







Static and dynamic beam dynamic effects in the e-, common and HE-linacs

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Machine layout, inputs, and targets

Static effects:

- Longitudinal phase space optimization
- Emittance growth due to elements misalignments and mitigation strategies

Energy compressor: why and where?

Dynamic effects: jitter amplification

- Single bunch
- Multi-bunch

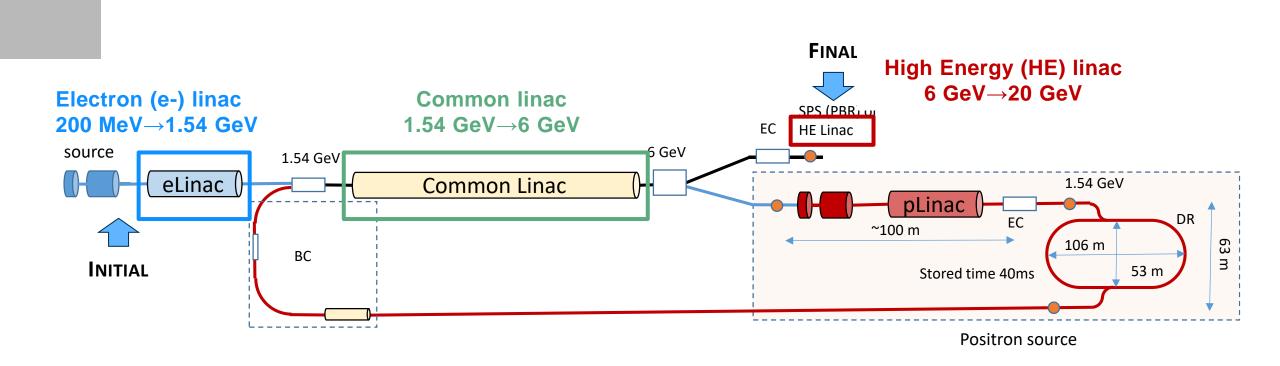
Implications of the 2.86 GeV damping ring for e⁻ e⁺

Conclusions



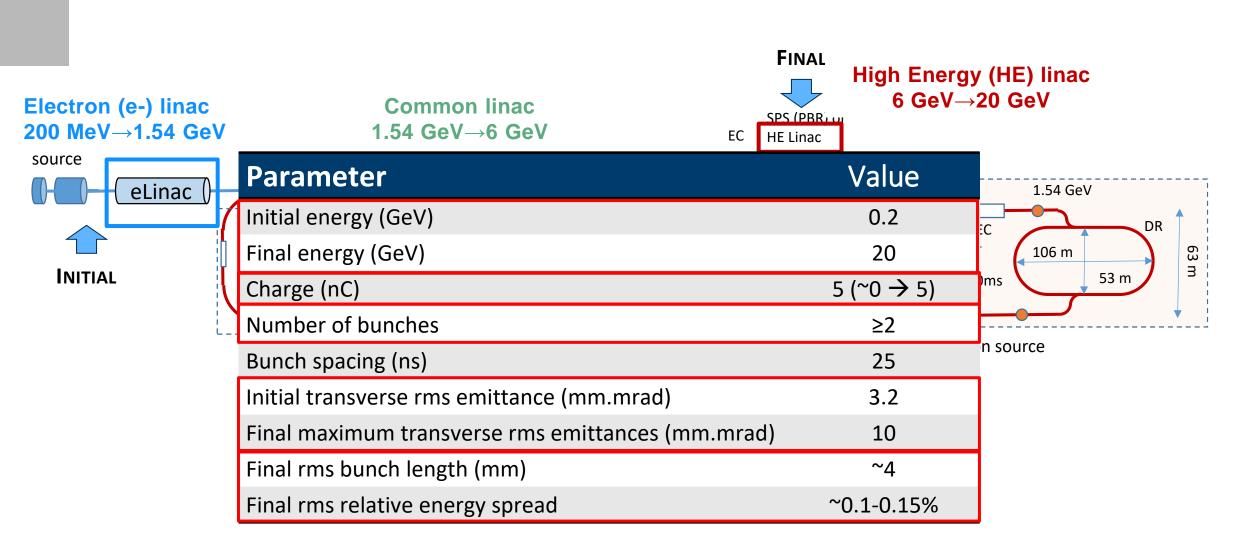


Layout, inputs, and acceptance





Layout, inputs, and acceptance



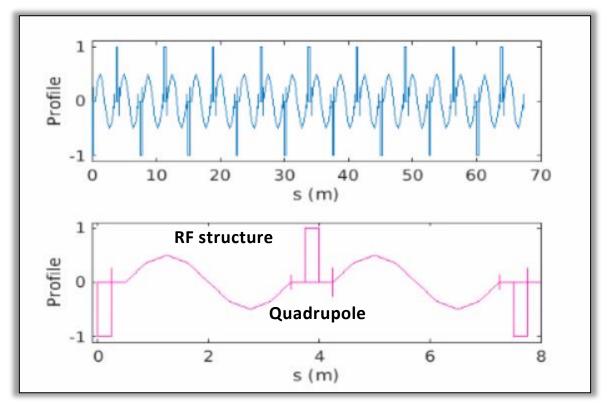


Lattice modeling:

- FODO lattice with 90 degs phase advance/cell
- One quadrupole/RF structure: distance among the quadrupoles~3 m
- RF structures' wakefield: Bane model (a in the following is the iris radius)
- 90 degrees of the RF cavity corresponds to on-crest operation
- \blacksquare a/ λ corresponds to the mean a/ λ



Very important for the single bunch jitter amplification



Simulation codes:

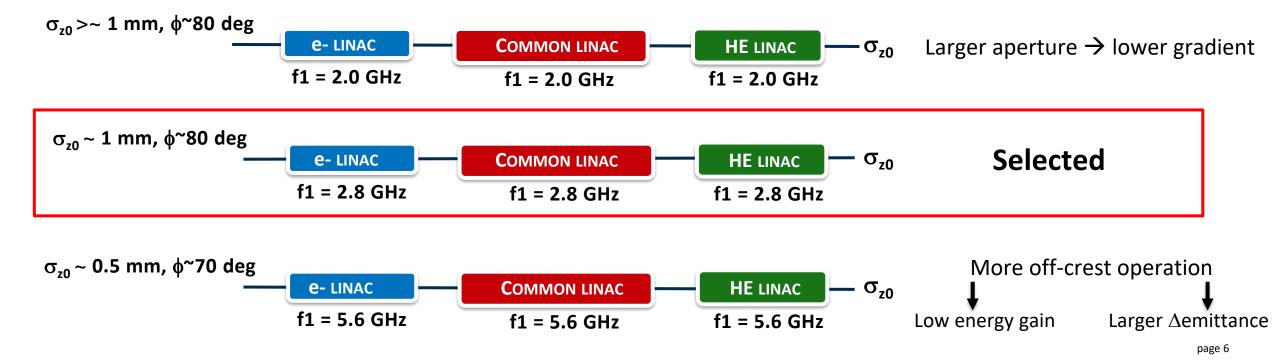
- MAD-X: optics matching
- Elegant: single bunch tracking simulations longitudinal plane (verified agreement with RF-Track)
- RF-Track: single and multi-bunch tracking simulations transverse plane (reached agreement RF-Track vs Elegant after that M. Borland modified Elegant-see FCC week 2023 presentation)



