

# The 3D nucleon imaging program at JLab 12 GeV

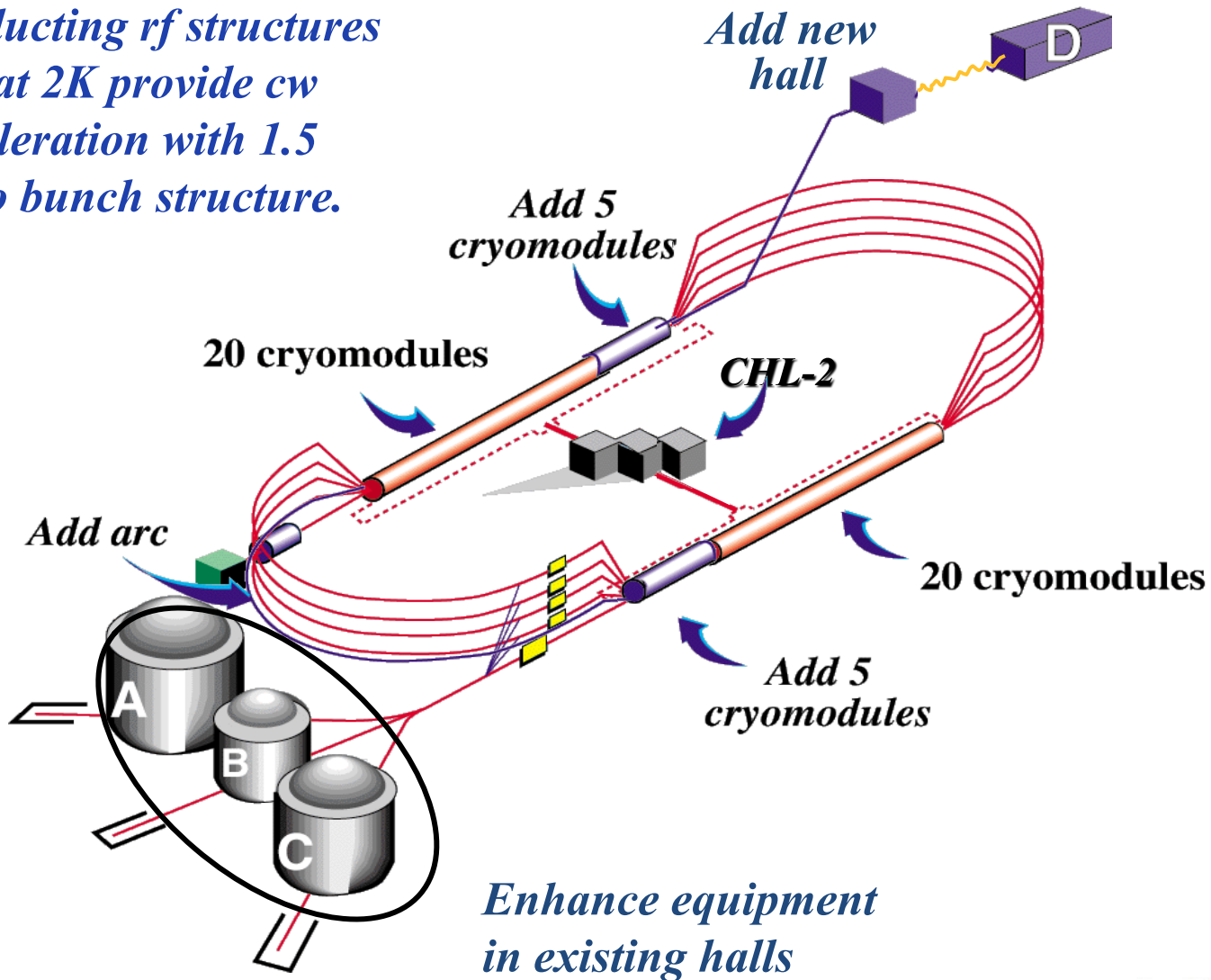
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Volker D. Burkert  
Jefferson Lab



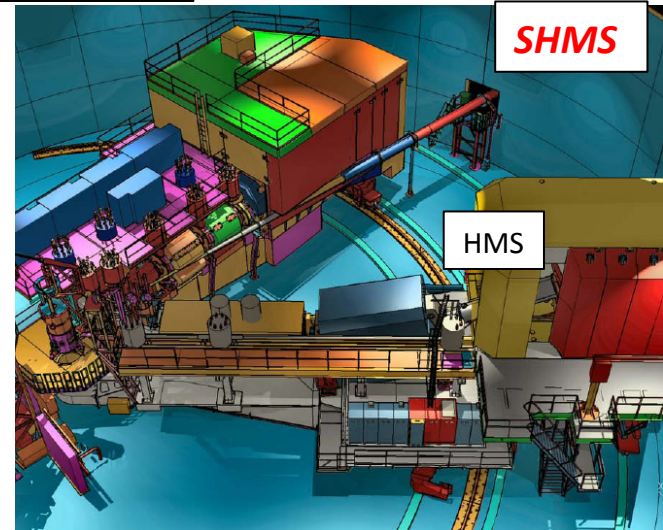
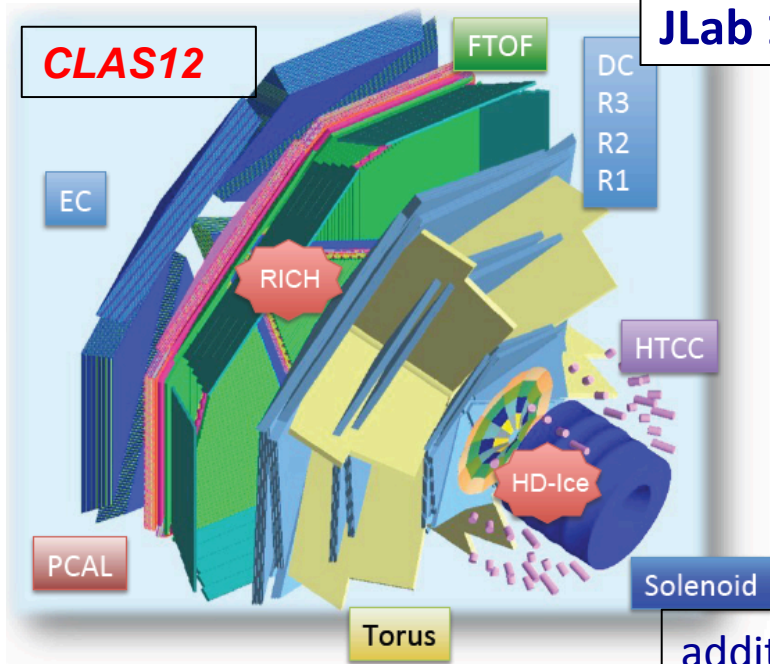
# CEBAF energy doubling from 6 GeV to 12 GeV

*Superconducting rf structures operating at 2K provide cw beam acceleration with 1.5 GHz micro bunch structure.*

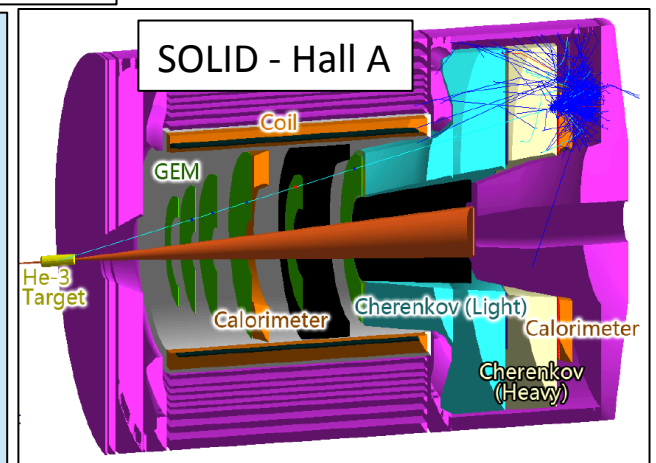
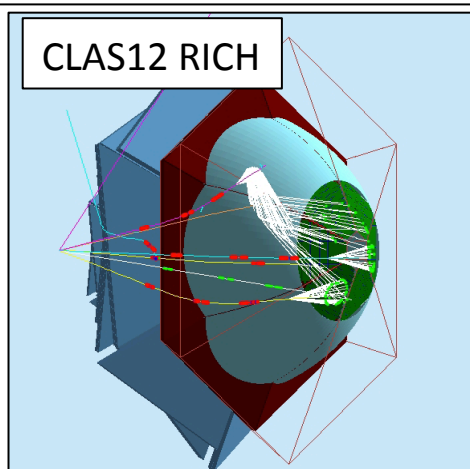
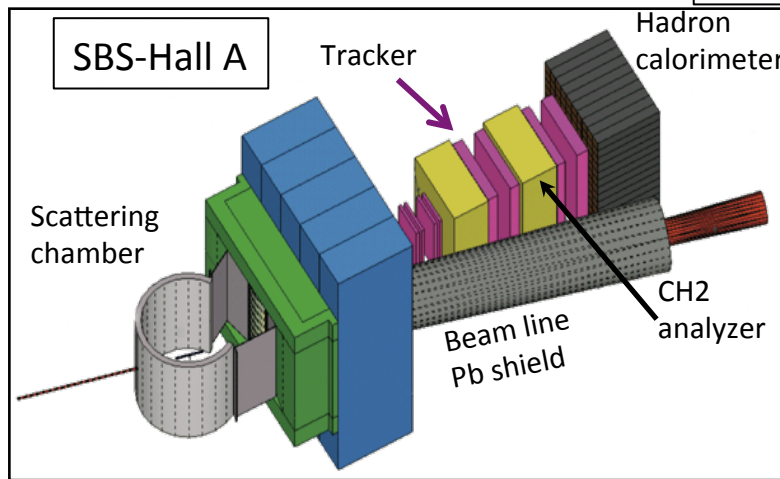


# Base equipment & proposed equipment

## JLab 12 GeV base equipment



## additional equipment (proposed)



# Wigner Function - GPDs and TMDs

(Quantum phase-space quark distribution in the nucleon)

$$W_{\Gamma}(\mathbf{r}, k) = \frac{1}{2M_N} \int \frac{d^3\mathbf{q}}{(2\pi)^3} e^{-i\mathbf{q}\cdot\mathbf{r}} \left\langle \mathbf{q}/2 \left| \hat{W}_{\Gamma}(0, k) \right| -\mathbf{q}/2 \right\rangle ,$$

$$W_{\Gamma}(\mathbf{r}, \mathbf{k}) = \int \frac{dk^-}{(2\pi)^2} W_{\Gamma}(\mathbf{r}, k)$$

Integrate over  
**spatial** dimensions

Integrate over  
**momentum** space

Transverse Momentum-dependent  
Distributions (**TMD**)

Generalized Parton  
Distributions (**GPD**)

3D imaging of the nucleon  
in momentum space

3D nucleon imaging in transverse  
coordinate and longitudinal  
momentum space.

# Physical content of GPDs $H, E$

Nucleon energy-momentum tensor of  $q$  flavored quarks:

$$\langle p_2 | \hat{T}_{\mu\nu}^q | p_1 \rangle = U(p_2) \left[ M_2^q(t) \frac{P_\mu P_\nu}{M} + J^q(t) \frac{i(P_\mu \sigma_{\nu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M} + d_1^q(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{5M} \right] U(p_1)$$

To measure gravitational FFs : **graviton** scattering or **GPDs** identities :

$$J^q(t) = \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)] , \quad M_2^q(t) + \frac{4}{5} d_1(t) \xi^2 = \frac{1}{2} \int_{-1}^1 dx x H^q(x, \xi, t)$$

(Ji's sum for t=0)

Fourier transformation relates  $J(t)$  to the quark angular momentum distribution in  $b_\perp$  space.

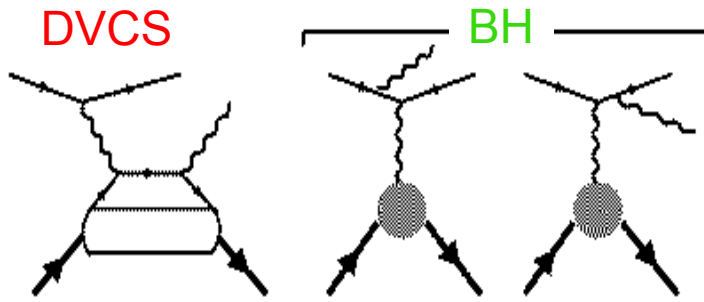
$M_2(t)$ : Mass distribution in  $b_\perp$  space

$d_2(t)$ : Pressure and force distribution on quarks.

K. Goeke et al., PRD75,  
2094021 (2007)

# DVCS and Bethe-Heitler Process

$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} \sim |\mathbb{T}^{\text{DVCS}} + \mathbb{T}^{\text{BH}}|^2$$

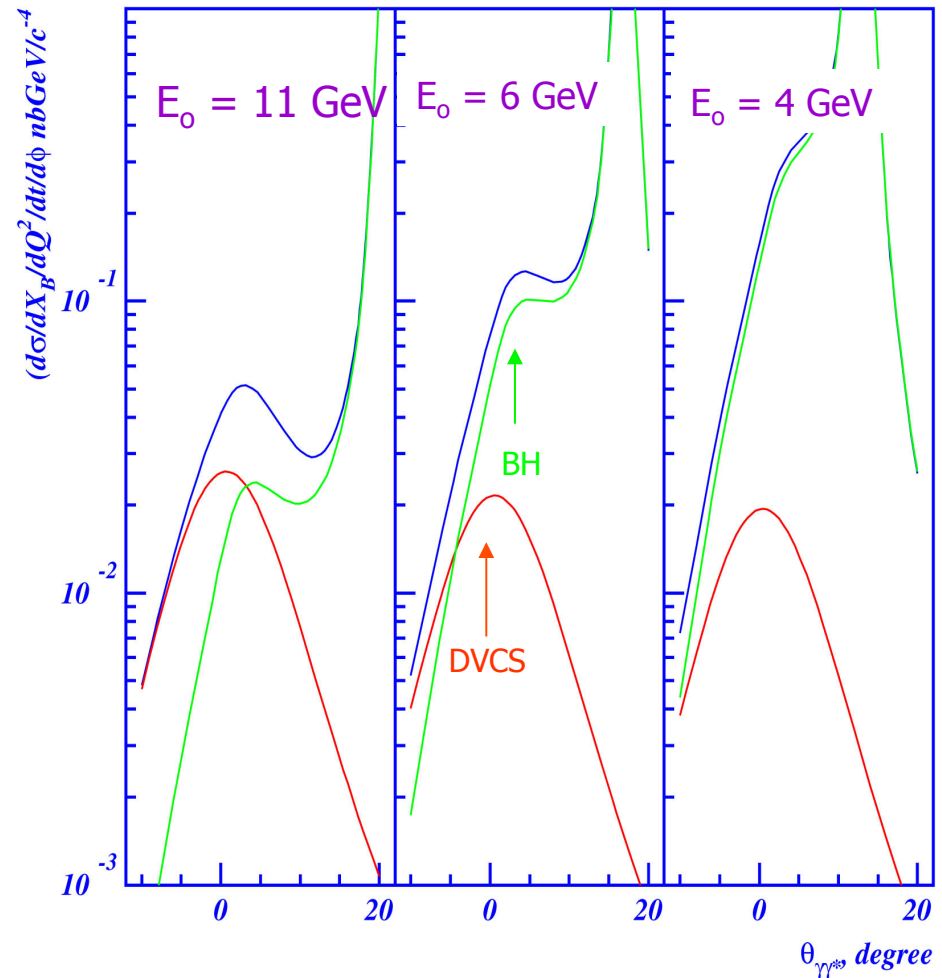


$\mathbb{T}^{\text{BH}}$ : given by elastic form factors

$\mathbb{T}^{\text{DVCS}}$ : determined by GPDs

BH-DVCS interference generates beam and target polarization asymmetries that encode the nucleon structure content.

