

Unleashing the power of generative models: Anomalies, Simulations, and other Surrogates

Gregor Kasieczka

Email: gregor.kasieczka@uni-hamburg.de

Twitter/X: [@GregorKasieczka](https://twitter.com/GregorKasieczka)

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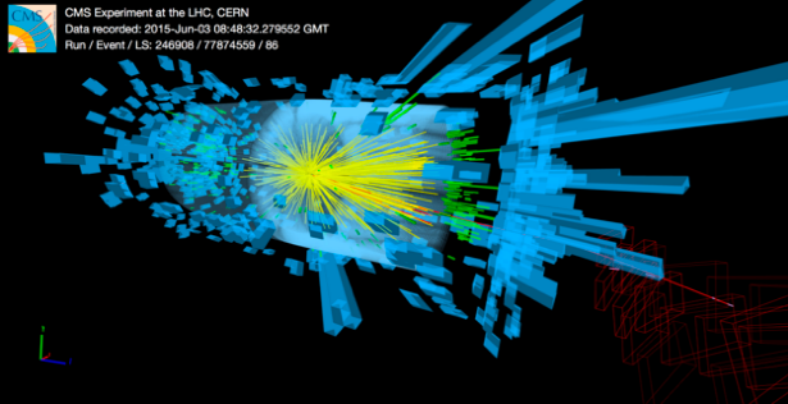
GEFÖRDERT VOM

 Bundesministerium
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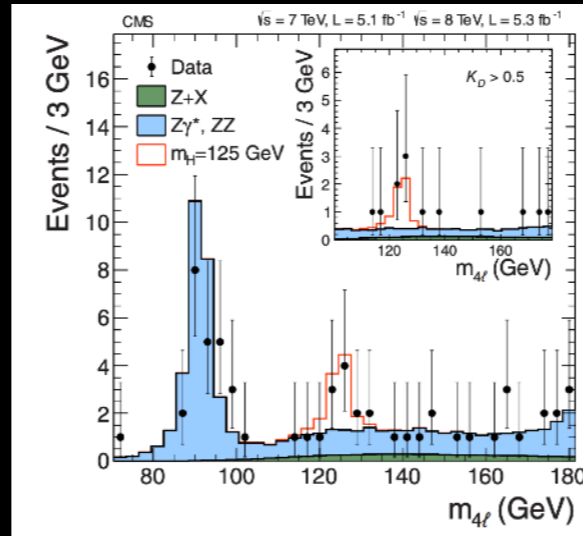
**Emmy Noether-
Programm**
Deutsche
Forschungsgemeinschaft
DFG



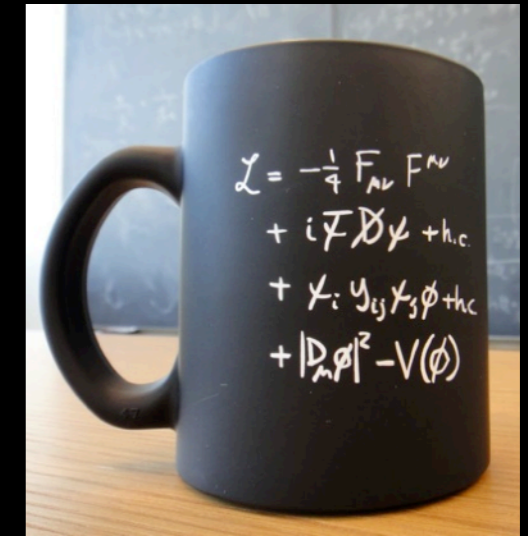
Data at CERN



What the media sees



What experimentalists see



What theorists see

```

GENIE GHEP event Record [print level: 0]
-----
Idx  Name  |  Ixt  |  PDG  |  Mother  |  Daughter  |  Px  |  Py  |  Pz  |  E  |  m
-----
0  nu_mu  |  0  |  14  |  -1  |  -1  |  4  |  4  |  0.083  |  -0.247  |  2.425  |  2.442  |  0.089
1  C12  |  0  |  1000000120  |  -1  |  -1  |  2  |  3  |  0.089  |  0.089  |  0.089  |  11.175  |  11.175
2  neutron  |  11  |  2112  |  1  |  -1  |  5  |  5  |  0.085  |  -0.083  |  -0.121  |  0.919  |  **0.940
3  C11  |  2  |  1000000110  |  1  |  -1  |  7  |  7  |  -0.085  |  0.083  |  0.121  |  10.255  |  10.254
4  mu_  |  -1  |  13  |  0  |  -1  |  9  |  12  |  0.534  |  -0.573  |  2.149  |  2.281  |  0.166
5  proton  |  14  |  2212  |  2  |  -1  |  6  |  6  |  -0.446  |  0.243  |  0.168  |  1.080  |  0.938
6  proton  |  -1  |  2212  |  5  |  -1  |  -1  |  -1  |  -0.482  |  0.219  |  -0.152  |  1.055  |  0.938
7  HadrBlob  |  15  |  2000000002  |  3  |  -1  |  -1  |  -1  |  -0.085  |  0.083  |  0.121  |  10.255  |  **0.080
8  NucBindF  |  -1  |  2000000101  |  -1  |  -1  |  -1  |  -1  |  -0.044  |  0.024  |  0.017  |  0.025  |  **0.080
9  mu_  |  1  |  13  |  4  |  -1  |  -1  |  -1  |  0.352  |  -0.349  |  1.342  |  1.432  |  0.160
10  gamma  |  1  |  22  |  4  |  -1  |  -1  |  -1  |  0.089  |  0.089  |  0.081  |  0.081  |  0.080
11  gamma  |  1  |  22  |  4  |  -1  |  -1  |  -1  |  -0.089  |  -0.089  |  0.089  |  0.089  |  0.080
12  gamma  |  1  |  22  |  4  |  -1  |  -1  |  -1  |  -0.089  |  -0.089  |  0.089  |  0.081  |  0.080
-----
Pin-Int:  |  0.264  |  0.089  |  -0.965  |  -1.927
Vertex:  nu_mu @ (x = 0.72958 m, y = -2.72705 m, z = 24.47174 m, t = 7.366651e-08 s)
-----
Error in <TBranchObject::TBranch::WriteBasketImpl>: basket's WriteBuffer failed.
Error in <TBranchObject::TBranch::Fill>: Failed to write out basket.
Error in <TTree::Fill>: Failed filling branch:gtree.gmcrec, nbytes=-1, entry=103
This error is symptomatic of a Tree created as a memory-resident Tree
Instead of doing:
  TTree *T = new TTree(...)
  TFile *f = new TFile(...)
you should do:
  TFile *f = new TFile(...)
  TTree *T = new TTree(...)
-----
rockprop::Propagator::RunPropagation -- Processing event: 1166
rockprop::PrimaryGeneratorAction::GeneratePrimitives -- FOUND UNKNOWN PARTICLE with PDG: 2000000101
rockprop::Propagator::RunPropagation -- Found 1 particles in event 1166. Dumping the event record
    
```

What grad students see

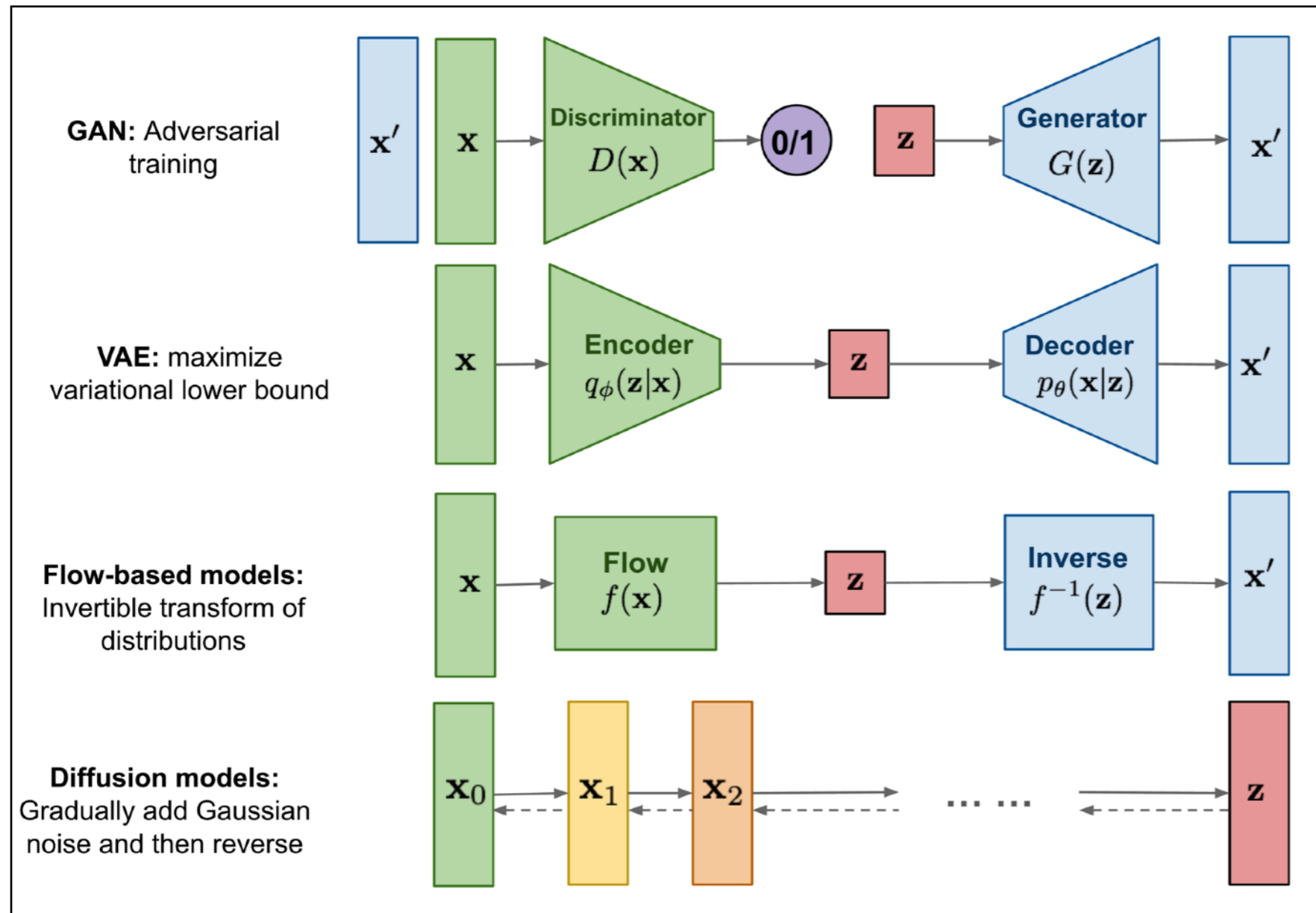


What tourists see

$$p(x)$$

What generative models see

Generative Models



Either **implicitly** or **explicitly** learn (an approximation) to

$$p(x)$$

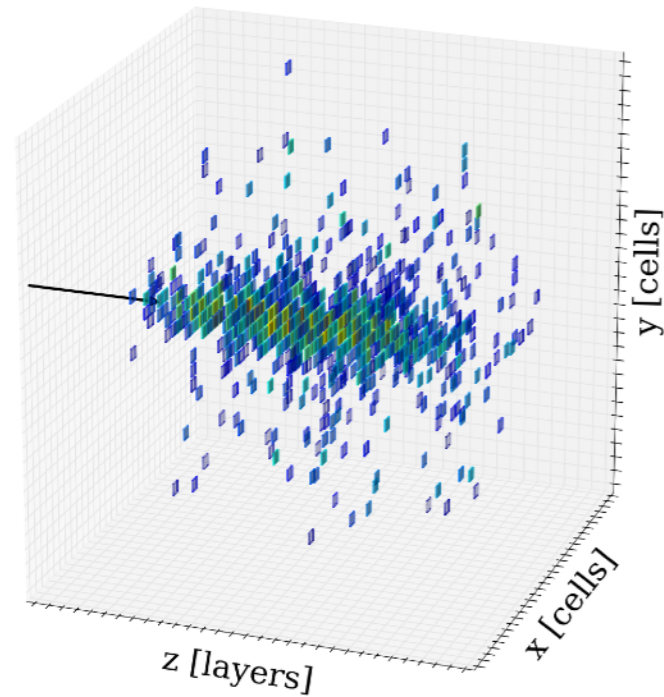
(the probability density of simulation or data)

Why generative models?

$$p(x)$$

Sample $X_i \sim p(x)$
to generate datapoints

Why generative models?



Showers in complex high-resolution calorimeters

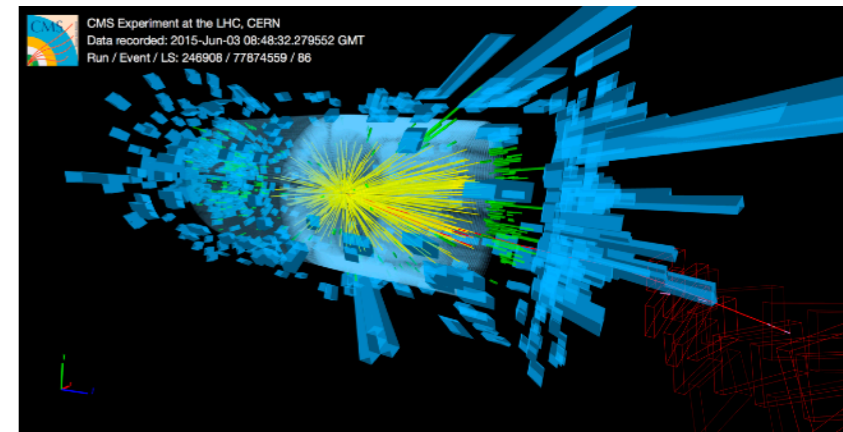
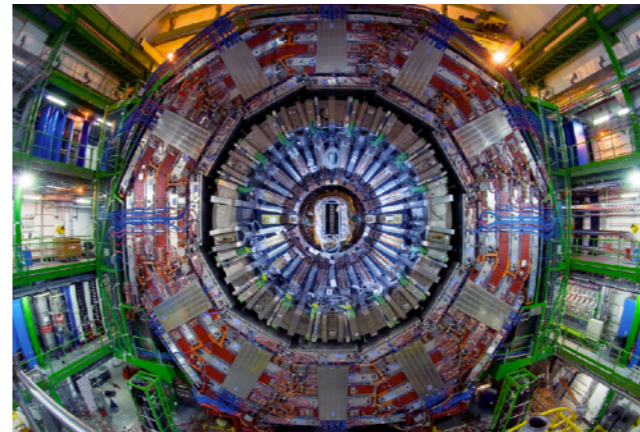
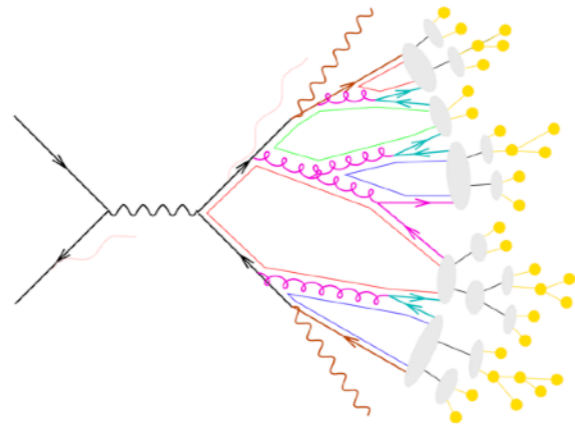
$$p(x)$$

Sample $X_i \sim p(x)$
to generate datapoints

Motivation

This happens in the experiment

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi} \not{D} \psi + h.c. \\ & + \chi_i Y_{ij} \chi_j \phi + h.c. \\ & + |D_\mu \phi|^2 - V(\phi) \end{aligned}$$



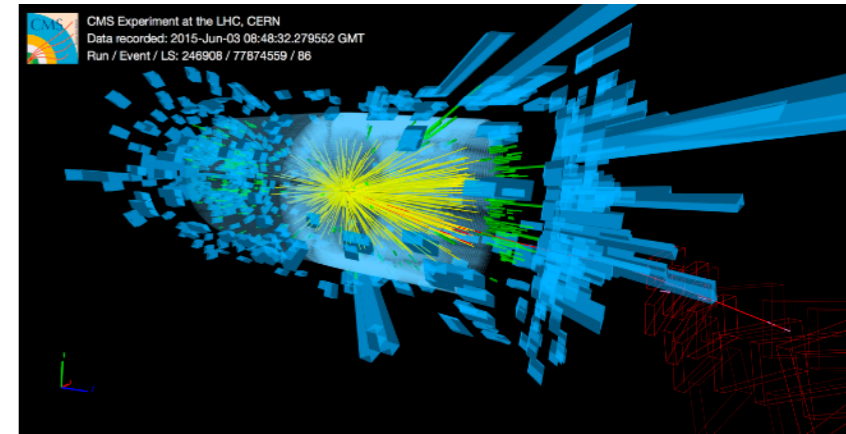
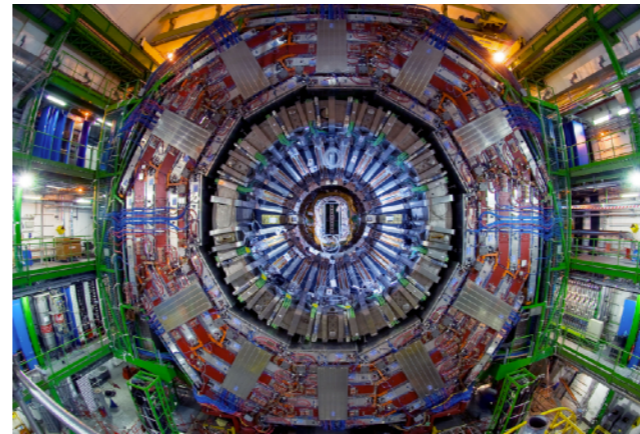
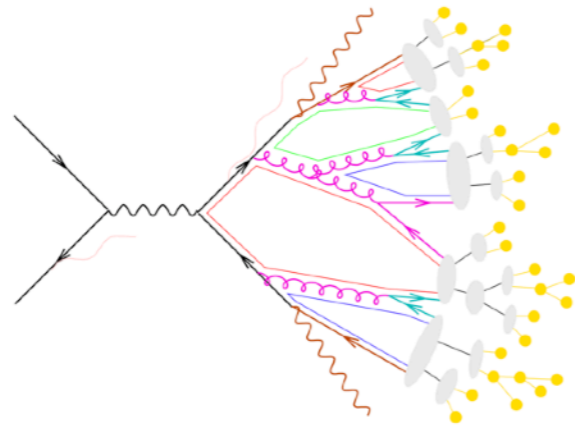
This is what we want to know

Simulation is crucial to connect
experimental data with theory
predictions

Motivation

This happens in the experiment

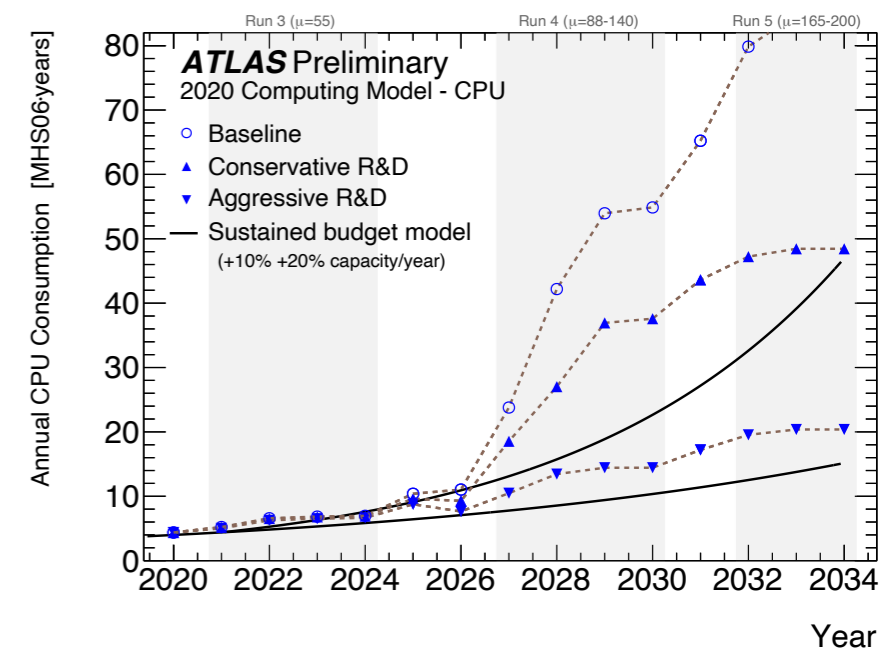
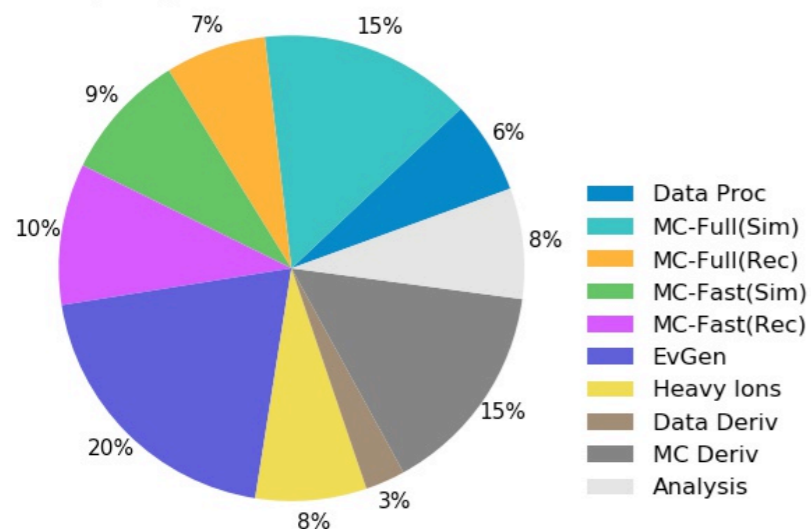
$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + h.c. + \chi_i Y_{ij} \chi_j \phi + h.c. + |D_\mu \phi|^2 - V(\phi)$$



This is what we want to know

Simulation is crucial to connect experimental data with theory predictions, **but computationally very costly**

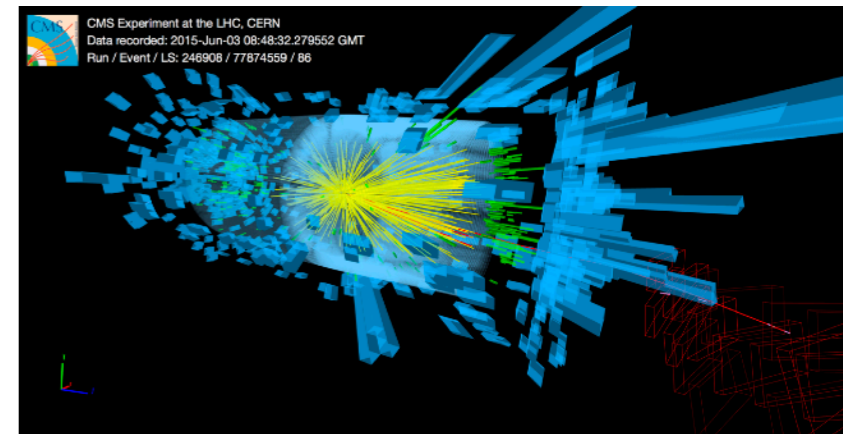
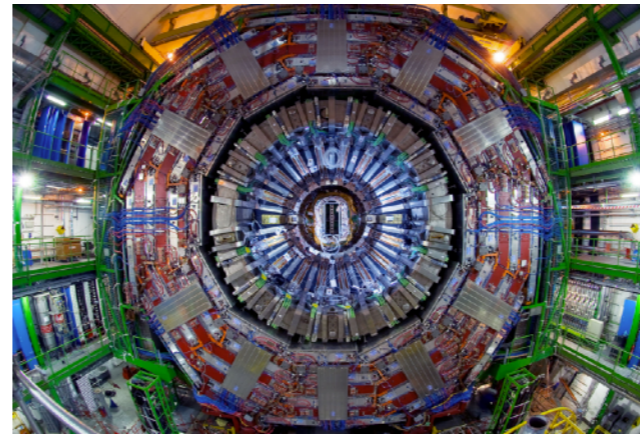
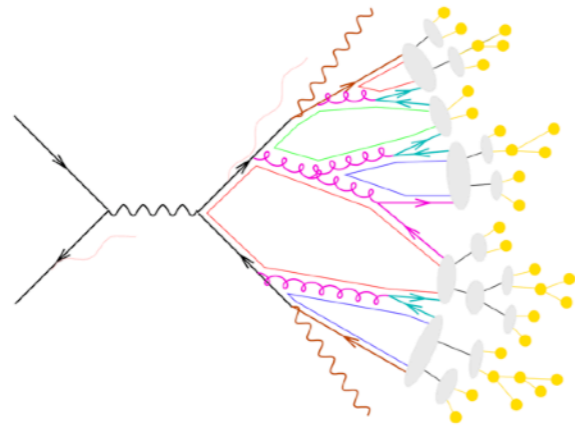
ATLAS Preliminary
2020 Computing Model -CPU: 2030: Baseline



Motivation

This happens in the experiment

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi} \not{D} \psi + h.c. \\ & + \chi_i Y_{ij} \chi_j \phi + h.c. \\ & + |D_\mu \phi|^2 - V(\phi) \end{aligned}$$

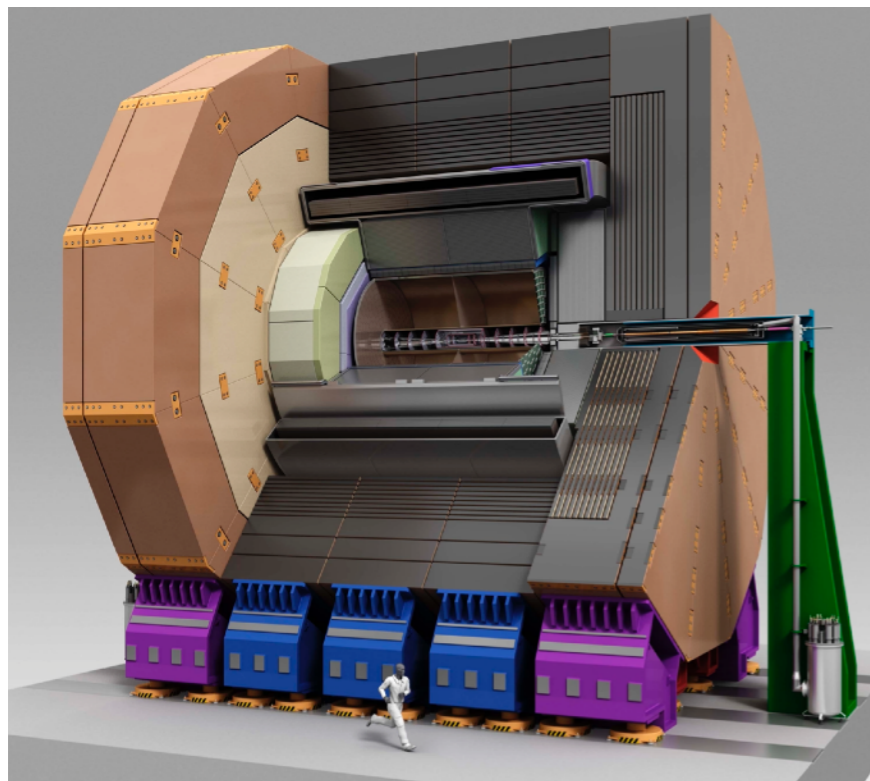
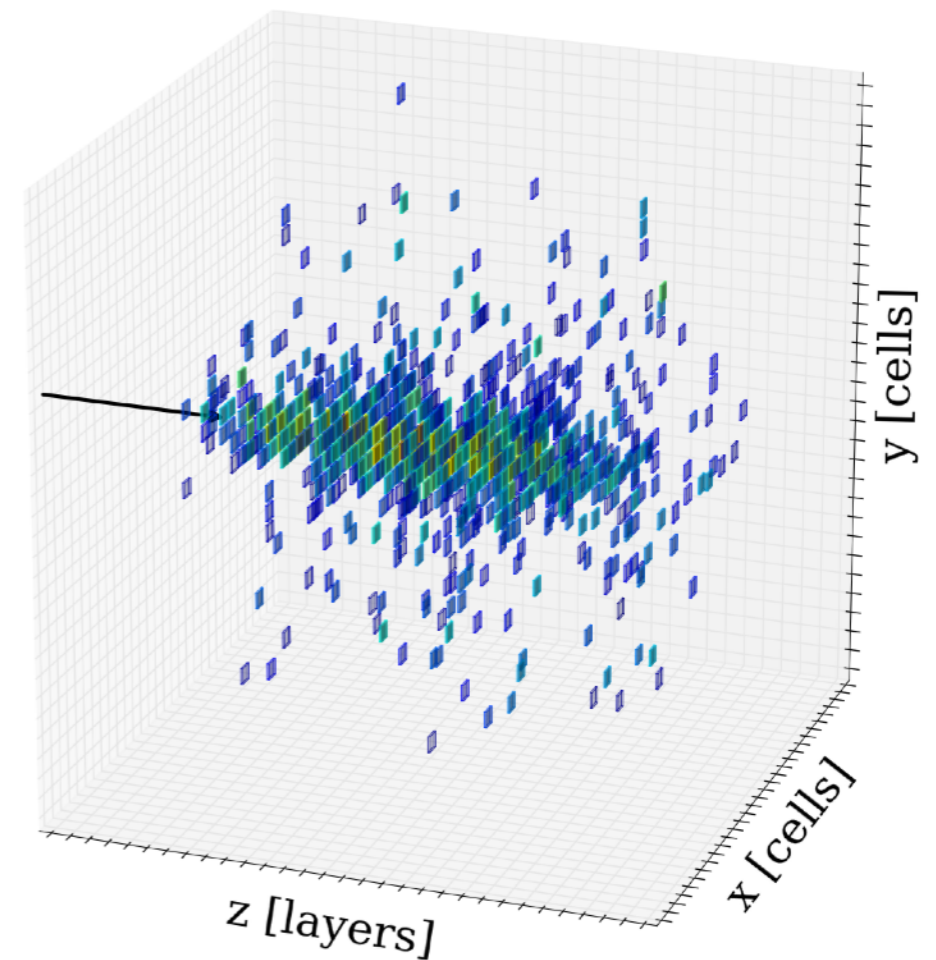
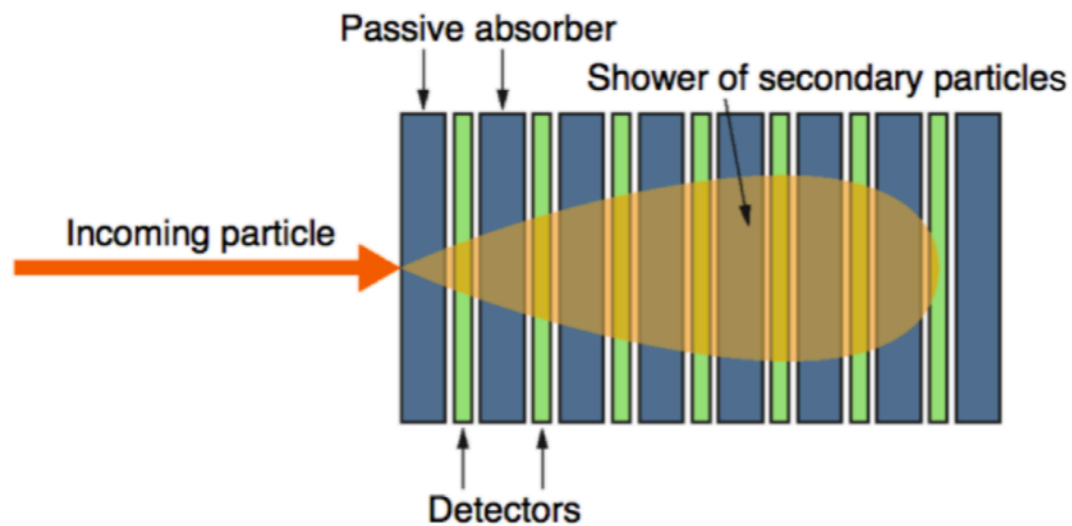


This is what we want to know

Simulation is crucial to connect experimental data with theory predictions, but computationally very costly

→ Use generative models trained on simulation or data to augment simulations

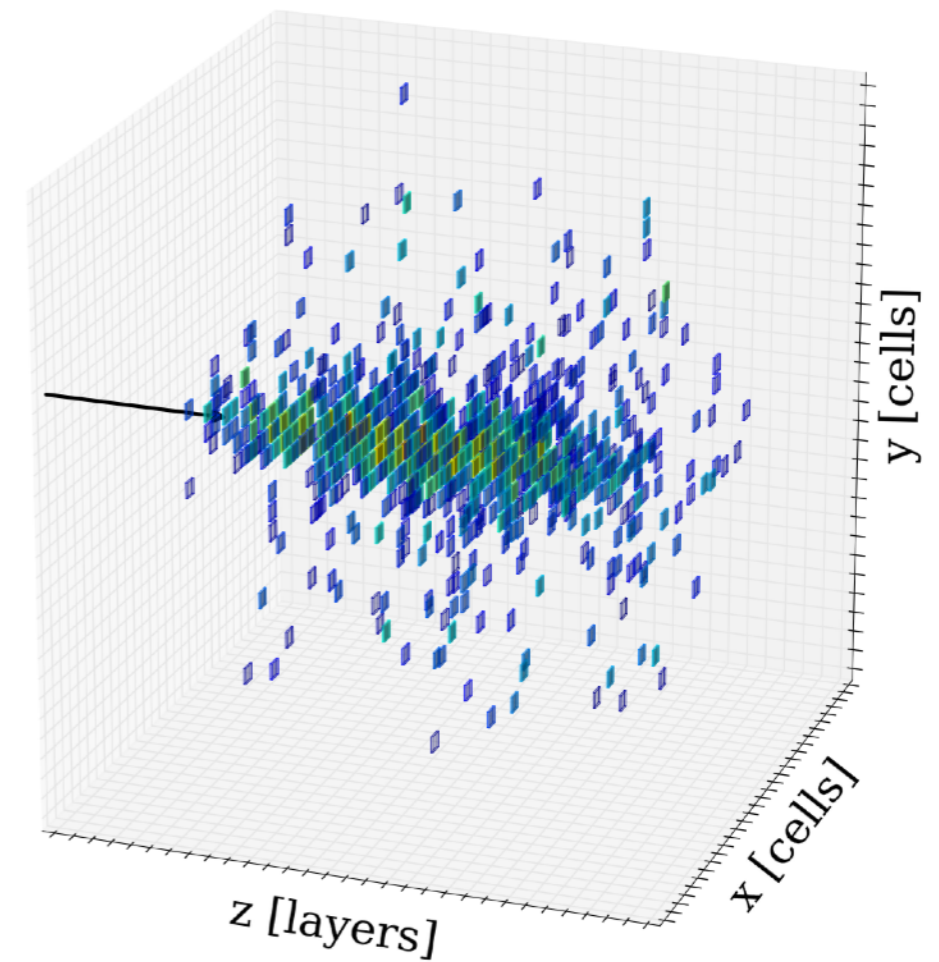
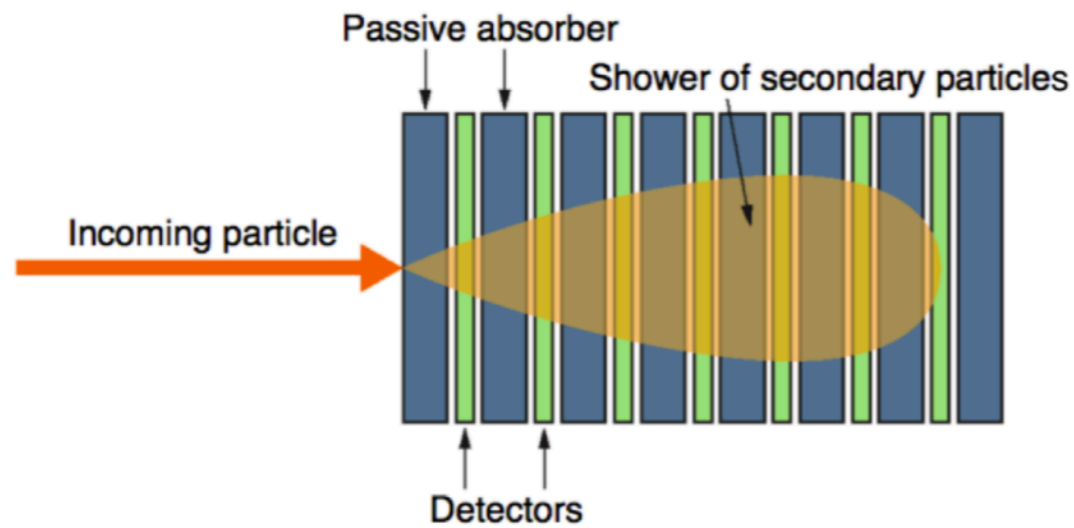
Simulation target



ILD Detector

- Shower in ILD Electromagnetic Calorimeter
- 30x30x30 cells (Si-W)
- Photon energies from 10 to 100 GeV
- Use 950k examples (uniform in energy) created with GEANT4 to train

Simulation target

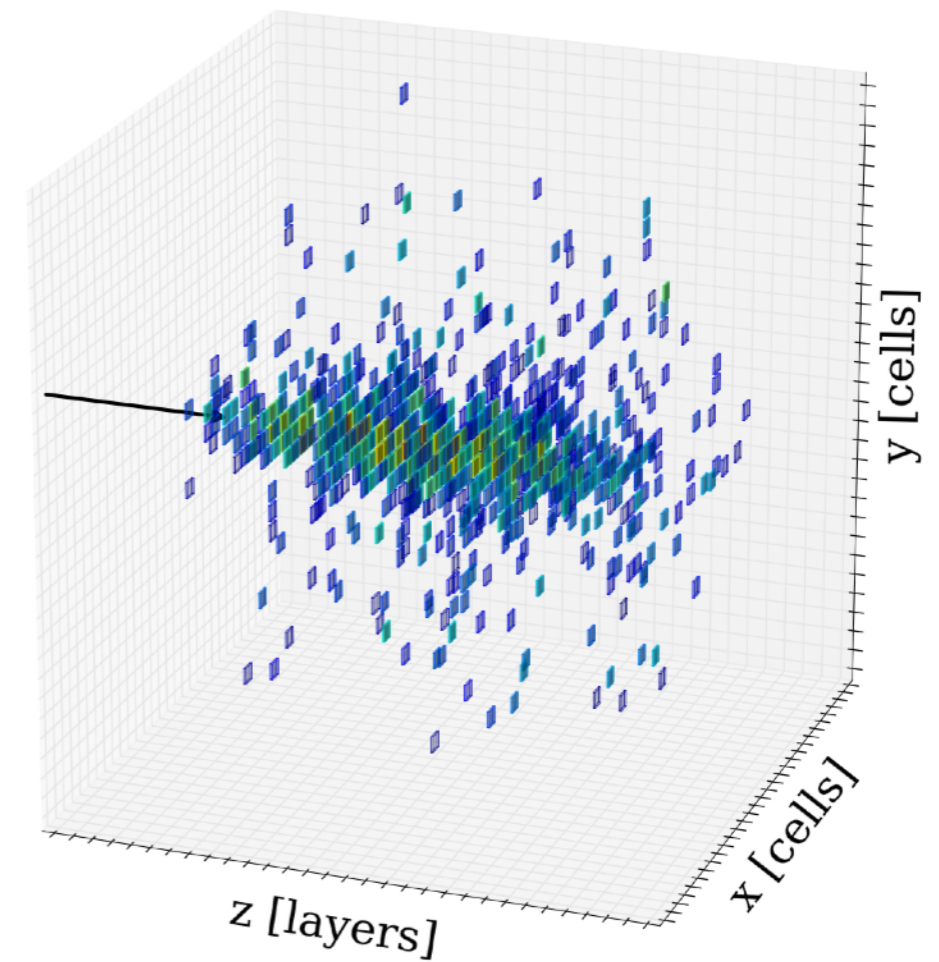
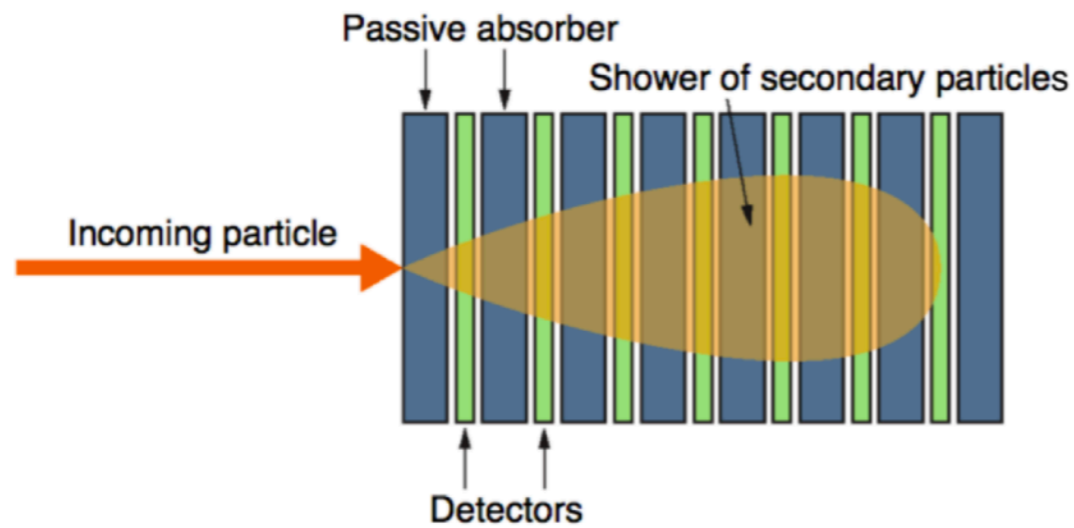


How to represent?

Tabular data:

Easy, insufficient for high-dimensions

Simulation target

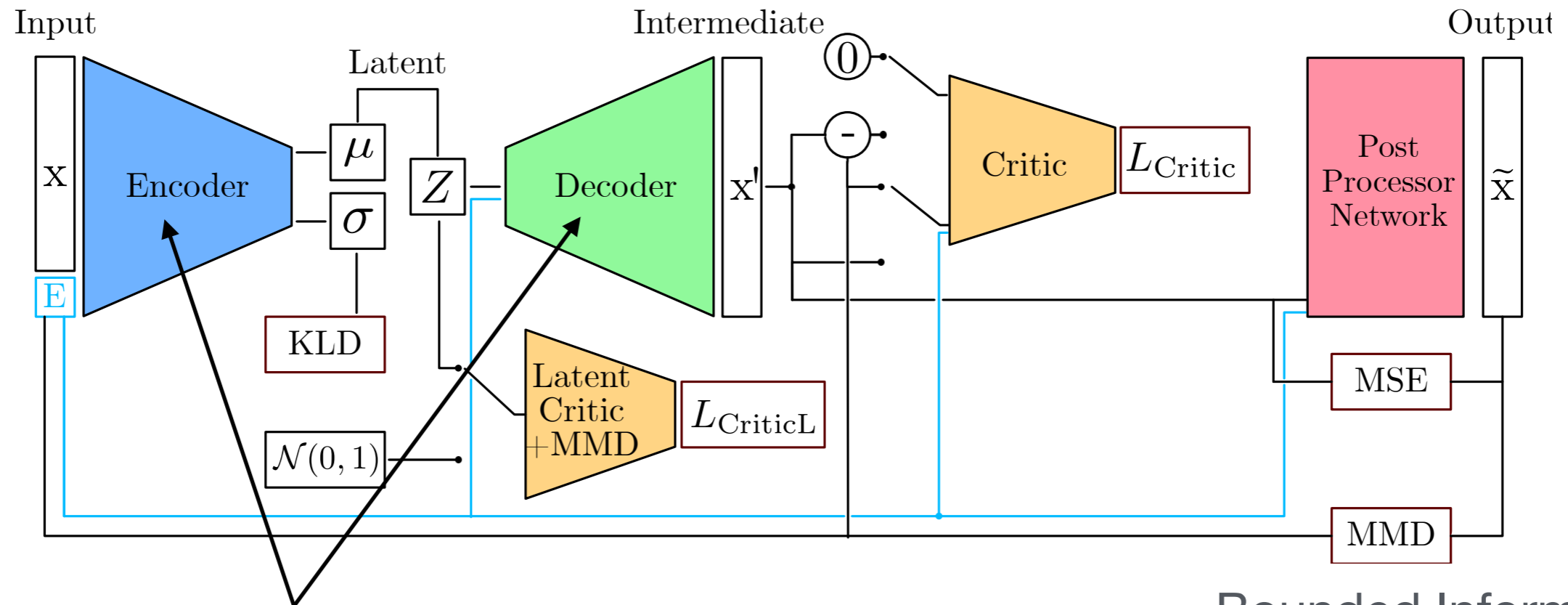


How to represent?

