

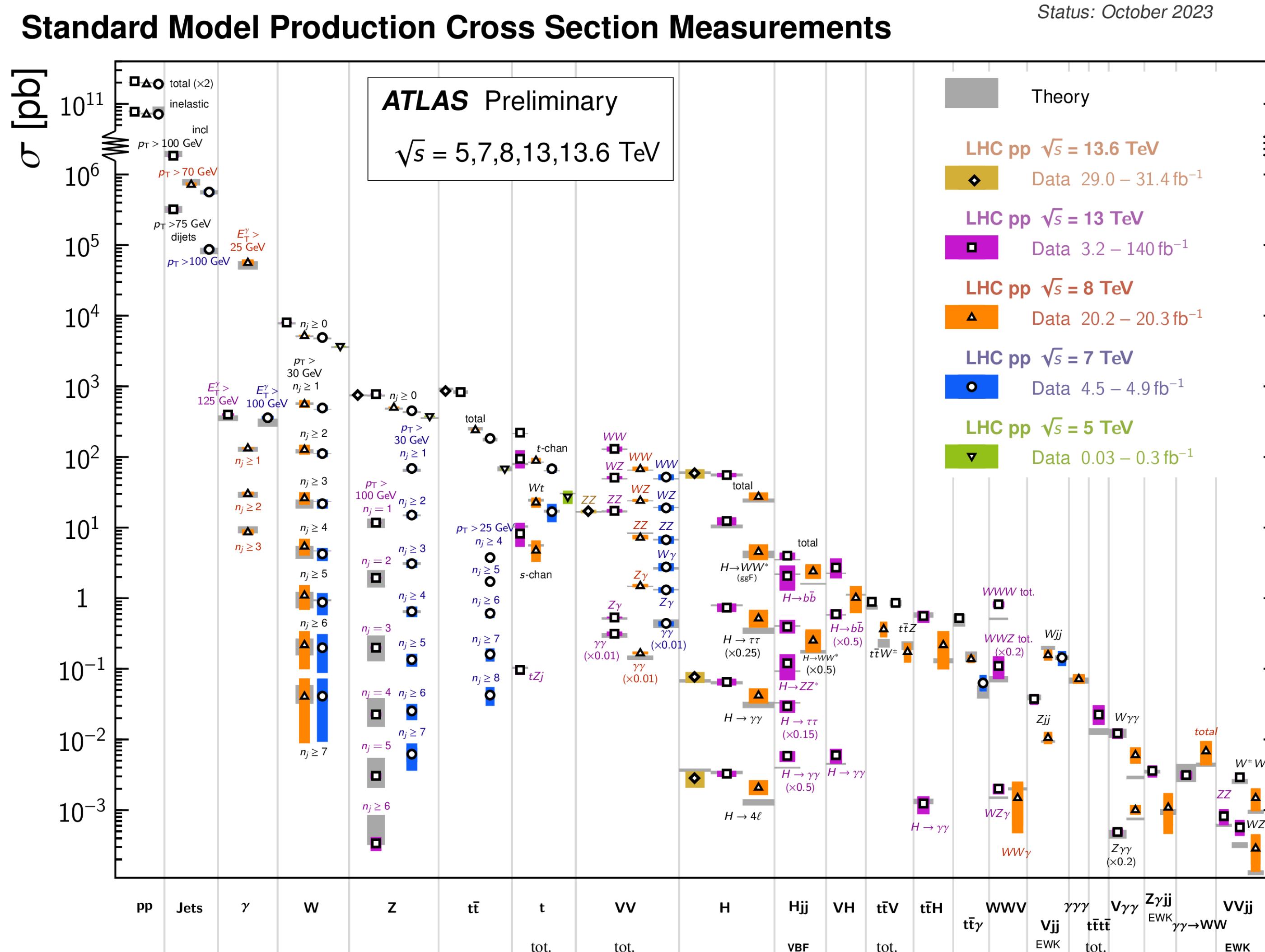
# SUSY and Electroweak Precision Tests at Tera-Z Colliders

**Kevin Langhoff**

(Work in progress with Simon Knapen and Zoltan Ligeti)

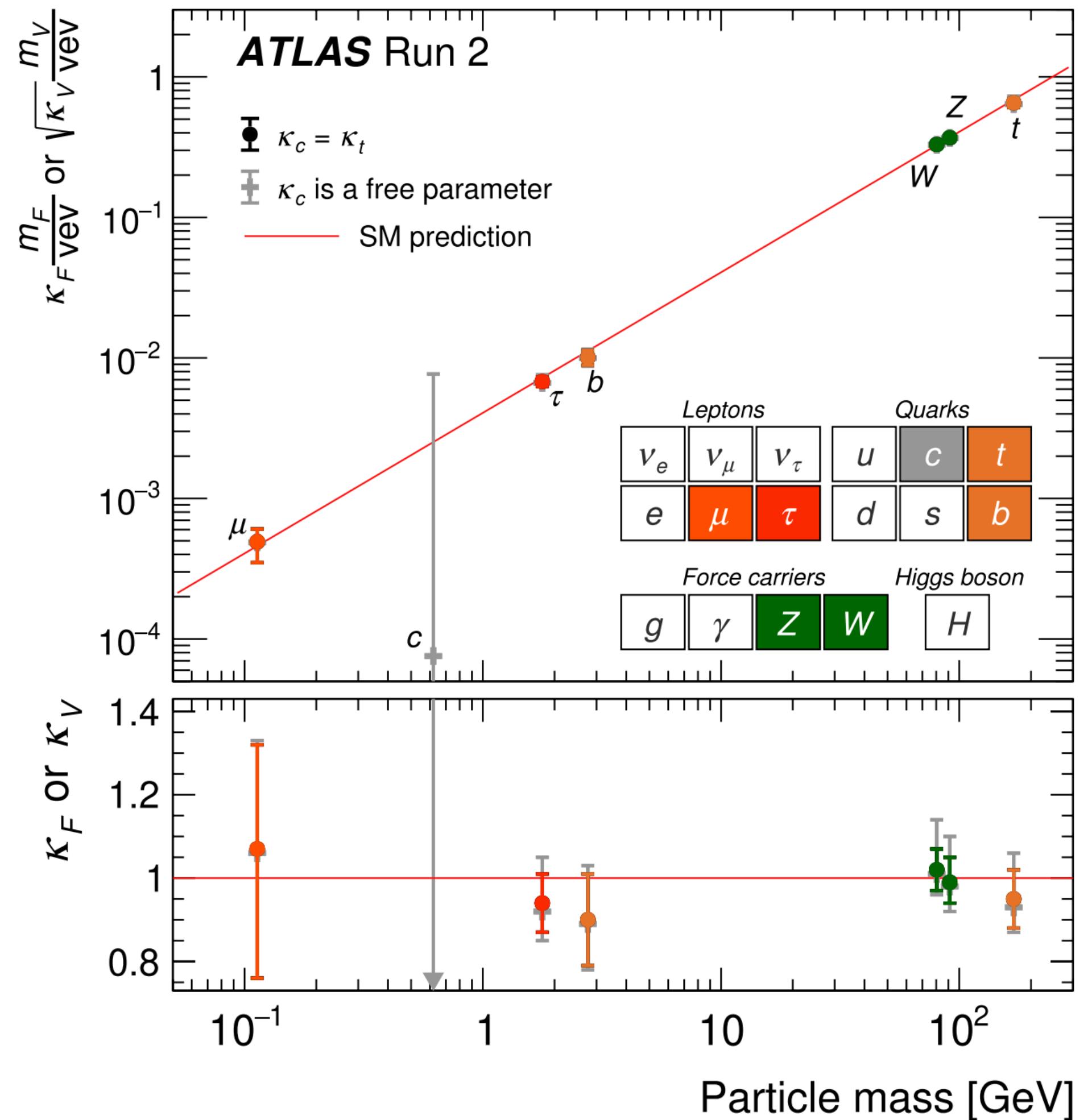
FCC-Week (June 11th, 2024)

# The Standard Model is extremely predictive!



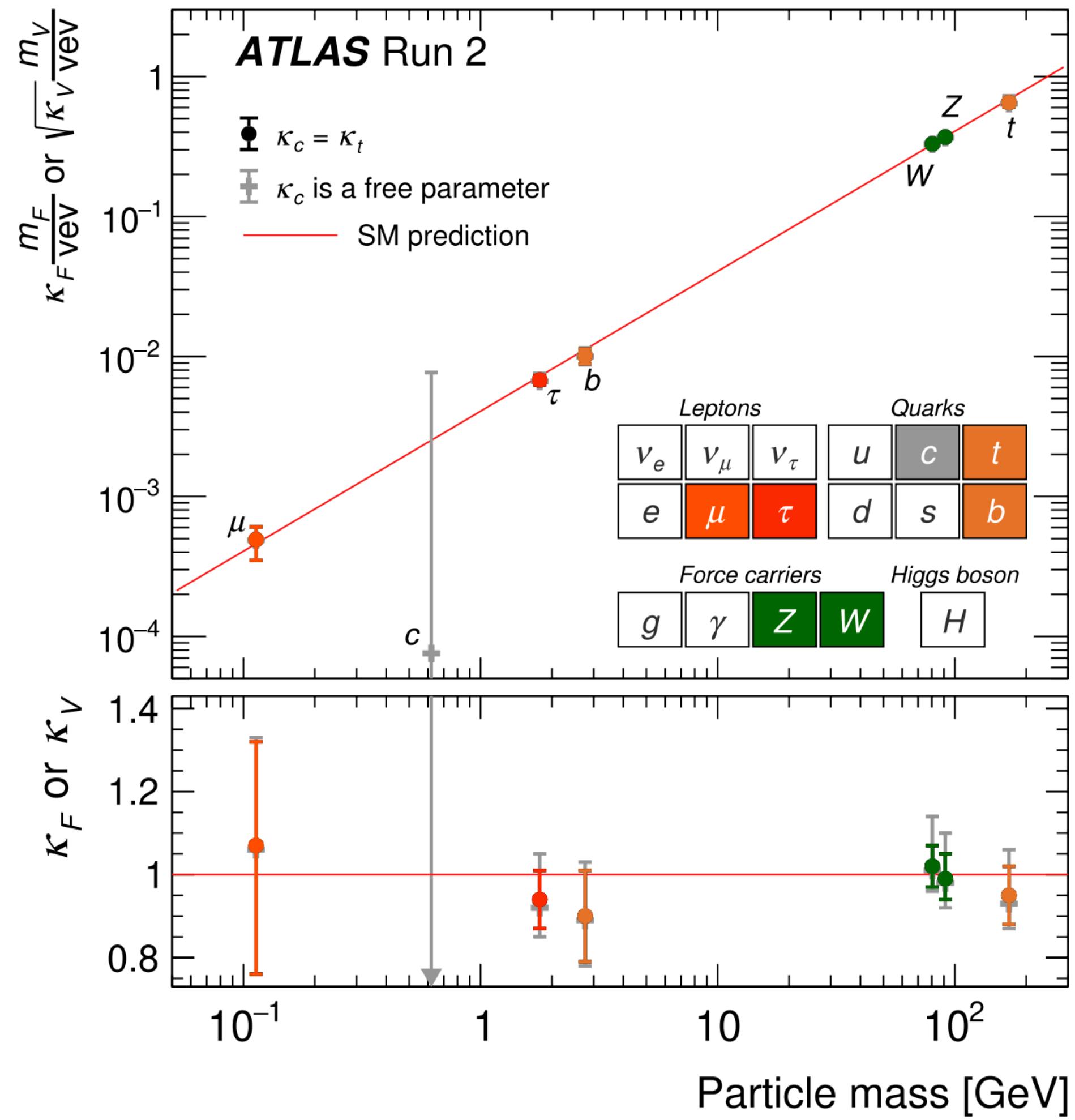
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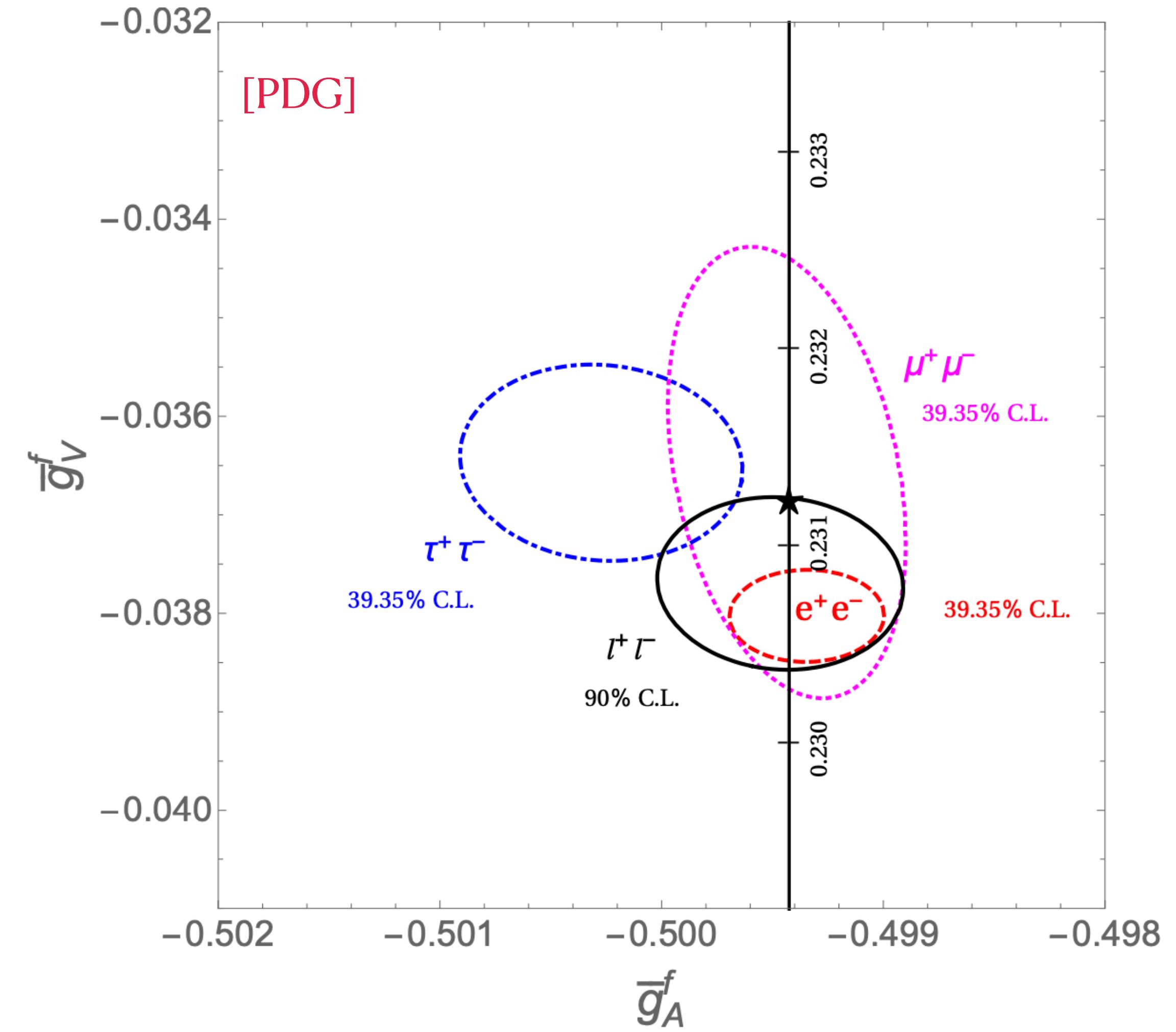


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## Observables

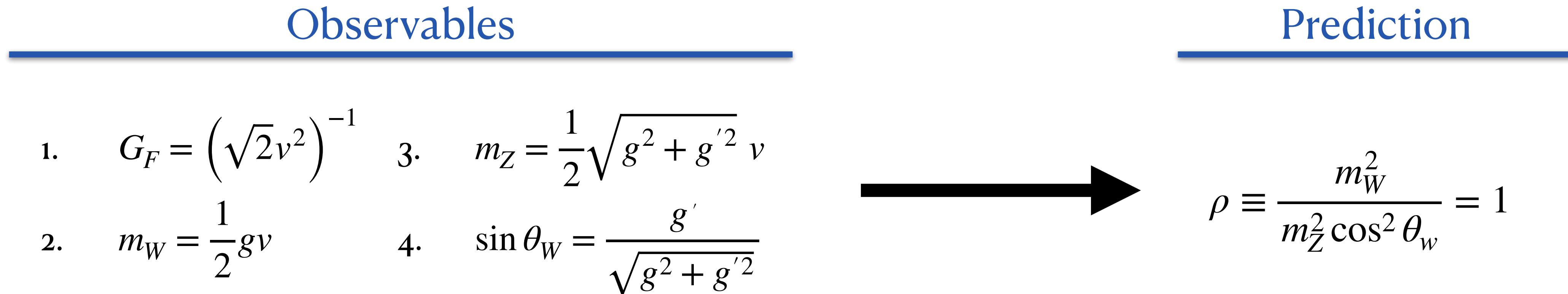
---

1.  $G_F = \left(\sqrt{2}v^2\right)^{-1}$
2.  $m_W = \frac{1}{2}gv$
3.  $m_Z = \frac{1}{2}\sqrt{g^2 + g'^2} v$
4.  $\sin \theta_W = \frac{g'}{\sqrt{g^2 + g'^2}}$

