

Sensing of cryogenic temperatures by superconducting NbTi(N) thin-film S-shaped Split Ring Resonators

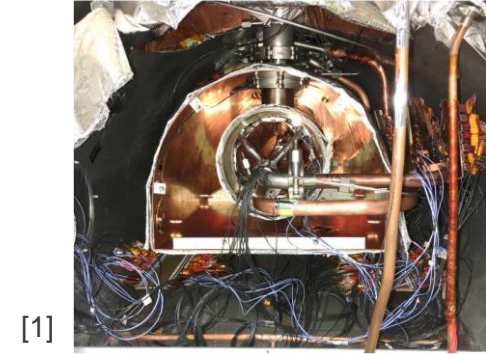
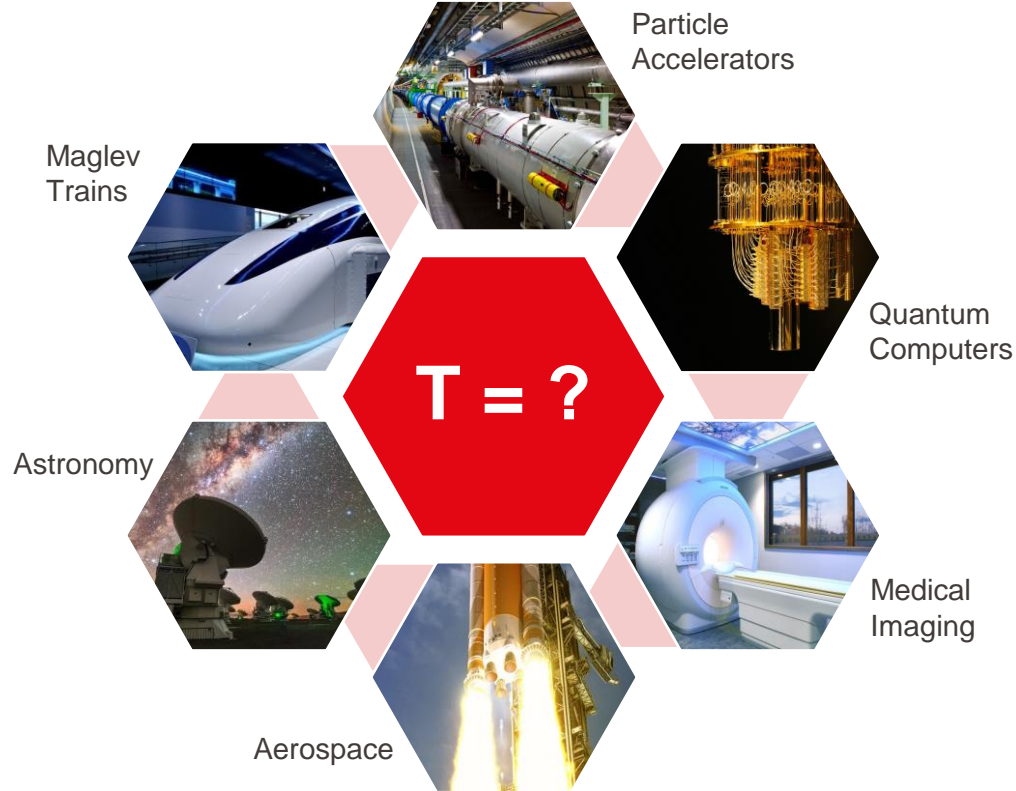
André Chatel, Roberto Russo, Luca Mazzone, Eric Richter, Reza Farsi, Jürgen Brugger, Giovanni Boero and Hernán Furci

 ICEC/ICMC

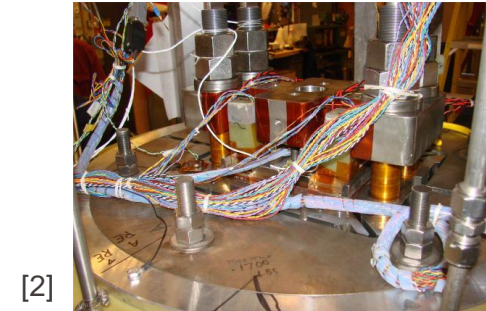
29th International Cryogenic Engineering Conference
International Cryogenic Materials Conference 2024

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Thermometry for Cryogenic Systems

