



# *Study of Collins Asymmetries at BaBar*

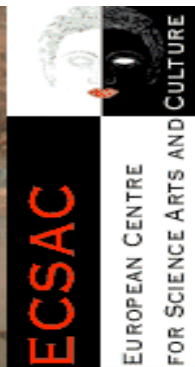
*Isabella Garzia*

On behalf of the BaBar Collaboration

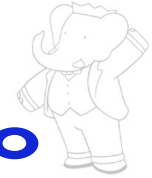
Università degli studi di Ferrara, INFN - Sezione di Ferrara



**Third International Workshop on  
*Transverse Polarization Phenomena In Hard Scattering*  
29 August - 2 September 2011  
Veli Lošinj - Croatia**



# OUTLINE



- **Introduction**
  - Fragmentation Functions (FFs)
  - Collins FF
  - Global analysis: first extraction of Transversity
  - Reference Frame
- **BaBar Detector**
- **Analysis:**
  - Analysis Strategy
  - Event and Tracks selection
  - Asymmetry dilution
- **Systematic study**
- **Preliminary Results**
- **Plans and Conclusions**

# Fragmentation Functions (FFs)



Fragmentation: hadron production from quark, antiquark or gluon.

FFs: probability that a parton fragments into an hadron carrying away a fraction of parton's momentum.

## Unpolarized FF

- Most of data are obtained at LEP energies
- At lower CMS energies and higher  $x$ , very little data are available
- BaBar and Belle  $\rightarrow$  results on FF for heavy quarks
- BaBar  $\rightarrow$  light-quark analysis ongoing
- Many attempts to extract FF from  $e^+e^-$  data: KKP, AKK, Kretzer...
  - $\rightarrow$  Large difference between different fits

(Nucl.Phys. **B725**,181(2006), Nucl.Phys. **B803**,42(2008), Phys.Rev. **D75**,094009 (2007) , Phys.Rev. **D62**,054001(2000), Nucl.Phys. **B582**,514(2000));

## Spin-dependent FFs

- Fundamental test for any approach to solve QCD at soft scales
- Test schemes of universality and factorization between  $e^+e^-$ , DIS, and p-p collision
- Test evolution as fundamental QCD prediction
- Connection between microscopic (quark spin) and macroscopic observables (azimuthal distribution of the hadrons produced)
- **Final spin analyzer for the study of the transversity parton distribution functions**

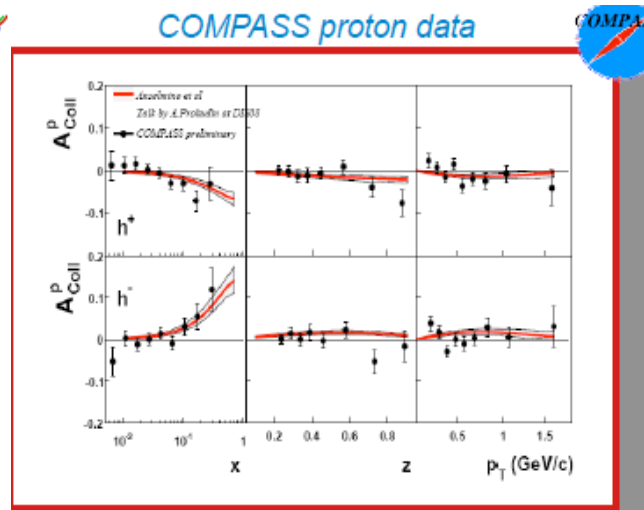
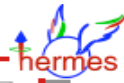
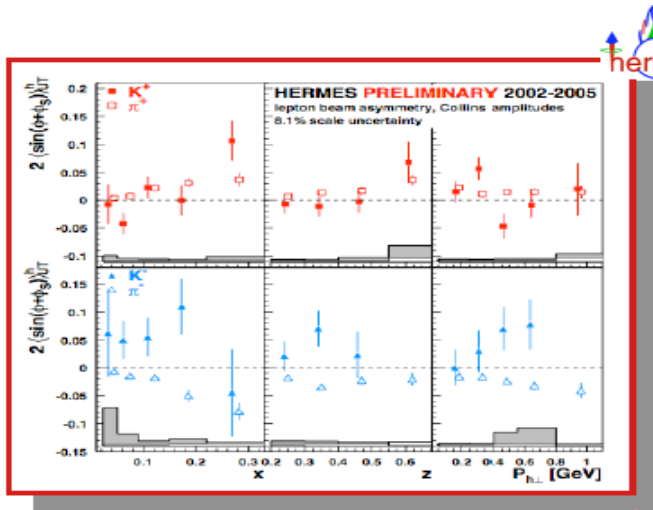


# Collins FF

- ➔ Spin dependent FF
- ➔ Chiral-odd function
- ➔ The Collins FF (CFF) is related to the probability that a transversely polarized quark will fragment into a spinless hadron:

$$D_{hq\uparrow} = D_1^q(z, P_{h\perp}^2) + H_1^{\perp q}(z, P_{h\perp}^2) \frac{\hat{k} \times \vec{P}_{h\perp} \cdot \vec{S}_q}{zM_h}$$

Unpolarized FF                      **Collins FF**  
 ↓    ↓



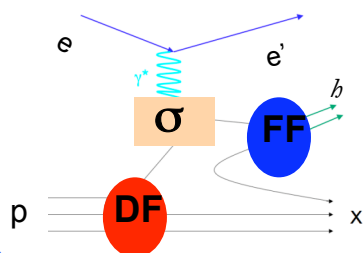
First experimental evidence of non zero Collins FF for pions came from SIDIS experiments: HERMES (PRL94,012002(2005)), COMPASS (PRL94,202002(2005))

- ➔ **B-Factories  $e^+e^- \rightarrow$  direct evidence of non-zero Collins FF**: DELPHI (Nucl.Phys.B79,554-556 (1999)), BELLE (PRL96,232002(2006), PRD78,032011(2008))

# Global analysis: first extraction of Transversity



## SIDIS: Semi Inclusive Deep Inelastic Scattering



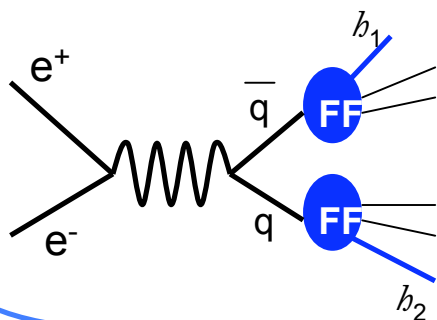
Factorization theorem:

$$\sigma^{ep \rightarrow ehX} = \sum_q DF \times \sigma(eq \rightarrow eq) \times FF$$

$$A_T \propto h_1(x) \times CFF(z)$$

Transversity function

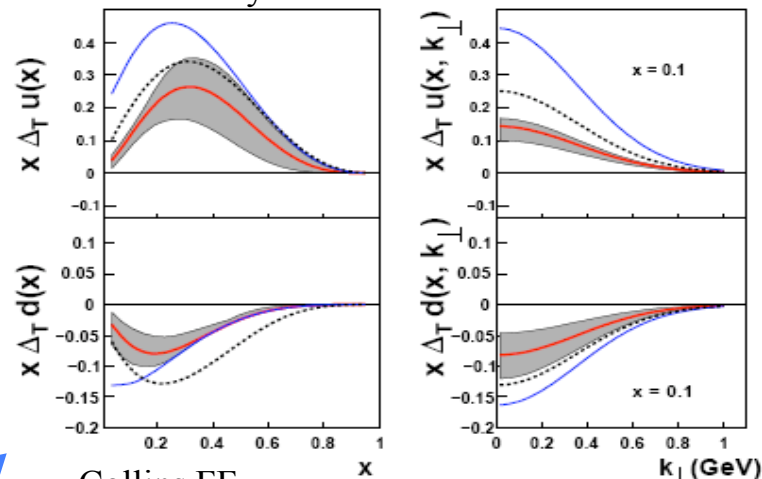
Global analysis (HERMES & COMPASS & BELLE): simultaneous determination of Transversity ( $h_1$ ) and Collins functions (CFF).



