

Forward Physics Facility Workshop

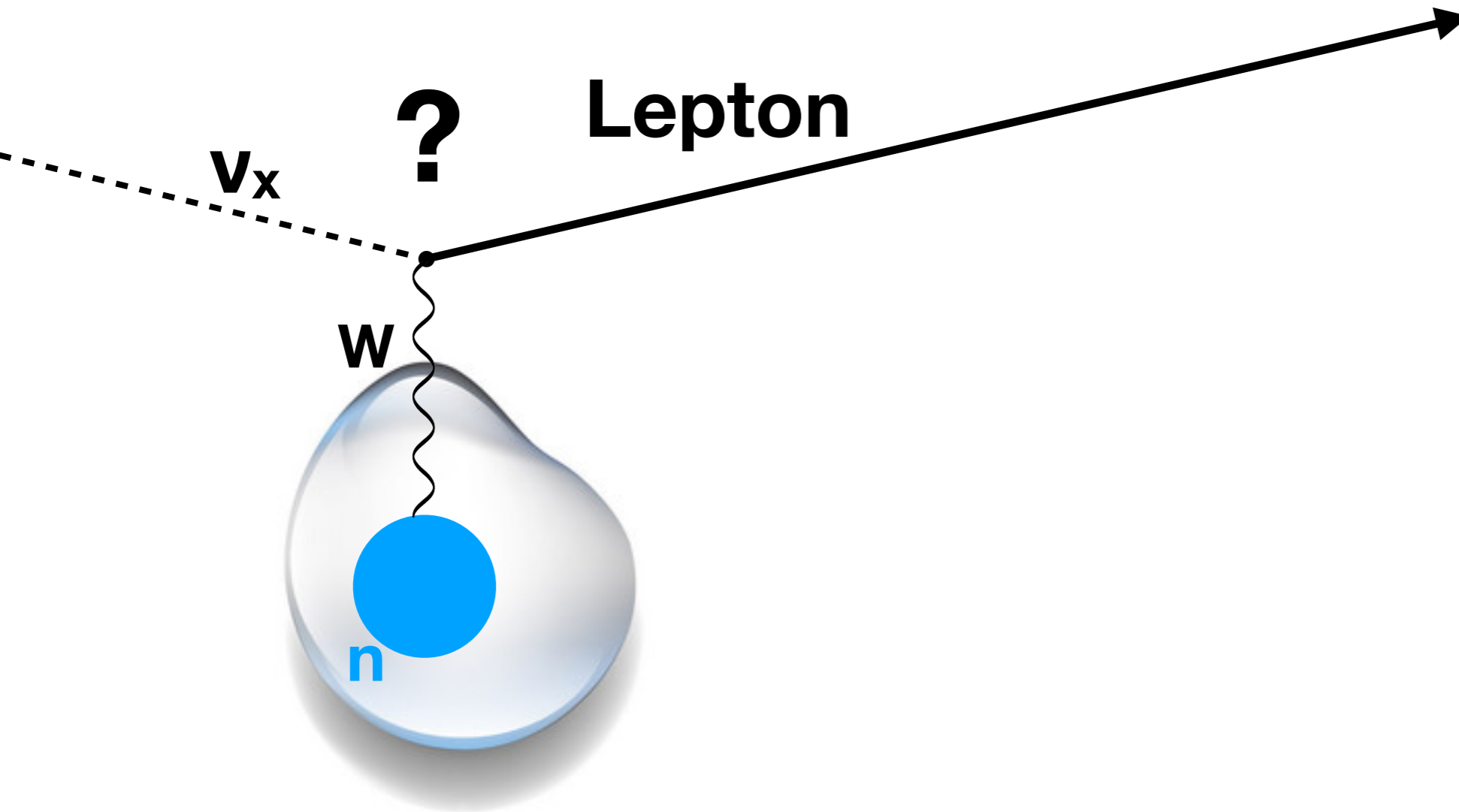
Neutrino Interaction Tools for the FPF



Alfonso Garcia

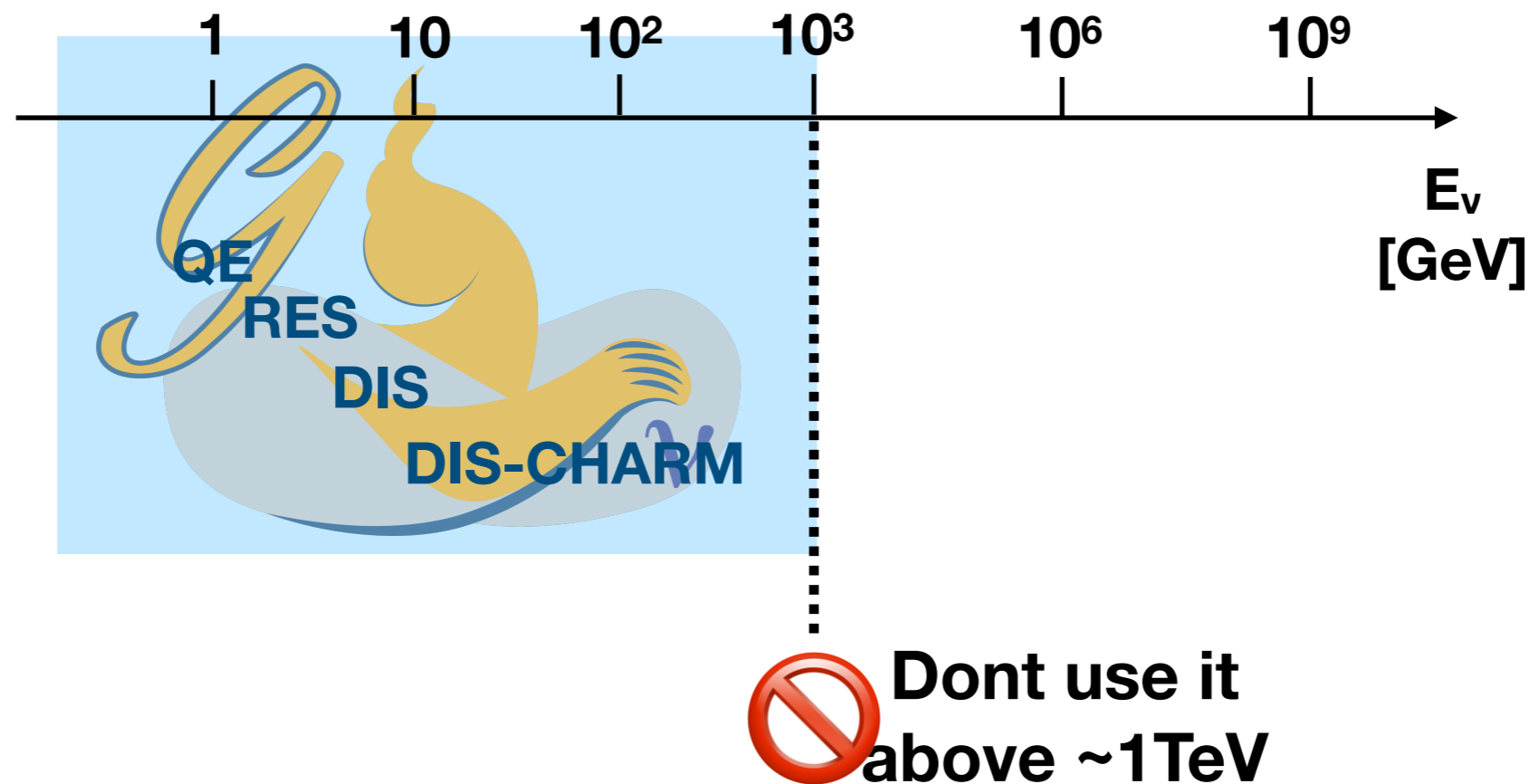
alfonsogarciasoto@fas.harvard.edu

Lepton level



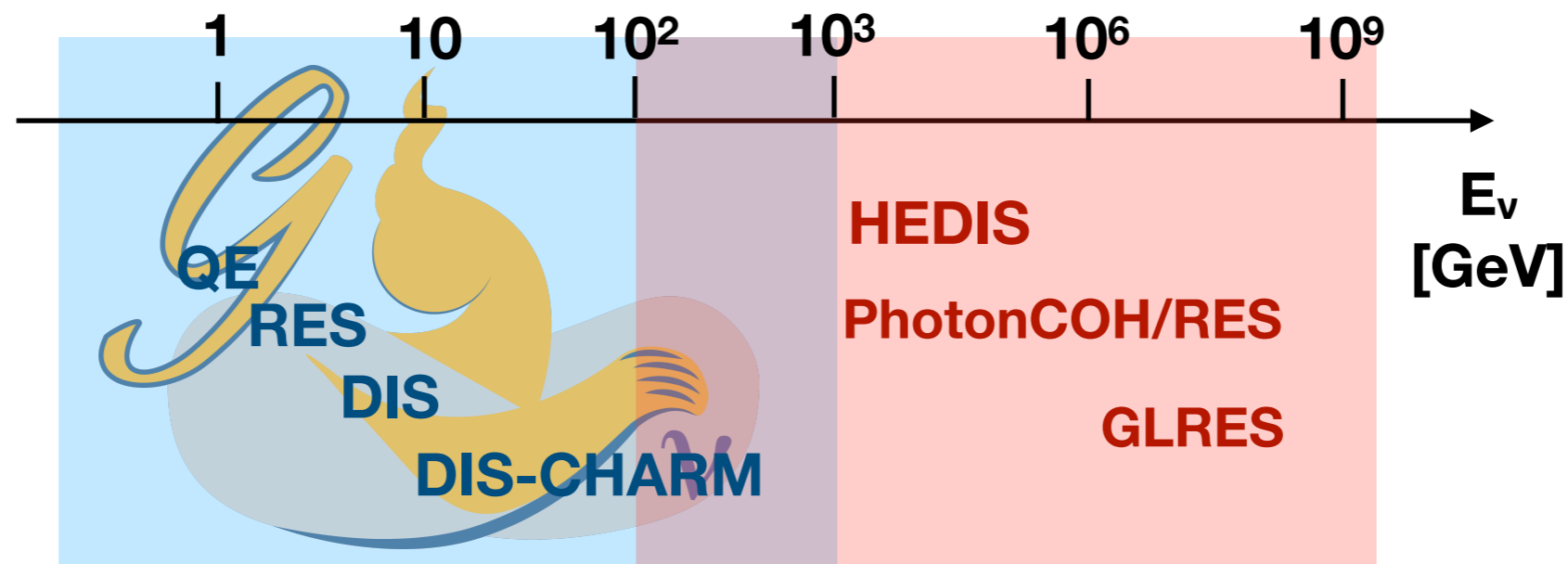
GENIE

- Current status of GENIE in the high energy regime:
 - DIS based on Bodek-Yang model -> optimised for low Q^2 .
 - Structure Function = $C_{ij} \text{LO} \otimes \text{PDF LO (GRV98 } Q^2[0.8, 2 \cdot 10^6])$.
 - Contributions from heavy quarks are not included.



