

Hyperon Polarization, Transversity and LHC Physics

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Presentation for Transversity

Veli Lošinj, Croatia

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Outline

$\Lambda_{s,c,b}$ polarization Puzzles and Uses

I. Large polarization in hadron processes

- I. Very large $p+p \rightarrow A_N, A_{NN}, \pi$'s (see A. Krisch talk)
- II. Very large Pol'zn for inclusive Λ & Σ
- III. Intriguing Systematics
- IV. Explanations? **Basic evidence** for non-perturbative systematics of hadron structure & formation.
- V. Charmed & heavy hyperons (Fermilab fixed target)
- VI. Will hyperons maintain large Pol'zn?? Need understanding of NPQCD mechanism
- VII. **If we do not understand large SSA's we do not understand NPQCD !**
(even Drell-Yan signs – see O. Denisov & D. Sivers talk)

II. Leptoproduction of Λ_s & Σ_s (theory workplace)

- I. Not outstanding Single Spin Asymmetries **yet**
- II. Large double correlations at small Q^2
- III. Analysis more tractable
- IV. Which formalism is most useful? TMDs, GPDs, Generalized Fracture Functions?

Outline (cont'd)

- I. Large polarization in hadron processes
- II. Leptoproduction of Λ_s & Σ_s
- III. Tool to get into transversity –
 - I. Chen, GG, Jaffe, Ji ($e^+e^- \rightarrow \Lambda_s \text{ anti}\Lambda_s X$)
 - II. “off-diagonal” SIDIS via Transversity odd distributions (intrinsic charm?)
 - III. Target fragmentation: GPDs, Fragmentation functions, Fracture Functions (many authors: D.Boer; M. Anselmino. et al.; A. Kotzinian; . . .)
 - IV. Collider production – target or central region (e.g. D. Sivers)
- IV. TMDs, GPDs, Generalized Fracture Functions
 - I. Why GPDs? Phases and transversity - - -
 - II. Preliminary results & relations

Transversity - some history

- 2-body scattering amps - Exclusive hadronic
 - $f_{a,b;c,d}(s,t)$ with spin projections $a,b;c,d$
- What *spin* frame leads to simplest description of theory or data? Amps to observables?
 - helicity has easy relativistic covariance - theory
 - states of $\mathbf{S} \cdot \mathbf{p}$, e.g. $|+1/2\rangle$, $|-1/2\rangle$, etc.
 - transversity: eigenstates of $\mathbf{S} \cdot (\mathbf{p}_1 \times \mathbf{p}_2)$
 - $|\pm 1/2\rangle_{\top} = \{|+1/2\rangle \pm (i) |-1/2\rangle\} / \sqrt{2}$ for spin 1/2, etc.

Especially for relating to **single spin asymmetries** - only $\mathbf{S} \cdot \mathbf{n}$

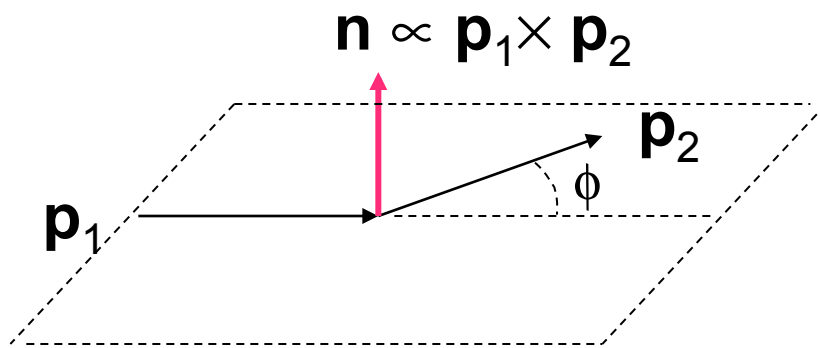
Goldstein & Moravcsik, Ann.Phys. 1976

Transversality & simplicity

- states of $\{\mathbf{S} \cdot (\mathbf{p}_1 \times \mathbf{p}_2)\}$ are transversity normal to scattering plane
 - $|\pm 1/2\rangle_T = \{|+1/2\rangle \pm (i) |-1/2\rangle\} / \sqrt{2}$ for spin 1/2
 - Spin 1: $|\pm 1\rangle_T = \{|+1\rangle \pm \sqrt{2} |0\rangle + |-1\rangle\} / 2$
 $|0\rangle_T = \{|+1\rangle - |-1\rangle\} / \sqrt{2}$
 - photon: $|\pm 1\rangle_T = \{|+1\rangle + |-1\rangle\} / \sqrt{2}$ linear polzn normal to plane

Phases & SSA

- Single Spin Asymmetries (SSA) in 2-body
- Parity allows only $\langle \mathbf{S} \cdot \mathbf{n} \rangle$ non-zero for any single spinning



particle. Requires some helicity flip or chirality flip for $m=0$ quarks & phase.

Cross section for spin $\mathbf{S} \cdot \mathbf{n} = +1/2$ minus that for $\mathbf{S} \cdot \mathbf{n} = -1/2$

$$\langle \mathbf{S} \cdot \mathbf{n} \rangle \propto \sum f_{ab,cd}^* [\boldsymbol{\sigma} \cdot \mathbf{n}]_{dd'} f_{ab,cd'} \propto \sum \text{Im}[f_{ab,c+}^* f_{ab,c-}] \text{ for D's SSA}$$

\mathbf{n} requires some \mathbf{p}_2 transverse to \mathbf{p}_1

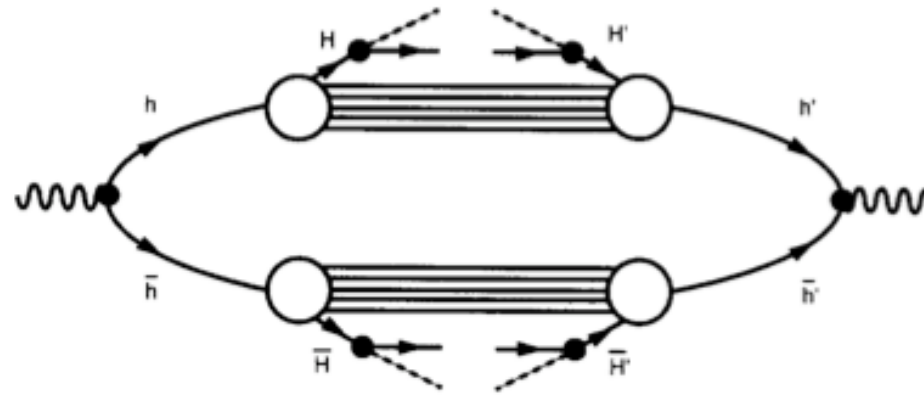
(at quark level? $m=0$ & PQCD - no SSA)

- Inclusive $A+B \rightarrow X+D$: sum over all C particles & relate to $A+B$ +anti-D forward elastic. GRG & J.F.Owens (76)



K. Chen et al. / Nuclear Physics B 445 (1995) 380–396

Tool for determining
transversity transfer
or $H_1(z)$



$$\hat{f}_1(z) = \frac{1}{4}z \int \frac{d\lambda}{2\pi} e^{-i\lambda/z} \langle 0 | \not{h} \psi(0) | \Lambda(PS) X \rangle \langle \Lambda(PS) X | \bar{\psi}(\lambda n) | 0 \rangle,$$

$$\hat{g}_1(z) = \frac{1}{4}z \int \frac{d\lambda}{2\pi} e^{-i\lambda/z} \langle 0 | \not{h} \gamma_5 \psi(0) | \Lambda(PS_{\parallel}) X \rangle \langle \Lambda(PS_{\parallel}) X | \bar{\psi}(\lambda n) | 0 \rangle,$$

$$\hat{h}_1(z) = \frac{1}{4}z \int \frac{d\lambda}{2\pi} e^{-i\lambda/z} \langle 0 | \not{h} \gamma_5 \not{s}_{\perp} \psi(0) | \Lambda(PS_{\perp}) X \rangle \langle \Lambda(PS_{\perp}) X | \bar{\psi}(\lambda n) | 0 \rangle,$$

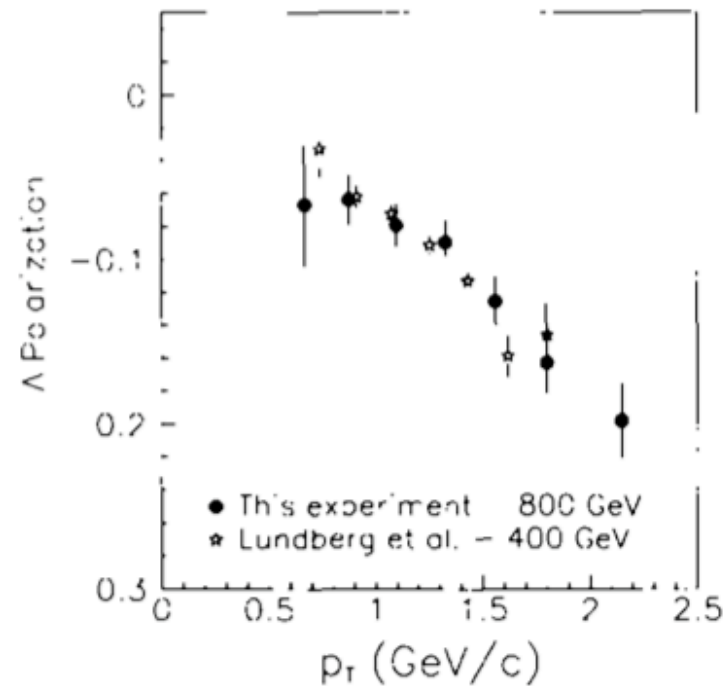
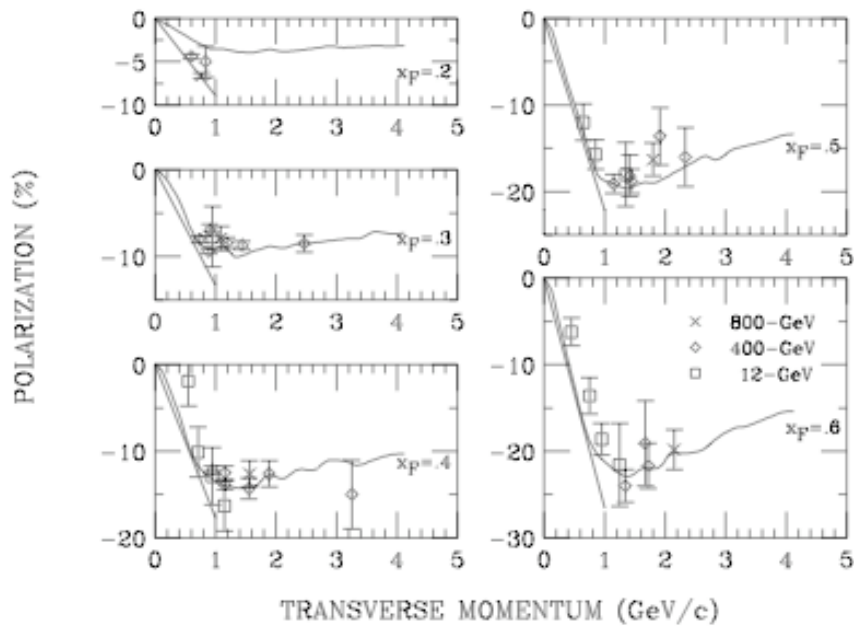
Predicts small back to back transverse spin correlations
ALEPH measurement at Z mass (ave. over $\Lambda \Lambda$ bar):

$$P_T^{\Lambda} = 0.016 \pm 0.007 \text{ for } p_T > 0.3 \text{ GeV}/c,$$

$$P_T^{\Lambda} = 0.019 \pm 0.007 \text{ for } p_T > 0.6 \text{ GeV}/c,$$



Large polarization in hadron+hadron



$p+p \rightarrow \Lambda + X$ Pol $_{\Lambda}$
 compiled by K.Heller (1997)

Fig. 4. Lambda polarization versus production transverse momentum (p_T). For comparison, data for 400 GeV production (Ref. 10) are also shown.