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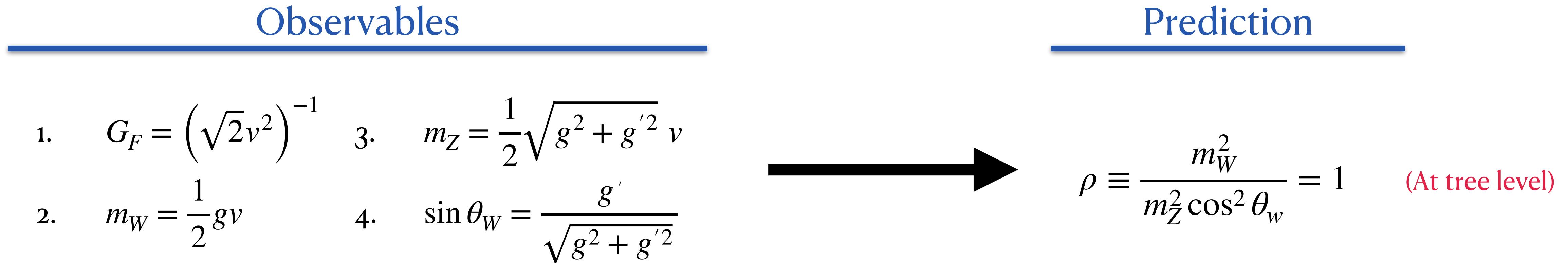
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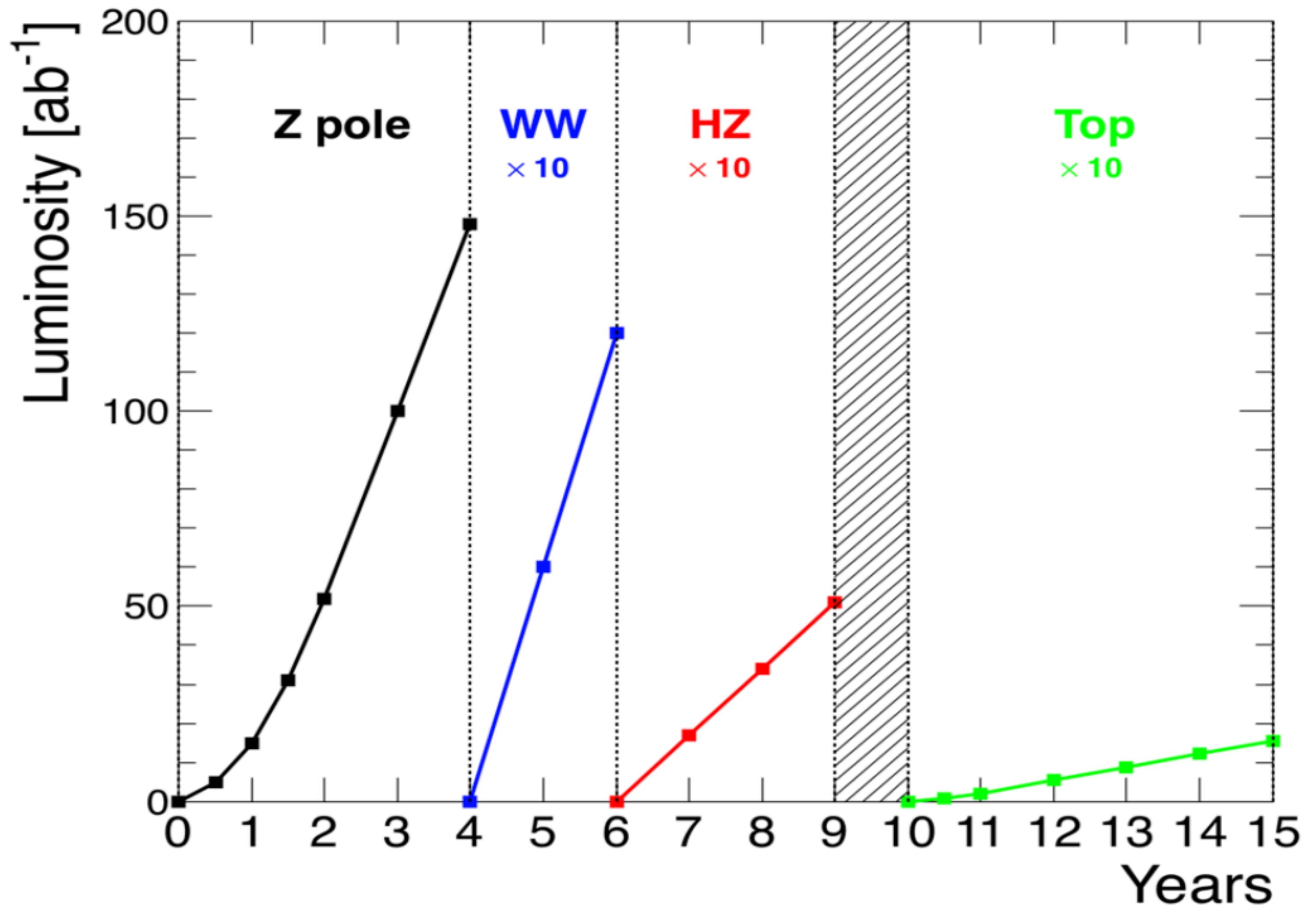
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- Checks like this give us a method of indirectly discovering new physics!

# The FCC-ee is an incredible precision device!

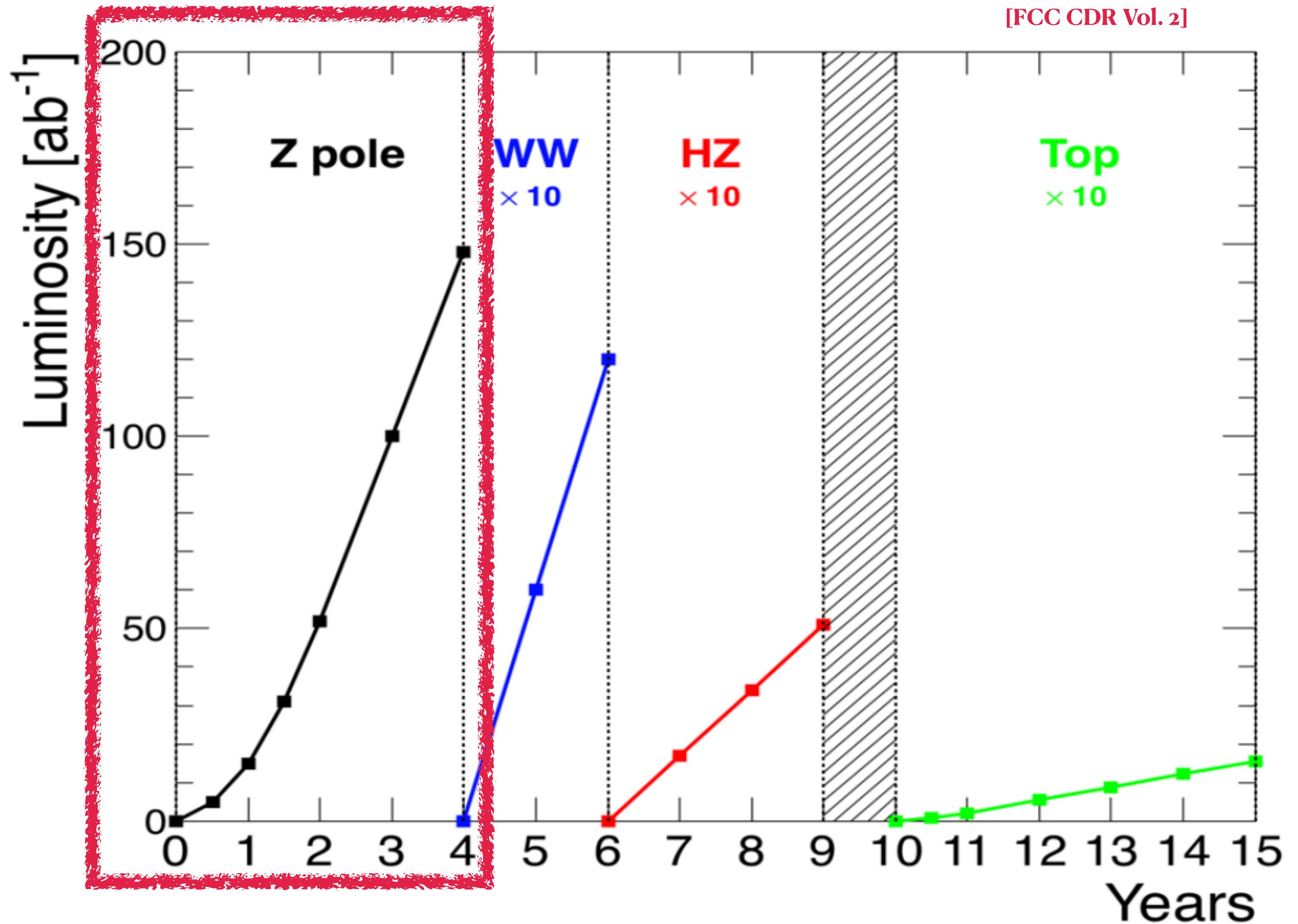
[FCC CDR Vol. 2]



# The FCC-ee is an incredible precision device!

The FCC-ee will produce roughly  $5 \times 10^{12}$  Z-bosons!

(Roughly a factor of  $10^5$  more than produced at LEP)



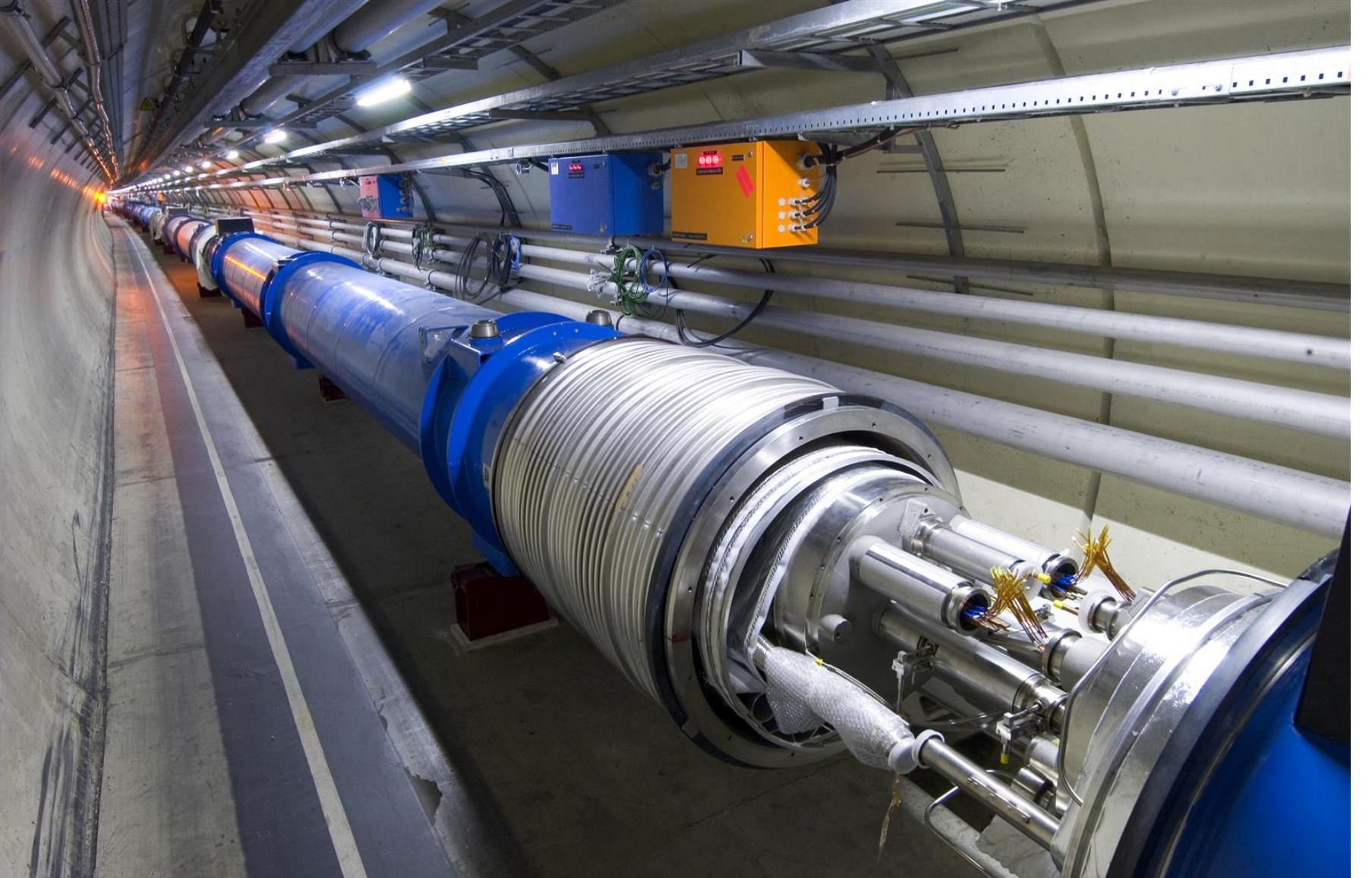
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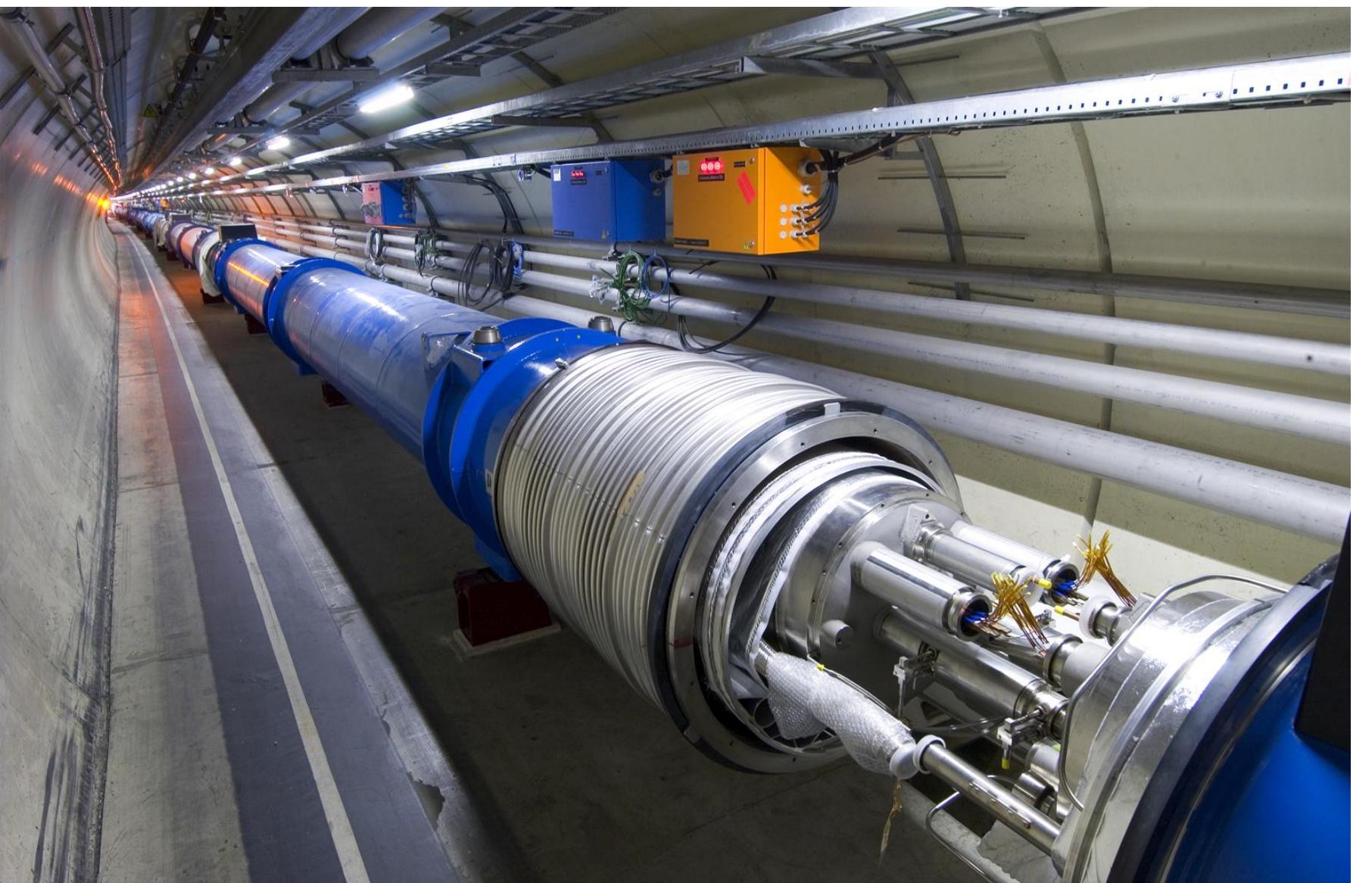
LHC?



Directly explores energy scales  $\Lambda \sim 10^3$  GeV.

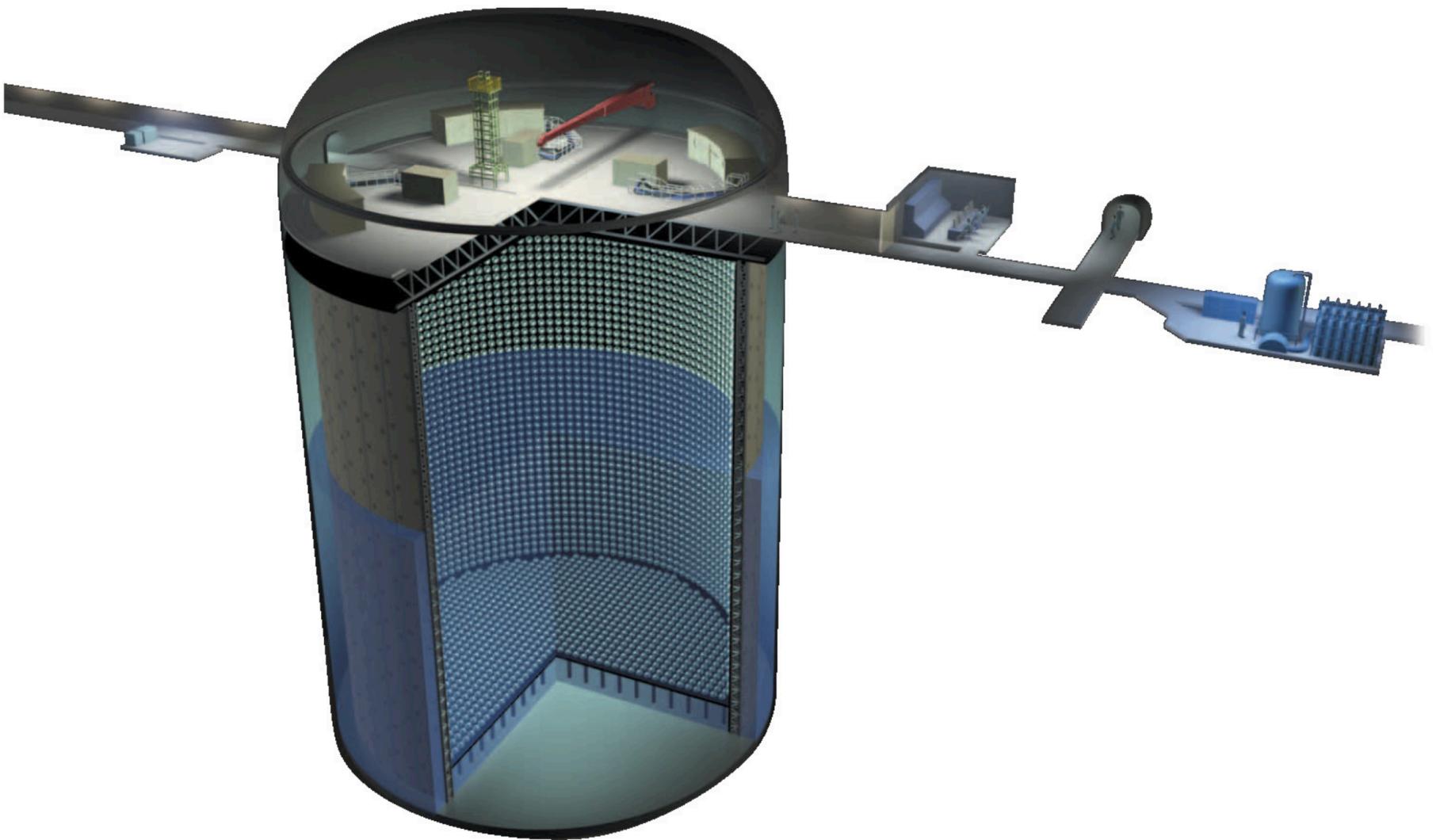
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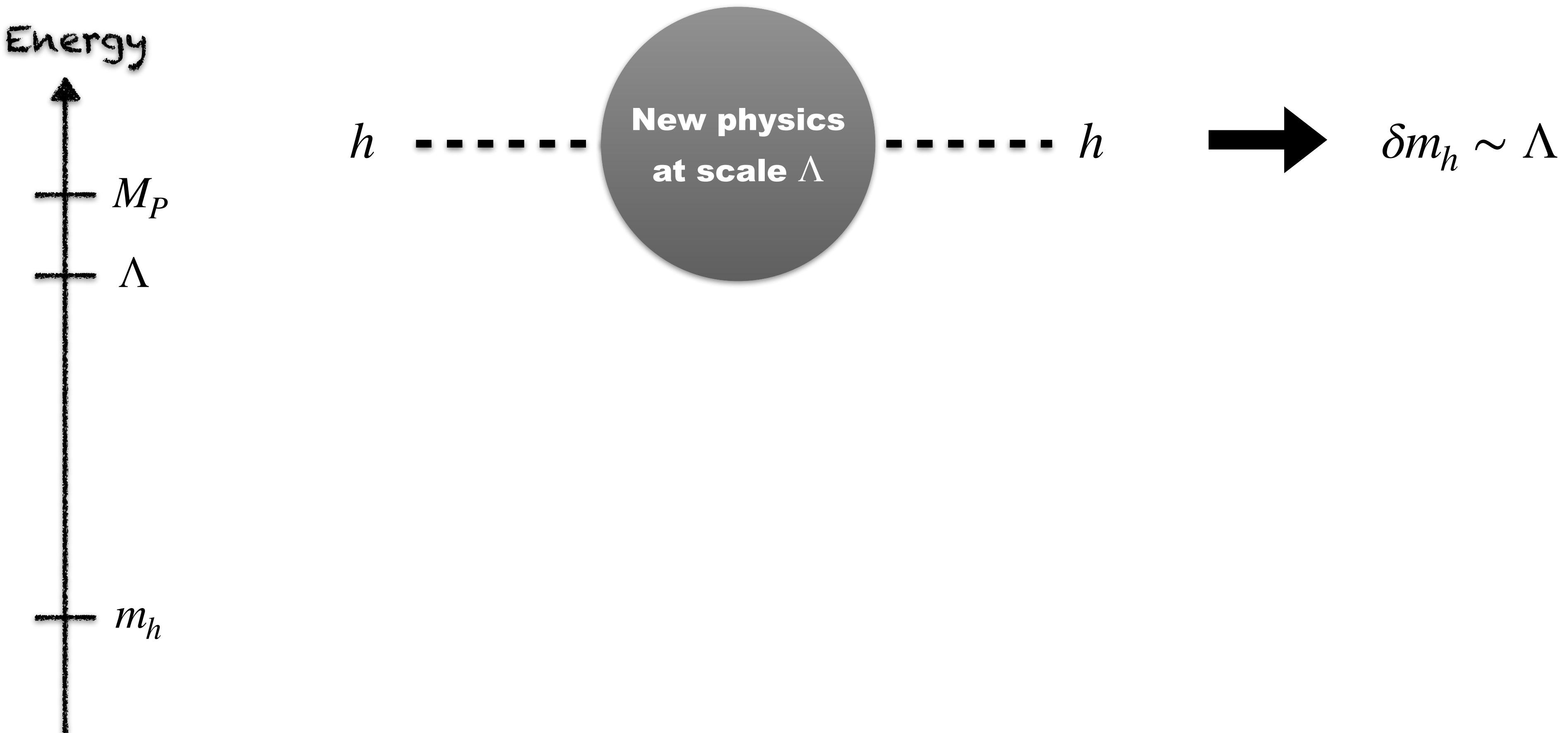
Super-Kamiokande



