

# Black Hole Quantum Matter



Karl Landsteiner



*Based on work t.a.h.s.*

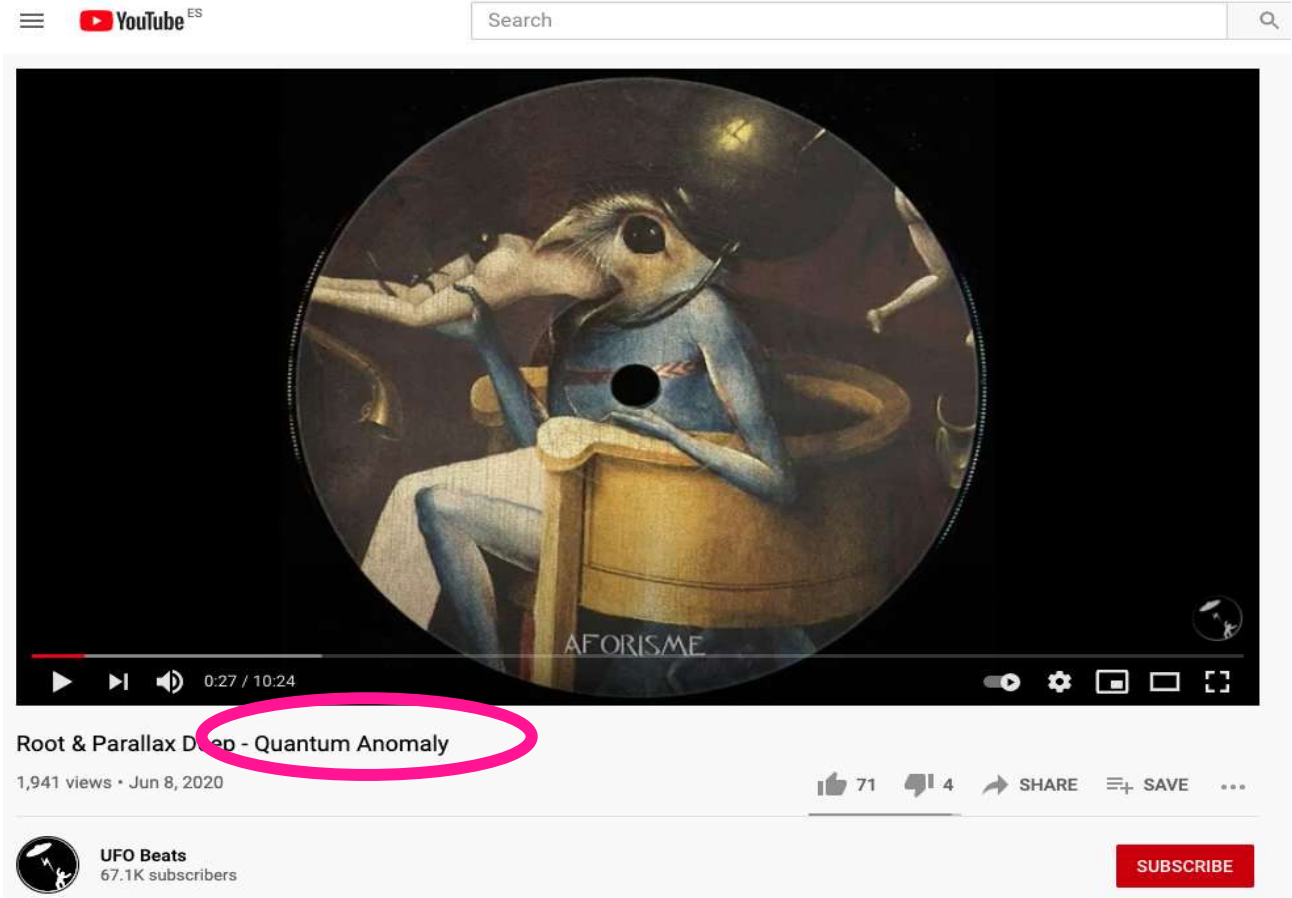
*DKPI Final Event, Vienna, 28.09.2023*

# Outline

- What is a quantum anomaly?
  - Experimental demonstration !!
- Topological quantum matter = Chern Simons on Black holes
- Quantum Hall physics
  - CME
  - CVE
  - Superfluids

# Quantum Anomalies

Popular views at times somewhat inaccurate...



The image shows a YouTube video player interface. At the top, there is a search bar and the YouTube logo. The video player itself shows a circular frame containing a blue, insect-like creature sitting in a wooden chair, holding a long, thin object. The word "AFORISME" is visible at the bottom of the video frame. Below the video player, the title "Root & Parallax Deep - Quantum Anomaly" is displayed, with the word "Anomaly" circled in pink. The video has 1,941 views and was uploaded on Jun 8, 2020. The channel name "UFO Beats" and "67.1K subscribers" are shown at the bottom left, along with a "SUBSCRIBE" button at the bottom right.