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- New extension allows UHE interaction -> HEDIS
 - Newer PDFs with broader Q^2 phase space.
 - Structure Functions = C_{ij} NLO \otimes PDF NLO.
 - Account for the heavy quark contributions.

$$F_i(x, Q^2) = \sum_j^{\text{qrks,gl}} \int_x^1 \frac{dz}{z} f_j(z, Q^2) C_{i,j}\left(\frac{x}{z}, Q^2\right)$$

Parton Density Functions

- Calculated from fit to hadron data.
- Available sets depend on fitted data and formalism.
- Lookup tables $(x, Q^2) \rightarrow$ LHAPDF

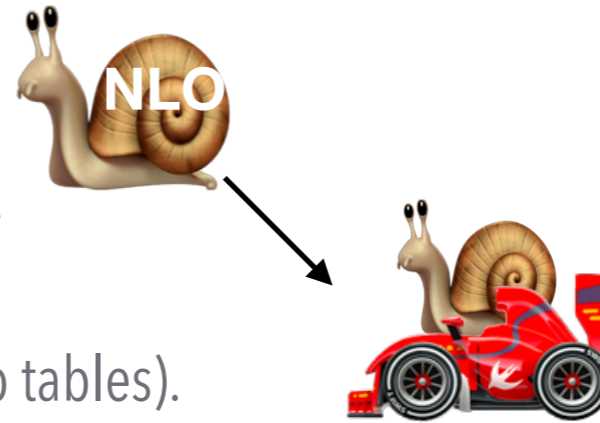
Coefficient functions

- Calculated from Feynman diagrams.
- Depend on order in pQCD.
- Implementation: APFEL.

- Low energy DIS module (Bodek-Yang) use LO Coefficient Functions.
 - Most C_{ij} become zero or delta functions.
 - Structure functions can be computed on the fly \rightarrow fast.
- Moving to NLO requires a new approach to compute Structure Functions.

HEDIS

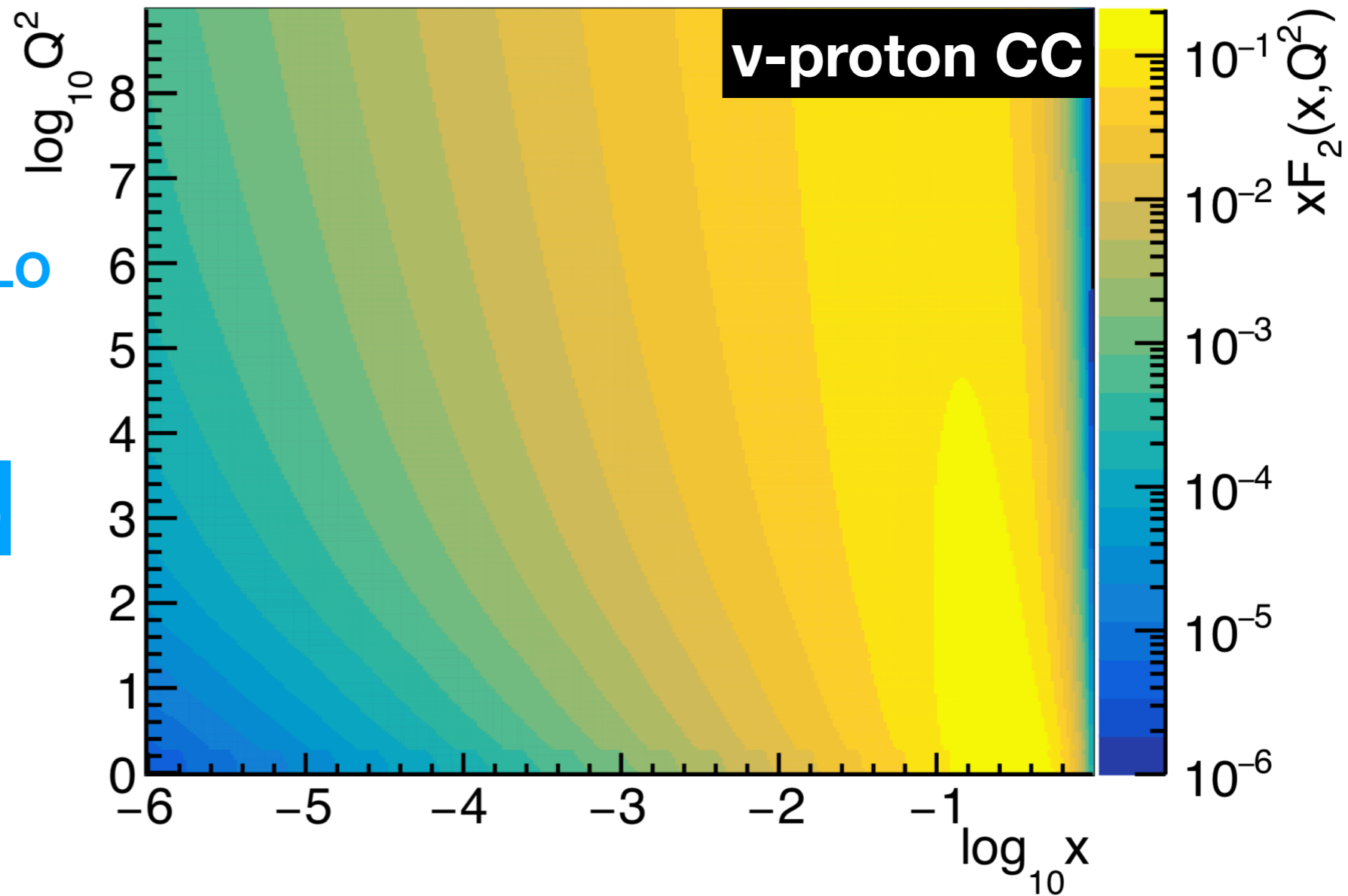
- The key feature:
 - Event generation using NLO Structure Functions!!!
- Solution:
 - Precomputation of the Structure Functions (lookup tables).



$$F_i = C_{ij}[\text{NLO}] \otimes \text{HERAPDF15NLO}$$

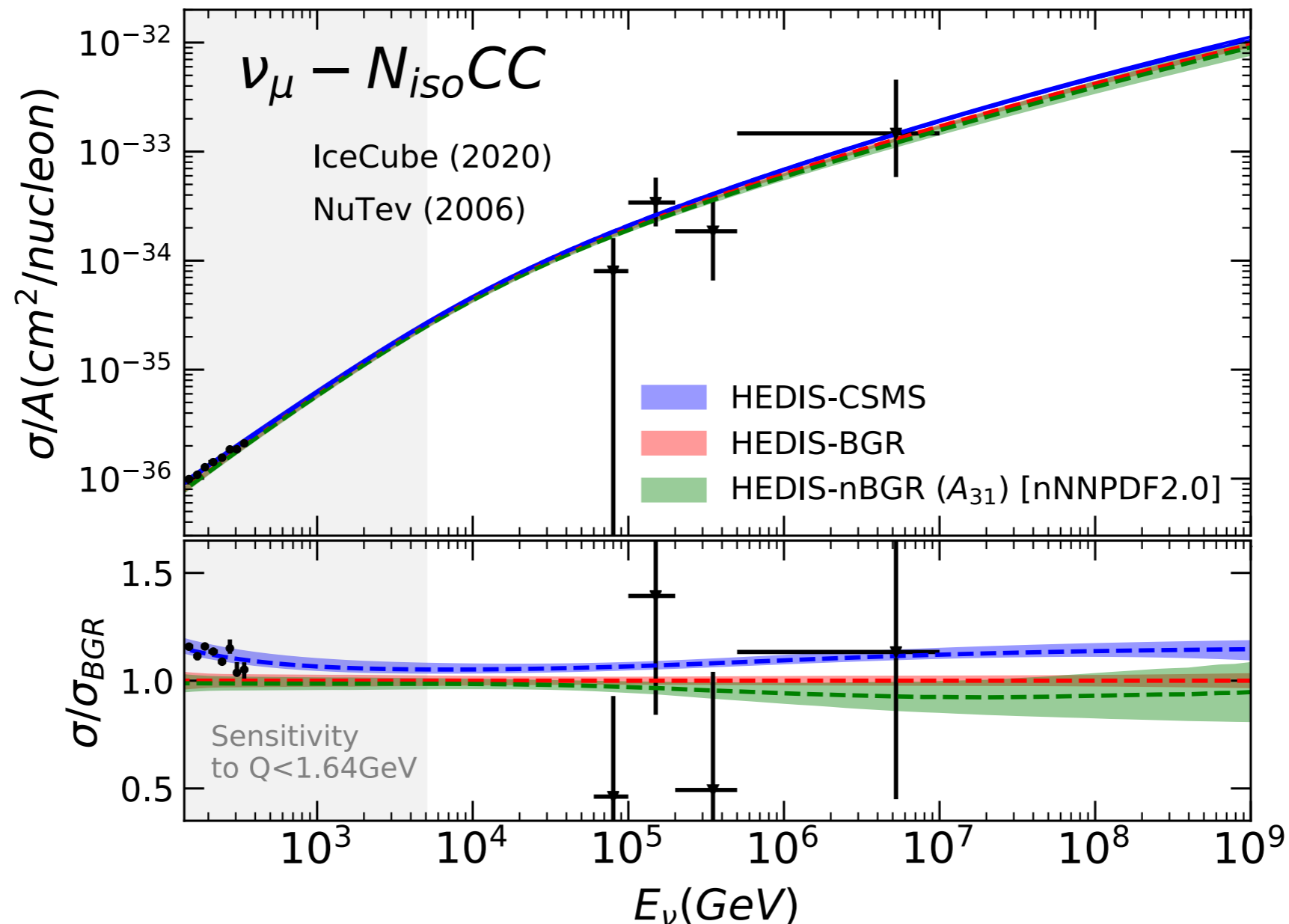
APFEL

LHAPDF6



HEDIS

- Theoreticians showed interested in this package.
- Several experiments will measure neutrino cross sections for $E > 1\text{TeV}$ in this decade.



