

# Leading Directions in SMEFT

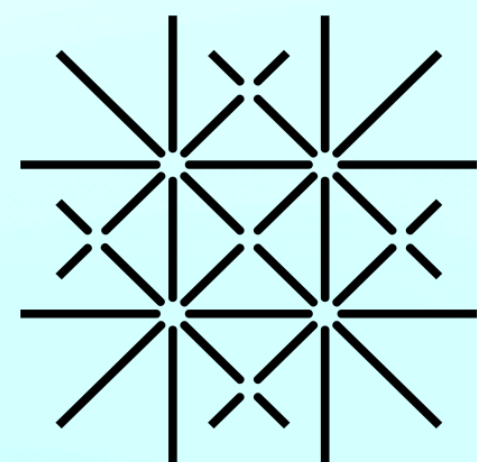
Ajdin Palavrić

In collaboration with: Admir Greljo and Anders Eller Thomsen

Based on arXiv: [2203.09561] and [2305.08898]

**6th General Meeting of the LHC EFT Working Group**

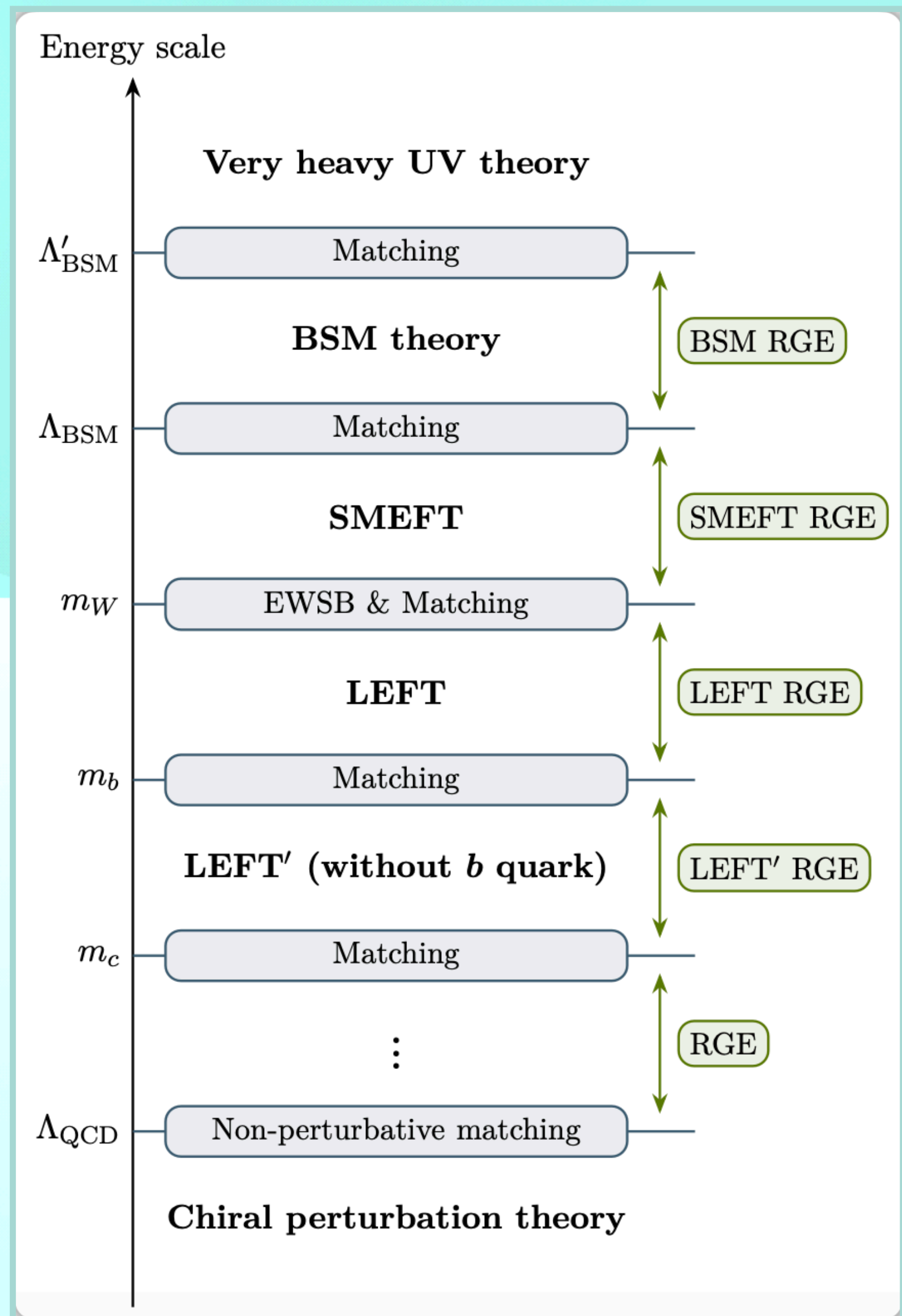
CERN, 17.11.2023.



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Basel**

# Introduction

# Introduction: EFT general perspective

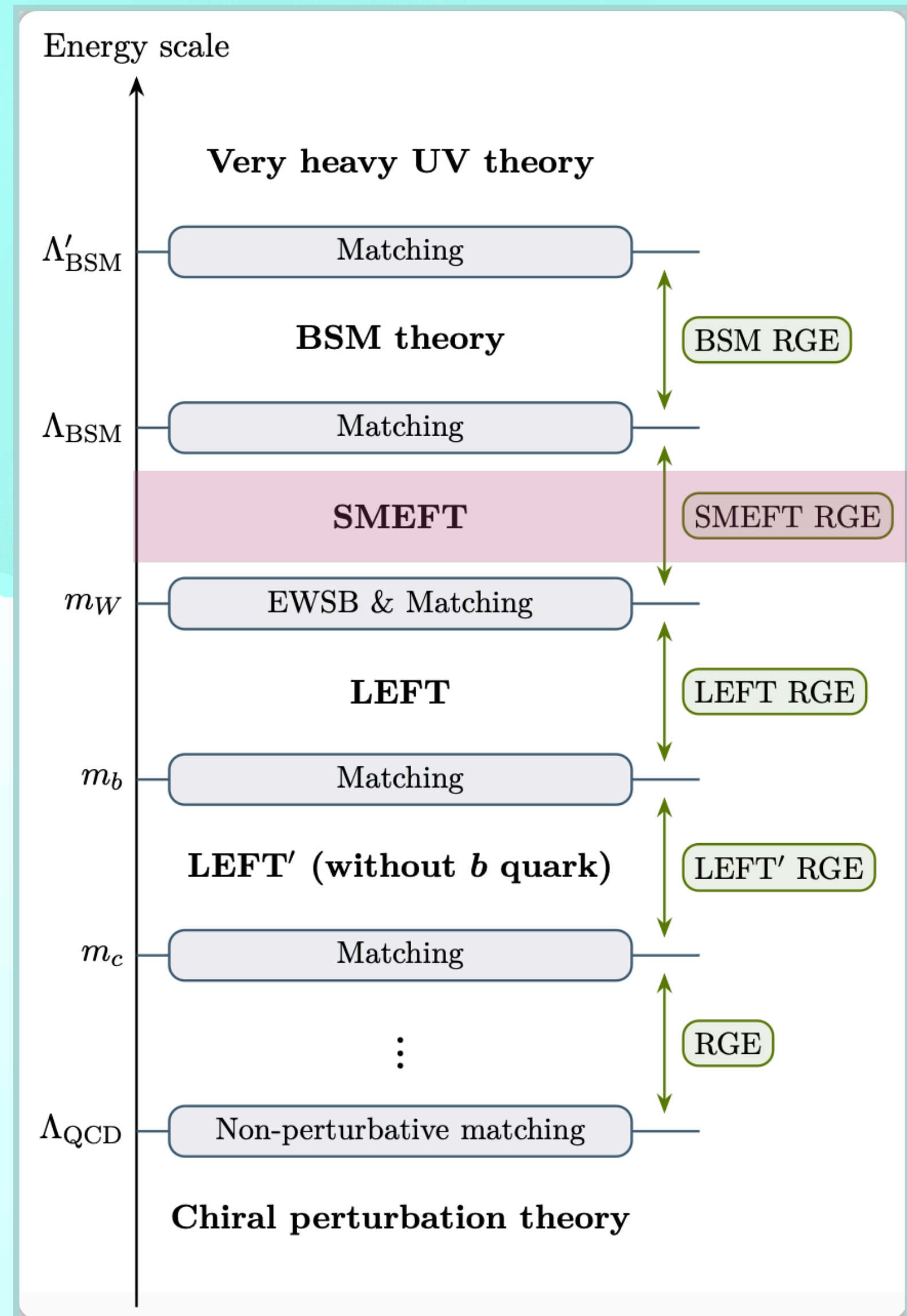


- Inclusion of the effects of the new physics in an EFT description

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}^{d=4} + \sum_{d=5}^{\infty} \sum_k \frac{C^{(d,k)}}{\Lambda^{d-4}} \mathcal{O}^{(d,k)}$$

- Wilson coefficients  $C^{(d,k)}$  contain the information on the UV physics
- Two distinct approaches in the construction of the EFTs
  - Bottom-up: model-independent analysis with deviations quantified as the  $E/\Lambda$  expansion
  - Top-down: starting from a higher scale, facilitate the precision computations in order to move towards the lower scales

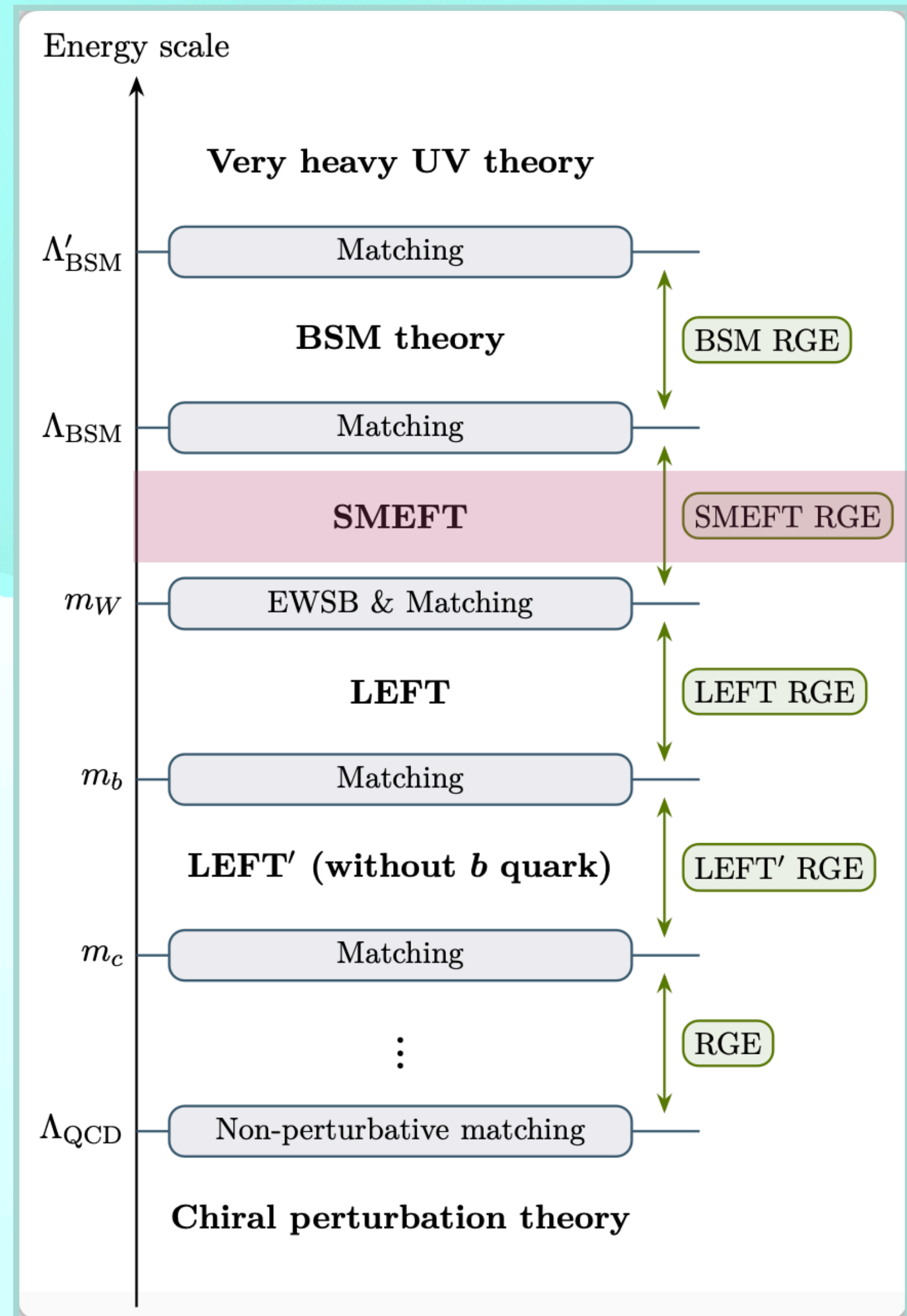
# Introduction: SMEFT



- In the EFT program, Standard Model effective field theory (SMEFT) is of particular relevance
- Connection of BSM physics and the low energy EFTs
- Construction of the SMEFT:
  - SM fields + symmetries (gauge and Poincaré)
  - Existence of the scale separation
  - Higher-dimensional operators

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \mathcal{O}(\Lambda^{-3})$$

# Introduction: SMEFT operators and bases

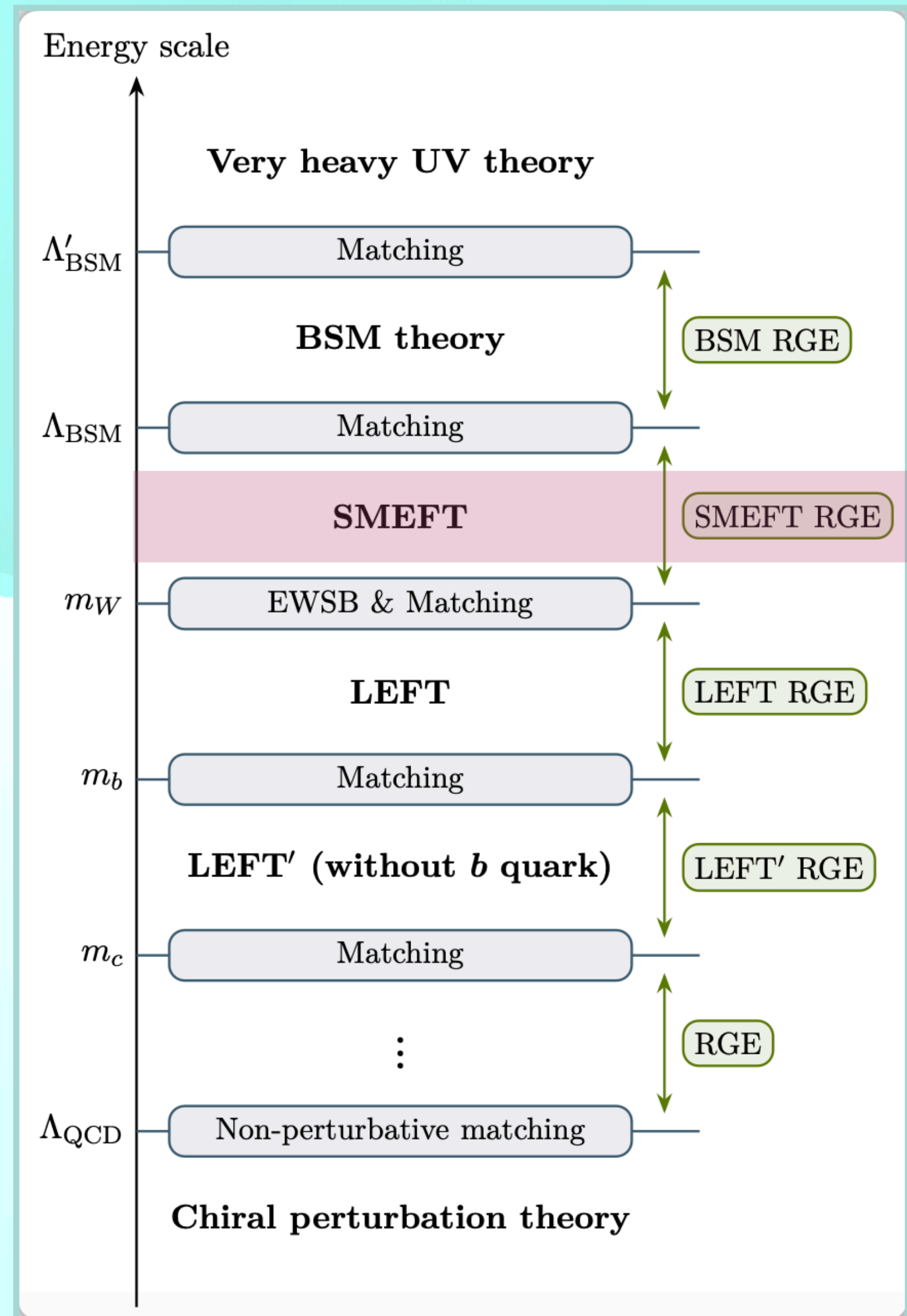


- Higher-dimensional operators are collected in the non-redundant operator bases
  - Dimension 6  
Grzadkowski, Iskrzynski, Misiak, Rosiek [1008.4884]
  - Dimension 7  
Liao, Ma [1612.04527], Lehman [1410.4193]
  - Dimension 8  
Murphy [2005.00059]
  - Hilbert series  
Henning, Lu, Melia, Murayama [1507.07240]  
Marinissen, Rahn, Waalewijn [2004.09521]
- Automation tools
  - Sym2Int  
Fonseca [1703.05221]
  - AutoEFT  
Harlander, Schaaf [2309.15783]



SYM2INT

# Introduction: SMEFT operators and bases



- Higher-dimensional operators are collected in the non-redundant operator bases

- Dimension 6**

Grzadkowski, Iskrzynski, Misiak, Rosiek [1008.4884]

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SYM2INT

# Introduction: dimension-6 operators

- Large number of independent parameters already at dimension 6
  - Single generation: 59
  - Three generations: 2499

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
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		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
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$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^m]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{dnu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
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# Introduction: dimension-6 operators

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  - Single generation: 59
  - Three generations: 2499
- This suggests that the proliferation of parameters originates from the **flavor structure**

