

Fast Generation of High Dimensional Point Clouds

Generative models for particle showers

Motivation: Computing Challenge

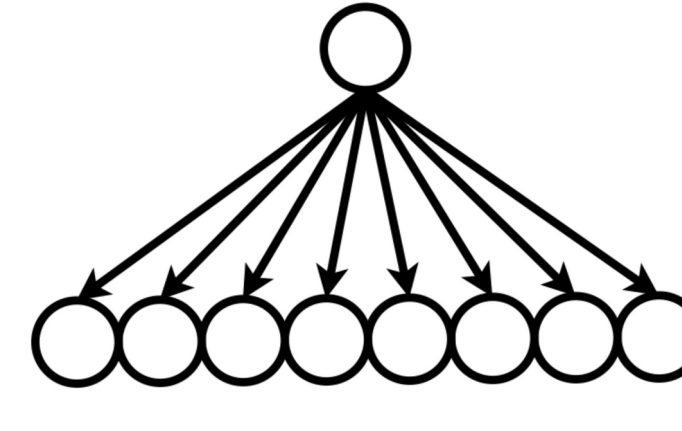
- Particle physics: simulate detector response and physical processes to test theories
→ Immense computational effort
- LHC High-Luminosity phase → More particles to simulate
- Future CMS high granularity calorimeter (HGCal): more than 6M channels
→ Time-consuming simulations
→ Projected compute budget insufficient
⇒ **Save CPU time by using a Neural Network to simulate HGCal data**

ML Challenges

- Future high granularity calorimeters:
- High number of Channels
 - Irregular Geometry
 - Sparse data
- ⇒ No ML model powerful enough yet
⇒ **Point Clouds (PCs)**
- Target PC size: 2k Hits × 5 [E,t,x,y,z]

Core problem: How do we upsample PCs?

