

(@COMPASS&NICA)

Transversity-2011

Veli Losinj, Croatia

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Oleg Teryaev

JINR, Dubna



Outline

- Angular distributions and positivity
- (Very) simple theory for LT
- Semi-exclusive pion-nucleon DY (COMPASS) and pion DA
- Exclusive DY (COMPASS, NICA) and TDA
- Transverse SSA in DY: contour gauge and factor 2
- BG-type duality in DY (@COMPASS&PANDA): Sivers function and time-like formfactors
- NICA&DY
- Spin effects in HIC



QCD factorization mechanisms

- Hard and Soft parts may change simultaneously for transition to different kinematical domains
- Various factorization mechanisms (duality, matching,...)
- Exclusivity for DY (TMD)pdf's- \rightarrow GPDs

Positivity for dilepton angular distribution

- Angular distribution

$$d\sigma \propto 1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + \frac{\nu}{2} \sin^2 \theta \cos 2\phi + \rho \sin 2\theta \sin \phi + \sigma \sin^2 \theta \sin 2\phi$$

- Positivity of the matrix (= hadronic tensor in dilepton rest frame)

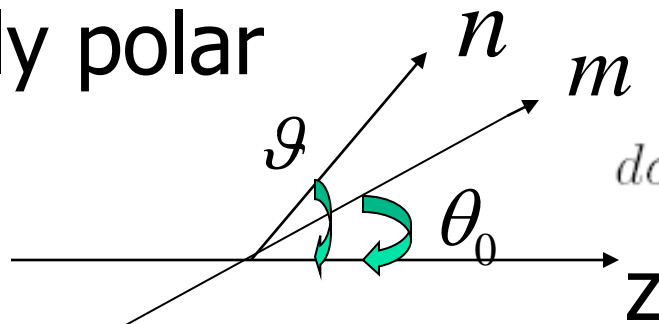
$$M_0 = \begin{pmatrix} \frac{1-\lambda}{2} & \mu & \rho \\ \mu & \frac{1+\lambda-\nu}{2} & \sigma \\ \rho & \sigma & \frac{1+\lambda+\nu}{2} \end{pmatrix} \quad \begin{aligned} |\lambda| \leq 1, \quad |\nu| \leq 1 + \lambda, \quad \mu^2 &\leq \frac{(1-\lambda)(1+\lambda-\nu)}{4} \\ \rho^2 &\leq \frac{(1-\lambda)(1+\lambda+\nu)}{4}, \quad \sigma^2 \leq \frac{(1+\lambda)^2 - \nu^2}{4} \end{aligned}$$

- + cubic – $\det M_0 > 0$

- 1st line – Lam&Tung by SF method

Kinematic azimuthal asymmetry from polar one by rotation ($\sim k_T$)

Only polar



$$d\sigma \propto 1 + \lambda_0 (\vec{n}\vec{m})^2 = 1 + \lambda_0 \cos^2 \theta_{nm}$$

asymmetry with respect to m !

$$\cos \theta_{nm} = \cos \theta \cos \theta_0 + \sin \theta \sin \theta_0 \cos \phi$$

- azimuthal

angle appears with new

$$\lambda = \lambda_0 \frac{2 - 3 \sin^2 \theta_0}{2 + \lambda_0 \sin^2 \theta_0}$$

$$\nu = \lambda_0 \frac{2 \sin^2 \theta_0}{2 + \lambda_0 \sin^2 \theta_0}$$



Matching with pQCD results (J. Collins, PRL 42,291,1979)

- Direct comparison: $\tan^2 \theta_0 = (k_T/Q)^2$
- Off-shellness effects for colliding (anti)quarks
– cancel in GI set
- New ingredient – expression for μ
- Linear in k_T
- Saturates positivity constraint!
- Tests by J.-C. Peng, J. Roloff: often close to saturation
- Extra probe of transverse momentum

Generalized Lam-Tung relation (OT'05)

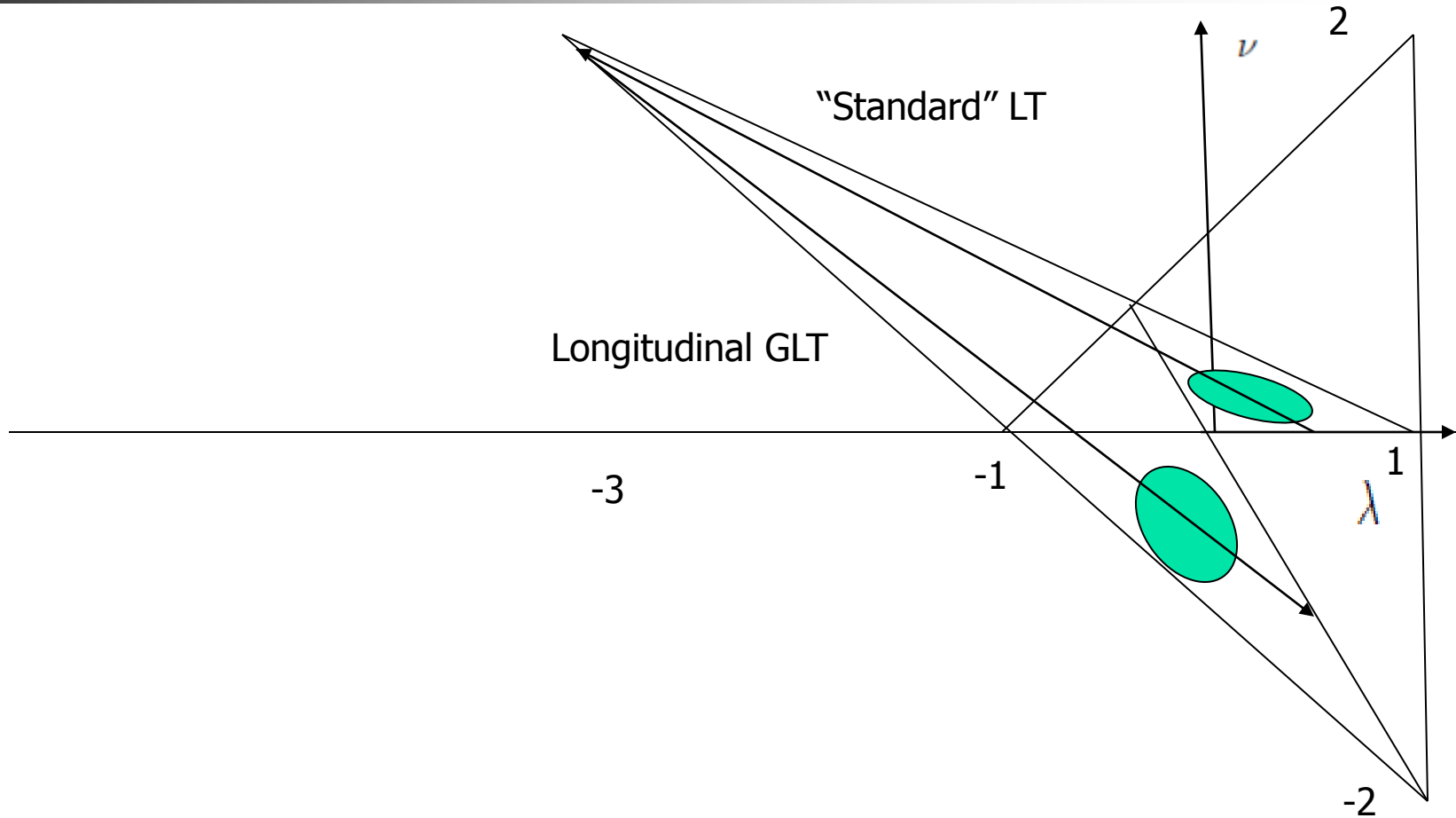


- Relation between coefficients (high school math sufficient!)