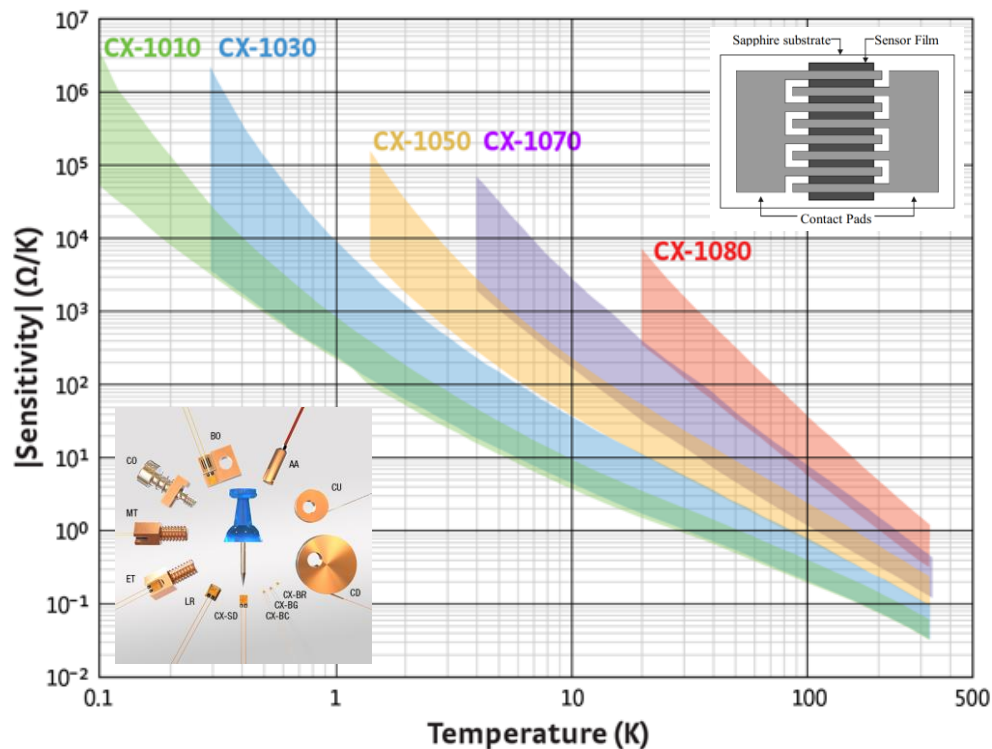


- Many wiring issues when dealing with mult-stages cryogenic environments...



[1] Courtesy of P. Borges de Sousa CERN, TE CRG CI
 [2] M. Turqueti et al., *Physics Procedia* 67 (2015)

- Cryogenic thermometry mainly achieved by **2 and 4-wires thermistors**
- **CERNOX®** thermometers [3-4]:
 - effective over wide T-ranges
 - $\Delta T = 0.1 - 320$ K
 - good sensitivity
 - $dR/dT > 10^3 \Omega/K$ for $T < 1$ K
 - mechanically robust
 - small and compact
 - insensitive to magnetic field
- **Main issues:**
 - need of 2/4 DC wires for each sensor \rightarrow feedthrough budget
 - non-linearity
 - heat conduction paths
 - wiring complexity

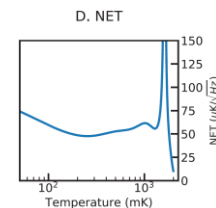
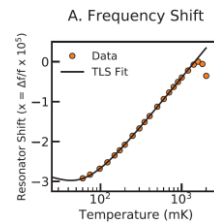
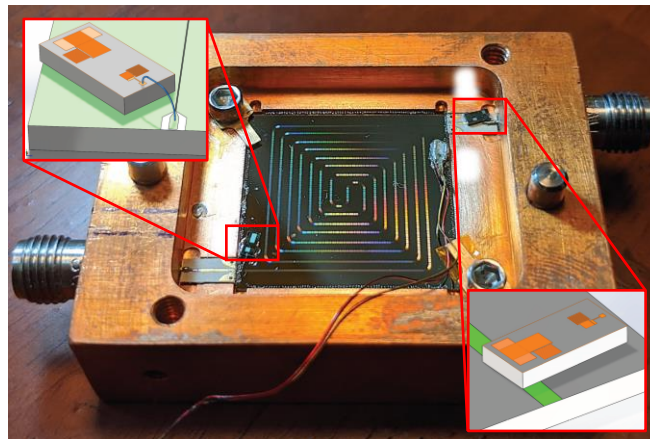
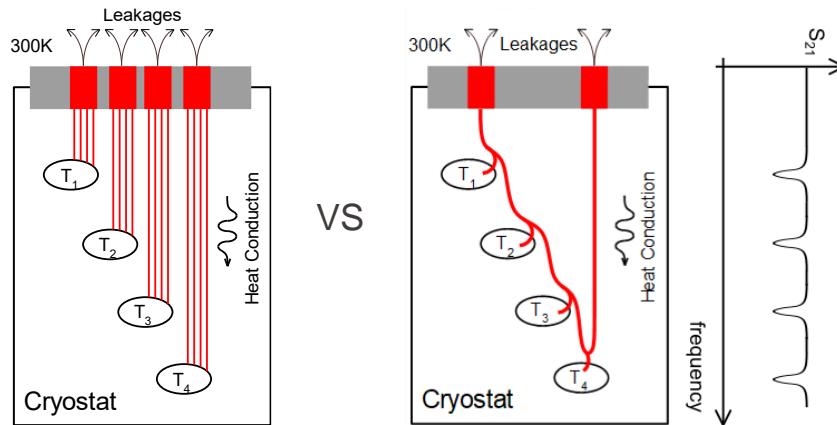


