



Integrated Beam Physics Simulation Framework

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Work supported by:





- **Introduction**
 - Motivation
 - Design goals and constraints
 - Architecture
 - Agile development
- **Lattice modeling, simulation and optimization**
 - Lattice modeling
 - Single-particle tracking
 - Dynamic parameter control
 - Multi-objective optimizer
- **Simulation of specific processes**
 - Particle-matter interaction
 - Synchrotron radiation
 - Collective effects
- **Final remarks**



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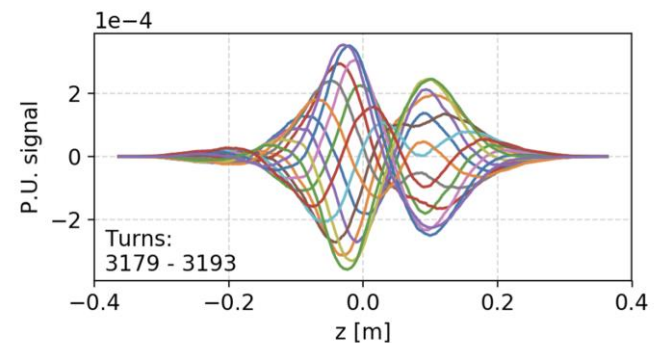
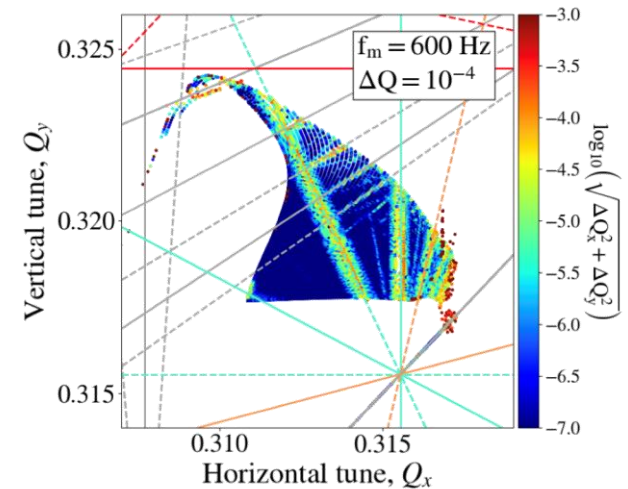
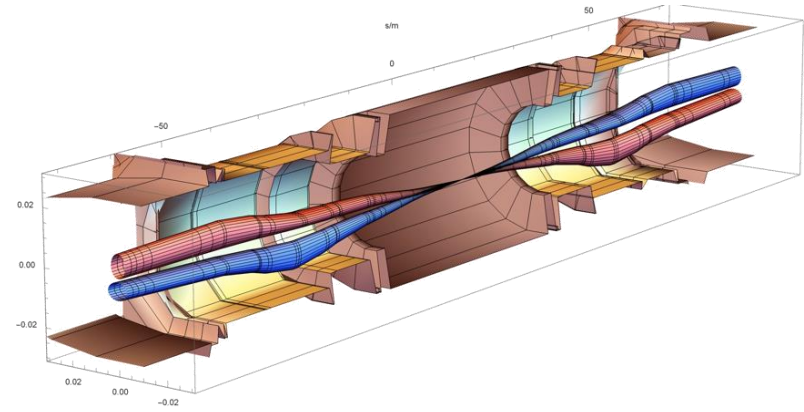
Coming from **long tradition** in the **development of software tools for beam physics**

Powerful **tools** provided to the user community:

- **MAD-X**, standard for lattice description, optics calculation and design, tracking
- **Sixtrack**, a **fast-tracking program** used mainly for long **single-particle simulations**
- **Sixtracklib**, a **C/C++ library for single-particle tracking** compatible with Graphics Processing Units (GPUs)
- **COMBI**, for the simulation of **beam-beam** effects using **strong-strong modelling**
- **PyHEADTAIL**, a **Python** toolkit for **collective effects** (impedance, feedbacks, space charge, and e-cloud).

Developed over decades, providing **powerful features** in their respective domains

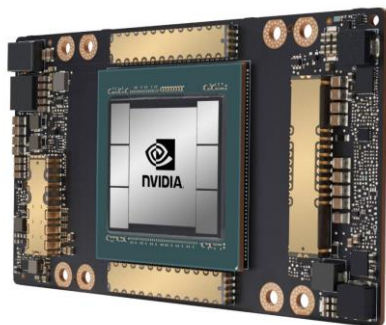
- Nevertheless, **limitations also became apparent...**



Over the years we started to **facing needs that could not be easily fulfilled with legacy tools:**



- **Integration**: very difficult to combine features from different codes to simulate complex heterogeneous effects
- **Extendability**: difficult to extend to present needs (notably those coming from FCC-ee)
- **User interface**: need to move away from custom interfaces (text files / ad-hoc scripting) towards standard **Python packages**
 - Present **de-facto standard in scientific computing**
 - Allows **leveraging an ever-growing arsenal of general-purpose Python libraries** (statistics, linear algebra, frequency analysis, optimization, plot, etc.)
 - Boosted by **large investments from industry** (big data, AI)
- **GPU acceleration**: mandatory for several applications but cumbersome to retrofit in the existing codes



