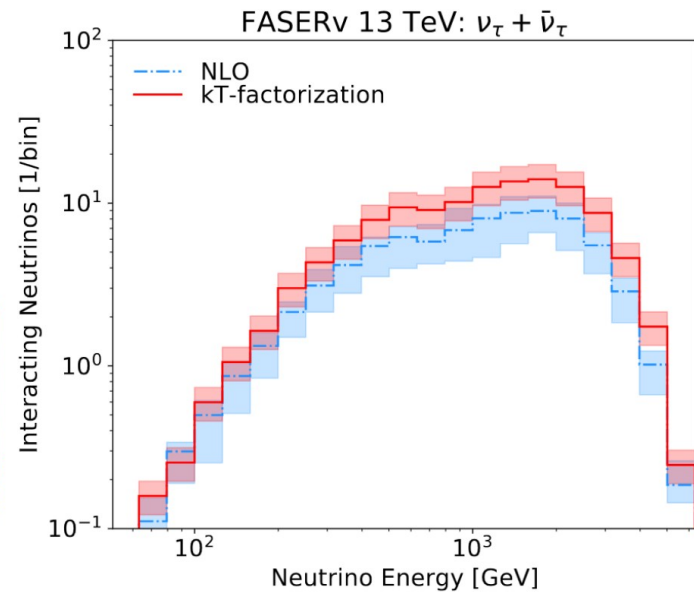
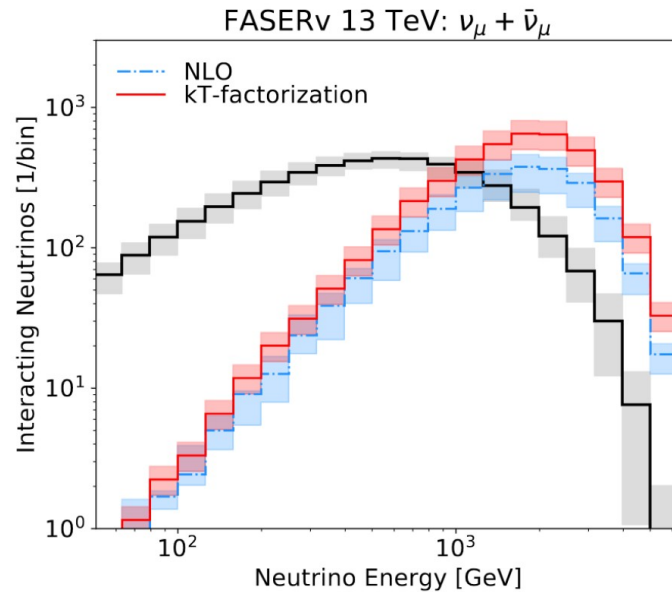
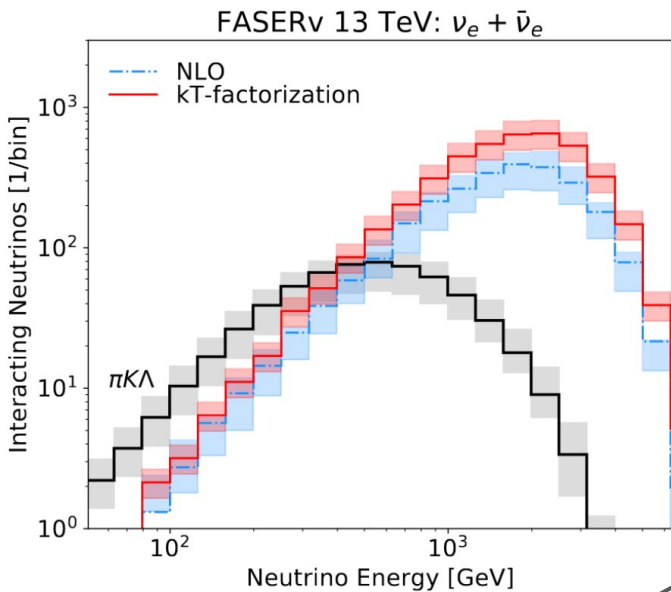


# Forward Neutrinos from Charm at Large Hadron Collider



arXiv:2306.01578

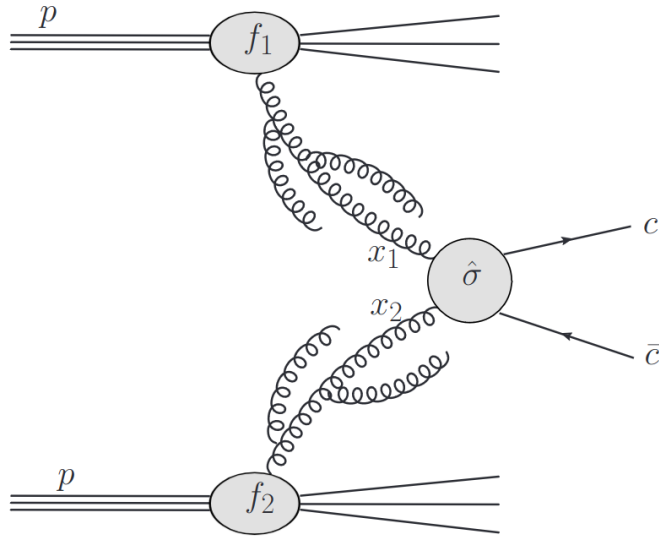
AB, Felix Kling,  
Ina Sarcevic, Anna Stasto