YouTube ES

Search

AFORISME

0:27 / 10:24

Root & Parallax Deep - Quantum Anomaly

1,941 views · Jun 8, 2020

UFO Beats  
67.1K subscribers

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71 4 SHARE SAVE ...

# Anomalies

## Ingredients to an anomaly:

- Classical symmetry broken by quantization
- Topology

# Anomalies

Can one see this anomaly in experiment?

20 October 1975

Volume 54A, number 6

PHYSICS LETTERS

20 October 1975

## VERIFICATION OF COHERENT SPINOR ROTATION OF FERMIONS <sup>☆</sup>

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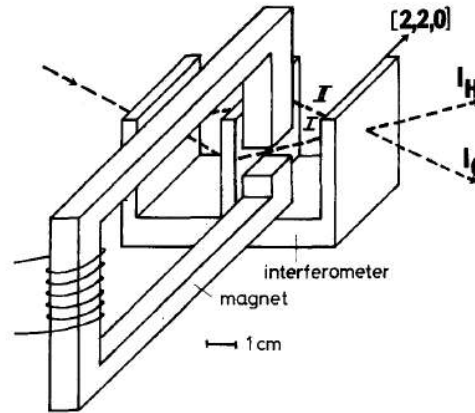


Fig. 1. Sketch of the experimental setup.

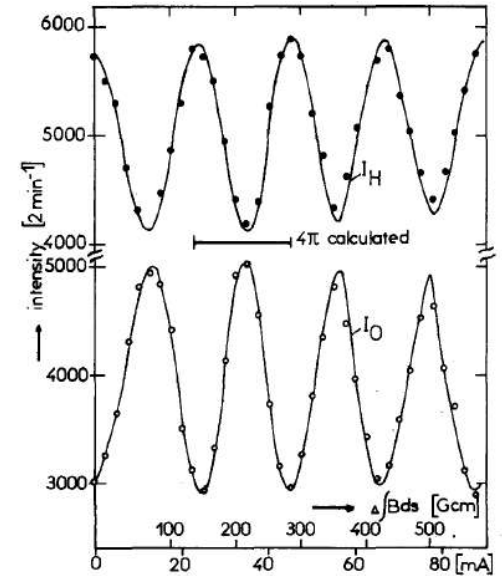


Fig. 2. Observed intensity oscillations of the 0- and H-beam as a function of the difference of the magnetic field action on beam I and II ( $\Delta \int B_z ds = \int B_z ds$  (path I) -  $\int B_z ds$  (path II)).

The oscillation period clearly shows that the identical wave function is reproduced after a spinor rotation of  $4\pi$  and a  $-1$  occurs for a  $2\pi$  rotation.

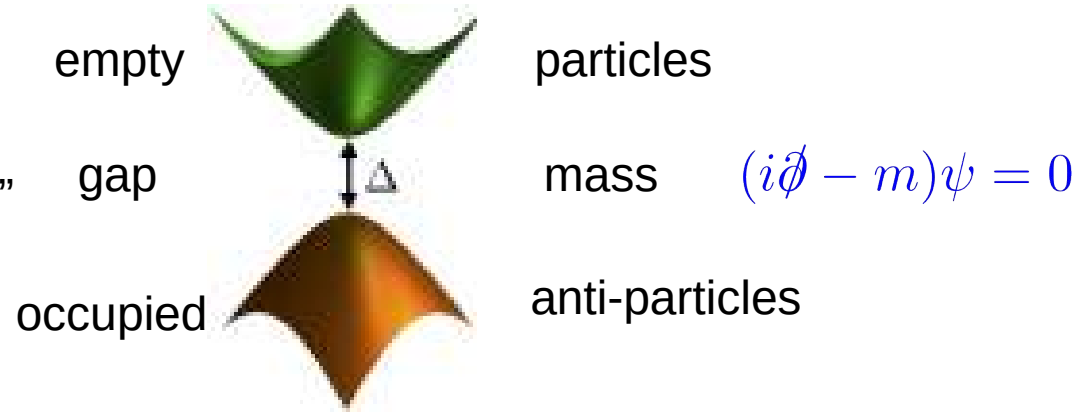
# Quantum Anomalous Hall Effect

Cond-mat/Hep dictionary:



“Edge Current”

“Band structure”



Berry connection:  $\mathcal{A}_i = \psi(p)^\dagger \frac{\partial \psi(p)}{\partial p_i}$