Naive approach:
Latent Vector → FFN → PCs

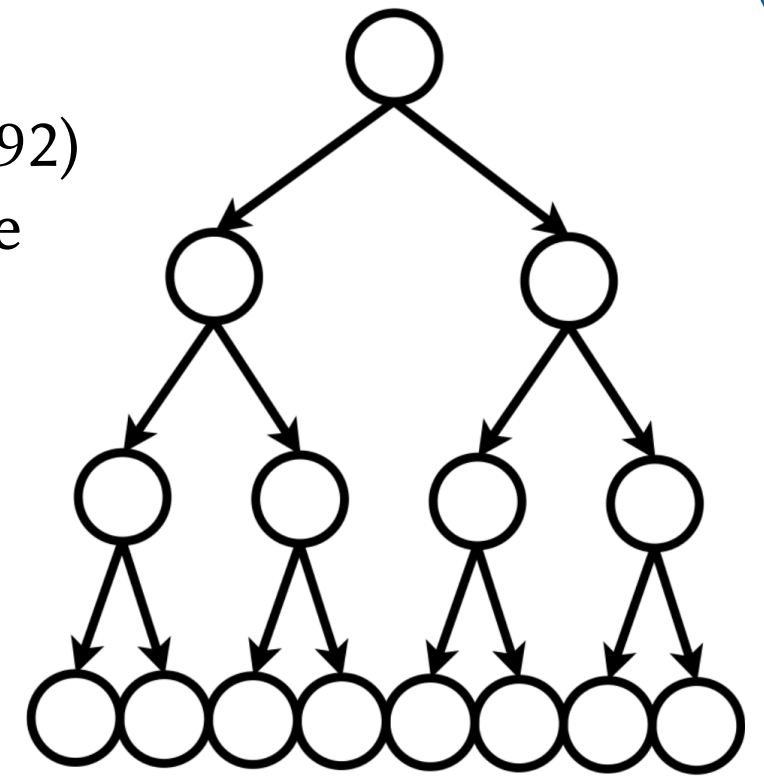


Number of parameters explodes
⇒ Not trainable

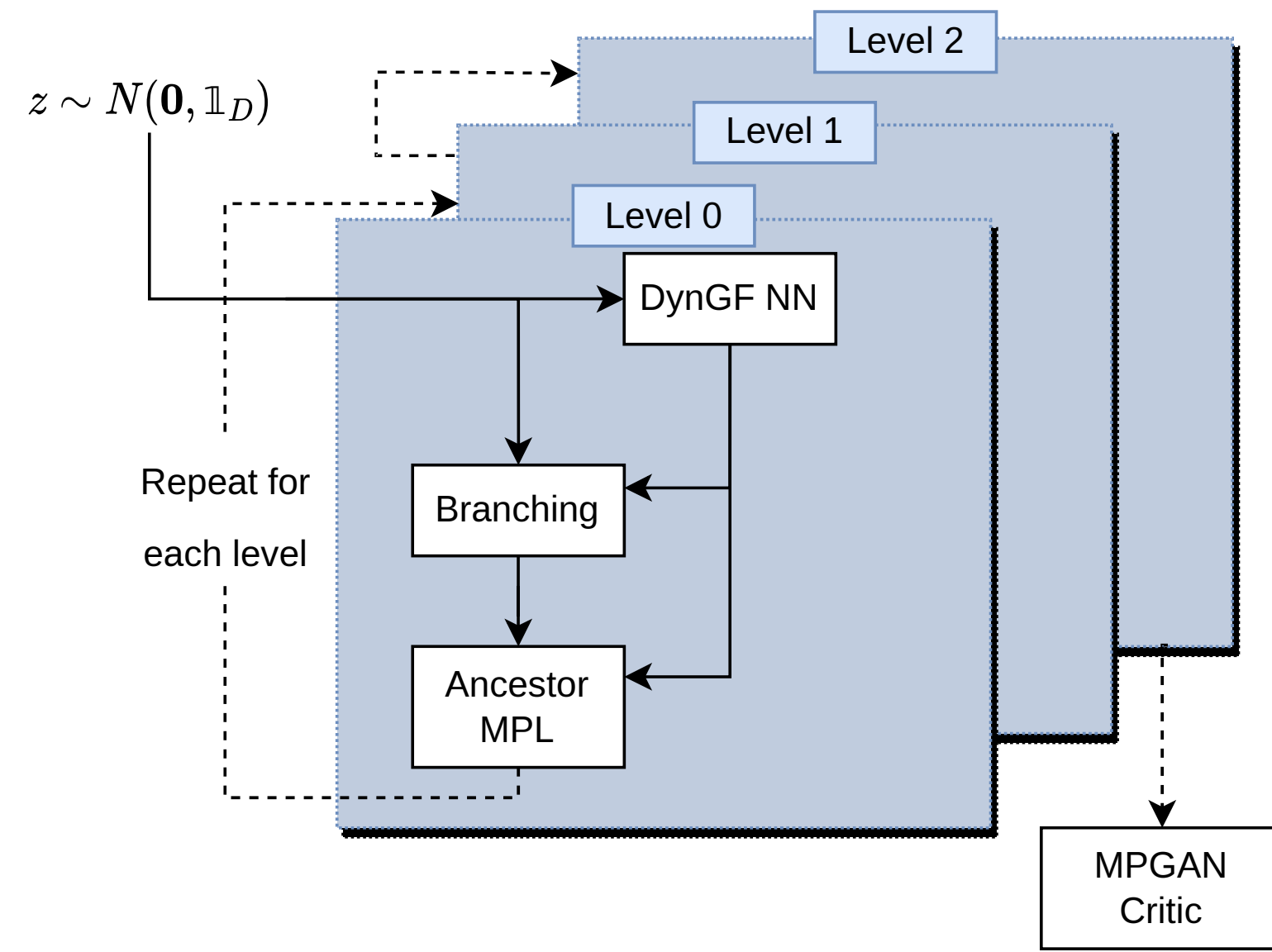
DeepTreeGAN:

- Inspired by TreeGAN (arXiv:1905.06292)
- FFN projects each particle to multiple
- Repeat to grow a tree
- After k projections: $\prod_i k_i$ particles

⇒ Small output space for each FFN
⇒ Small number of parameters
⇒ Sparse representation, no padding