- ✓ Different QCD schemes for  $c\bar{c}$  production
- ✓ Fragmentation schemes for  $c\bar{c} \rightarrow$  mesons
- ✓ Fitting to 13 TeV data from LHCb and neutrino fluxes

# QCD schemes:

$$pp \rightarrow c\bar{c}$$

## Collinear factorisation



## $k_T$ factorisation

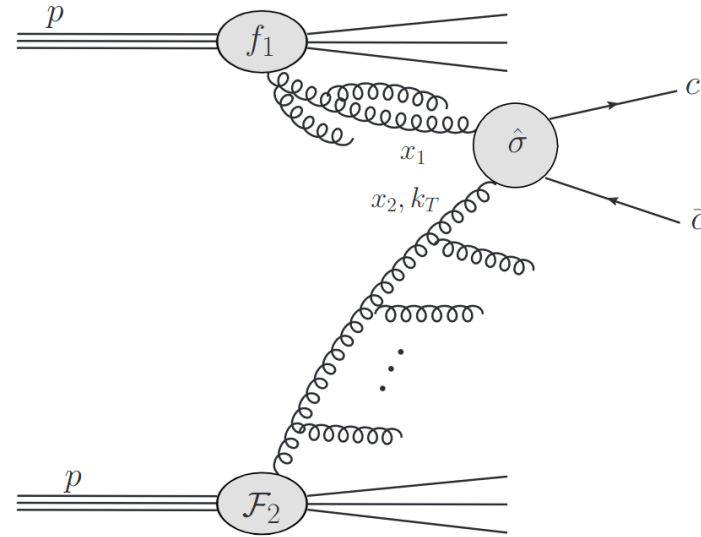


FIG. 1. Left: gluon-gluon fusion process for charm production in hadron-hadron collisions in the collinear factorization approach.  $f_1, f_2$  are the integrated gluon distribution functions which depend on the longitudinal momentum fractions  $x_1, x_2$  and the hard scale of the partonic sub-process. Right: the same process, illustrated for the case of forward production in the  $k_T$ -factorization. The gluon  $x_1$  is treated on-shell, and the gluon  $x_2$  is off-shell with transverse momentum  $k_T$ .  $\hat{\sigma}$  is the partonic cross section which is on-shell (left panel) and takes into account off-shellness of one gluon (right panel).

# QCD schemes:

$$pp \rightarrow c\bar{c}$$

## Collinear factorisation

$$\frac{d^2\sigma_{pp}}{dydp_T^2}(s, m_c^2) = \sum_{i,j=q,\bar{q},g} \int dx_1 dx_2 f_i(x_1, \mu_F^2) f_j(x_2, \mu_F^2) \frac{d^2\hat{\sigma}_{ij}}{dydp_T^2}(\hat{s}, m_c^2, \mu_F^2, \mu_R^2)$$

CT14nlo  
central

NLO

Scales

$\mu_F$ : factorisation  
 $\mu_R$ : renormalisation

$m_c = 1.3 \text{ GeV}$   
 $\sqrt{s} = 13 \text{ TeV}$

## $k_T$ factorisation

$$\sigma_{pp}(s, m_c^2) = \int dx_1 dx_2 \frac{d^2\mathbf{k}_T}{\pi} f(x_1, \mu^2) \mathcal{F}(x_2, \mathbf{k}_T) \hat{\sigma}^{\text{on-off}}(\hat{s}, \mathbf{k}_T, m_c)$$

Un-integrated  
 $k_T$ -dependent PDF

$g_1$  on-shell

$g_2$  off-shell

$\hat{\sigma}^{\text{on-off}}$  is LO  
 $\Rightarrow$  Introduce  $k$ -factor

# Fragmentation $c\bar{c} \rightarrow D\text{-Mesons}$

- ✗ Typical fragmentation functions determined from LEP data
- ✗ Not especially tailored to high rapidity and low  $p_T$  calculations needed for FPF
- ✗ Ignores hadronisation involving beam remnants
- ✗ Pion fixed target experiments: WA82, E769, E791
  - Hadron momentum spectrum as hard as or even harder than the charm quark spectra

$D_H(z) \equiv$  Charm energy fraction converted to hadron energy  
 $z = p_H/p_c$

## Pythia-inspired fragmentation

MC generators typically use more sophisticated hadronisation schemes. In particular, *Pythia* uses the Lund string model in which coloured objects are connected by a colour string containing the field lines of the strong force. This model can intuitively explain, for example, how a charm quark connected to a beam remnant valence quark will be pulled forward, potentially gaining energy.

# Fragmentation $c\bar{c} \rightarrow D\text{-Mesons}$

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## Pythia-inspired fragmentation

Charm production using Pythia produces a sampling of events, with each event characterized by the parton momentum  $\mathbf{p}_c$ , the hadron momentum  $\mathbf{p}_H$ , a hadron ID and an event weight  $w$ . The events in the sample follow a distribution  $d^2\sigma_c^{P8}$  for the charm quarks and  $d^2\sigma_H^{P8}$  for the charm hadrons. Re-weighting procedure: adjust weights

$$w \rightarrow w \times \frac{d^2\sigma_c/(dp_{T,c}dy_c)}{d^2\sigma_c^{P8}/(dp_{T,c}dy_c)}$$