Berry curvature:  $\mathcal{F} = \nabla_p \times \mathcal{A}$

Topological invariant:  $\int_{BZ} \mathcal{F} = \pm 2\pi$

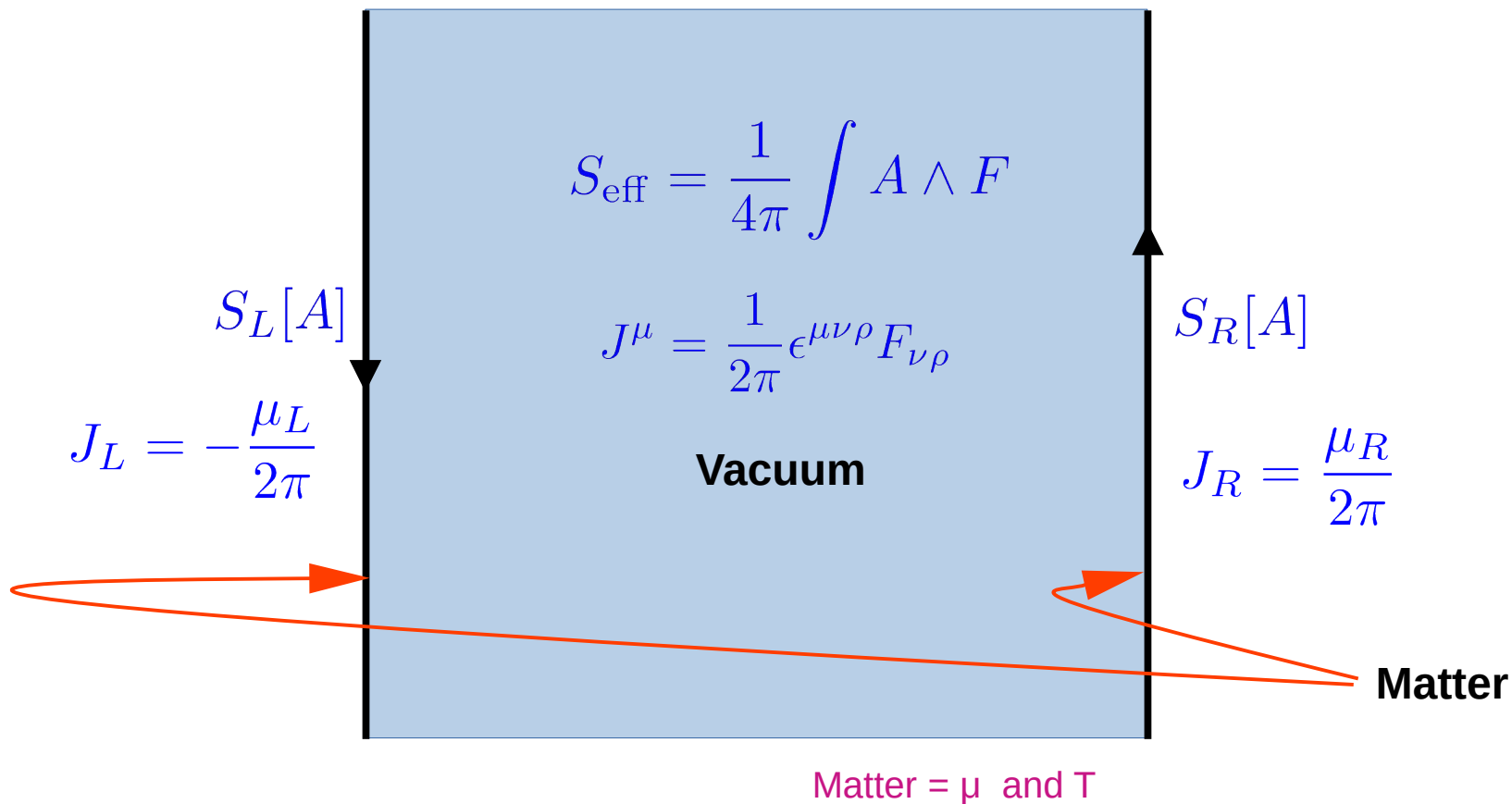
Quantized hall conductivity:

$$J^i = \frac{e^2}{h} \epsilon_{ij} E_j$$

[TKNN] 1982  
 [Haldane] 1988  
 [Golterman, Jansen, Kaplan] 1992

# QAHE

Quantum field point of view:



# Anomalies

## Chiral Fermions have anomalies

→ “Gauge” anomaly  $\mathcal{A} = c \int d^2x \lambda F$

→ Non-local in 2D  $c \int d^2x d^2y \frac{\partial A(x) F_{\mu\nu}(y) \epsilon^{\mu\nu}}{\square_{xy}} \quad \delta A_\mu = \partial_\mu \lambda$

