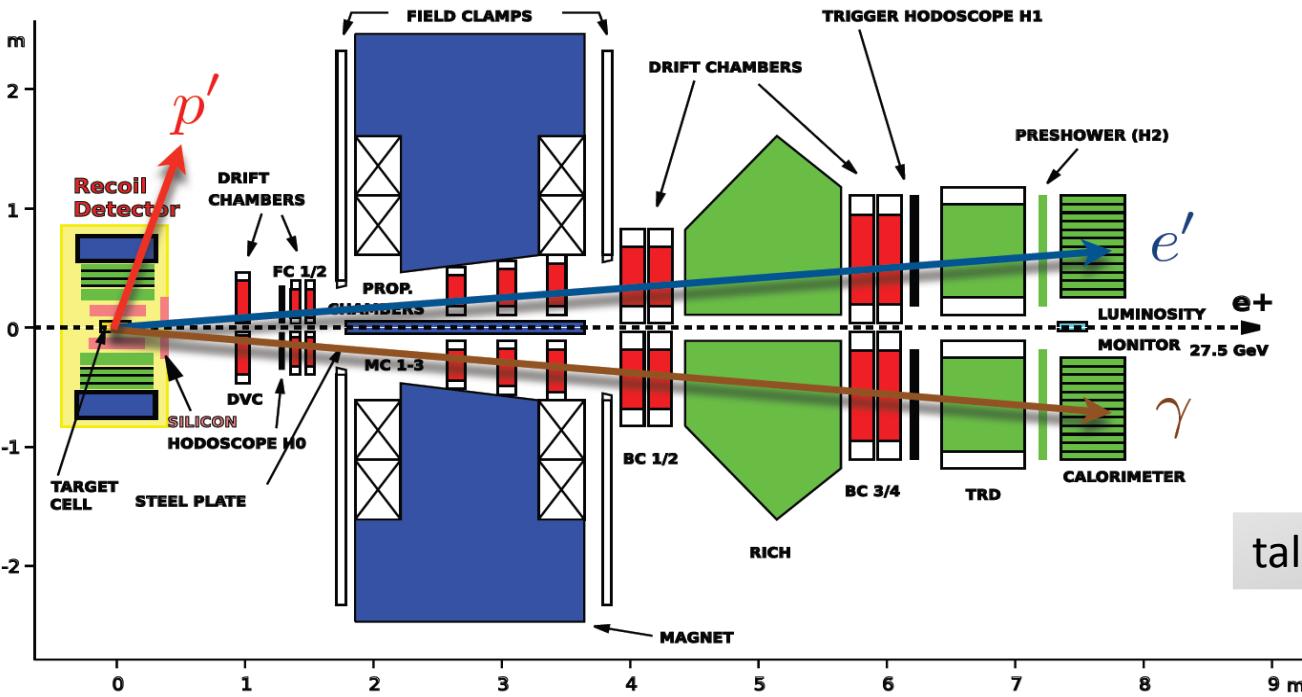
subtracted
very well understood

exclusivity

fixed target: via missing mass / energy



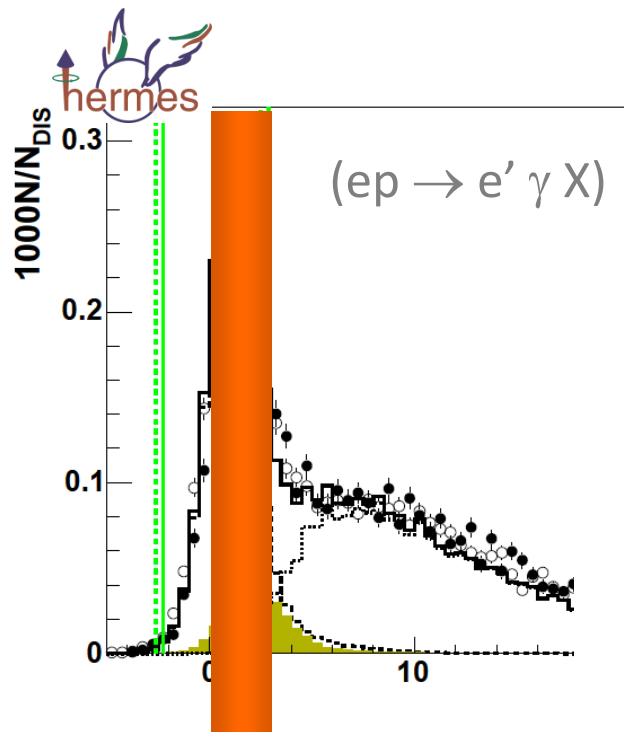
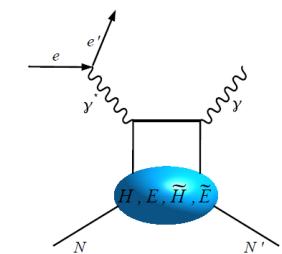
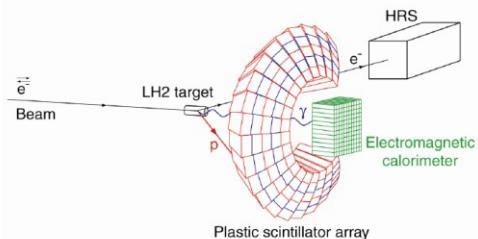
with p detection &
 Δ^+ ID: transition GPDs



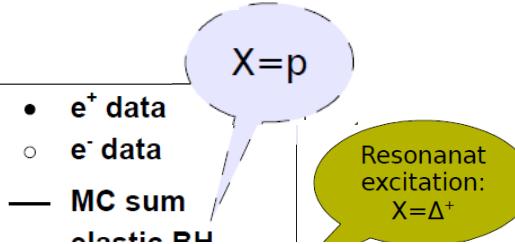
talk by S. Yaschenko

exclusivity

fixed target: via missing mass / energy

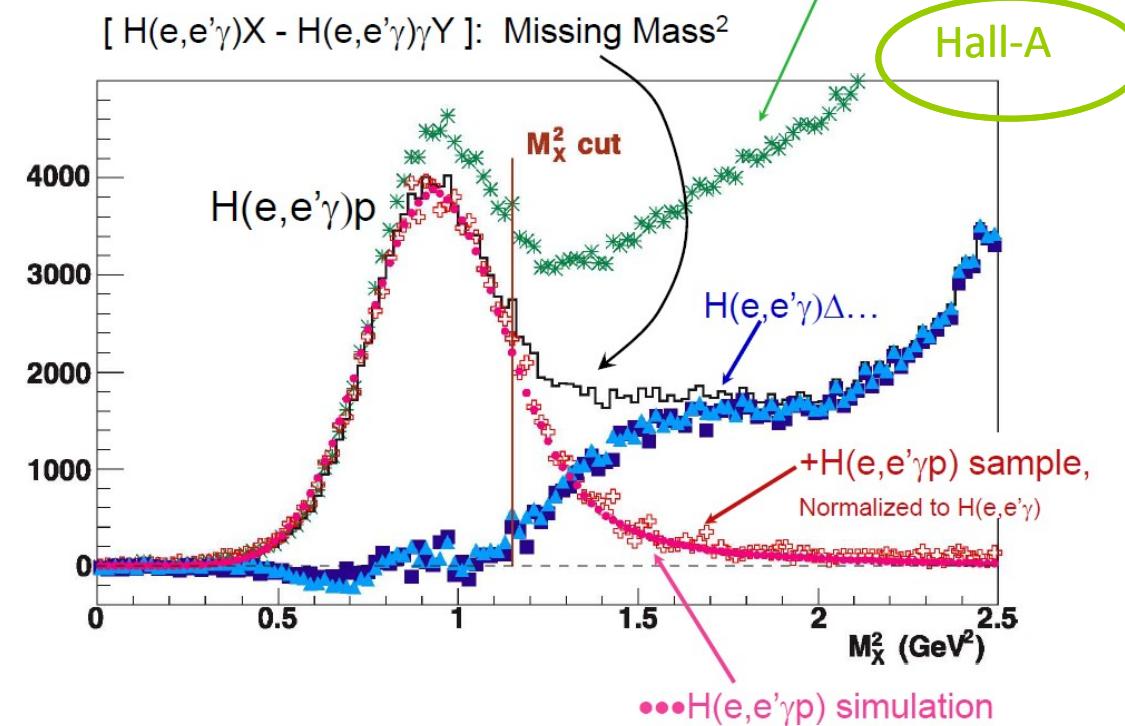


$(ep \rightarrow e' \gamma X)$



part of the signal

Raw $H(e,e'\gamma)X$ Missing Mass² (after accidental subtraction).



Hall-A

results on (off) the menu

data over wide kinematic range: HERA-collider → COMPASS → HERMES → JLab

□ VM production → H, E

- low x: gluon imaging
- high x: quarks & gluons ; role of NLO & power corrections
- low W data from Jlab (→ X. Girod, tomorrow)

□ ps meson production → \tilde{H}, \tilde{E}

- role of transverse photons: CLAS π^0, π^+ A_{LU} , HERMES π^+ A_{UT} , cross sec.
- relation to transversity: $H_T \rightarrow h_1$ from $\pi^0 A_{UT}$

□ DVCS → $H, E, \tilde{H}, \tilde{E}$... the golden channel & most rich plate

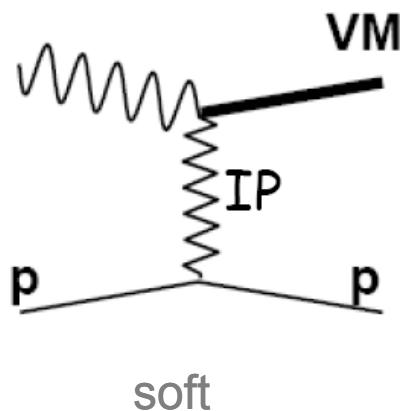
- nuclear modification of DVCS amplitudes: HERMES