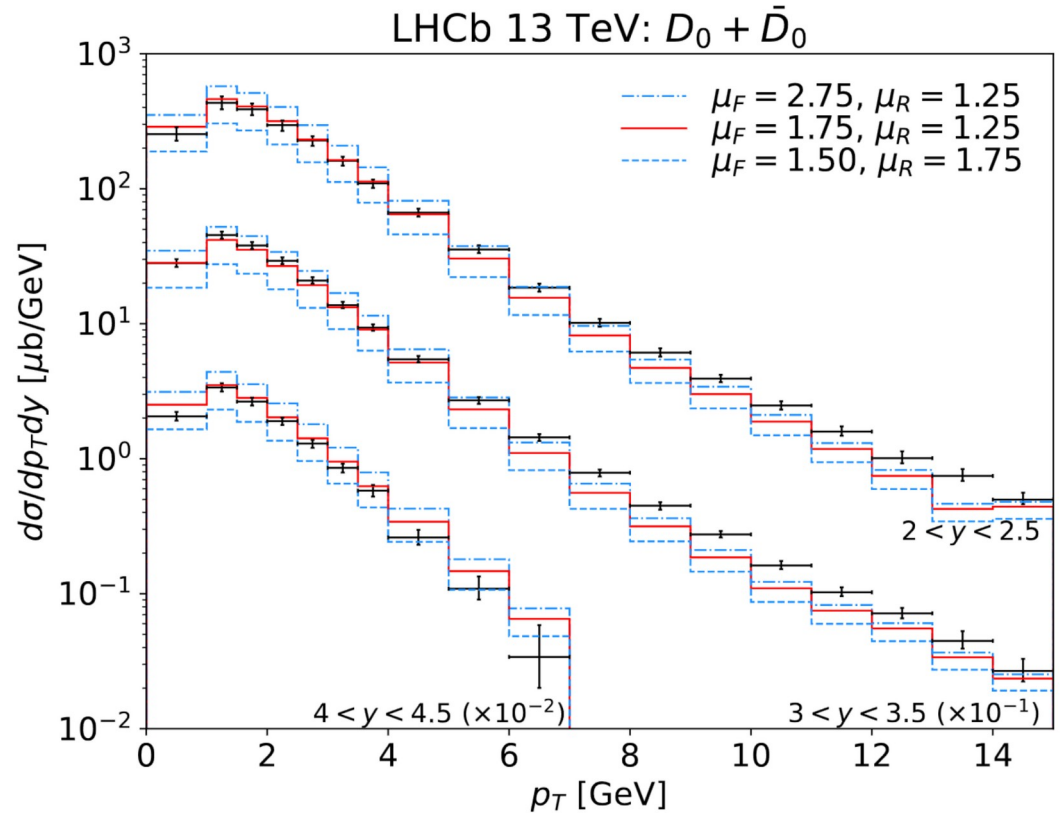
# Determining parameters Fitting $d^2\sigma$ to LHC data

- $D^0/\bar{D}^0$ ,  $D^\pm$ ,  $D_s$  data at 13 TeV from LHCb for reference
- Vary parameters pertinent to QCD scheme and compare against data
- Define  $\chi^2$  normalised to number of  $p_T$  bins
  - For forward predictions, important to ensure that fitting is not skewed by the availability of significantly more data at lower rapidities  $2 \leq y \leq 3$  rather at, say,  $y \geq 4$
- Determine  $\chi^2/\text{d.o.f}$  for each set of parameters
- Obtain best-fit parameter set that minimises  $\chi^2/\text{d.o.f}$ , and parameter uncertainties

## Determining parameters Fitting $d^2\sigma$ to LHC data

- Scales  $\{\mu_F, \mu_R\}$  as parameters
- *Introduce* Gaussian smearing on charm  $p_T$ 
  - Inspired by Bai et al<sup>†</sup>, but modified to maintain energy conservation
  - Needed to match  $p_T$ -shape of computed  $d^2\sigma$  vis-à-vis LHCb data
  - Finally,  $\langle k_T \rangle = 1.5$  GeV

