



# Monochromatization a new operation mode for $e^+e^-$ circular colliders

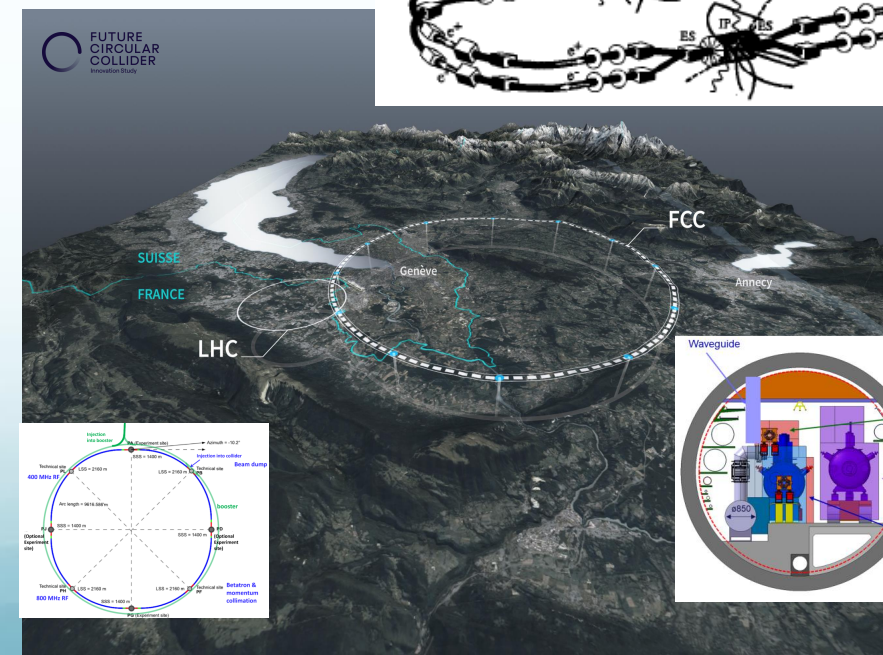
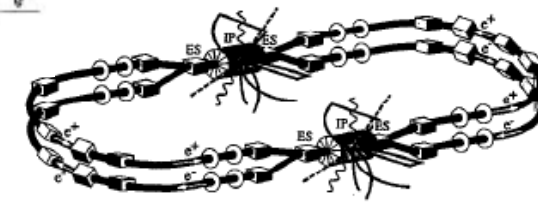
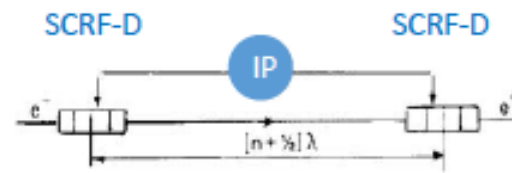
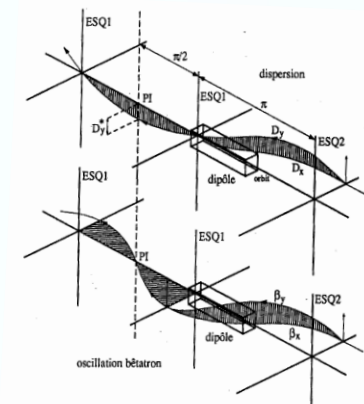
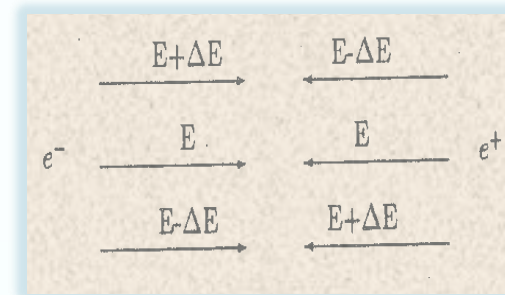
A. Faus-Golfe (IJCLab)

Z. Zhang (IJCLab & IHEP), P. Raimondi (FNAL), F. Zimmermann (CERN), K. Oide (UGE)

# Outline

- Monochromatization concept in  $e^+e^-$  colliders
  - Low-energy
  - High-energy: FCC-ee
- FCC-ee monochrom physics motivation and performance studies
- FCC-ee monochrom schemes and implementation studies
- Summary and Perspectives

## Monochromatization



Reducing the spread of the centre-of mass (CM) energies ( $\sigma_w$ ) of colliding beams is a way to increase the collision energy resolution, that is of particular interest when operating the collider on a narrow particle resonance or at the threshold of its pair production.

beam energy

$$\sigma_w = \sqrt{2} E_b \sigma_\delta$$

relative beam energy spread

$$\sigma_\delta^2 = \frac{55 \hbar c E_b^2}{32 \sqrt{3} (m c^2)^3} \frac{I_3}{I_2} \frac{1}{J_\epsilon}$$

$1/\rho$

spread of the CM energies

$$S_w \propto \frac{1}{\sqrt{r J_e}}$$

$\Downarrow S_w$

usual way

alternative way

$$\left\{ \begin{array}{l} r \gg \gg \text{bending radius} \\ 0.5 \leq J_e = 3 - J_x \leq 2.5 \\ \text{longitudinal partition number} \end{array} \right.$$

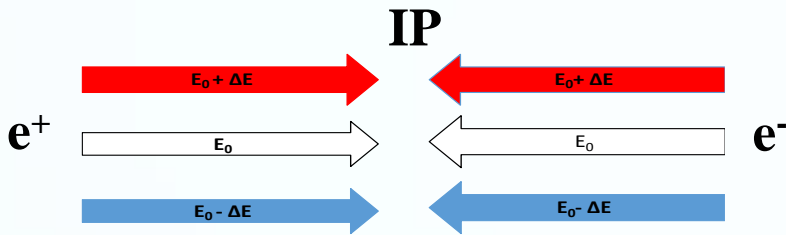
Relative energy spread is mainly due to Synchrotron Radiation (SR) emitted when a ultra-relativistic particle passes trough a bending magnet ( $\rho$ )

**Monochromatization** consists in reducing the spread of the CM energies, **without** necessarily reducing the inherent energy spread of the two individual beams



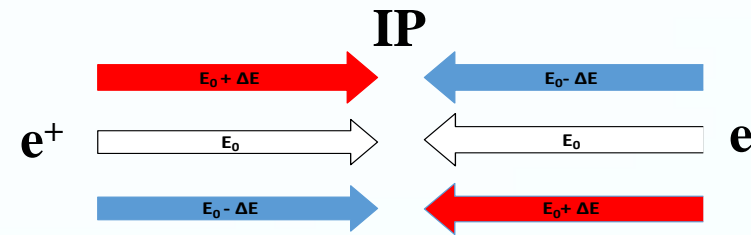
# Monochromatization Principle

## Standard



$D_{x,y}^* = 0$   
 correlation between transverse spatial position and energy deviation

## Monochromatization



$D_{x+}^* = -D_{x-}^* = D_x^*$   
 $D_{y+}^* = -D_{y-}^* = D_y^*$   
 Opposite correlations between transverse spatial position and energy deviation

$$w = 2(E_b + \Delta E)$$

$$\sigma_w = \sqrt{2}E_b\sigma_\delta$$

$$\lambda = 1$$

$$L_0 = \frac{k_b f_r N_+ N_-}{4\pi\sigma_{x\beta}^* \sigma_{y\beta}^*}$$

betatronic beam sizes at the IP

$$\sigma_{x,y}^* = \sqrt{\beta_{x,y}^* \epsilon_{x,y} + (D_{x,y}^* \sigma_\delta)^2}$$

dispersive beam size at the IP

CM energy

$$w = 2E_b + O(\Delta E)^2$$

Spread of the CM energies

$$\sigma_w = \frac{\sqrt{2}E_b\sigma_\delta}{\lambda}$$

Monochromatization factor

$$\lambda = \left( 1 + \sigma_\delta^2 \left( \frac{D_x^{*2}}{\sigma_{x\beta}^{*2}} + \frac{D_y^{*2}}{\sigma_{y\beta}^{*2}} \right) \right)^{1/2}$$

Luminosity

$$L = \frac{L_0}{\lambda}$$

**Enhancement of energy resolution, and sometimes increase of the relative frequency of the events at the center of of the distribution but luminosity loss !!!!**

# Monochromatization Principle

## Standard

IP

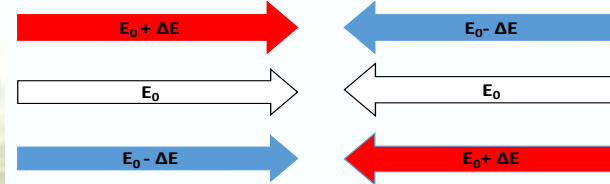
$D_{x,y}^* = 0$   
 correlation between



## Monochromatization

IP

$D_{x+}^* = -D_{x-}^* = D_x^*$   
 $D_{y+}^* = -D_{y-}^* = D_y^*$



Opposite correlations  
 between transverse spatial  
 position and energy deviation



Proposed by A. Renieri in 1975 for ADONE.  
 Smart idea, conceptually very simple, but never  
 tested experimentally !!!!!

$$w = 2E_b + \dots$$

$$\left( 1 + \sigma_\delta^2 \left( \frac{D_x^{*2}}{\sigma_{x\beta}^{*2}} + \frac{D_y^{*2}}{\sigma_{y\beta}^{*2}} \right) \right)^{1/2}$$

$$L = \frac{L_0}{\lambda}$$

betatronic beam sizes at the IP

$$\sigma_{x,y}^* = \sqrt{\beta_{x,y}^* \epsilon_{x,y} + (D_{x,y}^* \sigma_\delta)^2}$$

dispersive beam size at the IP

Enhancement of energy resolution, and sometimes  
 increase of the relative frequency of the events at the  
 centre of the distribution but **luminosity loss !!!!**

At **low-energy e<sup>+</sup>e<sup>-</sup> colliders**, with **flat beam schemes** ( $\sigma_y^* \ll \sigma_x^*$ ) and where the energy spread is mainly due to SR (“beamstrahlung” (BS) is not important), **we could optimize this scheme by playing with the beam-beam parameters and the emittances to avoid luminosity losses:**

with  $\left\{ \begin{array}{l} \beta_y^* \ll \beta_x^* \\ \varepsilon_y^* \ll \varepsilon_x^* \end{array} \right.$  beam emittances

$\sigma_y^* \ll \sigma_x^* \implies \begin{array}{l} D_{x+}^* = D_{x-}^* = 0 \\ D_{y+}^* = -D_{y-}^* = D_y^* \end{array}$ 
  
 Vertical dispersion different from zero

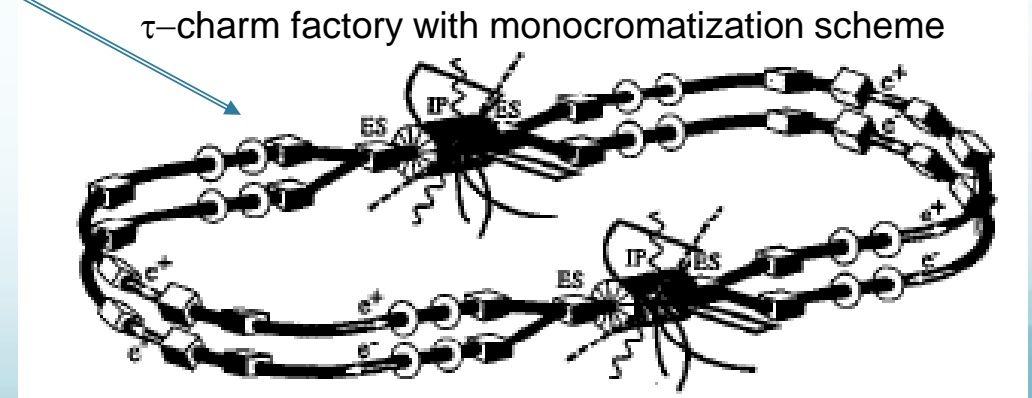
$\sigma_y^* \simeq \sigma_\varepsilon D_y^*$ 
  
 $\xi_y \ll \xi_x \simeq \xi_{max}$ 
  
 beam-beam parameter
   
 $\xi_{xy} = \frac{N_b r_e \beta_{xy}^*}{2\pi\gamma\sigma_{xy}^*(\sigma_x^* + \sigma_y^*)}$

$L \simeq \frac{I\gamma}{2er_e} \frac{\xi_x}{\beta_x^*}$ 
  
 $\frac{2\pi\gamma}{N_b r_e} \varepsilon_x \xi_x \frac{\beta_y^*}{\beta_x^*} \leq 1$ 
  
 with low-horizontal emittance

we could **gain in energy resolution** keeping the **luminosity constant** and the **beam-beam** in the **standard limits !!!!!**

## Monochromatization Design Studies for low-energy e<sup>+</sup>e<sup>-</sup> colliders:

- VEPP4: one ring, electrostatic quads (τ-charm)
- SPEAR: one ring, electrostatic quads, λ~8
- LEP: one ring, electrostatic quads (limited strength) and alternative RF magnetic quads, λ~3 (optics limitations)
- B-factory: Superconducting RF resonators
- τ-charm factory: two rings, vertical dipoles, λ~7.5



A. Faus-Golfe, J. Le Duff, Versatile DBA and TBA lattices for a tau charm factory with and without beam monochromatization. Nucl. Instrum. Methods A 372, 6–18 (1996)

# Monochromatization in High-energy Colliders

In the previous case for low-energy  $e^+e^-$  colliders, the **relative energy spread** is mainly given by **SR** in the colliders arcs ( $\sigma_\delta = \sigma_{\delta,SR}$ ). Alternatively in **high-energy  $e^+e^-$** , we have to take into account also the **SR** created by the strong opposing EM field during collision or “**beamstrahlung**”(BS) ( $N\gamma \propto 1/\sigma_z (\sigma_x^* + \sigma_y^*)$ , with  $\sigma_z$  the bunch length).

## Standard BS

$$D_{x,y}^* = 0$$

$$\sigma_{\delta,tot} = \sqrt{\frac{1}{2} \sigma_{\delta,SR}^2 + \sqrt{\frac{1}{4} \sigma_{\delta,SR}^4 + A \frac{\sigma_{\delta,SR}^2}{\sigma_{z,SR}^2}}}$$

$$A = \frac{275}{36} \frac{n_{IP} \tau_E r_e^5 N_b^3 \gamma^2}{\pi^{\frac{3}{2}} 4 T_{rev} \alpha \sigma_{x,SR}^3}$$

$$\epsilon_{x,tot} \approx \epsilon_{x,SR}$$

$$\sigma_{z,tot} = \frac{\alpha_c C}{2\pi Q_s} \sigma_{\delta,tot}$$

**BS at high-energy** with  $D_x^* = 0$ , has more **impact on energy spread** in standard mode than in monochromatization mode.

## Monochromatization BS

$$D_{x+}^* = -D_{x-}^* = D_x^*$$

$$D_{y+}^* = -D_{y-}^* = D_y^*$$

Coupled system to be solved numerically

$$\sigma_{\delta,tot}^2 = \sigma_{\delta,SR}^2 + \frac{B}{D_x^{*3} \sigma_{\delta,tot}^5}$$

$$B \approx 50 \frac{n_{IP} \tau_E r_e^5 N_b^3 \gamma^2}{T_{rev} (\alpha_c C / (2\pi Q_s))^2}$$

2B

$$\epsilon_{x,tot} \approx \epsilon_{x,SR} + \frac{2B}{D_x^* \beta_x^* \sigma_{\delta,tot}^5}$$

$$\sigma_{z,tot} = \frac{\alpha_c C}{2\pi Q_s} \sigma_{\delta,tot}$$

**BS with monochromatization at high-energy, avoids the blow up** of the relative beam energy spread, which is significant in standard mode with  $D_x^* = 0$ .

- In recent years interest in **monochromatization** has been renewed, as **FCC-ee** could directly produce the Higgs boson in s-channel annihilation  $e^+e^- \rightarrow H$  at **125 GeV**. This production mode is only possible if the default collision energy spread ( $\sim 50$  MeV) can be reduced to a level comparable with the natural width of the **Higgs boson**  $\Gamma_H = 4.2$  MeV, offering the only known path to measuring the **electron-Yukawa coupling** ( $y_e$ ).

S. Jadach, R.A. Kycia, Phys. Lett. B 755, 58 (2016). DOI: 10.1016/j.physletb.2016.01.065

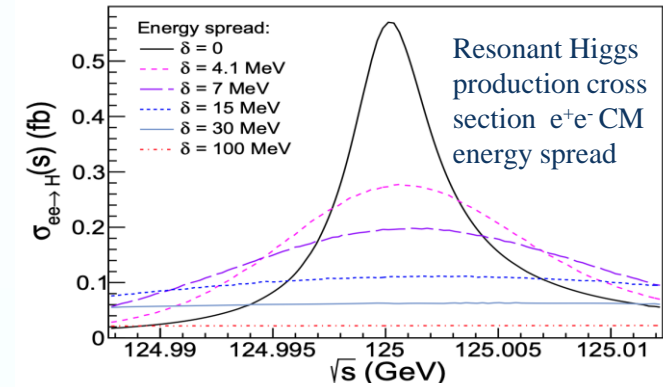
- **FCC-ee self-consistent parametric studies at 125 GeV** has been realized to identify the best scenario with  $D_x^* \neq 0$ .

A. Faus-Golfe, M. Valdivia Garcia, F. Zimmermann, The challenge of monochromatization Direct s-channel Higgs production:  $e^+e^- \rightarrow H$ , Eur. Phys. J. Plus (2022) 137:31, DOI: 10.1140/epjp/s13360-021-02151-y

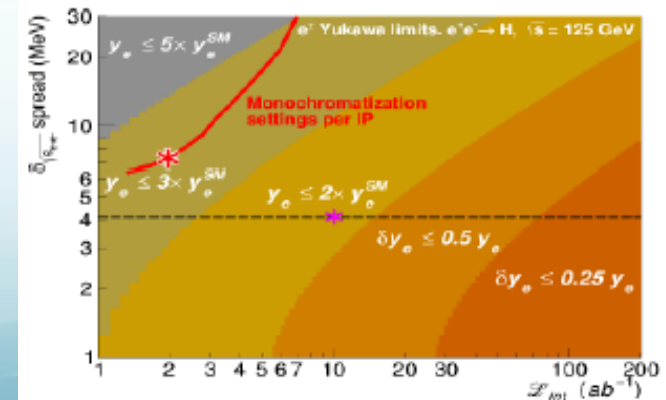
- Associated **upper limits contours** (95% CL) on the **electron Yukawa coupling** ( $y_e$ ) has been calculated.

Red curves show the range of parameters presently reached in self-parametric FCC-ee monochromatization studies. The red star indicates the best signal strength monochromatization point in the plane (the pink star over the  $\delta\sqrt{s} = \Gamma_H = 4.2$  MeV dashed line, indicates the ideal baseline point assumed in default analysis). All results are given per IP and per year.