Ramberg, et al.,(FNAL) PLB338, 403 (1994)



Evolving Ideas about Source of Λ Polarization in Hadrons (p+p)

- Semi-classical: Lund; Thomas precession; SU(6) re Λ, Σ, Ξ
- Q Field Th: Single polarization requires amplitude interference \Rightarrow Real x Im part & helicity flip
- Kane, Pumplin, Repko: PQCD $\rightarrow P_{\Lambda} \sim \alpha(\hat{s}) m_q / \sqrt{\hat{s}}$

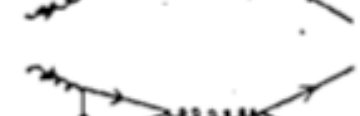
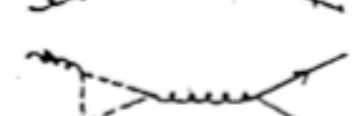
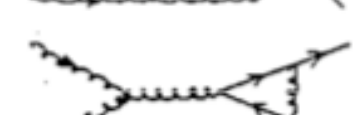
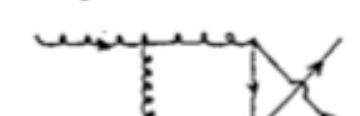
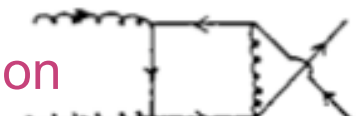
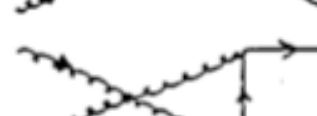
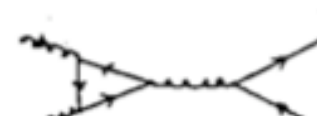
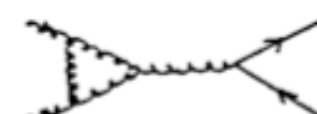
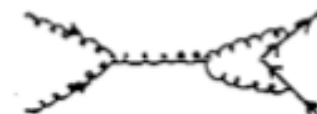
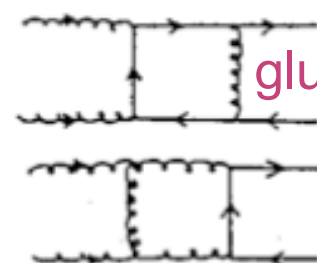
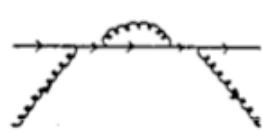


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- Q Field Th: Single polarization requires interference \Rightarrow Real x Im part & helicity flip
- Kane, Pumplin, Repko: PQCD (PRL41,1689(1978) $\rightarrow P_{\Lambda} \sim \alpha(\hat{s})m_q / \sqrt{\hat{s}}$
- Complete order α_s calculation of quark, antiquark, gluon 2-body scattering $\rightarrow s \uparrow + \bar{s}$ imbedded in hadron+hadron pdf's (but small m_s) (Dharmaratna & GG 1990,1996) How does $s \uparrow$ get translated to $\Lambda \uparrow$ & enhanced?

Contributions to order α_s Imaginary Part

(Dharmaratna & GG 1990,1996)

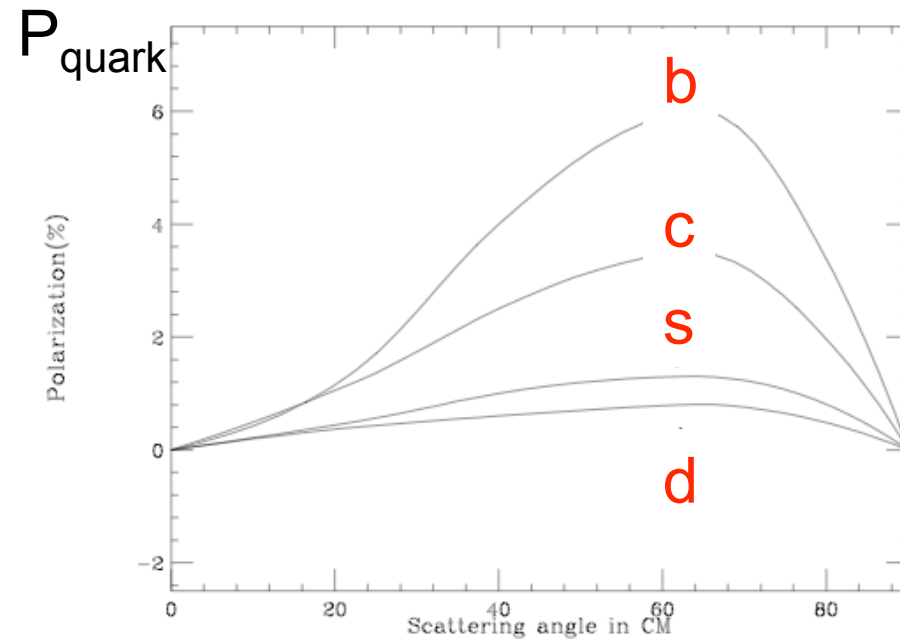




P_{quark} vs. flavor
from gluon fusion
grows with flavor

Does this give
larger P_{hadron} for
heavier flavor?

What sets scales?
quark “mass” or
hyperon mass



$g+g \rightarrow Q+X$

$\text{Pol}_{\text{zn}}(Q) \sim m_Q/v_s$

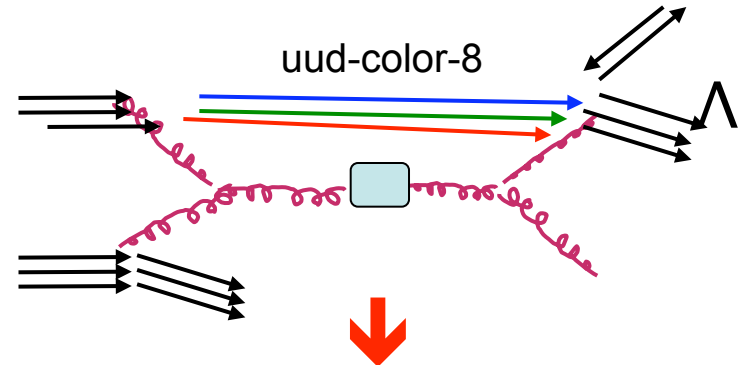
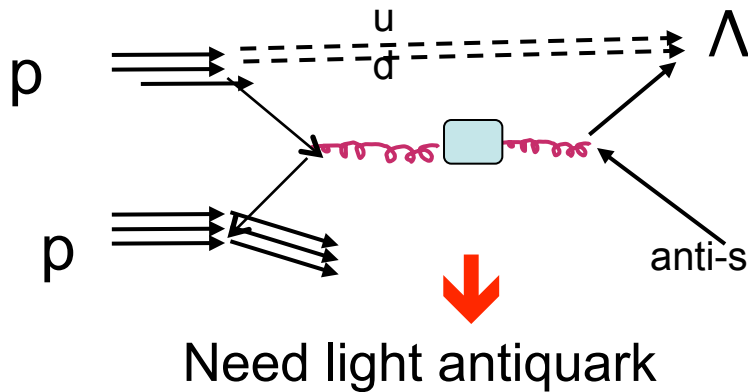
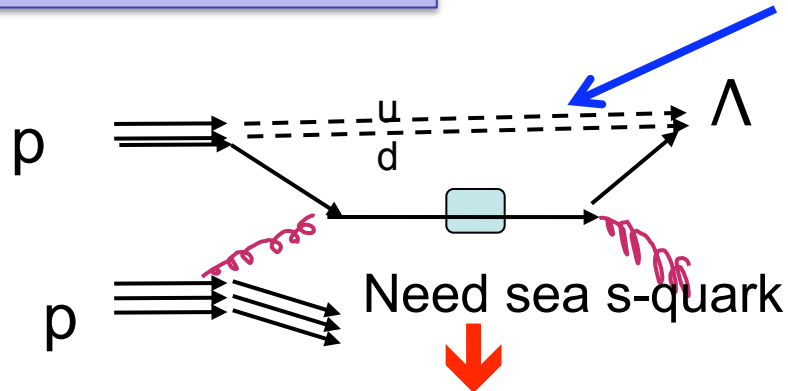


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- How does $s \uparrow$ get translated to $\Lambda \uparrow$ & enhanced?
- Soft "Recombination" with (ud) remnant of N.

How to get to hyperon Polz'n?

Soft "Recombination" with (ud) remnant of proton



Box represents loop contributions to Im part. Seen as *GPD* already have Im part!



Model of hyperon polarization

Dharmaratna & GRG (1990,96,99)

1. $p+p \rightarrow \Lambda^{\uparrow} + X$ has large negative P_{Λ} with flat s dependence & growth with p_{\perp} (see Heller . . .)

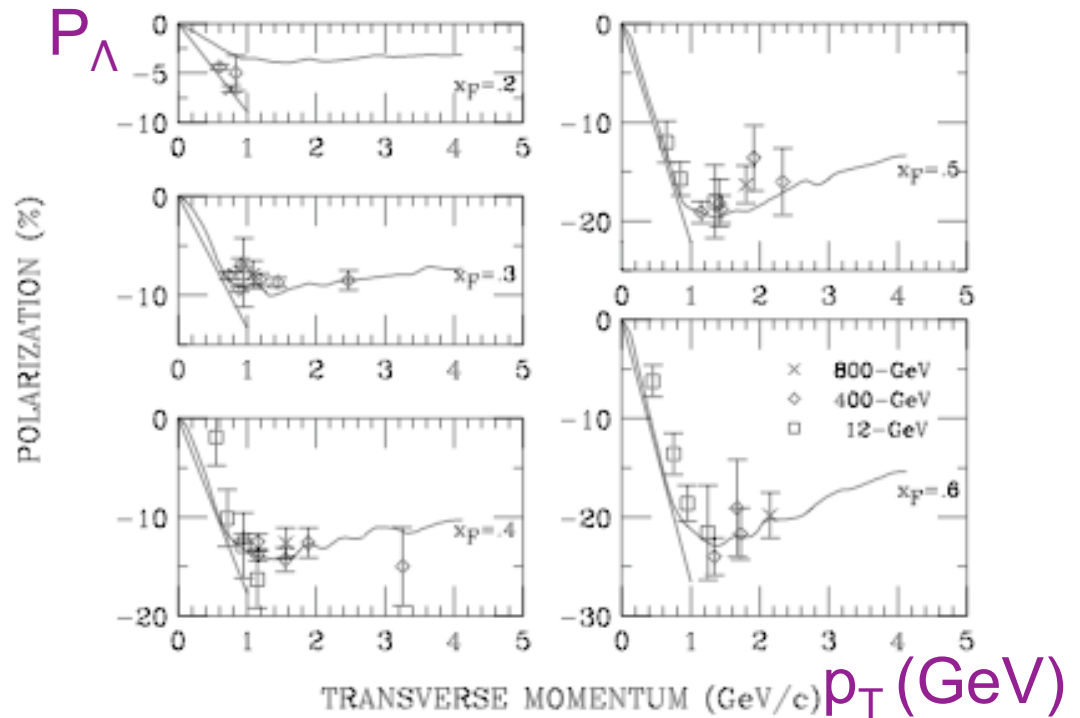
2. Clues: $K^- p \rightarrow \Lambda^{\uparrow} + X$ at 176 GeV/c or $\sqrt{s}=18\text{GeV}$
Polzn even larger - need s -quark?

3. Simple factorization expectation
Kane, Pumplin, Repko

$$P_{\Lambda} \sim \alpha(\hat{s}) m_q / \sqrt{\hat{s}}$$

helicity flip $\sim m_q/\text{hard energy scale}$
Soft phenomenon?