Cross section of  $ep \rightarrow ep\gamma$  at  $Q^2=2 \text{ GeV}/c^2$  and  $X_B=0.35$

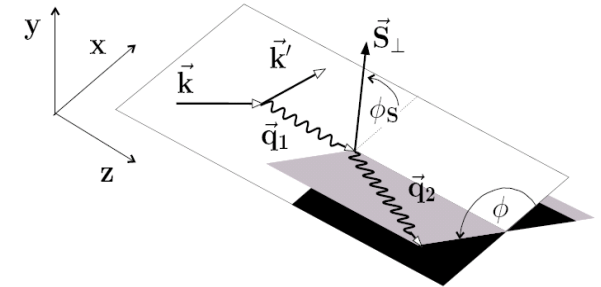


# A path towards extracting GPDs

$$A = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\Delta\sigma}{2\sigma}$$

$$\xi \sim x_B/(2-x_B)$$

$$k = t/4M^2$$



Polarized beam, unpolarized target:

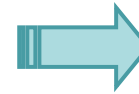
$$\Delta\sigma_{LU} \sim \sin\phi \{F_1 H + \xi(F_1 + F_2) \tilde{H} + kF_2 E\} d\phi$$



$$H(\xi, t)$$

Unpolarized beam, longitudinal target:

$$\Delta\sigma_{UL} \sim \sin\phi \{F_1 \tilde{H} + \xi(F_1 + F_2)(H + \xi/(1+\xi)E)\} d\phi$$



$$\tilde{H}(\xi, t)$$

Unpolarized beam, transverse target:

$$\Delta\sigma_{UT} \sim \cos\phi \sin(\phi_s - \phi) \{k(F_2 H - F_1 E)\} d\phi$$



$$E(\xi, t)$$

Unpolarized total cross section:

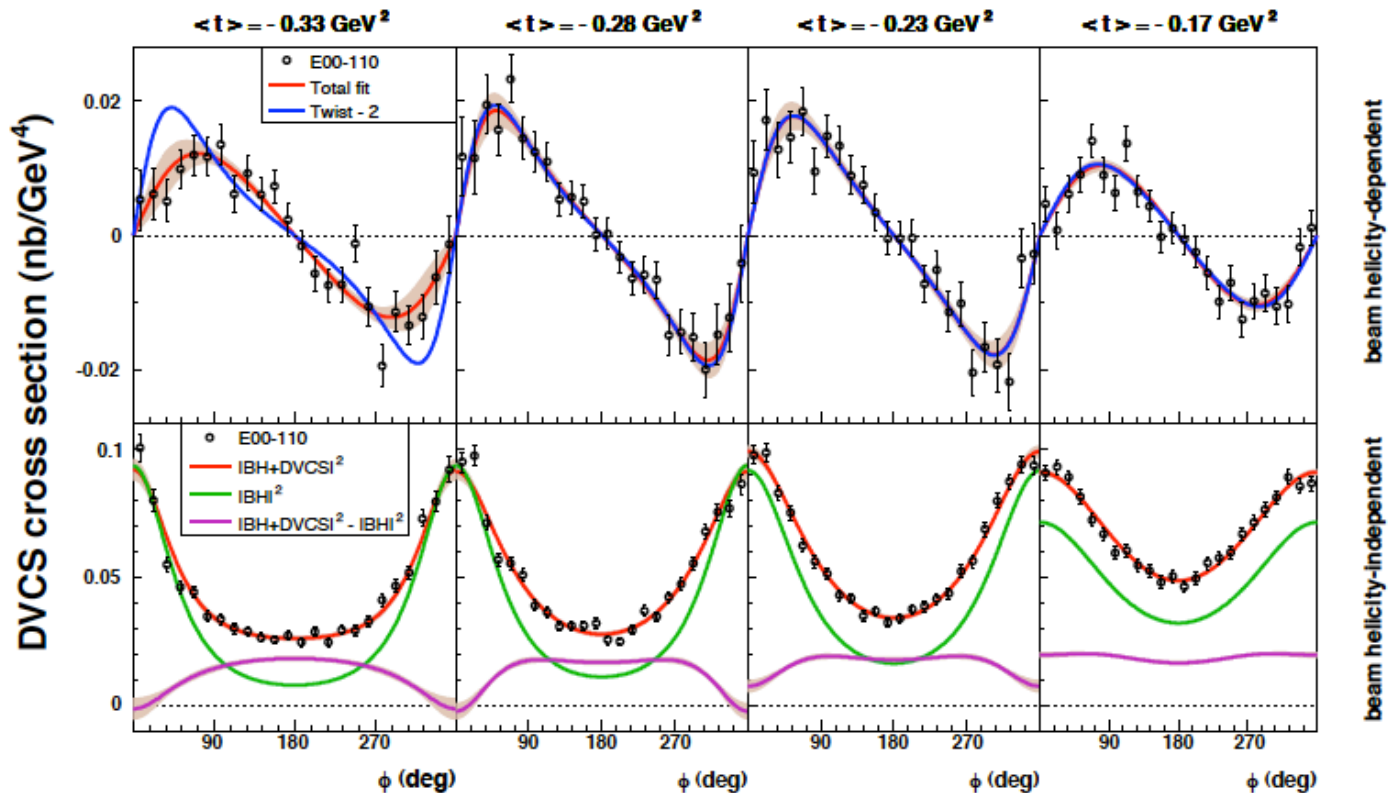
Separates h.t. contributions to DVCS



$$\text{Re}(T^{\text{DVCS}})$$

# Hall A DVCS/BH cross section on proton

C. Muñoz et al., Phys. Rev. Lett. 97 (2006) 262002



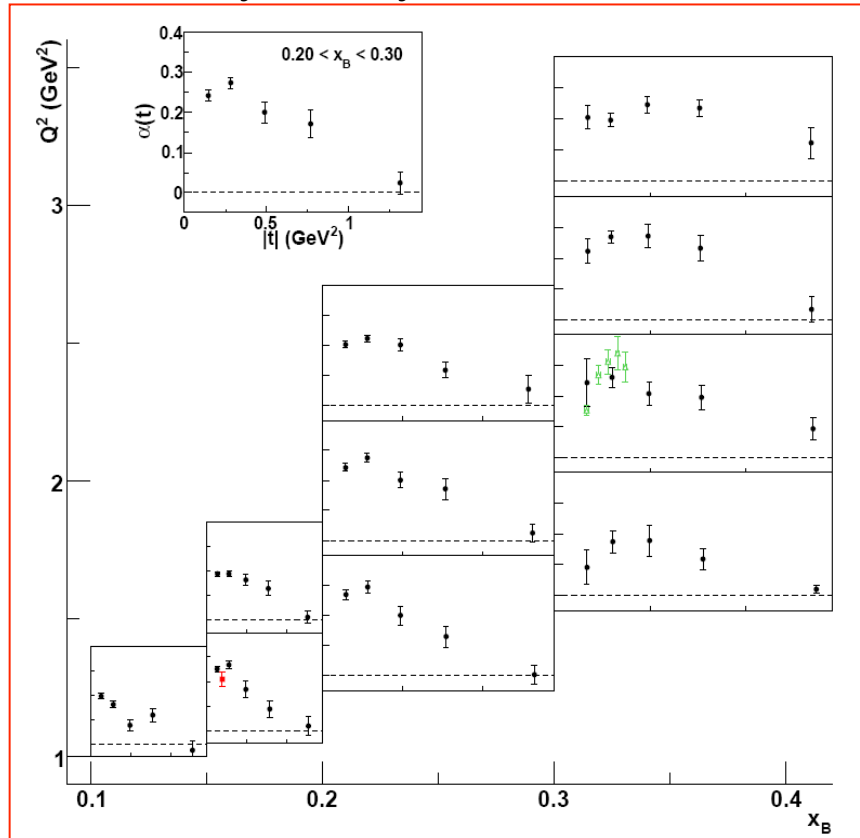
High statistics in small range in  $Q^2$ ,  $x_B$ ,  $t$   
Verify Bjorken scaling in small  $Q^2$  range

New data taken 2010 on hydrogen and deuterium at two beam energies



# Extraction of GPDs $H, \tilde{H}$ at 6 GeV

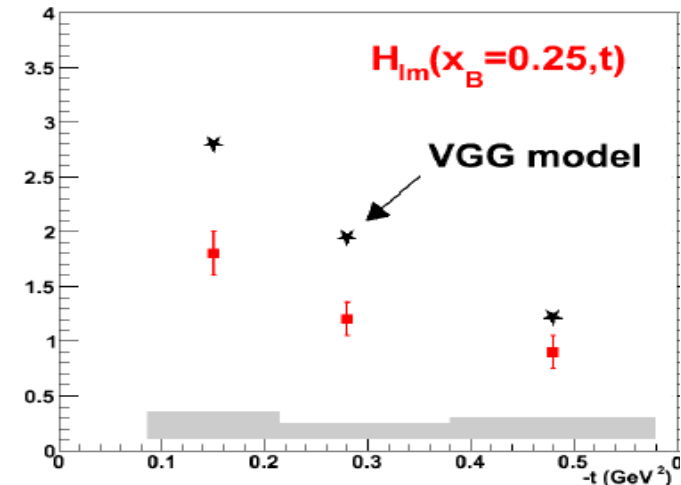
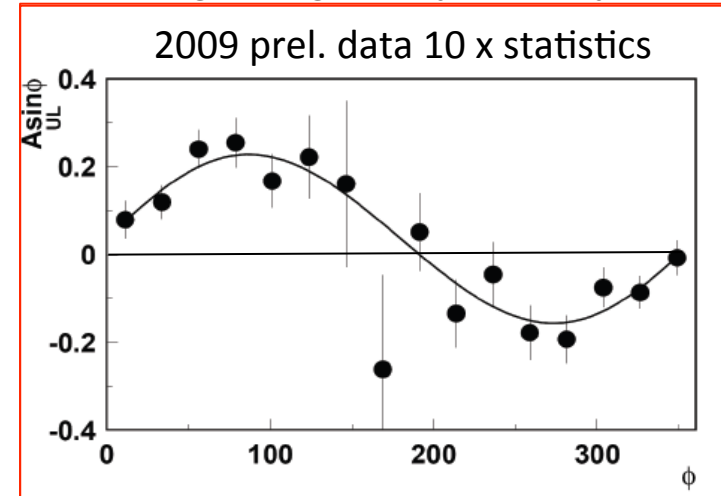
## Beam asymmetry



F.X. Girod et al. (CLAS), *Phys.Rev.Lett*100:162002,2008

S. Chen et al. (CLAS), *Phys.Rev.Lett*97:072002,2006

## Long. Target asymmetry

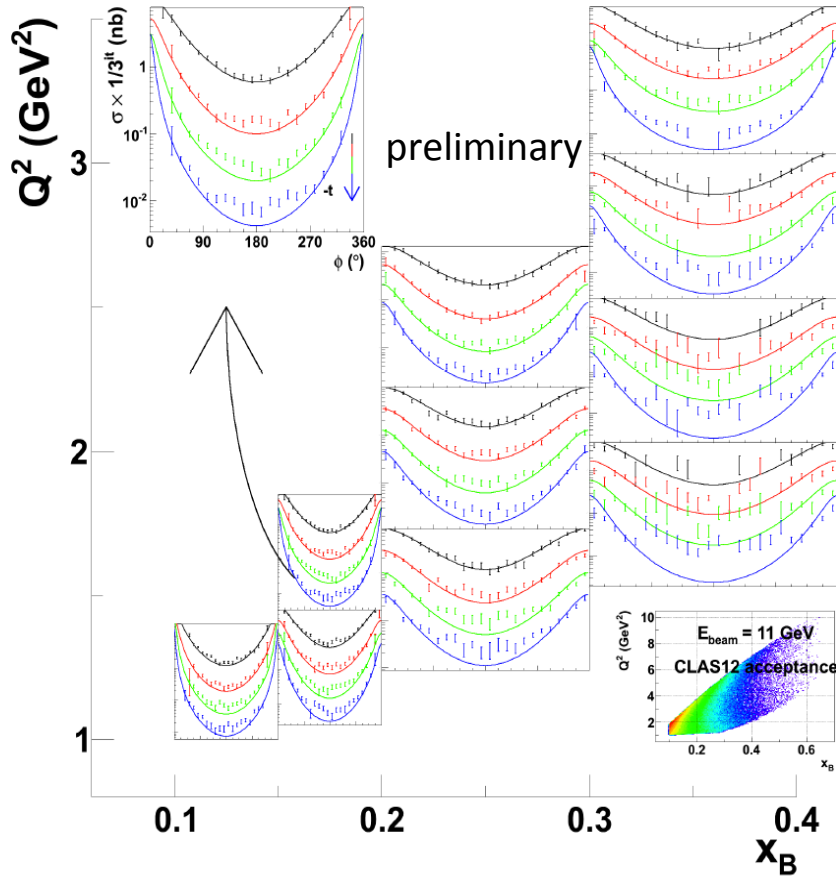


M. Guidal, *Phys.Lett.B*689, 156-162,2010

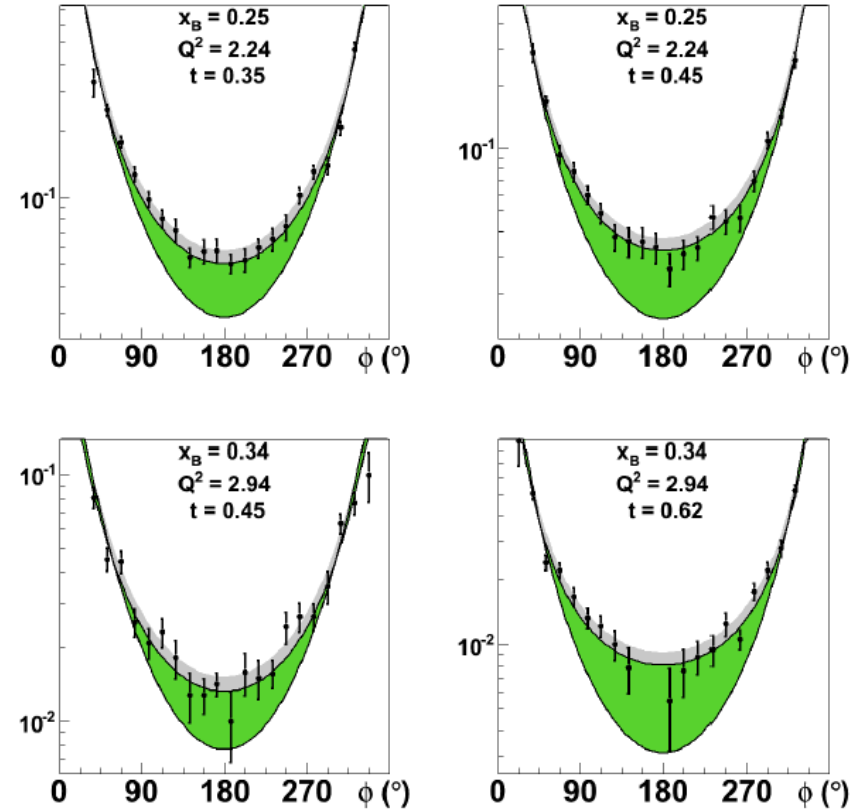
# CLAS DVCS/BH cross sections

Large kinematical range in  $Q^2$ ,  $x_B$ ,  $t$

**E01-113**,  $\sigma_{\text{DVCS}}$ ,  $F_1\mathcal{H} + \xi G_M\tilde{\mathcal{H}} - F_2\frac{t}{4M^2}\mathcal{E} + \dots$



Full exclusivity by detecting all particles (e, p,  $\gamma$ ) in the final state.



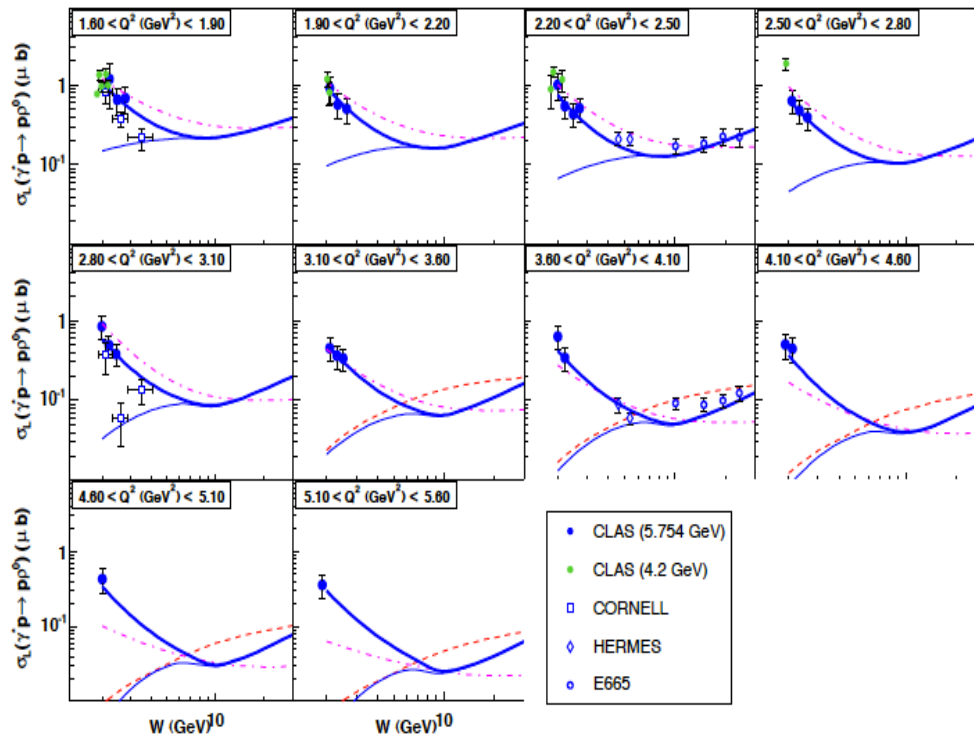
2009 data will double statistics

# CLAS Exclusive vector mesons

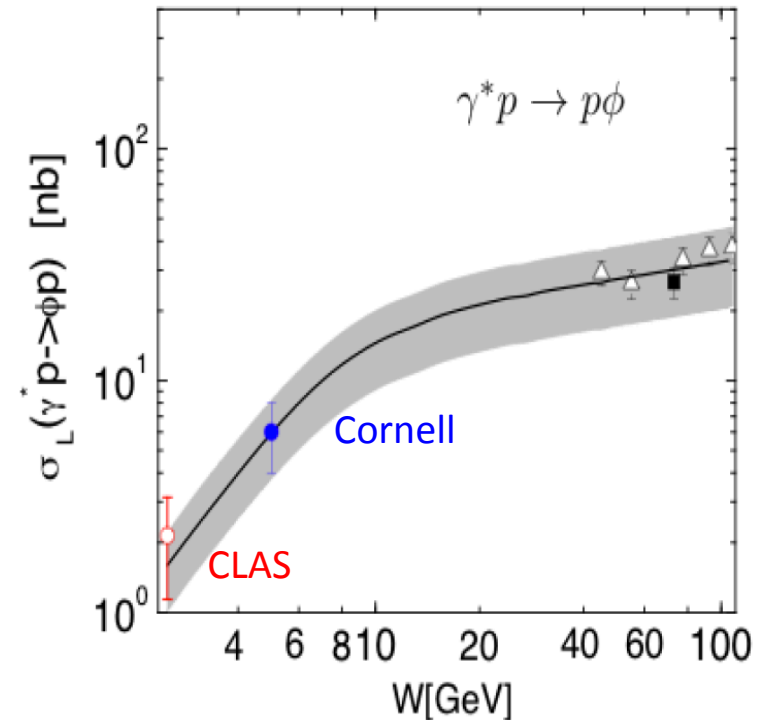
$\rho^0$  helps the flavor separation of GPDs:  $2u + d$

Longitudinal cross-section separated by angular analysis in the C.O.M.