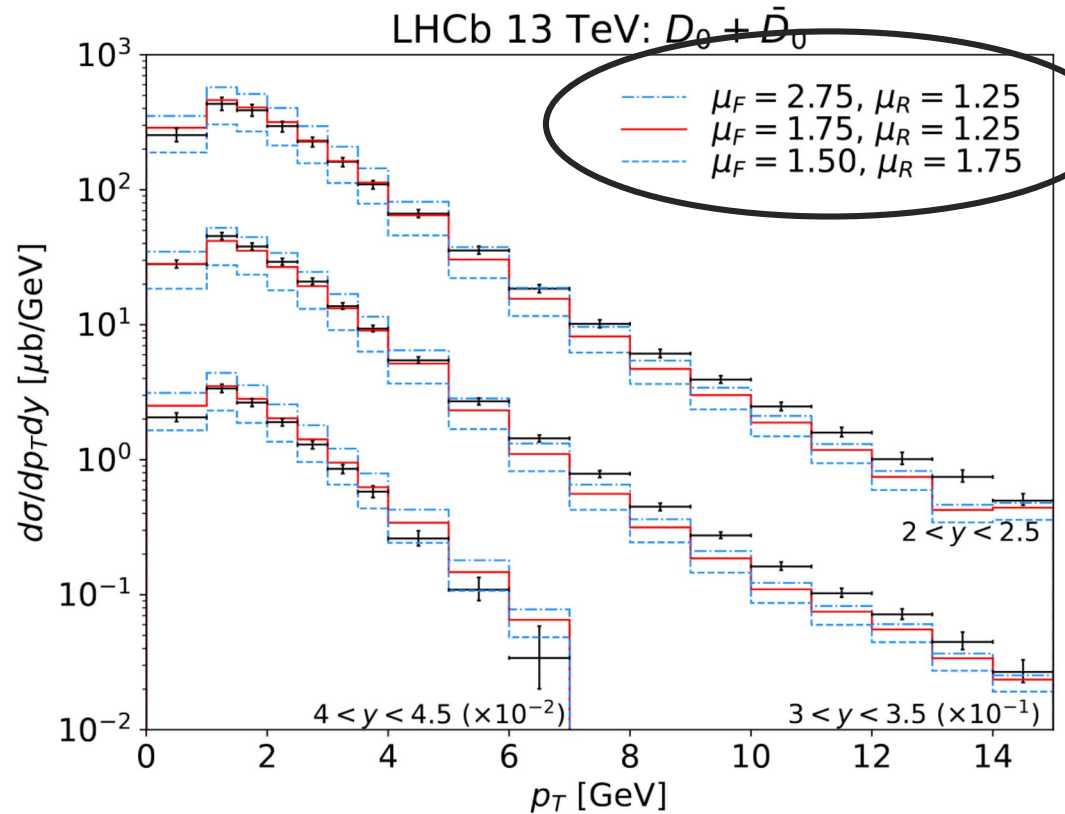
<sup>†</sup>arXiv:2002.03012



## Determining parameters Fitting $d^2\sigma$ to LHC data

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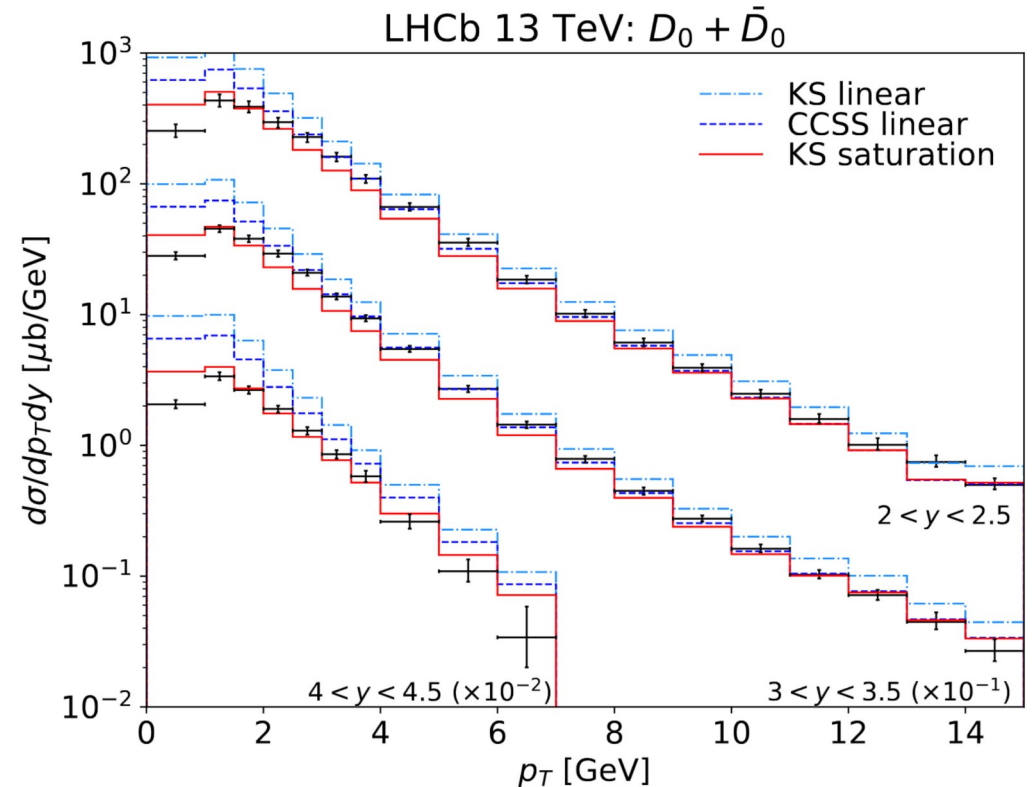
# $k_T$ factorisation

## Determining parameters Fitting $d^2\sigma$ to LHC data

- Different choices for  $\mathcal{F}(x_2, \mathbf{k}_T)$ 
  - Kutak-Sapeta (KS)<sup>†</sup> with non-linear evolution (saturation)
  - KS linear (w/o saturation)
  - Ciafaloni-Colferai-Salam-Stasto (CCSS) linear<sup>‡</sup>
- Fit parameter:  $k = 2.32 \pm 0.54$

<sup>†</sup> [arxiv:1205.5035](https://arxiv.org/abs/1205.5035)