- Dharmaratna & GRG: 1. Gluon fusion dominant mechanism for producing polarized massive quark pair
2. Low p_{\perp} phenomenon
3. Recombination rules

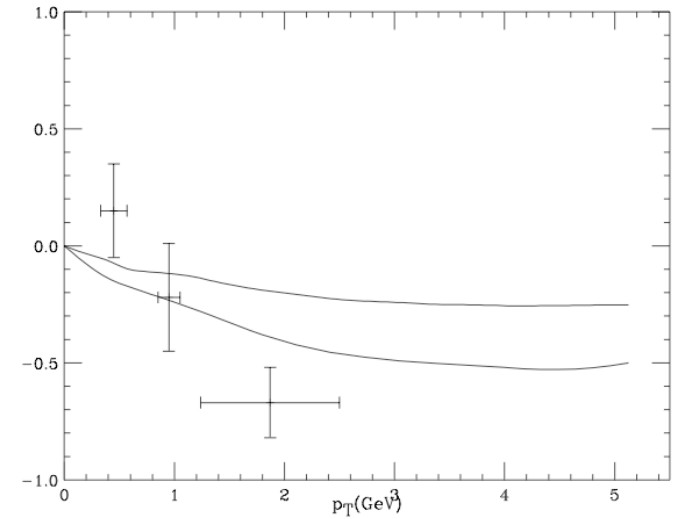
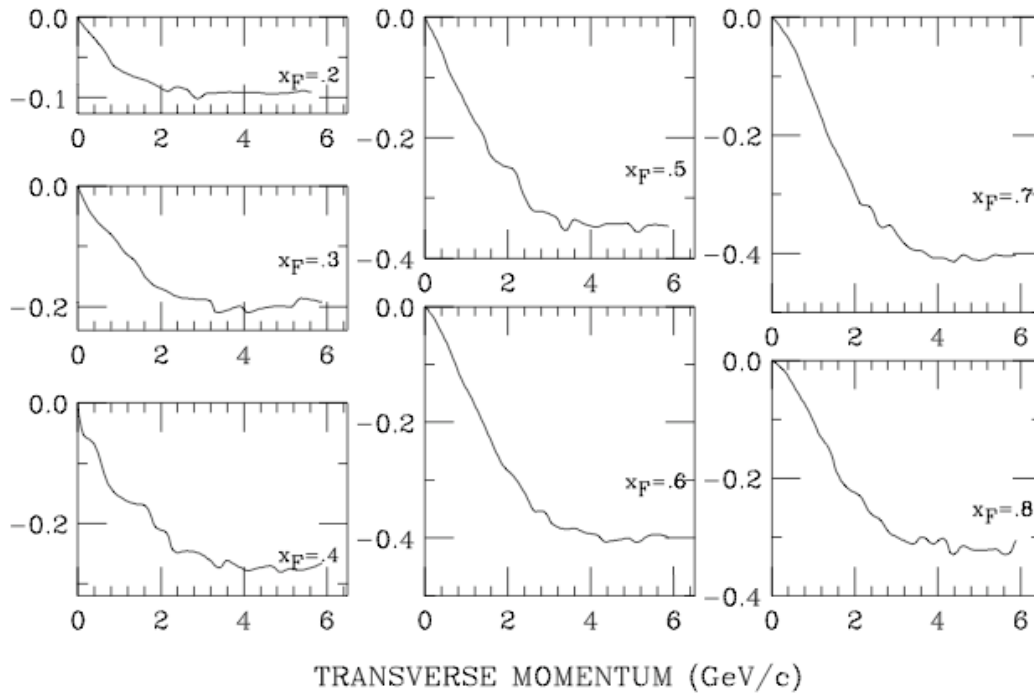


$p+p \rightarrow \Lambda + X$ Polzn(Λ)

compiled by K.Heller (1997)



Charmed Hyperon Polarization



$P(\Lambda_c)$ vs. p_T (GeV) for several x_F values)

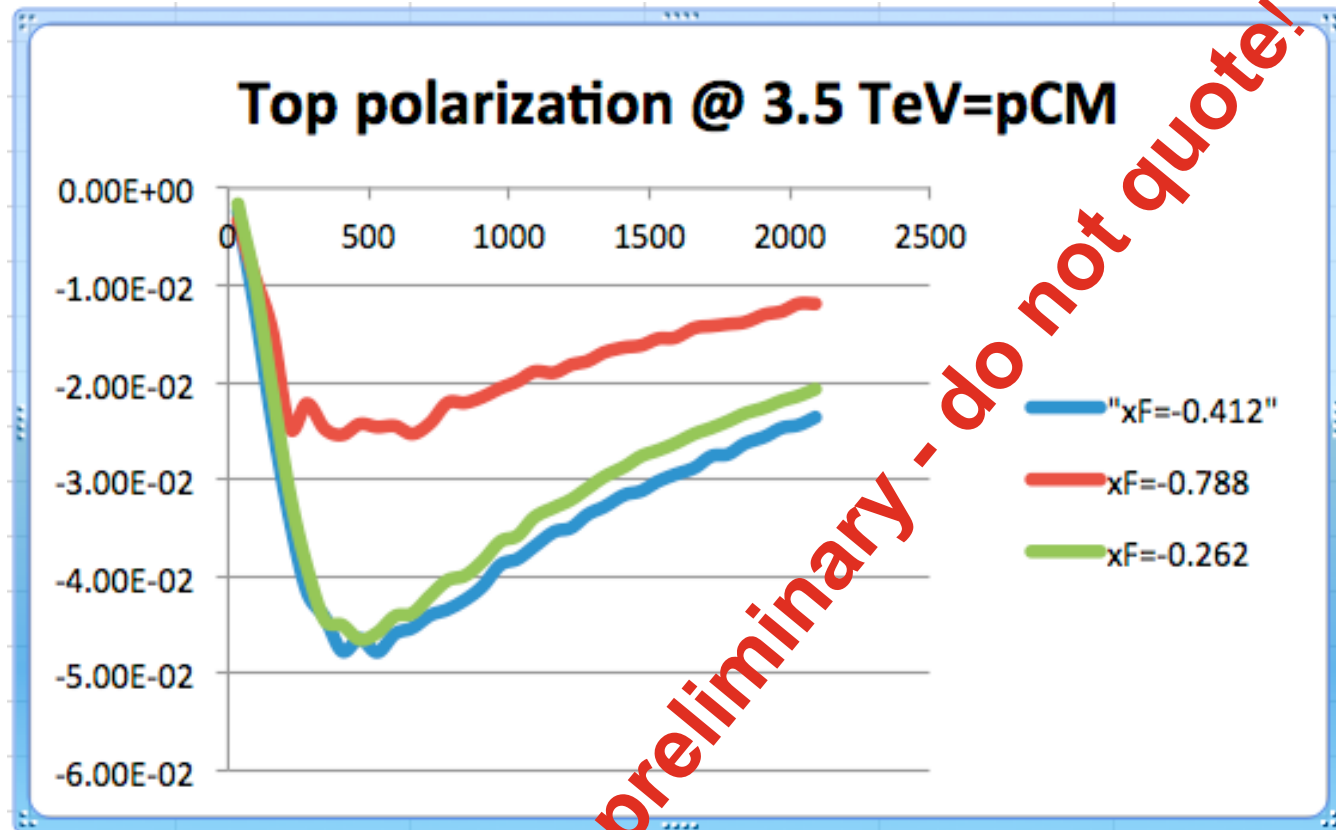
E.M. Aitala, et al. (E791 Collaboration) "Multidimensional Resonance Analysis of $\Lambda_c^+ \rightarrow pK^- \pi^+$ ", Fermilab 1999.

$P(\Lambda_c)$ does not fall off with p_T

Trend to be tested?



Direct measure of hard process - top polarization



Analyze $t \rightarrow W^+ b$



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- How does $s \uparrow$ get translated to $\Lambda \uparrow$ & enhanced?
- Soft "Recombination" with (ud) remnant of N.
- NPQCD must play a significant role in our understanding of orbital angular momentum & hadron formation.



Evolving Ideas about Source of Λ Polarization in Hadrons

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- Complete order α_s calculation of quark, antiquark, gluon 2-body scattering $\rightarrow s \uparrow + \bar{s}$ imbedded in hadron+hadron pdf's (Dharmaratna & GG 1990,1996)
- How does $s \uparrow$ get translated to $\Lambda \uparrow$?
- Consider electroproduction of Λ 's. Prelude to hadron production. QCD more under control.
 - Soft matrix elements from TMDs & SIDIS or GPDs &/or Fracture Functions



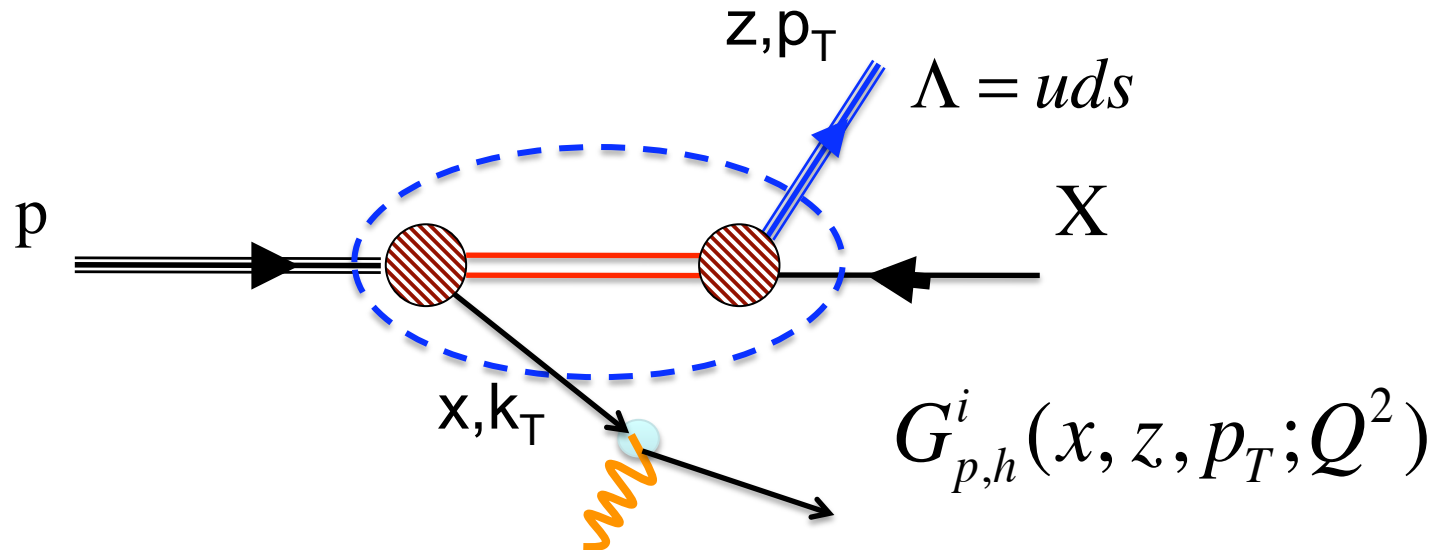
Electroproduction of Λ

Simple tree level model for **extended fracture function**
(Trentadue & Veneziano)