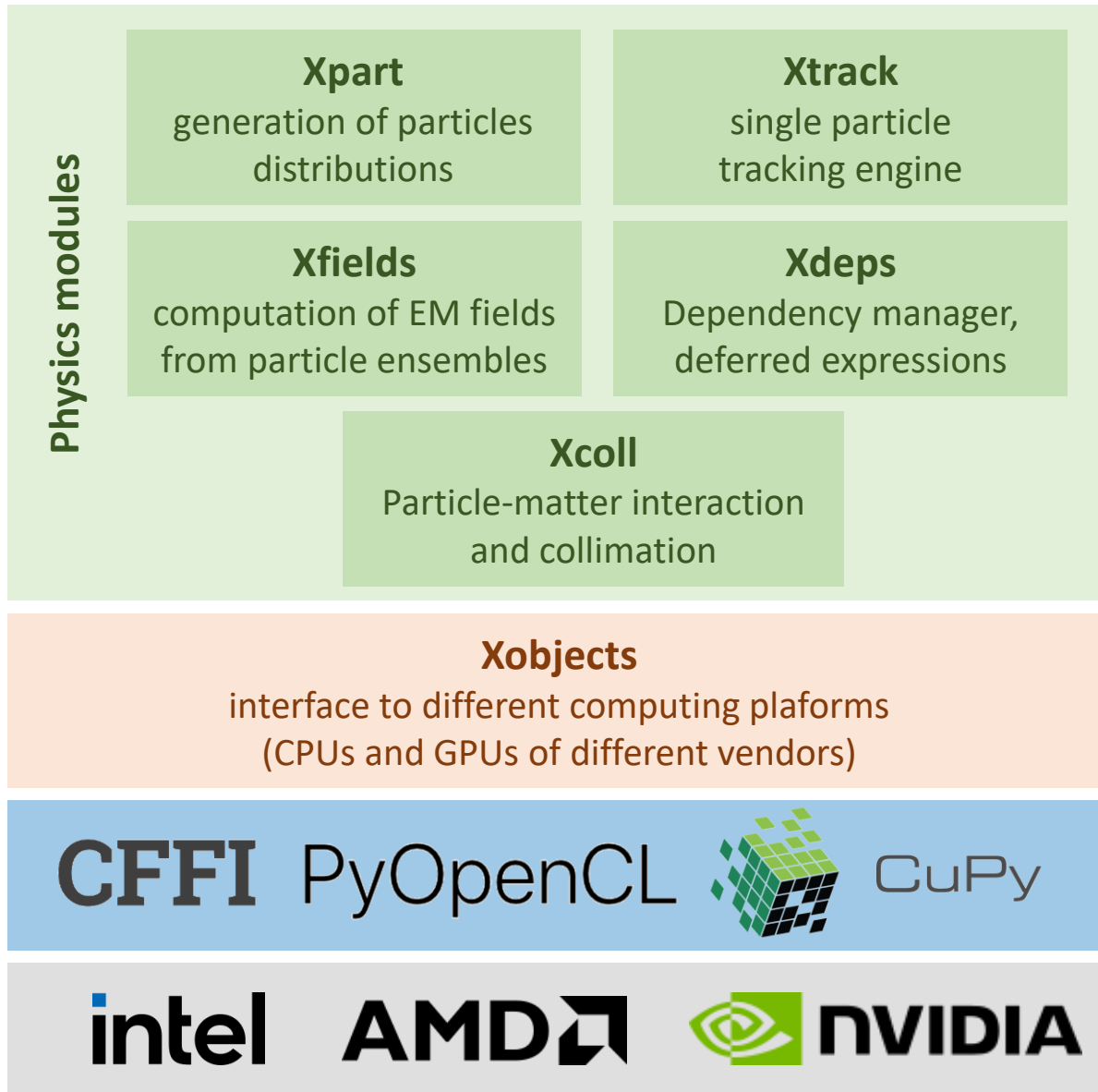


This led to the **launch of the Xsuite project** in **2021**

- **Main goal:** bring into a **modern Python toolkit** the know-how built in developing MAD, Sixtrack, COMBI...
 - **Cover with one toolkit** applications ranging from **low-energy hadron rings** to **high-energy lepton colliders**
- Designed for **seamless integration of components** and for **extendibility**
- Support **different computing platforms**, including **multicore CPUs and GPUs** from different vendors

Design constraints:

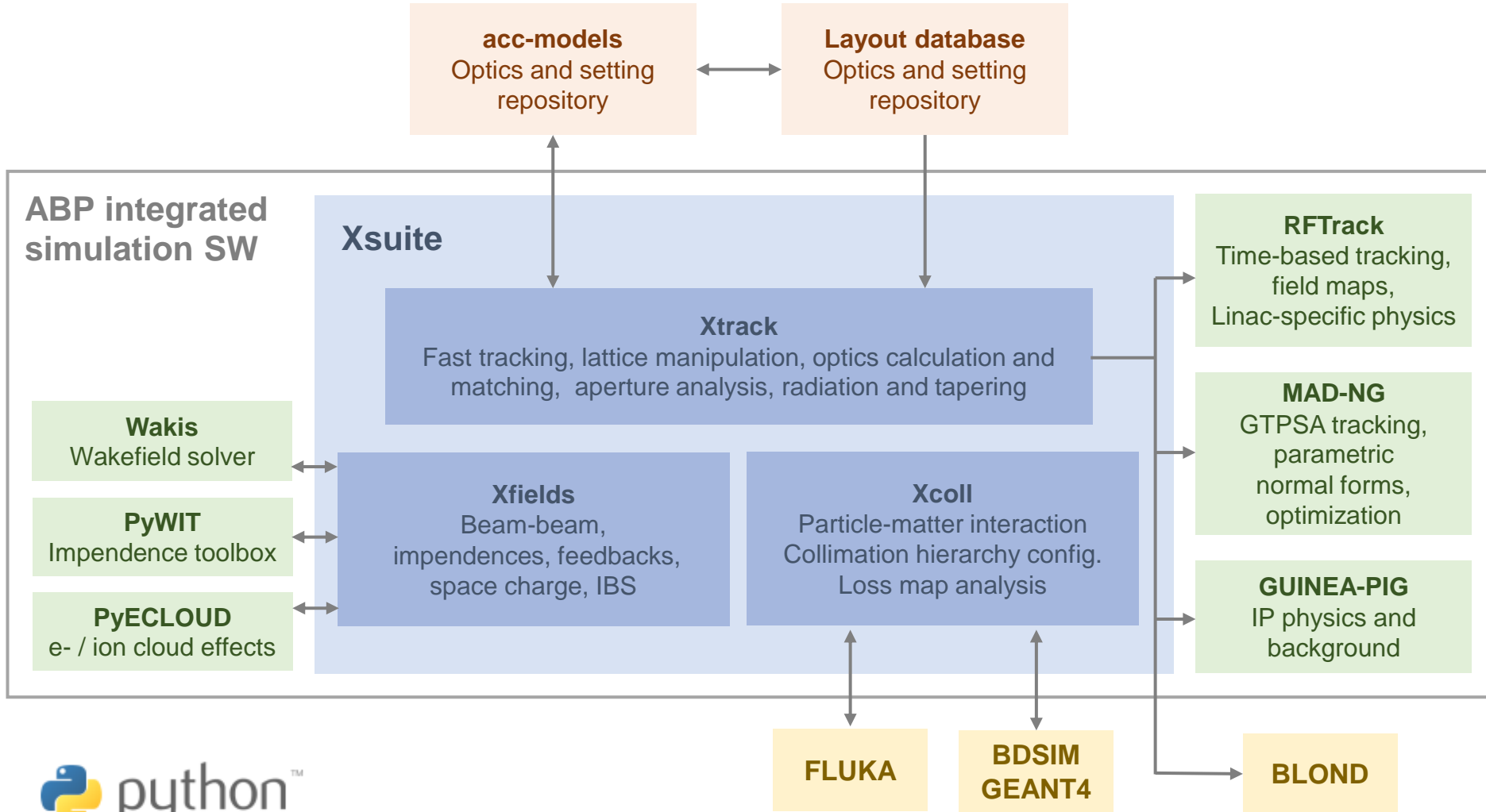
- Need **to grow the code in a “sustainable” way**, being managed and maintained by a **small core team** integrating (in a clean way!) contributions by a wide developer community
- Need **developer learning curve** to be short as possible
 - Field specific features developed **directly by field experts**





Broader software architecture

Xsuite working as aggregation point of a wider Python ecosystem (under development)



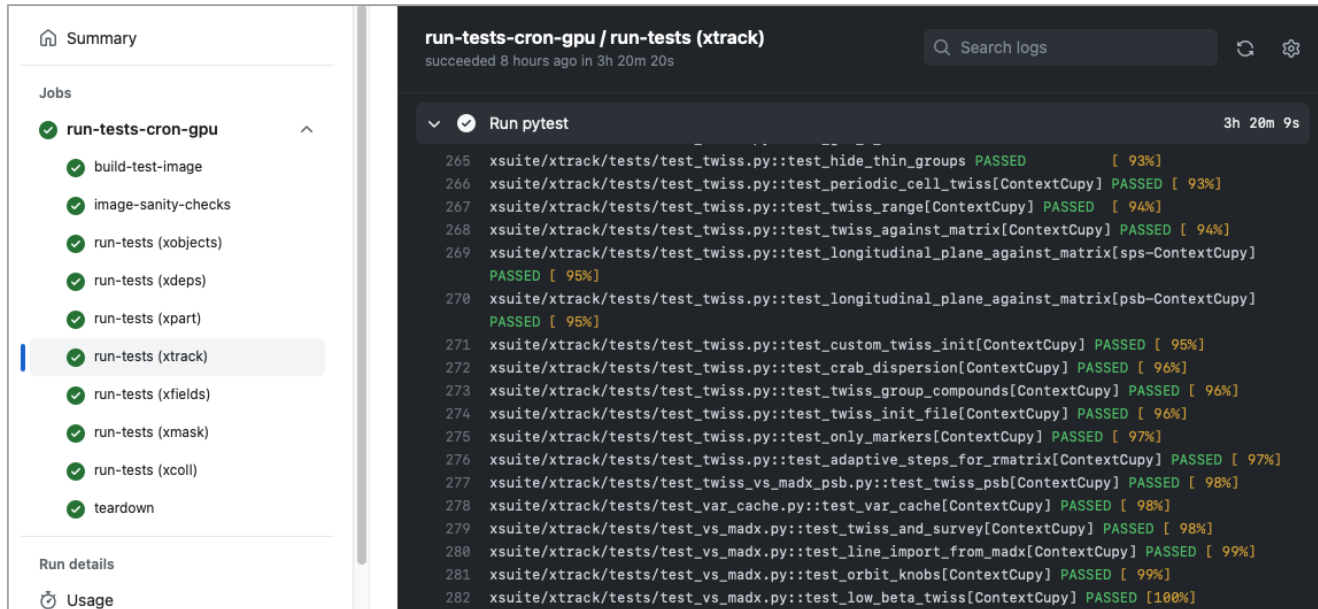
Project employs an “orthogonal” design strategy:

- Ensure that **each functional block** remains **well-isolated** and interacts with the others through **clearly defined interfaces**
- This approach has two key **advantages**:
 - Enables **contributors** to **modify or expand** specific components **without full knowledge of other parts** nor of underlying software infrastructure
 - **Minimize codebase complexity**, ensuring that it **increases linearly rather than exponentially** as new features are added