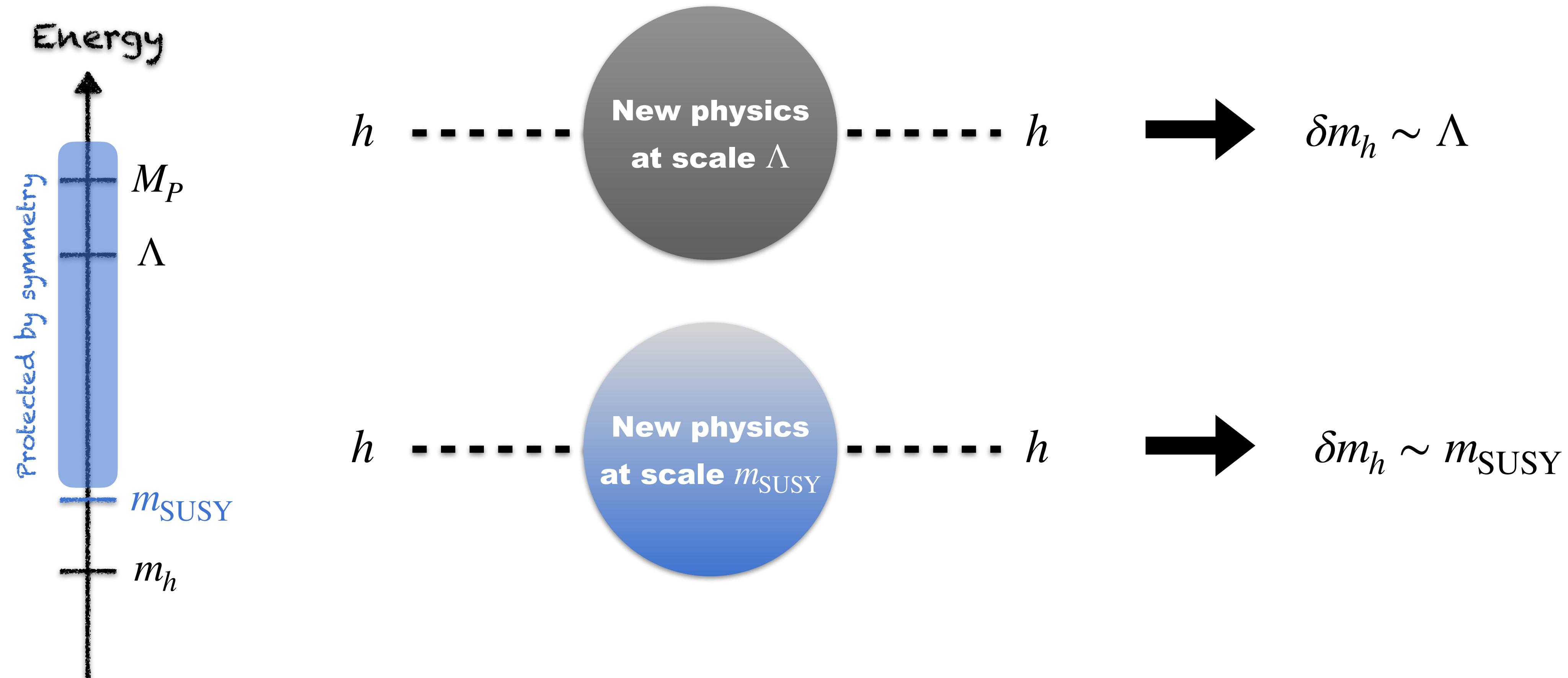
Using  $10^{34}$  protons, indirectly explores baryon violating Dim-6 operators at scales  $\Lambda \sim 10^{16}$  GeV.

What mysteries can we explore using these methods?

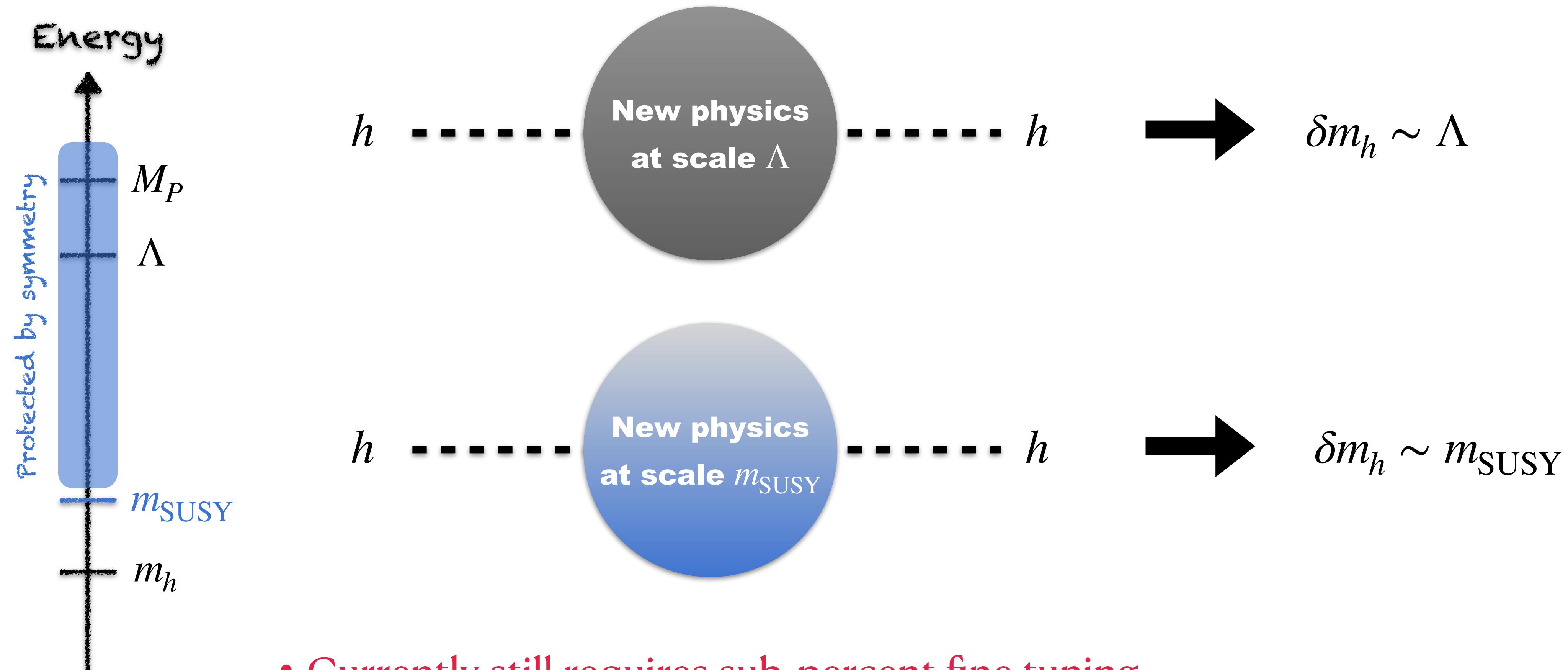
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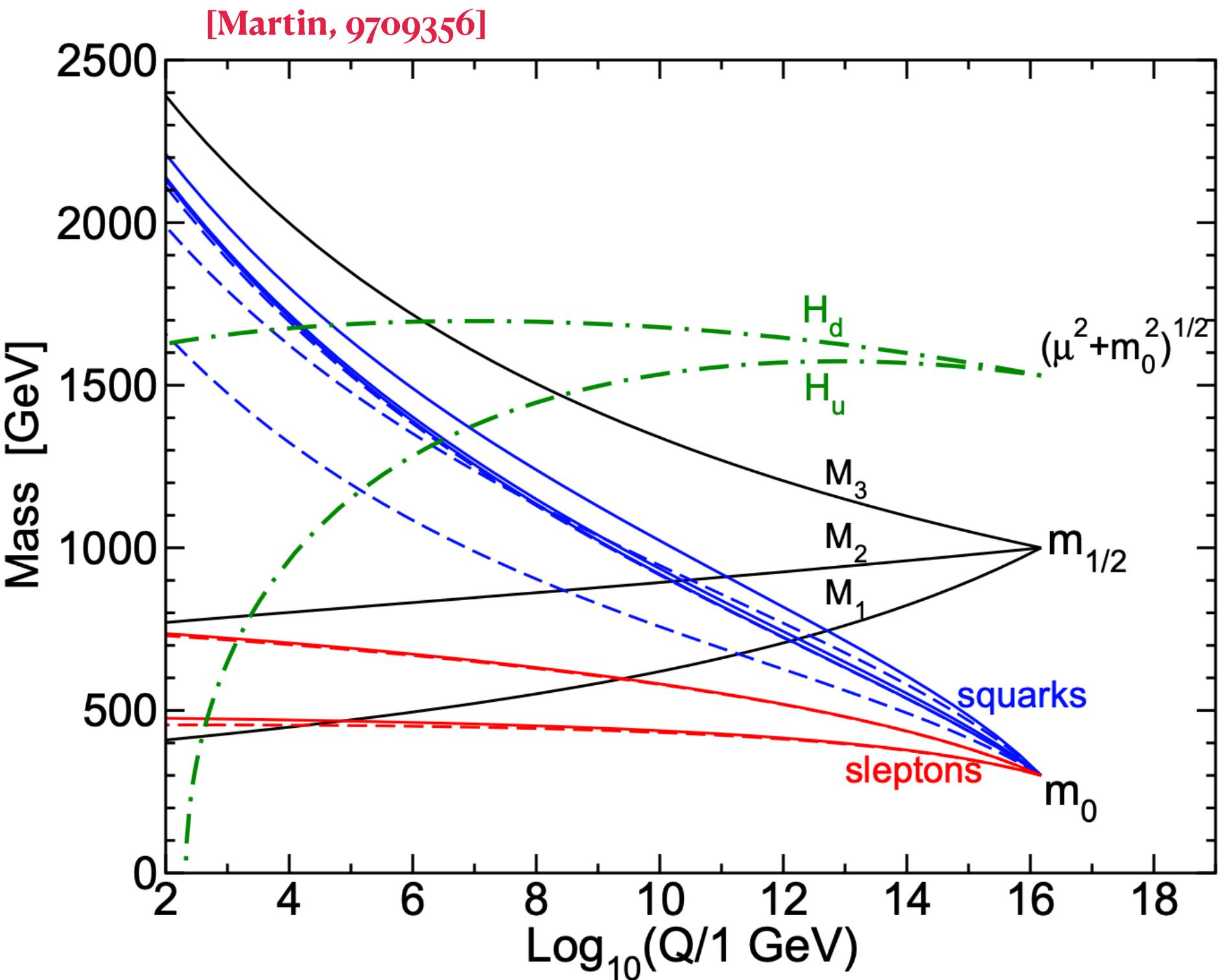


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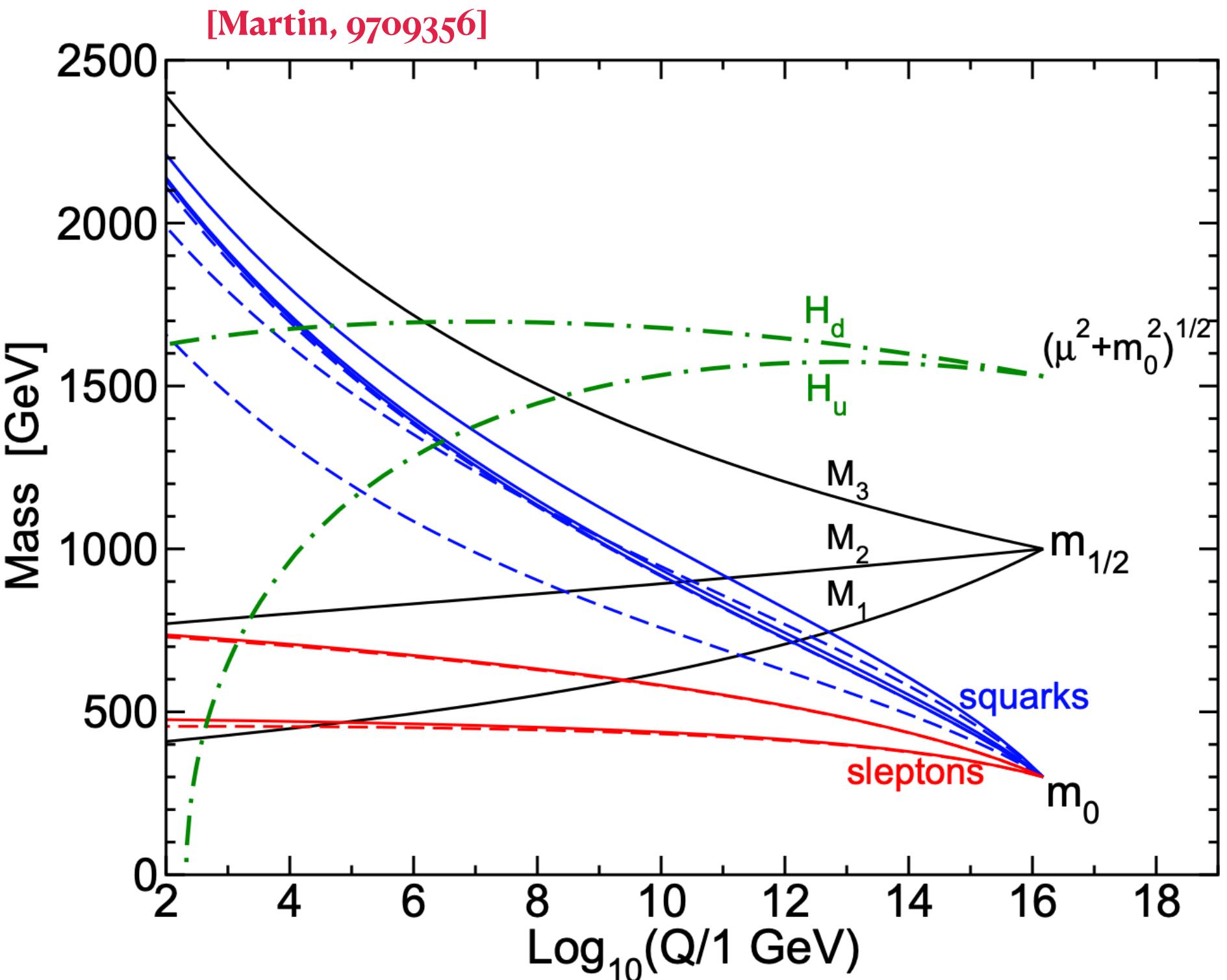
- Currently still requires sub-percent fine tuning.
- Strongest constraints are on colored sparticles (e.g. gluinos and squarks).