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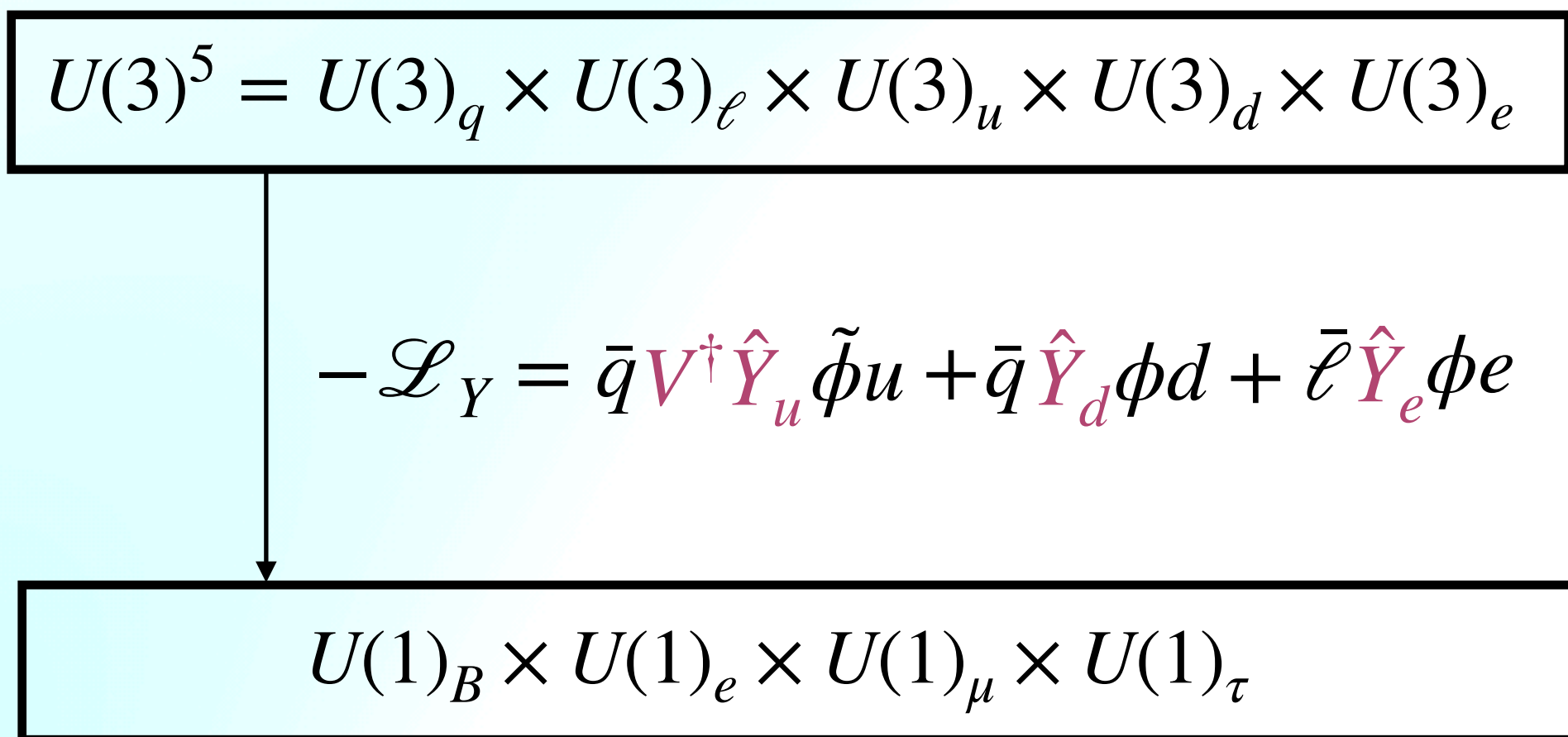
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Grzadkowski, Iskrzynski, Misiak, Rosiek [1008.4884]



# Introduction: dimension-6 operators

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  - Three generations: 2499
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- In the Standard Model

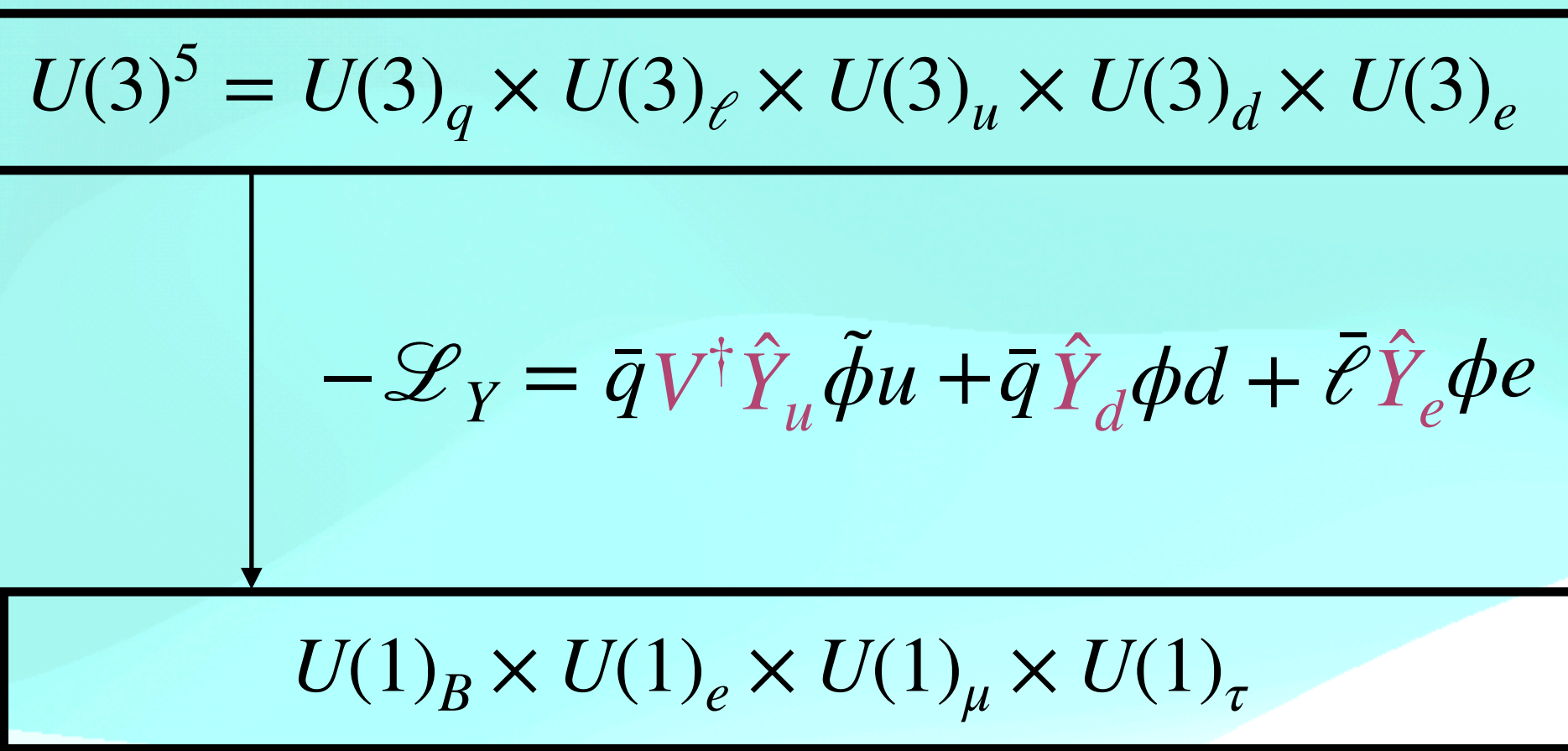


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$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^m]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

# Introduction: dimension-6 operators

- In the Standard Model



- However, observed mass hierarchy and the CKM alignment point to **approximate accidental symmetries**
- This is the starting point of our analysis

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_\mu^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_\mu^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_\mu^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_\mu^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{WB}}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_\mu^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\varphi^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^k q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jnk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

# Flavor structure of the SMEFT

# Viable options

- Subgroups of  $U(3)^5$  explored

$$U(3)^5 = U(3)_q \times U(3)_u \times U(3)_d \times U(3)_\ell \times U(3)_e$$

# Viable options: quark and lepton sector

- Subgroups of  $U(3)^5$  explored

$$U(3)^5 = U(3)_q \times U(3)_u \times U(3)_d \times U(3)_\ell \times U(3)_e$$

Quark sector

- $\text{MFV}_Q \equiv U(3)^3$
- $U(2)^2 \times U(3)_d$
- $U(2)^3 \times U(1)_{b_r}$
- $U(2)^3$

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## Quark sector

- $\text{MFV}_Q \equiv U(3)^3$
- $U(2)^2 \times U(3)_d$
- $U(2)^3 \times U(1)_{b_r}$
- $U(2)^3$

## Lepton sector

- $\text{MFV}_L \equiv U(3)^2$
- $U(3)_V, U(2)_V$
- $U(2)^2 \times U(1)^2, U(2)^2$
- $U(1)^6, U(1)^3$

# Viabile options: quark and lepton sector

- Subgroups of  $U(3)^5$  explored

$$U(3)^5 = U(3)_q \times U(3)_u \times U(3)_d \times U(3)_\ell \times U(3)_e$$

Quark sector

- $\text{MFV}_Q \equiv U(3)^3$
- $U(2)^2 \times U(3)_d$
- $U(2)^3 \times U(1)_{b_r}$
- $U(2)^3$

Lepton sector

- $\text{MFV}_L \equiv U(3)^2$
- $U(3)_V, U(2)_V$
- $U(2)^2 \times U(1)^2, U(2)^2$
- $U(1)^6, U(1)^3$

28 cases

# Construction of flavor invariants

- MFV<sub>Q</sub> example:  $G_F = U(3)_q \times U(3)_u \times U(3)_d$
- Fields  $q \sim (3,1,1)$ ,  $u \sim (1,3,1)$ ,  $d \sim (1,1,3)$
- Spurions  $Y_u \sim (3,\bar{3},1)$  and  $Y_d \sim (3,1,\bar{3})$



# Construction of flavor invariants

- MFV<sub>Q</sub> example:  $G_F = U(3)_q \times U(3)_u \times U(3)_d$
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- Spurions  $Y_u \sim (3,\bar{3},1)$  and  $Y_d \sim (3,1,\bar{3})$

## Examples of $2\psi$ flavor invariants

$$(\bar{q}q) : \begin{cases} \mathcal{O}(1) : (\bar{q}q) \\ \mathcal{O}(Y_u^2) : (\bar{q}Y_u Y_u^\dagger q) \\ \mathcal{O}(Y_d^2) : (\bar{q}Y_d Y_d^\dagger q) \end{cases}$$

$$(\bar{u}u) : \begin{cases} \mathcal{O}(1) : (\bar{u}u) \\ \mathcal{O}(Y_u^2) : (\bar{u}Y_u^\dagger Y_u u) \end{cases}$$

$$(\bar{d}d) : \begin{cases} \mathcal{O}(1) : (\bar{d}d) \\ \mathcal{O}(Y_d^2) : (\bar{d}Y_d^\dagger Y_d d) \end{cases}$$

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

# Construction of flavor invariants

- MFV<sub>Q</sub> example:  $G_F = U(3)_q \times U(3)_u \times U(3)_d$
- Fields  $q \sim (3,1,1)$ ,  $u \sim (1,3,1)$ ,  $d \sim (1,1,3)$
- Spurions  $Y_u \sim (3,\bar{3},1)$  and  $Y_d \sim (3,1,\bar{3})$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^j)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{quu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

## Examples of $4\psi$ flavor invariants

$$\begin{aligned}
 (\bar{q}q)(\bar{q}q) : & \left[ \begin{array}{l} \mathcal{O}(1) : (\bar{q}_i q^i)(\bar{q}_j q^j), (\bar{q}_i q^j)(\bar{q}_j q^i) \\ \mathcal{O}(Y_u^2) : (\bar{q} Y_u Y_u^\dagger q)(\bar{q}q), (\bar{q}_i q^j)(Y_u Y_u^\dagger)_k^i (\bar{q}^k q_j) \\ \mathcal{O}(Y_d^2) : (\bar{q} Y_d Y_d^\dagger q)(\bar{q}q), (\bar{q}_i q^j)(Y_d Y_d^\dagger)_k^i (\bar{q}^k q_j) \end{array} \right. \\
 (\bar{u}u)(\bar{u}u) : & \left[ \begin{array}{l} \mathcal{O}(1) : (\bar{u}_i u^i)(\bar{u}_j u^j), (\bar{u}_i u^j)(\bar{u}_j u^i) \\ \mathcal{O}(Y_u^2) : (\bar{u} Y_u^\dagger Y_u u)(\bar{u}u), (\bar{u}_i u^j)(Y_u^\dagger Y_u)_k^i (\bar{u}_j u^k) \end{array} \right. \\
 (\bar{d}d)(\bar{d}d) : & \left[ \begin{array}{l} \mathcal{O}(1) : (\bar{d}_i d^i)(\bar{d}_j d^j), (\bar{d}_i d^j)(\bar{d}_j d^i) \\ \mathcal{O}(Y_d^2) : (\bar{d} Y_d^\dagger Y_d d)(\bar{d}d), (\bar{d}_i d^j)(Y_d^\dagger Y_d)_k^i (\bar{d}_j d^k) \end{array} \right.
 \end{aligned}$$

# Flavor counting

MFV <sub>Q</sub>		$\mathcal{O}(1)$	$\mathcal{O}(Y_u)$	$\mathcal{O}(Y_u^2)$	$\mathcal{O}(Y_d)$	$\mathcal{O}(Y_d^2)$	$\mathcal{O}(Y_u Y_d)$	$\mathcal{O}(Y_u^2 Y_d, Y_d^2 Y_u)$	$\mathcal{O}(Y_u^3, Y_d^3)$
$\psi^2 H^3$	$Q_{uH}$		1 1					1 1	1 1
	$Q_{dH}$				1 1			1 1	1 1
$\psi^2 XH$	$Q_{u(G,W,B)}$		3 3					3 3	3 3
	$Q_{d(G,W,B)}$				3 3			3 3	3 3
$\psi^2 H^2 D$	$Q_{Hq}^{(1,3)}$	2		2		2			
	$Q_{Hu}$	1		1					
	$Q_{Hd}$	1				1			
	$Q_{Hud}$						1 1		
$(LL)(LL)$	$Q_{qq}^{(1,3)}$	4		4		4			
$(RR)(RR)$	$Q_{uu}$	2		2					
	$Q_{dd}$	2				2			
	$Q_{ud}^{(1,8)}$	2		2		2			
$(LL)(RR)$	$Q_{qu}^{(1,8)}$	2		6		2			
	$Q_{qd}^{(1,8)}$	2		2		6			
$(LR)(LR)$	$Q_{quqd}^{(1,8)}$						4 4		
Total		18	4 4	19	4 4	19	5 5	8 8	8 8

Greljo, AP, Thomsen [2203.09561]

# Flavor counting

SMEFT dim-6 operator class

MFV <sub>Q</sub>		$\mathcal{O}(1)$	$\mathcal{O}(Y_u)$	$\mathcal{O}(Y_u^2)$	$\mathcal{O}(Y_d)$	$\mathcal{O}(Y_d^2)$	$\mathcal{O}(Y_u Y_d)$	$\mathcal{O}(Y_u^2 Y_d, Y_d^2 Y_u)$	$\mathcal{O}(Y_u^3, Y_d^3)$
$\psi^2 H^3$	$Q_{uH}$		1 1					1 1	1 1
	$Q_{dH}$				1 1			1 1	1 1
$\psi^2 XH$	$Q_{u(G,W,B)}$		3 3					3 3	3 3
	$Q_{d(G,W,B)}$				3 3			3 3	3 3
$\psi^2 H^2 D$	$Q_{Hq}^{(1,3)}$	2		2		2			
	$Q_{Hu}$	1		1					
	$Q_{Hd}$	1				1			
	$Q_{Hud}$						1 1		
$(LL)(LL)$	$Q_{qq}^{(1,3)}$	4		4		4			
$(RR)(RR)$	$Q_{uu}$	2		2					
	$Q_{dd}$	2				2			
	$Q_{ud}^{(1,8)}$	2		2		2			
$(LL)(RR)$	$Q_{qu}^{(1,8)}$	2		6		2			
	$Q_{qd}^{(1,8)}$	2		2		6			
$(LR)(LR)$	$Q_{quqd}^{(1,8)}$						4 4		
Total		18	4 4	19	4 4	19	5 5	8 8	8 8

Greljo, AP, Thomsen [2203.09561]

# Flavor counting

Orders in spurion insertions

SMEFT dim-6 operator class

MFV <sub>Q</sub>		$\mathcal{O}(1)$	$\mathcal{O}(Y_u)$	$\mathcal{O}(Y_u^2)$	$\mathcal{O}(Y_d)$	$\mathcal{O}(Y_d^2)$	$\mathcal{O}(Y_u Y_d)$	$\mathcal{O}(Y_u^2 Y_d, Y_d^2 Y_u)$	$\mathcal{O}(Y_u^3, Y_d^3)$
$\psi^2 H^3$	$Q_{uH}$		1 1					1 1	1 1
	$Q_{dH}$				1 1			1 1	1 1
$\psi^2 XH$	$Q_{u(G,W,B)}$		3 3					3 3	3 3
	$Q_{d(G,W,B)}$				3 3			3 3	3 3
$\psi^2 H^2 D$	$Q_{Hq}^{(1,3)}$	2		2		2			
	$Q_{Hu}$	1		1					
	$Q_{Hd}$	1				1			
	$Q_{Hud}$						1 1		
$(LL)(LL)$	$Q_{qq}^{(1,3)}$	4		4		4			
$(RR)(RR)$	$Q_{uu}$	2		2					
	$Q_{dd}$	2				2			
	$Q_{ud}^{(1,8)}$	2		2		2			
$(LL)(RR)$	$Q_{qu}^{(1,8)}$	2		6		2			
	$Q_{qd}^{(1,8)}$	2		2		6			
$(LR)(LR)$	$Q_{quqd}^{(1,8)}$						4 4		
Total		18	4 4	19	4 4	19	5 5	8 8	8 8

Greljo, AP, Thomsen [2203.09561]

# Flavor counting

Orders in spurion insertions

SMEFT dim-6 operator class

MFV <sub>Q</sub>		$\mathcal{O}(1)$	$\mathcal{O}(Y_u)$	$\mathcal{O}(Y_u^2)$	$\mathcal{O}(Y_d)$	$\mathcal{O}(Y_d^2)$	$\mathcal{O}(Y_u Y_d)$	$\mathcal{O}(Y_u^2 Y_d, Y_d^2 Y_u)$	$\mathcal{O}(Y_u^3, Y_d^3)$
$\psi^2 H^3$	$Q_{uH}$		1 1					1 1	1 1
	$Q_{dH}$				1 1			1 1	1 1
$\psi^2 XH$	$Q_{u(G,W,B)}$		3 3					3 3	3 3
	$Q_{d(G,W,B)}$				3 3			3 3	3 3
$\psi^2 H^2 D$	$Q_{Hq}^{(1,3)}$	2		2		2			
	$Q_{Hu}$	1		1					
	$Q_{Hd}$	1				1			
	$Q_{Hud}$						1 1		
$(LL)(LL)$	$Q_{qq}^{(1,3)}$	4		4		4			
$(RR)(RR)$	$Q_{uu}$	2		2					
	$Q_{dd}$	2				2			
	$Q_{ud}^{(1,8)}$	2		2		2			
$(LL)(RR)$	$Q_{qu}^{(1,8)}$	2		6		2			
	$Q_{qd}^{(1,8)}$	2		2		6			
$(LR)(LR)$	$Q_{quqd}^{(1,8)}$						4 4		
Total		18	4 4	19	4 4	19	5 5	8 8	8 8

Total number of independent structures at the given order in spurion expansion

Greljo, AP, Thomsen [2203.09561]

# Flavor counting: full $\mathcal{O}(1)$ result

- Repeating the similar exercise both for quark and lepton sector

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$ )		Lepton sector															
		MFV <sub>L</sub>		U(3) <sub>V</sub>		U(2) <sup>2</sup> × U(1) <sup>2</sup>		U(2) <sup>2</sup>		U(2) <sub>V</sub>		U(1) <sup>6</sup>		U(1) <sup>3</sup>		No symm.	
Quark sector	MFV <sub>Q</sub>	41	6	45	9	59	6	62	9	67	13	81	6	93	18	207	132
	U(2) <sup>2</sup> × U(3) <sub>d</sub>	72	10	78	15	95	10	100	15	107	21	122	10	140	28	281	169
	U(2) <sup>3</sup> × U(1) <sub>d3</sub>	86	10	92	15	111	10	116	12	123	21	140	10	158	28	305	175
	U(2) <sup>3</sup>	93	17	100	23	118	17	124	23	132	30	147	17	168	38	321	191
	No symmetry	703	570	734	600	756	591	786	621	818	652	813	612	906	705	1350	1149