$$\lambda_0 = \frac{\lambda + \frac{3}{2}\nu}{1 - \frac{1}{2}\nu}$$

- Reduced to standard LT relation for transverse polarization ($\lambda_0 = 1$)
- LT - contains two very different inputs: kinematical asymmetry+transverse polarization

Positivity domain with (G)LT relations



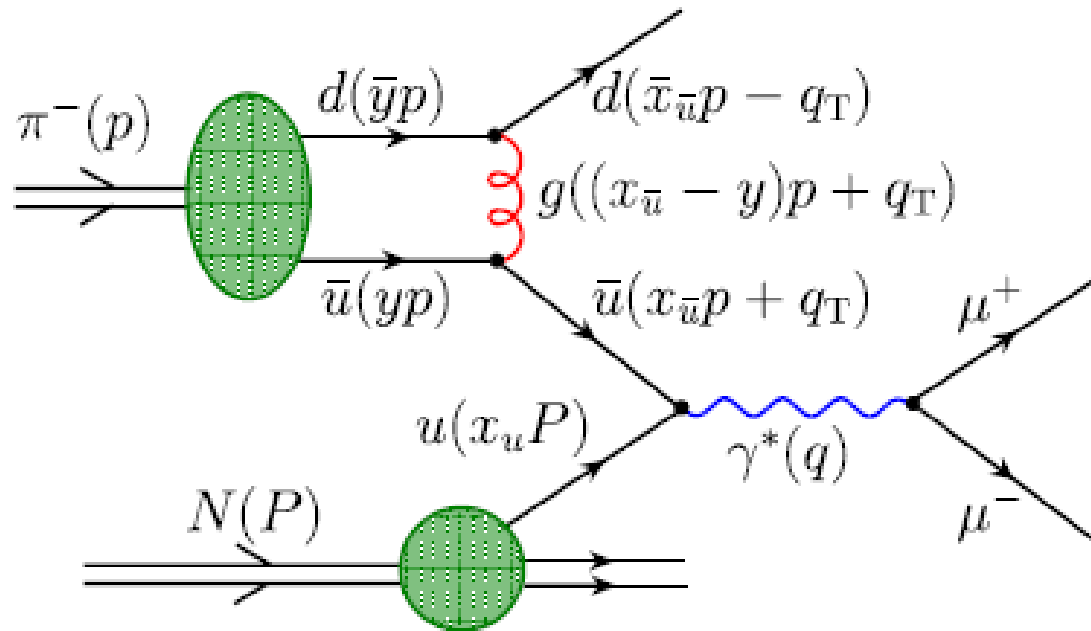


LT violation

- Azimuthal asymmetries at fundamental level required
- Privileged plane
- NLO-gluon emission
- BM-quark spins

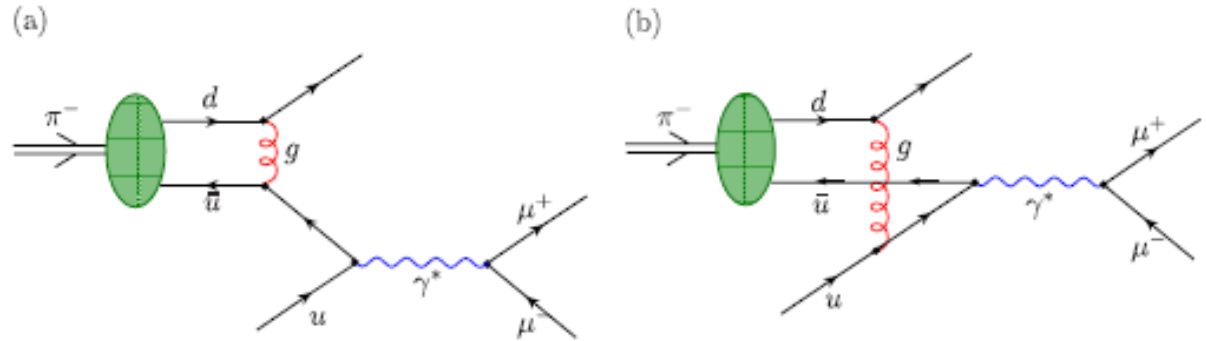
- Off-shell quarks (NLO,HT)

Semi-Exclusive DY (large x_F) - Pion participates through Distribution Amplitude (Light-cone WF)





GI ->



- Colour GI -> second diagram -> phase
- Unpolarized – Brandenburg, Brodsky, Mueller(94)
- Longitudinally polarized -> SSA – Brandenburg, Mueller, OT(95)
- Refined DA – Bakulev, Stefanis, OT(07)