- Generator develop for MINOS
 - Nuclear effects implemented at kinematical level.
 - Reweighting available for some parameters.

$$\xi_w = \frac{2x(Q^2 + M_f^2 + B)}{Q^2[1 + \sqrt{1 + (2Mx)^2/Q^2}] + 2Ax}$$

A	B	C_{v2d}	C_{v2u}
0.538	0.305	0.255	0.189
C_{sea}^{down}	C_{sea}^{up}	C_{v1d}	C_{v1u}
0.621	0.363	0.202	0.291
$C_{sea}^{strange}$		$\mathcal{F}_{valence}$	N
0.621		$[1 - G_D^2(Q^2)]$	1.015

$$K_{sea}(Q^2) = \frac{Q^2}{Q^2 + C_s}$$

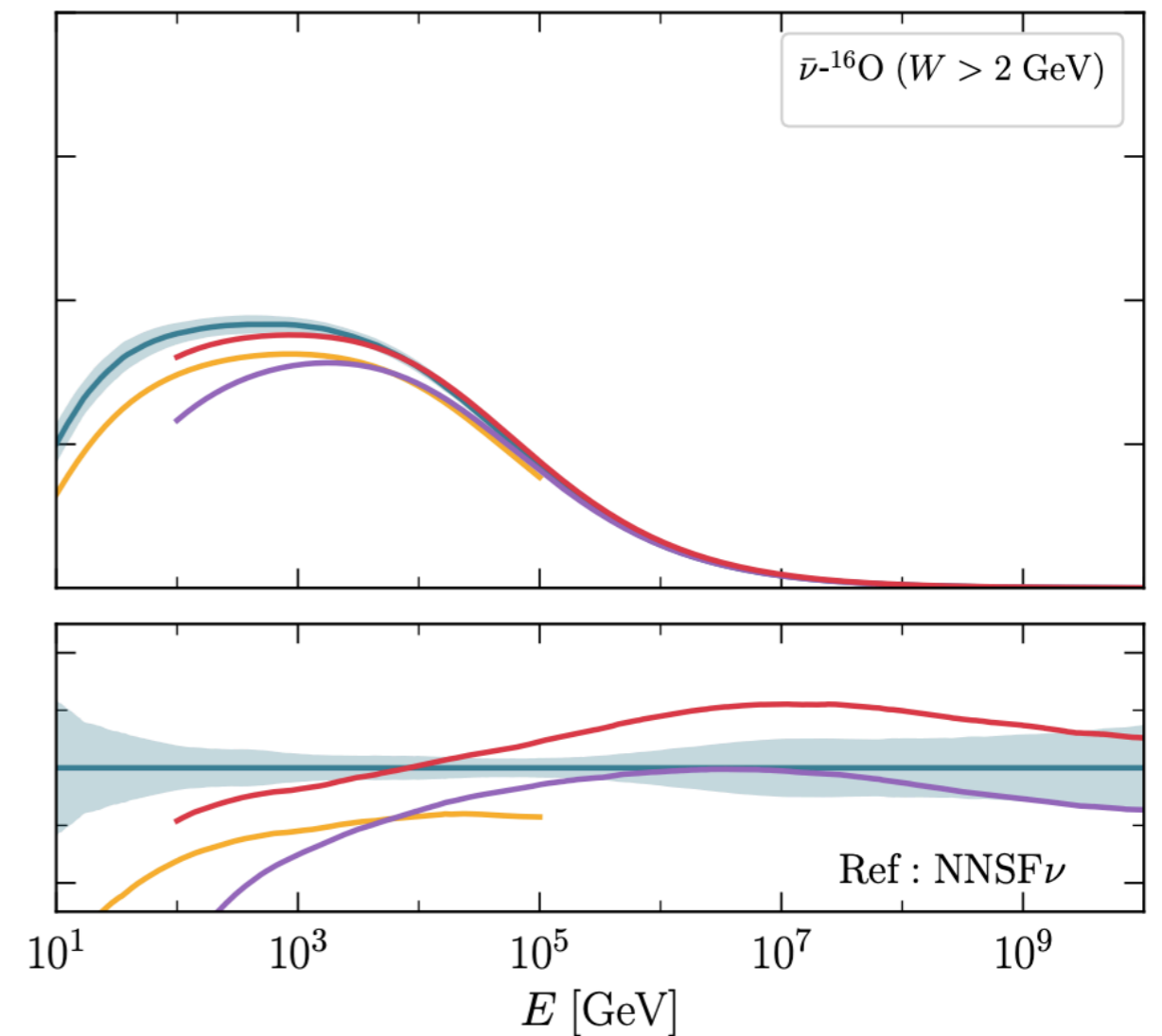
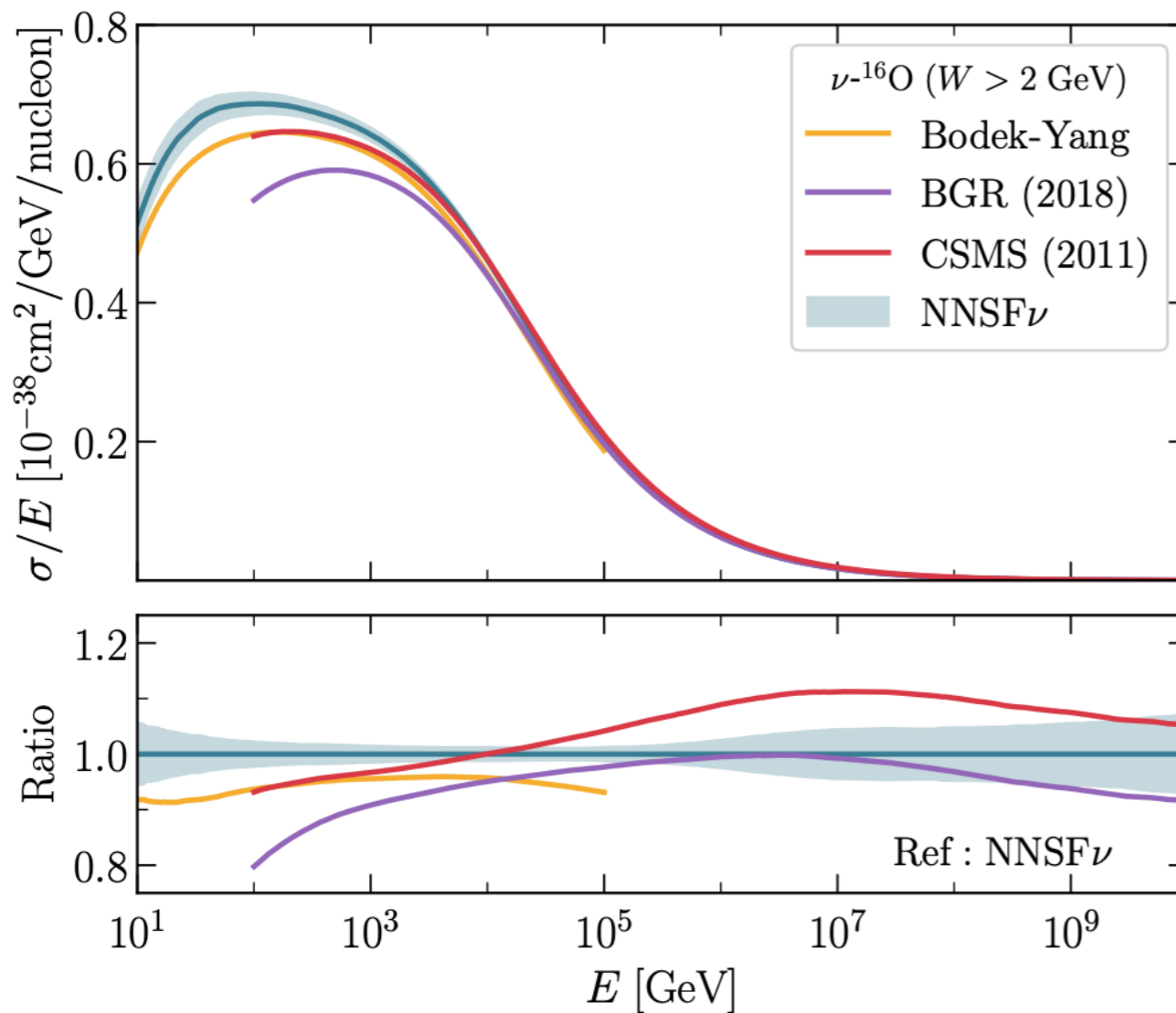
$$K_{valence}(Q^2) = [1 - G_D^2(Q^2)] \times \left(\frac{Q^2 + C_{v2}}{Q^2 + C_{v1}} \right)$$

$$F_2(x, Q^2 < 0.8) = K(Q^2) \times F_2(\xi, Q^2 = 8)$$

$x_{A_{HT}^{BY}}$	A_{HT} higher-twist param in BY model scaling variable ξ_w	$\pm 25\%$
$x_{B_{HT}^{BY}}$	B_{HT} higher-twist param in BY model scaling variable ξ_w	$\pm 25\%$
$x_{C_{V1u}^{BY}}$	C_{V1u} u valence GRV98 PDF correction param in BY model	$\pm 30\%$
$x_{C_{V2u}^{BY}}$	C_{V2u} u valence GRV98 PDF correction param in BY model	$\pm 40\%$
x_{CCDIS}	Inclusive CC cross-section normalization factor	
$x_{CC\bar{\nu}/\nu}$	$\bar{\nu}/\nu$ CC ratio	
$x_{DIS-NuclMod}$	DIS nuclear modification (shadowing, anti-shadowing, EMC)	