→ Local term in 3D  $S_{\text{CS}} = c \int_M A \wedge F$

→ Gauge Trafo:  $\delta S_{\text{CS}} = c \int_{\partial M} \lambda F$

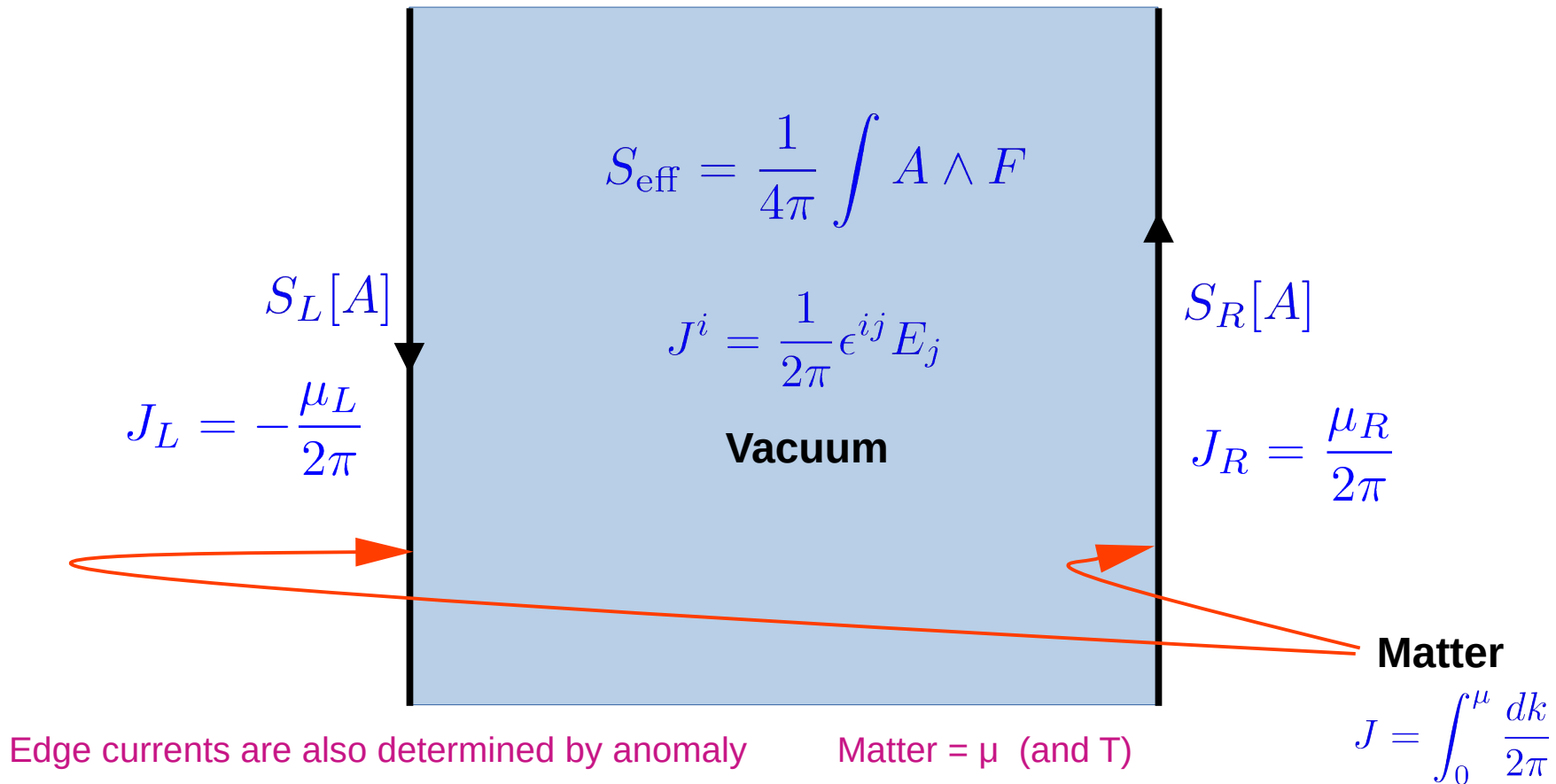
(Anomaly Inflow)