# Flavor counting: full $\mathcal{O}(1)$ result

- Repeating the similar exercise both for quark and lepton sector

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$ )		Lepton sector															
		MFV <sub>L</sub>		U(3) <sub>V</sub>		U(2) <sup>2</sup> × U(1) <sup>2</sup>		U(2) <sup>2</sup>		U(2) <sub>V</sub>		U(1) <sup>6</sup>		U(1) <sup>3</sup>		No symm.	
Quark sector	MFV <sub>Q</sub>	41	6	45	9	59	6	62	9	67	13	81	6	93	18	207	132
	U(2) <sup>2</sup> × U(3) <sub>d</sub>	72	10	78	15	95	10	100	15	107	21	122	10	140	28	281	169
	U(2) <sup>3</sup> × U(1) <sub>d3</sub>	86	10	92	15	111	10	116	12	123	21	140	10	158	28	305	175
	U(2) <sup>3</sup>	93	17	100	23	118	17	124	23	132	30	147	17	168	38	321	191
	No symmetry	703	570	734	600	756	591	786	621	818	652	813	612	906	705	1350	1149

47 parameters in the MFV



# Flavor counting: full $\mathcal{O}(1)$ result

- Repeating the similar exercise both for quark and lepton sector

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$ )		Lepton sector															
		MFV <sub>L</sub>		U(3) <sub>V</sub>		U(2) <sup>2</sup> × U(1) <sup>2</sup>		U(2) <sup>2</sup>		U(2) <sub>V</sub>		U(1) <sup>6</sup>		U(1) <sup>3</sup>		No symm.	
Quark sector	MFV <sub>Q</sub>	41	6	45	9	59	6	62	9	67	13	81	6	93	18	207	132
	U(2) <sup>2</sup> × U(3) <sub>d</sub>	72	10	78	15	95	10	100	15	107	21	122	10	140	28	281	169
	U(2) <sup>3</sup> × U(1) <sub>d3</sub>	86	10	92	15	111	10	116	12	123	21	140	10	158	28	305	175
	U(2) <sup>3</sup>	93	17	100	23	118	17	124	23	132	30	147	17	168	38	321	191
	No symmetry	703	570	734	600	756	591	786	621	818	652	813	612	906	705	1350	1149

47 parameters in the MFV

147 parameters in  $U(2)^5$

Faroughy, Isidori, Wilsch, Yamamoto [2005.05366]

Greljo, AP, Thomsen [2203.09561]

# Flavor counting: full $\mathcal{O}(1)$ result

- Repeating the similar exercise both for quark and lepton sector

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$ )		Lepton sector															
		MFV <sub>L</sub>		U(3) <sub>V</sub>		U(2) <sup>2</sup> × U(1) <sup>2</sup>		U(2) <sup>2</sup>		U(2) <sub>V</sub>		U(1) <sup>6</sup>		U(1) <sup>3</sup>		No symm.	
Quark sector	MFV <sub>Q</sub>	41	6	45	9	59	6	62	9	67	13	81	6	93	18	207	132
	U(2) <sup>2</sup> × U(3) <sub>d</sub>	72	10	78	15	95	10	100	15	107	21	122	10	140	28	281	169
	U(2) <sup>3</sup> × U(1) <sub>d3</sub>	86	10	92	15	111	10	116	12	123	21	140	10	158	28	305	175
	U(2) <sup>3</sup>	93	17	100	23	118	17	124	23	132	30	147	17	168	38	321	191
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47 parameters in the MFV

147 parameters in  $U(2)^5$

Faroughy, Isidori, Wilsch, Yamamoto [2005.05366]

2499 parameters without any symmetries

Greljo, AP, Thomsen [2203.09561]

# **Leading directions in the SMEFT**

# Leading directions: MFV basis

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$ )		Lepton sector															
		MFV <sub>L</sub>		U(3) <sub>V</sub>		U(2) <sup>2</sup> × U(1) <sup>2</sup>		U(2) <sup>2</sup>		U(2) <sub>V</sub>		U(1) <sup>6</sup>		U(1) <sup>3</sup>		No symm.	
Quark sector	MFV <sub>Q</sub>	41	6	45	9	59	6	62	9	67	13	81	6	93	18	207	132
	U(2) <sup>2</sup> × U(3) <sub>d</sub>	72	10	78	15	95	10	100	15	107	21	122	10	140	28	281	169
	U(2) <sup>3</sup> × U(1) <sub>d3</sub>	86	10	92	15	111	10	116	12	123	21	140	10	158	28	305	175
	U(2) <sup>3</sup>	93	17	100	23	118	17	124	23	132	30	147	17	168	38	321	191
	No symmetry	703	570	734	600	756	591	786	621	818	652	813	612	906	705	1350	1149

47 parameters in the MFV

Class	Label	Operator	Label	Operator
$(\bar{L}L)(\bar{L}L)$	$\mathcal{O}_{\ell\ell}^D$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{\ell}_j\gamma_\mu\ell^j)$	$\mathcal{O}_{\ell q}^{(1)}$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{q}_j\gamma_\mu q^j)$
	$\mathcal{O}_{\ell\ell}^E$	$(\bar{\ell}_i\gamma^\mu\ell^j)(\bar{\ell}_j\gamma_\mu\ell^i)$	$\mathcal{O}_{\ell q}^{(3)}$	$(\bar{\ell}_i\gamma^\mu\sigma^a\ell^i)(\bar{q}_j\gamma_\mu\sigma^a q^j)$
	$\mathcal{O}_{qq}^{(1)D}$	$(\bar{q}_i\gamma^\mu q^i)(\bar{q}_j\gamma_\mu q^j)$	$\mathcal{O}_{qq}^{(3)D}$	$(\bar{q}_i\gamma^\mu\sigma^a q^i)(\bar{q}_j\gamma_\mu\sigma^a q^j)$
	$\mathcal{O}_{qq}^{(1)E}$	$(\bar{q}_i\gamma^\mu q^j)(\bar{q}_j\gamma_\mu q^i)$	$\mathcal{O}_{qq}^{(3)E}$	$(\bar{q}_i\gamma^\mu\sigma^a q^j)(\bar{q}_j\gamma_\mu\sigma^a q^i)$
$(\bar{R}R)(\bar{R}R)$	$\mathcal{O}_{ee}$	$(\bar{e}_i\gamma^\mu e^i)(\bar{e}_j\gamma_\mu e^j)$	$\mathcal{O}_{dd}^D$	$(\bar{d}_i\gamma^\mu d^i)(\bar{d}_j\gamma_\mu d^j)$
	$\mathcal{O}_{uu}^D$	$(\bar{u}_i\gamma^\mu u^i)(\bar{u}_j\gamma_\mu u^j)$	$\mathcal{O}_{dd}^E$	$(\bar{d}_i\gamma^\mu d^j)(\bar{d}_j\gamma_\mu d^i)$
	$\mathcal{O}_{uu}^E$	$(\bar{u}_i\gamma^\mu u^j)(\bar{u}_j\gamma_\mu u^i)$	$\mathcal{O}_{ud}^{(1)}$	$(\bar{u}_i\gamma^\mu u^i)(\bar{d}_j\gamma_\mu d^j)$
	$\mathcal{O}_{eu}$	$(\bar{e}_i\gamma^\mu e^i)(\bar{u}_j\gamma_\mu u^j)$	$\mathcal{O}_{ud}^{(8)}$	$(\bar{u}_i\gamma^\mu T^A u^i)(\bar{d}_j\gamma_\mu T^A d^j)$
$(\bar{L}L)(\bar{R}R)$	$\mathcal{O}_{le}$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{e}_j\gamma_\mu e^j)$	$\mathcal{O}_{qu}^{(1)}$	$(\bar{q}_i\gamma^\mu q^i)(\bar{u}_j\gamma_\mu u^j)$
	$\mathcal{O}_{qe}$	$(\bar{q}_i\gamma^\mu q^i)(\bar{e}_j\gamma_\mu e^j)$	$\mathcal{O}_{qu}^{(8)}$	$(\bar{q}_i\gamma^\mu T^A q^i)(\bar{u}_j\gamma_\mu T^A u^j)$
	$\mathcal{O}_{lu}$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{u}_j\gamma_\mu u^j)$	$\mathcal{O}_{qd}^{(1)}$	$(\bar{q}_i\gamma^\mu q^i)(\bar{d}_j\gamma_\mu d^j)$
	$\mathcal{O}_{ld}$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{d}_j\gamma_\mu d^j)$	$\mathcal{O}_{qd}^{(8)}$	$(\bar{q}_i\gamma^\mu T^A q^i)(\bar{d}_j\gamma_\mu T^A d^j)$
$\psi^2\phi^2D$	$\mathcal{O}_{\phi\ell}^{(1)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{\ell}_i\gamma^\mu\ell^i)$	$\mathcal{O}_{\phi e}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{e}_i\gamma^\mu e^i)$
	$\mathcal{O}_{\phi\ell}^{(3)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu^a\phi)(\bar{\ell}_i\gamma^\mu\sigma^a\ell^i)$	$\mathcal{O}_{\phi u}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{u}_i\gamma^\mu u^i)$
	$\mathcal{O}_{\phi q}^{(1)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{q}_i\gamma^\mu q^i)$	$\mathcal{O}_{\phi d}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{d}_i\gamma^\mu d^i)$
	$\mathcal{O}_{\phi q}^{(3)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu^a\phi)(\bar{q}_i\gamma^\mu\sigma^a q^i)$		

Class	Label	Operator	Label	Operator
$X^3$ Loop generated	$\mathcal{O}_W$	$\varepsilon_{abc}W_\mu^{a\nu}W_\nu^{b\rho}W_\rho^{c\mu}$	$\mathcal{O}_G$	$f_{ABC}G_\mu^{A\nu}G_\nu^{B\rho}G_\rho^{C\mu}$
	$\mathcal{O}_{\tilde{W}}$	$\varepsilon_{abc}\tilde{W}_\mu^{a\nu}W_\nu^{b\rho}W_\rho^{c\mu}$	$\mathcal{O}_{\tilde{G}}$	$f_{ABC}\tilde{G}_\mu^{A\nu}G_\nu^{B\rho}G_\rho^{C\mu}$
$\phi^6$	$\mathcal{O}_\phi$	$(\phi^\dagger\phi)^3$		
$\phi^4D^2$	$\mathcal{O}_{\phi\Box}$	$(\phi^\dagger\phi)\Box(\phi^\dagger\phi)$	$\mathcal{O}_{\phi D}$	$(\phi^\dagger D_\mu\phi)[(D^\mu\phi)^\dagger\phi]$
	$\mathcal{O}_{\phi B}$	$(\phi^\dagger\phi)B_{\mu\nu}B^{\mu\nu}$	$\mathcal{O}_{\phi WB}$	$(\phi^\dagger\sigma^a\phi)W_{\mu\nu}^a B^{\mu\nu}$
	$\mathcal{O}_{\phi\tilde{B}}$	$(\phi^\dagger\phi)\tilde{B}_{\mu\nu}B^{\mu\nu}$	$\mathcal{O}_{\phi\tilde{W}B}$	$(\phi^\dagger\sigma^a\phi)\tilde{W}_{\mu\nu}^a B^{\mu\nu}$
	$X^2\phi^2$ Loop generated	$\mathcal{O}_{\phi W}$	$(\phi^\dagger\phi)W_{\mu\nu}^a W^{a\mu\nu}$	$\mathcal{O}_{\phi G}$
$\mathcal{O}_{\phi\tilde{W}}$		$(\phi^\dagger\phi)\tilde{W}_{\mu\nu}^a W^{a\mu\nu}$	$\mathcal{O}_{\phi\tilde{G}}$	$(\phi^\dagger\phi)\tilde{G}_{\mu\nu}^A G^{A\mu\nu}$

Class	Label	Operator	Label	Operator
$\psi^2\phi^3$	$[\mathcal{O}_{e\phi}]_{i\ell}^{j_e}$	$(\phi^\dagger\phi)(\bar{\ell}_i\ell^j e^e)$	$[\mathcal{O}_{u\phi}]_{iq}^{ju}$	$(\phi^\dagger\phi)(\bar{q}_i q^j u^u)$
	$[\mathcal{O}_{d\phi}]_{iq}^{jd}$	$(\phi^\dagger\phi)(\bar{q}_i q^j d^d)$		
$\psi^2 X\phi$ Loop generated	$[\mathcal{O}_{eB}]_{i\ell}^{j_e}$	$(\bar{\ell}_i\sigma^{\mu\nu}e^e)\phi B_{\mu\nu}$	$[\mathcal{O}_{eW}]_{i\ell}^{j_e}$	$(\bar{\ell}_i\sigma^{\mu\nu}e^e)\sigma^a\phi W_{\mu\nu}^a$
	$[\mathcal{O}_{uB}]_{iq}^{ju}$	$(\bar{q}_i\sigma^{\mu\nu}u^j)\phi B_{\mu\nu}$	$[\mathcal{O}_{uW}]_{iq}^{ju}$	$(\bar{q}_i\sigma^{\mu\nu}u^j)\sigma^a\phi W_{\mu\nu}^a$
	$[\mathcal{O}_{dB}]_{iq}^{jd}$	$(\bar{q}_i\sigma^{\mu\nu}d^j)\phi B_{\mu\nu}$	$[\mathcal{O}_{dW}]_{iq}^{jd}$	$(\bar{q}_i\sigma^{\mu\nu}d^j)\sigma^a\phi W_{\mu\nu}^a$
	$[\mathcal{O}_{uG}]_{iq}^{ju}$	$(\bar{q}_i\sigma^{\mu\nu}T^A u^j)\phi G_{\mu\nu}^A$	$[\mathcal{O}_{dG}]_{iq}^{jd}$	$(\bar{q}_i\sigma^{\mu\nu}T^A d^j)\phi G_{\mu\nu}^A$

# Leading directions: MFV basis

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$ )		Lepton sector															
		MFV <sub>L</sub>		U(3) <sub>V</sub>		U(2) <sup>2</sup> × U(1) <sup>2</sup>		U(2) <sup>2</sup>		U(2) <sub>V</sub>		U(1) <sup>6</sup>		U(1) <sup>3</sup>		No symm.	
Quark sector	MFV <sub>Q</sub>	41	6	45	9	59	6	62	9	67	13	81	6	93	18	207	132
	U(2) <sup>2</sup> × U(3) <sub>d</sub>	72	10	78	15	95	10	100	15	107	21	122	10	140	28	281	169
	U(2) <sup>3</sup> × U(1) <sub>d3</sub>	86	10	92	15	111	10	116	12	123	21	140	10	158	28	305	175
	U(2) <sup>3</sup>	93	17	100	23	118	17	124	23	132	30	147	17	168	38	321	191
	No symmetry	703	570	734	600	756	591	786	621	818	652	813	612	906	705	1350	1149

47 parameters in the MFV

- In a renormalizable UV completion, operators can be generated at tree-level
- What are all tree-level UV completions that match to these operators?

Class	Label	Operator	Label	Operator
$(\bar{L}L)(\bar{L}L)$	$\mathcal{O}_{\ell\ell}^D$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{\ell}_j\gamma_\mu\ell^j)$	$\mathcal{O}_{\ell q}^{(1)}$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{q}_j\gamma_\mu q^j)$
	$\mathcal{O}_{\ell\ell}^E$	$(\bar{\ell}_i\gamma^\mu\ell^j)(\bar{\ell}_j\gamma_\mu\ell^i)$	$\mathcal{O}_{\ell q}^{(3)}$	$(\bar{\ell}_i\gamma^\mu\sigma^a\ell^i)(\bar{q}_j\gamma_\mu\sigma^a q^j)$
	$\mathcal{O}_{qq}^{(1)D}$	$(\bar{q}_i\gamma^\mu q^i)(\bar{q}_j\gamma_\mu q^j)$	$\mathcal{O}_{qq}^{(3)D}$	$(\bar{q}_i\gamma^\mu\sigma^a q^i)(\bar{q}_j\gamma_\mu\sigma^a q^j)$
	$\mathcal{O}_{qq}^{(1)E}$	$(\bar{q}_i\gamma^\mu q^j)(\bar{q}_j\gamma_\mu q^i)$	$\mathcal{O}_{qq}^{(3)E}$	$(\bar{q}_i\gamma^\mu\sigma^a q^j)(\bar{q}_j\gamma_\mu\sigma^a q^i)$
$(\bar{R}R)(\bar{R}R)$	$\mathcal{O}_{ee}$	$(\bar{e}_i\gamma^\mu e^i)(\bar{e}_j\gamma_\mu e^j)$	$\mathcal{O}_{dd}^D$	$(\bar{d}_i\gamma^\mu d^i)(\bar{d}_j\gamma_\mu d^j)$
	$\mathcal{O}_{uu}^D$	$(\bar{u}_i\gamma^\mu u^i)(\bar{u}_j\gamma_\mu u^j)$	$\mathcal{O}_{dd}^E$	$(\bar{d}_i\gamma^\mu d^j)(\bar{d}_j\gamma_\mu d^i)$
	$\mathcal{O}_{uu}^E$	$(\bar{u}_i\gamma^\mu u^j)(\bar{u}_j\gamma_\mu u^i)$	$\mathcal{O}_{ud}^{(1)}$	$(\bar{u}_i\gamma^\mu u^i)(\bar{d}_j\gamma_\mu d^j)$
	$\mathcal{O}_{eu}$	$(\bar{e}_i\gamma^\mu e^i)(\bar{u}_j\gamma_\mu u^j)$	$\mathcal{O}_{ud}^{(8)}$	$(\bar{u}_i\gamma^\mu T^A u^i)(\bar{d}_j\gamma_\mu T^A d^j)$
$(\bar{L}L)(\bar{R}R)$	$\mathcal{O}_{le}$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{e}_j\gamma_\mu e^j)$	$\mathcal{O}_{qu}^{(1)}$	$(\bar{q}_i\gamma^\mu q^i)(\bar{u}_j\gamma_\mu u^j)$
	$\mathcal{O}_{qe}$	$(\bar{q}_i\gamma^\mu q^i)(\bar{e}_j\gamma_\mu e^j)$	$\mathcal{O}_{qu}^{(8)}$	$(\bar{q}_i\gamma^\mu T^A q^i)(\bar{u}_j\gamma_\mu T^A u^j)$
	$\mathcal{O}_{lu}$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{u}_j\gamma_\mu u^j)$	$\mathcal{O}_{qd}^{(1)}$	$(\bar{q}_i\gamma^\mu q^i)(\bar{d}_j\gamma_\mu d^j)$
	$\mathcal{O}_{ld}$	$(\bar{\ell}_i\gamma^\mu\ell^i)(\bar{d}_j\gamma_\mu d^j)$	$\mathcal{O}_{qd}^{(8)}$	$(\bar{q}_i\gamma^\mu T^A q^i)(\bar{d}_j\gamma_\mu T^A d^j)$
$\psi^2\phi^2D$	$\mathcal{O}_{\phi\ell}^{(1)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{\ell}_i\gamma^\mu\ell^i)$	$\mathcal{O}_{\phi e}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{e}_i\gamma^\mu e^i)$
	$\mathcal{O}_{\phi\ell}^{(3)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu^a\phi)(\bar{\ell}_i\gamma^\mu\sigma^a\ell^i)$	$\mathcal{O}_{\phi u}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{u}_i\gamma^\mu u^i)$
	$\mathcal{O}_{\phi q}^{(1)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{q}_i\gamma^\mu q^i)$	$\mathcal{O}_{\phi d}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu\phi)(\bar{d}_i\gamma^\mu d^i)$
	$\mathcal{O}_{\phi q}^{(3)}$	$(\phi^\dagger i\overleftrightarrow{D}_\mu^a\phi)(\bar{q}_i\gamma^\mu\sigma^a q^i)$		