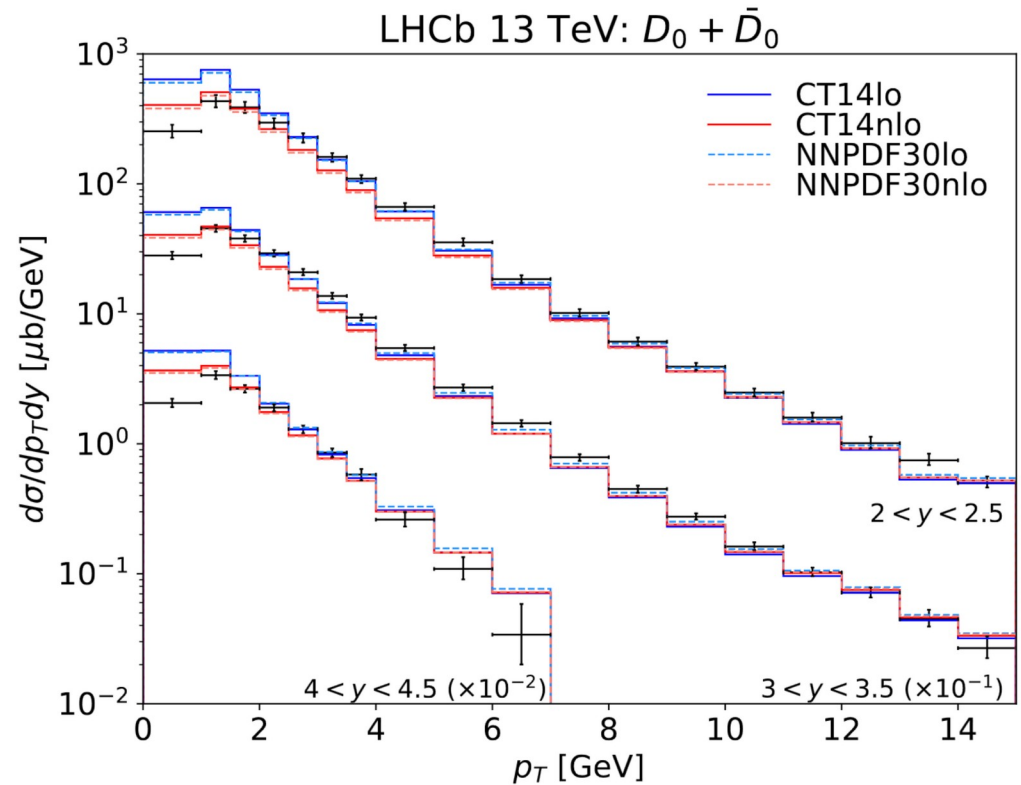
<sup>‡</sup> [arxiv:hep-ph/0307188](https://arxiv.org/abs/hep-ph/0307188)



# $k_T$ factorisation

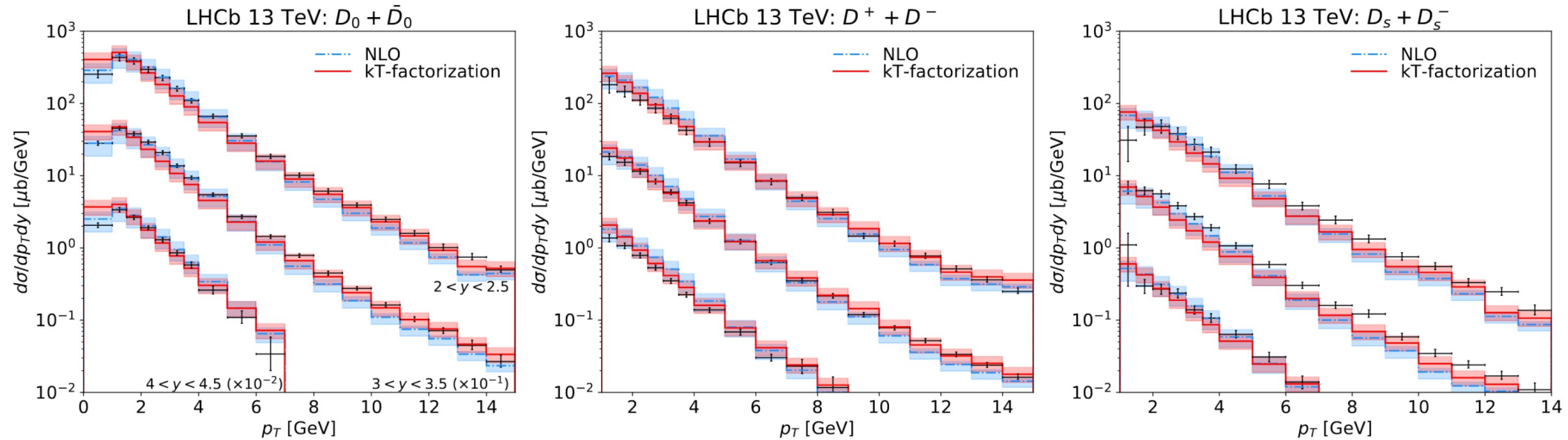
## Determining parameters Fitting $d^2\sigma$ to LHC data

- Different high- $x$  gluon PDF
- Strong coupling variation
- Different scale choices for  $k_T$ -factorisation