□ models & GPDs

□ hunting the OAM

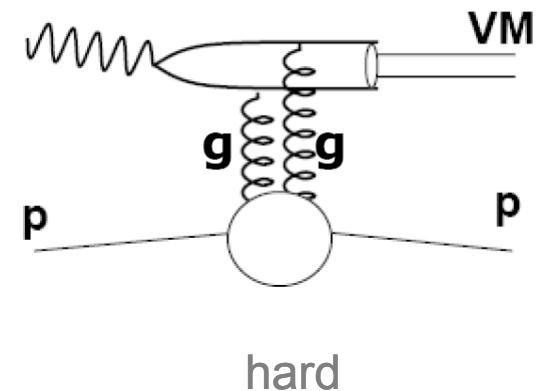
VM production @low x

W & t dependences: probe transition from soft to hard regime



$$\sigma(W) \propto W^\delta$$

$$\frac{d\sigma}{dt} \propto e^{-b|t|}$$



soft

hard

→expect δ to increase from ~0.2 to ~0.8

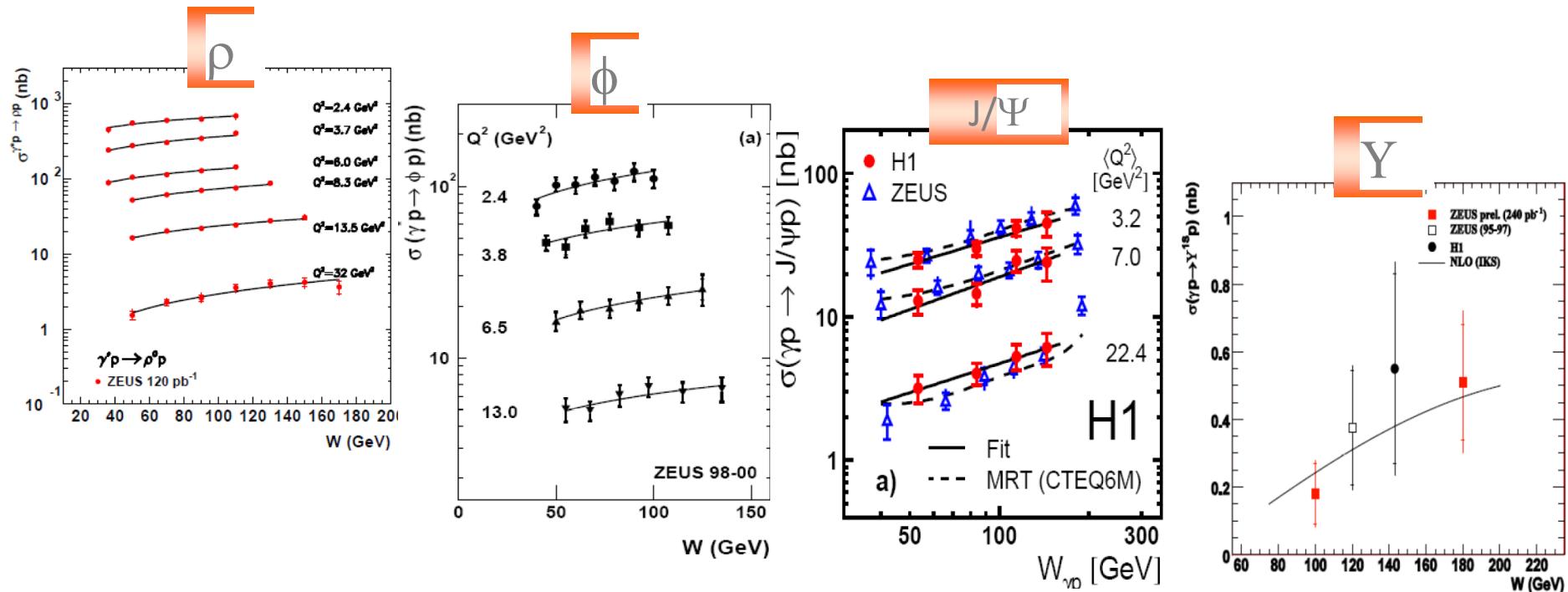
b to decrease from ~10 to ~4-5 GeV 2



VM production @low x



W dependence: probe transition from soft to hard regime



two ways to set a *hard* scale: ▀ large Q^2
▀ mass of produced VM

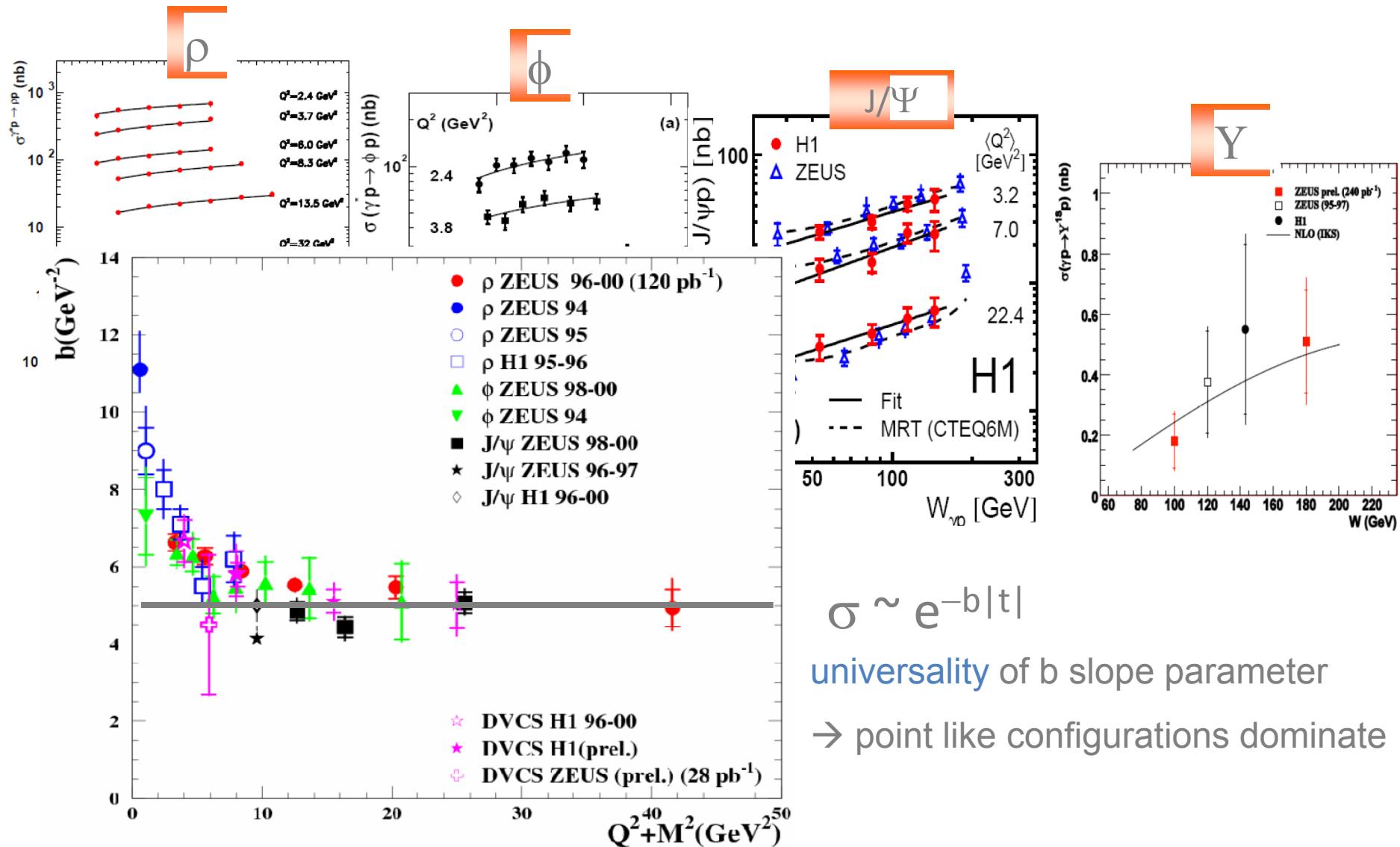
universality: ρ and ϕ at large $Q^2 + M^2$ similar to J/Ψ , Y



VM production @low x

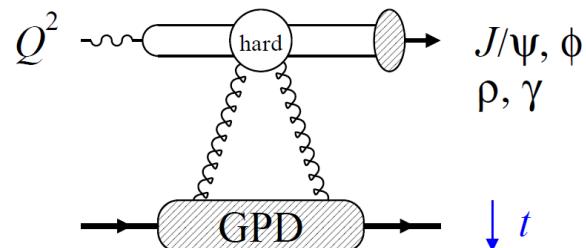
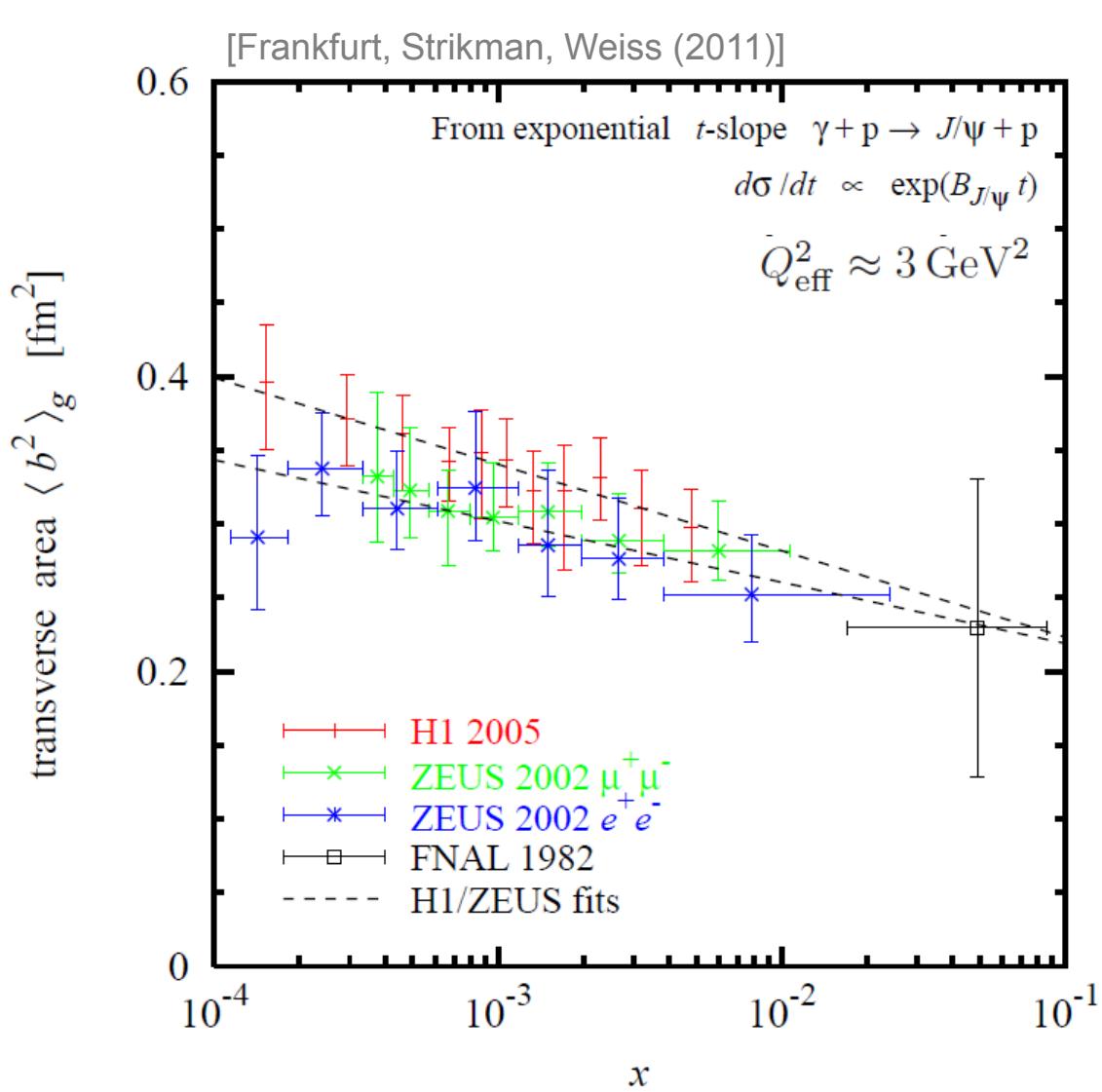


t dependence: probe transition from soft to hard regime



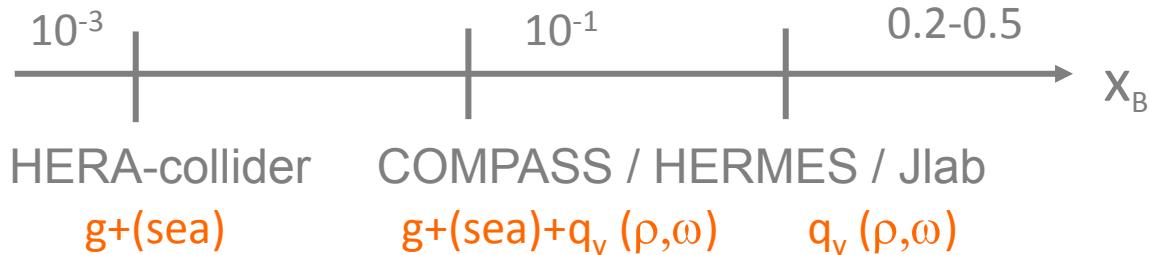


gluon imaging: J/ψ

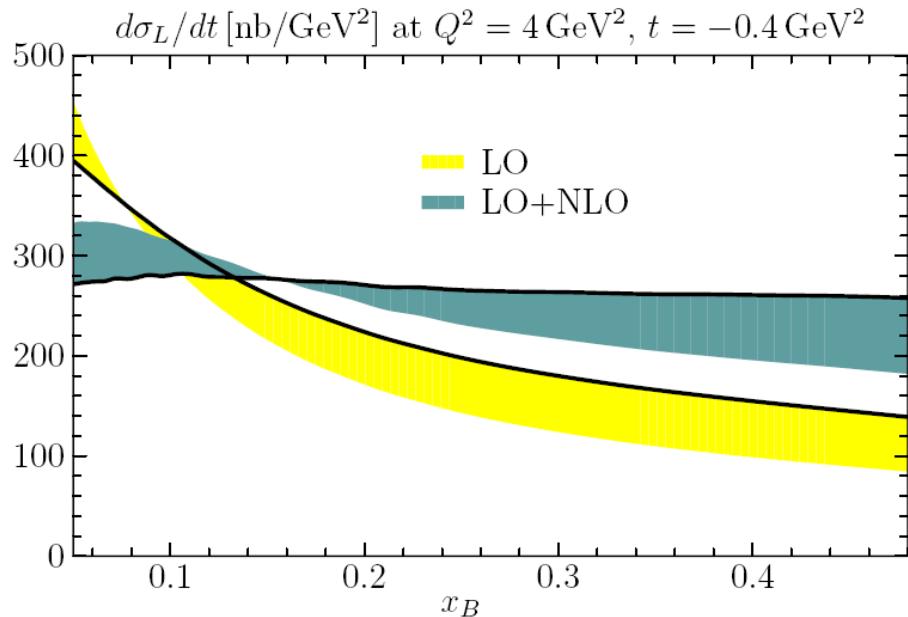


▪ FT \rightarrow average impact parameter

VM production from low → high x

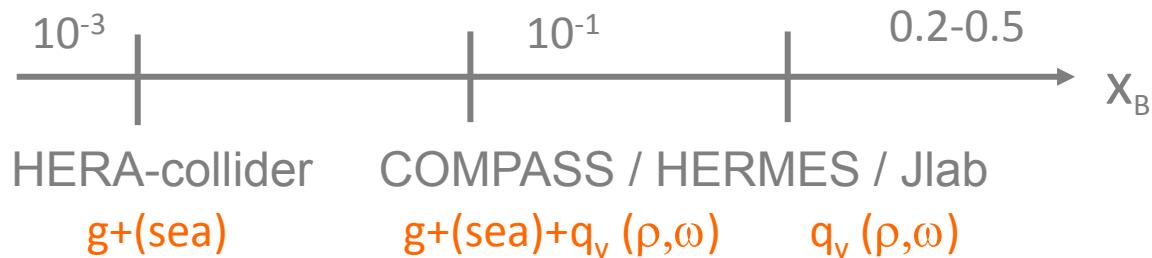


- NLO corrections to VM production are large: [M. Diehl, W. Kugler (2007)]