Class	Label	Operator	Label	Operator
$X^3$ Loop generated	$\mathcal{O}_W$	$\varepsilon_{abc}W_\mu^{a\nu}W_\nu^{b\rho}W_\rho^{c\mu}$	$\mathcal{O}_G$	$f_{ABC}G_\mu^{A\nu}G_\nu^{B\rho}G_\rho^{C\mu}$
	$\mathcal{O}_{\tilde{W}}$	$\varepsilon_{abc}\tilde{W}_\mu^{a\nu}W_\nu^{b\rho}W_\rho^{c\mu}$	$\mathcal{O}_{\tilde{G}}$	$f_{ABC}\tilde{G}_\mu^{A\nu}G_\nu^{B\rho}G_\rho^{C\mu}$
$\phi^6$	$\mathcal{O}_\phi$	$(\phi^\dagger\phi)^3$		
$\phi^4D^2$	$\mathcal{O}_{\phi\Box}$	$(\phi^\dagger\phi)\Box(\phi^\dagger\phi)$	$\mathcal{O}_{\phi D}$	$(\phi^\dagger D_\mu\phi)[(D^\mu\phi)^\dagger\phi]$
$X^2\phi^2$ Loop generated	$\mathcal{O}_{\phi B}$	$(\phi^\dagger\phi)B_{\mu\nu}B^{\mu\nu}$	$\mathcal{O}_{\phi WB}$	$(\phi^\dagger\sigma^a\phi)W_{\mu\nu}^a B^{\mu\nu}$
	$\mathcal{O}_{\phi\tilde{B}}$	$(\phi^\dagger\phi)\tilde{B}_{\mu\nu}B^{\mu\nu}$	$\mathcal{O}_{\phi\tilde{W}B}$	$(\phi^\dagger\sigma^a\phi)\tilde{W}_{\mu\nu}^a B^{\mu\nu}$
	$\mathcal{O}_{\phi W}$	$(\phi^\dagger\phi)W_{\mu\nu}^a W^{a\mu\nu}$	$\mathcal{O}_{\phi G}$	$(\phi^\dagger\phi)G_{\mu\nu}^A G^{A\mu\nu}$
	$\mathcal{O}_{\phi\tilde{W}}$	$(\phi^\dagger\phi)\tilde{W}_{\mu\nu}^a W^{a\mu\nu}$	$\mathcal{O}_{\phi\tilde{G}}$	$(\phi^\dagger\phi)\tilde{G}_{\mu\nu}^A G^{A\mu\nu}$

Class	Label	Operator	Label	Operator
$\psi^2\phi^3$	$[\mathcal{O}_{e\phi}]_{i\ell}^{j_e}$	$(\phi^\dagger\phi)(\bar{\ell}_i\ell^j e^e)$	$[\mathcal{O}_{u\phi}]_{iq}^{ju}$	$(\phi^\dagger\phi)(\bar{q}_i q^j u^u)$
	$[\mathcal{O}_{d\phi}]_{iq}^{jd}$	$(\phi^\dagger\phi)(\bar{q}_i q^j d^d)$		
$\psi^2 X\phi$ Loop generated	$[\mathcal{O}_{eB}]_{i\ell}^{j_e}$	$(\bar{\ell}_i\sigma^{\mu\nu}e^j)\phi B_{\mu\nu}$	$[\mathcal{O}_{eW}]_{i\ell}^{j_e}$	$(\bar{\ell}_i\sigma^{\mu\nu}e^j)\sigma^a\phi W_{\mu\nu}^a$
	$[\mathcal{O}_{uB}]_{iq}^{ju}$	$(\bar{q}_i\sigma^{\mu\nu}u^j)\phi B_{\mu\nu}$	$[\mathcal{O}_{uW}]_{iq}^{ju}$	$(\bar{q}_i\sigma^{\mu\nu}u^j)\sigma^a\phi W_{\mu\nu}^a$
	$[\mathcal{O}_{dB}]_{iq}^{jd}$	$(\bar{q}_i\sigma^{\mu\nu}d^j)\phi B_{\mu\nu}$	$[\mathcal{O}_{dW}]_{iq}^{jd}$	$(\bar{q}_i\sigma^{\mu\nu}d^j)\sigma^a\phi W_{\mu\nu}^a$
	$[\mathcal{O}_{uG}]_{iq}^{ju}$	$(\bar{q}_i\sigma^{\mu\nu}T^A u^j)\phi G_{\mu\nu}^A$	$[\mathcal{O}_{dG}]_{iq}^{jd}$	$(\bar{q}_i\sigma^{\mu\nu}T^A d^j)\phi G_{\mu\nu}^A$

# Leading directions: SM + 1 NP

- Assume the extension of the Standard Model by one New Physics mediator

# Leading directions: SM + 1 NP

- Assume the extension of the Standard Model by one New Physics mediator

NP Mediators

Scalars

$\mathcal{S}$	$\mathcal{S}_1$	$\mathcal{S}_2$	$\varphi$	$\Xi$	$\Xi_1$	$\Theta_1$	$\Theta_3$
$(1,1)_0$	$(1,1)_1$	$(1,1)_2$	$(1,2)_{\frac{1}{2}}$	$(1,3)_0$	$(1,3)_1$	$(1,4)_{\frac{1}{2}}$	$(1,4)_{\frac{3}{2}}$
$\omega_1$	$\omega_2$	$\omega_4$	$\Pi_1$	$\Pi_7$	$\zeta$		
$(3,1)_{-\frac{1}{3}}$	$(3,1)_{\frac{2}{3}}$	$(3,1)_{-\frac{4}{3}}$	$(3,2)_{\frac{1}{6}}$	$(3,2)_{\frac{7}{6}}$	$(3,3)_{-\frac{1}{3}}$		
$\Omega_1$	$\Omega_2$	$\Omega_4$	$\Upsilon$	$\Phi$			
$(6,1)_{\frac{1}{3}}$	$(6,1)_{-\frac{2}{3}}$	$(6,1)_{\frac{4}{3}}$	$(6,3)_{\frac{1}{3}}$	$(8,2)_{\frac{1}{2}}$			

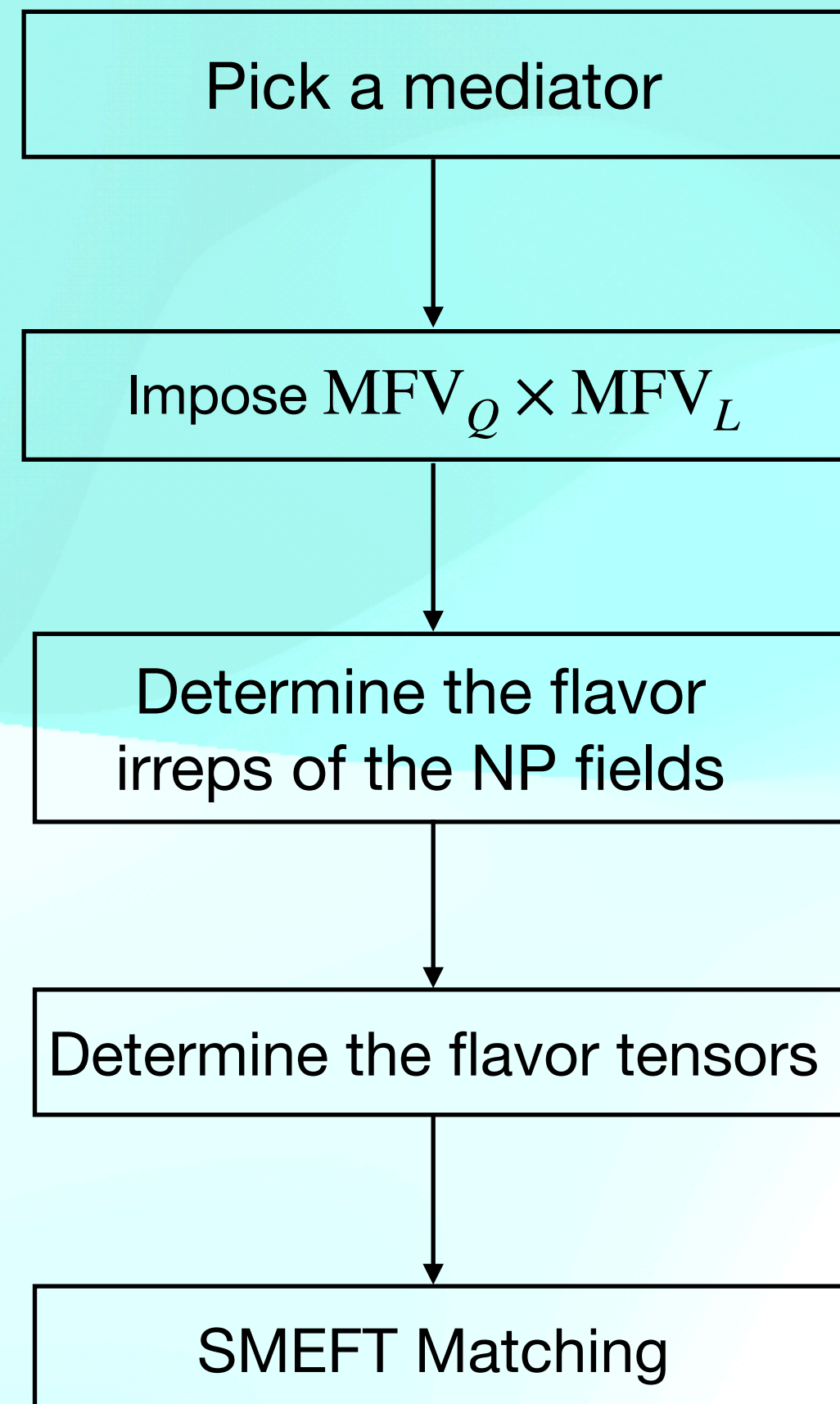
Fermions

$N$	$E$	$\Delta_1$	$\Delta_3$	$\Sigma$	$\Sigma_1$	
$(1,1)_0$	$(1,1)_{-1}$	$(1,2)_{-\frac{1}{2}}$	$(1,2)_{-\frac{3}{2}}$	$(1,3)_0$	$(1,3)_{-1}$	
$U$	$D$	$Q_1$	$Q_5$	$Q_7$	$T_1$	$T_2$
$(3,1)_{\frac{2}{3}}$	$(3,1)_{-\frac{1}{3}}$	$(3,2)_{\frac{1}{6}}$	$(3,2)_{-\frac{5}{6}}$	$(3,2)_{\frac{7}{6}}$	$(3,3)_{-\frac{1}{3}}$	$(3,3)_{\frac{2}{3}}$

Vectors

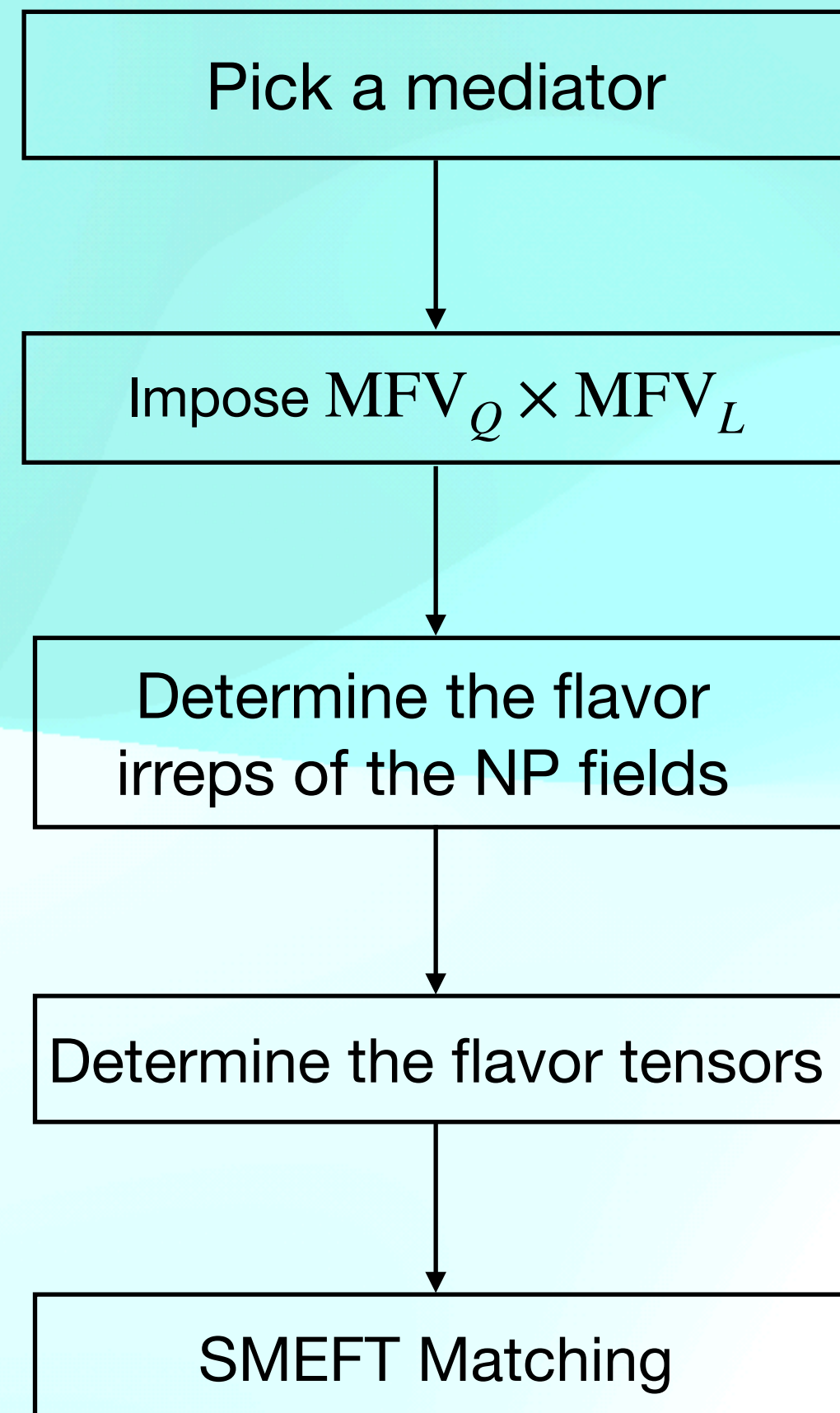
$\mathcal{B}$	$\mathcal{B}_1$	$\mathcal{W}$	$\mathcal{W}_1$	$\mathcal{G}$	$\mathcal{G}_1$	$\mathcal{H}$	$\mathcal{L}_1$
$(1,1)_0$	$(1,1)_1$	$(1,3)_0$	$(1,3)_1$	$(8,1)_0$	$(8,1)_1$	$(8,3)_0$	$(1,2)_{\frac{1}{2}}$
$\mathcal{L}_3$	$\mathcal{U}_2$	$\mathcal{U}_5$	$\mathcal{Q}_1$	$\mathcal{Q}_5$	$\mathcal{X}$	$\mathcal{Y}_1$	$\mathcal{Y}_5$
$(1,2)_{-\frac{3}{2}}$	$(3,1)_{\frac{2}{3}}$	$(3,1)_{\frac{5}{3}}$	$(3,2)_{\frac{1}{6}}$	$(3,2)_{-\frac{5}{6}}$	$(3,3)_{\frac{2}{3}}$	$(\bar{6},2)_{\frac{1}{6}}$	$(\bar{6},2)_{-\frac{5}{6}}$

# Leading directions: Procedure and example



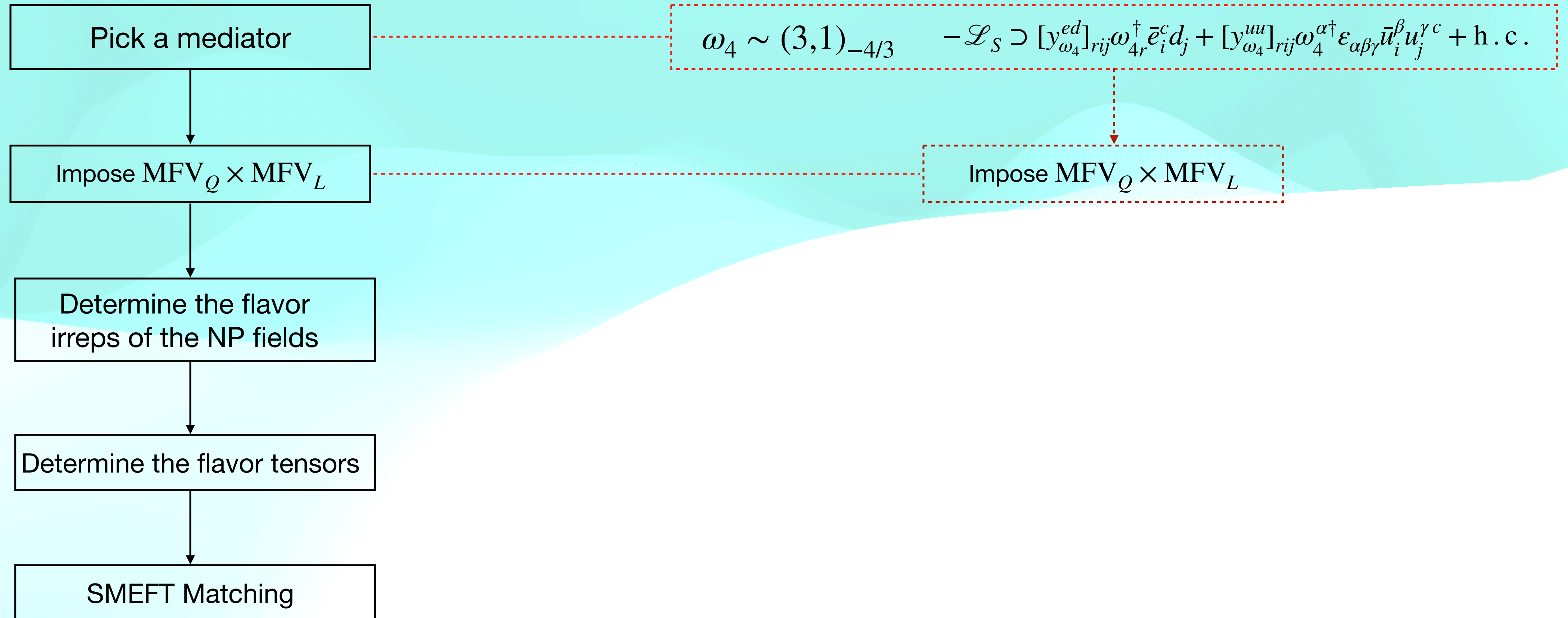


# Leading directions: Procedure and example

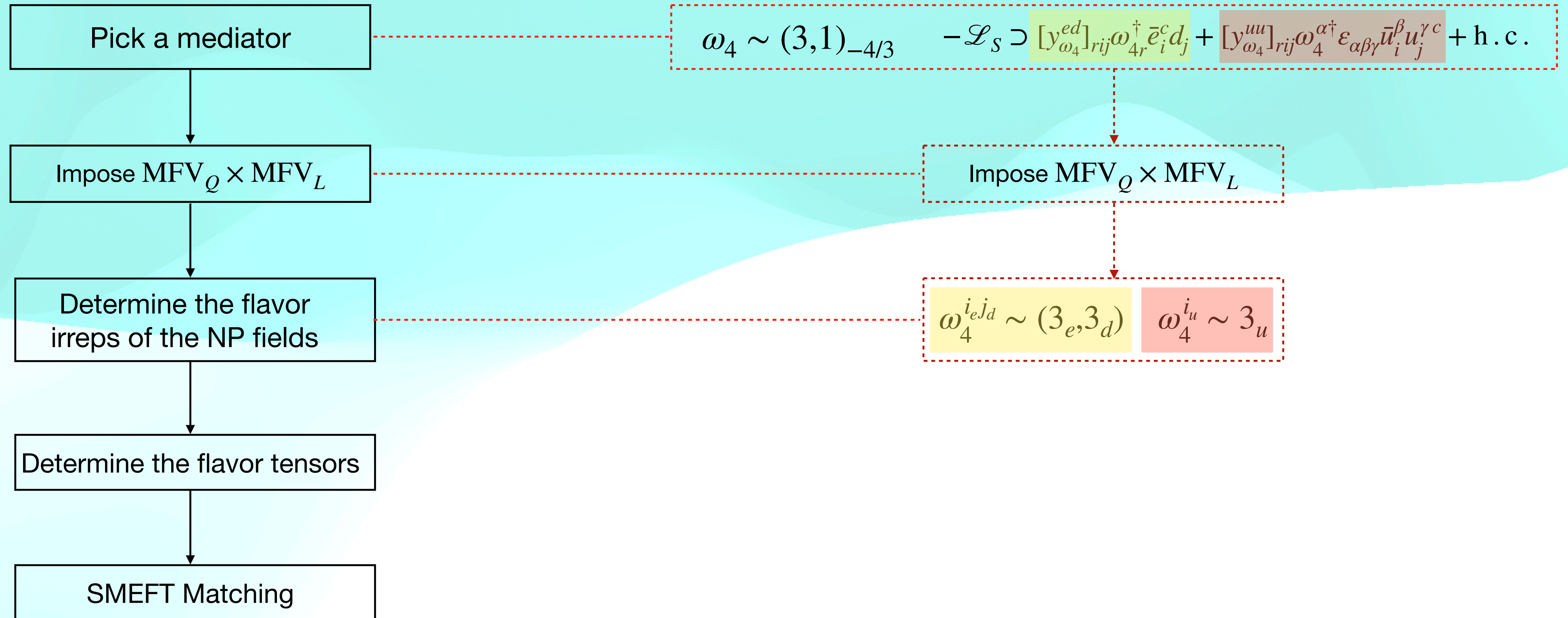


$$\omega_4 \sim (3,1)_{-4/3} \quad -\mathcal{L}_S \supset [y_{\omega_4}^{ed}]_{rij} \omega_{4r}^\dagger \bar{e}_i^c d_j + [y_{\omega_4}^{uu}]_{rij} \omega_4^{\alpha\dagger} \epsilon_{\alpha\beta\gamma} \bar{u}_i^\beta u_j^{\gamma c} + \text{h.c.}$$