Diquark spectator & fragmentation

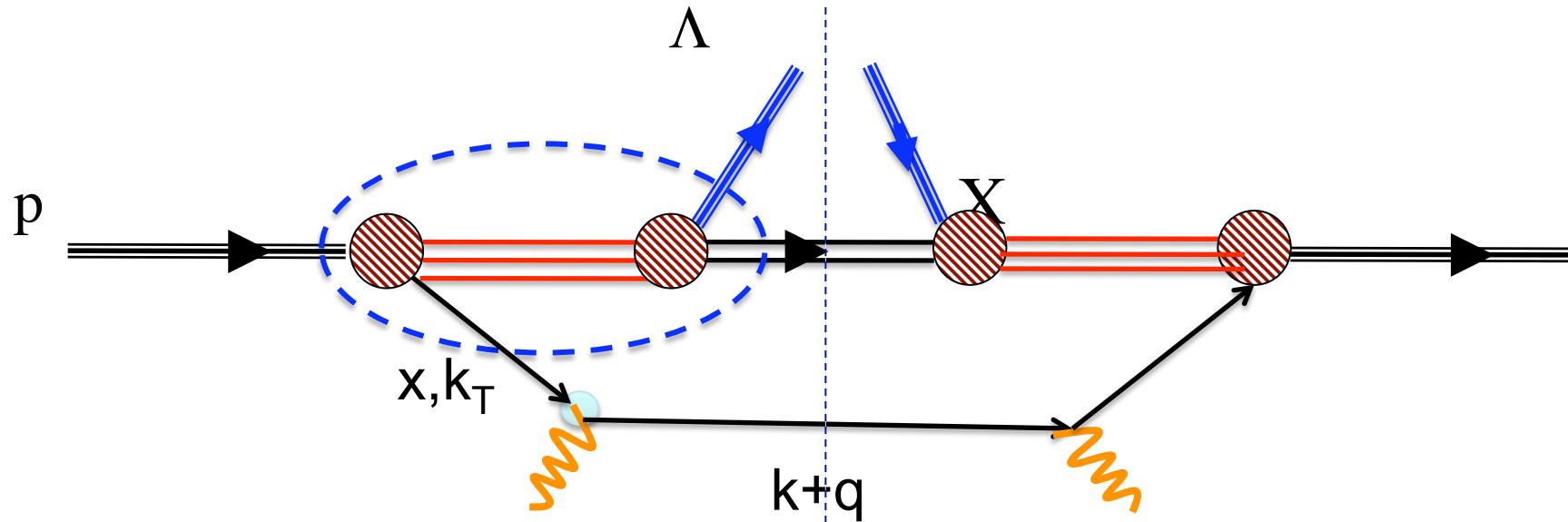
“ $d\sigma$ ” squares & sums over X states with anti-s flavor

Diquark $\rightarrow \Lambda + s\text{-bar}$ simple vertex



$$z = E_{\Lambda} / (1-x) E_{\gamma P_{CM}} \text{ for target fragment}$$

$$\text{or } P_{\Lambda}^{+} = z(1-x) P^{+}$$



$$(P - k)^2 = m_s^2 + \frac{M_\Lambda^2}{z} + \frac{1-z}{z} \left(\vec{P}_{\Lambda T} - \frac{z}{1-z} \vec{P}_{XT} \right)^2$$

Dipole form factors dampen $P \rightarrow u + \text{diq}$ vertex
 Λ , diquark, struck quark all on shell

$$k^2 = xM^2 - \frac{\vec{k}_T^2}{(1-x)} - \frac{x}{(1-x)} (P - k)^2 \quad \delta((k+q)^2) \rightarrow x = x_{Bj}$$



diquark model extended fracture function

$$(P - k)^2 = m_s^2 + \frac{M_\Lambda^2}{z} + \frac{1-z}{z} \left(\vec{P}_{\Lambda T} - \frac{z}{1-z} \vec{P}_{XT} \right)^2$$

$$k^2 = xM^2 - \frac{\vec{k}_T^2}{(1-x)} - \frac{x}{(1-x)} (P - k)^2$$

$$\mathcal{F}_{\Lambda_N, \Lambda_\Lambda}^{\lambda_q}(x, k_T, z, p_T, Q^2) = \sum_{\Lambda_X} \int \frac{d^3 P_X}{(2\pi)^3 2E_X} \int \frac{d^4 \xi}{(2\pi)^4} e^{ik \cdot \xi} \langle P | \bar{\psi}(\xi) | P_h; X \rangle \langle P_h; X | \psi(0) | P \rangle.$$

quark correlator for Extended Fracture Functions

helicity labels $\langle P, \Lambda_N |$ & $| P_h, \Lambda_\Lambda ; X \rangle$

For unpolarized $d\sigma$, sum over all helicity labels.

For polarized Λ , keep floating

diquark model extended fracture function

In the spectator model

$$\mathcal{F}_{\lambda_q, \Lambda_N}^{\Lambda_\Lambda, \Lambda'_\Lambda}(x, k_T, z, p_T, Q^2) = A_{\Lambda_N, \lambda_q} \sum_{\Lambda_X} B_{\Lambda_X}^{\Lambda_\Lambda, \Lambda'_\Lambda}$$

where

$$A_{\Lambda_N, \lambda_q} = |\phi_{\lambda, \Lambda}(k, P)|^2,$$

with

$$\phi_{\lambda, \Lambda}(k, P) = \Gamma(k) \frac{\bar{u}(k, \lambda_q) U(P, \Lambda_N)}{k^2 - m^2},$$

and

$$k = P - P_X - P_\Lambda \Rightarrow k^2 = k^2(x, \mathbf{k}_T, z, \mathbf{p}_T)$$

whereas

$$B_{\Lambda_X}^{\Lambda_\Lambda, \Lambda'_\Lambda} = \tilde{\phi}_{\Lambda_X, \Lambda'_\Lambda}^*(P_X, P_h) \tilde{\phi}_{\Lambda_X, \Lambda_\Lambda}(P_X, P_h),$$

with

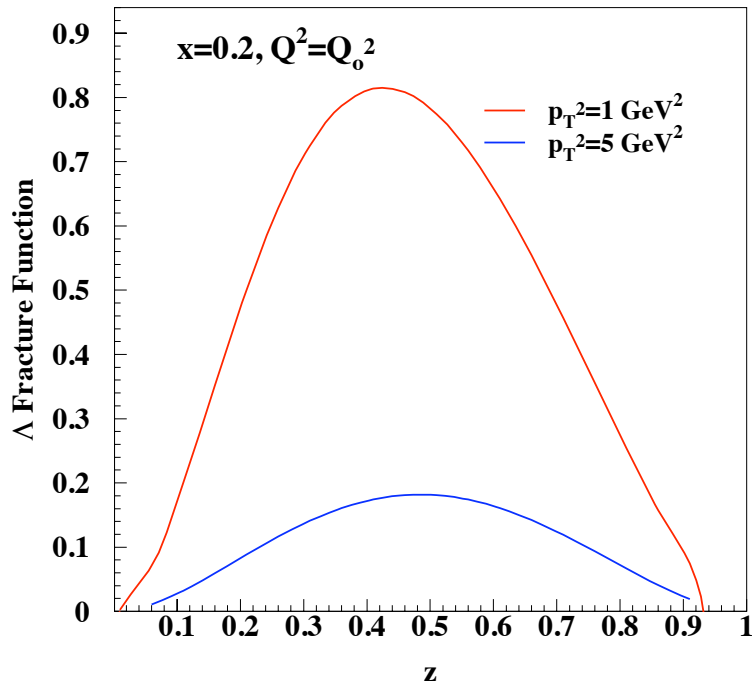
$$\tilde{\phi}_{\Lambda_X, \Lambda_\Lambda}(P_X, P_h) = \Gamma(P_X) \bar{v}(P_X, \Lambda_X) U(P_h, \Lambda_\Lambda)$$

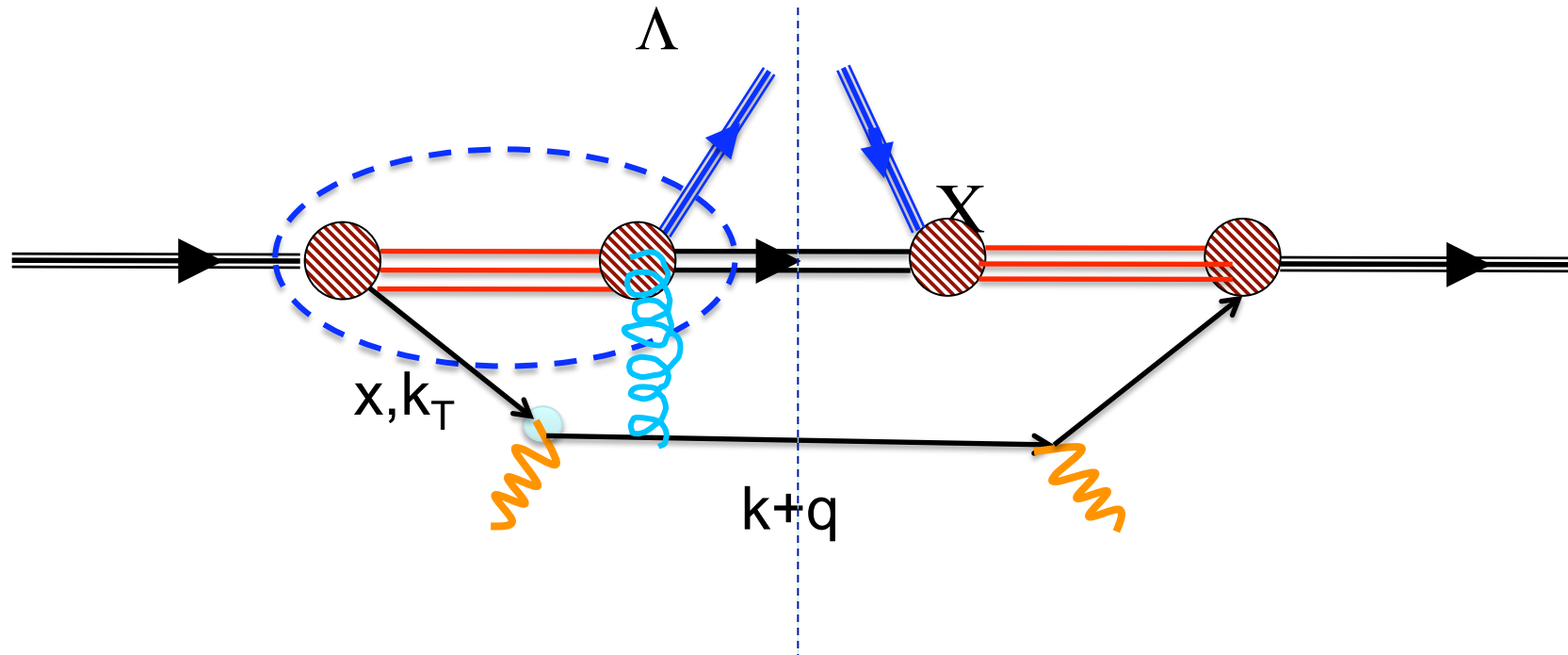
diquark model extended fracture function

$$\sum_{\Lambda_X} B_{\Lambda_X}^{\Lambda_\Lambda, \Lambda'_\Lambda} = (1-x)^2 \left([-zM_X + (1-z)M_\Lambda]^2 + p_T^2 \right) \delta_{\Lambda_\Lambda, \Lambda'_\Lambda}$$

A_{Λ_N, λ_q} is squared & summed over

$$\rightarrow f(x, k_T) / (k^2 - m_{dipole}^2)^4 \Big|_{P_X^2 = (P-k-P_\Lambda)^2 = m_s^2}$$





Spin dependence?