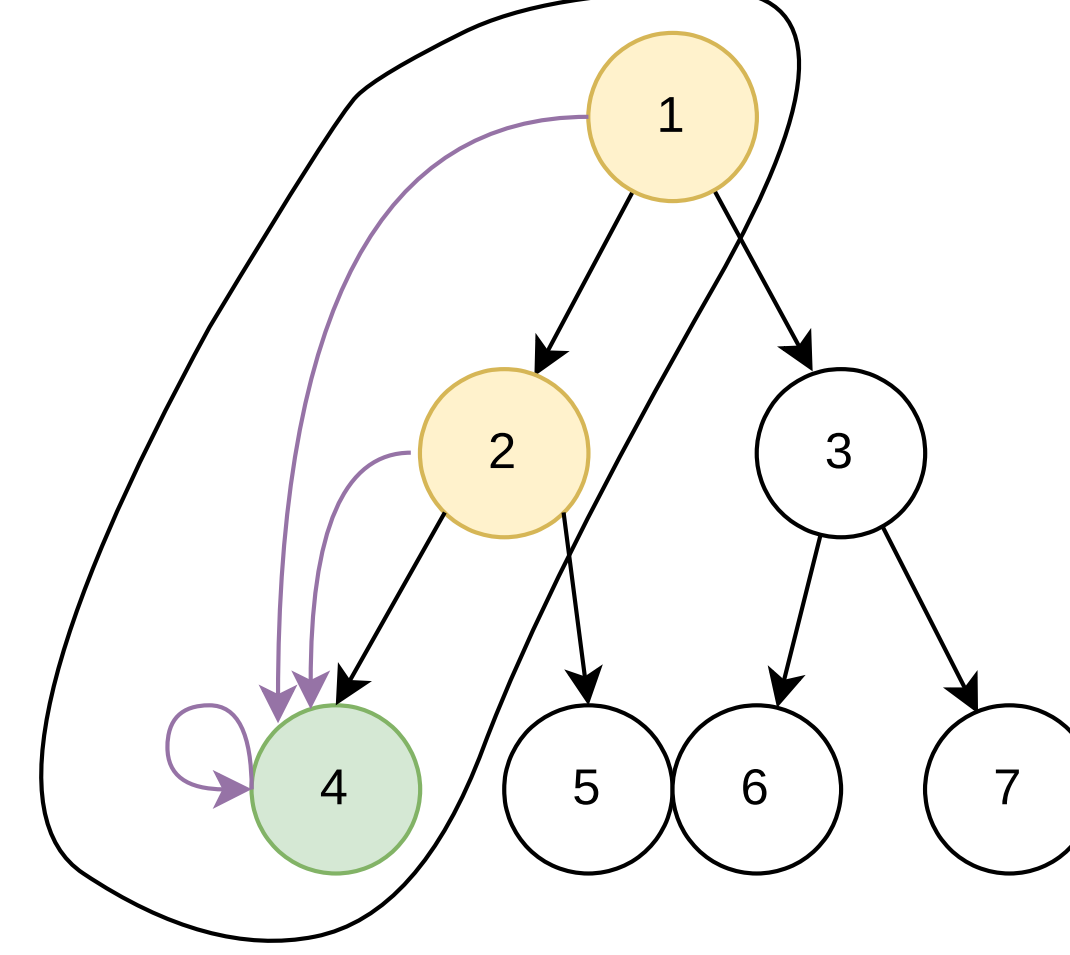
Model Overview



- Start with random vector z
- Repeat for each level:
 - DynGF:** Encode the global state of the leaves (FFN → Sum → FFN)
 - Branching:** Split each of the leaves
 - Ancestor MPL:** Pass information down from ancestors to their children
- Last level: Take the first n points, to match the simulation