[3] <https://www.lakeshore.com/products/categories/overview/temperature-products/cryogenic-temperature-sensors/cernox>

[4] S. S. Courts et al., *AIP Conference Proceedings* 684 (2003)

RF Superconducting Thermometry

- **Multiplexing is possible in frequency domain** with temperature sensitive resonating systems
- **RF superconducting resonators** in GHz range can deliver:
 - $> 10^4$ Q-factors
 - sub-mK resolution
 - single-line parallel readout of several sensors
 - small and compact dimensions
- Several alternative approaches based on different physical phenomena
- 2 GHz Nb lumped elements thin film resonators exploiting **Two-Levels Systems (TLSs)** [5]
- For $T < 1$ K:
 - $Q > 35^4$
 - $\Delta f_{\max} = 60$ kHz
 - NET $< 100 \mu\text{K}/\text{Hz}^{1/2}$

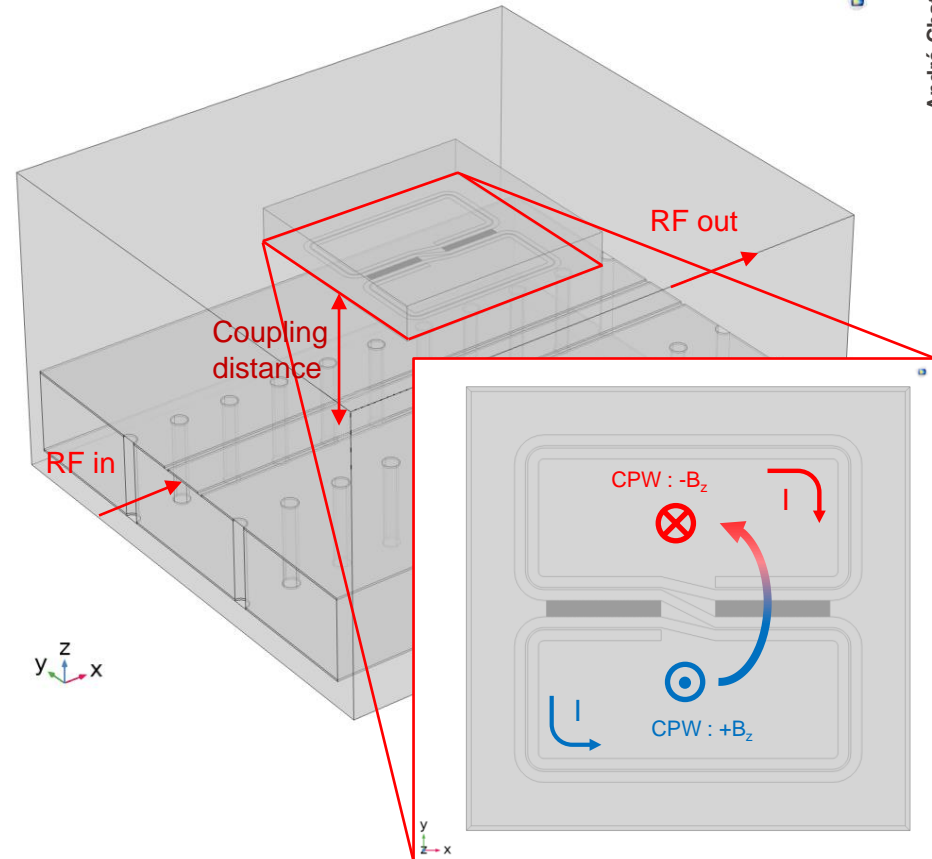


[5] J. Wheeler et al., *Appl. Phys. Lett.* 117 (2020)

S-shaped Split Ring Resonator (S-SRR)

- Temperature monitored through variations of the thin film **kinetic inductance** $L_K(T)$
 - kinetic/inductive energy of Cooper pairs

$$\frac{1}{2}(2m_e v^2)(n_S(T)lA) = \frac{1}{2}L_K I^2$$
 - $$L_K(T) = \left(\frac{m_e}{2n_S(T)e^2}\right)\left(\frac{l}{A}\right)$$
 - $$f_{res}(T) = \frac{1}{2\pi\sqrt{(L_G+L_K(T))\cdot C_G}}$$
- Antisymmetric S-SRRs geometry for optimal electromagnetic proximity coupling** with standard Cu CPWs [6-7]
- Devices designed to resonate ~ 1 GHz



[6] F. Aznar et al., *AIP Journal of Applied Physics* 104 (2008)