Missing strength at low W : higher-twist or missing contribution in the D-term



Gluon-GPD handbag works for  $\phi$ 's



Also longitudinal cross section data for  $\rho^+$  production.

# GPDs in DVCS experiments at JLab12

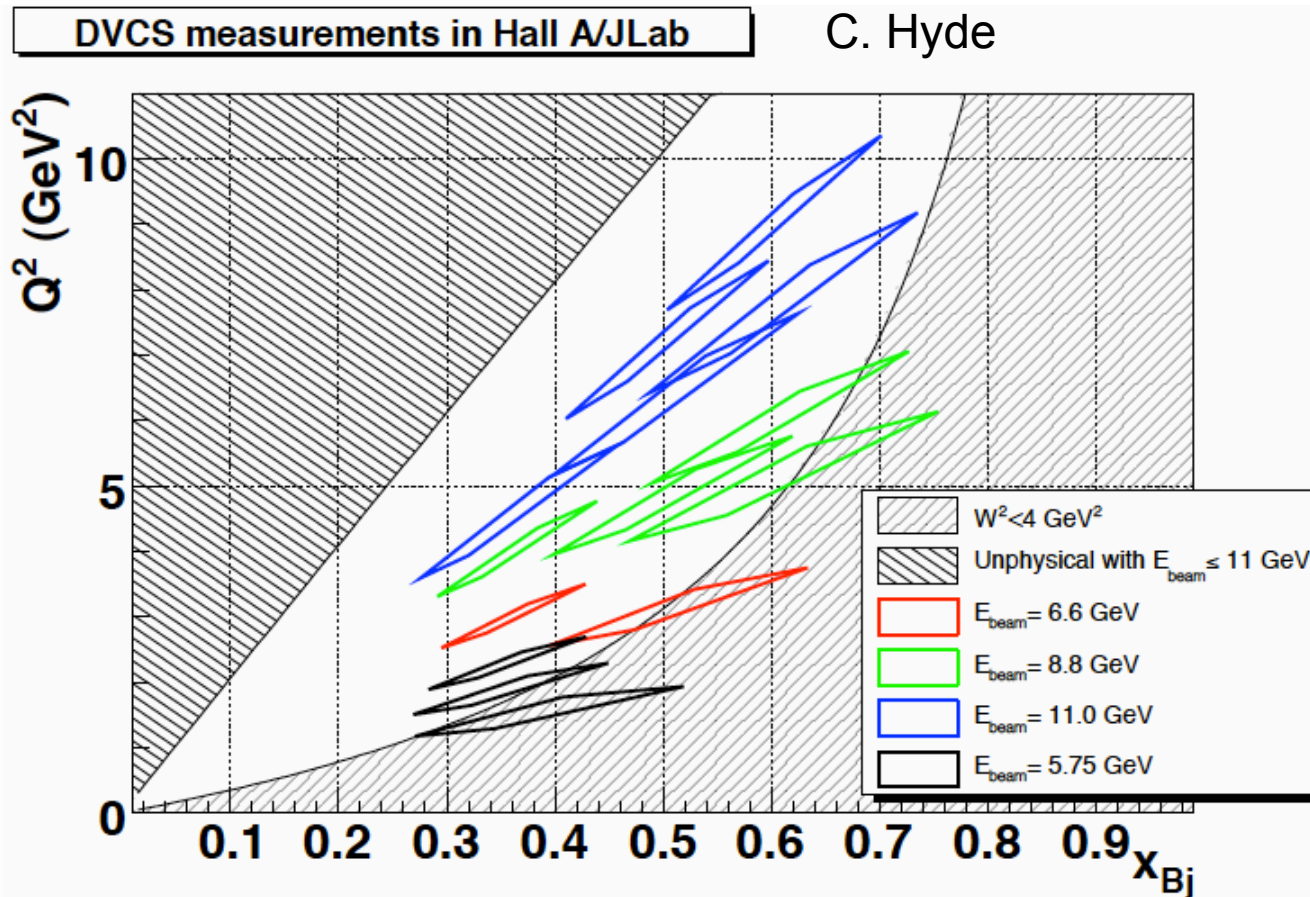
Nucleon polarization	Sensitivity to GPDs	Experiments
UP	$H, \tilde{H}, E$	E12-06-114 : $\gamma, \pi^0$ (A) proton E12-06-119 : $\gamma, \pi^0$ (B) proton E12-11-003: $\gamma, \pi^0$ (B) neutron
LP	$\tilde{H}, H, E$	E12-06-119 : $\gamma, \pi^0$ (NH <sub>3</sub> ) (B) proton
TP	$E, H$	LOI12-11-105 : $\gamma, \pi^0$ (HD) (B) proton

The JLab DVCS program will be carried out in two experimental Halls: **A & B (CLAS12)**

# Hall A DVCS at 12 GeV

E12-06-114

$$\Delta\sigma_{LU} \sim \sin\phi \{F_1 H + \xi(F_1 + F_2) \tilde{H} + kF_2 E\} d\phi$$

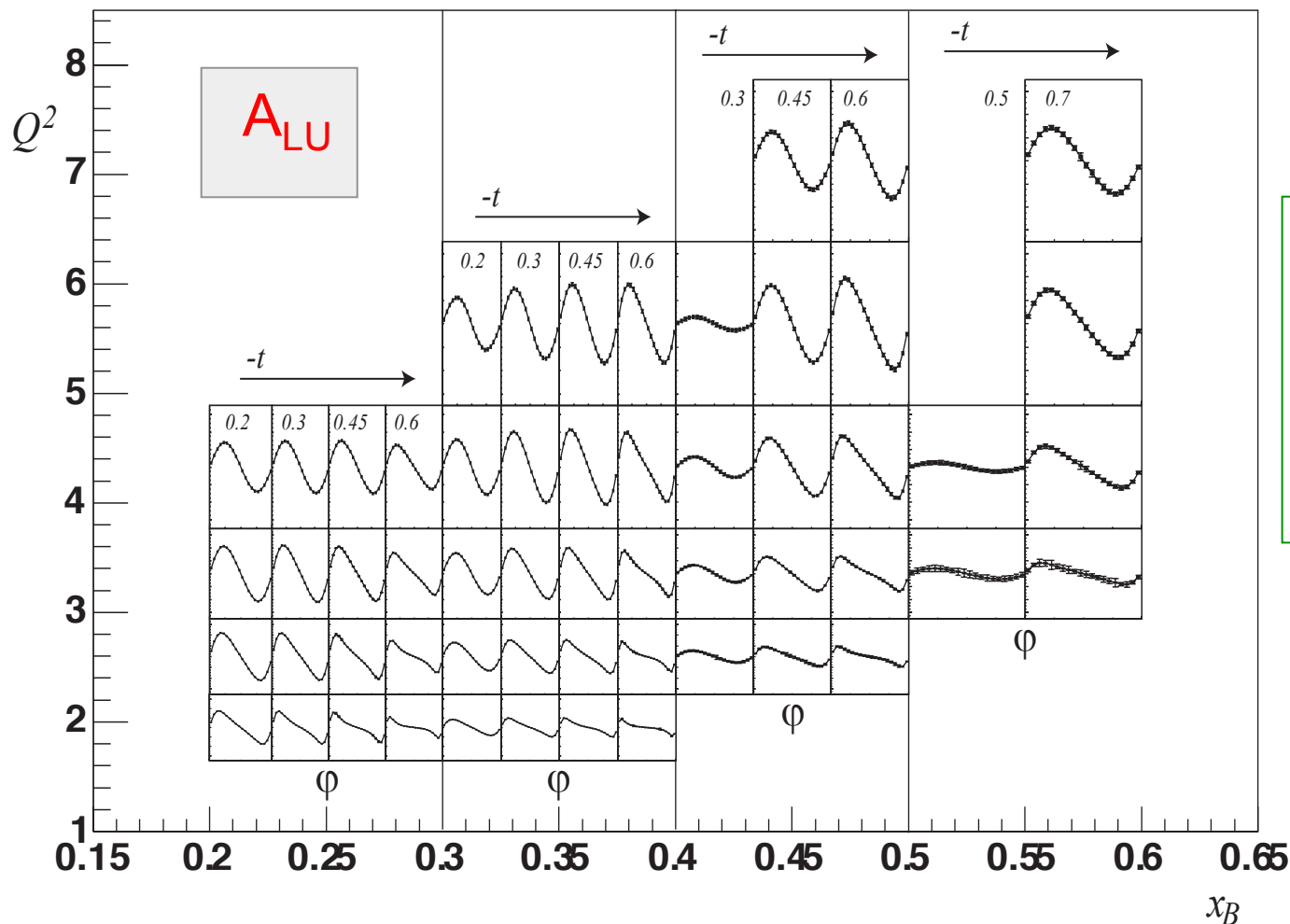


# DVCS/BH $A_{LU}$ projections on protons

$$\Delta\sigma_{LU} \sim \sin\phi \{F_1 H + \xi(F_1 + F_2)\tilde{H} + kF_2 E\} d\phi$$

F. Sabatié, C. Hyde

E12-06-119/CLAS12  
E12-06-114/Hall A



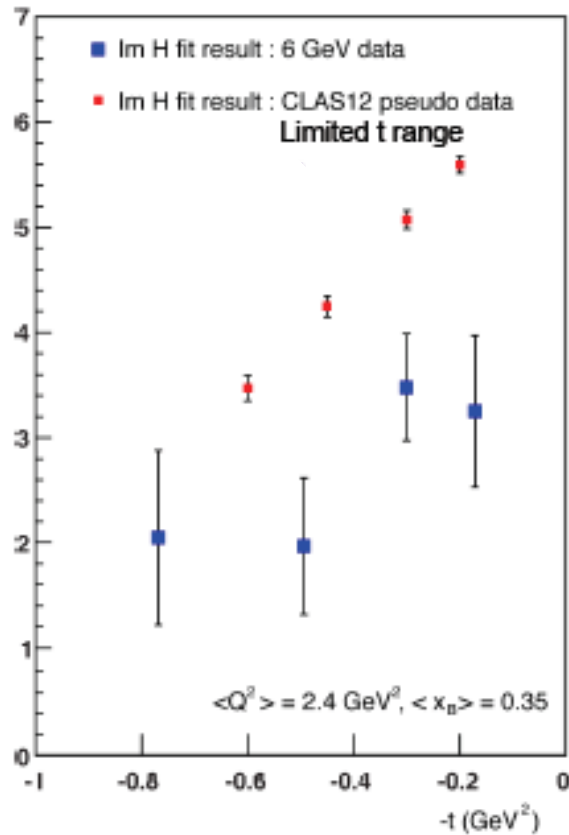
With large acceptance  
measure large  $Q^2$ ,  $x_B$ ,  $t$   
ranges simultaneously.

$A_{LU}(Q^2, x_B, t)$   
 $\Delta\sigma(Q^2, x_B, t)$   
 $\sigma(Q^2, x_B, t)$

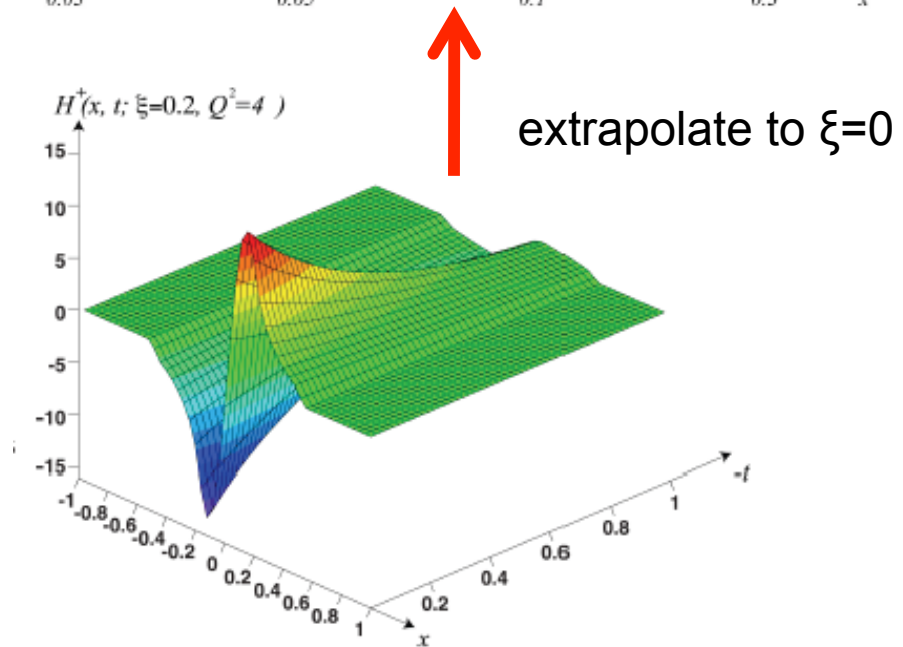
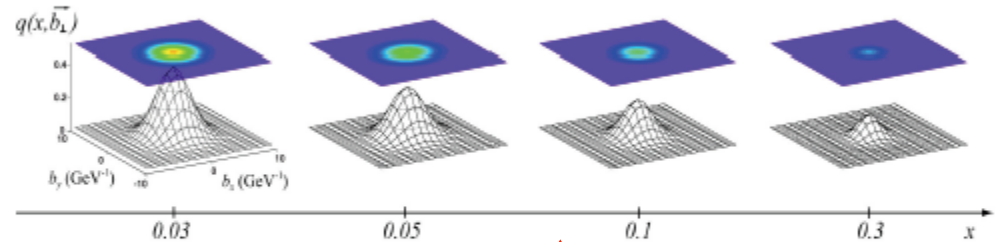
# GPDs from simulated CLAS12 data

E12-06-119

GPD H only contribution



$$q(x, \vec{b}_\perp) = \int \frac{d^2 \vec{\Delta}_\perp}{(2\pi)^2} e^{i\vec{b}_\perp \cdot \vec{\Delta}_\perp} H(x, \xi=0, -\Delta_\perp^2)$$