D. d'Enterria, A. Poldaru, G. Wojcik, Measuring the electron Yukawa coupling via resonant s-channel Higgs production at FCC-ee, arXiv:2107.02686v1 [hep-ex] 6 Jul 2021



| Parameter  |                            | Units                               |
|--|----------------------------|-------------------------------------|
| CM Energy, $\sqrt{s}$  | 125                        | [GeV]                               |
| Horizontal, vertical RMS emittances with (without) beamstrahlung, $\epsilon_{x,y}$ | 2.5 (0.51), 0.002          | [nm]                                |
| Relative RMS momentum deviation, $\sigma_p$  | 0.052                      | %                                   |
| RMS bunch length, $\sigma_z$   | 3.3                        | [mm]                                |
| Horizontal dispersion at IP, $D_x^*$   | 0.105                      | [m]                                 |
| Beta functions at the IP, $\beta_{x,y}^*$  | 90, 1                      | [mm]                                |
| RMS beam size at the IP, $\sigma_{x,y}^*$  | 55, 0.045                  | [ $\mu$ m]                          |
| Full crossing angle, $\theta_c$  | 30                         | [mrad]                              |
| Vertical beam-beam tune shift, $\xi_y$   | 0.106                      |                                     |
| Total beam current, $I_e$  | 395                        | [mA]                                |
| Bunch population, $N_b$  | $6.0 \times 10^{10}$       |                                     |
| Bunches per beam, $n_b$  | 13420                      |                                     |
| Luminosity (without crab cavities) per IP, $L$                                     | $2.6 (2.3) \times 10^{35}$ | [cm <sup>-2</sup> s <sup>-1</sup> ] |
| RMS CM energy spread (without crab cavities), $\sigma_w$                           | 13(25)                     | [MeV]                               |



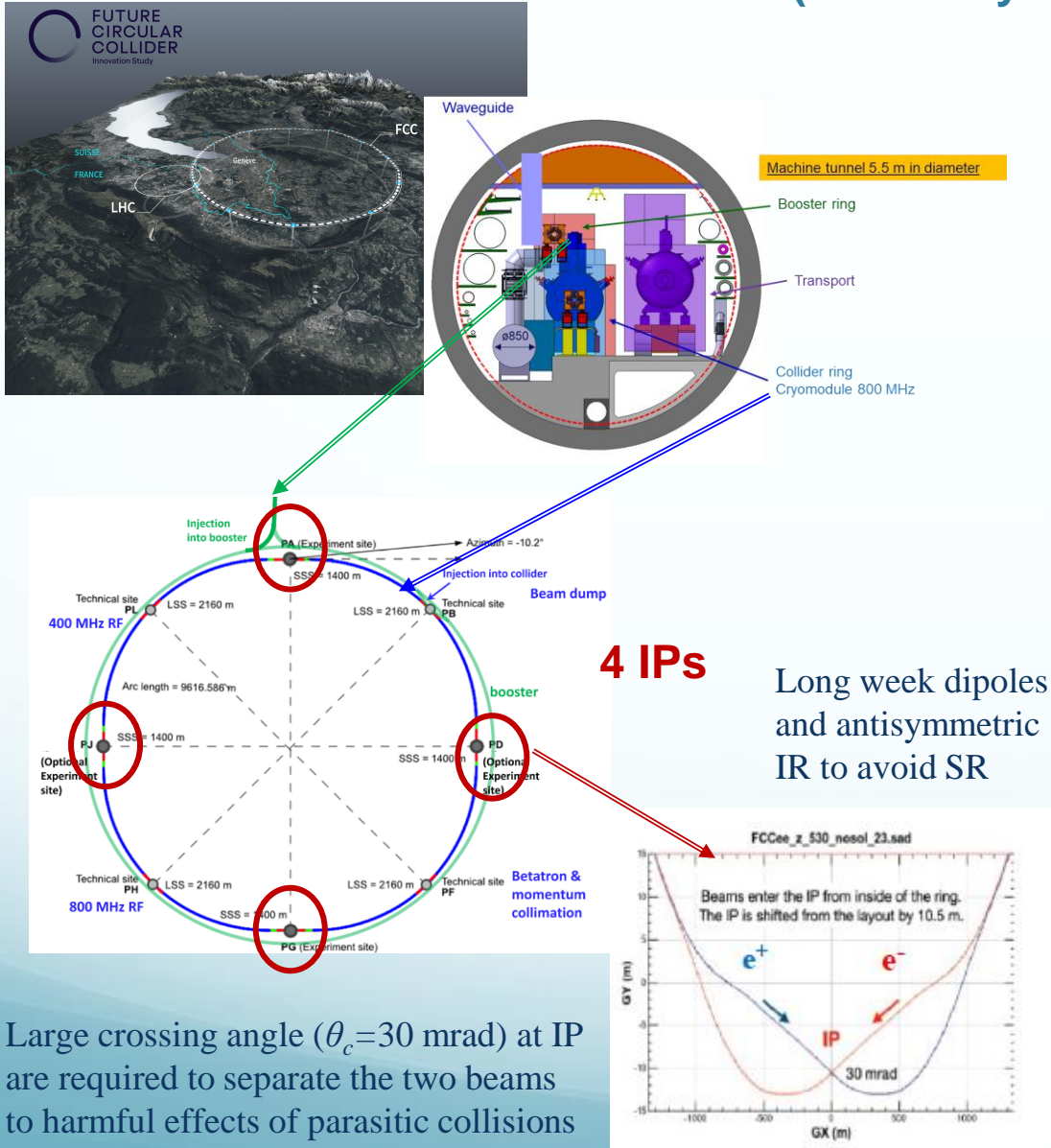


# The FCC-ee GHC Standard Lattice & Performances

## (Global Hybrid Correction)

**4 operation modes:** Z, WW, ZH, tbar

FCC-ee GHC Performance Table for V22



**4 IPs** Long week dipoles and antisymmetric IR to avoid SR

Large crossing angle ( $\theta_c=30$  mrad) at IP are required to separate the two beams to harmful effects of parasitic collisions

| Beam energy                           | [GeV]                             | 45.6                | 80            | 120                  | 182.5         |
|---------------------------------------|-----------------------------------|---------------------|---------------|----------------------|---------------|
| Layout                                |                                   | PA31-1.0            |               |                      |               |
| # of IPs                              |                                   | 4                   |               |                      |               |
| Circumference                         | [km]                              | 91.174117           |               | 91.174107            |               |
| Bending radius of arc dipole          | [km]                              | 9.937               |               |                      |               |
| Energy loss / turn                    | [GeV]                             | 0.0391              | 0.370         | 1.869                | 10.0          |
| SR power / beam                       | [MW]                              | 50                  |               |                      |               |
| Beam current                          | [mA]                              | 1280                | 135           | 26.7                 | 5.00          |
| Bunches / beam                        |                                   | 10000               | 880           | 248                  | 40            |
| Bunch population                      | [ $10^{11}$ ]                     | 2.43                | 2.91          | 2.04                 | 2.37          |
| Horizontal emittance $\epsilon_x$     | [nm]                              | 0.71                | 2.16          | 0.64                 | 1.49          |
| Vertical emittance $\epsilon_y$       | [pm]                              | 1.42                | 4.32          | 1.29                 | 2.98          |
| Arc cell                              |                                   | Long 90/90          |               | 90/90                |               |
| Momentum compaction $\alpha_p$        | [ $10^{-6}$ ]                     | 28.5                |               | 7.33                 |               |
| Arc sextupole families                |                                   | 75                  |               | 146                  |               |
| $\beta_{x/y}^*$                       | [mm]                              | 100 / 0.8 200 / 1.0 |               | 300 / 1.0 1000 / 1.6 |               |
| Transverse tunes/IP $Q_{x/y}$         |                                   | 53.563 / 53.600     |               | 100.565 / 98.595     |               |
| Energy spread (SR/BS) $\sigma_\delta$ | [%]                               | 0.038 / 0.132       | 0.069 / 0.154 | 0.103 / 0.185        | 0.157 / 0.221 |
| Bunch length (SR/BS) $\sigma_z$       | [mm]                              | 4.38 / 15.4         | 3.55 / 8.01   | 3.34 / 6.00          | 1.95 / 2.75   |
| RF voltage 400/800 MHz                | [GV]                              | 0.120 / 0           | 1.0 / 0       | 2.08 / 0             | 2.5 / 8.8     |
| Harmonic number for 400 MHz           |                                   | 121648              |               |                      |               |
| RF frequency (400 MHz)                | MHz                               | 399.994581          |               | 399.994627           |               |
| Synchrotron tune $Q_s$                |                                   | 0.0370              | 0.0801        | 0.0328               | 0.0826        |
| Long. damping time                    | [turns]                           | 1168                | 217           | 64.5                 | 18.5          |
| RF acceptance                         | [%]                               | 1.6                 | 3.4           | 1.9                  | 3.0           |
| Energy acceptance (DA)                | [%]                               | $\pm 1.3$           | $\pm 1.3$     | $\pm 1.7$            | $-2.8 + 2.5$  |
| Beam-beam $\xi_x/\xi_y^a$             |                                   | 0.0023 / 0.135      | 0.011 / 0.125 | 0.014 / 0.131        | 0.093 / 0.140 |
| Luminosity / IP                       | [ $10^{34}/\text{cm}^2\text{s}$ ] | 182                 | 19.4          | 7.26                 | 1.25          |
| Lifetime (q + BS + lattice)           | [sec]                             | 840                 | -             | < 1065               | < 4062        |
| Lifetime (lum)                        | [sec]                             | 1129                | 1070          | 596                  | 744           |

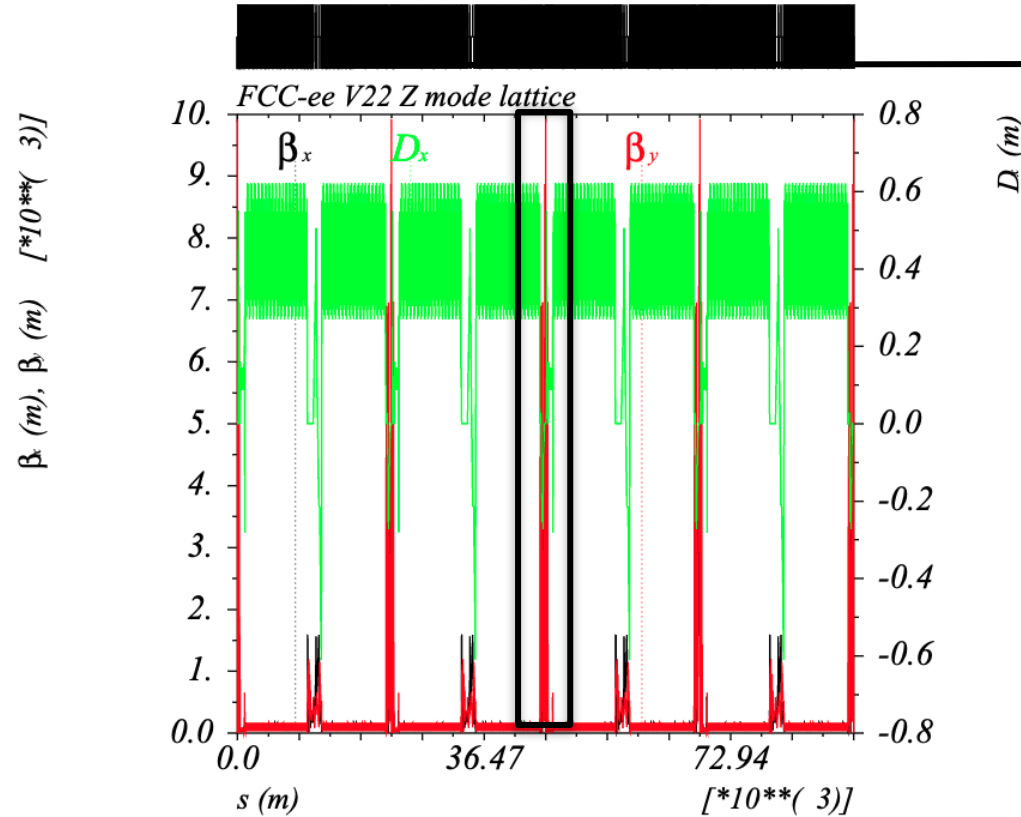
<sup>a</sup>incl. hourglass.

## Z mode lattice with Long 90/90 arc cells

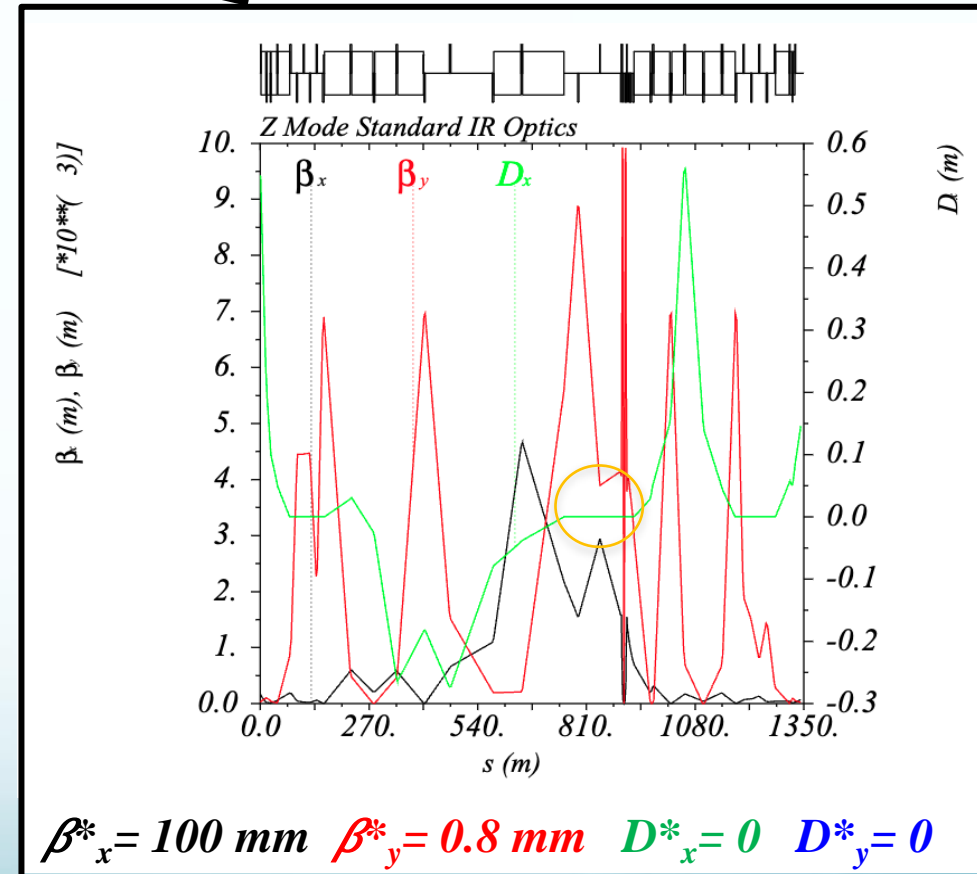
## IR Crab waist type Z mode Lattice

Highly asymmetric IR lattice around the IP to mitigate the SR impact

IP



Energy: 45.6 GeV,  $E_x=0.71$  nm,  $E_y=1.42$  pm

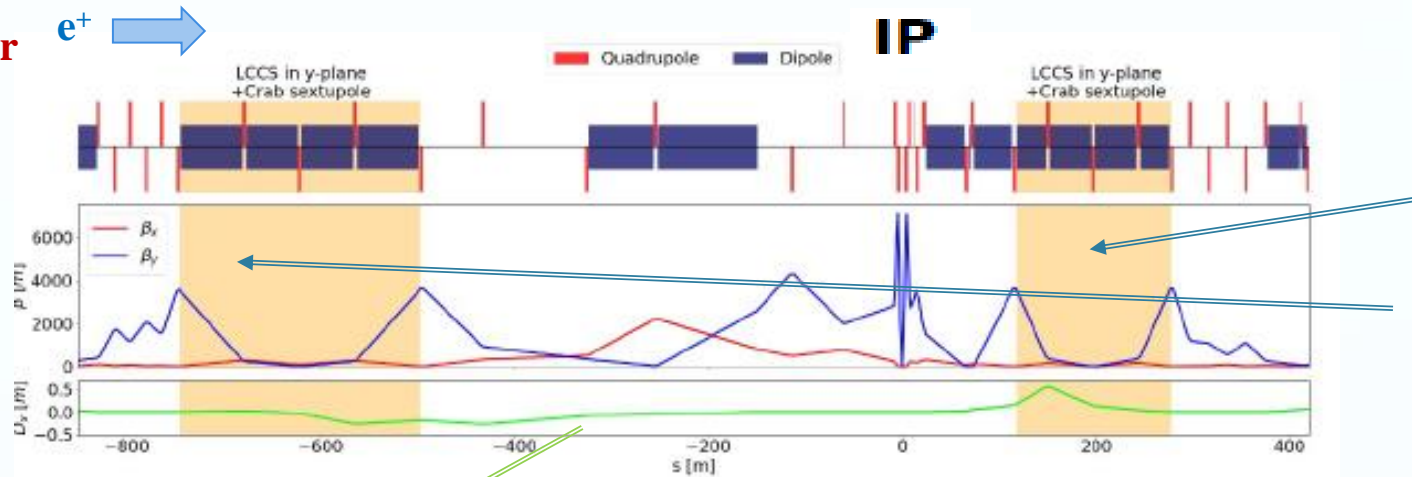


$\beta_x^* = 100$  mm  $\beta_y^* = 0.8$  mm  $D_x^* = 0$   $D_y^* = 0$

Despite the **simplicity** of the **monochromatization concept**, the **creation** and the **control** of the necessary **H/V dispersion function** of opposite signs at the IP could be **rather difficult to implement**.

## Monochromatization factor

$$\lambda = \sqrt{1 + \sigma_{\delta,SR}^2 \left( \frac{D_x^{*2}}{\sigma_{x\beta}^{*2}} + \frac{D_y^{*2}}{\sigma_{y\beta}^{*2}} \right)}$$



**IR GHC: Local Chromaticity Correction Section (LCCS) with Crab Sextupoles (CS) in the vertical to produce a crab waist collision**

### ➤ $D_x^* \neq 0$ generation at the IP

In FCC-ee IR region, the **large crossing angle of 30 mrad** in the H-plane and the **LCCS** is made possible with **H-dipoles** at the two sides of the IP creating some **H-dispersion**  $D_x^*$  ( $D_x \neq 0$  in the LCCS and  $D_x = 0$  close to the IP for high-luminosity).  $D_x^* \neq 0$  could be generated (**~10 cm**) by **mismatching  $D_x$**  in the LCCS.

### ➤ $D_y^* \neq 0$ generation at the IP

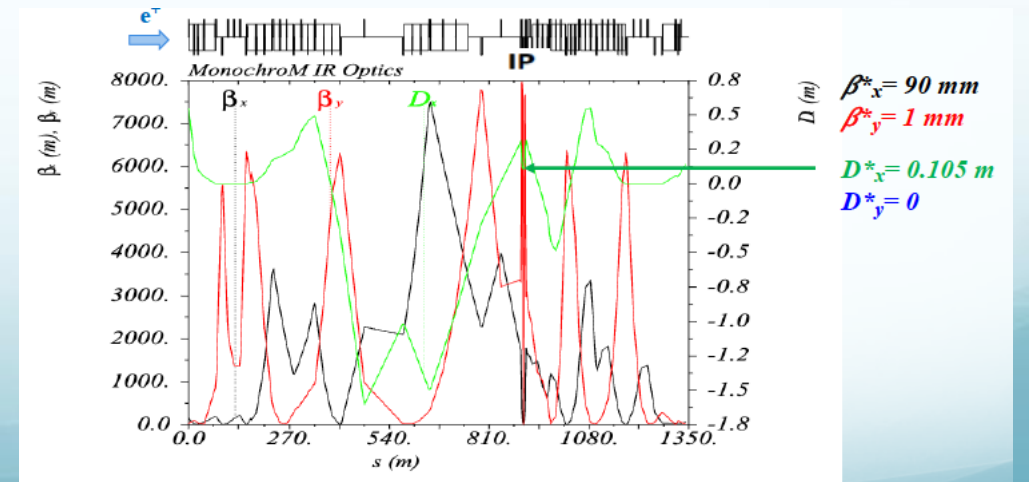
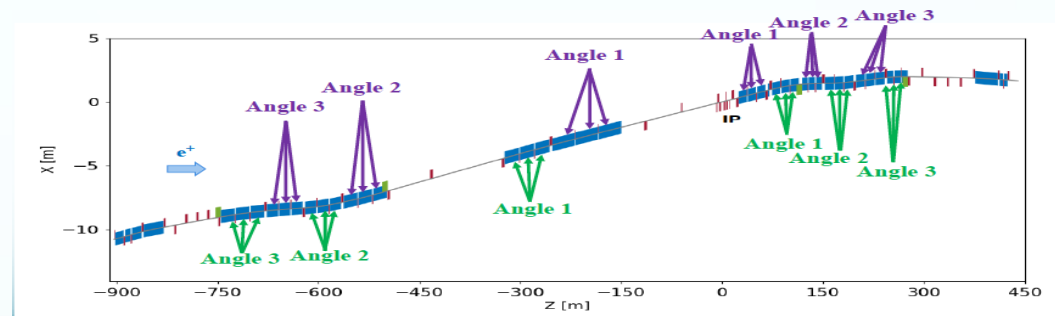
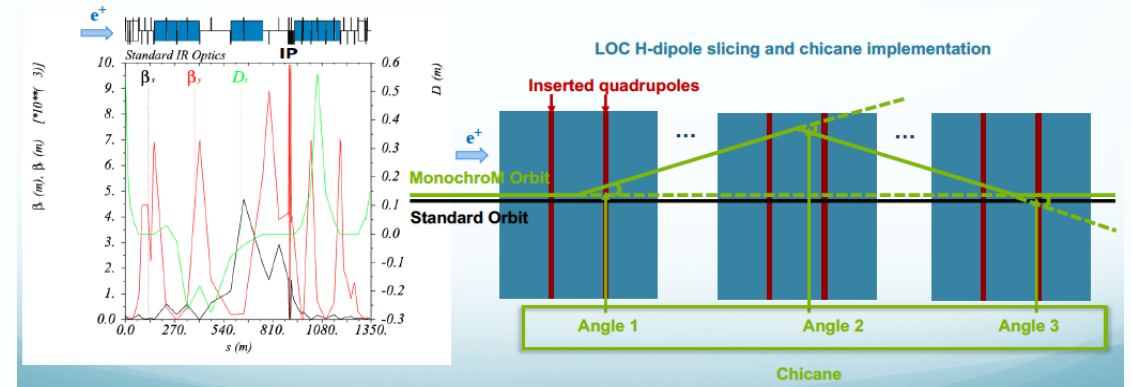
Because  $\sigma_{y\beta}^* \ll \sigma_{x\beta}^*$ , about **100 times smaller  $D_y^*$  (~mm)** is needed to get the same monochromatization factor. Therefore  $D_y^* \neq 0$  could be generated by implementing **skew quadrupoles** around IP. These quadrupoles could be located where the CS pairs are located in the LCC system.