[Callan, Harvey] 1985



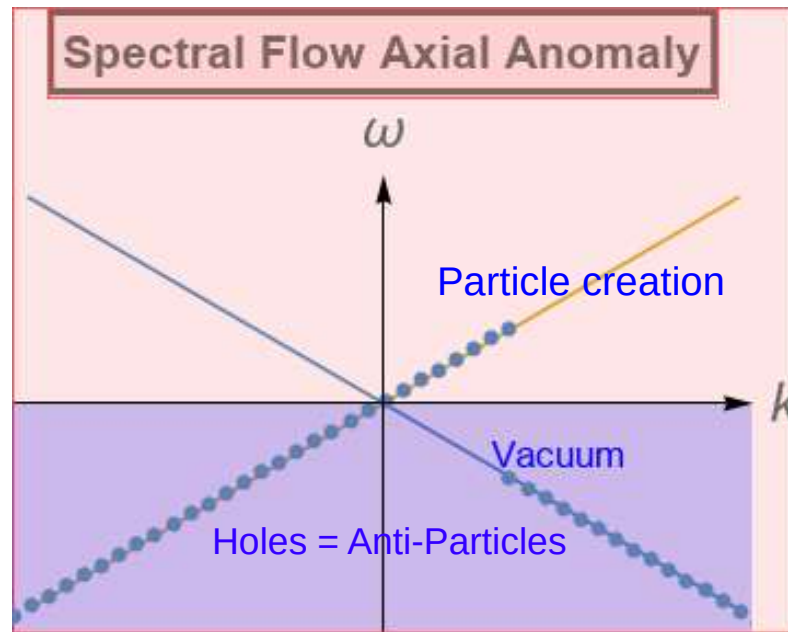
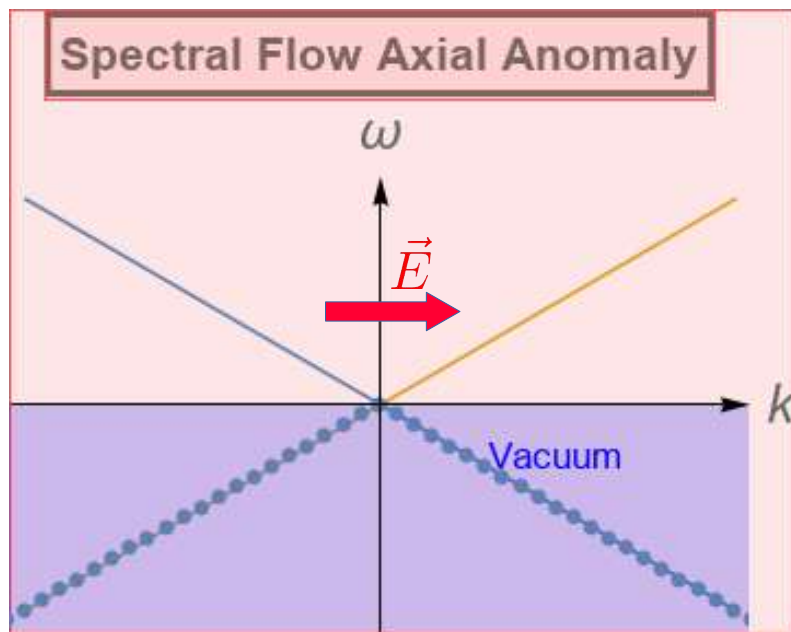
# QAHE

Quantum field point of view:



# (Edge) Anomaly

1 left handed + 1 right handed



$$\frac{dn_{R,L}}{dt} = \pm \frac{1}{2\pi} E$$

$$\frac{d}{dt}(n_R + n_L) = 0$$

# Direct visualization of electronic transport in a quantum anomalous Hall insulator

Received: 4 May 2022

Accepted: 26 June 2023

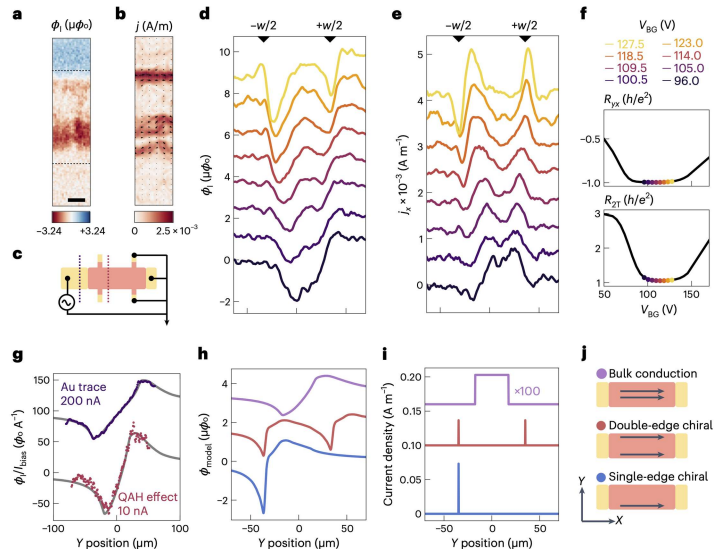
Published online: 3 August 2023

 Check for updates

 G. M. Ferguson<sup>1</sup>, Run Xiao<sup>2</sup>, Anthony R. Richardella<sup>2</sup>, David Low<sup>1</sup>,  
 Nitin Samarth<sup>2</sup> & Katja C. Nowack<sup>1,3</sup> ✉