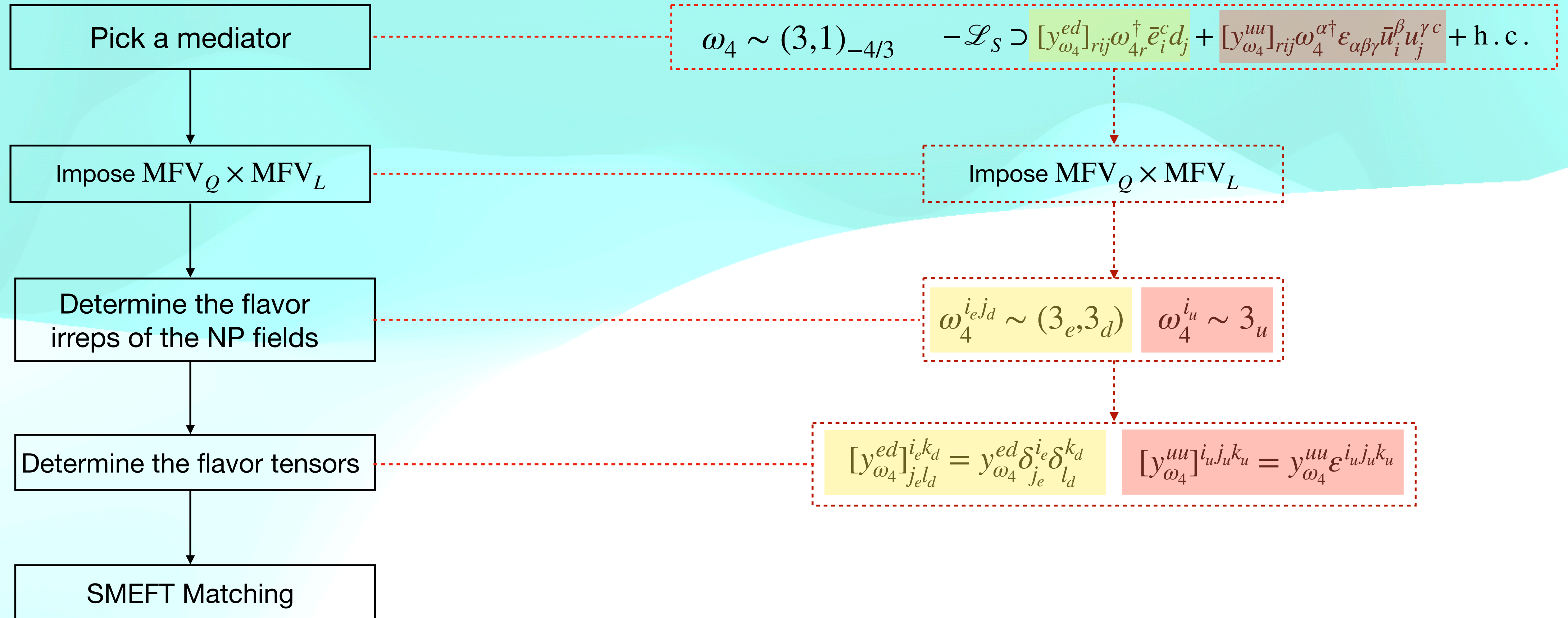
# Leading directions: Procedure and example



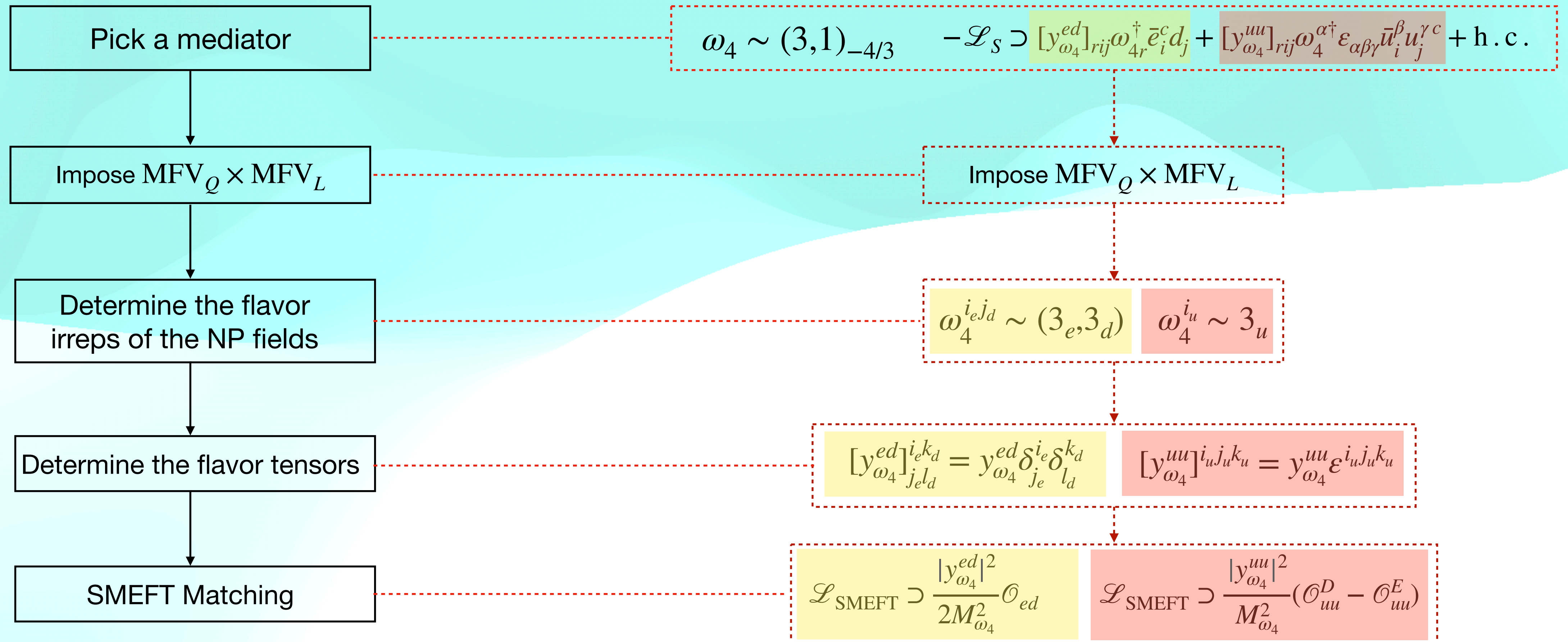
# Leading directions: Procedure and example



# Leading directions: Procedure and example



# Leading directions: Procedure and example



# Leading directions: Results

Field	Irrep	Normalization	Operator
$S_1 \sim (\mathbf{1}, \mathbf{1})_1$	$\mathbf{3}_\ell$	$ y_{S_1} ^2/M_{S_1}^2$	$\mathcal{O}_{\ell\ell}^D - \mathcal{O}_{\ell\ell}^E$
$S_2 \sim (\mathbf{1}, \mathbf{1})_2$	$\bar{\mathbf{6}}_e$	$ y_{S_2} ^2/(2M_{S_2}^2)$	$\mathcal{O}_{ee}$
$\varphi \sim (\mathbf{1}, \mathbf{2})_{\frac{1}{2}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_\ell)$	$- y_{\varphi^e} ^2/(2M_{\varphi^e}^2)$	$\mathcal{O}_{\ell e}$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_q)$	$- y_{\varphi^d} ^2/(6M_{\varphi^d}^2)$	$\mathcal{O}_{qd}^{(1)} + 6\mathcal{O}_{qd}^{(8)}$
	$(\bar{\mathbf{3}}_q, \mathbf{3}_u)$	$- y_{\varphi^u} ^2/(6M_{\varphi^u}^2)$	$\mathcal{O}_{qu}^{(1)} + 6\mathcal{O}_{qu}^{(8)}$
$\Xi_1 \sim (\mathbf{1}, \mathbf{3})_1$	$\bar{\mathbf{6}}_\ell$	$ y_{\Xi_1} ^2/(2M_{\Xi_1}^2)$	$\mathcal{O}_{\ell\ell}^D + \mathcal{O}_{\ell\ell}^E$
	$(\mathbf{3}_q, \mathbf{3}_\ell)$	$ y_{\omega_1^{q\ell}} ^2/(4M_{\omega_1^2}^2)$	$\mathcal{O}_{\ell q}^{(1)} - \mathcal{O}_{\ell q}^{(3)}$
	$(\mathbf{3}_e, \mathbf{3}_u)$	$ y_{\omega_1^{eu}} ^2/(2M_{\omega_1^2}^2)$	$\mathcal{O}_{eu}$
$\omega_1 \sim (\mathbf{3}, \mathbf{1})_{-\frac{1}{3}}$	$\bar{\mathbf{6}}_q$	$ y_{\omega_1^q} ^2/(4M_{\omega_1^2}^2)$	$\mathcal{O}_{qq}^{(1)D} - \mathcal{O}_{qq}^{(3)D} + \mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(3)E}$
	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_u)$	$ y_{\omega_1^{du}} ^2/(3M_{\omega_1^2}^2)$	$\mathcal{O}_{ud}^{(1)} - 3\mathcal{O}_{ud}^{(8)}$
$\omega_2 \sim (\mathbf{3}, \mathbf{1})_{\frac{2}{3}}$	$\mathbf{3}_d$	$ y_{\omega_2} ^2/M_{\omega_2}^2$	$\mathcal{O}_{dd}^D - \mathcal{O}_{dd}^E$
$\omega_4 \sim (\mathbf{3}, \mathbf{1})_{-\frac{4}{3}}$	$(\mathbf{3}_e, \mathbf{3}_d)$	$ y_{\omega_4^{ed}} ^2/(2M_{\omega_4}^2)$	$\mathcal{O}_{ed}$
	$\mathbf{3}_u$	$ y_{\omega_4^{uu}} ^2/M_{\omega_4}^2$	$\mathcal{O}_{uu}^D - \mathcal{O}_{uu}^E$
$\Pi_1 \sim (\mathbf{3}, \mathbf{2})_{\frac{1}{6}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_d)$	$- y_{\Pi_1} ^2/(2M_{\Pi_1}^2)$	$\mathcal{O}_{\ell d}$
$\Pi_7 \sim (\mathbf{3}, \mathbf{2})_{\frac{7}{6}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_u)$	$- y_{\Pi_7^{\ell u}} ^2/(2M_{\Pi_7}^2)$	$\mathcal{O}_{\ell u}$
	$(\bar{\mathbf{3}}_e, \mathbf{3}_q)$	$- y_{\Pi_7^{qe}} ^2/(2M_{\Pi_7}^2)$	$\mathcal{O}_{qe}$
$\zeta \sim (\mathbf{3}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{3}_q, \mathbf{3}_\ell)$	$ y_{\zeta^{q\ell}} ^2/(4M_{\zeta}^2)$	$3\mathcal{O}_{\ell q}^{(1)} + \mathcal{O}_{\ell q}^{(3)}$
	$\mathbf{3}_q$	$ y_{\zeta^{qq}} ^2/(2M_{\zeta}^2)$	$3\mathcal{O}_{qq}^{(1)D} + \mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(3)E}$
$\Omega_1 \sim (\mathbf{6}, \mathbf{1})_{\frac{1}{3}}$	$(\mathbf{3}_u, \mathbf{3}_d)$	$ y_{\Omega_1^{ud}} ^2/(6M_{\Omega_1}^2)$	$2\mathcal{O}_{ud}^{(1)} + 3\mathcal{O}_{ud}^{(8)}$
	$\bar{\mathbf{3}}_q$	$ y_{\Omega_1^{qq}} ^2/(4M_{\Omega_1}^2)$	$\mathcal{O}_{qq}^{(1)D} - \mathcal{O}_{qq}^{(3)D} - \mathcal{O}_{qq}^{(1)E} + \mathcal{O}_{qq}^{(3)E}$
$\Omega_2 \sim (\mathbf{6}, \mathbf{1})_{-\frac{2}{3}}$	$\mathbf{6}_d$	$ y_{\Omega_2} ^2/(4M_{\Omega_2}^2)$	$\mathcal{O}_{dd}^D + \mathcal{O}_{dd}^E$
$\Omega_4 \sim (\mathbf{6}, \mathbf{1})_{\frac{4}{3}}$	$\mathbf{6}_u$	$ y_{\Omega_4} ^2/(4M_{\Omega_4}^2)$	$\mathcal{O}_{uu}^D + \mathcal{O}_{uu}^E$
$\Upsilon \sim (\mathbf{6}, \mathbf{3})_{\frac{1}{3}}$	$\mathbf{6}_q$	$ y_{\Upsilon} ^2/(8M_{\Upsilon}^2)$	$3\mathcal{O}_{qq}^{(1)D} + \mathcal{O}_{qq}^{(3)D} + 3\mathcal{O}_{qq}^{(1)E} + \mathcal{O}_{qq}^{(3)E}$
$\Phi \sim (\mathbf{8}, \mathbf{2})_{\frac{1}{2}}$	$(\bar{\mathbf{3}}_q, \mathbf{3}_u)$	$- y_{\Phi^{qu}} ^2/(18M_{\Phi}^2)$	$4\mathcal{O}_{qu}^{(1)} - 3\mathcal{O}_{qu}^{(8)}$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_q)$	$- y_{\Phi^{dq}} ^2/(18M_{\Phi}^2)$	$4\mathcal{O}_{qd}^{(1)} - 3\mathcal{O}_{qd}^{(8)}$

Field	Irrep	Normalization	Operator
$\mathcal{B} \sim (\mathbf{1}, \mathbf{1})_0$	$\mathbf{8}_\ell$	$-(g_{\mathcal{B}}^\ell)^2/(12M_{\mathcal{B}}^2)$	$3\mathcal{O}_{\ell\ell}^E - \mathcal{O}_{\ell\ell}^D$
	$\mathbf{8}_e$	$-(g_{\mathcal{B}}^e)^2/(6M_{\mathcal{B}}^2)$	$\mathcal{O}_{ee}$
	$\mathbf{8}_q$	$-(g_{\mathcal{B}}^q)^2/(12M_{\mathcal{B}}^2)$	$3\mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(1)D}$
	$\mathbf{8}_u$	$-(g_{\mathcal{B}}^u)^2/(12M_{\mathcal{B}}^2)$	$3\mathcal{O}_{uu}^E - \mathcal{O}_{uu}^D$
$\mathcal{B}_1 \sim (\mathbf{1}, \mathbf{1})_1$	$\mathbf{8}_d$	$-(g_{\mathcal{B}}^d)^2/(12M_{\mathcal{B}}^2)$	$3\mathcal{O}_{dd}^E - \mathcal{O}_{dd}^D$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_u)$	$- g_{\mathcal{B}_1}^{du} ^2/(3M_{\mathcal{B}_1}^2)$	$\mathcal{O}_{ud}^{(1)} + 6\mathcal{O}_{ud}^{(8)}$
$\mathcal{W} \sim (\mathbf{1}, \mathbf{3})_0$	$\mathbf{8}_q$	$-(g_{\mathcal{W}}^q)^2/(48M_{\mathcal{W}}^2)$	$3\mathcal{O}_{qq}^{(3)E} - \mathcal{O}_{qq}^{(3)D}$
	$\mathbf{8}_\ell$	$(g_{\mathcal{W}}^\ell)^2/(48M_{\mathcal{W}}^2)$	$5\mathcal{O}_{\ell\ell}^E - 7\mathcal{O}_{\ell\ell}^D$
$\mathcal{L}_3 \sim (\mathbf{1}, \mathbf{2})_{-\frac{3}{2}}$	$(\mathbf{3}_e, \mathbf{3}_\ell)$	$ g_{\mathcal{L}_3} ^2/M_{\mathcal{L}_3}^2$	$\mathcal{O}_{\ell e}$
$\mathcal{U}_2 \sim (\mathbf{3}, \mathbf{1})_{\frac{2}{3}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_d)$	$- g_{\mathcal{U}_2}^{ed} ^2/M_{\mathcal{U}_2}^2$	$\mathcal{O}_{ed}$
	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_q)$	$- g_{\mathcal{U}_2}^{\ell q} ^2/(2M_{\mathcal{U}_2}^2)$	$\mathcal{O}_{\ell q}^{(1)} + \mathcal{O}_{\ell q}^{(3)}$
$\mathcal{U}_5 \sim (\mathbf{3}, \mathbf{1})_{\frac{5}{3}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_u)$	$- g_{\mathcal{U}_5} ^2/M_{\mathcal{U}_5}^2$	$\mathcal{O}_{eu}$
$\mathcal{Q}_1 \sim (\mathbf{3}, \mathbf{2})_{\frac{1}{6}}$	$(\mathbf{3}_u, \mathbf{3}_\ell)$	$ g_{\mathcal{Q}_1}^{u\ell} ^2/M_{\mathcal{Q}_1}^2$	$\mathcal{O}_{\ell u}$
	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_q)$	$2 g_{\mathcal{Q}_1}^{dq} ^2/(3M_{\mathcal{Q}_1}^2)$	$\mathcal{O}_{qd}^{(1)} - 3\mathcal{O}_{qd}^{(8)}$
$\mathcal{Q}_5 \sim (\mathbf{3}, \mathbf{2})_{-\frac{5}{6}}$	$(\mathbf{3}_d, \mathbf{3}_\ell)$	$ g_{\mathcal{Q}_5}^{d\ell} ^2/M_{\mathcal{Q}_5}^2$	$\mathcal{O}_{\ell d}$
	$(\mathbf{3}_e, \mathbf{3}_q)$	$ g_{\mathcal{Q}_5}^{eq} ^2/M_{\mathcal{Q}_5}^2$	$\mathcal{O}_{qe}$
	$(\bar{\mathbf{3}}_u, \bar{\mathbf{3}}_q)$	$2 g_{\mathcal{Q}_5}^{uq} ^2/(3M_{\mathcal{Q}_5}^2)$	$\mathcal{O}_{qu}^{(1)} - 3\mathcal{O}_{qu}^{(8)}$
$\mathcal{X} \sim (\mathbf{3}, \mathbf{3})_{\frac{2}{3}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_q)$	$- g_{\mathcal{X}} ^2/(8M_{\mathcal{X}}^2)$	$3\mathcal{O}_{\ell q}^{(1)} - \mathcal{O}_{\ell q}^{(3)}$
$\mathcal{Y}_1 \sim (\bar{\mathbf{6}}, \mathbf{2})_{\frac{1}{6}}$	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_q)$	$ g_{\mathcal{Y}_1} ^2/(3M_{\mathcal{Y}_1}^2)$	$2\mathcal{O}_{qd}^{(1)} + 3\mathcal{O}_{qd}^{(8)}$
$\mathcal{Y}_5 \sim (\bar{\mathbf{6}}, \mathbf{2})_{-\frac{5}{6}}$	$(\bar{\mathbf{3}}_u, \bar{\mathbf{3}}_q)$	$ g_{\mathcal{Y}_5} ^2/(3M_{\mathcal{Y}_5}^2)$	$2\mathcal{O}_{qu}^{(1)} + 3\mathcal{O}_{qu}^{(8)}$
$\mathcal{G} \sim (\mathbf{8}, \mathbf{1})_0$	$\mathbf{8}_q$	$-(g_{\mathcal{G}}^q)^2/(144M_{\mathcal{G}}^2)$	$11\mathcal{O}_{qq}^{(1)D} - 9\mathcal{O}_{qq}^{(1)E} + 9\mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(3)E}$
	$\mathbf{8}_u$	$(g_{\mathcal{G}}^u)^2/(36M_{\mathcal{G}}^2)$	$3\mathcal{O}_{uu}^E - 5\mathcal{O}_{uu}^D$
	$\mathbf{8}_d$	$(g_{\mathcal{G}}^d)^2/(36M_{\mathcal{G}}^2)$	$3\mathcal{O}_{dd}^E - 5\mathcal{O}_{dd}^D$
$\mathcal{G}_1 \sim (\mathbf{8}, \mathbf{1})_1$	$(\bar{\mathbf{3}}_d, \mathbf{3}_u)$	$ g_{\mathcal{G}_1} ^2/(9M_{\mathcal{G}_1}^2)$	$-4\mathcal{O}_{ud}^{(1)} + 3\mathcal{O}_{ud}^{(8)}$
$\mathcal{H} \sim (\mathbf{8}, \mathbf{3})_0$	$\mathbf{8}_q$	$-(g_{\mathcal{H}})^2/(576M_{\mathcal{H}}^2)$	$27\mathcal{O}_{qq}^{(1)D} - 9\mathcal{O}_{qq}^{(1)E} - 7\mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(3)E}$