Most promising layouts

f (GHz)	G (MV/m)	a/λ	a (mm)	Maximum σ _z (mm)		Maximum	phase (deg)	
				δ_{E} = 0.1 %	δ_{E} = 0.15 %	δ_{E} = 0.1 %	$\delta_{\rm E}$ = 0.15 %	,
2.8	25	0.15	16.1	0.8	1	79	82	
5.6	25	0.2	10.7	0.5	0.6	74	66	
5.6	40	0.2	10.7	0.4	0.5	67	72	
2.0	25	0.1	15	1	1.2	78	81	

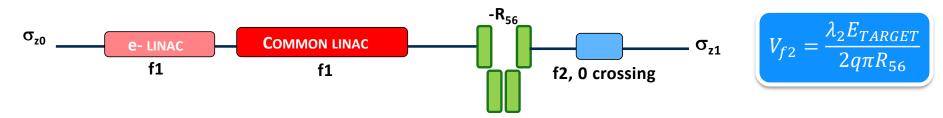
- With <u>all these configurations</u> we reach an <u>energy</u> spread ~ 0.1-0.15%
- ¹ The RF aperture (a/ λ), operating phase, and **bunch length**, given the bunch charge, are optimized to obtain the target energy spread:
 - Optimal bunch length is of the order of few mm (from ~1 mm up to about 2 mm with the linearizing cavity)
 - Bunch decompressor needed





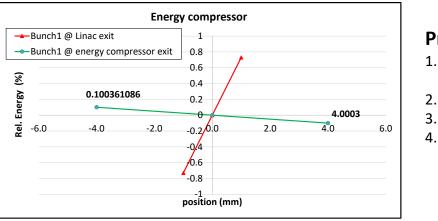
The energy compressor "a la SuperKEKB"

Goal: manipulate the bunch longitudinal phase space \rightarrow change the energy spread and the bunch length



Method:

- Chicane transforms energy difference \rightarrow arrival time difference
- **RF** cavity transforms the arrival time difference \rightarrow phase difference
- RF cavity compensates the incoming energy difference (inside the bunch or bunch-to-bunch) by applying the appropriate voltage downstream of the chicane



Procedure:

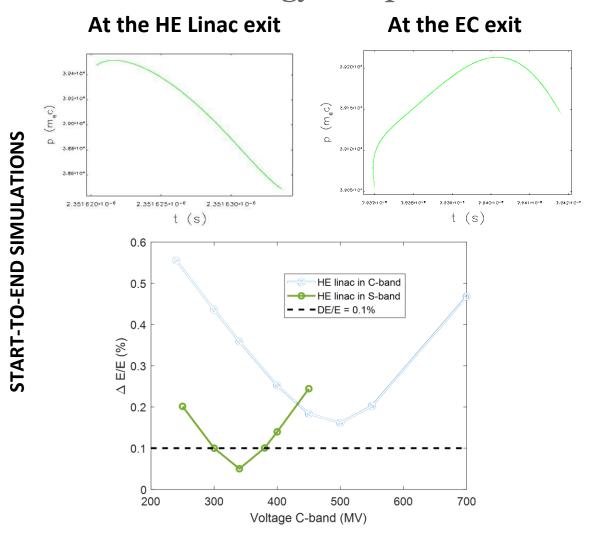
- 1. Chirp determined by the upstream linacs (operating phase+beam loading at a given bunch length and charge) \rightarrow increased on purpose
 - Determine R₅₆ to have the target bunch length
 - Given R₅₆, compute the voltage to have the desired energy spread
 - Verify the results with tracking simulations. Necessary, because the energy-time distribution may be non-linear

Advantages:

- Bunch length and energy spread match the booster requirements
- **Tunability** of the bunch length and energy spread separately and without modifying the upstream linacs
- Bunch energy spread variation compensation due to charge scan



Energy compressor: results



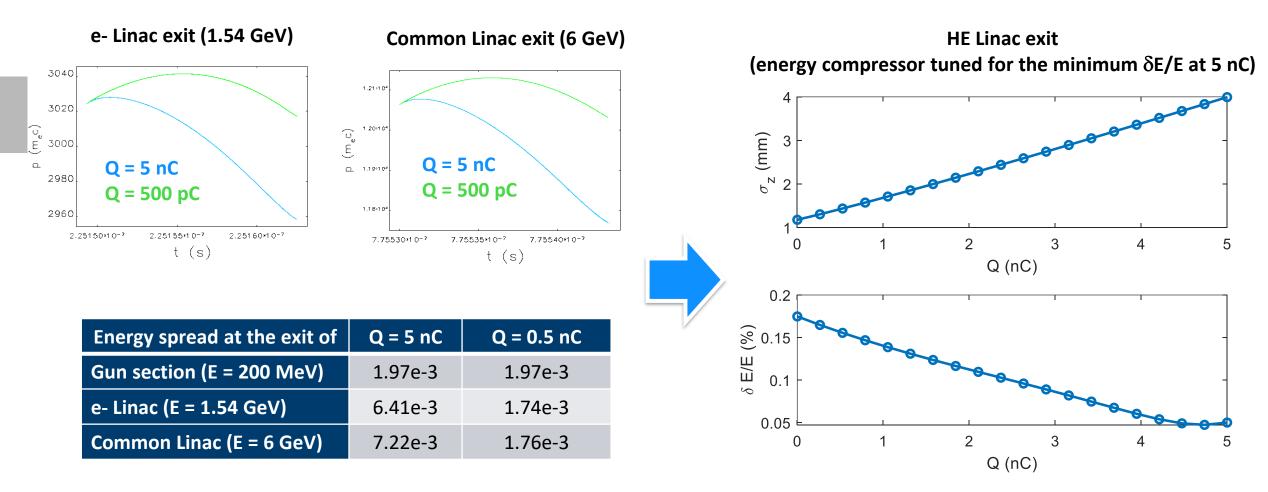
Initial HE Linac δ E/E (%)	0.75
R ₅₆ (m)	0.41
Voltage X δ E/E = 0.15% (MV)	135
Voltage C δ E/E = 0.15% (MV)	270
Voltage X minimum δ E/E (MV)	170
Voltage C minimum δ E/E (MV)	340
Length X-band cavities min (m)*	3.4
Length C-band cavities min (m)*	11.8
Minimum δE/E	5.1e-4
Energy spread reduction	14
Initial bunch length (mm)	1
Final bunch length (mm)	4

* Assuming one module/structure: C-band: 28.8 MV/m, X-band: 50 MV/m

More than a factor 2 margin in <15 m (C-band) < 5 m (X-band) length allocated for the RF structures



Impact of the different bunch charges: scan of the charge

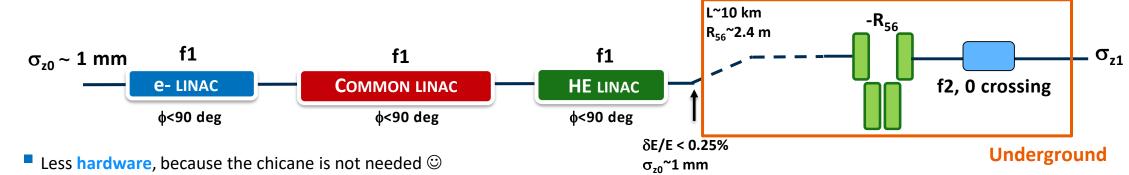


Energy spread from 0.05% to 0.2%, bunch length ~few mm (shorter only for lower charge beams)



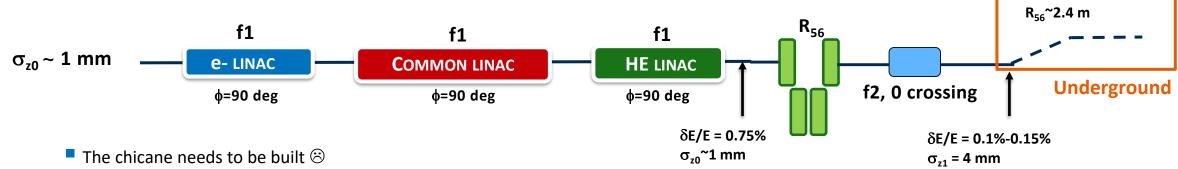
Energy compressor: where?