Tabular data

Fixed grid: Voxel image
(allows using e.g. convolutional networks)

Generative Architecture



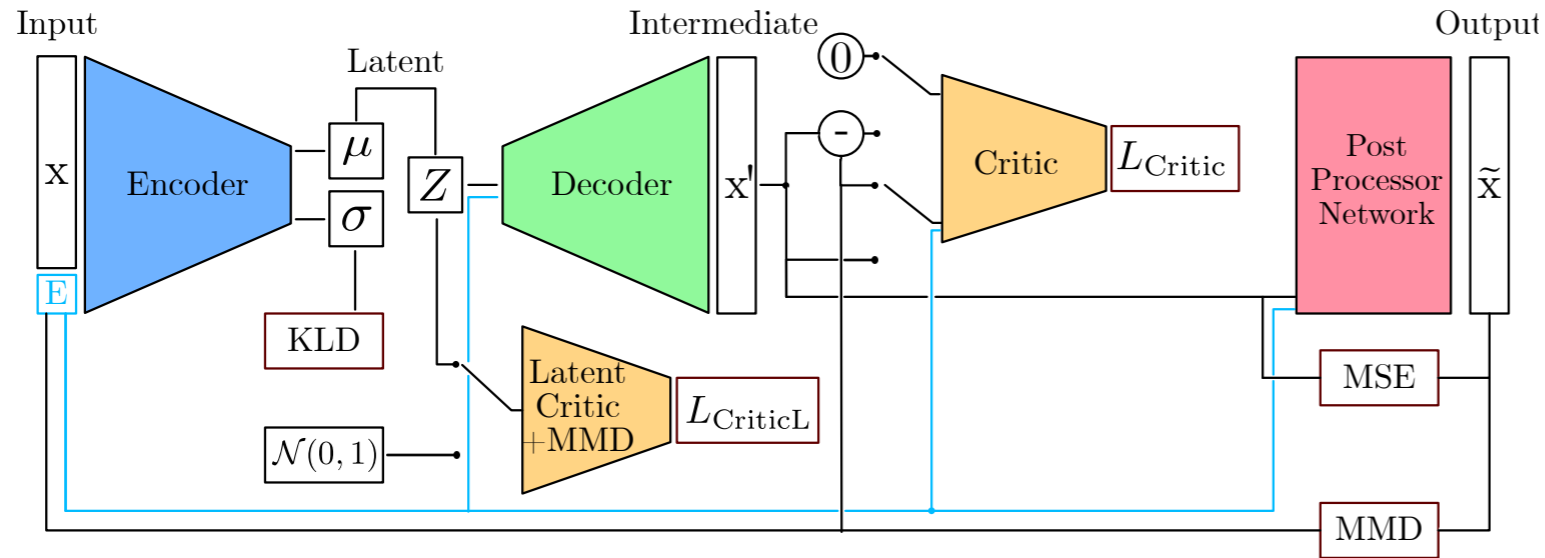
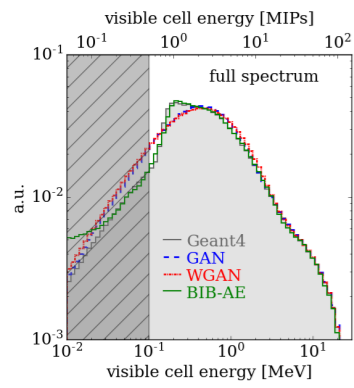
(Transposed) Convolution

Bounded Information Bottleneck AE

BIB-AE (GAN + VAE)

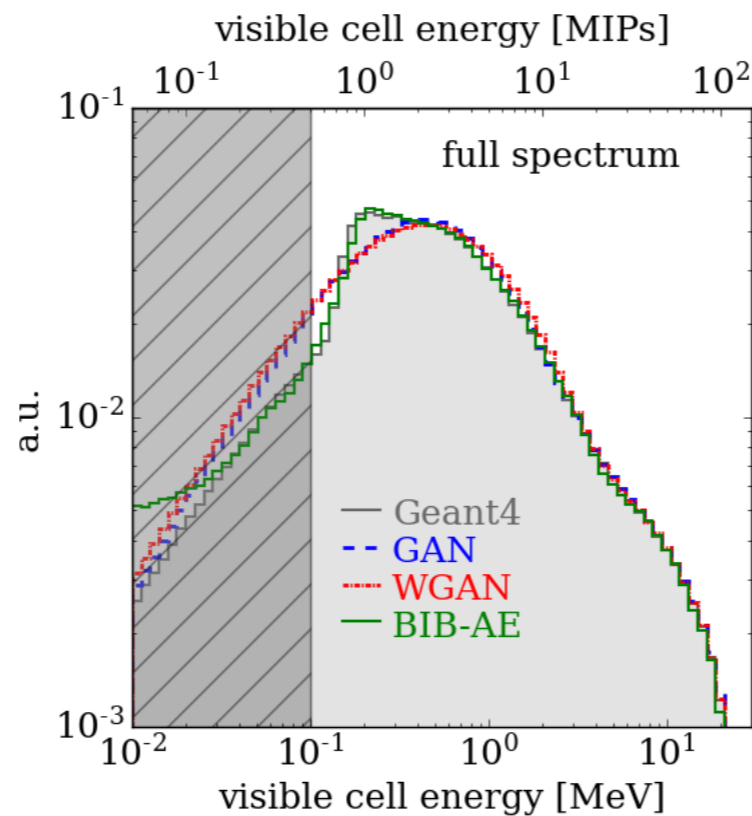
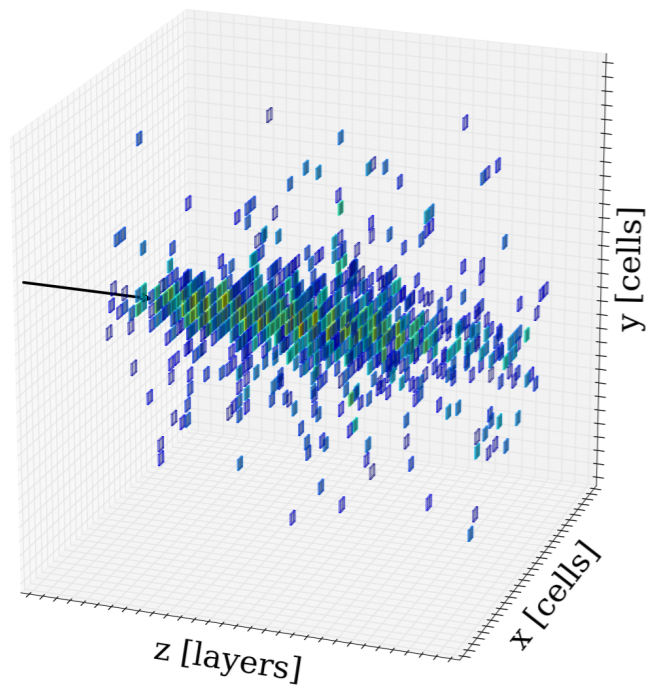
$$\begin{aligned}
 L_{\text{BIB-AE}} = & -\beta_{C_L} \cdot \mathbb{E}[C_L(N_E(x))] && \text{Latent Critic} \\
 & -\beta_C \cdot \mathbb{E}[C_E(D_E(N_E(x)))] && \text{Critic} \\
 & -\beta_{C_D} \cdot \mathbb{E}[C_{D,E}(D_E(N_E(x)) - x)] && \text{Difference Critic} \\
 & +\beta_{\text{KLD}} \cdot \text{KLD}(N_E(x)) && \text{Latent Regularisation} \\
 & +\beta_{\text{MMD}} \cdot \text{MMD}(N_E(x), \mathcal{N}(0, 1)).
 \end{aligned}$$

Generative progress

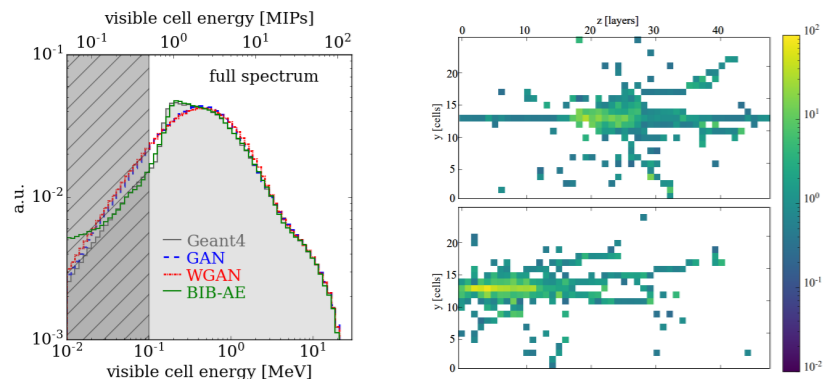


Progress

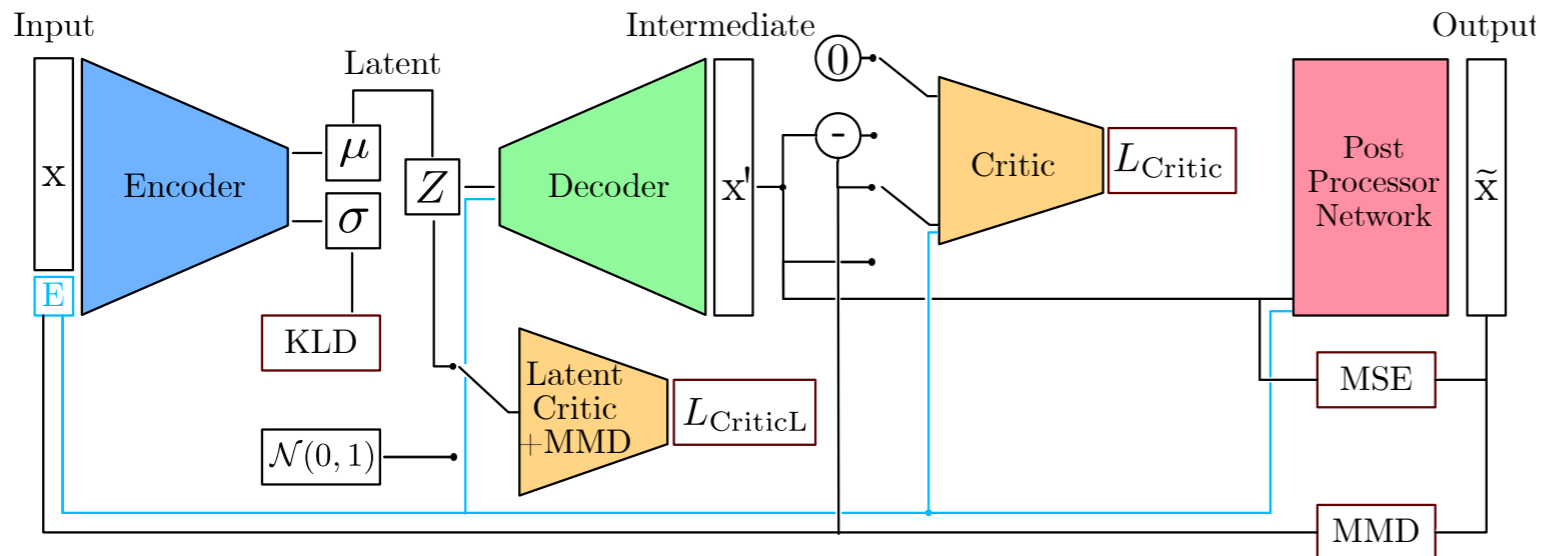
BIB-AE (GAN + VAE):
1st simulation of Photon
shower in 27k cell
calorimeter



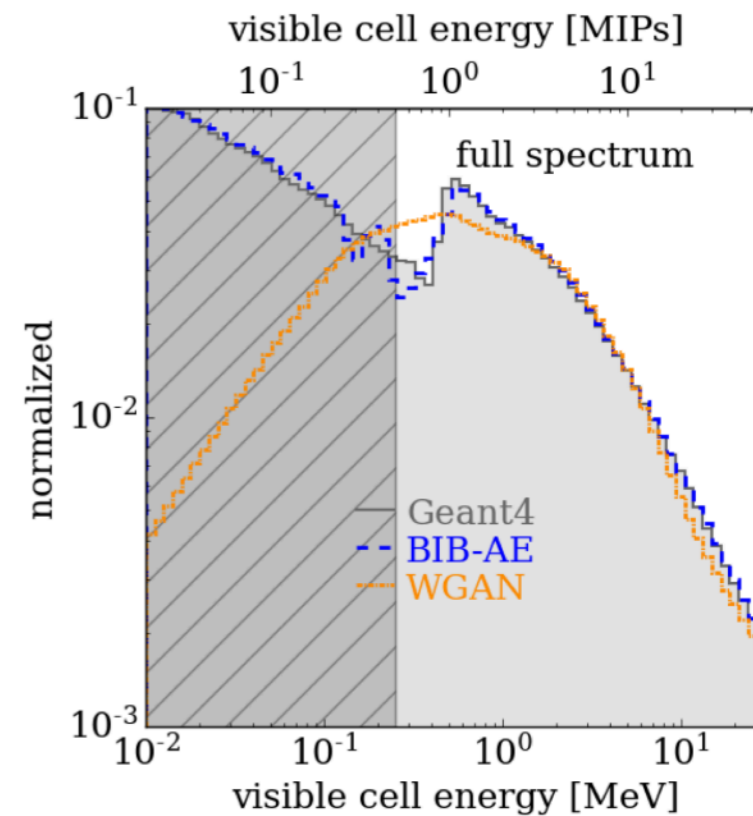
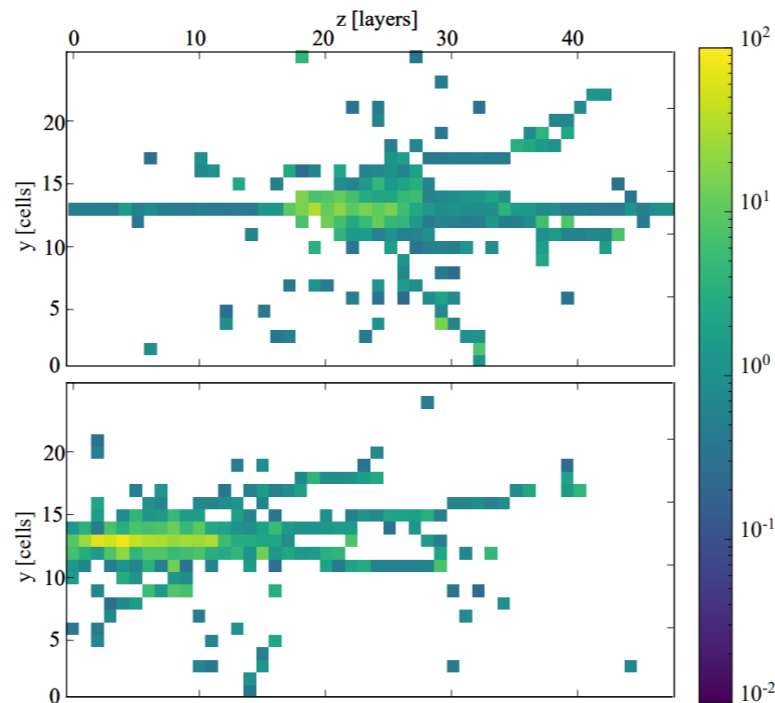
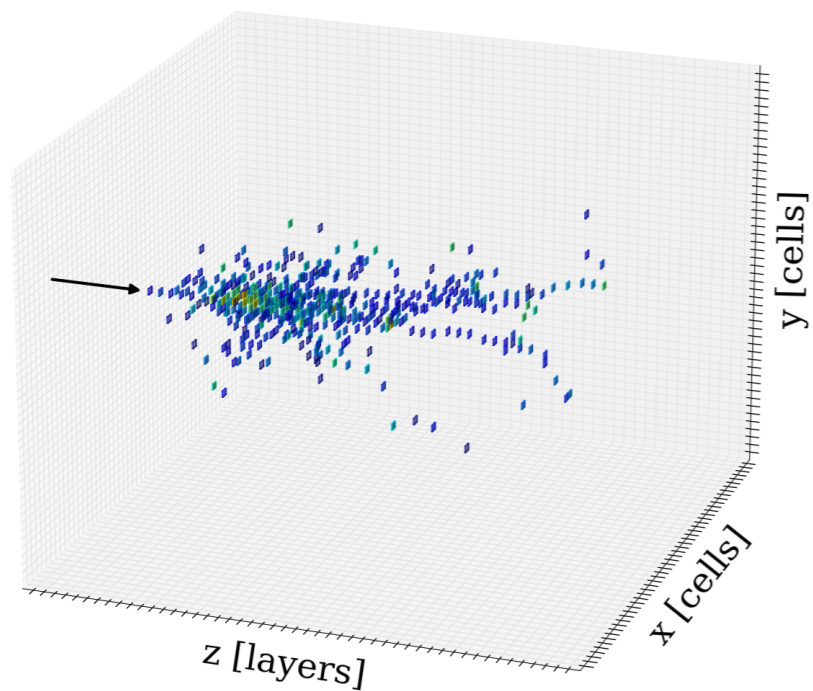
Iterative progress

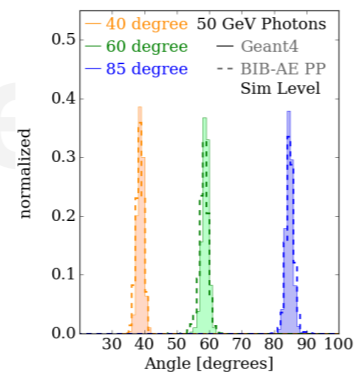
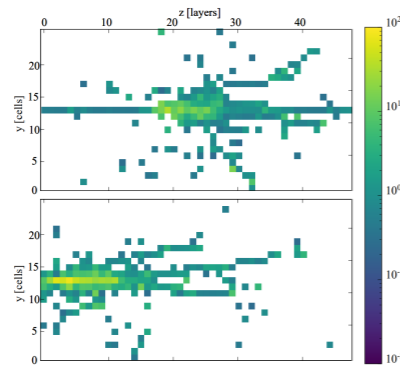
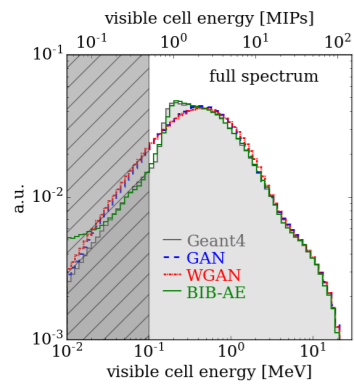


Progress

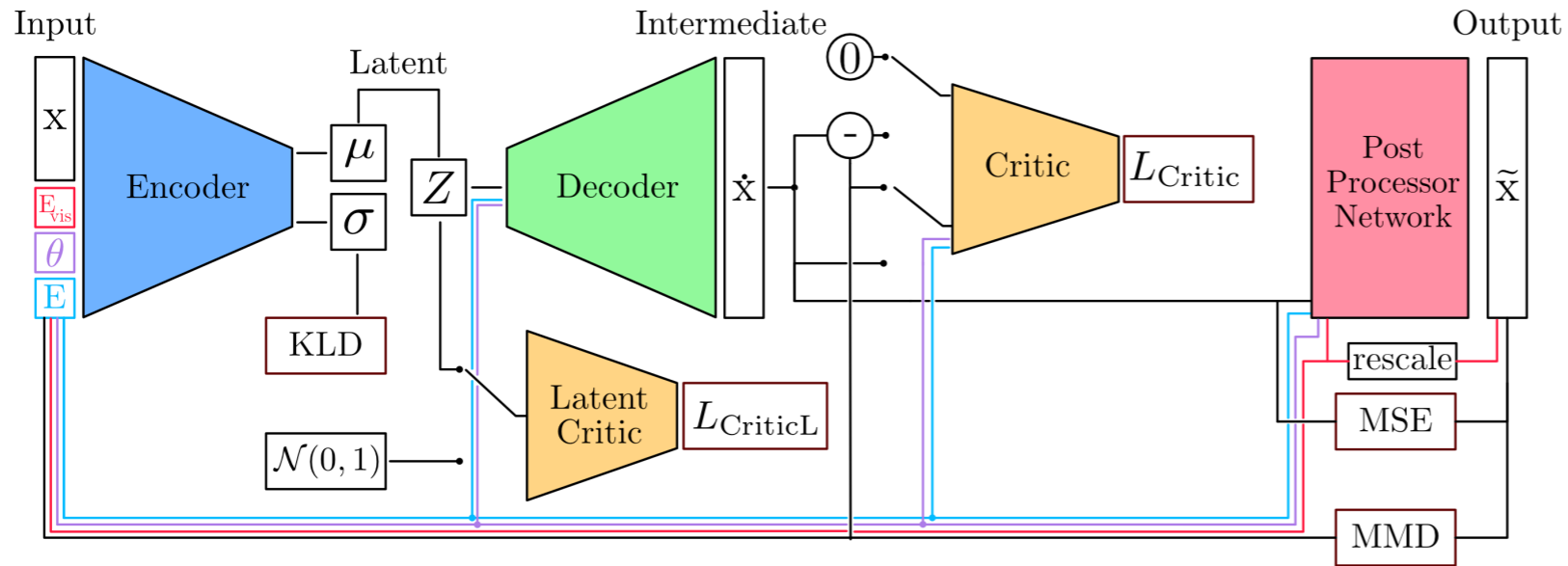


Handle **more complex** pion showers in hadronic calorimeter



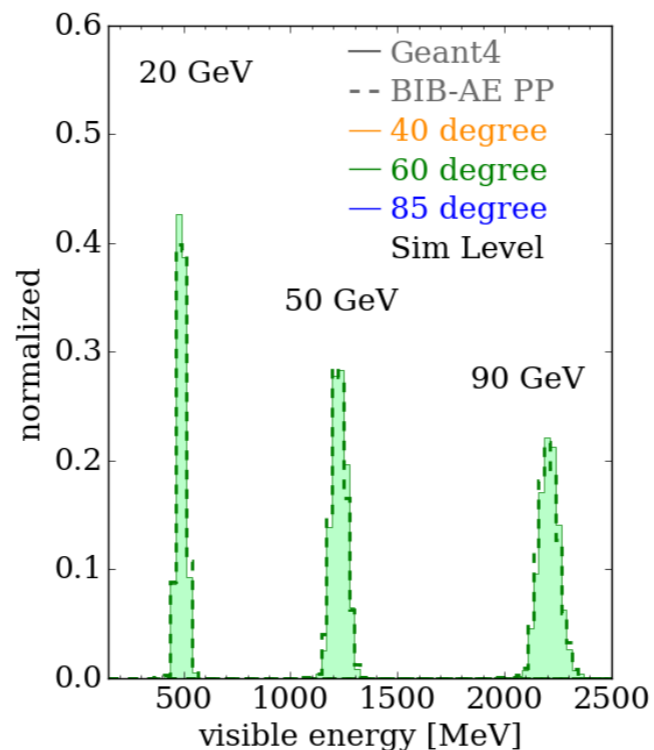
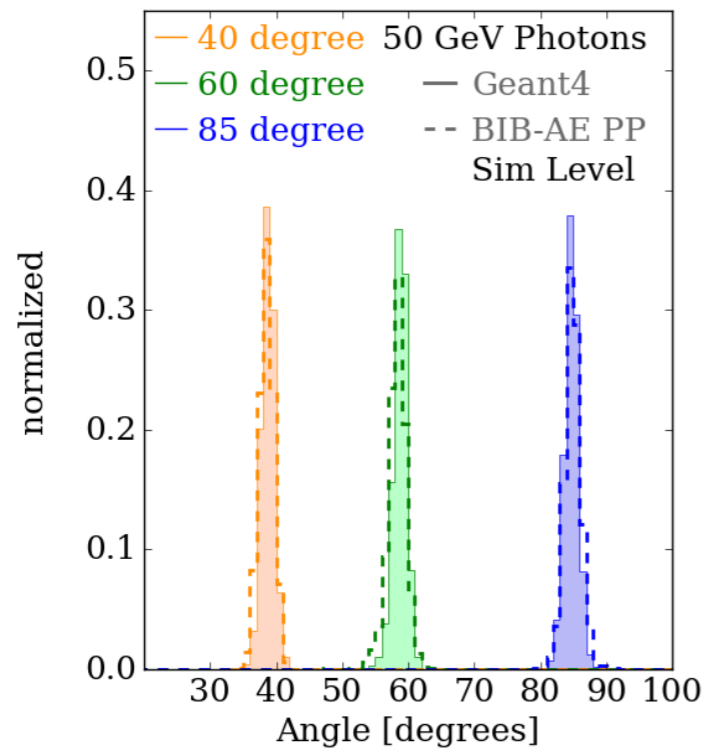


Progress

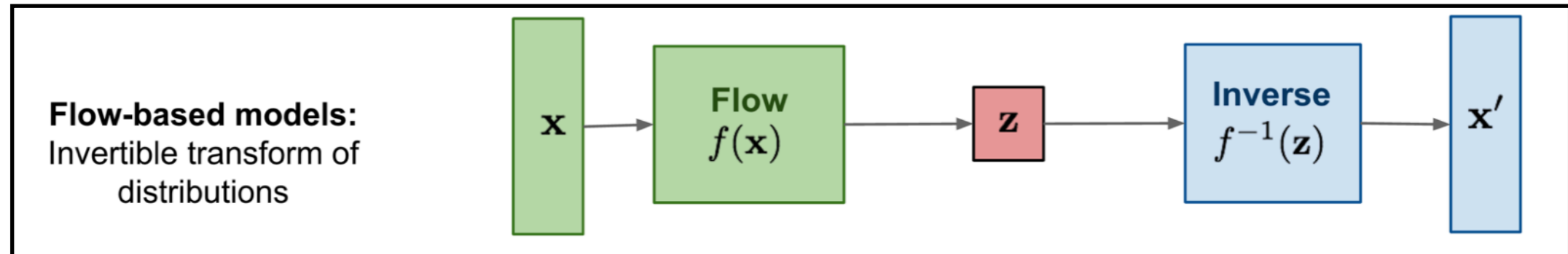


Progress

Extend to condition on angles



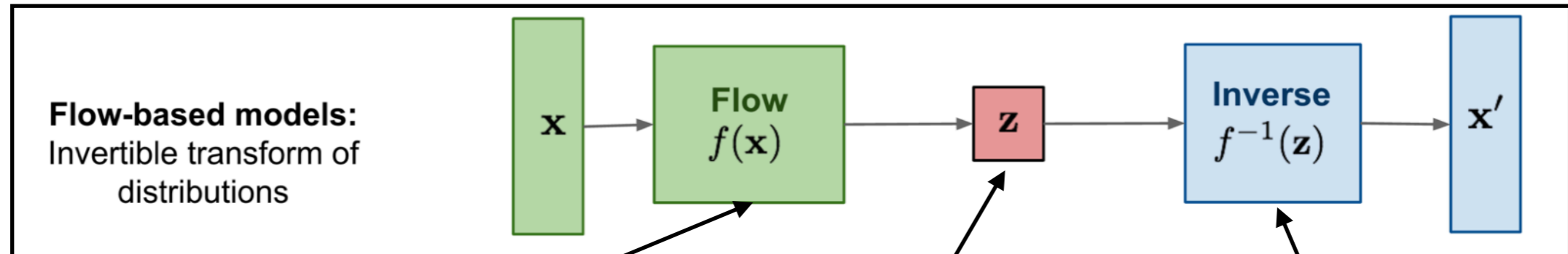
Normalising Flows



In auto-encoders, the decoder learns to ‘undo’ the encoder

Can we make this exact and directly learn the likelihood?

Normalising Flows



Take into account
Jacobian
determinant to
evaluate probability
density

Choose latent
space, e.g. standard
normal distribution
(normalising flow!)
Same dimension as
data!

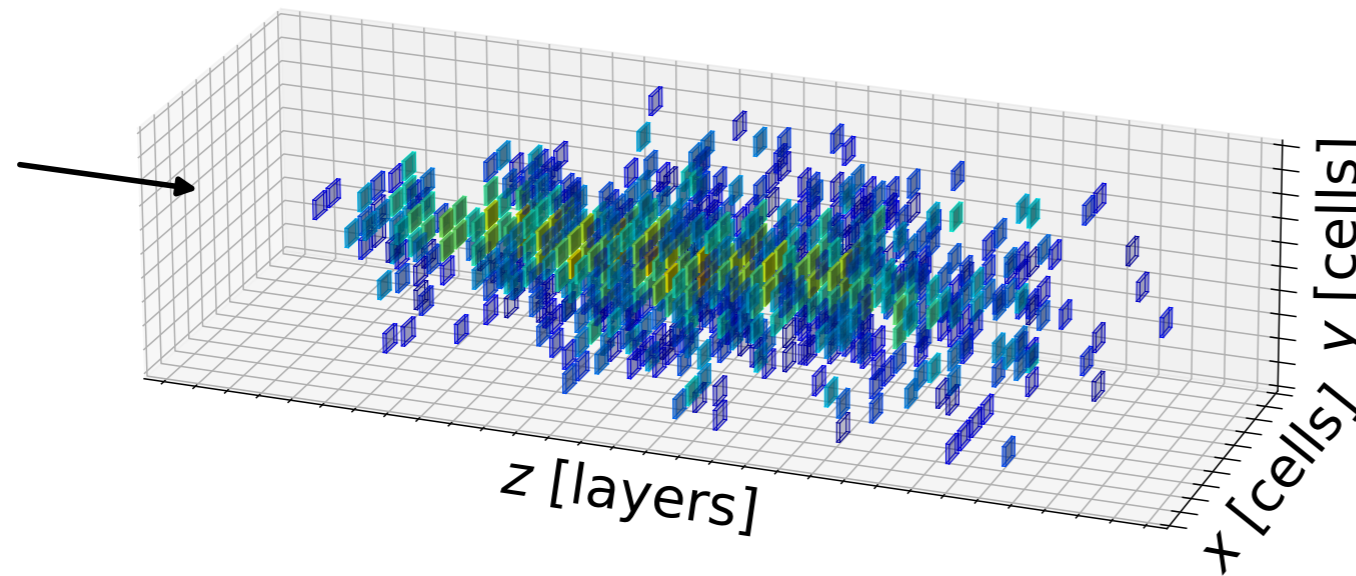
f^{-1} is not a learned
inversion, but exact
inverse by construction

Learn a diffeomorphism between data
and latent-space

Bijjective, invertable

Learn likelihood of data

Flows for detector simulation



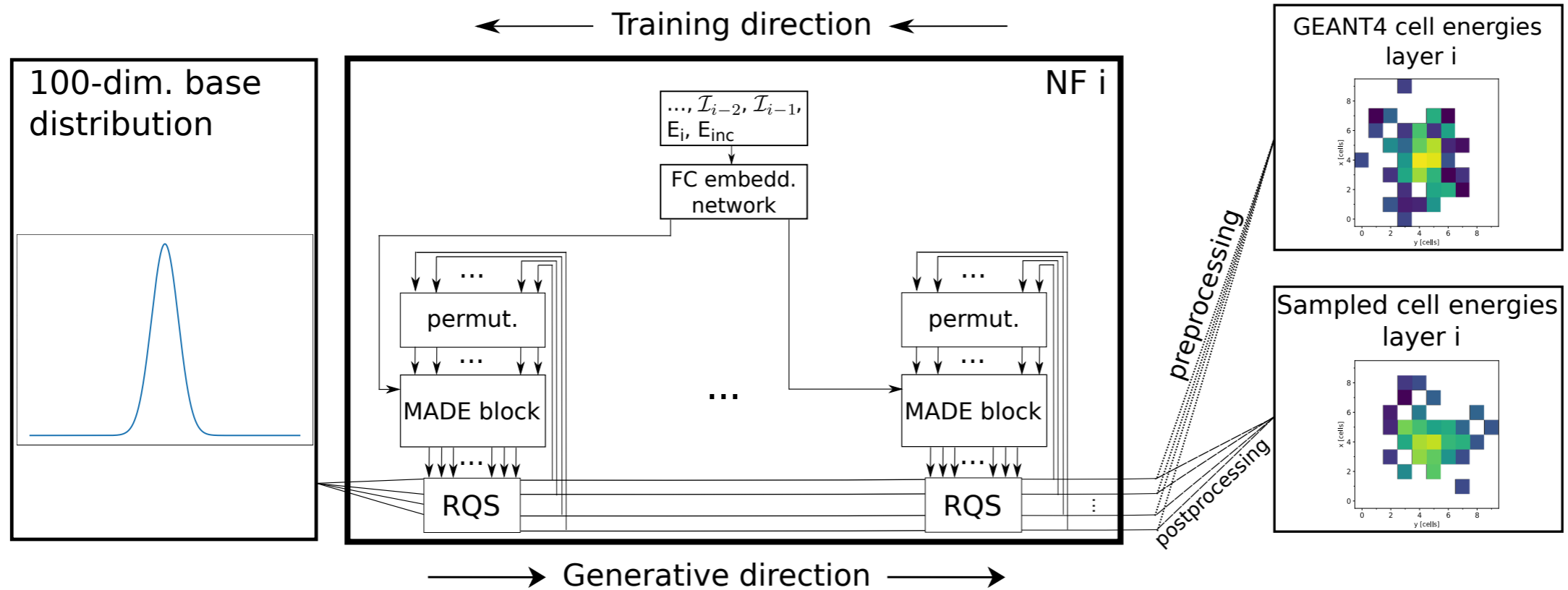
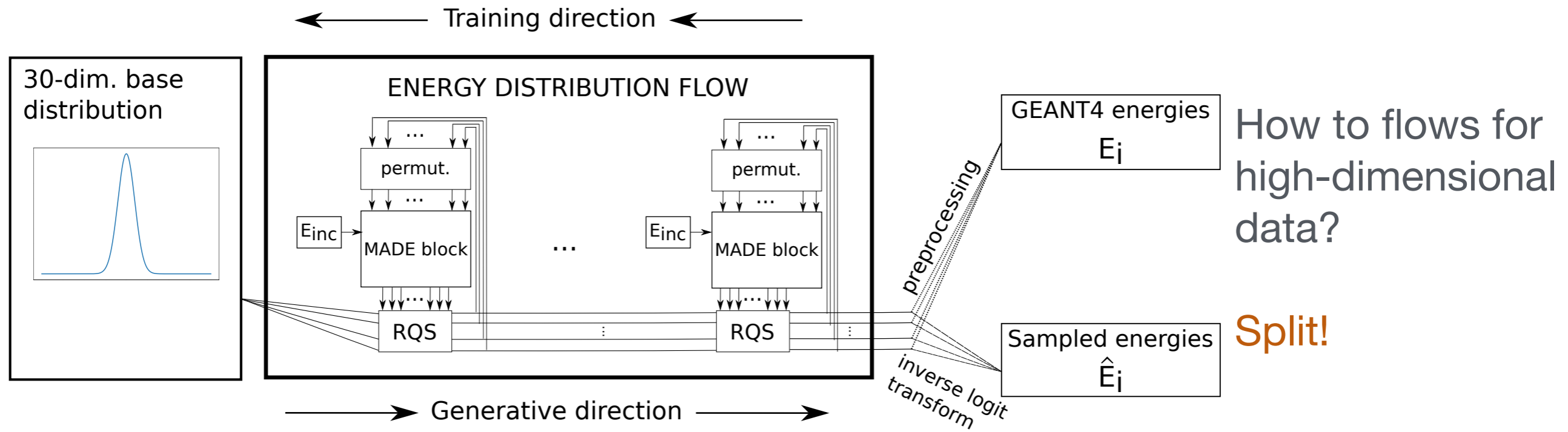
10x10 cells / layer
30 layers

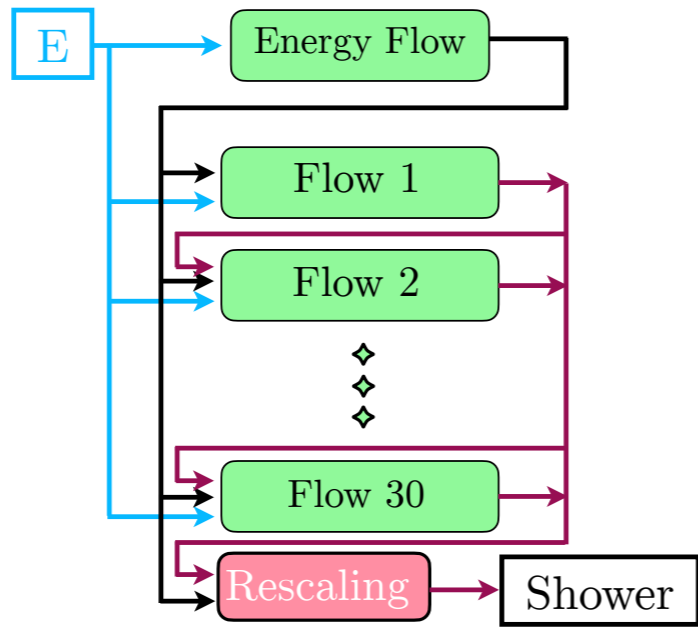
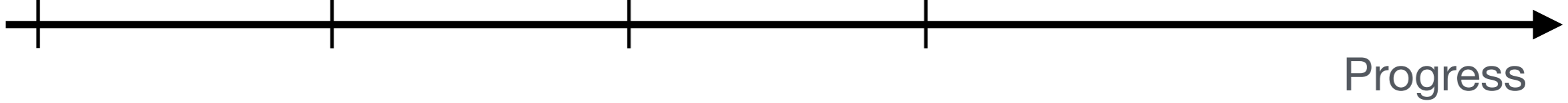
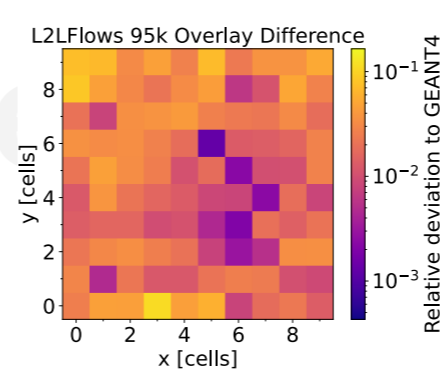
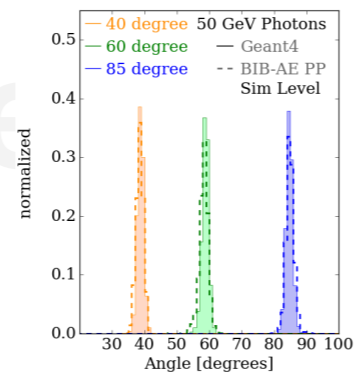
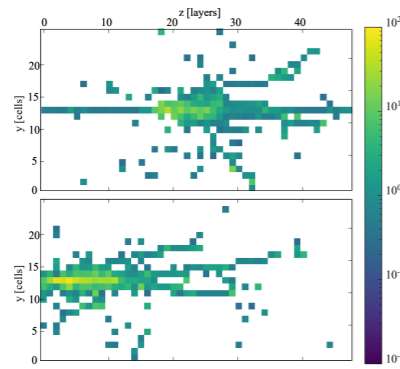
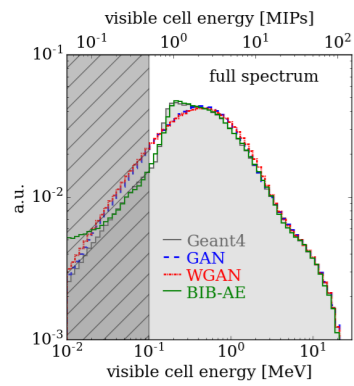
By directly learning the likelihood, flows should be of higher fidelity than GAN/VAE.

But inefficient scaling with data dimension.