# Can the FCC-ee See What The LHC Can't?



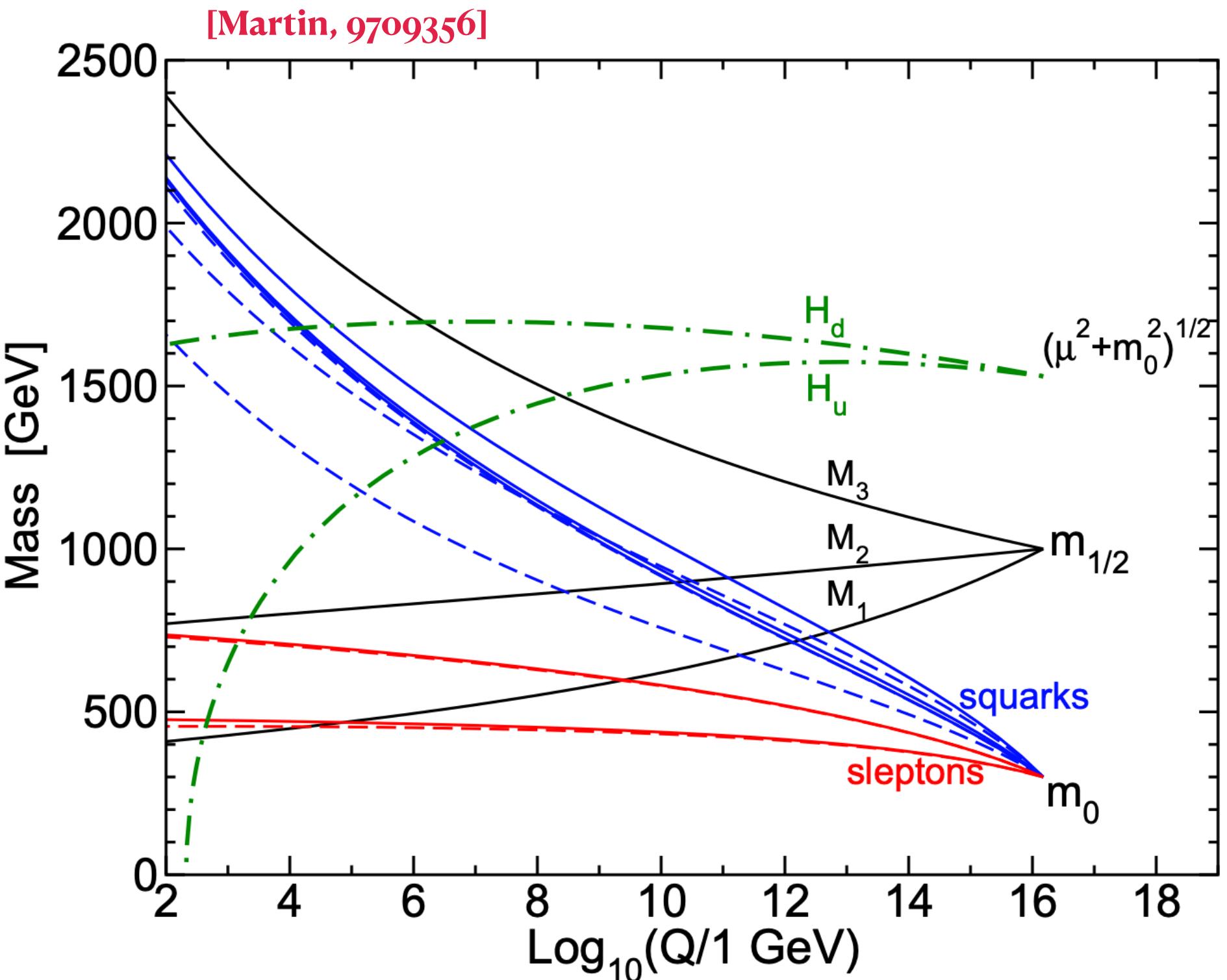
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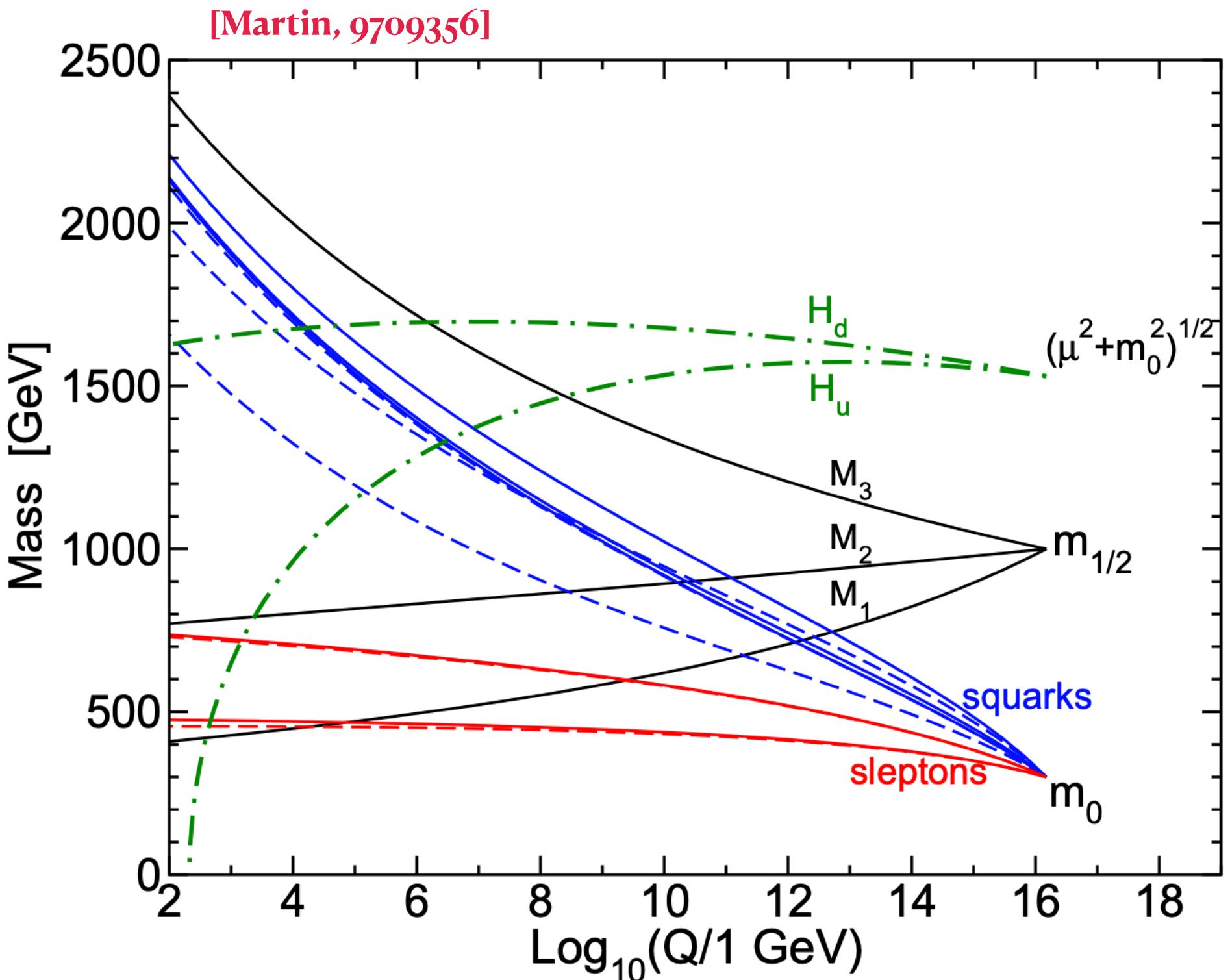
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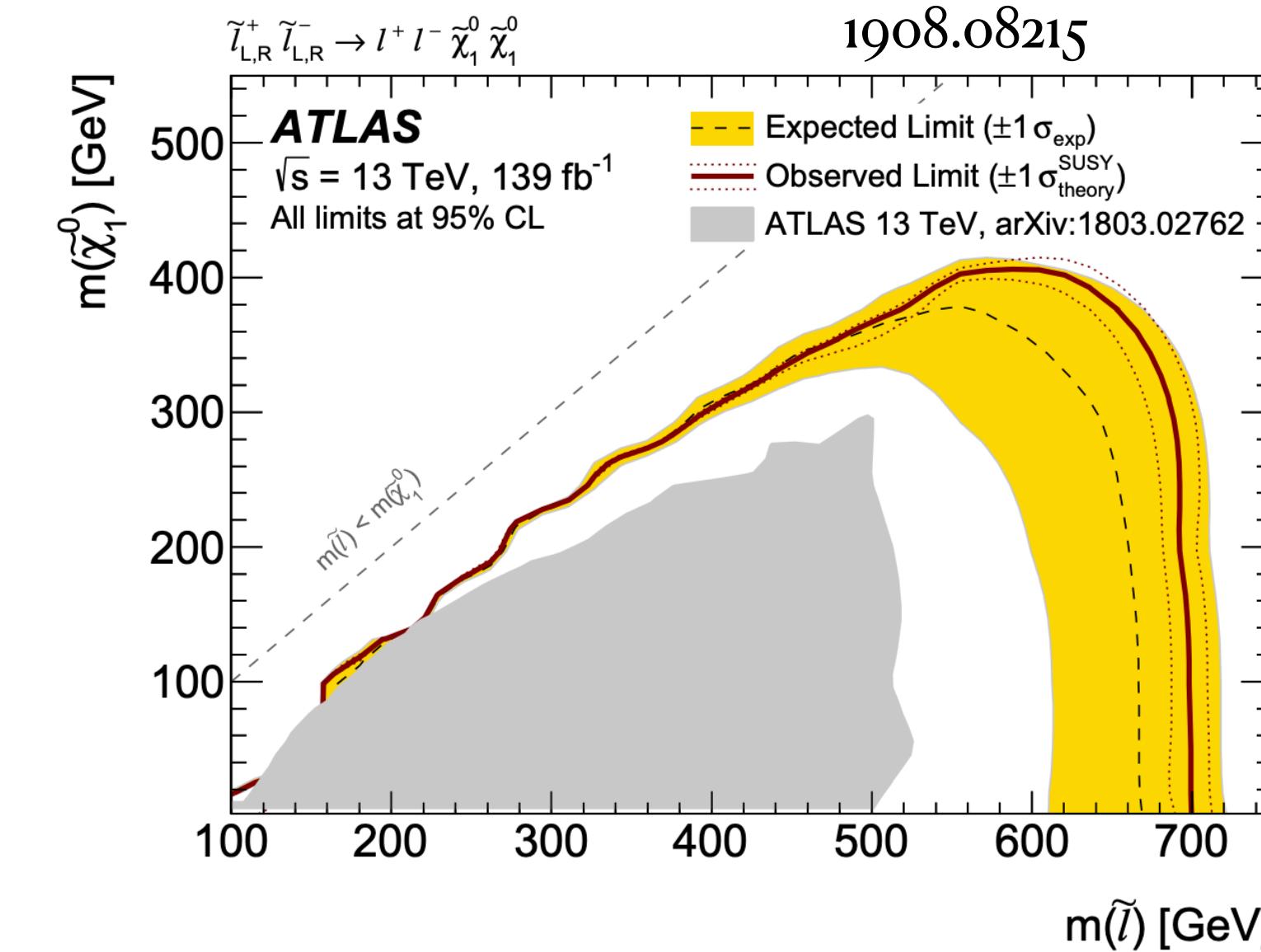
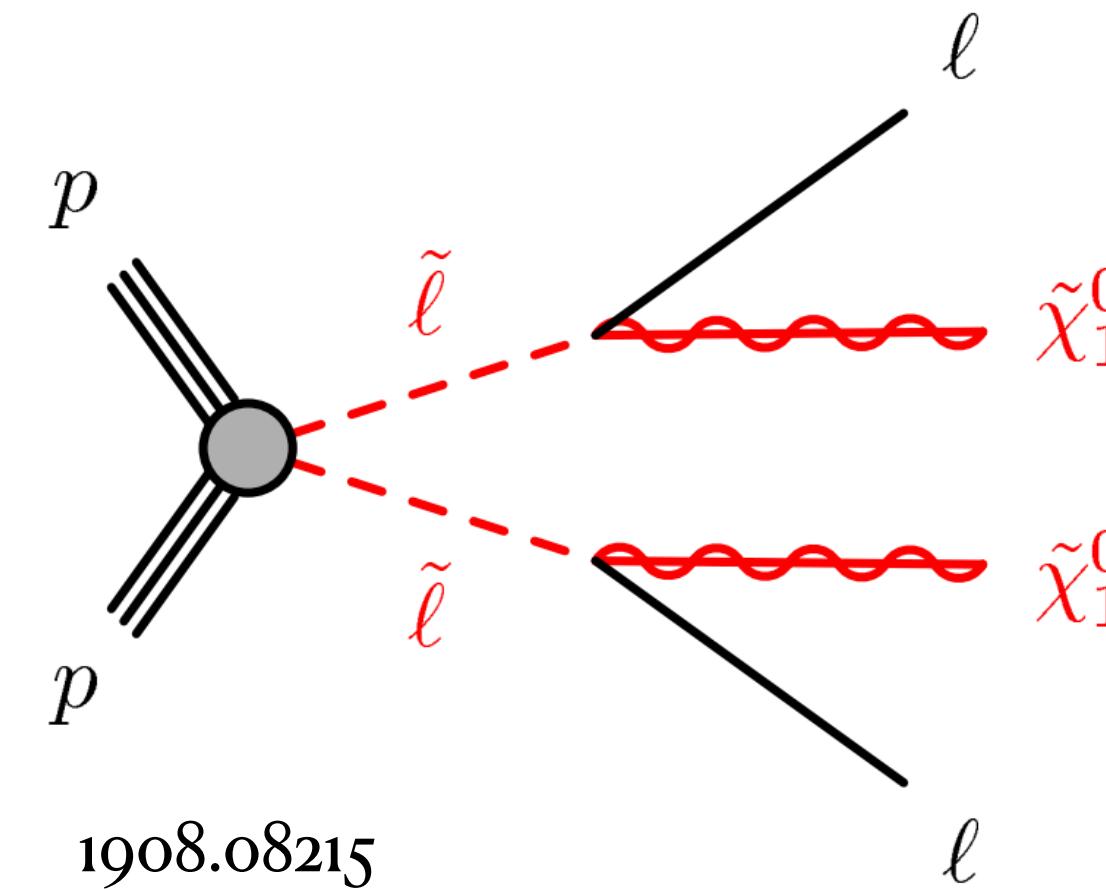


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⇒ FCC-ee may indirectly see SUSY using EWPTs even if the LHC sees nothing.

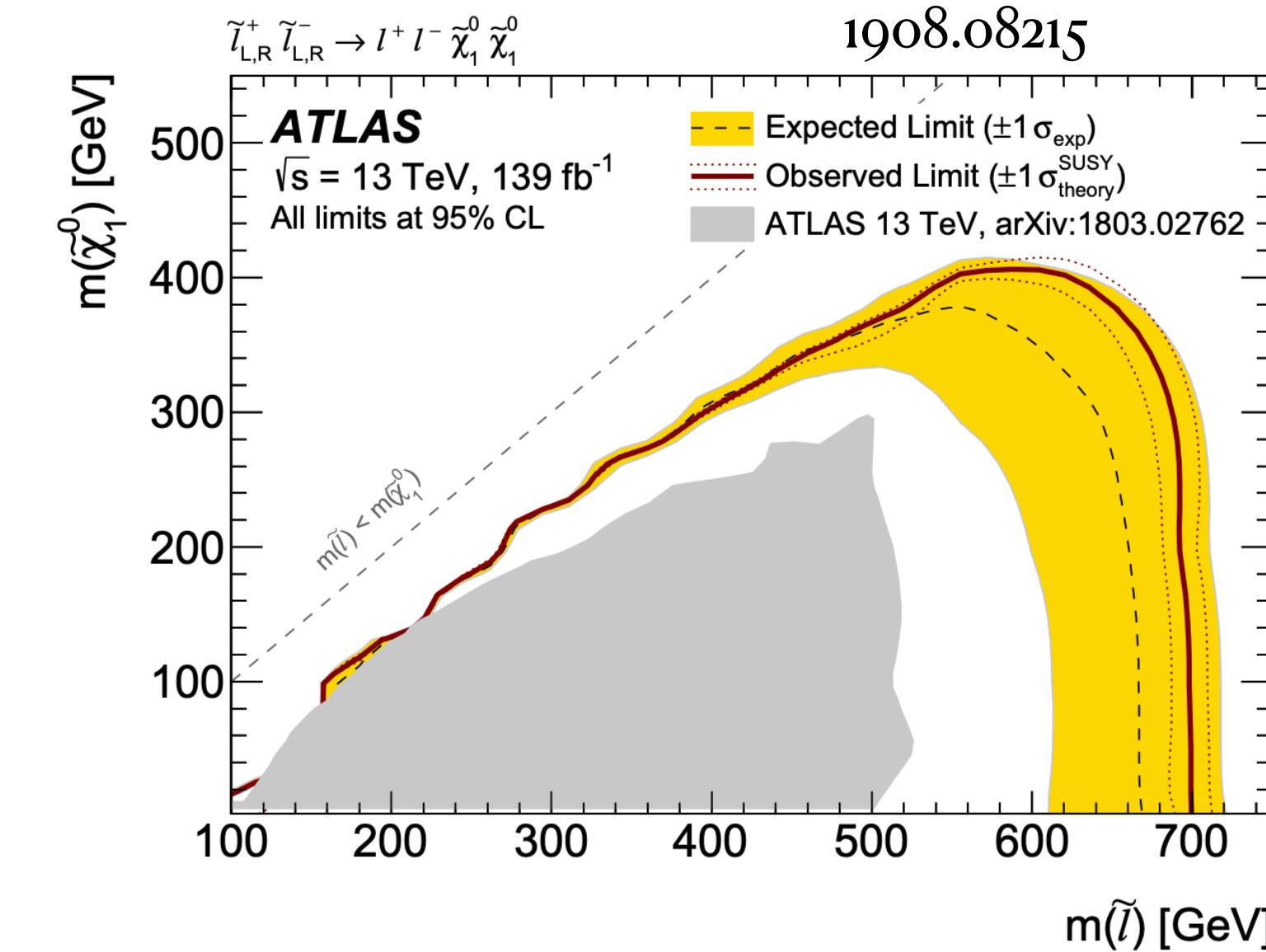
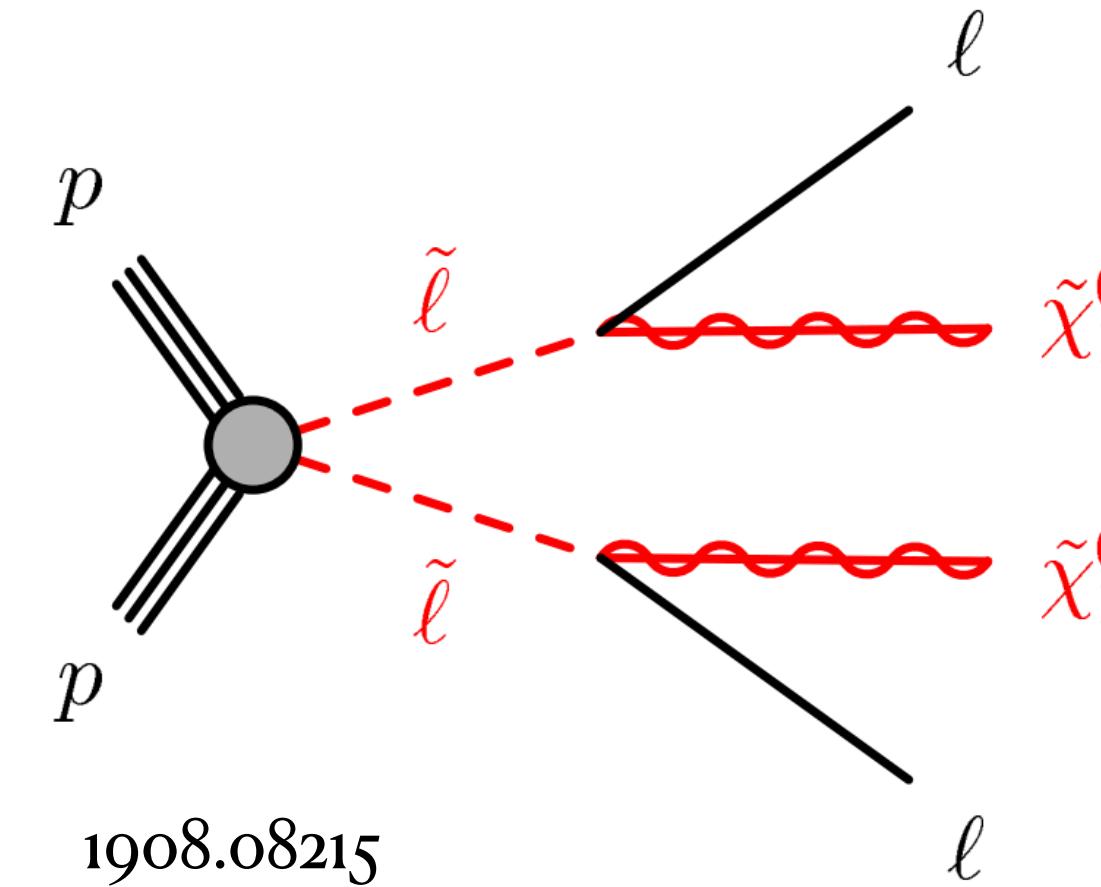
# Simplified SUSY Models

LHC SUSY searches often consider representative simplified models.