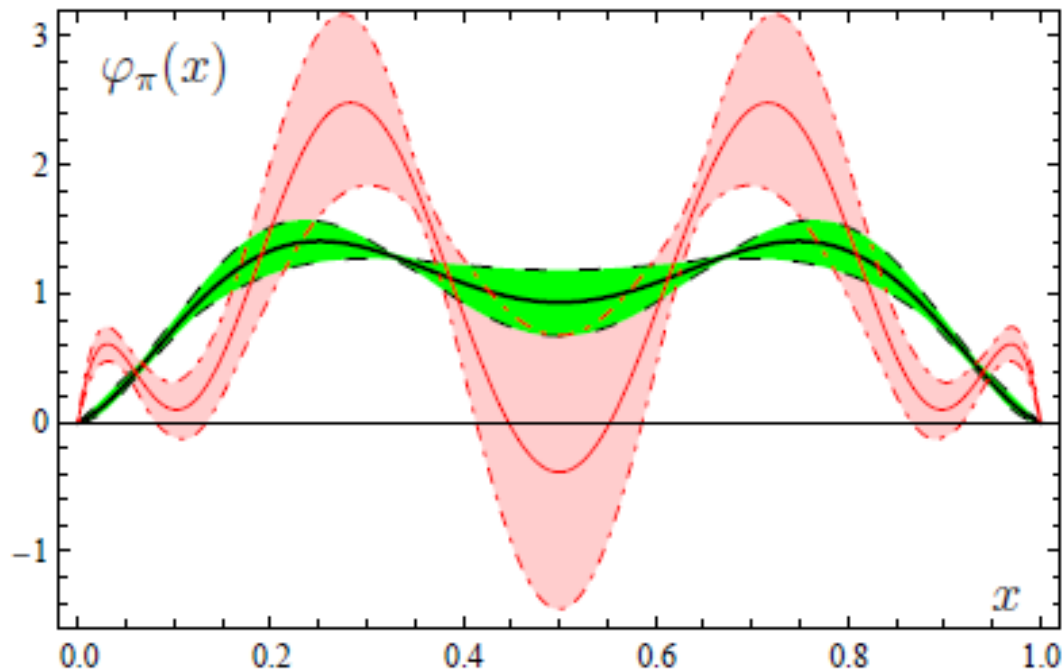


Pion DA

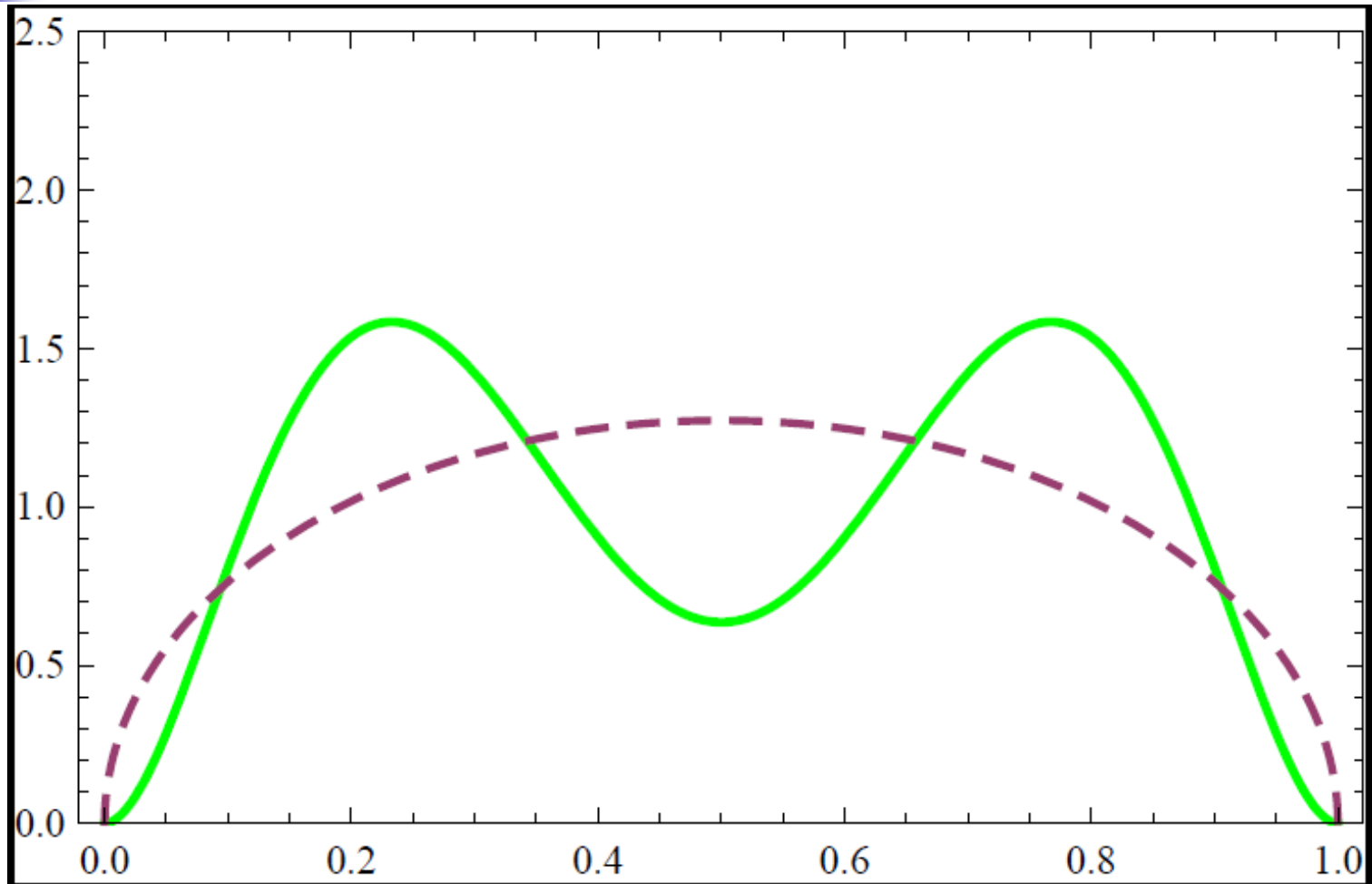
- Element of **ERBL** factorization
- Describes probability amplitude for the (anti) quark carrying given light-cone momentum fraction
- Interest recently increased due to BaBar data for pion-photon transition formfactor-simplest exclusive process

Pion DA

- (Conservative) model of Bakulev, Mikhailov, Stefanis vs (3D) fit



Comparison to holographic model



Angular distributions – probes of DA

■ Unpolarized

$$F = \int_0^1 dy \frac{\varphi(y, \tilde{Q}^2)}{y},$$

$$I(\tilde{x}) = \int_0^1 dy \frac{\varphi(y, \tilde{Q}^2)}{y(y + \tilde{x} - 1 + i\epsilon)}$$

$$\tilde{x}(x_L, \rho) \equiv \frac{x_L + \sqrt{x_L^2 + 4(1 + \rho^2)\tau}}{2(1 + \rho^2)}.$$

$$\rho \equiv Q_T/Q.$$

$$x_L = 2Q_L/\sqrt{s} < 1:$$

■ Polarized

$$\lambda(\tilde{x}, \rho) = \frac{2}{N} \{ (1 - \tilde{x})^2 [(\text{Im}I(\tilde{x}))^2 + (F + \text{Re}I(\tilde{x}))^2] - (4 - \rho^2)\rho^2\tilde{x}^2F^2 \}, \quad (2.19)$$

$$\mu(\tilde{x}, \rho) = -\frac{4}{N} \rho \tilde{x} F \{ (1 - \tilde{x}) [F + \text{Re}I(\tilde{x})] + \rho^2 \tilde{x} F \}, \quad (2.20)$$

$$\nu(\tilde{x}, \rho) = -\frac{8}{N} \rho^2 \tilde{x} (1 - \tilde{x}) F [F + \text{Re}I(\tilde{x})], \quad (2.21)$$

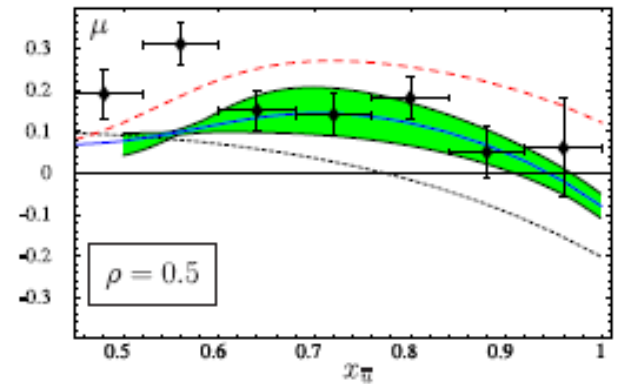
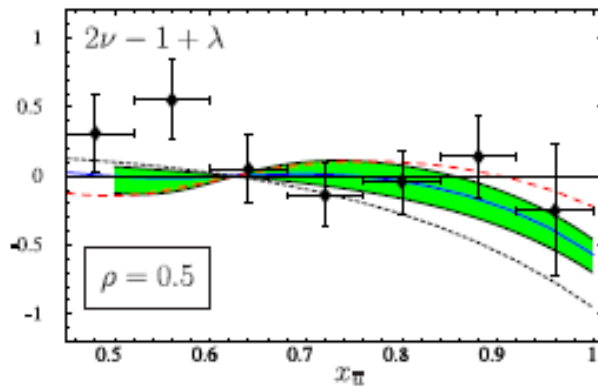
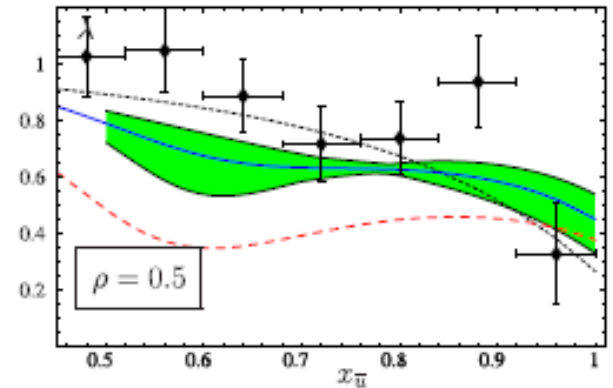
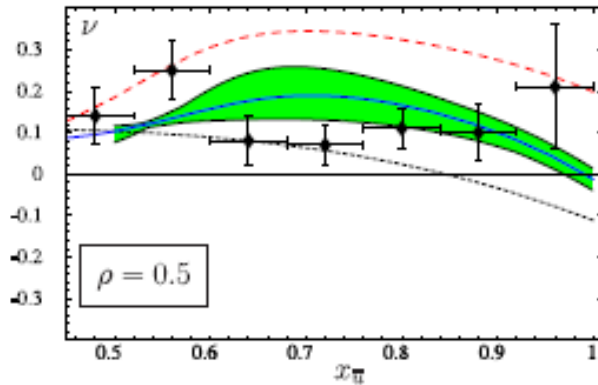
$$N(\tilde{x}, \rho) = 2 \{ (1 - \tilde{x})^2 [(\text{Im}I(\tilde{x}))^2 + (F + \text{Re}I(\tilde{x}))^2] + (4 + \rho^2)\rho^2\tilde{x}^2F^2 \} \quad (2.22)$$

$$\bar{\mu}(\tilde{x}, \rho) = \frac{-2\pi s_e \rho \tilde{x} F \varphi(\tilde{x}, \tilde{Q}^2)}{(1 - \tilde{x})^2 [(F + \text{Re}I(\tilde{x}))^2 + \pi^2 \varphi(\tilde{x})^2] + (4 + \rho^2)\rho^2\tilde{x}^2F^2} \bar{\mu}_{\text{nucl}},$$