- a. non-trivial quark or proton- Λ spin correlation \rightarrow axial diquark
- b. SSA need phase \rightarrow beyond tree

Figure shows final state interaction contribution to $\Lambda \uparrow$

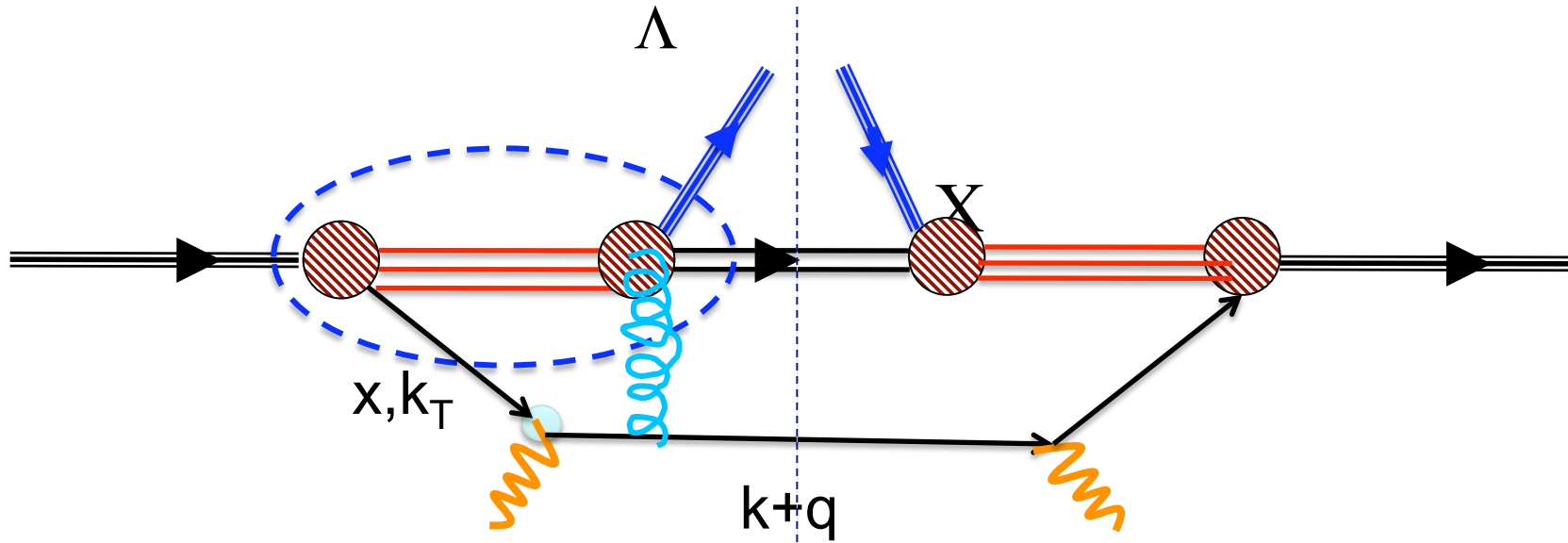
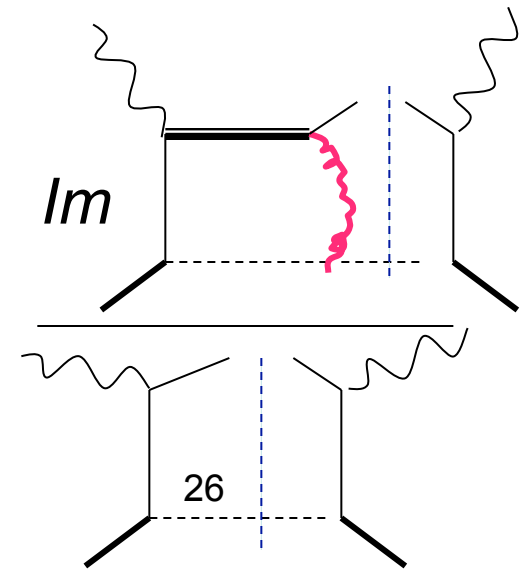


Figure shows final state interaction contribution to $\Lambda \uparrow$

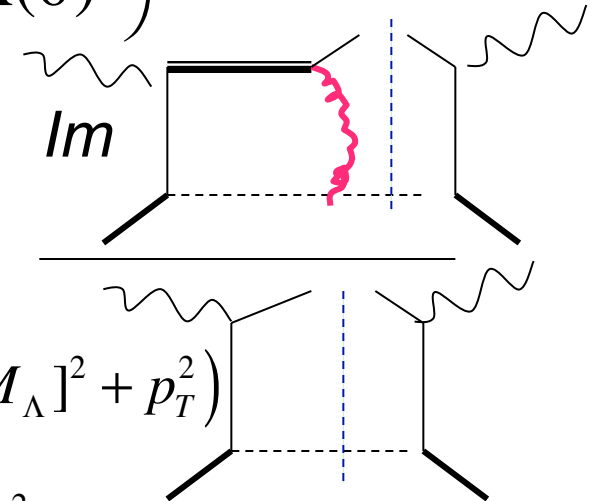


Final State Interactions or gauge links

Recall f.s.i. (e.g. Brodsky, Hwang & Schmidt; Gamberg & Goldstein, etc.)

$$P_y = C_F \alpha_s(\mu^2) \frac{(xM + m)k_x}{[(xM + m)^2 + \vec{k}_\perp^2]} \frac{\Lambda(\vec{k}_\perp^2)}{\vec{k}_\perp^2} \ln \left(\frac{\Lambda(\vec{k}_\perp^2)}{\Lambda(0)} \right)$$

$$\Lambda(\vec{k}_\perp^2) = \vec{k}_\perp^2 + x(1-x) \left(-M^2 + \frac{m^2}{x} + \frac{\lambda^2}{1-x} \right)$$



For Frac.Fn. model replace denom with $([-zM_X + (1-z)M_\Lambda]^2 + p_T^2)$

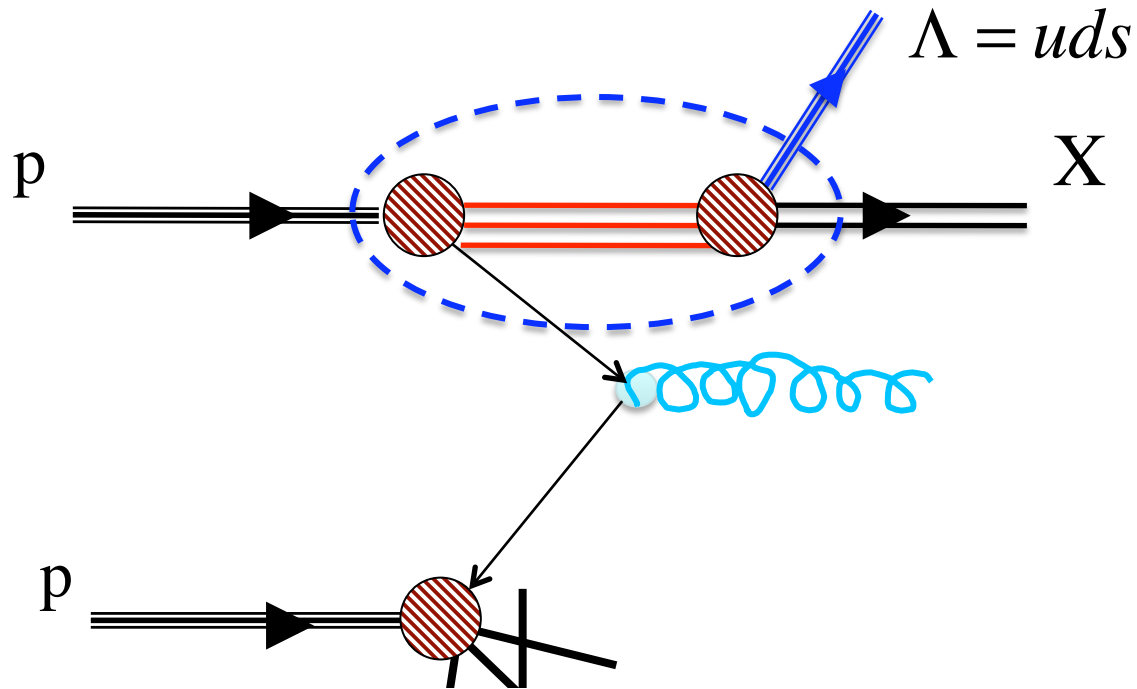
$$\Omega(\vec{k}_T^2, \vec{p}_T^2) = xM^2 - \left\{ \vec{k}_T^2 + x \left[m_s^2 + \frac{M_\Lambda^2}{z} + \frac{1-z}{z} \left(\vec{p}_T - \frac{z}{1-z} \vec{p}_{XT} \right)^2 \right] \right\} / (1-x)$$

numerator with $(1-x)^2 k_T (zM_X - (1-z)M_\Lambda^2)$ from Im flip \times non-flip



PDFs + Fracture functions
Incorporated into P + P

$$\langle p | \bar{\psi} | \Lambda X \rangle$$

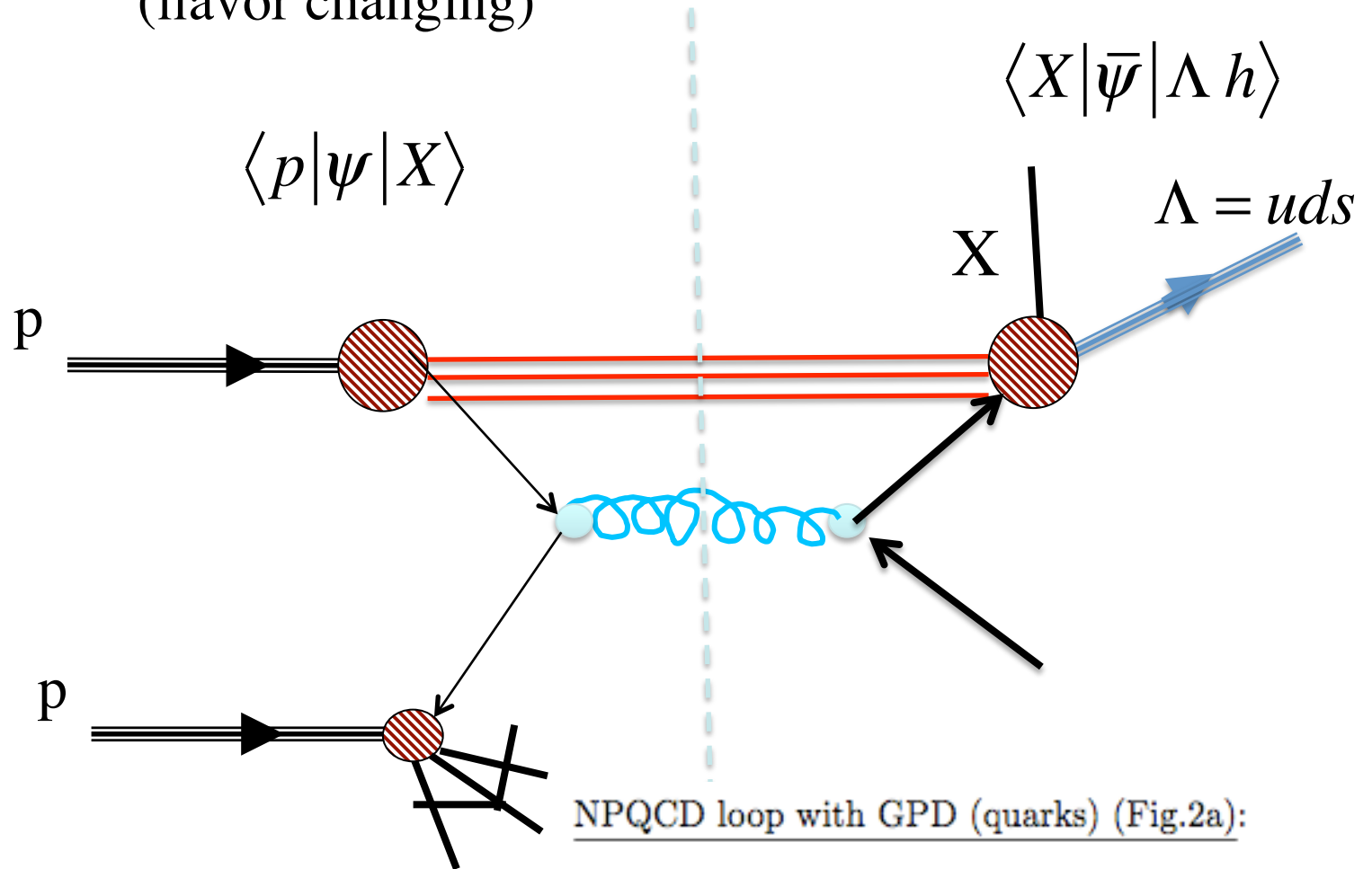


Formally, for a quark-nucleon FF,

$$\begin{aligned} \mathcal{F}(x, k_T, z, p_T, Q^2) = & \sum_X \int \frac{d^3 P_X}{(2\pi)^3 2E_X} \int \frac{d^4 \zeta}{(2\pi)^4} e^{ik \cdot \zeta} \\ & \times \langle P | \bar{\psi}(\zeta) | P_{hadron}; X \rangle \\ & \times \langle P_{hadron}; X | \psi(0) | P \rangle. \quad (6) \end{aligned}$$