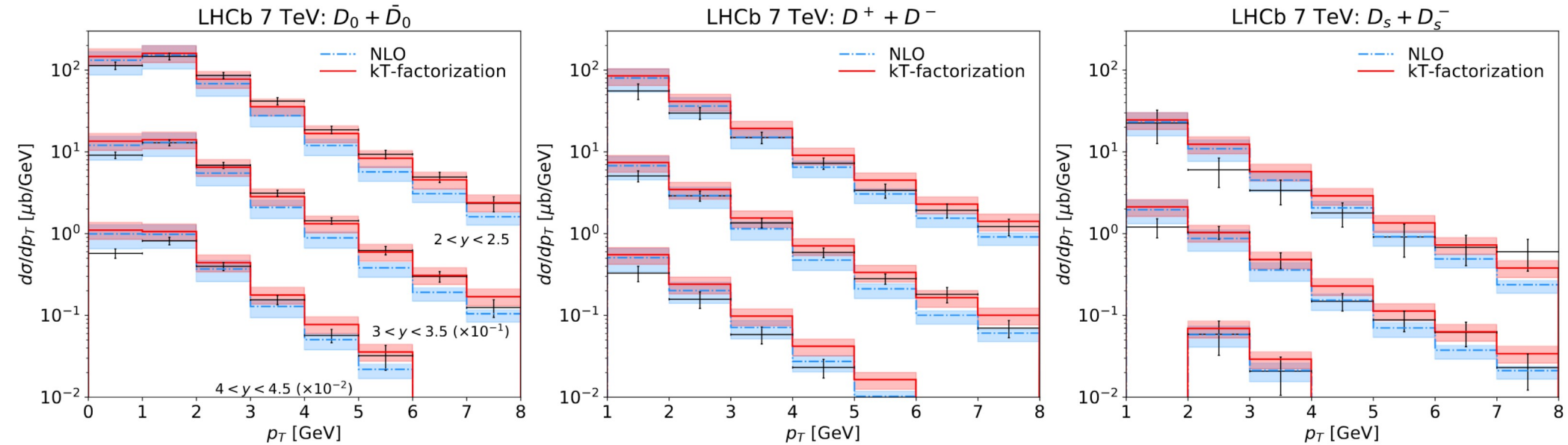
# Comparisons

Collinear vs  $k_T$  factorisation @ 13 TeV



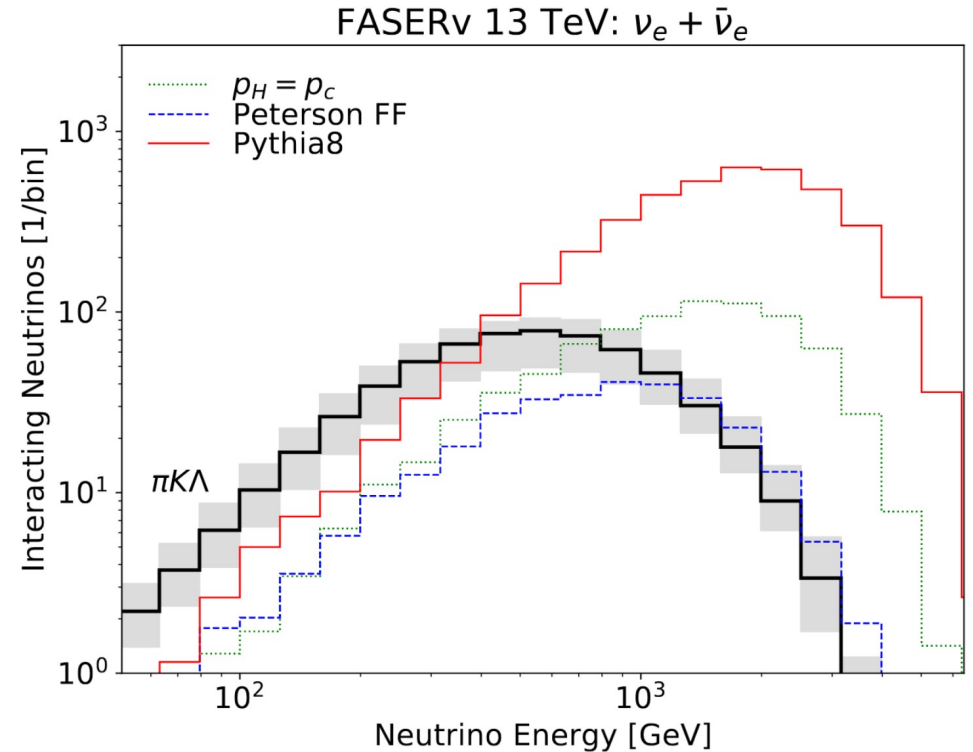
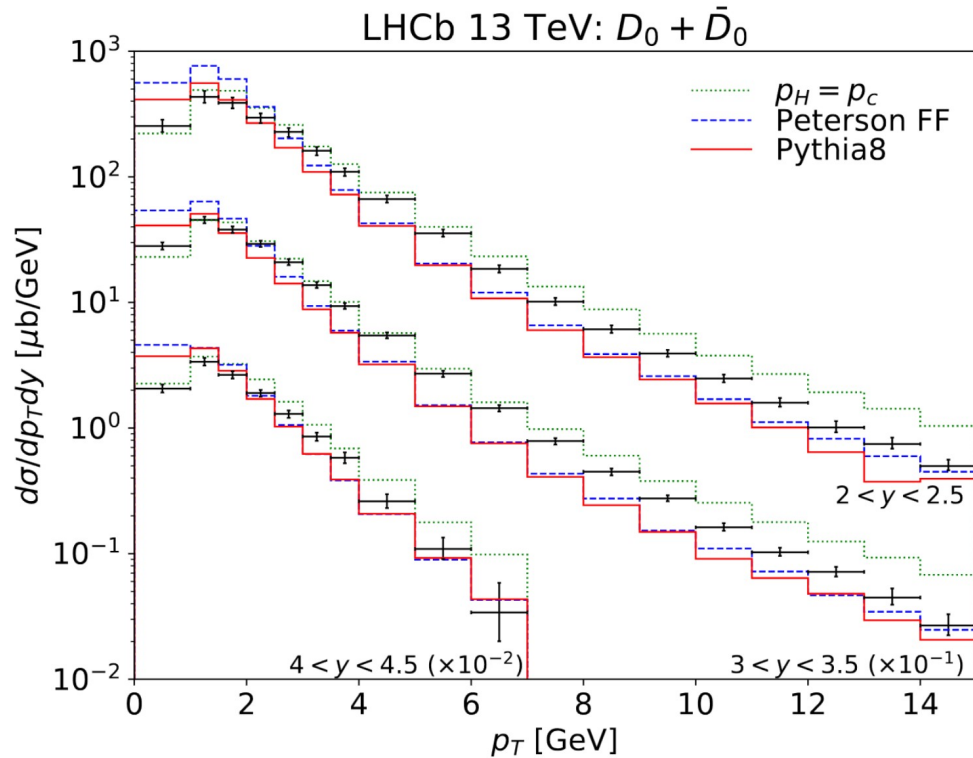
# Comparisons