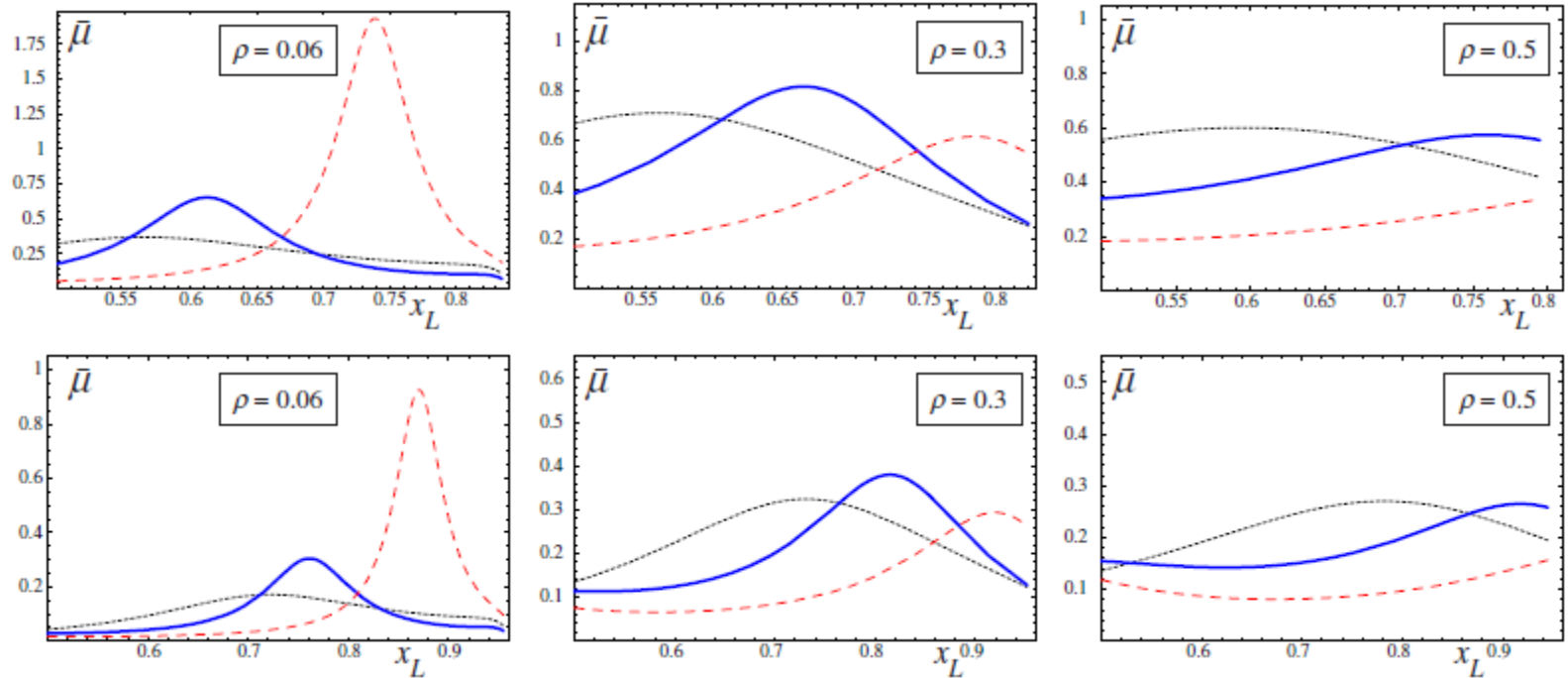
$$\bar{\mu}_{\text{nucl}} \equiv \frac{\frac{4}{9} \Delta q_u^v(x_p; \mu^2) + \frac{4}{9} \Delta q_u^s(x_p; \mu^2) + \frac{1}{9} \Delta q_d^s(x_p; \mu^2)}{\frac{4}{9} q_u^v(x_p; \mu^2) + \frac{4}{9} q_u^s(x_p; \mu^2) + \frac{1}{9} q_d^s(x_p; \mu^2)},$$

$$\bar{\nu}(\tilde{x}, \rho) = 2\rho \bar{\mu}(\tilde{x}, \rho),$$

Asymmetries vs data

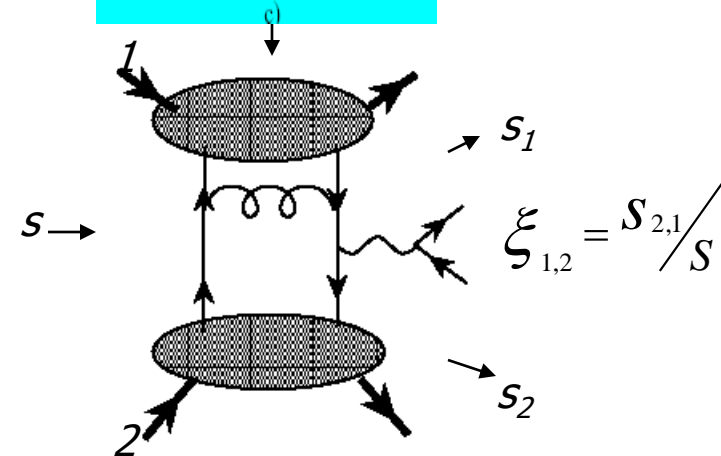
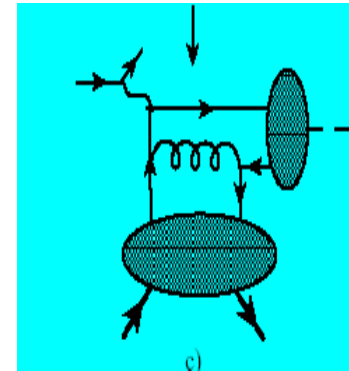
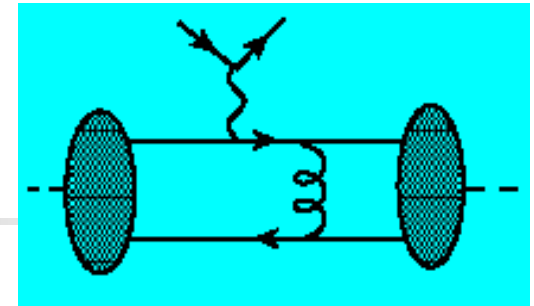


Polarization -> scanning of DA



From semi- to pure exclusive

- Simplest case - pion FF(ERBL)
- Change DA to GPD-exclusive electroproduction (talks of Delia, Nicole, Volker)
- Time from right to left-exclusive DY (DAXGPD)-Pire, Szymanowski
- Second DA->GPD-another mechanism- OT'05 (problems with factorization -analytic continuation to be performed)