The Generator

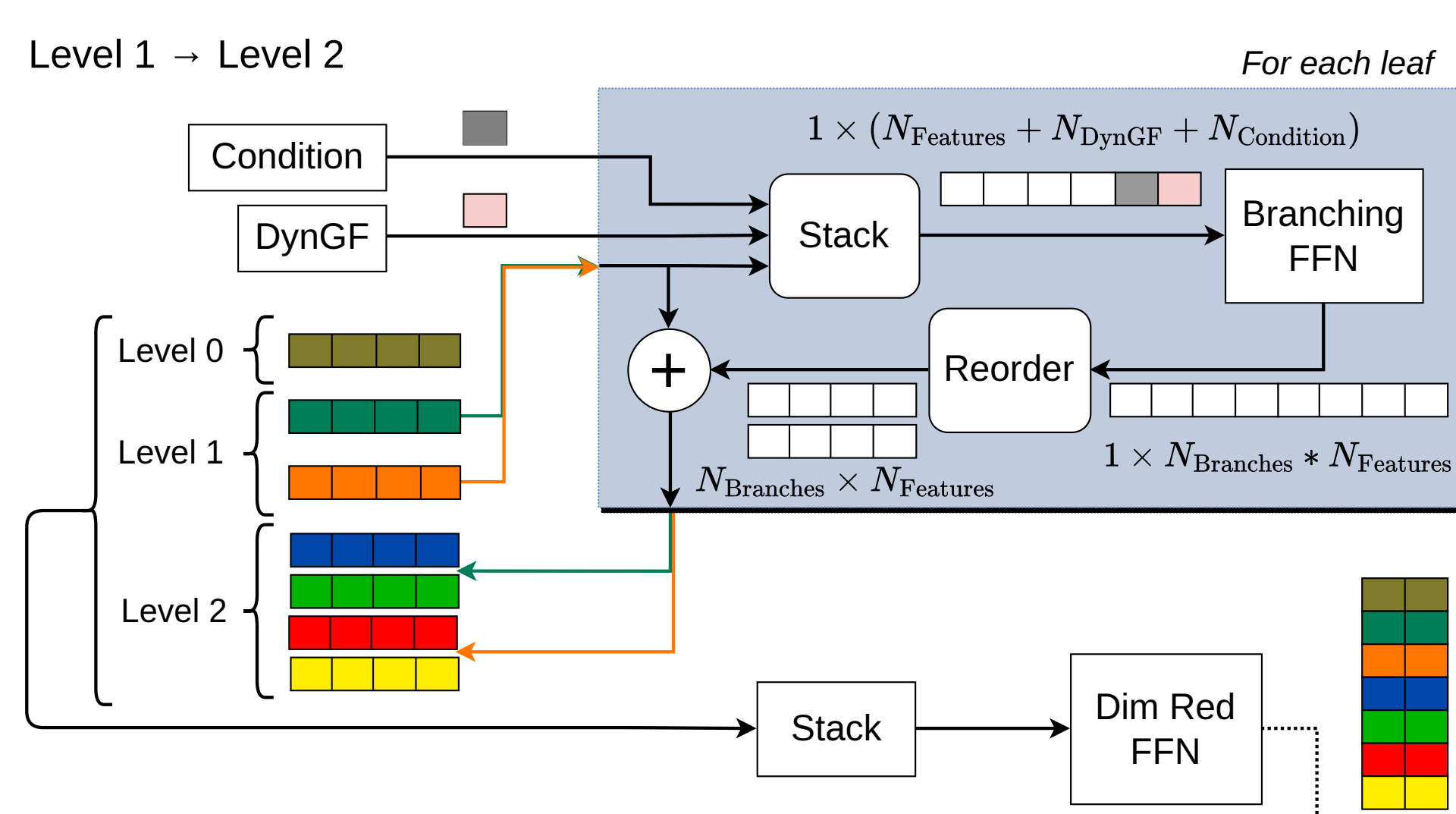
Ancestor Message Passing Layer



Selected MPL: GINConv (arXiv: 1810.00826)

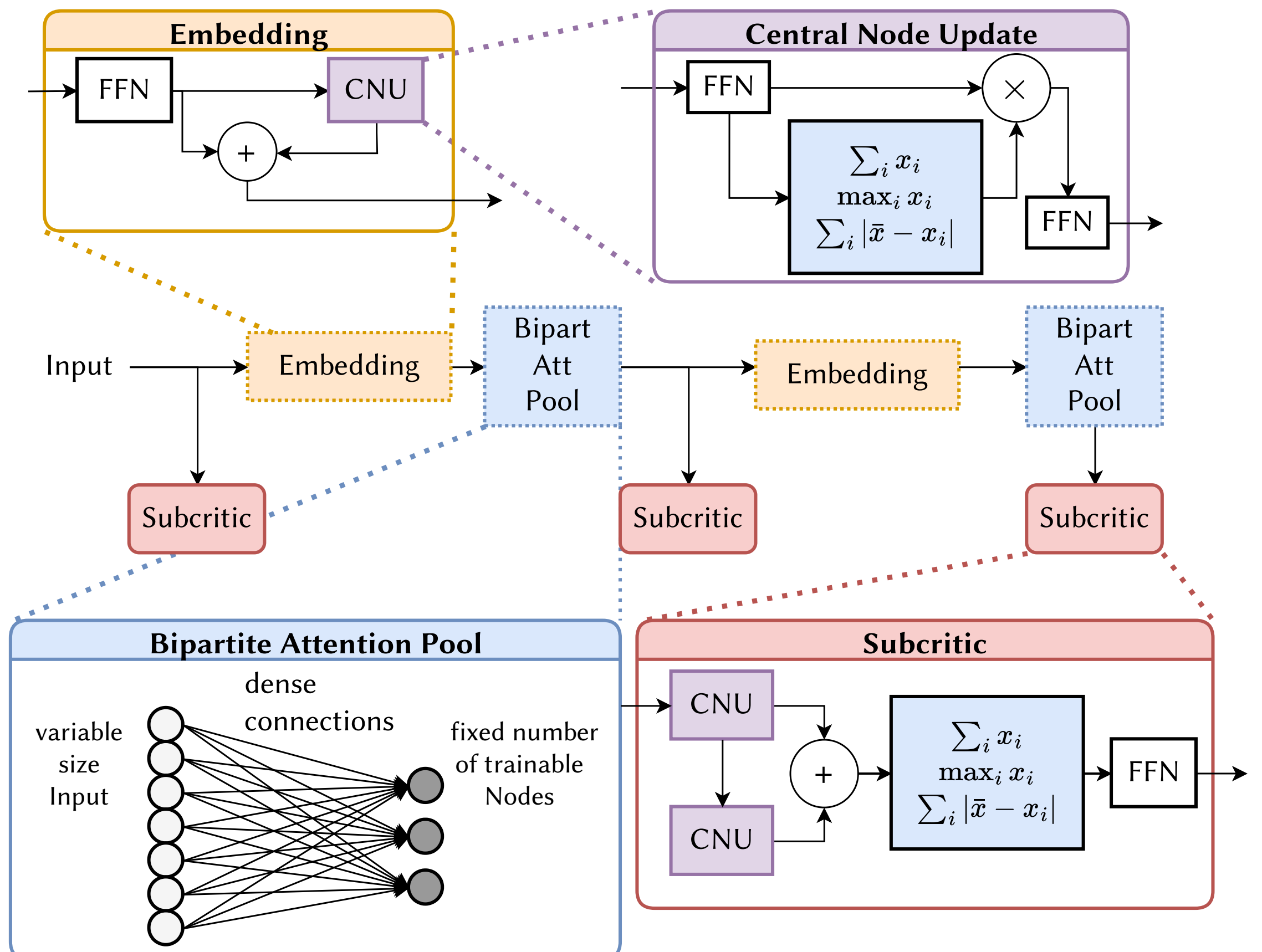
- Message: $Msg_{j \rightarrow i} = x_j$
- Aggregate: $Aggr_i = \sum_{j \in N(i)} Msg_{j \rightarrow i}$
- Update: $x_i \leftarrow NN((1 + \epsilon)x_i + Aggr_i) + x_i$