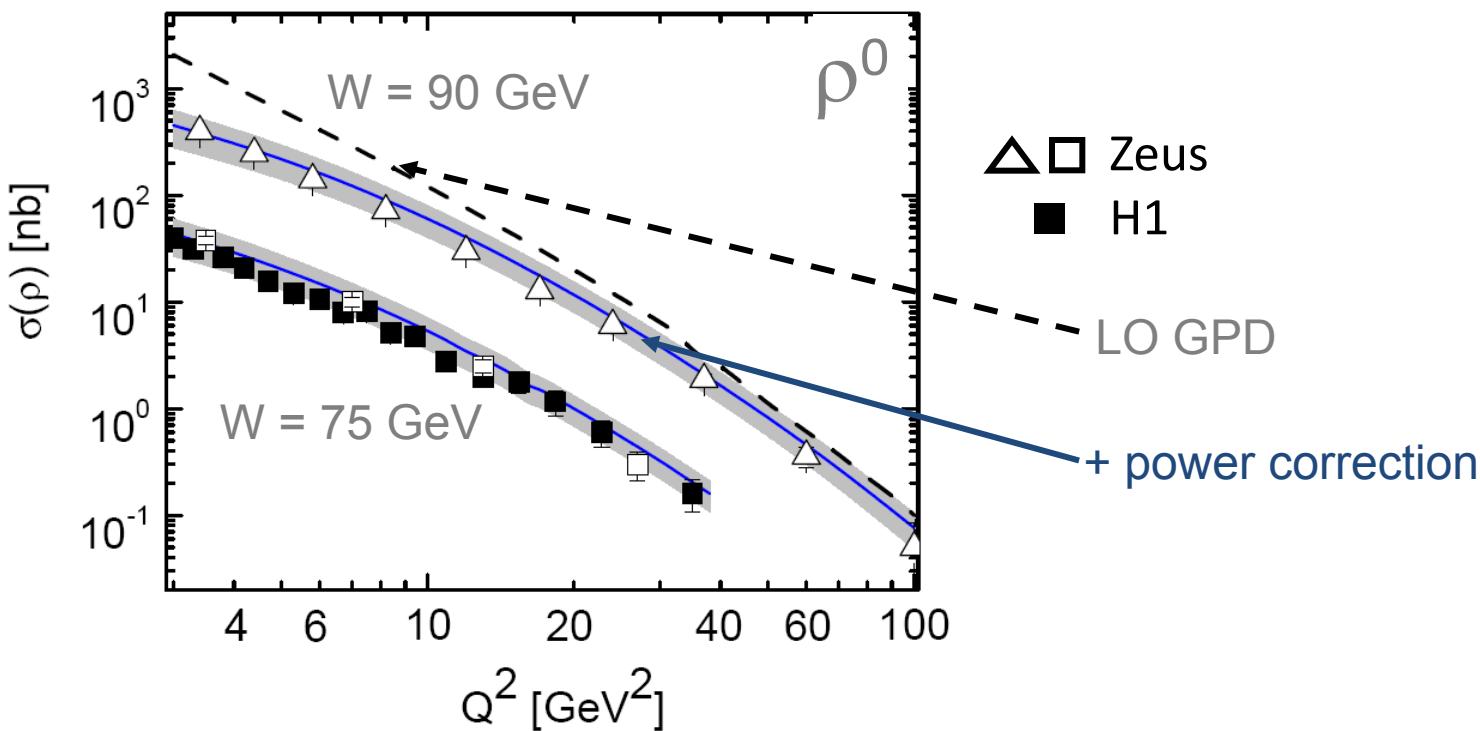


ρ^0 cross section @typical
kinematics of COMPASS /
HERMES / JLab12

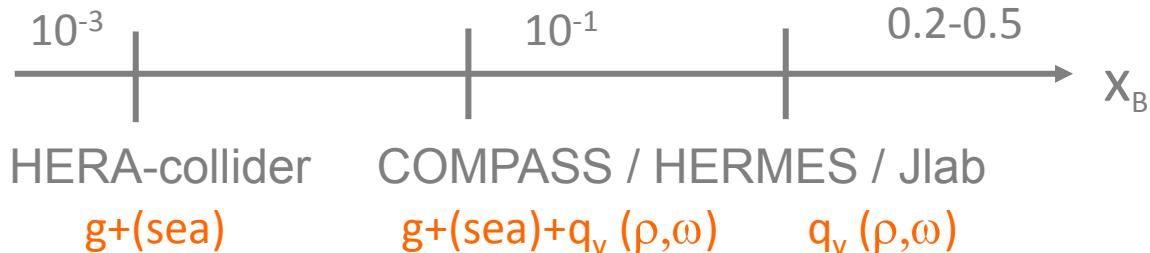
VM production from low → high x



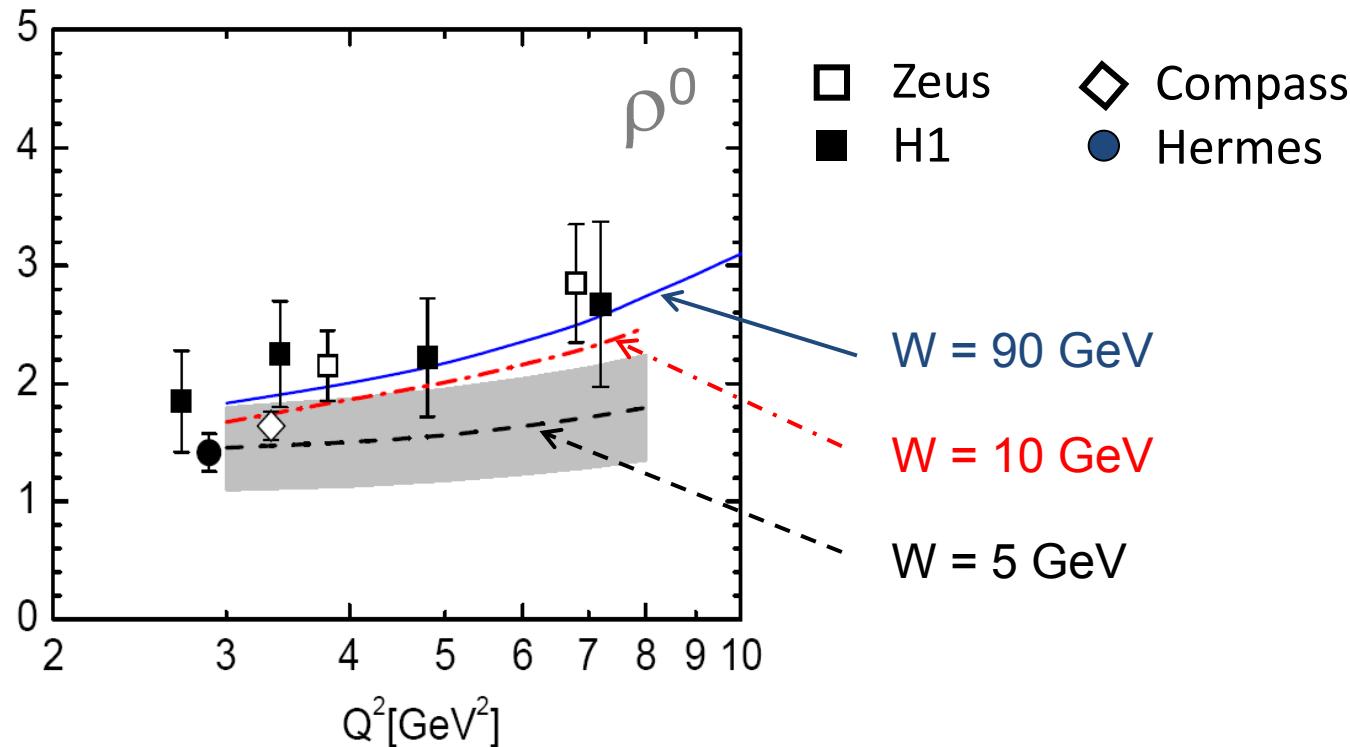
- ... despite, LO GPD model (handback fact.; DD ansatz): [S. Goloskokov, P. Kroll (2007, 2010)]
+ power corrections:



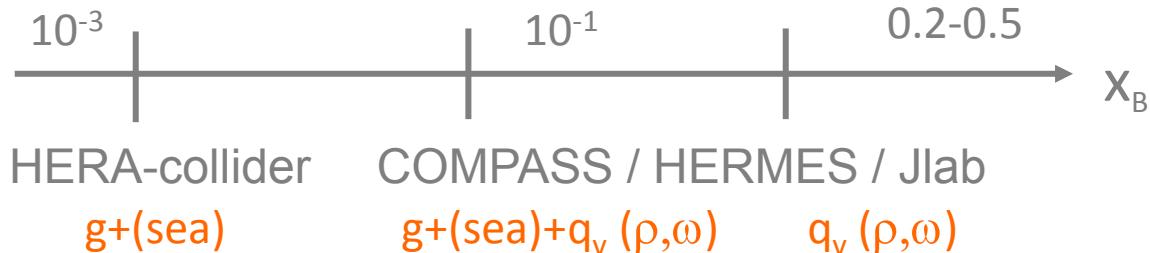
VM production from low → high x



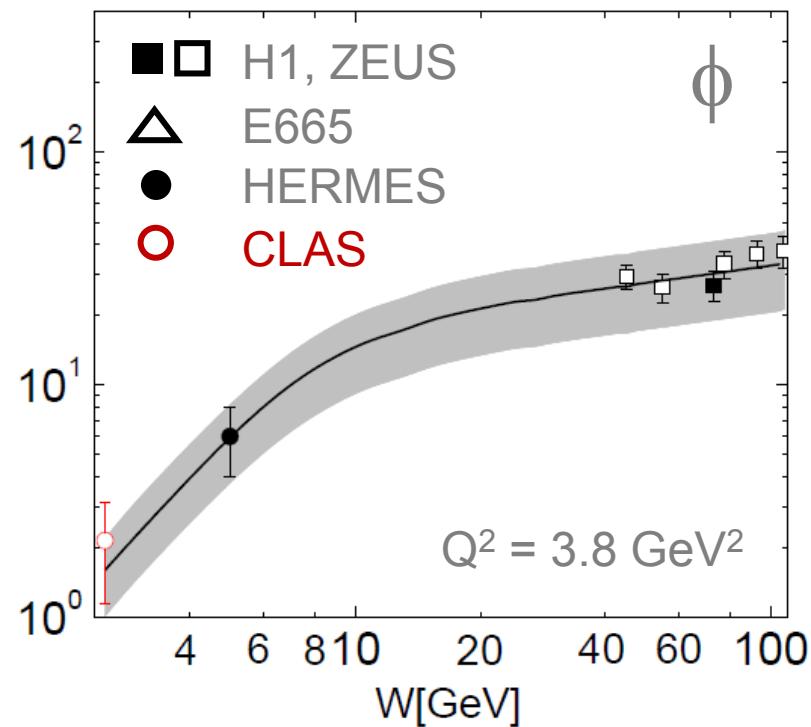
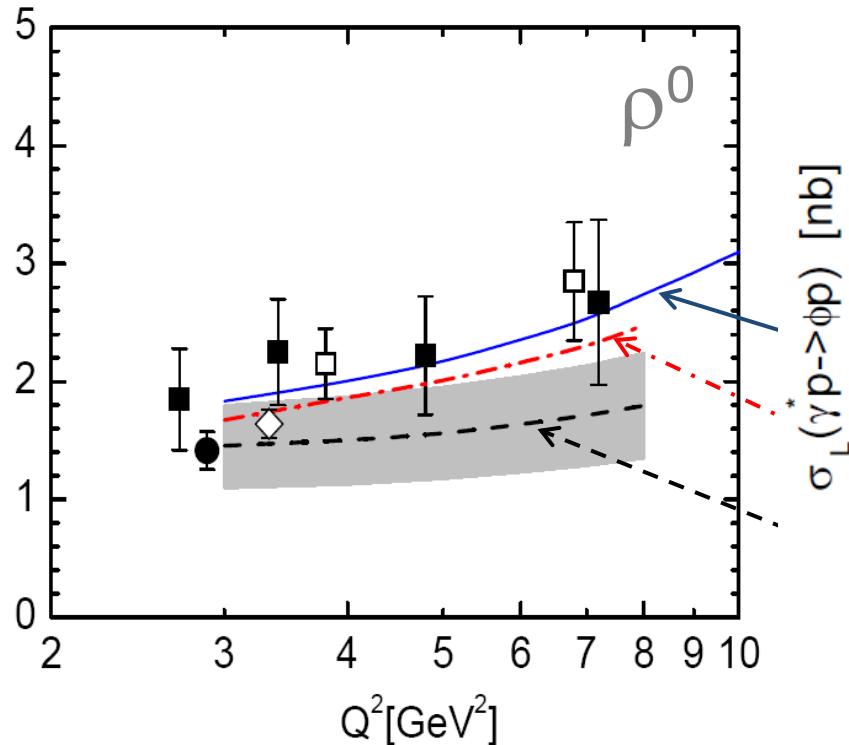
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VM production from low \rightarrow high x



- ... despite, LO GPD model (handback fact.; DD ansatz): [S. Goloskokov, P. Kroll (2007, 2010)]
+ power corrections:

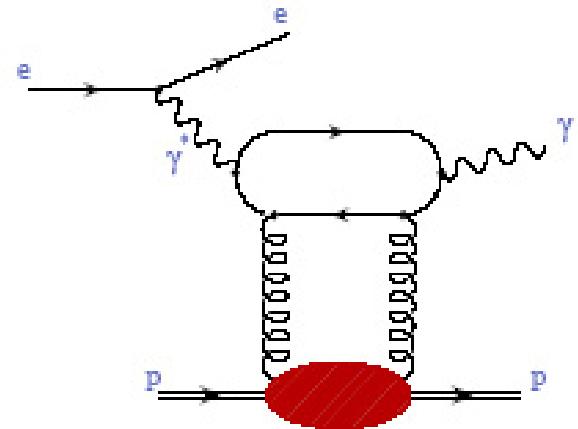


Deeply Virtual Compton Scattering

$\rightarrow H, \tilde{H}, E, \tilde{E}$

- DVCS cross sections @ low x

$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2$$



$$\frac{d\sigma}{dt} \propto e^{-|t|}$$

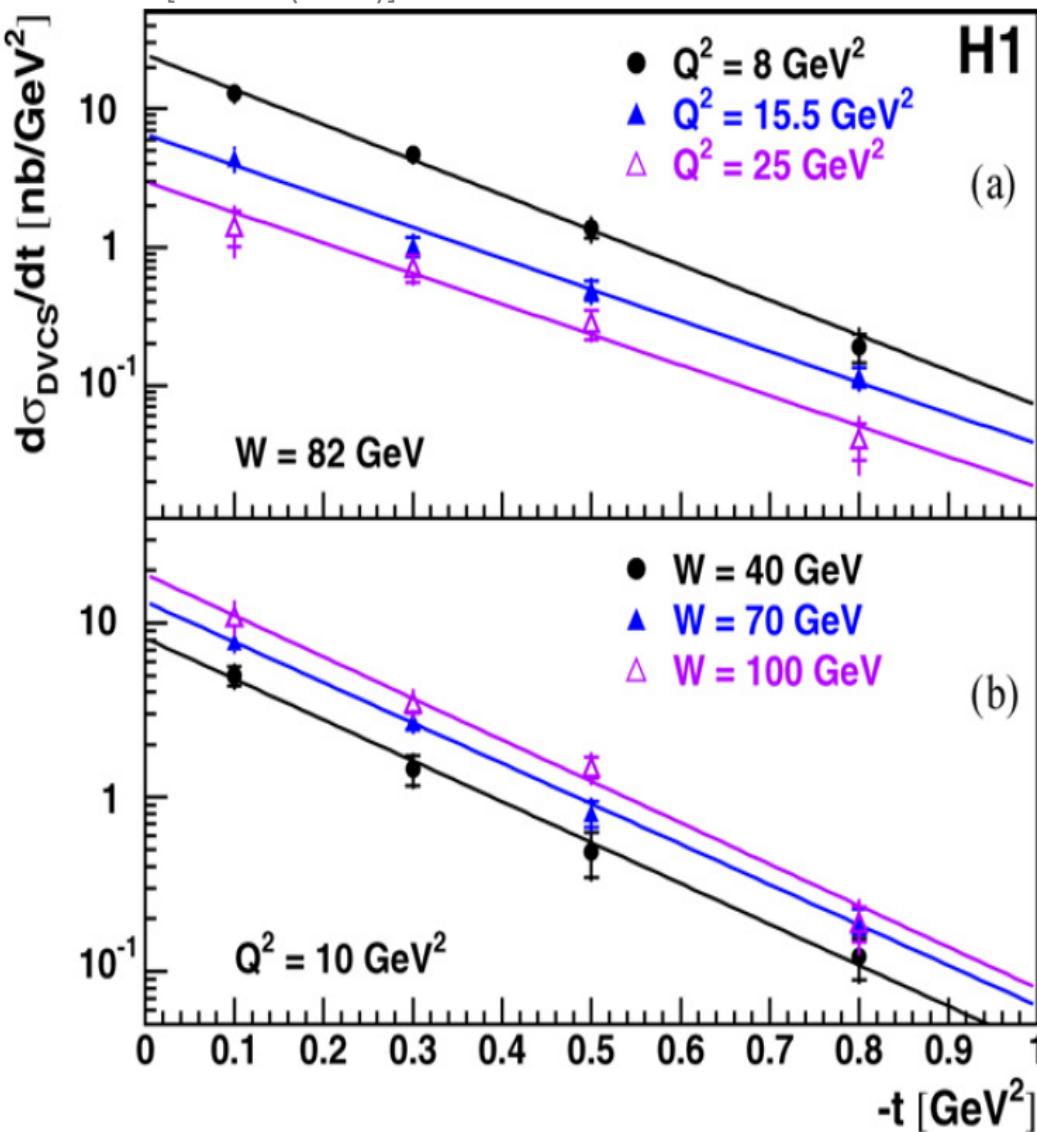
- t slope provides absolute normalisation
- FT \rightarrow average impact parameter



DVCS cross section



[PLB659(2008)]