## Collinear vs $k_T$ factorisation @ 7 TeV



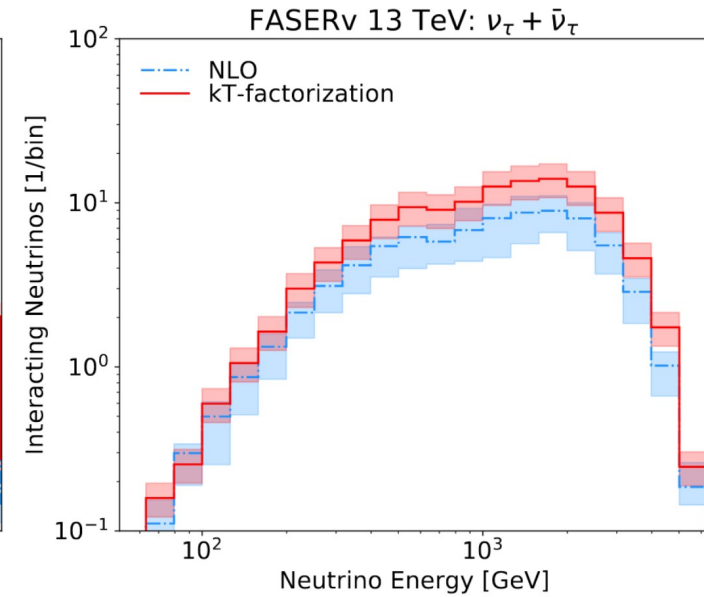
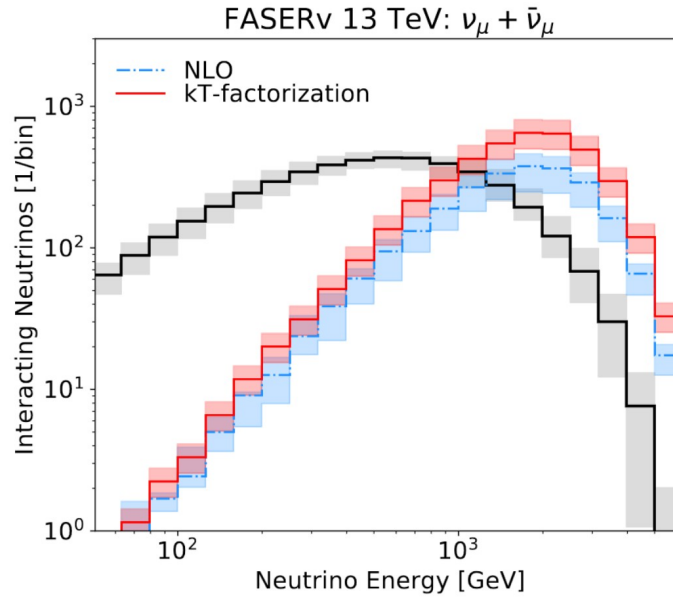
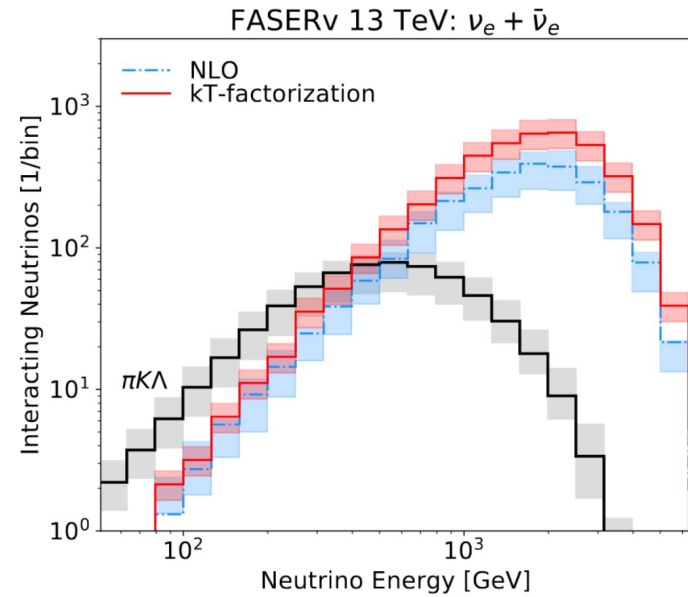
# Comparisons