Properties of exclusive DY

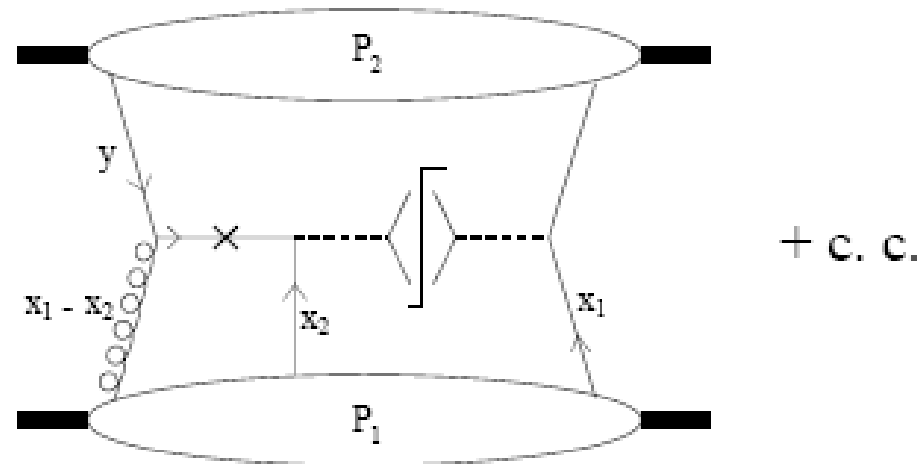
- Polarization T- \rightarrow L
- Difference in sign between imaginary parts of electroproduction and DY- \rightarrow exclusive analog of famous Sivers function sign change
- Final proton is not mandatory – small missing mass (cf Hoyer et al) \sim at rest for fixed target-possible at COMPASS (talk of O.Denisov)
- PP(NICA): TDA p- \rightarrow pp (to be compared with p- \rightarrow D)
- Test of scaling in various momenta
- Estimates for COMPASS $\sim 10^3$ events
- Exclusive limit with antiproton beam – relation to time-like FF's

SSA in DY

- TM integrated DY with one transverse polarized beam – unique SSA – gluonic pole (Hammon, Schaefer, OT) – “factor 2” problem

$$A = g \frac{\sin 2\theta \cos \phi \left[T(x, x) - x \frac{dT(x, x)}{dx} \right]}{M [1 + \cos^2 \theta] q(x)}$$

- Positivity: twist 4 in denominator required



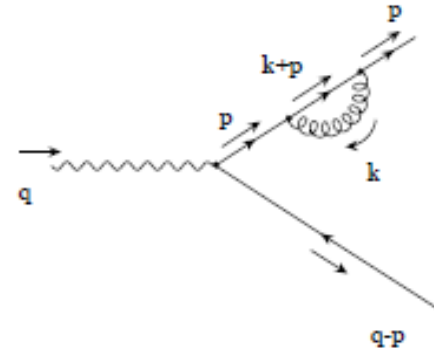
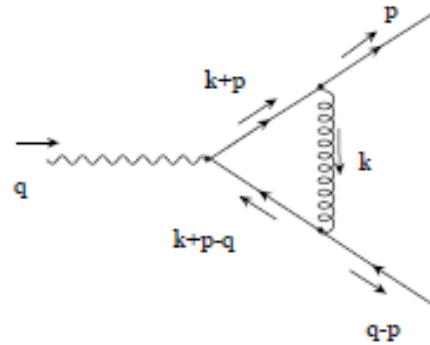
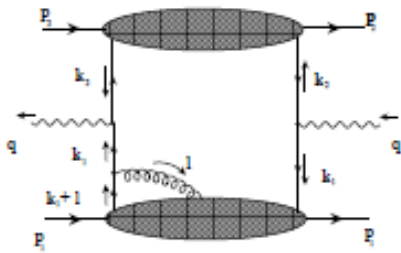
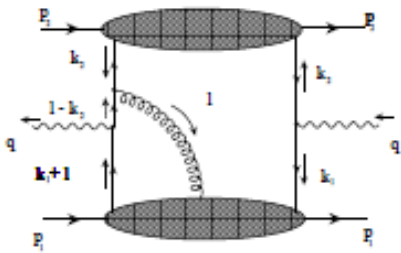
Contour gauge in DY:

(Anikin, OT [arXiv:1003.1482](https://arxiv.org/abs/1003.1482) and PLB)

- Motivation of contour gauge – $[-\infty^-, 0^-] = 1$
elimination of link $[-\infty^-, 0^-] = P \exp \left\{ -ig \int_{-\infty}^0 dz^- A^+(0, z^-, \vec{0}_T) \right\}$
- Appearance of infinity – mirror diagrams subtracted rather than added
- Field $A^\mu(z) = \int_{-\infty}^{\infty} d\omega^- \theta(z^- - \omega^-) G^{+\mu}(\omega^-) + A^\mu(-\infty)$
- Gluonic pole appearance $B^V(x_1, x_2) = \frac{T(x_1, x_2)}{x_1 - x_2 + i\epsilon}$
- cf naïve expectation $B^V(x_1, x_2) = \frac{\mathcal{P}}{x_1 - x_2} T(x_1, x_2)$
- Source of phase?!

Phases without cuts

- EM GI (experience from a_2 DV/CS) — 2 contributions



- Cf PI — only one of two diagrams contribute to SSA and required for GI
- NP tw3 analog - GI only if GP absent
- **GI** with GP — “phase without cut”



Analogs/implications

- Analogous pole – in gluon GPD
- Prescription – also process-dependent: 2-jet diffractive production (Braun et al.)
- Analogous diagram for GI – Boer, Qiu(04)
- Our work besides consistency proof – factor **2** for asymmetry (missed before)
- GI $Z_\mu = \hat{p}_{1\mu} - \hat{p}_{2\mu} \quad (zq)=0$
- Naïve $\hat{p}_{1\mu} \implies \hat{p}_{1\mu} - q_\mu \frac{\hat{p} \cdot q}{Q^2} = \frac{p_{1\mu} - p_{2\mu}}{2}$.
- But! Metz&Zhou 2- \rightarrow 1/2 (“factor of 2 puzzle” in addition to sign puzzle)

Sivers function and formfactors



- Relation between Sivers function and AMM known on the level of matrix elements (Brodsky, Schmidt, Burkardt)
- Phase?
- Duality for observables?



BG/DYW type duality for DY SSA in exclusive limit

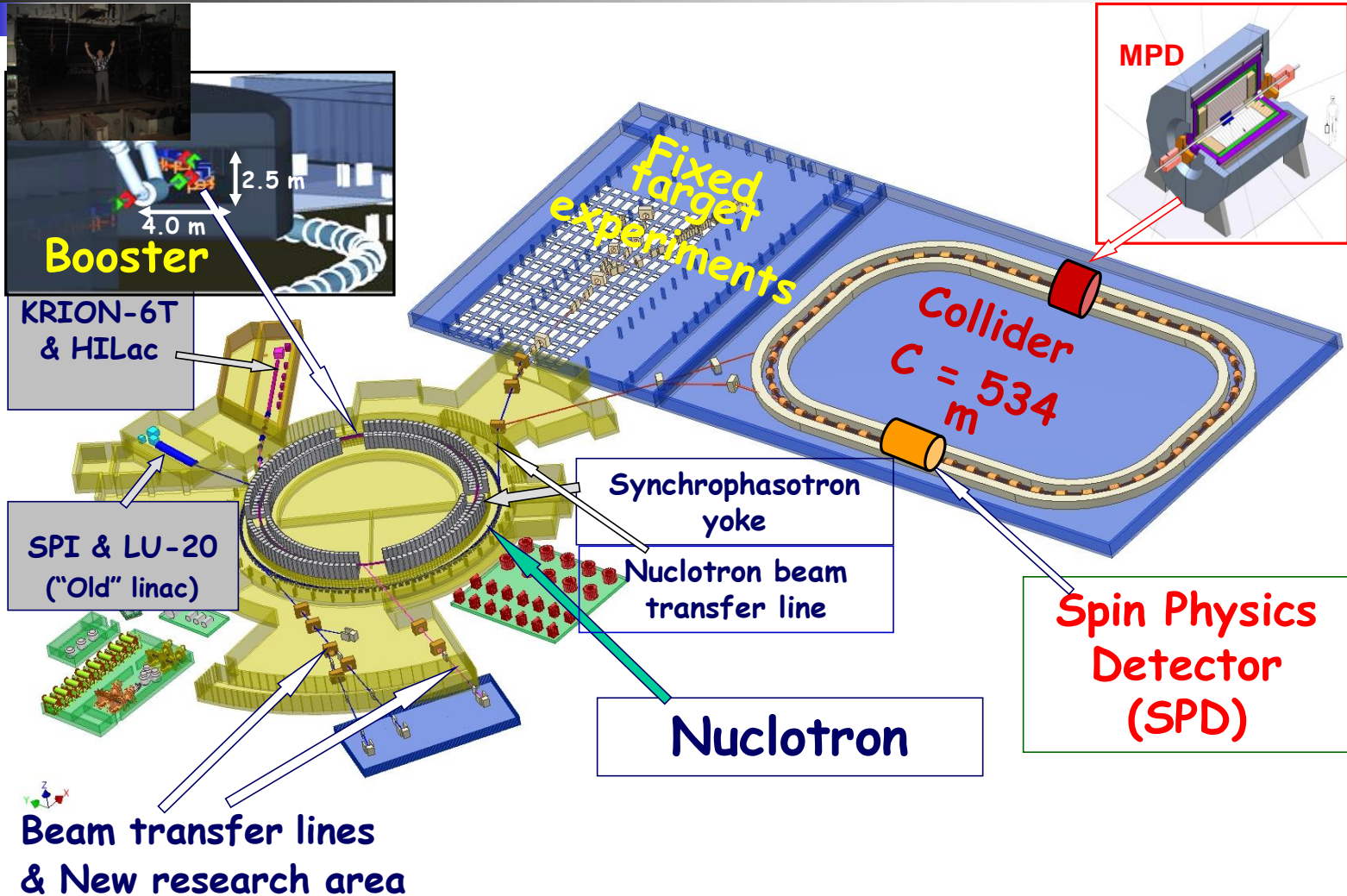
- Proton-antiproton DY – valence annihilation - cross section is described by Dirac FF squared
- The same SSA due to interference of Dirac and Pauli FF's with a phase shift (Rekalo, Brodsky)
- Exclusive large energy limit; $x \rightarrow 1$:
 $T(x,x)/q(x) \rightarrow \text{Im } F_2/F_1$
- Both directions – estimate of Sivers at large x and explanation of phases in FF's