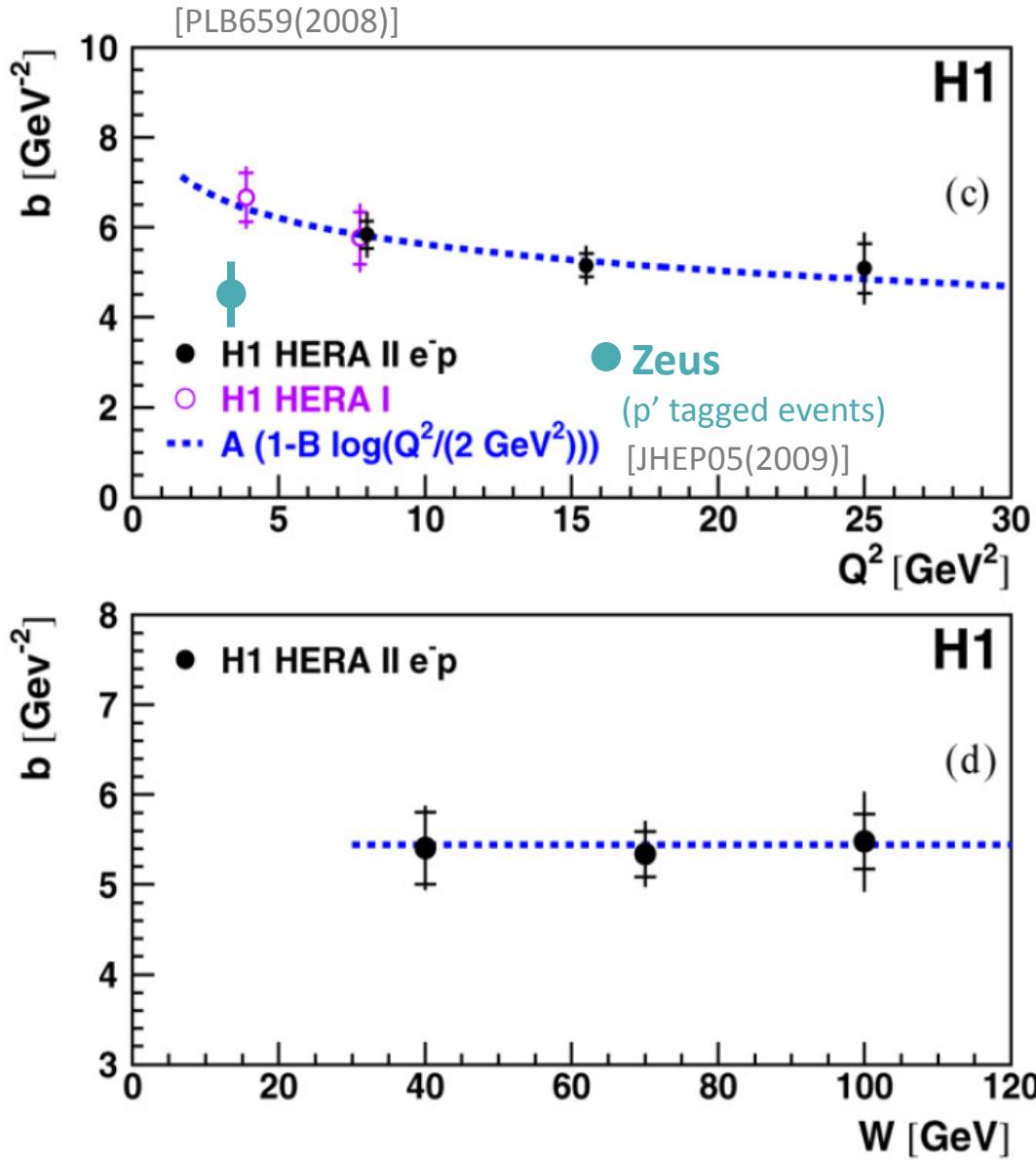


- t slope measurement provides absolute normalisation

$$\frac{d\sigma}{dt} \propto e^{-|t|}$$



DVCS cross section



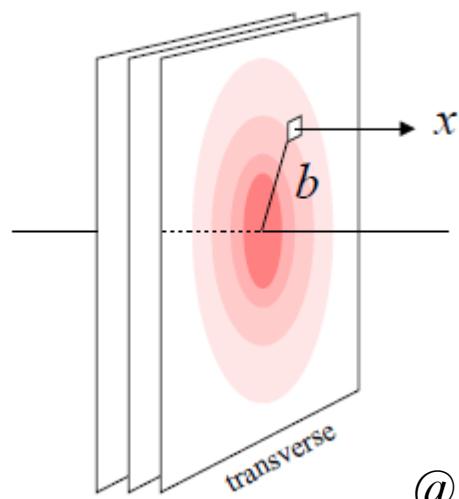
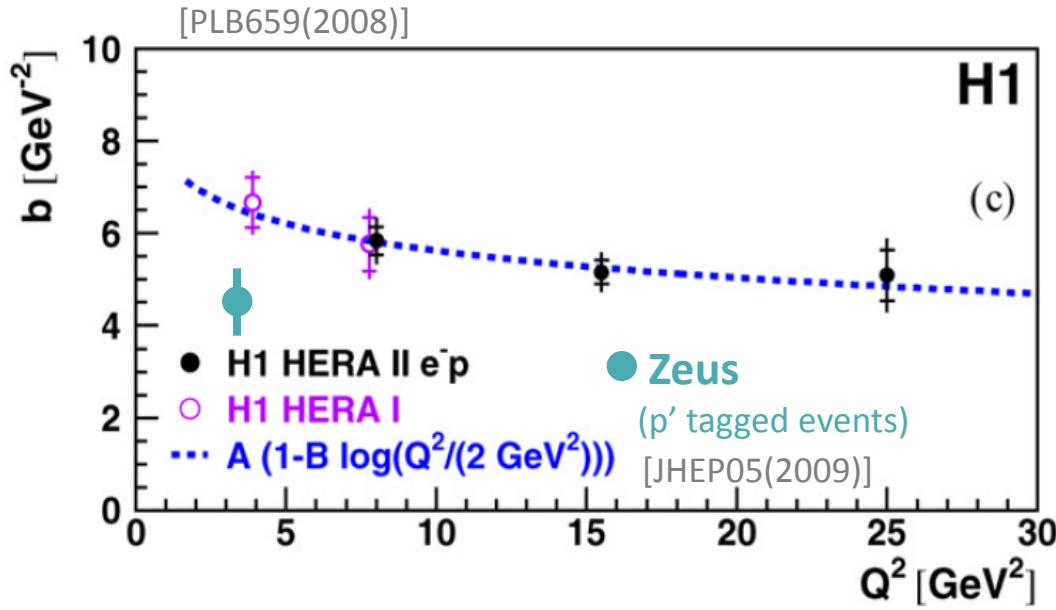
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- universality of slope parameter: pointlike configurations dominate



DVCS cross section



[courtesy of C. Weiss]

@ $x_B = 10^{-3}$

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- $FT \rightarrow$ average impact parameter

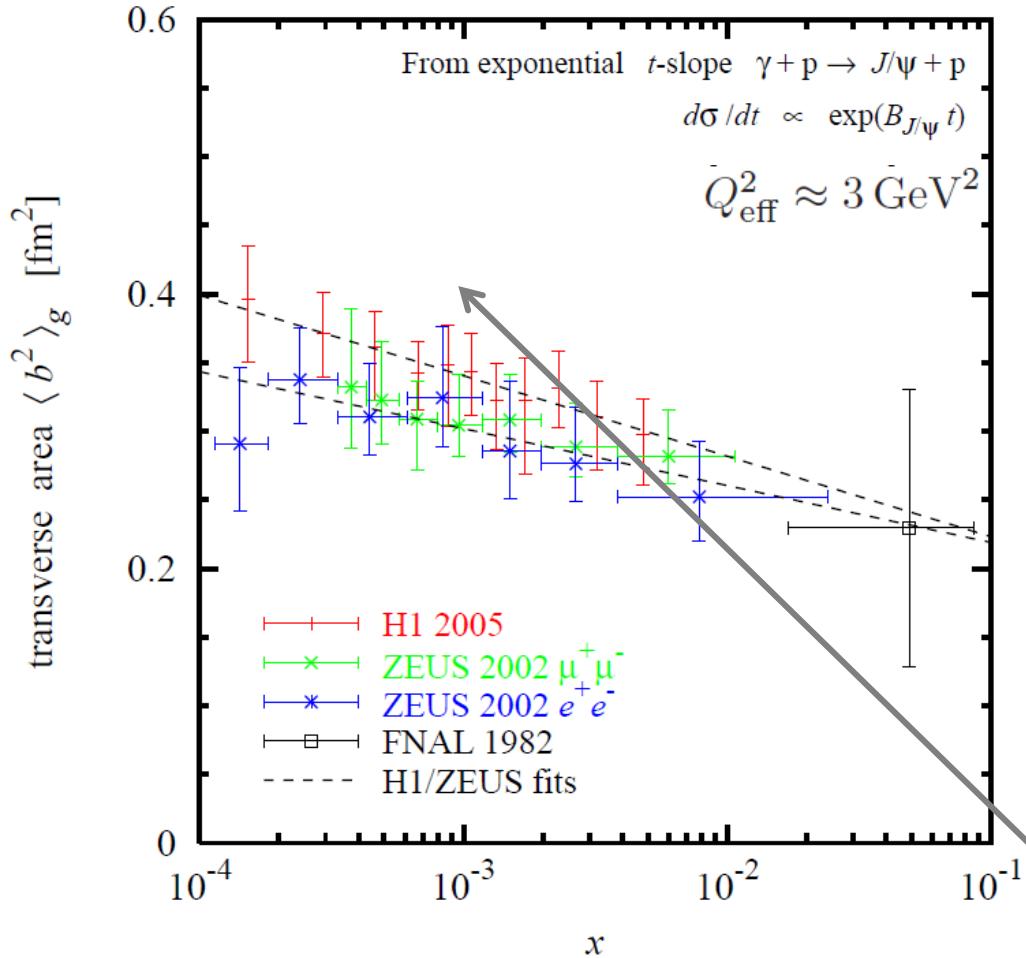
$$\sqrt{\langle b_T^2 \rangle} = 0.65 \pm 0.02 \text{ fm}$$

@ $x_B = 10^{-3}$

$\langle Q^2 \rangle = 8.0 \text{ GeV}^2$



sea quark & gluon imaging



→ remember J/ψ

- universality of slope parameter:
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- $FT \rightarrow$ average impact parameter

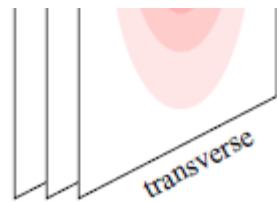
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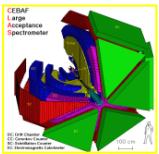
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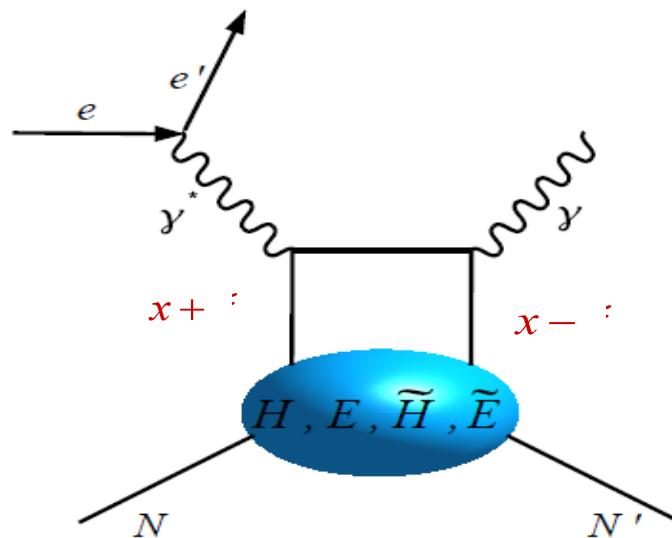


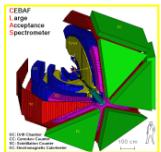


DVCS interference term

$$d\sigma \propto |t_{BH}|^2 + \text{gray oval} + \tau_{BH}^* \tau_{DVCS} + (\tau_{DVCS}^* \tau_{BH})$$

→ bilinear in GPDs → *linear* in GPDs





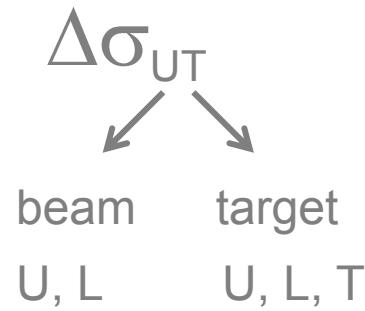
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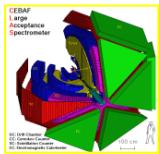
→ bilinear in GPDs → linear in GPDs

isolate interference term:

- different beam charges: $e^+ e^-$ ([only @HERA](#), upcoming @COMPASS)
- polarisation observables



Unpolarised, Longitudinally, Transversely polarised



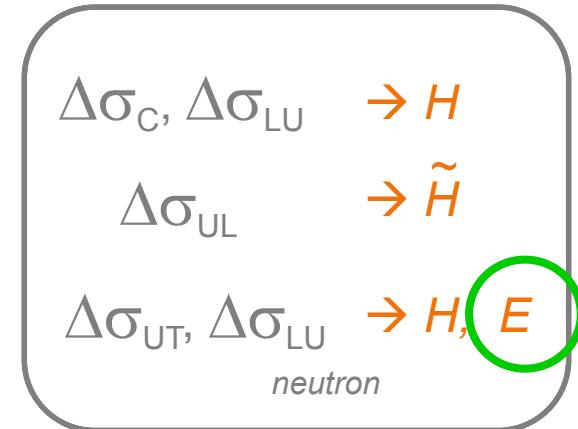
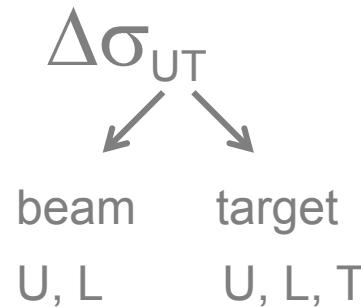
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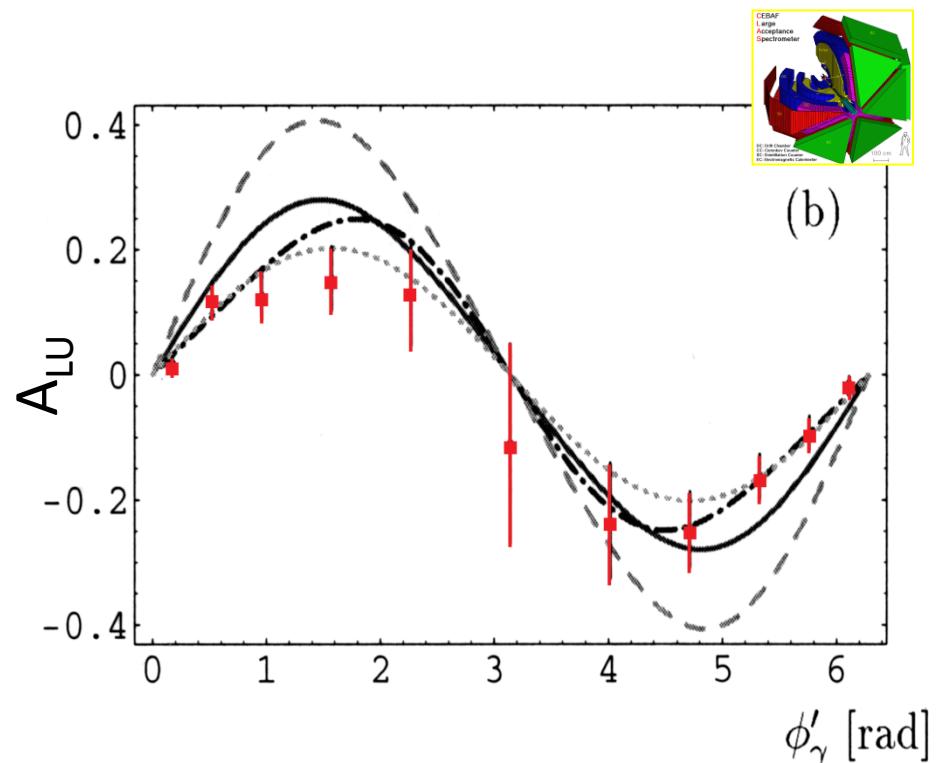
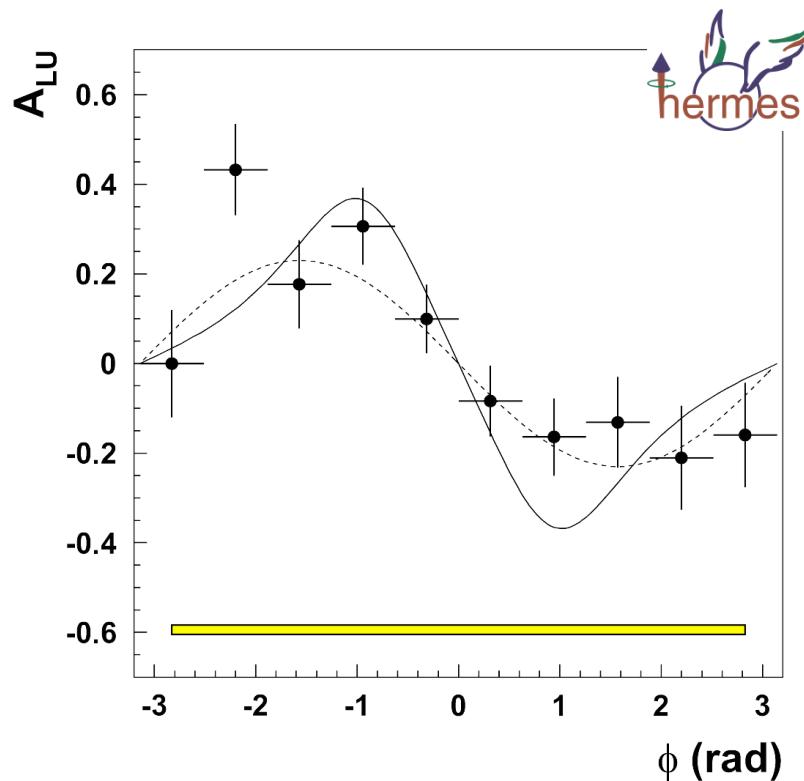


@kinematics of current fixed target exp.