**Step 1:** All LCCS H-dipoles (blue) are cut into three pieces and quadrupoles (red) are inserted between them for matching flexibility. Additional chicanes are implemented in each upstream and downstream LCCS H-dipole to create the dispersion at the IP while keeping the orbit.

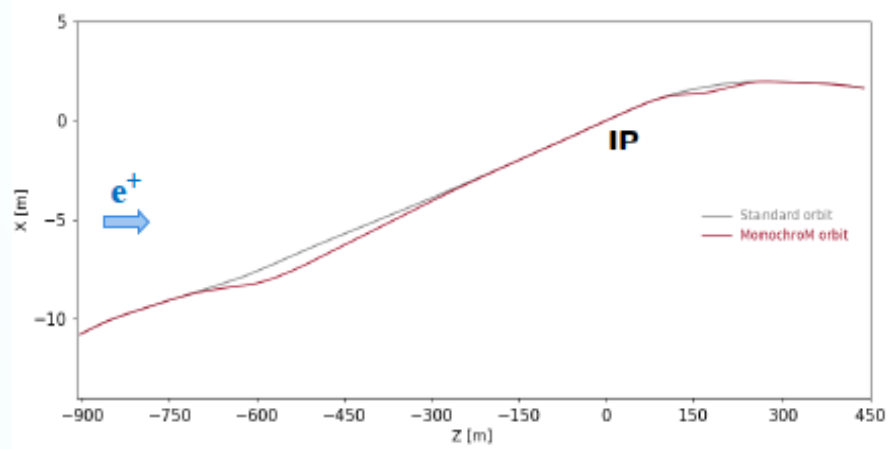
**Step 2:** To mitigate the horizontal emittance blowup, two long chicanes are implemented to each upstream and downstream. And each angle of chicane is equally distributed to all the three pieces of each LCCS H-dipole.

**Step 3:** The IP beam parameters are matched to FCC-ee Monochrom self-consistent parameters\* while keeping the beam parameters at the entrance and exit of the IR similar to those of standard mode, including phase advances between sextupoles and crab sextupoles.

\* A. Faus-Golfe, M. Valdivia Garcia, F. Zimmermann, The challenge of monochromatization Direct s-channel Higgs production:  $e^+e^- \rightarrow H$ , Eur. Phys. J. Plus (2022) 137:31, <https://doi.org/10.1140/epjp/s13360-021-02151-y>



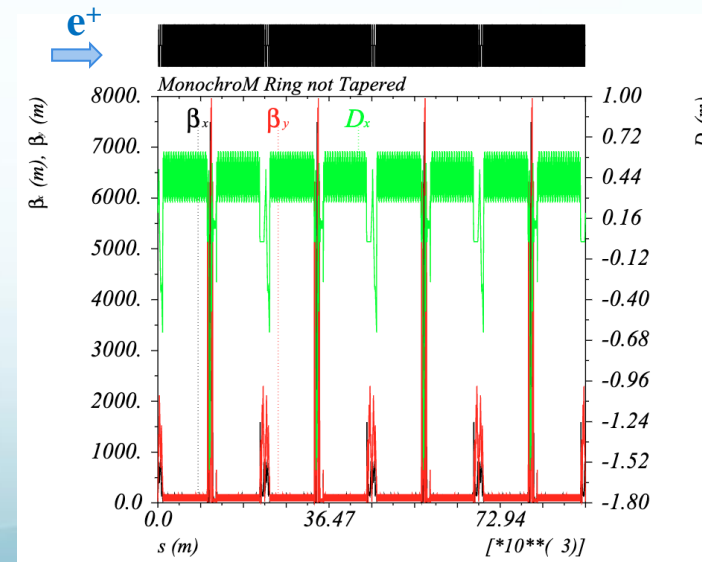
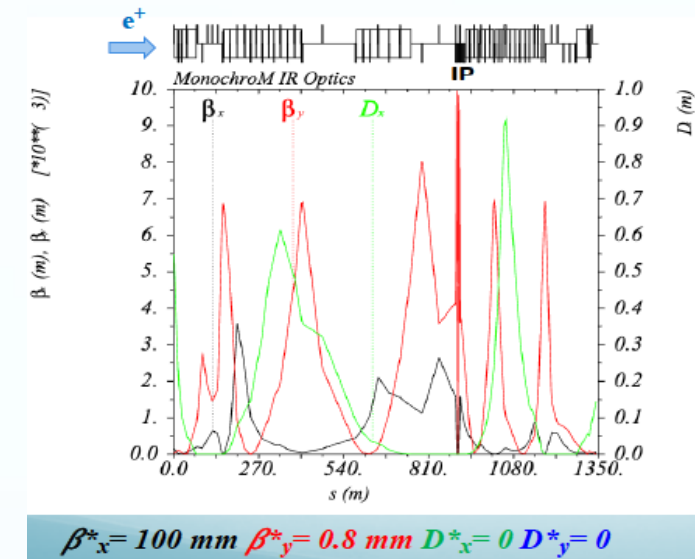
**Step 4:** Compatibility orbit checking for the standard mode with  $D_x = 0$ .



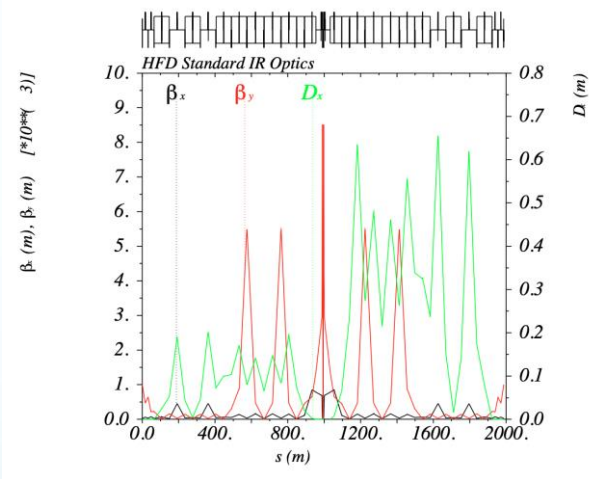
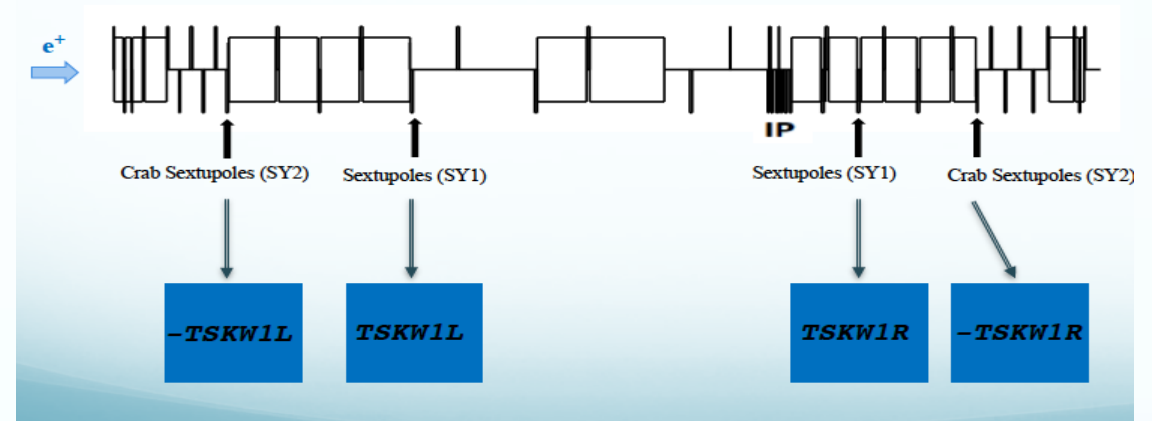
**Step 5:** IR Monochrom is implemented in the four IPs and global matching:

- LCCS chromaticity correction
- Global arc chromaticity correction
- Tune correction
- Emittance checks and SR-RF strategy compensation
- Preliminary Tracking and DA calculations

**IPAC2024:**  
**WEPR21, TUYD1**



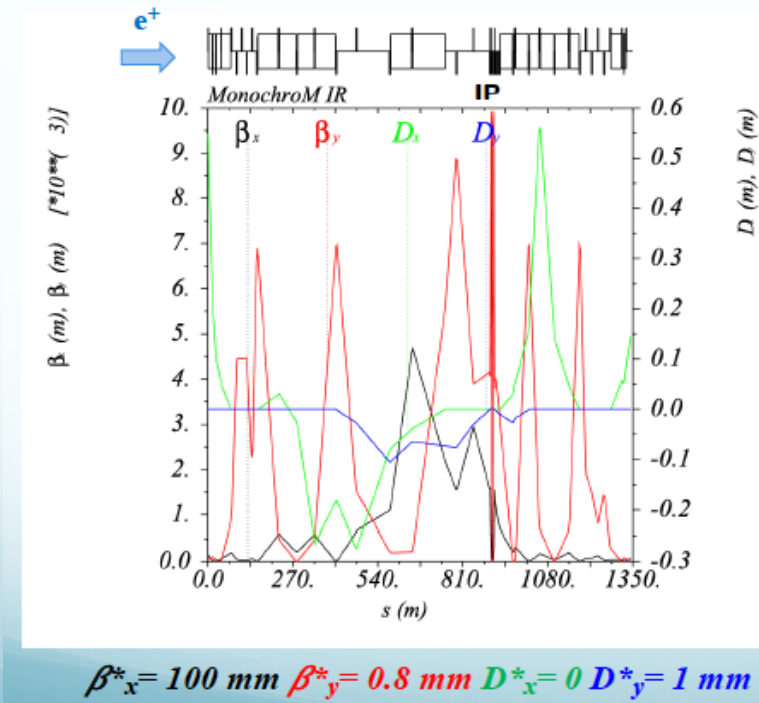
**Step 1:** Therefore  $D_y^* \neq 0$  could be generated by implementing **skew quadrupoles** around IP. These quadrupoles could be located where the CS pairs are located in the LCC system.



Inspired in **Local Chromaticity Correction (LCC)** IR optics solenoid compensation scheme

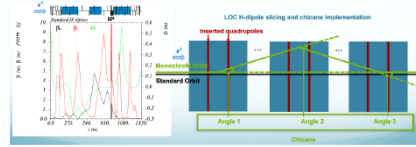
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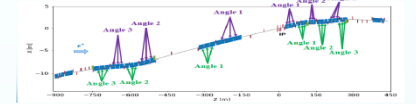


$D_x^*$

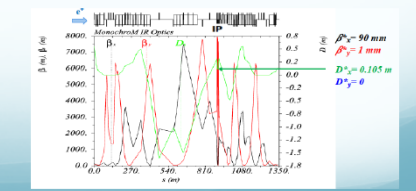
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**Step 2:** To mitigate the horizontal emittance blowup, two long chicanes are implemented to each upstream and downstream. And each angle of chicane is equally distributed to all the three pieces of each LCCS H-dipole.

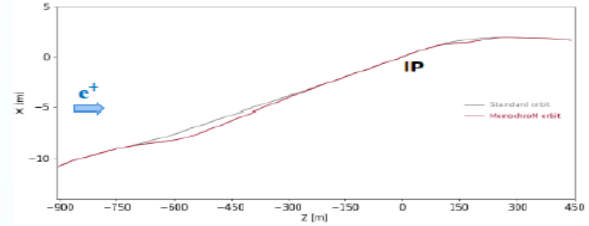


**Step 3:** The IP beam parameters are matched to FCC-ee Monochrom self-consistent parameters\* while keeping the beam parameters at the entrance and exit of the IR similar to those of standard mode, including phase advances between sextupoles and crab sextupoles.



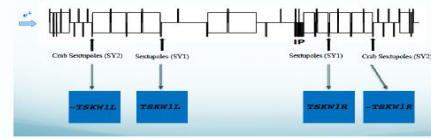
\* A. Faus-Goffe, M. Valdivia Garcia, F. Zimmermann, The challenge of monochromatization Direct s-channel Higgs production: e+e- -> H, Eur. Phys. J. Plus (2022) 137:31, https://doi.org/10.1140/epj/s13360-021-02151-y

**Step 4:** Compatibility orbit checking for the standard mode with  $D_x = 0$ .



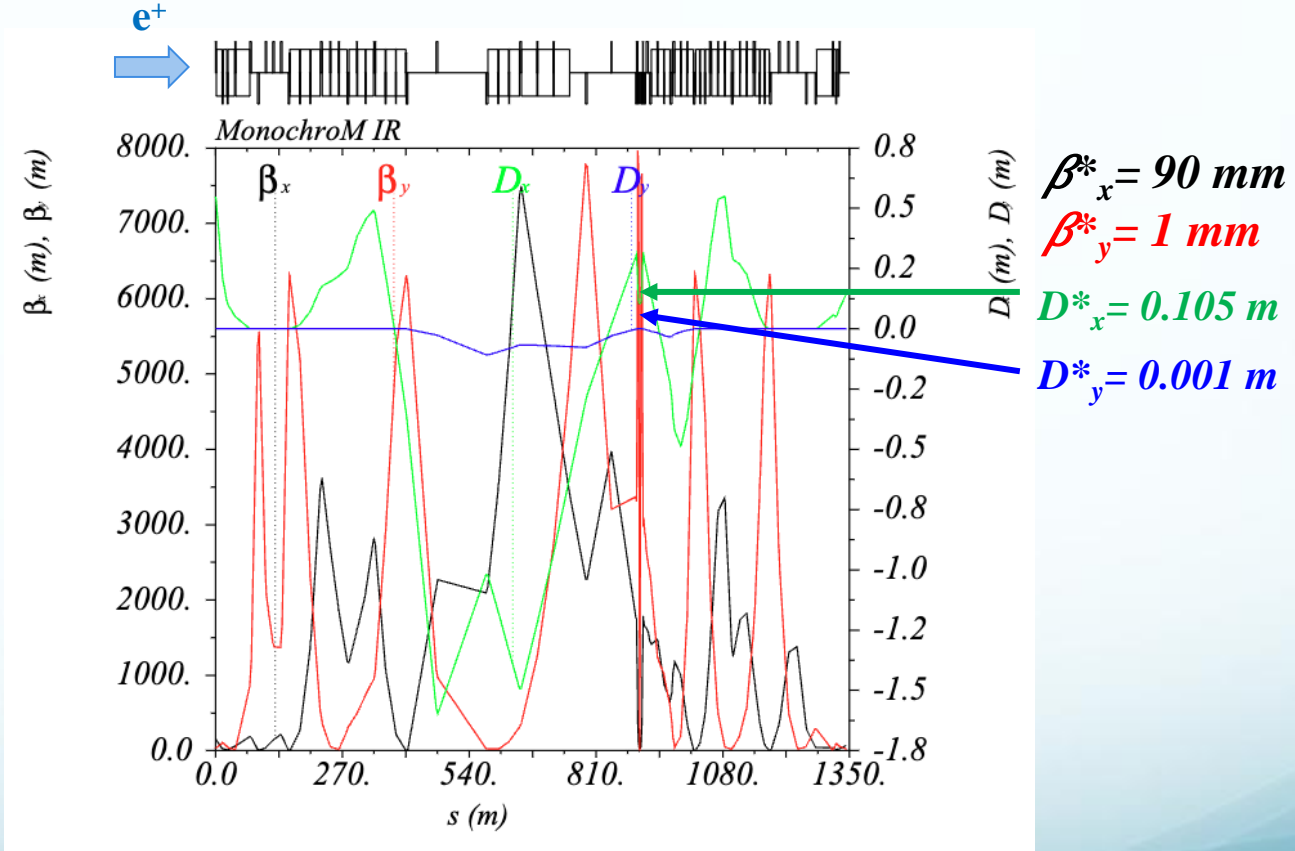
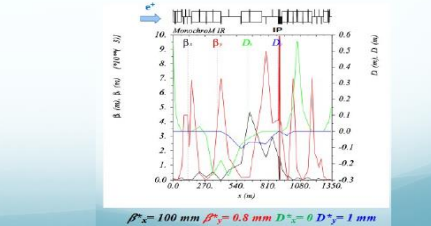
$D_y^*$

**Step 1:** Therefore  $D_y^* \neq 0$  could be generated by implementing skew quadrupoles around IP. These quadrupoles could be located where the CS pairs are located in the LCC system.



**Step 2:** IR Monochrom is implemented in the four IPs and global matching:

- LCCS chromaticity correction
- Global arc chromaticity correction
- Tune correction
- Emittance checks
- Preliminary Tracking and DA calculations

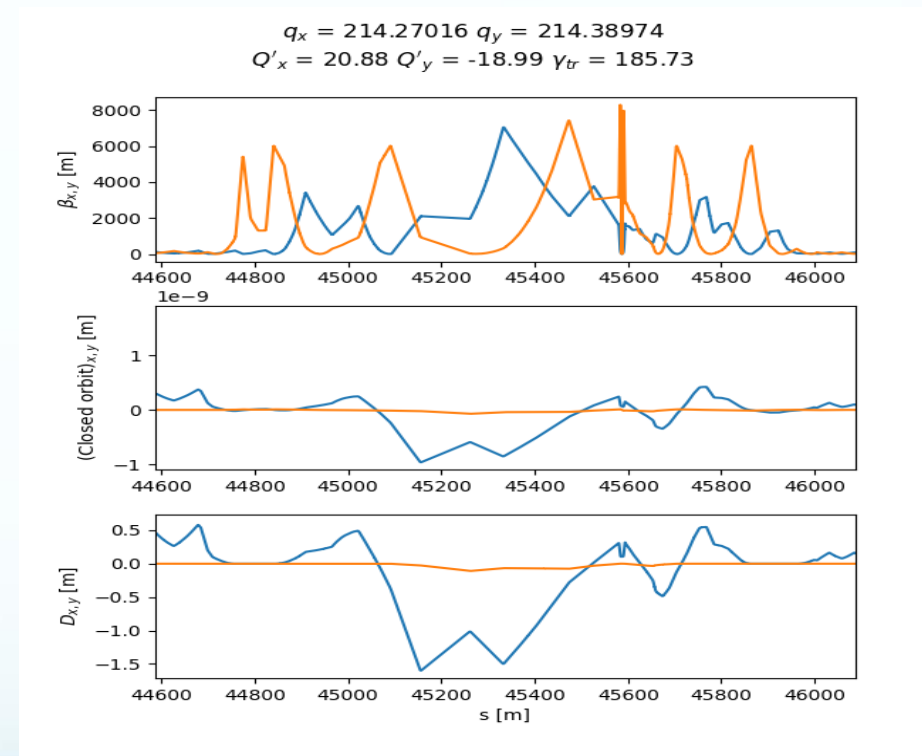


**IPAC2024:**  
**WEPR21, TUYD1**

# FCC-ee GHC Monochrom Lattices

7 kinds of **FCC-ee GHC V22 Monochrom** optics design based on **Z mode** and 7 lattices based on **ttbar mode** has been completed with different possible combination of **H, V, H/V** dispersions and number of **IPs**.

| FCC-ee GHC             | Orbit changed or not | $Dx^*$  | $Dy^*$  |
|------------------------|----------------------|---------|---------|
| <i>standard_625</i>    | No                   | 0       | 0       |
| <i>monochrom_h_4ip</i> | Yes                  | 0.105 m | 0       |
| <i>monochrom_h_2ip</i> | Yes                  | 0.105 m | 0       |
| <i>monochrom_h_d0</i>  | Yes                  | 0       | 0       |
| <i>monochrom_v_1</i>   | No                   | 0       | 0.001 m |
| <i>monochrom_v_2</i>   | No                   | 0       | 0.002 m |
| <i>monochrom_mix</i>   | Yes                  | 0.105 m | 0.001 m |



MADX - Methodical Accelerator Design. <http://madx.web.cern.ch/madx/>  
 Xsuite. <https://xsuite.readthedocs.io/>

Xsuite Monochrom mixed based on Z mode lattice.