Our development follows the **agile principles**:

- **We engaged with the user community**, encouraging and **supporting users to test and exploit** available features in **full-scale studies since early development stages**
- Code **evolves incrementally**, promptly applying needed fixes and improvements
- **Rely on fast release cycle** (new versions released multiple times per month) while ensuring **no disruption due to version changes** on the user's side.
- Made possible by large investment **automatic testing**: each version of Xsuite undergoing over a **thousand automatic checks** (on CPU and GPU)



The screenshot displays a CI/CD pipeline interface. On the left, a 'Summary' panel lists jobs, with 'run-tests-cron-gpu' selected. The main panel shows the execution of 'Run pytest' for 'run-tests-cron-gpu / run-tests (xtrack)', which succeeded 8 hours ago. The test results are as follows:

| Line | Test Command | Result | Pass Rate |
|------|--|--------|-----------|
| 265 | xsuite/xtrack/tests/test_twiss.py::test_hide_thin_groups | PASSED | [93%] |
| 266 | xsuite/xtrack/tests/test_twiss.py::test_periodic_cell_twiss[ContextCupy] | PASSED | [93%] |
| 267 | xsuite/xtrack/tests/test_twiss.py::test_twiss_range[ContextCupy] | PASSED | [94%] |
| 268 | xsuite/xtrack/tests/test_twiss.py::test_twiss_against_matrix[ContextCupy] | PASSED | [94%] |
| 269 | xsuite/xtrack/tests/test_twiss.py::test_longitudinal_plane_against_matrix[sps-ContextCupy] | PASSED | [95%] |
| 270 | xsuite/xtrack/tests/test_twiss.py::test_longitudinal_plane_against_matrix[psb-ContextCupy] | PASSED | [95%] |
| 271 | xsuite/xtrack/tests/test_twiss.py::test_custom_twiss_init[ContextCupy] | PASSED | [95%] |
| 272 | xsuite/xtrack/tests/test_twiss.py::test_orab_dispersion[ContextCupy] | PASSED | [96%] |
| 273 | xsuite/xtrack/tests/test_twiss.py::test_twiss_group_compounds[ContextCupy] | PASSED | [96%] |
| 274 | xsuite/xtrack/tests/test_twiss.py::test_twiss_init_file[ContextCupy] | PASSED | [96%] |
| 275 | xsuite/xtrack/tests/test_twiss.py::test_only_markers[ContextCupy] | PASSED | [97%] |
| 276 | xsuite/xtrack/tests/test_twiss.py::test_adaptive_steps_for_rmatrix[ContextCupy] | PASSED | [97%] |
| 277 | xsuite/xtrack/tests/test_twiss_vs_madx_psb.py::test_twiss_psb[ContextCupy] | PASSED | [98%] |
| 278 | xsuite/xtrack/tests/test_var_cache.py::test_var_cache[ContextCupy] | PASSED | [98%] |
| 279 | xsuite/xtrack/tests/test_vs_madx.py::test_twiss_and_survey[ContextCupy] | PASSED | [98%] |
| 280 | xsuite/xtrack/tests/test_vs_madx.py::test_line_import_from_madx[ContextCupy] | PASSED | [99%] |
| 281 | xsuite/xtrack/tests/test_vs_madx.py::test_orbit_knobs[ContextCupy] | PASSED | [99%] |
| 282 | xsuite/xtrack/tests/test_vs_madx.py::test_low_beta_twiss[ContextCupy] | PASSED | [100%] |



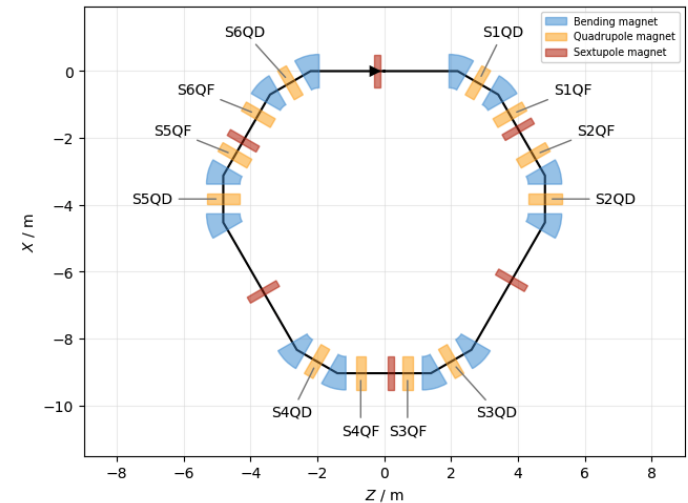
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- The **beam line** is represented as a **sequence of Python objects**, each corresponding to an accelerator element or to other physical processes (e.g. magnets, cavities, aperture restrictions, etc.).
 - Can be **defined manually** or **imported from MAD-X**
 - Including **tilts, misalignments** and **multipolar errors**

Xsuite model of a ring
(represented with the [Xplt package](#))

```
survey = tracker.survey()
```

```
plot = xplt.FloorPlot(survey, line, labels="S.Q.")
plot.legend()
```