How to do **flows for high-dimensional data?**

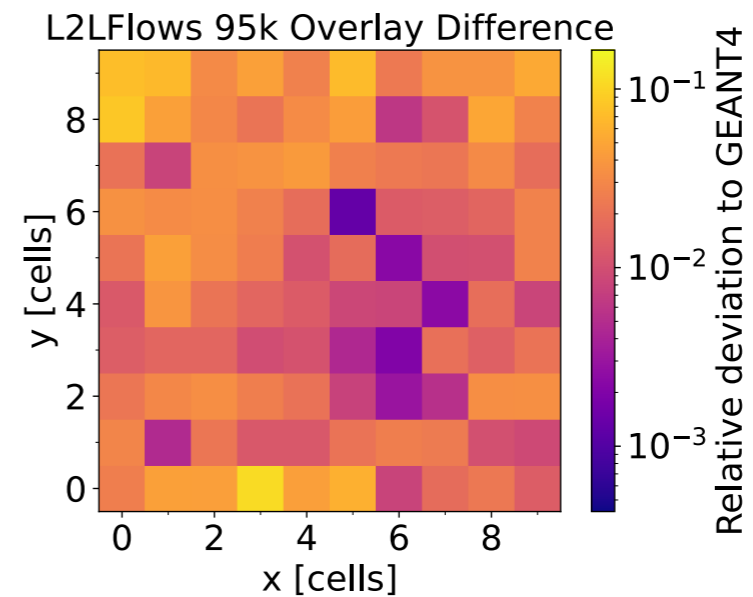
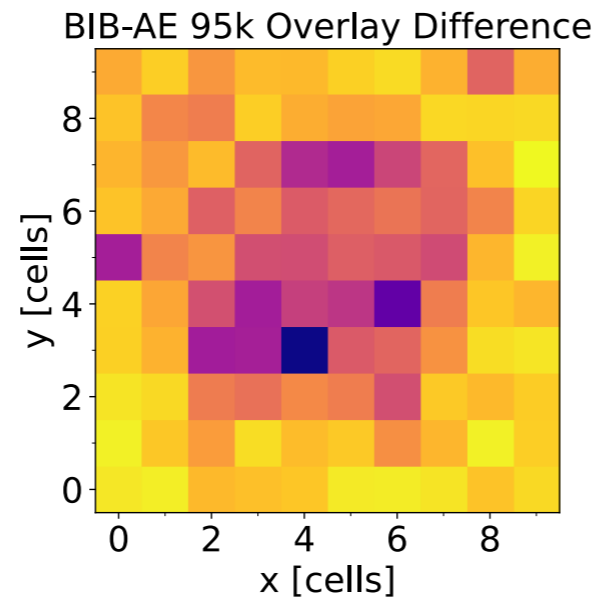
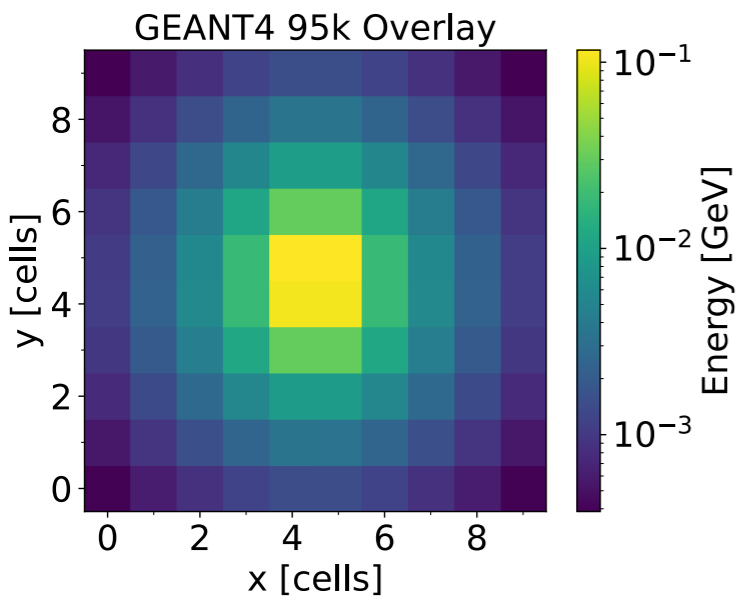
Flows for detector simulation





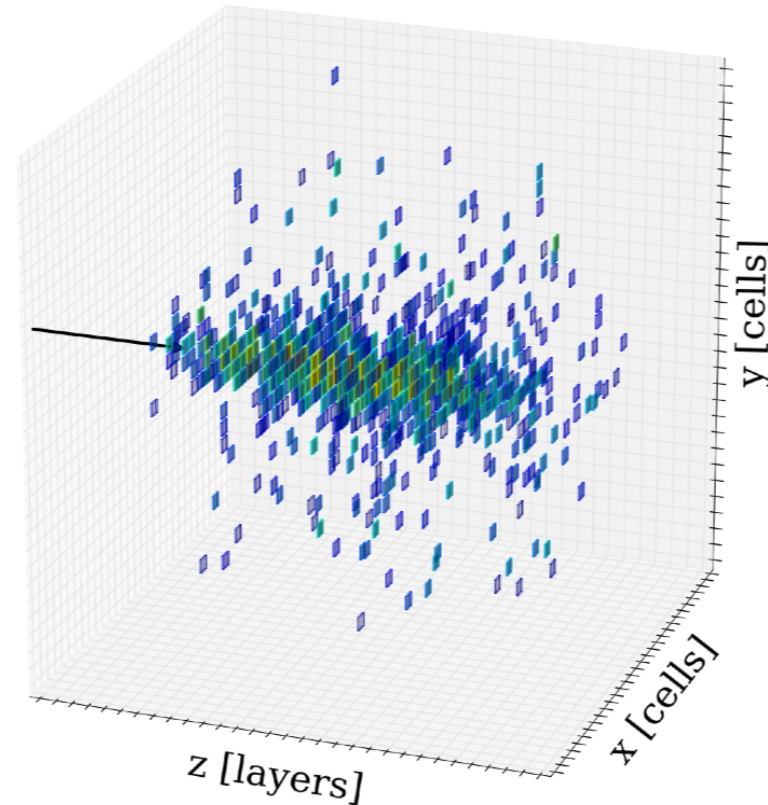
Better convergence of **normalising flows**:
 → better fidelity

Individual flows per layer for efficiency

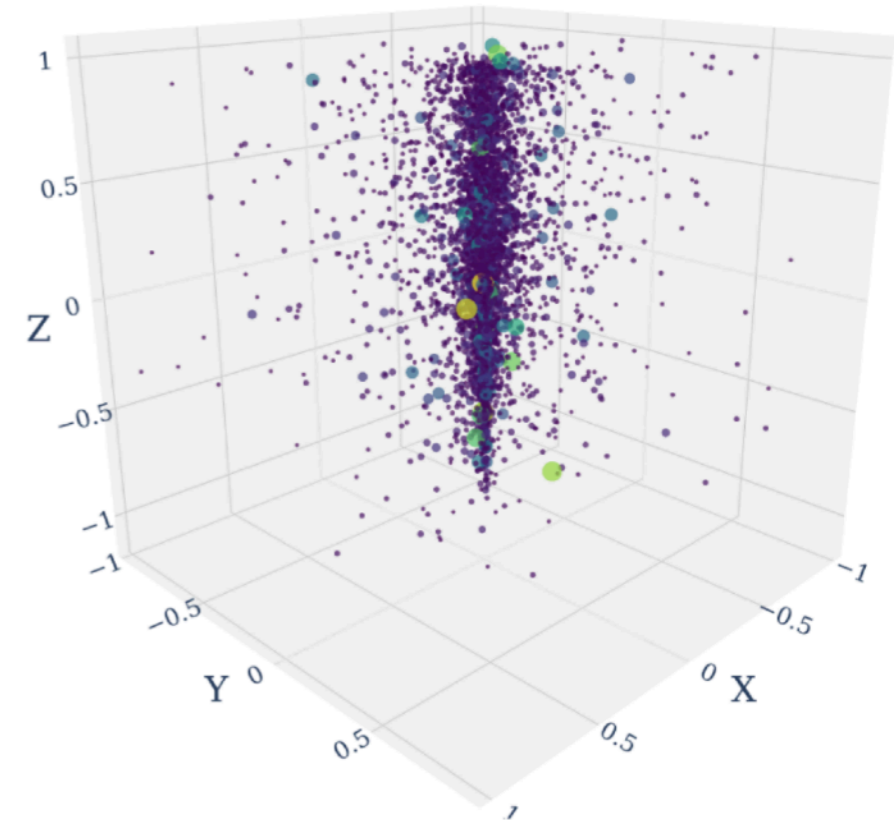


CaloClouds

To improve the generative fidelity, move to a **point cloud** diffusion model



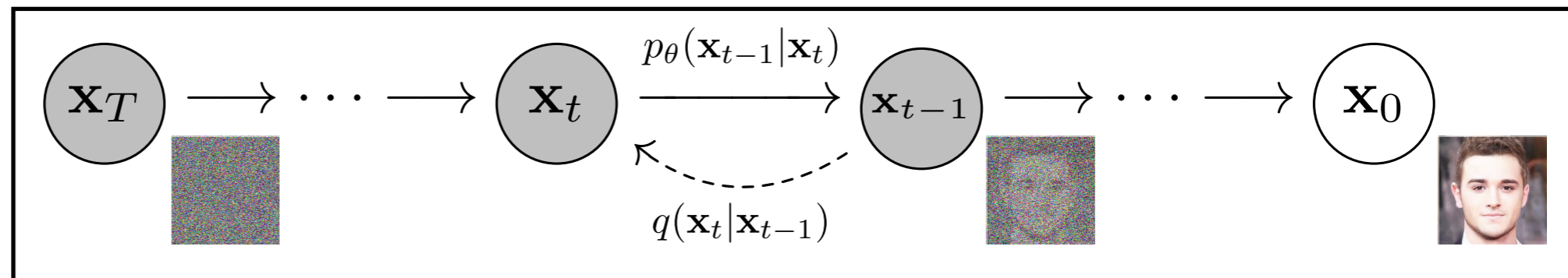
Fixed grid (voxels)
Limiting for high-dimensions (sparse data)



Point cloud:
Only simulate non-zero hits → better scaling

CaloClouds

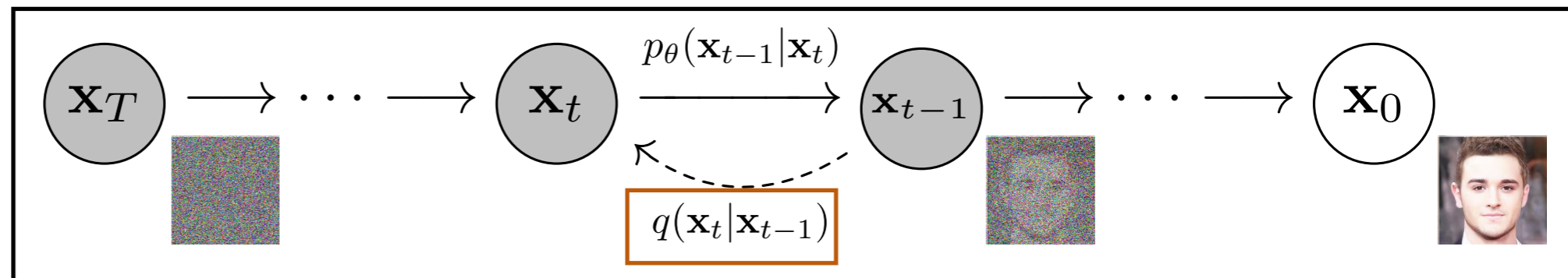
To improve the generative fidelity, move to a point cloud **diffusion model**



Core idea: **Stepwise noising/**
denoising

Diffusion

To improve the generative fidelity, move to a point cloud **diffusion model**



Forward
(Data \rightarrow Noise)

$$q(\mathbf{x}_t|\mathbf{x}_{t-1}) := \mathcal{N}(\mathbf{x}_t; \sqrt{1 - \beta_t}\mathbf{x}_{t-1}, \beta_t\mathbf{I})$$

Individual step

Noise schedule
(hyper-parameter)

$$\mathbf{x}_t(\mathbf{x}_0, \boldsymbol{\epsilon}) = \sqrt{\bar{\alpha}_t}\mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t}\boldsymbol{\epsilon} \text{ for } \boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$$

Rewrite: State at **any time**

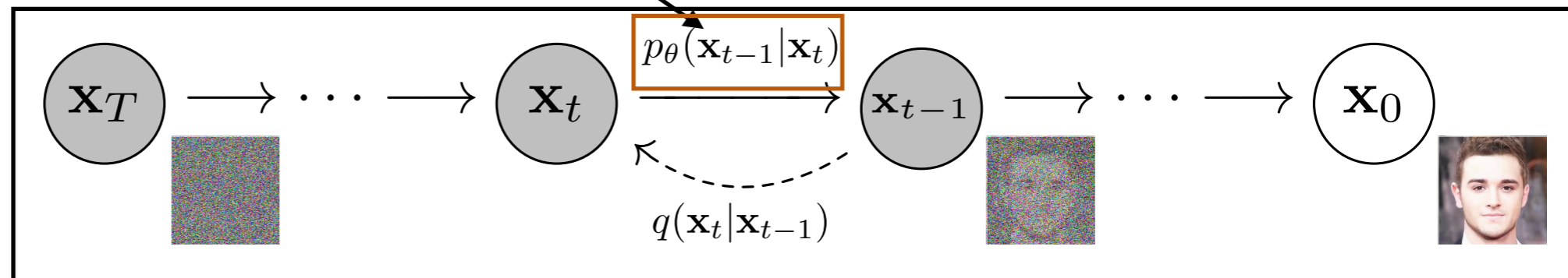
Will try to **predict**

$$\alpha_t := 1 - \beta_t \quad \bar{\alpha}_t := \prod_{s=1}^t \alpha_s$$

Diffusion

To improve the generative fidelity, move to a point cloud **diffusion model**

$$p_{\theta}(\mathbf{x}_{t-1}|\mathbf{x}_t) := \mathcal{N}(\mathbf{x}_{t-1}; \boldsymbol{\mu}_{\theta}(\mathbf{x}_t, t), \boldsymbol{\Sigma}_{\theta}(\mathbf{x}_t, t))$$



Backward
(**Noise** → **Data**)

$$L_{\text{simple}}(\theta) := \mathbb{E}_{t, \mathbf{x}_0, \boldsymbol{\epsilon}} \left[\left\| \boldsymbol{\epsilon} - \boldsymbol{\epsilon}_{\theta}(\sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \boldsymbol{\epsilon}, t) \right\|^2 \right]$$

Noisy image

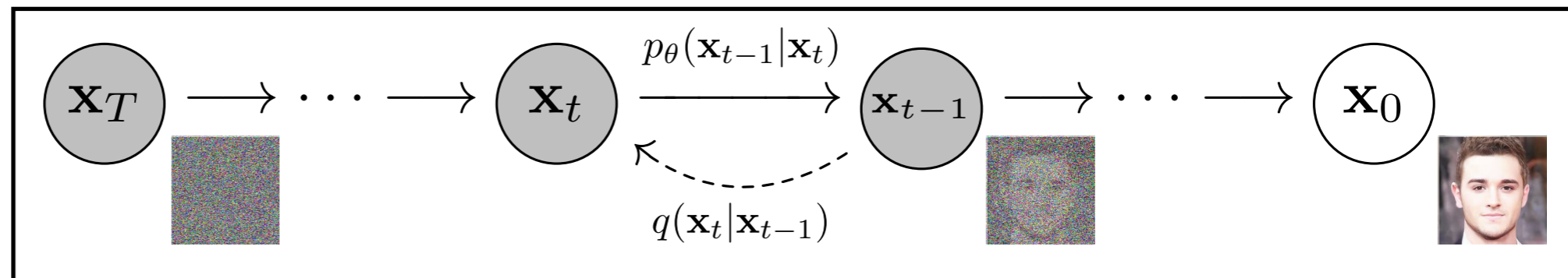
Reminder: Forward
diffusion to time t

$$\mathbf{x}_t(\mathbf{x}_0, \boldsymbol{\epsilon}) = \sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \boldsymbol{\epsilon}$$

Timestep

Diffusion

To improve the generative fidelity, move to a point cloud **diffusion model**



Algorithm 1 Training

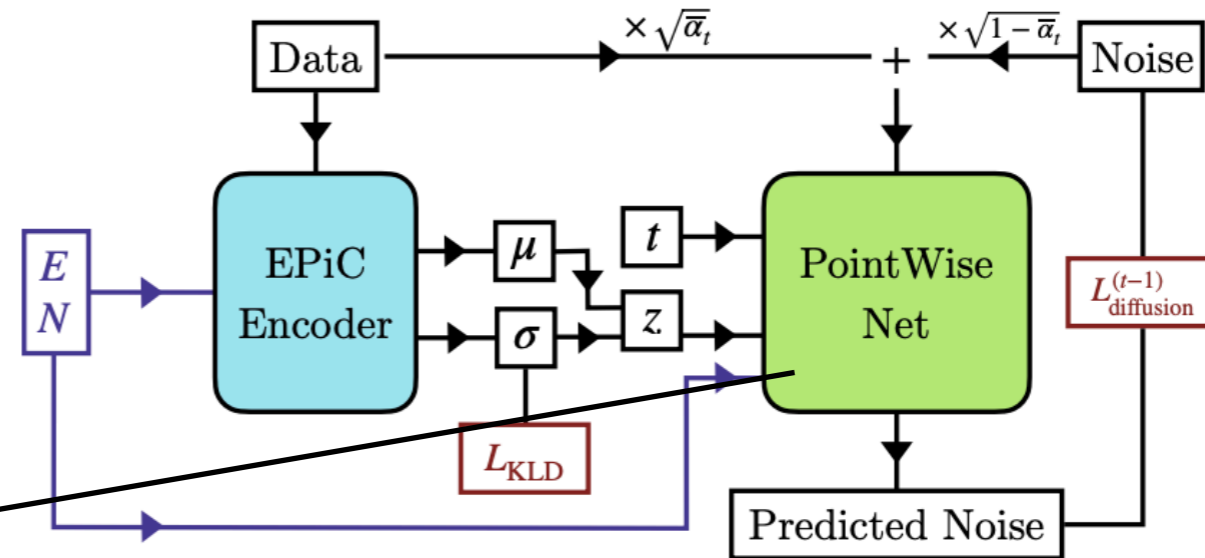
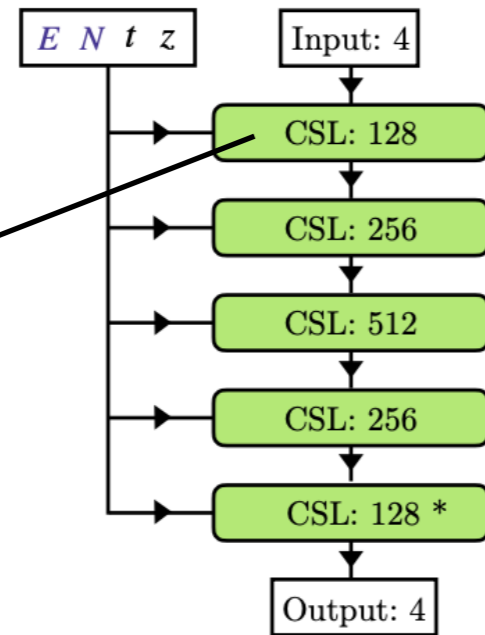
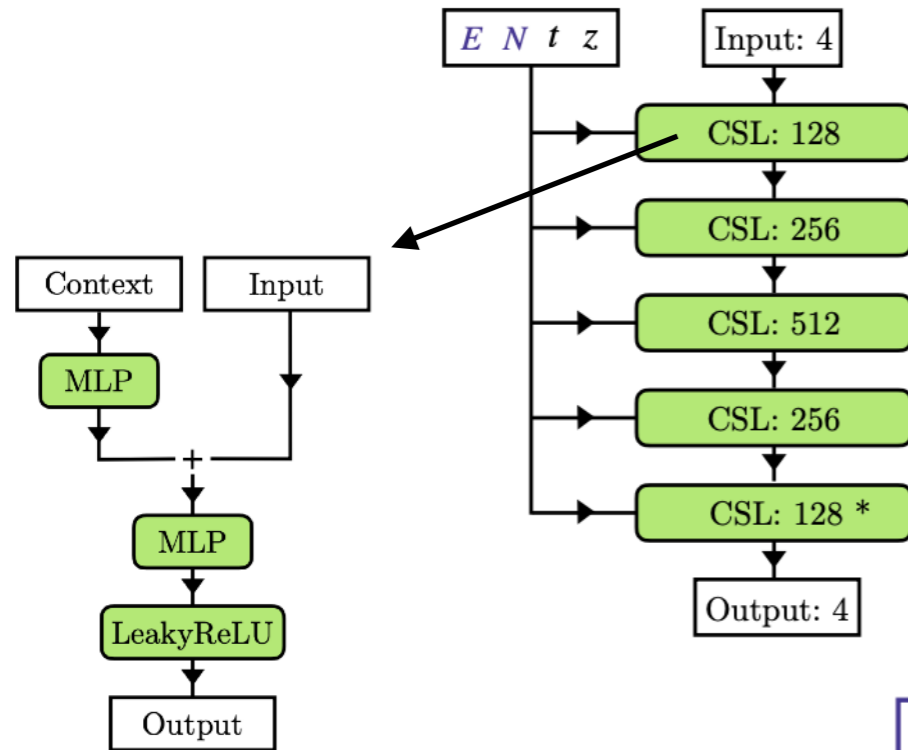
- 1: **repeat**
 - 2: $\mathbf{x}_0 \sim q(\mathbf{x}_0)$
 - 3: $t \sim \text{Uniform}(\{1, \dots, T\})$
 - 4: $\boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
 - 5: Take gradient descent step on
$$\nabla_{\theta} \|\boldsymbol{\epsilon} - \boldsymbol{\epsilon}_{\theta}(\sqrt{\bar{\alpha}_t}\mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t}\boldsymbol{\epsilon}, t)\|^2$$
 - 6: **until** converged
-

Algorithm 2 Sampling

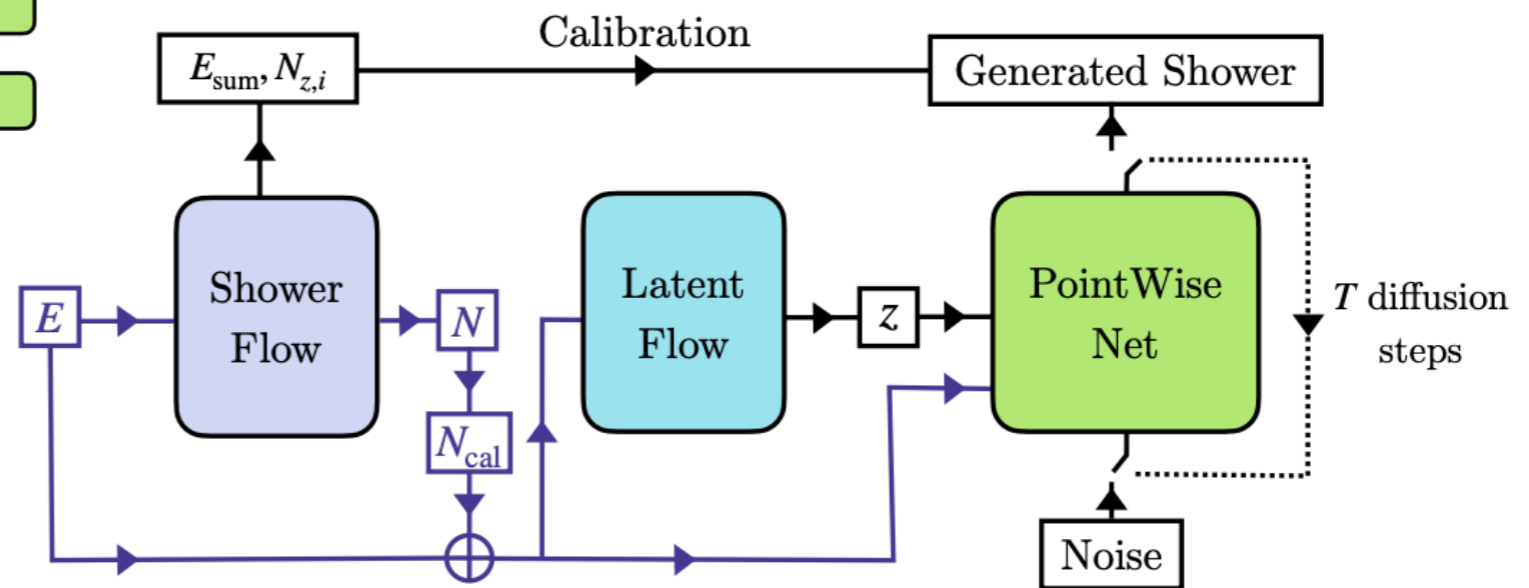
- 1: $\mathbf{x}_T \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
 - 2: **for** $t = T, \dots, 1$ **do**
 - 3: $\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$ if $t > 1$, else $\mathbf{z} = \mathbf{0}$
 - 4: $\mathbf{x}_{t-1} = \frac{1}{\sqrt{\alpha_t}} \left(\mathbf{x}_t - \frac{1 - \alpha_t}{\sqrt{1 - \bar{\alpha}_t}} \boldsymbol{\epsilon}_{\theta}(\mathbf{x}_t, t) \right) + \sigma_t \mathbf{z}$
 - 5: **end for**
 - 6: **return** \mathbf{x}_0
-

CaloClouds

To improve the generative fidelity, move to a point cloud diffusion model



(a) Training at random time step t

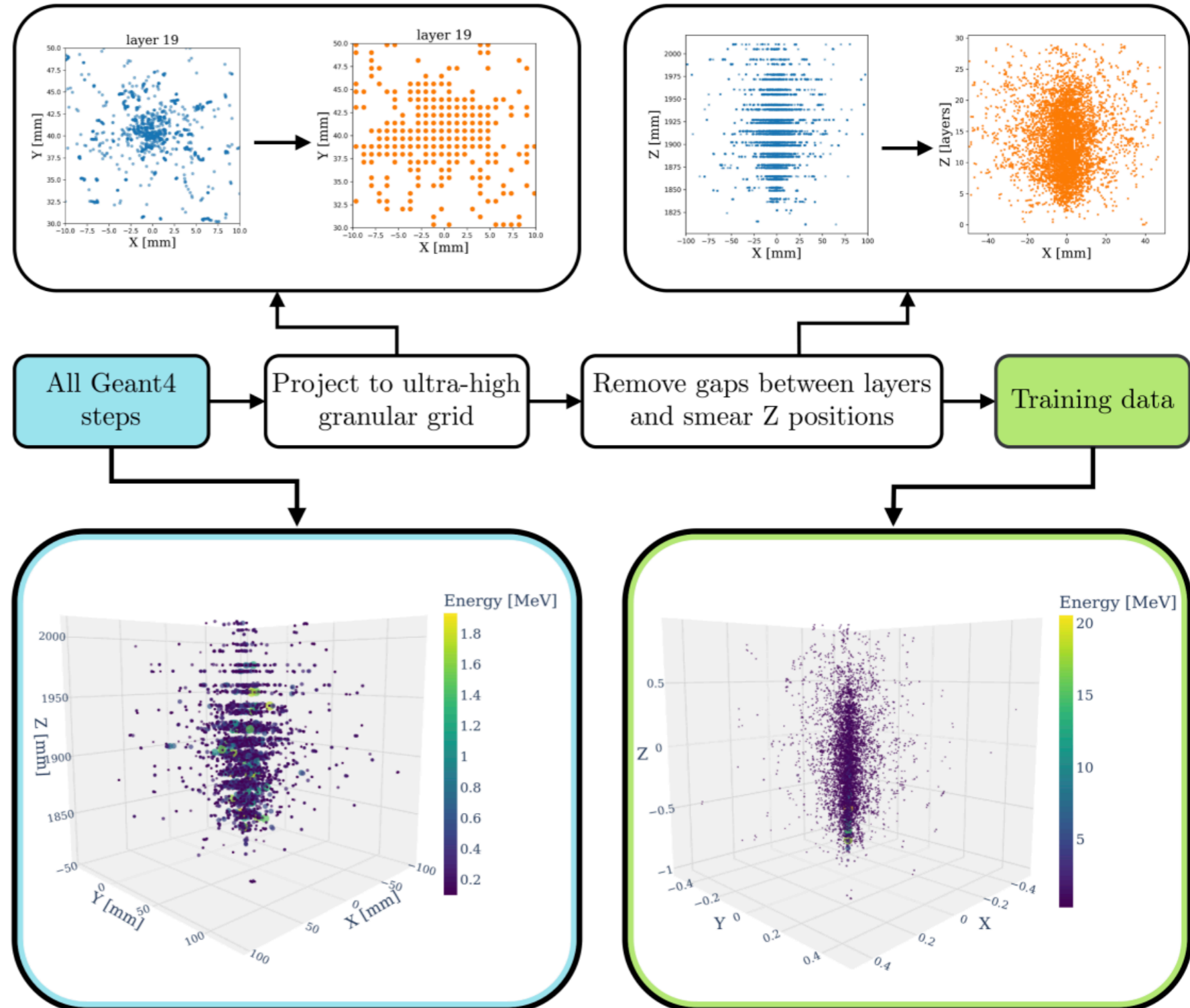


(b) Sampling with reverse diffusion through all time steps T

CaloClouds

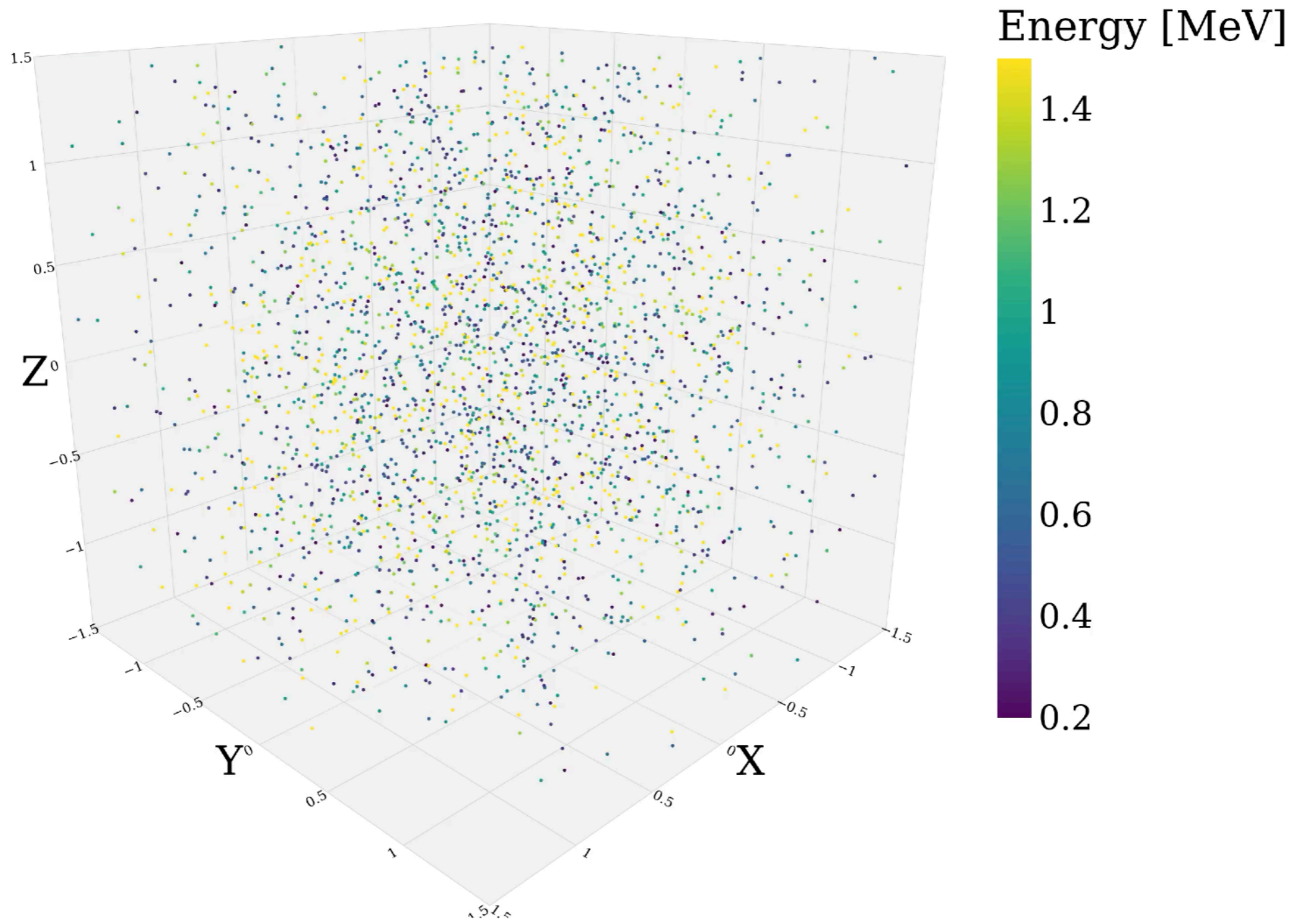
To improve the generative fidelity, move to a point cloud diffusion model

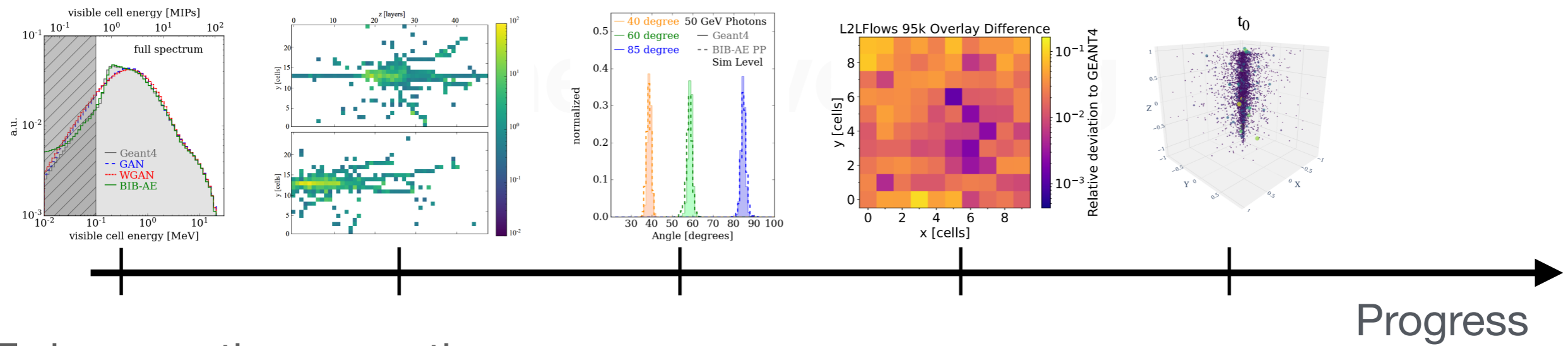
Some **input processing** needed



CaloClouds

CaloCloud, time stamp: t_{99}

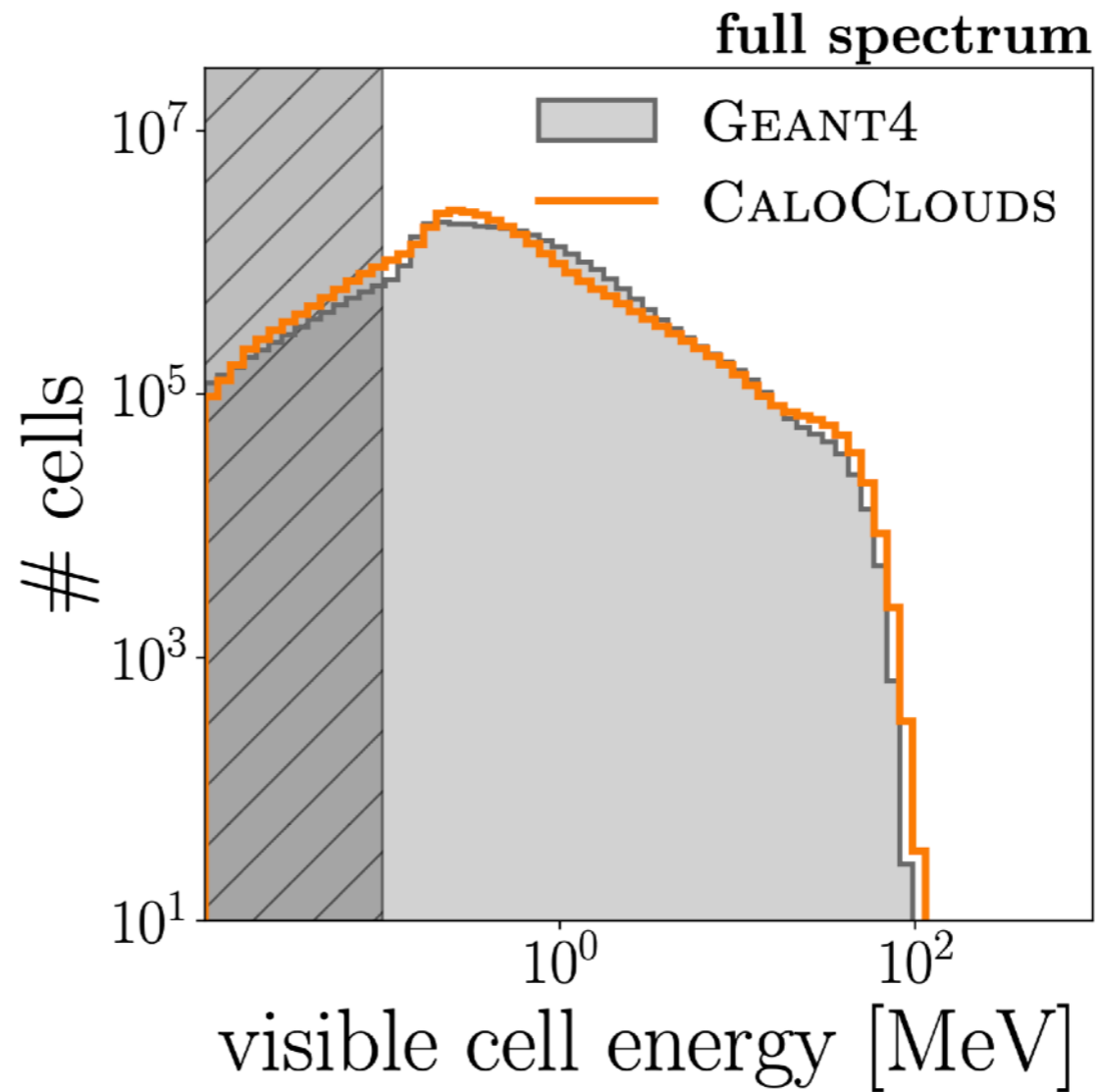




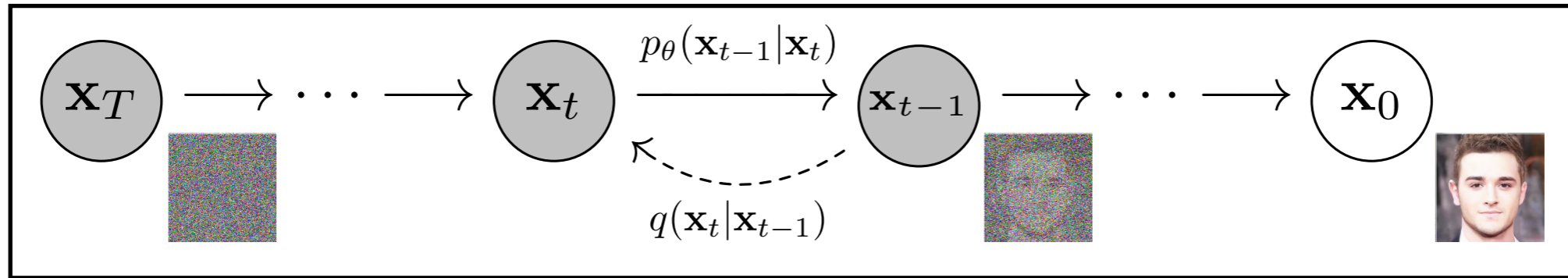
To improve the generative fidelity, move to a point cloud diffusion model

Close in accuracy to fixed grid.
Fairly slow.

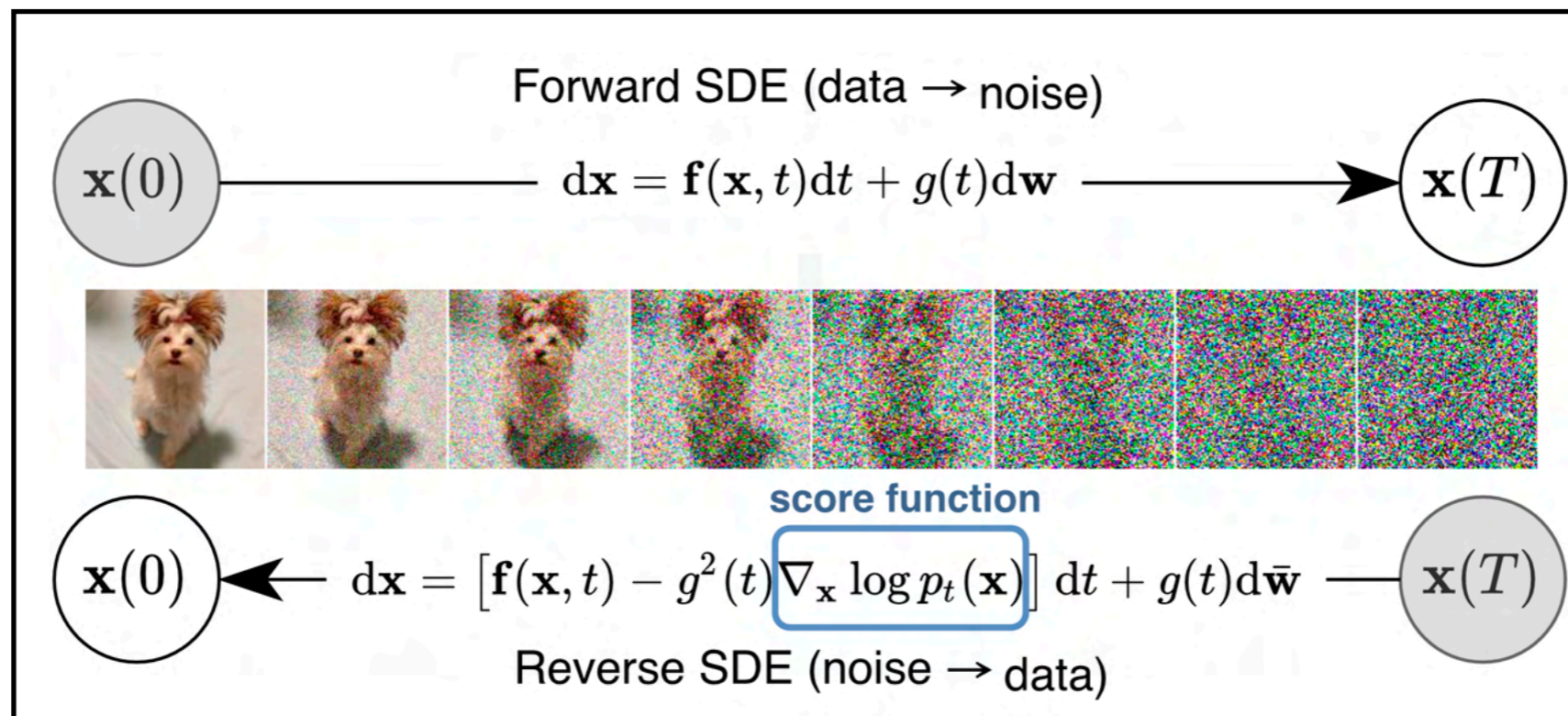
Can we improve further?



CaloClouds II



Replace **discrete** noise steps



with **stochastic differential equations** (SDEs)

CaloClouds II

$$L_{\text{simple}}(\theta) := \mathbb{E}_{t, \mathbf{x}_0, \epsilon} \left[\left\| \epsilon - \epsilon_{\theta}(\sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \epsilon, t) \right\|^2 \right]$$

Replace learning **added noise**



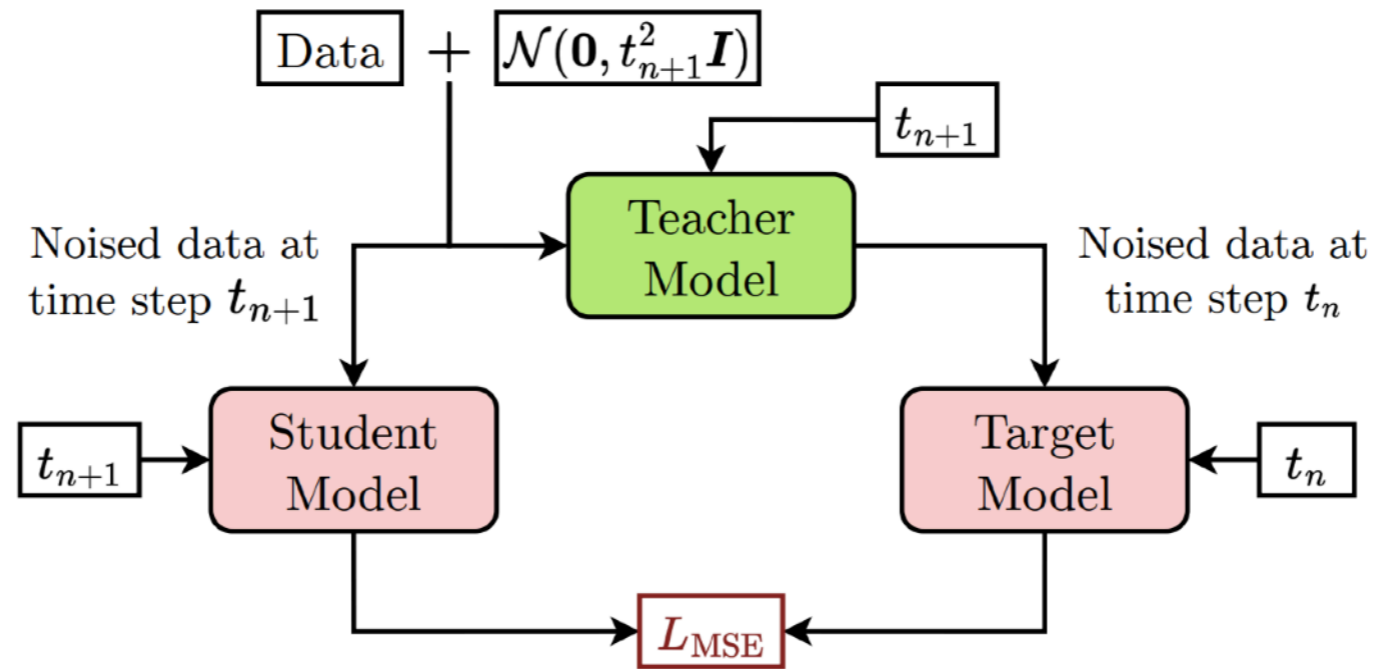
$$\theta^* = \arg \min_{\theta} \mathbb{E}_t \left\{ \lambda(t) \mathbb{E}_{\mathbf{x}(0)} \mathbb{E}_{\mathbf{x}(t) | \mathbf{x}(0)} \left[\left\| \mathbf{s}_{\theta}(\mathbf{x}(t), t) - \nabla_{\mathbf{x}(t)} \log p_{0t}(\mathbf{x}(t) | \mathbf{x}(0)) \right\|_2^2 \right] \right\}$$

with learning a **score function** with conditional probability paths

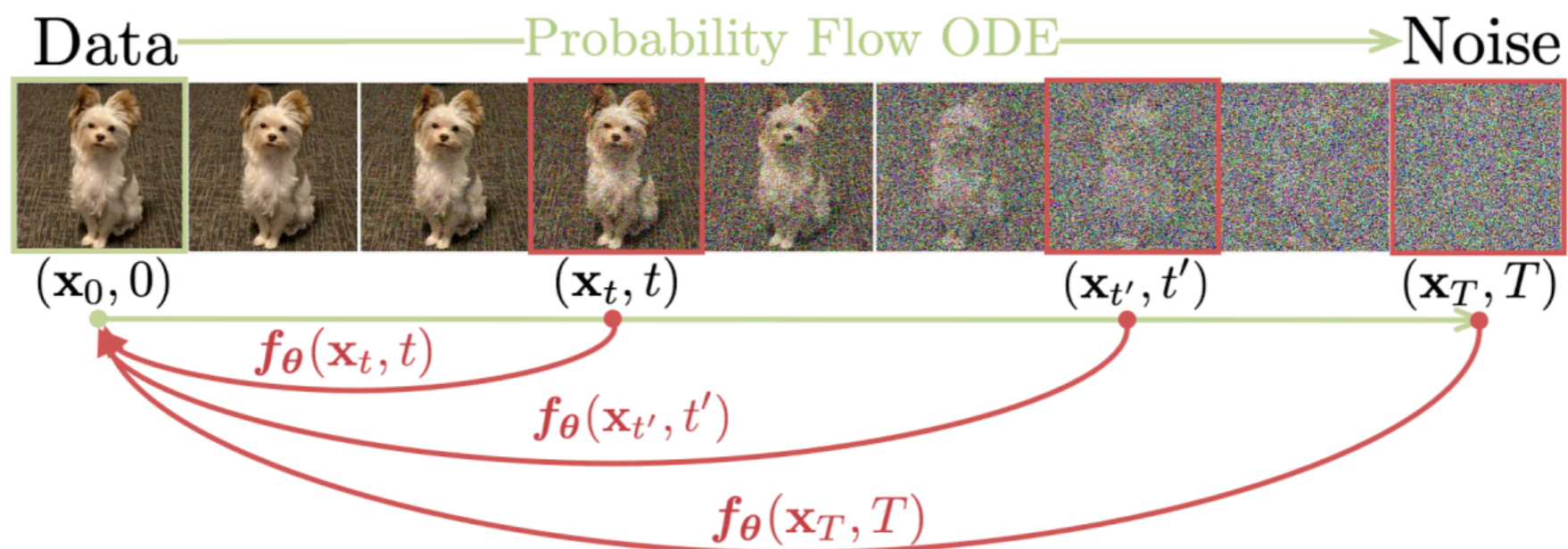
$$d\mathbf{x} = [\mathbf{f}(\mathbf{x}, t) - g(t)^2 \nabla_{\mathbf{x}} \log p_t(\mathbf{x})] dt + g(t) d\bar{\mathbf{w}}$$

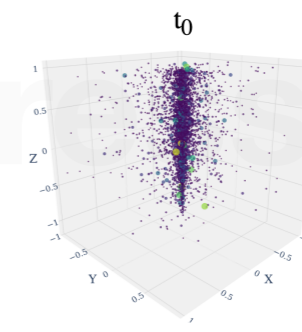
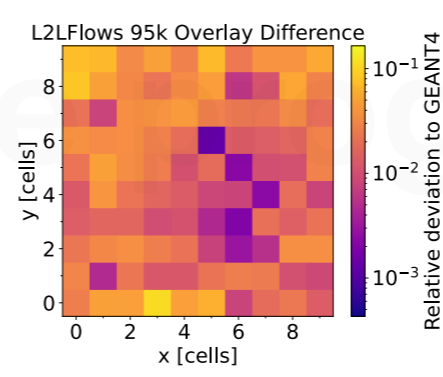
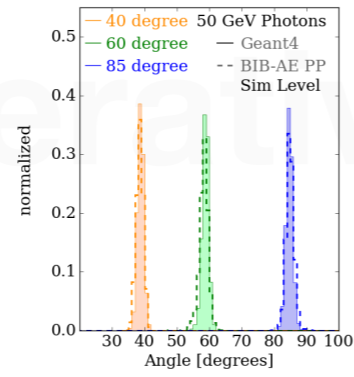
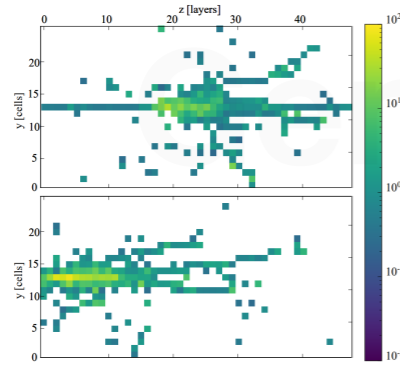
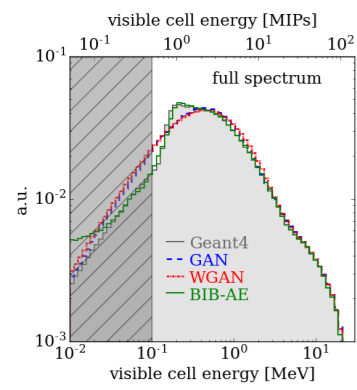
and numerically solve SDE to transport to data space