Use the R₅₆ in the transfer line to the booster:



- RF power needs to be brought ~100 m underground 🙁
- Dispersion in the transfer line sets a limit on the maximum energy spread (off-crest operation or another energy compressor), and after chirp must be added to decompress the beam

Build a dedicated chicane (or arc) at the end of the HE linac:



- RF power at "surface" ⁽¹⁾
- The linacs may be operated on-crest → better for emittance preservation and energy efficiency ☺
- Smaller beam size with the same dispersion \rightarrow smaller aperture magnets (cost) \odot
- Less CSR (longer bunch length) and chromaticity (smaller energy spread) related effects along the transfer line ©

L~10 km

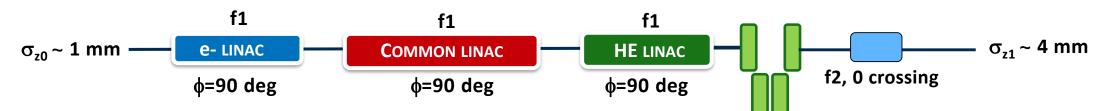


Layout <u>without</u> the energy compressor:



- Determined an optimal combination of bunch length, RF operating frequency, phase and geometry to obtain the target energy spread
 - Optimal bunch length and phase @ 2.8 GHz -> ~1 mm
 - Optimal bunch length and phase @ 5.6 GHz -> ~0.5 mm
- Both are far from the required 4 mm \rightarrow bunch must be decompressed upstream of the booster injection

Layout with the energy compressor:

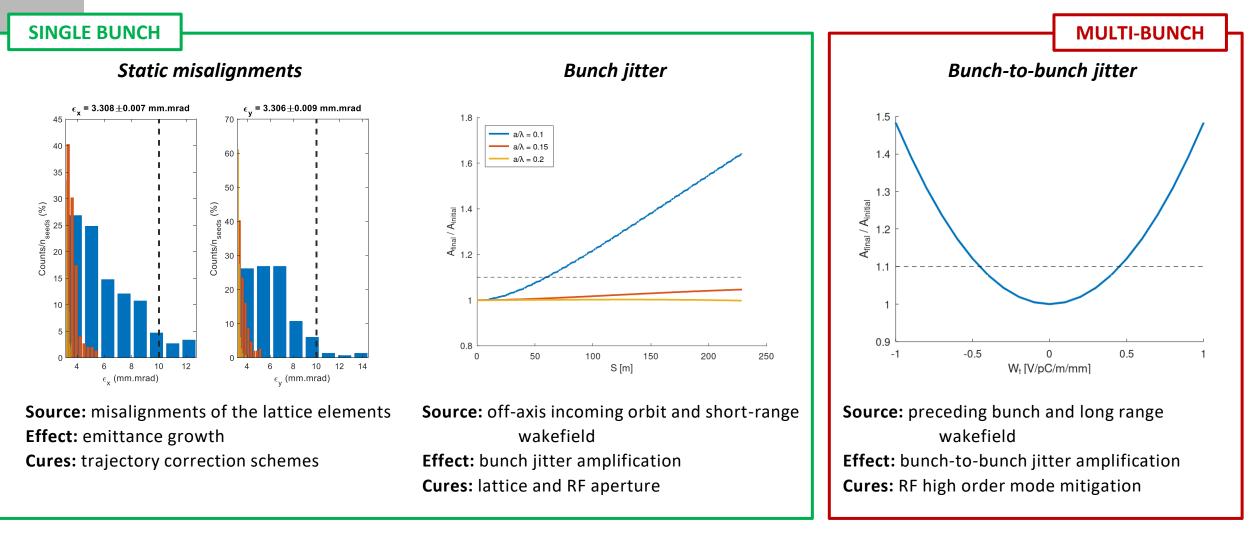


- We use the energy compressor to reach the target bunch length and energy spread (with a margin factor 2-3)
- We can operate the linacs on-crest \rightarrow better for emittance growth and energy efficiency
- The bunch **energy jitter** is reduced
- Added tunability for the bunch length and the energy spread



Transverse dynamics

Single and multi-bunch effects are dominated by long and short-range wakefield, elements misalignment, and incoming jitter





Static single bunch: errors and mitigation strategy

Elements misalignments **Quadrupoles** Offset x, y = 50 μm rms

Gaussian distribution

RF cavities

Offset x, y = 100 μ m rms

Gaussian distribution

BPM

Offset x, y = 30 μ m rms Resolution x, y = 10 μ m Gaussian distributions

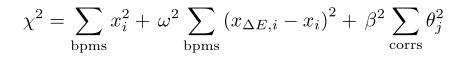
Steering algorithms

One-to-one orbit correction

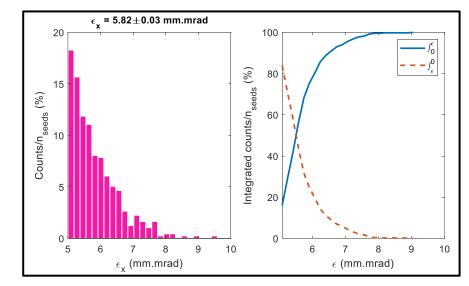
- 1. Orbit *x_i* with errors computed
- 2. Response matrix computed
- 3. Correctors strengths calculated (SVD) to steer the beam

Dispersion Free Steering (DFS)

- 1. Orbit x_i with errors computed
- 2. Response matrix computed
- 3. Off-energy beam (different RF phase) orbit $X_{\Delta E,i}$ computed
- 4. Response matrix computed
- 5. Correctors strengths calculated, minimizing X^2 defined as:



Parameters for the simulations

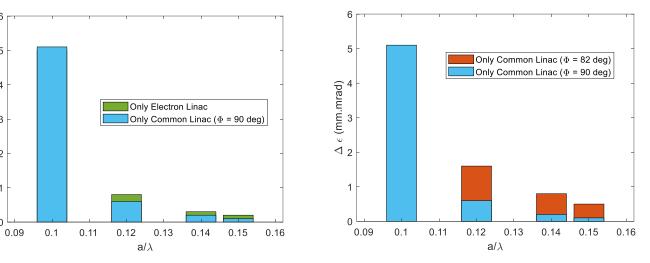


- Between few hundreds and 1000 seeds
- Initial emittance is <u>3.2 mm.mrad</u> at 5 nC with 1 mm rms laser pulse length (Z. Vostrel and S. Doebert)
- Very <u>pessimistic assumption</u>: 99% of the good seeds (CLIC for example uses 90% of the seeds)