[7] A. K. Horestani et al., *IEEE Ant. and Wir. Prop. Lett.* 13 (2014)

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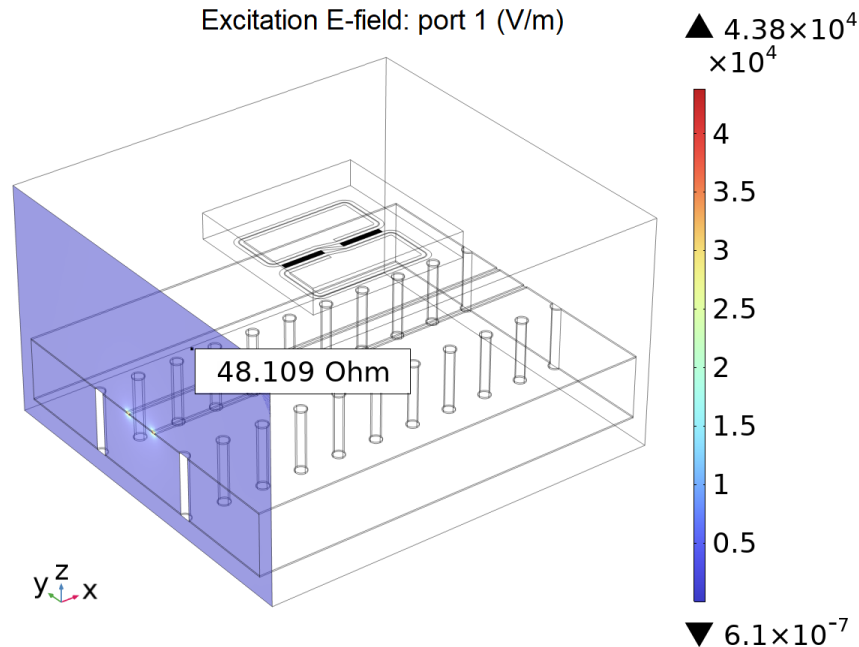
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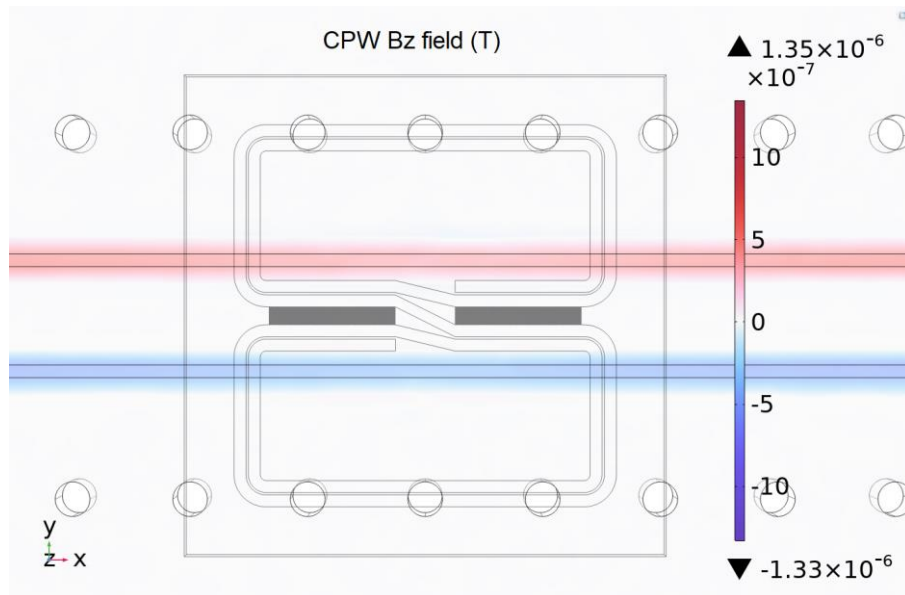