➤ FCC-ee GHC Monochrom Optics Performance based on Z mode lattice (w/o BS effect)

| Parameters                                   | Units                                  | Standard        | Standard_625*   | Monochrom_h_4ip | Monochrom_h_2ip | Monochrom_h_d0  | Monochrom_v_1   | Monochrom_v_2   | Monochrom_mix   |
|--|--|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Beam Energy $E$                              | GeV                                    | 45.6            | 62.5            | 62.5            | 62.5            | 62.5            | 62.5            | 62.5            | 62.5            |
| # of IPs                                     | /                                      | 4               | 4               | 4               | 4               | 4               | 4               | 4               | 4               |
| Circumference                                | m                                      | 91174.117       | 91174.117       | 91174.117       | 91174.117       | 91174.117       | 91174.117       | 91174.117       | 91174.117       |
| Energy Loss/turn                             | MeV                                    | 39.1            | 137.9           | 142.7           | 140.2           | 142.7           | 137.8           | 137.7           | 142.7           |
| SR power loss                                | MW                                     | 50.0            | 54.5            | 56.4            | 55.4            | 56.4            | 54.4            | 54.4            | 56.4            |
| Beam current                                 | mA                                     | 1280            | 395             | 395             | 395             | 395             | 395             | 395             | 395             |
| Bunches/beam $n_b$                           | /                                      | 10000           | 13420           | 13420           | 13420           | 13420           | 13420           | 13420           | 13420           |
| Bunch population $N_b$                       | $10^{11}$                              | 2.43            | 0.56            | 0.56            | 0.56            | 0.56            | 0.56            | 0.56            | 0.56            |
| Horizontal emittance (SR/BS) $\varepsilon_x$ | nm                                     | 0.71 / 0.71     | 1.33 / 1.33     | 2.09 / 4.94     | 1.71 / 4.73     | 1.66 / 1.66     | 1.32 / 1.32     | 1.32 / 1.32     | 2.03 / 4.88     |
| Vertical emittance (SR/BS) $\varepsilon_y$   | pm                                     | 1.42 / 1.42     | 2.65 / 2.65     | 4.17 / 4.17     | 3.42 / 3.42     | 3.33 / 3.33     | 2.65 / 2.65     | 2.63 / 2.63     | 4.06 / 4.06     |
| Momentum compaction $\alpha_c$               | $10^{-6}$                              | 28.2            | 28.0            | 27.4            | 27.7            | 27.6            | 27.9            | 27.9            | 27.4            |
| $\beta_{x/y}^*$                              | mm                                     | 100 / 0.8       | 100 / 0.8       | 90 / 1          | 90 / 1          | 100 / 0.8       | 100 / 0.8       | 100 / 0.8       | 90 / 1          |
| $D_{x/y}^*$                                  | m                                      | 0 / 0           | 0 / 0           | 0.105 / 0       | 0.105 / 0       | 0 / 0           | 0 / 0.001       | 0 / 0.002       | 0.105 / 0.001   |
| Energy Spread (SR/BS) $\sigma_\delta$        | %                                      | 0.0392 / 0.2804 | 0.0537 / 0.0910 | 0.0548 / 0.0559 | 0.0543 / 0.0554 | 0.0548 / 0.0852 | 0.0537 / 0.0910 | 0.0537 / 0.0911 | 0.0548 / 0.0559 |
| Monochrom Factor (SR/BS) $\lambda$           | /                                      | 1 / 1           | 1 / 1           | 4.32 / 2.96     | 4.70 / 2.99     | 1 / 1           | 11.72 / 19.80   | 23.44 / 39.75   | 9.66 / 9.26     |
| CM energy spread (SR/BS) $\sigma_W$          | MeV                                    | 25.3 / 180.8    | 47.47 / 80.42   | 11.22 / 16.70   | 10.21 / 16.36   | 48.46 / 75.28   | 4.05 / 4.06     | 2.03 / 2.03     | 5.02 / 5.33     |
| Bunch length (SR/BS) $\sigma_z$              | mm                                     | 4.38 / 30.96    | 4.09 / 6.80     | 4.15 / 4.16     | 4.13 / 4.14     | 4.17 / 6.36     | 4.10 / 6.81     | 4.10 / 6.82     | 4.15 / 4.16     |
| Synchrotron tune $Q_s$                       | /                                      | 0.037           | 0.054           | 0.053           | 0.054           | 0.054           | 0.054           | 0.054           | 0.053           |
| Longitudinal damping time                    | turns                                  | 1168            | 453             | 438             | 446             | 438             | 454             | 454             | 438             |
| Luminosity (SR/BS)                           | $10^{34} \text{cm}^{-2} \text{s}^{-1}$ | 5476 / 5476     | 206.9 / 206.9   | 28.69 / 27.23   | 32.12 / 30.35   | 164.8 / 164.8   | 17.68 / 10.46   | 8.89 / 5.24     | 3.24 / 3.13     |

\* Not realistic only scaling

➤ FCC-ee GHC Monochrom Optics Performance based on tbar mode lattice (w/o BS effect)

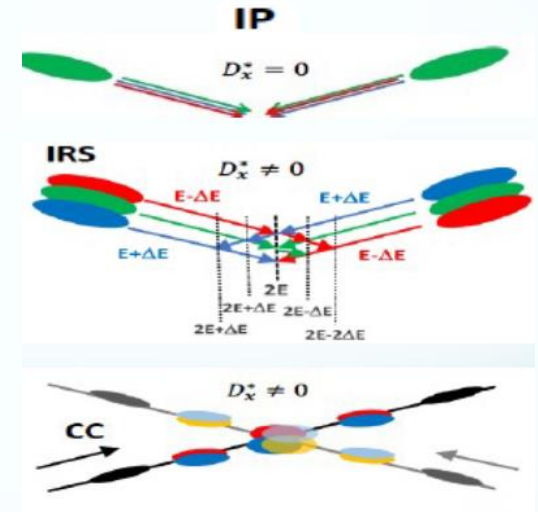
| Parameters                                   | Units                                  | Standard        | Standard_625*   | Monochrom_h_4ip | Monochrom_h_2ip | Monochrom_h_d0  | Monochrom_v_1   | Monochrom_v_2   | Monochrom_mix   |
|--|--|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Beam Energy $E$                              | GeV                                    | 182.5           | 62.5            | 62.5            | 62.5            | 62.5            | 62.5            | 62.5            | 62.5            |
| # of IPs                                     | /                                      | 4               | 4               | 4               | 4               | 4               | 4               | 4               | 4               |
| Circumference                                | m                                      | 91174.117       | 91174.117       | 91174.117       | 91174.117       | 91174.117       | 91174.117       | 91174.117       | 91174.117       |
| Energy Loss/turn                             | MeV                                    | 10000.0         | 137.6           | 143.5           | 140.5           | 143.4           | 137.6           | 137.6           | 143.4           |
| SR power loss                                | MW                                     | 50.0            | 54.3            | 56.7            | 55.5            | 56.7            | 54.3            | 54.3            | 56.7            |
| Beam current                                 | mA                                     | 5               | 395             | 395             | 395             | 395             | 395             | 395             | 395             |
| Bunches/beam $n_b$                           | /                                      | 40              | 13420           | 13420           | 13420           | 13420           | 13420           | 13420           | 13420           |
| Bunch population $N_b$                       | $10^{11}$                              | 2.37            | 0.56            | 0.56            | 0.56            | 0.56            | 0.56            | 0.56            | 0.56            |
| Horizontal emittance (SR/BS) $\varepsilon_x$ | nm                                     | 1.49 / 1.49     | 0.17 / 0.17     | 1.48 / 4.31     | 0.84 / 3.97     | 0.35 / 0.35     | 0.17 / 0.17     | 0.17 / 0.17     | 1.48 / 4.31     |
| Vertical emittance (SR/BS) $\varepsilon_y$   | pm                                     | 2.98 / 2.98     | 0.34 / 0.34     | 2.96 / 2.96     | 1.68 / 1.68     | 0.71 / 0.71     | 0.35 / 0.35     | 0.35 / 0.35     | 2.96 / 2.96     |
| Momentum compaction $\alpha_c$               | $10^{-6}$                              | 6.99            | 7.30            | 6.92            | 7.12            | 7.06            | 7.31            | 7.31            | 6.92            |
| $\beta_{x/y}^*$                              | mm                                     | 1000 / 1.6      | 1000 / 1.6      | 90 / 1          | 90 / 1          | 1000 / 1.6      | 1000 / 1.6      | 1000 / 1.6      | 90 / 1          |
| $D_{x/y}^*$                                  | m                                      | 0 / 0           | 0 / 0           | 0.105 / 0       | 0.105 / 0       | 0 / 0           | 0 / 0.001       | 0 / 0.002       | 0.105 / 0.001   |
| Energy Spread (SR/BS) $\sigma_\delta$        | %                                      | 0.1569 / 0.2180 | 0.0537 / 0.0861 | 0.0552 / 0.0563 | 0.0545 / 0.0556 | 0.0552 / 0.0714 | 0.0537 / 0.0861 | 0.0537 / 0.0861 | 0.0552 / 0.0563 |
| Monochrom Factor (SR/BS) $\lambda$           | /                                      | 1 / 1           | 1 / 1           | 5.12 / 3.16     | 6.65 / 3.25     | 1 / 1           | 22.81 / 36.55   | 45.58 / 73.08   | 11.38 / 10.82   |
| CM energy spread (SR/BS) $\sigma_W$          | MeV                                    | 404.91 / 562.75 | 47.46 / 76.10   | 9.54 / 15.73    | 7.24 / 15.14    | 48.81 / 63.08   | 2.08 / 2.08     | 1.04 / 1.04     | 4.29 / 4.60     |
| Bunch length (SR/BS) $\sigma_z$              | mm                                     | 2.03 / 2.70     | 3.86 / 6.18     | 4.05 / 4.13     | 3.95 / 4.03     | 4.09 / 5.28     | 3.86 / 6.18     | 3.86 / 6.18     | 4.05 / 4.13     |
| Synchrotron tune $Q_s$                       | /                                      | 0.082           | 0.015           | 0.014           | 0.014           | 0.014           | 0.015           | 0.015           | 0.014           |
| Longitudinal damping time                    | turns                                  | 18.5            | 454             | 436             | 445             | 436             | 454             | 454             | 436             |
| Luminosity (SR/BS)                           | $10^{34} \text{cm}^{-2} \text{s}^{-1}$ | 2.21 / 2.21     | 353.2 / 353.2   | 34.1 / 32.3     | 46.19 / 43.53   | 173.5 / 173.5   | 15.49 / 9.66    | 7.750 / 4.834   | 3.227 / 3.116   |

\* Not realistic only scaling

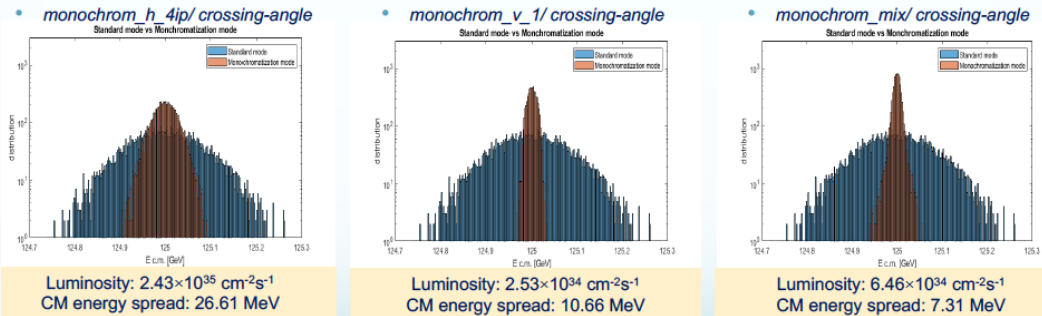
Lower CM energy spread compared to Z mode

Luminosity and CM Energy Spread (with BS) calculated with Guinea-pig for FCC-ee GHC monochrom based on Z mode lattice for: **monochrom crab cavities (CC)** and **monochrom (crossing or Integrated Resonances Scan IRS)** compared to standard (crossing)

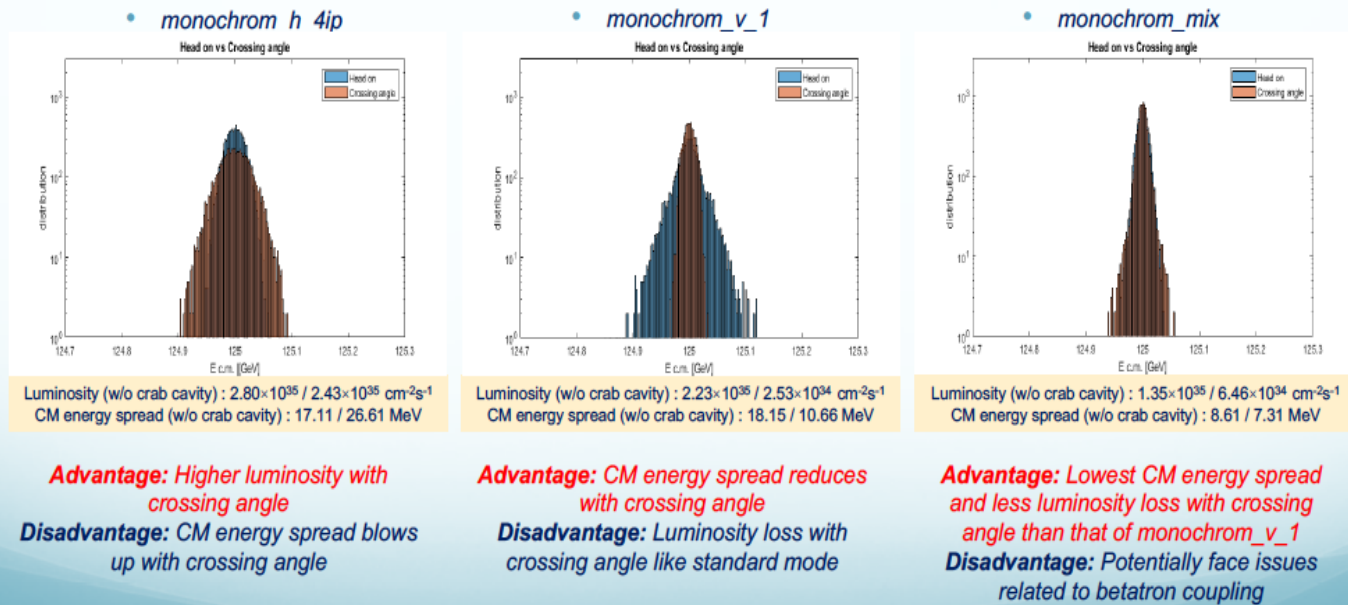
## ➤ Monochrom CC vs Standard



Standard\_625/crossing-angle: Luminosity:  $4.50 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ , CM energy spread: 80.33 MeV

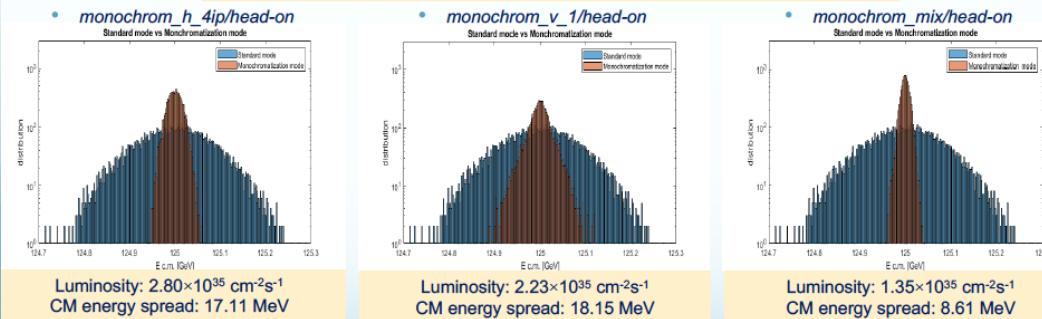


## ➤ Monochrom CC vs IRS



## ➤ Monochrom IRS vs Standard

Standard\_625/head-on: Luminosity:  $1.20 \times 10^{36} \text{ cm}^{-2}\text{s}^{-1}$ , CM energy spread: 80.12 MeV



## ➤ FCC-ee GHC Monochrom Optics based on Z mode lattice

| Parameters                         | Units                                  | Standard        | Standard_625  | Monochrom_h_4ip | Monochrom_h_2ip | Monochrom_h_d0 | Monochrom_v_1 | Monochrom_v_2 | Monochrom_mix |
|------------------------------------|--|-----------------|---------------|-----------------|-----------------|----------------|---------------|---------------|---------------|
| Luminosity (w/o crab cavity)       | $10^{34} \text{cm}^{-2} \text{s}^{-1}$ | 449 / 99.3      | 120 / 45.0    | 28.0 / 24.3     | 31.2 / 27.8     | 99.8 / 42.7    | 22.3 / 2.53   | 9.92 / 1.28   | 13.5 / 6.46   |
| CM energy spread (w/o crab cavity) | MeV                                    | 180.38 / 182.85 | 80.12 / 80.33 | 17.11 / 26.61   | 16.31 / 26.18   | 76.65 / 75.52  | 18.15 / 10.66 | 9.12 / 9.66   | 8.61 / 7.31   |

## ➤ FCC-ee GHC Monochrom Optics based on ttbar mode lattice

| Parameters                         | Units                                  | Standard       | Standard_625  | Monochrom_h_4ip | Monochrom_h_2ip | Monochrom_h_d0 | Monochrom_v_1 | Monochrom_v_2 | Monochrom_mix |
|------------------------------------|--|----------------|---------------|-----------------|-----------------|----------------|---------------|---------------|---------------|
| Luminosity (w/o crab cavity)       | $10^{34} \text{cm}^{-2} \text{s}^{-1}$ | 1.83 / 1.52    | 399 / 122     | 33.7 / 29.4     | 45.3 / 40.6     | 210 / 91.2     | 21.2 / 2.98   | 9.08 / 1.45   | 14.8 / 6.43   |
| CM energy spread (w/o crab cavity) | MeV                                    | 547.02 / 542.7 | 75.94 / 76.65 | 15.86 / 25.88   | 15.32 / 25.10   | 63.43 / 64.39  | 9.10 / 4.94   | 5.94 / 4.51   | 7.64 / 6.36   |

**Monochrom optics based on ttbar mode lattice has lower CM energy spread than the one based on Z mode lattice**

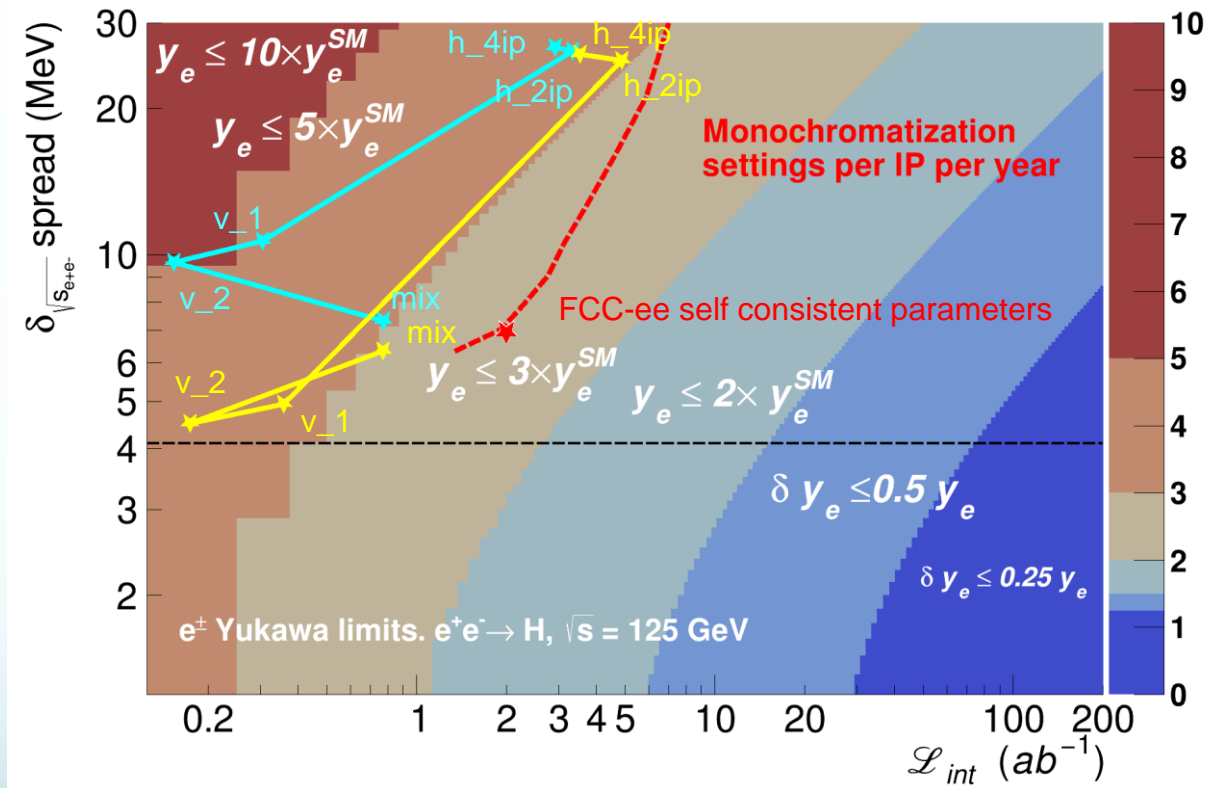
## Associated upper limits contours (95% CL) on the electron Yukawa ( $y_e$ )

FCC-ee monochrom parametric studies (red line\*), Z mode lattice based monochrom performance (light blue), ttbar mode lattice based monochrom performance (yellow).