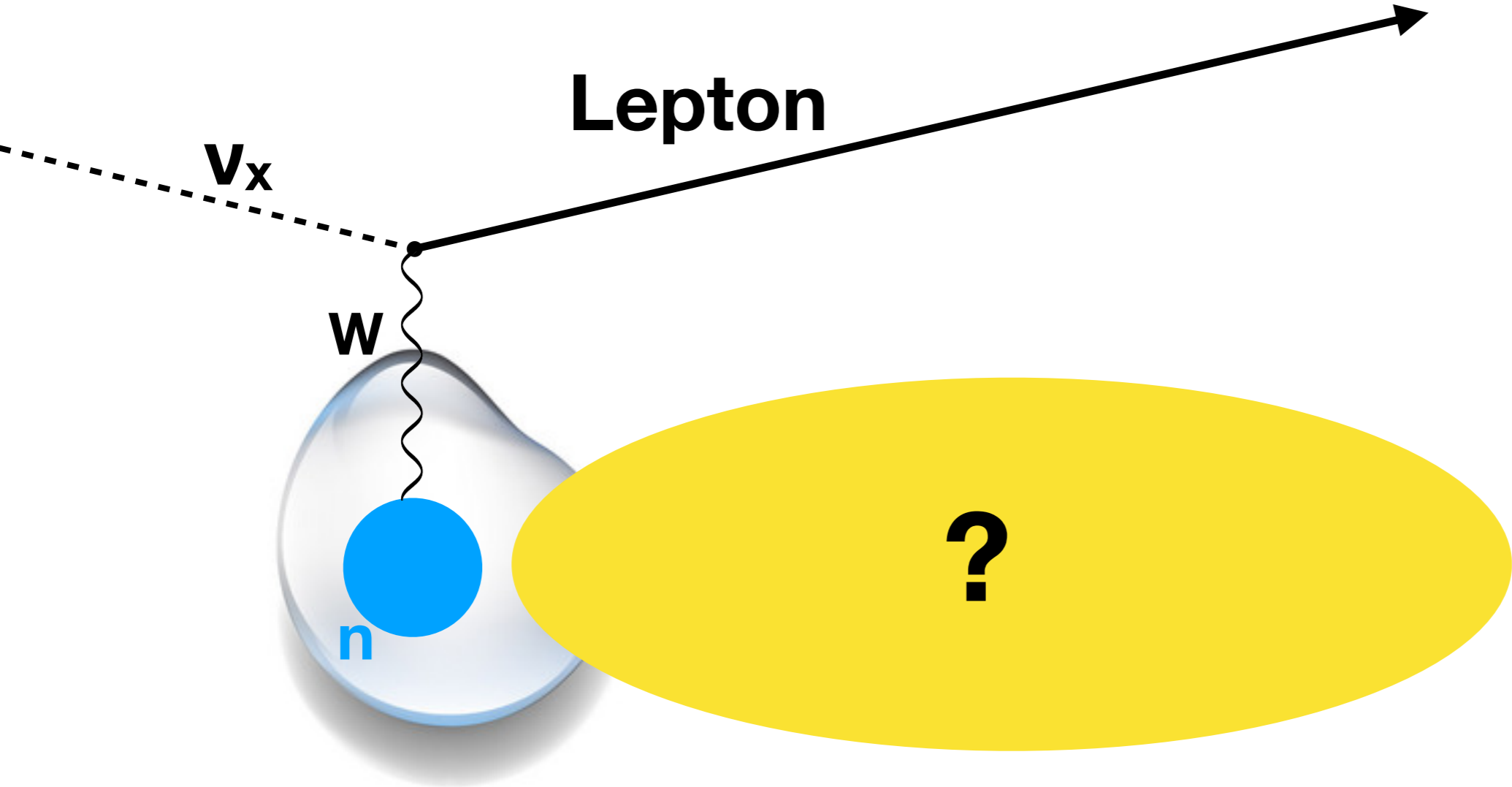
Comparison

- Main points:
 - CSMS overestimates at TeV-PeV (treatment of top quark production).
 - Nuclear effects are relatively small for Oxygen.



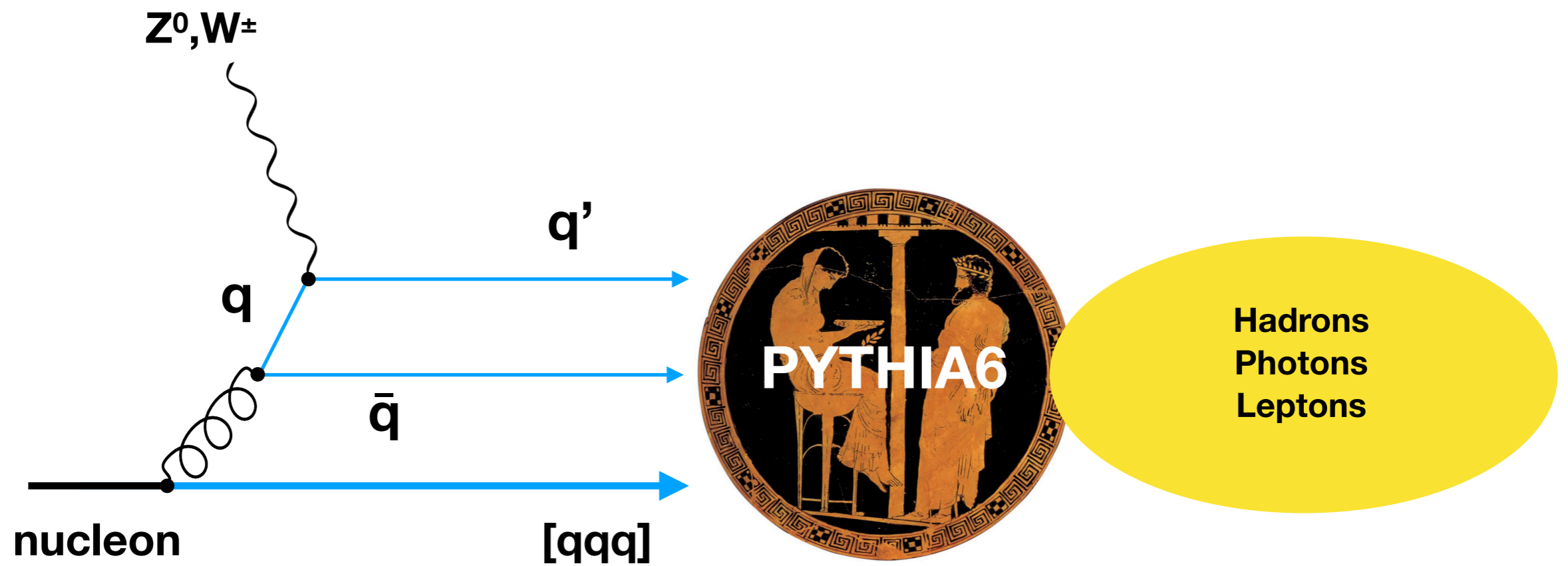
Hadron level

Hadron level



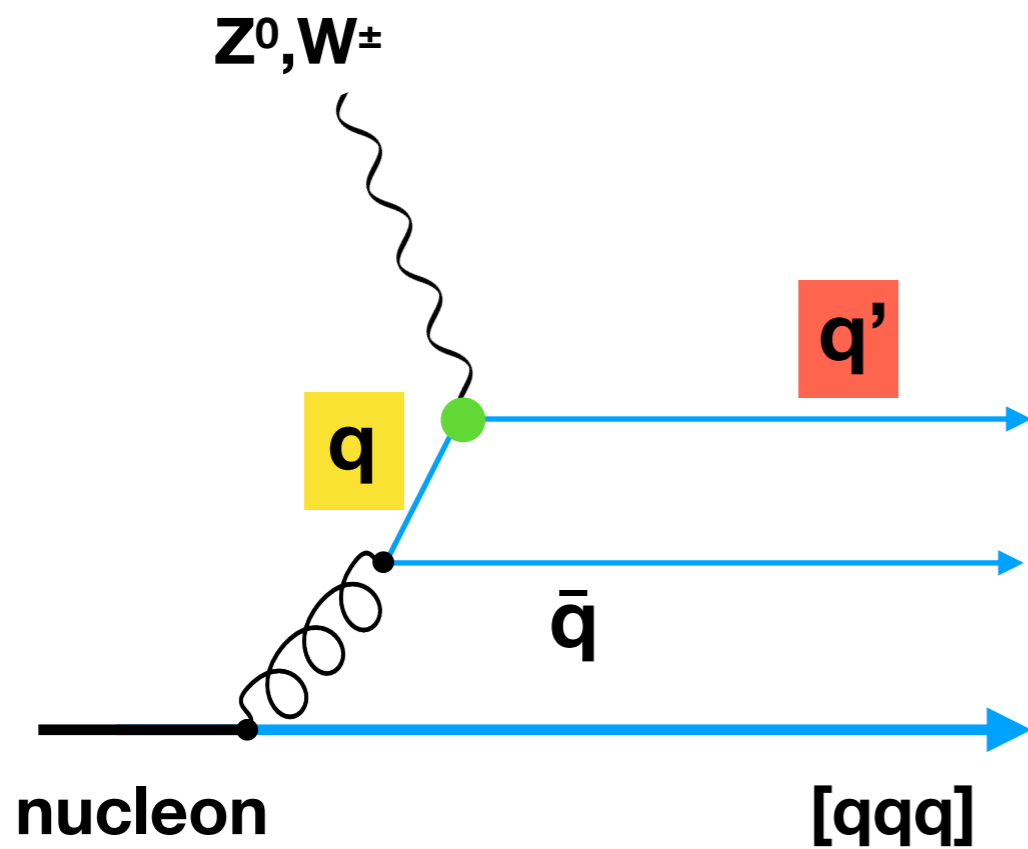
Hadronization-HEDIS

- Quark combination input to PYTHIA6.



Hadronization-HEDIS

- Quark combination input to PYTHIA6.
- Relative contribution from each quark using LO expression.
- Details of hadronic showers not relevant (yet) for neutrino telescopes.

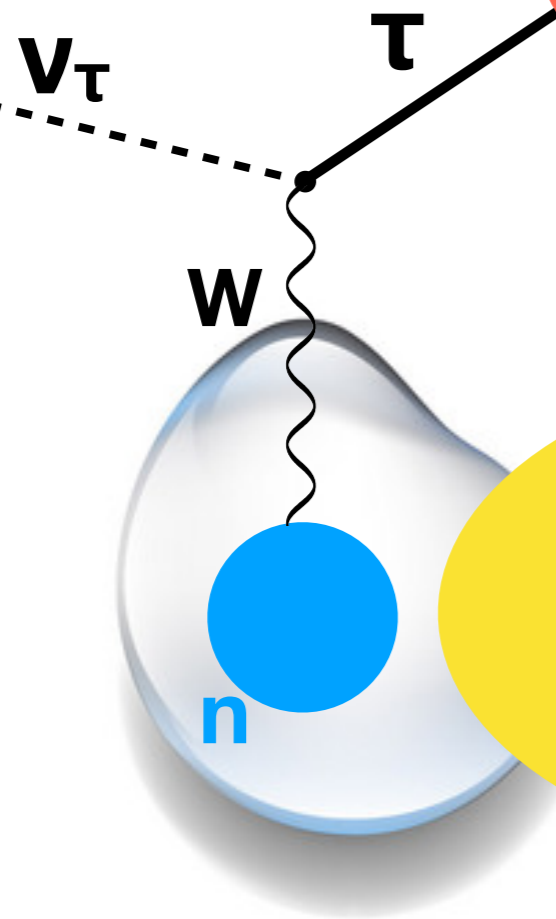


$$\mathbf{F}_q \otimes \mathbf{CKM}_{q,q'} \otimes \mathbf{Mass}_{q'}$$

||

$$P_{q \rightarrow q'} = \frac{\sigma_{q \rightarrow q'}^{LO}}{\sigma^{LO}}$$

Hadronization-HEDIS



- No PYTHIA running
- No formation zone
- No final state interactions
- **$W > 2\text{GeV}$**