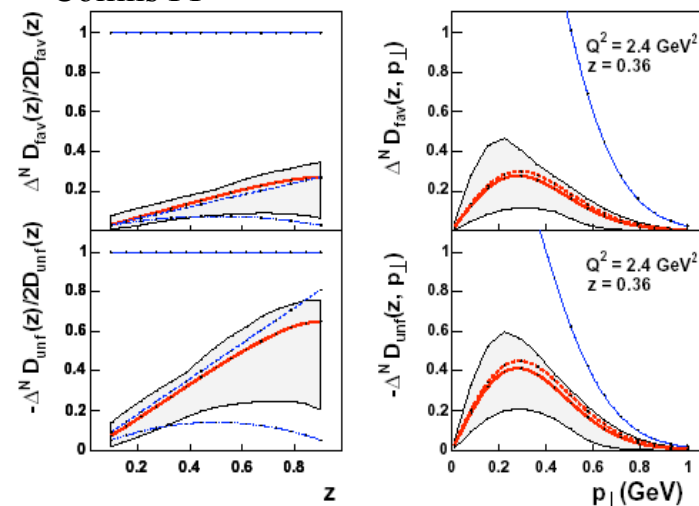
$$e^+e^- \rightarrow b_1 b_2 X$$

Collins and IFF asymmetries in  $e^+e^-$  annihilation are:  
 $\propto CFF(z_1) \times CFF(z_2)$

## Transversity PDF

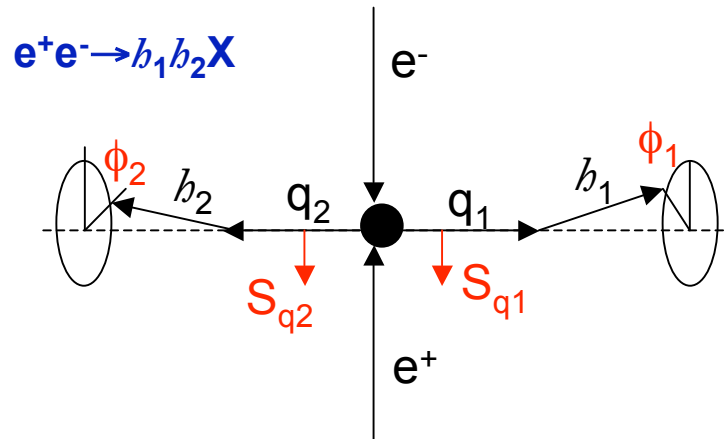


## Collins FF



Anselmino et al., PRD75,05032(2007)  
 Nucl.Phys. Proc. Suppl. 191,(2009)

# Collins effect in di-hadron correlation



- quark spin direction unknown: measurements of Collins FFs in one jet is not possible;
- Correlation between two hemispheres: cosine modulation of the observed di-hadron yield.

Detect pion pairs with same or opposite charge  $\Rightarrow$  sensitivity to **favored** and **disfavored** FFs

- **favored** fragmentation processes describe the fragmentation of a quark of flavor  $q$  into an hadron with a valence quark of the same flavor: i.e.: ( $u \rightarrow \pi^+$ ) and ( $d \rightarrow \pi^-$ )
- **disfavored** for ( $d \rightarrow \pi^+$ ) and ( $u \rightarrow \pi^-$ ).

Unlike sign pion pairs:

$$\pi^+ \pi^- \text{ (UL): } (\text{fav} \times \text{fav}) + (\text{dis} \times \text{dis})$$

Like sign pion pairs:

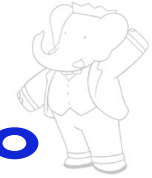
$$\pi^+ \pi^+ \text{ (L): } (\text{fav} \times \text{dis}) + (\text{dis} \times \text{fav})$$

Different combination of fav and dis FFs in the cross section:

$$N^{UL} = \frac{d\sigma(e^+e^- \rightarrow \pi^\pm \pi^\mp X)}{d\Omega dz_1 dz_2} \approx (1 + \cos^2\theta) \sum_q e_q^2 (D_1^{fav} \bar{D}_2^{fav} + D_1^{dis} \bar{D}_2^{dis})$$

$$N^L = \frac{d\sigma(e^+e^- \rightarrow \pi^\pm \pi^\pm X)}{d\Omega dz_1 dz_2} \approx (1 + \cos^2\theta) \sum_q e_q^2 (D_1^{fav} \bar{D}_2^{dis} + D_1^{dis} \bar{D}_2^{fav})$$

# Reference Frames (RF)

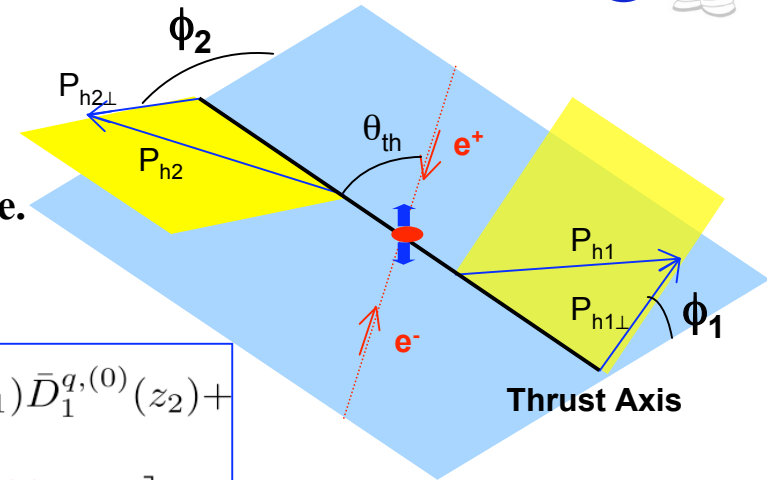


## $\phi_1 + \phi_2$ or Thrust RF

$\theta$ : angle between the  $e^+e^-$  axis and the thrust axis;  
 $\phi_{1,2}$ : azimuthal angles between  $P_{h1(h2)}$  and the scattering plane.

All quantities in  $e^+e^-$  center of mass

$$\frac{d\sigma(e^+e^- \rightarrow h_1h_2X)}{d\Omega dz_1 dz_2 d\phi_1 d\phi_2} = \sum_{q,\bar{q}} \frac{3\alpha^2 e_q^2}{Q^2} \frac{z_1^2 z_2^2}{4} \left[ (1 + \cos^2\theta) D_1^{q,(0)}(z_1) \bar{D}_1^{q,(0)}(z_2) + \sin^2(\theta) \cos(\phi_1 + \phi_2) H_1^{\perp,(1),q}(z_1) \bar{H}_1^{\perp,(1),q}(z_2) \right]$$



Daniel Boer

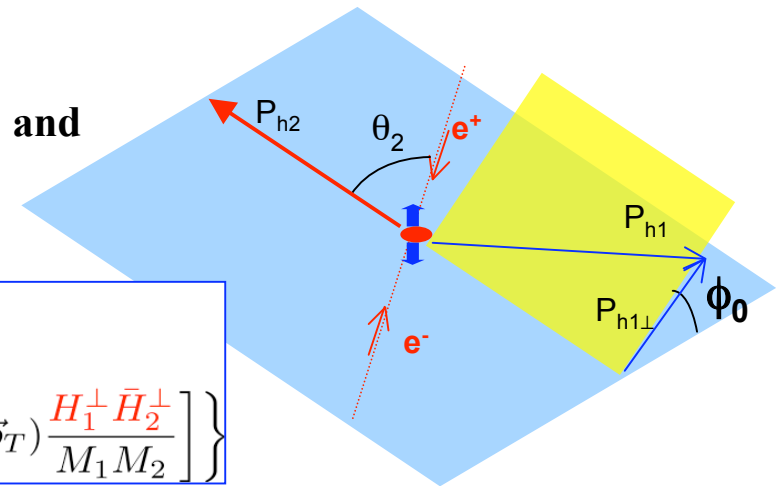
Nucl. Phys. B 806,23-67(2009)  
 [arXiv:0804.2408v2]

## $2\phi_0$ or $P_{h2}$ RF

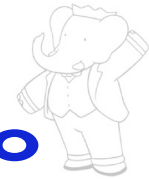
$\theta_2$ : angle between the  $e^+e^-$  axis and  $P_{h2}$ ;  
 $\phi_0$ : angle between the plane spanned by  $P_{h2}$  and the  $e^+e^-$  axis, and the direction of  $P_{h1}$  perpendicular to  $P_{h2}$ .

All quantities in  $e^+e^-$  center of mass

$$\frac{d\sigma(e^+e^- \rightarrow h_1h_2X)}{d\Omega dz_1 dz_2 d^2\vec{q}_T} = \frac{3\alpha^2}{Q^2} z_1^2 z_2^2 \left\{ A(y) \mathcal{F}[D_1 \bar{D}_2] + B(y) \cos(2\phi_0) \mathcal{F} \left[ (2\hat{h} \cdot \vec{k}_T \hat{h} \cdot \vec{p}_T - \vec{k}_T \cdot \vec{p}_T) \frac{H_1^\perp \bar{H}_2^\perp}{M_1 M_2} \right] \right\}$$



# PEP-II and BaBar Detector @ SLAC



- SVT: 5 Layers → Precise measurement of the decay vertex;  
 $\sigma_z = 65 \mu\text{m}$ ,  $\sigma_d = 55 \mu\text{m}$ ;
- DCH resolution:  $\sigma_{p_T}/p_T = (0.13 \pm 0.01)\% * p_T + (0.45 \pm 0.03)\%$
- PID:
  - Low momenta:  $dE/dx$  in the DCH and SVT;
  - DIRC: above 700 MeV/c;  $>3\sigma$  K/ $\pi$  separation up to 4 GeV/c.