Static single bunch: results

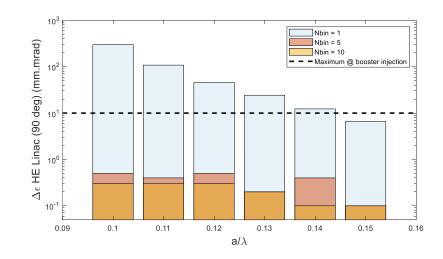
a/λ	a (mm)	e- Linac	Common Linac (82 deg)	Common Linac (90 deg)
0.10	10.7	5.0	/	5.1
0.12	12.9	0.8	1.6	0.6
0.13	13.9	/	/	/
0.14	15.0	0.3	0.8	0.2
0.15	16.1	0.2	0.5	0.1



Outcomes:

- Largest emittance growth/length at the low energy section → important reduction in case of the <u>e- damping ring</u> option
- Emittance growth strongly depends on the RF operating phase

a/λ	a (mm)	e- linac	Common linac (90 deg)	HE linac, Nbins = 10
0.10	10.7	5.0	5.1	0.3
0.11	11.8	2.4	1.7	0.3
0.12	12.9	0.8	0.6	0.3
0.13	13.9	0.7	0.3	0.2
0.14	15.0	0.3	0.2	0.1
0.15	16.1	0.2	0.1	0.1



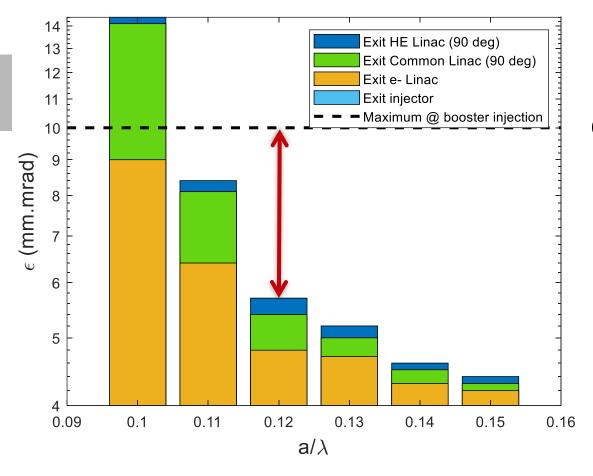
Outcome:

Essential to separate the orbit steering/DFS in several sections (what we defined bins)

LOWER ENERGY



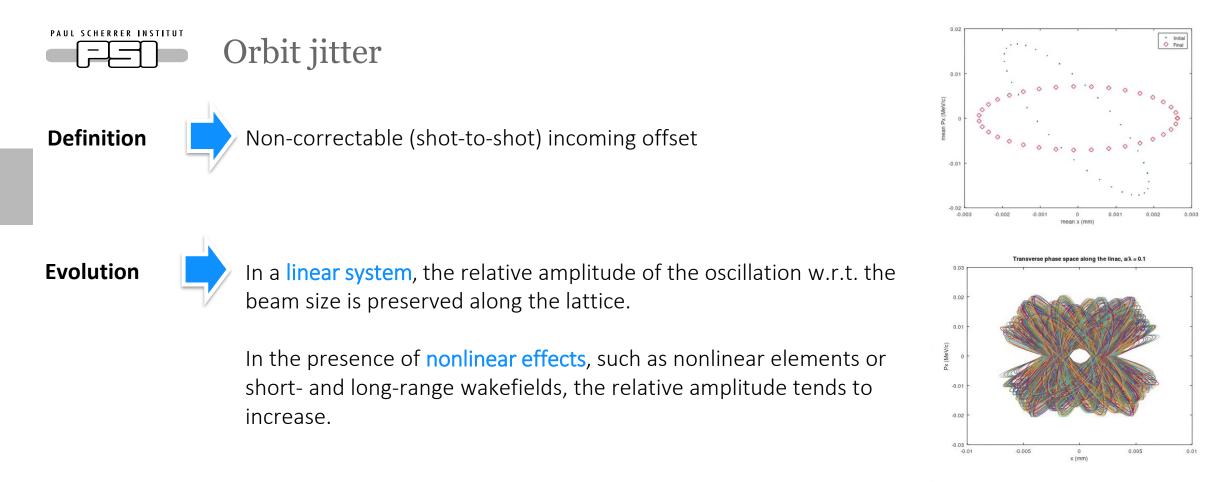
Static single bunch: summary



Outcomes:

- Relatively small emittance growth in the HE linac compared to the lower energy sections → important in case we go to the <u>e- damping ring</u>
- Quite an important impact of the RF operating phase on the emittance growth

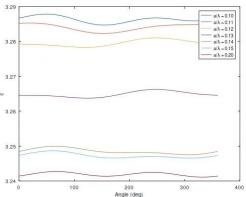
About a factor 2 margin for $a/\lambda \ge 0.12$





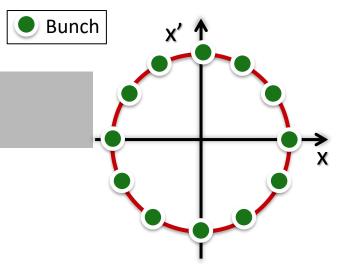
- The <u>short-range</u> depends on *cell geometry*
- The long-range depends on high-order modes damping

The total jitter amplification factor is the **product of the two**.





"Painting" of the transverse phase space



Jitter amplification computation:

- Single bunches distributed on a circle (in 10 degrees step size) injected to the line with different (x,x')
- Computed the area in the initial beam transverse phase space $\rightarrow A_0$
- Computed the area in the final beam transverse phase space $\rightarrow A_F$
- Jitter amplification, JA, is defined as the ratio of the areas \rightarrow A_F /A₀

Advantages of this approach (already applied to the CLIC design):

- JA is independent on the initial jitter
- JA considers the effect on the transverse phase space, and not only in x OR x' (y or y') → it does not depend on the location where it is determined
- The impact of jitter is largely on the orbit. The emittance is mostly unaffected (orbit much on-axis than that corresponding to the static error studies)
- Given JA of a generic kth section, *JA_k*, the total jitter amplification *JA_{tot}* is given by the product of all of them:

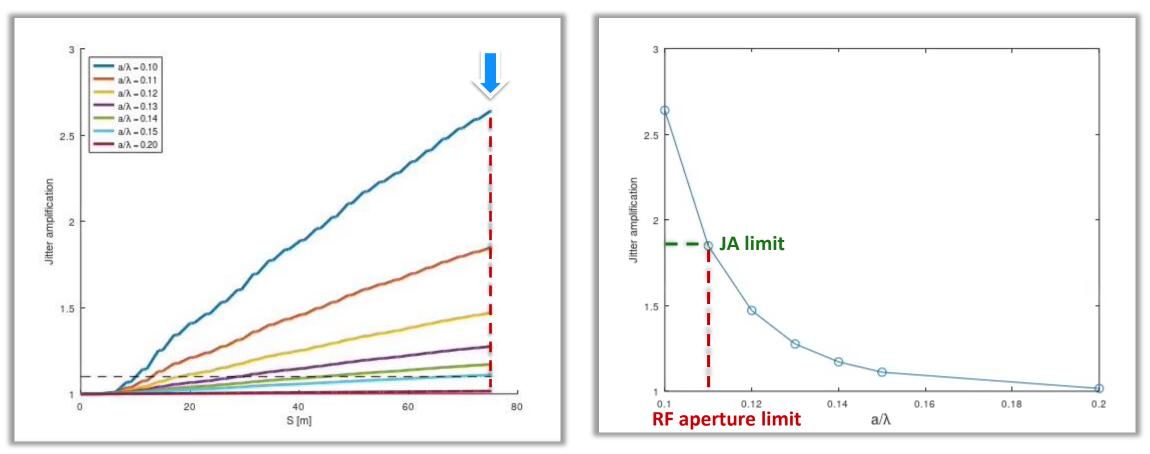
$$JA_{tot} = \prod_{k=1}^{N} JA_k$$



Jitter amplification: procedure

Simulation setup:

- Compute the JA along the considered linac
- Determine the JA at the end of the considered linac
- Given the maximum acceptable jitter, determine the specifications for the RF design



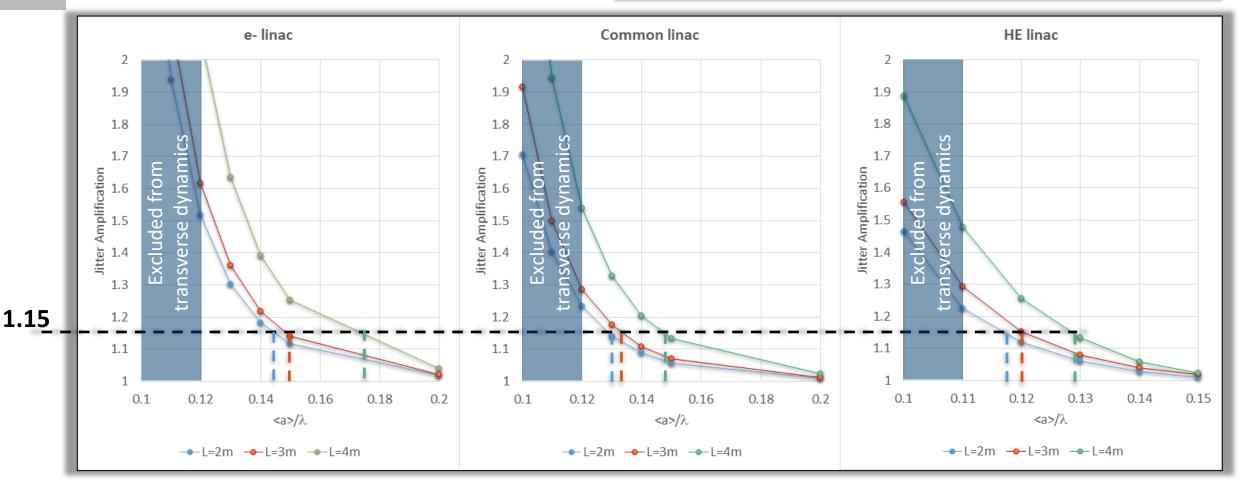


Jitter amplification: results

Assumed full linacs chain jitter amplification: $A_k = 1.15/\text{linac} \rightarrow A_{tot single} = 1.15 * 1.15 * 1.15 = 1.52$

Optimal RF structure length = 3 m (compromise between shunt impedance and aperture-**see A. Kurtulus' talk**)

e- linac		Common linac		HE linac
Energy range	[0.2,1.54) GeV	[1.54,2.8) GeV	[2.8,6) GeV	[6,20] GeV
<a>/λ	0.15	0.15	0.12	0.12

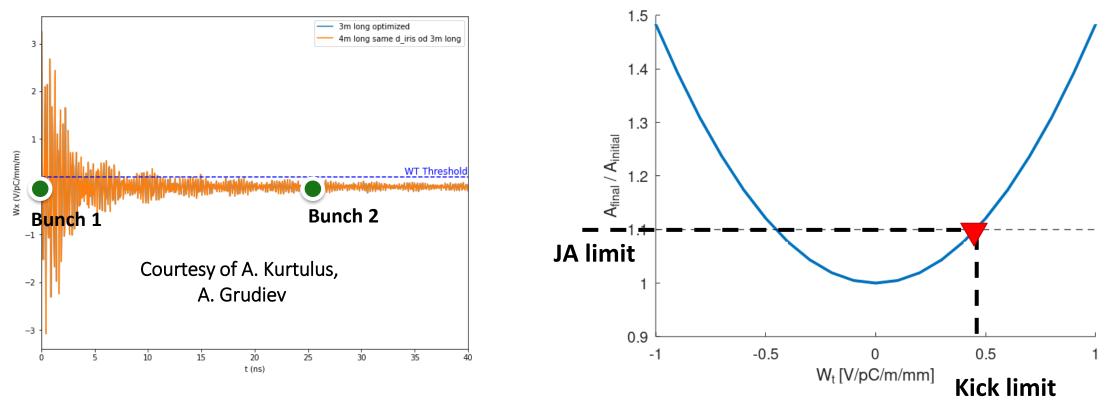




Multi-bunch jitter amplification: procedure

Simulations' strategy: provide specifications for the RF design

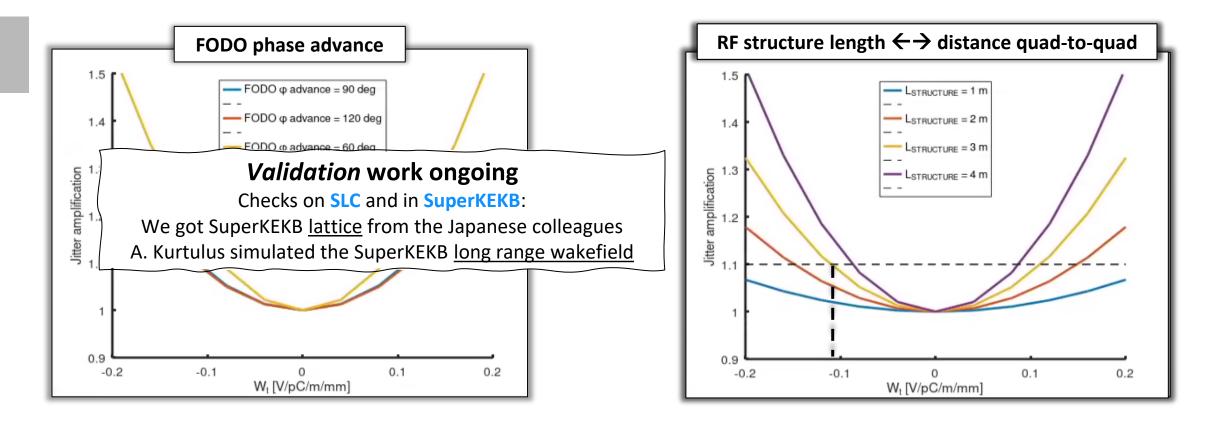
- Imposed a kick to the second bunch to simulate the long-range wakefield generated by the first bunch to the following one: independent on the bunch time separation
- Determined the tolerable kick to maintain the JA below the defined threshold
- RF design aims to produce transverse wakefield below this value
- This method is independent on the minimum bunch separation