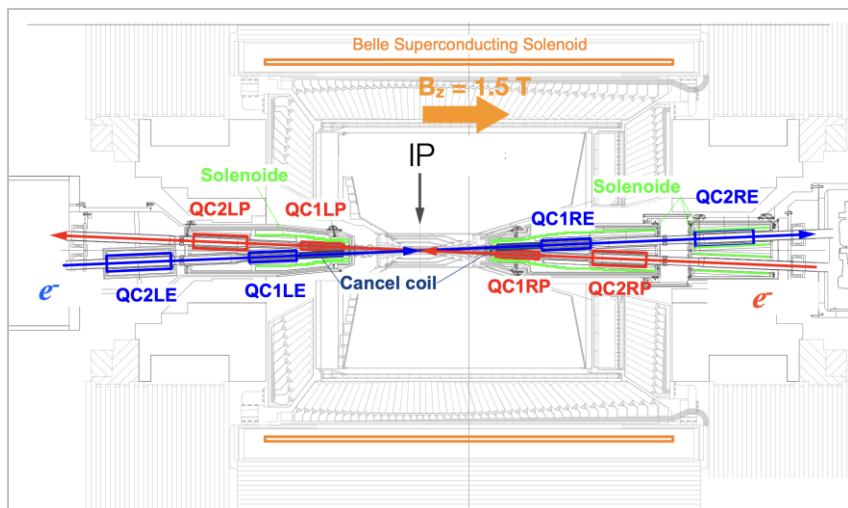
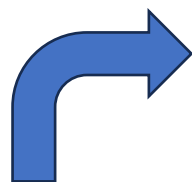


We provide:

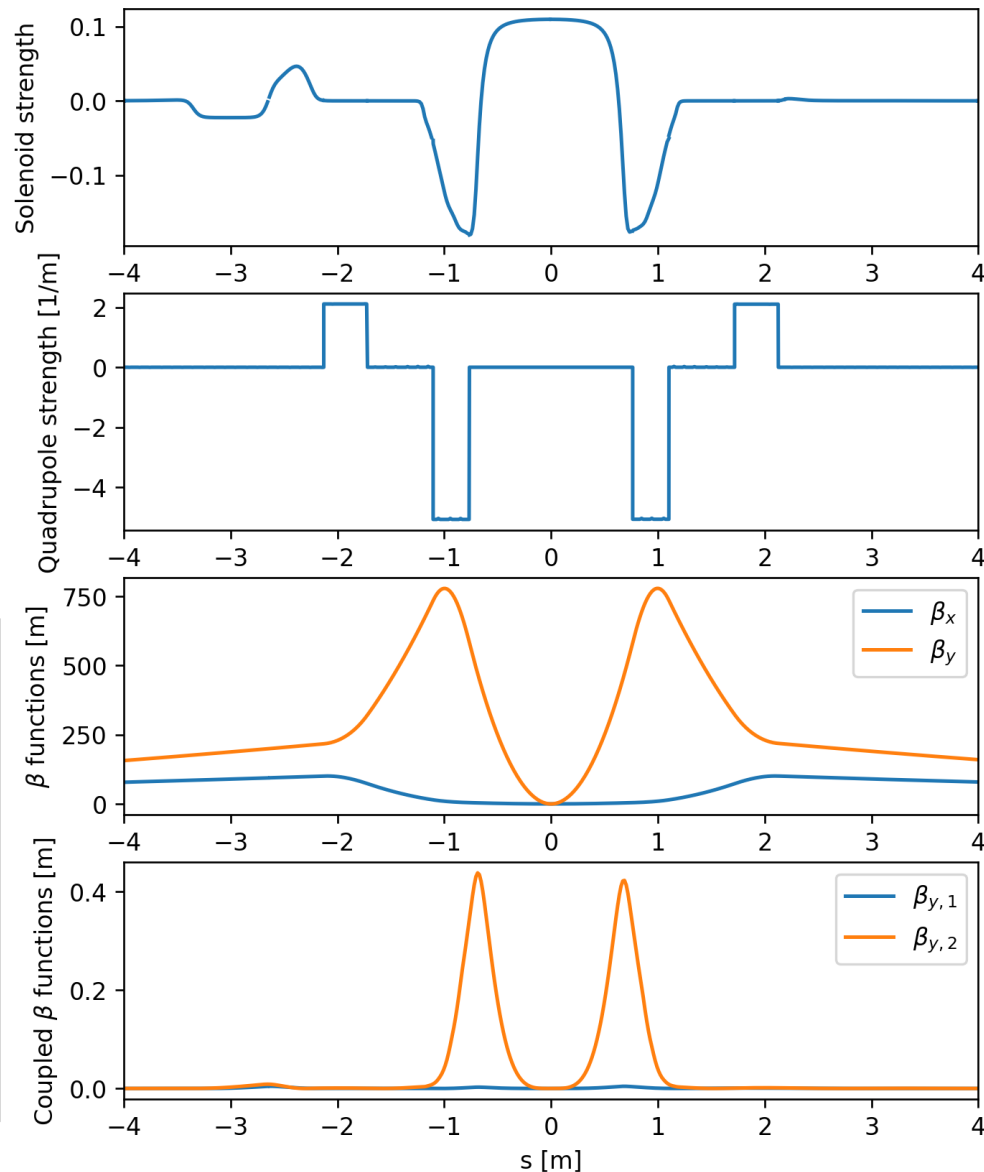
- **“Thin” lattice integration**, largely based on the Sixtrack and Sixtracklib experience
- **“Thick” maps** for bending and quadrupole magnets
- **Dipole edge effects** including **fringe fields** can be modeled either in their **linearized form** or as **full non-linear maps** (same fringe model as in MAD-NG and PTC).