Field	Irrep	Normalization	Operator
$N \sim (\mathbf{1}, \mathbf{1})_0$	$\mathbf{3}_\ell$	$ \lambda_N ^2/(4M_N^2)$	$\mathcal{O}_{\phi\ell}^{(1)} - \mathcal{O}_{\phi\ell}^{(3)}$
$E \sim (\mathbf{1}, \mathbf{1})_{-1}$	$\mathbf{3}_\ell$	$- \lambda_E ^2/(4M_E^2)$	$\mathcal{O}_{\phi\ell}^{(1)} + \mathcal{O}_{\phi\ell}^{(3)} - [2y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Delta_1 \sim (\mathbf{1}, \mathbf{2})_{-\frac{1}{2}}$	$\mathbf{3}_e$	$ \lambda_{\Delta_1} ^2/(2M_{\Delta_1}^2)$	$\mathcal{O}_{\phi e} + [y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Delta_3 \sim (\mathbf{1}, \mathbf{2})_{-\frac{3}{2}}$	$\mathbf{3}_e$	$- \lambda_{\Delta_3} ^2/(2M_{\Delta_3}^2)$	$\mathcal{O}_{\phi e} - [y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Sigma \sim (\mathbf{1}, \mathbf{3})_0$	$\mathbf{3}_\ell$	$ \lambda_{\Sigma} ^2/(16M_{\Sigma}^2)$	$3\mathcal{O}_{\phi\ell}^{(1)} + \mathcal{O}_{\phi\ell}^{(3)} + [4y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Sigma_1 \sim (\mathbf{1}, \mathbf{3})_{-1}$	$\mathbf{3}_\ell$	$ \lambda_{\Sigma_1} ^2/(16M_{\Sigma_1}^2)$	$\mathcal{O}_{\phi\ell}^{(3)} - 3\mathcal{O}_{\phi\ell}^{(1)} + [2y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$U \sim (\mathbf{3}, \mathbf{1})_{\frac{2}{3}}$	$\mathbf{3}_q$	$ \lambda_U ^2/(4M_U^2)$	$\mathcal{O}_{\phi q}^{(1)} - \mathcal{O}_{\phi q}^{(3)} + [2y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$D \sim (\mathbf{3}, \mathbf{1})_{-\frac{1}{3}}$	$\mathbf{3}_q$	$- \lambda_D ^2/(4M_D^2)$	$\mathcal{O}_{\phi q}^{(1)} + \mathcal{O}_{\phi q}^{(3)} - [2y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_1 \sim (\mathbf{3}, \mathbf{2})_{\frac{1}{6}}$	$\mathbf{3}_u$	$- \lambda_{Q_1}^u ^2/(2M_{Q_1}^2)$	$\mathcal{O}_{\phi u} - [y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
	$\mathbf{3}_d$	$ \lambda_{Q_1}^d ^2/(2M_{Q_1}^2)$	$\mathcal{O}_{\phi d} + [y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_5 \sim (\mathbf{3}, \mathbf{2})_{-\frac{5}{6}}$	$\mathbf{3}_d$	$- \lambda_{Q_5} ^2/(2M_{Q_5}^2)$	$\mathcal{O}_{\phi d} - [y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_7 \sim (\mathbf{3}, \mathbf{2})_{\frac{7}{6}}$	$\mathbf{3}_u$	$ \lambda_{Q_7} ^2/(2M_{Q_7}^2)$	$\mathcal{O}_{\phi u} + [y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$T_1 \sim (\mathbf{3}, \mathbf{3})_{-\frac{1}{3}}$	$\mathbf{3}_q$	$ \lambda_{T_1} ^2/(16M_{T_1}^2)$	$\mathcal{O}_{\phi q}^{(3)} - 3\mathcal{O}_{\phi q}^{(1)} + [2y_d^* \mathcal{O}_{d\phi} + 4y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$T_2 \sim (\mathbf{3}, \mathbf{3})_{\frac{2}{3}}$	$\mathbf{3}_q$	$ \lambda_{T_2} ^2/(16M_{T_2}^2)$	$\mathcal{O}_{\phi q}^{(3)} + 3\mathcal{O}_{\phi q}^{(1)} + [4y_d^* \mathcal{O}_{d\phi} + 2y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$

# Leading directions: Results

Field	Irrep	Normalization	Operator
$S_1 \sim (\mathbf{1}, \mathbf{1})_1$	$\mathbf{3}_\ell$	$ y_{S_1} ^2/M_{S_1}^2$	$\mathcal{O}_{\ell\ell}^D - \mathcal{O}_{\ell\ell}^E$
$S_2 \sim (\mathbf{1}, \mathbf{1})_2$	$\bar{\mathbf{6}}_e$	$ y_{S_2} ^2/(2M_{S_2}^2)$	$\mathcal{O}_{ee}$
$\varphi \sim (\mathbf{1}, \mathbf{2})_{\frac{1}{2}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_\ell)$	$- y_\varphi^e ^2/(2M_\varphi^2)$	$\mathcal{O}_{\ell e}$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_q)$	$- y_\varphi^d ^2/(6M_\varphi^2)$	$\mathcal{O}_{qd}^{(1)} + 6\mathcal{O}_{qd}^{(8)}$
	$(\bar{\mathbf{3}}_q, \mathbf{3}_u)$	$- y_\varphi^u ^2/(6M_\varphi^2)$	$\mathcal{O}_{qu}^{(1)} + 6\mathcal{O}_{qu}^{(8)}$
$\Xi_1 \sim (\mathbf{1}, \mathbf{3})_1$	$\bar{\mathbf{6}}_\ell$	$ y_{\Xi_1} ^2/(2M_{\Xi_1}^2)$	$\mathcal{O}_{\ell\ell}^D + \mathcal{O}_{\ell\ell}^E$
	$(\mathbf{3}_q, \mathbf{3}_\ell)$	$ y_{\omega_1}^{q\ell} ^2/(4M_{\omega_1}^2)$	$\mathcal{O}_{\ell q}^{(1)} - \mathcal{O}_{\ell q}^{(3)}$
$\omega_1 \sim (\mathbf{3}, \mathbf{1})_{-\frac{1}{3}}$	$(\mathbf{3}_e, \mathbf{3}_u)$	$ y_{\omega_1}^{eu} ^2/(2M_{\omega_1}^2)$	$\mathcal{O}_{eu}$
	$\bar{\mathbf{6}}_q$	$ y_{\omega_1}^{qq} ^2/(4M_{\omega_1}^2)$	$\mathcal{O}_{qq}^{(1)D} - \mathcal{O}_{qq}^{(3)D} + \mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(3)E}$
	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_u)$	$ y_{\omega_1}^{du} ^2/(3M_{\omega_1}^2)$	$\mathcal{O}_{ud}^{(1)} - 3\mathcal{O}_{ud}^{(8)}$
$\omega_2 \sim (\mathbf{3}, \mathbf{1})_{\frac{2}{3}}$	$\mathbf{3}_d$	$ y_{\omega_2} ^2/M_{\omega_2}^2$	$\mathcal{O}_{dd}^D - \mathcal{O}_{dd}^E$
$\omega_4 \sim (\mathbf{3}, \mathbf{1})_{-\frac{4}{3}}$	$(\mathbf{3}_e, \mathbf{3}_d)$	$ y_{\omega_4}^{ed} ^2/(2M_{\omega_4}^2)$	$\mathcal{O}_{ed}$
	$\mathbf{3}_u$	$ y_{\omega_4}^{uu} ^2/M_{\omega_4}^2$	$\mathcal{O}_{uu}^D - \mathcal{O}_{uu}^E$
$\Pi_1 \sim (\mathbf{3}, \mathbf{2})_{\frac{1}{6}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_d)$	$- y_{\Pi_1} ^2/(2M_{\Pi_1}^2)$	$\mathcal{O}_{\ell d}$
$\Pi_7 \sim (\mathbf{3}, \mathbf{2})_{\frac{7}{6}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_u)$	$- y_{\Pi_7}^{\ell u} ^2/(2M_{\Pi_7}^2)$	$\mathcal{O}_{\ell u}$
	$(\bar{\mathbf{3}}_e, \mathbf{3}_q)$	$- y_{\Pi_7}^{qe} ^2/(2M_{\Pi_7}^2)$	$\mathcal{O}_{qe}$
$\zeta \sim (\mathbf{3}, \mathbf{3})_{-\frac{1}{3}}$	$(\mathbf{3}_q, \mathbf{3}_\ell)$	$ y_\zeta^{q\ell} ^2/(4M_\zeta^2)$	$3\mathcal{O}_{\ell q}^{(1)} + \mathcal{O}_{\ell q}^{(3)}$
	$\mathbf{3}_q$	$ y_\zeta^{qq} ^2/(2M_\zeta^2)$	$3\mathcal{O}_{qq}^{(1)D} + \mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(3)E}$
$\Omega_1 \sim (\mathbf{6}, \mathbf{1})_{\frac{1}{3}}$	$(\mathbf{3}_u, \mathbf{3}_d)$	$ y_{\Omega_1}^{ud} ^2/(6M_{\Omega_1}^2)$	$2\mathcal{O}_{ud}^{(1)} + 3\mathcal{O}_{ud}^{(8)}$
	$\bar{\mathbf{3}}_q$	$ y_{\Omega_1}^{qq} ^2/(4M_{\Omega_1}^2)$	$\mathcal{O}_{qq}^{(1)D} - \mathcal{O}_{qq}^{(3)D} - \mathcal{O}_{qq}^{(1)E} + \mathcal{O}_{qq}^{(3)E}$
$\Omega_2 \sim (\mathbf{6}, \mathbf{1})_{-\frac{2}{3}}$	$\mathbf{6}_d$	$ y_{\Omega_2} ^2/(4M_{\Omega_2}^2)$	$\mathcal{O}_{dd}^D + \mathcal{O}_{dd}^E$
$\Omega_4 \sim (\mathbf{6}, \mathbf{1})_{\frac{4}{3}}$	$\mathbf{6}_u$	$ y_{\Omega_4} ^2/(4M_{\Omega_4}^2)$	$\mathcal{O}_{uu}^D + \mathcal{O}_{uu}^E$
$\Upsilon \sim (\mathbf{6}, \mathbf{3})_{\frac{1}{3}}$	$\mathbf{6}_q$	$ y_\Upsilon ^2/(8M_\Upsilon^2)$	$3\mathcal{O}_{qq}^{(1)D} + \mathcal{O}_{qq}^{(3)D} + 3\mathcal{O}_{qq}^{(1)E} + \mathcal{O}_{qq}^{(3)E}$
$\Phi \sim (\mathbf{8}, \mathbf{2})_{\frac{1}{2}}$	$(\bar{\mathbf{3}}_q, \mathbf{3}_u)$	$- y_\Phi^{qu} ^2/(18M_\Phi^2)$	$4\mathcal{O}_{qu}^{(1)} - 3\mathcal{O}_{qu}^{(8)}$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_q)$	$- y_\Phi^{dq} ^2/(18M_\Phi^2)$	$4\mathcal{O}_{qd}^{(1)} - 3\mathcal{O}_{qd}^{(8)}$

Field	Irrep	Normalization	Operator
$\mathcal{B} \sim (\mathbf{1}, \mathbf{1})_0$	$\mathbf{8}_\ell$	$-(g_\mathcal{B}^\ell)^2/(12M_\mathcal{B}^2)$	$3\mathcal{O}_{\ell\ell}^E - \mathcal{O}_{\ell\ell}^D$
	$\mathbf{8}_e$	$-(g_\mathcal{B}^e)^2/(6M_\mathcal{B}^2)$	$\mathcal{O}_{ee}$
	$\mathbf{8}_q$	$-(g_\mathcal{B}^q)^2/(12M_\mathcal{B}^2)$	$3\mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(1)D}$
	$\mathbf{8}_u$	$-(g_\mathcal{B}^u)^2/(12M_\mathcal{B}^2)$	$3\mathcal{O}_{uu}^E - \mathcal{O}_{uu}^D$
$\mathcal{B}_1 \sim (\mathbf{1}, \mathbf{1})_1$	$\mathbf{8}_d$	$-(g_\mathcal{B}^d)^2/(12M_\mathcal{B}^2)$	$3\mathcal{O}_{dd}^E - \mathcal{O}_{dd}^D$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_u)$	$- g_{\mathcal{B}_1}^{du} ^2/(3M_{\mathcal{B}_1}^2)$	$\mathcal{O}_{ud}^{(1)} + 6\mathcal{O}_{ud}^{(8)}$
$\mathcal{W} \sim (\mathbf{1}, \mathbf{3})_0$	$\mathbf{8}_q$	$-(g_\mathcal{W}^q)^2/(48M_\mathcal{W}^2)$	$3\mathcal{O}_{qq}^{(3)E} - \mathcal{O}_{qq}^{(3)D}$
	$\mathbf{8}_\ell$	$(g_\mathcal{W}^\ell)^2/(48M_\mathcal{W}^2)$	$5\mathcal{O}_{\ell\ell}^E - 7\mathcal{O}_{\ell\ell}^D$
$\mathcal{L}_3 \sim (\mathbf{1}, \mathbf{2})_{-\frac{3}{2}}$	$(\mathbf{3}_e, \mathbf{3}_\ell)$	$ g_{\mathcal{L}_3} ^2/M_{\mathcal{L}_3}^2$	$\mathcal{O}_{\ell e}$
$\mathcal{U}_2 \sim (\mathbf{3}, \mathbf{1})_{\frac{2}{3}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_d)$	$- g_{\mathcal{U}_2}^{ed} ^2/M_{\mathcal{U}_2}^2$	$\mathcal{O}_{ed}$
	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_q)$	$- g_{\mathcal{U}_2}^{\ell q} ^2/(2M_{\mathcal{U}_2}^2)$	$\mathcal{O}_{\ell q}^{(1)} + \mathcal{O}_{\ell q}^{(3)}$
$\mathcal{U}_5 \sim (\mathbf{3}, \mathbf{1})_{\frac{5}{3}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_u)$	$- g_{\mathcal{U}_5} ^2/M_{\mathcal{U}_5}^2$	$\mathcal{O}_{eu}$
$\mathcal{Q}_1 \sim (\mathbf{3}, \mathbf{2})_{\frac{1}{6}}$	$(\mathbf{3}_u, \mathbf{3}_\ell)$	$ g_{\mathcal{Q}_1}^{u\ell} ^2/M_{\mathcal{Q}_1}^2$	$\mathcal{O}_{\ell u}$
	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_q)$	$2 g_{\mathcal{Q}_1}^{dq} ^2/(3M_{\mathcal{Q}_1}^2)$	$\mathcal{O}_{qd}^{(1)} - 3\mathcal{O}_{qd}^{(8)}$
$\mathcal{Q}_5 \sim (\mathbf{3}, \mathbf{2})_{-\frac{5}{6}}$	$(\mathbf{3}_d, \mathbf{3}_\ell)$	$ g_{\mathcal{Q}_5}^{d\ell} ^2/M_{\mathcal{Q}_5}^2$	$\mathcal{O}_{\ell d}$
	$(\mathbf{3}_e, \mathbf{3}_q)$	$ g_{\mathcal{Q}_5}^{eq} ^2/M_{\mathcal{Q}_5}^2$	$\mathcal{O}_{qe}$
	$(\bar{\mathbf{3}}_u, \bar{\mathbf{3}}_q)$	$2 g_{\mathcal{Q}_5}^{uq} ^2/(3M_{\mathcal{Q}_5}^2)$	$\mathcal{O}_{qu}^{(1)} - 3\mathcal{O}_{qu}^{(8)}$
$\mathcal{X} \sim (\mathbf{3}, \mathbf{3})_{\frac{2}{3}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_q)$	$- g_\mathcal{X} ^2/(8M_\mathcal{X}^2)$	$3\mathcal{O}_{\ell q}^{(1)} - \mathcal{O}_{\ell q}^{(3)}$
$\mathcal{Y}_1 \sim (\bar{\mathbf{6}}, \mathbf{2})_{\frac{1}{6}}$	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_q)$	$ g_{\mathcal{Y}_1} ^2/(3M_{\mathcal{Y}_1}^2)$	$2\mathcal{O}_{qd}^{(1)} + 3\mathcal{O}_{qd}^{(8)}$
$\mathcal{Y}_5 \sim (\bar{\mathbf{6}}, \mathbf{2})_{-\frac{5}{6}}$	$(\bar{\mathbf{3}}_u, \bar{\mathbf{3}}_q)$	$ g_{\mathcal{Y}_5} ^2/(3M_{\mathcal{Y}_5}^2)$	$2\mathcal{O}_{qu}^{(1)} + 3\mathcal{O}_{qu}^{(8)}$
$\mathcal{G} \sim (\mathbf{8}, \mathbf{1})_0$	$\mathbf{8}_q$	$-(g_\mathcal{G}^q)^2/(144M_\mathcal{G}^2)$	$11\mathcal{O}_{qq}^{(1)D} - 9\mathcal{O}_{qq}^{(1)E} + 9\mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(3)E}$
	$\mathbf{8}_u$	$(g_\mathcal{G}^u)^2/(36M_\mathcal{G}^2)$	$3\mathcal{O}_{uu}^E - 5\mathcal{O}_{uu}^D$
	$\mathbf{8}_d$	$(g_\mathcal{G}^d)^2/(36M_\mathcal{G}^2)$	$3\mathcal{O}_{dd}^E - 5\mathcal{O}_{dd}^D$
$\mathcal{G}_1 \sim (\mathbf{8}, \mathbf{1})_1$	$(\bar{\mathbf{3}}_d, \mathbf{3}_u)$	$ g_{\mathcal{G}_1} ^2/(9M_{\mathcal{G}_1}^2)$	$-4\mathcal{O}_{ud}^{(1)} + 3\mathcal{O}_{ud}^{(8)}$
$\mathcal{H} \sim (\mathbf{8}, \mathbf{3})_0$	$\mathbf{8}_q$	$-(g_\mathcal{H})^2/(576M_\mathcal{H}^2)$	$27\mathcal{O}_{qq}^{(1)D} - 9\mathcal{O}_{qq}^{(1)E} - 7\mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(3)E}$