Multi-bunch jitter amplification: dependences

Simulations → full linac chain from 200 MeV (gun section exit) to 20 GeV

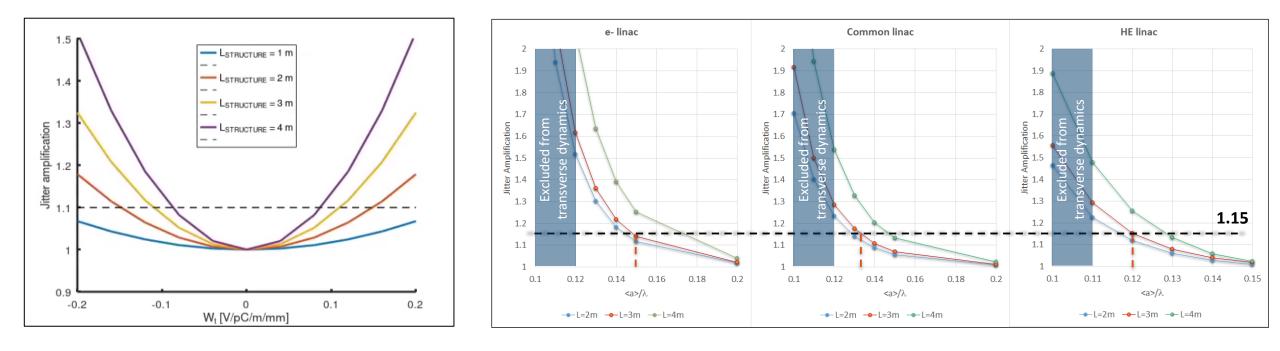


RF structure length = 3 m Maximum tolerated kick = 0.11 V/pC/m/mm



Dynamic effects transverse: summary

Effec	t	JA	Optimization knob	Settings
Single	e bunch	1.52	RF aperture	<a>/λ = [0.15,0.12]
Multi	i-bunch	1.1	RF structure length ($\leftarrow \rightarrow$ distance quad-to-quad)	3 m

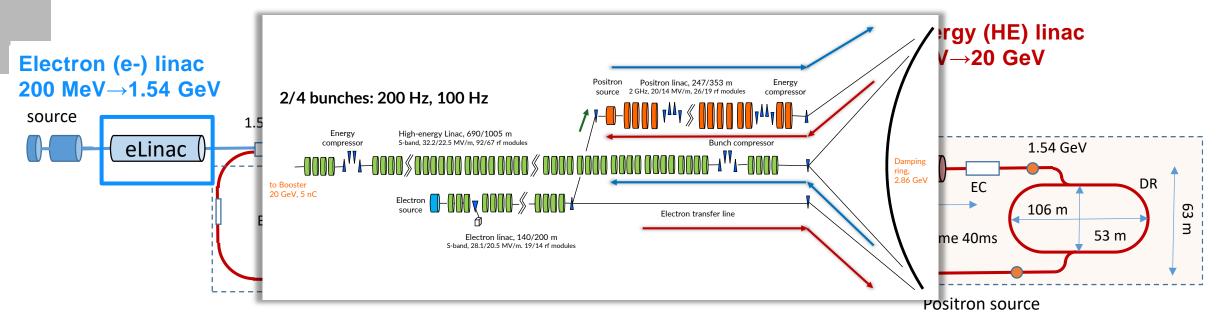


$$A_{tot} = 1.52x1.1 \sim 1.70$$

Total jitter amplification~30% margin



The proposed use of the DR for e+ at 2.86 GeV instead of 1.54 GeV gives also the possibility to use the damping ring for the e- as well



Advantages	Disadvantages
Relax the constraint on the emittance growth up to 2.86 GeV	Bunch will need to be compressed at the DR extraction
Reduce emittances	
Produce flat beam ($\epsilon_y << \epsilon_x$)-recent booster wish	
Relax the jitter amplification constraint up to 2.86 GeV	



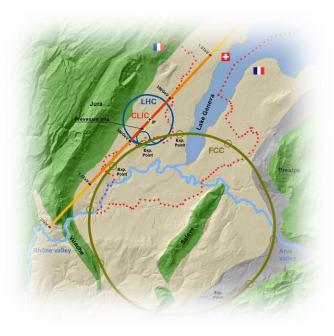
Complete beam dynamics design of the full FCCee linac chain has been shown

Longitudinal dynamics (single bunch): energy spread and bunch length

- Design <u>without energy compressor</u>: booster requirements on energy spread fulfilled, but the bunch needs to be decompressed to reach the target bunch length
- Design <u>with energy compressor</u>: all <u>booster requirements fulfilled</u> in terms of energy spread and bunch length with an improved bunch energy stability (charge scan)

Transverse dynamics (static single bunch): emittance growth

• Defined a range of RF aperture $(a/\lambda \ge 0.12 \rightarrow a \ge 12.9 \text{ mm})$ giving a *factor 2 margin* in emittance growth



Transverse dynamics (dynamic single and multi-bunch): jitter

- Determined the optics, RF structures aperture (from $a/\lambda = 0.15$ to 0.12) and length (3 m) to control the bunch jitter
- Determined the maximum kick to control the bunch-to-bunch jitter (0.11 V/pC/m/mm)
- The jitter amplification fulfills the transfer line/booster injection requirements with a *30% margin*
- More work ongoing to validate our modeling with other machines (SLC and SuperKEKB)

Ready to optimize the "new baseline design" (2.86 GeV damping ring) having fruitful interactions with the damping ring , transfer line and booster groups



RF structure design requests from beam dynamics

From the other sections' requirements to the linacs' beam dynamics: requirements and achievements

I	Parameter	Transfer line request	Booster request	Achieved
	Bunch length (mm)		4	4 tunable from <1 mm to few mm
	Energy spread	<0.25%	0.1-0.15%	0.15% tunable from 0.05% to % level
	Jitter amplification	2		1.7
	Maximum emittances x, y (mm.mrad)		<10	<6
	Maximum emittances x,y (mm.mrad)-recent		Smaller in y (2), ok in x (20)	Probably possible with the e- DR option

From the linacs' beam dynamics to the RF design

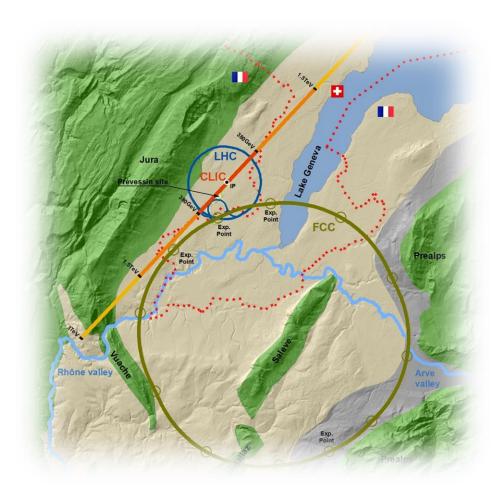
Effect to control/parameter to match	Effect	RF specification	Value	
Bunch length (mm)	Short range longitudinal wakefield	a/ λ , for given bunch length	Between 0.1 and 0.2. More flexibility and energy stability adding the energy compressor	
Energy spread	Short range longitudinar wakened	(and charge)		
Jitter amplification (single bunch)	Short range transverse wakefield	Length, a/ λ	3 m, <a>/λ = 0.12 and 0.15	
Jitter amplification (multi-bunch)	Long range transverse wakefield	HOM damping	Max kick = 0.11 V/pC/m/mm	
Emittances (mm.mrad)	Short range transverse wakefield and misalignements	a/λ	>0.12	



Acknowledgments...