# CLAS12 DVCS/BH $A_{UL}$ on protons

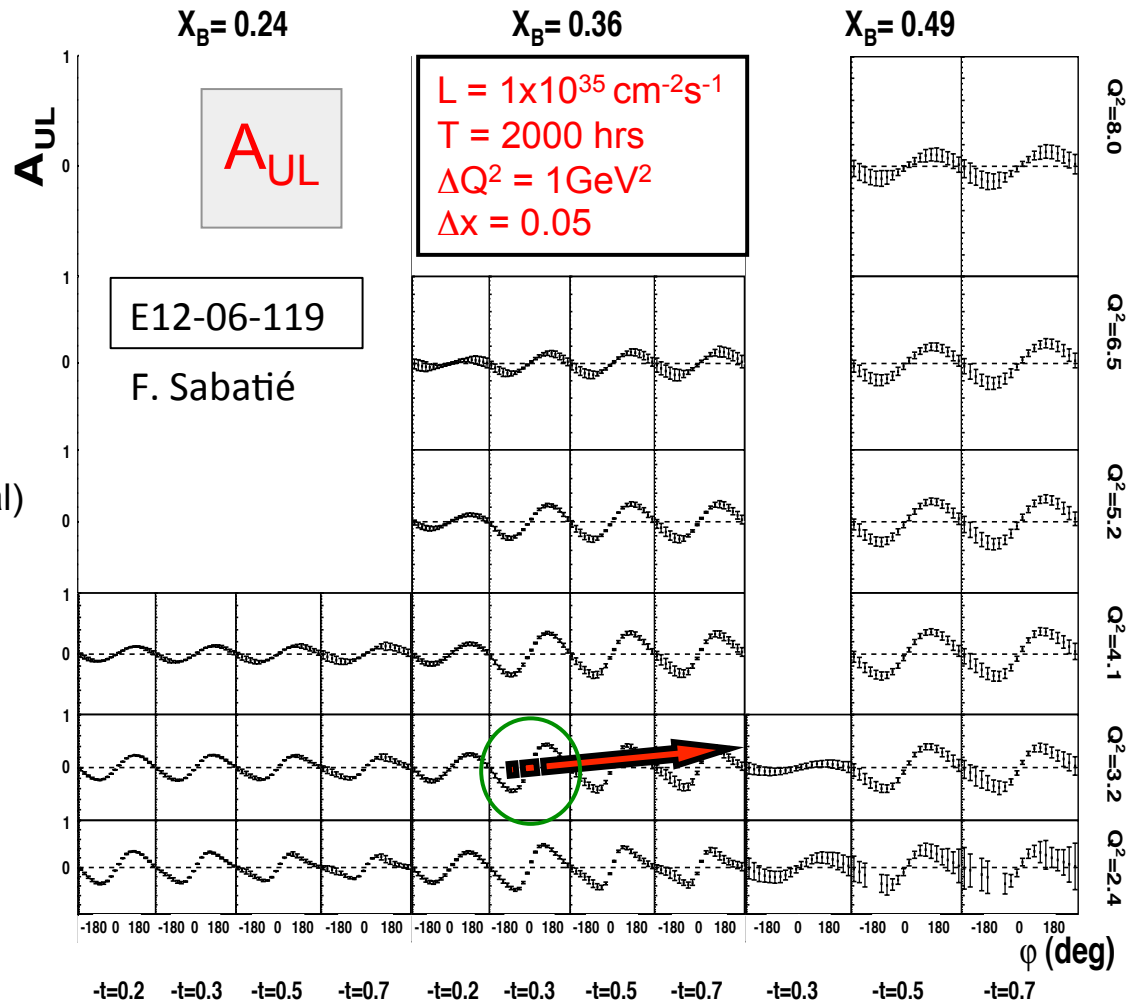
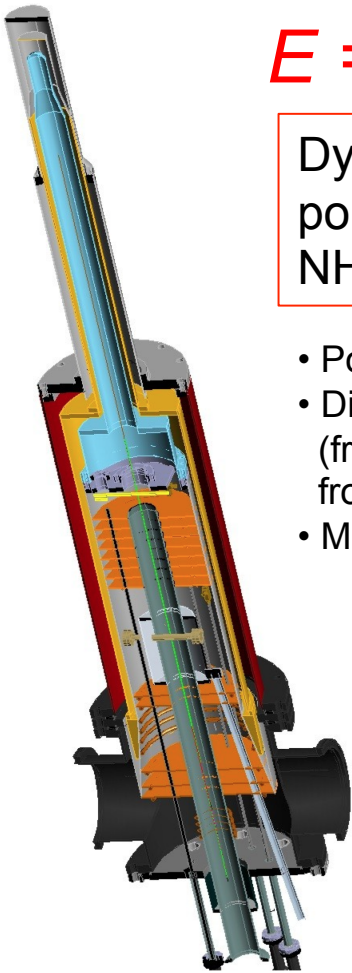
$$e \vec{p} \rightarrow e p \gamma$$

$$\Delta\sigma_{UL} \sim \sin\phi \{F_1 \tilde{H} + \xi(F_1 + F_2)(H + \xi/(1+\xi)E)\} d\phi$$

$E = 11 \text{ GeV}$

Dynamically  
polarized target  
 $\text{NH}_3, \text{ND}_3$

- Polarization: 0.8
- Dilution factor: 0.15  
(fraction of events from polarized material)
- Magnetic field: 5T



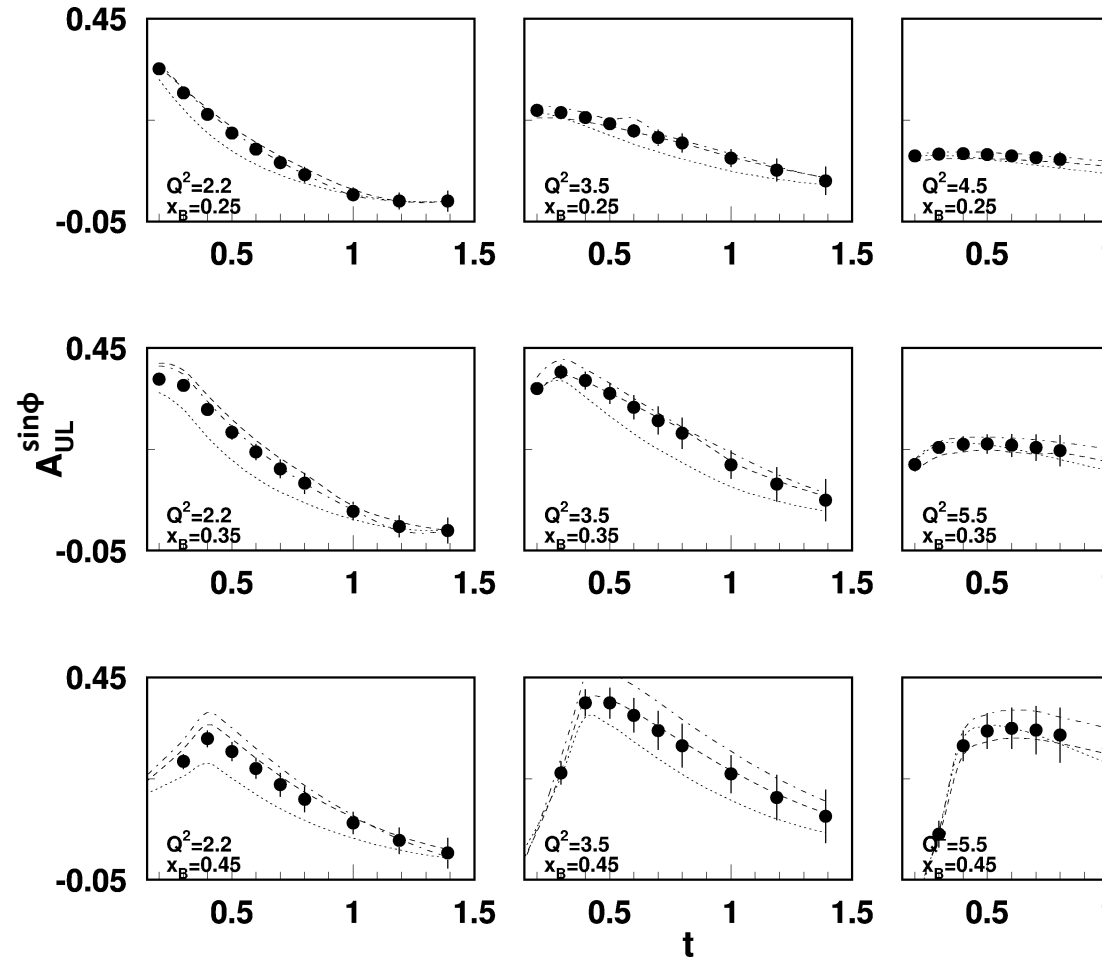


# CLAS12 $A_{UL} \sin\phi$ moment on protons

E12-06-119

F. Sabatié

Spin asymmetry with longitudinally polarized proton target

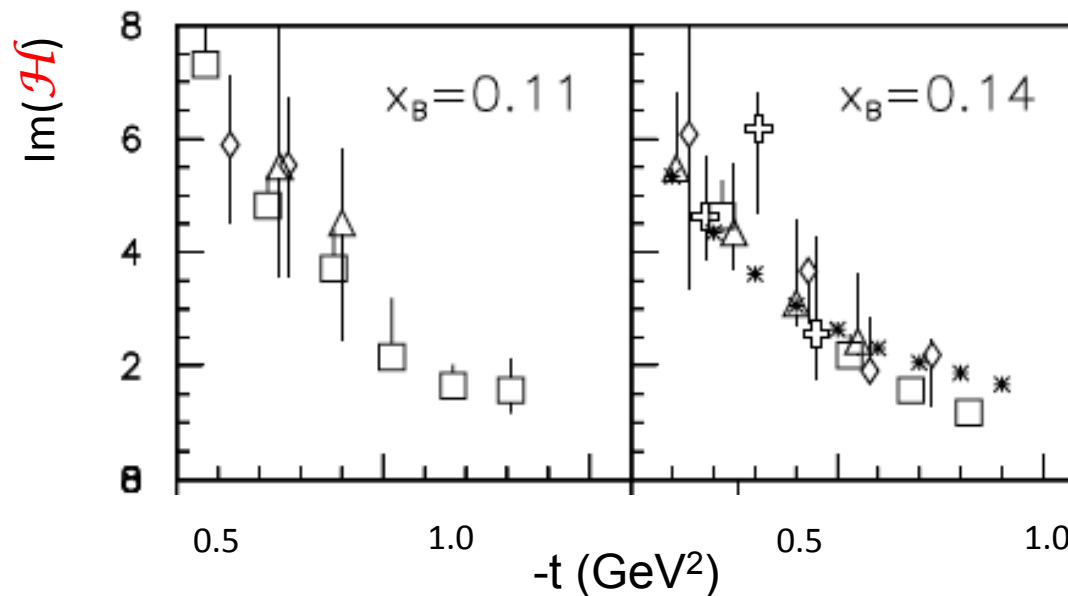


# Extraction of $\mathcal{H}$ & $\tilde{\mathcal{H}}$ from $A_{LU}$ and $A_{UL}$

$Q^2=1.5-7.5 \text{ GeV}^2$

3% of  
expected  
statistics

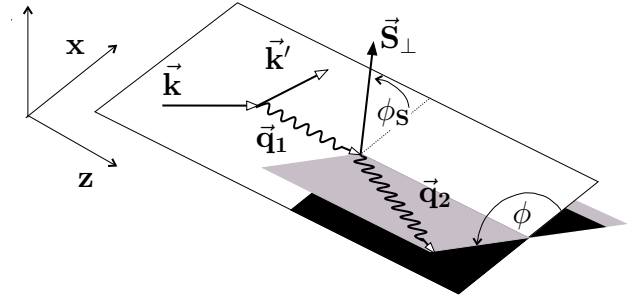
E12-06-119



M. Guidal: Model-independent analysis in leading twist

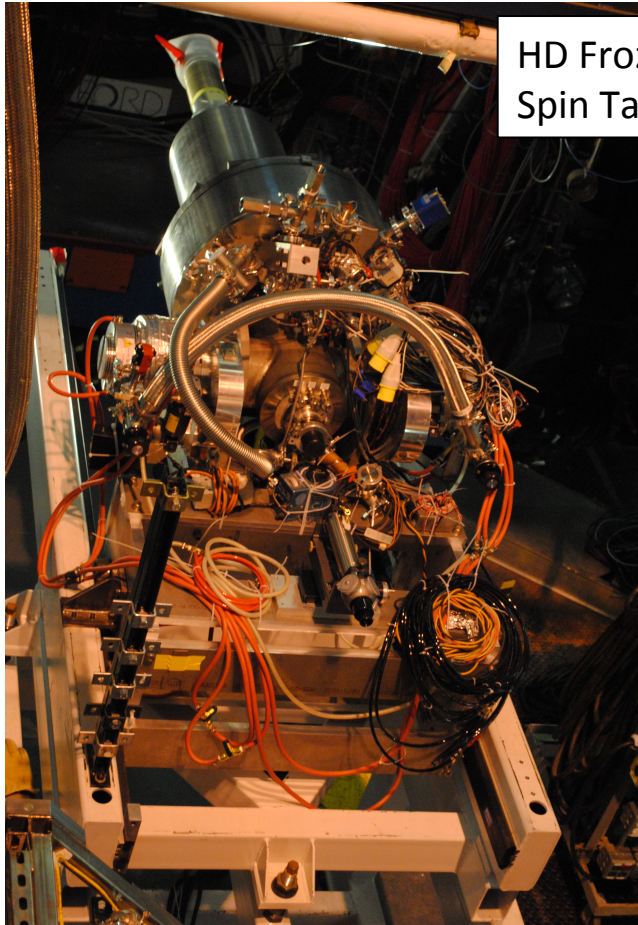
# CLAS12 Target spin asymmetry $A_{UT}$

$$\Delta\sigma \sim \cos\phi \sin(\phi - \phi_s) \text{Im}\{k_1(F_2 H - F_1 E)\} d\phi$$



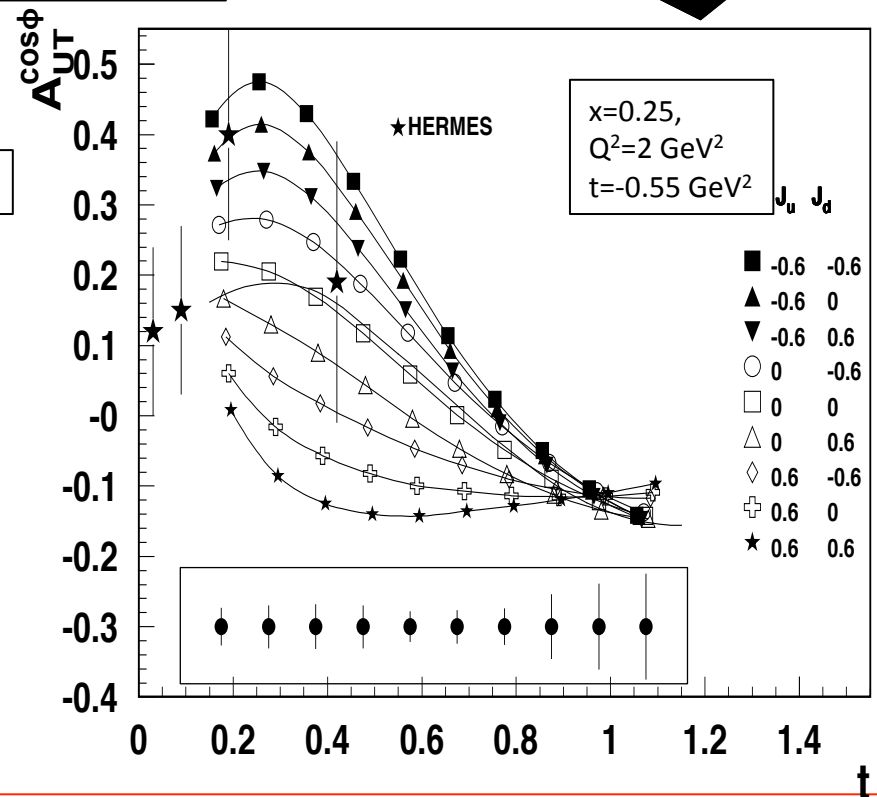
$P_p = 0.75$   
 $L = 10^{34} \text{cm}^{-2}\text{s}^{-1}$   
 2000 hrs

HD Frozen  
 Spin Target



LOI12-11-105

L. Elouadrhiri



$A_{UT}$  and  $A_{LT}$  are sensitive to the u and d-quark helicity content of the proton spin

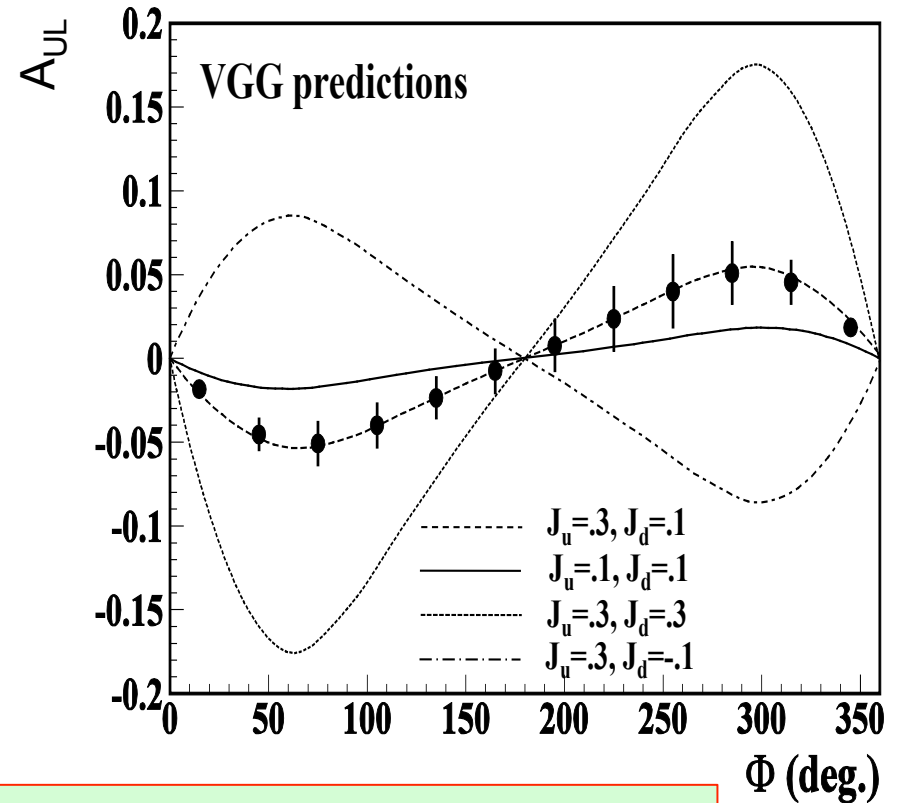
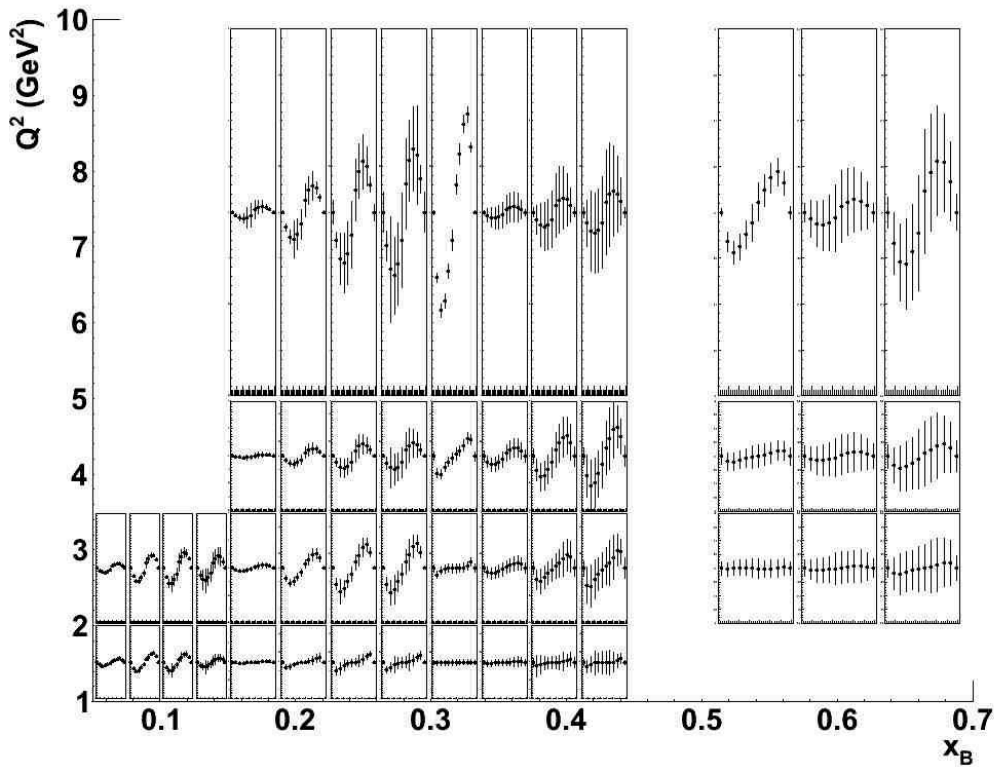
# CLAS12 DVCS/BH Beam asymmetries $A_{LU}$ neutrons