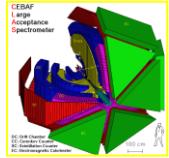
first DVCS signals

-- interference term --

[PRL87(2001)]

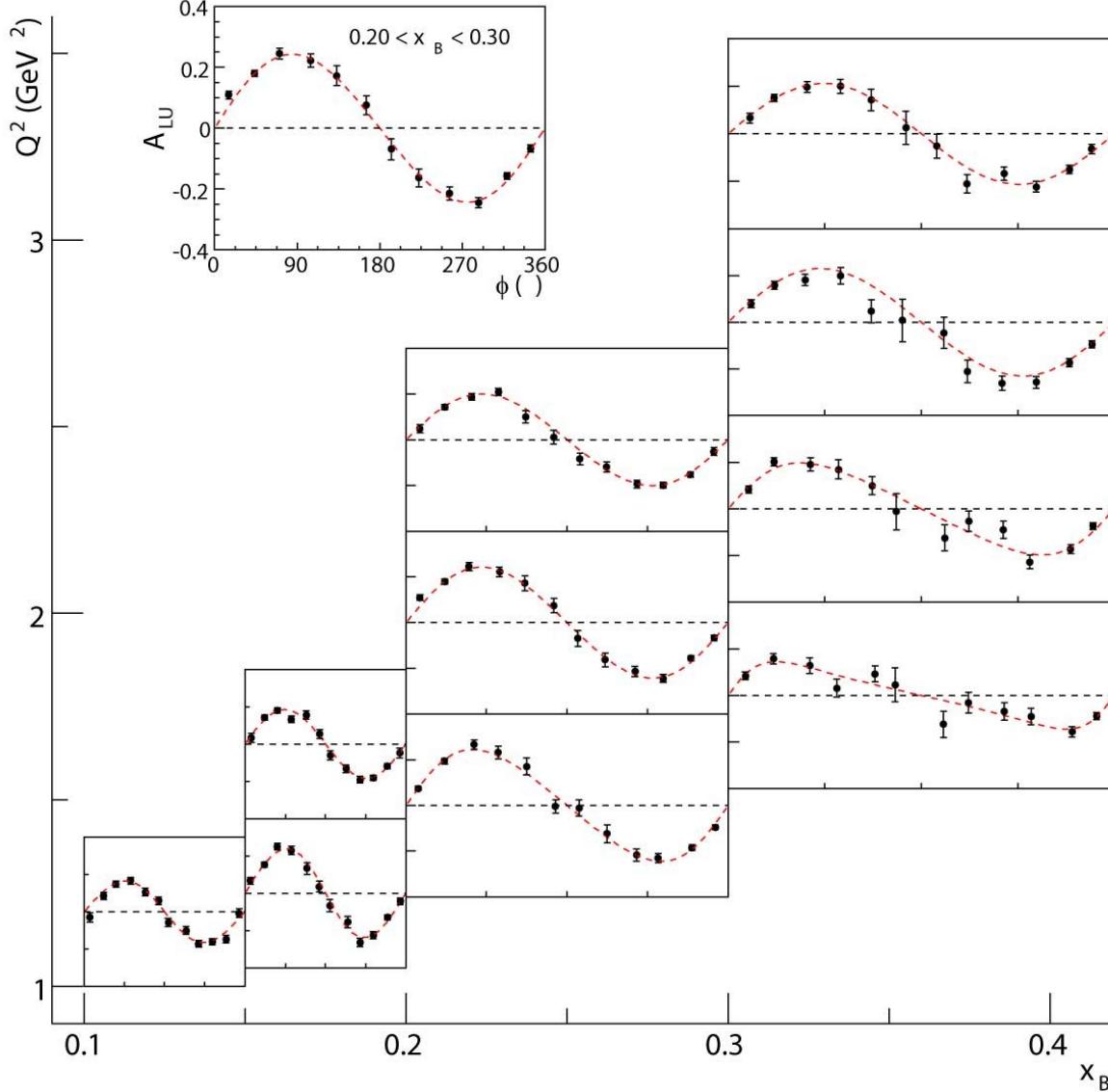


→ $\sin\phi$ dependence indicates dominance of handback contribution

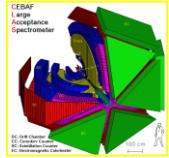


call for high statistics

JLab-e1: DVCS beam-spin asymmetry [PRL100(2008)]

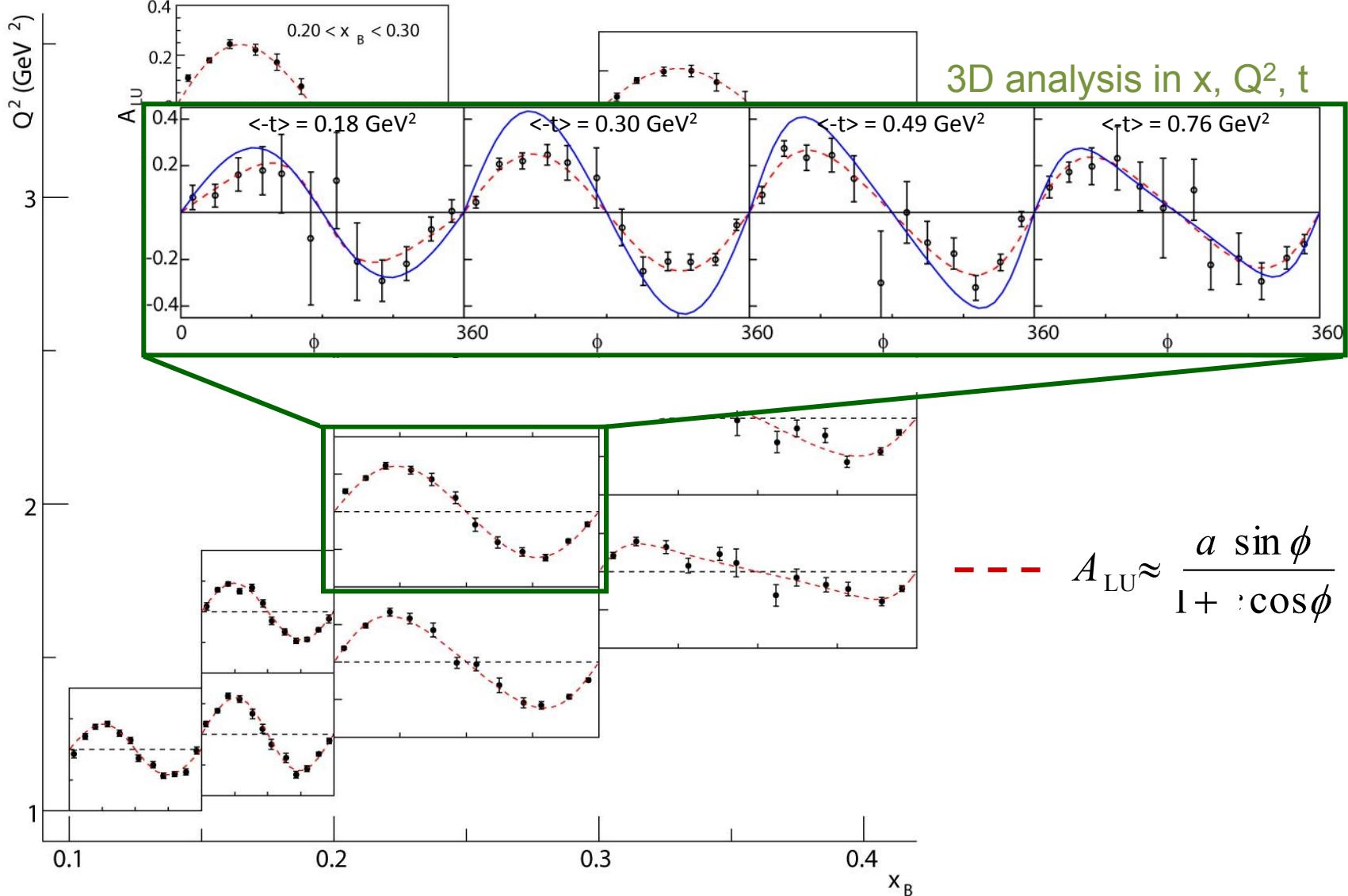


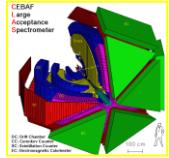
$$A_{LU} \approx \frac{a \sin \phi}{1 + b \cos \phi}$$



call for high statistics

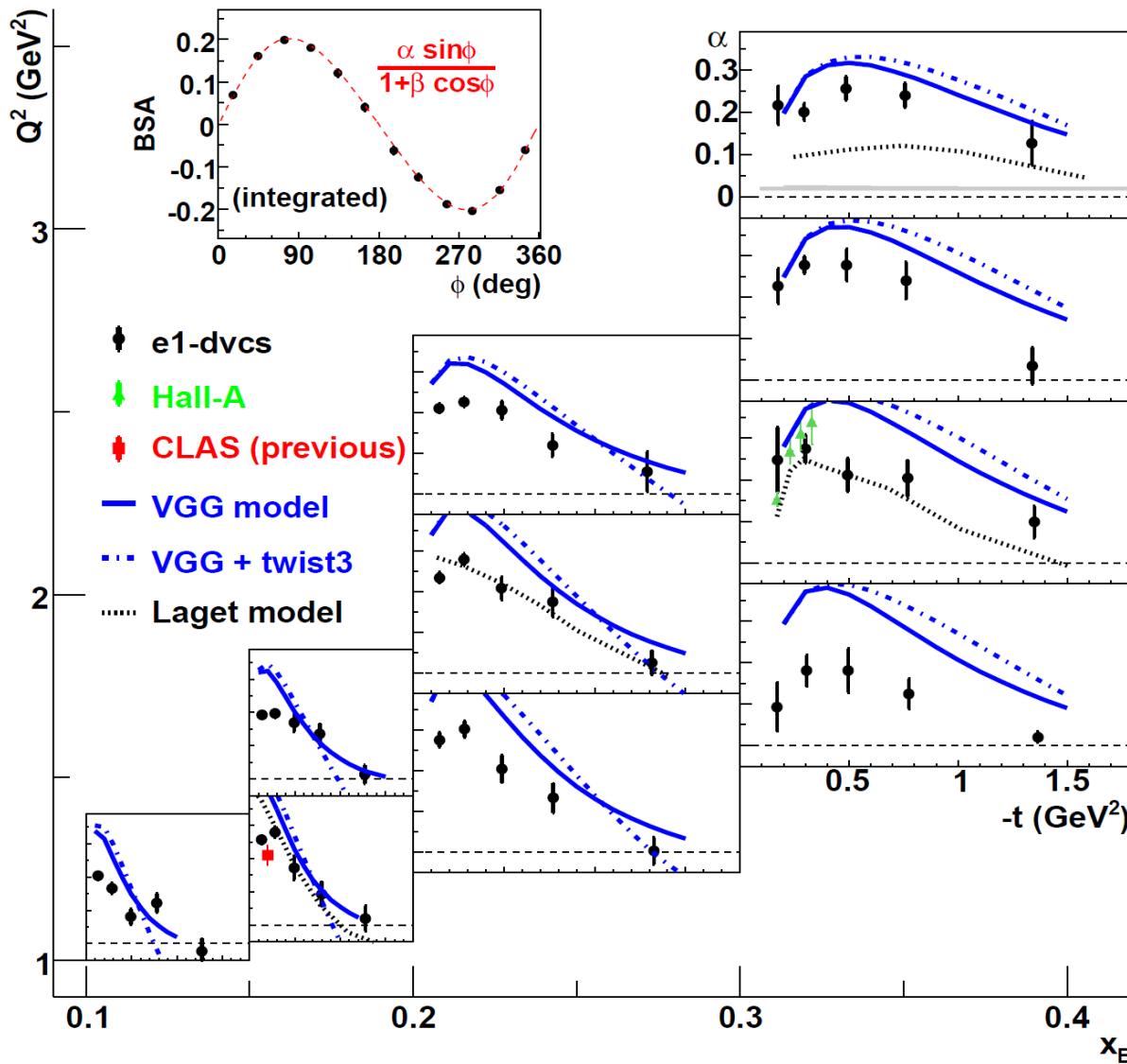
JLab-e1: DVCS beam-spin asymmetry [PRL100(2008)]





call for high statistics

JLab-e1: DVCS beam-spin asymmetry [PRL100(2008)]



$$\alpha \propto n(F_1 H)$$

Hall-A

... cross section from
interference term

talk by X. Girod

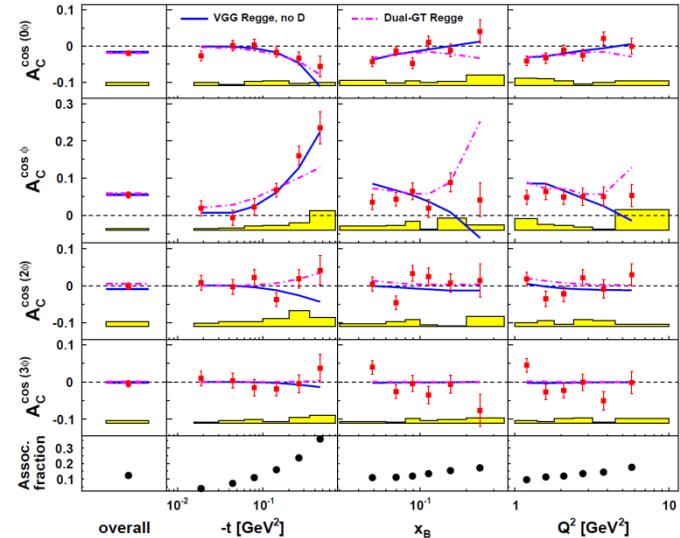
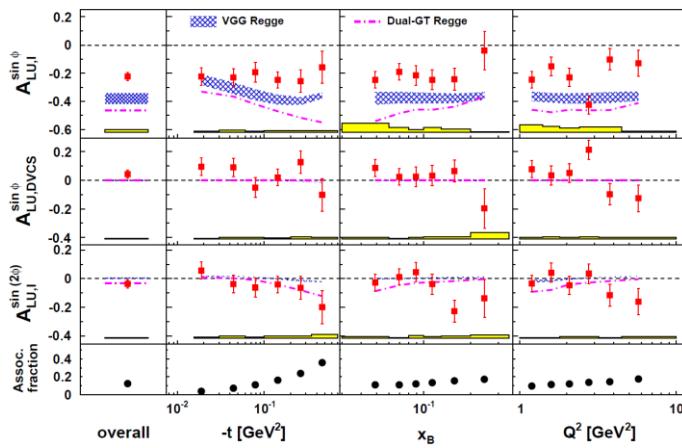
call for new analysis methods

combined analysis of charge & polarisation observables

→ separation of interference & DVCS² amplitudes

$$\sigma_{LU}(\phi; P_1, e_1) = \sigma_{UU}(\phi) \cdot \{1 + P_1 A_{LU}^{\text{DVCS}}(\phi) + e_1 P_1 A_{LU}^I(\phi) + e_1 A_C(\phi)\}$$