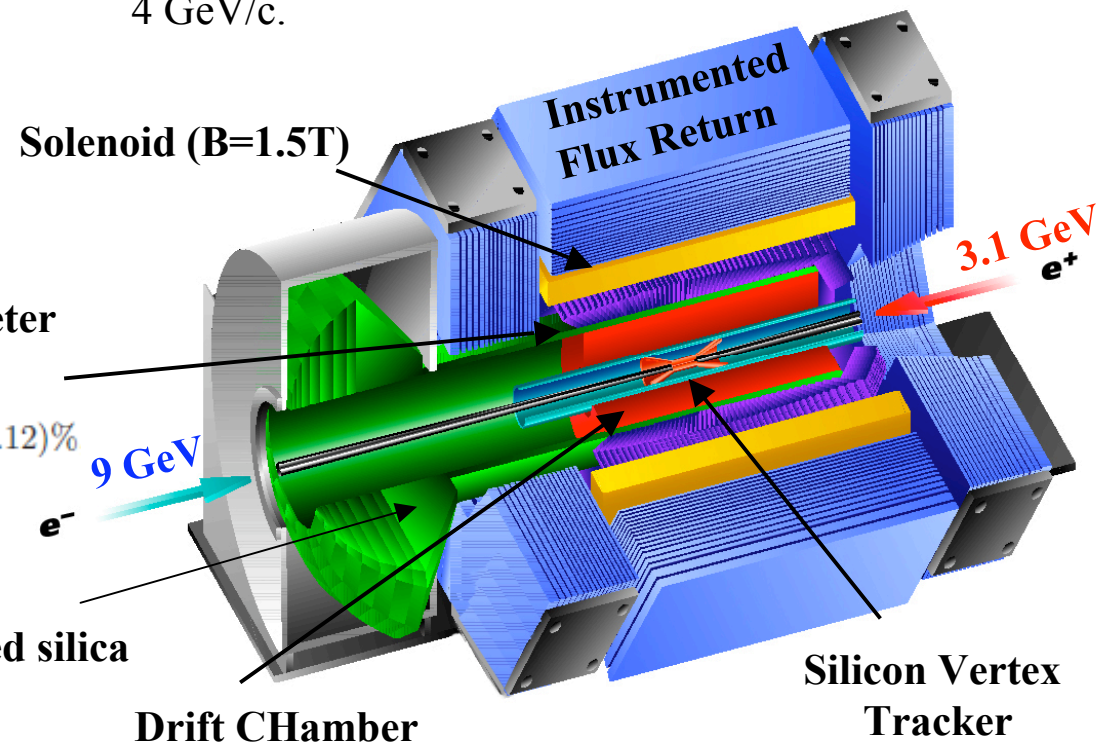
- Asymmetric-energy collider
- High Energy Ring (HER): 9.0 GeV  $e^-$
- Low Energy Ring (LER): 3.1 GeV  $e^+$
- $\beta\gamma \approx 0.56$

Electromagnetic Calorimeter  
6580 CsI(Tl) crystals

$$\frac{\sigma_E}{E} = \frac{(2.32 \pm 0.30)\%}{\sqrt[4]{E(\text{GeV})}} \oplus (1.85 \pm 0.12)\%$$

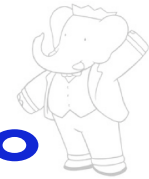
DIRC

144 bars of fused silica

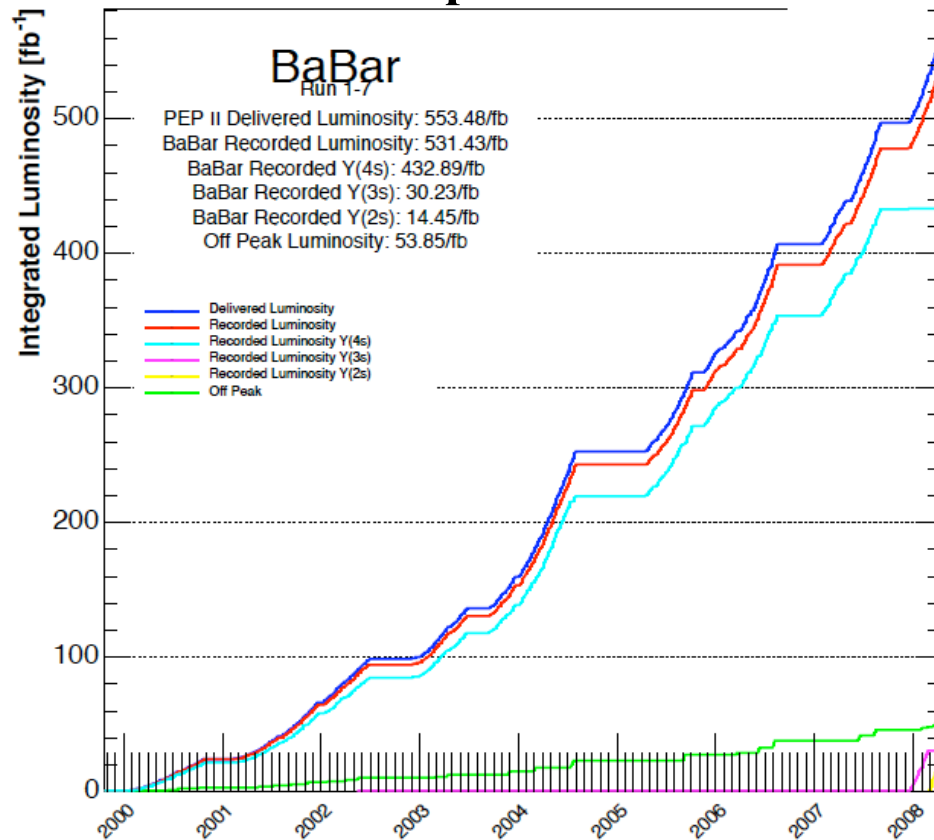




# PEP-II Luminosity

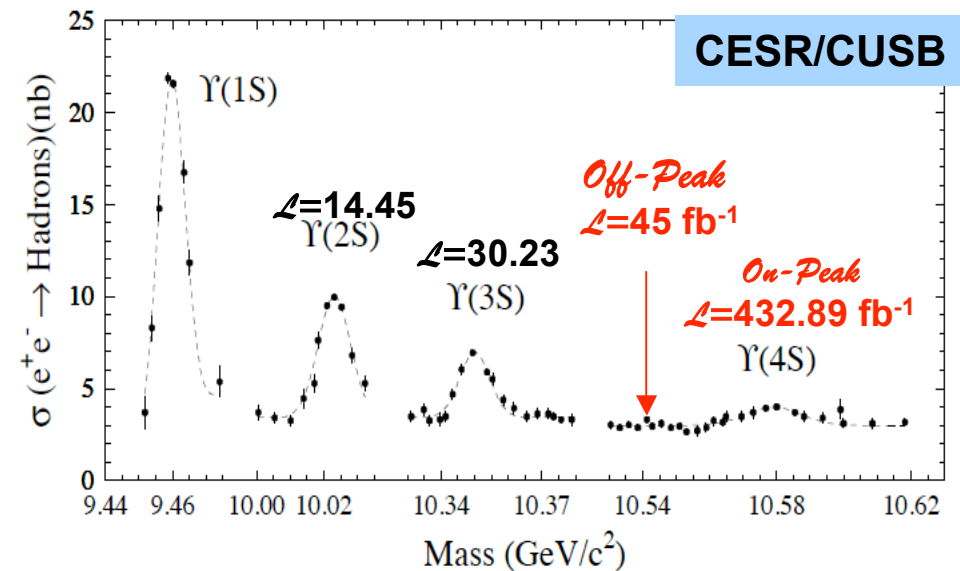


October 1999 - April 2008



- $\sqrt{s}=10.58$  GeV:  $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$
- Off-resonance:  $\sqrt{s}=10.54$  GeV

$e^+e^- \rightarrow$	Cross section (nb)
$u\bar{u}$	1.39
$d\bar{d}$	0.35
$s\bar{s}$	0.35
$c\bar{c}$	1.30
$b\bar{b}$	1.05
$\tau^+\tau^-$	0.94

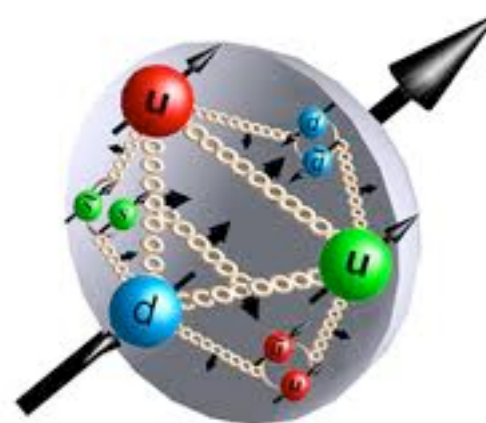


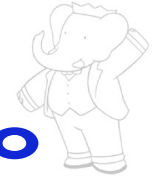


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# *Analysis*

## Measurement of Collins Asymmetries at BaBar





## Analysis Strategy

The analysis for the preliminary results is based on the full off-peak sample ( $45 \text{ fb}^{-1}$ ).

$$e^+e^- \rightarrow \pi\pi X$$

1. Event and tracks selection
2. Assumption: thrust axis in  $e^+e^-$  CM as the  $q\bar{q}$  direction
3. Selection of pions in opposite jets according to the thrust axis
4. Measurement of the azimuthal angles ( $\phi_i$ ) in the two reference frames (see slide 7)
5. Fit to the azimuthal distributions
6. Estimate and subtraction of tau and charm contributions
7. Study of systematic effects