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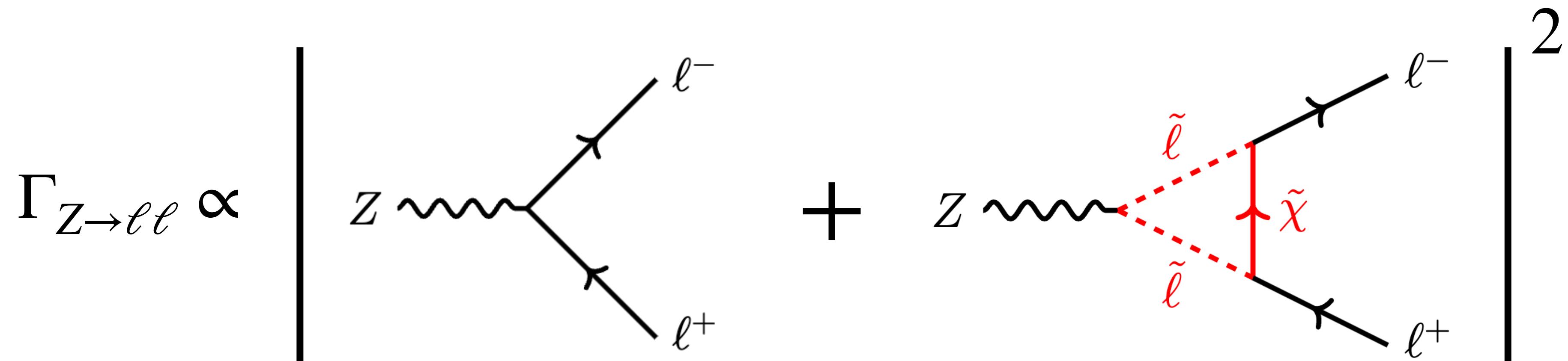


For simplicity we will do the same:

1. Pure Bino + RH Slepton model  $\supset (\tilde{B}, \tilde{e})$
2. Pure Wino + LH Slepton model  $\supset (\tilde{W}, \tilde{L})$ .

# How might SUSY show up in EWPTs?

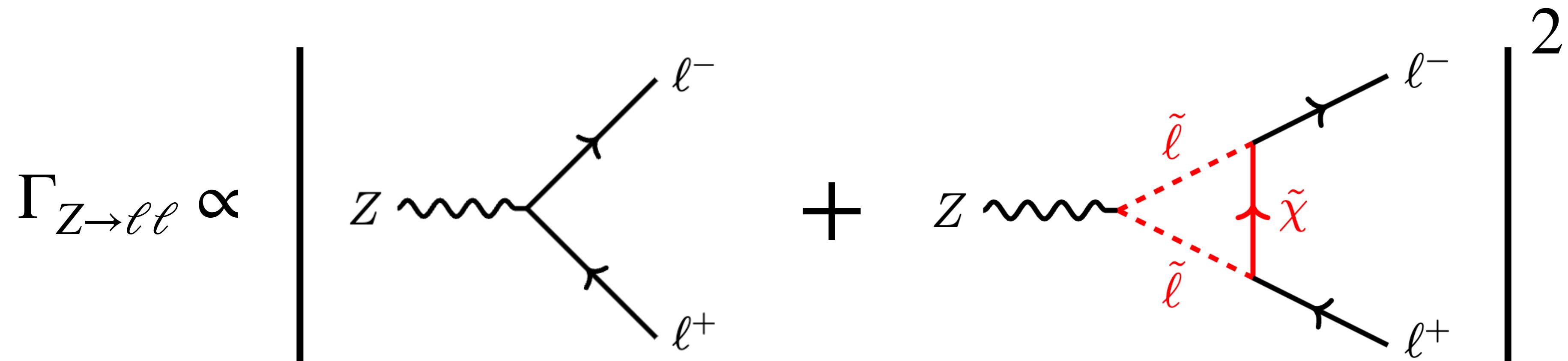
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$$\frac{\Gamma_{Z \rightarrow \ell\ell} - \Gamma_{Z \rightarrow \ell\ell}^{(SM)}}{\Gamma_{Z \rightarrow \ell\ell}^{(SM)}} \propto \frac{g^2}{16\pi^2} \left( \frac{m_Z}{M_{SUSY}} \right)^2 \longrightarrow M_{SUSY}^{\text{probed}} \sim 1 \text{ TeV} \times \left( \frac{\delta\Gamma/\Gamma}{10^{-5}} \right)$$

# Some details

---

$\Gamma(Z \rightarrow \ell\bar{\ell})$  is not the best observable. Instead we use

$$R_\ell \equiv \frac{\Gamma(Z \rightarrow \text{hadrons})}{\Gamma(Z \rightarrow \ell\bar{\ell})}$$

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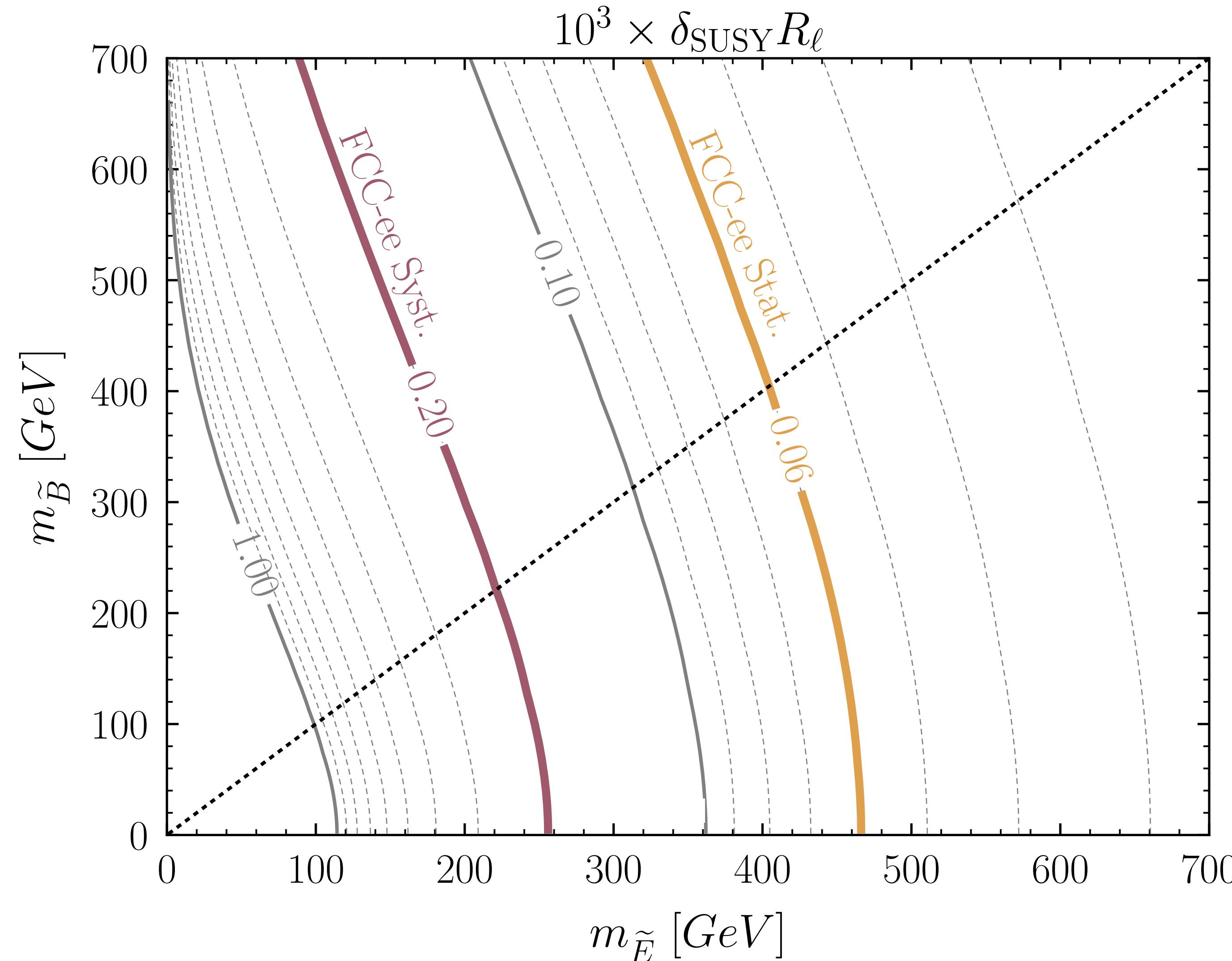
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Still depends on  $\theta_W$  and  $\alpha_s(M_Z)$ . These must be determined by other measurements.

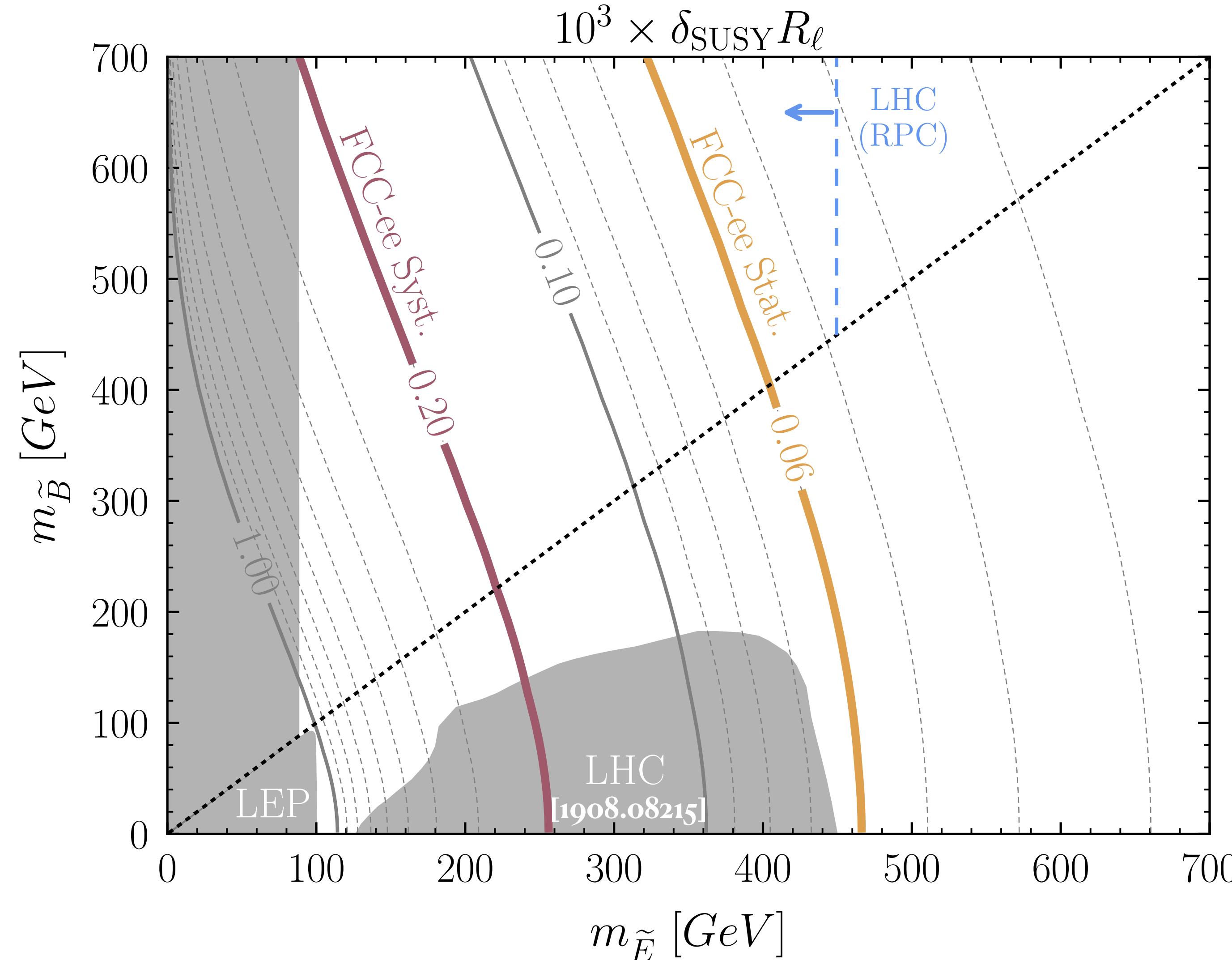
# Results

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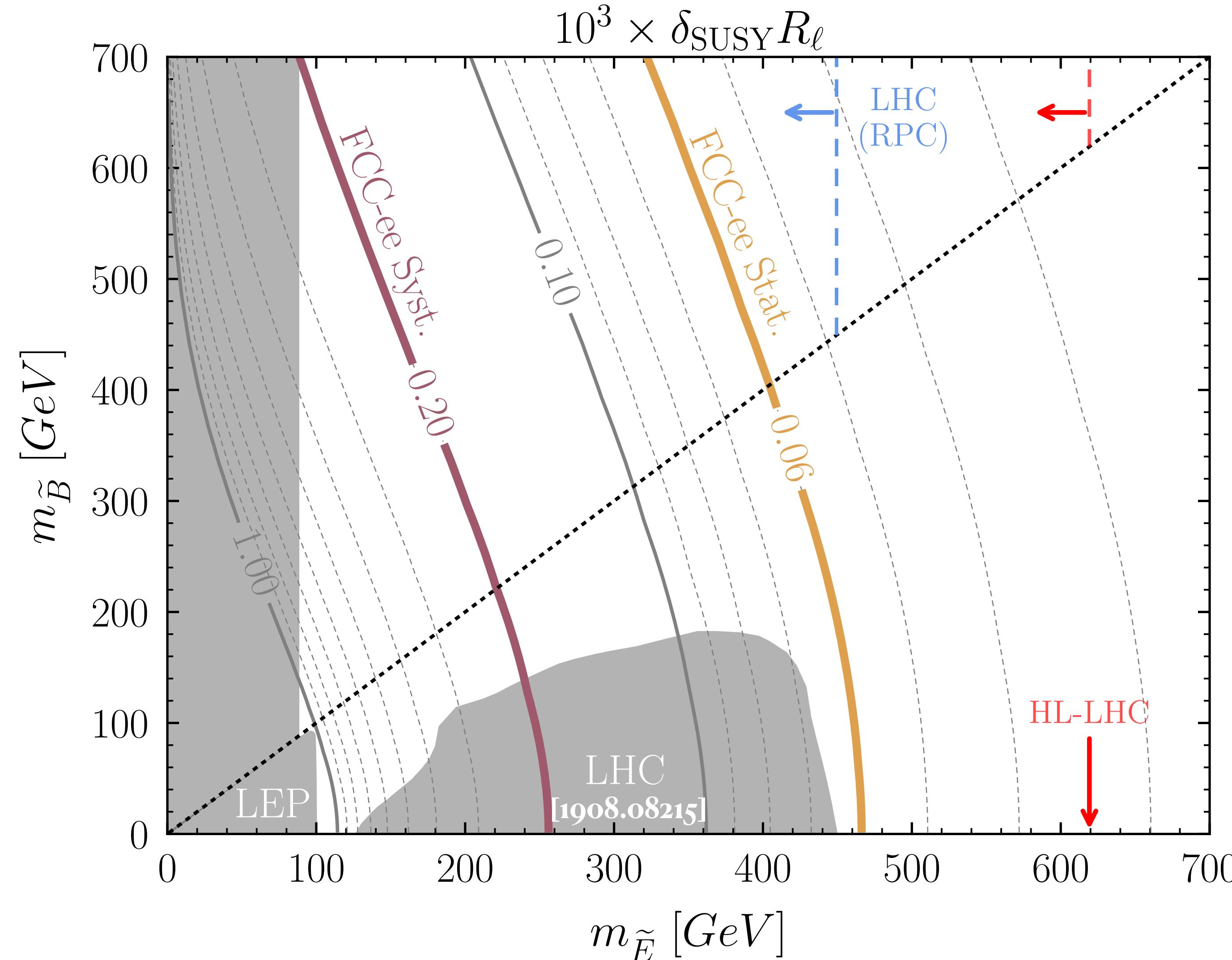
**Bino + RH Slepton  
(Preliminary)**

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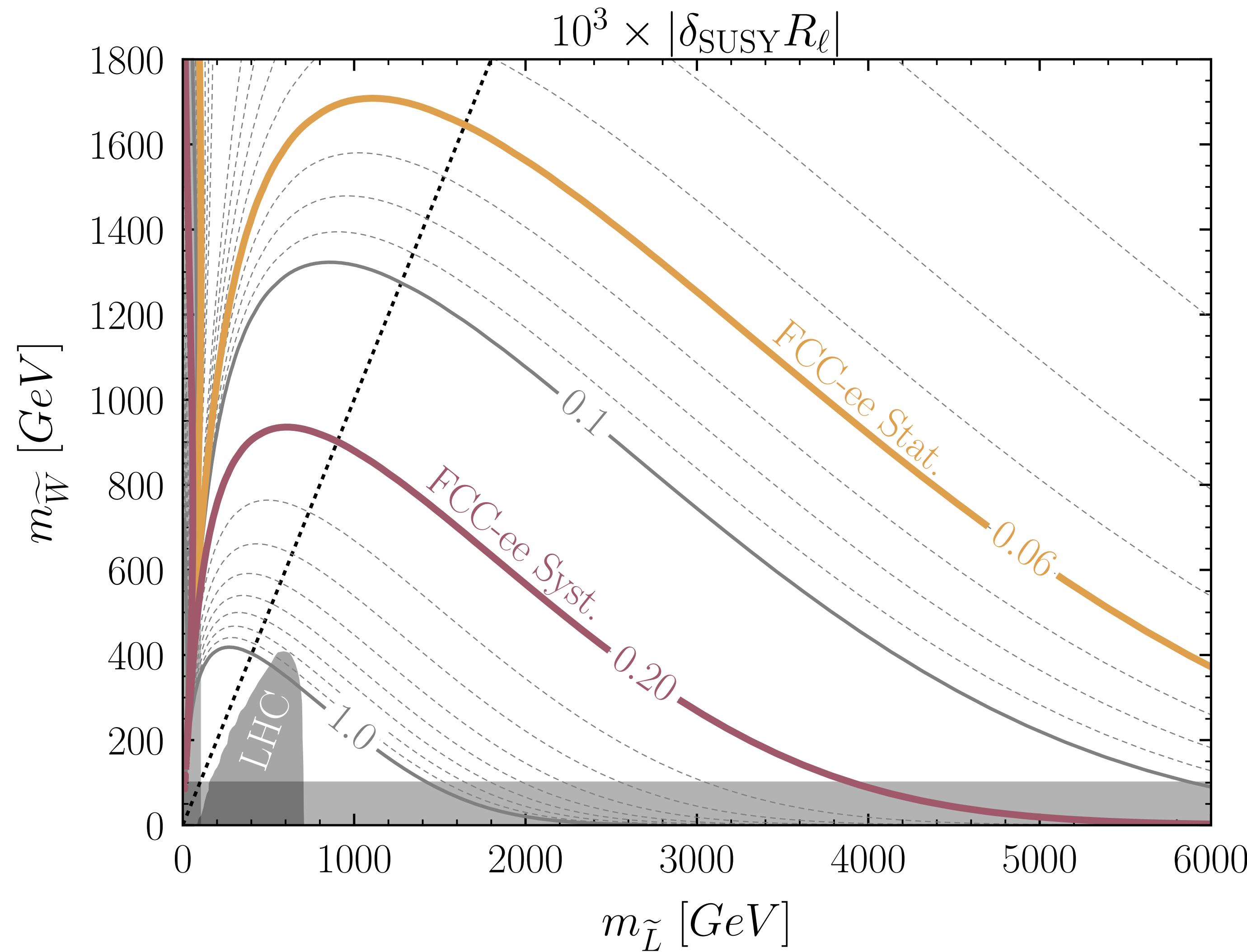
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# Results