A quantum anomalous Hall (QAH) insulator is characterized by quantized Hall and vanishing longitudinal resistances at zero magnetic field that are protected against local perturbations and independent of sample details. This insensitivity makes the microscopic details of the local current distribution inaccessible to global transport measurements. Accordingly, the current distributions that give rise to transport quantization are unknown. Here we use magnetic imaging to directly visualize the transport current in the QAH regime. As we tune through the QAH plateau by electrostatic gating, we clearly identify a regime in which the sample transports current primarily in the bulk rather than along the edges. Furthermore, we image the local response of equilibrium magnetization

to electrostatic gating. Combined, these measurements suggest that the current flows through incompressible regions whose spatial structure can change throughout the QAH regime. Identification of the appropriate microscopic picture of electronic transport in QAH insulators and other topologically non-trivial states of matter is a crucial step towards realizing their potential in next-generation quantum devices.



# Chern Simons and Black Holes

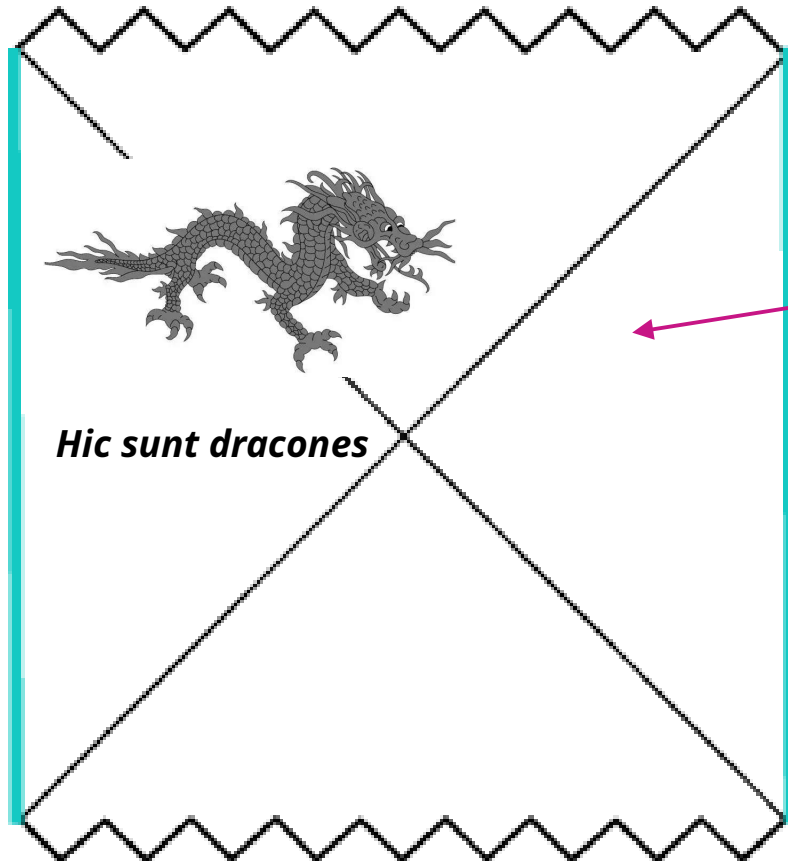
- Bulk insulator is described by effective Chern-Simons action
- Gauge invariance restored by chiral anomaly from edge modes
- Claim: edge modes are described by Chern-Simons on Black hole

$$S_{\text{eff}} = c \int_M A \wedge F - c \int_{BH} A \wedge F$$

$$\partial M = \partial(BH)$$

# Anomalous currents from black holes

Black Hole encodes “quantum matter” =  $T, \mu$



“We live here”

What we can see

*Hic sunt dracones*

$$ds^2 = dr^2 - f(r)^2 dt^2 + g(r)^2 d\vec{x}^2$$

$$f(b) = g(b) = 1$$

$$2\pi T = f'(r_h)$$

# Anomalous currents from black holes

3 dimensions:

$$S_{\text{eff}} = \int_{BH} A \wedge F$$

$$\delta S = 2 \int_{BH} \delta A \wedge F + (\delta A \wedge A)|_{\partial BH}$$

$$F = \partial_r A_t dr \wedge dt$$

$$\mu = A_t(b) - A_t(r_h)$$

Encodes chemical potential  $\mu$

$$\delta S = \delta A \cdot J$$

$$J = 2\mu - A_t(b)$$

Current of 2D Chiral Fermion!  
(covariant vs consistent anomaly)