E12-11-003

S. Niccolai

Total of 588 bins  
in  $t$ ,  $Q^2$ ,  $x_B$ ,  $\phi$

$t = -0.35 \text{ GeV}^2$   
 $Q^2 = 2.75 \text{ GeV}^2$   
 $x_B = 0.225$

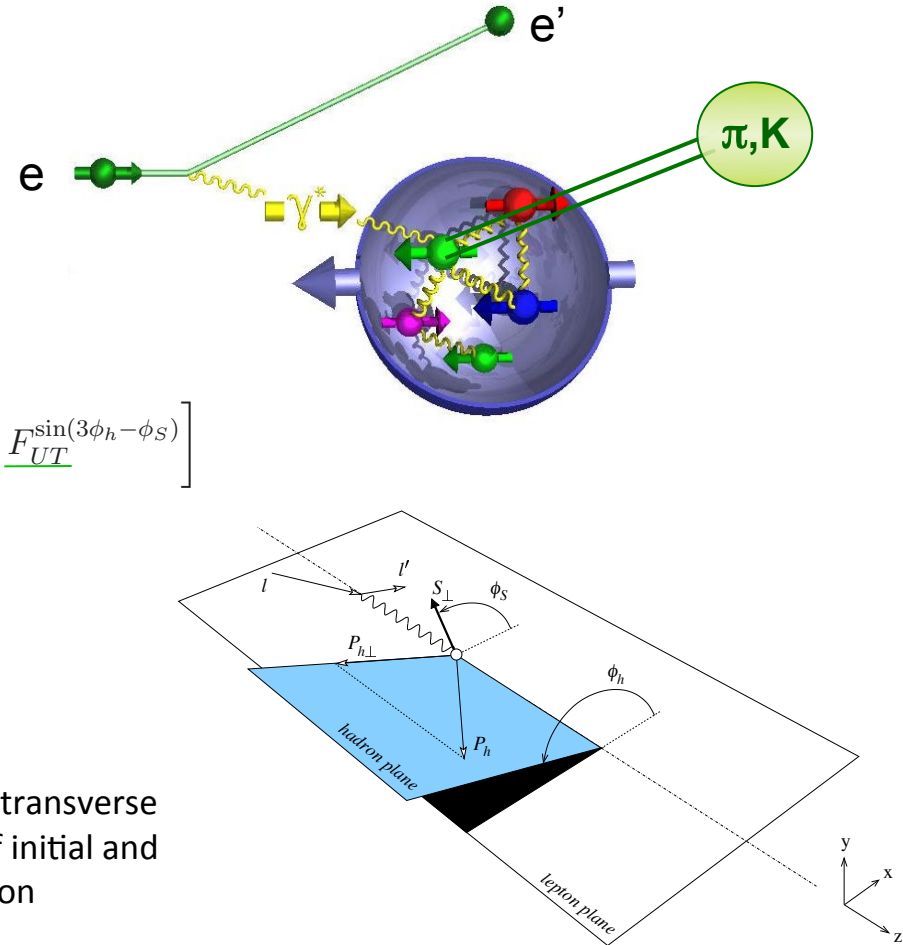


$A_{LU}$  is highly sensitive to d-quark helicity content of the neutron.

# SIDIS and Transverse Momentum Distribution

SIDIS cross section in leading twist:

$$\frac{d\sigma}{dx dy dz d\phi_S d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xQ^2} \frac{y}{2(1-\varepsilon)} \times \left\{ \begin{aligned} &F_{UU,T} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + S_L \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \\ &+ S_L \lambda_e \sqrt{1-\varepsilon^2} F_{LL} + S_T \left[ \sin(\phi_h - \phi_S) F_{UT,T}^{\sin(\phi_h - \phi_S)} \right. \\ &\quad \left. + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right] \\ &+ S_T \lambda_e \left[ \sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} \right] \end{aligned} \right\},$$



The 8 structure functions factorize into TMD parton distributions, fragmentation functions, and hard parts:

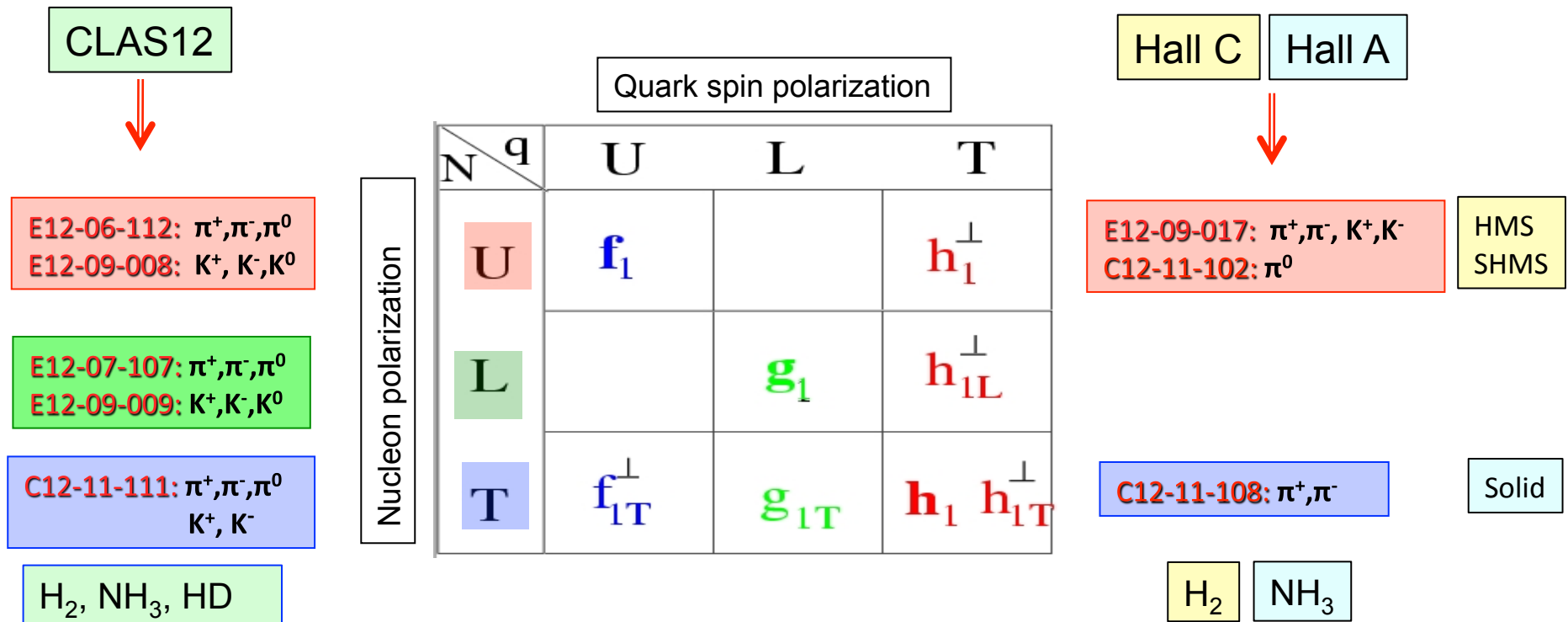
$$\begin{aligned} F_{UU} &\propto \boxed{f_1(x, k_\perp)} \boxed{D_1(z_h, p_\perp)} \boxed{H_{UU}(Q^2)} \\ F_{LL} &\propto \boxed{g_{1L}(x, k_\perp)} \boxed{D_1(z_h, p_\perp)} \boxed{H_{LL}(Q^2)} \\ F_{UL} &\propto \boxed{h_{1L}^\perp(x, k_\perp)} \boxed{H_1^\perp(z_h, p_\perp)} \boxed{H_{UL}(Q^2)}, \end{aligned}$$

Integrals over transverse momentum of initial and scattered parton

A full program to extract L.T. TMDs from measurements requires separation of the structure function using polarization, and coverage of a large range in  $x$ ,  $z$ ,  $P_T$  along with sensitivity to  $Q^2$ , and the flavor separation in  $u$ ,  $d$ ,  $s$  quarks.

# JLab TMD Proton Program @ 12 GeV

Leading twist TMD parton distributions:  
information on correlations between  
*quark orbital motion* and *spin*



The TMD program will map the 4D phase space in  $Q^2, x, z, P_T$

# CLAS12 $A_{UU}$ for pions on unpolarized protons.

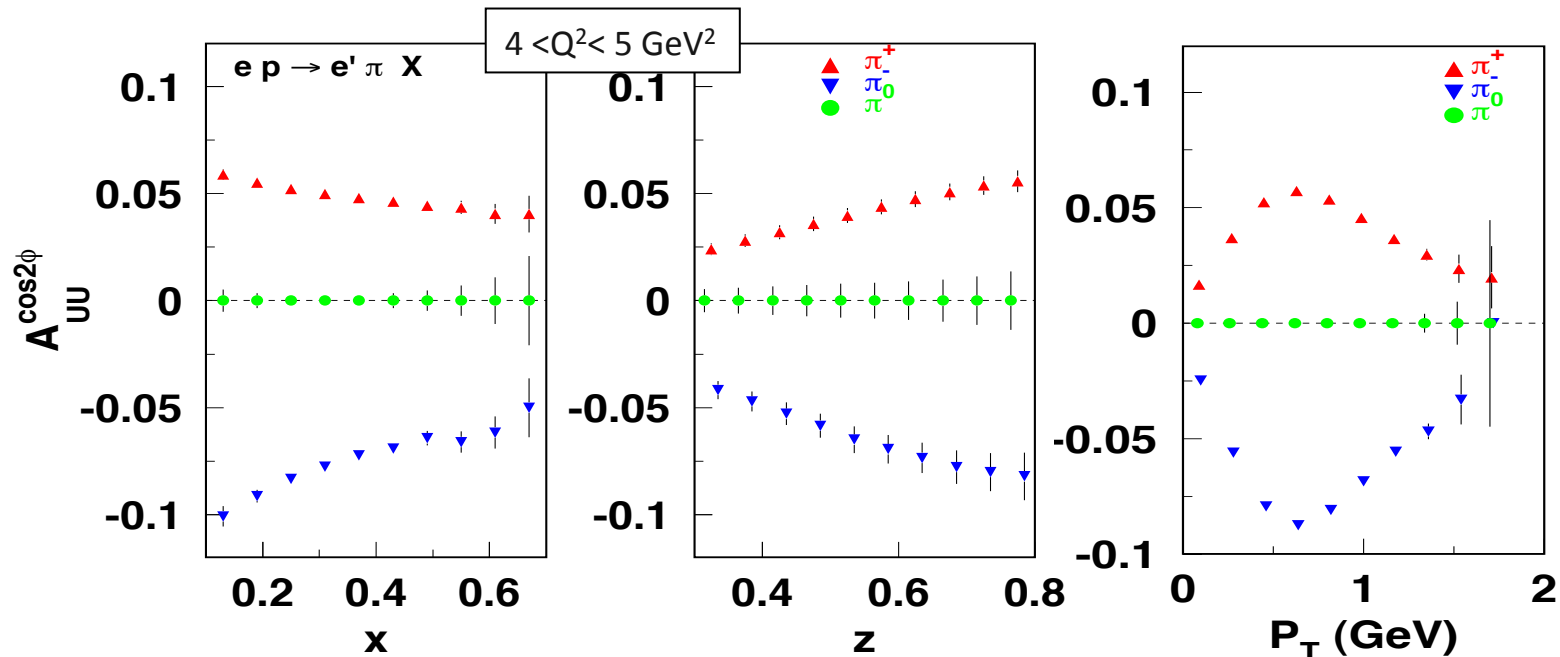
E12-06-112

H. Avakian

N \ q	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1^\perp \quad h_{1T}^\perp$

$$\frac{d\sigma}{dx_B dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \epsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right\},$$

Measures momentum distribution of **trans.** pol. quarks in unpol. nucleon



Wide  $x$  and  $P_T$  range needed to map out phase space in longitudinal and transverse quark momentum

# SIDIS pion/kaon on unpolarized protons.

N \ q	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1 h_{1T}^\perp$

$$\frac{d\sigma}{dx_B dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \epsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right\}$$

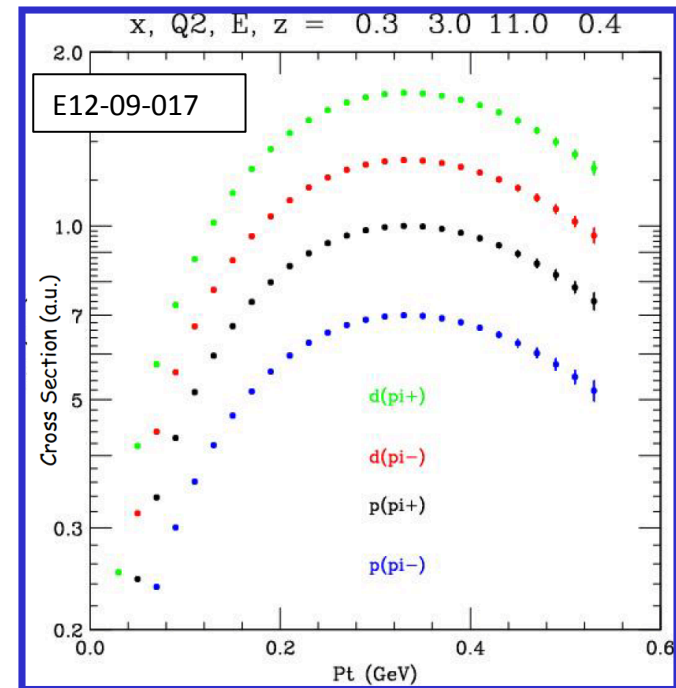
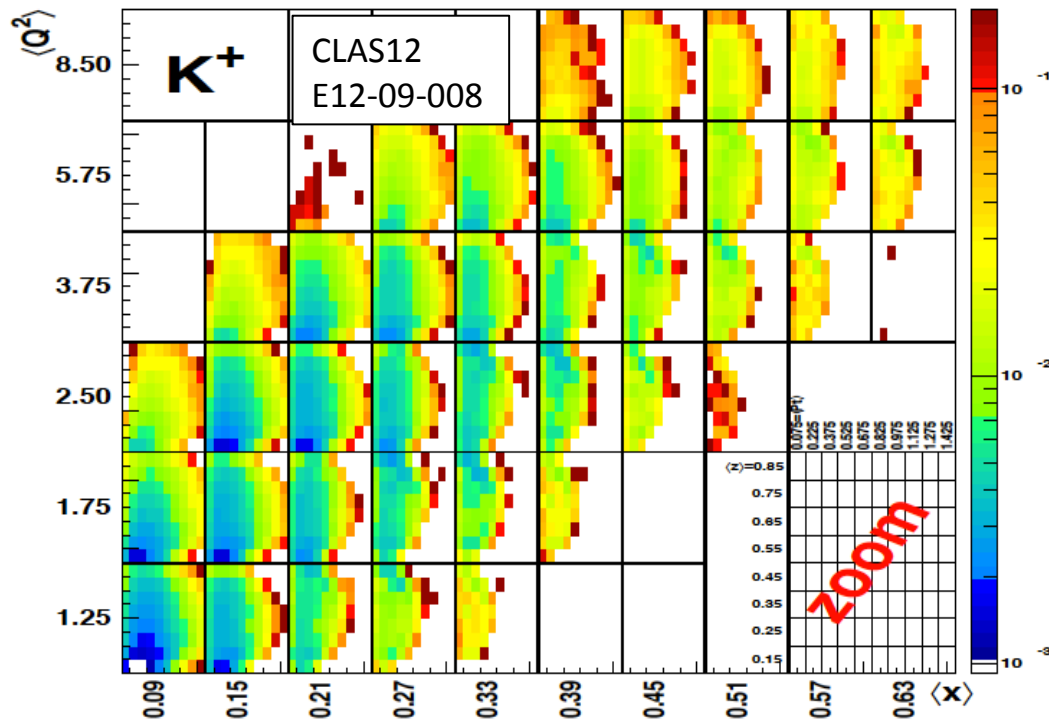
E12-09-008