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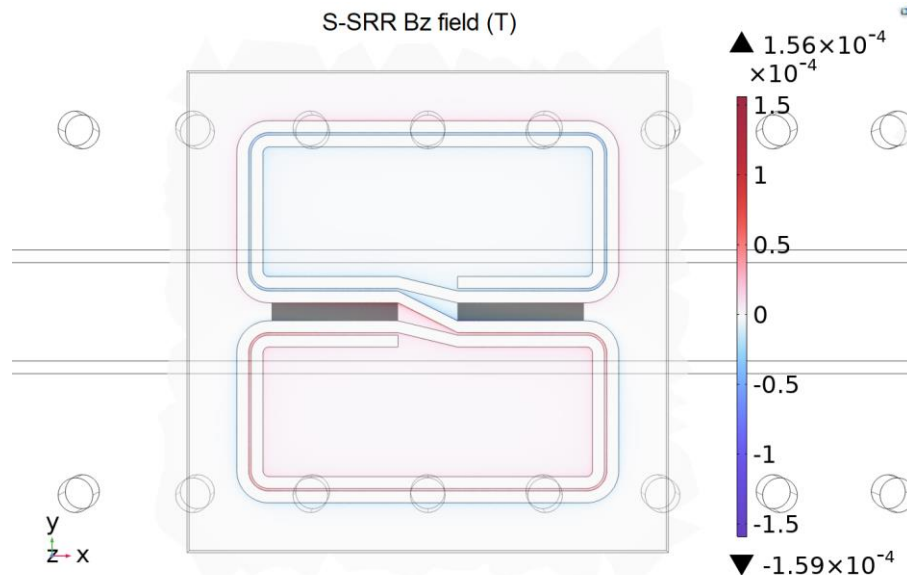
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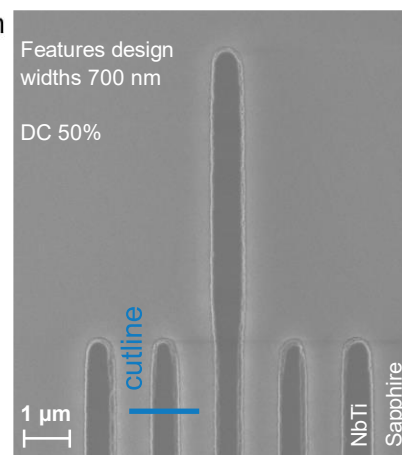
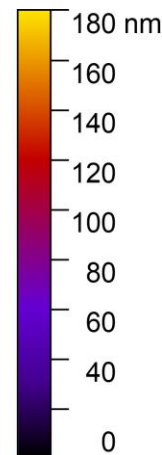
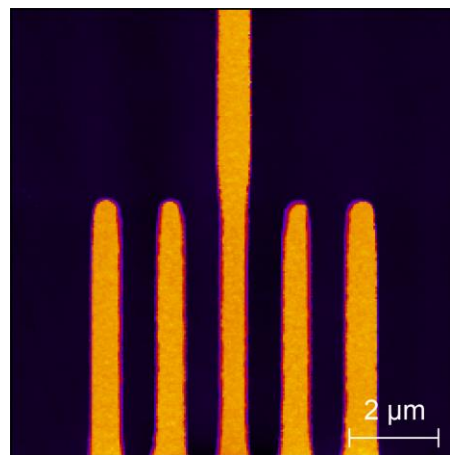
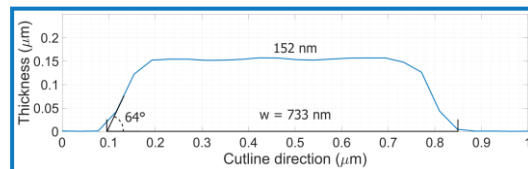