••••to the entire WP1, the booster and the transfer line and booster WPs •••

····CHART* and you for your attention





*This work was done under the auspices of CHART (Swiss Accelerator Research and Technology) Collaboration



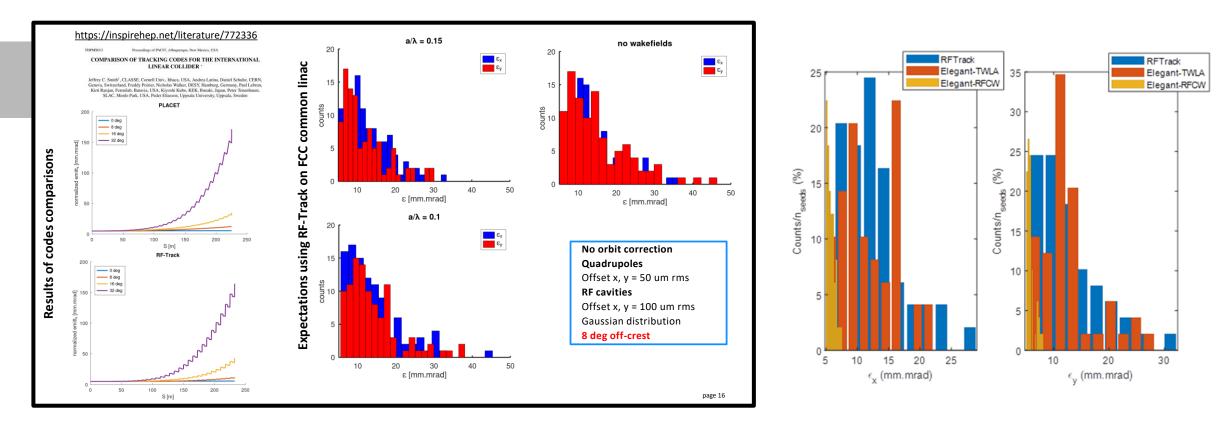
FCCIS: 'This project has received funding from the European Union's Horizon 2020 research and innovation programme under the European
Union's Horizon 2020 research and innovation programme under grant agreement No 951754.'





Simulation code: RF-Track vs Elegant

From the Orsay Mini-workshop presentation



Codes benchmarking

- Elegant foresaw a very small emittance increase
- Disagreement Elegant vs RF-Track
- Agreement RF-Track vs other codes, like Placet (verification by A. Latina)
- Problem pointed to M. Borland, new Elegant release in Feb 2023 to simulate the correct emittance growth in RF structure with also wakefield included

Important change in the design considerations!



Toward 4 bunches operation mode

0.02

0.01

2600

2700

2800

2900

3000

t (ns)

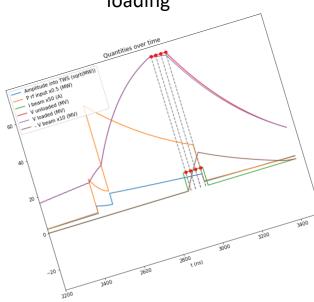
3100

3200

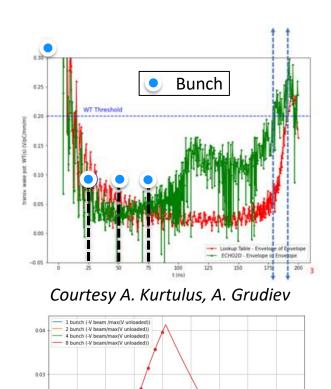
3300

Go to 4 bunches operation mode to reduce the linacs operating frequency

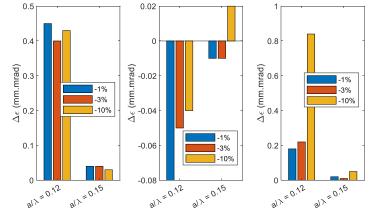
The bunches see a different beam loading

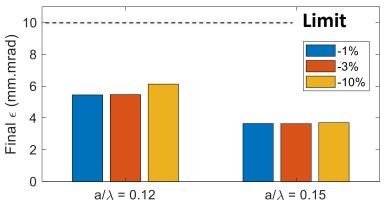


See A. Kurtulus talk



The bunches see $\Delta energy \rightarrow$ optics mismatch $\rightarrow \Delta emittance$





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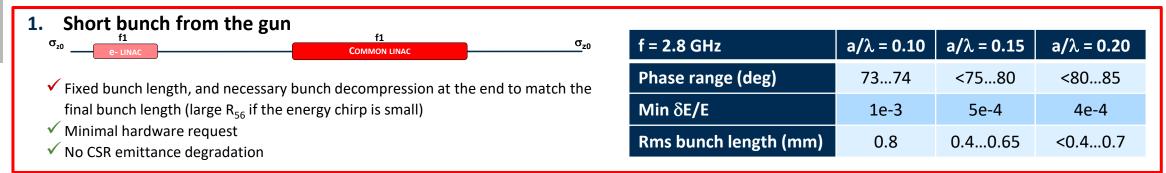


Optimized scenarios

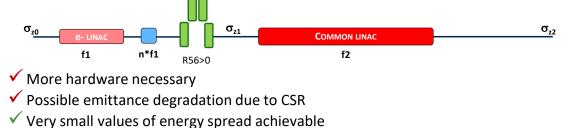
More reported at previous FCC Weeks

Goal: optimize the bunch length, the RF parameters (phase and aperture) to match the target energy spread and final

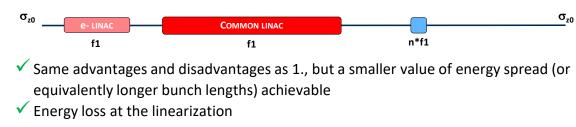
bunch length **Considered scenarios**:



2. Bunch compressor at the exit of e- Linac



3. Shorter bunch from the gun and linearization

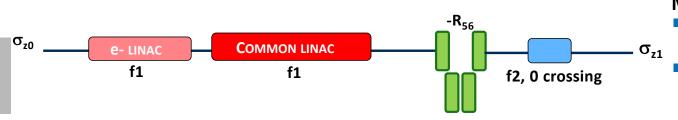


f = 2.8 GHz	a/λ = 0.10	a/λ = 0.15	a/λ = 0.20
Phase range (deg)	<7075	86>90	<8085
Min δE/E	1e-4	1e-4	1e-4
Rms bunch length (mm)		0.457	

f = 2.8 GHz	a/λ = 0.10	a/λ = 0.15	a/λ = 0.20
Phase range (deg)	6670	7780	8185
Min δE/E	2e-4	3e-4	3e-4
Rms bunch length (mm)		0.650	

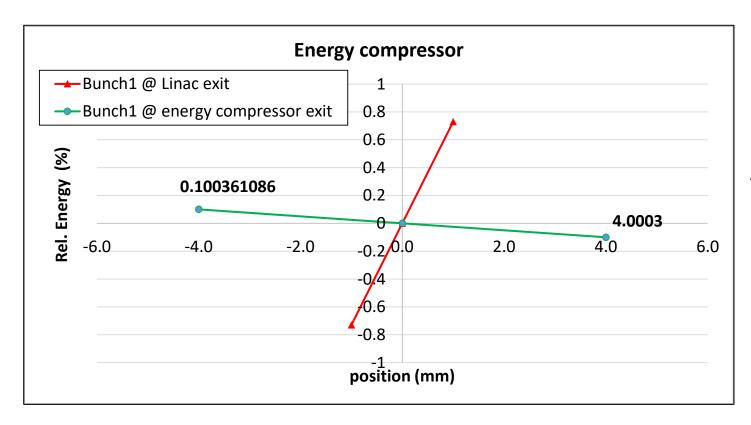


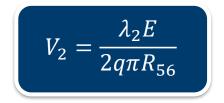
Energy compressor à la SuperKekB (a special thank to R. Zennaro)