H. Avakian, P. Rossi

E12-09-017

R. Ent

Hall C: Precise measurement in small  $P_T$  range  
(Kinematics II,  $z = 0.4$  bin only)





# Extraction of $f_1(x, z^2, b_T^2)$

Project x-section onto  $b_T$ -space to avoid convolution + Bessel weighting

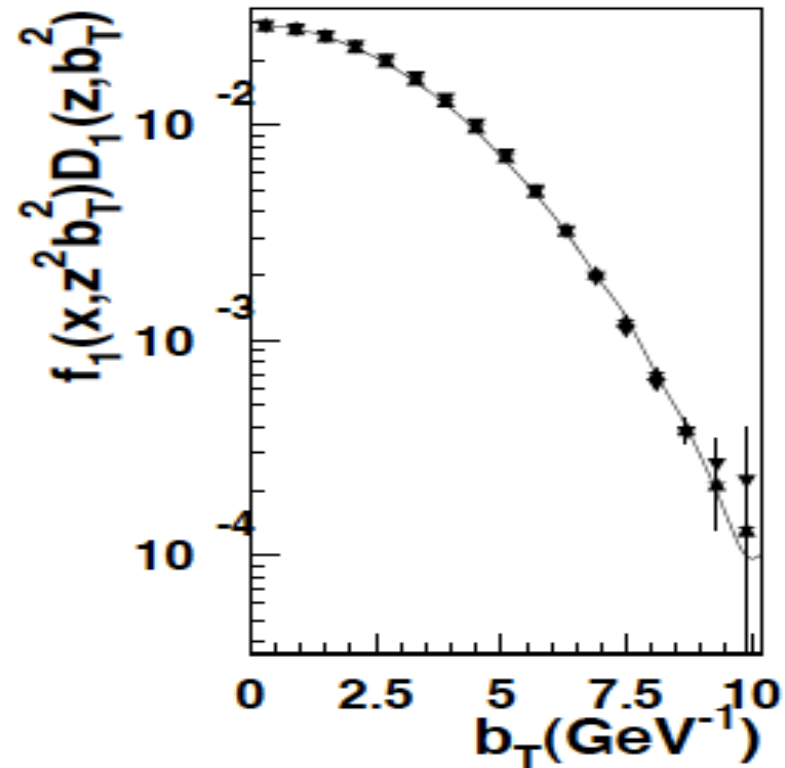
$$\int_0^\infty d|P_{h\perp}| |P_{h\perp}| J_0(|P_{h\perp}| |b_T|) \left[ \frac{d\sigma}{dx_B dy d\phi_S dz_h d\phi_h |P_{h\perp}| d|P_{h\perp}|} \right]$$

Boer, Gamberg, Musch,  
Prokudin, arXiv:1107.5294

$$\tilde{f}_1^q(x, z^2 b_T^2) \tilde{D}_1^{q \rightarrow \pi}(z, b_T^2)$$

- provides a model independent way to study kinematical dependences of TMDs
- requires wide range in hadron  $P_T$

Example of simulated data with CLAS12



# CLAS12 $A_{UL}$ on longitudinally polarized target

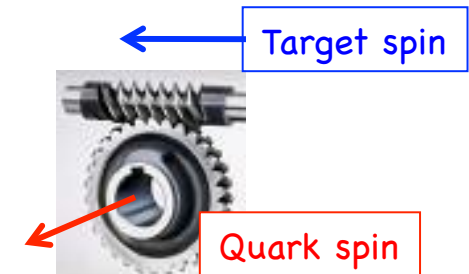
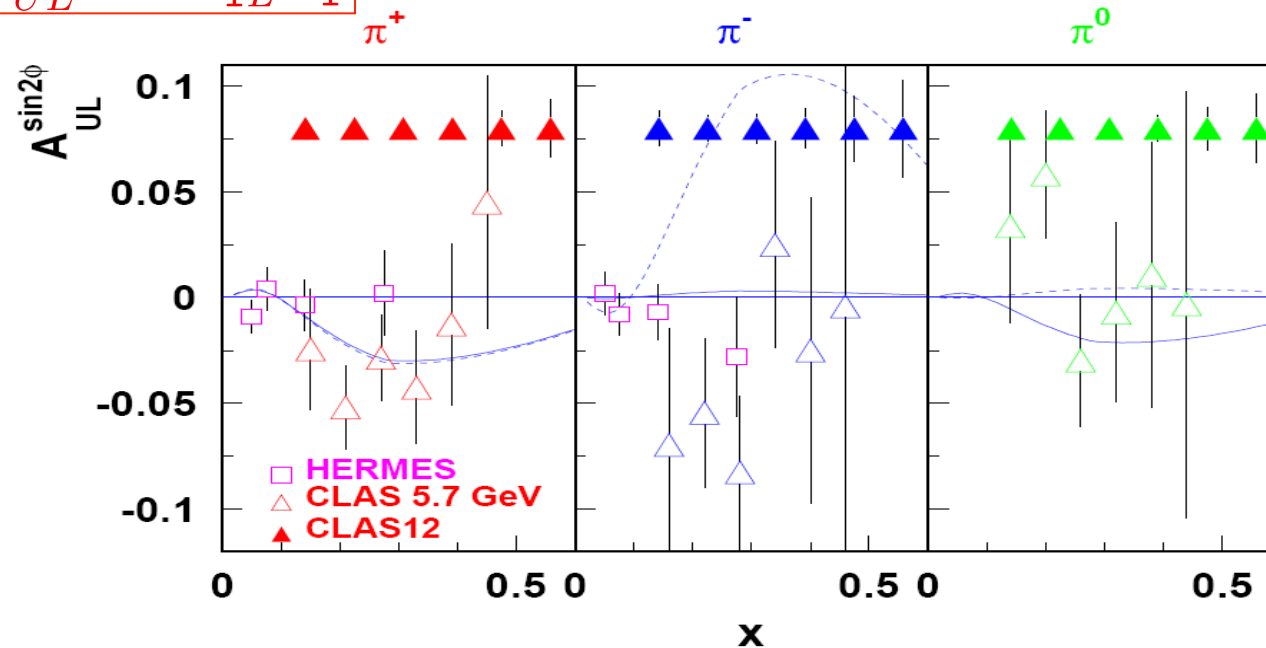
$Z \backslash q$	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1 h_{1T}^\perp$

The Kotzinian-Mulders function measures the momentum distribution of transversely polarized quarks in a longitudinally polarized nucleon.

E12-09-008

H. Avakian

$$A_{UL}^{\sin 2\phi} \sim h_{1L}^\perp H_1^\perp$$



- This is the only leading twist azimuthal moment for longitudinally polarized target. The  $\sin 2\phi$  moment is sensitive to spin-orbit correlations.

# CLAS12 $A_{LL}$ in double polarization

N \ q	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1^\perp h_{1T}^\perp$

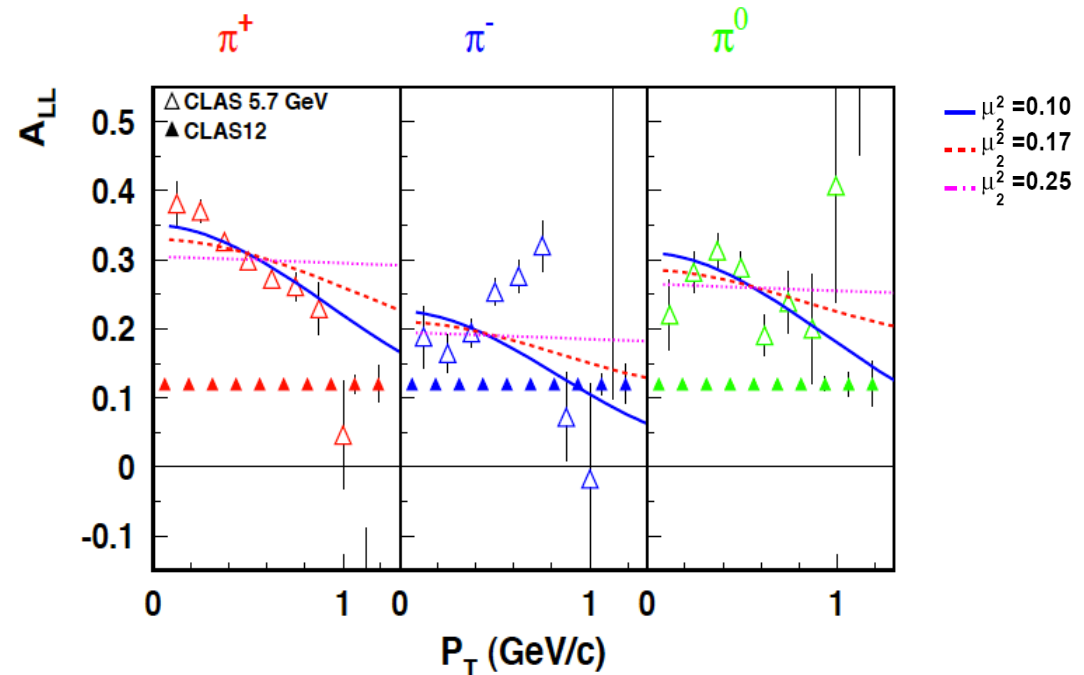
Transverse momentum dependence of longitudinally polarized quarks in longitudinally polarized protons.

M. Anselmino et al Phys.Rev.D74:074015,2006

E12-07-107

H. Avakian  
P. Rossi

The double polarization asymmetry is sensitive to the difference in the  $k_T$  distribution of quarks with spin orientation parallel and anti-parallel to proton spin.



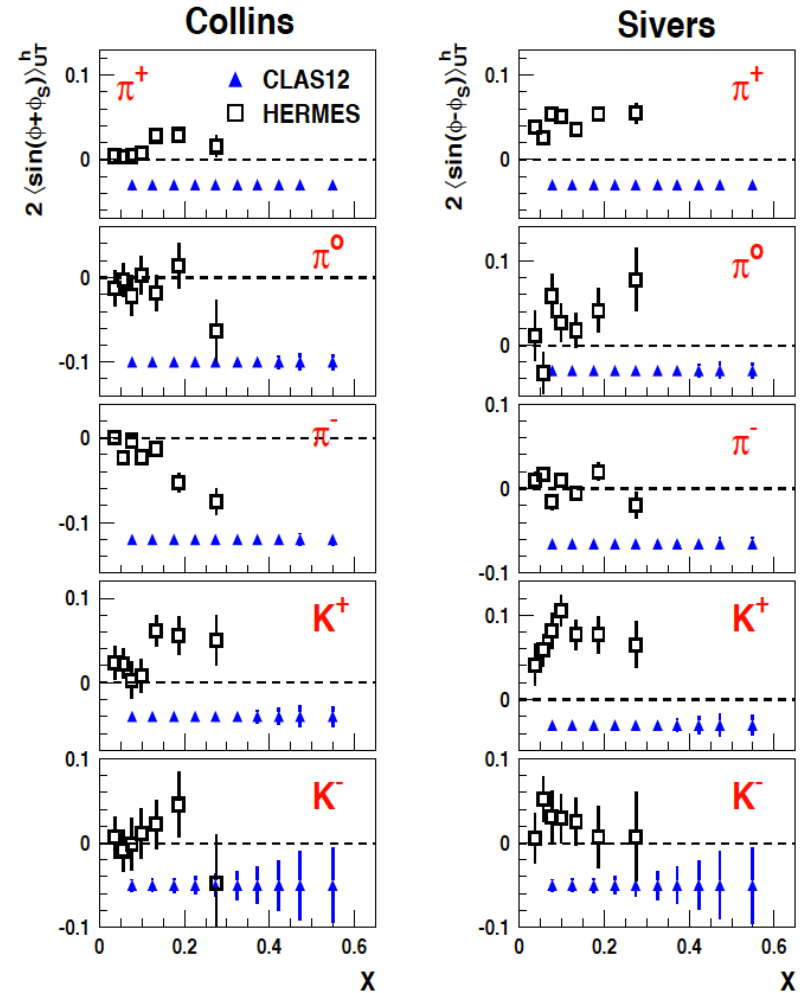
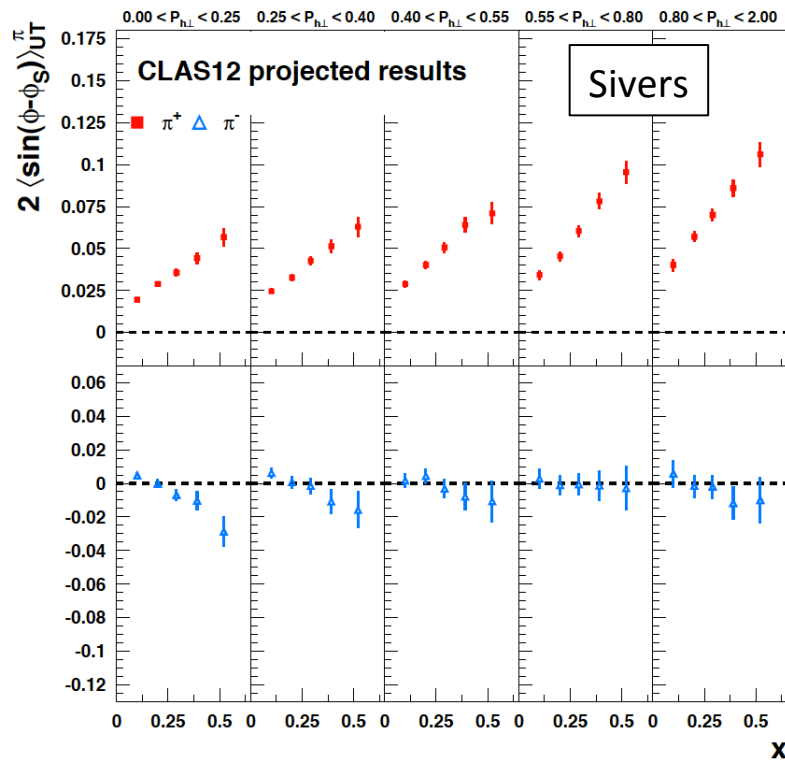
H. Avakian et al, (CLAS), Phys.Rev.Lett. 105 (2010) 262002

# CLAS12 $A_{UT}$ with transverse proton target

$Z \backslash q$	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1^\perp, h_{1T}^\perp$