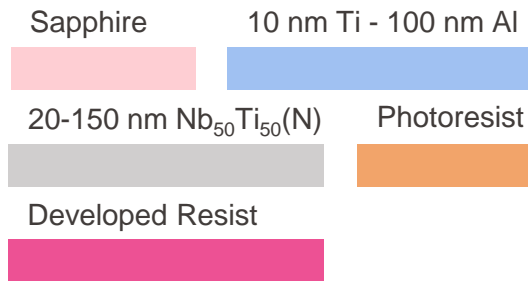
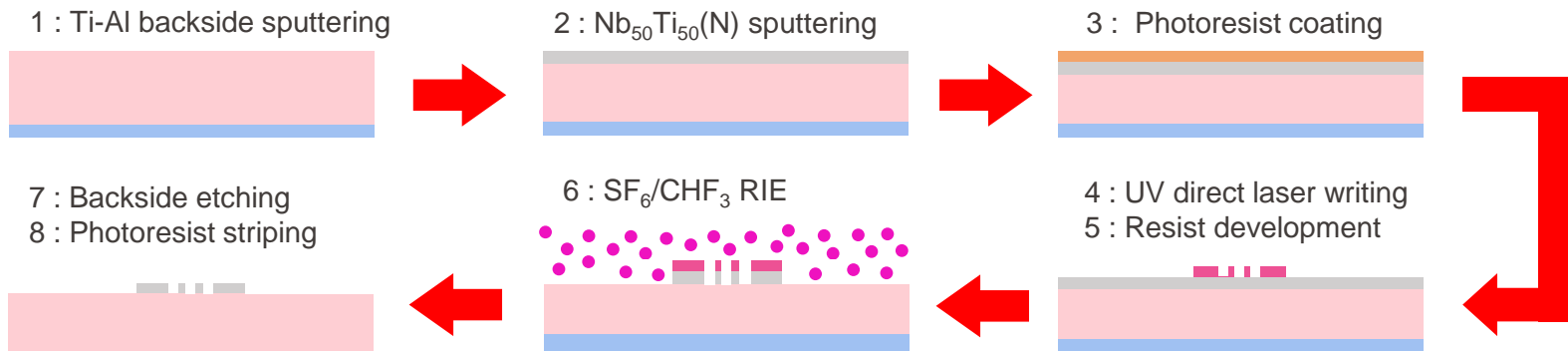
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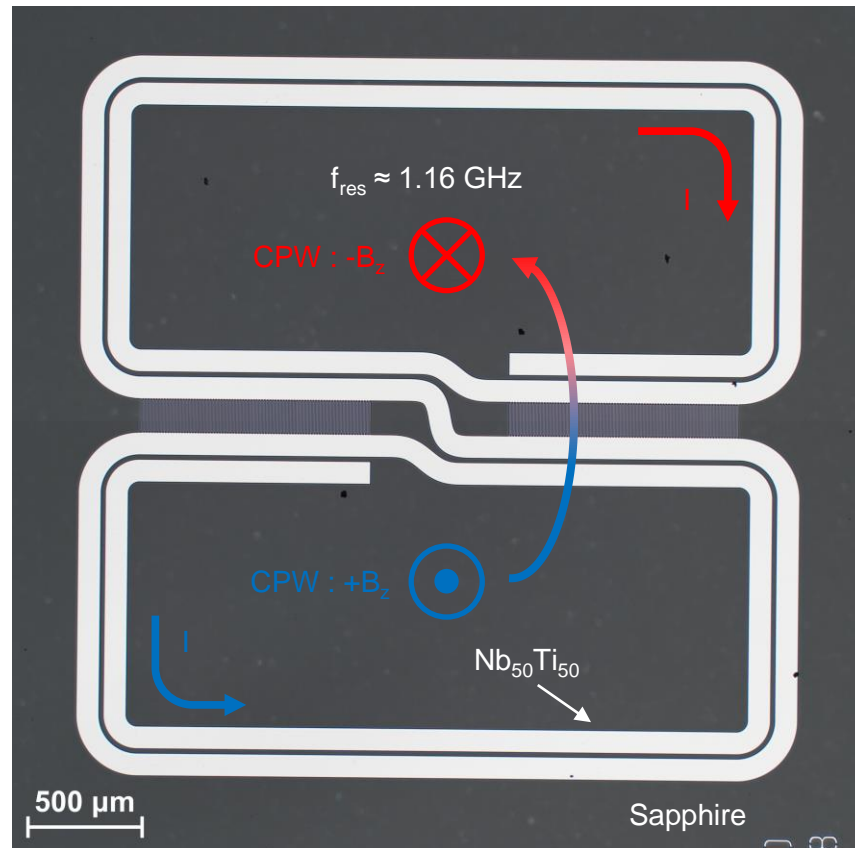
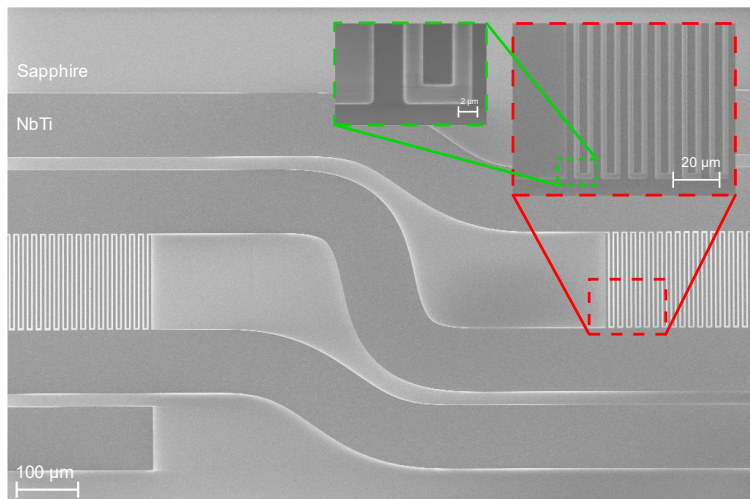
[7] A. K. Horestani et al., *IEEE Ant. and Wir. Prop. Lett.* 13 (2014)