Branching



- Branch from Level 1 to Level 2
- For each leaf separately:
 - DynGF:** Stack leaf with condition and global feature vector
 - Branching FFN: Project to target dimension
 - Split into the number of branches
 - Add the parent on top
 - Stack up all levels of the tree
 - Reduce the number of features with a FFN

Critic



Central Node Update (CNU)

- Pass points through feed-forward network (FFN)
 - Aggregate points (sum+max+width)
 - Pass aggregate & points through 2nd FFN
- Embedding**
- Map points in higher dim. space with FFN
 - Pass through CNU (+residual connection)
- Subcritic**
- Pass through 2 CNU (+residual connection)
 - Aggregate points (sum+max+width)
 - Map aggregate to dim 1 with FFN
 - Hinge Loss

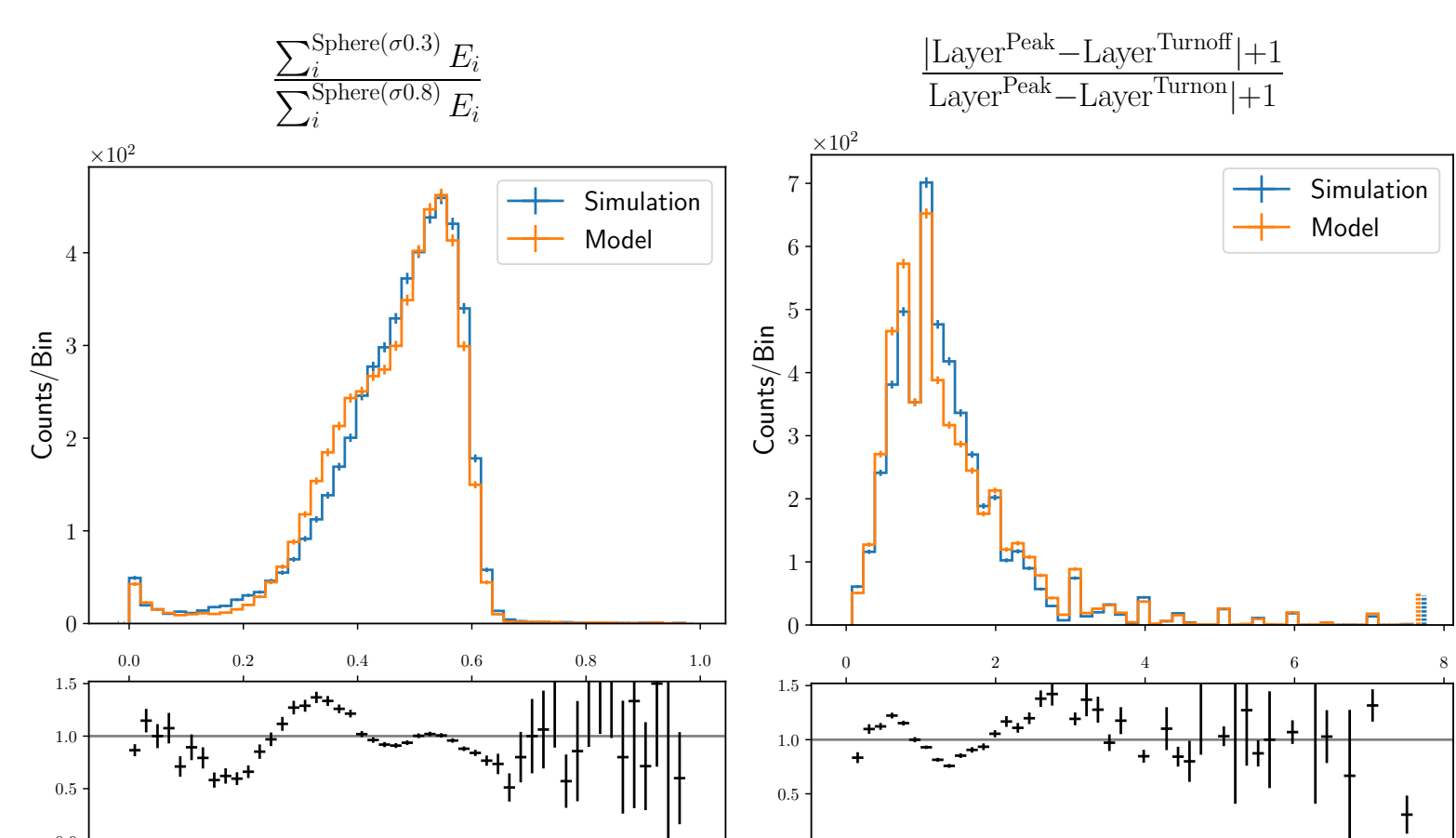
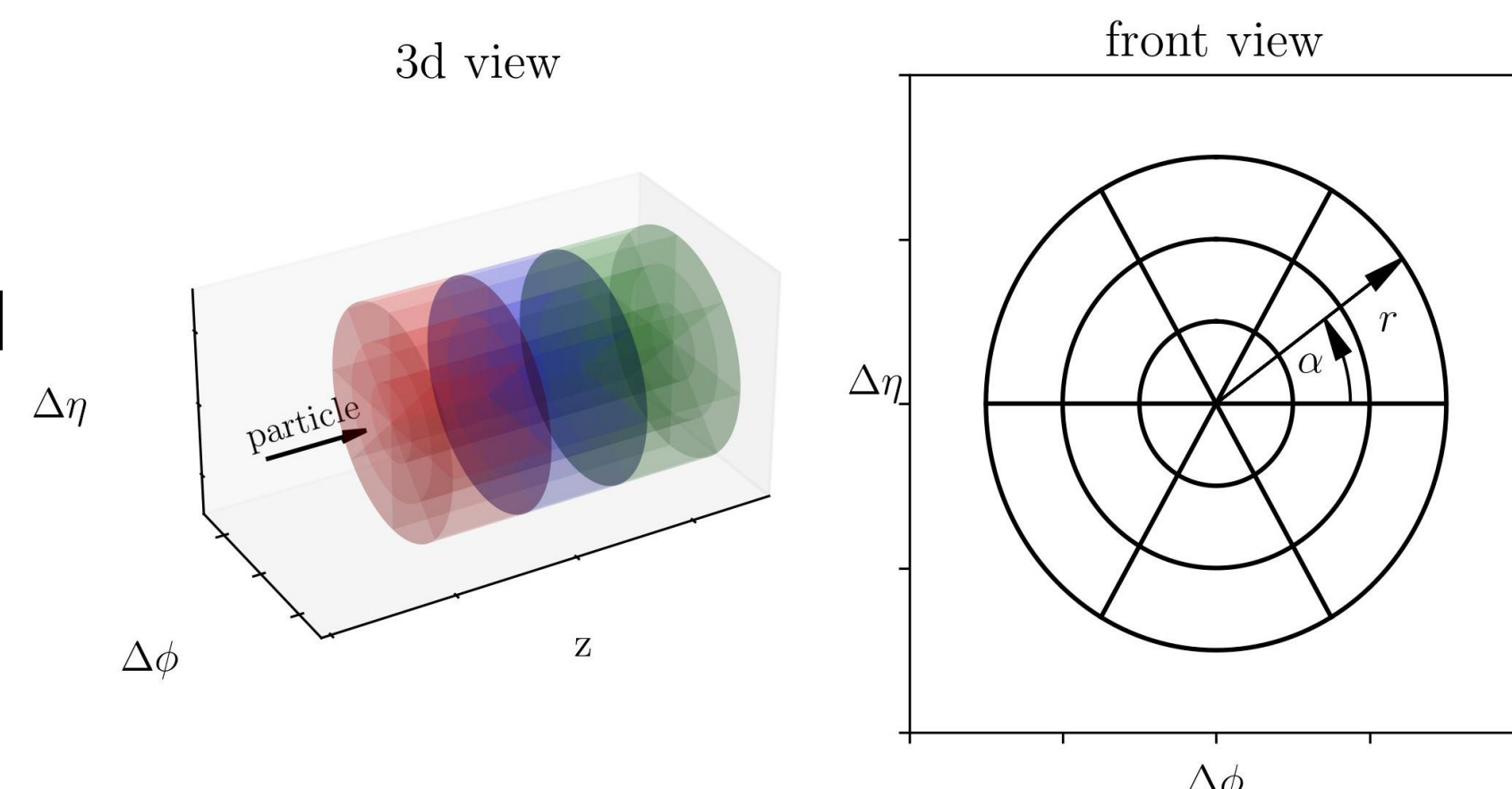
Bipartite Attention Pool