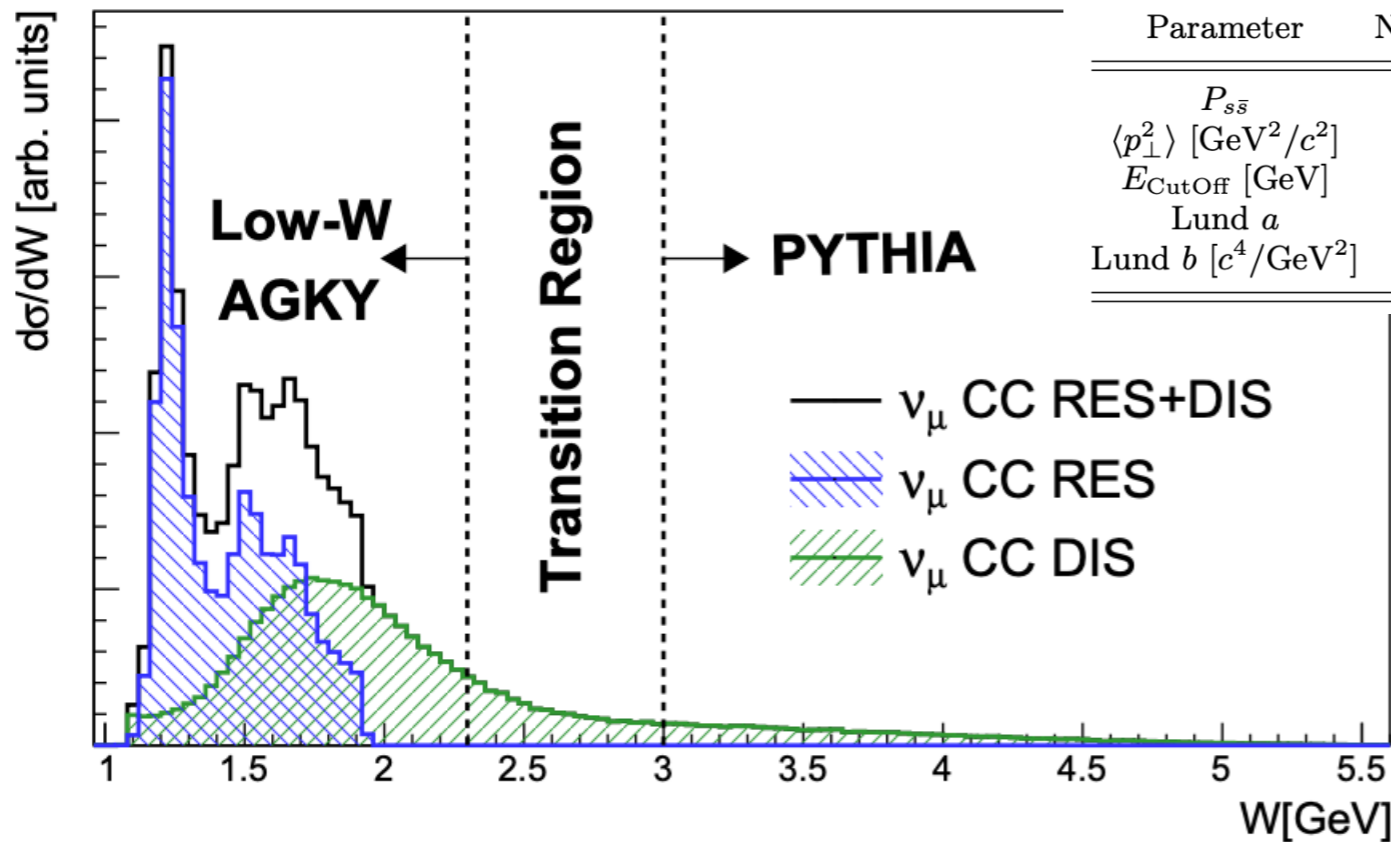
```

--> nu_tau (primary neutrino) E=8360.21
  `tau- (leading_lepton) E=5554.04
    +-nu_tau E=3297.56 status/id=1/5
    `rho- E=2256.48 status/id=3/6
      +-pi- E=1290.81 status/id=1/7
      `pi0 E=965.675 status/id=3/8
        +-gamma E=890.175
        `gamma E=75.4996
--> unnamed state (1000080160) E=14.8951
  +-neutron E=0.922834
    `unnamed state (2000000001) E=2807.09
      +-u E=2806.31
        `string E=2807.09
          +-eta E=2243.06
            | +-gamma E=1083.88
            | `gamma E=1159.18
          +-rho+ E=542.988
            | +-pi+ E=159.131
            | `pi0 E=383.856
              +-gamma E=243.584
              `gamma E=140.273
          +-pi- E=9.73694
          +-pi0 E=5.21542
            | +-gamma E=1.08007
            | `gamma E=4.13535
          +-omega E=3.59776
            | +-gamma E=0.0816192
            | `pi0 E=3.51614
              +-gamma E=3.20452
              `gamma E=0.311622
          `Delta+ E=2.49298
            +-proton E=2.00807
            `pi0 E=0.484947
              +-gamma E=0.0471374
              `gamma E=0.437831
        `ud_1 E=0.780469
      `unnamed state (1000080150) E=13.9722
  
```

Hadronization-DIS

- Hybrid model depending on the W of the interaction.
 - At $W > 3\text{GeV}$ a PYTHIA tuned version is used.

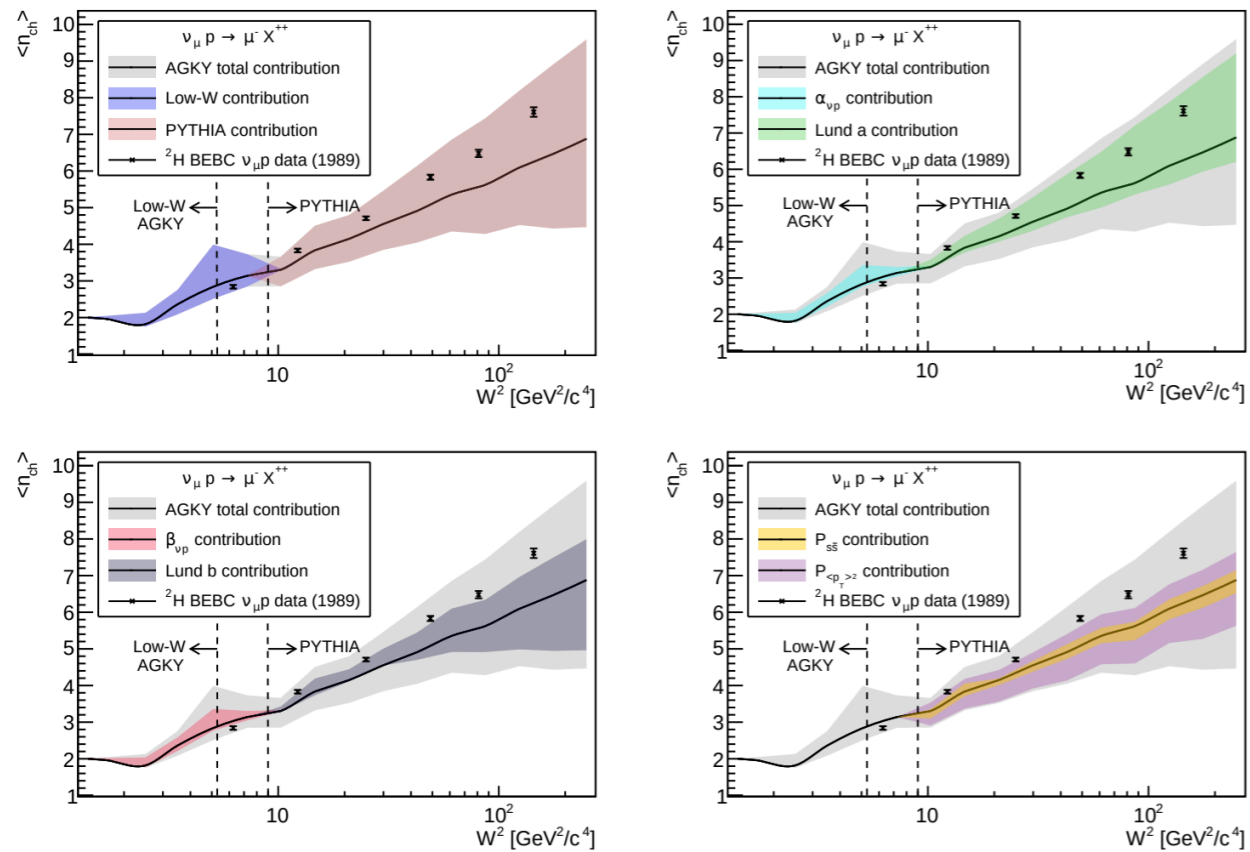
DUNE flux



Parameter	Name in PYTHIA	PYTHIA default	NUX tune	HERMES tune	2010 GENIE tune
$P_{s\bar{s}}$	PARJ(2)	0.30	0.21	0.25	0.30
$\langle p_{\perp}^2 \rangle$ [GeV^2/c^2]	PARJ(21)	0.36	0.44	0.42	0.44
E_{CutOff} [GeV]	PARJ(33)	0.80	0.20	0.47	0.20
Lund a	PARJ(41)	0.30	0.30	0.68	0.30
Lund b [c^4/GeV^2]	PARJ(42)	0.58	0.58	0.35	0.58

Hadronization-DIS

- New tuned has been recently developed.



<https://arxiv.org/abs/2106.05884>

Parameter	GENIE parameter name	2010 GENIE	Allowed range	2021 Global Fit	2021 ${}^2\text{H}$ Fit
Low-W empirical model					
α_{vp}	KNO-Alpha- νp	0.40	[-1.0, 2.0]	1.1 ± 0.3	1.2 ± 0.4
α_{vn}	KNO-Alpha- νn	-0.20	[-1.0, 2.0]	$1.75^{+0.14}_{-0.11}$	-0.58 ± 0.07
$\alpha_{\bar{\nu}p}$	KNO-Alpha- $\bar{\nu} p$	0.02	[-1.0, 2.0]	$1.32^{+0.16}_{-0.14}$	1.9 ± 0.08
$\alpha_{\bar{\nu}n}$	KNO-Alpha- $\bar{\nu} n$	0.80	[-1.0, 2.0]	1.11 ± 0.09	1.07 ± 0.3
β_{vp}	KNO-Beta- νp	1.42	[0.0, 2.5]	0.79 ± 0.15	0.9 ± 0.3
β_{vn}	KNO-Beta- νn	1.42	[0.0, 2.5]	0.5 ± 0.1	1.9 ± 0.3
$\beta_{\bar{\nu}p}$	KNO-Beta- $\bar{\nu} p$	1.28	[0.0, 2.5]	0.8 ± 0.1	0.3 ± 0.1
$\beta_{\bar{\nu}n}$	KNO-Beta- $\bar{\nu} n$	0.95	[0.0, 2.5]	$0.88^{+0.09}_{-0.08}$	0.9 ± 0.2
PYTHIA					
$P_{s\bar{s}}$	PYTHIA-SSBarSuppression	0.30	[0.0, 1.0]	0.27 ± 0.04	0.29 ± 0.05
$\langle p_{\perp}^2 \rangle$ [GeV $^2/c^2$]	PYTHIA-GaussianPt2	0.44	[0.1, 0.7]	0.46 ± 0.05	0.43 ± 0.04
E_{CutOff} [GeV]	PYTHIA-RemainingEnergyCutoff	0.20	[0.0, 1.0]	0.30 ± 0.04	0.24 ± 0.05
Lund a	PYTHIA-Lunda	0.30	[0.0, 2.0]	1.53 ± 0.13	1.85 ± 0.15
Lund b [c 4 /GeV 2]	PYTHIA-Lundb	0.58	[0.0, 1.5]	1.16 ± 0.09	1.0 ± 0.2
				$\chi^2 =$	87.9/62 DoF 29.5/32 DoF