$\cos(2\beta) = 0$



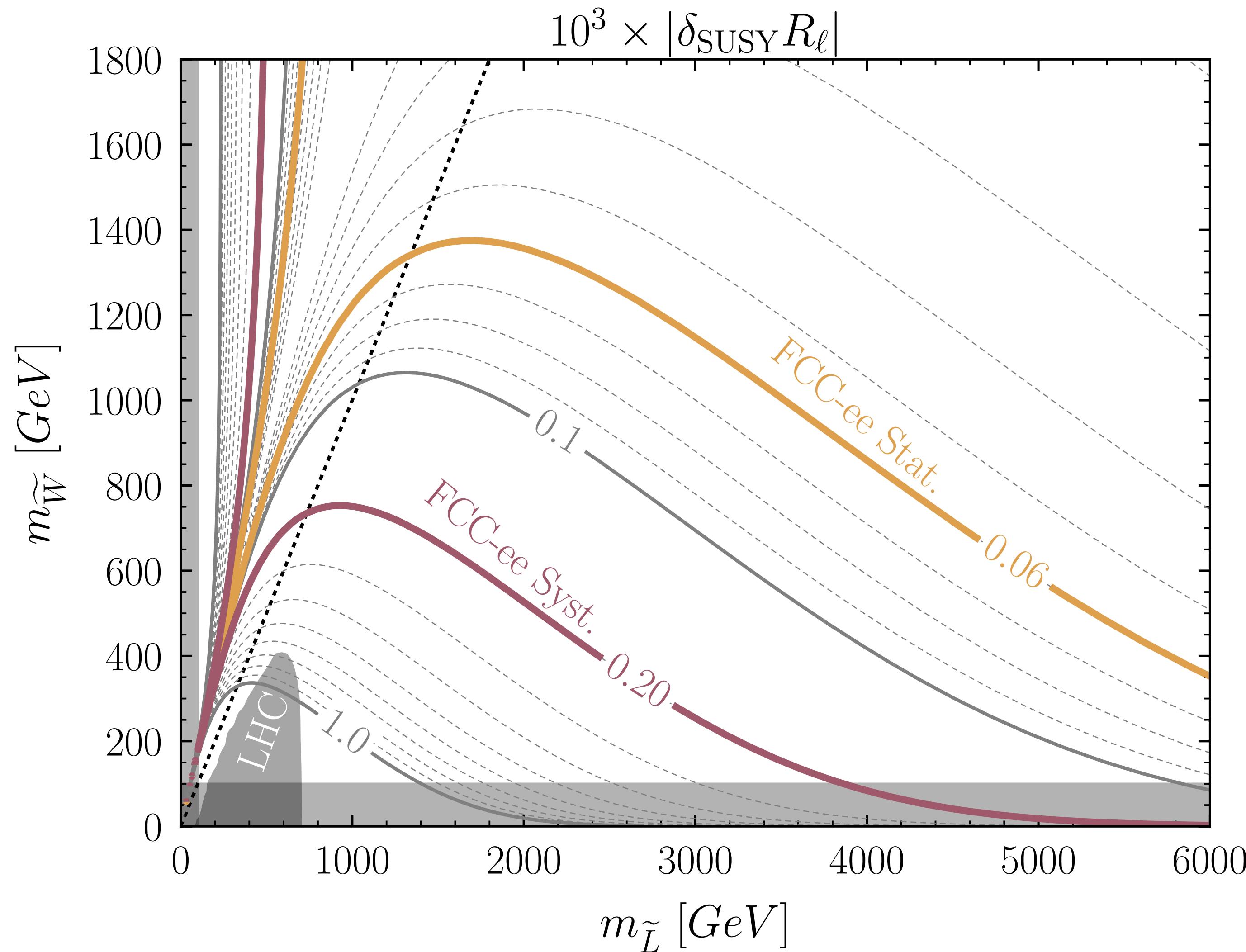
**Wino + LH Slepton  
(Preliminary)**

[1908.08215]

Kevin Langhoff - SUSY at Tera-Z

# Results

$\cos(2\beta) = -1$



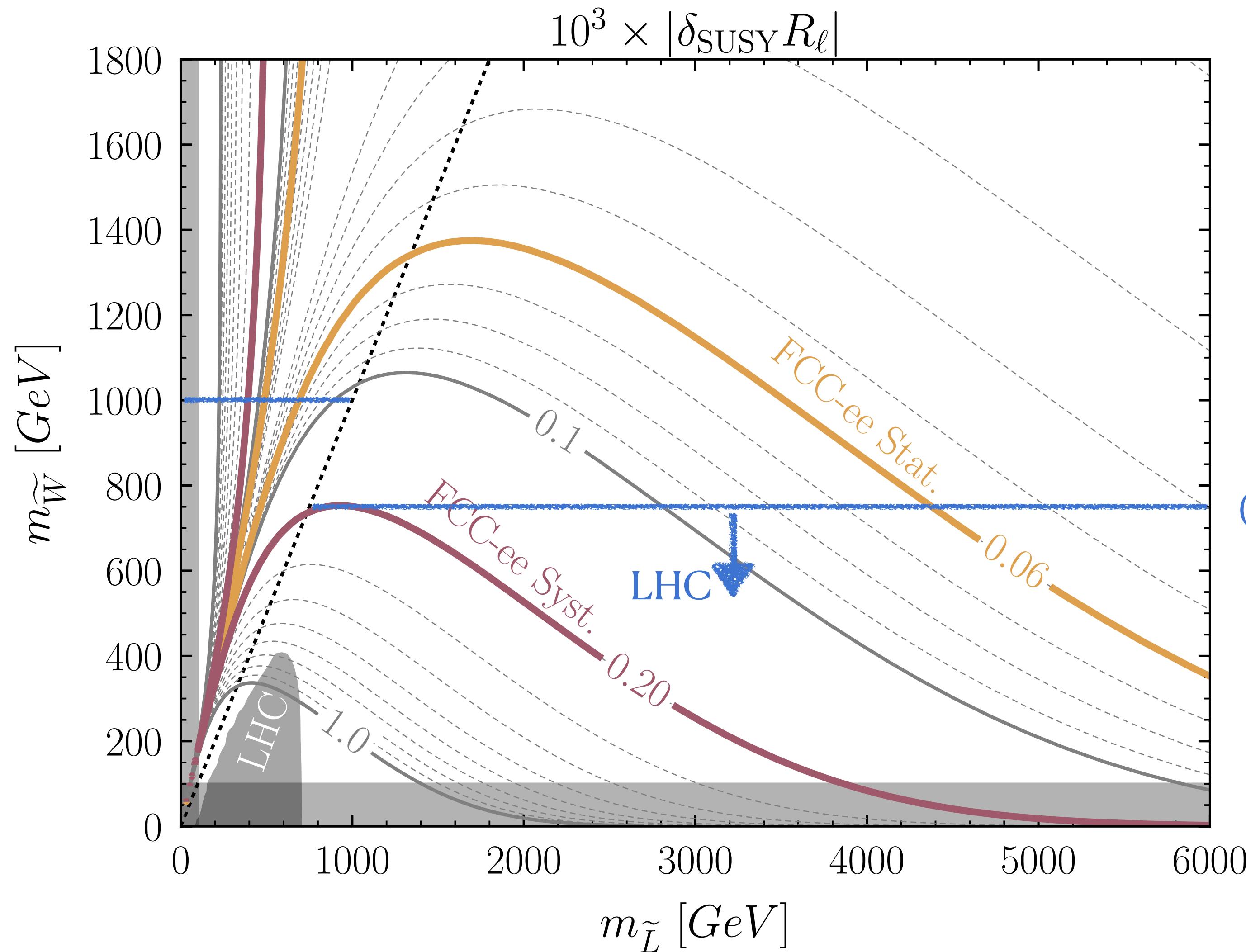
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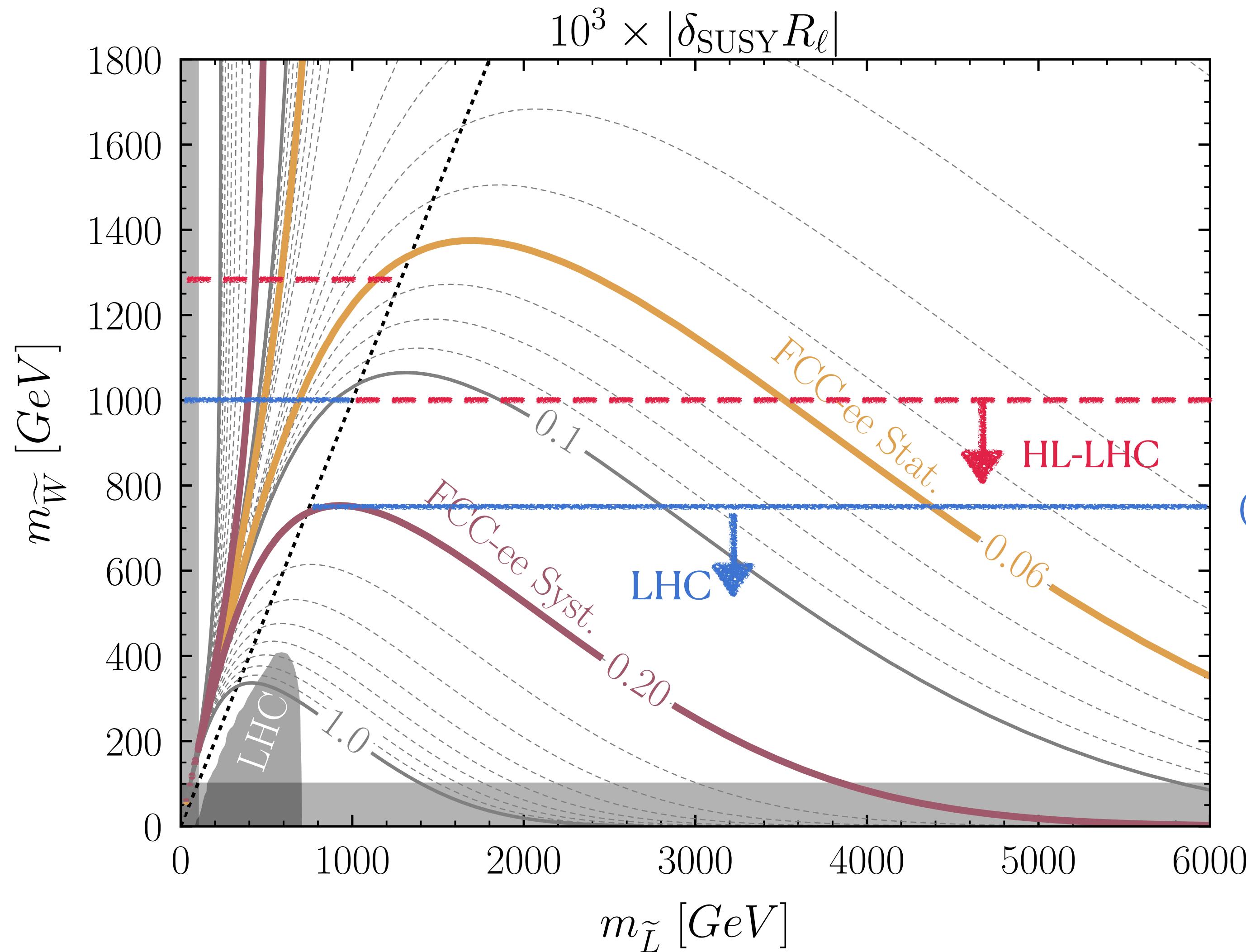
(Depends on  $m_{\chi_1^0}$ !)

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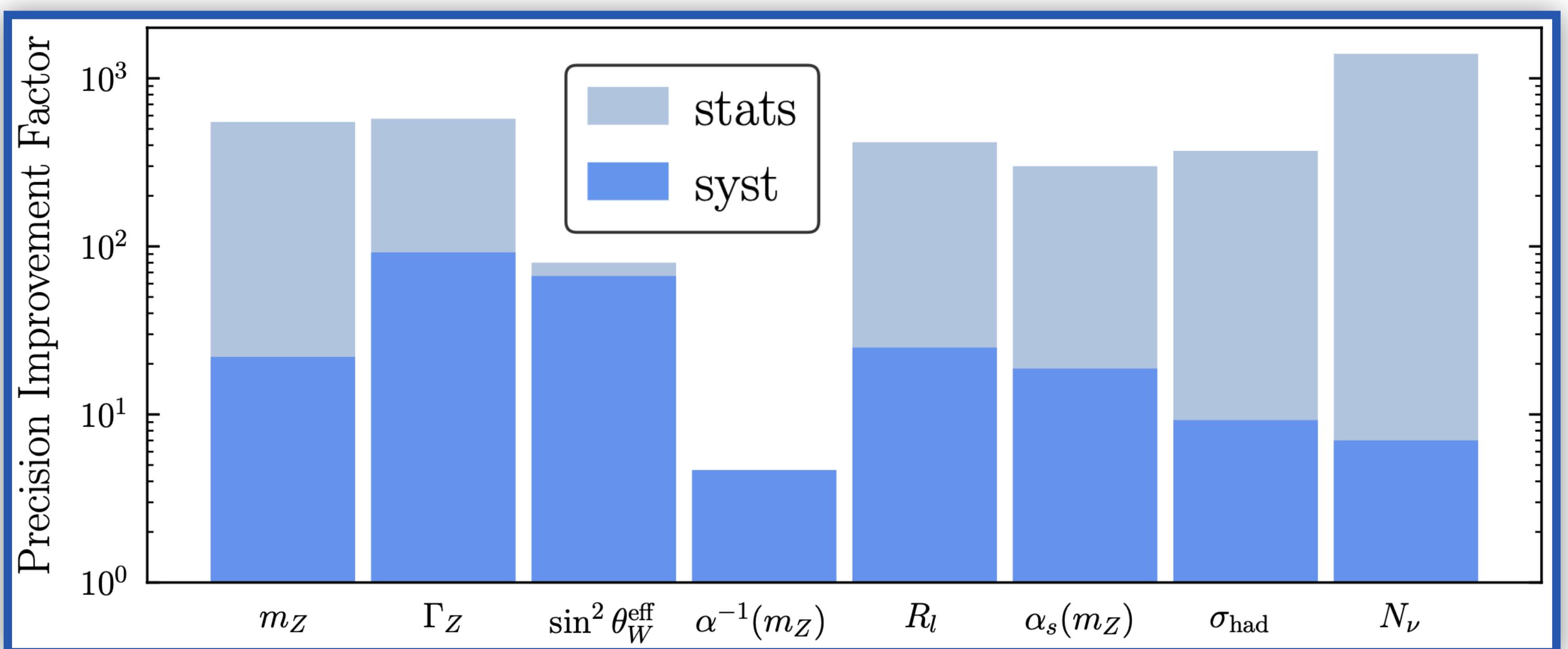
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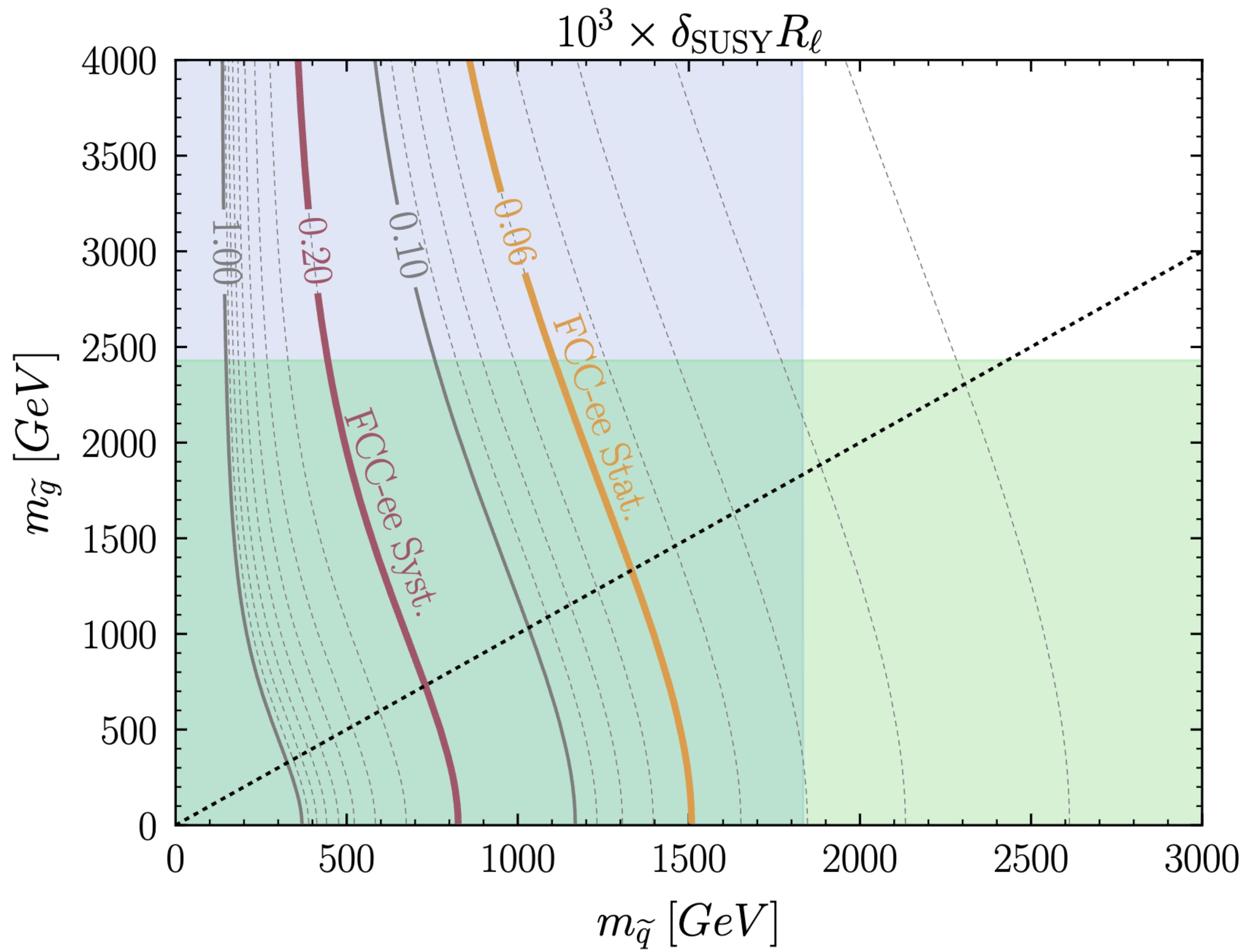
Kevin Langhoff - SUSY at Tera-Z

# Conclusion

- EWPTs at the FCC-ee are interesting/complimentary ways to search for new physics.
- There exists some SUSY parameter space which may be explored at the FCC-ee.
- A more thorough investigation into which observables/signatures are motivated by various models may motivate further dedication to the reduction of certain systematics.