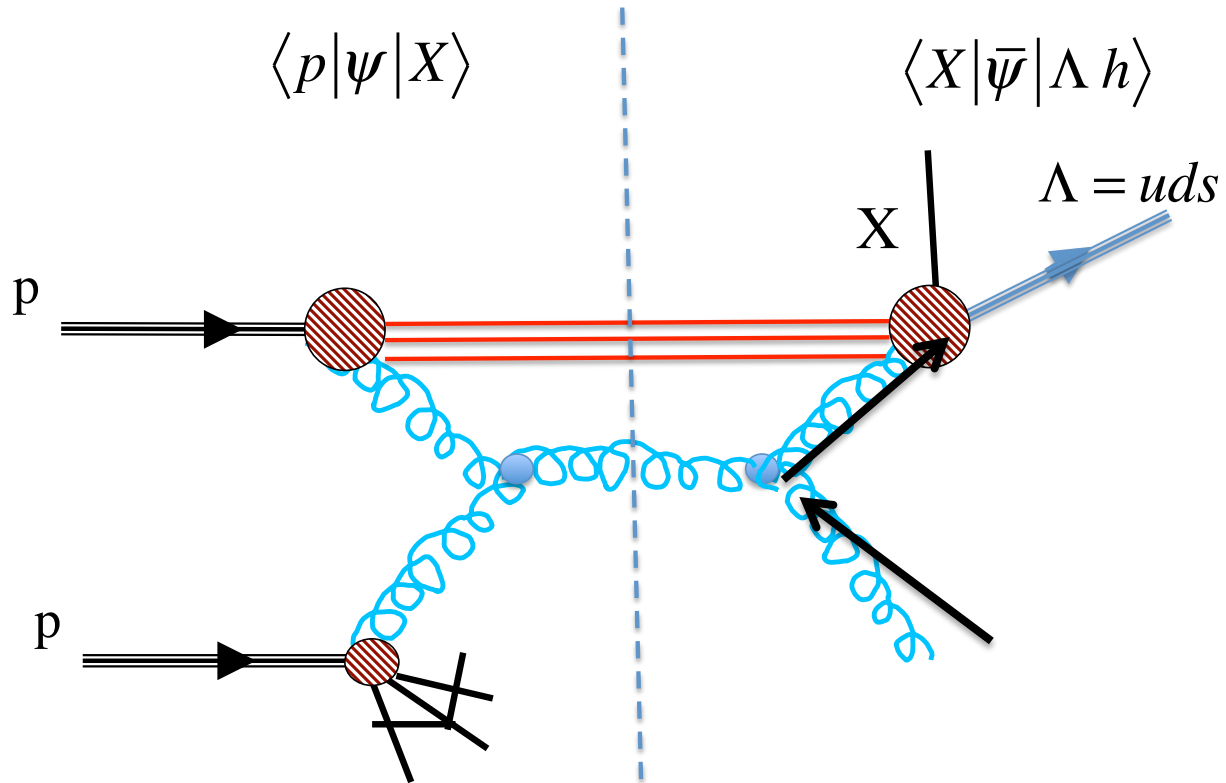


Generalized Fracture Function \rightarrow extended GPDs
(flavor changing)



$$\int dx_1 dx_2 [\mathcal{H}_{N \rightarrow Y}^* \mathcal{H}_{N \rightarrow Y}] (x_1, \zeta, t, Q^2) \times f(x_2, Q^2) \hat{\sigma}_{12 \rightarrow sX}^{LO}(x_1, x_2, x_F^s, p_T)$$

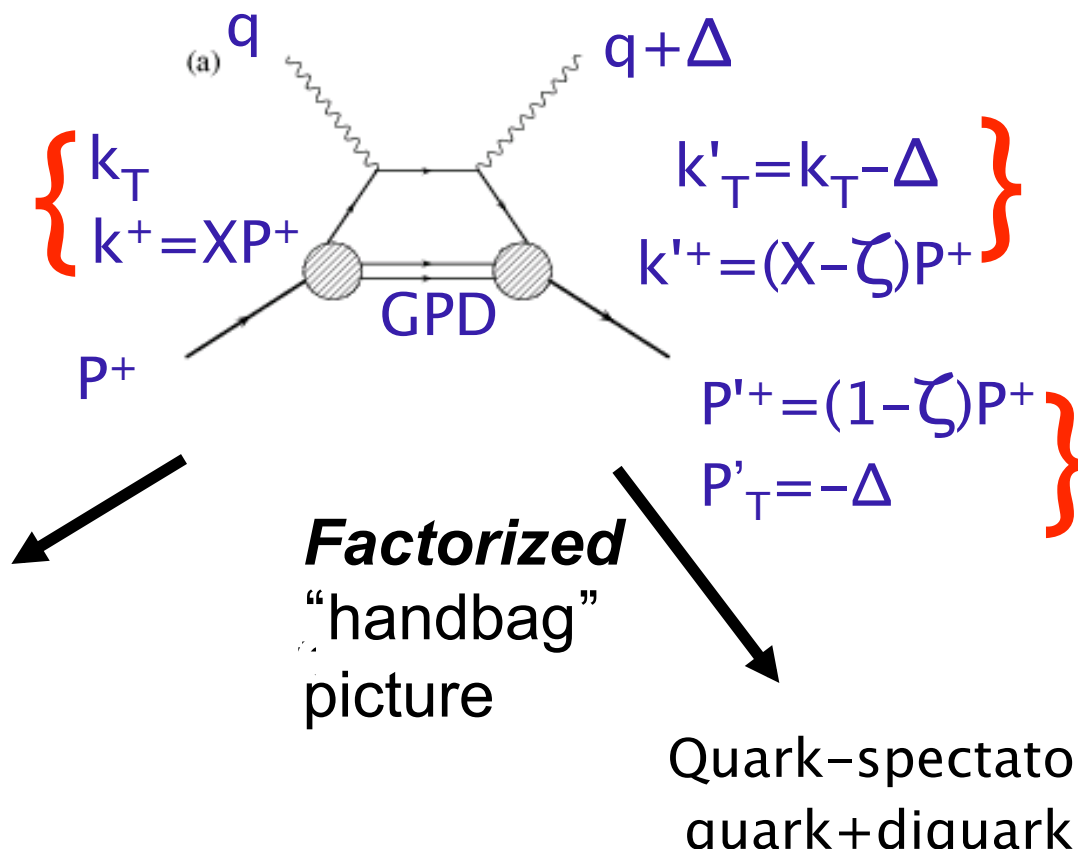
Generalized Fracture Function



Gluon fusion is largest source of polarized quarks & gluons . . .
Gluons will be plentiful at LHC. Move toward Gluon GPDs



DVCS & DVMP $\gamma^*(Q^2)+P \rightarrow (\gamma \text{ or meson})+P'$
 partonic picture

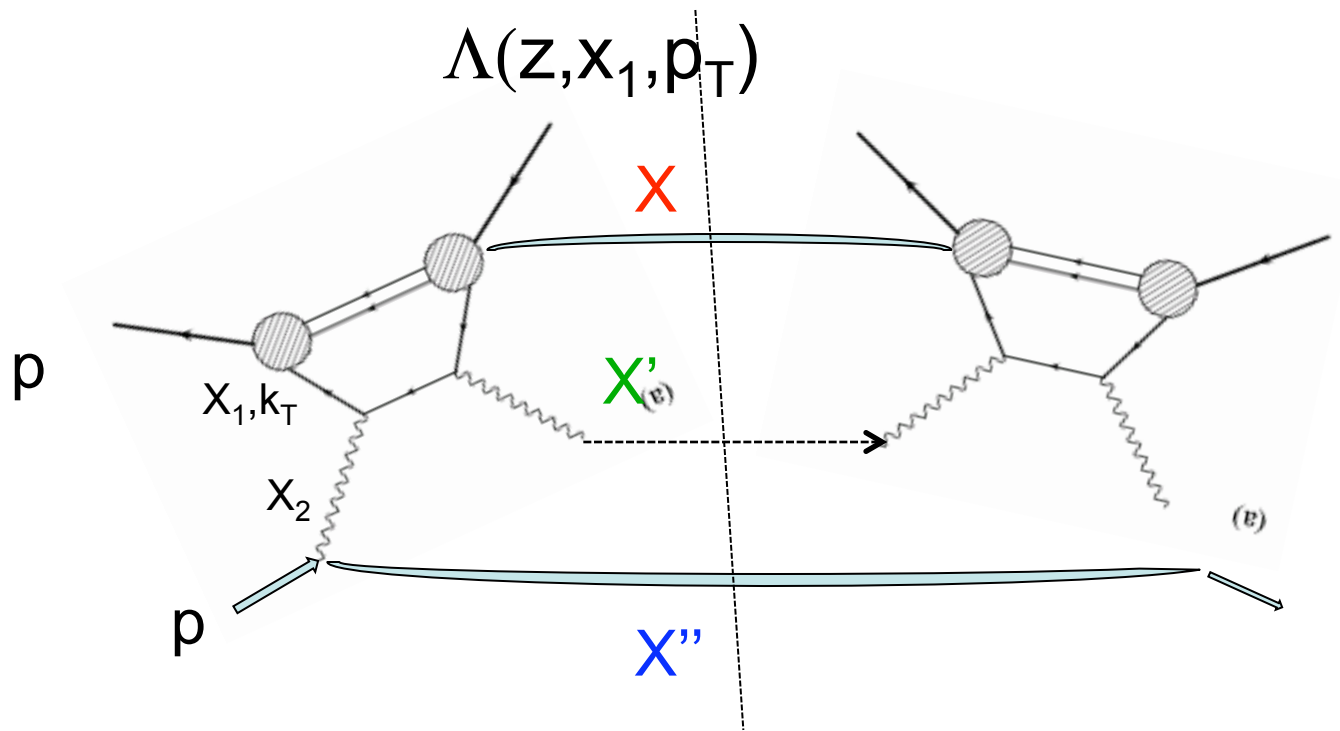


$\zeta \rightarrow 0$
 Regge

$X > \zeta$ DGLAP
 $X < \zeta$ ERBL

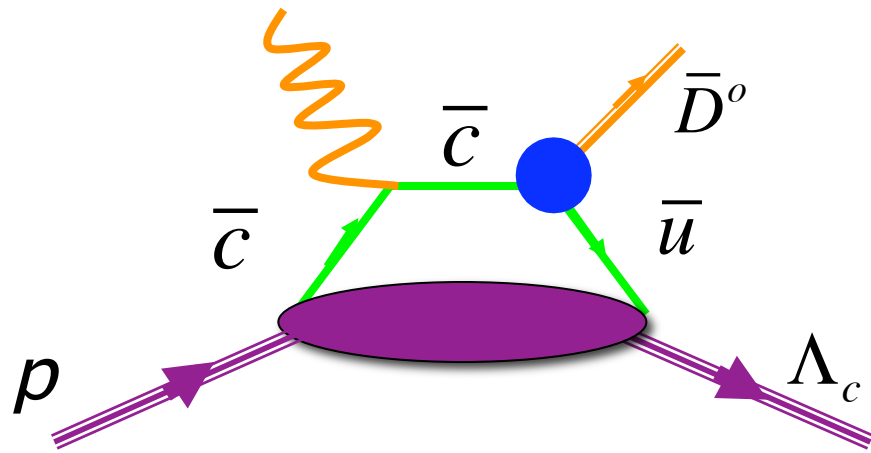
see Ahmad, GG, Liuti, PRD79, 054014, (2009) for first chiral odd GPD
 G.G., O. Gonzalez Hernandez, S. Liuti, PRD84, 034007 (2011)