Method:

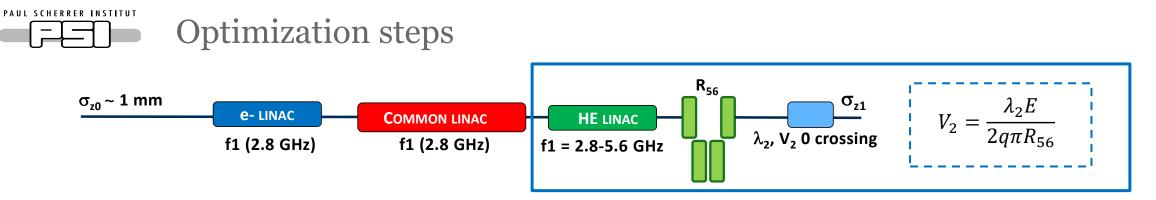
- Chicane: energy difference → arrival time difference → phase difference
- Compensate the energy difference by applying the appropriate voltage downstream of the chicane (cavities at f2)





Advantages:

- Final energy spread and bunch length are not independent but separately adjustable
- Possible to use the R₅₆ in the transfer line to the ring (transfer line group)

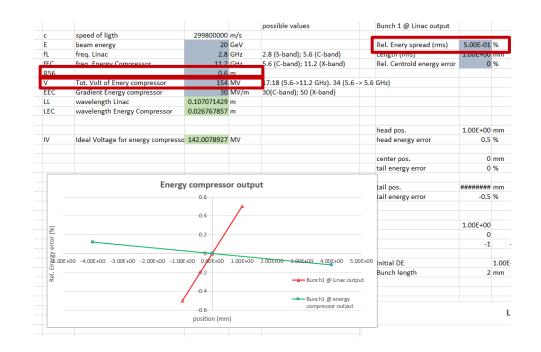


Procedure:

- 1. Chirp determined by the upstream linacs (operating phase+beam loading at a given bunch length and charge)
- 2. Determine R_{56} to have the target bunch length
- 3. Given R₅₆ compute the voltage to have the desired energy spread
- 4. Verify the results with tracking simulations. Necessary, because the energy-time distribution may be non-linear

Target values:

- Final energy spread ~0.1-0.15%. Determined the minimum achievable
- Final bunch length up to 4 mm. Less implies a smaller R₅₆ and a larger RF voltage, more a larger R₅₆ and a smaller RF voltage

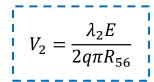


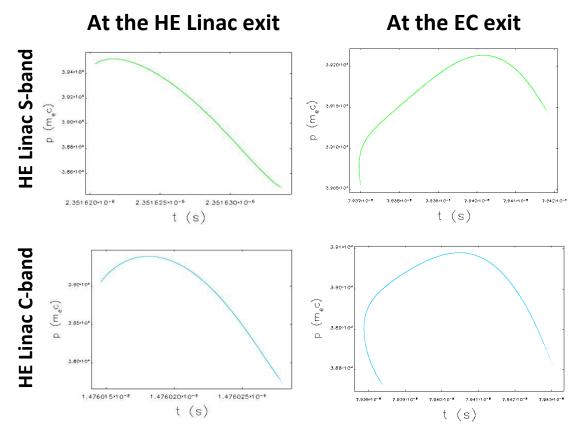
Comments:

- Different linac(s) RF structures' settings correspond to only different initial energy chirp: more R₅₆ smaller voltage V₂
- For the time being simulated a four dipoles chicane. In reality the R₅₆≠ 0 element will be the line to the ring (transfer line WG)



Setting Common (S-band) and HE Linac **on-crest**

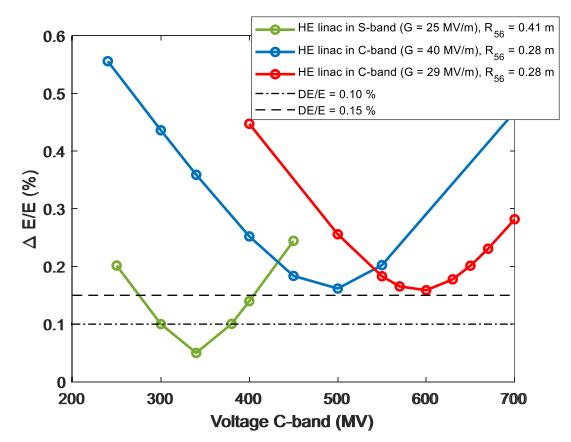




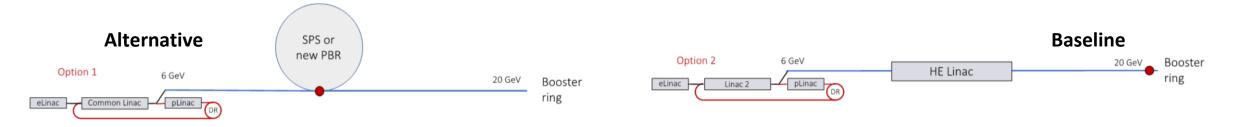
Assumed target bunch length = 4 mm (longer is even better for RF)

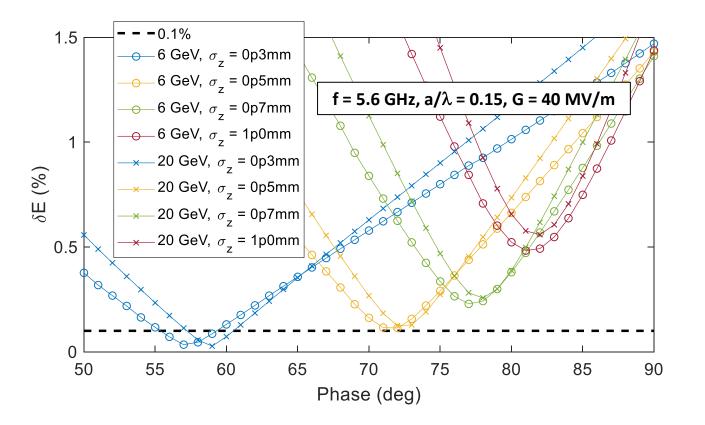
- S-band HE Linac on-crest: δ E/E = 0.05% achievable with 340 MV in C-band and 170 MV in X-band
- C-band HE Linac on crest: minimum of δ E/E limited to ~0.15% with 600 MV in C-band, 300 MV in X-band

	HE linac S-band (G = 25 MV/m)	HE linac C-band a/λ = 0.20 (G = 40 MV/m)	HE linac C-band, a/λ = 0.19 (G = 29 MV/m)
Exit HE Linac δE/E (%)	0.74	1.1	1.3
R ₅₆ (m)	0.41	0.28	0.28



Toward the High Energy (HE) linac (E = $6 \text{ GeV} \rightarrow 20 \text{ GeV}$)





20 GeV vs 6 GeV linac:

- Minimum of the energy spread and corresponding working point (bunch length and operating phase) similar for the two cases → we can use the same table of the previous slide
- Strong impact on the linearizing cavity amplitude (in case we want to move to another scenario): alternative solutions must be considered



From A. Grudiev, 6th June 2024 coordination meeting