NbTi(N)-over-Sapphire Microfabrication



- 100 μm wide **loop-inductance** lines
- 4 μm wide and 2 μm spaced **interdigitated fingers capacitance**
 - lower resonance frequency \rightarrow lower RF losses
 - keeping the sensor compact

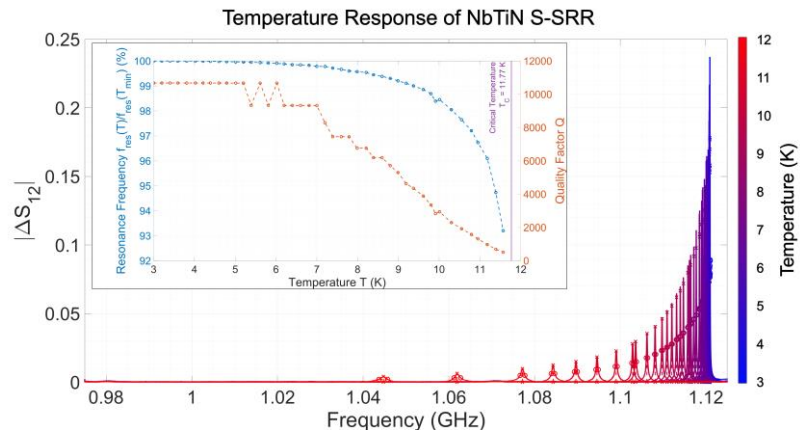
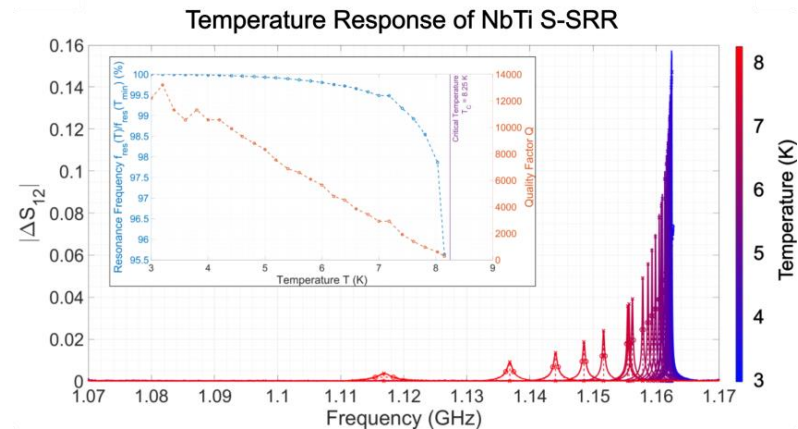
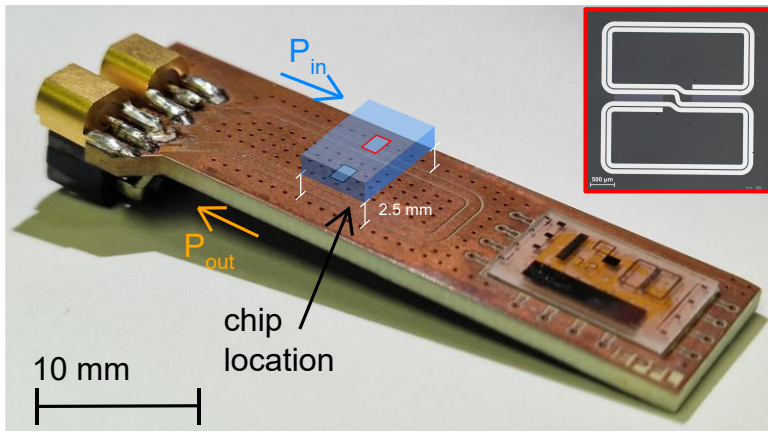
$$f_{\text{res}}(T) = \frac{1}{2\pi\sqrt{L \cdot C_G}}$$



Temperature Responses

- 100 nm thin S-SRRs tested in the **VTI of a closed loop dry cryomagnet** at 0 T magnetic field
- 18 dBm excitation power

	NbTi	NbTiN
f_{res} (3 K)	1.16 GHz	1.12 GHz
$\Delta f_{\text{MAX}}\%$	4.5% (~ 53 MHz)	7% (~ 78 MHz)
T_C	8.3 K	11.8 K
Q_{MAX}	> 13'000	> 11'000



Estimation of NET

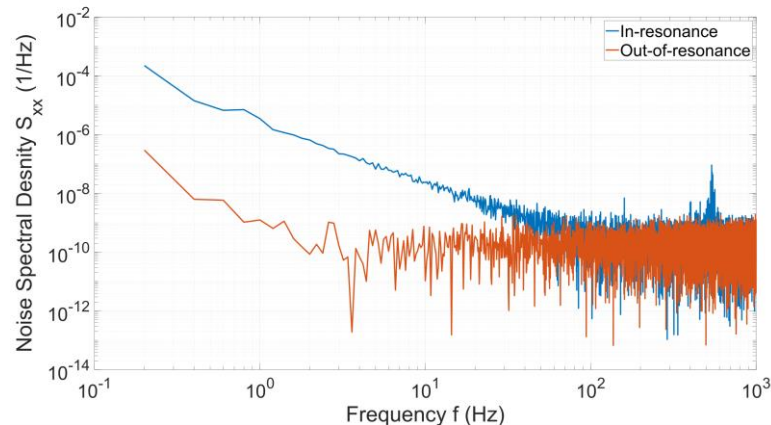
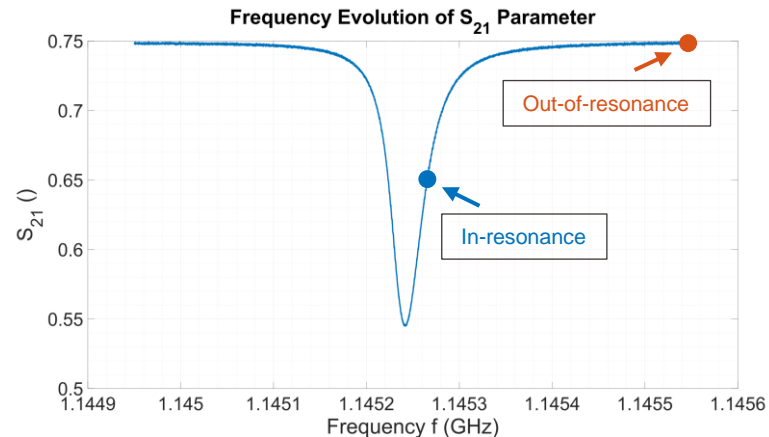
- Ultimate **S-SRR T-resolution** can be estimated by analyzing 2 physical parameters:
 - noise spectral density** $\rightarrow S_{xx}$
 - device responsivity** $\rightarrow \frac{dS_{21}}{dT}$
- Experiments performed for a NbTi 150 nm thin S-SRR:
 - @ 3 K (minimum reachable VT I T)
 - @ 0 T B-field
 - @ -18 dBm RF excitation power
 - CW mode scanning for 5 s at 2 kHz rate