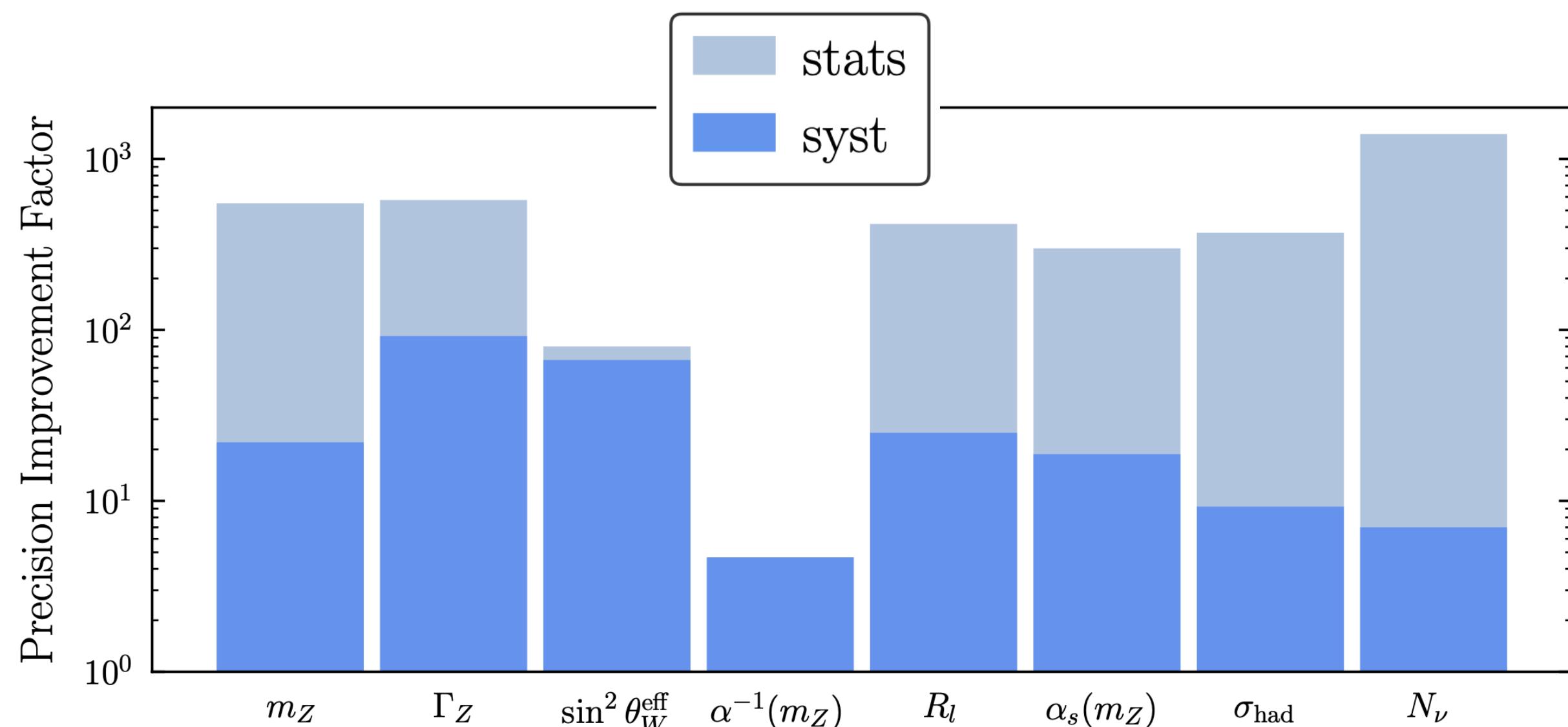


# Backup Slides



# Electroweak Precision Tests at the Z-pole

There are many measurements which can be performed at the Z-pole.



Many measurements are systematics limited!

Which systematics should we prioritize reducing?

Observable	Present value $\pm$ error	FCC-ee Stat.	FCC-ee Syst.
$m_Z$ (keV)	$91,186,700 \pm 2200$	5	100
$\Gamma_Z$ (keV)	$2,495,200 \pm 2300$	8	100
$R_\ell^Z (\times 10^3)$	$20,767 \pm 25$	0.06	0.2–1.0
$\alpha_s(m_Z) (\times 10^4)$	$1196 \pm 30$	0.1	0.4–1.6
$R_b (\times 10^6)$	$216,290 \pm 660$	0.3	< 60
$\sigma_{\text{had}}^0 (\times 10^3)$ (nb)	$41,541 \pm 37$	0.1	4
$N_\nu (\times 10^3)$	$2991 \pm 7$	0.005	1
$\sin^2 \theta_W^{\text{eff}} (\times 10^6)$	$231,480 \pm 160$	3	2–5
$1/\alpha_{\text{QED}}(m_Z) (\times 10^3)$	$128,952 \pm 14$	4	Small
$A_{\text{FB}}^{b,0} (\times 10^4)$	$992 \pm 16$	0.02	1–3
$A_{\text{FB}}^{\text{pol},\tau} (\times 10^4)$	$1498 \pm 49$	0.15	< 2
$m_W$ (MeV)	$80,350 \pm 15$	0.5	0.3
$\Gamma_W$ (MeV)	$2085 \pm 42$	1.2	0.3
$\alpha_s(m_W) (\times 10^4)$	$1170 \pm 420$	3	Small
$N_\nu (\times 10^3)$	$2920 \pm 50$	0.8	Small
$m_{\text{top}}$ (MeV)	$172,740 \pm 500$	17	Small
$\Gamma_{\text{top}}$ (MeV)	$1410 \pm 190$	45	Small
$\lambda_{\text{top}}/\lambda_{\text{top}}^{\text{SM}}$	$1.2 \pm 0.3$	0.1	Small
ttZ couplings	$\pm 30\%$	0.5–1.5%	Small

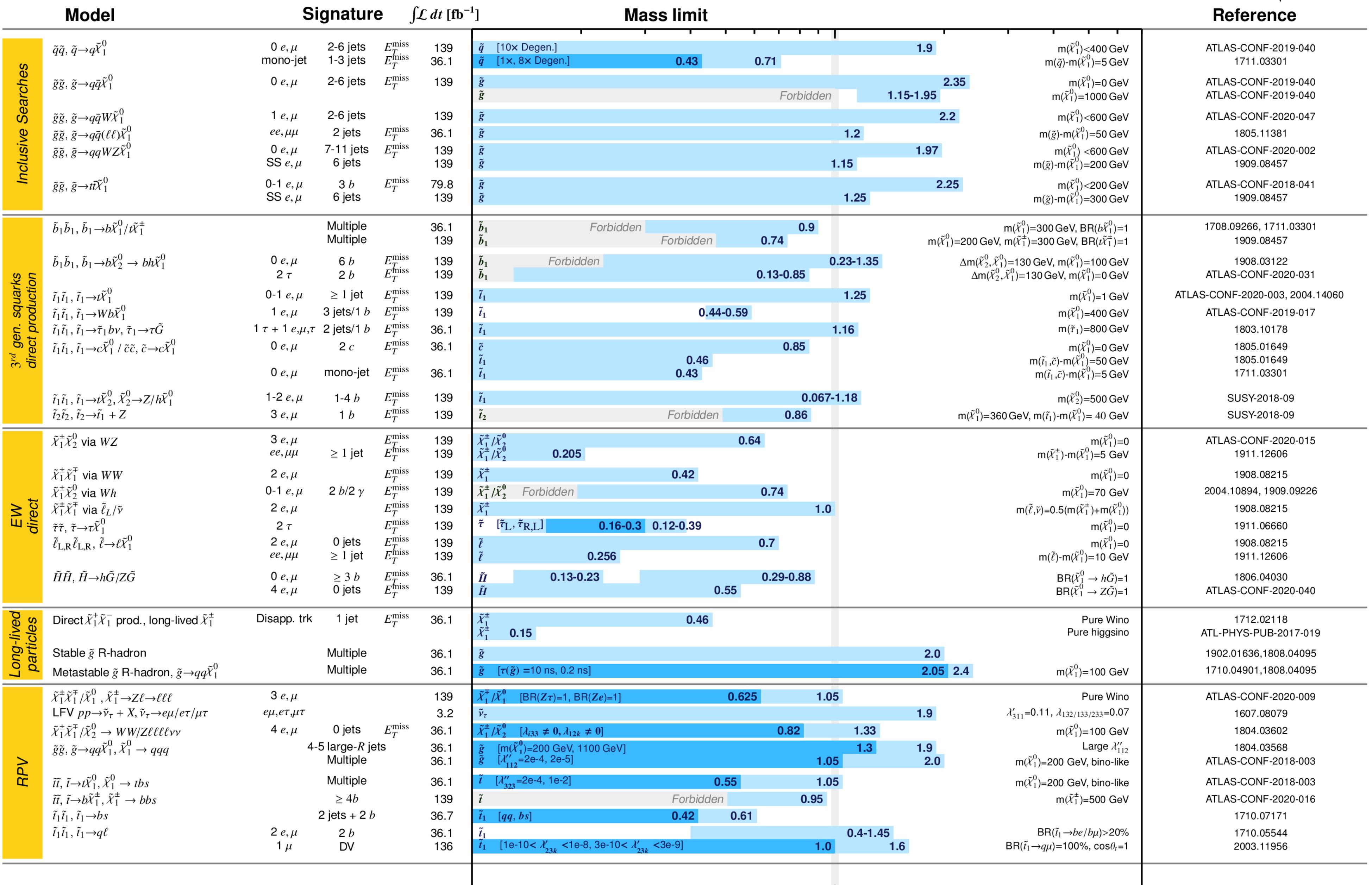
[FCC CDR]

# ATLAS SUSY Searches\* - 95% CL Lower Limits

July 2020

ATLAS Preliminary

$\sqrt{s} = 13 \text{ TeV}$



\*Only a selection of the available mass limits on new states or phenomena is shown. Many of the limits are based on simplified models, c.f. refs. for the assumptions made.

# Oblique Corrections

- Assuming heavy new physics dominantly modifies SM gauge boson propagators, corrections from heavy new physics can be quantified by a set of oblique parameters.



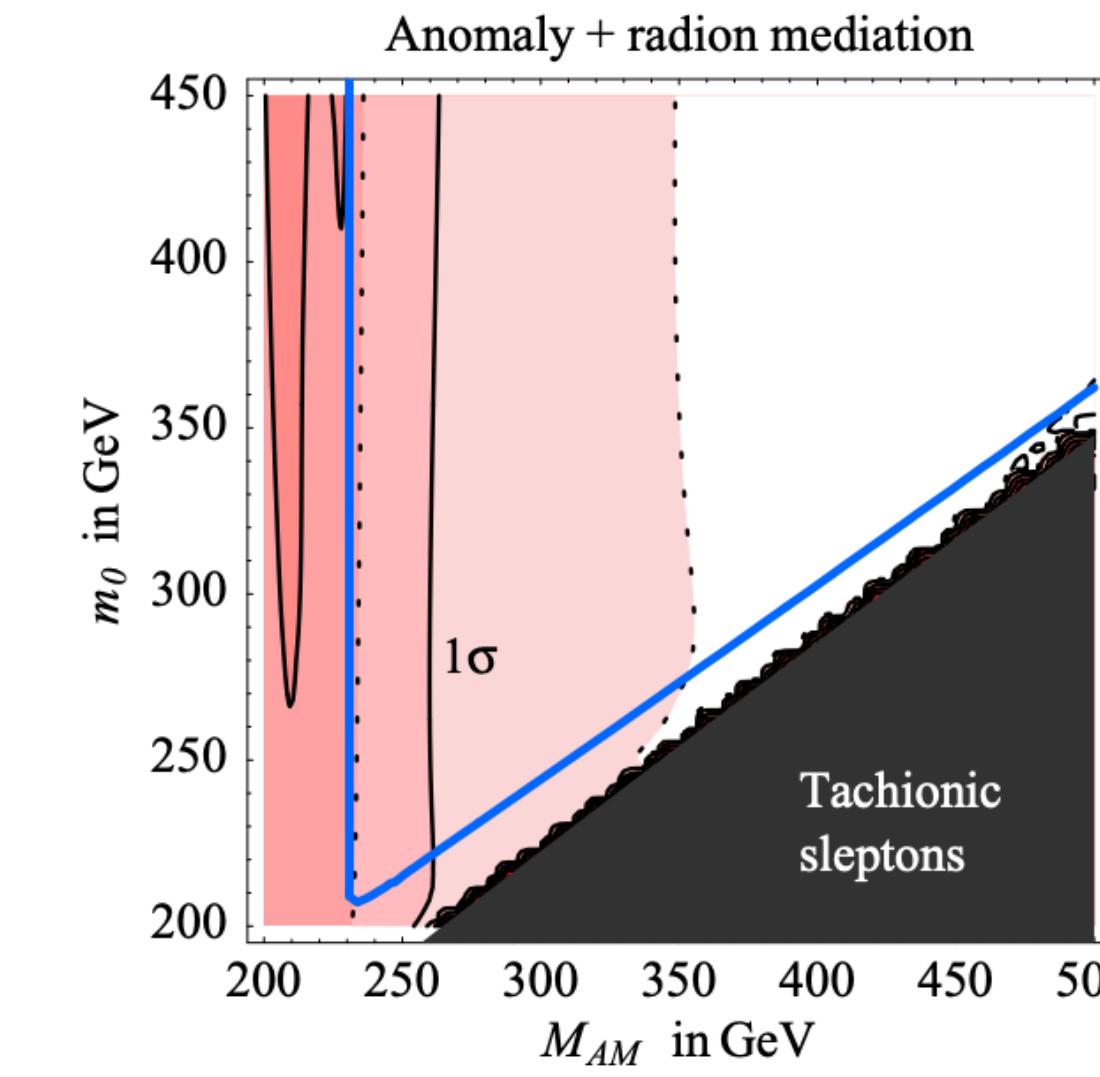
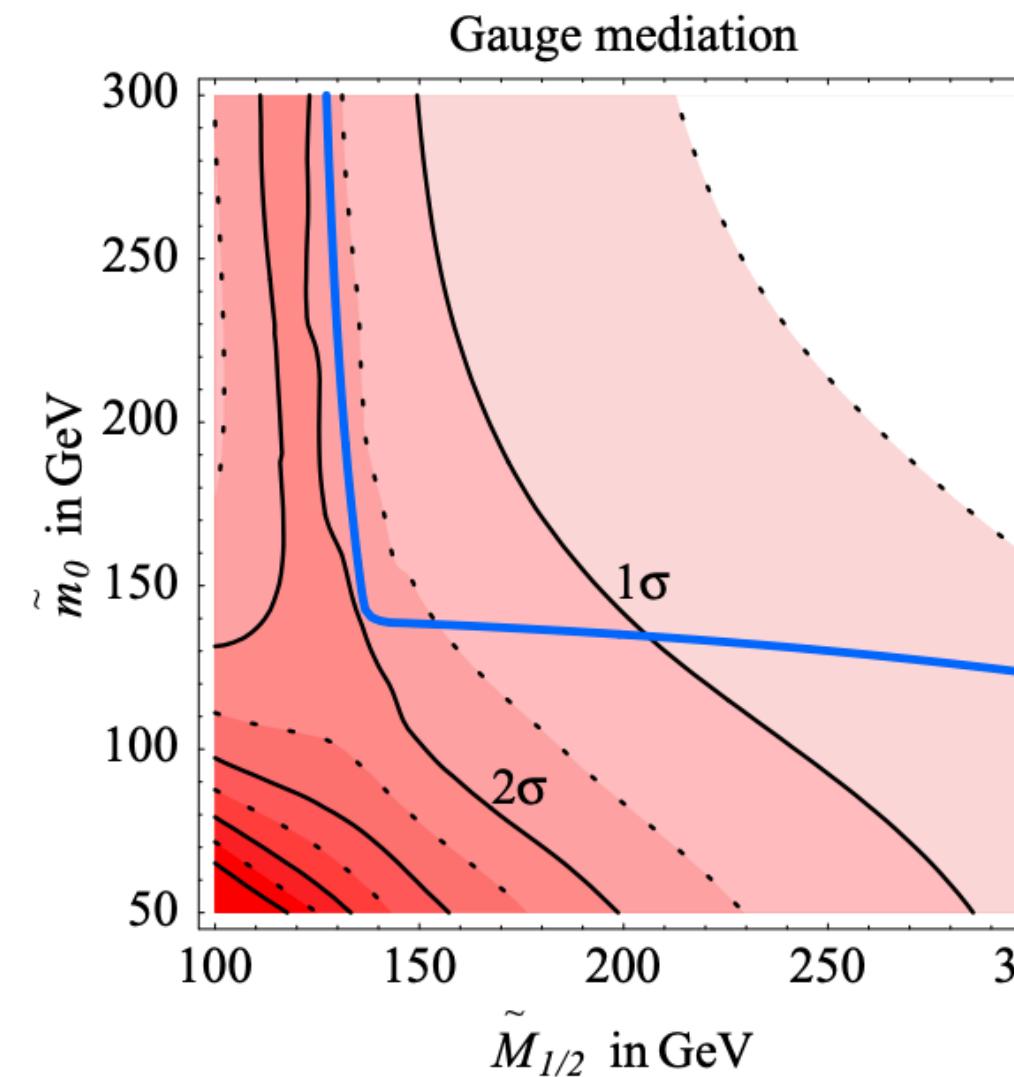
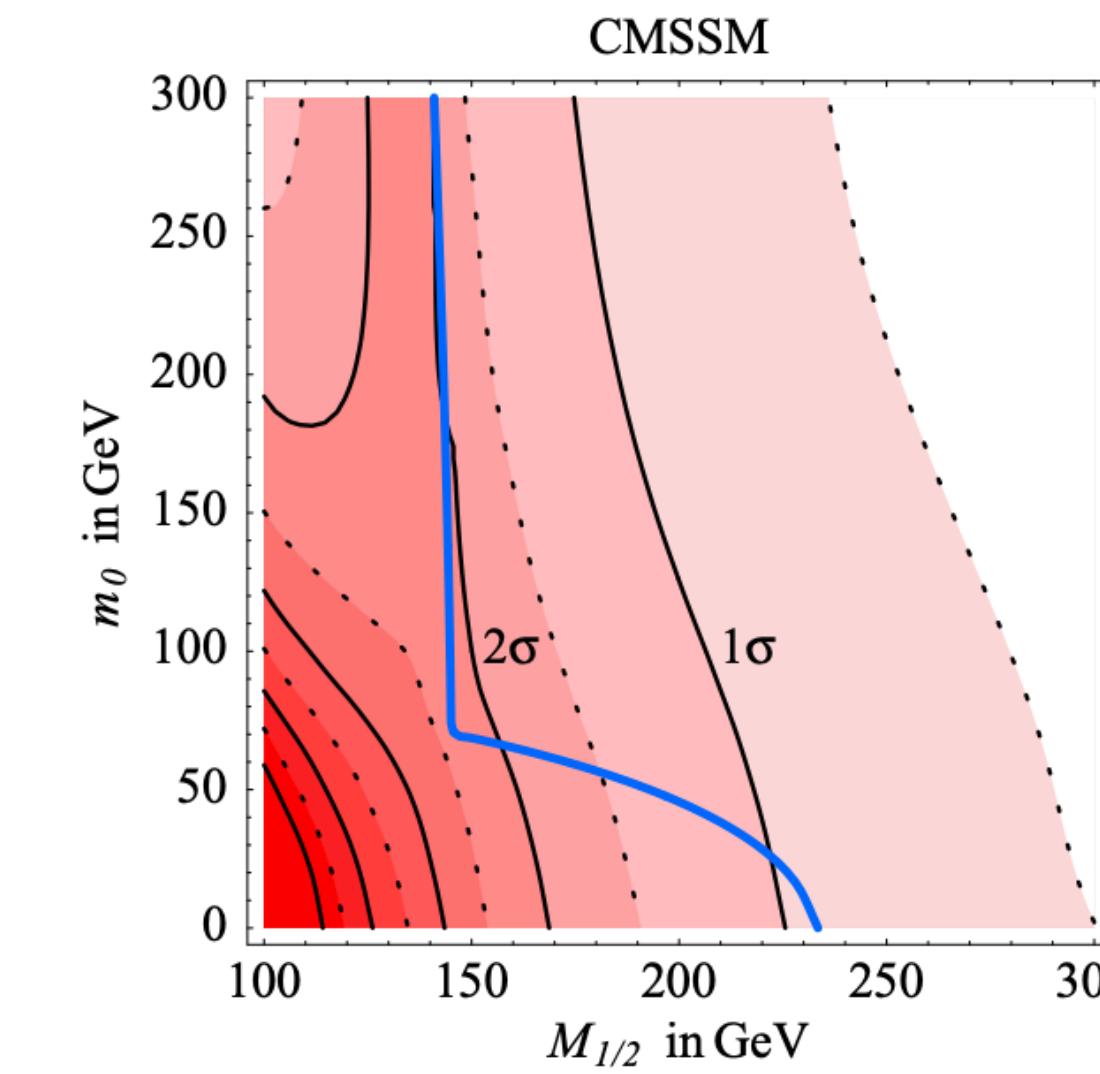
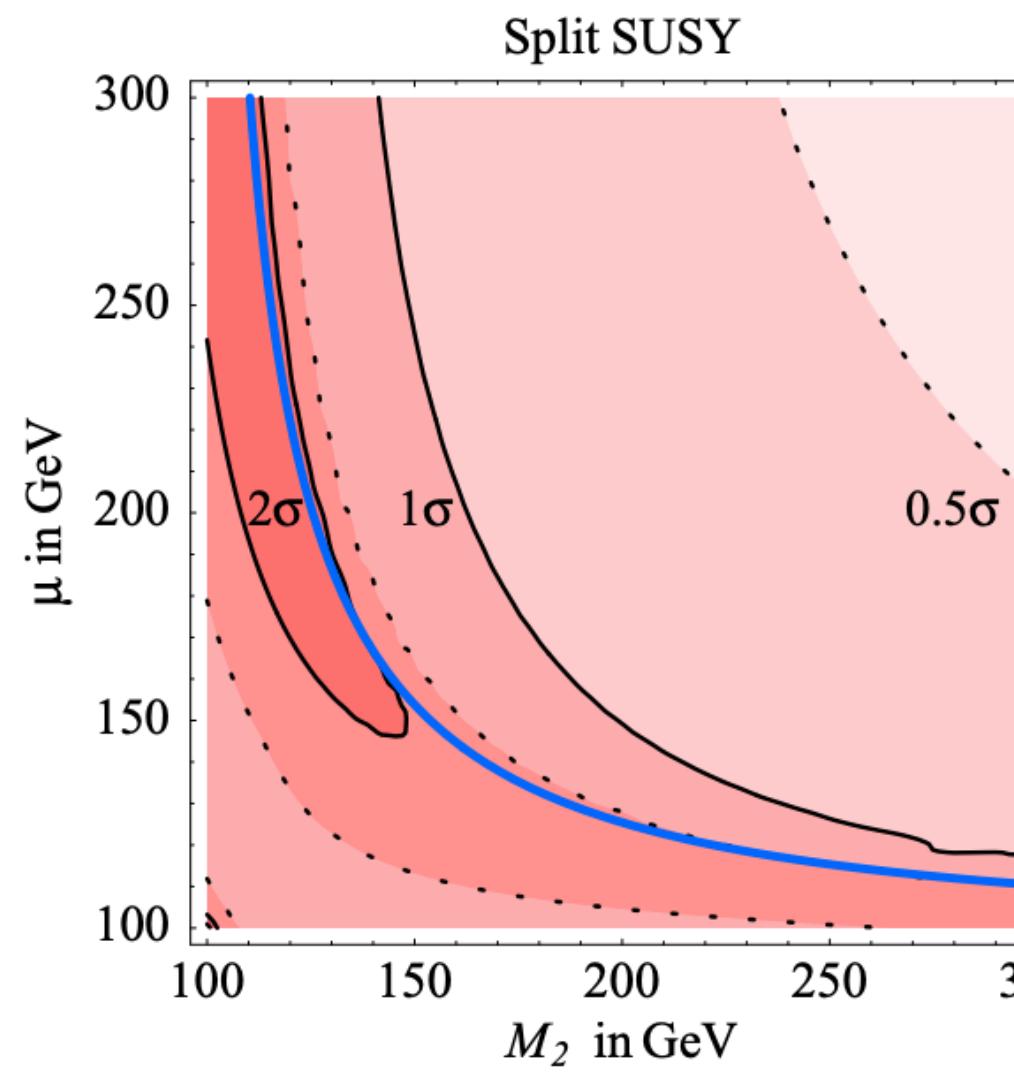
Oblique parameter	Corresponding dim-6 operator
$\hat{S} = \frac{g}{g'} \Pi'_{W^3 B}(0)$	$\mathcal{O}_S = H^\dagger \tau^a H W_{\mu\nu}^a B^{\mu\nu}$
$\hat{T} = m_W^{-2} [\Pi_{W^3 W^3}(0) - \Pi_{W^+ W^-}(0)]$	$\mathcal{O}_T =  H^\dagger D_\mu H ^2$
$W = \frac{1}{2} m_W^2 \Pi''_{W^3 W^3}(0)$	$\mathcal{O}_W = \frac{1}{2} (D_\rho W_{\mu\nu}^a)^2$
$Y = \frac{1}{2} m_W^2 \Pi''_{BB}(0)$	$\mathcal{O}_Y = \frac{1}{2} (\partial_\rho B_{\mu\nu})^2$