# Events and Tracks Selection

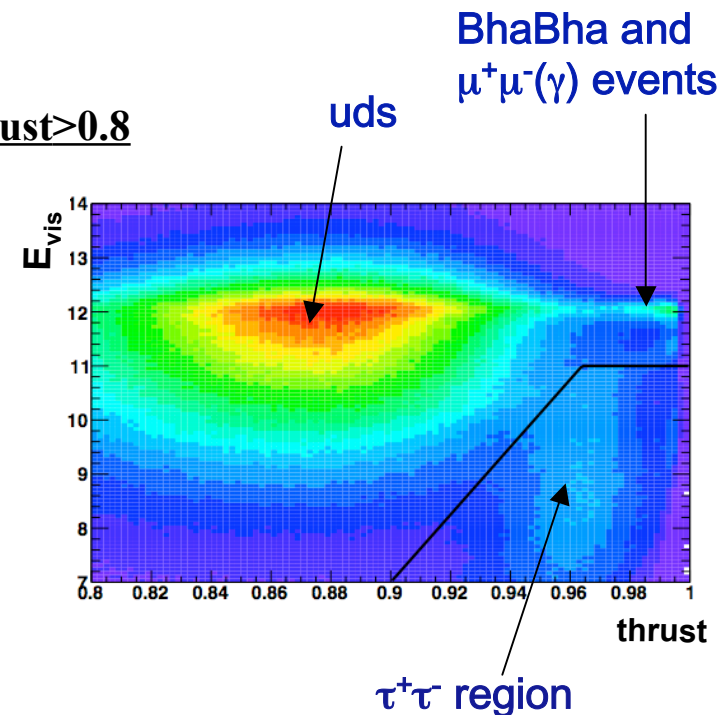
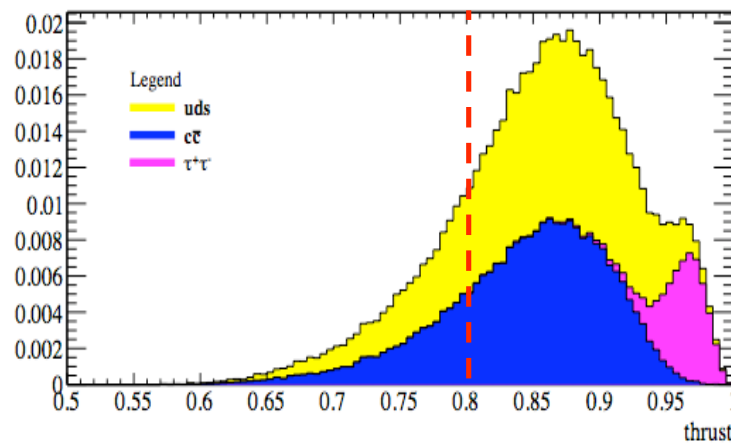


1) Preselection:

- Selection of multi-hadron events
- Visible energy:  $E_{\text{vis}} > 7 \text{ GeV}$

2) Tracks in the DIRC acceptance for the PID

3) Selection of two-jet topology events requiring thrust > 0.8



4)  $\mu^\pm$  and  $e^\pm$  veto, and Tight pion ID required

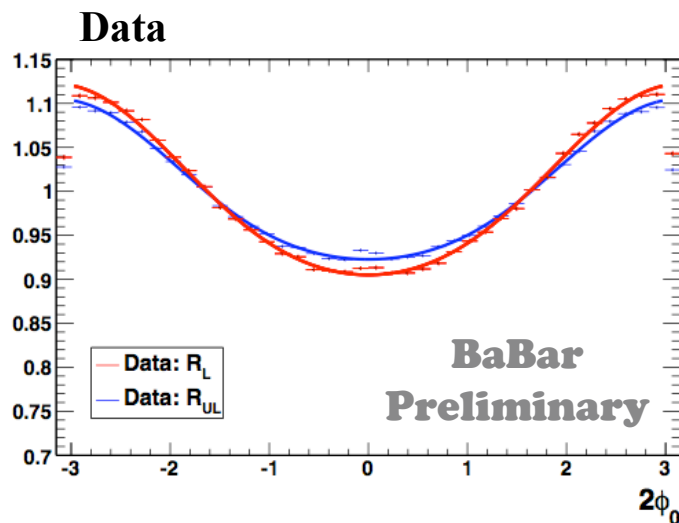
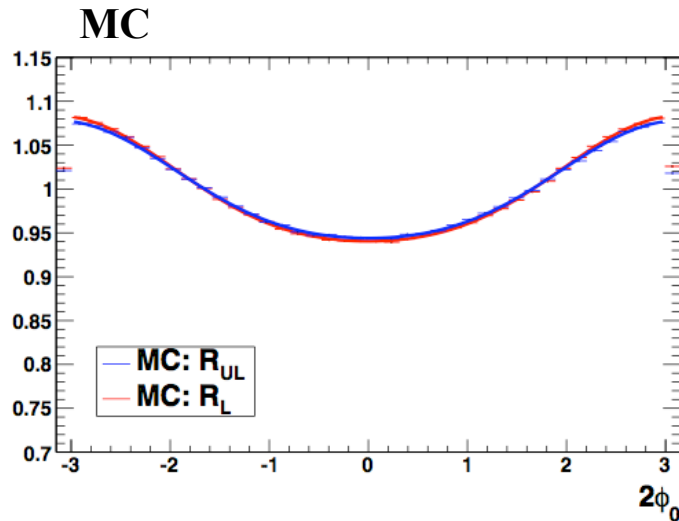
5) Events in the  $\tau^+\tau^-$  region removed

6) Analysis restricted to pion fractional energies  $z=2E_h/\sqrt{s} > 0.2$

- for small  $z$  values the mass correction terms become important

7)  $Q_t < 3.5 \text{ GeV}$ , where  $Q_t$  is the transverse momentum of the virtual photon in the pions CMS

# Raw Asymmetries



**Accessing the Collins Asymmetries:** measurement of cosine modulation of hadron pairs ( $N(\phi)$ ) on top of a flat distribution due to unpolarized part of the fragmentation function (normalized raw distribution):

$$R_\alpha = \frac{N(\phi_\alpha)}{\langle N_\alpha \rangle} = a + b \cdot \cos(\phi_\alpha)$$

Information about the Collins asymmetry

In the MC sample, the polarized FF (Collins FF) are not implemented  $\rightarrow$  flat distribution at generator level

**Reconstructed distribution affected by large detector acceptances effects**



# Double Ratio

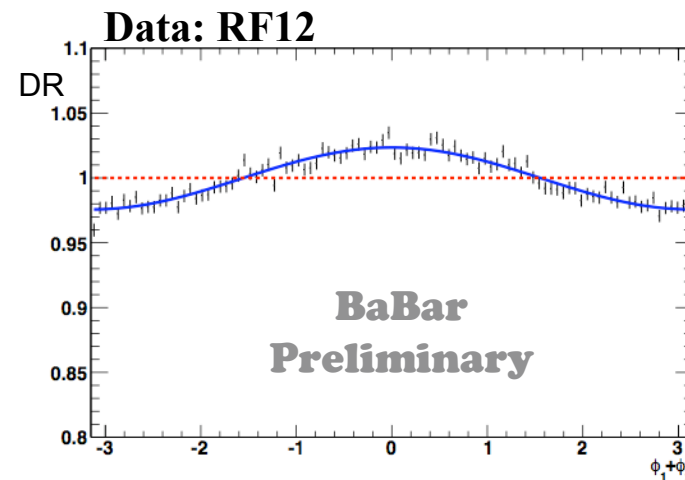
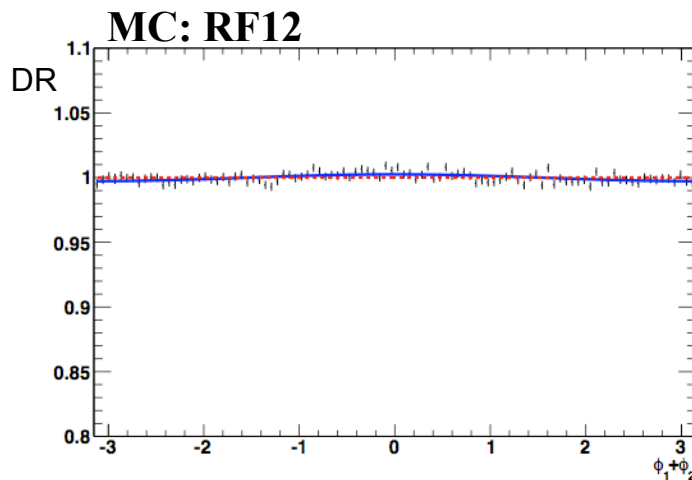
Double Ratio (DR) of Un-Like sign over Like sign pion pairs:

Eliminate the acceptance effects and the first order radiative effects

- acceptances and radiative contributions do not depend on the charge combination of the pion pair;
- approximation holds for small asymmetries.