## Fragmentation schemes



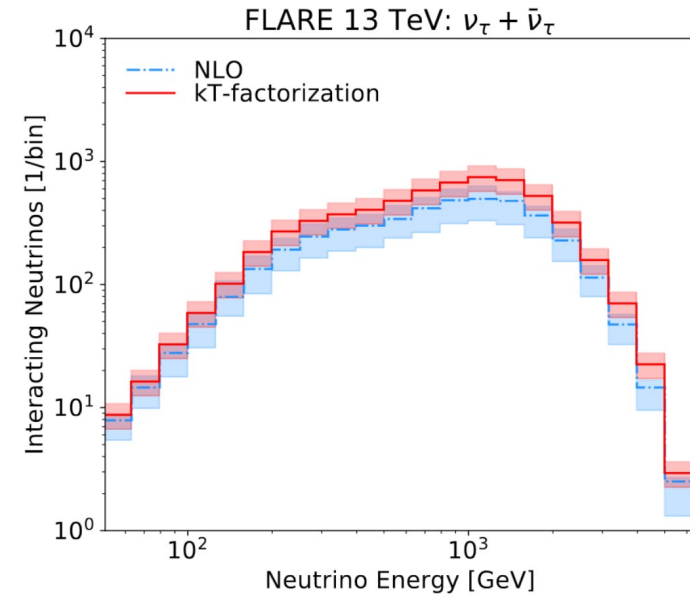
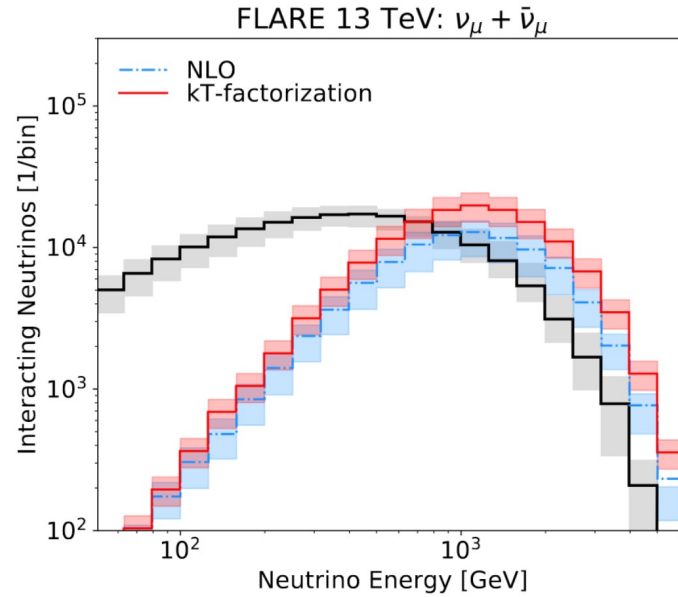
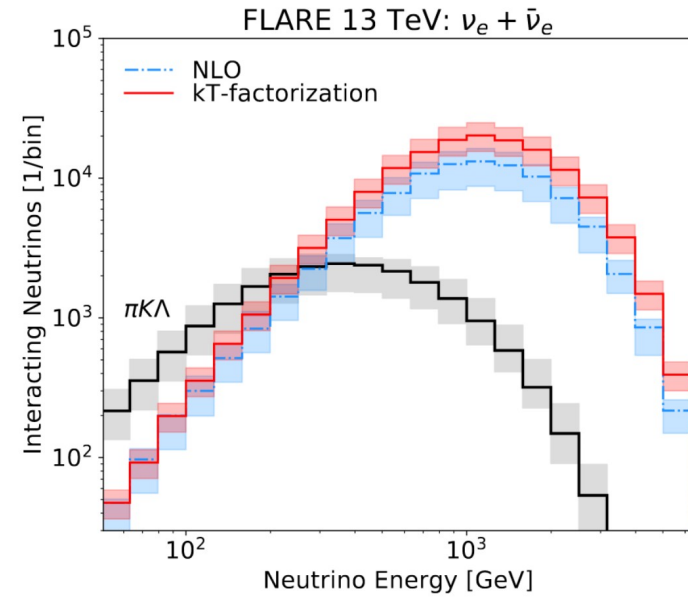
4000  $\nu_e$ , 4000  $\nu_\mu$ , and 120  $\nu_\tau$   
@FASERv during LHC Run 3

# Neutrino fluxes Estimates for FASERv



140,000  $\nu_e$  and  $\bar{\nu}_e$ , and 6000  $\nu_\tau$   
@FLARE during HL-LHC

# Neutrino fluxes Estimates for FLARE



# Conclusions

## Results

- ✓  $pp \rightarrow c\bar{c}$ : NLO-collinear and  $k_T$  factorisations
- ✓ Best-fits against LHCb 13 TeV data; associated uncertainties
- ✓ Pythia-based fragmentation scheme to better model high- $y$ , low- $p_T$  hadronisation
- ✓ Consistency check against 7 TeV LHCb data (not used for fits)
- ✓ Predictions for neutrino events at FASER $\nu$  and, for the future, at FLARE

## TODO

- $k_T$  factorisation: Need NLO-level cross-sections
  - ◆ Data-driven  $k$ -factor precludes proper comparisons
- Fragmentation schemes relevant for forward kinematics
- Comparisons involving different event generators



# Outlook

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- LHC-FPF driving us into an era of forward neutrino detection
- FASER $\nu$  and SND@LHC currently operational
  - Proposed detector FLARE during HL-LHC
- $\nu_e$  and  $\nu_\tau$  channels provide potential for detecting neutrinos from charmed mesons
- With future collider data, *and more theoretical work*, potential for constraining QCD parameters related to charm
- Improved atmospheric  $\nu$  background estimates for high-energy neutrino telescopes thanks to better QCD