GPD source of $\Lambda \uparrow$
 CFF \rightarrow Re & Im parts



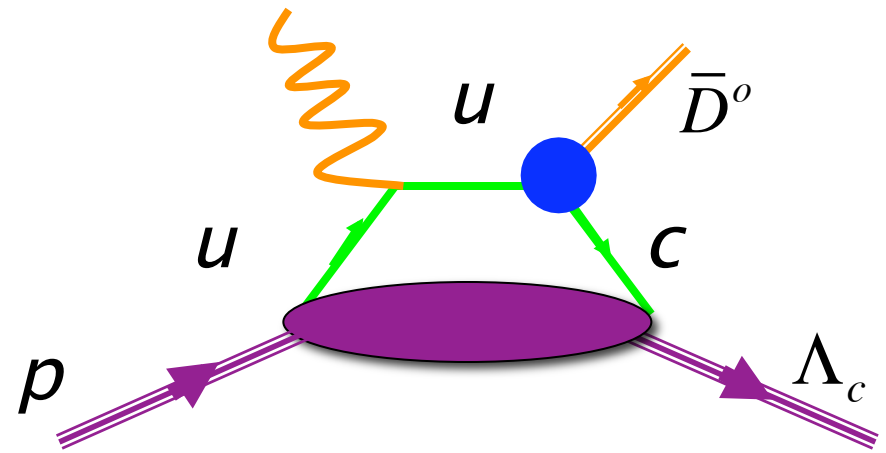
Each line has helicity summed over except Λ_Λ & Λ'_Λ
 Real & Im CFF multiplied for Polzn

Flavor off-diagonal GPDs – example: charm production



$$\propto H_c$$

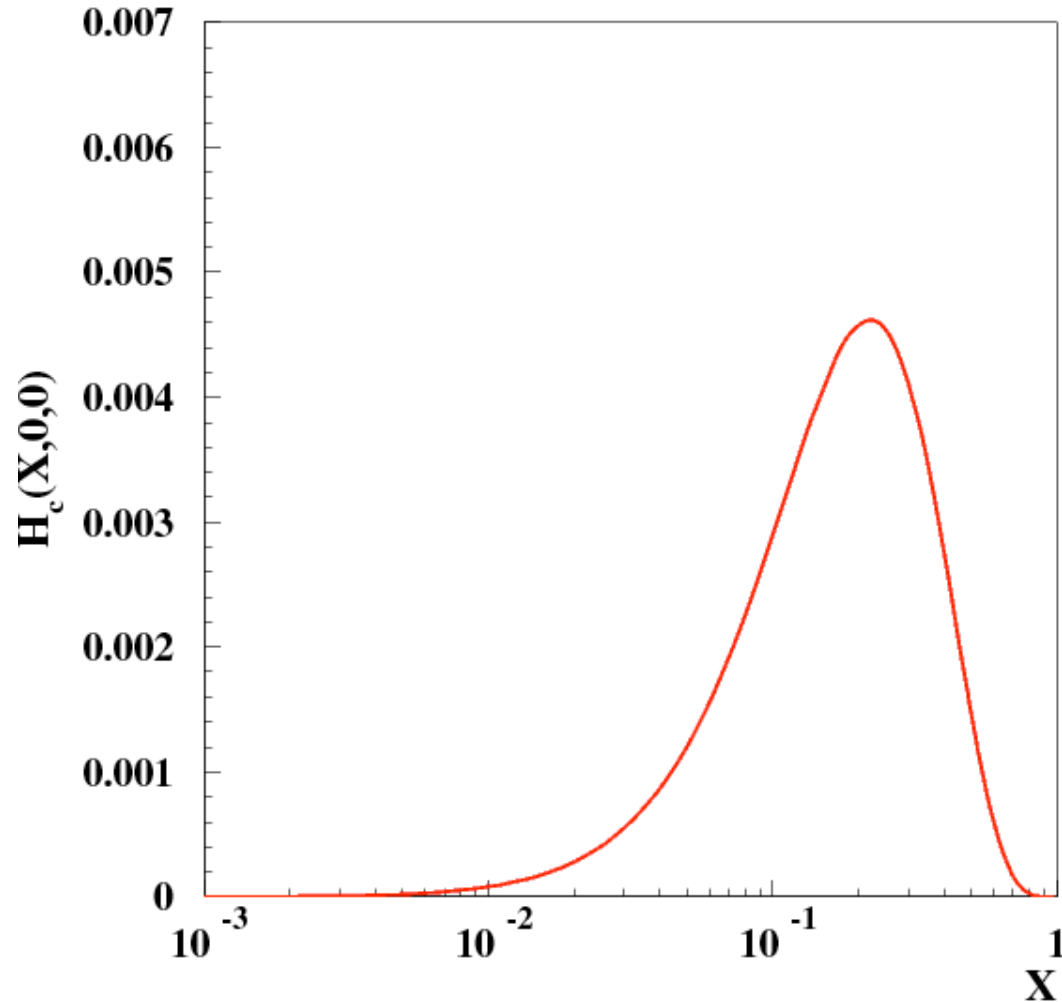
$$p \rightarrow c\text{-bar} + c u u d$$



$$\propto H_u$$

$$p \rightarrow u + u d$$

Example charm GPD

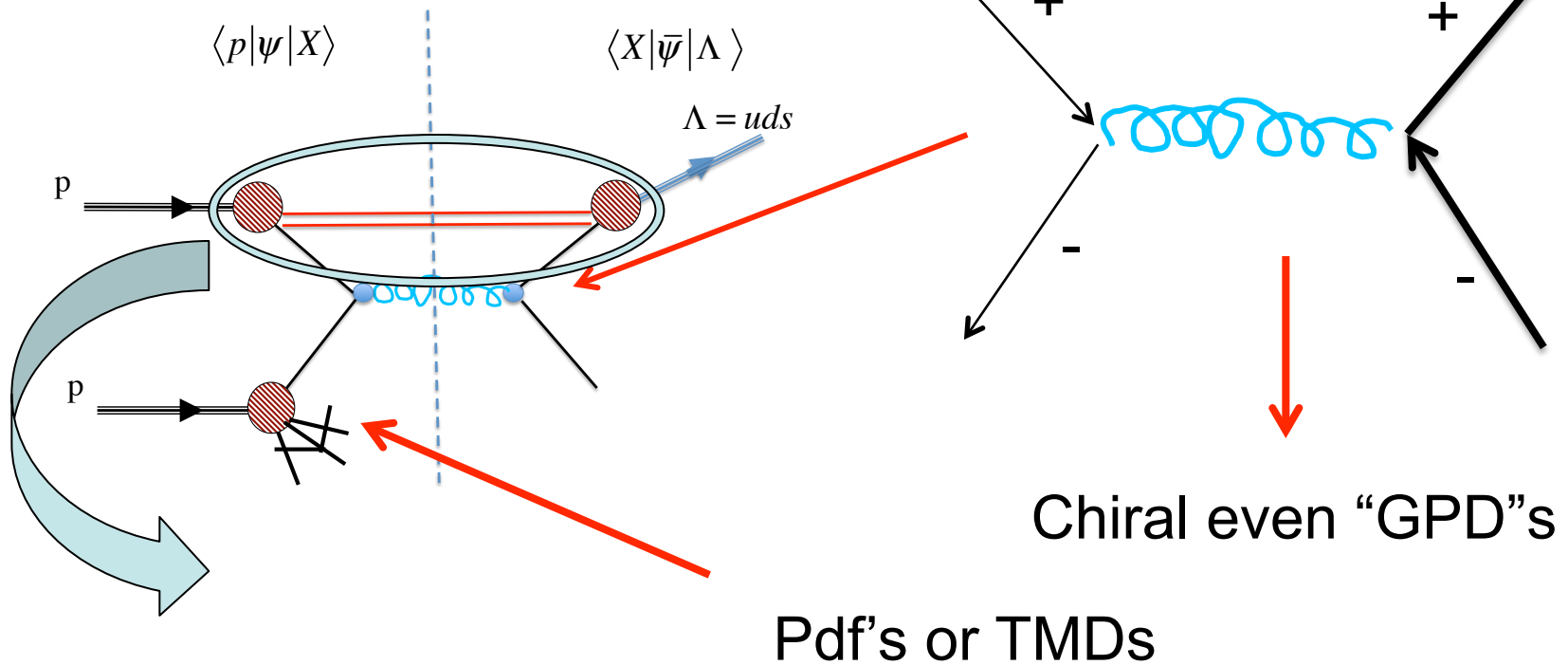


Next fold into $x_2 P^-$
as “q” & pdf’s.
Extract Im from $x=\zeta$ &
Real from P.V. integral.
Then Polzn can be
straightforwardly
determined.

GG & Liuti, Proc. EIC
Meeting SBU, Sept.2010.

Qualitative results

Generalized (Flavor Changing) Parton Distribution



$$A_{\Lambda(\Lambda) \lambda(s), \Lambda(P) \lambda(u)}(x_1, \zeta, p_T \text{ or } t, s\text{-hat})$$

$$\rightarrow A_{\Lambda(\Lambda) +, \Lambda(P) +} \& A_{\Lambda(\Lambda) -, \Lambda(P) -}$$



GPD definitions

Momentum space nucleon matrix elements of quark field correlators

see, e.g. M. Diehl, Eur. Phys. J. C 19, 485 (2001).

$$\frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p', \lambda' | \bar{\psi}(-\frac{1}{2}z) \gamma^+ \psi(\frac{1}{2}z) | p, \lambda \rangle \Big|_{z^+=0, z_T=0}$$

$$= \frac{1}{2P^+} \bar{u}(p', \lambda') \left[H^q \gamma^+ + E^q \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} \right] u(p, \lambda),$$

$$\frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p', \lambda' | \bar{\psi}(-\frac{1}{2}z) \gamma^+ \gamma_5 \psi(\frac{1}{2}z) | p, \lambda \rangle \Big|_{z^+=0, z_T=0}$$

$$= \frac{1}{2P^+} \bar{u}(p', \lambda') \left[\tilde{H}^q \gamma^+ \gamma_5 + \tilde{E}^q \frac{\gamma_5 \Delta^+}{2m} \right] u(p, \lambda),$$

Chiral even GPDs

$$\frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p', \lambda' | \bar{\psi}(-\frac{1}{2}z) i\sigma^{+i} \psi(\frac{1}{2}z) | p, \lambda \rangle \Big|_{z^+=0, z_T=0}$$

$$= \frac{1}{2P^+} \bar{u}(p', \lambda') \left[H_T^q i\sigma^{+i} + \tilde{H}_T^q \frac{P^+ \Delta^i - \Delta^+ P^i}{m^2} \right.$$

$$\left. + E_T^q \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2m} + \tilde{E}_T^q \frac{\gamma^+ P^i - P^+ \gamma^i}{m} \right] u(p, \lambda).$$