Formation zone

- DIS includes a formation zone calculation
 - Hadron/nucleon dependent.
 - Reweigh is available

```
<!--
~~~~~
Parameters relevant to formation zone simulation
- ct0 is the formation time times the speed of light (given in fm)
- KPt2 is the parameter multiplying pT2 in formation zone calc.
-->
<param type="double" name="FZONE-ct0pion">    0.342  </param>
<param type="double" name="FZONE-ct0nucleon">  2.300  </param>
<param type="double" name="FZONE-KPt2">       0.0    </param>
```

```
//-----
double genie::utils::phys::FormationZone(
    double m, const TLorentzVector & p4,
    const TVector3 & p3hadr, double ct0 /*in fm*/, double K)
{
    // m -> hadon mass (on-shell)
    // p -> hadron momentum 4-vector (Lab)
    // p3hadr -> hadronic-system momentum 3-vector (Lab)

    TVector3 p3 = p4.Vect(); // hadron's: p (px,py,pz)
    double m2 = m*m; // m^2
    double P = p4.P(); // |p|
    double Pt = p3.Pt(p3hadr); // pT
    double Pt2 = Pt*Pt; // pT^2
    double fz = P*ct0*m/(m2+K*Pt2); // formation zone, in fm

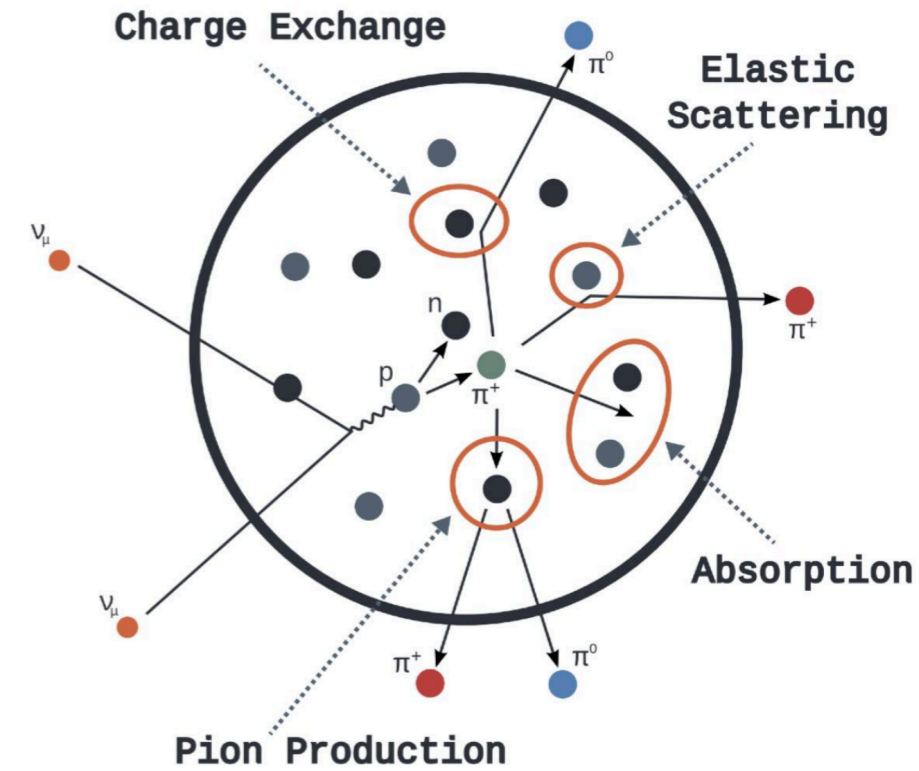
    LOG("PhysUtil", pNOTICE)
        << "Formation zone(|P| = " << P << " GeV, Pt = " << Pt
        << " GeV, ct0 = " << ct0 << " fm, K = " << K << ") = " << fz << " fm";