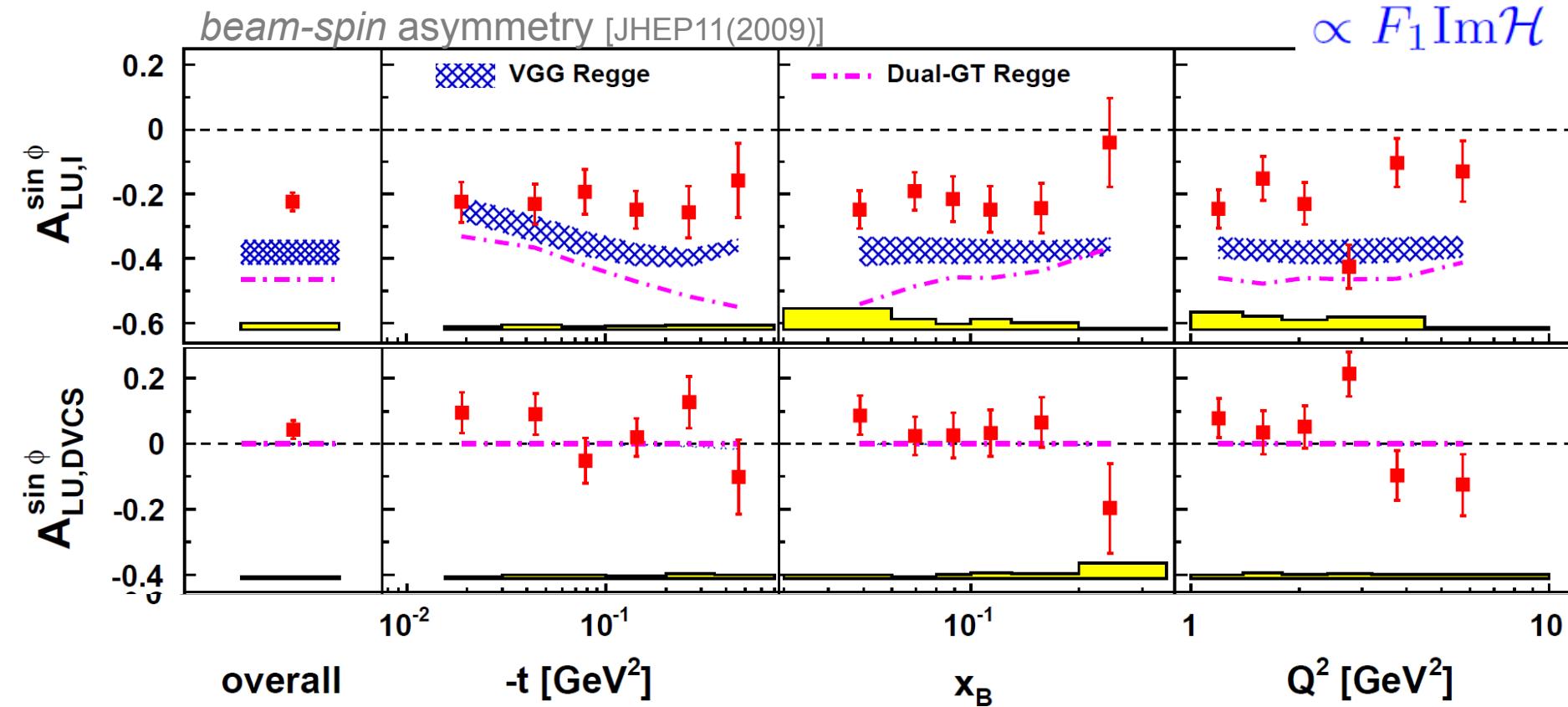
$s_1^{\text{DVCS}} \sin(\phi)$ $\sum_{n=1}^2 s_n^I \sin(n\phi)$ $\sum_{n=0}^3 c_n^I \cos(n\phi)$



call for new analysis methods

combined analysis of charge & polarisation observables

→ separation of interference & DVCS² amplitudes



GPD models:

- DD [VGG(1999)]

- minimal-dual [GT(2007)]

more, recent results

talk by S. Yaschenko

call for new analysis methods

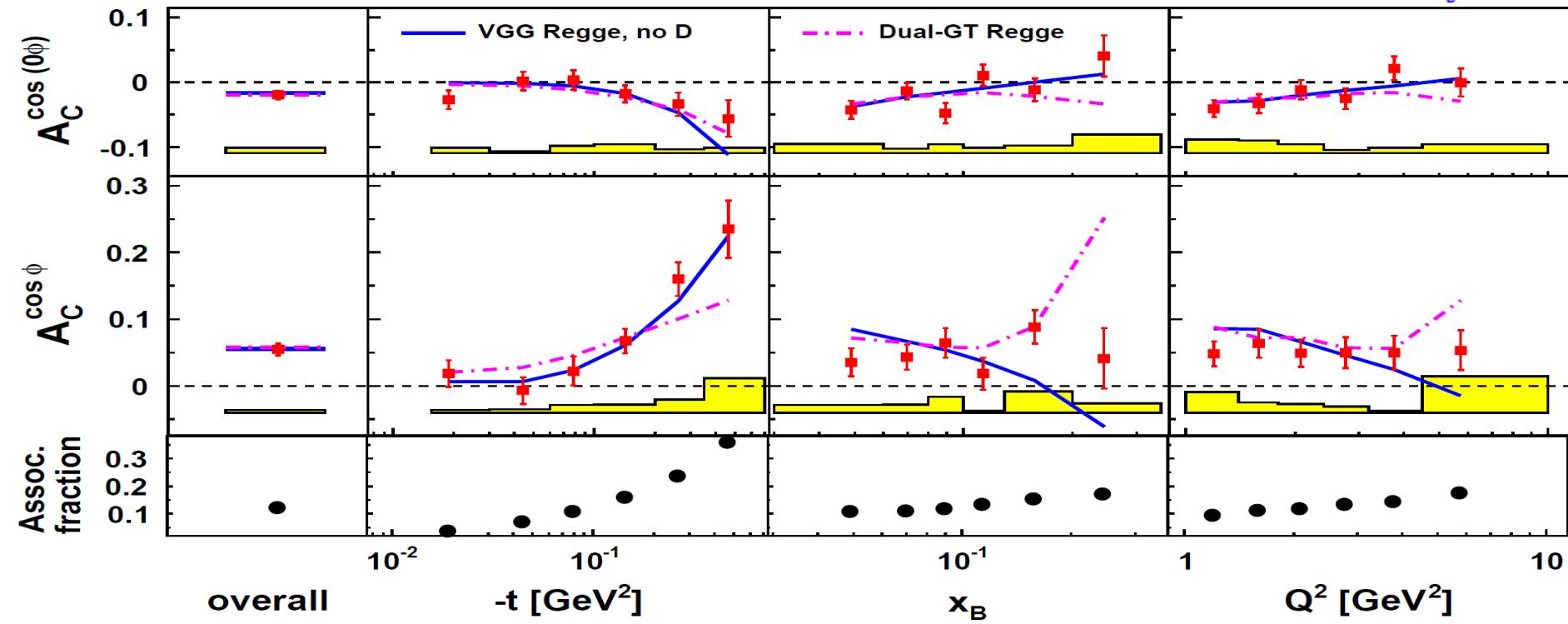
combined analysis of charge & polarisation observables

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beam-charge asymmetry [JHEP11(2009)]

$$A_C^{\cos \phi} \propto F_1 \text{Re} \mathcal{H}$$

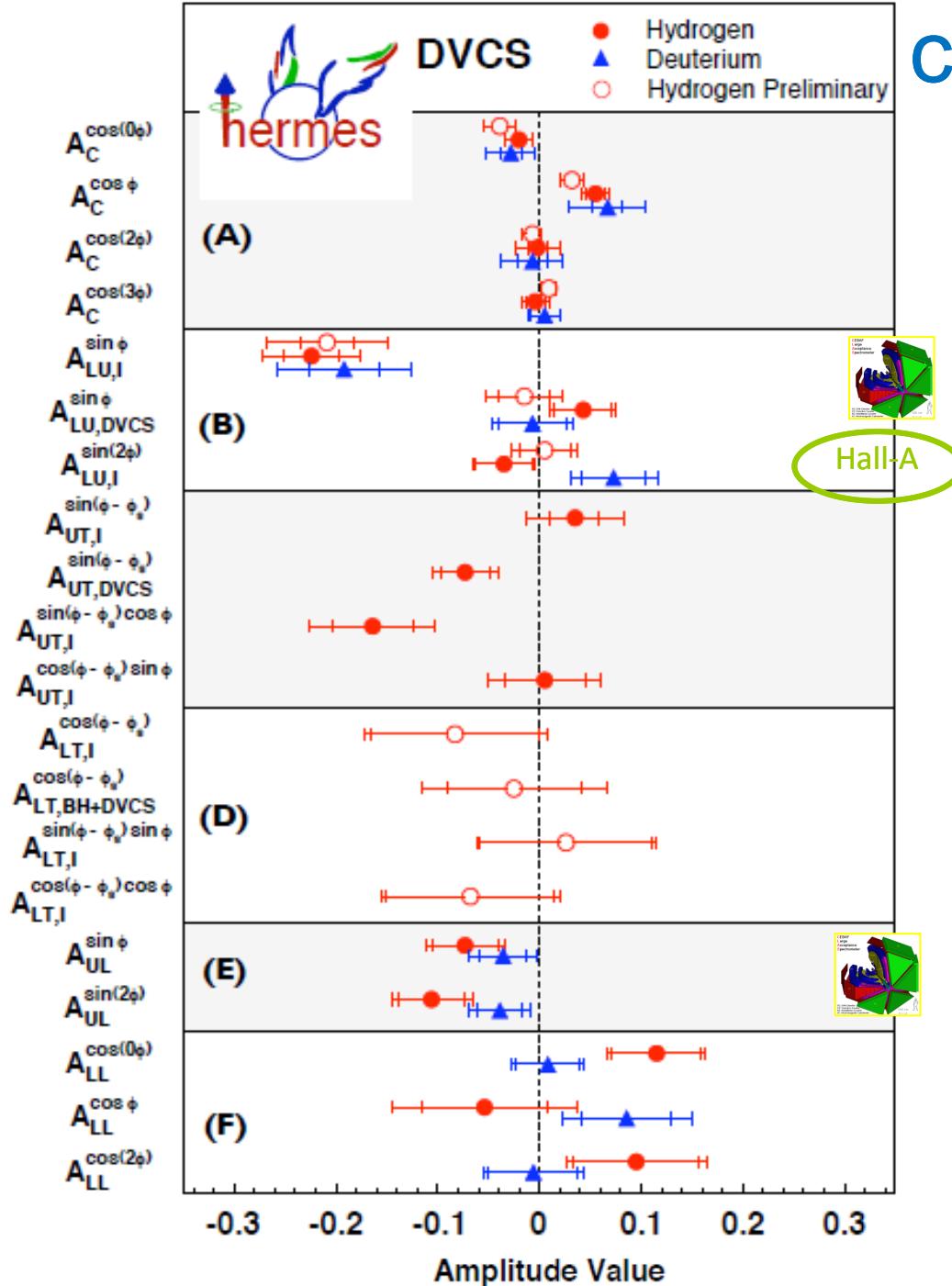
$$A_C^{\cos 0\phi} \propto -\frac{t}{Q} A_C^{\cos \phi}$$



GPD models: — DD, no D-term [VGG(1999)]
 — · · · minimal-dual [GT(2007)]

more, recent results
 talk by S. Yaschenko

call for completeness



→ charge asymmetry

$\text{Re } (H)$

→ beam-spin asymmetry

$\text{Im } (H)$

→ transverse target spin asymmetry

$\text{Im } (H-E)$

→ transverse-target double-spin

$\text{Re } (H-E)$

→ longitudinal target spin asymm.