The best performance is obtained with the **ttbar lattice based “mix” mode**, which reaches an upper limit of  $y_e < 2.9 \cdot y_e(\text{SM})$  in the Higgs-electron coupling.

**Re-optimization of the beam parameters should give better performances.**

D. d'Enterria, A. Poldaru, G. Wojcik, Measuring the electron Yukawa coupling via resonant s-channel Higgs production at FCC-ee, arXiv:2107.02686v1 [hep-ex] 6 Jul 2021



\* A. Faus-Golfe, M. Valdivia Garcia, F. Zimmermann, The challenge of monochromatization Direct s-channel Higgs production:  $e^+e^- \rightarrow H$ , Eur. Phys. J. Plus (2022) 137:31, <https://doi.org/10.1140/epjp/s13360-021-02151-y>

# Summary and Perspectives

- Monochromatization is a **simple conceptual idea** but not easy to implement in a collider, if not integrated from the beginning in the optics IR design as a dedicated operation mode.
- However, the monochromatization principle research **never reached a maturity level** allowing **implementation** and **experimental testing**. A flexible lattice with two modes of operation with/without monochromatization is mandatory.
- Different **FCC-ee GHC Monochrom “realistic” optics** lattices has been completed for V22 featuring very **promising performances**.
- Further studies on FCC-ee GHC Monochrom lattices are needed: to evaluate the impact of the **beam-beam with  $D_{x,y}^* \neq 0$**  and to optimize the DA for these new type of operation mode.
- Implementation and comparison with the LCC FCC-ee kind of lattice with more symmetric IRs will be carried out.
- Monochrom optics design for CEPC is ongoing (IR more symmetric)
- Experimental proof of monochromatization concept in running e+e- low energy colliders are under study for BEPCII (IHEP China), Daphne and maybe in SuperKEKB.



**THE BRAVE COLLABORATORS**  
*MonochroM team*

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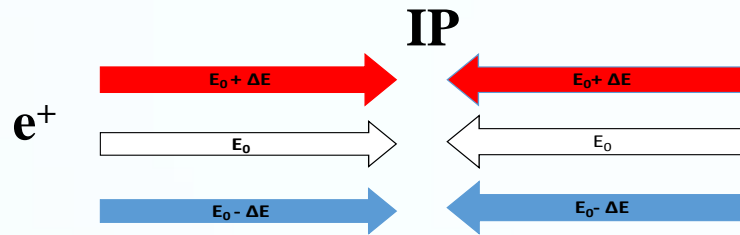


**Back-up slides**



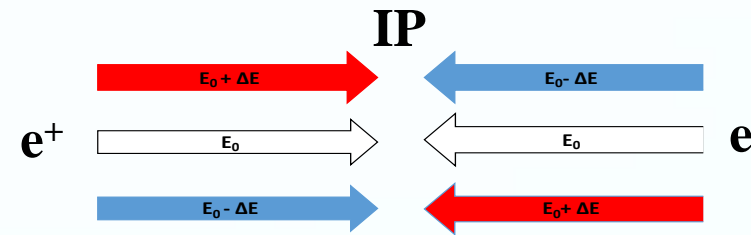
# Monochromatization principle

## Standard



$D_{x,y}^* = 0$   
 correlation between transverse spatial position and energy deviation

## Monochromatization



$D_{x+}^* = -D_{x-}^* = D_x^*$   
 $D_{y+}^* = -D_{y-}^* = D_y^*$   
 Opposite correlations between transverse spatial position and energy deviation

$$w = 2(E_b + \Delta E)$$

$$\sigma_w = \sqrt{2} E_b \sigma_\delta \quad \text{Relative energy spread}$$

$$\lambda = 1$$

$$L_0 = \frac{k_b f_r N_+ N_- \text{ Particles per bunch}}{4\pi \sigma_{x\beta}^* \sigma_{y\beta}^*} \quad \text{betatronic beam sizes at the IP}$$

$$\sigma_{x,y}^* = \sqrt{\beta_{x,y}^* \epsilon_{x,y} + (D_{x,y}^* \sigma_\delta)^2} \quad \text{dispersive beam size at the IP}$$

### CM energy

$$w = 2E_b + O(\Delta E)^2$$

### Spread of the CM energies

$$\sigma_w = \frac{\sqrt{2} E_b \sigma_\delta}{\lambda}$$

### Monochromatization factor

$$\lambda = \left( 1 + \sigma_\delta^2 \left( \frac{D_x^{*2}}{\sigma_{x\beta}^{*2}} + \frac{D_y^{*2}}{\sigma_{y\beta}^{*2}} \right) \right)^{1/2}$$

### Luminosity

$$L = \frac{L_0}{\lambda}$$

**Enhancement of energy resolution, and sometimes increase of the relative frequency of the events at the center of of the distribution but **luminosity loss !!!!****

# Monochromatization in high-energy colliders

In the previous case for low-energy  $e^+e^-$  colliders, the **relative energy spread** is mainly given by **SR** in the colliders arcs ( $\sigma_\delta = \sigma_{\delta,SR}$ ). Alternatively in **high-energy  $e^+e^-$** , we have to take into account also the **SR** created by the strong opposing EM field during collision or “**beamstrahlung**”(BS) ( $N\gamma \propto 1/\sigma_z (\sigma_x^* + \sigma_y^*)$ , with  $\sigma_z$  the bunch length).

## Standard BS $D_{x,y}^* = 0$

Energy spread w/o BS

$$\sigma_{\delta,tot} = \sqrt{\frac{1}{2} \sigma_{\delta,SR}^2 + \sqrt{\frac{1}{4} \sigma_{\delta,SR}^4 + A \frac{\sigma_{\delta,SR}^2}{\sigma_{z,SR}^2}}}$$

Bunch length w/o BS

$$A = \frac{275}{36} \frac{n_{IP} \tau_E r_e^5 N_b^3 \gamma^2}{\pi^{\frac{3}{2}} 4 T_{rev} \alpha \sigma_{x,SR}^3}$$

Beam size w/o BS  
Revolution time

$$\varepsilon_{x,tot} \approx \varepsilon_{x,SR}$$

Horizontal emittance without BS

Momentum compaction factor

$$\sigma_{z,tot} = \frac{\alpha_c C}{2\pi Q_s} \sigma_{\delta,tot}$$

Circumference  
Synchrotron tune

**BS at high-energy** with  $D_x^* = 0$ , has more **impact** on **energy spread** in standard mode than in monochromatization mode.

## Monochromatization BS $D_{x+}^* = -D_{x-}^* = D_x^*$ $D_{y+}^* = -D_{y-}^* = D_y^*$

Energy spread

$$\sigma_{\delta,tot}^2 = \sigma_{\delta,SR}^2 + \frac{B}{D_x^{*3} \sigma_{\delta,tot}^5}$$

Coupled system to be solved numerically

$$B \approx 50 \frac{n_{IP} \tau_E r_e^5 N_b^3 \gamma^2}{T_{rev} (\alpha_c C / (2\pi Q_s))^2}$$

Horizontal emittance

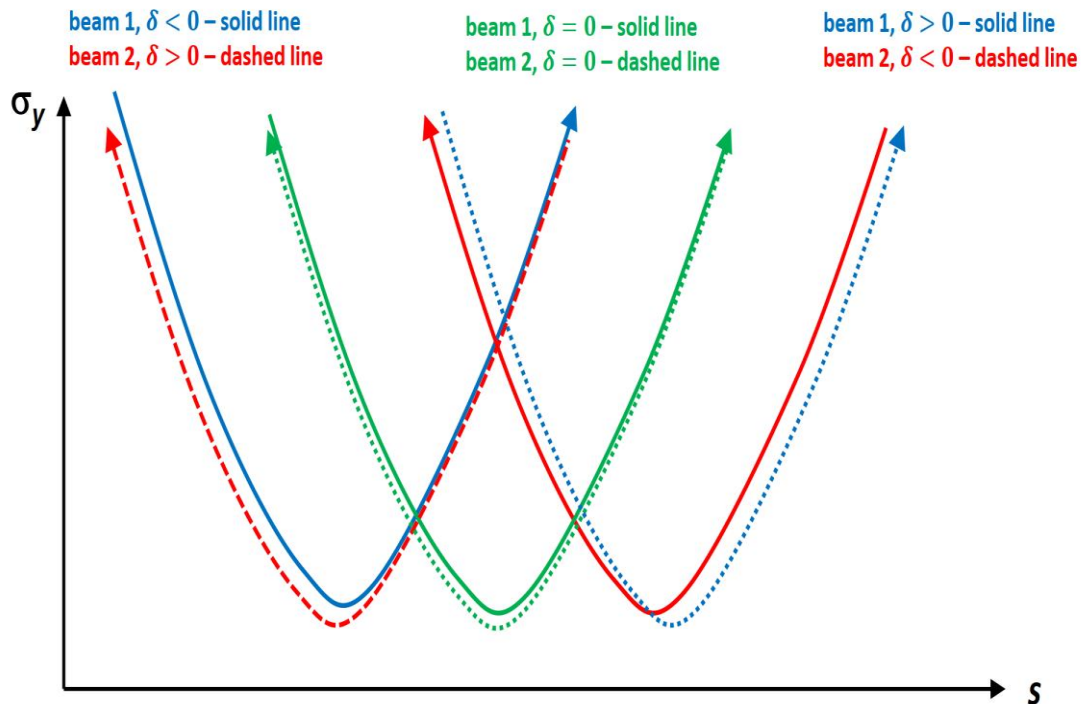
$$\varepsilon_{x,tot} \approx \varepsilon_{x,SR} + \frac{2B}{D_x^* \beta_x^* \sigma_{\delta,tot}^5}$$

## Bunch length

$$\sigma_{z,tot} = \frac{\alpha_c C}{2\pi Q_s} \sigma_{\delta,tot}$$

**BS with monochromatization at high-energy**, avoids the **blow up** of the relative beam energy spread, which is significant in standard mode with  $D_x^* = 0$ .

- Monochromatization could be obtained by operating with a **residual nonzero local vertical chromaticity** (RLC). This enables the focal length of the final quadrupoles to change with the momentum deviation of a beam particle, and establishes a dependence between the vertical beam size waist and momentum offset. An effective monochromatization could be obtained, without adding any new hardware. The resulting monochromatization factor will be enhanced for smaller  $\mathcal{R}_y^*$ , but limited  $\lambda$  possible.



Waist location for beam 1 with momentum offset  $\delta$ , can be made to coincide with the waist location for beam 2 with momentum offset  $-\delta$ , leading to an effective monochromatization, without adding any new hardware.

P. Raimondi, F. Zimmermann, private communication

- Monochromatization with **dispersion inside the deflecting RF cavities (SCRF-D)** on either side of the collision point.



$$E_s = -E_{s0} \sin k_x x \cdot \cos k_z z \cdot \cos(\omega t + \phi),$$

$$H_x = \frac{k_z}{k} E_{s0} \sin k_x x \cdot \sin k_z z \cdot \sin(\omega t + \phi), \quad (1)$$

$$H_z = -\frac{k_x}{k} E_{s0} \cos k_x x \cdot \cos k_z z \cdot \sin(\omega t + \phi),$$

where  $E_{s0}$  is the amplitude of electric field;  $\omega$ ,  $\phi$  are the frequency and phase of oscillations;  $k_x = 2\pi/a_x$ ,  $k_z = \pi/a_z$ ,  $k^2 = k_x^2 + k_z^2$ .

A.A. Zholents, Sophisticated accelerator techniques for colliding beam experiments. Nucl. Instrum. Methods A 265, 179–185 (1988)

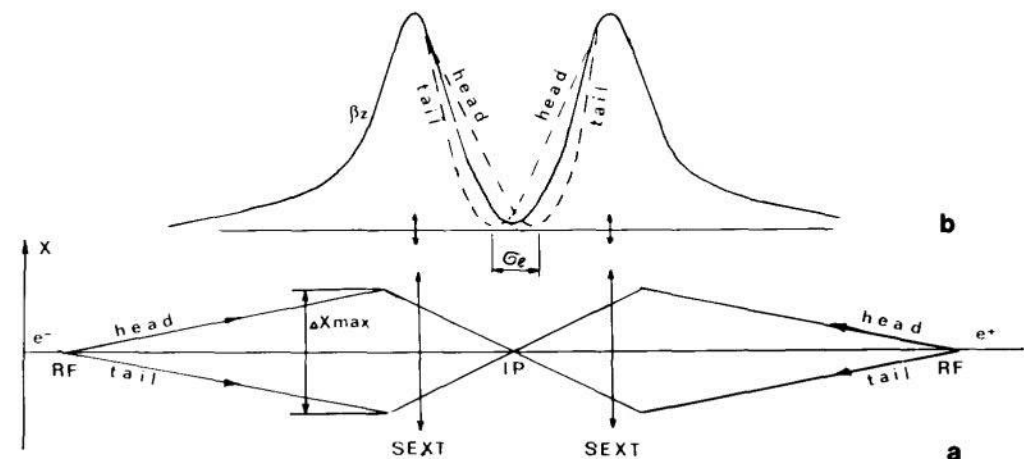
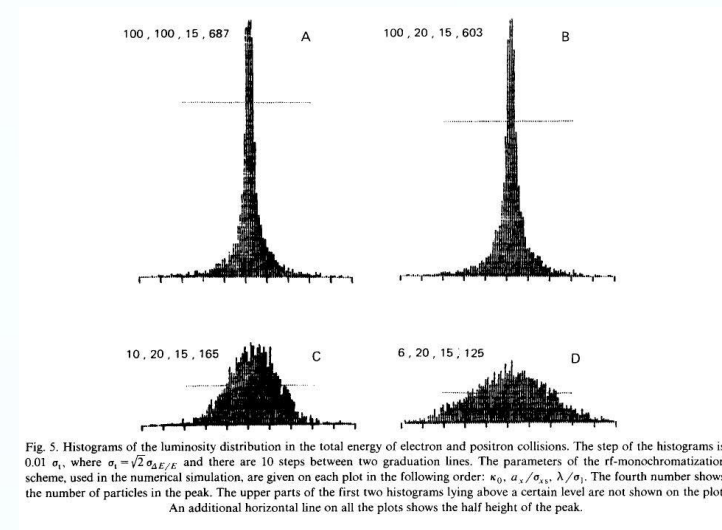


Fig. 6. a) The trajectories of the head and the tail of the bunch in the region between AS. b) The behaviour of  $\beta_z$ -function.

- Local Chromaticity Correction

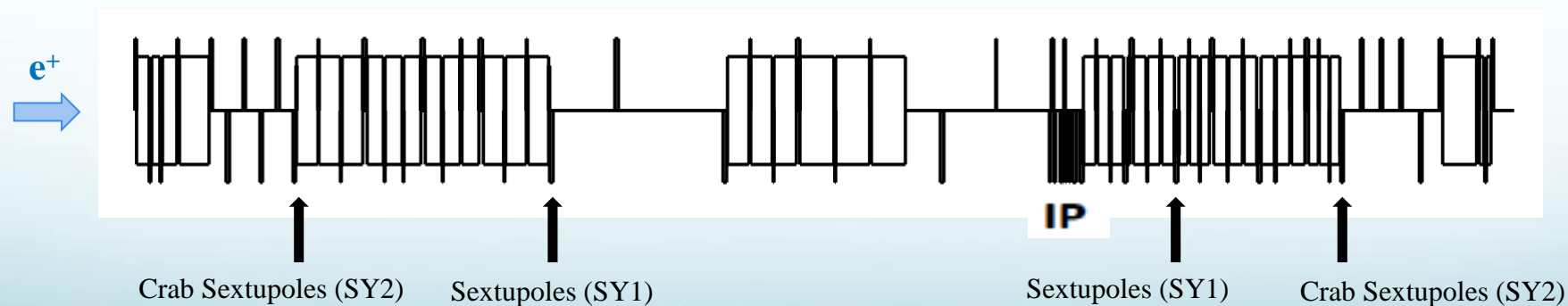
- Load monochromatization ring lattice, and extract sequence from IP to crab sextupoles.
- Turned off all the sextupoles including crab sextupoles SY2.
- Match the vertical chromaticity from IP to crab sextupoles to 0 using the sextupoles SY1.
- Calculate the strength of crab sextupoles (SY2) with the following formula [6]:

$$K2_{SY2} = K2_{SY1} \pm crab_{factor} \cdot crab_{strength}$$

The crab strength is given by:

$$crab_{strength} = \frac{1}{L_{SY2} * \theta_{CROSS} * BY_{IP} * BY_{CS}} * \sqrt{\frac{BX_{IP}}{BX_{CS}}}$$

The crab factor is determined from Beam-beam studies, at Z it's 97%, W 87%, so ~90% for Higgs mode seems a good starting guess.



[6] K. Oide, M. Aiba, S. Aumon, M. Benedikt, A. Blondel et al. "Design of beam optics for the future circular collider  $e^+e^-$  collider rings", Physical Review Accelerators and Beams, 19, 111005 (2016)

- **Global Chromaticity Correction**

With the matched strength of the SY1 and the strength of SY2 calculated by the formula, the global chromaticity correction is done by matching the strength of all the sextupoles in the arc.

There are two kinds of sextupoles in the arc, focus sextupoles and defocus sextupoles. The strength of all the focus sextupoles is multiplied by the coefficient  $kn_{sf}$ , while the strength of all the defocus sextupoles is multiplied by the coefficient  $kn_{sd}$ .

The horizontal chromaticity (DQ1) and vertical chromaticity (DQ2) are matched to 5 with the two coefficient, because positive chromaticity is benefit for the beam stability.

- **Tune Correction**

By varying the strength of quadrupoles around the RF cavities in the arc, the horizontal tune Q1 and vertical tune Q2 are matched to be same with the standard mode while keeping the beam parameters at the IRs.

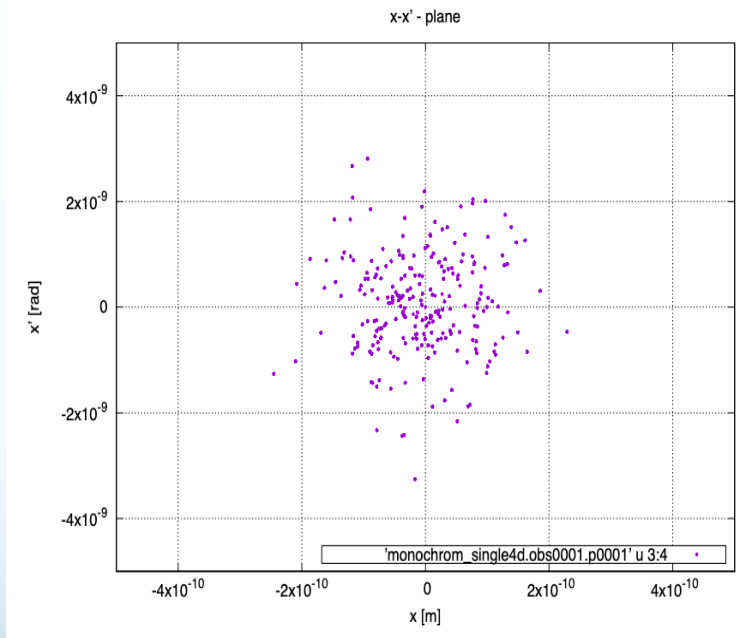
- **Emittance Check**

Switching on the RF cavities and considering the energy loss due to synchrotron radiation, the longitudinal energy difference ( $p\hat{t}$ ) are matched to zero by varying the voltage and the phase of the RF cavities in tapering twiss model.