    return fz;
}
```

Final-state interactions

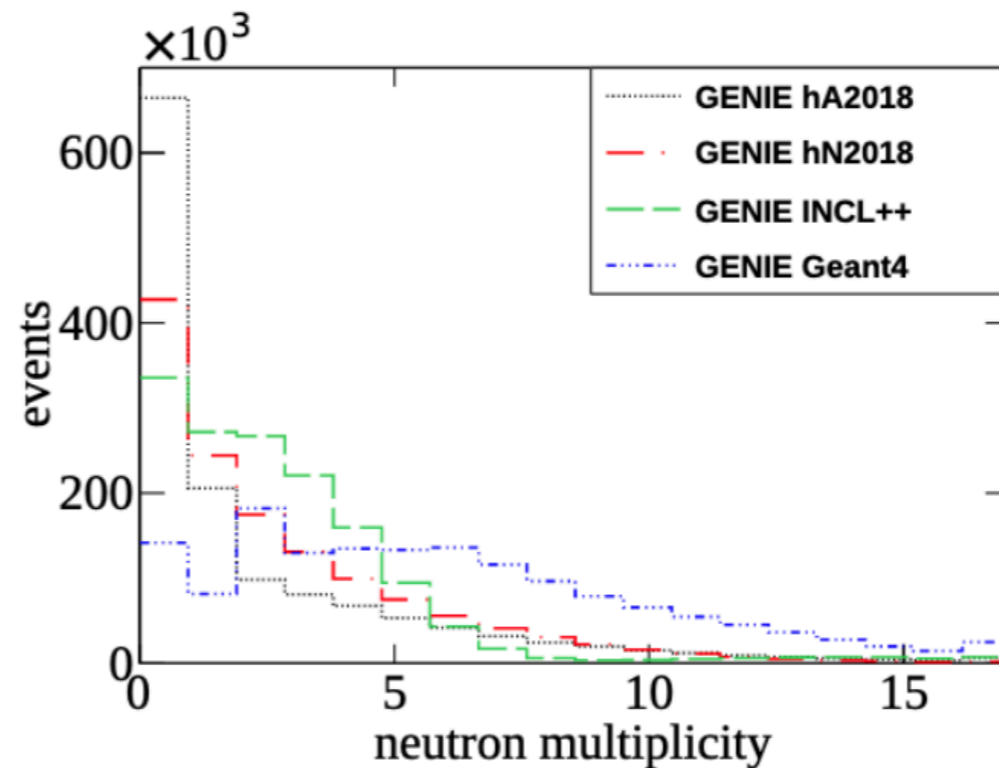
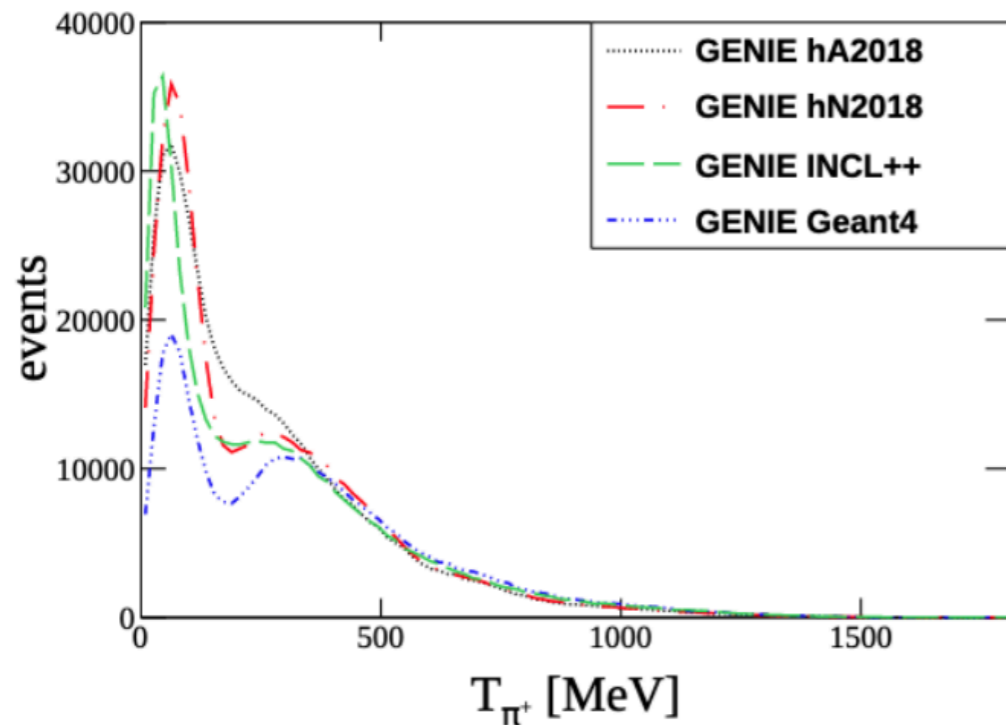
- Based on intranuclear cascade (INC) model.
 - Simple: $hA \rightarrow$ For $E < 1.2 \text{ GeV}$
 - Sophisticated: $hN \rightarrow$ $E > 50 \text{ MeV}$
 - INCL++
 - GEANT4

Image: T. Golan



$$\lambda(E, r) = \frac{1}{\sigma_{hN, tot} * \rho(r)}$$

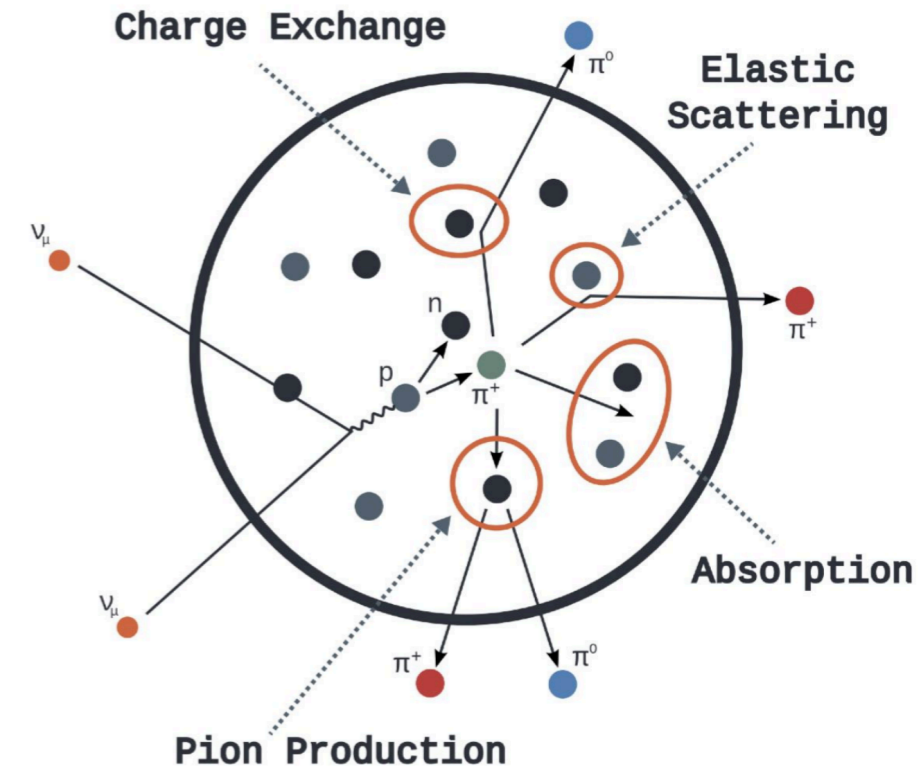
2GeV numu+Ar



Final-state interactions

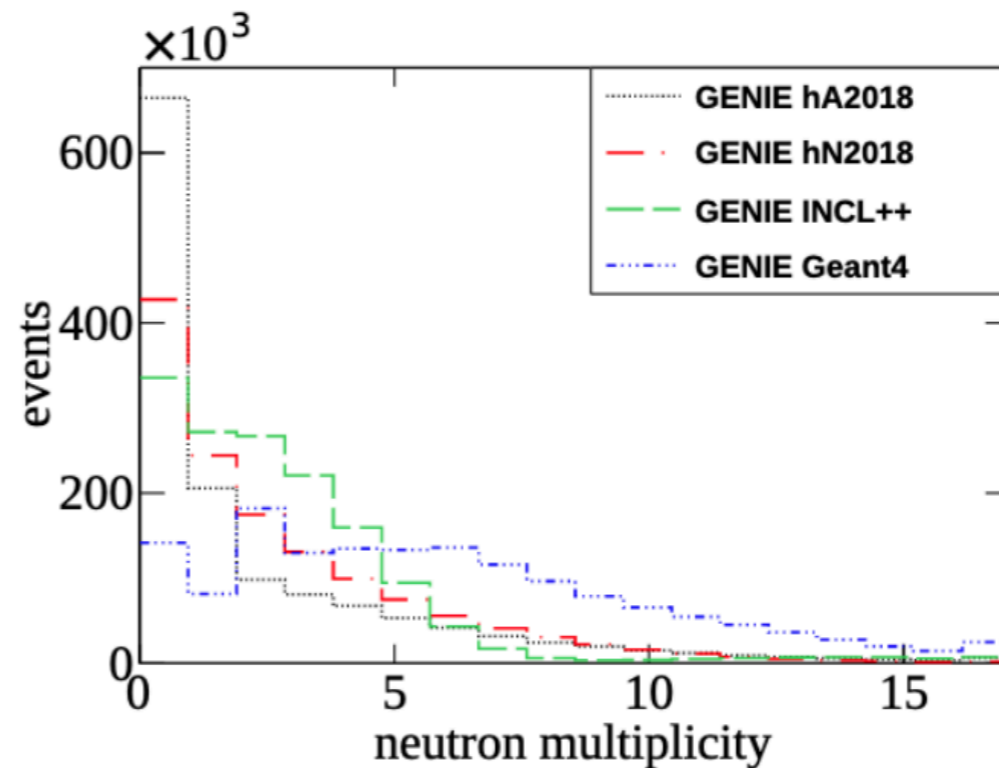
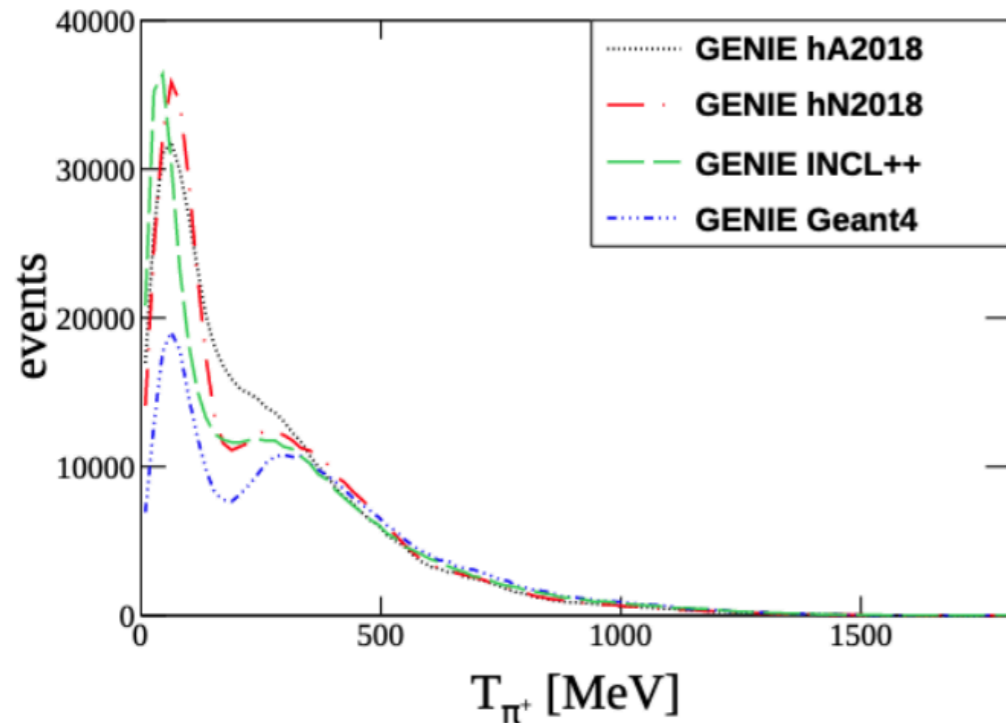