Recent developments allow modelling of **experimental solenoids** of lepton colliders also in the presence of **overlapping multipole fields**

- Tested on **FCC-ee** and **SuperKEKb** models



SuperKEKb interaction region



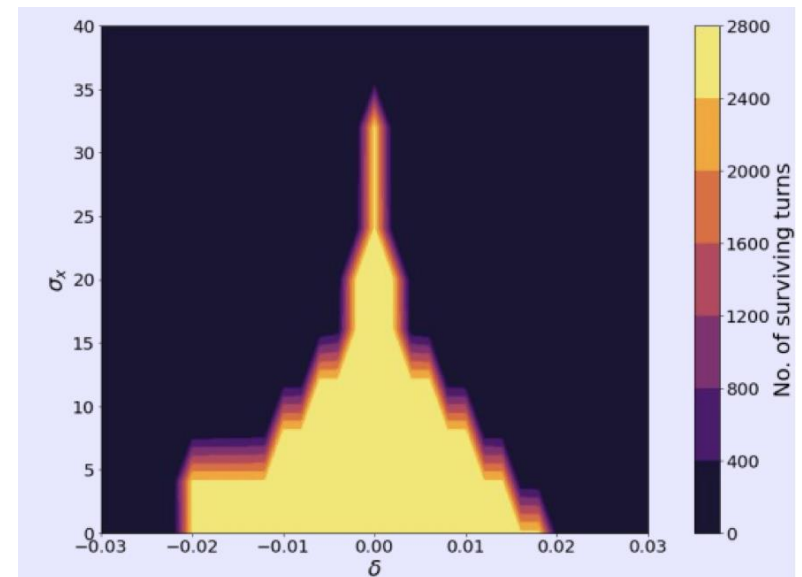


- Multiturn **element-by-element tracking speed** is critical for several application
- To **speed up tracking simulations**, Xsuite assembles and compiles a **C kernel** (callable from Python) **optimized for the given beamline** and **specialized for the chosen platform** (CPU or GPU)
 - The **tracking speed** is found to be **similar to Sixtrack** for single-core CPU and **about two orders of magnitudes faster than that on high-end GPUs**
 - Developments are well advanced to deploy Xsuite on the **LHC@Home** volunteer computing platform (collaboration with EPFL)

Tracking time for a typical LHC simulation

| Platform | Computing time |
|-----------------------------------|---|
| CPU (single core) | 190 ($\mu\text{s}/\text{part.}/\text{turn}$) |
| GPU (NVIDIA V100, cudy) | 0.80 ($\mu\text{s}/\text{part.}/\text{turn}$) |
| GPU (NVIDIA V100 pyopencl) | 0.85 ($\mu\text{s}/\text{part.}/\text{turn}$) |

Example: Xsuite simulations used to study FCC-ee DA and momentum acceptance

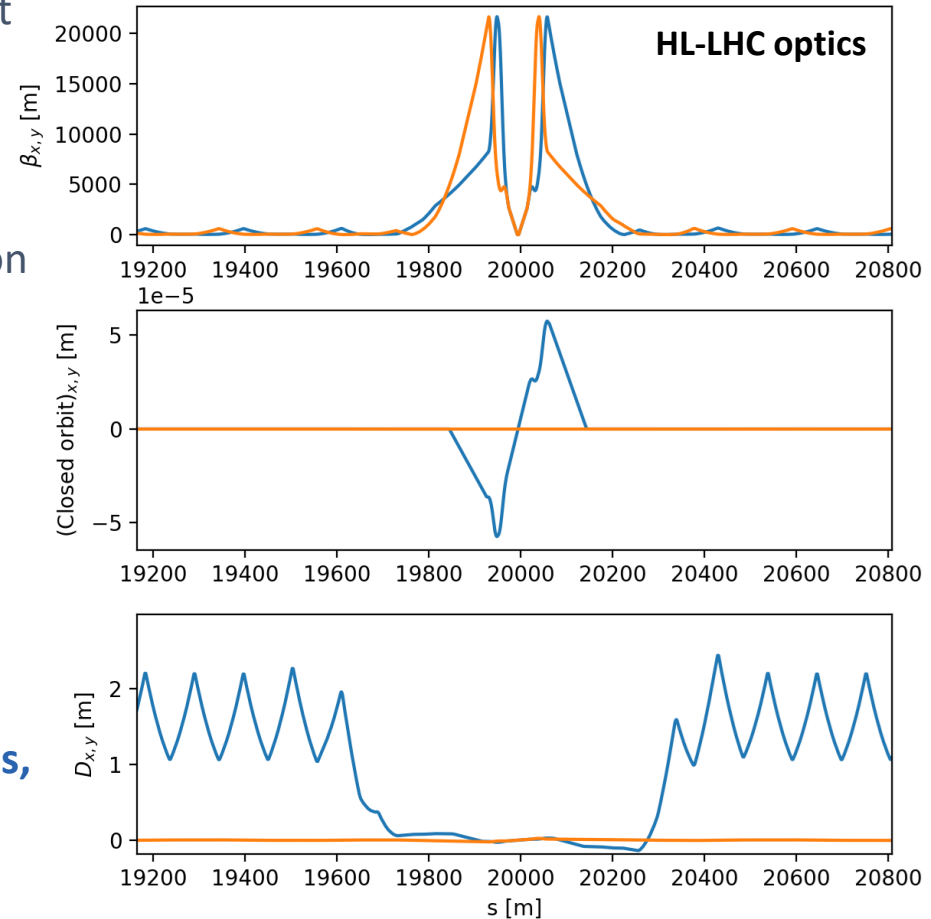


Courtesy M. Hofer



$$q_x = 0.31000 \quad q_y = 0.32000 \\ Q'_x = 2.00 \quad Q'_y = 2.00 \quad \gamma_{tr} = 53.57$$

- The **Xsuite Twiss** module can be used to extract **lattice functions** of a ring or a beamline
- The calculation **probes the lattice simply by tracking particles**:
 - **Closed orbit** obtained by applying a Python root finder on the tracking
 - The **Jacobian** matrix obtained by **tracking (central differences)**
 - Compute “**Linear Normal Form**” of the Jacobian matrix (diagonalization)
 - **Propagate eigenvectors** by **tracking**
 - Obtain from the eigenvectors **Twiss parameters** (α, β, γ), **dispersion functions**, **phase advances**, **coupling coefficients**
- Computation can be done with **assigned beam momentum** to get **off-momentum beta-beating**, **non-linear chromaticity**, **non-linear dispersion**, etc.