Consistency Distillation

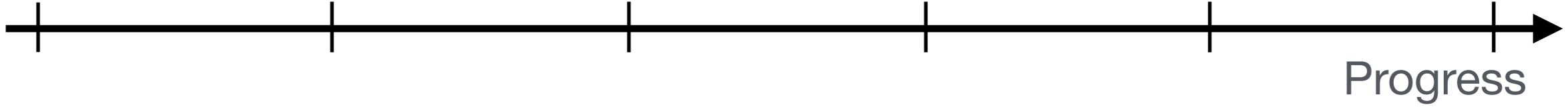


Speed up by training a model to allow single step generation



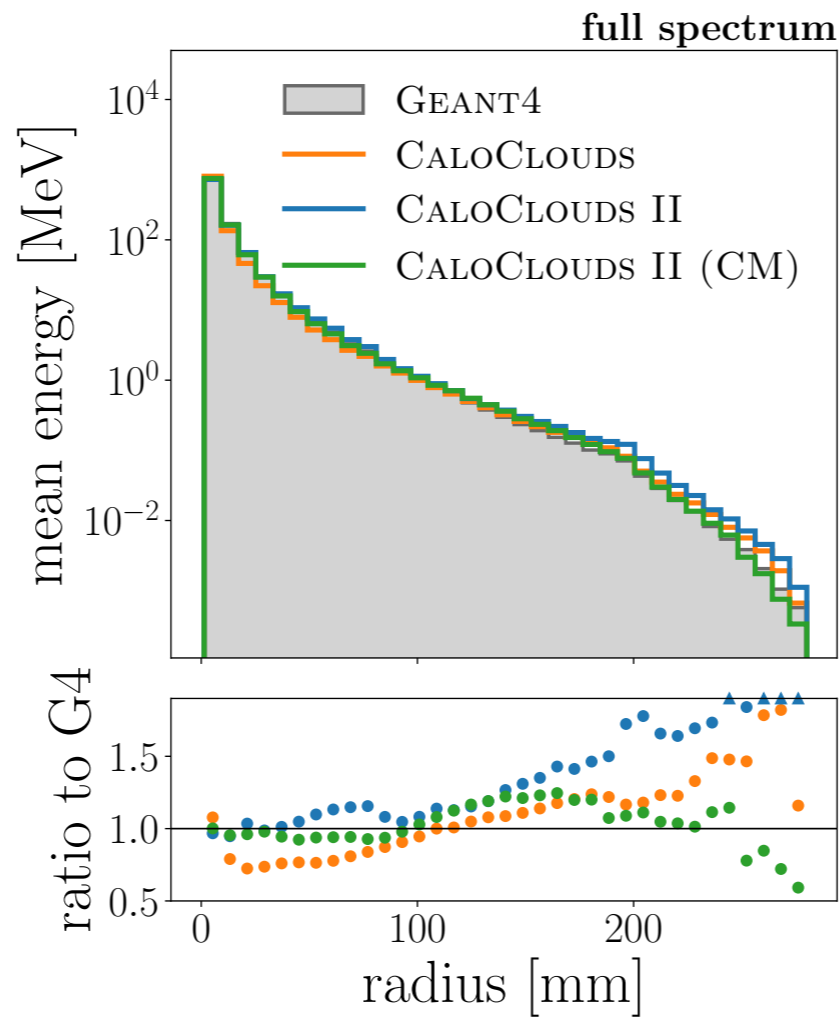
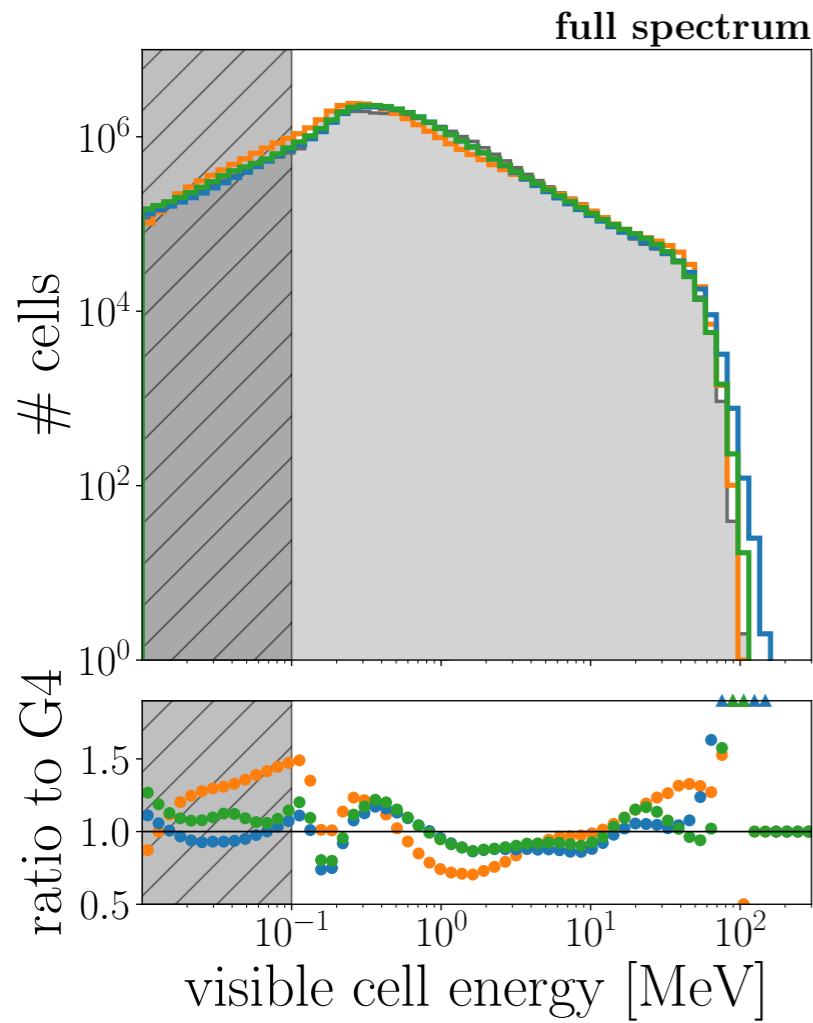
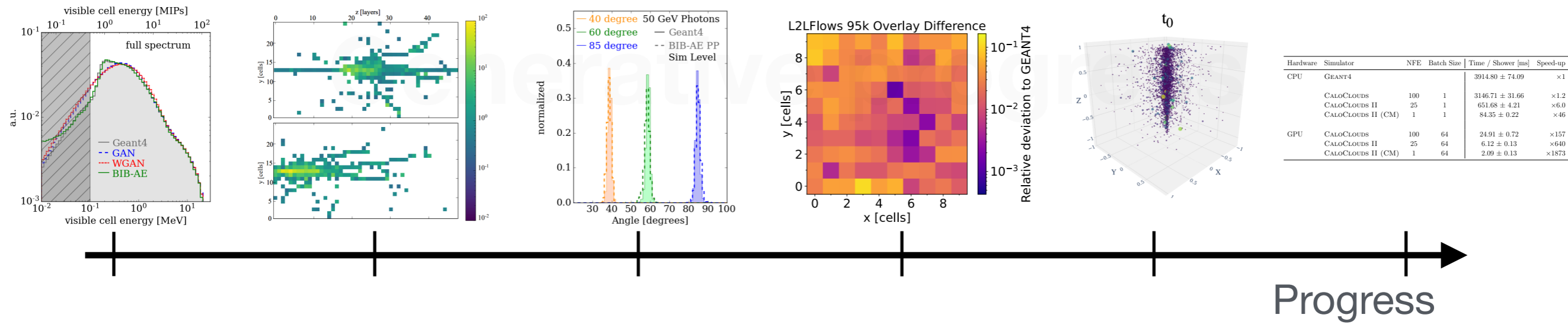


Hardware	Simulator	NFE	Batch Size	Time / Shower [ms]	Speed-up
CPU	GEANT4			3914.80 ± 74.09	×1
	CALOCLOUDS	100	1	3146.71 ± 31.66	×1.2
	CALOCLOUDS II	25	1	651.68 ± 4.21	×6.0
	CALOCLOUDS II (CM)	1	1	84.35 ± 0.22	×46
GPU	CALOCLOUDS	100	64	24.91 ± 0.72	×157
	CALOCLOUDS II	25	64	6.12 ± 0.13	×640
	CALOCLOUDS II (CM)	1	64	2.09 ± 0.13	×1873



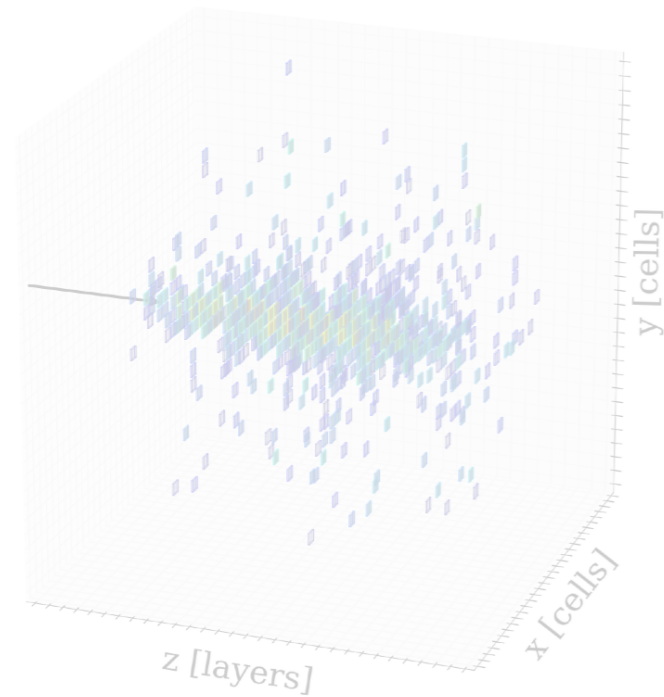
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Use continuous time diffusion and **consistency distillation:** Better quality and faster

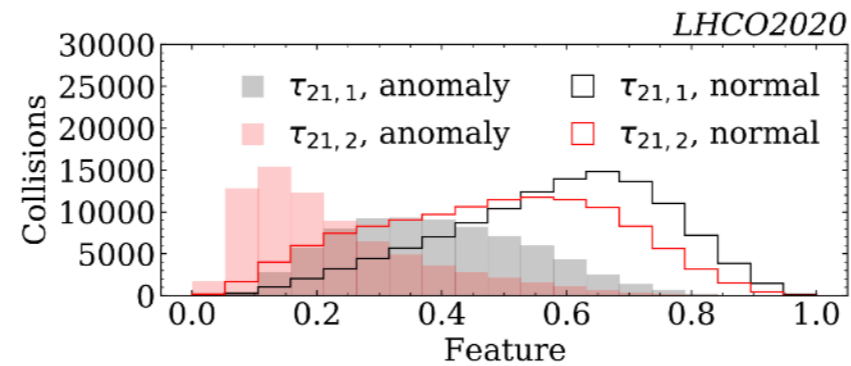


Use continuous time diffusion and **consistency distillation**: Better quality and faster

Why generative models?



Showers in complex high-resolution calorimeters



High-level jet features
for background estimation

$$p(x)$$

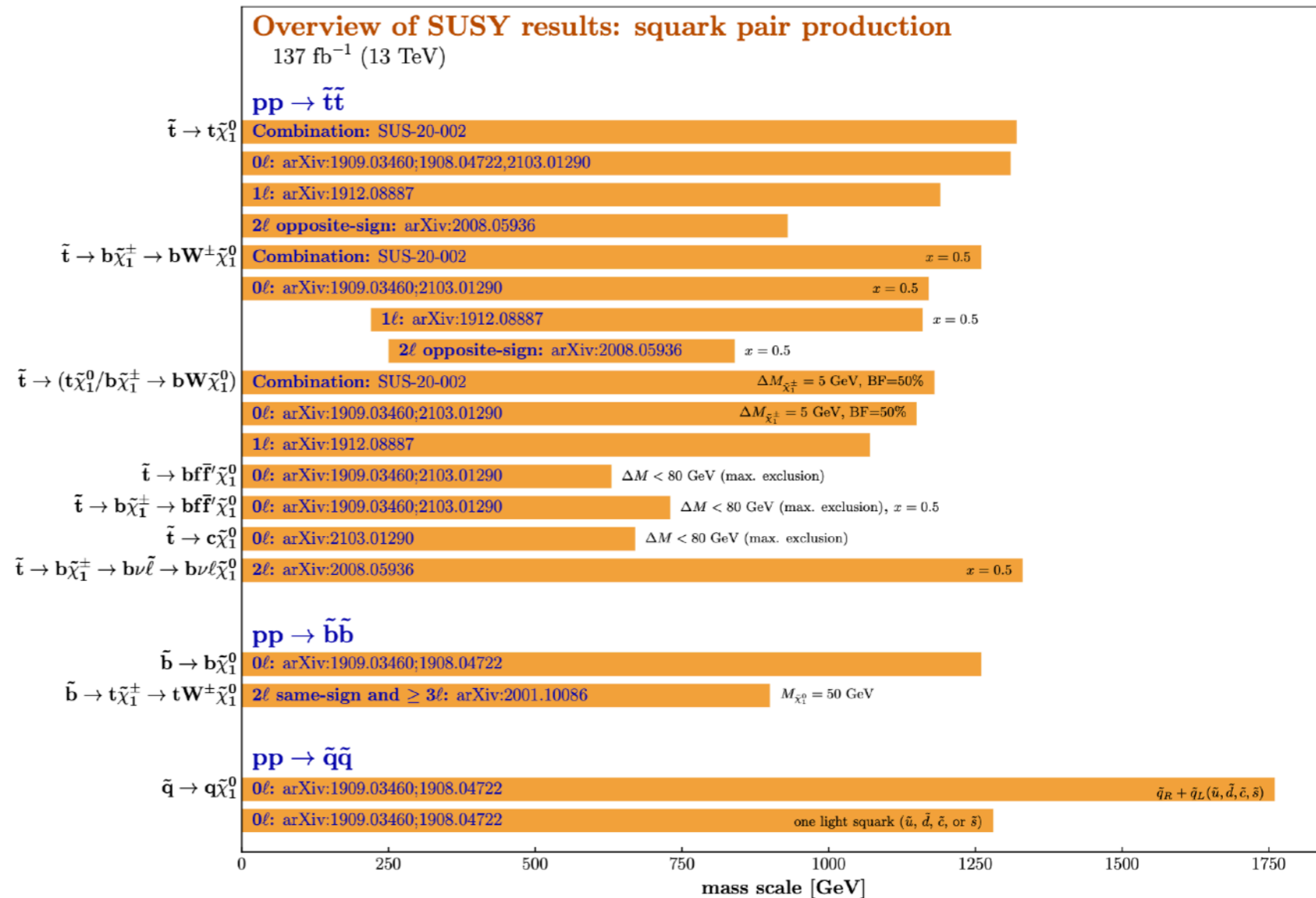
Sample $X_i \sim p(x)$
to generate datapoints

Anomaly detections

- Expect physics beyond the Standard Model
- Only negative results in searches
- Two discovery strategies:
 - Model-specific
 - Model independent

CMS (preliminary)

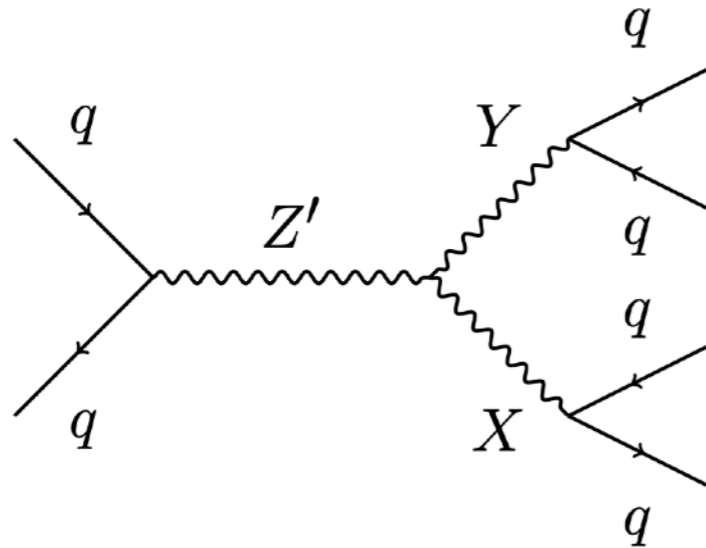
Moriond 2021



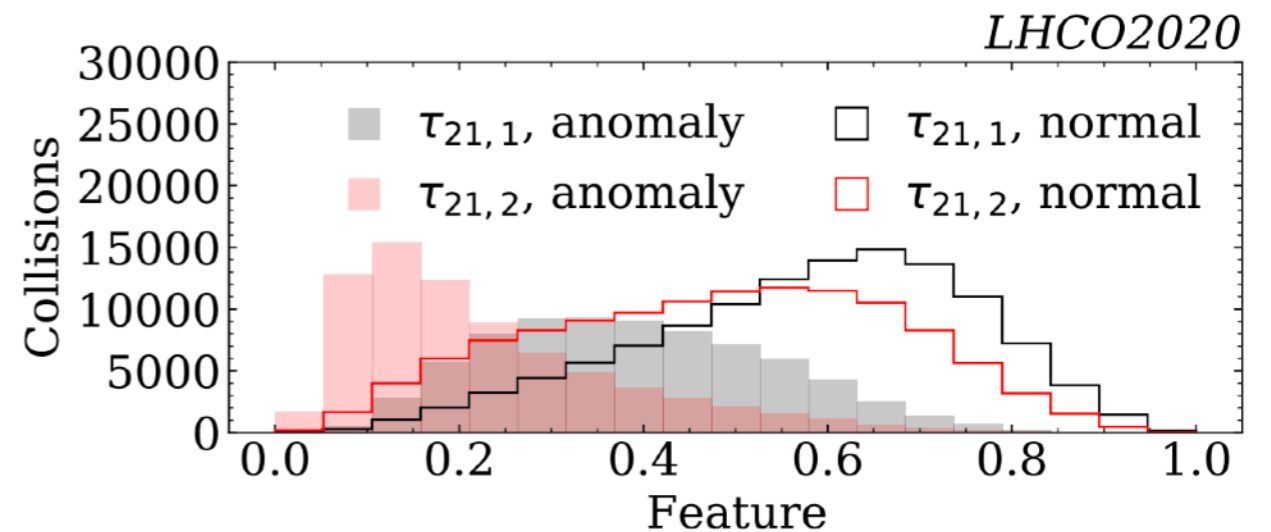
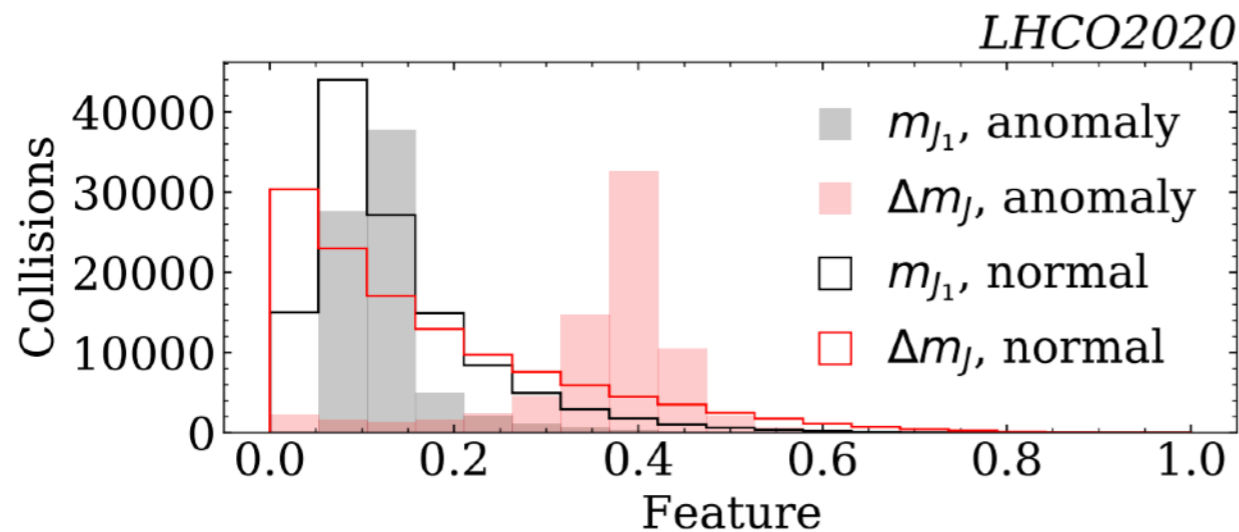
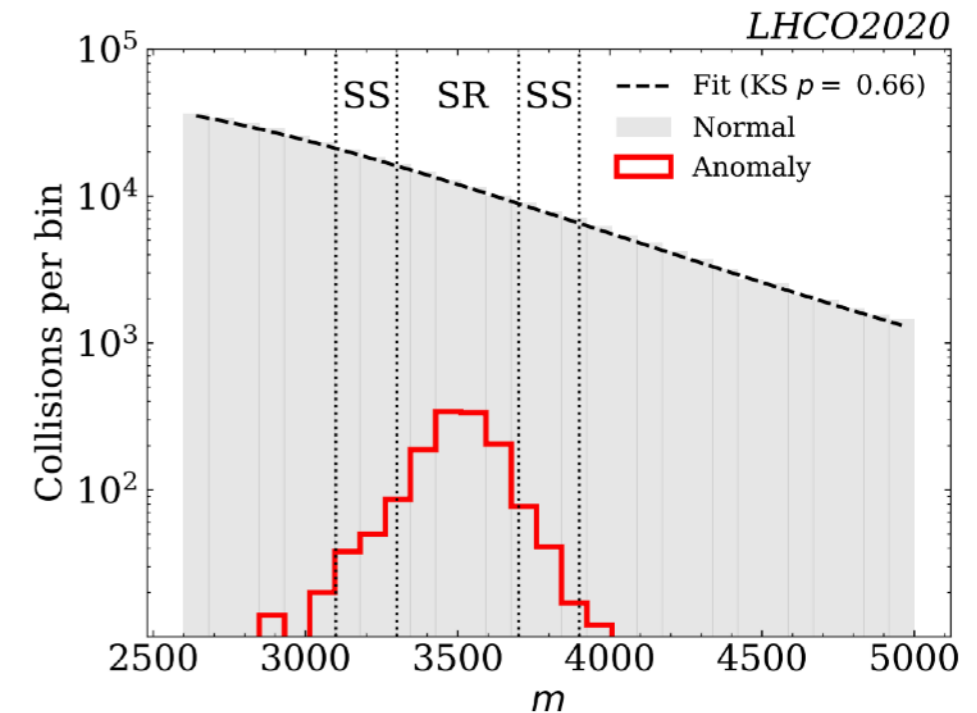
Selection of observed limits at 95% C.L. (theory uncertainties are not included). Probe up to the quoted mass limit for light LSPs unless stated otherwise. The quantities ΔM and x represent the absolute mass difference between the primary sparticle and the LSP, and the difference between the intermediate sparticle and the LSP relative to ΔM , respectively, unless indicated otherwise.

Dataset

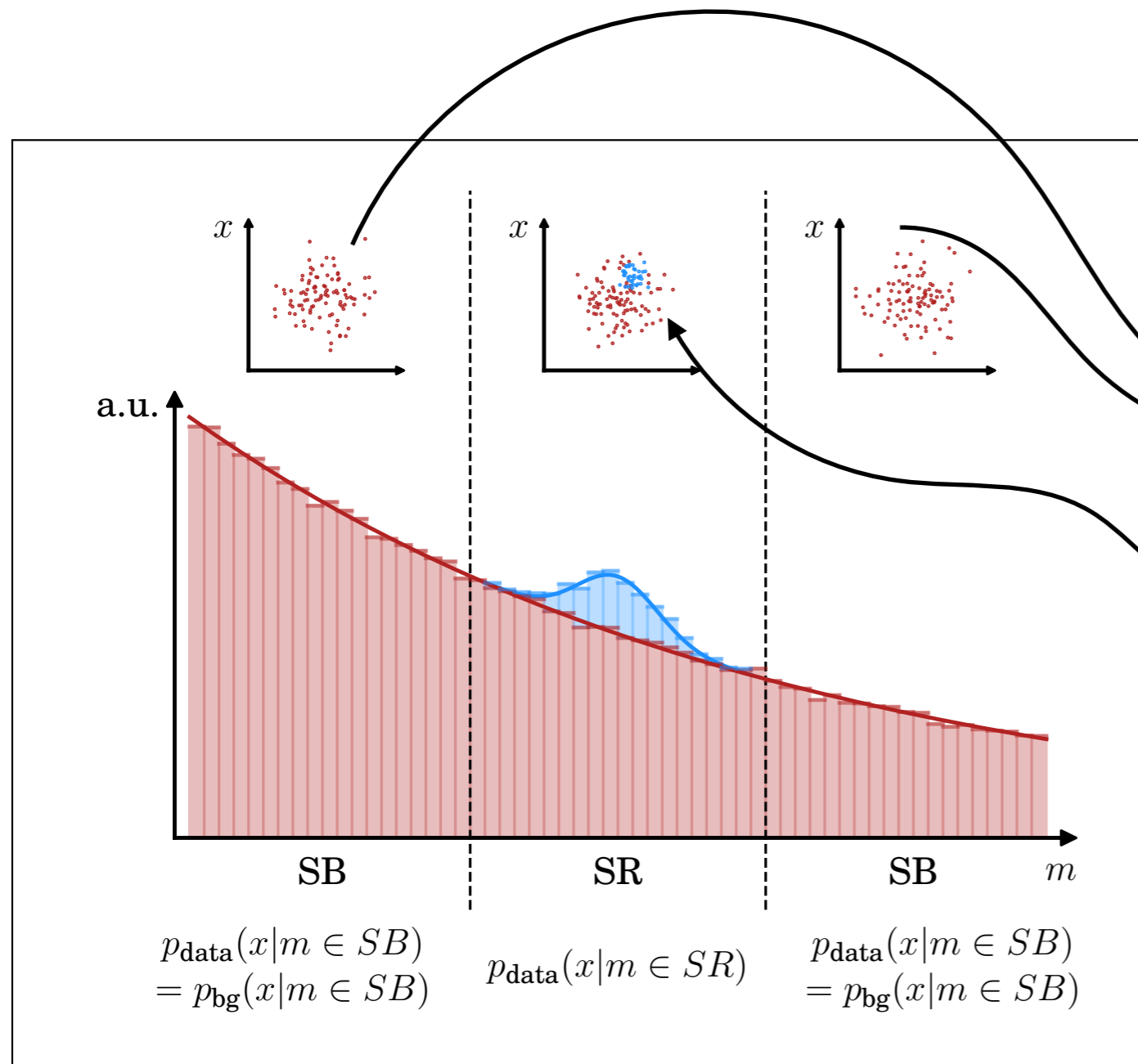
- **LHC Olympics (LHCO):** Community dataset for anomaly detection development
- Z' signal, QCD di-jet backgrounds



$m(Z') = 3500 \text{ GeV}$
 $m(X) = 500 \text{ GeV}$
 $m(Y) = 100 \text{ GeV}$
 (R&D dataset)

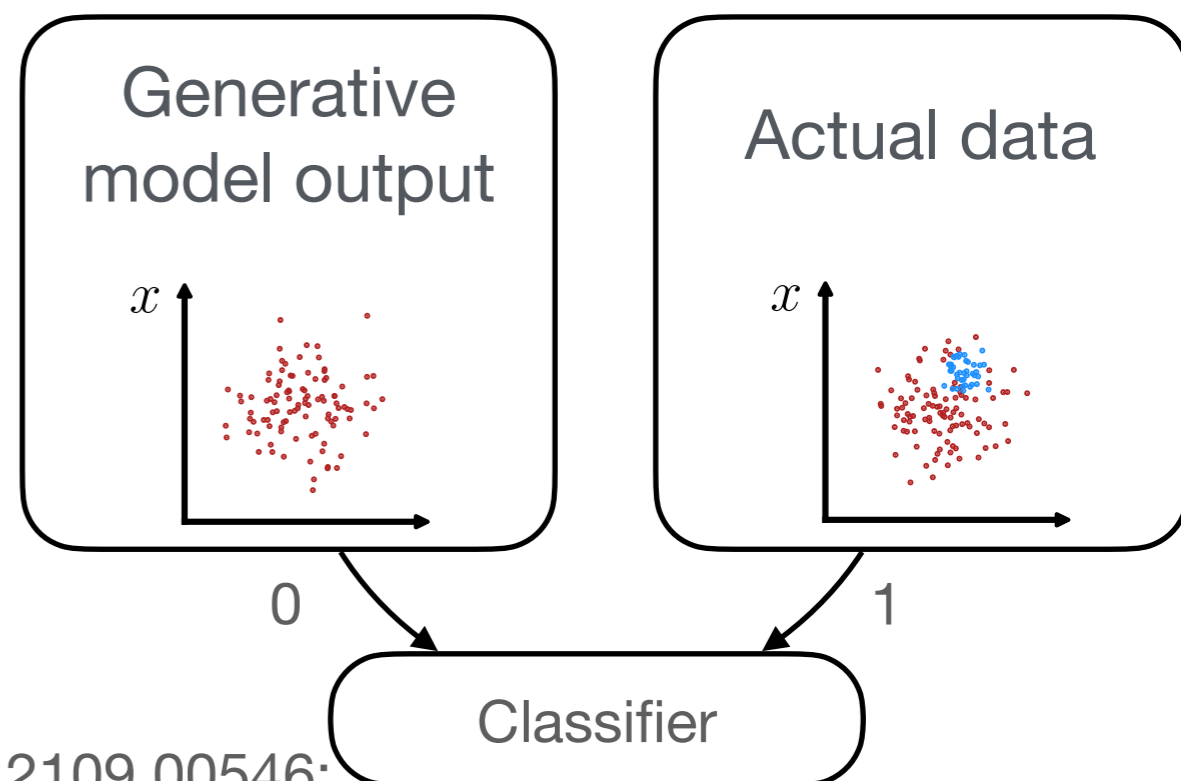


CATHODE

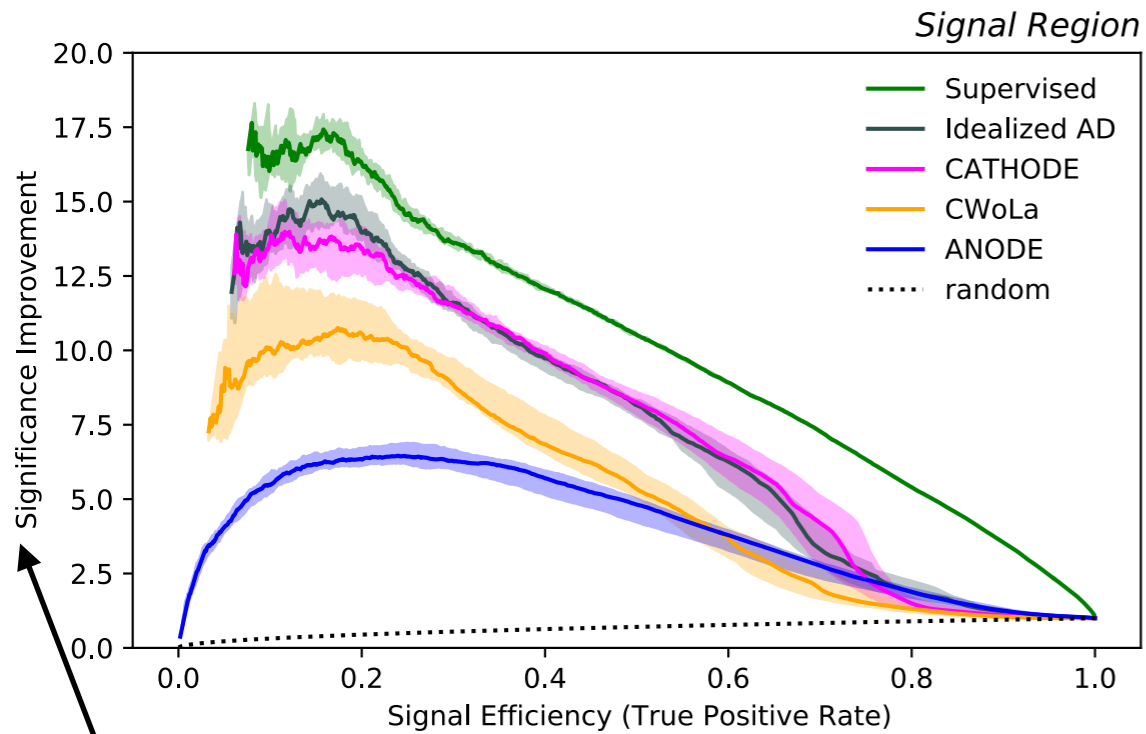


Method for **resonant anomaly detection**

1. Train **generative** model (conditional normalising flow)
2. Interpolate and sample
3. Use classifier to identify potential anomaly



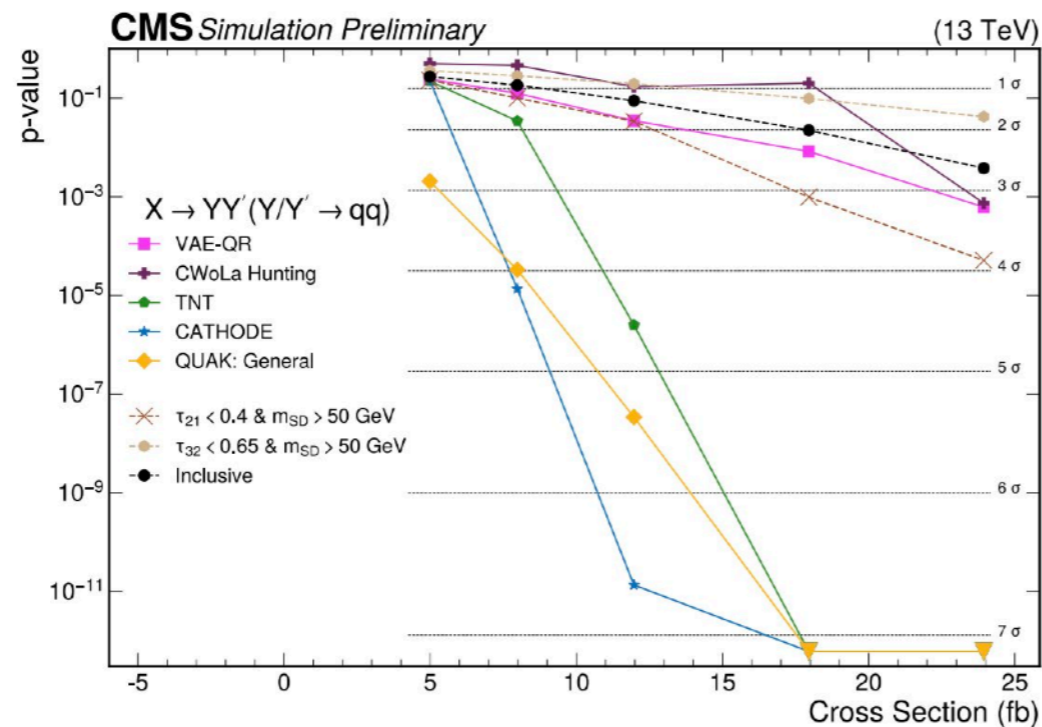
CATHODE



Method for **resonant anomaly detection**

1. Train **generative** model (conditional normalising flow)
2. Interpolate and sample
3. Use classifier to identify potential anomaly

$$\text{SIC} = \frac{\epsilon_S}{\sqrt{\epsilon_B}}$$



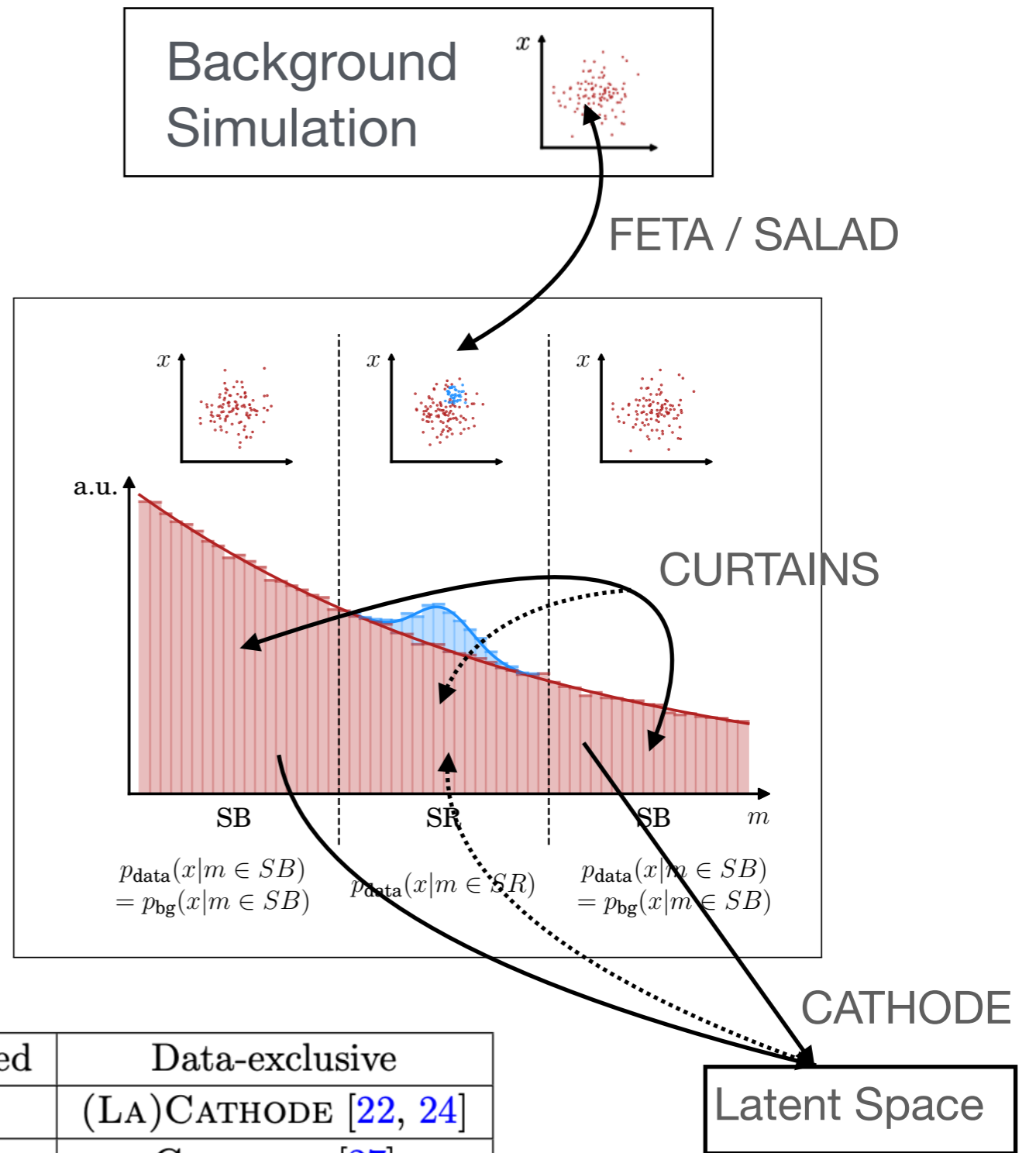
Alternatives

CATHODE: Conditional generative model interpolates into signal region

CURTAINS: Learns a conditioned morphing function for data

SALAD: Learns weights to for background simulation on the signal region

FETA: Learns a flow to morph background into the signal region



	Simulation-assisted	Data-exclusive
Likelihood learning	SALAD [17]	(LA)CATHODE [22, 24]
Feature morphing	FETA [26]	CURTAINS [27]

Alternatives

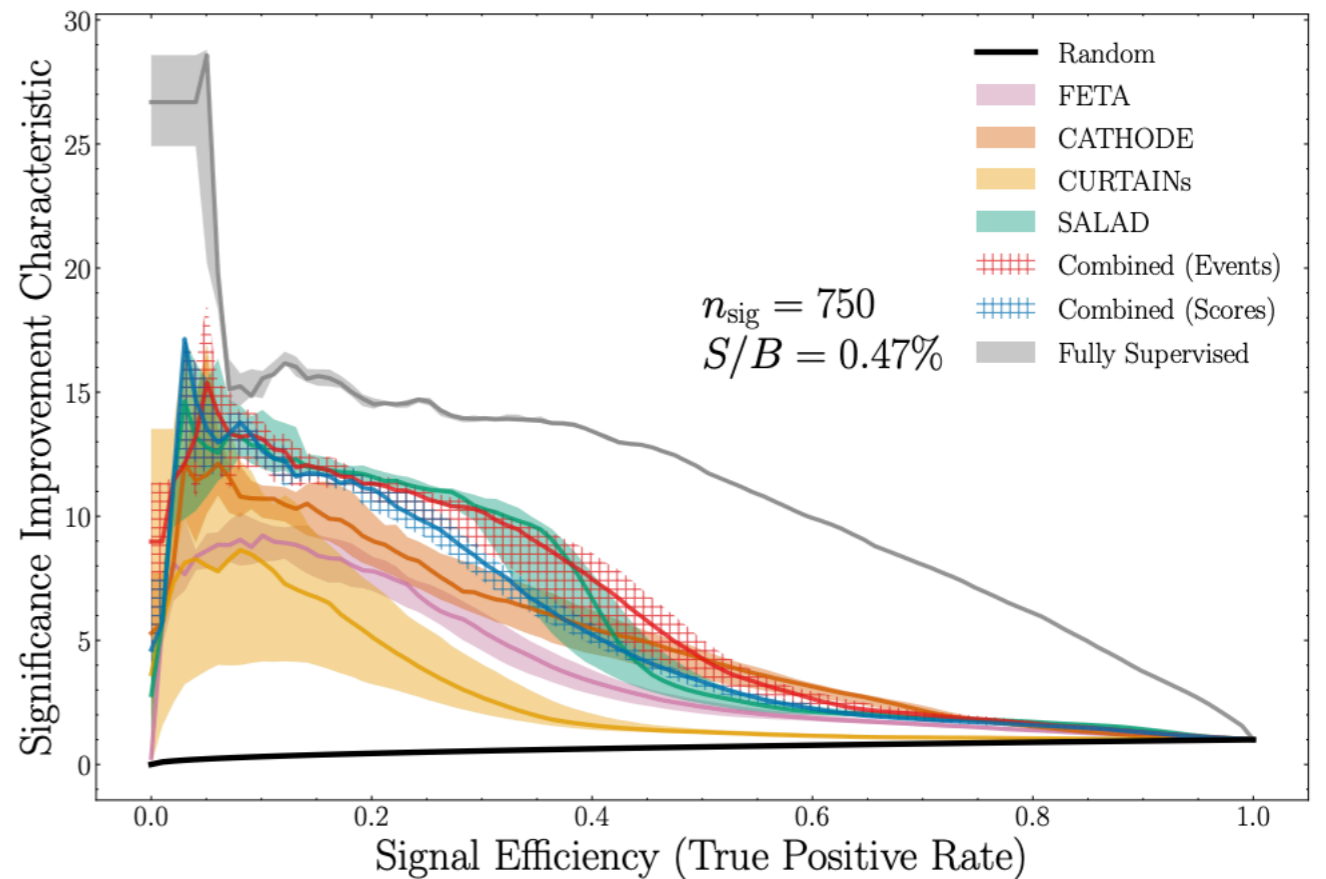
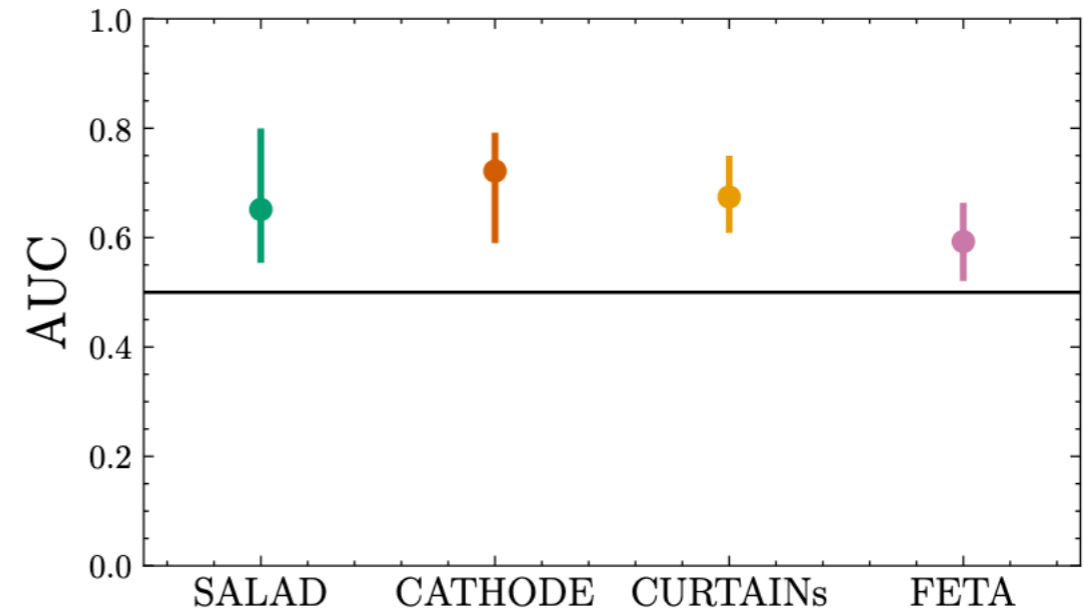
CATHODE: Conditional generative model interpolates into signal region