$\text{Im } (\tilde{H})$

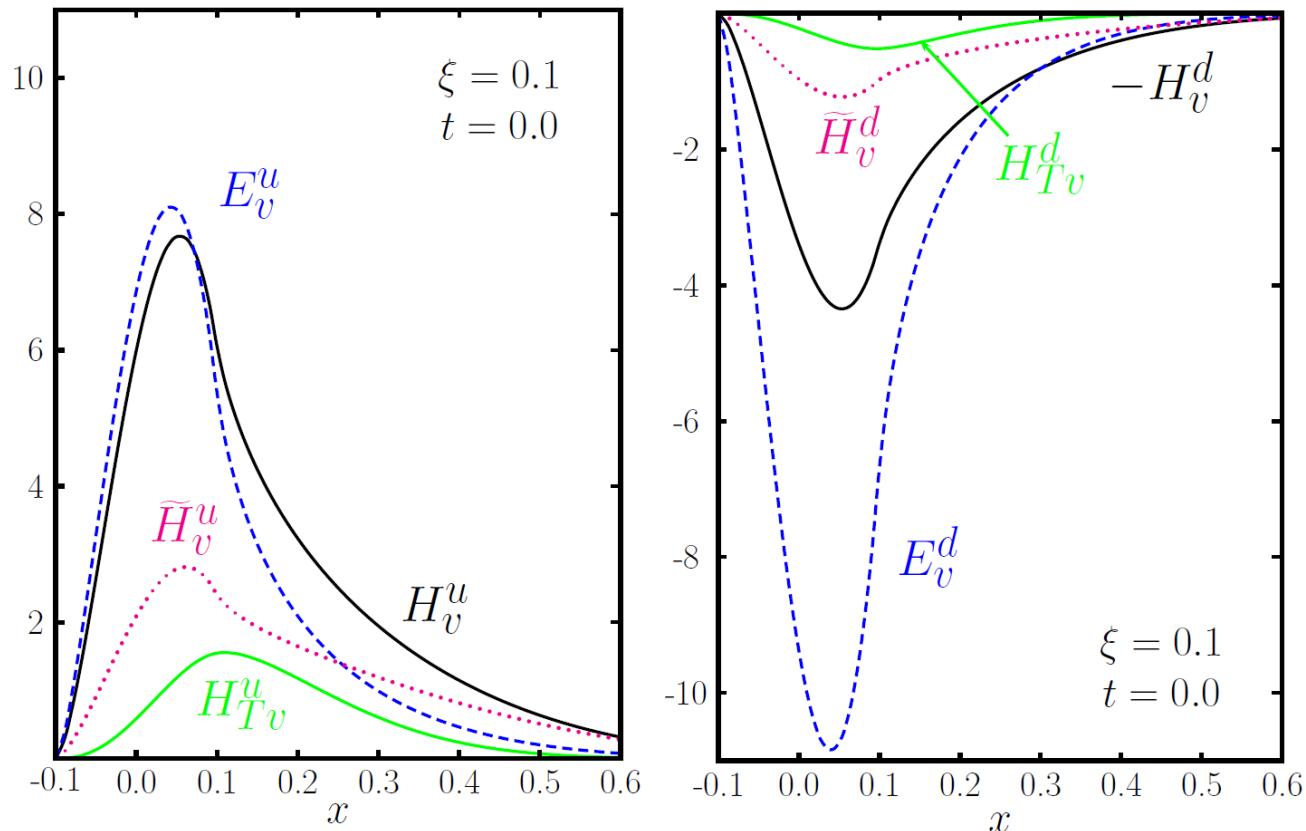
→ longitudinal-target double-spin

$\text{Re } (\tilde{H})$

towards GPDs

recent developments (beyond VGG(1999)…)

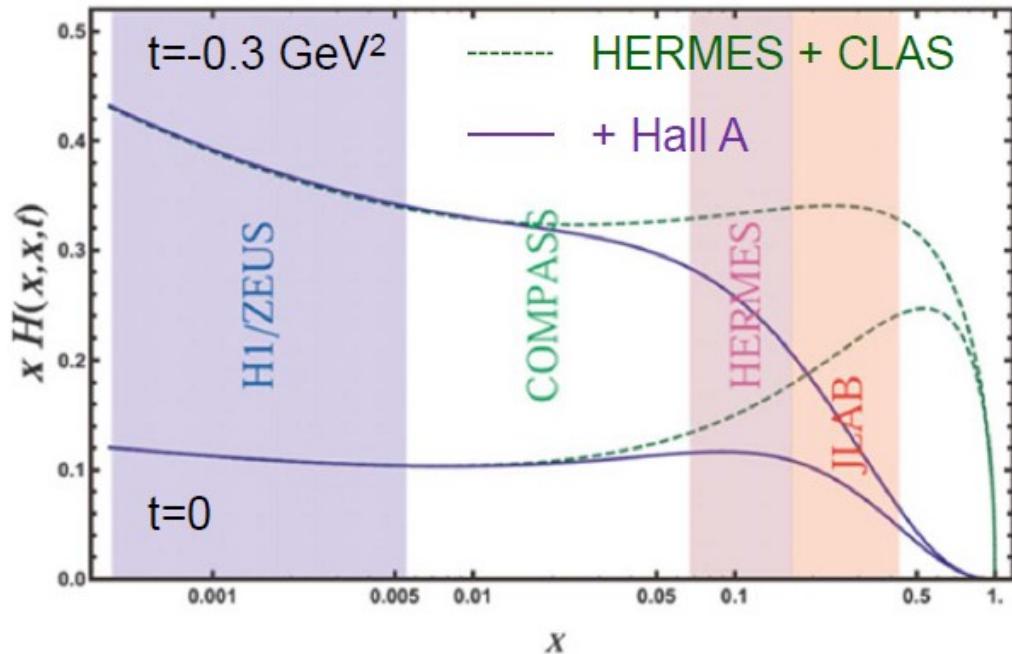
- Goloskokov, Kroll (2007):
 - LO GPD model using *DD, regge t dep., power corrections*
 - fit to **exclusive meson production** data



towards GPDs

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 - partial wave expansion of GPDs, *regge t dep., dispersion relations*
 - fit to **DVCS** data



towards GPDs

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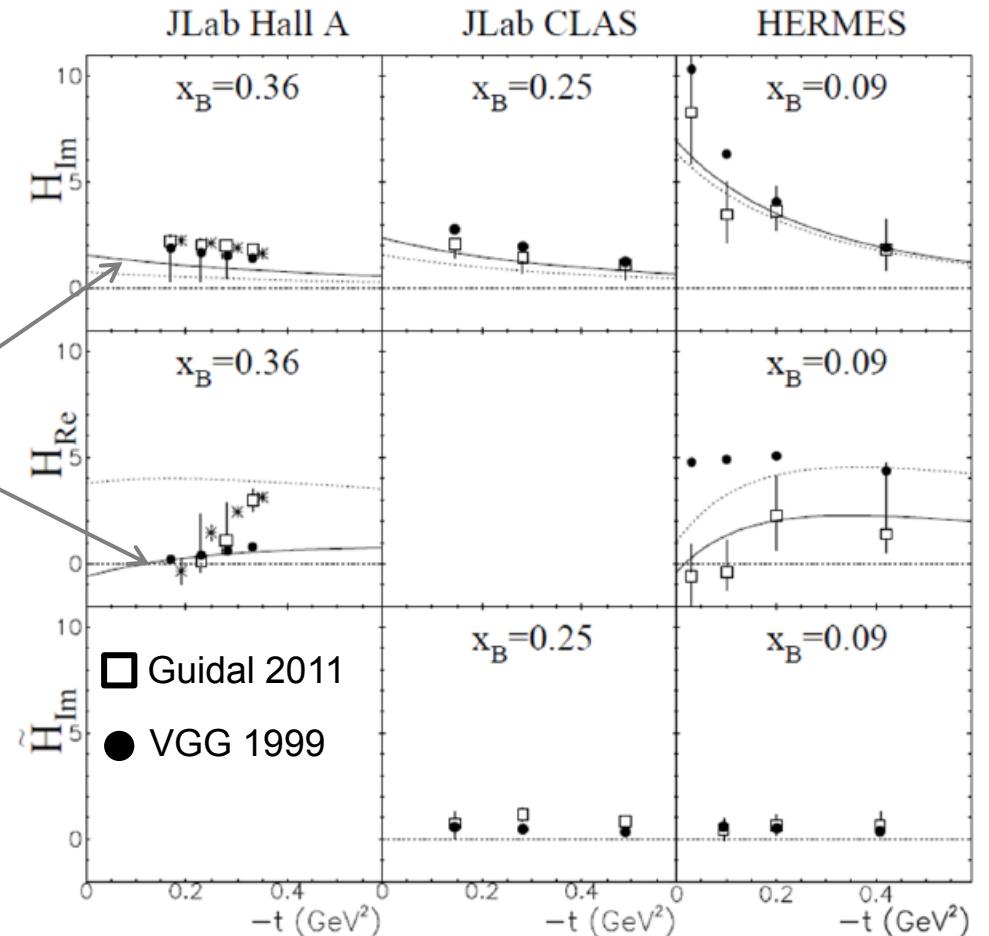
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 - fit to **DVCS** data

talk by S. Liuti [tomorrow]

towards GPDs

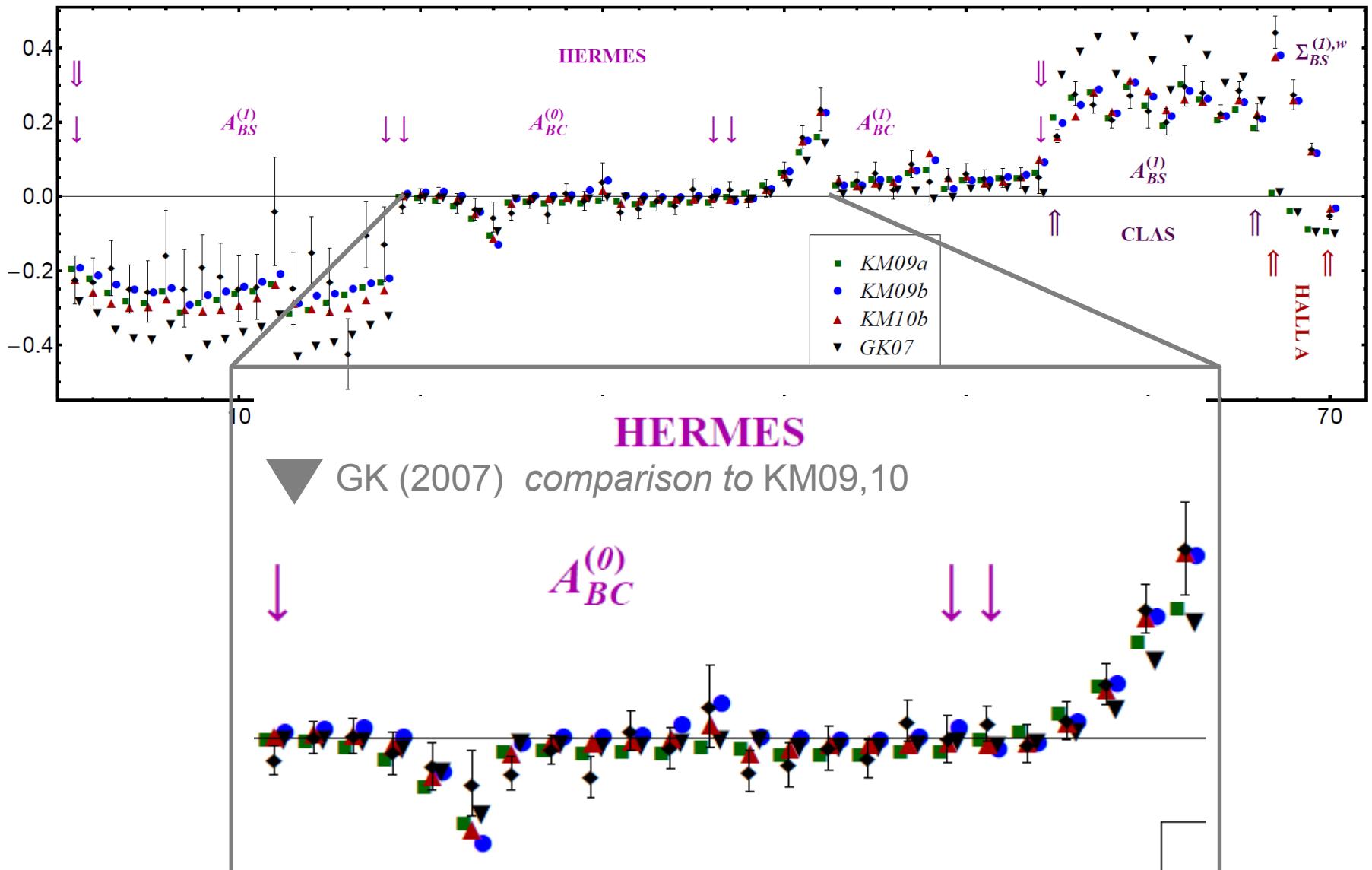
recent developments (beyond VGG)

- Goloskokov, Kroll (2007):
 - LO GPD model using D
 - fit to **exclusive meson p**
- Kumericki, Müller (2010):
 - partial wave expansion ζ
 - fit to **DVCS** data
- Goldstein, Hernandez,Liuti (2011)
 - quark-diquark model of ζ
 - fit to **DVCS** data
- Guidal (2011):
 - *model independent* extraction of **CFF** (GPD extr. requires model ansatz)
 - kinematic fitting of **DVCS** data (per experiment)

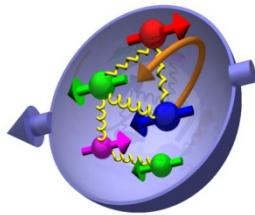


towards global analysis of GPDs

-- employ all available exclusive data (DVCS & meson production) --



hunting the OAM



- attempts to constrain J^q

$$J^q = \frac{1}{2} \int_{-1}^1 x dx \left[H^q(x, \xi, t) - E^q(x, \xi, t) \right]_{t=0}$$

→ GPD models: J^q free parameter in ansatz for E

- observables sensitive to E :
- pDVCS: $A_{UT} \rightarrow$ HERMES
 - nDVCS: $A_{LU} \rightarrow$ HallA
 - meson prod. A_{UT} : $\rho^0 \rightarrow$ HERMES, COMPASS
...also $\omega, \phi, \rho^+, K^{*0}$

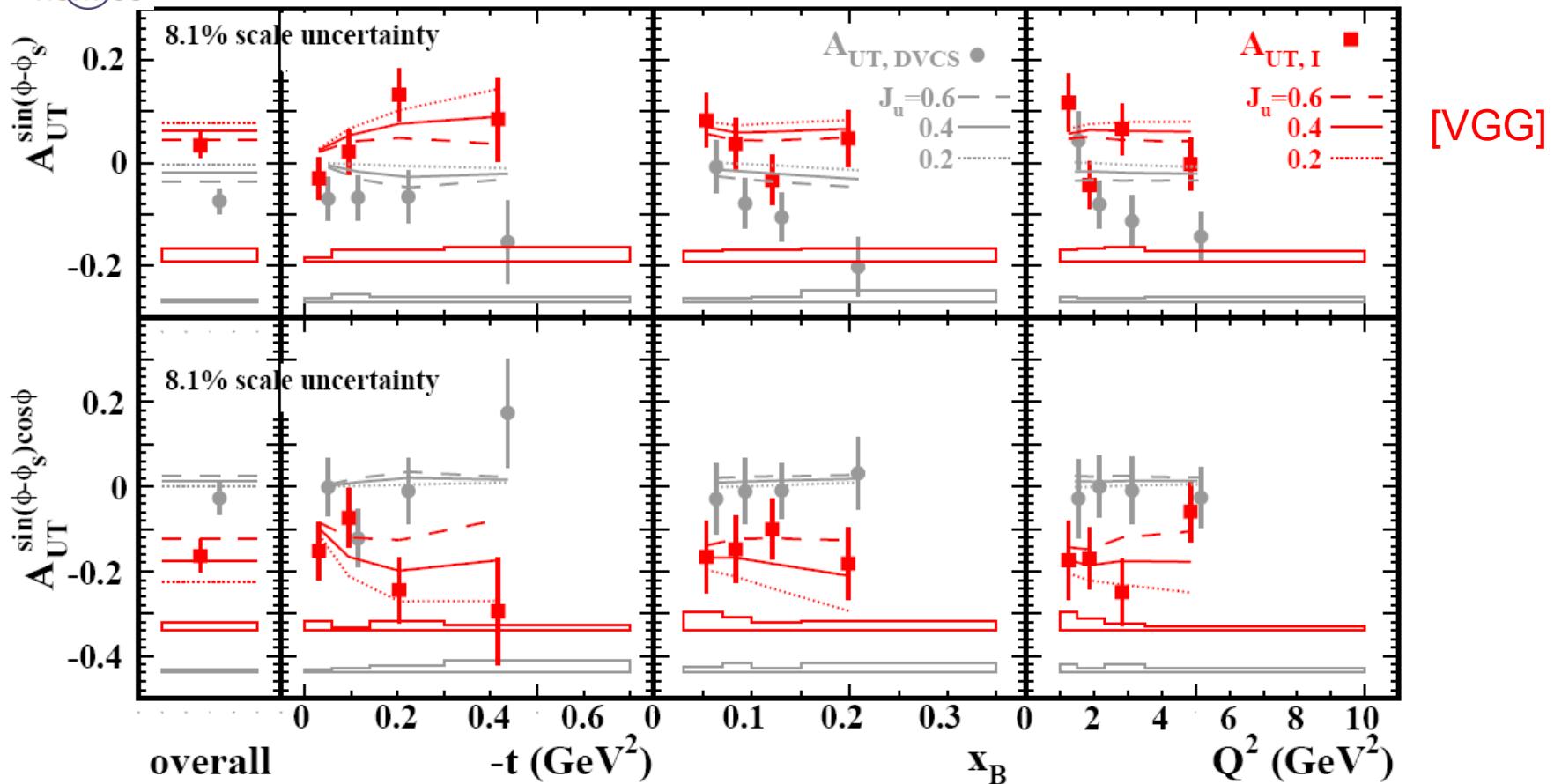
hunting the OAM

-- pDVCS : transverse target-spin asymmetry --



→ GPD models: J^q free parameter in ansatz for E

[JHEP06(2008)]