The goal of the NICA project is construction at JINR of the new accelerator facility that consists of

- cryogenic heavy ion source,
- source of polarized protons and deuterons,
- "old" linac LU-20,
- a new heavy ion linear accelerator,
- a new Booster-synchrotron,
- the existing proton synchrotron Nuclotron, upgraded to Nuclotron-M,
- two new superconducting storage rings of the collider,
- new set of transfer channels.

<http://nica.jinr.ru>

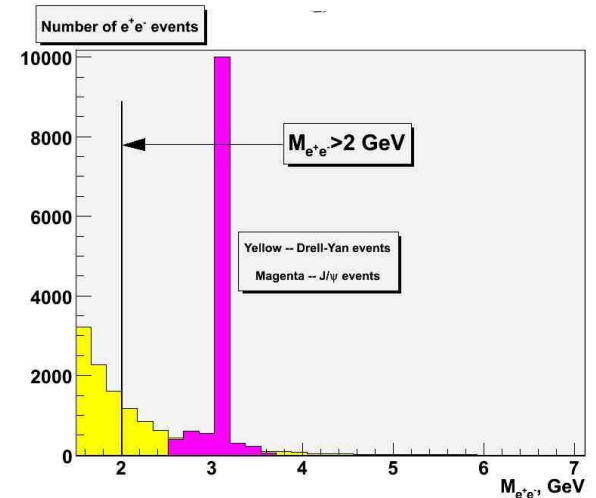
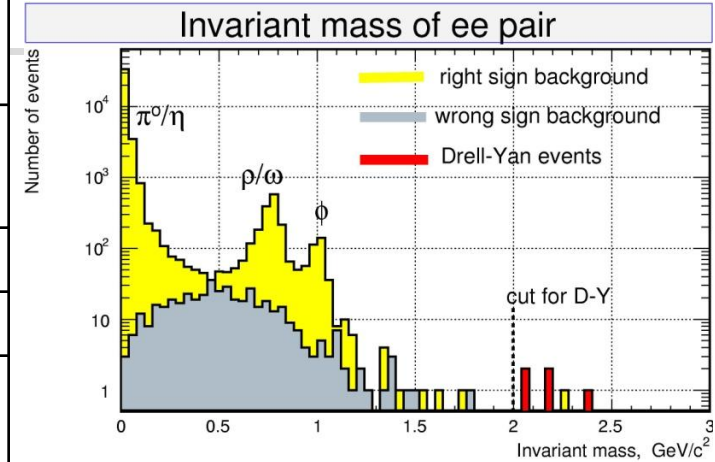
NICA@JINR (slides by A. Nagaytsev)



Spin Physics at NICA. Proposed measurements

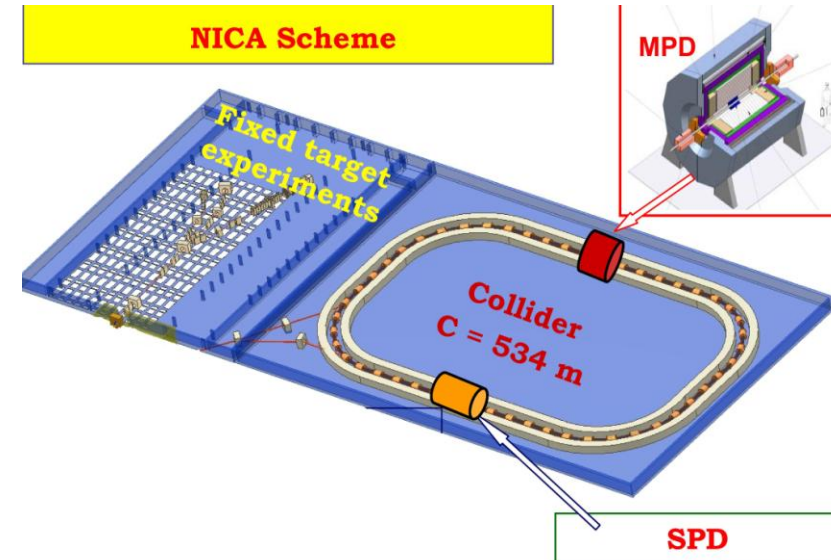
Estimations were done for 1 month of data taking.
For 6 years of data taking: we expect to take ~100K DY events