$$\frac{R_{UL}}{R_L} = \frac{N^{UL}(\phi) / \langle N^{UL}(\phi) \rangle}{N^L(\phi) / \langle N^L(\phi) \rangle} \rightarrow P_0 + P_1 \cdot \cos(\phi)$$

Contain only the Collins effects and higher order radiative effects



MC: we measure a small deviation from zero ( $\sim 0.2\%$ ), and assign a systematic error for that

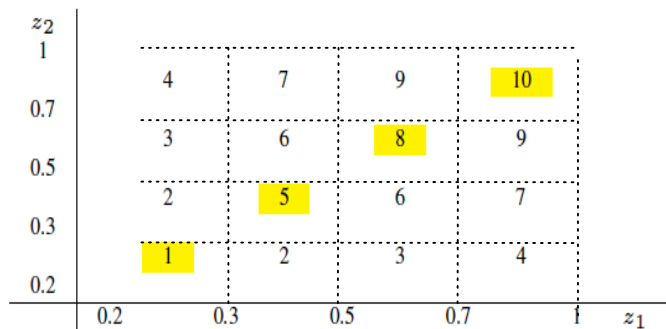
Asymmetry values before any correction

RF12:  $(2.39 \pm 0.07)\%$   
 RF0:  $(1.71 \pm 0.07)\%$

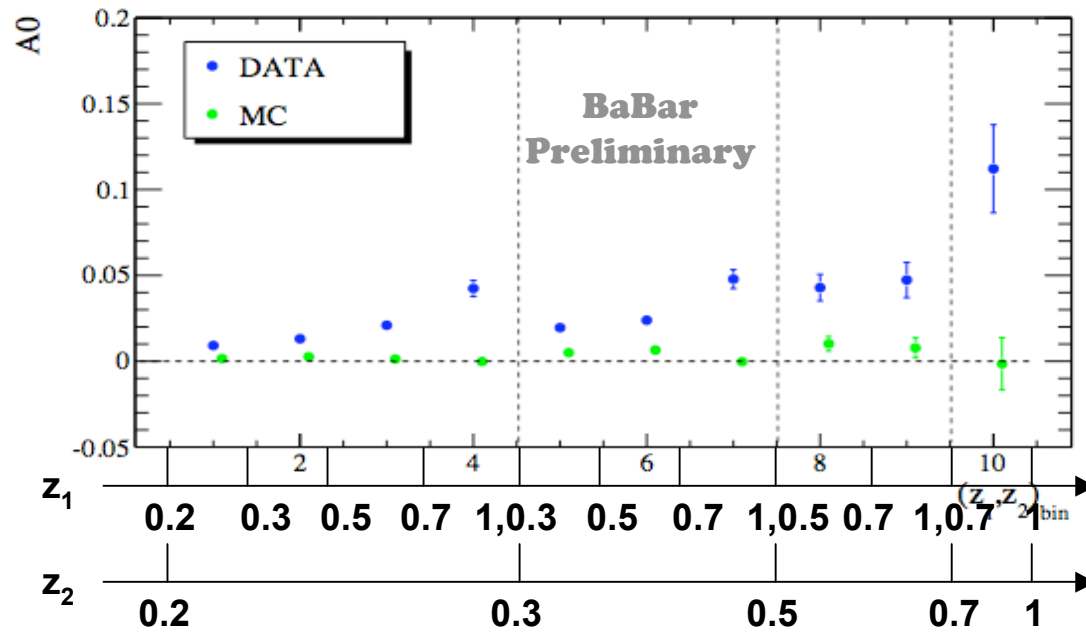
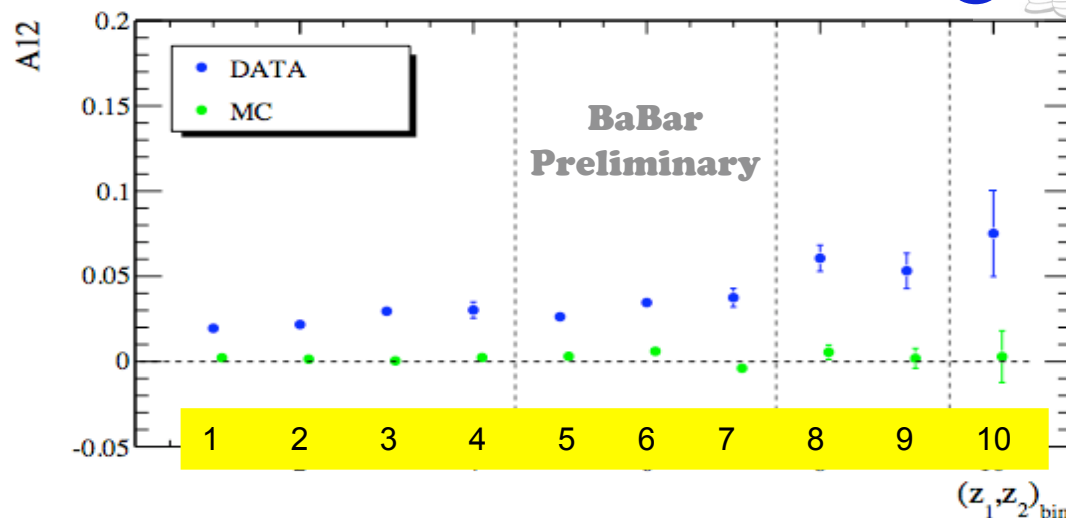


# Measured Asymmetry vs z

The large amount of data ( $\sim 10^8$  light quark events), allows the extraction of the asymmetries in bins of fractional energies ( $z$ ) of selected pions. We choose the following 10 symmetric bin subdivision:



This choice allows a direct comparison with Belle results obtained on off-peak data.





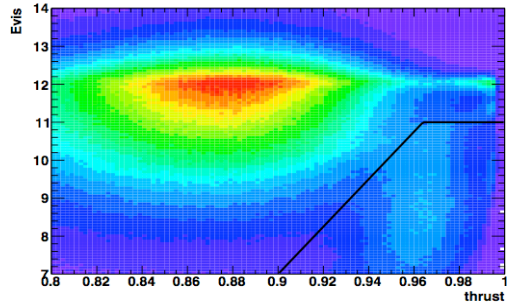
# Asymmetry dilution due to Tau and Charm events

Measured asymmetries are diluted by the presence of background sources:

$$A_{measured} = (1 - \sum_i D_i) \cdot A_{uds} + \sum_i D_i \cdot A_{i,bkg}$$

$D_i$  = fraction of pion pairs due to the i-th background process.

## $e^+e^- \rightarrow \tau^+\tau^-$ CONTRIBUTION



- Using  $\tau$ -MC, and the  $\tau$ -enhanced data sample in the region removed, we find  $A_\tau=0$ ;
- The cut reduces tau contamination to  $D_\tau \approx 3\%$  (it ranges from about 1 to 18% in the individual z-bins);
- we correct the data as follows:

$$A_{uds} = \frac{A_{measured}}{1 - D_\tau}$$

## $e^+e^- \rightarrow c\bar{c}$ CONTRIBUTION

In this case, both fragmentation processes and weak decays can introduce azimuthal asymmetries. Use a  $D^*$ -enhanced data sample for estimating the charm-induced asymmetry.

$$A_{measured} = (1 - D) \cdot A_{uds} + D \cdot A_{charm}$$

$$A_{D^*} = d \cdot A_{charm} + (1 - d) \cdot A_{uds}$$

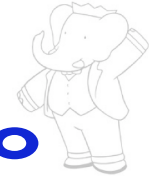
$D \sim 25\%$

$d \sim$  charm fraction in the  $D^*$ -enhanced data sample

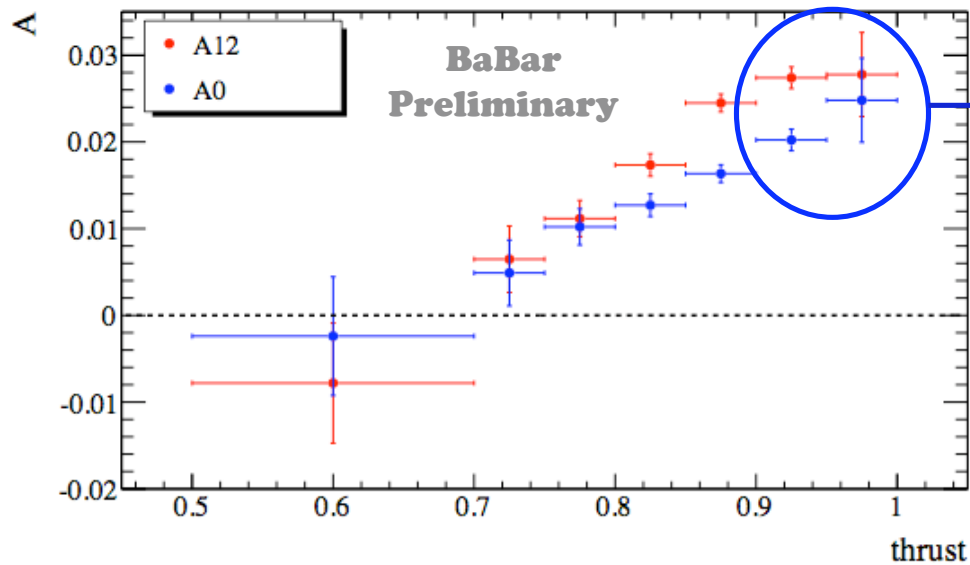
Solving the system equations, we extract  $A_{uds}$  and  $A_{charm}$



# Measured asymmetry vs thrust



We studied also the behaviour of the asymmetry as a function of the thrust value.