CURTAINS: Learns a conditioned morphing function for data

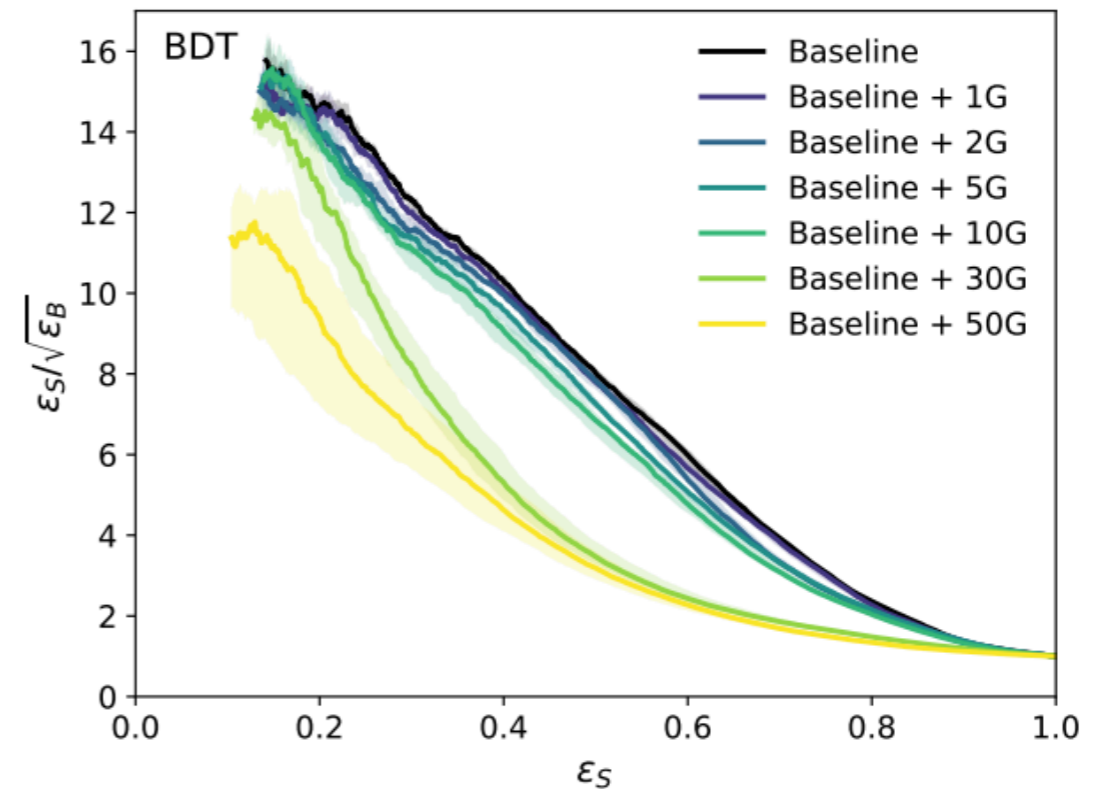
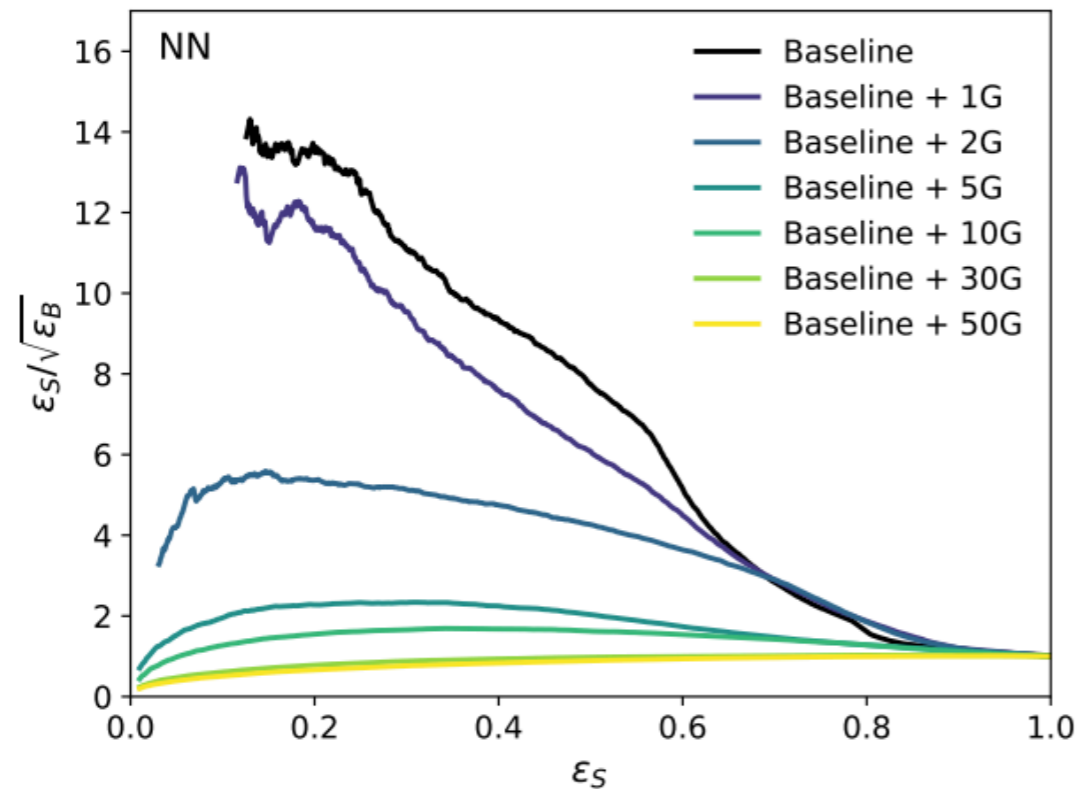
SALAD: Learns weights to for background simulation on the signal region

FETA: Learns a flow to morph background into the signal region

Similar **performance**, slight gain from **combination**



Side Note: Noisy Features

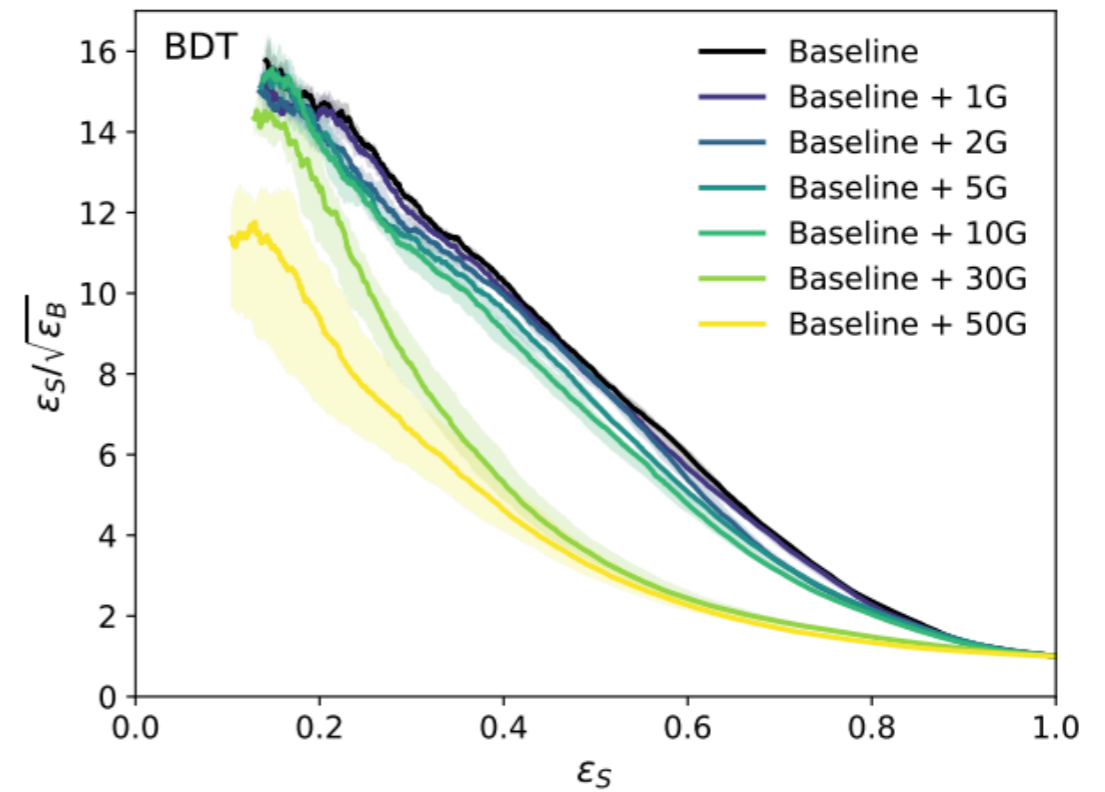
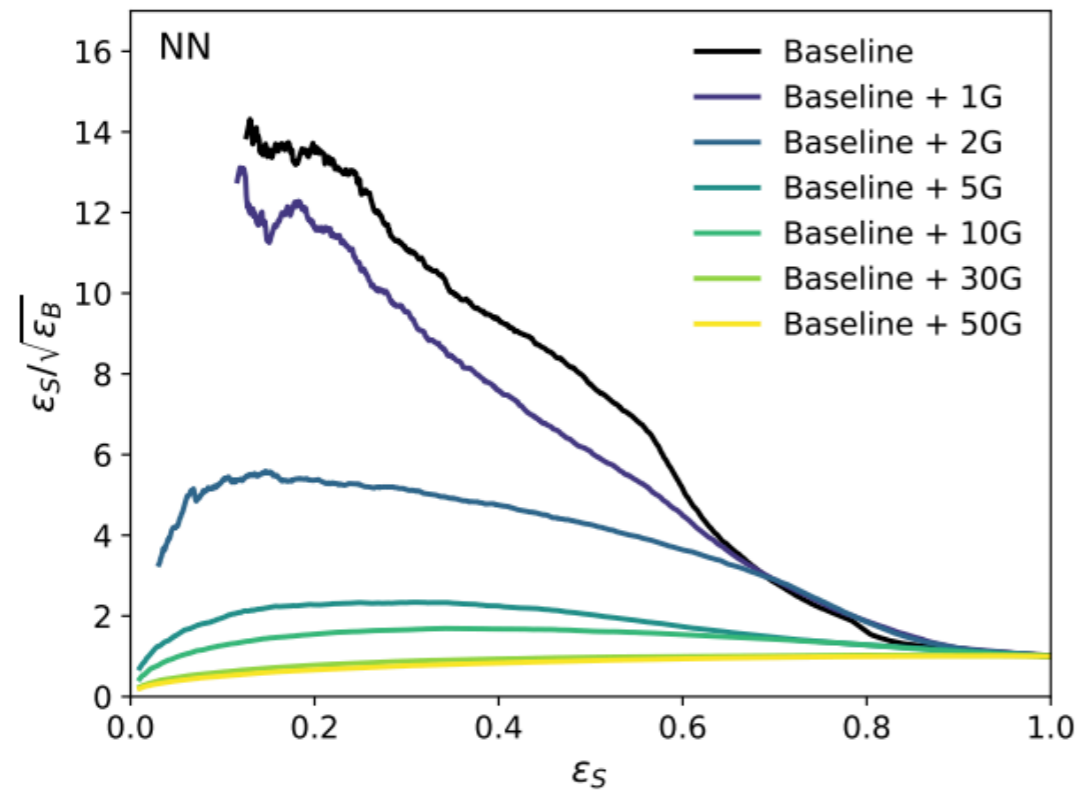


We don't know in which feature is anomalous: Use **more input features**

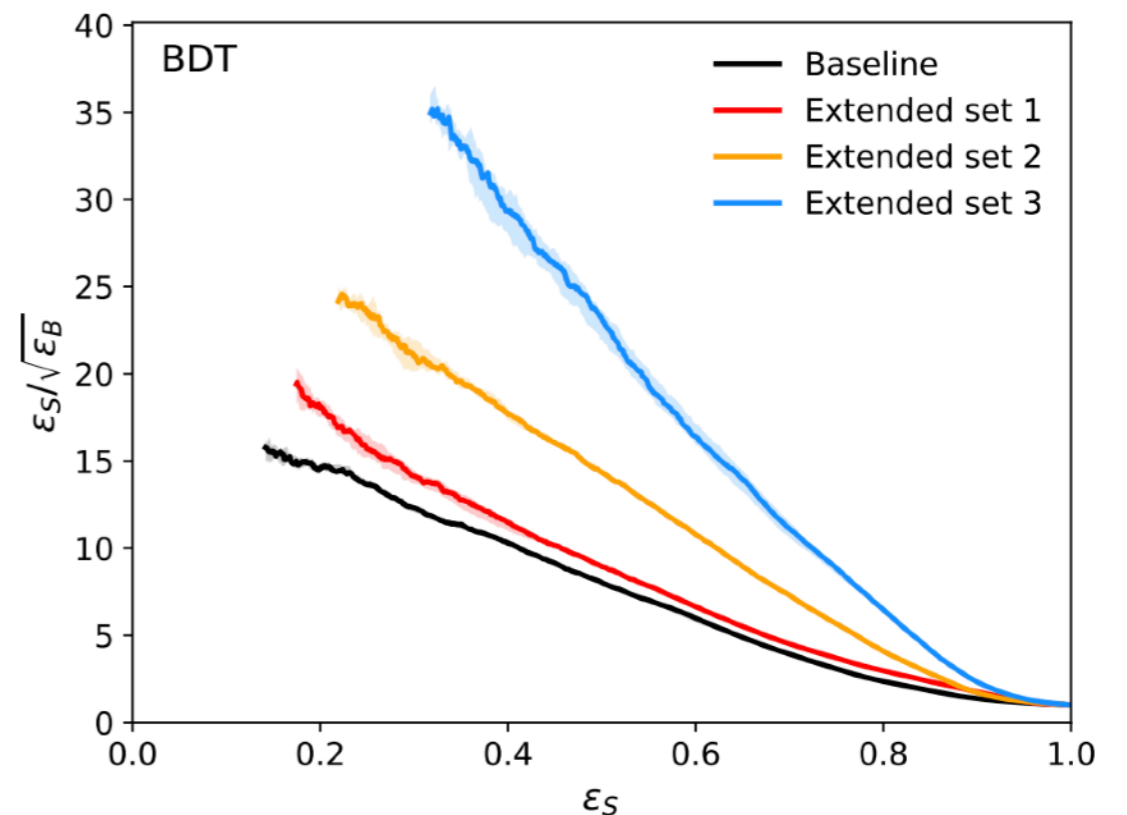
But: degrades performance

BDTs are **more robust** against noisy features

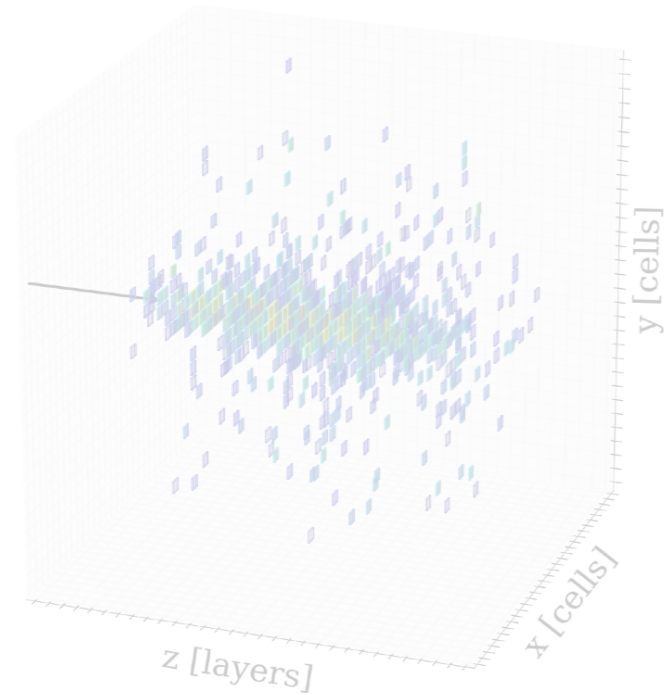
Side Note: Noisy Features



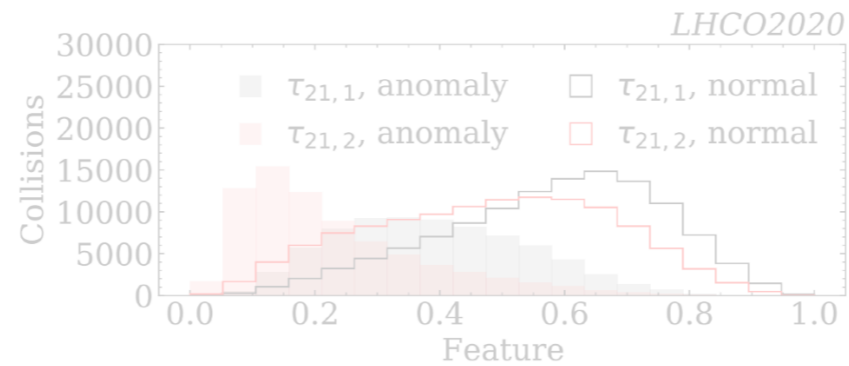
Allows adding **more inputs!**



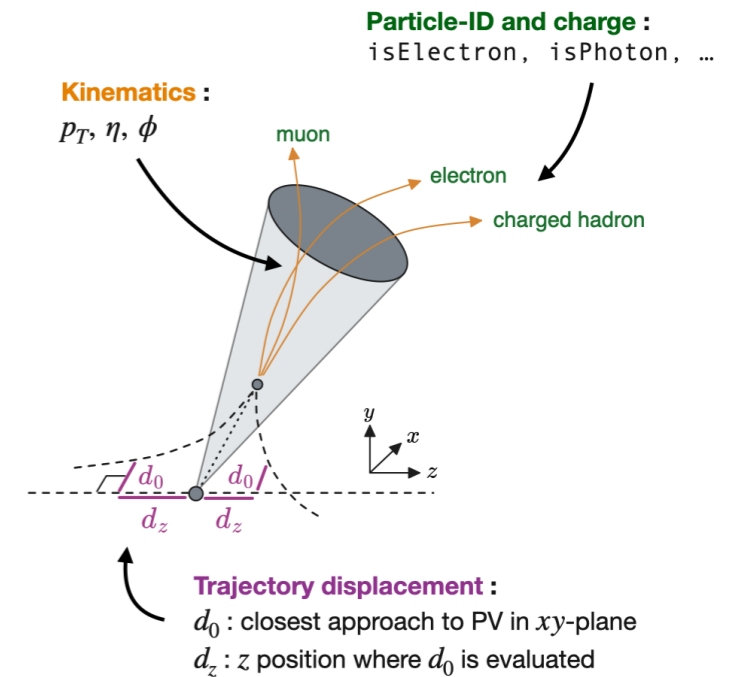
Why generative models?



Showers in complex high-resolution calorimeters



High-level jet features



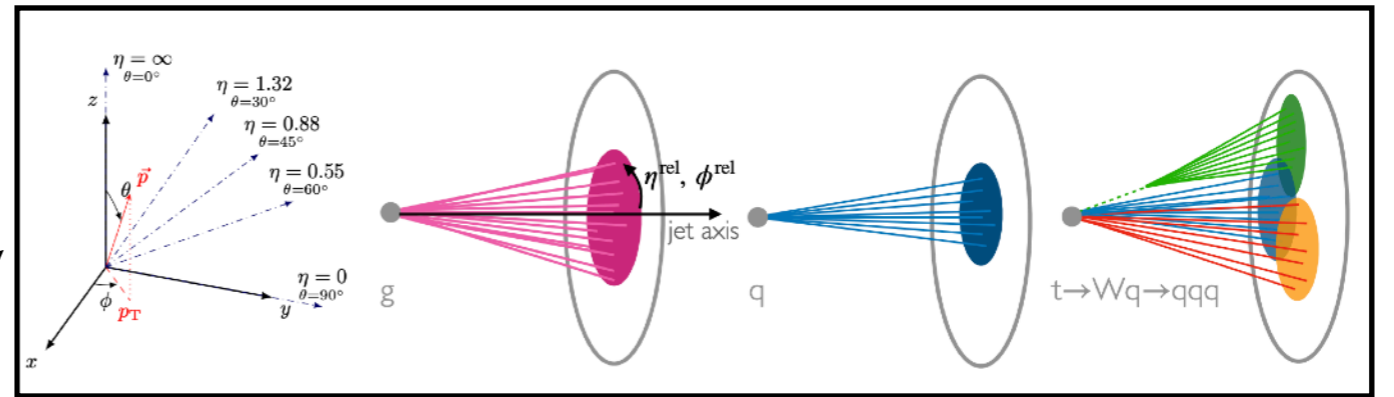
Jet constituents

$$p(x)$$

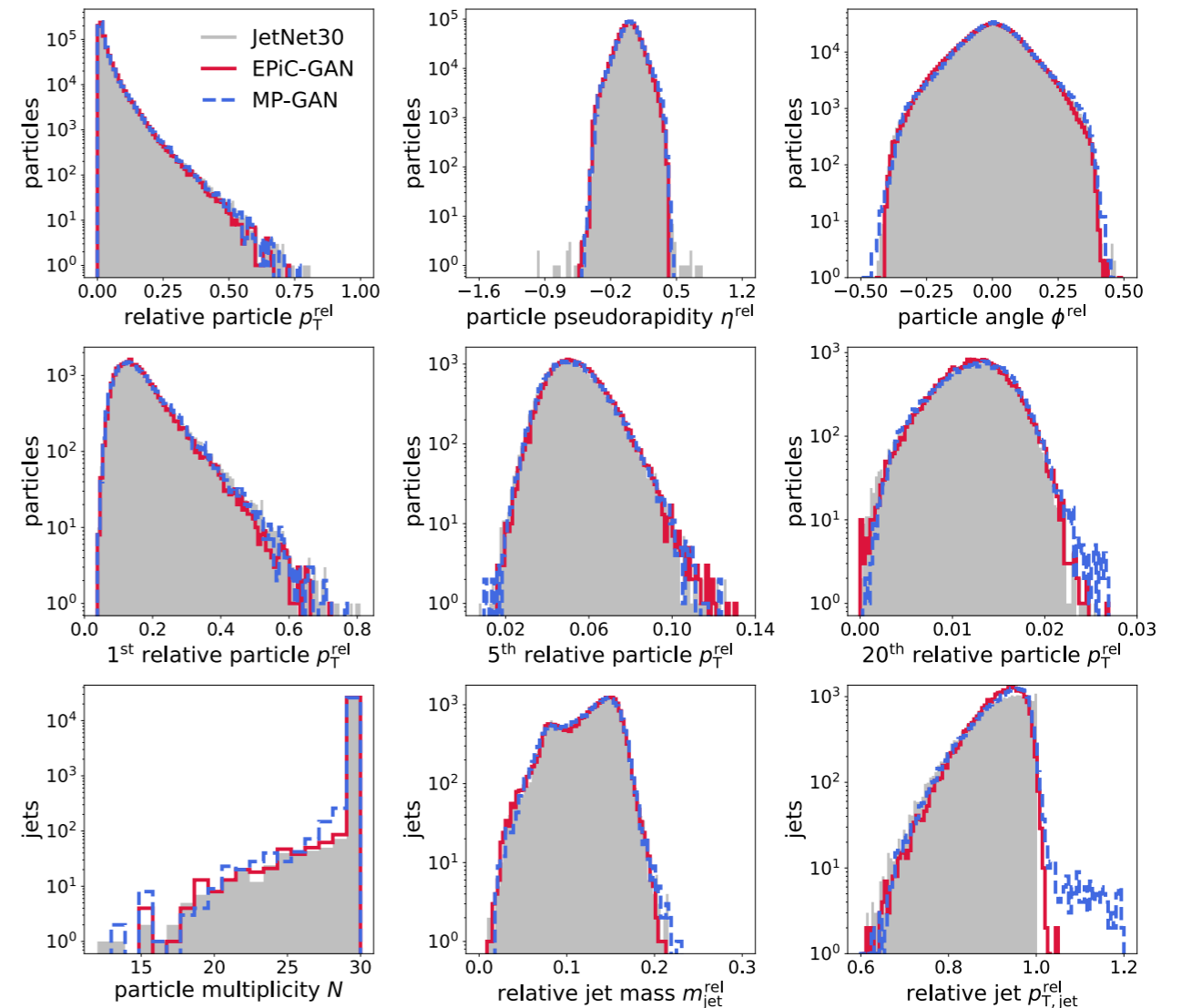
Sample $X_i \sim p(x)$
to generate datapoints

Simulation targets

Improve anomaly detection (and other background estimation tasks) by learning jet constituents instead of high-level features



	JetNet [3]
Jet types	5 types
Dataset size	180 thousand jets per class
Features	Kinematics

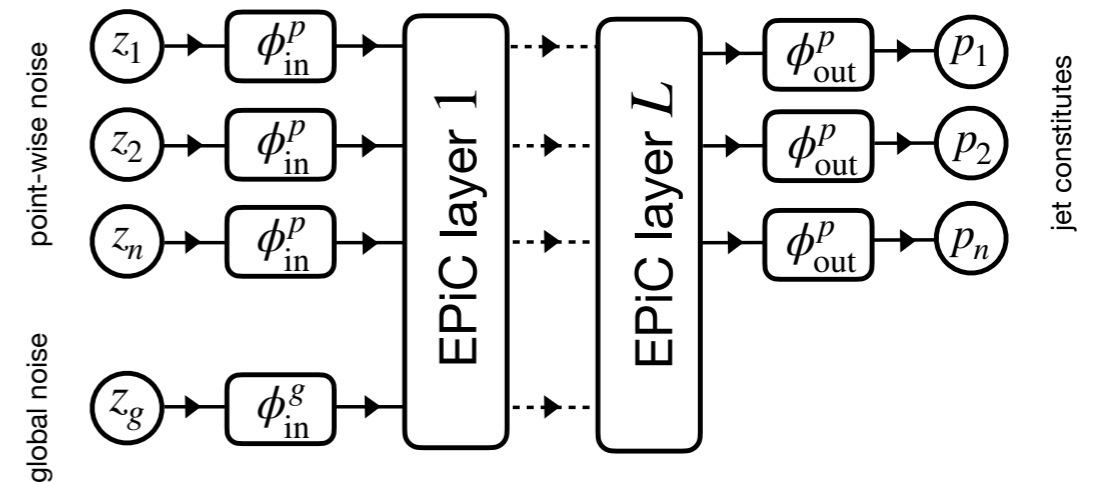
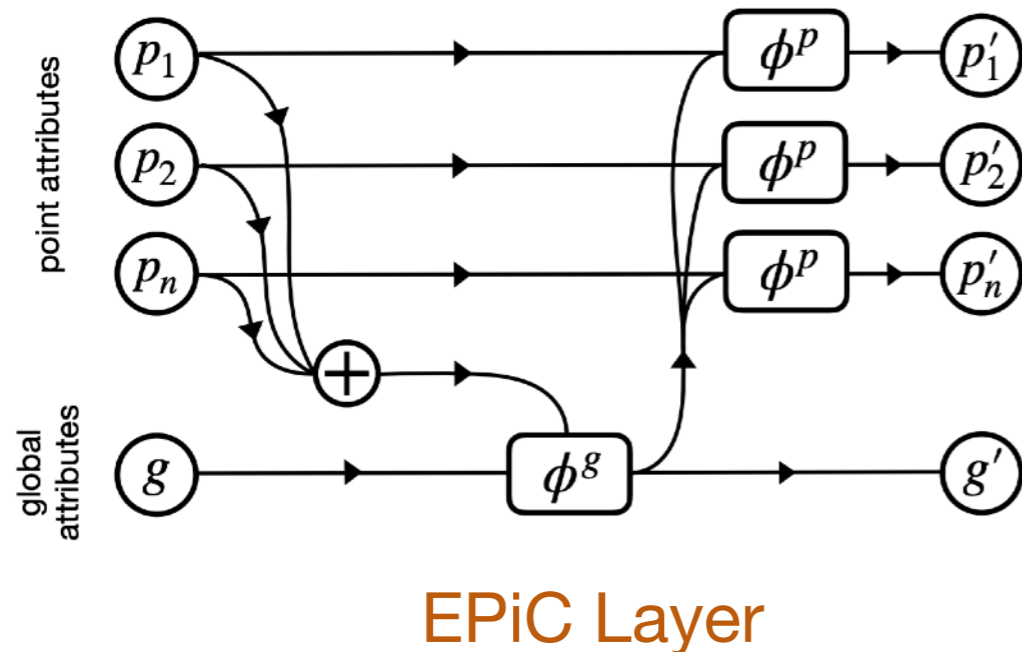


Simulation targets

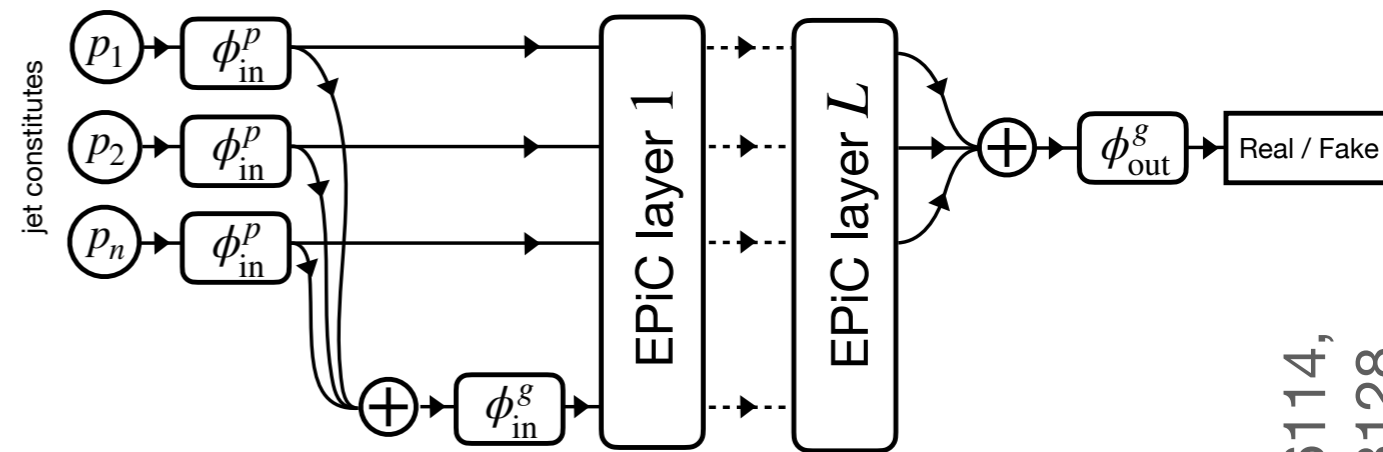
Improve anomaly detection (and other background estimation tasks) by learning jet constituents instead of high-level features.

Treat as **point cloud** & use a **permutation invariant GAN**

	JetNet [3]
Jet types	5 types
Dataset size	180 thousand jets per class
Features	Kinematics



(a) Generator



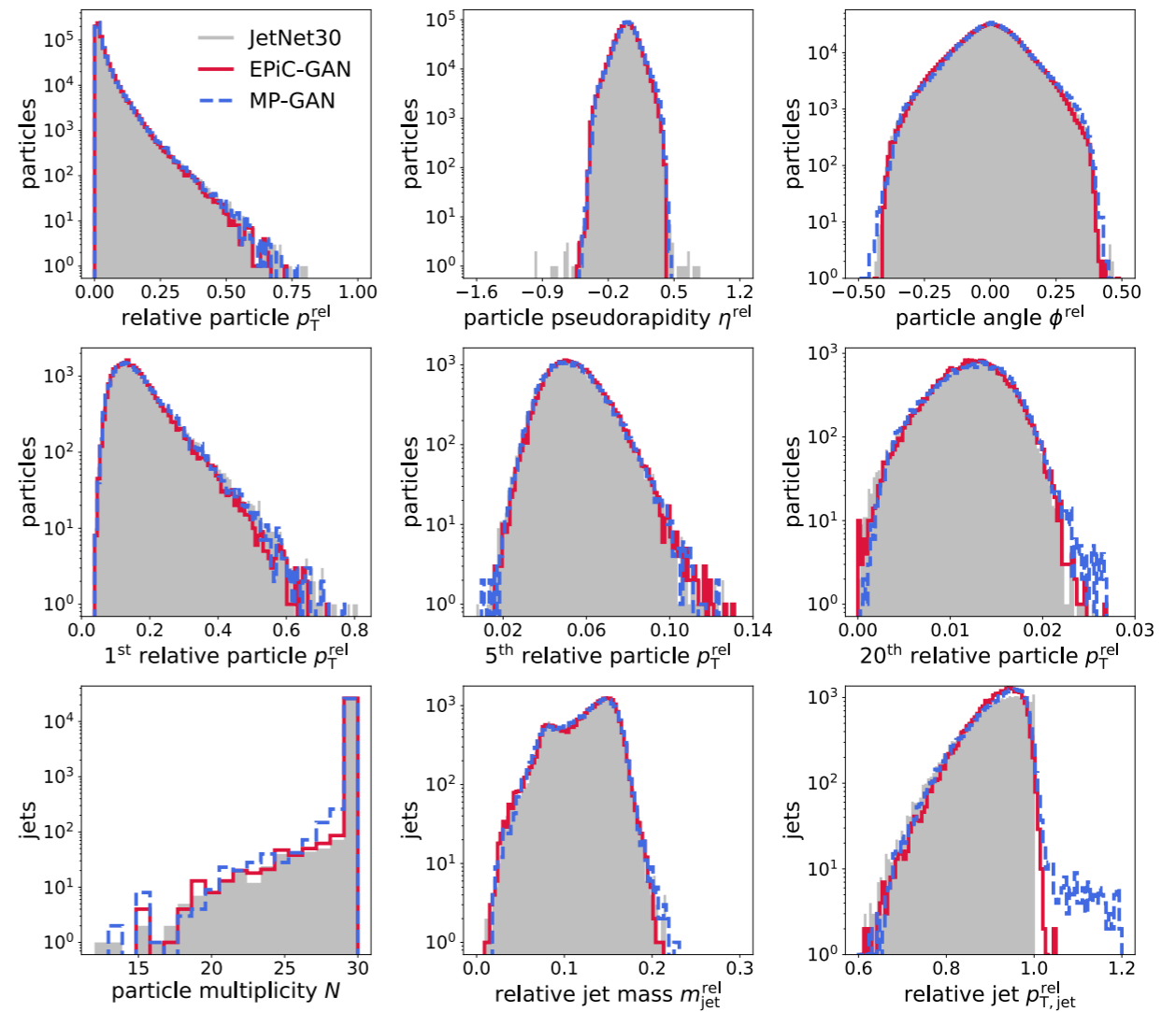
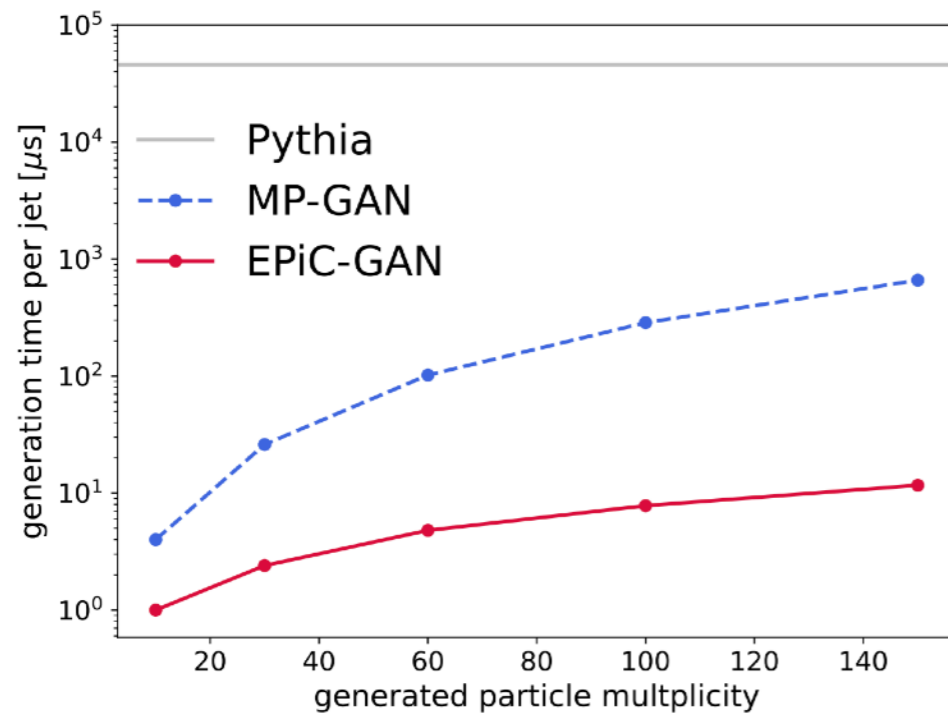
(b) Discriminator

Simulation targets

Improve anomaly detection (and other background estimation tasks) by learning jet constituents instead of high-level features.

Treat as **point cloud** & use a **permutation invariant GAN**

	JetNet [3]
Jet types	5 types
Dataset size	180 thousand jets per class
Features	Kinematics

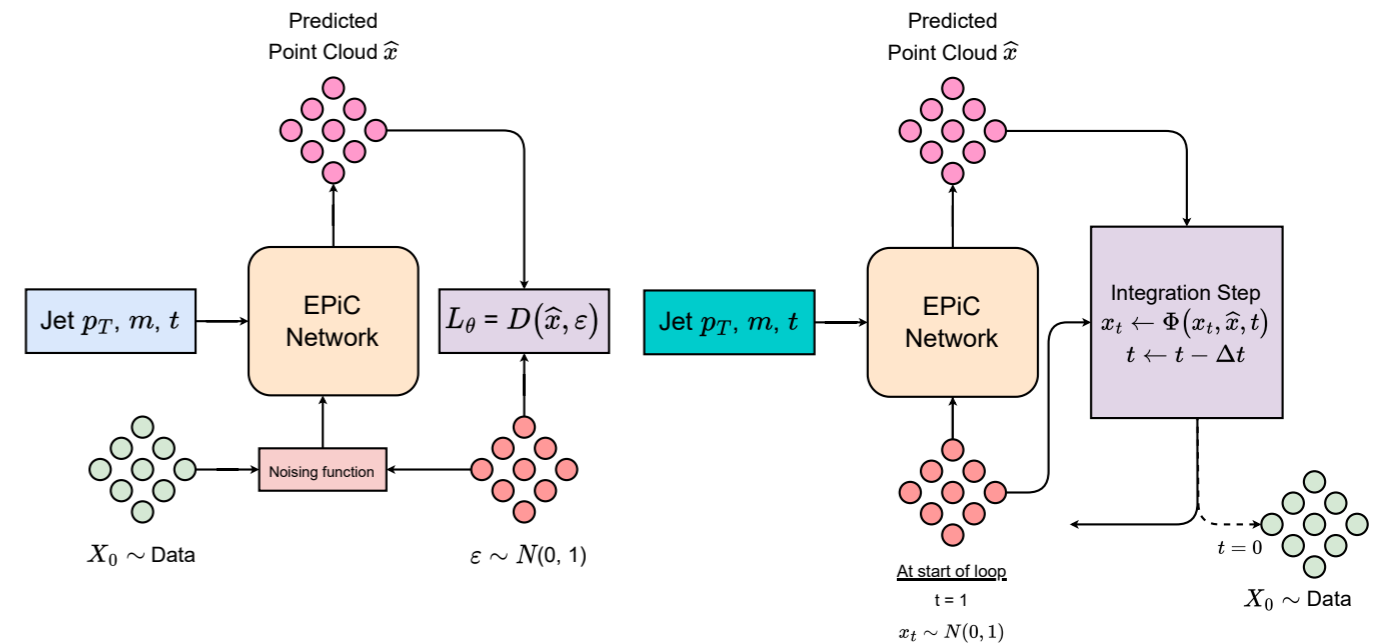


Simulation targets

Improve anomaly detection (and other background estimation tasks) by learning jet constituents instead of high-level features.