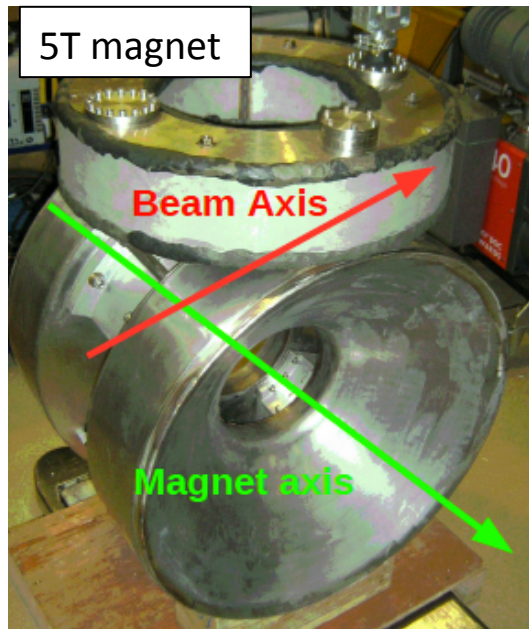
C12-11-111

M. Contalbrigo



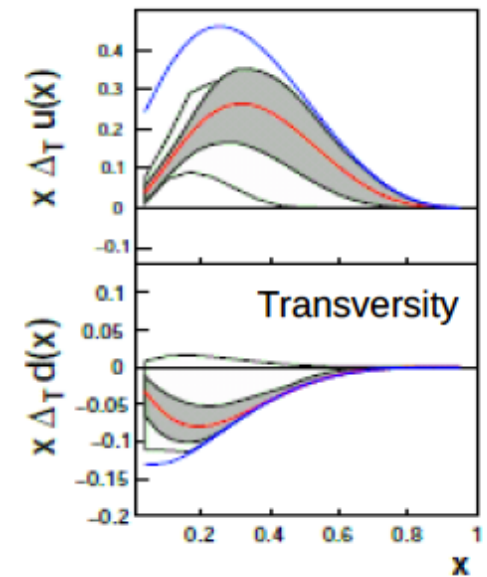
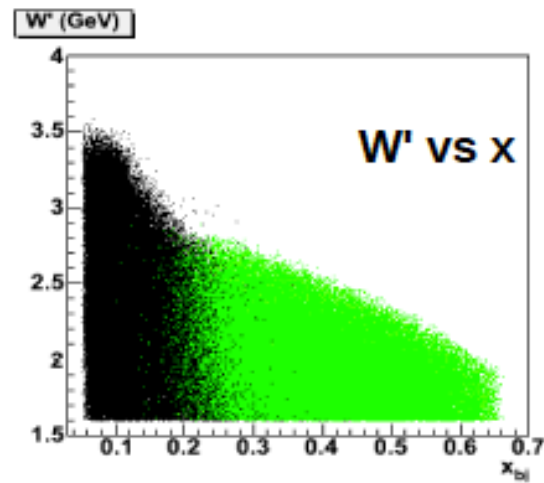
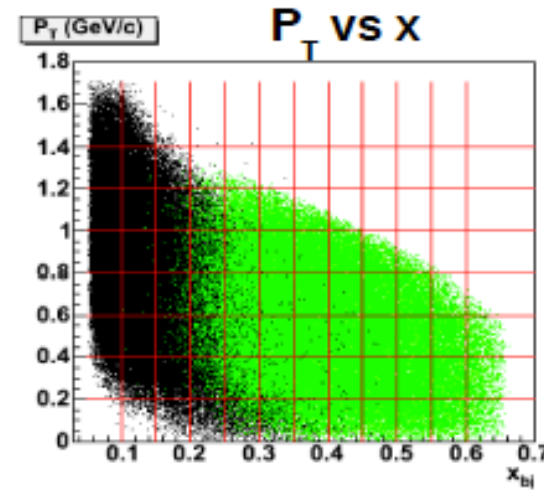
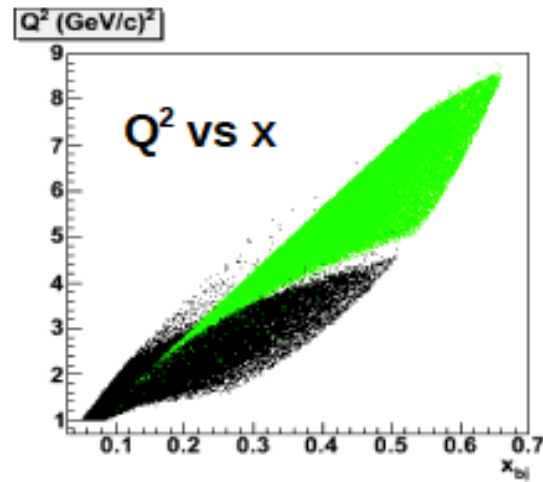
The high statistics allows for  $x$ - $P_\perp$  bins

# SOLID $A_{UT}$ with transverse proton target



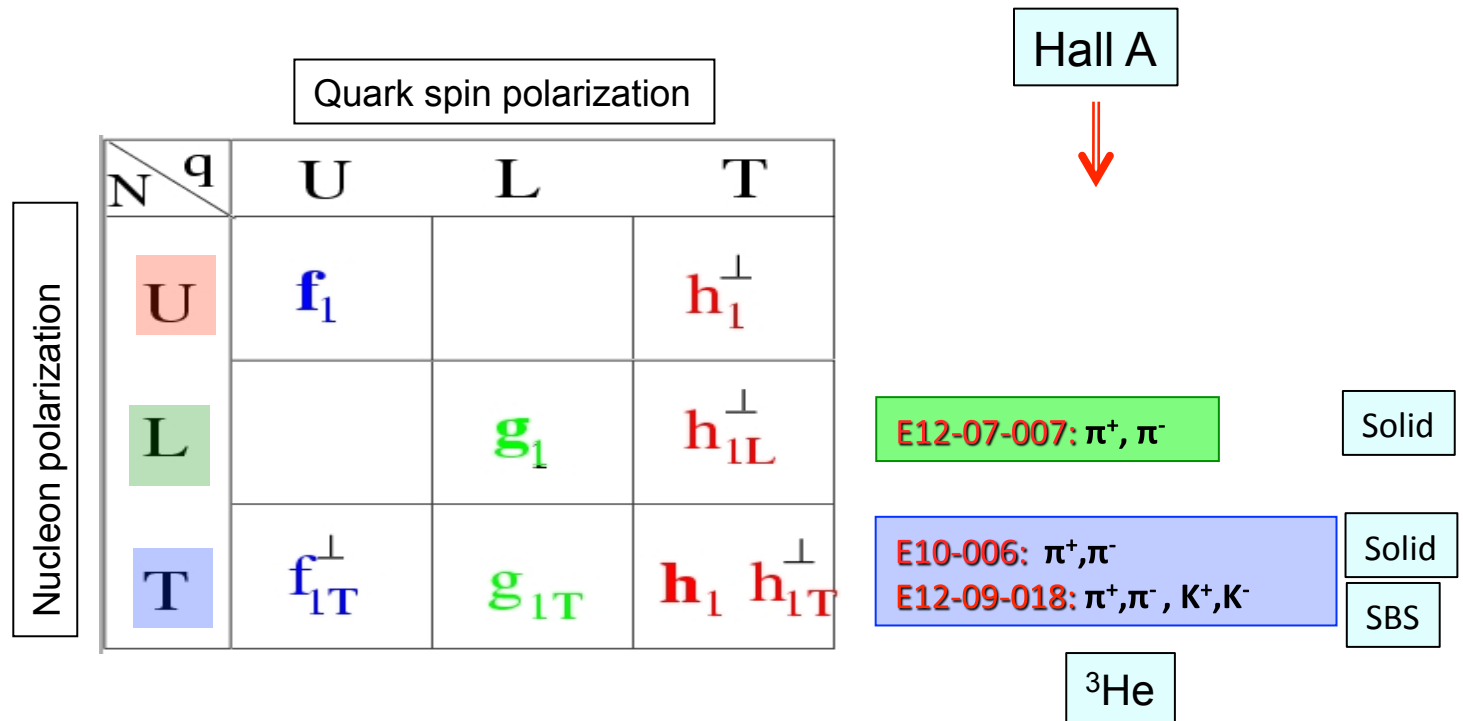
E12-11-108

K. Allada



# JLab TMD $^3\text{He}$ Program @ 12 GeV

Leading twist TMD parton distributions:  
information on correlations between  
*quark orbital motion* and *spin*

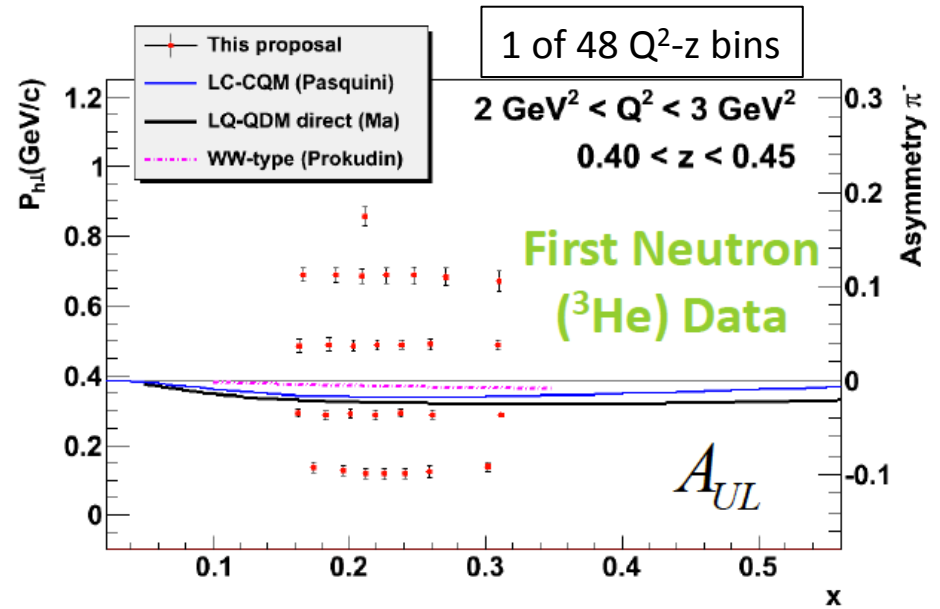
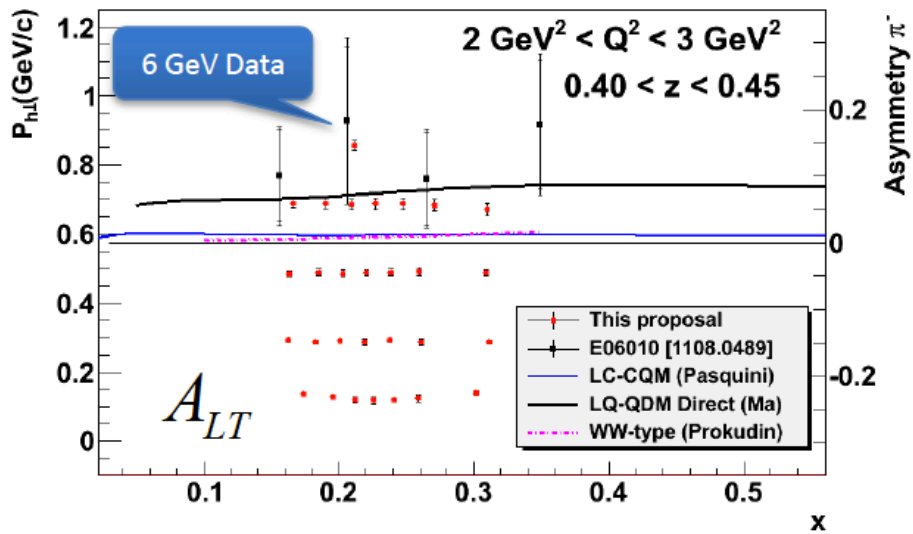


# SOLID $A_{UL}$ on ${}^3\text{He}$

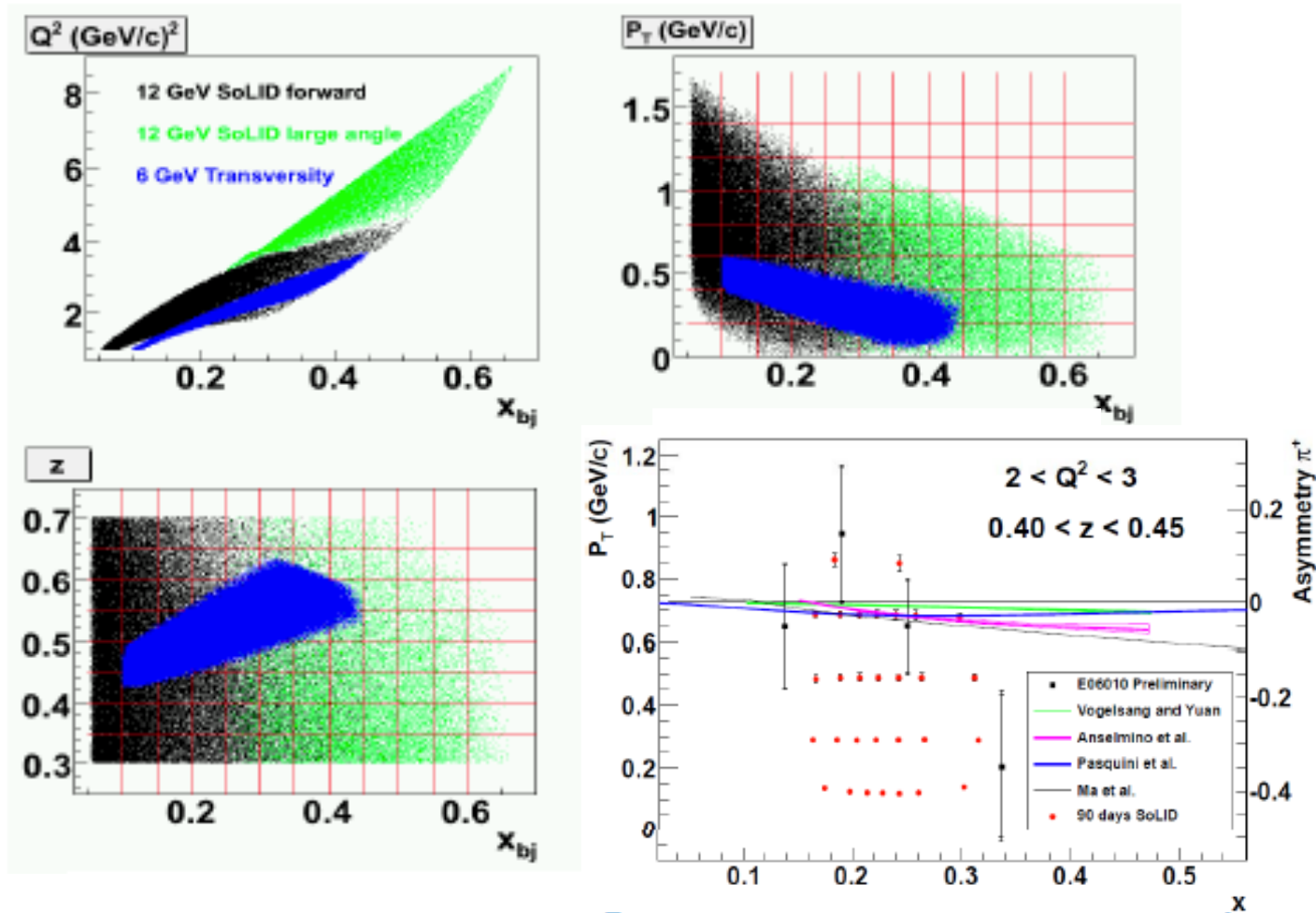
Z \ q	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1^\perp, h_{1T}^\perp$

E12-11-007

$e^3\text{He} \rightarrow e\pi^+X$



# SOLID $A_{UT}$ on $^3\text{He}$ Target

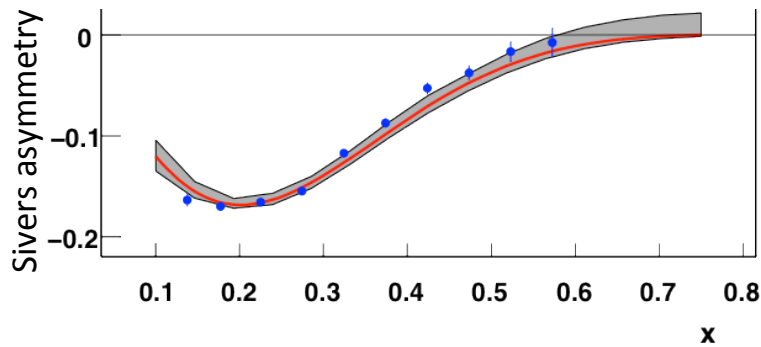
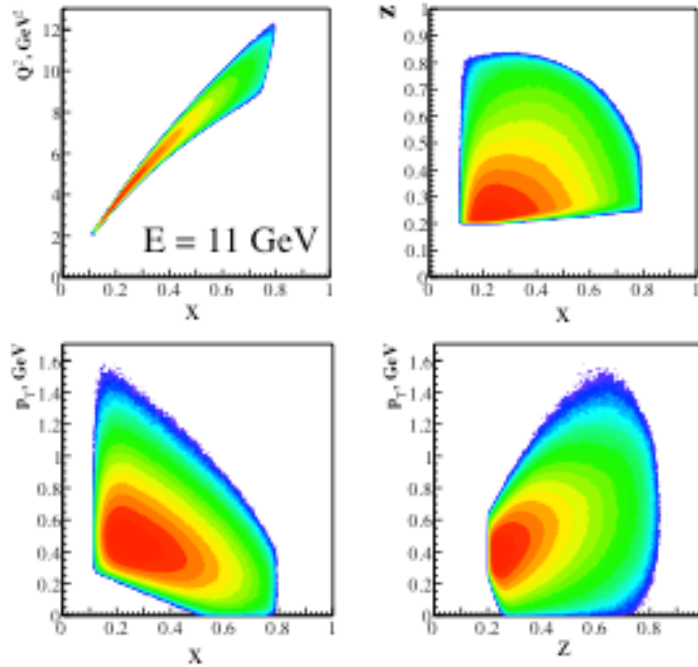