→ Tau correction applied.

- Linear dependence of  $A_{12,0}$  on thrust
- The asymmetry is consistent with zero at low thrust value

This behavior is essentially due to two effects:

- 1) **More spherical events, higher multiplicity**
- 2) **Glun emission**



$q\bar{q}$  correlation lost.



## Study of systematic effects

The measurements are affected by a number of **systematic effects**

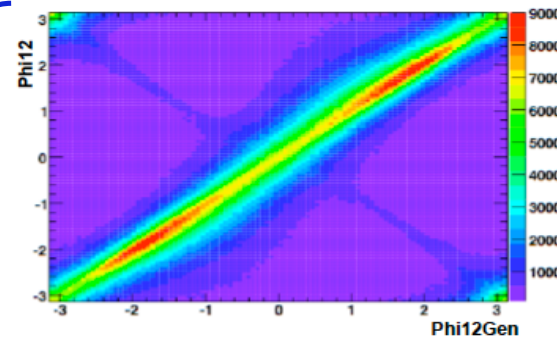
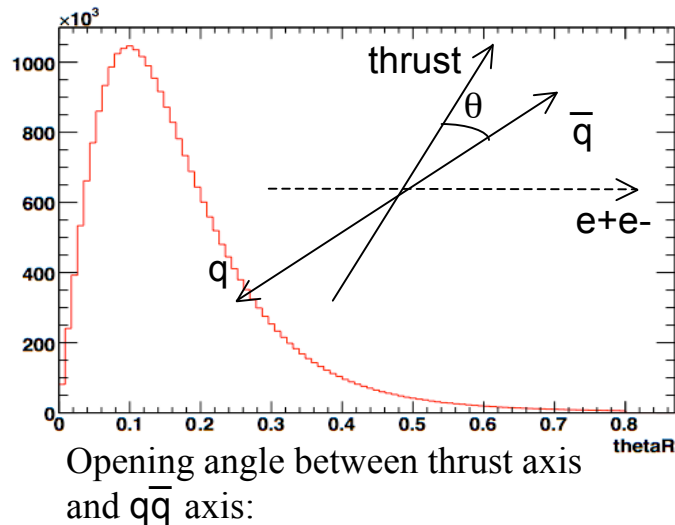
- If needed, we correct the asymmetries and assign a systematic error
- In other cases, we only check that no unexpected features are present
- When possible we evaluate the correction **independently for each z-bin**



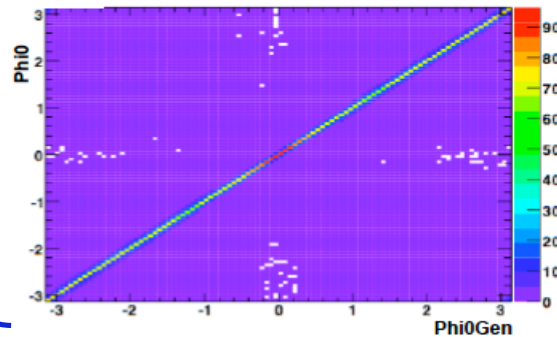
# Dilution due to the thrust reconstruction

The experimental method assume the thrust axis as  $\bar{q}\bar{q}$  direction:

- This is only a rough approximation



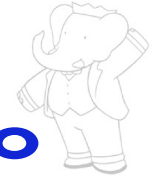
- RF12: the azimuthal angles are calculated with respect to the thrust axis → large smearing



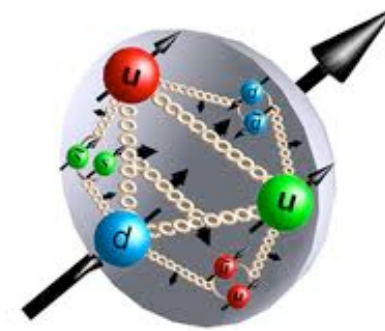
- RF0: the azimuthal angle is calculated with respect to the momentum of the second hadron → small smearing due to PID and tracking resolution

The MC generator does not include the Collins FF → we introduce a modulation to the generated angular distribution by applying a different weight to every selected pion pair:  $w^{UL,L} = 1 \pm a \cdot \cos(\phi_{gen12,0})$

	DR12		DR0	
	Average $A_{12}$	Correction factor	Average $A_0$	Correction factor
We found:	$(59.2 \pm 2.2)\%$	$1.68 \pm 0.06$	$(99.8 \pm 3.2)\%$	$1.002 \pm 0.03$



# Preliminary Results



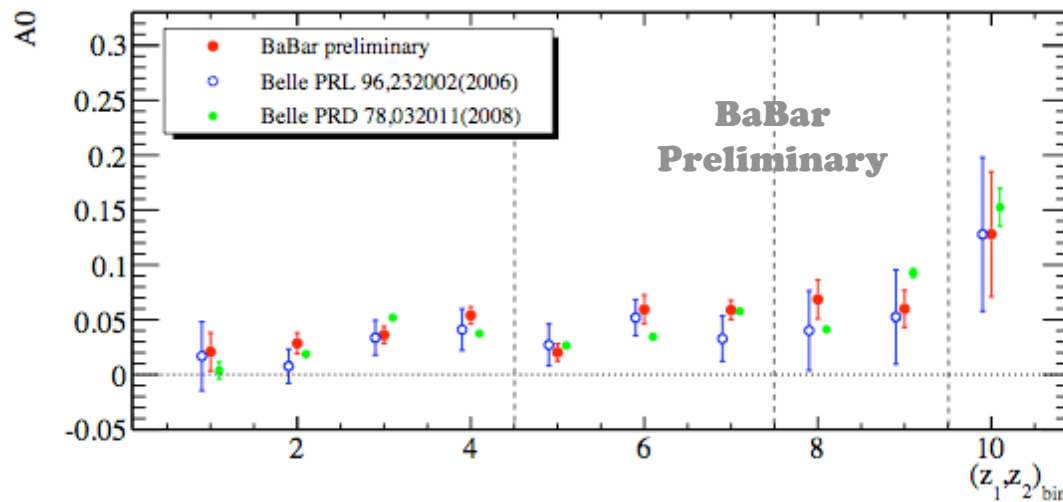
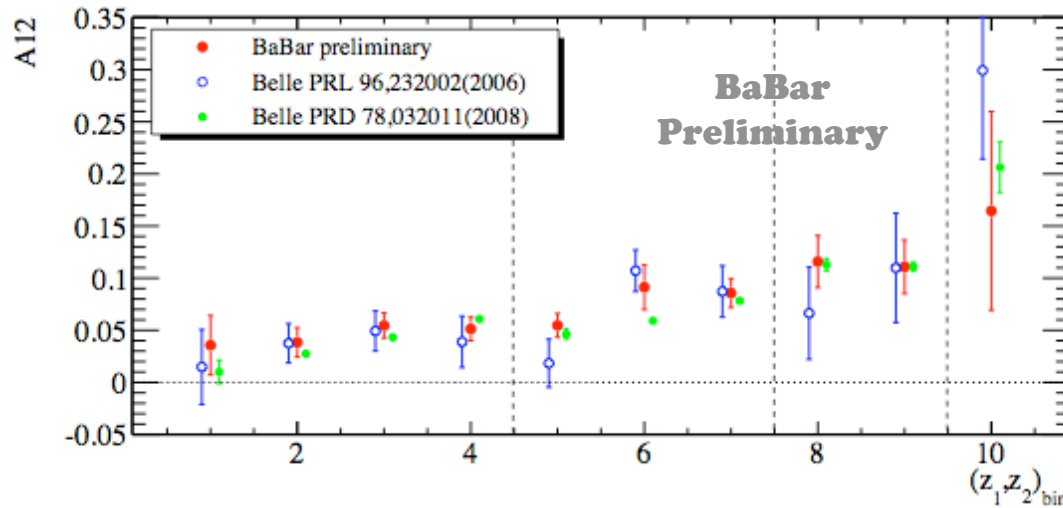


# Results: Asymmetry vs $(z_1, z_2)$ bins

BaBar preliminary:  
 $\mathcal{L} \approx 45 \text{ fb}^{-1}$

Belle Off-peak:  
 $\mathcal{L} \approx 29 \text{ fb}^{-1}$

Belle full statistics  
(supersede previous results)  
 $\mathcal{L} \approx 547 \text{ fb}^{-1}$



- In the later Belle publication (Phys.Rev.D78,032011(2008)), they estimated a new correction factor of  $1.66 \pm 0.04$  due to the thrust approximation as the real  $\bar{q}q$  axis. Therefore, the **Belle off-peak results** for the RF12 frame, **are corrected by a factor 1.66/1.21**