Field	Irrep	Normalization	Operator
$N \sim (\mathbf{1}, \mathbf{1})_0$	$\mathbf{3}_\ell$	$ \lambda_N ^2/(4M_N^2)$	$\mathcal{O}_{\phi\ell}^{(1)} - \mathcal{O}_{\phi\ell}^{(3)}$
$E \sim (\mathbf{1}, \mathbf{1})_{-1}$	$\mathbf{3}_\ell$	$- \lambda_E ^2/(4M_E^2)$	$\mathcal{O}_{\phi\ell}^{(1)} + \mathcal{O}_{\phi\ell}^{(3)} - [2y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Delta_1 \sim (\mathbf{1}, \mathbf{2})_{-\frac{1}{2}}$	$\mathbf{3}_e$	$ \lambda_{\Delta_1} ^2/(2M_{\Delta_1}^2)$	$\mathcal{O}_{\phi e} + [y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Delta_3 \sim (\mathbf{1}, \mathbf{2})_{-\frac{3}{2}}$	$\mathbf{3}_e$	$- \lambda_{\Delta_3} ^2/(2M_{\Delta_3}^2)$	$\mathcal{O}_{\phi e} - [y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Sigma \sim (\mathbf{1}, \mathbf{3})_0$	$\mathbf{3}_\ell$	$ \lambda_\Sigma ^2/(16M_\Sigma^2)$	$3\mathcal{O}_{\phi\ell}^{(1)} + \mathcal{O}_{\phi\ell}^{(3)} + [4y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Sigma_1 \sim (\mathbf{1}, \mathbf{3})_{-1}$	$\mathbf{3}_\ell$	$ \lambda_{\Sigma_1} ^2/(16M_{\Sigma_1}^2)$	$\mathcal{O}_{\phi\ell}^{(3)} - 3\mathcal{O}_{\phi\ell}^{(1)} + [2y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$U \sim (\mathbf{3}, \mathbf{1})_{\frac{2}{3}}$	$\mathbf{3}_q$	$ \lambda_U ^2/(4M_U^2)$	$\mathcal{O}_{\phi q}^{(1)} - \mathcal{O}_{\phi q}^{(3)} + [2y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$D \sim (\mathbf{3}, \mathbf{1})_{-\frac{1}{3}}$	$\mathbf{3}_q$	$- \lambda_D ^2/(4M_D^2)$	$\mathcal{O}_{\phi q}^{(1)} + \mathcal{O}_{\phi q}^{(3)} - [2y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_1 \sim (\mathbf{3}, \mathbf{2})_{\frac{1}{6}}$	$\mathbf{3}_u$	$- \lambda_{Q_1}^u ^2/(2M_{Q_1}^2)$	$\mathcal{O}_{\phi u} - [y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
	$\mathbf{3}_d$	$ \lambda_{Q_1}^d ^2/(2M_{Q_1}^2)$	$\mathcal{O}_{\phi d} + [y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_5 \sim (\mathbf{3}, \mathbf{2})_{-\frac{5}{6}}$	$\mathbf{3}_d$	$- \lambda_{Q_5} ^2/(2M_{Q_5}^2)$	$\mathcal{O}_{\phi d} - [y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_7 \sim (\mathbf{3}, \mathbf{2})_{\frac{7}{6}}$	$\mathbf{3}_u$	$ \lambda_{Q_7} ^2/(2M_{Q_7}^2)$	$\mathcal{O}_{\phi u} + [y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$T_1 \sim (\mathbf{3}, \mathbf{3})_{-\frac{1}{3}}$	$\mathbf{3}_q$	$ \lambda_{T_1} ^2/(16M_{T_1}^2)$	$\mathcal{O}_{\phi q}^{(3)} - 3\mathcal{O}_{\phi q}^{(1)} + [2y_d^* \mathcal{O}_{d\phi} + 4y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$T_2 \sim (\mathbf{3}, \mathbf{3})_{\frac{2}{3}}$	$\mathbf{3}_q$	$ \lambda_{T_2} ^2/(16M_{T_2}^2)$	$\mathcal{O}_{\phi q}^{(3)} + 3\mathcal{O}_{\phi q}^{(1)} + [4y_d^* \mathcal{O}_{d\phi} + 2y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$

- Most of cases integrate out to a single linear combination of operators in the MFV basis.

# Leading directions: Results

Field	Irrep	Normalization	Operator
$S_1 \sim (1, 1)_1$	$\mathbf{3}_\ell$	$ y_{S_1} ^2/M_{S_1}^2$	$\mathcal{O}_{\ell\ell}^D - \mathcal{O}_{\ell\ell}^E$
$S_2 \sim (1, 1)_2$	$\bar{\mathbf{6}}_e$	$ y_{S_2} ^2/(2M_{S_2}^2)$	$\mathcal{O}_{ee}$
$\varphi \sim (1, 2)_{\frac{1}{2}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_\ell)$	$- y_\varphi^e ^2/(2M_\varphi^2)$	$\mathcal{O}_{\ell e}$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_q)$	$- y_\varphi^d ^2/(6M_\varphi^2)$	$\mathcal{O}_{qd}^{(1)} + 6\mathcal{O}_{qd}^{(8)}$
	$(\bar{\mathbf{3}}_q, \mathbf{3}_u)$	$- y_\varphi^u ^2/(6M_\varphi^2)$	$\mathcal{O}_{qu}^{(1)} + 6\mathcal{O}_{qu}^{(8)}$
$\Xi_1 \sim (1, 3)_1$	$\bar{\mathbf{6}}_\ell$	$ y_{\Xi_1} ^2/(2M_{\Xi_1}^2)$	$\mathcal{O}_{\ell\ell}^D + \mathcal{O}_{\ell\ell}^E$
	$(\mathbf{3}_q, \mathbf{3}_\ell)$	$ y_{\omega_1}^{q\ell} ^2/(4M_{\omega_1}^2)$	$\mathcal{O}_{\ell q}^{(1)} - \mathcal{O}_{\ell q}^{(3)}$
$\omega_1 \sim (3, 1)_{-\frac{1}{3}}$	$(\mathbf{3}_e, \mathbf{3}_u)$	$ y_{\omega_1}^{eu} ^2/(2M_{\omega_1}^2)$	$\mathcal{O}_{eu}$
	$\bar{\mathbf{6}}_q$	$ y_{\omega_1}^{qq} ^2/(4M_{\omega_1}^2)$	$\mathcal{O}_{qq}^{(1)D} - \mathcal{O}_{qq}^{(3)D} + \mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(3)E}$
	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_u)$	$ y_{\omega_1}^{du} ^2/(3M_{\omega_1}^2)$	$\mathcal{O}_{ud}^{(1)} - 3\mathcal{O}_{ud}^{(8)}$
$\omega_2 \sim (3, 1)_{\frac{2}{3}}$	$\mathbf{3}_d$	$ y_{\omega_2} ^2/M_{\omega_2}^2$	$\mathcal{O}_{dd}^D - \mathcal{O}_{dd}^E$
$\omega_4 \sim (3, 1)_{-\frac{4}{3}}$	$(\mathbf{3}_e, \mathbf{3}_d)$	$ y_{\omega_4}^{ed} ^2/(2M_{\omega_4}^2)$	$\mathcal{O}_{ed}$
	$\mathbf{3}_u$	$ y_{\omega_4}^{uu} ^2/M_{\omega_4}^2$	$\mathcal{O}_{uu}^D - \mathcal{O}_{uu}^E$
$\Pi_1 \sim (3, 2)_{\frac{1}{6}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_d)$	$- y_{\Pi_1} ^2/(2M_{\Pi_1}^2)$	$\mathcal{O}_{\ell d}$
$\Pi_7 \sim (3, 2)_{\frac{7}{6}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_u)$	$- y_{\Pi_7}^{\ell u} ^2/(2M_{\Pi_7}^2)$	$\mathcal{O}_{\ell u}$
	$(\bar{\mathbf{3}}_e, \mathbf{3}_q)$	$- y_{\Pi_7}^{qe} ^2/(2M_{\Pi_7}^2)$	$\mathcal{O}_{qe}$
$\zeta \sim (3, 3)_{-\frac{1}{3}}$	$(\mathbf{3}_q, \mathbf{3}_\ell)$	$ y_\zeta^{q\ell} ^2/(4M_\zeta^2)$	$3\mathcal{O}_{\ell q}^{(1)} + \mathcal{O}_{\ell q}^{(3)}$
	$\mathbf{3}_q$	$ y_\zeta^{qq} ^2/(2M_\zeta^2)$	$3\mathcal{O}_{qq}^{(1)D} + \mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(3)E}$
$\Omega_1 \sim (6, 1)_{\frac{1}{3}}$	$(\mathbf{3}_u, \mathbf{3}_d)$	$ y_{\Omega_1}^{ud} ^2/(6M_{\Omega_1}^2)$	$2\mathcal{O}_{ud}^{(1)} + 3\mathcal{O}_{ud}^{(8)}$
	$\bar{\mathbf{3}}_q$	$ y_{\Omega_1}^{qq} ^2/(4M_{\Omega_1}^2)$	$\mathcal{O}_{qq}^{(1)D} - \mathcal{O}_{qq}^{(3)D} - \mathcal{O}_{qq}^{(1)E} + \mathcal{O}_{qq}^{(3)E}$
$\Omega_2 \sim (6, 1)_{-\frac{2}{3}}$	$\mathbf{6}_d$	$ y_{\Omega_2} ^2/(4M_{\Omega_2}^2)$	$\mathcal{O}_{dd}^D + \mathcal{O}_{dd}^E$
$\Omega_4 \sim (6, 1)_{\frac{4}{3}}$	$\mathbf{6}_u$	$ y_{\Omega_4} ^2/(4M_{\Omega_4}^2)$	$\mathcal{O}_{uu}^D + \mathcal{O}_{uu}^E$
$\Upsilon \sim (6, 3)_{\frac{1}{3}}$	$\mathbf{6}_q$	$ y_\Upsilon ^2/(8M_\Upsilon^2)$	$3\mathcal{O}_{qq}^{(1)D} + \mathcal{O}_{qq}^{(3)D} + 3\mathcal{O}_{qq}^{(1)E} + \mathcal{O}_{qq}^{(3)E}$
$\Phi \sim (8, 2)_{\frac{1}{2}}$	$(\bar{\mathbf{3}}_q, \mathbf{3}_u)$	$- y_\Phi^{qu} ^2/(18M_\Phi^2)$	$4\mathcal{O}_{qu}^{(1)} - 3\mathcal{O}_{qu}^{(8)}$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_q)$	$- y_\Phi^{dq} ^2/(18M_\Phi^2)$	$4\mathcal{O}_{qd}^{(1)} - 3\mathcal{O}_{qd}^{(8)}$

Field	Irrep	Normalization	Operator
$\mathcal{B} \sim (1, 1)_0$	$\mathbf{8}_\ell$	$-(g_\mathcal{B}^\ell)^2/(12M_\mathcal{B}^2)$	$3\mathcal{O}_{\ell\ell}^E - \mathcal{O}_{\ell\ell}^D$
	$\mathbf{8}_e$	$-(g_\mathcal{B}^e)^2/(6M_\mathcal{B}^2)$	$\mathcal{O}_{ee}$
	$\mathbf{8}_q$	$-(g_\mathcal{B}^q)^2/(12M_\mathcal{B}^2)$	$3\mathcal{O}_{qq}^{(1)E} - \mathcal{O}_{qq}^{(1)D}$
	$\mathbf{8}_u$	$-(g_\mathcal{B}^u)^2/(12M_\mathcal{B}^2)$	$3\mathcal{O}_{uu}^E - \mathcal{O}_{uu}^D$
$\mathcal{B}_1 \sim (1, 1)_1$	$\mathbf{8}_d$	$-(g_\mathcal{B}^d)^2/(12M_\mathcal{B}^2)$	$3\mathcal{O}_{dd}^E - \mathcal{O}_{dd}^D$
	$(\bar{\mathbf{3}}_d, \mathbf{3}_u)$	$- g_{\mathcal{B}_1}^{du} ^2/(3M_{\mathcal{B}_1}^2)$	$\mathcal{O}_{ud}^{(1)} + 6\mathcal{O}_{ud}^{(8)}$
$\mathcal{W} \sim (1, 3)_0$	$\mathbf{8}_q$	$-(g_\mathcal{W}^q)^2/(48M_\mathcal{W}^2)$	$3\mathcal{O}_{qq}^{(3)E} - \mathcal{O}_{qq}^{(3)D}$
	$\mathbf{8}_\ell$	$(g_\mathcal{W}^\ell)^2/(48M_\mathcal{W}^2)$	$5\mathcal{O}_{\ell\ell}^E - 7\mathcal{O}_{\ell\ell}^D$
$\mathcal{L}_3 \sim (1, 2)_{-\frac{3}{2}}$	$(\mathbf{3}_e, \mathbf{3}_\ell)$	$ g_{\mathcal{L}_3} ^2/M_{\mathcal{L}_3}^2$	$\mathcal{O}_{\ell e}$
$\mathcal{U}_2 \sim (3, 1)_{\frac{2}{3}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_d)$	$- g_{\mathcal{U}_2}^{ed} ^2/M_{\mathcal{U}_2}^2$	$\mathcal{O}_{ed}$
	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_q)$	$- g_{\mathcal{U}_2}^{\ell q} ^2/(2M_{\mathcal{U}_2}^2)$	$\mathcal{O}_{\ell q}^{(1)} + \mathcal{O}_{\ell q}^{(3)}$
$\mathcal{U}_5 \sim (3, 1)_{\frac{5}{3}}$	$(\bar{\mathbf{3}}_e, \mathbf{3}_u)$	$- g_{\mathcal{U}_5} ^2/M_{\mathcal{U}_5}^2$	$\mathcal{O}_{eu}$
$\mathcal{Q}_1 \sim (3, 2)_{\frac{1}{6}}$	$(\mathbf{3}_u, \mathbf{3}_\ell)$	$ g_{\mathcal{Q}_1}^{u\ell} ^2/M_{\mathcal{Q}_1}^2$	$\mathcal{O}_{\ell u}$
	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_q)$	$2 g_{\mathcal{Q}_1}^{dq} ^2/(3M_{\mathcal{Q}_1}^2)$	$\mathcal{O}_{qd}^{(1)} - 3\mathcal{O}_{qd}^{(8)}$
$\mathcal{Q}_5 \sim (3, 2)_{-\frac{5}{6}}$	$(\mathbf{3}_d, \mathbf{3}_\ell)$	$ g_{\mathcal{Q}_5}^{d\ell} ^2/M_{\mathcal{Q}_5}^2$	$\mathcal{O}_{\ell d}$
	$(\mathbf{3}_e, \mathbf{3}_q)$	$ g_{\mathcal{Q}_5}^{eq} ^2/M_{\mathcal{Q}_5}^2$	$\mathcal{O}_{qe}$
	$(\bar{\mathbf{3}}_u, \bar{\mathbf{3}}_q)$	$2 g_{\mathcal{Q}_5}^{uq} ^2/(3M_{\mathcal{Q}_5}^2)$	$\mathcal{O}_{qu}^{(1)} - 3\mathcal{O}_{qu}^{(8)}$
$\mathcal{X} \sim (3, 3)_{\frac{2}{3}}$	$(\bar{\mathbf{3}}_\ell, \mathbf{3}_q)$	$- g_\mathcal{X} ^2/(8M_\mathcal{X}^2)$	$3\mathcal{O}_{\ell q}^{(1)} - \mathcal{O}_{\ell q}^{(3)}$
$\mathcal{Y}_1 \sim (\bar{\mathbf{6}}, 2)_{\frac{1}{6}}$	$(\bar{\mathbf{3}}_d, \bar{\mathbf{3}}_q)$	$ g_{\mathcal{Y}_1} ^2/(3M_{\mathcal{Y}_1}^2)$	$2\mathcal{O}_{qd}^{(1)} + 3\mathcal{O}_{qd}^{(8)}$
$\mathcal{Y}_5 \sim (\bar{\mathbf{6}}, 2)_{-\frac{5}{6}}$	$(\bar{\mathbf{3}}_u, \bar{\mathbf{3}}_q)$	$ g_{\mathcal{Y}_5} ^2/(3M_{\mathcal{Y}_5}^2)$	$2\mathcal{O}_{qu}^{(1)} + 3\mathcal{O}_{qu}^{(8)}$
$\mathcal{G} \sim (8, 1)_0$	$\mathbf{8}_q$	$-(g_\mathcal{G}^q)^2/(144M_\mathcal{G}^2)$	$11\mathcal{O}_{qq}^{(1)D} - 9\mathcal{O}_{qq}^{(1)E} + 9\mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(3)E}$
	$\mathbf{8}_u$	$(g_\mathcal{G}^u)^2/(36M_\mathcal{G}^2)$	$3\mathcal{O}_{uu}^E - 5\mathcal{O}_{uu}^D$
	$\mathbf{8}_d$	$(g_\mathcal{G}^d)^2/(36M_\mathcal{G}^2)$	$3\mathcal{O}_{dd}^E - 5\mathcal{O}_{dd}^D$
$\mathcal{G}_1 \sim (8, 1)_1$	$(\bar{\mathbf{3}}_d, \mathbf{3}_u)$	$ g_{\mathcal{G}_1} ^2/(9M_{\mathcal{G}_1}^2)$	$-4\mathcal{O}_{ud}^{(1)} + 3\mathcal{O}_{ud}^{(8)}$
$\mathcal{H} \sim (8, 3)_0$	$\mathbf{8}_q$	$-(g_\mathcal{H})^2/(576M_\mathcal{H}^2)$	$27\mathcal{O}_{qq}^{(1)D} - 9\mathcal{O}_{qq}^{(1)E} - 7\mathcal{O}_{qq}^{(3)D} - 3\mathcal{O}_{qq}^{(3)E}$