Again, improve by moving from GAN to diffusion/flow matching

	JetNet [3]
Jet types	5 types
Dataset size	180 thousand jets per class
Features	Kinematics

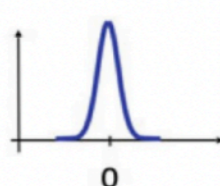


Training

Generation

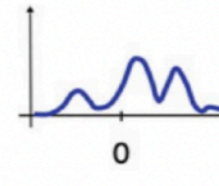
Generation	Model	FPND	NLP	$KL^m (\times 10^{-3})$	$KL^{p_T^{\text{const}}} (\times 10^{-3})$	$KL^{\tau_{21}} (\times 10^{-3})$	$KL^{\tau_{32}} (\times 10^{-3})$	$KL^{D_2} (\times 10^{-3})$
Conditional	PC-JeDi	0.40	3.08	8.56 ± 0.75	3.25 ± 0.09	12.82 ± 1.16	27.08 ± 1.40	11.91 ± 0.92
	EPiC-JeDi	0.42	3.1	5.26 ± 0.51	2.99 ± 0.05	7.81 ± 0.61	17.34 ± 1.08	6.58 ± 0.73
	EPiC-FM	0.11	1.35	3.77 ± 0.50	2.03 ± 0.02	7.40 ± 0.64	8.09 ± 0.93	4.31 ± 0.46
Unconditional	EPiC-GAN	0.34	3.43	3.71 ± 0.42	3.33 ± 0.03	8.28 ± 0.76	17.68 ± 0.91	13.18 ± 1.04
	EPiC-JeDi	1.63	3.11	18.42 ± 1.12	3.73 ± 0.08	8.00 ± 0.80	15.27 ± 1.35	12.33 ± 1.06
	EPiC-FM	0.14	1.38	5.80 ± 0.54	2.03 ± 0.01	7.69 ± 0.71	9.24 ± 1.00	4.51 ± 0.58

Aside: Flow Matching



$x_0 \sim p_0$

$f_0(x_0) \rightarrow x_t := f(x_t, t) \rightarrow f_1(x_1) \rightarrow \frac{\partial x_t}{\partial t} = v_\theta(x_t, t) \rightarrow f_{T-1}(x_{T-1})$



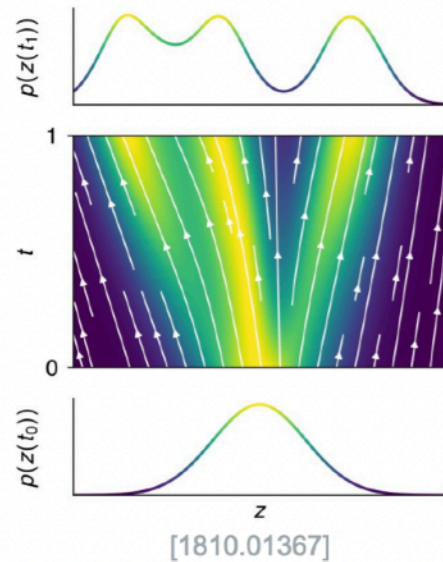
$x_1 \sim p_1$

	Normalizing Flow (NF)	Continuous Normalizing Flow (CNF)
Training:	$\log p_T(x_T) = \log p_0(x_0) - \log \left \frac{\partial f_t^\theta}{\partial x_t} \right $	$\log p_1(x_1) = \log p_0(x_0) - \int_{t_0}^t \text{Tr} \left(\frac{\partial v_\theta}{\partial x_t} \right) dt$
Sampling:	$x_T = f_{T-1} \circ \dots \circ f_0(x_0)$ <ul style="list-style-type: none"> ▪ f must be invertible ▪ Determinant computationally expensive <ul style="list-style-type: none"> ➢ Restricted transformations needed 	Solve ODE (ordinary differential equation) <ul style="list-style-type: none"> ▪ f has no restrictions ▪ Trace is easier to calculate ▪ Still computationally expensive

Chen et al.; Neural Ordinary Differential Equations; arxiv:1806.07366

Formally **similar to diffusion models**

Aside: Flow Matching



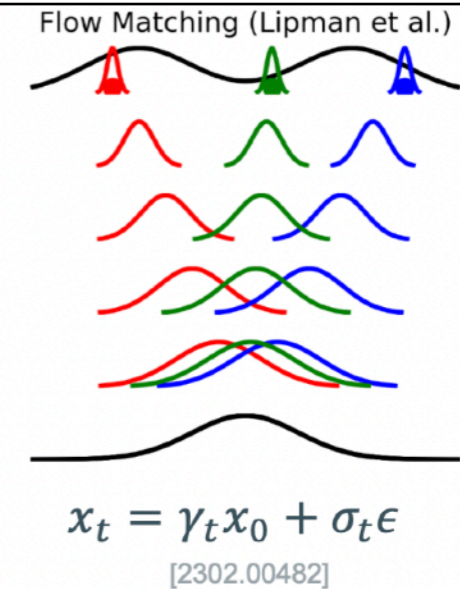
Continuous Normalizing Flow (CNF)

Training:

- Training is difficult because ODE needs to be solved

$$\log p_1(x_1) = \log p_0(x_0) - \int_{t_0}^t \text{Tr} \left(\frac{\partial v_\theta}{\partial x_t} \right) dt$$

$$L_{FM} = \left\| v_\theta(x_t) - u_t(x_t | x_0) \right\|^2$$



Flow Matching (FM)

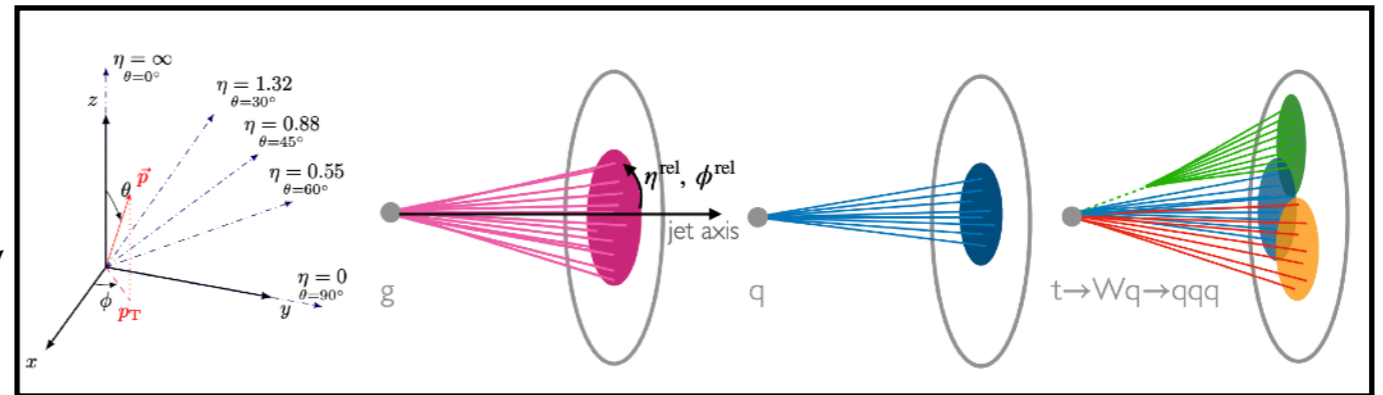
Training:

- Simulation-free training objective (no ODE solving during training)
- Regressing against conditional flows
- Much faster training

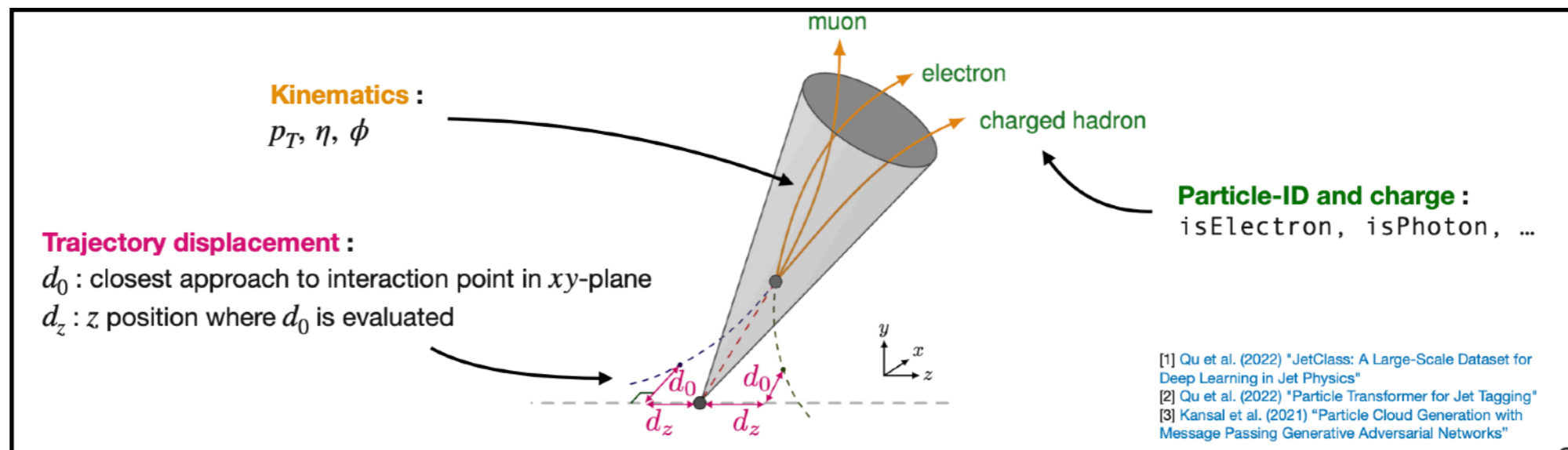
$$\frac{\partial x_t}{\partial t} = v_\theta(x_t, t)$$

Simulation targets

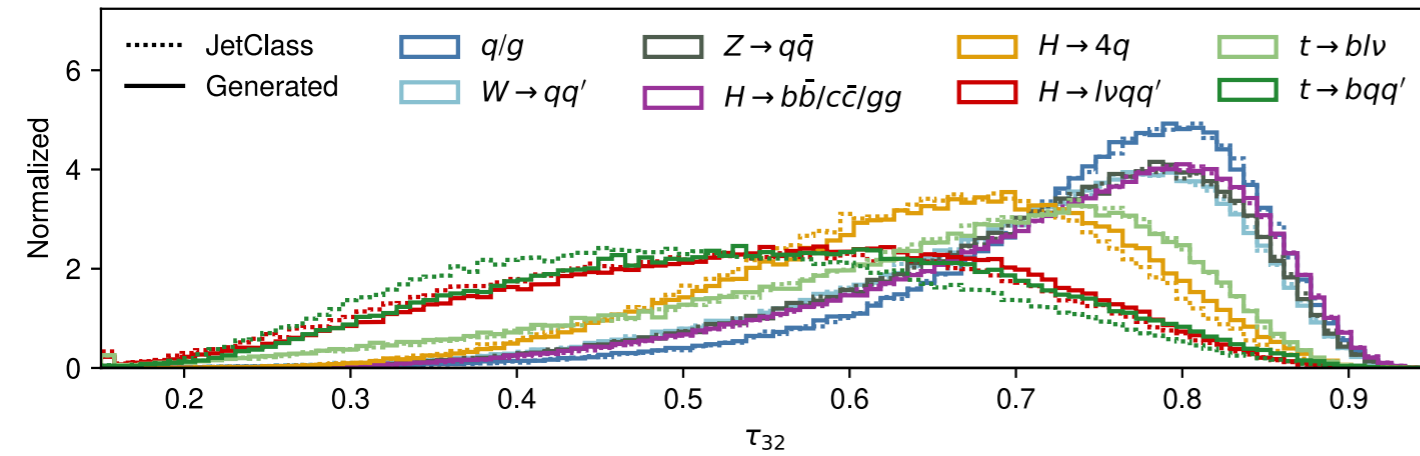
Improve anomaly detection (and other background estimation tasks) by learning jet constituents instead of high-level features



	JetNet [3]	JetClass [1]
Jet types	5 types	10 types (several decay channels for top and H jets)
Dataset size	180 thousand jets per class	12.5 million jets per class (70x more than JetNet)
Features	Kinematics	Kinematics, Particle-ID and charge, trajectory displacement

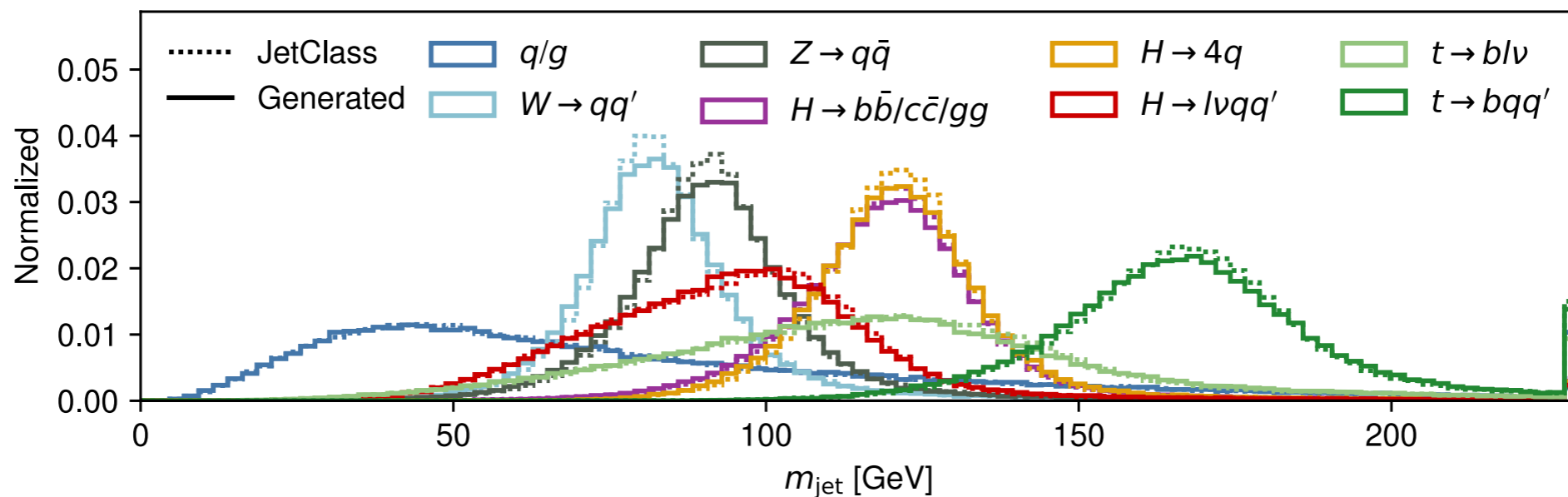
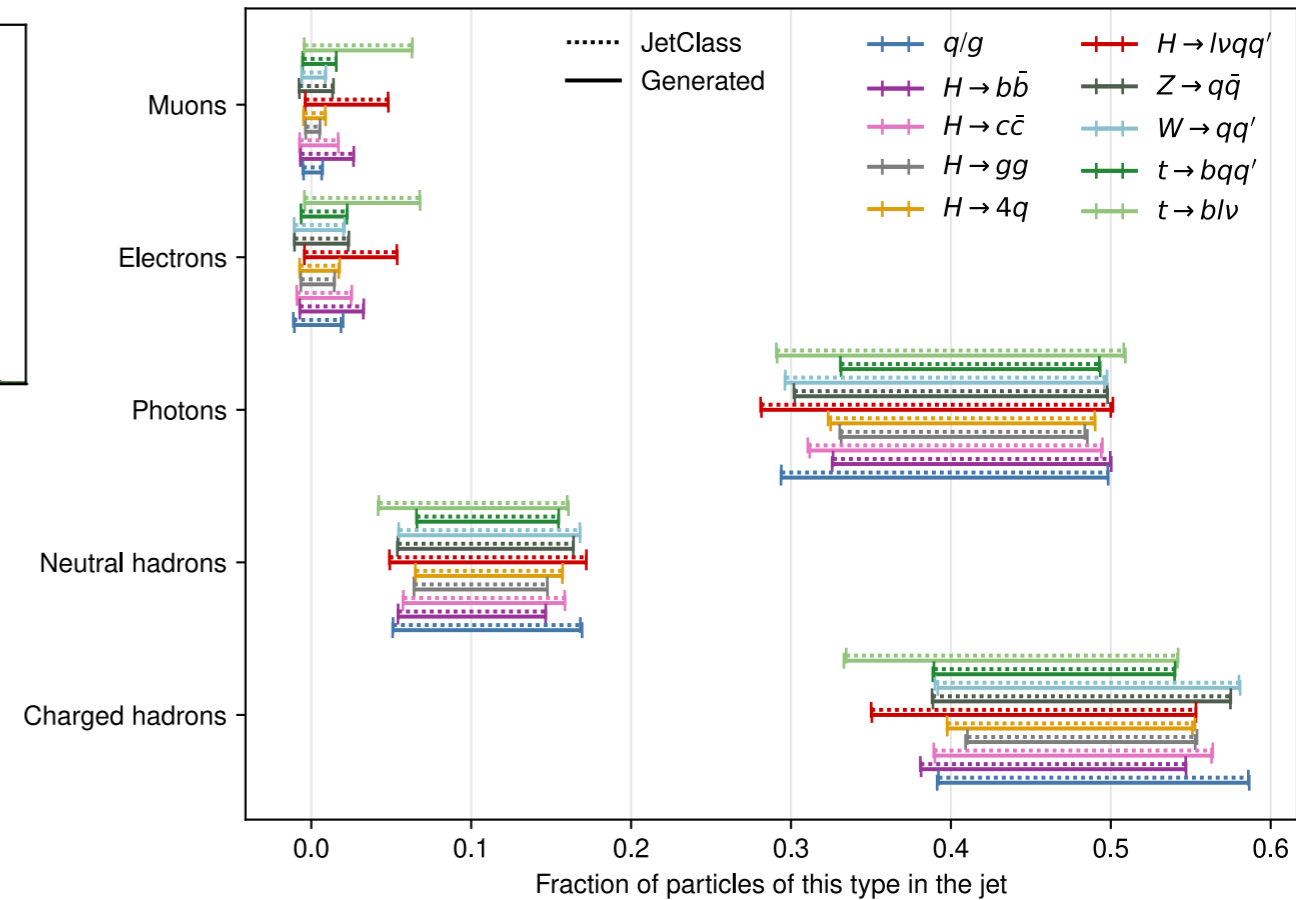


Simulation targets

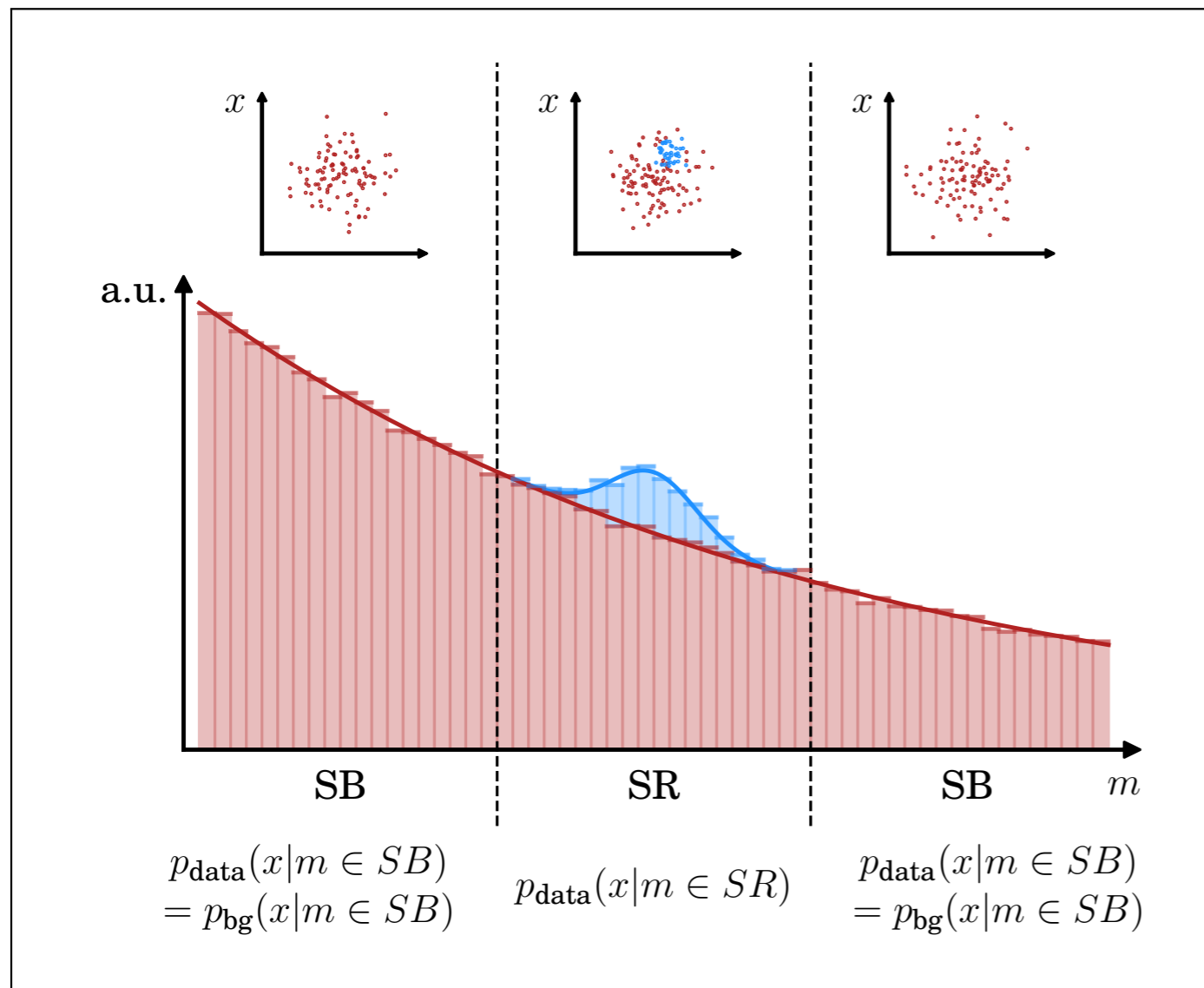


Apply **EPiC + Flow matching** to additional features

Good agreement across distributions

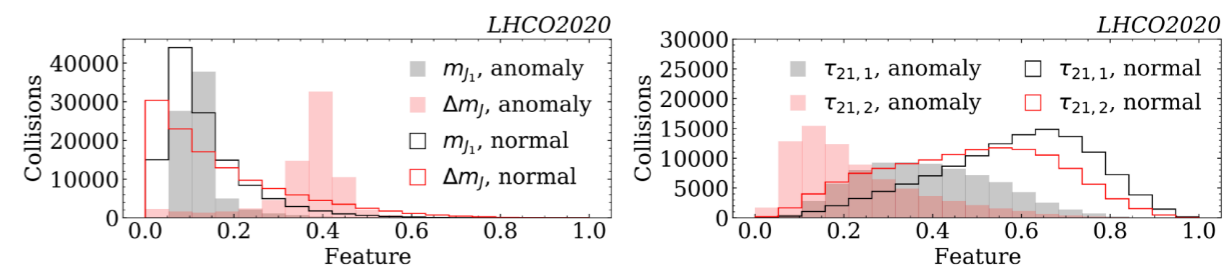


Reminder: CATHODE



1. Train **generative** model (conditional normalising flow)

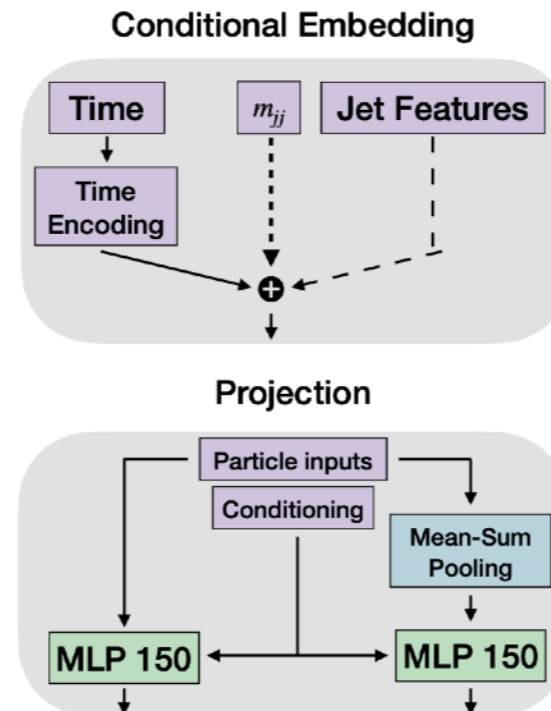
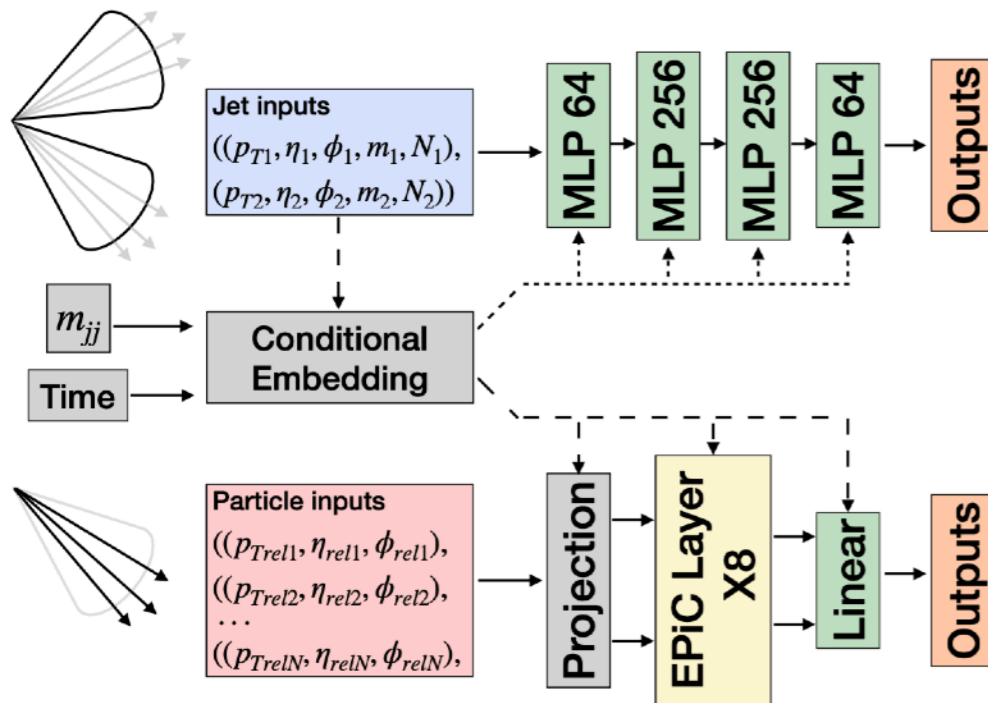
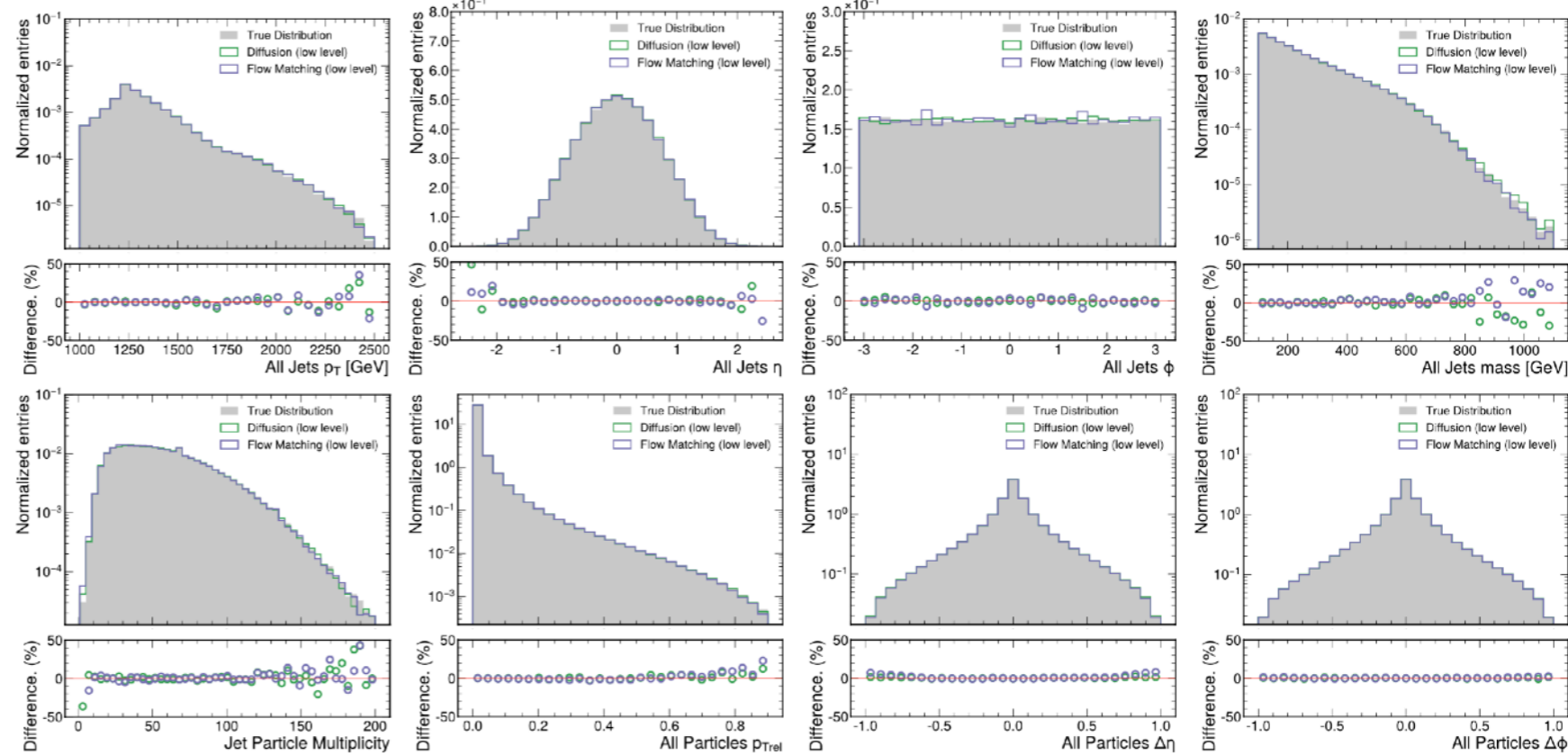
Replace **4 high level** features:



with **1674 low-level features** (279 constituent 3-vectors each for 2 jets)

Particle Inputs

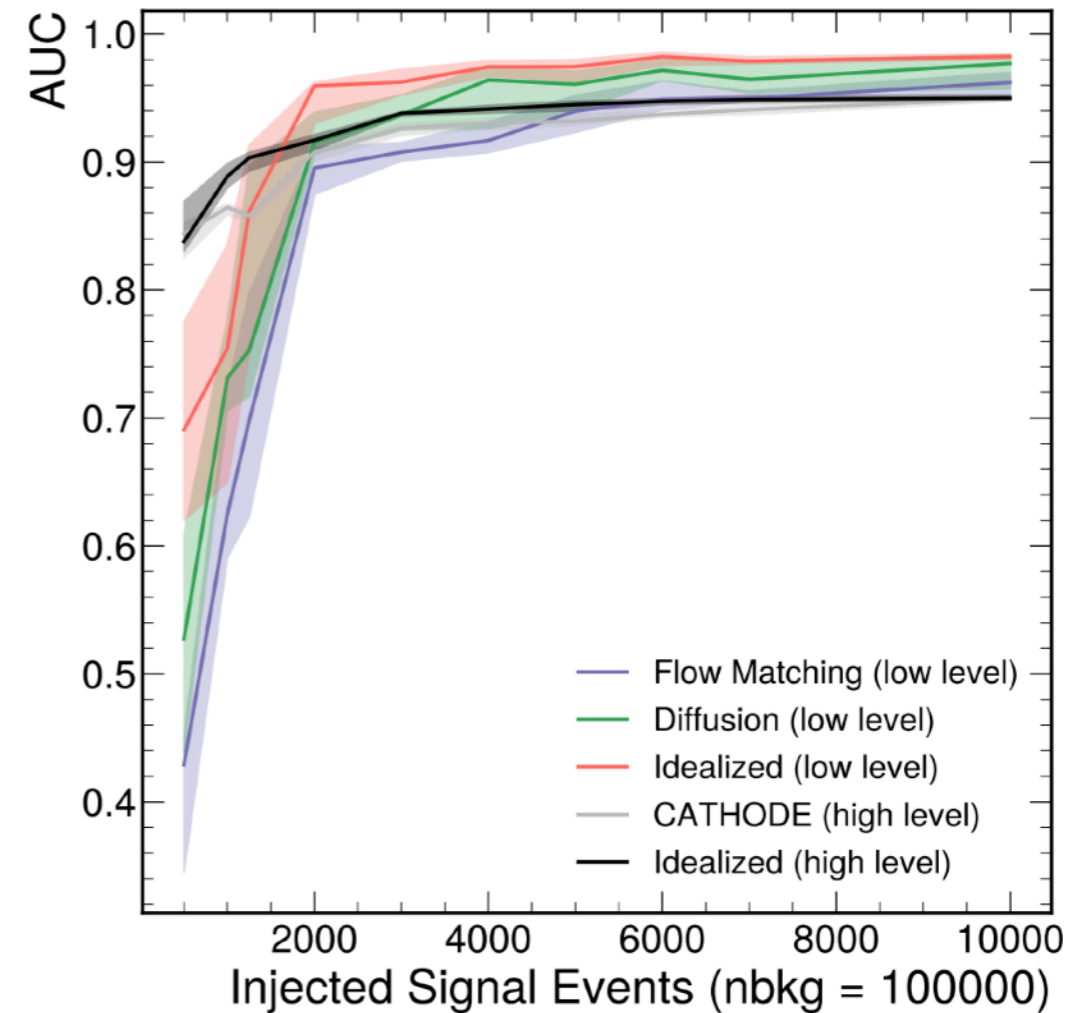
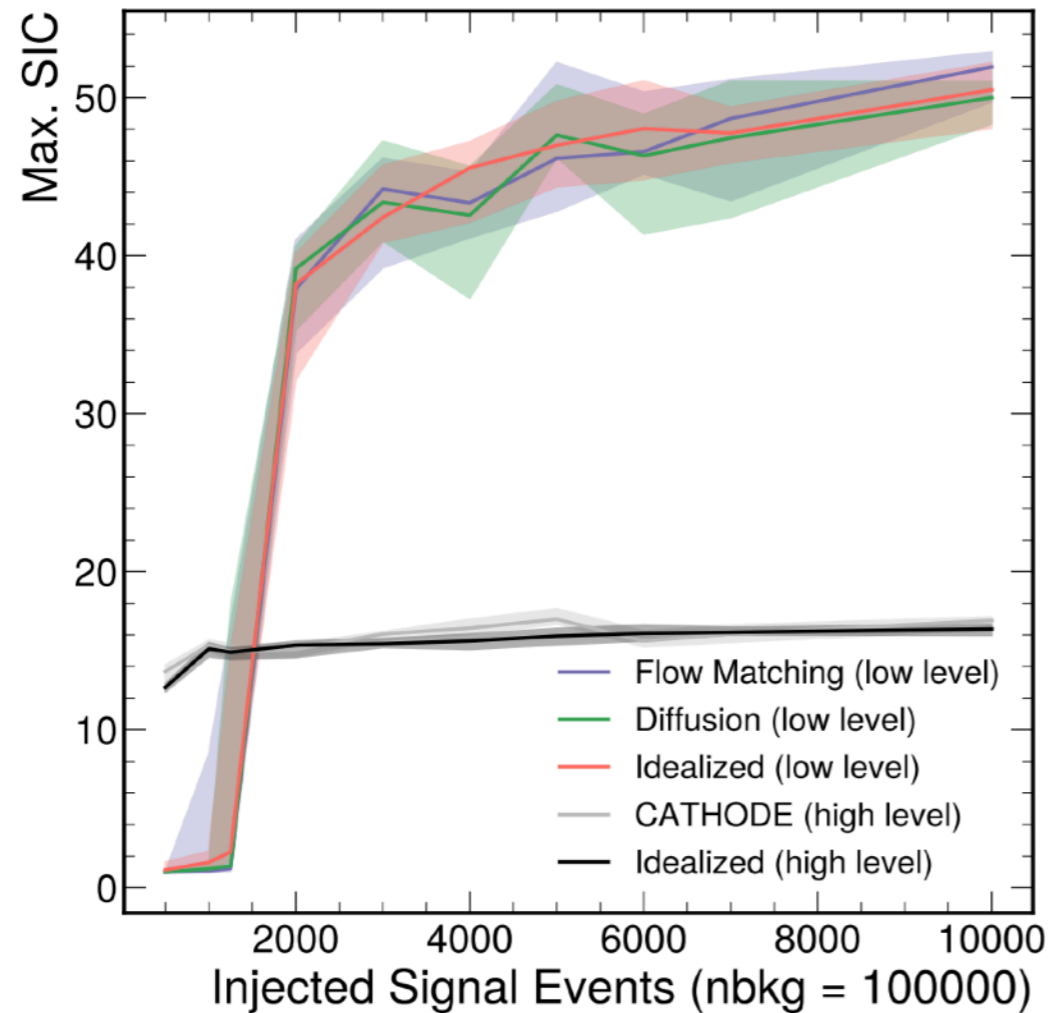
Using all **low-level features** in-principle includes all properties



Use **point cloud diffusion/flow matching**

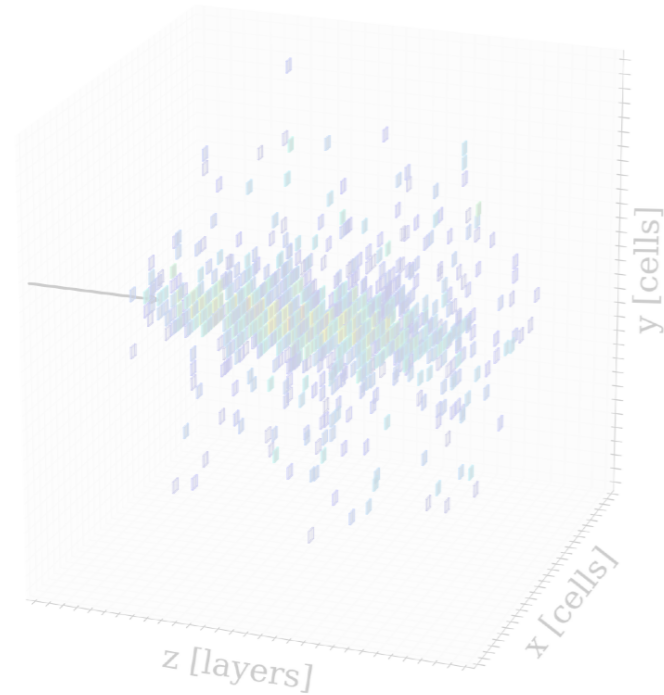
CATHODE classifier is a transformer

Particle Inputs

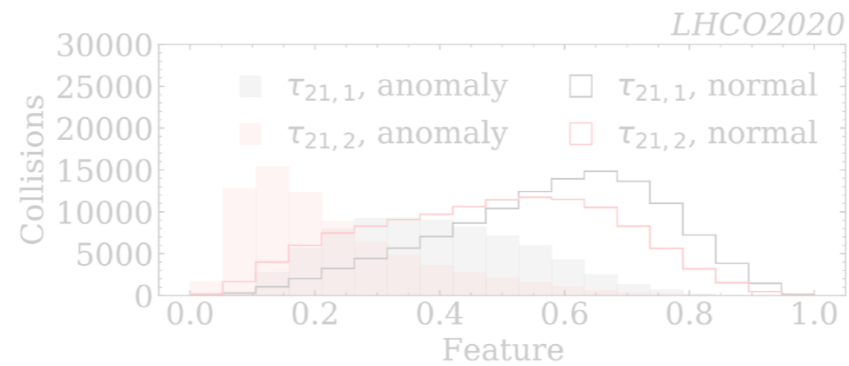


Greatly **improves maximum SIC**, but currently requires **more initial signal**

Why generative models?



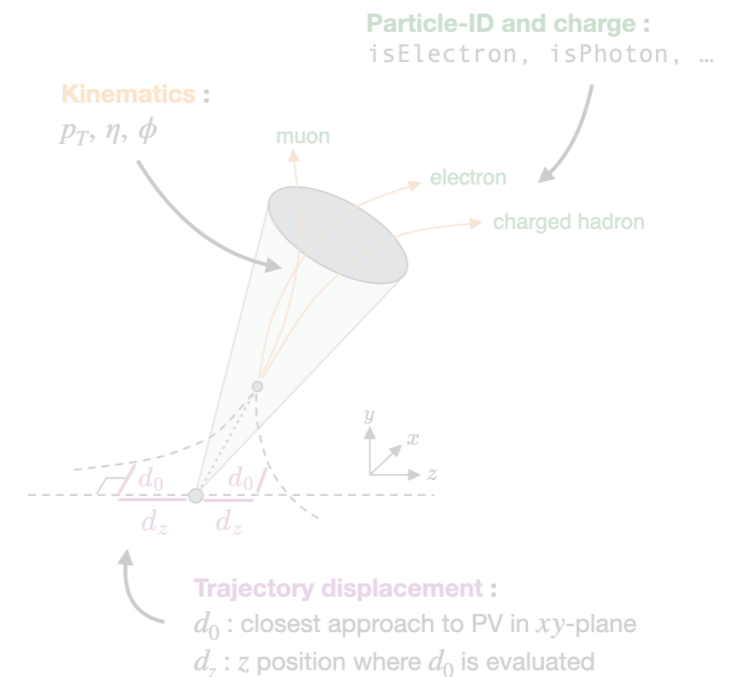
Showers in complex high-resolution calorimeters



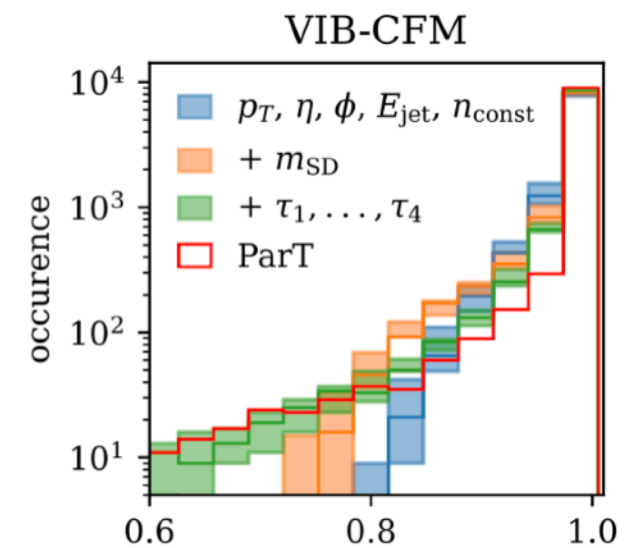
High-level jet features

$$p(x)$$

Sample $X_i \sim p(x)$
to generate datapoints



Jet constituents



Classifier surrogates

Classifier Surrogates: Motivation

Les Houches guide to reusable ML models in LHC analyses

Jack Y. Araz¹, Andy Buckley², Gregor Kasieczka³, Jan Kieseler⁴, Sabine Kraml⁵, Anders Kvellestad⁶, Andre Lessa⁷, Tomasz Procter², Are Raklev⁶, Humberto Reyes-Gonzalez^{8,9,10}, Krzysztof Rolbiecki¹¹, Sezen Sekmen¹², Gokhan Unel¹³

¹ Jefferson Lab, Newport News, VA 23606, USA

² University of Glasgow, Glasgow, UK

³ Univ. Hamburg, Germany

⁴ Karlsruhe Institute for Technology, Karlsruhe, Germany

⁵ Univ. Grenoble Alpes, CNRS, Grenoble INP, LPSC-IN2P3, 38000 Grenoble, France

⁶ University of Oslo, 0316 Oslo, Norway

⁷ Universidade Federal do ABC, Santo André, 09210-580 SP, Brazil

⁸ Department of Physics, University of Genova, Via Dodecaneso 33, 16146 Genova, Italy

⁹ INFN, Sezione di Genova, Via Dodecaneso 33, I-16146 Genova, Italy

¹⁰ Institut für Theoretische Teilchenphysik und Kosmologie, RWTH Aachen, 52074 Aachen, Germany

¹¹ Faculty of Physics, University of Warsaw, 02-093 Warsaw, Poland

¹² Department of Physics, Kyungpook National University, Daegu, South Korea

¹³ U.C. Irvine, Physics & Astronomy Dept., Irvine, CA, USA

Abstract

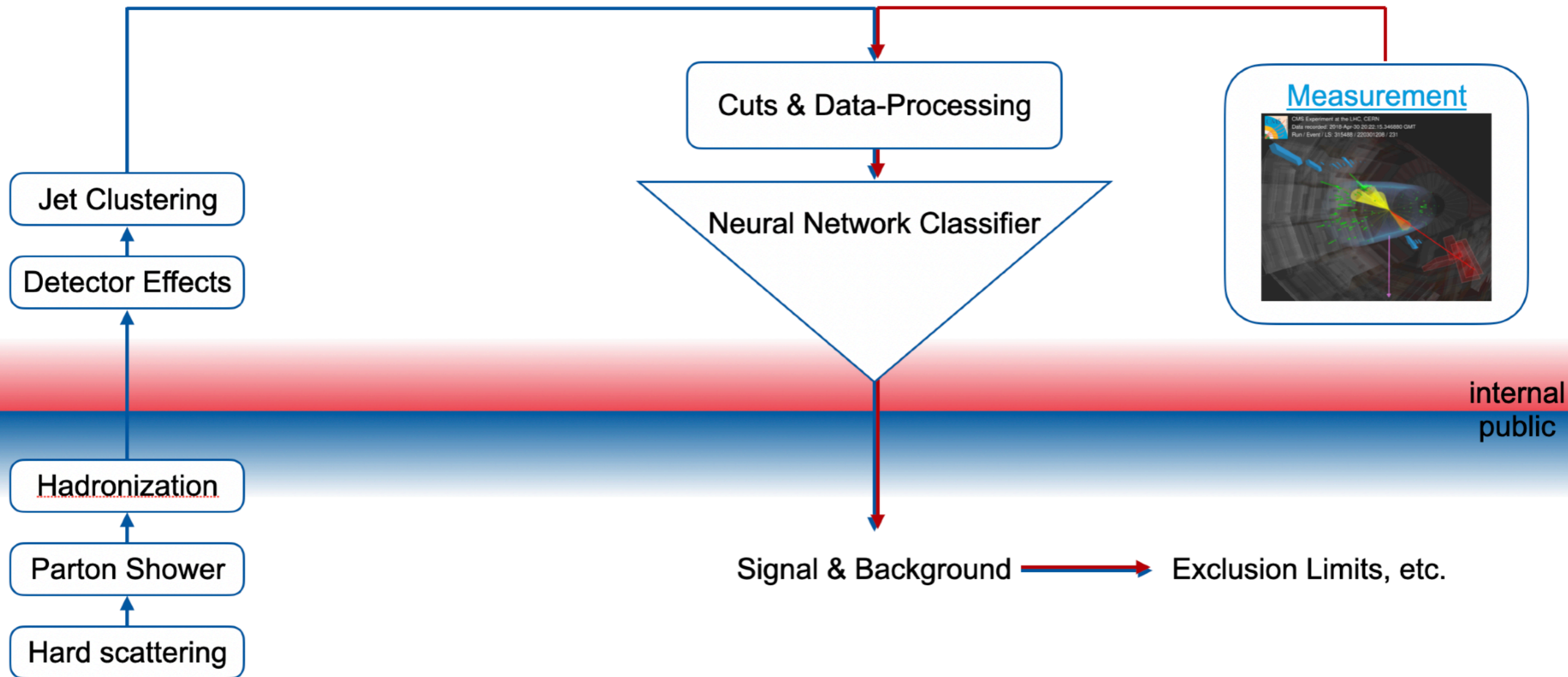
With the increasing usage of machine-learning in high-energy physics analyses, the publication of the trained models in a reusable form has become a crucial question for analysis preservation and reuse. The complexity of these models creates practical issues for both reporting them accurately and for ensuring the stability of their behaviours in different environments and over extended timescales. In this note we discuss the current state of affairs, highlighting specific practical issues and focusing on the most promising technical and strategic approaches to ensure trustworthy analysis-preservation. This material originated from discussions in the LHC Reinterpretation Forum and the 2023 PhysTeV workshop at Les Houches.