- Results of the **full Belle statistic analysis** have been average in symmetric  $(z_1, z_2)$  bins

- Agreement with Belle data in both reference frame

# Results: Asymmetry vs “ $\theta_{th}$ ” and “ $\theta_2$ ”

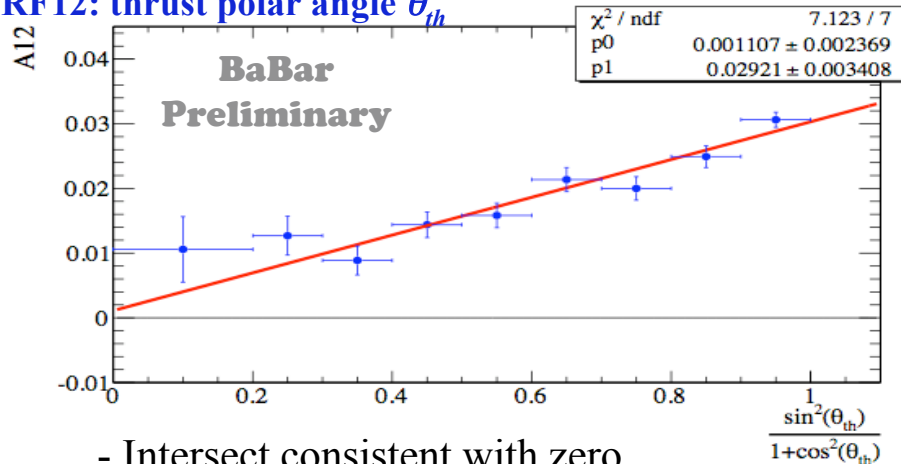


$$\frac{R_{12}^{UL}}{R_{12}^L} \propto 1 + \frac{\sin^2 \theta_{th}}{1 + \cos^2 \theta_{th}} \cos(\phi_1 + \phi_2) \{G^{UL} - G^L\}$$

$$\frac{R_0^{UL}}{R_0^L} \propto 1 + \frac{\sin^2 \theta_2}{1 + \cos^2 \theta_2} \cos(2\phi_0) \{G^{UL} - G^L\}$$

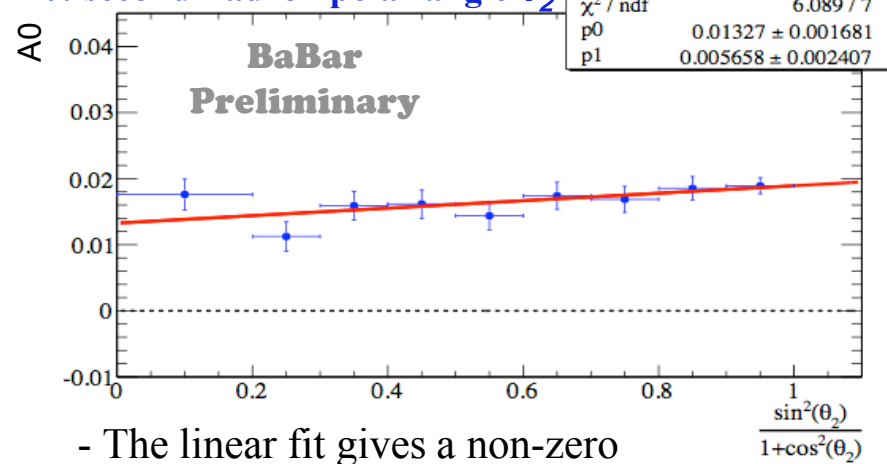
- Two different polar angles appear in the DR expressions for the two reference frames:

RF12: thrust polar angle  $\theta_{th}$



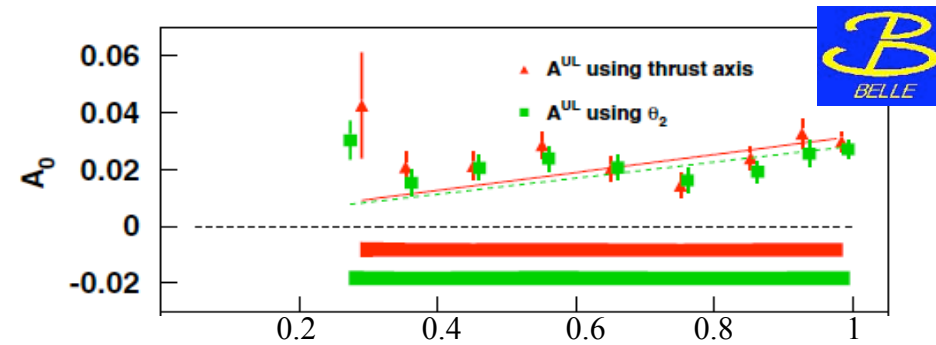
- Intersect consistent with zero, as expected

RF0: second-hadron polar angle  $\theta_2$



- The linear fit gives a non-zero constant parameter

- Similar result found by Belle



# Conclusions and Plans



-We present a preliminary measurement of the Collins Asymmetry in the sample of  $45 \text{ fb}^{-1}$  of data collected at 10.54 GeV by the BaBar Detector

- Measurement performed in two different reference frames
- Clear evidence of **non-zero asymmetries** in light-quark fragmentation
- Measured asymmetries increase with fractional energies of the pions, in agreement with expectations
- A roughly linear dependence of the asymmetries on thrust value is seen
- The expected behaviour of the asymmetries as a function of  $\sin^2\theta/(1+\cos^2\theta)$  seems not to hold for  $A_0$ , when the polar angle of the second hadron is considered
- There is an overall good agreement with Belle data
- These preliminary results are the starting point for a more complete study on the full BaBar data sample

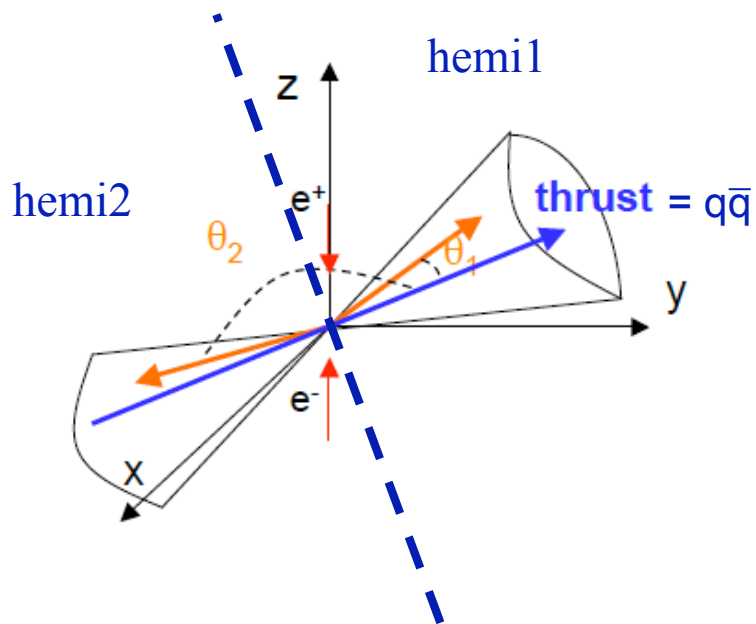
*Thanks for your attention*



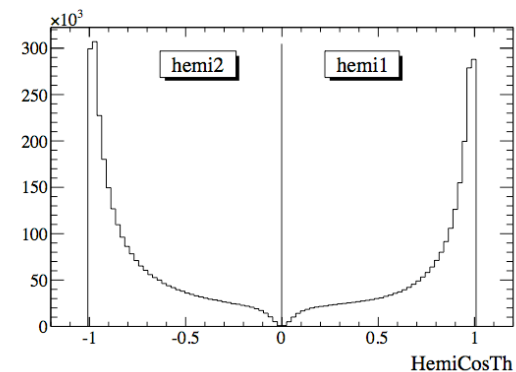
# *Backup slides*



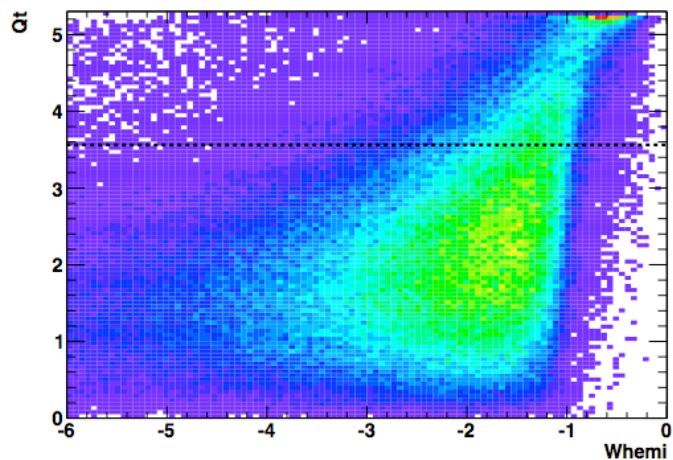
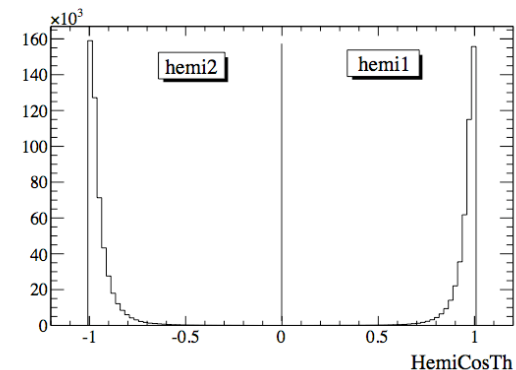
# EVENTS AND TRACKS SELECTION