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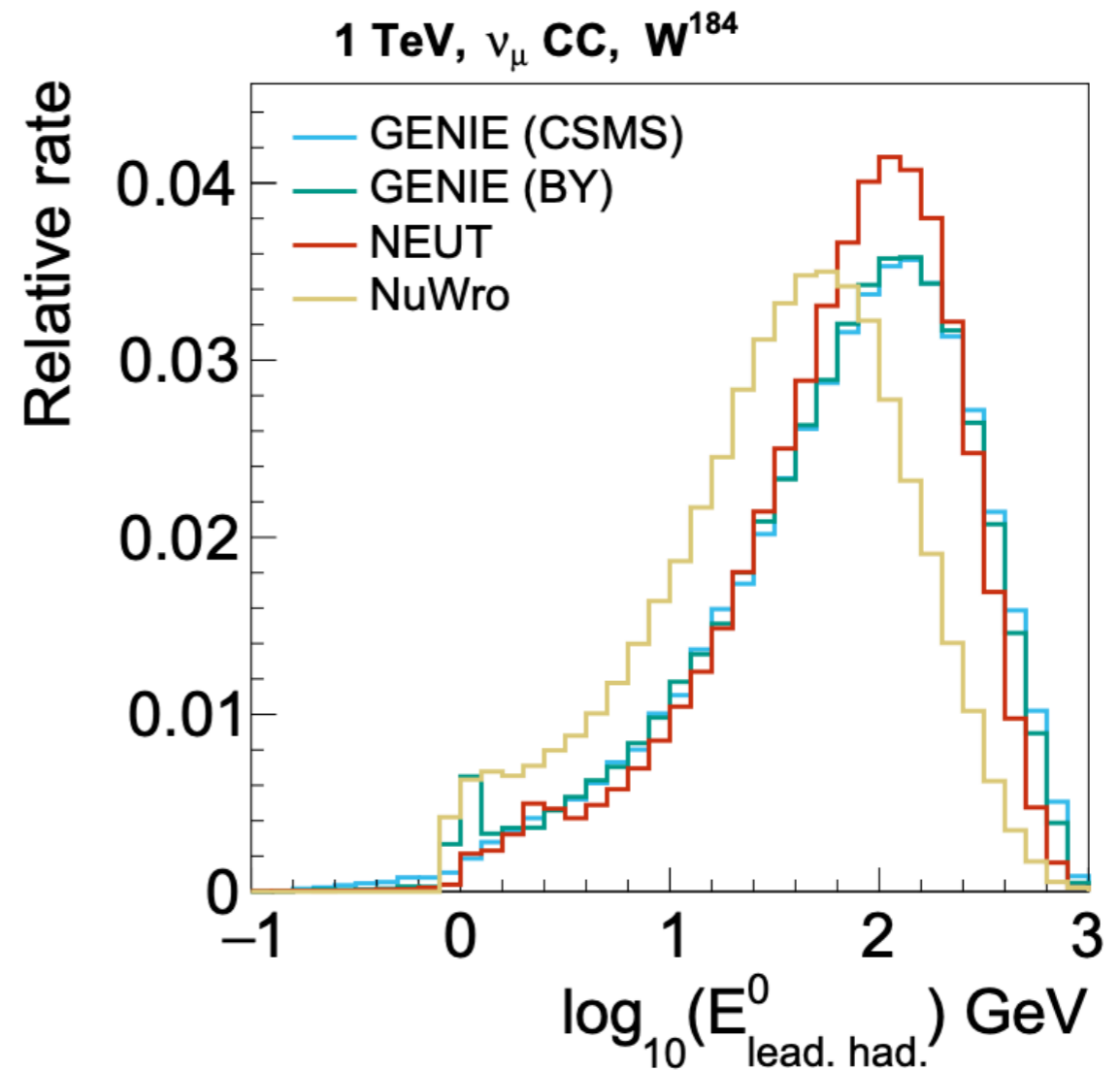
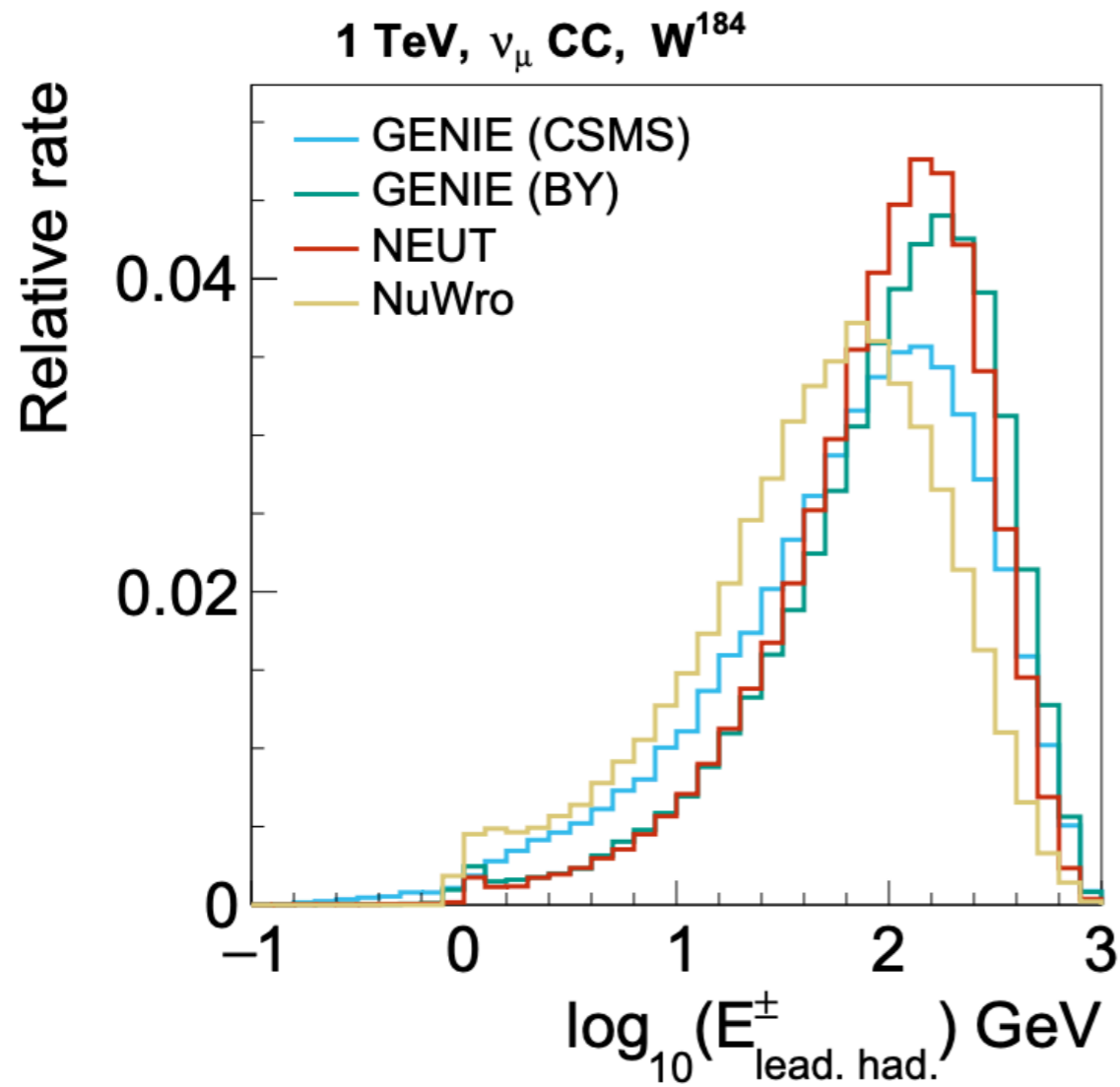
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2GeV numu+Ar



Comparison

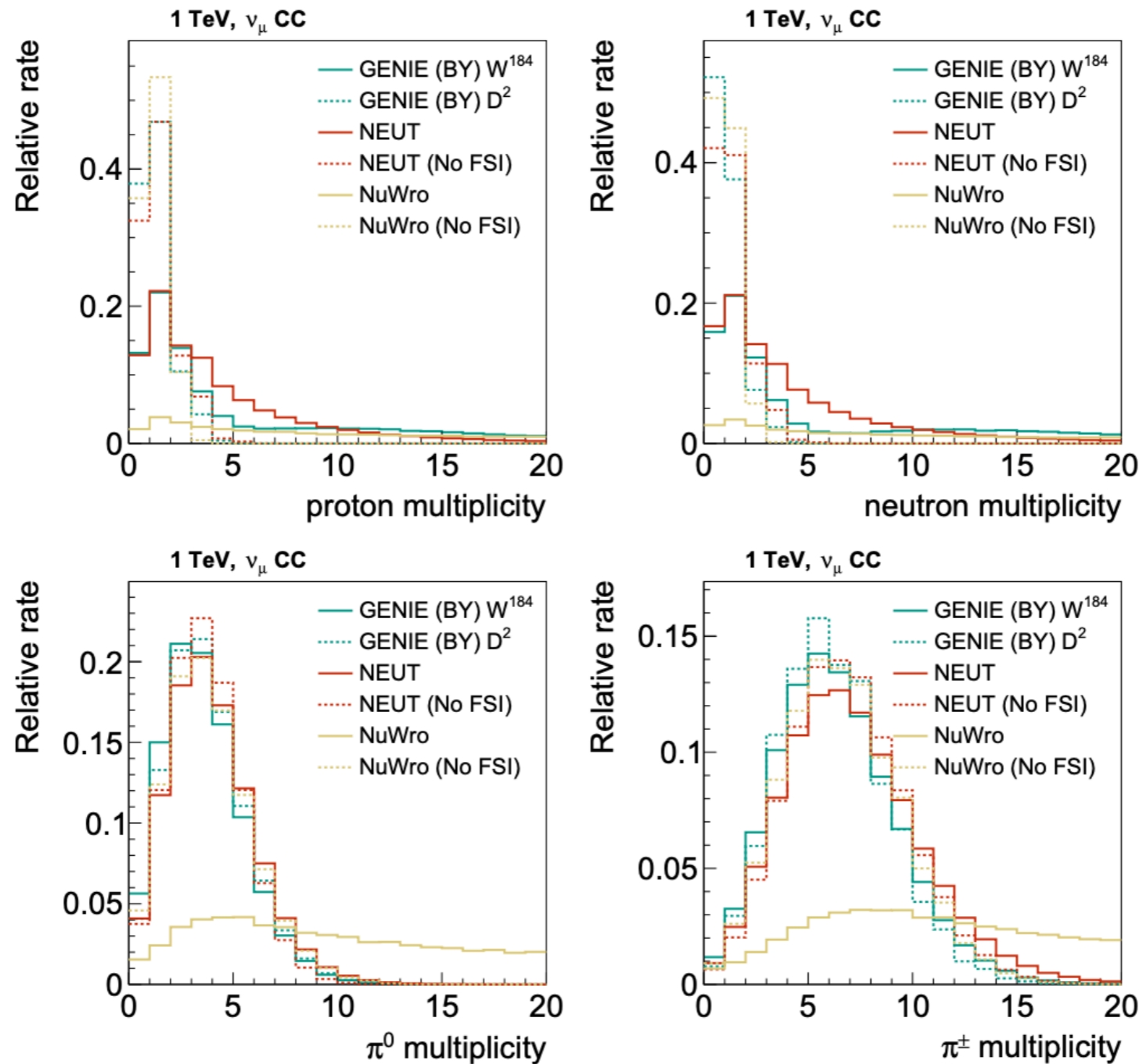
- Energy of leading hadrons



arXiv:2203.05090

Comparison

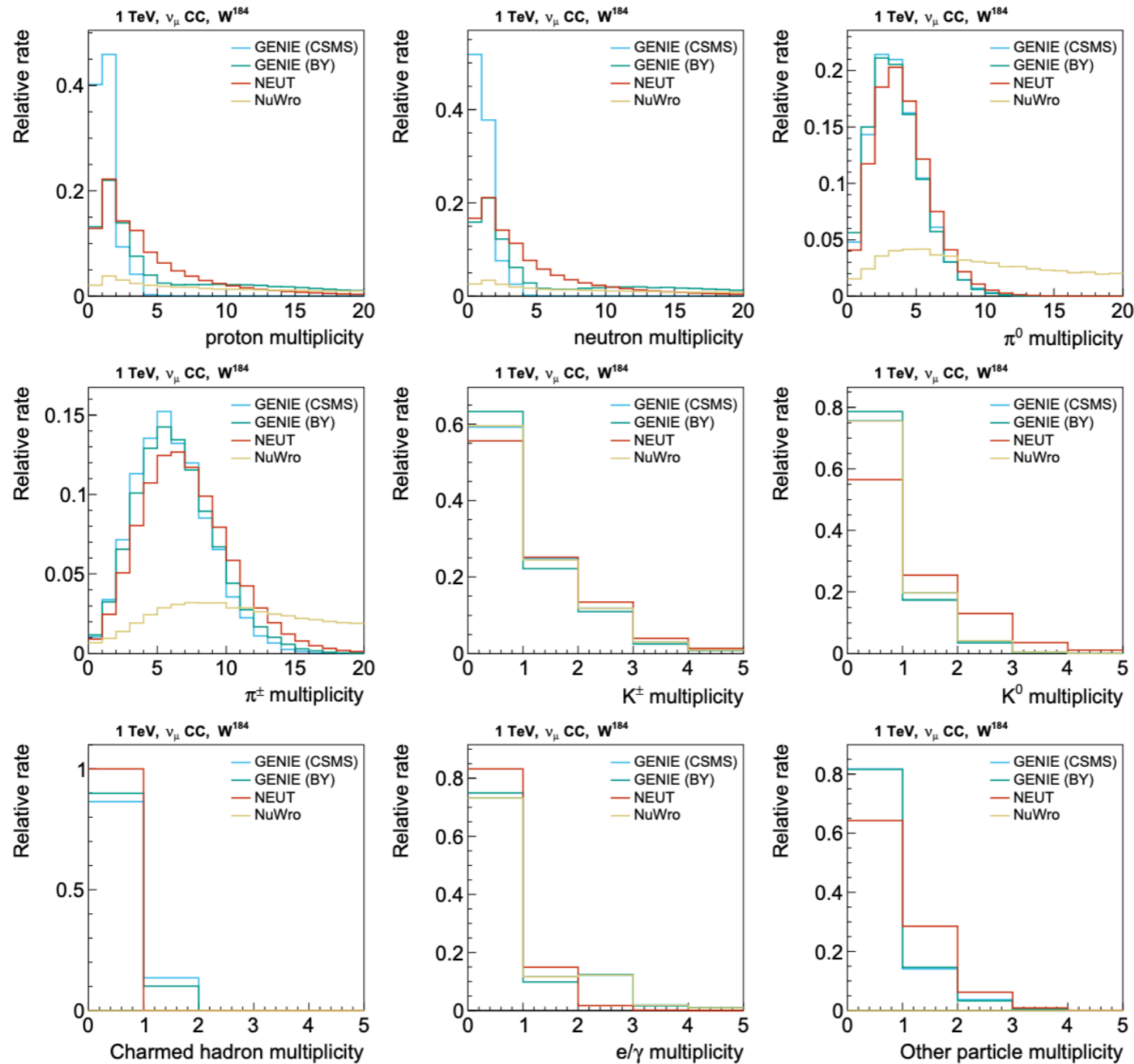
- Hadron multiplicity with/without NSI



arXiv:2203.05090

Comparison

- Hadron multiplicity



arXiv:2203.05090

Acknowledgements

This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 101025085.