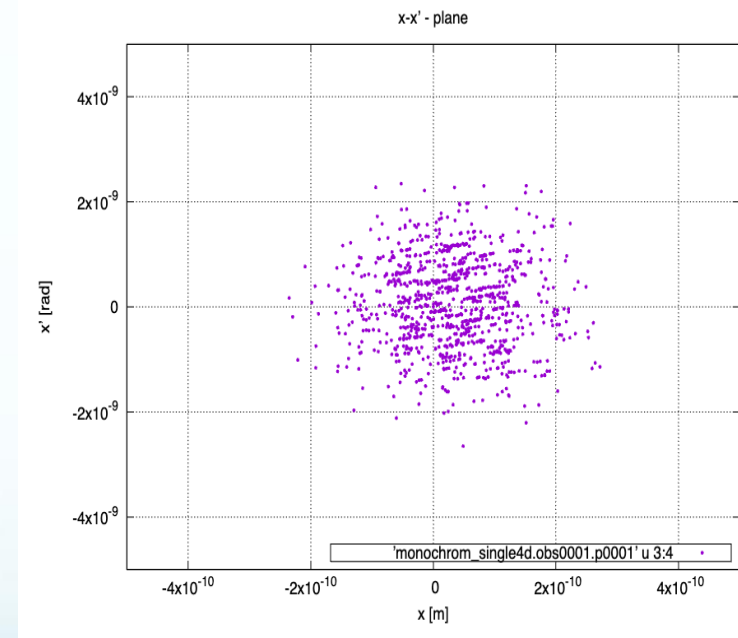
- Preliminary Single Particle Tracking in MADX-PTC

1000-turn single particle tracking (4D) calculated with MADX-PTC (FCC-ee monochromatization optics base on Z mode lattice)

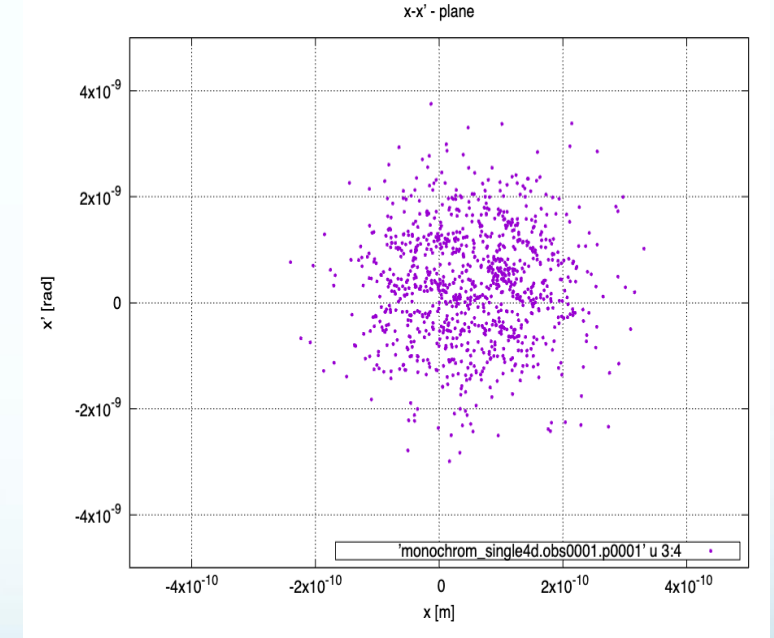
- *monochrom\_h\_4ip*



- *monochrom\_v\_1*



- *monochrom\_mix*



# Monochromatization IR Performance Check

- Preliminary Dynamic Aperture Particle Tracking in MADX-PTC

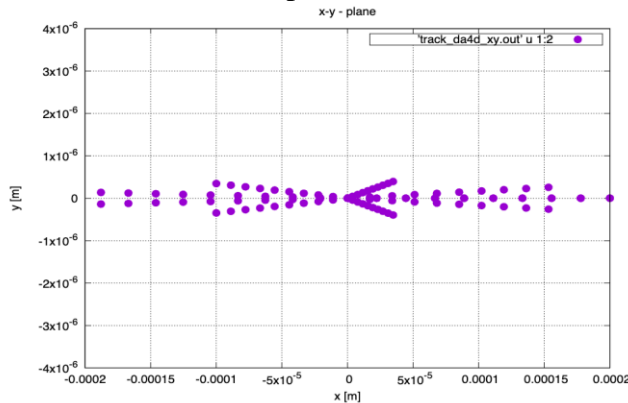
1000-turn dynamic aperture particle tracking (4D) calculated with MADX-PTC taking 100 particles without family sextupole optimization in the arc (FCC monochromatization optics base on Z mode lattice)

- *monochrom\_h\_4ip*

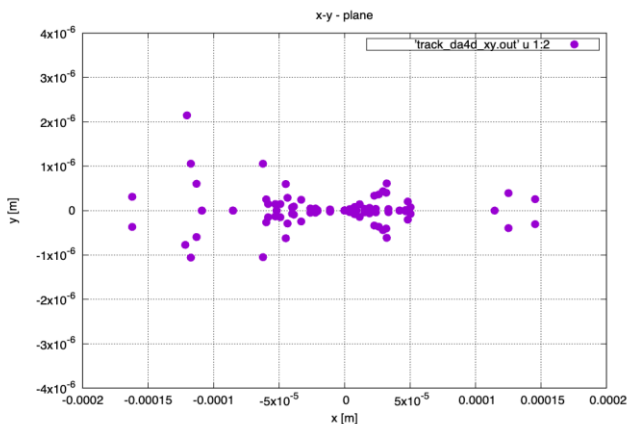
- *monochrom\_v\_1*

- *monochrom\_mix*

Input Particles

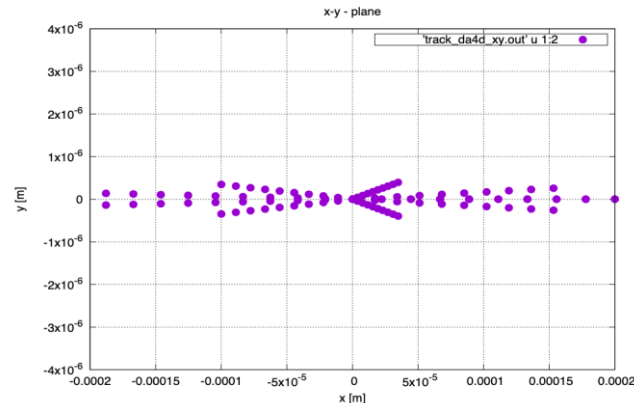


Stable Cloud

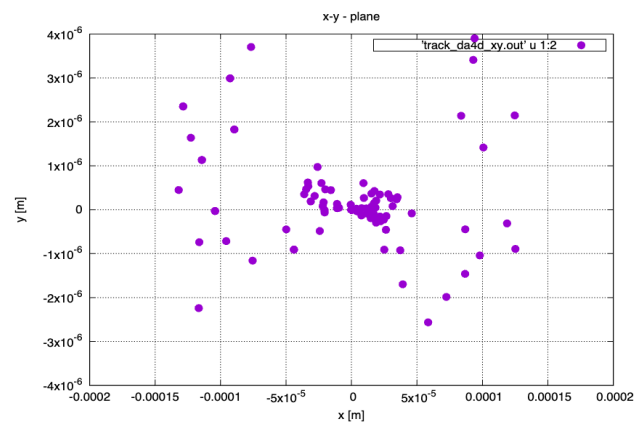


100% particles survive after 1000 turns

Input Particles

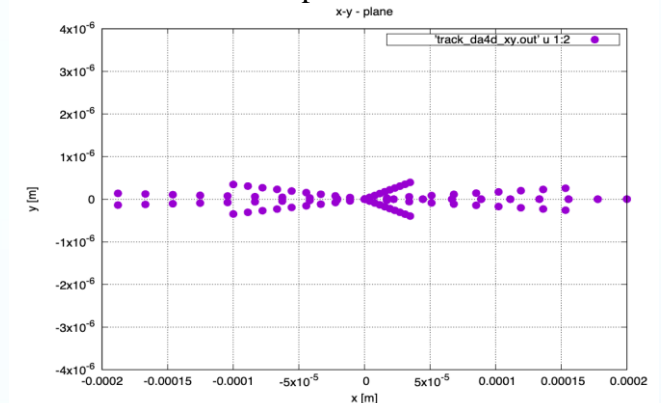


Stable Cloud

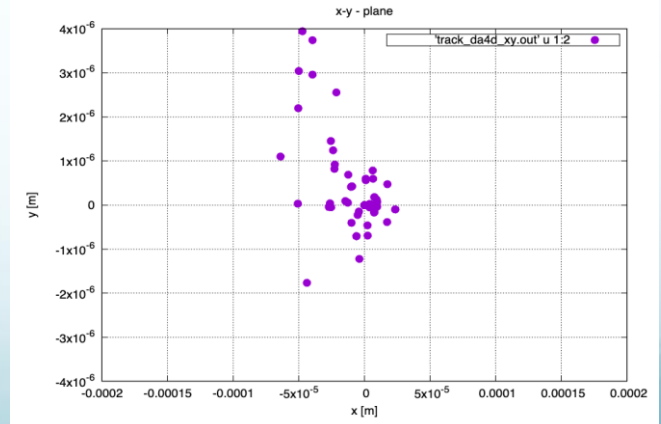


100% particles survive after 1000 turns

Input Particles



Stable Cloud



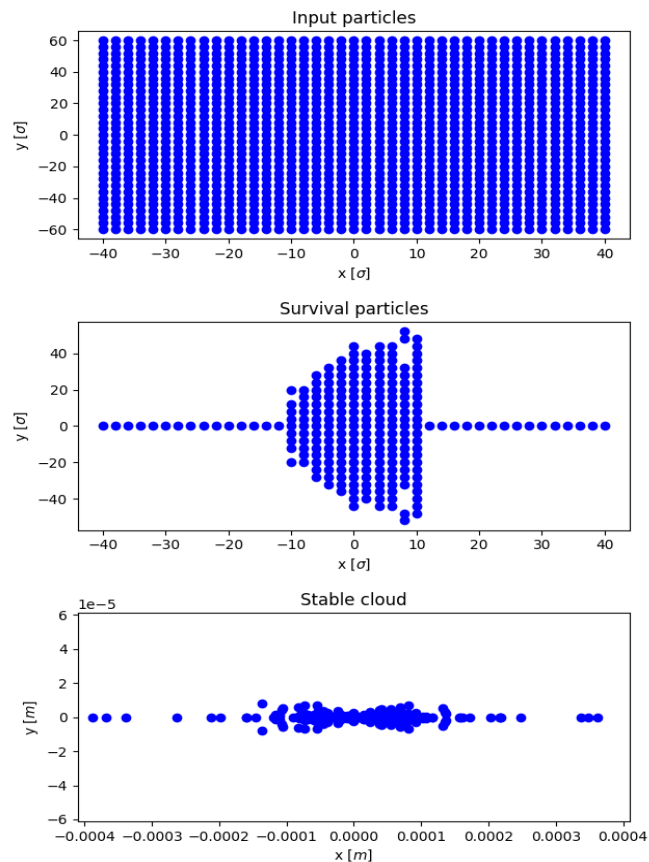
70% particles survive after 1000 turns



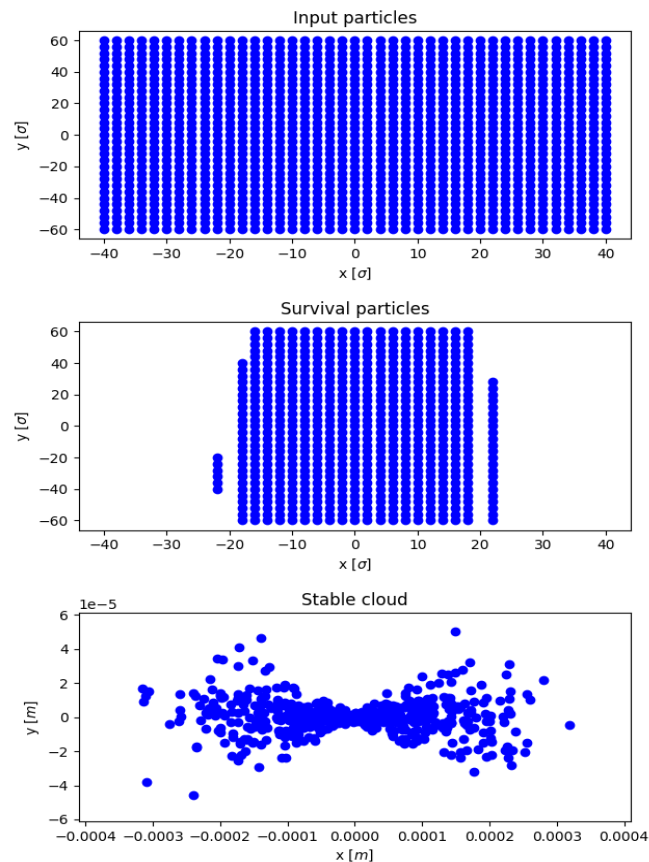
- Preliminary Dynamic Aperture Particle Tracking in Xsuite**

1000-turn dynamic aperture particle tracking (4D) calculated with Xsuite without family sextupole optimization in the arc (FCC-ee monochromatization optics base on Z mode lattice).

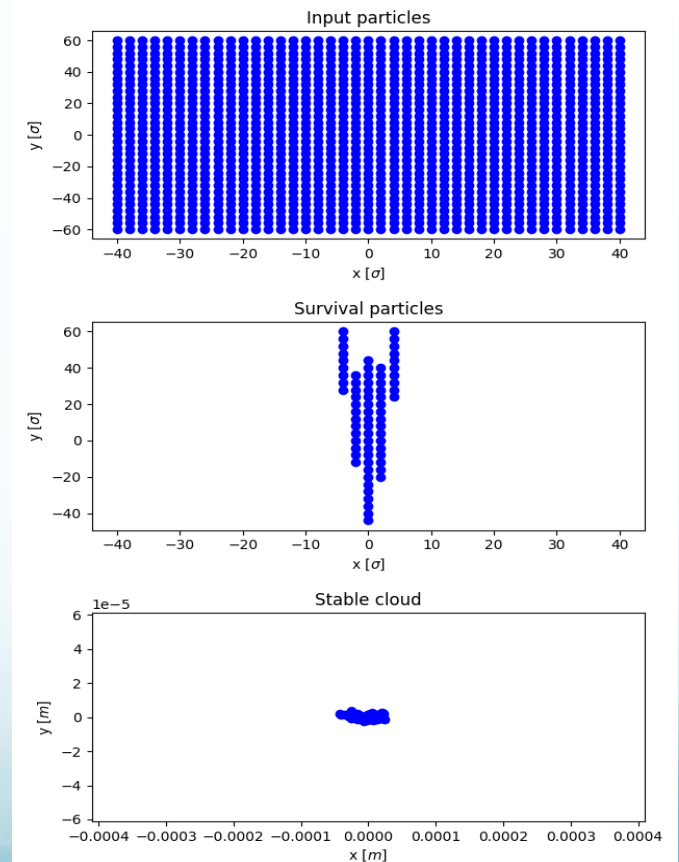
- monochrom\_h\_4ip*



- monochrom\_v\_1*



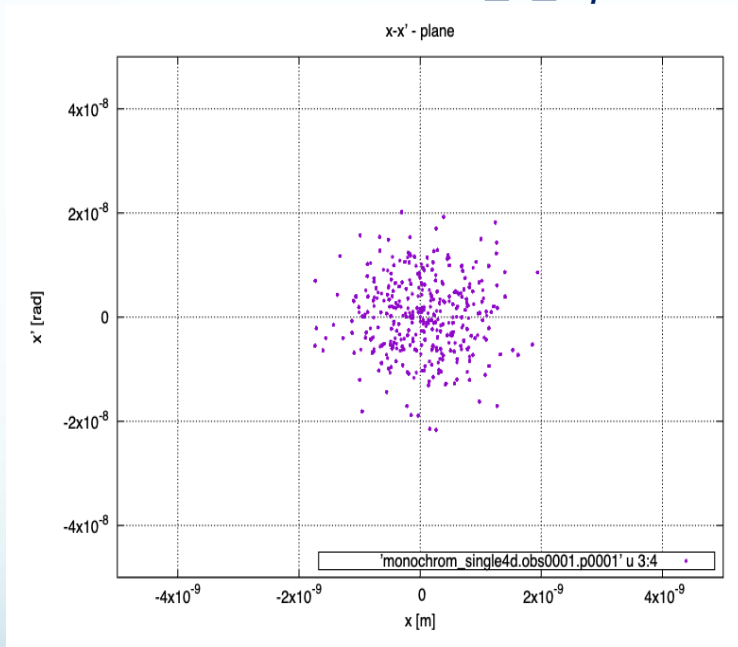
- monochrom\_mix*



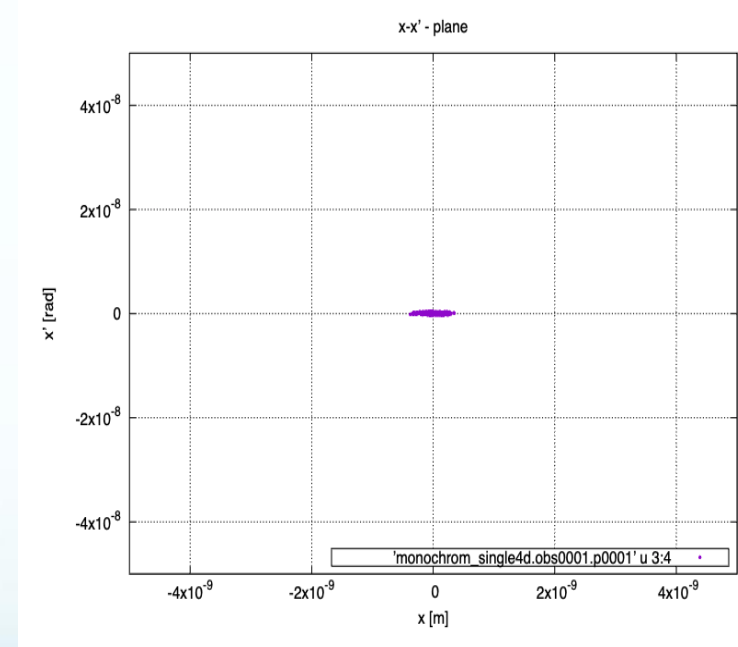
- Preliminary Single Particle Tracking in MADX-PTC

1000-turn single particle tracking (4D) calculated with MADX-PTC (FCC-ee monochromatization optics base on ttbar mode lattice)

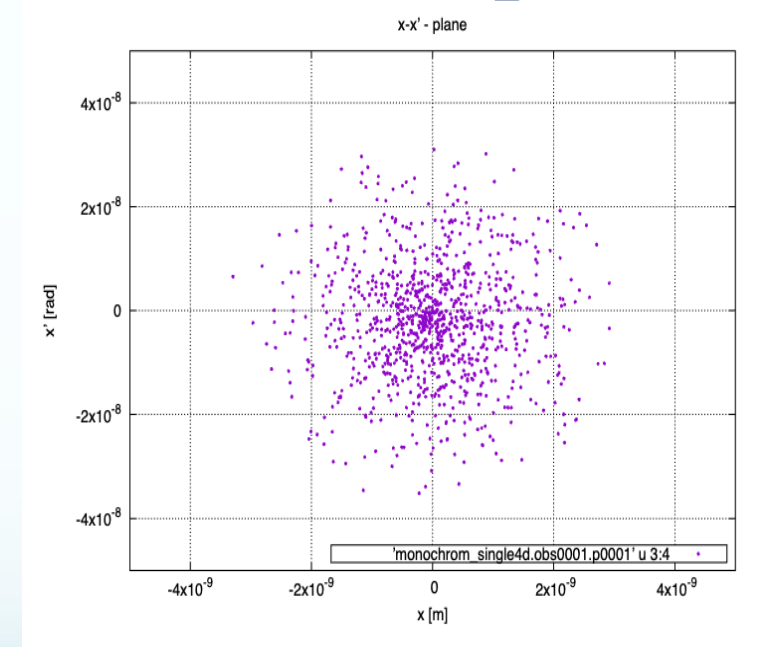
- *monochrom\_h\_4ip*



- *monochrom\_v\_1*



- *monochrom\_mix*



# Monochromatization IR Performance Check

- Preliminary Dynamic Aperture Particle Tracking in MADX-PTC

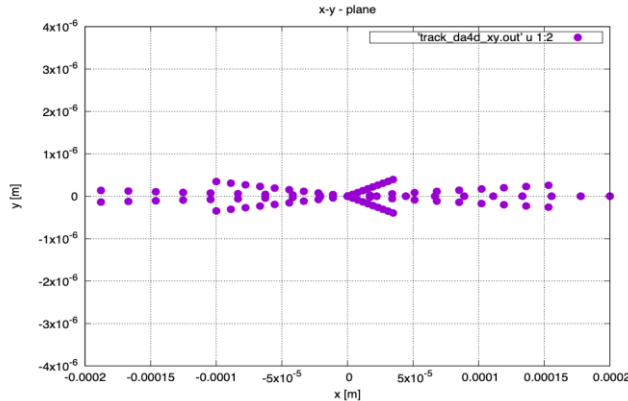
1000-turn dynamic aperture particle tracking (4D) calculated with MADX-PTC taking 100 particles without family sextupole optimization in the arc (FCC monochromatization optics base on tbar mode lattice)