[Bardeen, Zumino] 1984

# Anomalous currents from black holes

Gravitational CS term:  $S = \int_{BH} (\Gamma d\Gamma + \frac{2}{3}\Gamma^3)$

$$x^\mu \rightarrow x^\mu + \xi^\mu$$

$$\delta\Gamma = (i_\xi d + di_\xi)\Gamma - D\Lambda_\xi$$

$$(\Lambda_\xi)^\alpha_\beta = \frac{\partial \xi^\alpha}{\partial x^\beta} \quad D \cdot = d \cdot + [\Gamma, \cdot]$$

$$\delta S = \int_{\partial} \Lambda_\xi R$$

2D Gravitational anomaly on boundary


Important detail: **vanishing extrinsic curvature on boundary!**

# Anomalous currents from black holes

Calculate current as before:

$$ds^2 = dr^2 - f(r)^2(dt - \delta A_g dx)^2 + g(r)^2 dx^2$$

“Gravito-electric” potential  
(Source for energy current)



$$\delta S = 2A_g \int_{r_H}^b \left[ \frac{f f' g'}{g} - (f')^2 \right]' dr$$

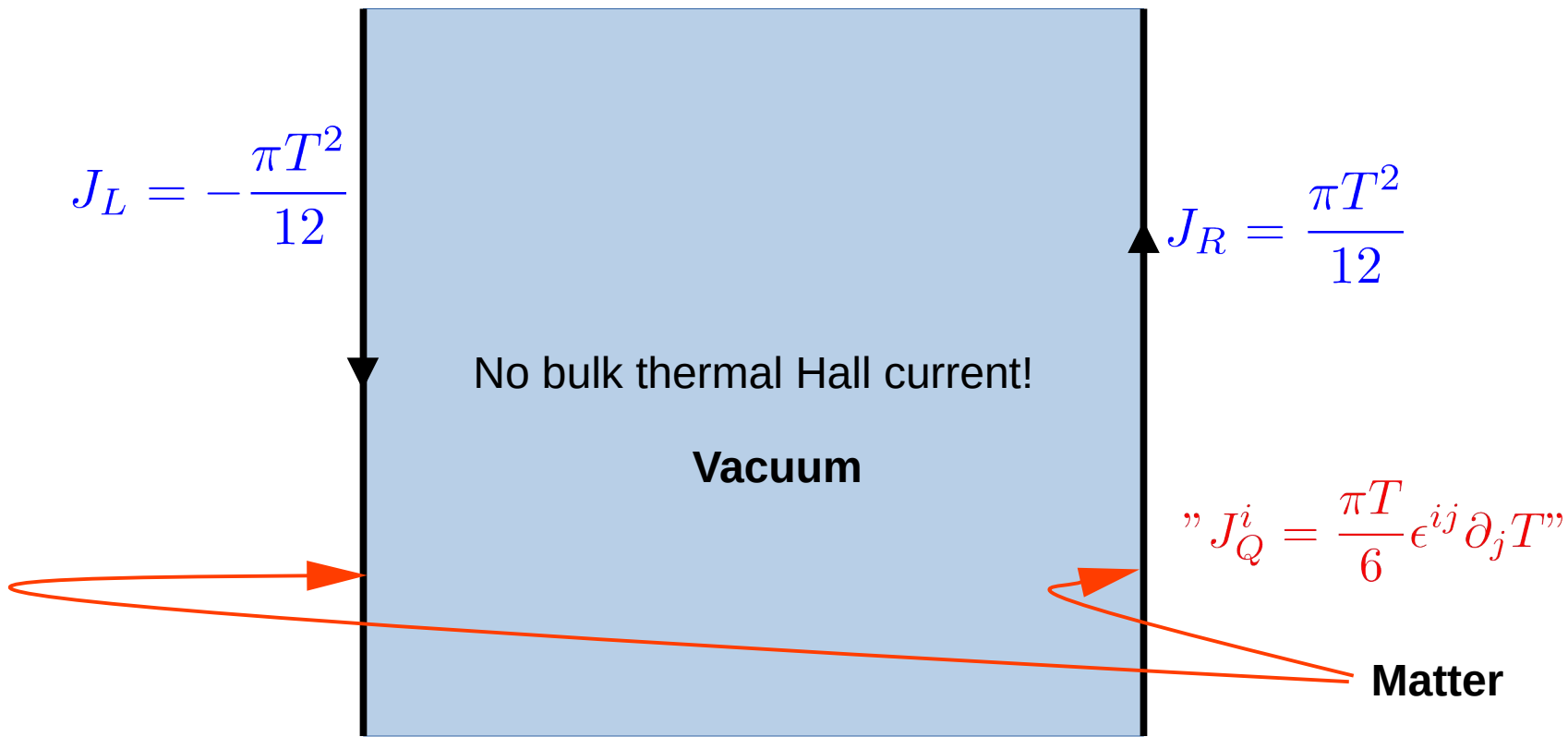
$$T^{tx} = J_E = 8\pi^2 T^2$$

Energy current of chiral fermion