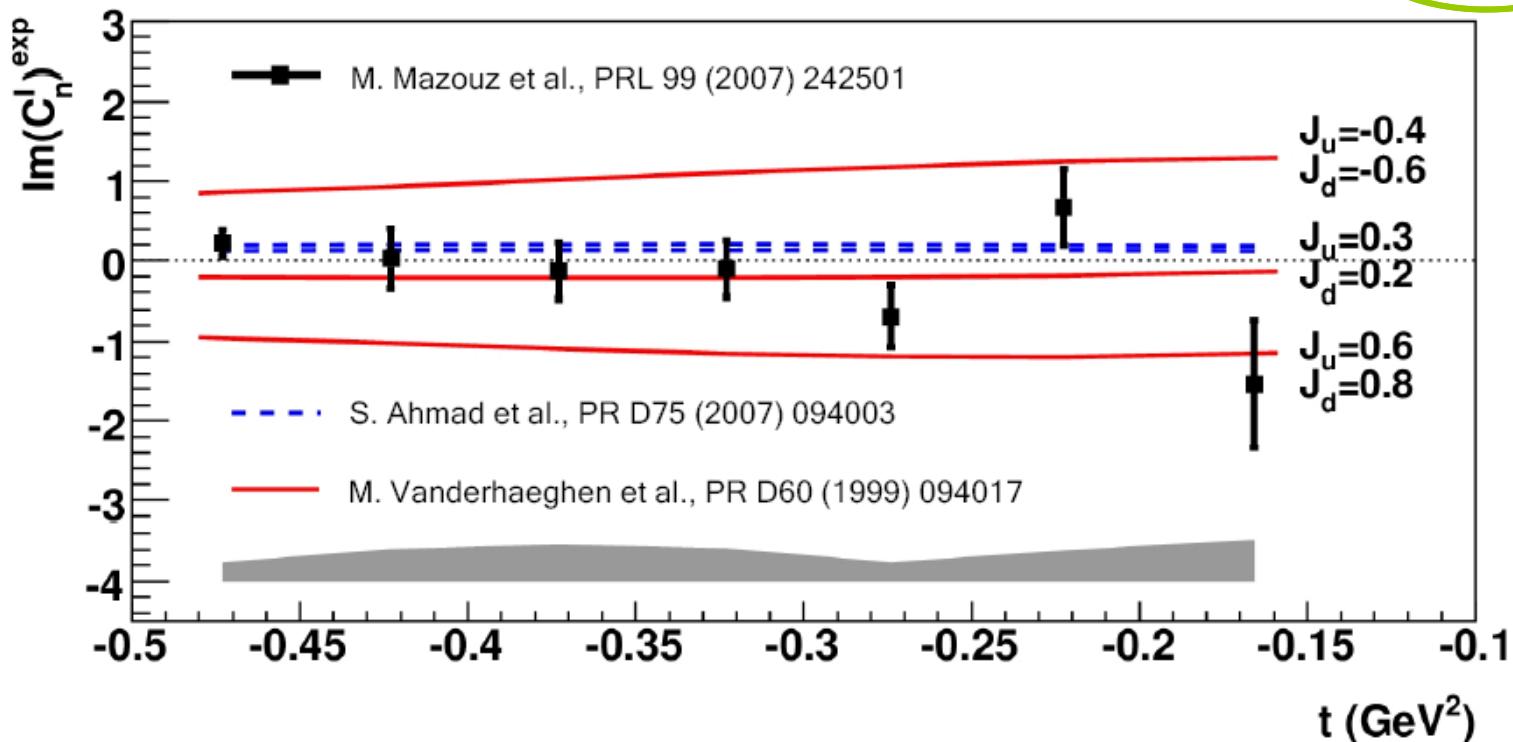


hunting the OAM

-- nDVCS : beam-spin cross section difference --

→ GPD models: J^q free parameter in ansatz for E

Hall-A



hunting the OAM

-- ρ^0 : transverse target-spin asymmetry --

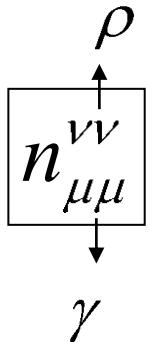


[PLB679(2009)]

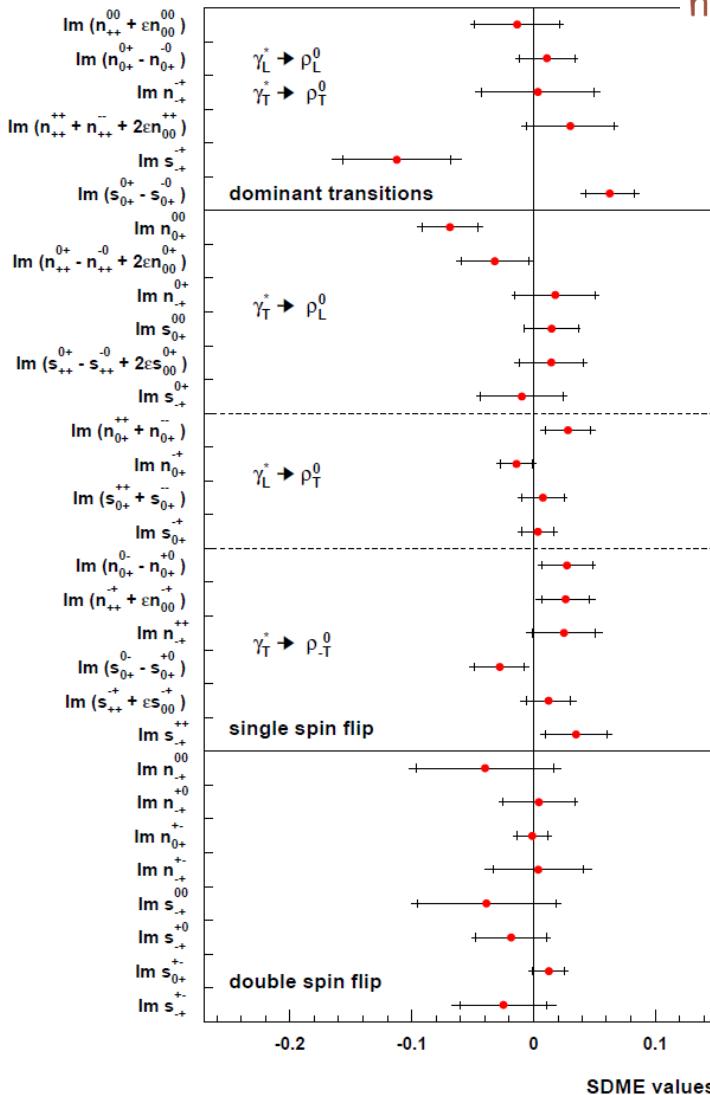
after the full glory of SDME extractions
[formalism by M. Diehl (2007)]

$(\gamma \rightarrow \rho)$:

$$A_{UT}^{\gamma^*}(\phi, \phi_s) = \frac{\text{Im } n_{00}^{00}}{u_{00}^{00}}$$



$\mu, \nu = 1, \pm$
long.pol: 0
transv.pol: ± 1



hunting the OAM

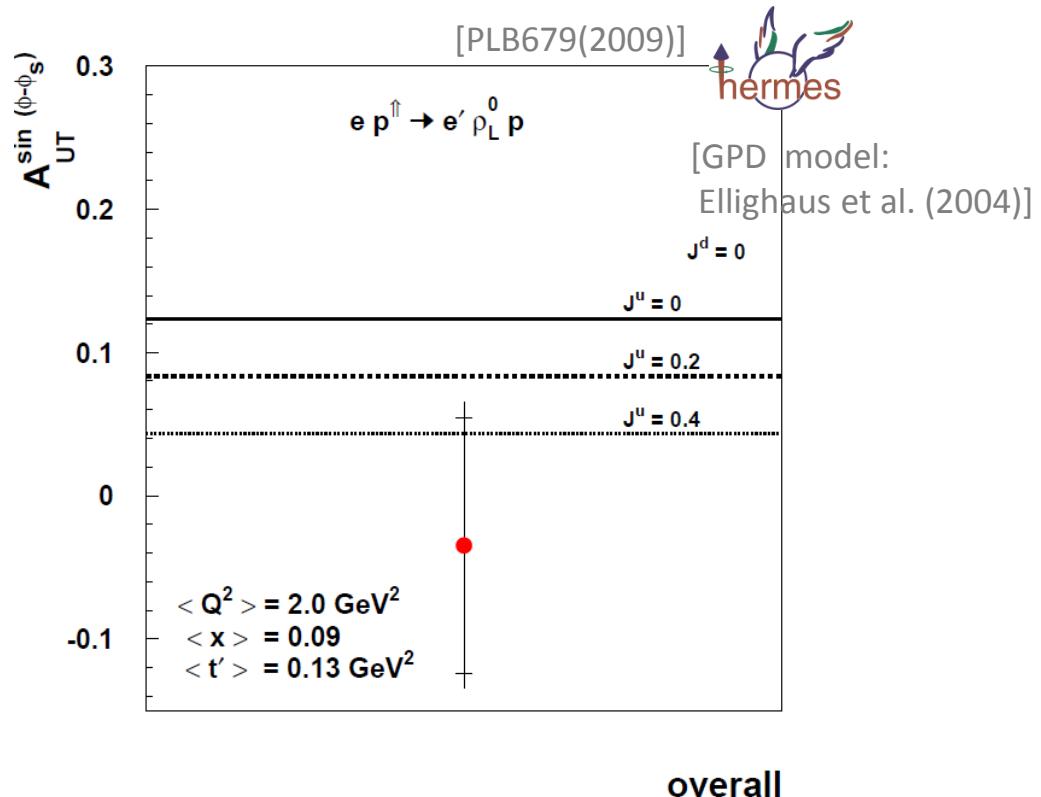
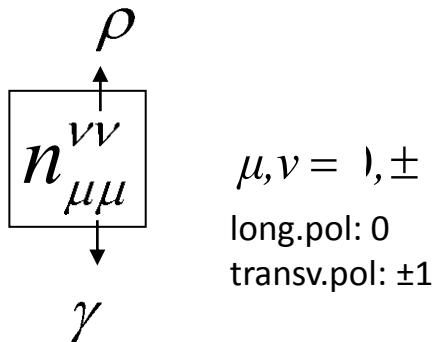
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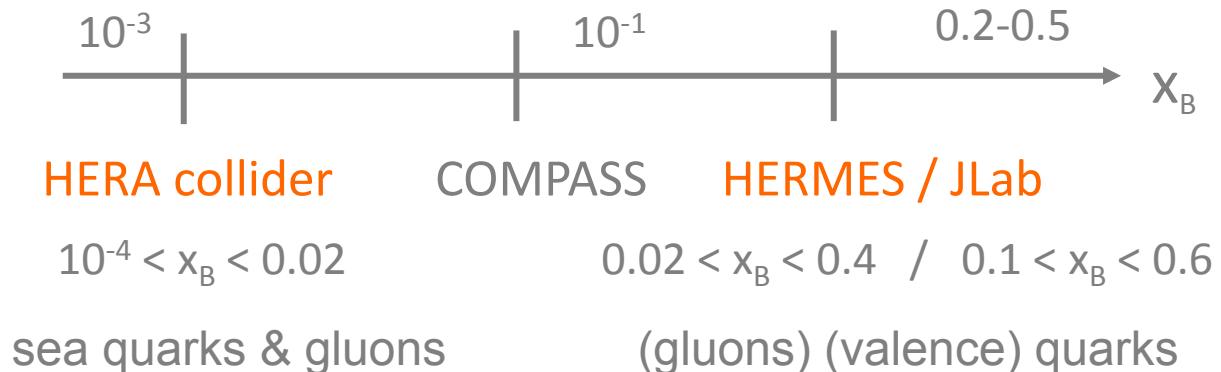
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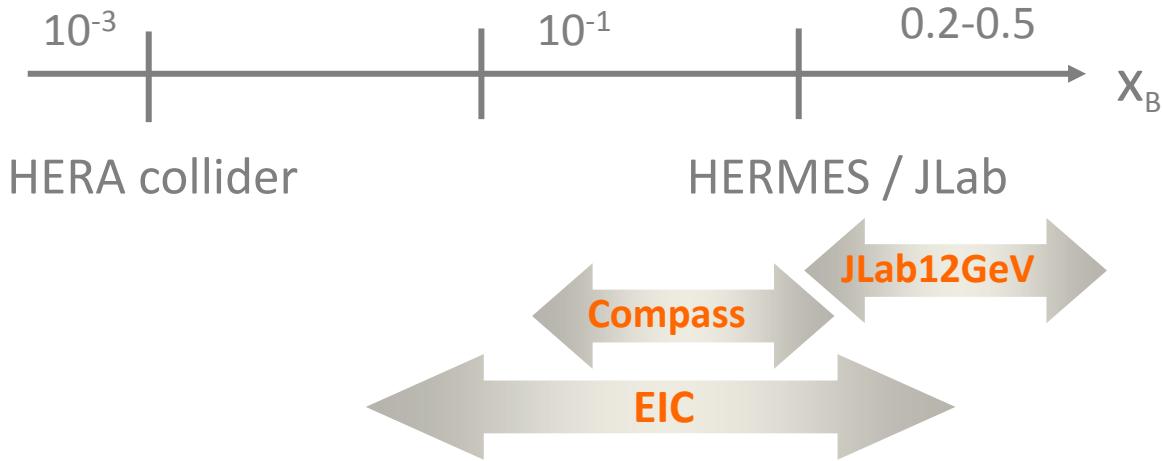
- more data coming: COMPASS, JLab12 with transv. Target
- more models: Goloskokov, Kroll

conclusions & perspectives



- increasing amount and precision of experimental data
- progress in model calculations, plenty of room for more work...

conclusions & perspectives



- increasing amount and precision of experimental data
- progress in model calculations, plenty of room for more work...

- bright future for GPD studies:

talks by V. Burkert, N. D'Hose, F. Maas

→ JLab12

→ COMPASS-II with recoil

→ EIC/ENC (mapping of GPDs from Q^2 evolution)