- Simple, but not completely general.

$X$	$\hat{S} \times \left( \frac{m_X^2}{m_W^2} \right)$	$\hat{T} \times \left( \frac{m_X^2}{m_W^2} \right)$	$W \times \left( \frac{m_X^2}{m_W^2} \right)$	$Y \times \left( \frac{m_X^2}{m_W^2} \right)$
$\tilde{E}$	0	0	0	$\frac{\alpha_Y}{40\pi}$
$\tilde{L}$	$-\frac{\alpha_W c_{2\beta}}{16\pi}$	$\frac{\alpha_W c_{2\beta}^2}{16\pi}$	$\frac{\alpha_W}{80\pi}$	$\frac{\alpha_Y}{80\pi}$
$\tilde{B}$	0	0	0	0
$\tilde{W}$	0	0	$\frac{\alpha_W}{15\pi}$	0

# Supersymmetry and precision data after LEP2 [0502095]

Guido Marandella<sup>a</sup>, Christian Schappacher<sup>b</sup>, Alessandro Strumia<sup>c</sup>



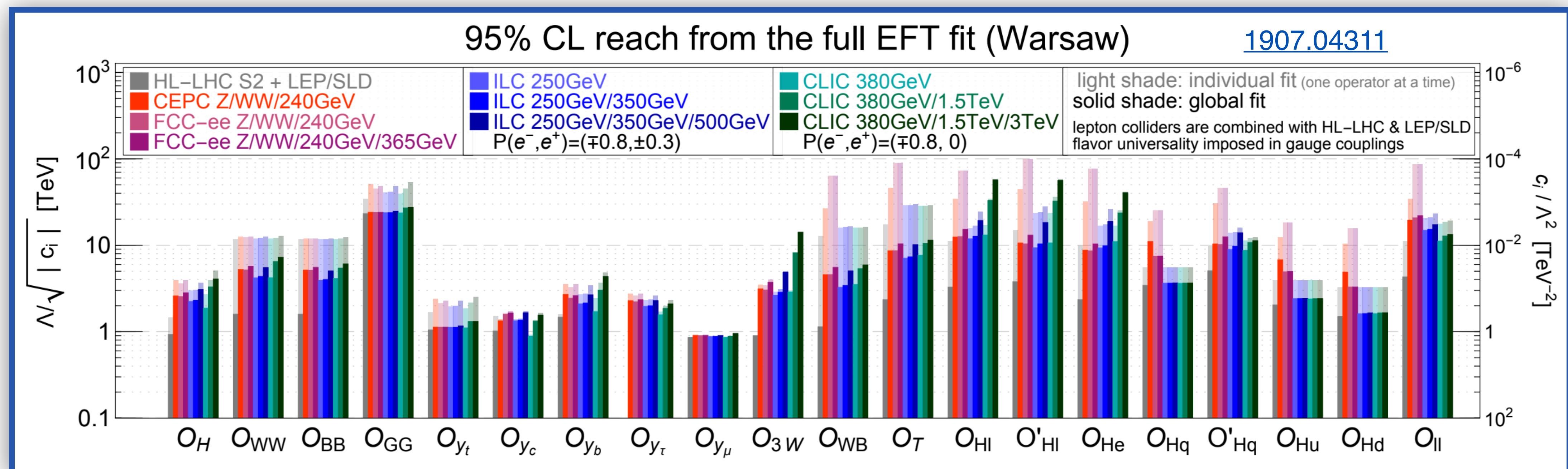
Focuses on  
oblique corrections

# Electroweak Precision Tests

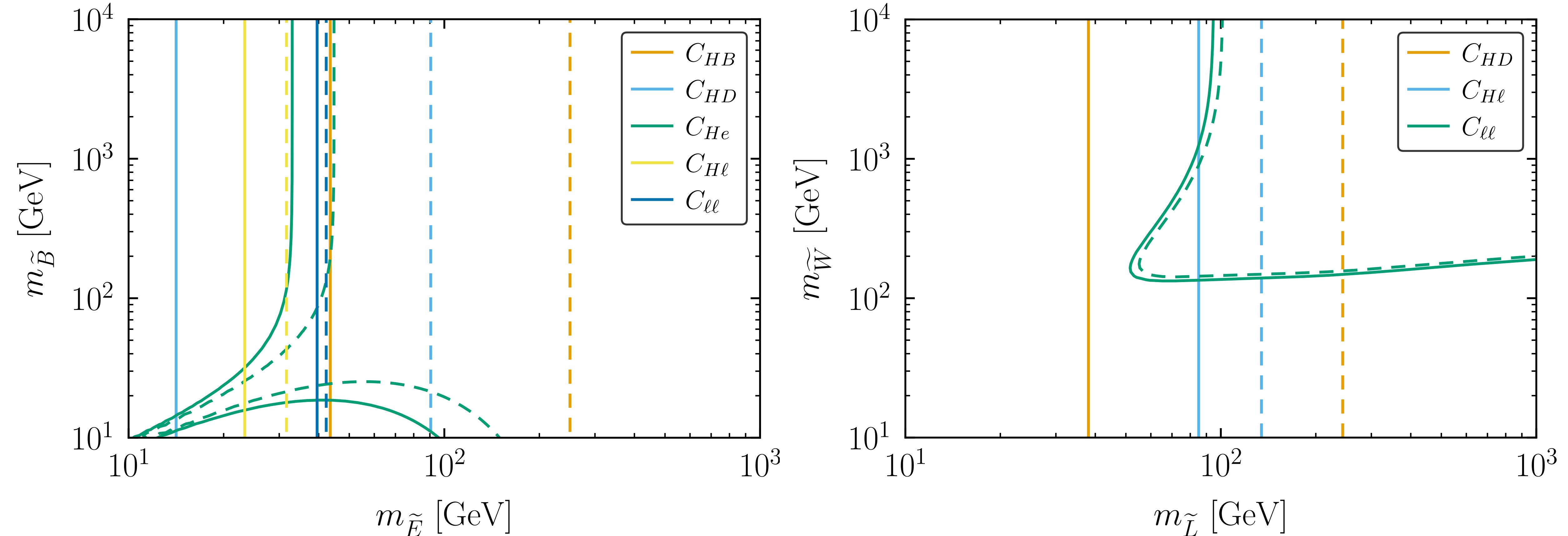
- The most general method of indirectly searching for heavy new physics is SMEFT.

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{n=5}^{\infty} \sum_i \frac{c_i^{(n)}}{\Lambda^{n-4}} \mathcal{O}_i^{(n)}$$

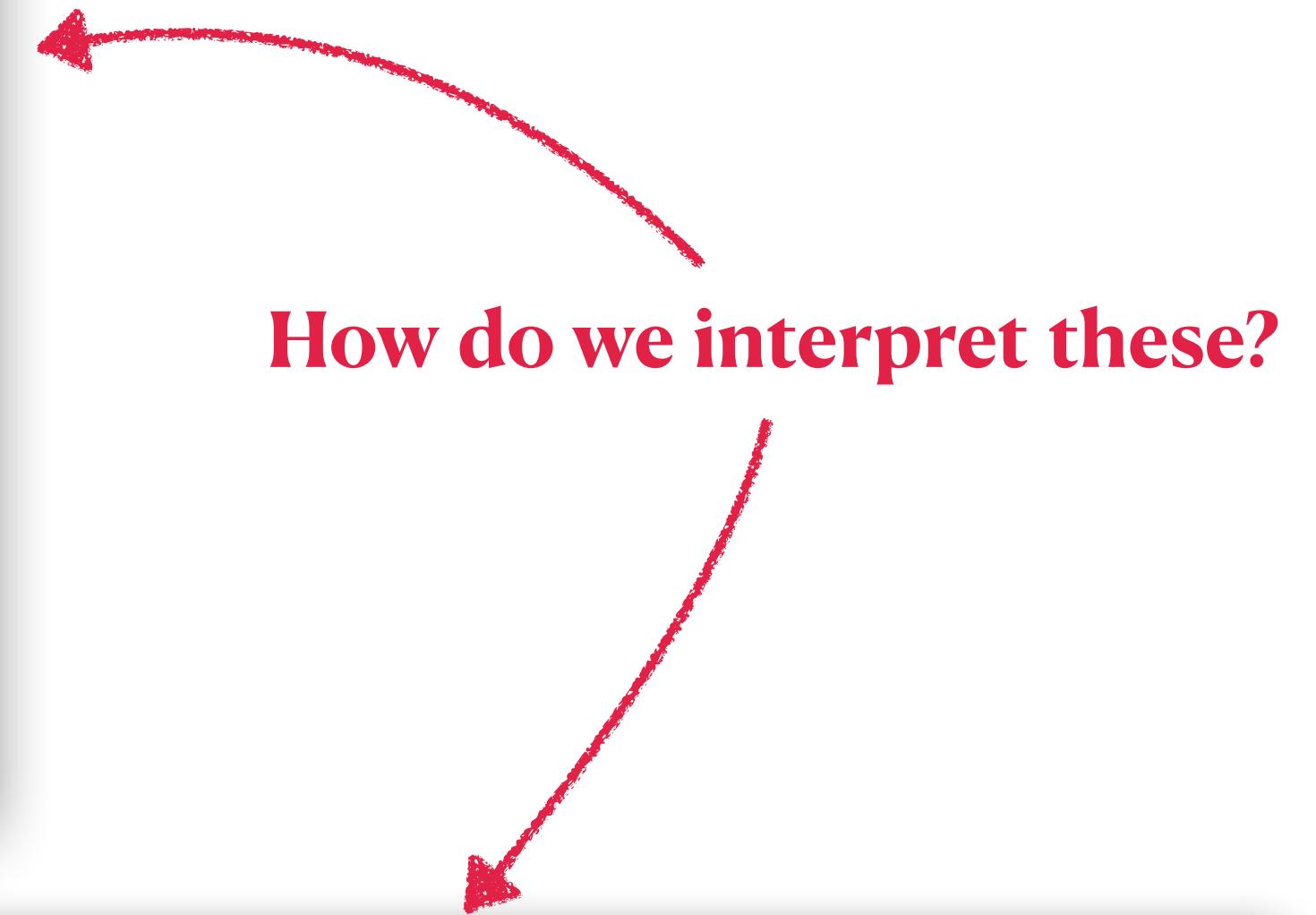
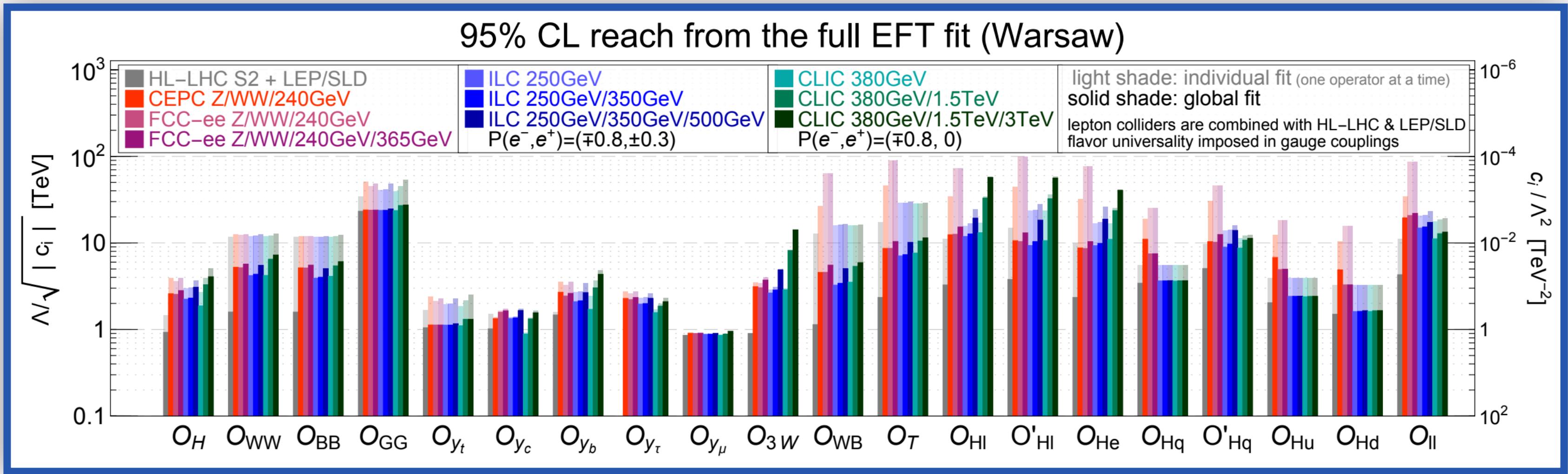
- Assuming CP conservation and MFV, about 20 operators are relevant for EWPTs.



# Constraints from SMEFT



# A Tale of Two Bar Plots



## Questions

1. Which SMEFT operators are most interesting?
2. Which systematics should experimentalists be most motivated to decrease?