# Application: thermal QHE

$$S = c_g \int_M (\Gamma d\Gamma + \frac{2}{3}\Gamma^3) - c_g \int_{BH} (\Gamma d\Gamma + \frac{2}{3}\Gamma^2)$$



# Application: CME

## 4D anomalies and 5D Chern-Simons forms:

● Chiral Magnetic Effect:  $S_{\text{eff}} = C \int_{\mathcal{BH}} A \wedge F_V \wedge F_V$

$$\vec{J} = 2C(\mu_5 - A_t)\vec{B}$$

● Chiral Separation Effect:  $S_{\text{eff}} = C \int_{\mathcal{BH}} A \wedge F_V \wedge F_V$

$$\vec{J}_5 = 2C\mu\vec{B}$$

● Chiral Vortical Effect:  $S_{\text{eff}} = C_g \int_{\mathcal{BH}} A \wedge \text{tr}(R \wedge R)$

$$\vec{J} = 16\pi^2 C_g T^2 \vec{\Omega}$$

→ Superfluidity as BF theory:  $S_{\text{eff}} = \int_{\mathcal{BH}} B_3 \wedge F$

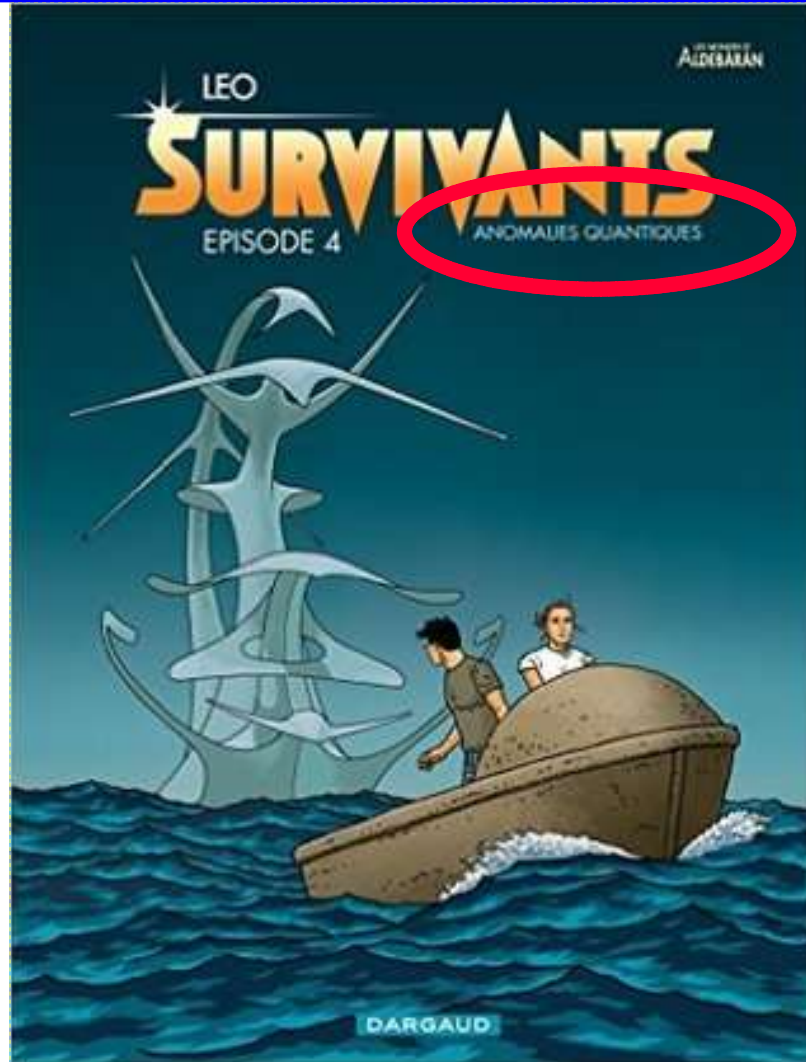
$$\omega^2 - v_s k^2 = 0$$

“anomaly” in higher form symmetry = vortex creation

2<sup>nd</sup> sound

# Quantum Anomalies

The good news:  
you can survive them



# Summary



[Fan Zhang]

=



**Thank you!**