Keywords

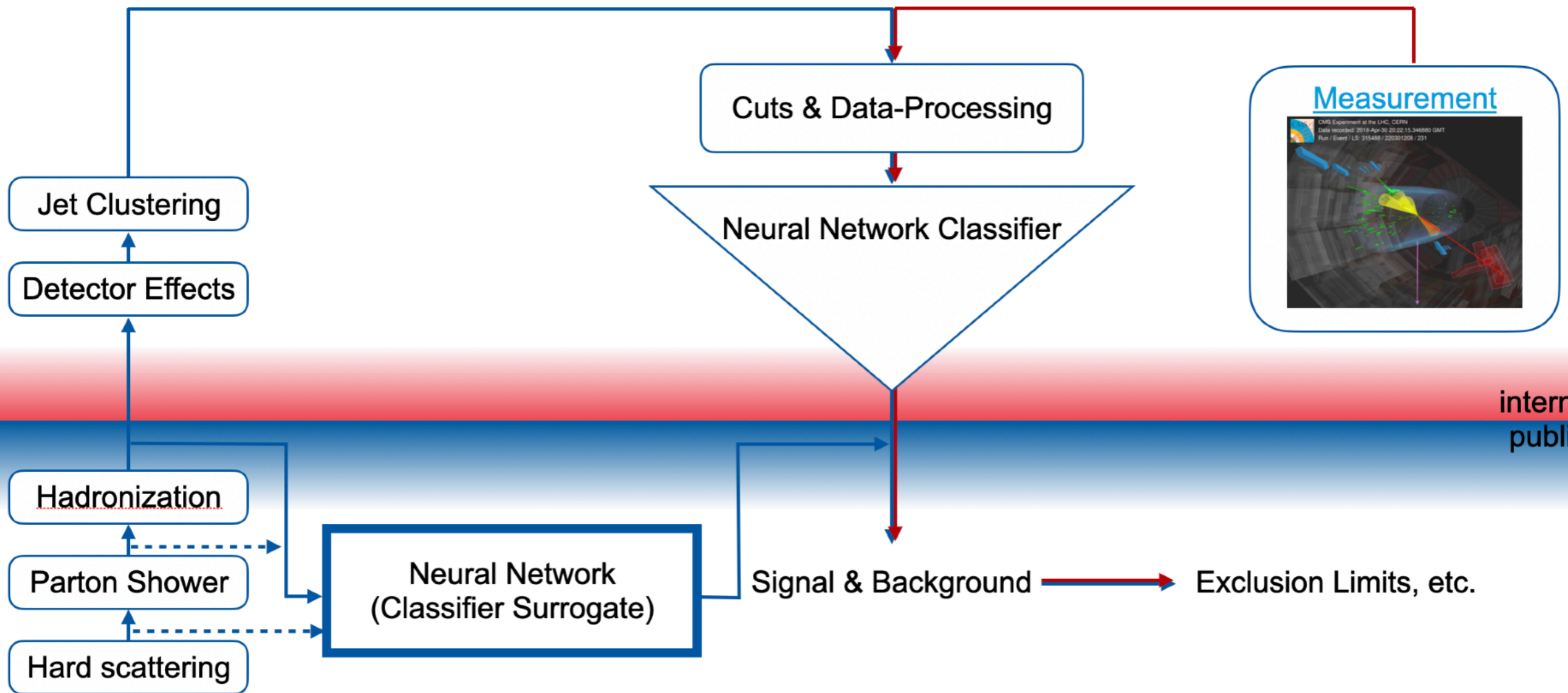
BSM; Tools; Machine-learning; Reinterpretation.

Guidelines for ML model exchange including suggestion of **surrogate models**

Classifier Surrogates

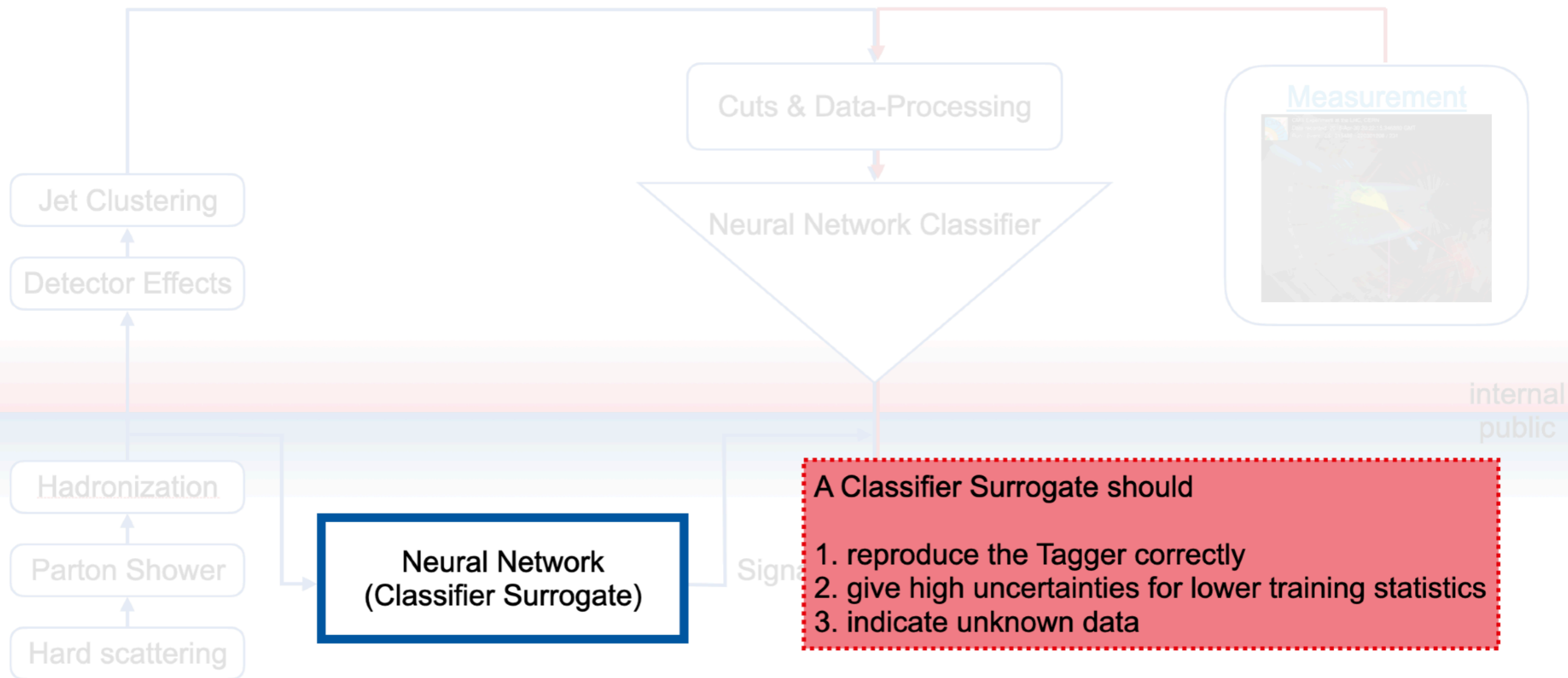


Classifier Surrogates

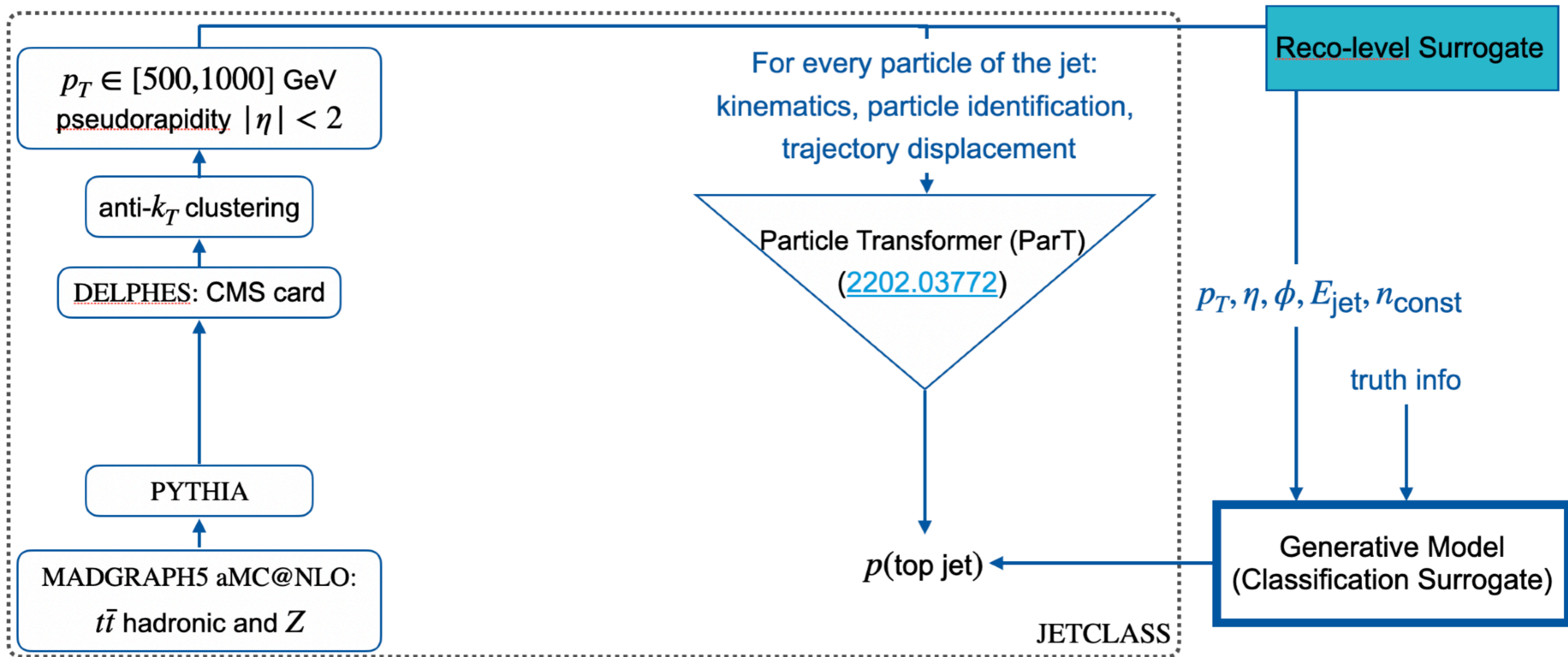


internal
public

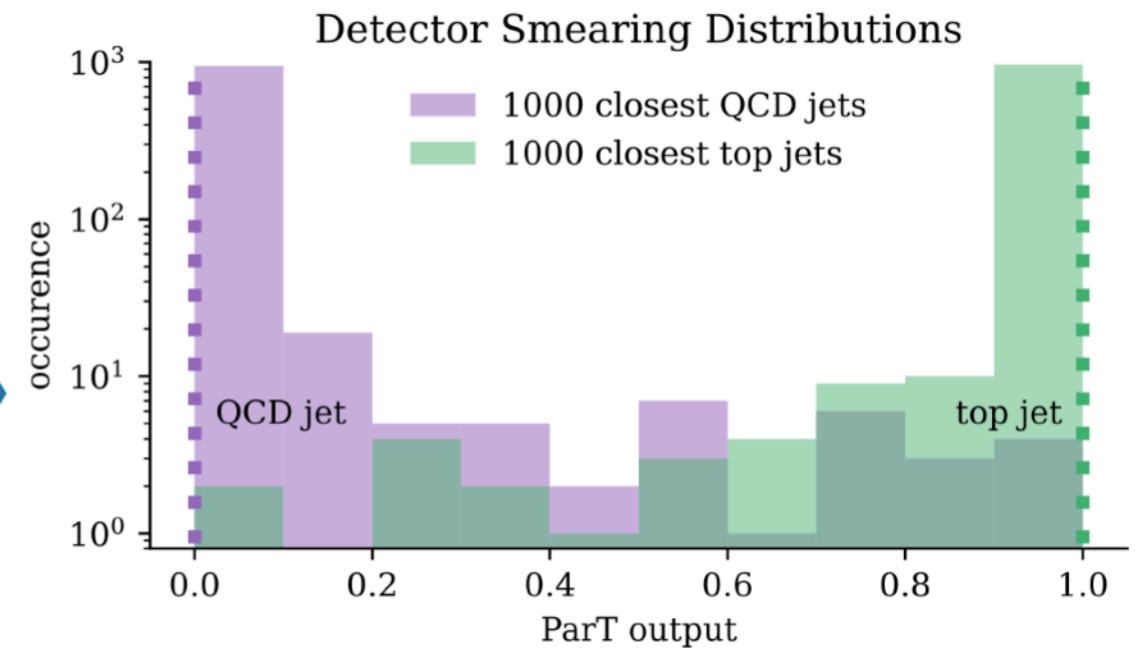
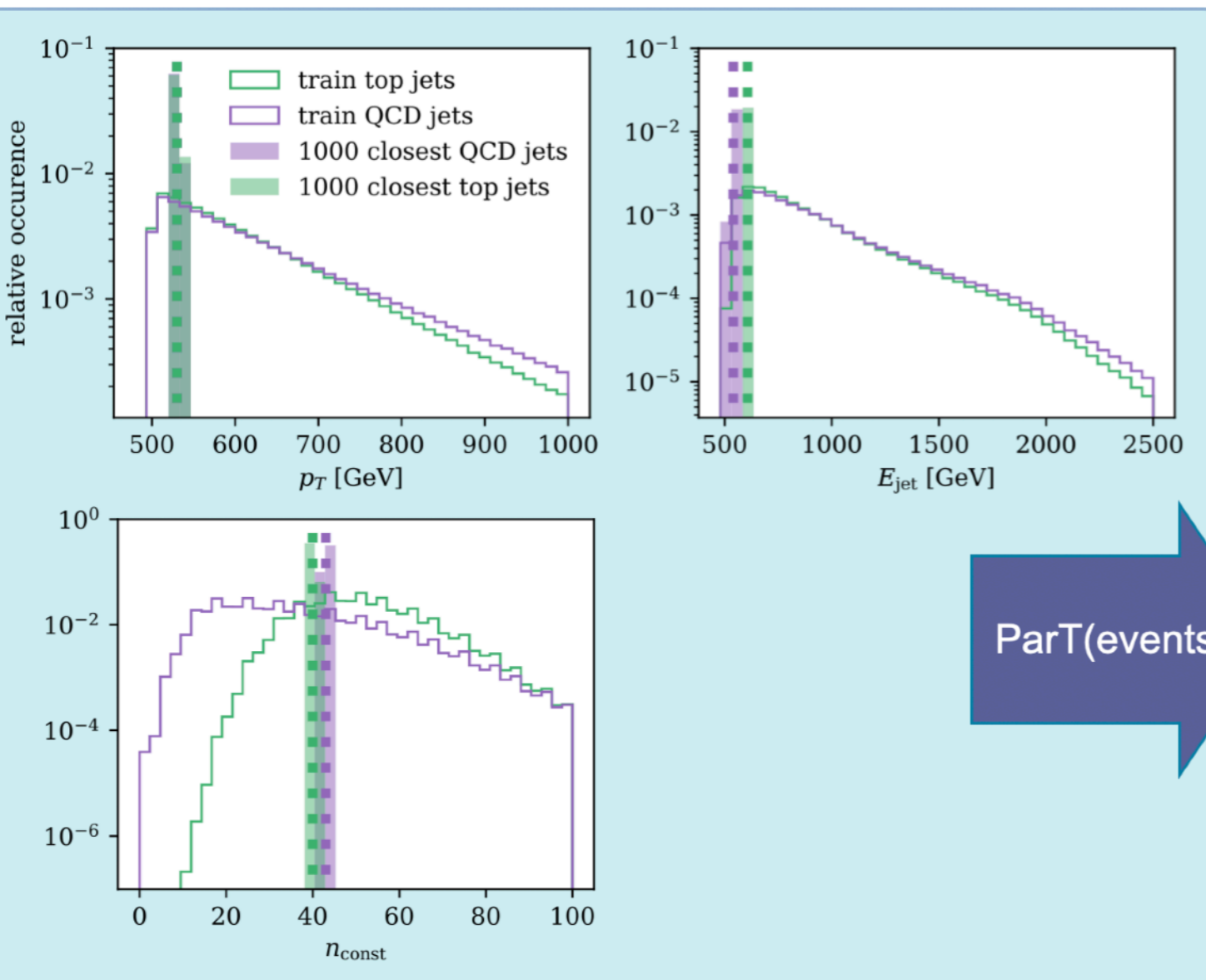
Classifier Surrogates



The Toy Setup



Detector Smearing Distribution



A Classifier Surrogate has to be a **Generative Model**

The Generative Model

Continuous Normalizing Flow:

- Flow $\phi : [0,1] \times \mathbb{R}^d \rightarrow \mathbb{R}^d$ defined via

$$\frac{d}{dt}\phi_t(x) = v_t(\phi_t(x)) = \tilde{v}_t(x, \theta)$$

- solve the ODE to train and sample
- linear trajectory
- transforms probability distributions

$$p_t(x) = p_0(\phi_t^{-1}(x)) \det \left[\frac{\partial \phi_t^{-1}}{\partial x}(x) \right]$$

Conditional Flow Matching:

- loss that does not ODE solving

$$\mathcal{L}_{\text{FM}}(\theta) = \mathbb{E}_{t, p_t(x)} \left\| v_t(x) - \tilde{v}_t(x, \theta) \right\|^2$$

- by choice of p_t and v_t

$$\mathcal{L}_{\text{CFM}}(\theta) = \mathbb{E}_{t, p_t(x), \epsilon} \left[\tilde{v}_t((1-t)x_0 + t\epsilon, \theta) - (\epsilon - x_0) \right]^2$$

- not a log-Likelihood loss

Variational Inference Bayesian Conditional Flow Matching:

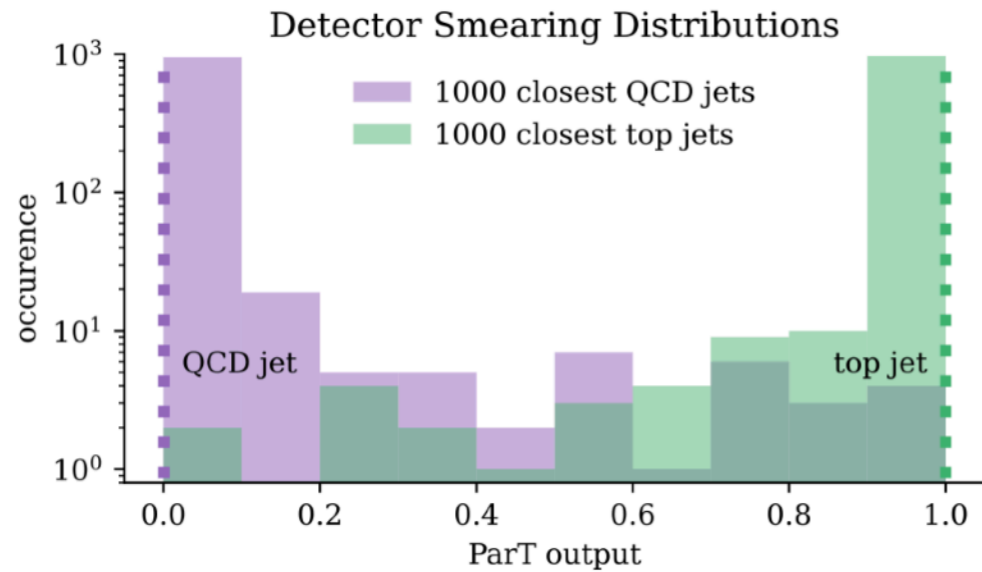
- Bayesian loss $\mathcal{L}_{\text{BNN}} = \text{KL} [q(\theta), p(\theta | x)] = - \int d\theta q(\theta) \log p(x | \theta) + \text{KL}[q(\theta), p(\theta)] + \text{const.}$

- connect both $\mathcal{L}_{\text{B-CFM}} = \langle \mathcal{L}_{\text{CFM}} \rangle_{\theta \sim q(\theta)} + c\text{KL}[q(\theta), p(\theta)]$, with $q(\theta)$ uncorrelated Gaussian shape

Adam-MCMC Bayesian Conditional Flow Matching:

- train the network with CFM
- start Markov Chain from this point (independent of starting point):
 - 1D problem: Solve ODE to get log-Likelihood of batch for update steps and acceptance rates

Is the Classifier reproduced correctly?

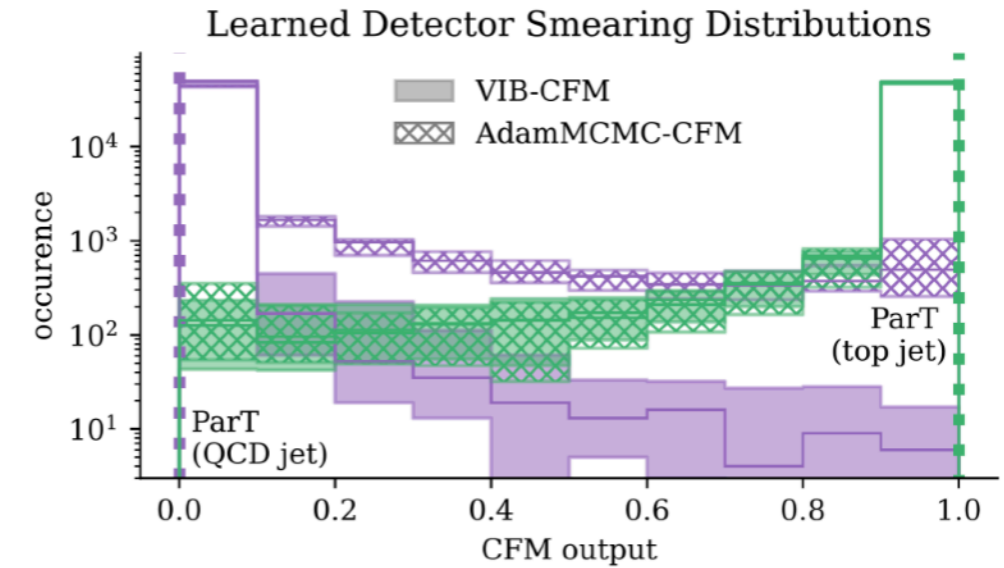


$p_T, \eta, \phi, E_{\text{jet}}, n_{\text{const}}$

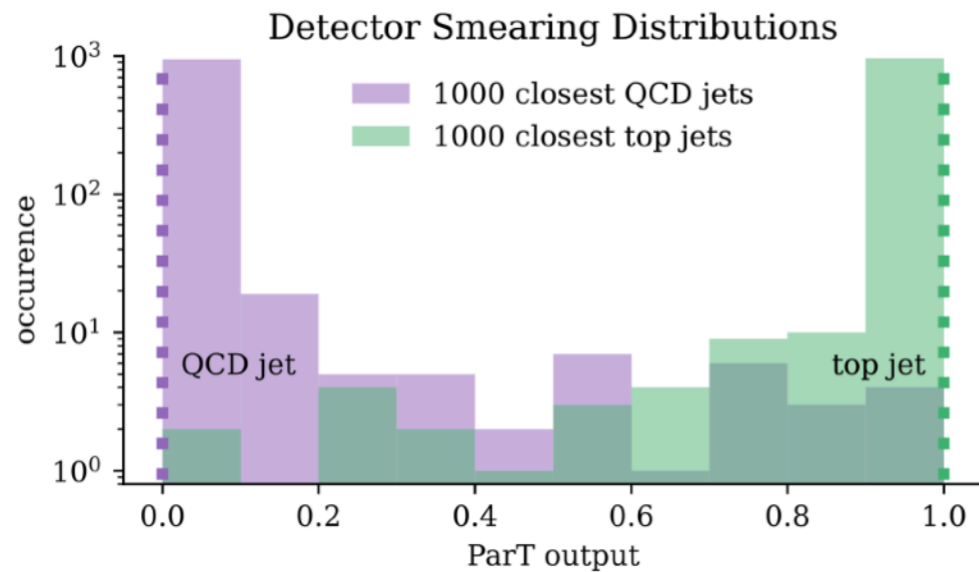
truth info

Conditional Flow Matching (CFM) + Bayesian

$z \propto \mathcal{N}(0,1) \times 50000$



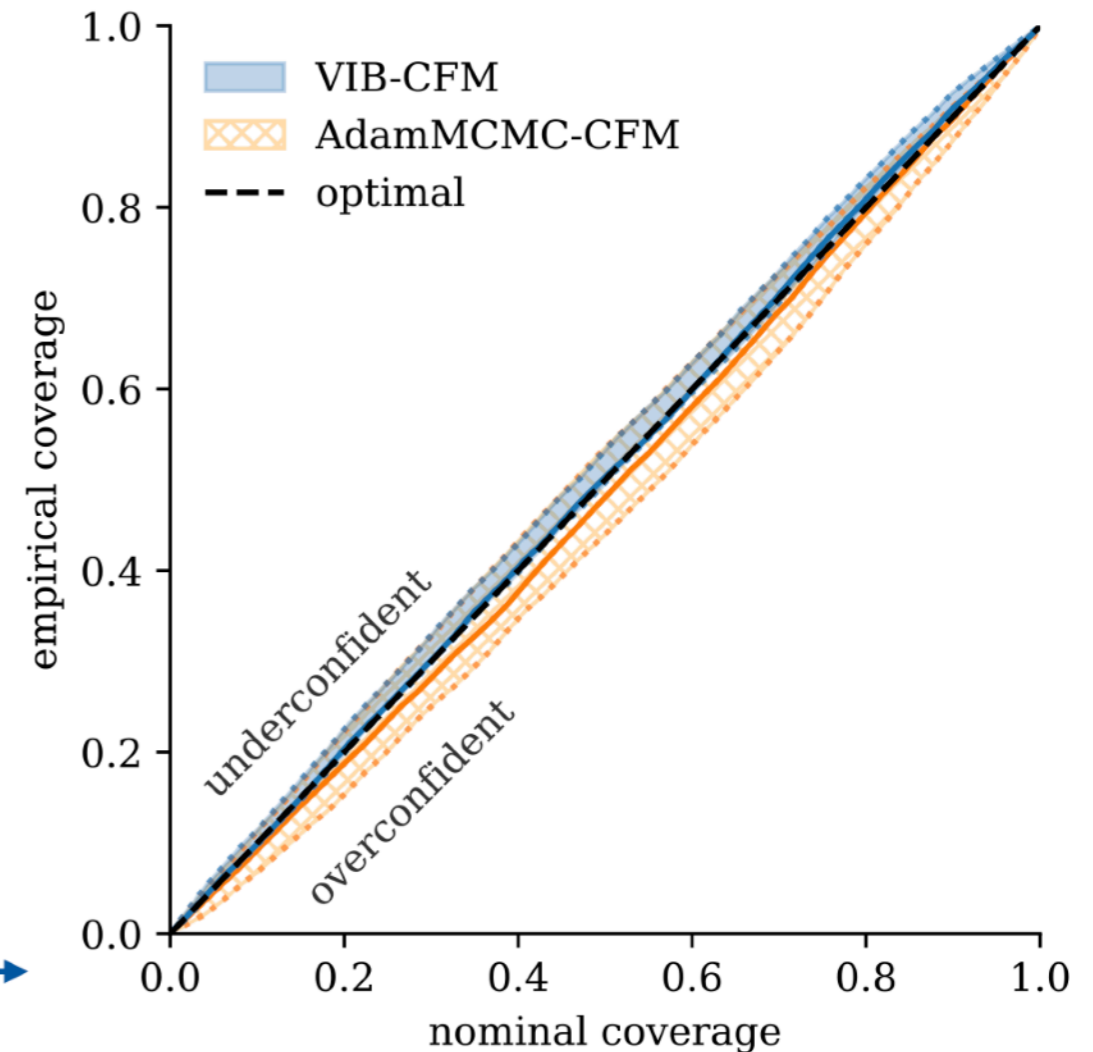
Is the Classifier reproduced correctly?



$10000 \times \{p_T, \eta, \phi, E_{\text{jet}}, n_{\text{const}}\}$

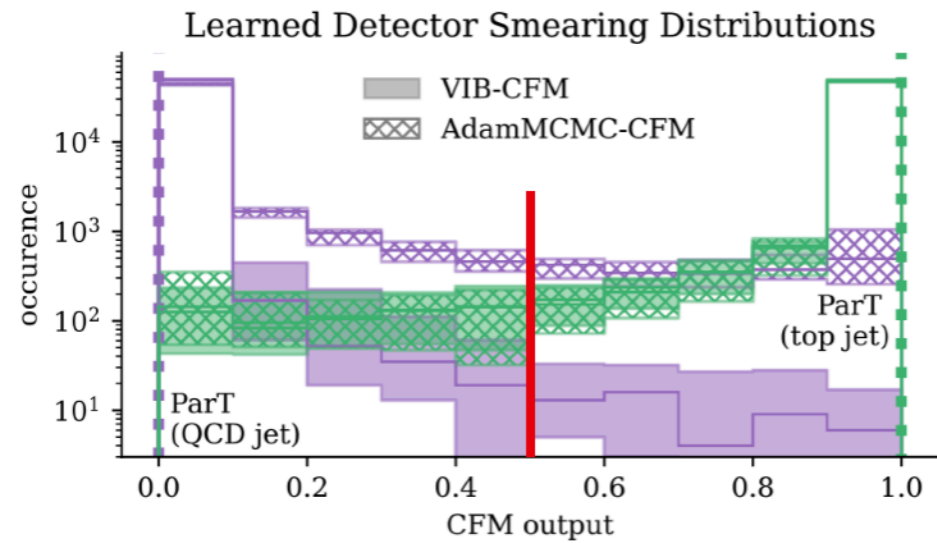
truth info

Conditional Flow Matching (CFM) + Bayesian



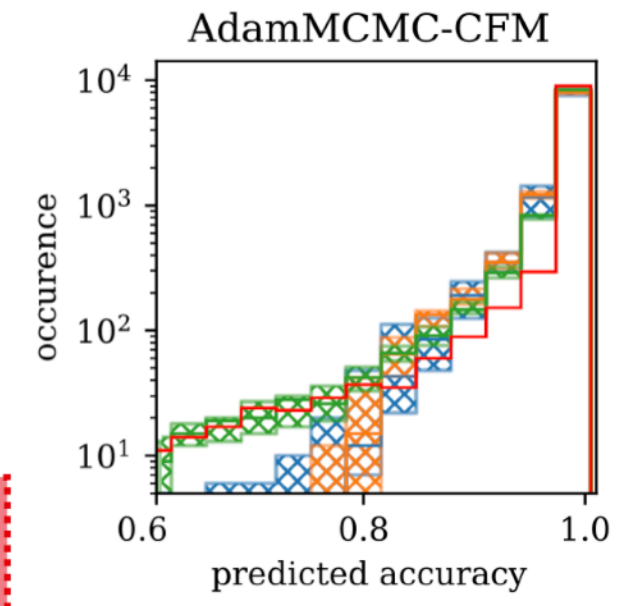
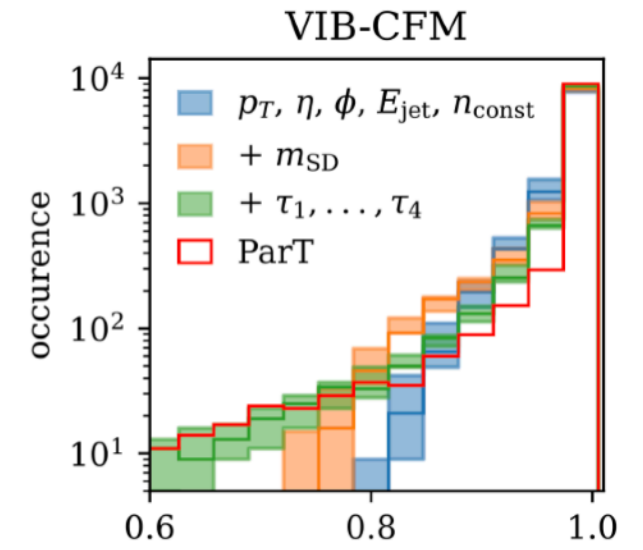
Both architectures deliver well calibrated Surrogates

Is the Classifier reproduced correctly?



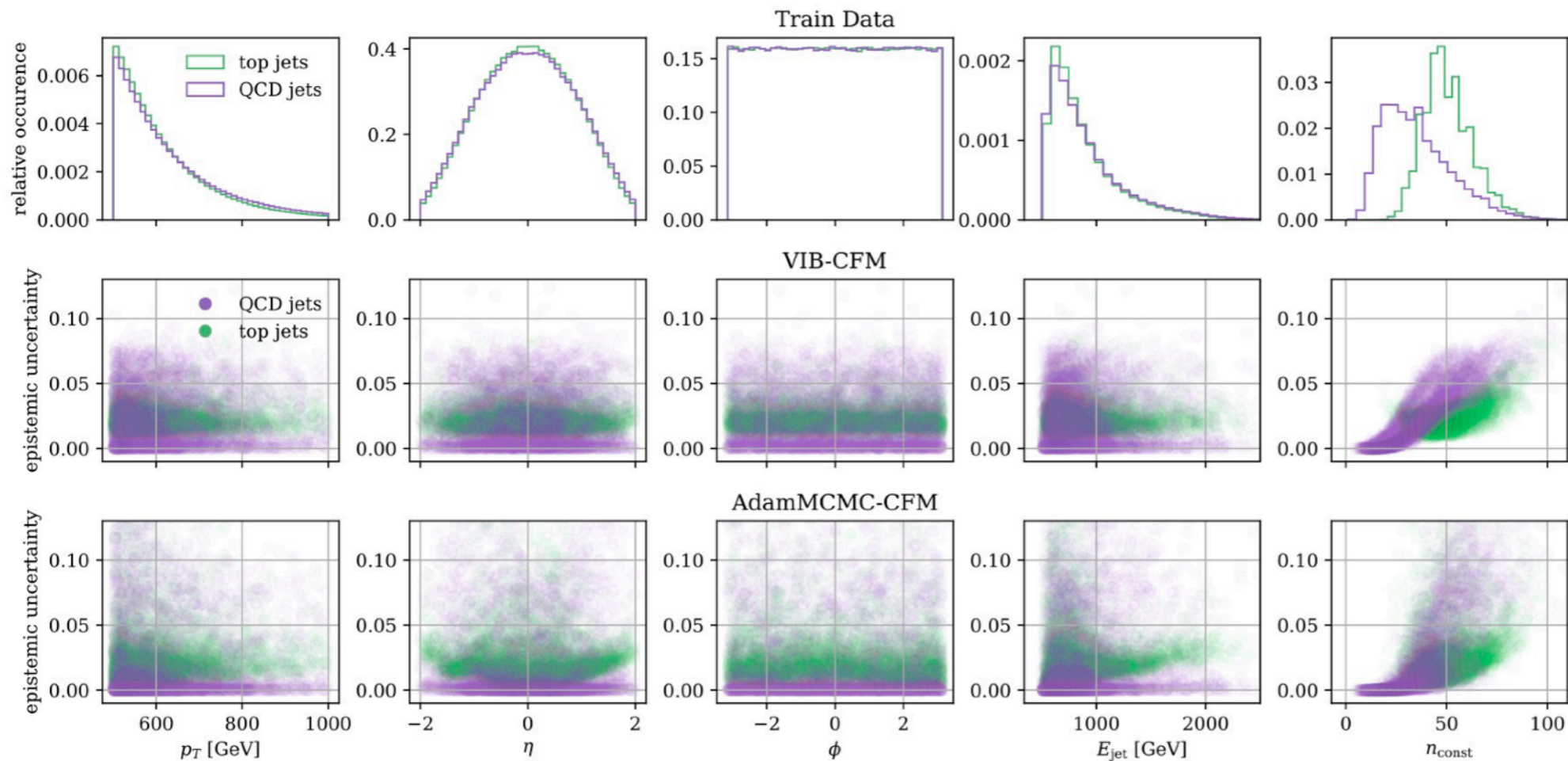
accuracy =

$$\frac{1}{1000} \sum_{i=0}^{1000} \left(\mathbf{1}_{[0.5,1]}(\phi_{0,\theta}(x_i)) \mathbf{1}(\text{top jet}) + \mathbf{1}_{[0,0.5)}(\phi_{0,\theta}(x_i)) \mathbf{1}(\text{QCD jet}) \right)$$



Quality of the Surrogate depends on input information

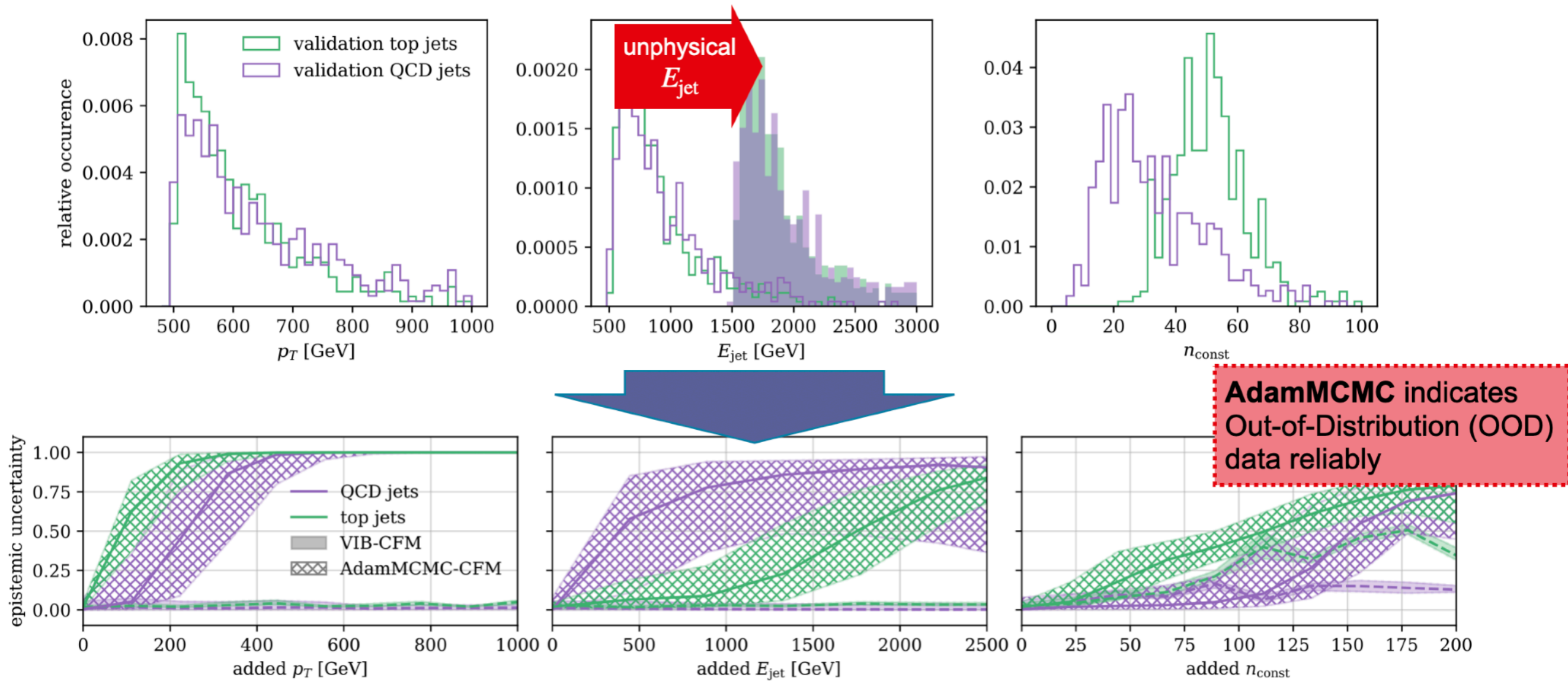
Are high uncertainties produced for lower training statistic?



Uncertainties scale towards edges of train distribution

$$\text{epistemic uncertainty} = \frac{1}{n_{\text{stat}}} \sum_{i=0}^{n_{\text{stat}}} \left(\max_{\theta} \phi_{0,\theta}(x_i) - \min_{\theta} \phi_{0,\theta}(x_i) \right)$$

Is OOD data indicated?



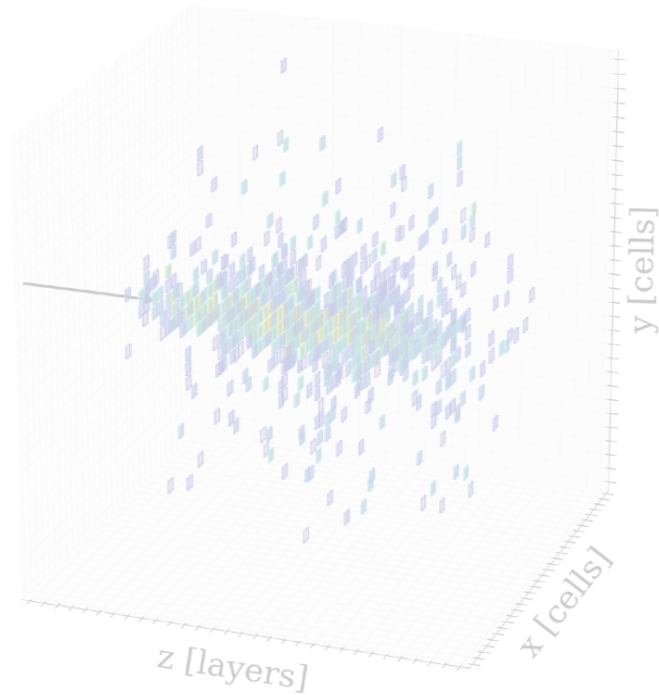
Comments

A Bayesian - Conditional Flow Matching Surrogate can

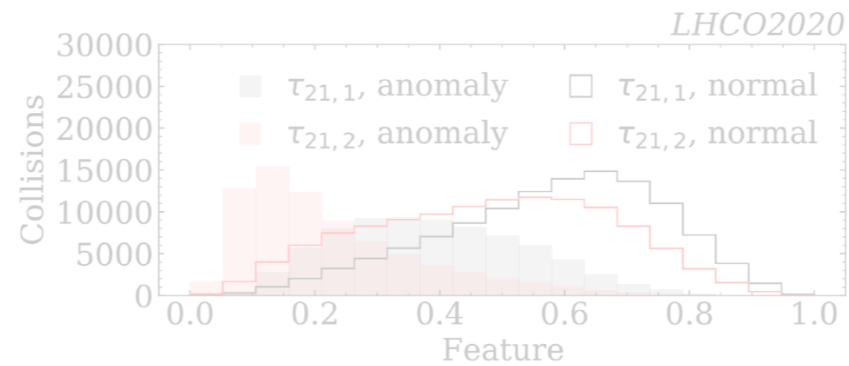
- ✓ learn Tagger output well calibrated and to high accuracy
- ✓ indicate data sparse areas
- ✓ report high uncertainties for unknown input if sampled with MCMC

Paper is coming soon!

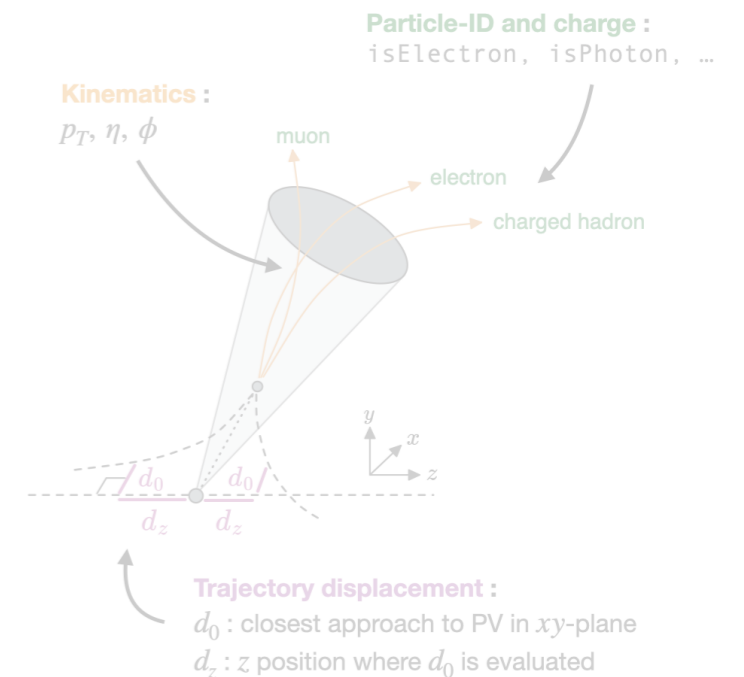
Why generative models?