Before cuts



After cuts



$$W_{\text{hemi}} = (P_1 \cdot \hat{n}) (P_2 \cdot \hat{n}) < 0$$

Whemi near to zero: higher probability that one of the two tracks has been assigned to the wrong hemisphere® we can suppress this effect selecting pairs with  $Q_t < 3.5$  GeV, where  $Q_t$  is the transverse momentum of the virtual photon in the pions CMS

# Study of systematic effects

The measurements are affected by a number of systematic effects

- If needed, we correct the asymmetries and assign a systematic error
- In other cases, we only check that no unexpected features are present
- When possible we evaluate the correction independently for each z-bin

- Dilution because of thrust reconstruction
- Test of the DR methods on Montecarlo
- Particle identification
- Fit bin size
- Higher harmonic contributions
- $\pi^+\pi^+ / \pi^-\pi^-$  Double Ratio test
- Single Spin Asymmetries (SSA)
- Subtraction and Double Ratio (DR) methods
- Beam polarization studies
- Toy MC studies

# Double Ratio

Double Ratio (DR) of Un-Like sign over Like sign pion pairs:

➤ **eliminate the acceptance effects and the first order radiative effects**

- acceptances and radiative contributions do not depend on the charge combination of the pion pair
- approximation hold for small asymmetries

$$\frac{R_{12}^{UL}}{R_{12}^L} = \frac{1 + \frac{\sin^2 \theta}{1 + \cos^2 \theta} \cos(\phi_1 + \phi_2) G^{UL}}{1 + \frac{\sin^2 \theta}{1 + \cos^2 \theta} \cos(\phi_1 + \phi_2) G^L} \simeq 1 + \frac{\sin^2 \theta}{1 + \cos^2 \theta} \cos(\phi_1 + \phi_2) \{G^{UL} - G^L\}$$

$$G^{UL} = \frac{\sum_q e_q^2 \mathcal{F}(H_1^{fav} H_2^{fav} + H_1^{dis} H_2^{dis})}{\sum_q e_q^2 (D_1^{fav} D_2^{fav} + D_1^{dis} D_2^{dis})} \quad G^L = \frac{\sum_q e_q^2 \mathcal{F}(H_1^{fav} H_2^{dis} + H_1^{dis} H_2^{fav})}{\sum_q e_q^2 (D_1^{fav} D_2^{dis} + D_1^{dis} D_2^{fav})}$$

$$\frac{R_{UL}}{R_L} = \frac{N^{UL}(\phi) / \langle N^{UL}(\phi) \rangle}{N^L(\phi) / \langle N^L(\phi) \rangle} \rightarrow P_0 + \underbrace{(P_1)}_{\downarrow} \cos(\phi)$$

Contain only the Collins effects and higher order radiative effects

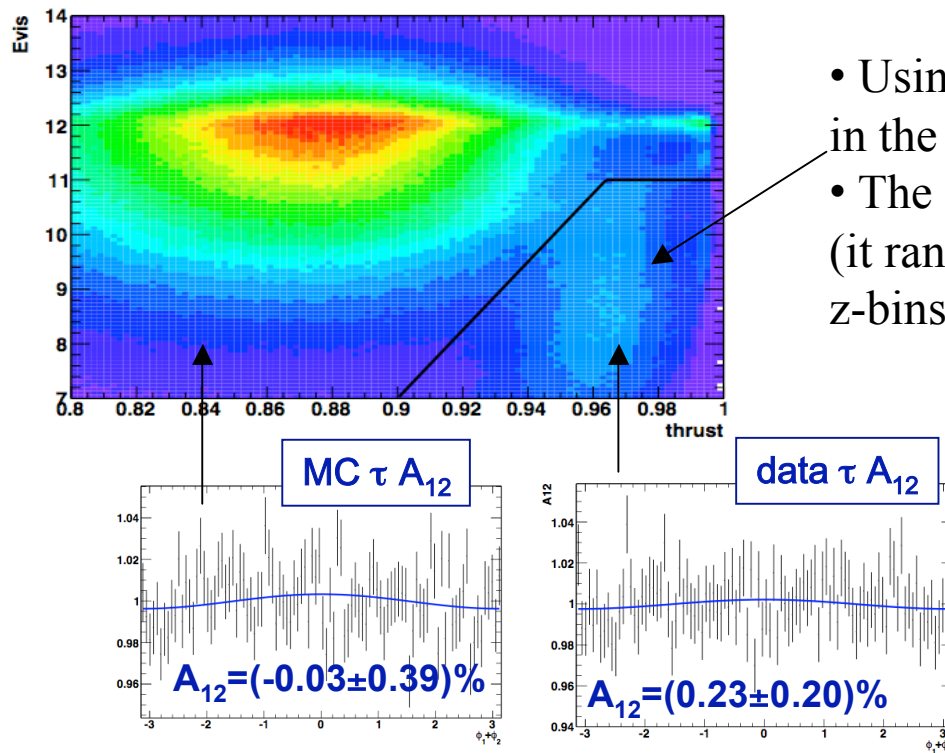
# Asymmetry dilution due to Tau and Charm events (I)

Measured asymmetries are diluted by the presence of background sources:

$$A_{measured} = (1 - \sum_i D_i) \cdot A_{uds} + \sum_i D_i \cdot A_{i,bkg}$$

$D_i$  = fraction of pion pairs due to the  $i$ -th background process.

## $e^+e^- \rightarrow \tau^+\tau^-$ CONTRIBUTION



- Using  $\tau$ -MC, and the  $\tau$  -enhanced data sample in the cutted region, we find  $A_\tau=0$
- The cut reduce tau contamination to  $D_\tau \approx 3\%$  (it ranges from about 1 to 18% in the individual z-bins)

- We correct the data as follow:

$$A_{uds} = \frac{A_{measured}}{1 - D_\tau}$$

75% of  $\tau\tau$  events

## Asymmetry dilution due to Tau and Charm events (II)

### $e^+e^- \rightarrow c\bar{c}$ CONTRIBUTION

In this case, both fragmentation processes and weak decays can introduce azimuthal asymmetries.  
Use a  $D^*$ -enhanced data sample for estimating the the charm-induced asymmetry. ( $D_{\text{charm}} \sim 25\%$ )

- generic  $c\bar{c}$  MC
- data sample

relative contribution  
 $D = N_{cc}/N_{\text{all}}$

- $D^*$ -enhanced MC sample
- $D^*$ -enhanced data sample

relative contribution  
 $d = N_{ccD^*}/N_{D^*}$

$$\begin{cases} A_{\text{measured}} = (1 - D) \cdot A_{uds} + D \cdot A_{\text{charm}} \\ A_{D^*} = d \cdot A_{\text{charm}} + (1 - d) \cdot A_{uds} \end{cases}$$

Solving the system equations, we extract  $A_{uds}$  and  $A_{\text{charm}}$

# Summary of main Systematic Errors



z-bins	Bins	PID	RF12 Weight	MC	total	Bins	PID	RF0 Weight	MC	total
1	0.0002	0.0015	0.0013	0.0022	0.30%	0.0004	0.0041	0.0007	0.0029	0.51%
2	0.0005	0.0007	0.0014	0.0020	0.26%	0.0007	0.0035	0.0009	0.0029	0.47%
3	0.0009	0.0013	0.0020	0.0041	0.48%	0.0019	0.0024	0.0012	0.0029	0.44%
4	0.0008	0.0014	0.0018	0.0023	0.34%	0.0009	0.0010	0.0017	0.0029	0.36%
5	0.0021	0.0021	0.0022	0.0030	0.48%	0.0000	0.0016	0.0006	0.0050	0.53%
6	0.0011	0.0029	0.0028	0.0060	0.73%	0.0015	0.0024	0.0014	0.0050	0.59%
7	0.0027	0.0011	0.0031	0.0020	0.47%	0.0005	0.0005	0.0019	0.0029	0.35%
8	0.0008	0.0011	0.0042	0.0054	0.70%	0.0032	0.0027	0.0022	0.0102	1.12%
9	0.0069	0.0035	0.0040	0.0020	0.89%	0.0021	0.0032	0.0020	0.0078	0.89%
10	0.0223	0.0041	0.0060	0.0028	2.36%	0.0186	0.0096	0.0041	0.0029	2.15%
all	0.0007	0.0022	0.0019	0.0020	0.36%	0.0006	0.0023	0.0010	0.0029	0.39%

All systematic errors are added in quadrature;