Chiral odd GPDs



Recall that helicity amps are linear combinations of GPDs

$$\begin{aligned}
 A_{+,+;+,+} &= \sqrt{1-\xi^2} \left[\frac{H + \tilde{H}}{2} - \frac{\xi^2}{1-\xi^2} \frac{E + \tilde{E}}{2} \right] \\
 A_{-,+;-,+} &= \sqrt{1-\xi^2} \left[\frac{H - \tilde{H}}{2} - \frac{\xi^2}{1-\xi^2} \frac{E - \tilde{E}}{2} \right] \\
 A_{+,+;-,+} &= -\frac{\sqrt{t_0-t}}{4M} (E - \xi \tilde{E}) \\
 A_{-,+;+,+} &= \frac{\sqrt{t_0-t}}{4M} (E + \xi \tilde{E})
 \end{aligned}$$

for chiral even GPDs and

$$\begin{aligned}
 A_{+-,++} &= -\frac{\sqrt{t_0-t}}{2M} \left[\tilde{H}_T + \frac{1+\xi}{2} E_T - \frac{1+\xi}{2} \tilde{E}_T \right] \\
 A_{++,--} &= \sqrt{1-\xi^2} \left[H_T + \frac{t_0-t}{4M^2} \tilde{H}_T - \frac{\xi^2}{1-\xi^2} E_T + \frac{\xi}{1-\xi^2} \tilde{E}_T \right] \\
 A_{+,-,+} &= -\sqrt{1-\xi^2} \frac{t_0-t}{4M^2} \tilde{H}_T \\
 A_{++,+-} &= \frac{\sqrt{t_0-t}}{2M} \left[\tilde{H}_T + \frac{1-\xi}{2} E_T + \frac{1-\xi}{2} \tilde{E}_T \right],
 \end{aligned}$$

for chiral odd GPDs, where for consistency with previous literature we have

In diquark spectator models $A_{+,+;+,+}$, etc. are calculated directly. Inverted \rightarrow GPDs



Invert to obtain model for GPDs

Scalar
diquark:

$$\begin{aligned}
 A_{++, -+} &= -A_{++, +-} & H(x, \xi, t) &= \frac{1}{\sqrt{1-\xi^2}}(A_{+, +; +, +} + A_{-, +; -, +}) - \frac{2M\xi^2}{\Delta(1-\xi^2)}(A_{+, +; -, +} - A_{-, +; +, +}) \\
 A_{-, +, ++} &= -A_{+, -, ++} & E(x, \xi, t) &= -\frac{2M}{\Delta}(A_{+, +, -, +} - A_{-, +; +, +}) \\
 A_{++, ++} &= A_{++, --} & \tilde{H}(x, \xi, t) &= \frac{1}{\sqrt{1-\xi^2}}(A_{+, +; +, +} - A_{-, +; -, +}) + \frac{2M\xi}{\Delta(1-\xi^2)}(A_{+, +, -, +} + A_{-, +; +, +}) \\
 & & \tilde{E}(x, \xi, t) &= \frac{2M}{\Delta\xi}(A_{+, +, -, +} + A_{-, +; +, +})
 \end{aligned}$$

for chiral even GPDs and

$$\begin{aligned}
 H_T(x, \xi, t) &= \frac{1}{\sqrt{1-\xi^2}}(A_{+, +; -, -} + A_{-, +; +, -}) + \frac{2M\xi}{\Delta(1-\xi^2)}(A_{+, +; +, -} - A_{-, +; -, -}) \\
 \xi E_T(x, \xi, t) - \tilde{E}_T(x, \xi, t) &= \frac{2M}{\Delta}(A_{+, +; +, -} - A_{-, +; -, -}) \\
 E_T(x, \xi, t) + \tilde{E}_T(x, \xi, t) &= \frac{\Delta}{2M(1-\xi)}[2A_{+, +; +, -} + \frac{4M}{\Delta\sqrt{1-\xi^2}}A_{-, +; +, -}] \\
 \text{double flip } \tilde{H}_T(x, \xi, t) &= \frac{4M^2}{\Delta^2\sqrt{1-\xi^2}}A_{-, +; +, -}
 \end{aligned}$$

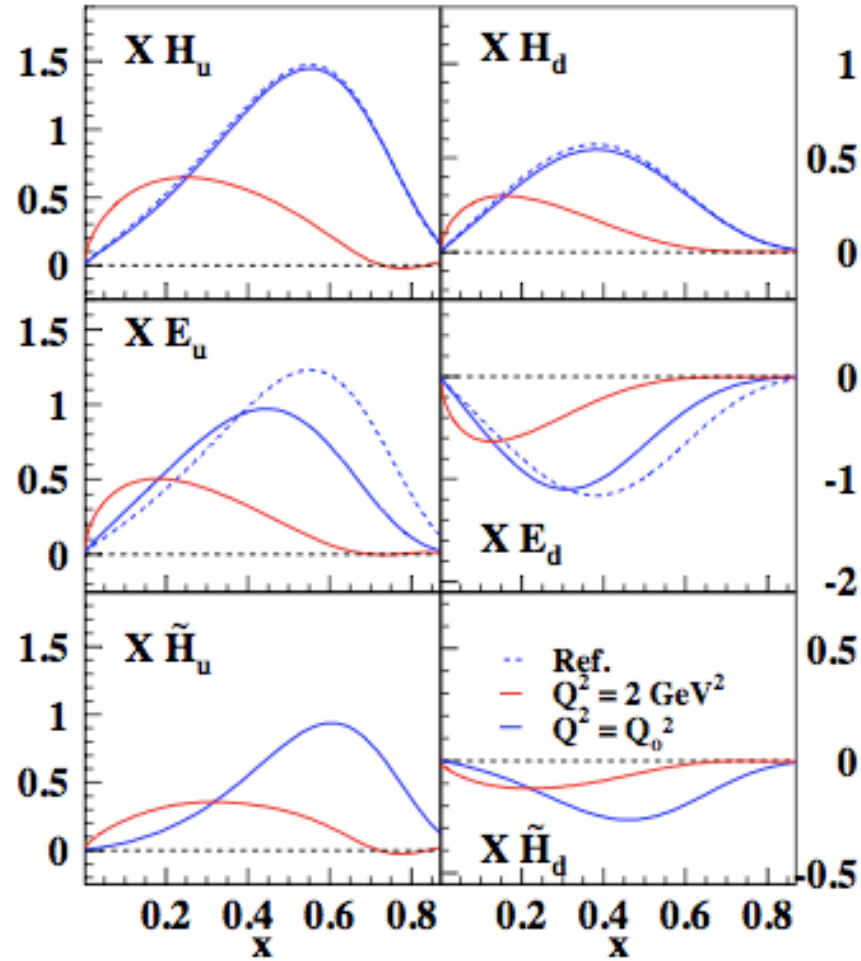


FIG. 6: (color online) GPDs $F_q(X, 0, 0) \equiv \{H_q, E_q, \tilde{H}_q\}$, for $q = u$ (left) and $q = d$ (right), evaluated at the initial scale, $Q_0^2 = 0.0936 \text{ GeV}^2$, and at $Q^2 = 2 \text{ GeV}^2$, respectively. The dashed lines were calculated using the model in Refs. [24, 25] at the initial scale.

Summary

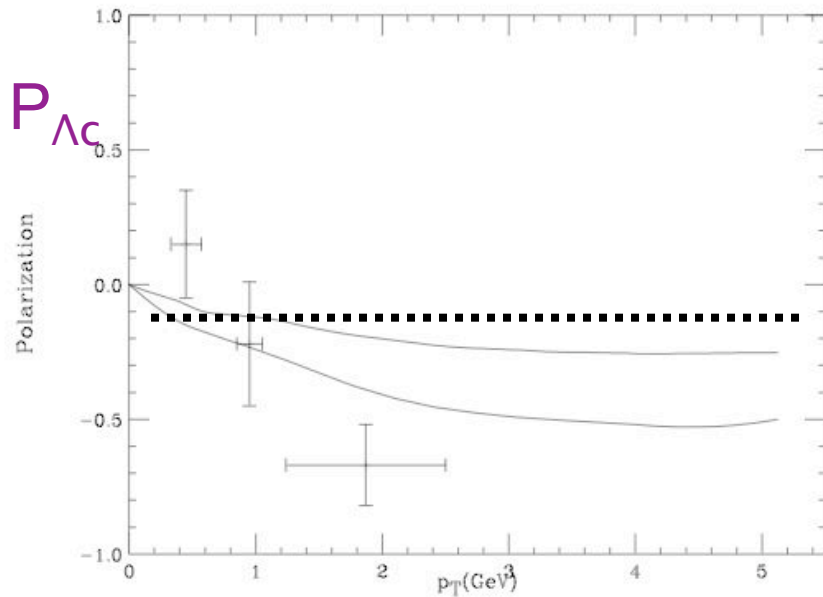
- Hyperon polarization is touchstone for understanding transversity & hence NPQCD
- Several ways to begin to explain phenomena
- “Upside down” TMDs with f.s.i.
- Extended GPDs → Extended Fracture Functions
- Work in progress



Hyperon and Charmed Hyperon Polarization

GG, S. Liuti ~ with P. Di Nezza

Interpretation in new language of GPDs?:
Generalized Fracture Functions
(Trentadue & Veneziano)



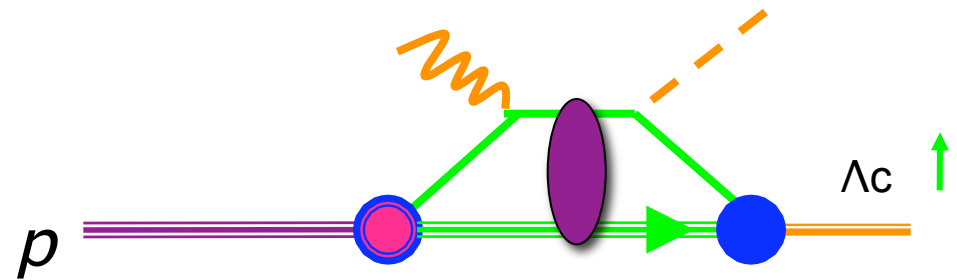
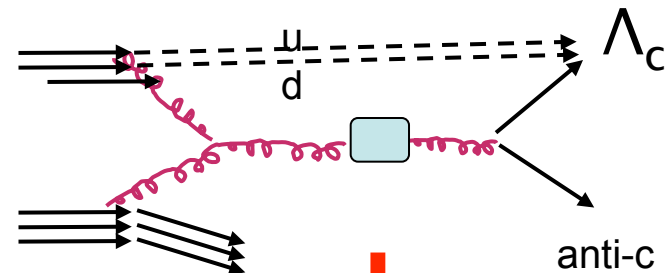
$\pi+p \rightarrow \Lambda_c + X$ Polzn(Λ_c) E791

$\Lambda_c^+ \rightarrow p + \pi^+ + K^-$

Large mass scale

p_T (GeV)

$$G_{p,h}^i(x, z, \zeta, t)$$



9/1/11

41



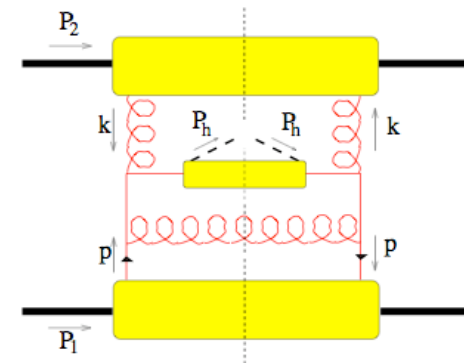
Target Fragmentation approach

D_{1T}^\perp has been extracted from fixed target $p + p(Be) \rightarrow \Lambda^\uparrow(\bar{\Lambda}^\uparrow) + X$ data

Anselmino, D.B., D'Alesio & Murgia, PRD 63 (2001) 054029

D. Boer, DIS 2010

Outstanding puzzle!



Collinear Factorization

$$P_\Lambda \sim q(x_1) \otimes g(x_2) \otimes \hat{\sigma}_{qg \rightarrow qg} \otimes ?$$

Non Collinear Factorization

Go beyond collinear factorization,
Insert k_T and polarization dependent
Fragmentation function

→ Polarizing Fragmentation Function
Does this vitiate gluon fusion?