- *monochrom\_h\_4ip*

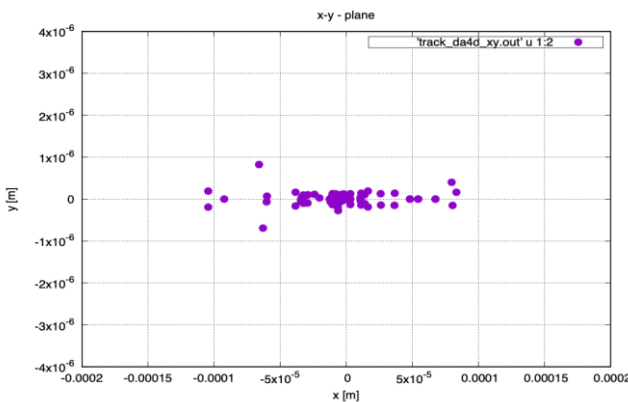
- *monochrom\_v\_1*

- *monochrom\_mix*

Input Particles

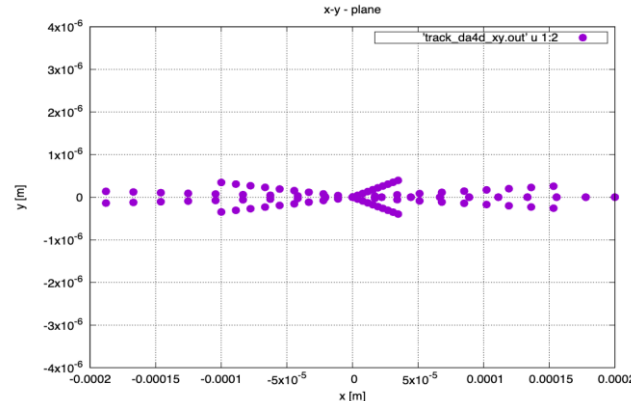


Stable Cloud

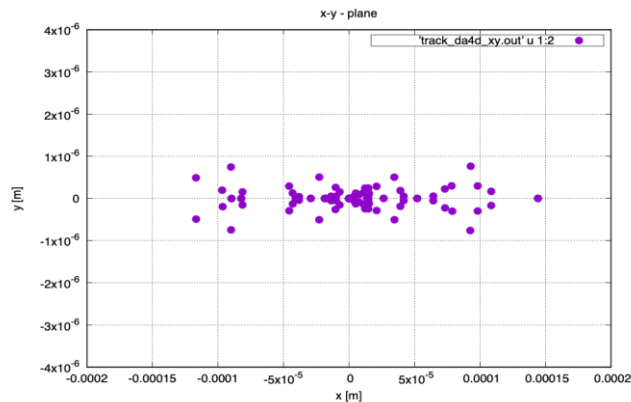


82% particles survive after 1000 turns

Input Particles

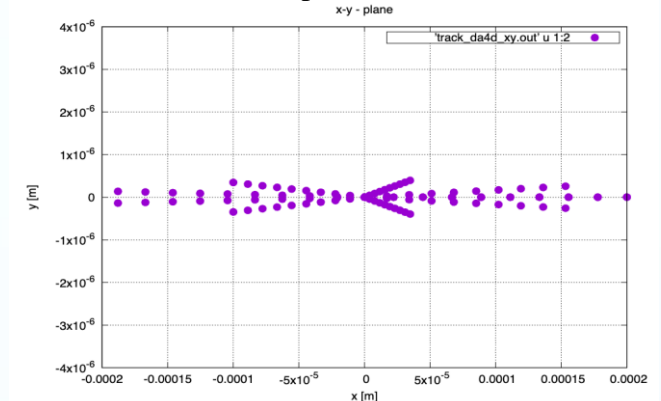


Stable Cloud

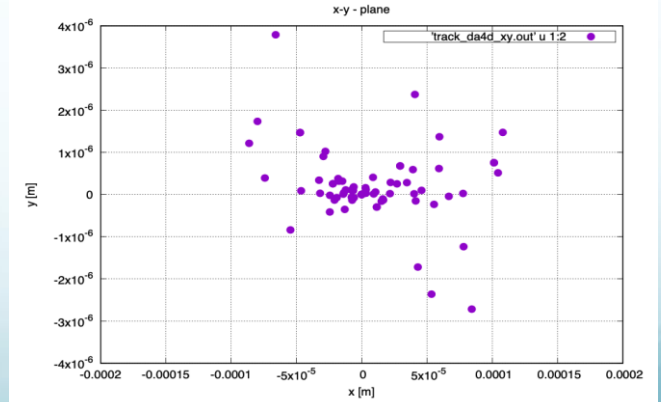


100% particles survive after 1000 turns

Input Particles



Stable Cloud

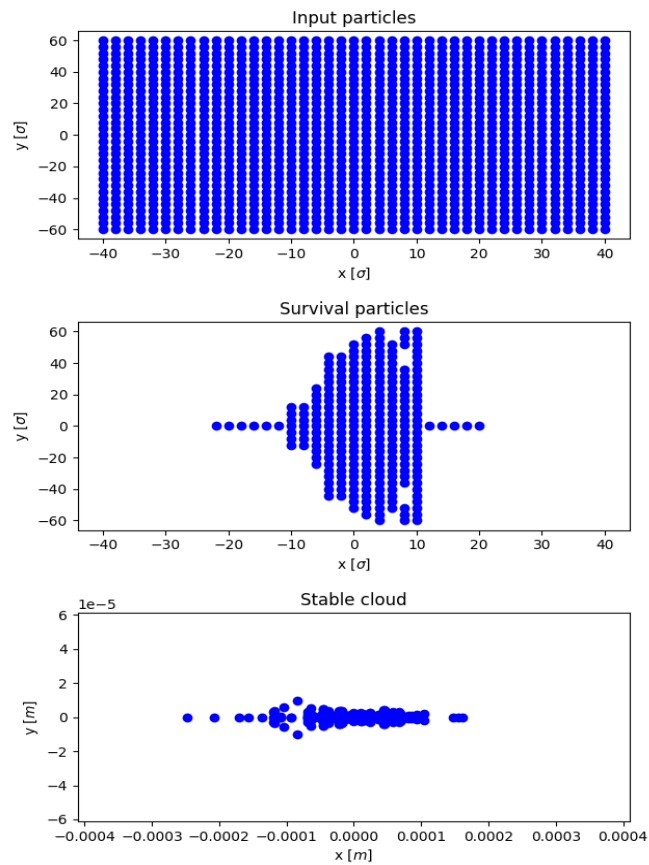


78% particles survive after 1000 turns

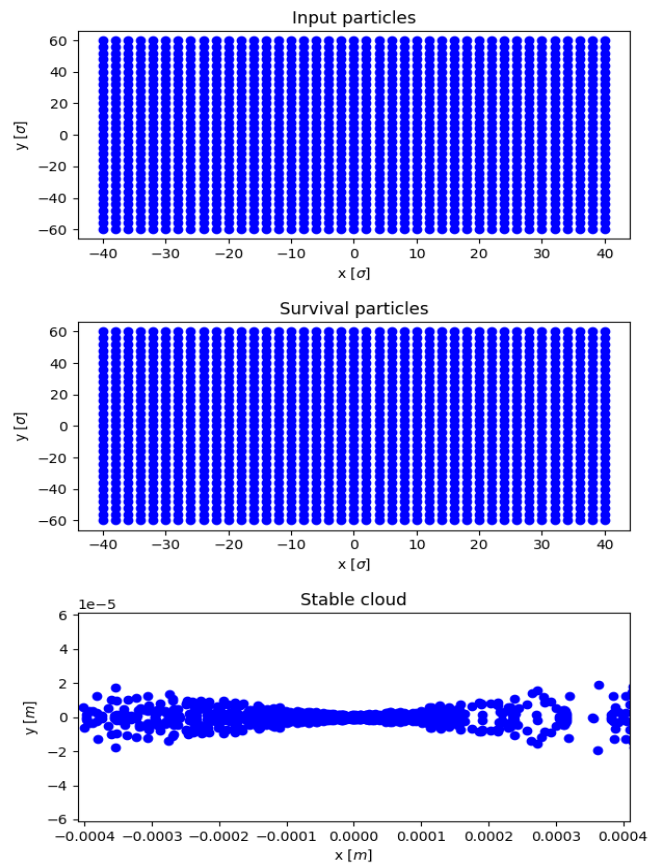
- Preliminary Dynamic Aperture Particle Tracking in Xsuite

1000-turn dynamic aperture particle tracking (4D) calculated with Xsuite without family sextupole optimization in the arc (FCC-ee monochromatization optics base on tbar mode lattice).

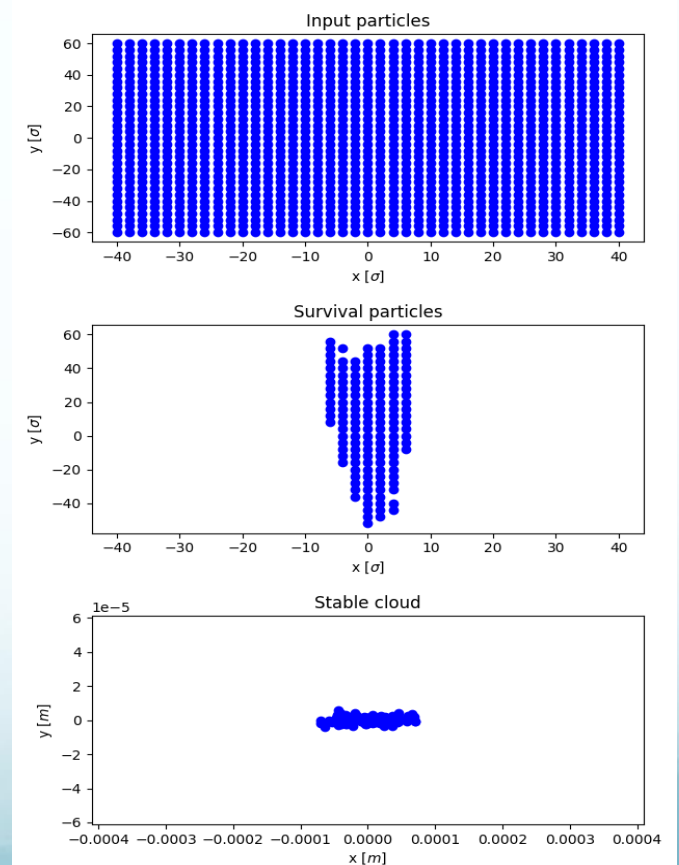
- *monochrom\_h\_4ip*



- *monochrom\_v\_1*



- *monochrom\_mix*

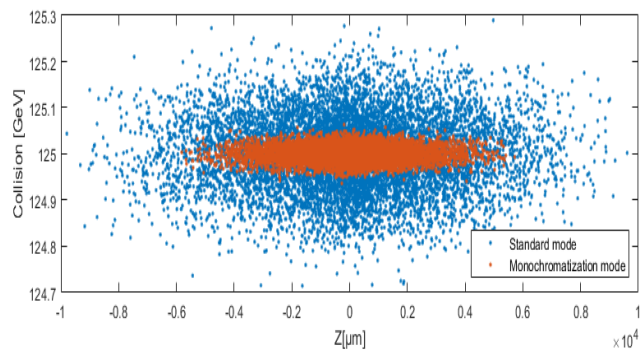
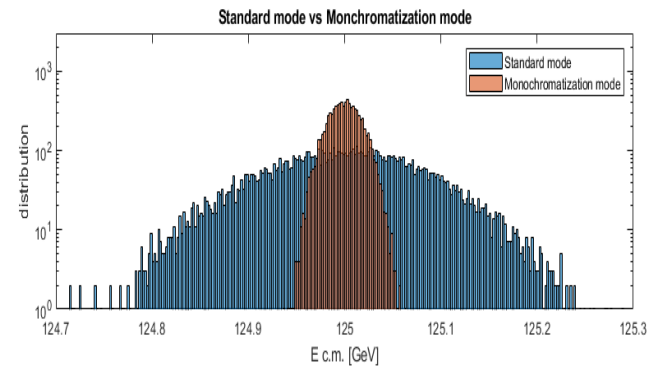


- Luminosity and CM Energy Spread (with BS effect)**

The following figures show the Guinea-pig calculation result of FCC-ee monochromatization optics base on Z mode lattice with crab cavities (head-on) compared with that of the scaled standard mode.

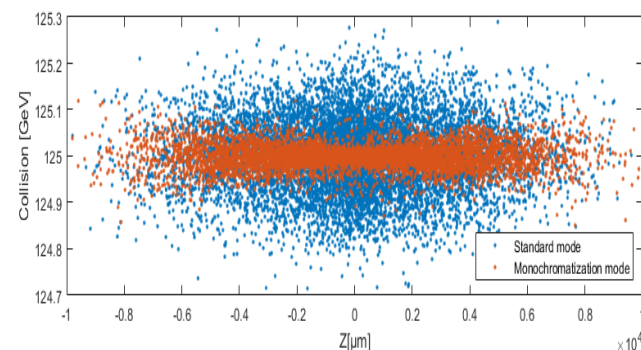
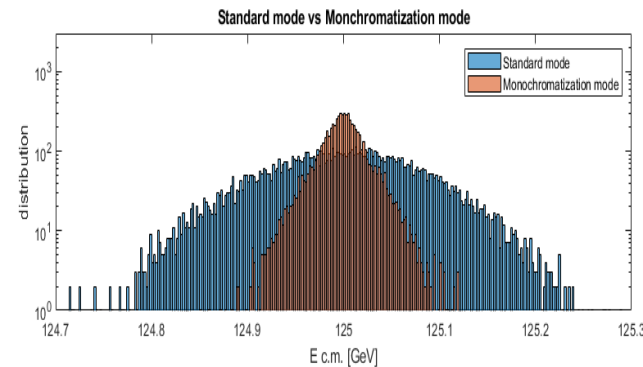
Standard\_625/head-on: Luminosity:  $1.20 \times 10^{36} \text{ cm}^{-2}\text{s}^{-1}$ , CM energy spread: 80.12 MeV

- monochrom\_h\_4ip/head-on*



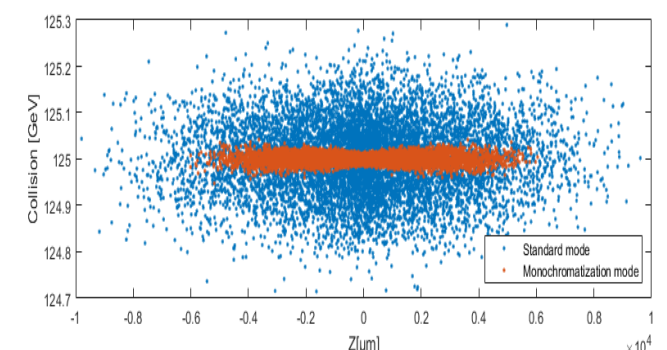
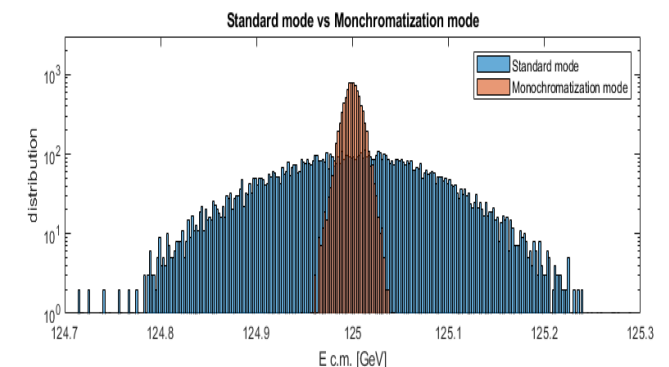
Luminosity:  $2.80 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread: 17.11 MeV

- monochrom\_v\_1/head-on*



Luminosity:  $2.23 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread: 18.15 MeV

- monochrom\_mix/head-on*



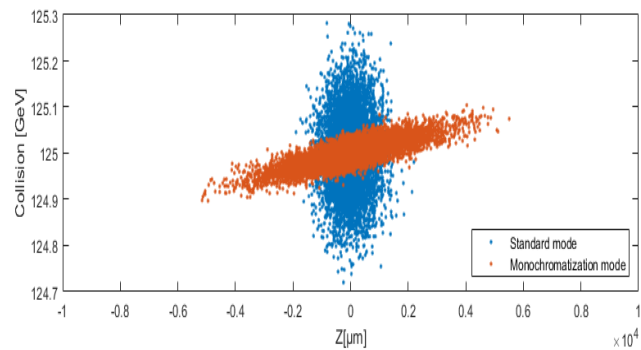
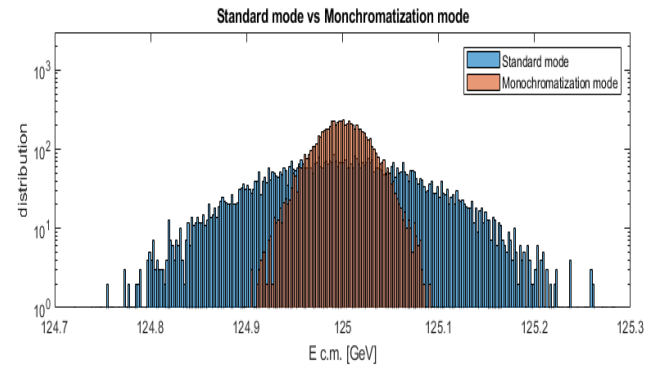
Luminosity:  $1.35 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread: 8.61 MeV

- Luminosity and CM Energy Spread (with BS effect)**

The following figures show the Guinea-pig calculation result of FCC-ee monochromatization optics base on Z mode lattice without crab cavities (crossing-angle) compared with that of the scaled standard mode.

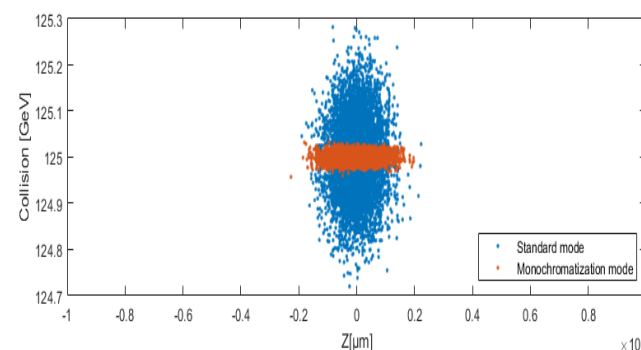
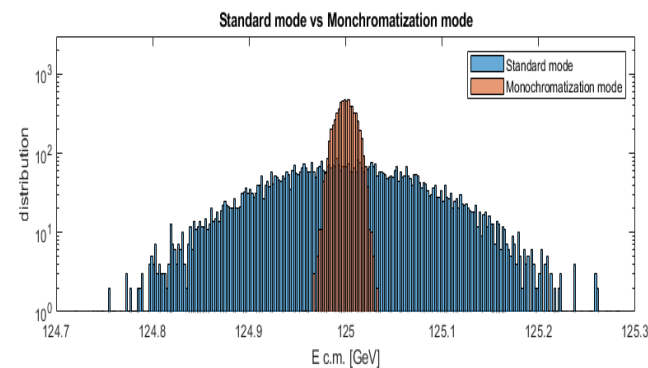
Standard\_625/crossing-angle: Luminosity:  $4.50 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ , CM energy spread: 80.33 MeV

- monochrom\_h\_4ip/crossing-angle*



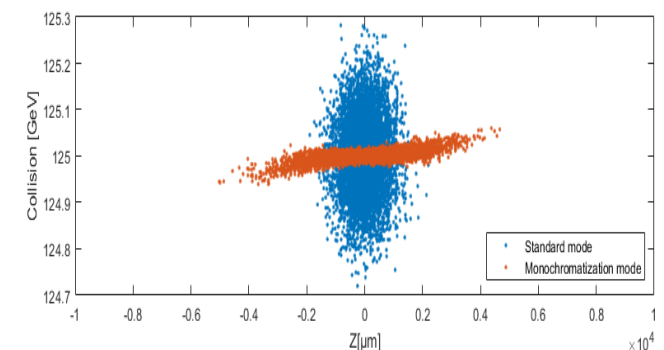
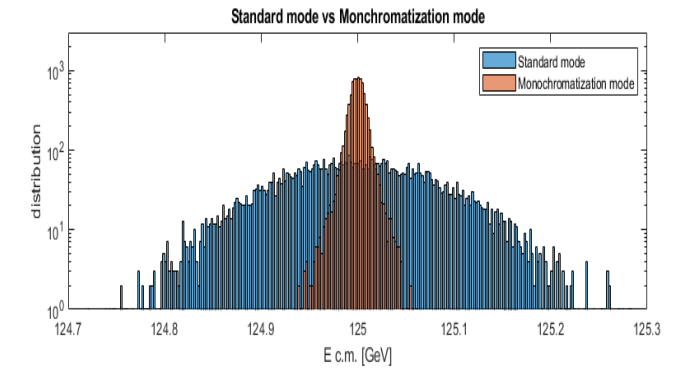
Luminosity:  $2.43 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread: 26.61 MeV

- monochrom\_v\_1/crossing-angle*



Luminosity:  $2.53 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread: 10.66 MeV

- monochrom\_mix/crossing-angle*

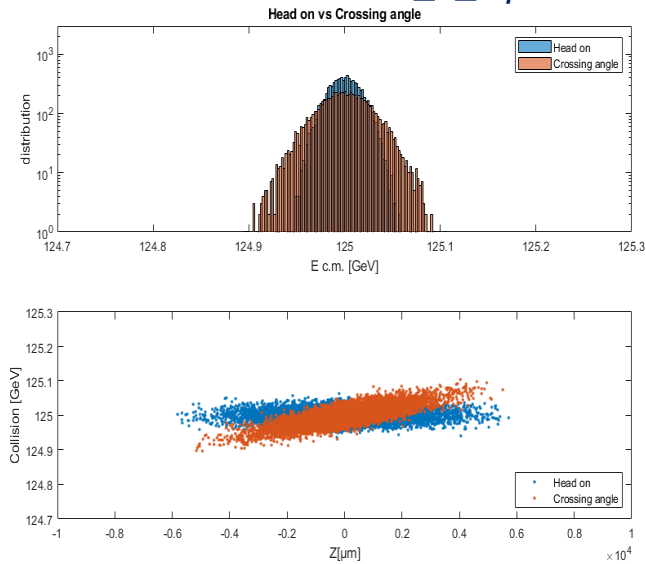


Luminosity:  $6.46 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread: 7.31 MeV

- Luminosity and CM Energy Spread (with BS effect)**

The following figures show the comparison of the Guinea-pig calculation result with/without crab cavities of FCC-ee monochromatization optics design base on Z mode lattice.