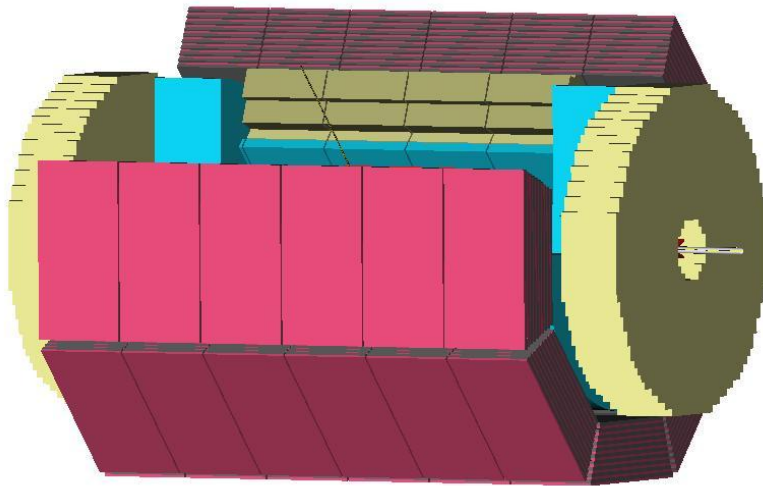
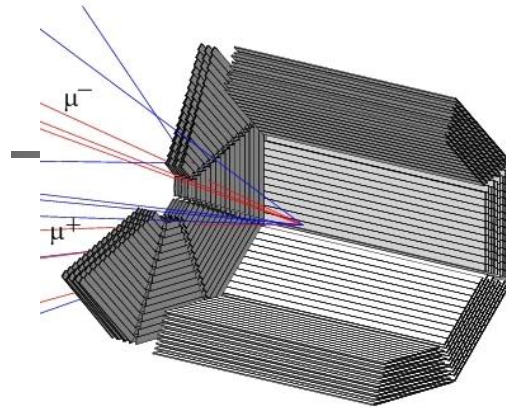
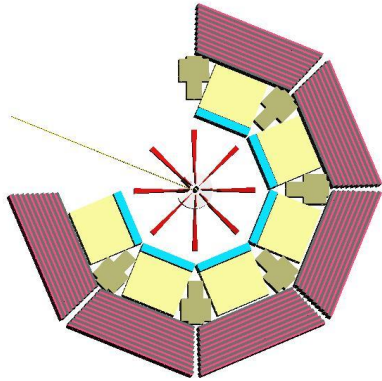
	σ_{DY} , total, nb		L , $\text{cm}^{-2}\text{s}^{-1}$				K events		
PAX, $\sqrt{s}=14.6$ GeV	2		10^{30}				~10		
NICA, $\sqrt{s}=20$ GeV	1.3		10^{30}				5		
NICA, $\sqrt{s}=26$ GeV	1.3		10^{30}				7		
Cut on Q, GeV	1.5	1.6	1.7	1.8	1.9	2.0			
NICA, $\sqrt{s}=20$ GeV									
σ_{DY} , total, nb	2.5	1.9	1.6	1.3	1.1	0.9			
# per month (in K)	14	11	9	7	6	5			
NICA, $\sqrt{s}=26$ GeV									
σ_{DY} , total, nb	3.3	2.7	2.3	1.9	1.6	1.3			
# per month (in K)	18	15	13	10	9	7			
PAX, $\sqrt{s}=14.6$ GeV									
σ_{DY} , total, nb	5.1	4.3	3.5	2.9	2.5	2.1			
# per month (in K)	24	21	17	14	12	10			
\sqrt{s} , GeV	20	26	\sqrt{s} , GeV			20	26		
$\sigma_{J/\psi}$, $B_{\mu\mu}$, nb	10	16	σ_{DY} , nb			0.9	1.3		
# per month (in K)	55	88	# per month (in K)			5	7		



Important requirements for detector (SPD) :

- 1) 4π geometry
- 2) Precision vertex reconstruction
- 3) Advanced tracking system
- 4) Good angular resolution – very important for azimuthal spin asymmetries measurements in the wide kinematical region
- 5) Particle identification



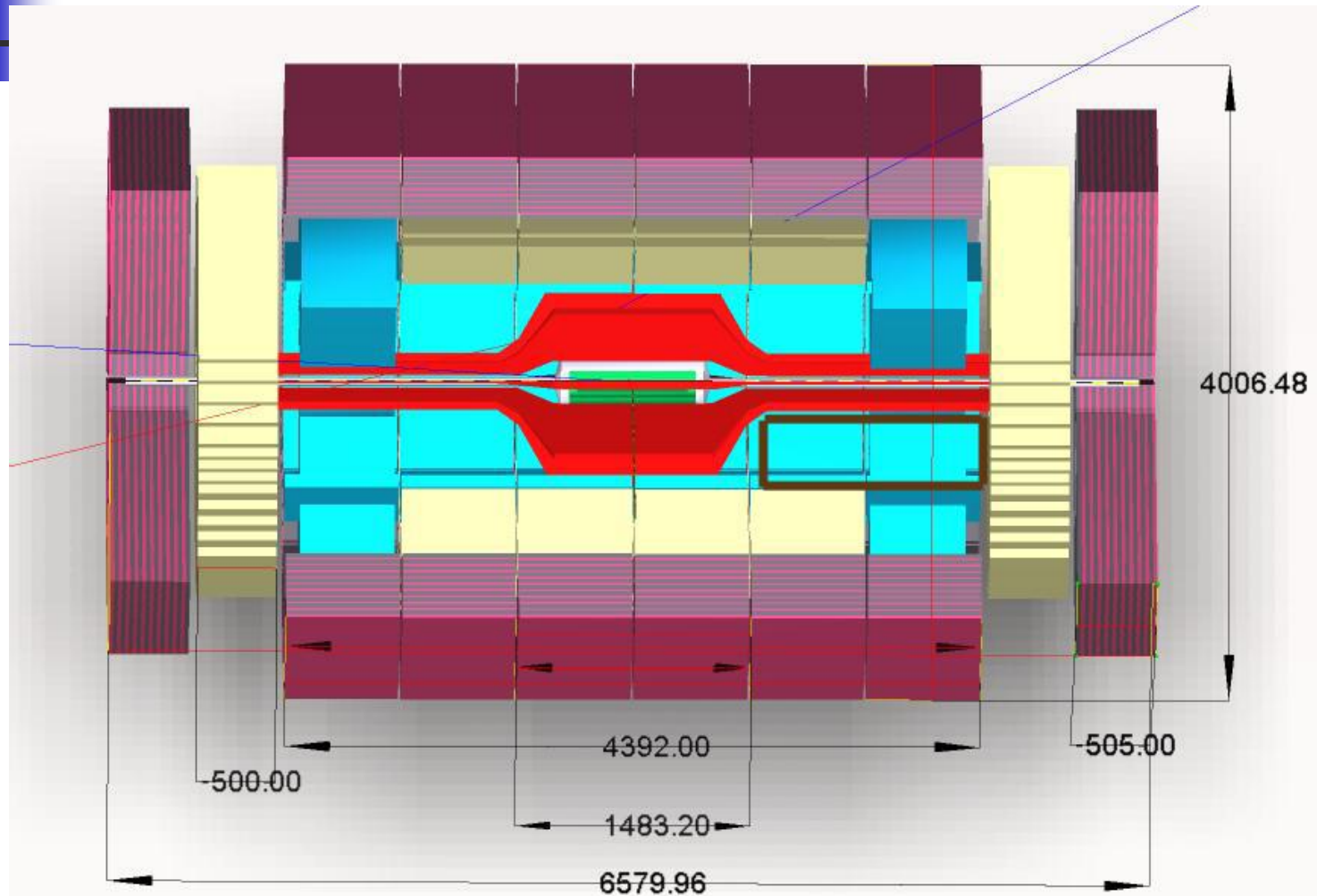


SPD Barell is about 1.9 m in radius
SPD lenght is about 5 m

Preliminary scheme of the SPD:

- Toroid magnet system
 - about 60 cm in radius
- Silicon or MicroMega (Vertex)
- Drift chambers (DC)
- EM Calorimeter (EMC)
 - inner radius is about 80 cm
 - outer radius is about 130 cm
- Range System (RS)
 - (PANDA Moun System, JINR contrib.)
 - inner radius is about 130 cm
 - outer radius is about 180 cm
- Trigger counters
- EndCap detectors with RS, tracking system and EMC

SPD



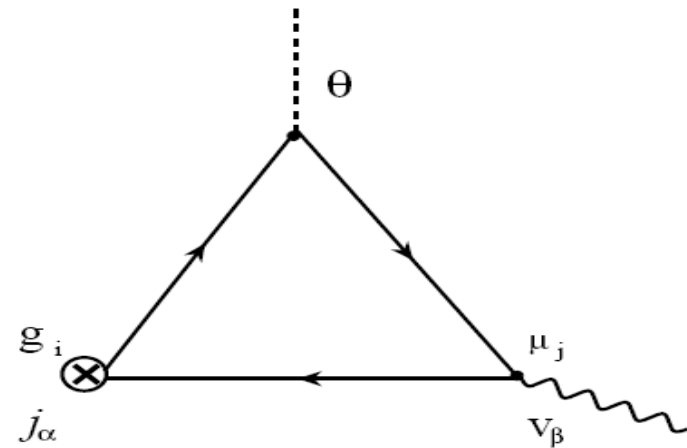


Spin physics at MPD

- Multi Purpose Detector – studies of heavy-ion collisions
- Possible to use also with p/D beams
- Spin-related studies (exclusive, exotics, spin-dependent DY with associated particles)
- Spin effects in HIC – vorticity
- In-between nucleon OAM (talks of Masashi, Elliot, Matthias, Cedric) and classical rotation