- Construct dense, bipartite graph from input to trainable nodes
- Apply GATv2Conv Message Passing Layer
 - differentiable
 - permutation invariant
 - variable sized input
 - fixed size output

Benchmark II: CaloChallenge Dataset 2

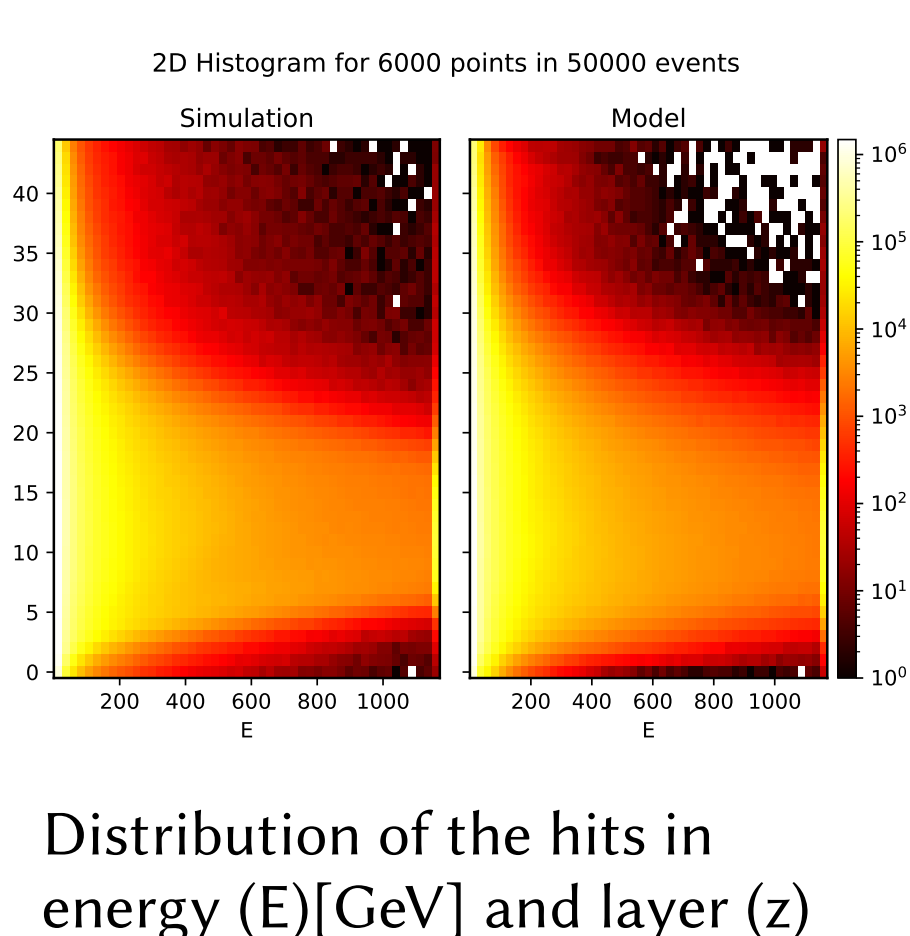
Public dataset: DOI 10.5281/ calochallenge.github.io/homepage/