1/48 bins  
in  $Q^2, z$



# SBS/BB $A_{UT}$ on $^3\text{He}$ Target

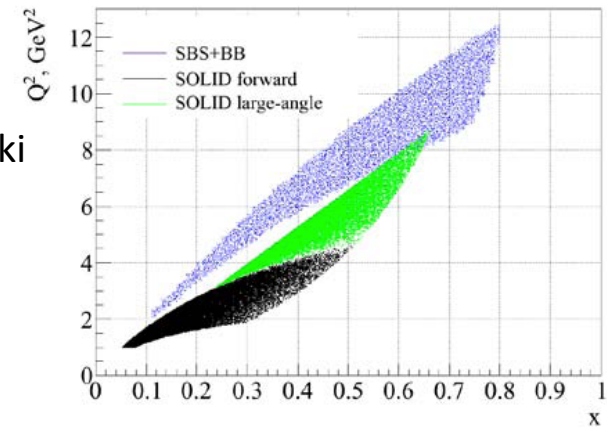
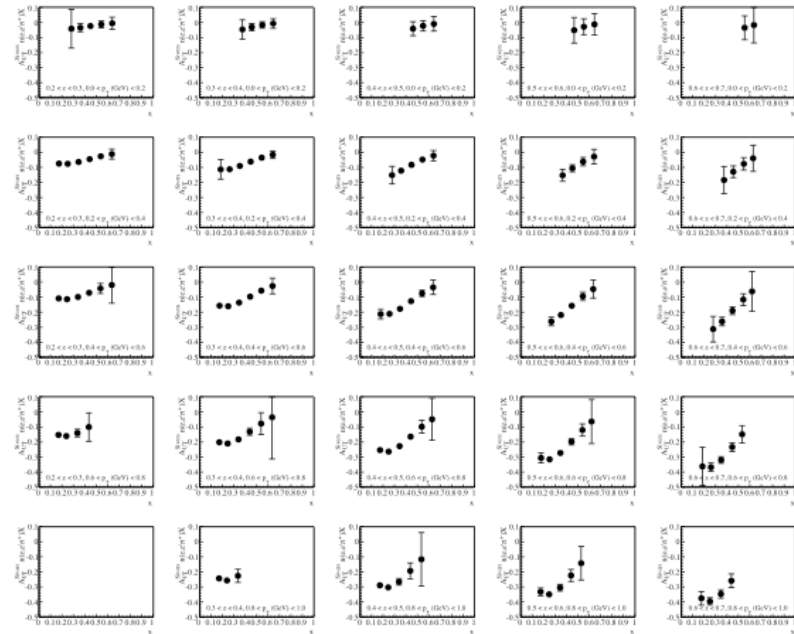
$^3\text{He}(e, e' \pi^{+, -, 0}), ^3\text{He}(e, eK^{+, -})$



C12-09-018

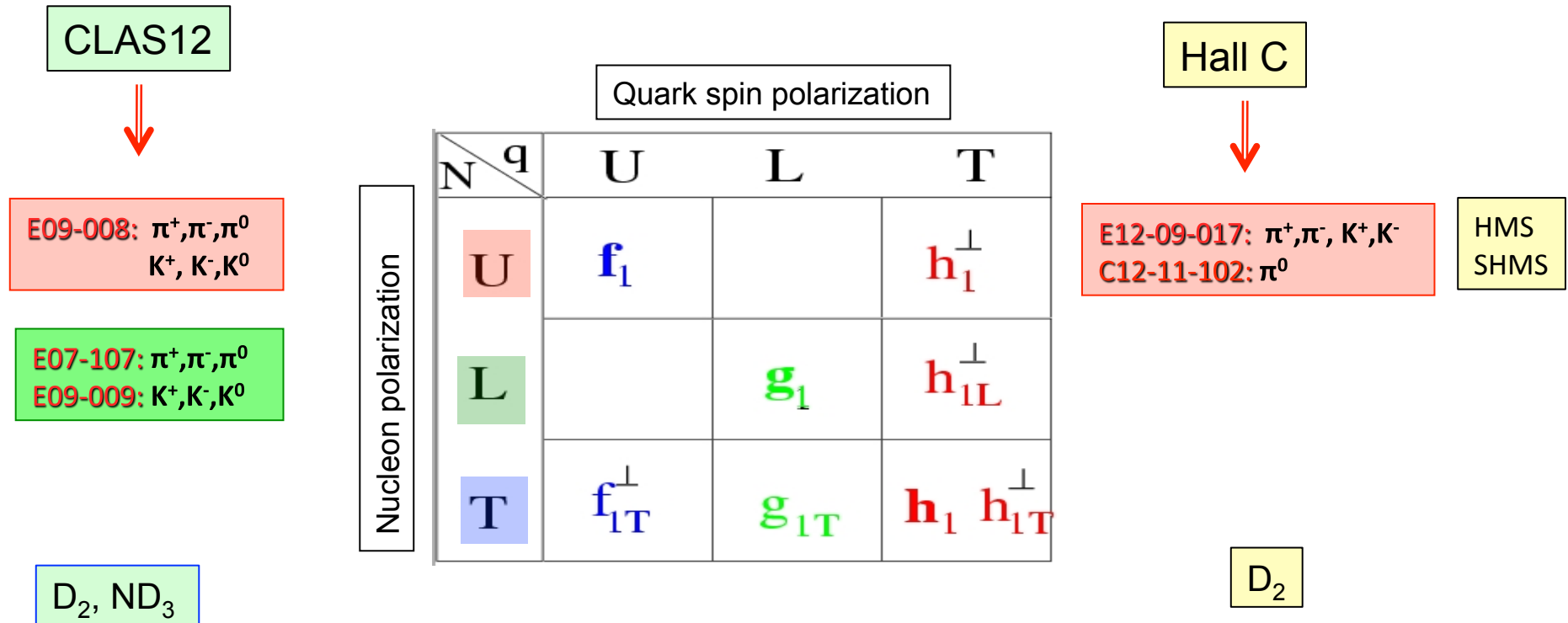
B. Wojtsekhowski

$n(e, e' \pi^+)$



# JLab TMD $D_2$ Program @ 12 GeV

Leading twist TMD parton distributions:  
information on correlations between  
*quark orbital motion* and *spin*



The JLab TMD program will chart the 4D phase space in  $Q^2, x, z, P_T$

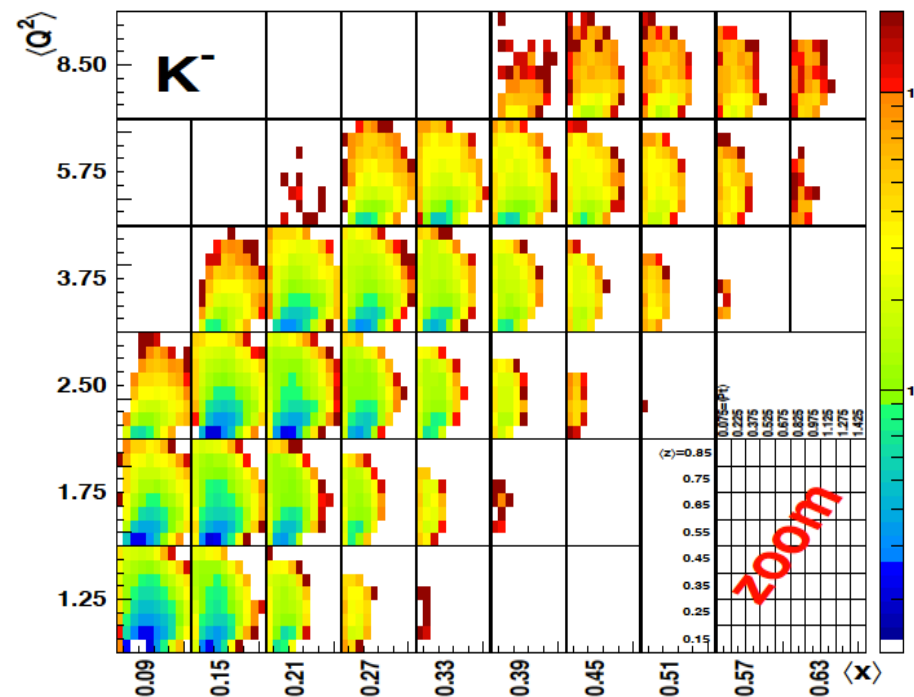
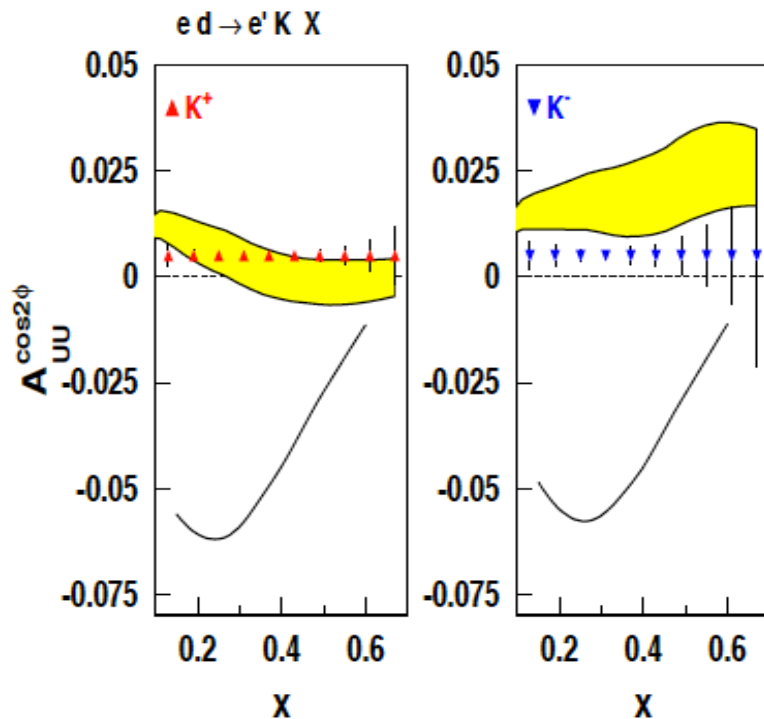
# CLAS12 Kaon $A_{UU}$ on unpolarized $D_2$

$Z \backslash q$	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1^\perp, h_{1T}^\perp$

$$\frac{d\sigma}{dx_B dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \epsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right\},$$

CLAS12 acceptance

P. Rossi

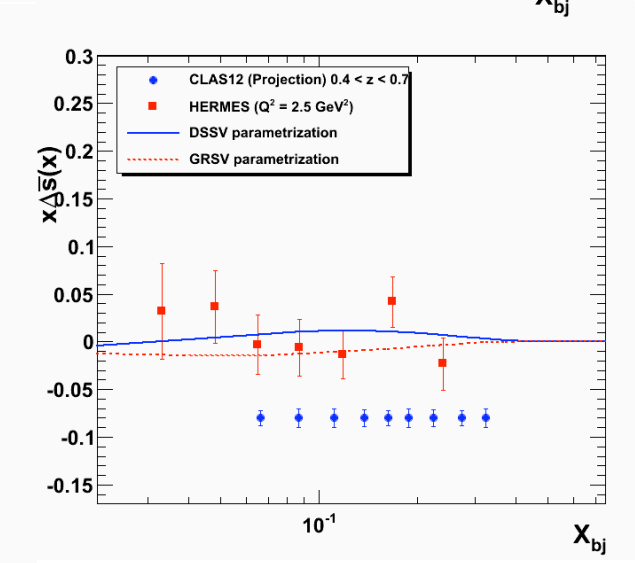
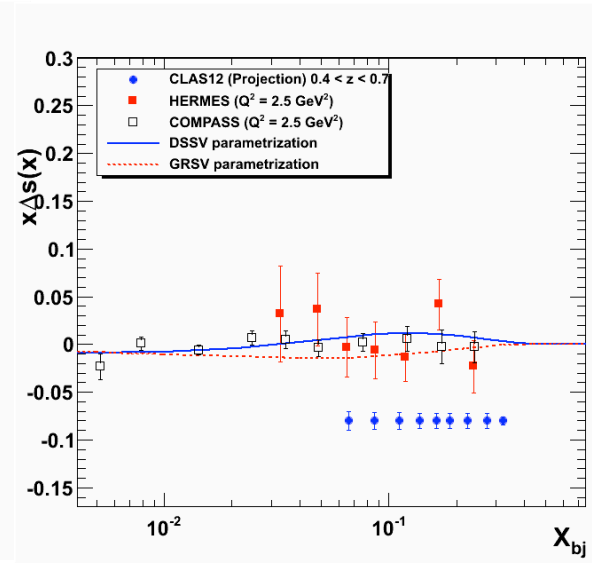
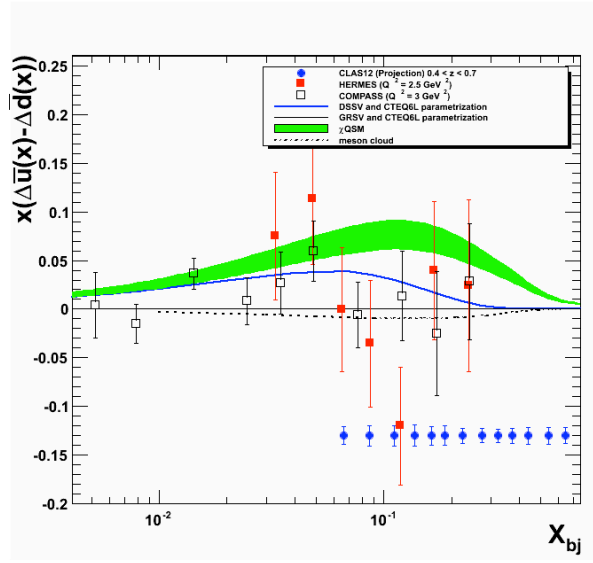
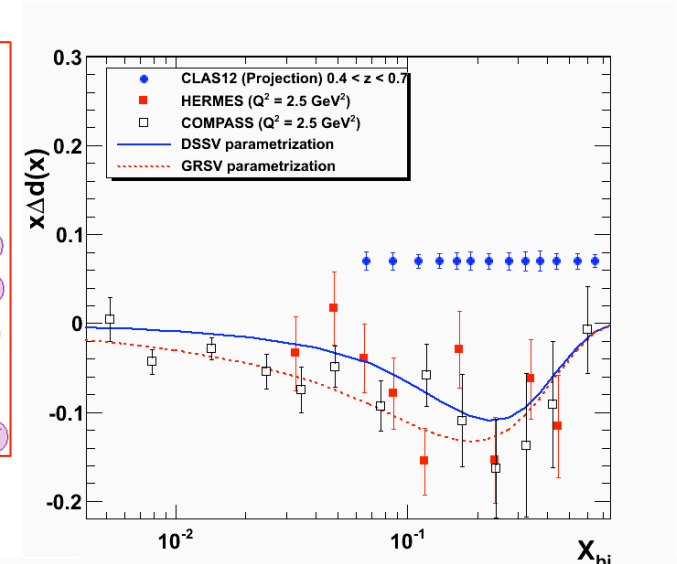
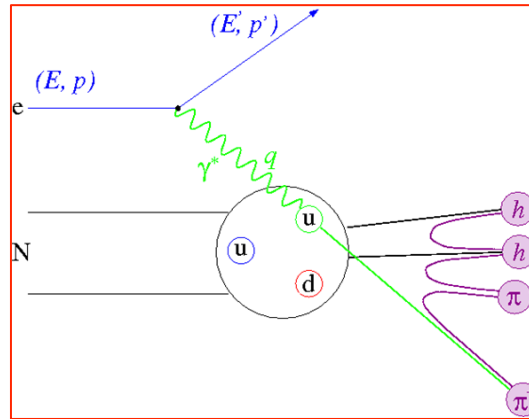


# CLAS12 PDFs in $\pi/K$ SIDIS

Extraction of the individual contributions of quarks and anti-quarks to the nucleon spin. Use polarized & unpolarized proton and deuteron targets.

E12-09-002

K. Hafidi



# Conclusions

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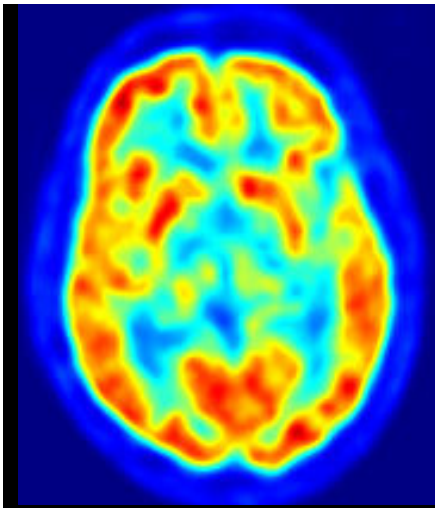
- Several detectors under construction or proposed – CLAS12, SBS, SOLID to carry out 3D nucleon imaging program
- JLab12 has a well defined and broad experimental program to measure DVCS in the full phase space available at 12 GeV:  $Q^2 < 9\text{GeV}^2$ ,  $0.5 < x_B < 0.7$ ,  $-t < 2.5\text{GeV}^2$ .
- CLAS12 is the major detector system to measure DVCS cross section and target polarization observables
- High statistics data are expected from Hall A for DVCS cross sections in reduced kinematics
- JLab12 has a broad program defined to measure TMDs in 4D phase space  $Q^2$ ,  $x_B$ ,  $z$ ,  $P_T$
- Use of full acceptance detectors with excellent Kaon identification essential for complete program
- Use of polarized proton ( $\text{NH}_3$ ) and neutron ( $\text{ND}_3$ ,  $^3\text{He}$ ) targets with longitudinal and transverse polarization are available for complete program



# Promise of GPDs & TMDs: Imaging of the Proton

$$\varepsilon(x, b_{\perp}) = \int \frac{d^2 \Delta_{\perp}}{(2\pi)^2} e^{i\Delta_{\perp} b_{\perp}} E_q(x, \Delta_{\perp})$$

Cat scan of the human brain



TMDs extend the image to include the quarks orbital motion.