Anomaly in medium – new external lines in VVA graph

- Gauge field \rightarrow velocity
- Chiral Vortical Effect
- Kharzeev, Zhitnitsky (07) – EM current
- Straightforward generalization: any (e.g. baryonic) current – neutron asymmetries@NICA - Rogachevsky, Sorin, OT - **Phys.Rev.C82:054910,2010.**





Baryon charge with neutrons – (Generalized) Chiral Vortical Effect

- Coupling: $e_j A_\alpha J^\alpha \Rightarrow \mu_j V_\alpha J^\alpha$

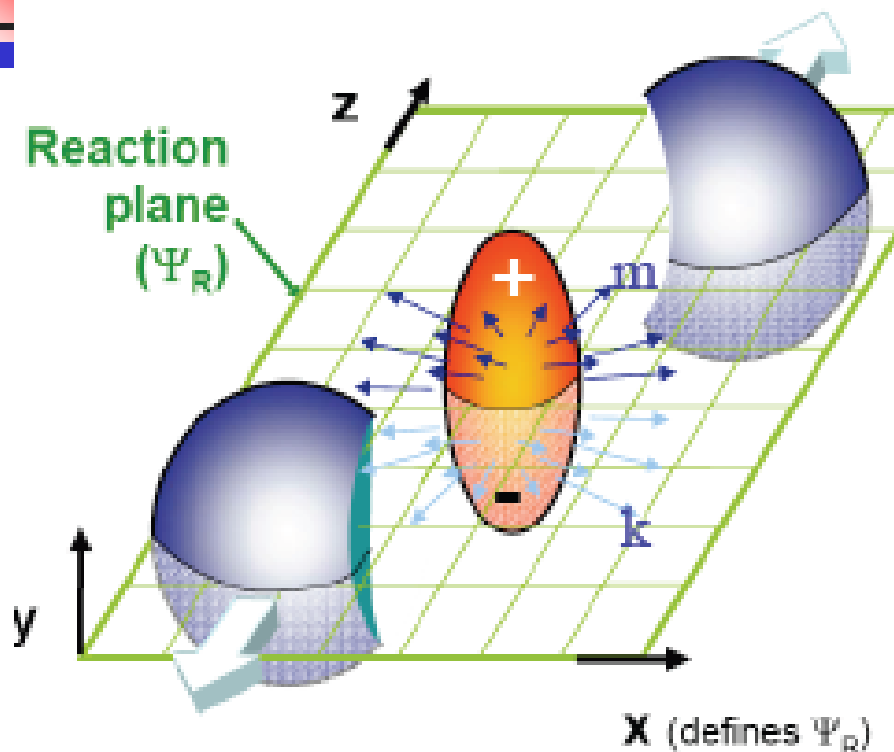
- Current: $J_e^\gamma = \frac{N_c}{4\pi^2 N_f} \varepsilon^{\gamma\beta\alpha\rho} \partial_\alpha V_\rho \partial_\beta (\theta \sum_j e_j \mu_j)$

- - Uniform chemical potentials: $J_i^\nu = \frac{\sum_j g_{i(j)} \mu_j}{\sum_j e_j \mu_j} J_e^\nu$

- - Rapidly (and similarly) changing chemical potentials:

$$J_i^0 = \frac{|\vec{\nabla} \sum_j g_{i(j)} \mu_j|}{|\vec{\nabla} \sum_j e_j \mu_j|} J_e^0$$

Charge asymmetry w.r.t. reaction plane: how to detect it?



$$\begin{aligned} \langle \cos(\phi_\alpha + \phi_\beta - 2\Psi_{RP}) \rangle &= \\ &= \langle \cos \Delta\phi_\alpha \cos \Delta\phi_\beta \rangle - \langle \sin \Delta\phi_\alpha \sin \Delta\phi_\beta \rangle \\ &= [\langle v_{1,\alpha} v_{1,\beta} \rangle + B^{in}] - [\langle a_\alpha a_\beta \rangle + B^{out}], \end{aligned}$$

S.Voloshin, hep-ph/0406311

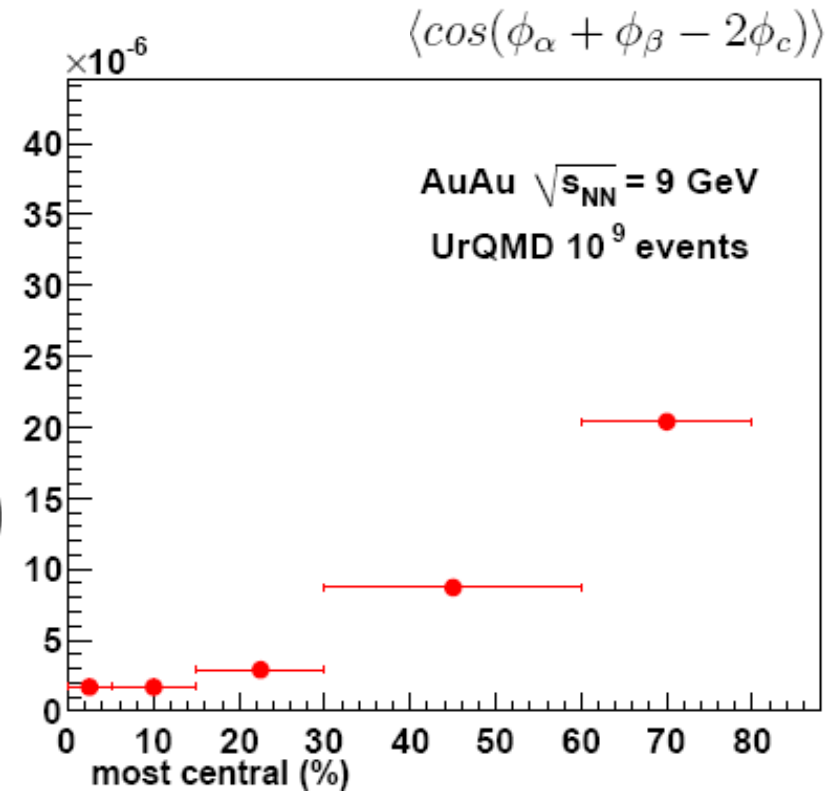
A sensitive measure
of the asymmetry:

$$a^k a^m = \left\langle \sum_{ij} \sin(\varphi_i^k - \Psi_R) \sin(\varphi_j^m - \Psi_R) \right\rangle$$

Expect $a^+ a^+ = a^- a^- > 0$; $a^+ a^- < 0$

Estimates of statistical accuracy at NICA MPD (months of running)

- UrQMD model : $Au + Au$ at $\sqrt{s_{NN}} = 9$ GeV
- 2-particles \rightarrow 3-particles correlations
no necessity to fix the event plane
- 2 neutrons from mid-rapidity ($|\eta| < 1$)
- +1 from ZDC ($|\eta| > 3$)



New sources of Λ polarization coupling to rotation

- Bilinear effect of vorticity – generates quark axial current (Son, Surowka)
- Strange quarks - should lead to Λ polarization
- Proportional to square of chemical potential – small at RHIC – may be probed at FAIR & NICA

$$j_A^\mu \sim \mu^2 \left(1 - \frac{2 \mu \pi}{3 (\epsilon + P)} \right) \epsilon^{\mu\nu\lambda\rho} V_\nu \partial_\lambda V_\rho$$



Conclusions

- (Semi)exclusive limits of DY – interesting theoretically
- Feasibility at various experiments remains to be studied
- NICA@JINR has a possibility studies of various spin physics in hadronic and HIC
- New suggestions welcomed
- Better to see once than to hear 100 times;
WELCOME to SPIN 2012