Accuracy compared to MAD-X: $\Delta\beta / \beta \ll 10^{-4}$
Computation time is very similar

```
In [37]: tw.bety[0] # xsuite
Out[37]: 149.4305507849305

In [38]: mad.table.twiss.bety[0] # madx
Out[38]: 149.43055000962505

In [39]: t_mad_ms
Out[39]: 202.0

In [40]: t_xsuite_ms
Out[40]: 185.0
```

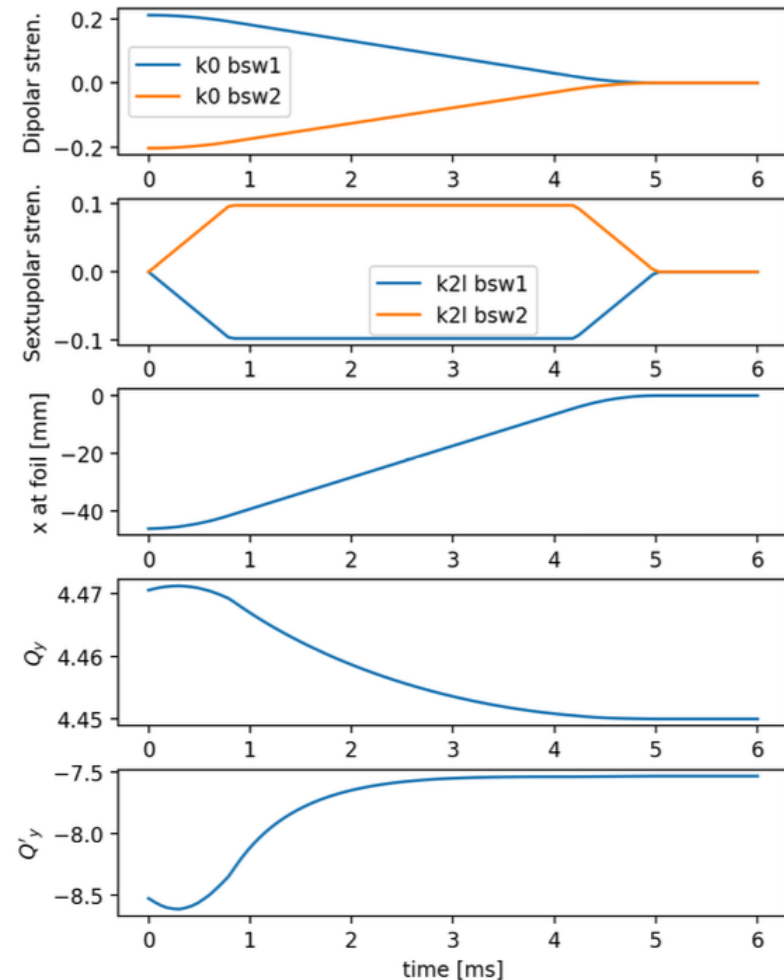
Example

- In accelerators often a single **high-level parameter** can be used to control **groups of components** with complex dependency relations. (e.g. circuits with multiple magnets, groups of RF cavities, etc.)
- The **Xdeps module** provides the capability to **include such dependencies in the simulation model** (as done by MAD-X deferred expressions)
- Example**, LHC crossing angle knob:
 - At any time, the user can set:


```
lhc.vars['on_x1'] = 160 # murad
```

 which **automatically changes the strength of 40 dipole correctors** to get the required crossing angle
- User can also use **“Time functions”**, i.e. **time dependent knobs** that are updated automatically during the simulation

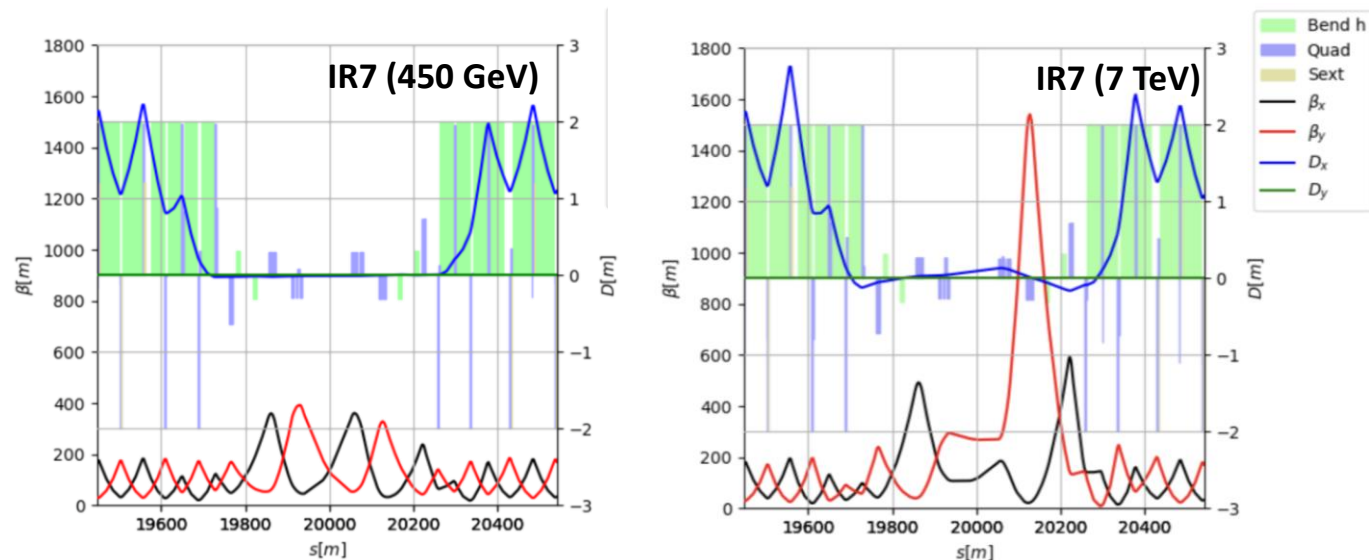
Simulation of a fast orbit bump used for the H⁻ injection into the CERN PS Booster