$$\frac{df_0}{dT} \approx \frac{\Delta f_0}{\Delta T} = \dots = 0.66 \frac{\text{MHz}}{\text{K}}$$

$$\frac{dS_{21}}{df} \approx \frac{\Delta S_{21}}{\Delta f} = \dots = 4.29 \frac{1}{\text{MHz}}$$

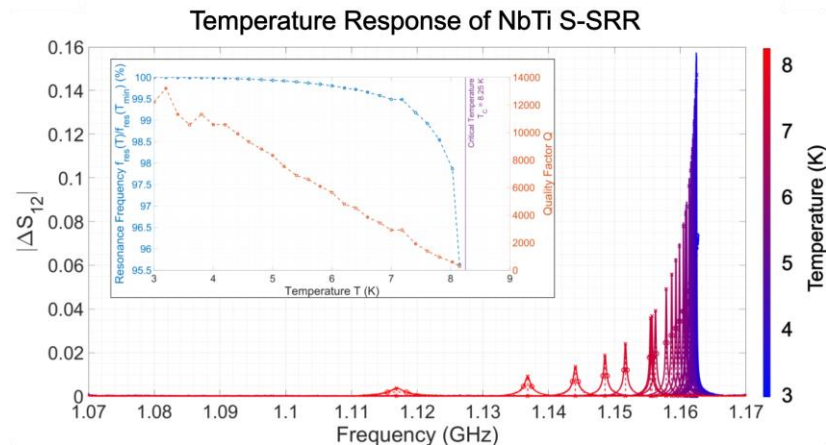
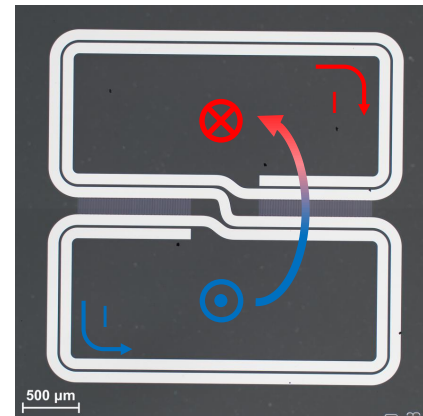
$$S_{xx}(1 \text{ Hz}) \approx 3.48 \times 10^{-6} \frac{1}{\text{Hz}}$$

$$\text{NET}(1 \text{ Hz}) = \frac{\sqrt{S_{xx}(1 \text{ Hz})}}{\frac{dS_{21}}{dT}} \approx \dots \approx 655 \frac{\mu\text{K}}{\sqrt{\text{Hz}}}$$



Conclusions and Future Perspectives

- S-SRR kinetic inductance superconducting thermometer demonstrated:**
 - wire-free cryogenic temperature measurement by EM coupling to an RF line
 - multi-location monitoring possible (frequency range tagging)
- Sensing properties:**
 - high Q-factors $> 10'000$ @ 3 K
 - frequency-shifts as large as 7% from 3 to 12 K
 - sensitivity 0.2 MHz/K @ 3 K
 - resolution < 1 mK/Hz^{1/2} @ 3 K
- Improvements ongoing:**
 - material choices for T-range definition (Al for $T < 1$ K, HTS for $T > 50$ K, etc.)
 - low-T sensitivity increase by surface modification of the thin films



EPFL

CMi EPFL Center of
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**Thank you for the
attention!**

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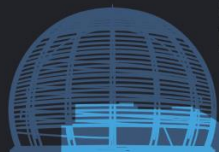
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