Field	Irrep	Normalization	Operator
$N \sim (1, 1)_0$	$\mathbf{3}_\ell$	$ \lambda_N ^2/(4M_N^2)$	$\mathcal{O}_{\phi\ell}^{(1)} - \mathcal{O}_{\phi\ell}^{(3)}$
$E \sim (1, 1)_{-1}$	$\mathbf{3}_\ell$	$- \lambda_E ^2/(4M_E^2)$	$\mathcal{O}_{\phi\ell}^{(1)} + \mathcal{O}_{\phi\ell}^{(3)} - [2y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Delta_1 \sim (1, 2)_{-\frac{1}{2}}$	$\mathbf{3}_e$	$ \lambda_{\Delta_1} ^2/(2M_{\Delta_1}^2)$	$\mathcal{O}_{\phi e} + [y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Delta_3 \sim (1, 2)_{-\frac{3}{2}}$	$\mathbf{3}_e$	$- \lambda_{\Delta_3} ^2/(2M_{\Delta_3}^2)$	$\mathcal{O}_{\phi e} - [y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Sigma \sim (1, 3)_0$	$\mathbf{3}_\ell$	$ \lambda_\Sigma ^2/(16M_\Sigma^2)$	$3\mathcal{O}_{\phi\ell}^{(1)} + \mathcal{O}_{\phi\ell}^{(3)} + [4y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$\Sigma_1 \sim (1, 3)_{-1}$	$\mathbf{3}_\ell$	$ \lambda_{\Sigma_1} ^2/(16M_{\Sigma_1}^2)$	$\mathcal{O}_{\phi\ell}^{(3)} - 3\mathcal{O}_{\phi\ell}^{(1)} + [2y_e^* \mathcal{O}_{e\phi} + \text{h.c.}]$
$U \sim (3, 1)_{\frac{2}{3}}$	$\mathbf{3}_q$	$ \lambda_U ^2/(4M_U^2)$	$\mathcal{O}_{\phi q}^{(1)} - \mathcal{O}_{\phi q}^{(3)} + [2y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$D \sim (3, 1)_{-\frac{1}{3}}$	$\mathbf{3}_q$	$- \lambda_D ^2/(4M_D^2)$	$\mathcal{O}_{\phi q}^{(1)} + \mathcal{O}_{\phi q}^{(3)} - [2y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_1 \sim (3, 2)_{\frac{1}{6}}$	$\mathbf{3}_u$	$- \lambda_{Q_1}^u ^2/(2M_{Q_1}^2)$	$\mathcal{O}_{\phi u} - [y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
	$\mathbf{3}_d$	$ \lambda_{Q_1}^d ^2/(2M_{Q_1}^2)$	$\mathcal{O}_{\phi d} + [y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_5 \sim (3, 2)_{-\frac{5}{6}}$	$\mathbf{3}_d$	$- \lambda_{Q_5} ^2/(2M_{Q_5}^2)$	$\mathcal{O}_{\phi d} - [y_d^* \mathcal{O}_{d\phi} + \text{h.c.}]$
$Q_7 \sim (3, 2)_{\frac{7}{6}}$	$\mathbf{3}_u$	$ \lambda_{Q_7} ^2/(2M_{Q_7}^2)$	$\mathcal{O}_{\phi u} + [y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$T_1 \sim (3, 3)_{-\frac{1}{3}}$	$\mathbf{3}_q$	$ \lambda_{T_1} ^2/(16M_{T_1}^2)$	$\mathcal{O}_{\phi q}^{(3)} - 3\mathcal{O}_{\phi q}^{(1)} + [2y_d^* \mathcal{O}_{d\phi} + 4y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$
$T_2 \sim (3, 3)_{\frac{2}{3}}$	$\mathbf{3}_q$	$ \lambda_{T_2} ^2/(16M_{T_2}^2)$	$\mathcal{O}_{\phi q}^{(3)} + 3\mathcal{O}_{\phi q}^{(1)} + [4y_d^* \mathcal{O}_{d\phi} + 2y_u^* \mathcal{O}_{u\phi} + \text{h.c.}]$

- Most of cases integrate out to a single linear combination of operators in the MFV basis.
- Leading directions suitable for 1D pheno analysis



# Leading directions: Phenomenology

- Compilation of the EFT bounds
- Phenomenological classes
  - Class I: 4-lepton
  - Class II: 2-quark-2-lepton
  - Class III: 4-quark
  - Class IV: W/Z corrections
  - Class V: oblique/Higgs

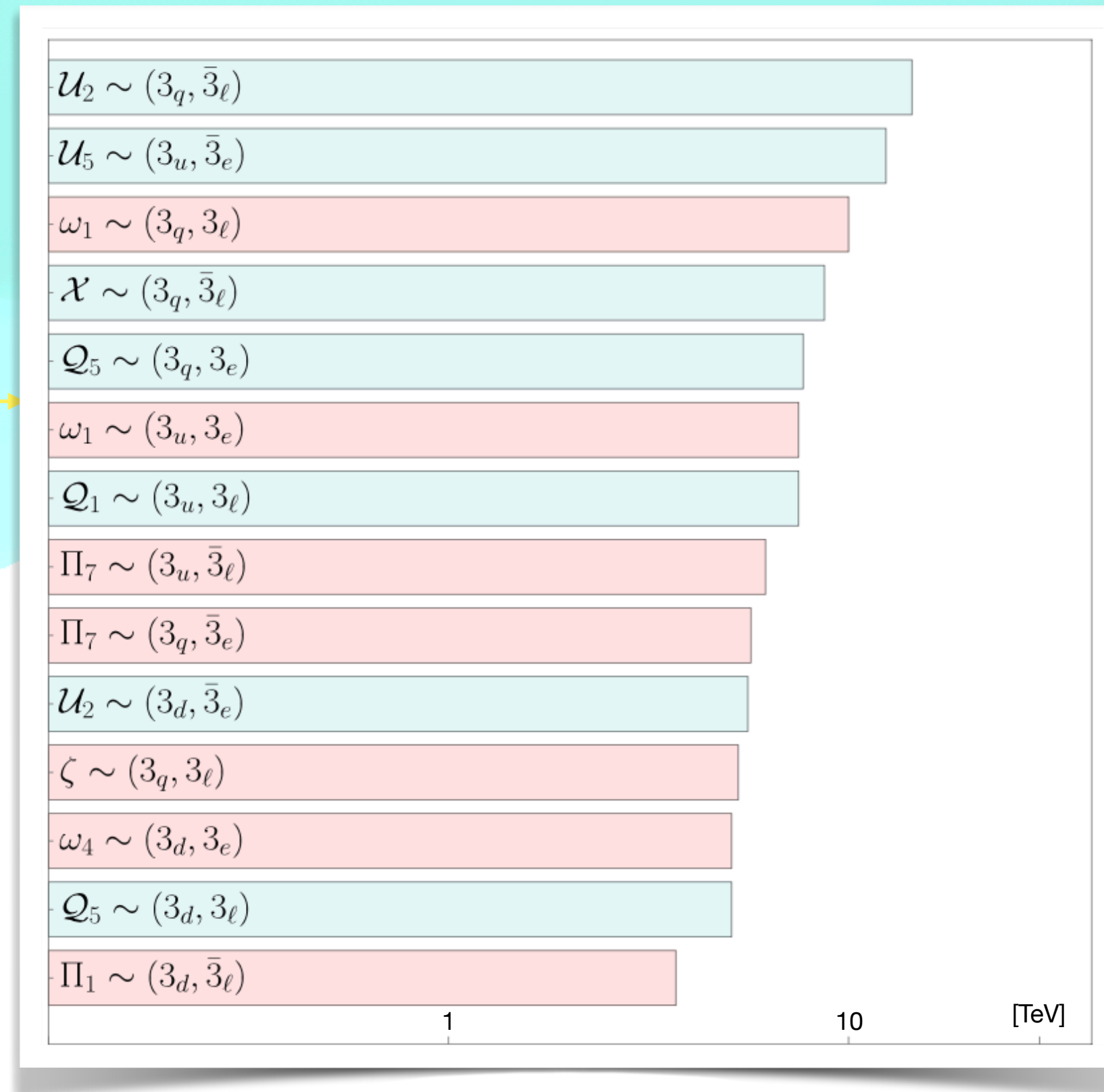
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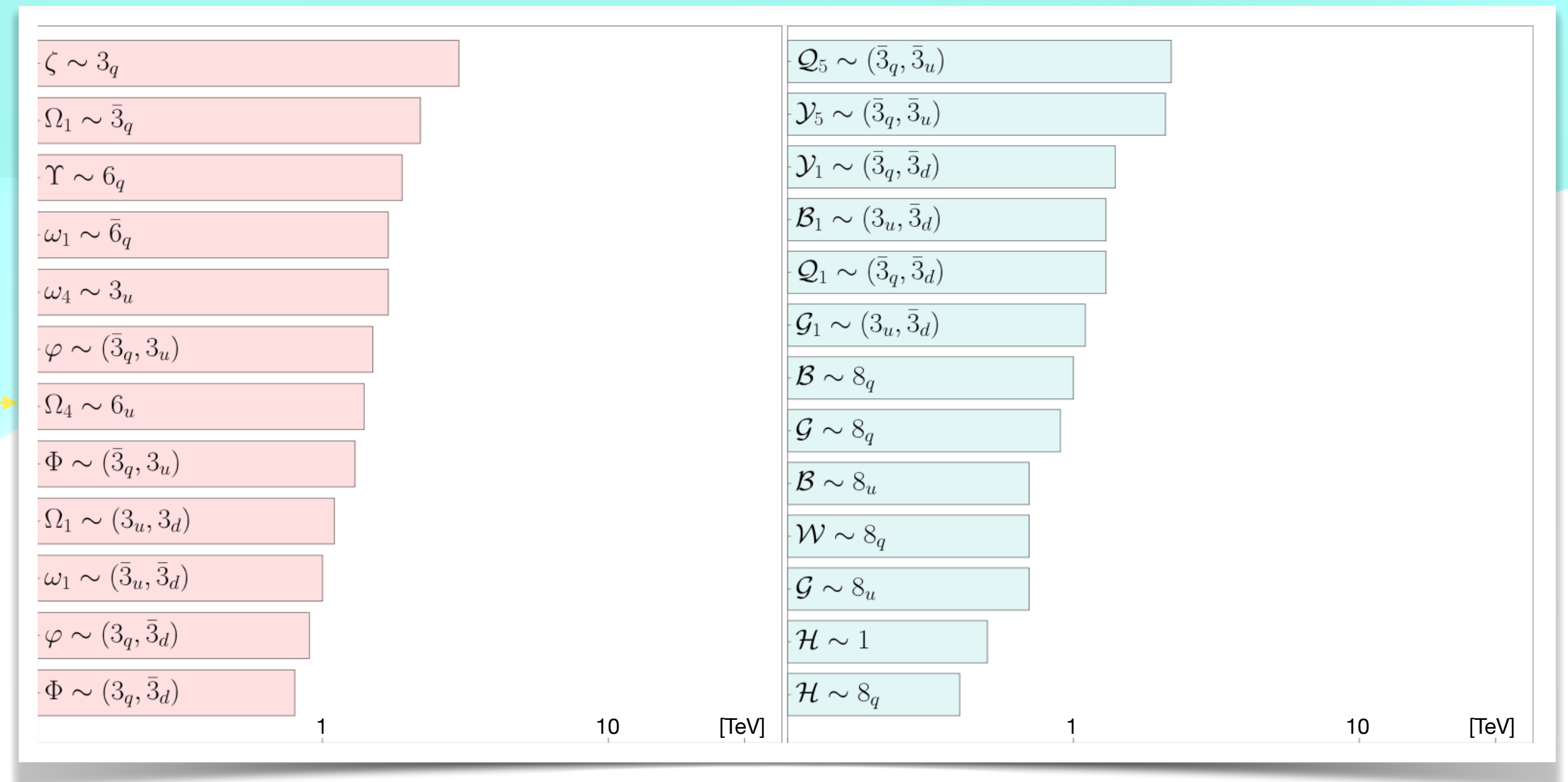
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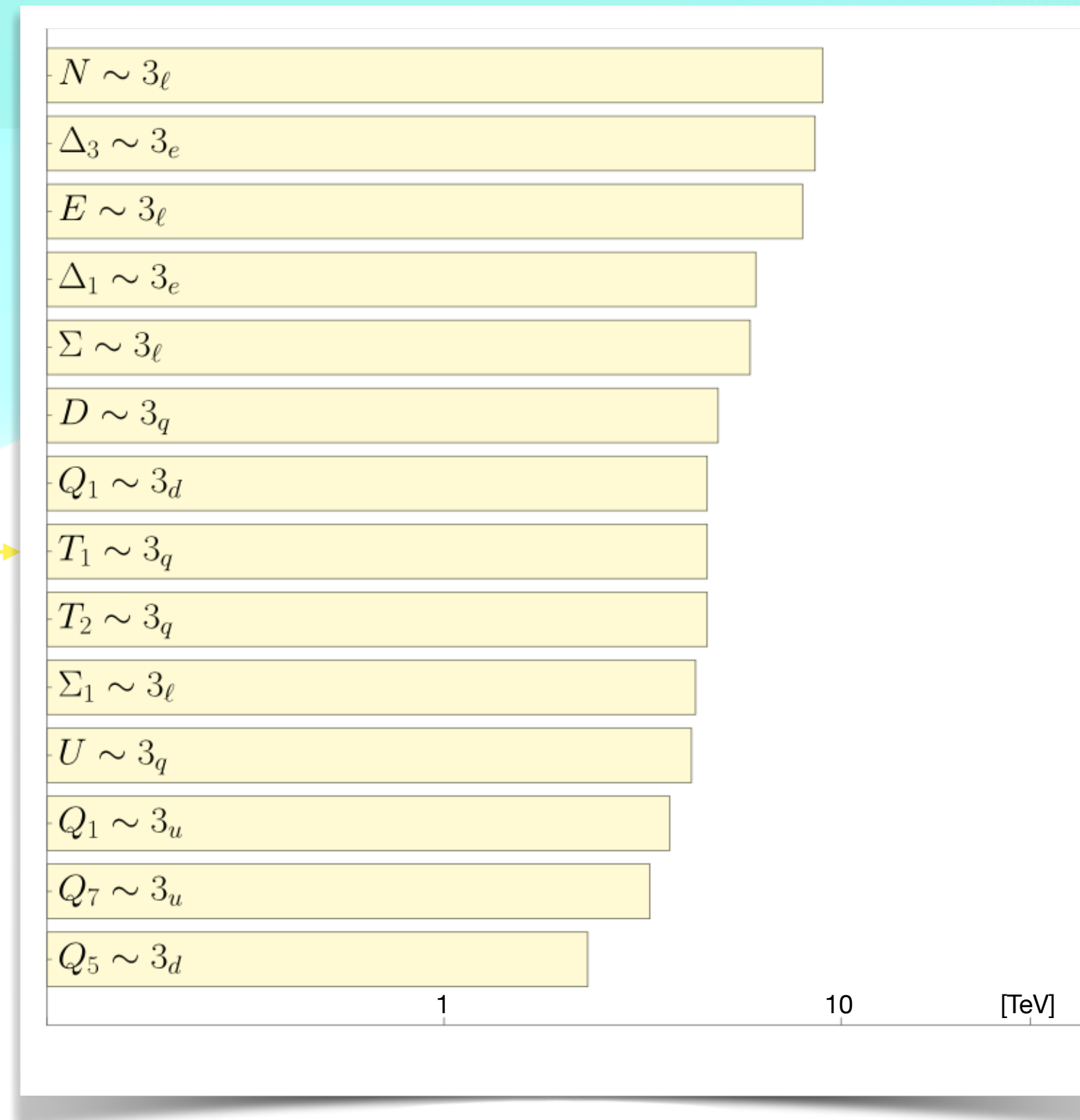
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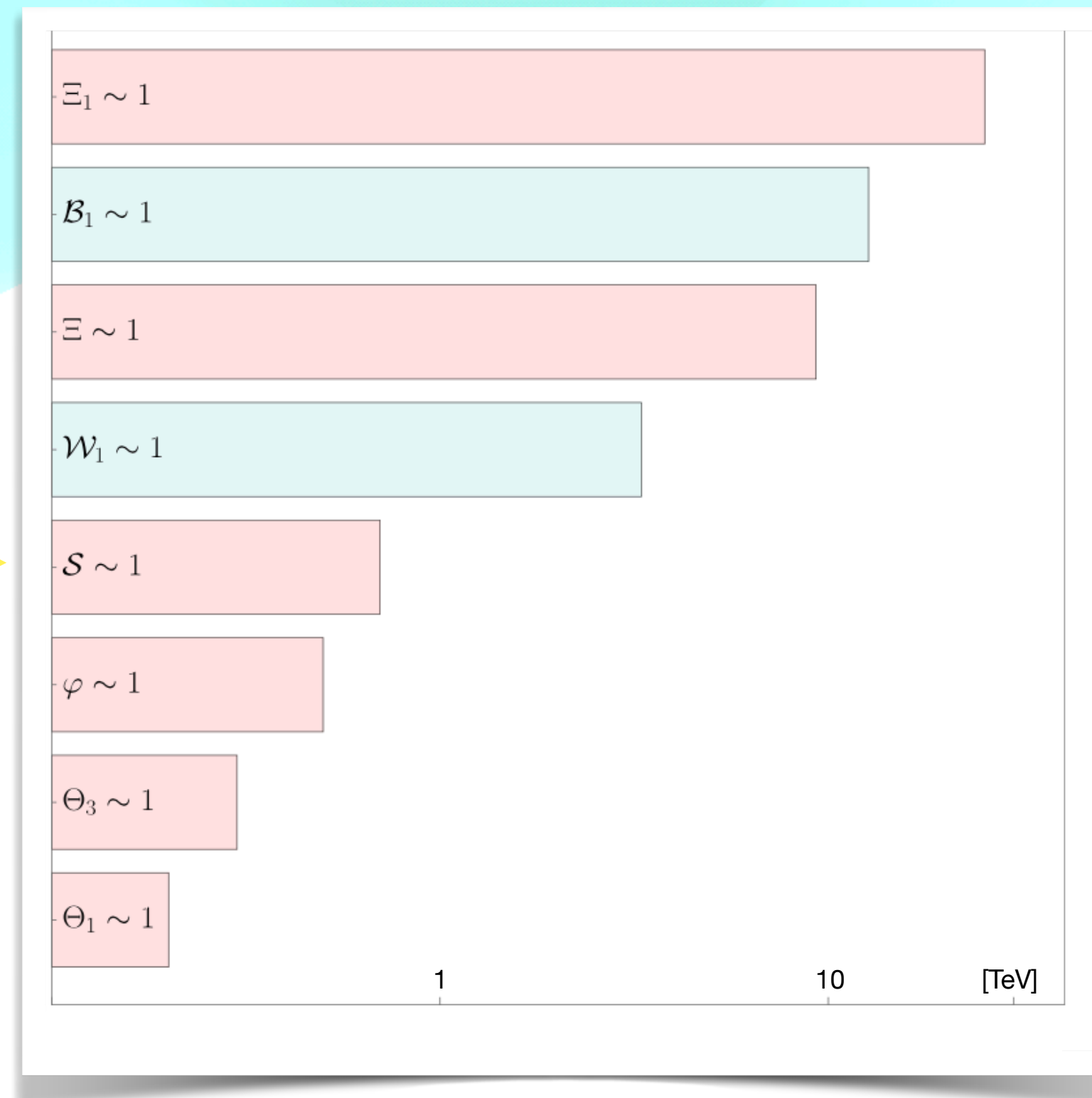
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- Comprehensive bottom-up study as the interplay of flavor symmetries and UV completions
- Several interesting improvements and promising directions for future study
  - RGE analysis of the MFV directions
  - $U(2)^5$  directions



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