- monochrom\_h\_4ip*

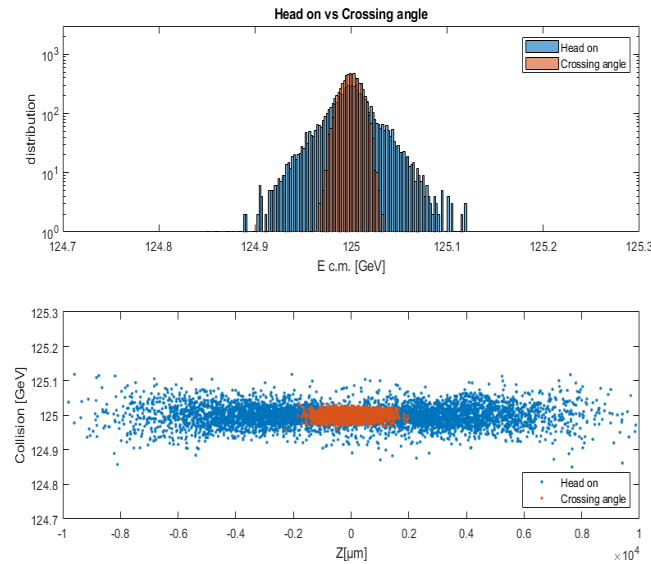


Luminosity (w/o crab cavity) :  $2.80 \times 10^{35} / 2.43 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread (w/o crab cavity) : 17.11 / 26.61 MeV

**Advantage:** Higher luminosity with crossing angle

**Disadvantage:** CM energy spread blows up with crossing angle

- monochrom\_v\_1*

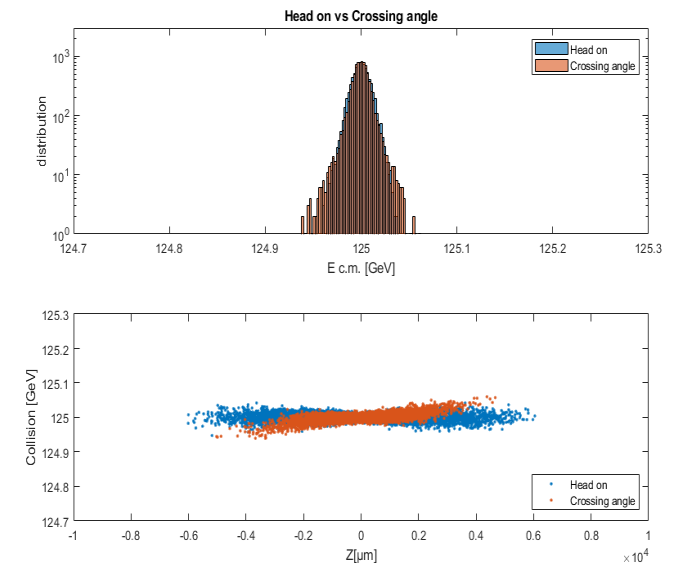


Luminosity (w/o crab cavity) :  $2.23 \times 10^{35} / 2.53 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread (w/o crab cavity) : 18.15 / 10.66 MeV

**Advantage:** CM energy spread reduces with crossing angle

**Disadvantage:** Luminosity loss with crossing angle like standard mode

- monochrom\_mix*



Luminosity (w/o crab cavity) :  $1.35 \times 10^{35} / 6.46 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$   
 CM energy spread (w/o crab cavity) : 8.61 / 7.31 MeV

**Advantage:** Lowest CM energy spread and less luminosity loss with crossing angle than that of *monochrom\_v\_1*

**Disadvantage:** Potentially face issues related to betatron coupling

# Status

- ✓ The monochromatization IR optics design
- ✓ Chromaticity correction, tune correction and emittance check of monochromatization optics
- ✓ Luminosity and CM energy calculation in Guinea-Pig
- ✓ Single particle tracking and dynamic aperture particle tracking
- Dynamic aperture optimization is in progress
- Beam-beam calculation is in progress
- Monochromatization optics design for CEPC
- Experimental proof of monochromatization concept in running  $e^+e^-$  low energy colliders

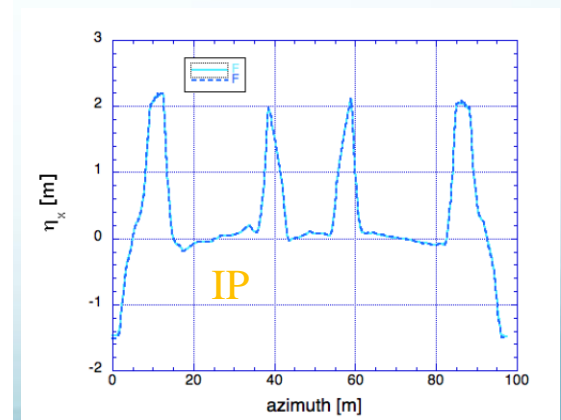
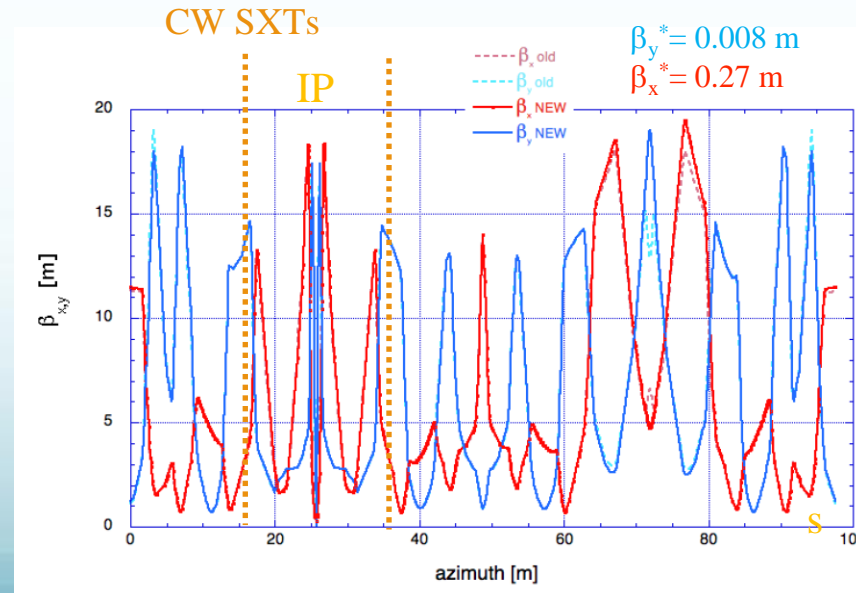
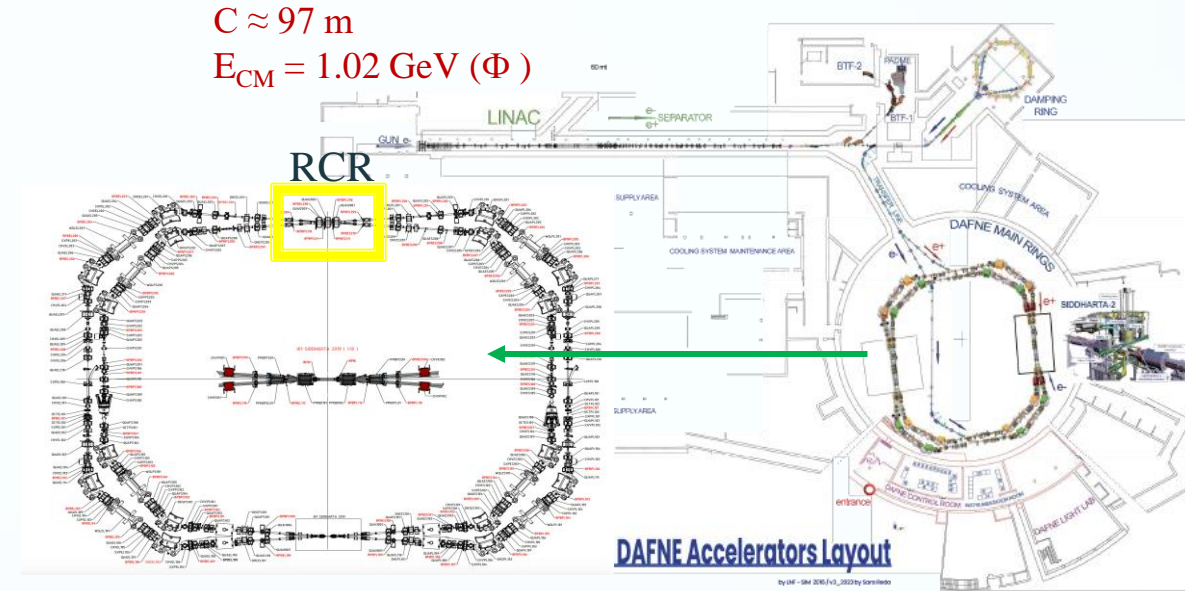


## New Crab-Waist ring optics:

- simplified focusing structure in the RCR,
- 2 QUADs where beams pass off-axis are switched off, thus eliminating spurious component in the QUADs magnetic field,
- Same optics parameters in the IR.

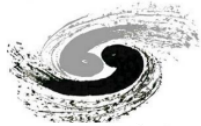
|  | DAΦNE native | DAΦNE Crab-Waist |
|--|--------------|------------------|
| Energy (MeV)                               | 510          | 510              |
| $\theta_{\text{cross}}/2$ (mrad)           | 12.5         | 25               |
| $\varepsilon_x$ (mm·mrad)                  | 0.34         | 0.28             |
| $\beta_x^*$ (cm)                           | 160          | 23               |
| $\sigma_x^*$ (mm)                          | 0.70         | 0.25             |
| $\Phi_{\text{Piwinski}}$                   | 0.6          | 1.5              |
| $\beta_y^*$ (cm)                           | 1.80         | 0.8              |
| $\sigma_y^*$ ( $\mu\text{m}$ ) low current | 5.4          | 3.0              |
| Coupling, %                                | 0.5          | 0.2              |
| Bunch spacing (ns)                         | 2.7          | 2.7              |
| $I_{\text{bunch}}$ (mA)                    | 13           | 15               |
| $\sigma_z$ (mm)                            | 25           | 15               |
| $h$  | 120          | 120              |

New optics improves closed orbit correction allowing to reduce the total strength of the used steering magnets, thus also contributing to minimize vertical dispersion

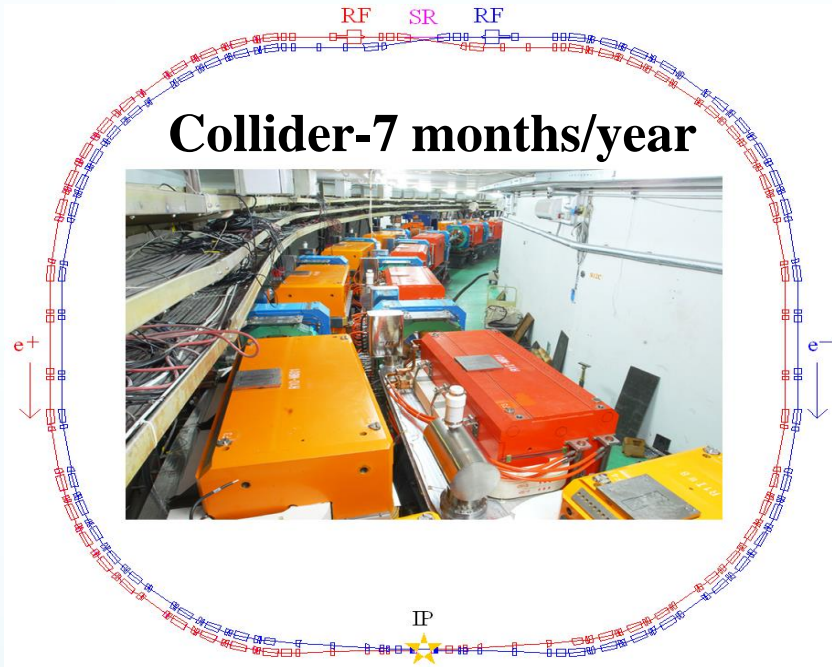


MRs working point:

$$\begin{aligned}
 Q_x^- &= 0.103 & Q_x^+ &= 0.114 \\
 Q_y^- &= 0.162 & Q_y^+ &= 0.180
 \end{aligned}$$



# BEPCII- Upgrade

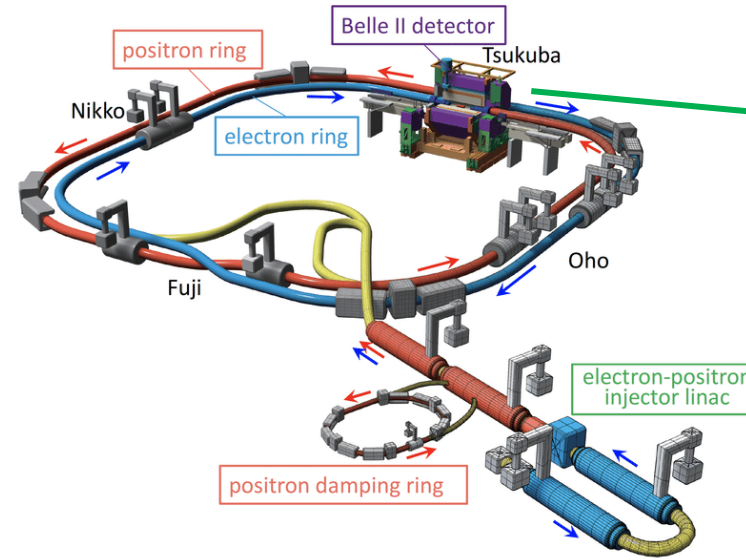


- BEPCII has achieved or exceeded design parameters
- Detailed design for **BEPCII upgrade** has been finished
- The upgrade is optimized at **2.35 GeV** with tripled luminosity, and with maximum beam energy of 2.8 GeV

## Beam Energy: 2.35GeV

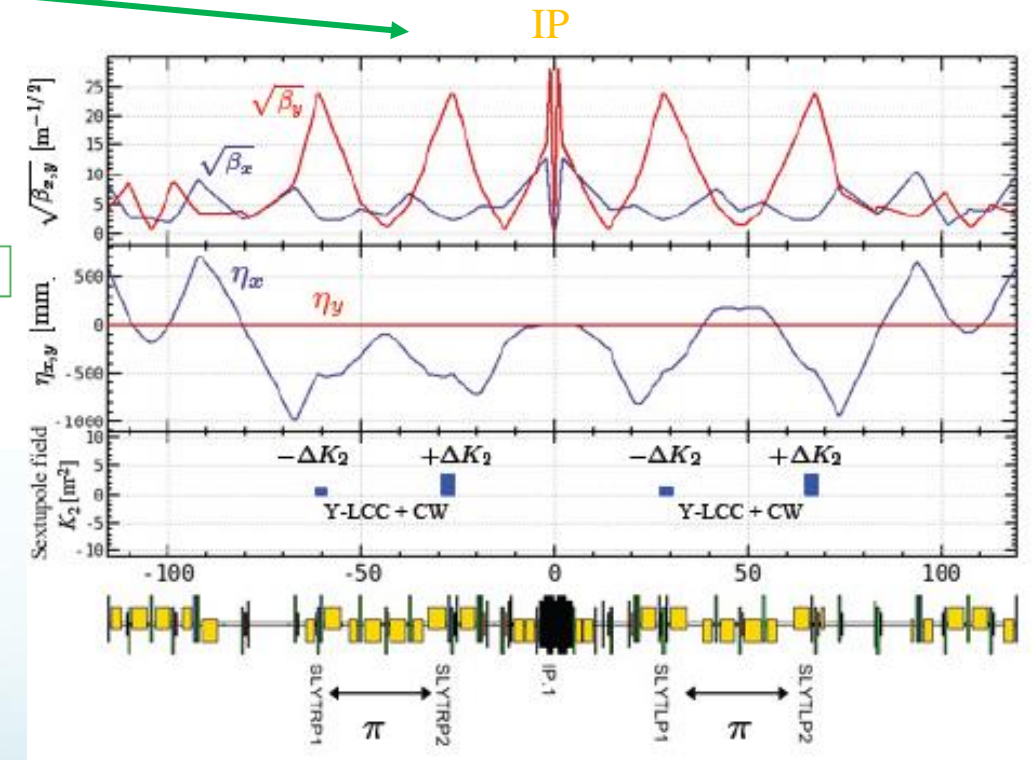
|  | BEPCII        | BEPCII-U      |
|--|---------------|---------------|
| Lum [ $10^{32}\text{cm}^{-2}\text{s}^{-1}$ ] | <b>3.5</b>    | <b>11</b>     |
| $\beta_y^*$ [cm]                             | <b>1.5</b>    | <b>1.3</b>    |
| Bunch Current [mA]                           | 7.1           | 7.5           |
| Bunch Number                                 | <b>56</b>     | <b>120</b>    |
| SR Power [kW]                                | <b>110</b>    | <b>250</b>    |
| $\xi_{y,\text{lum}}$                         | <b>0.029</b>  | <b>0.036</b>  |
| Emittance [nmrad]                            | 147           | 152           |
| Coupling [%]                                 | <b>0.53</b>   | <b>0.35</b>   |
| Bucket Height                                | 0.0069        | 0.011         |
| $\sigma_{z,0}$ [cm]                          | 1.54          | 1.04          |
| $\sigma_z$ [cm]                              | <b>1.69</b>   | <b>1.3</b>    |
| RF Voltage                                   | <b>1.6 MV</b> | <b>3.3 MV</b> |

- $\beta_y^* = 1 \text{ mm}$  at present operation, while the **final target** is  $\beta_y^* = 0.3 \text{ mm}$ .
- Operation with  $\beta_y^* = 0.8 \text{ mm}$  was carried out for **short-term trial**. The achievable bunch currents is smaller than of  $\beta_y^* = 1 \text{ mm}$ , case due to poor injection efficiency.
- **Improvement of the injection efficiency** is a major issue in both squeezing  $\beta_y^*$  and increasing stored beam current.



$$\beta_y^* = 0.001 \text{ m}$$

$$\beta_x^* = 0.8 \text{ m}$$



Crab- Waist (CW) and Vertical Local Chromaticity Correction (Y-LCC) with Sextupoles (SYL)

| Parameters                            | 4 GeV  | 7 GeV                 |
|---------------------------------------|--------|-----------------------|
| Beam Energy (GeV)                     | 4      | 7                     |
| I (A)                                 | 1.321  | 1.099                 |
| $n_b$                                 |        | 2249                  |
| $I_b$ (mA)                            | 0.587  | 0.489                 |
| $\beta_x^*$ (mm)                      | 80     | 60                    |
| $\beta_y^*$ (mm)                      | 1.0    | 1.0                   |
| $\zeta_y$                             | 0.0407 | 0.0279                |
| $\epsilon_y$ (pm)                     | 31.7   | 31.7                  |
| $\sigma_z$ (mm)                       | 5.69   | 6.02                  |
| CW ratio (%)                          | 80     | 40                    |
| L (cm <sup>-2</sup> s <sup>-1</sup> ) |        | $4.65 \times 10^{34}$ |