- 100k GEANT4-simulated electrons showers for training/testing
- Energies with log-uniform distribution [1 GeV, 1 TeV]
- Concentric cylinder detector geometry
- 45 layers(z) × 9 radial segments (r) × 16 angular segments (α) = 6480 voxels



Check on the density: Energy contained in Sphere around center with radius 0.3*std vs 0.8*std

Check on shower shape: Distance turnon (1/2 maximum) → peak vs turnover → peak



Distribution of the hits in energy (E)[GeV] and layer (z)

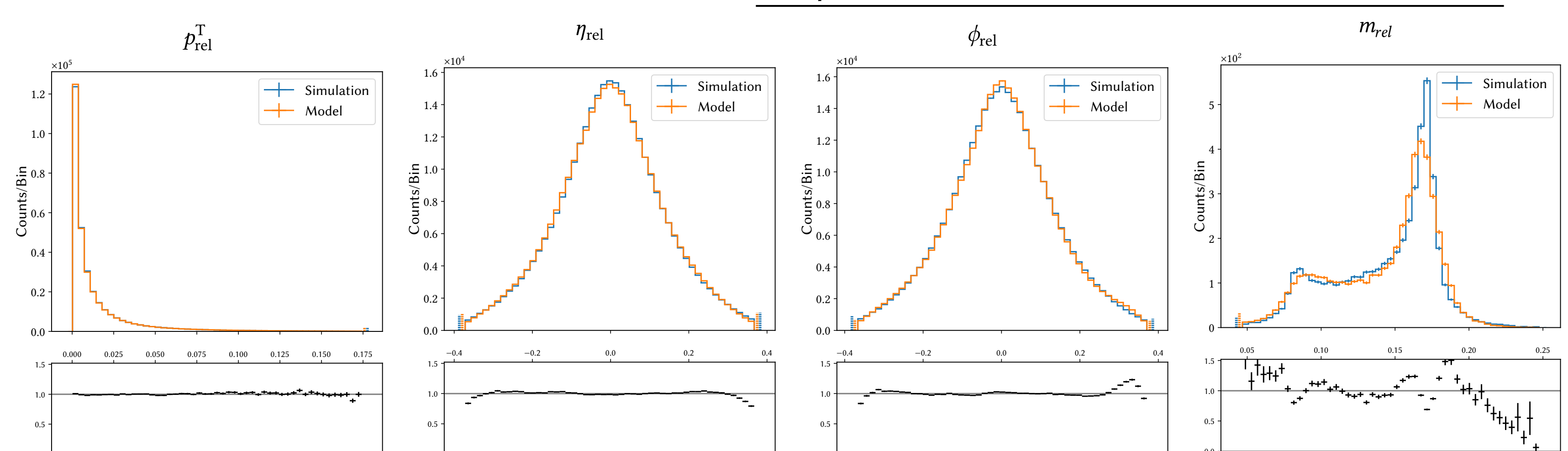
Benchmark I: JetNet 150 Top-Quarks

JetNet (arXiv:2106.11535) dataset:

- Hadronized jets, anti-kT (R=0.8)
- 170k gluon/light quark/top jets
- Leading 150 constituents by p^T
- Metrics for benchmarking

Metrics compared to other models, lower is better, best in bold
arxiv: 2305.15254 (MDAM) 2301.08128 (EpiC-GAN)

Model	W ₁ ^M × 10 ³	W ₁ ^P × 10 ³	W ₁ ^{EP} × 10 ⁵	FPD × 10 ⁴
In Sample	0.42 ± 0.09	0.12 ± 0.04	1.22 ± 0.32	1.2 ± 0.6
EpiC-GAN	0.69 ± 0.08	0.65 ± 0.03	2.67 ± 0.39	22 ± 1
MDMA	0.57 ± 0.09	0.10 ± 0.02	2.12 ± 0.64	5.3 ± 0.9
DeepTree(v2)	1.49 ± 0.04	0.13 ± 0.02	5.01 ± 0.08	3.4 ± 0.7



The marginal distributions of the constituents and the mass of the top-initiated jets

$$P_{rel}^T = \frac{P_{particle}^T}{P_{jet}^T}, \eta_{rel} = \eta_{particle} - \eta_{jet}, \phi_{rel} = \phi_{particle} - \phi_{jet}, m_{rel} = \frac{m_{jet}}{P_{jet}^T}$$

⇒ **Almost identical architecture for jets and calo. showers**

⇒ **New, differentiable up/downscaling methods for point clouds**

⇒ **Promising model to scale to even larger point clouds (e.g. HGCal)**