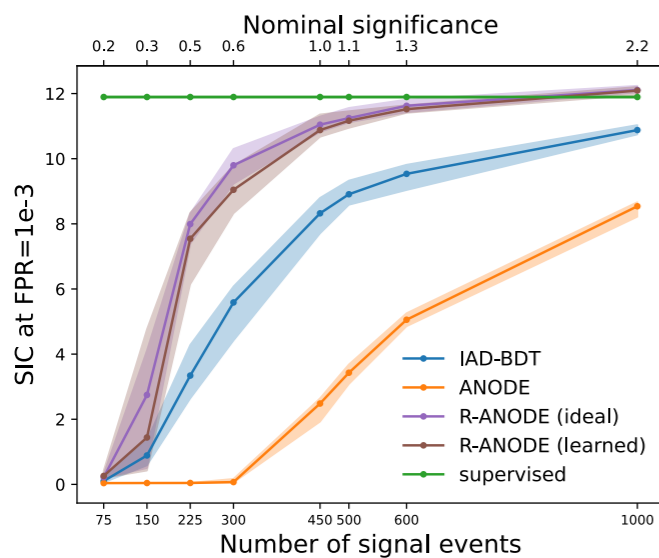
Showers in complex high-resolution calorimeters



High-level jet features



Jet constituents

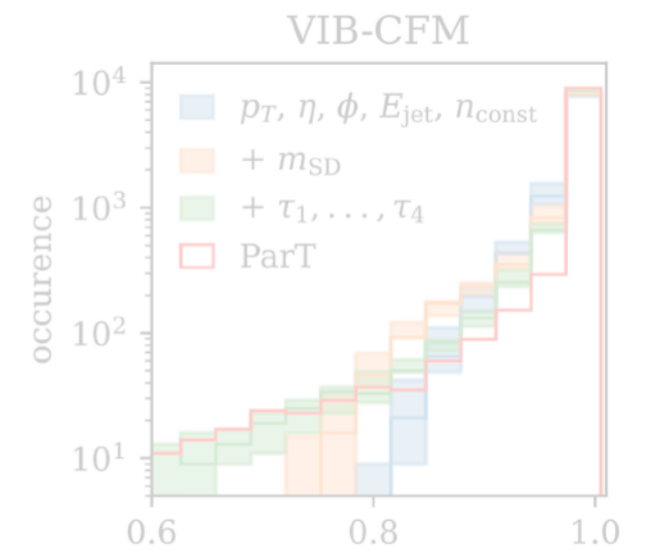


Detect anomalies

$$p(x)$$

Sample $X_i \sim p(x)$
to generate datapoints

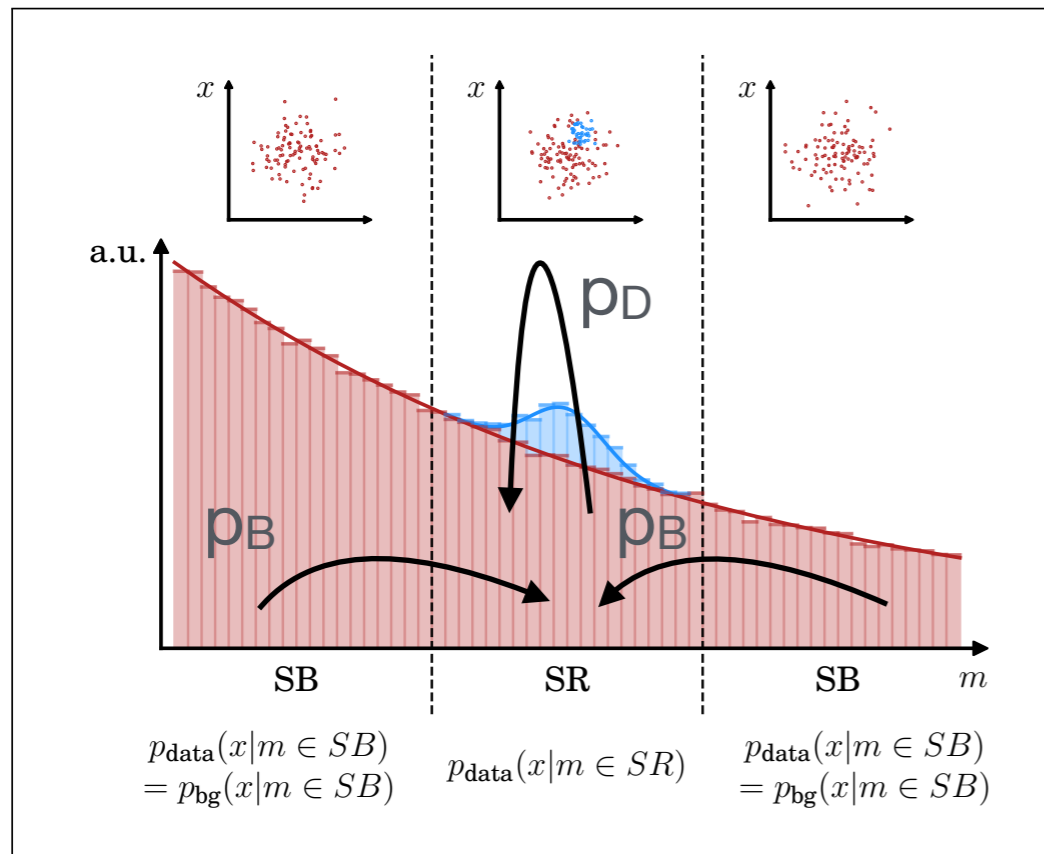
Evaluate $p(x)$ directly as
likelihood



Classifier surrogates

ANODE

Before CATHODE,
there was ANODE



ANODE:

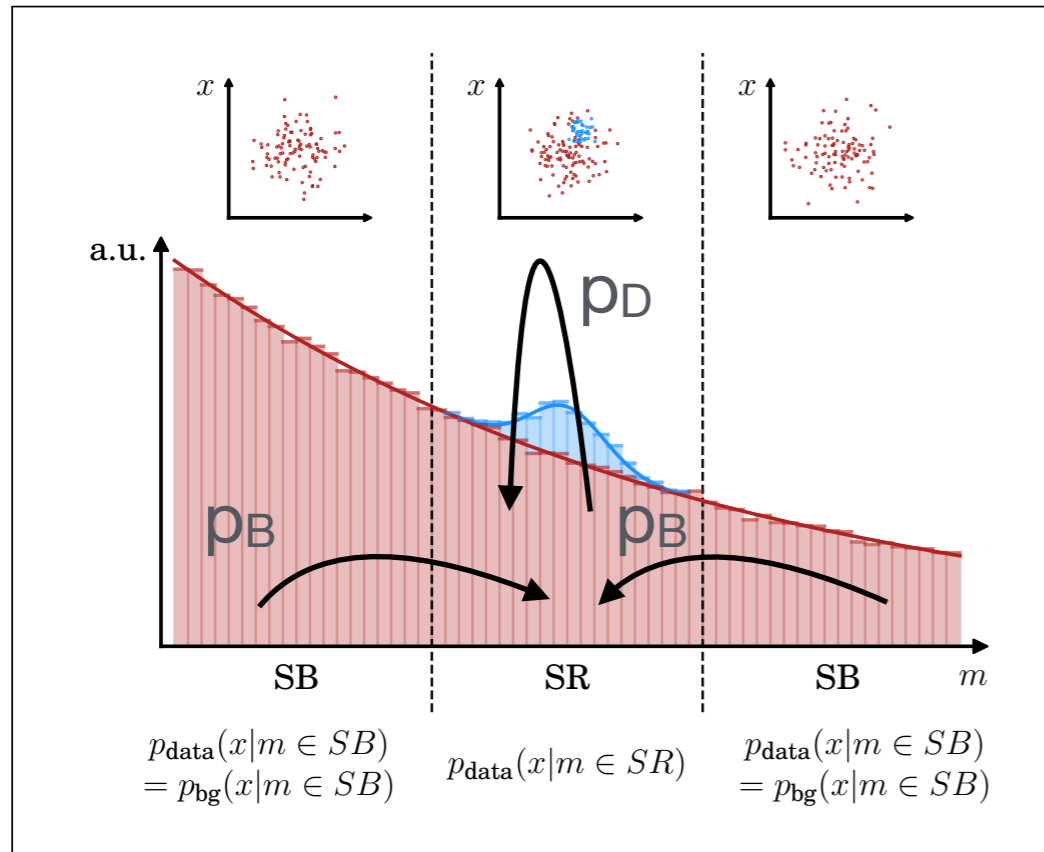
Train and interpolate
background flow p_B
(as in CATHODE)

Train signal-region flow p_D

Anomaly score = p_D/p_B

ANODE

Before CATHODE,
there was ANODE

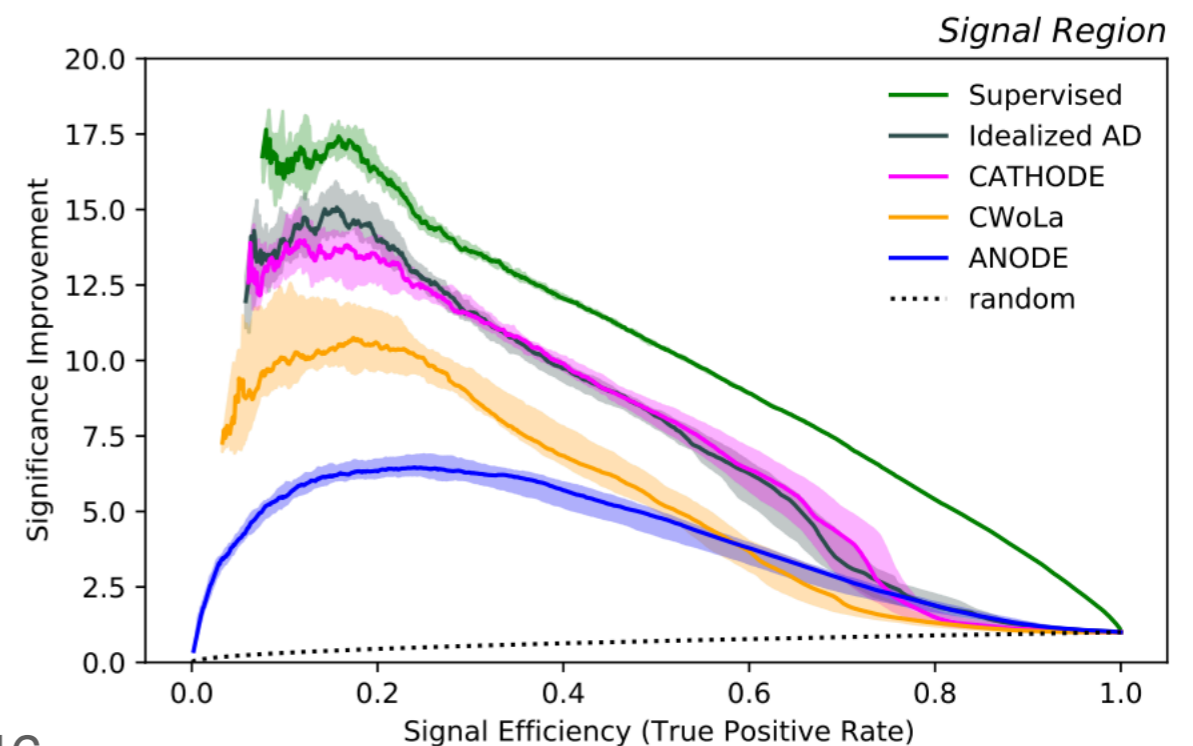


ANODE:
Train and interpolate
background flow p_B
(as in CATHODE)

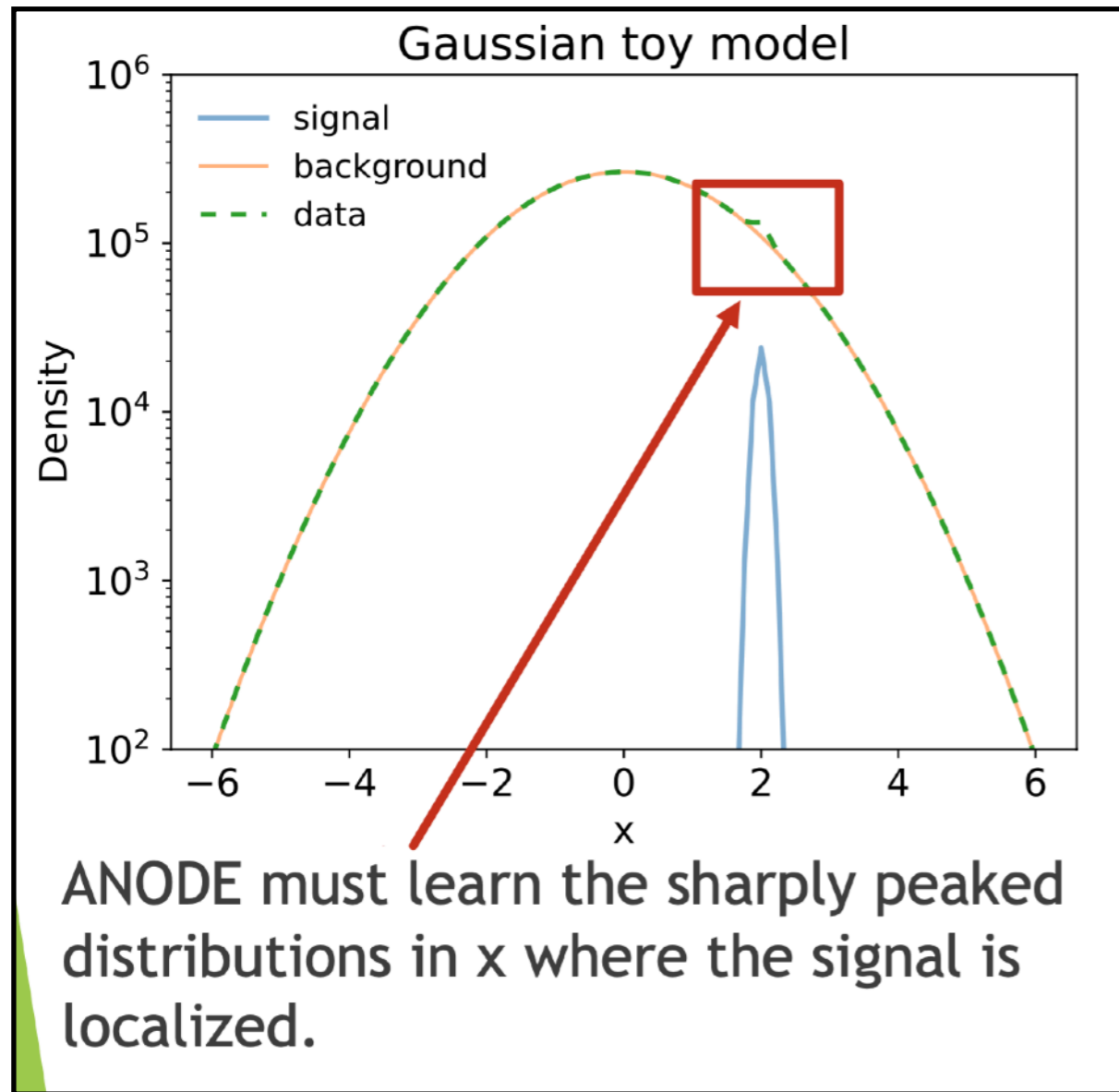
Train signal-region flow p_D

Anomaly score = p_D/p_B

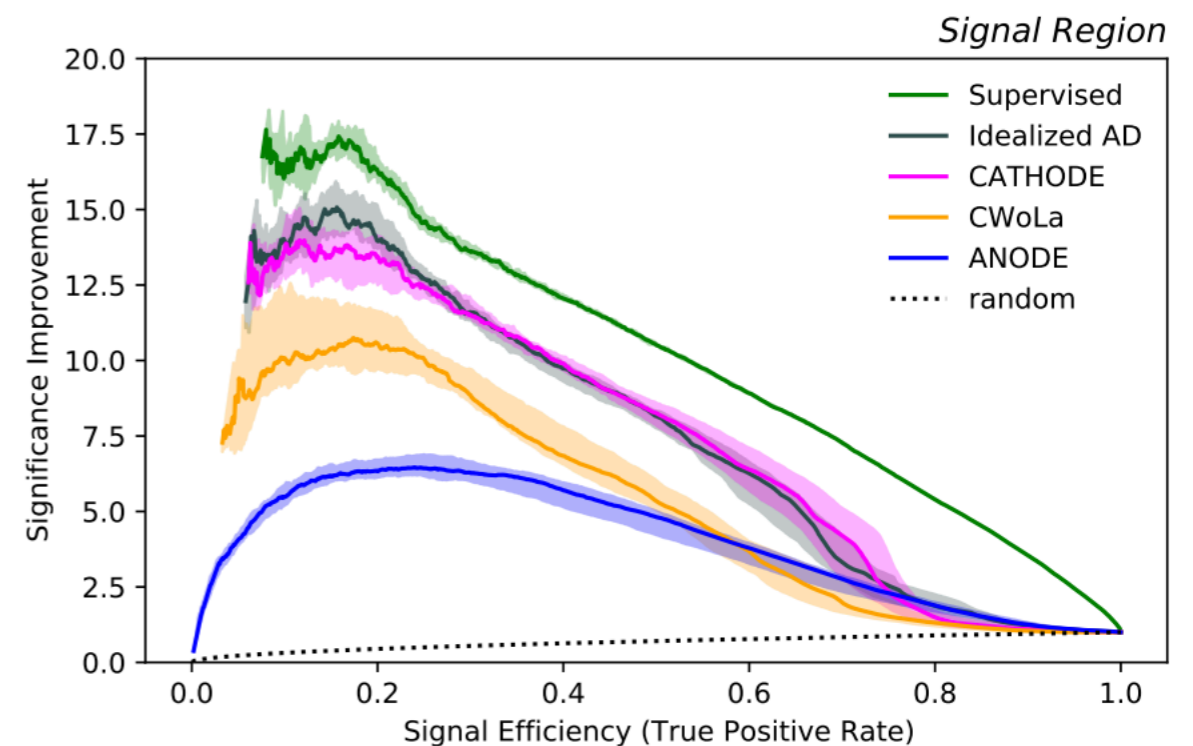
Original ANODE:
Worse than CATHODE



ANODE



Original ANODE:
Worse than CATHODE



Residual ANODE

R-ANODE:

Train and interpolate
background flow p_B

(as in ANODE, CATHODE)

Train signal contribution
flow using background

(Assumed) Fraction of signal in signal region

$$p_{\text{data}}(x, m) = w p_{\text{sig}}(x, m) + (1 - w) p_{\text{bg}}(x, m)$$

Learn in signal
region via

Interpolated
background
density

$$L = -\mathbb{E}_{x, m \sim \text{SR data}} \log p_{\text{data}}(x, m)$$

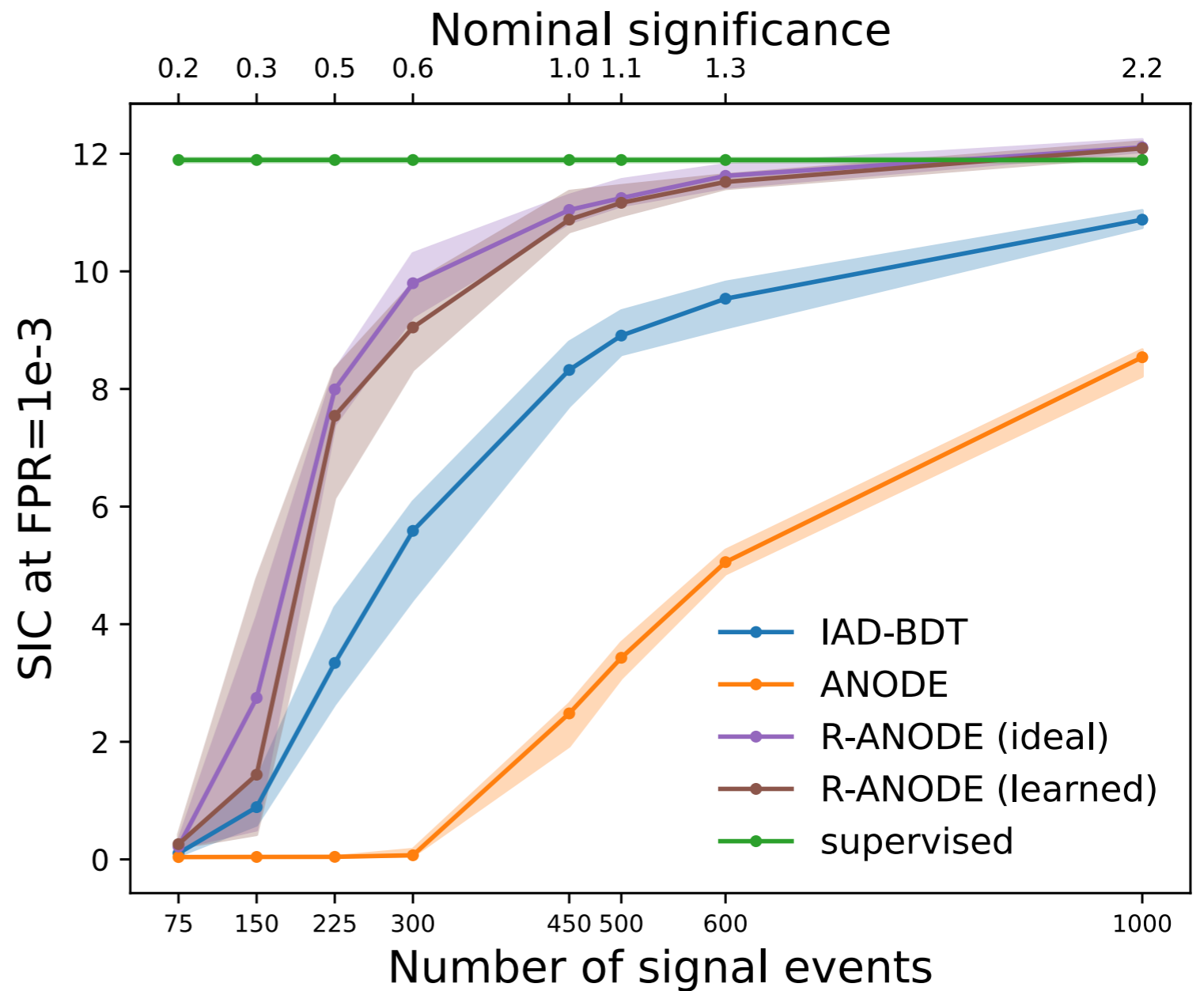
Anomaly score

$$R(x, m) = \frac{p_{\text{sig}}(x, m)}{p_{\text{bg}}(x, m)}$$

R-ANODE

R-ANODE **outperforms**
idealised anomaly detector
(upper limit of CATHODE)

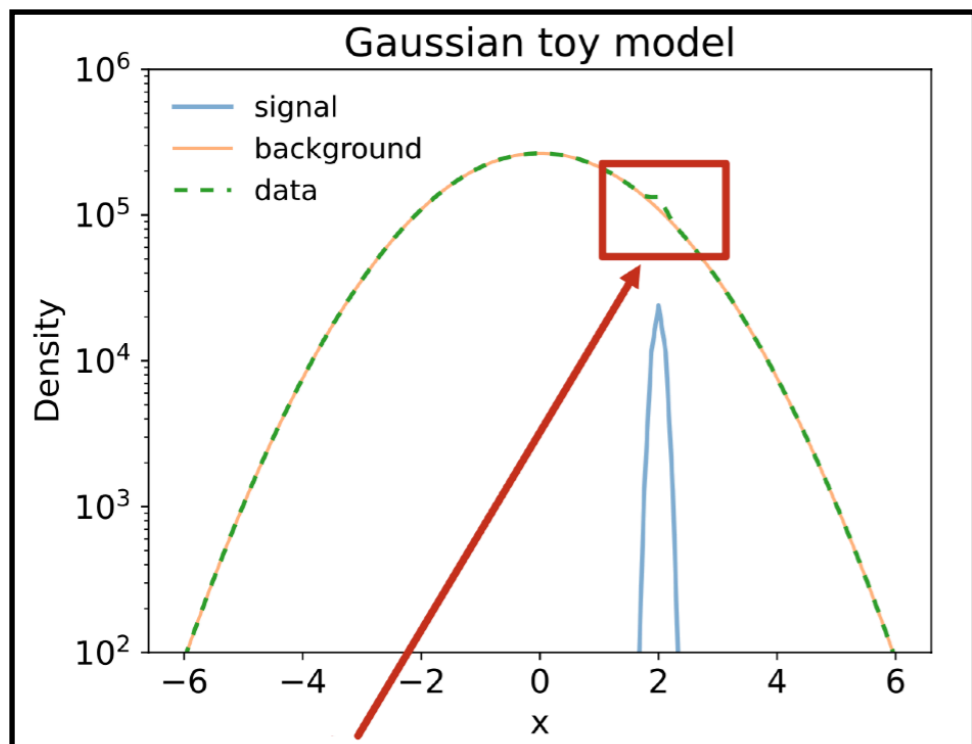
Work both with assuming
known w , **and without**



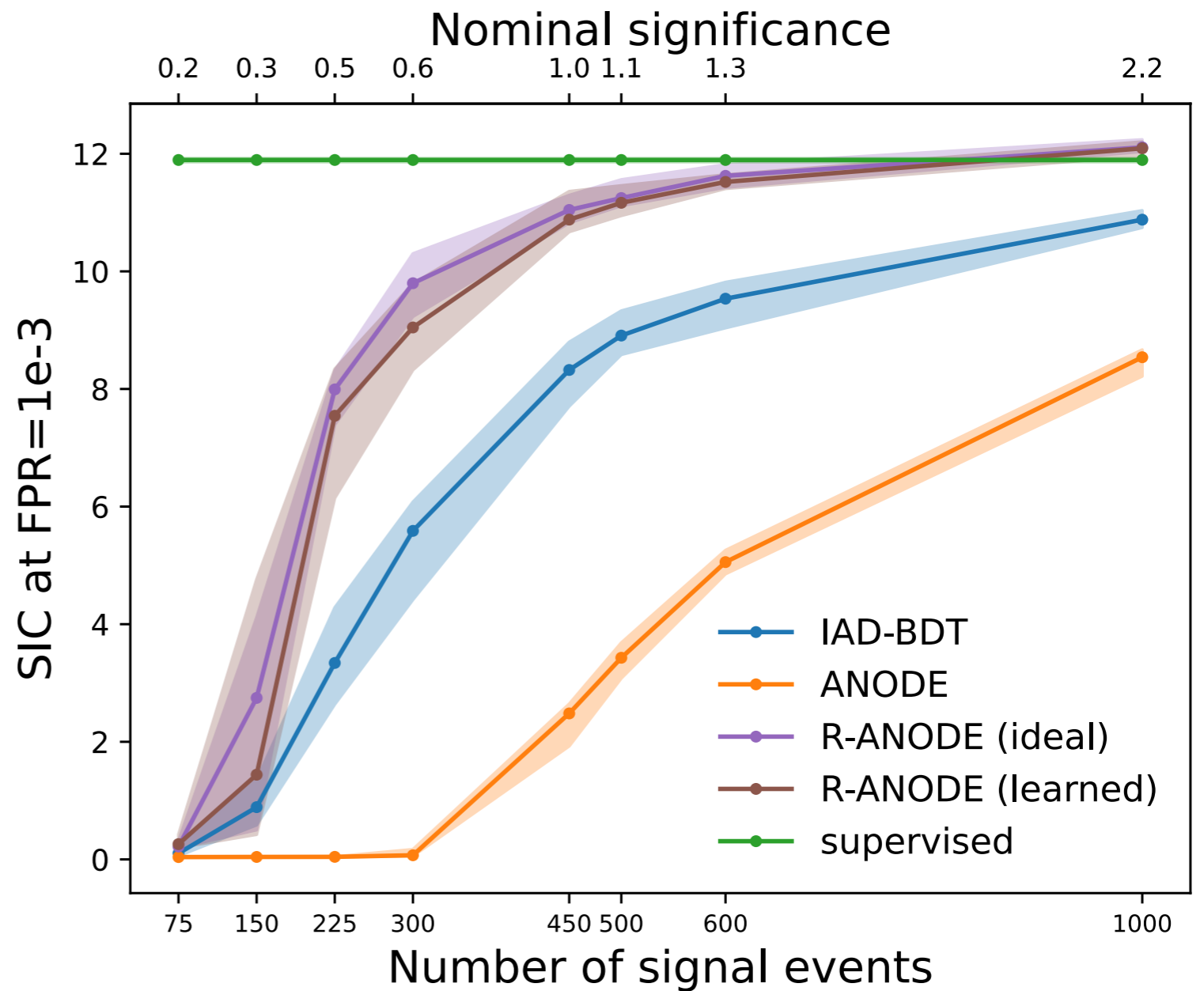
R-ANODE

R-ANODE **outperforms** **idealised** anomaly detector (upper limit of CATHODE)

Work both with assuming known w , **and without**



Why? Assume fixed background, just need to **fit extra peak**

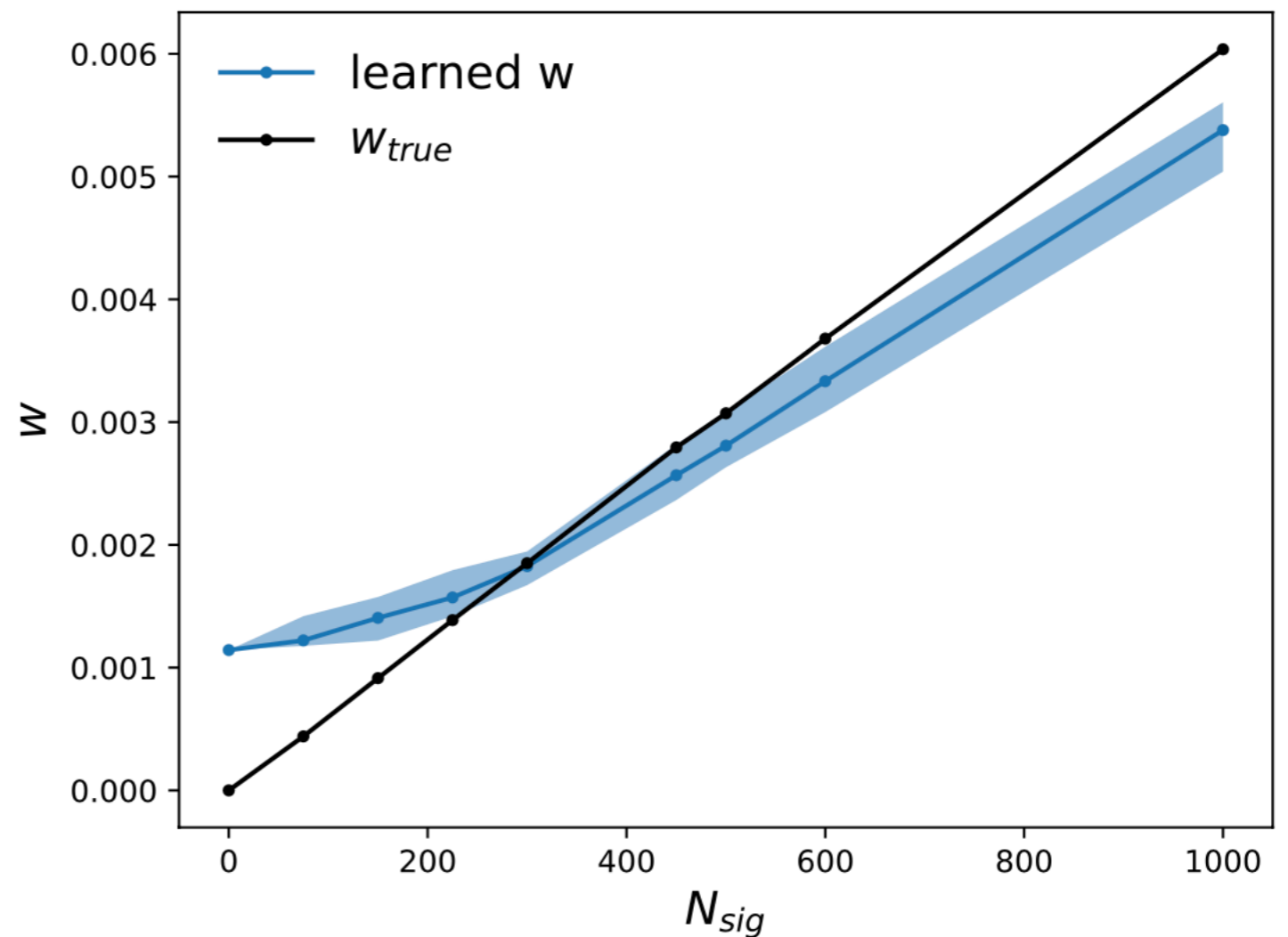


R-ANODE

R-ANODE outperforms idealised anomaly detector (upper limit of CATHODE)

Work both with assuming known w , and without

How good is the learned w ?



Selection bias at low w , otherwise good.

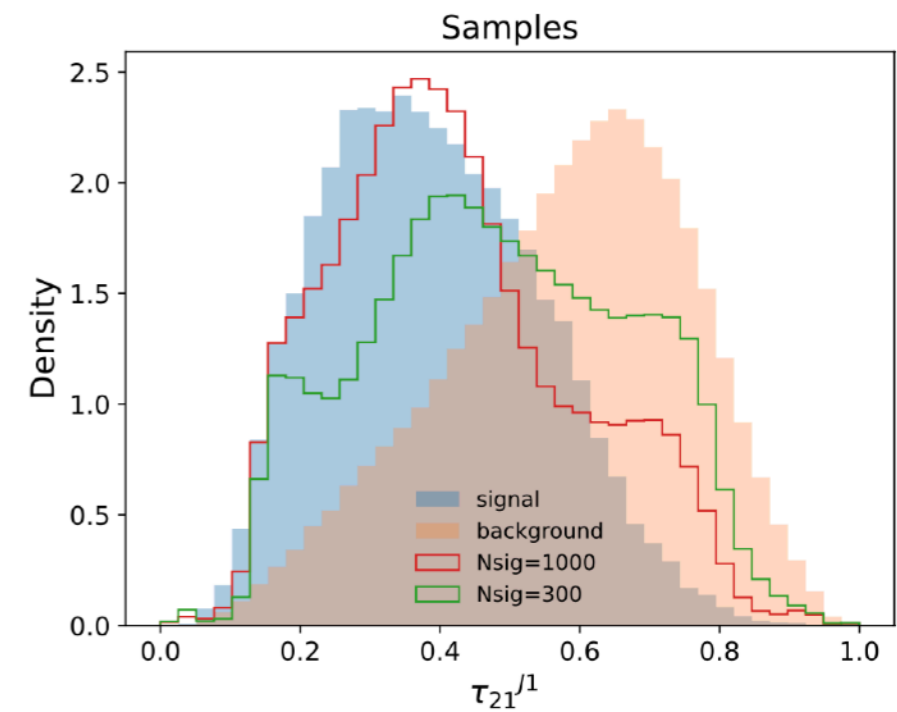
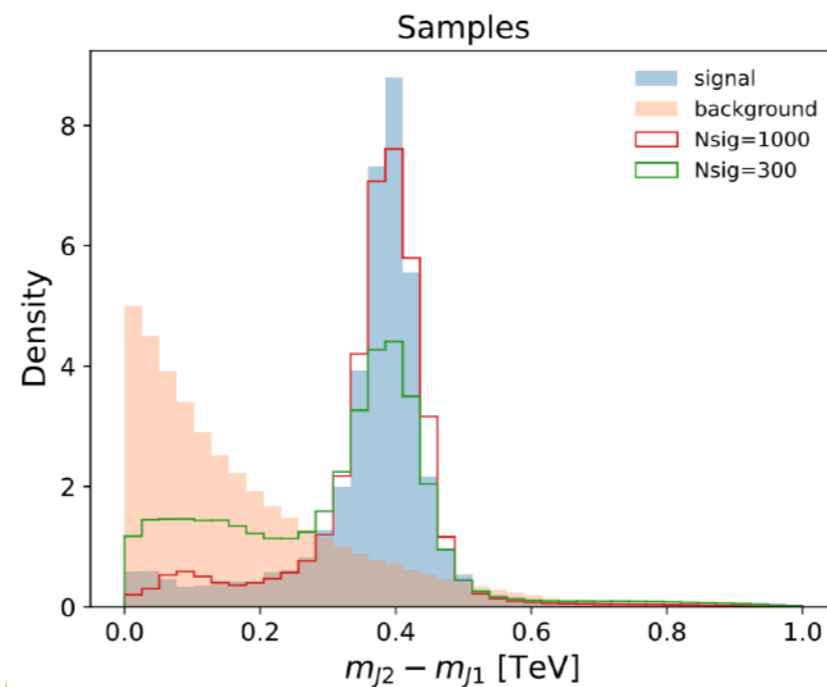
R-ANODE

R-ANODE outperforms idealised anomaly detector (upper limit of CATHODE)

Work both with assuming known w , and without

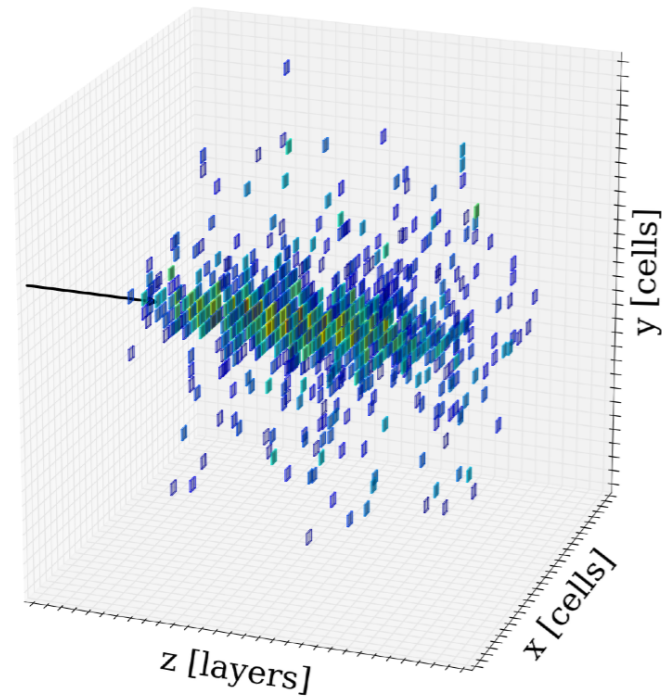
How good is the learned w ?

Can we interpret p_{sig} ?

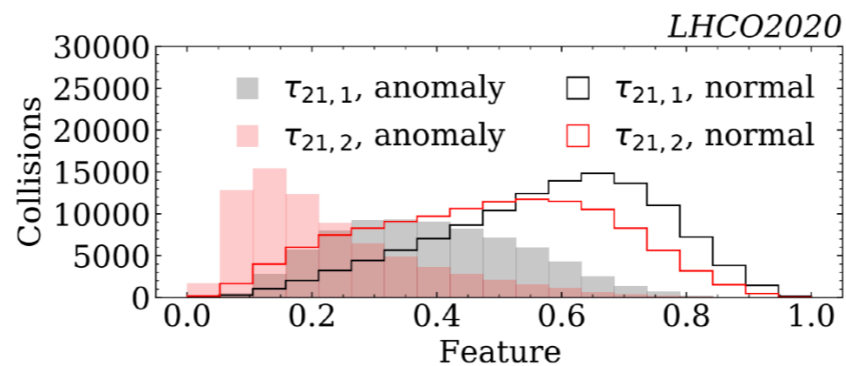


Yes!

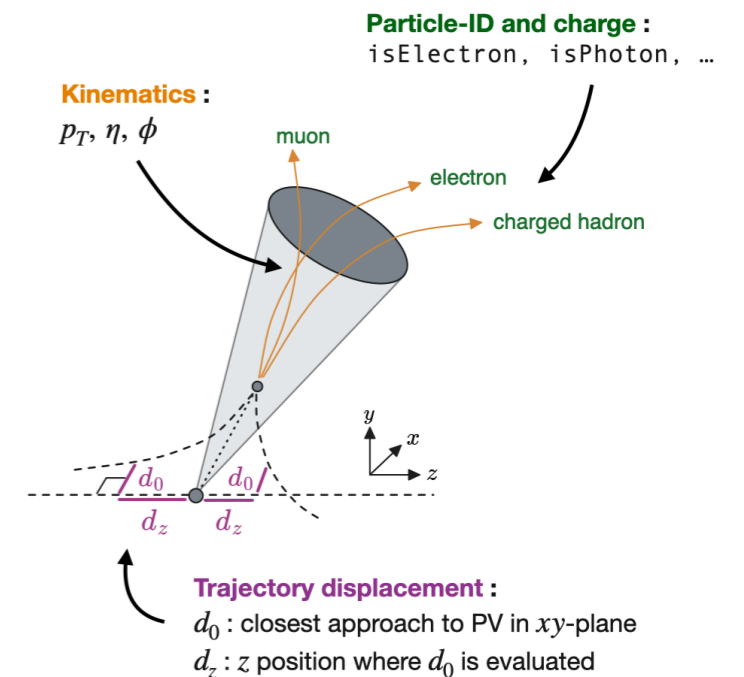
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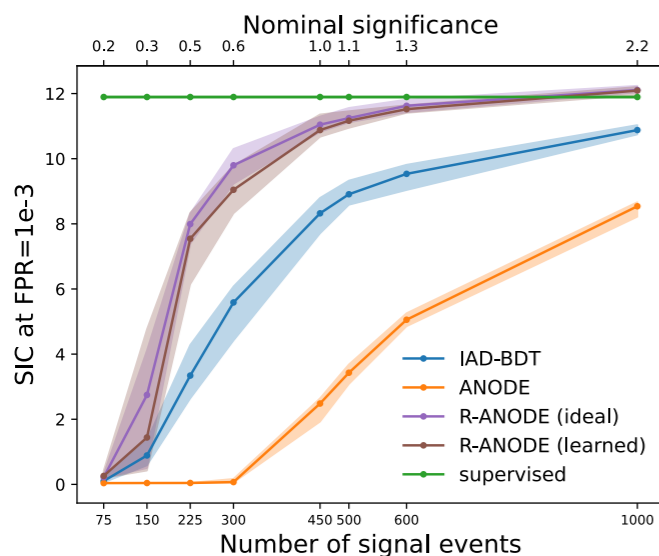
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High-level jet features



Jet constituents

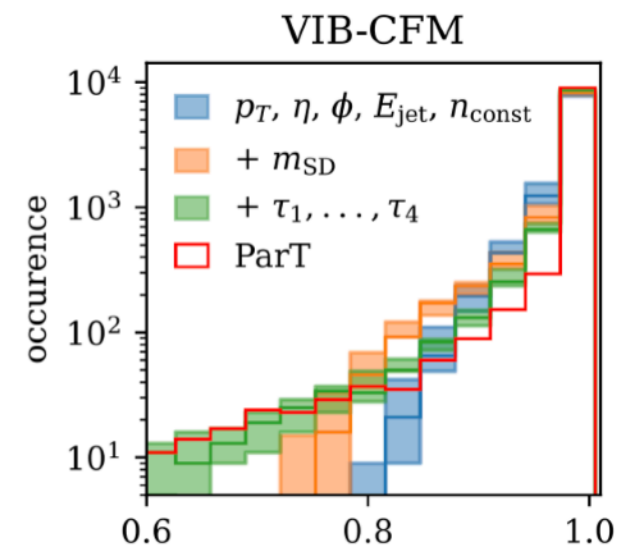


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Sample $X_i \sim p(x)$ to generate datapoints

Evaluate $p(x)$ directly as **likelihood**



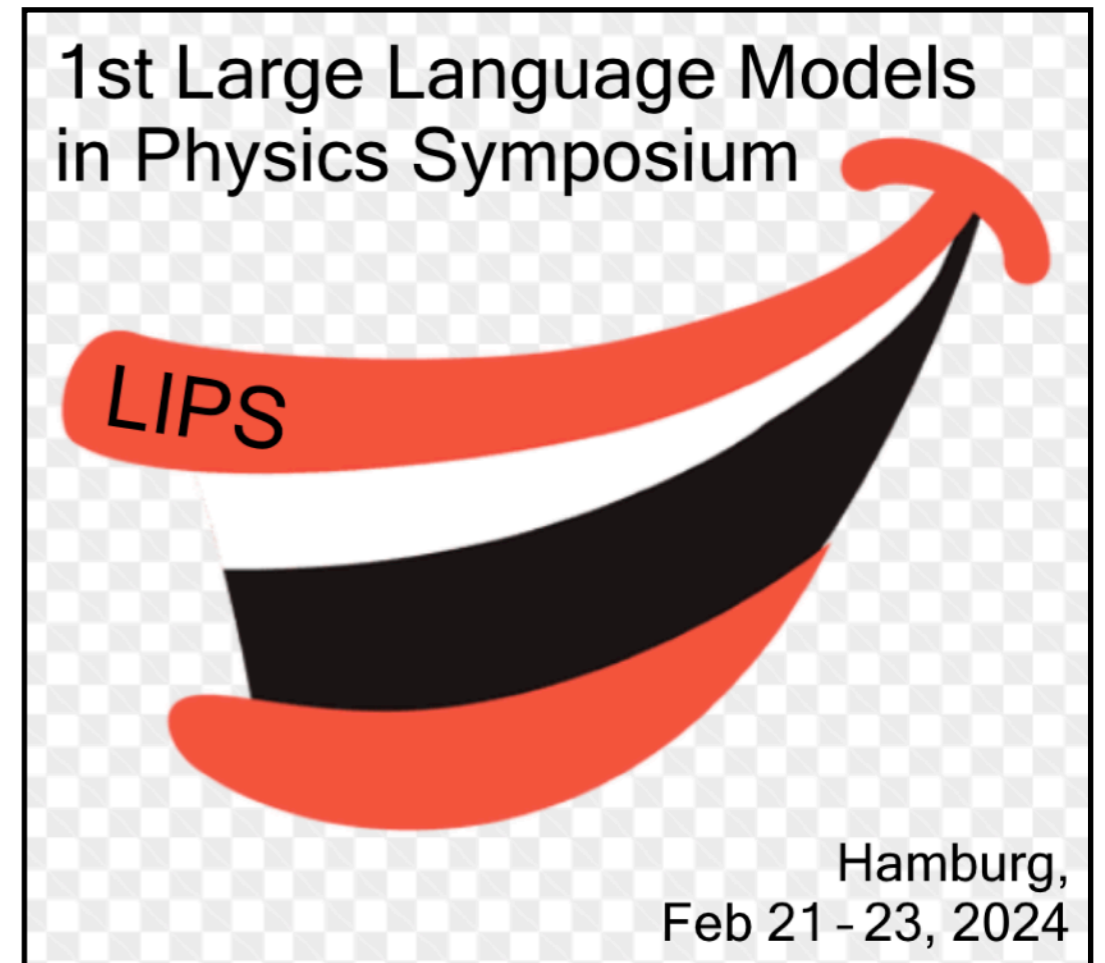
Classifier surrogates

Conclusions

Generative models have **wide range of applications** for simulation, background, estimation and as other surrogates

Recent progress (**diffusion/flow matching + point clouds**) allow modelling many high dimensional distributions

Models with **tractable likelihood** (i.e. normalising flow) enable further new applications



<https://indico.desy.de/event/38849/>

Thank you!