Xsuite provides a **multi-objective optimizer** to "match" model parameters to assigned constraints (e.g. control tunes, chromaticity, build orbit bumps, design the optics)

- Based on the **extensive experience of MAD-X** → Uses the **same optimization algorithm** (Jacobian, proven robustness)
- Interface **designed for usage flexibility**. User can **intervene in the optimization** by:
 - Enabling/disabling targets or knobs, rolling back optimization steps, changing knob limits, target values, convergence tolerances
- Used for **optics matching of the LHC and of FCC-ee colliders**
 - Proved capability of handling **large problems** with several constraints and degrees of freedom

First full cycle designed with Xsuite tested at the LHC in 2024
(including combined ramp&squeeze for all insertions)



Courtesy R. De Maria and B. Lindstrom



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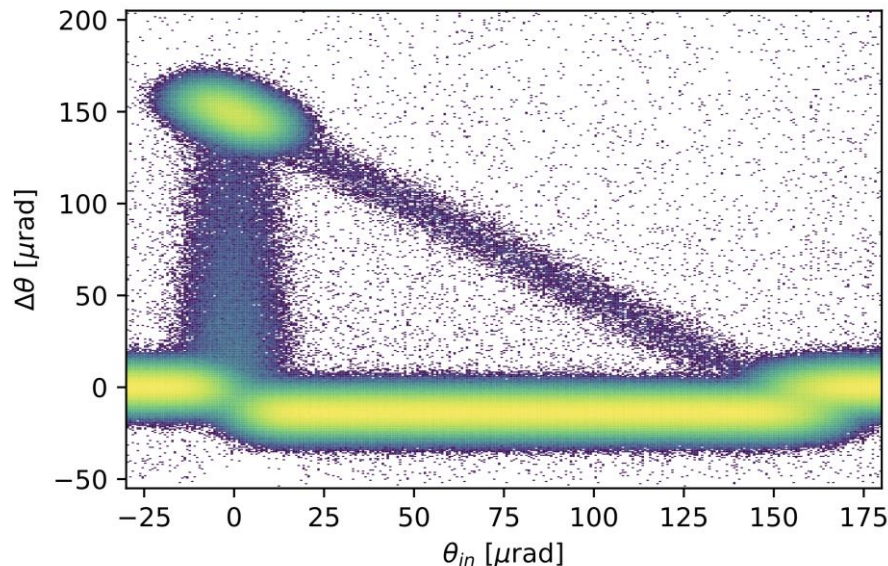
For collimation studies, the **Xcoll module** provides **three particle-matter sim. engines**:

- The **“Everest” engine** embedded in Xcoll (evolution of K2 module from Sixtrack)
- The **“Geant 4” engine**, based on an **interface with BDSIM-Geant4**
 - **Used for FCC-ee collimation studies** (see presentation by G. Broggi)
- The **“FLUKA” engine**, based on an interface with the **FLUKA** Monte Carlo code

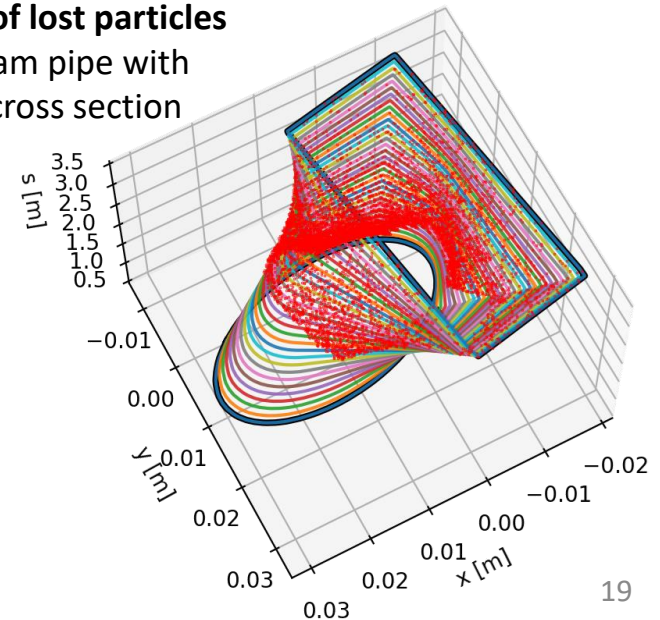
To support collimation studies, Xsuite provides:

- Tools to **automatically install and set collimators** in the simulation model
- Support for **complex aperture modelling** and **accurate localization of the lost particles along** the beam line (typically within 1-10 cm)

Particle deflection from a bent crystal (Everest engine)



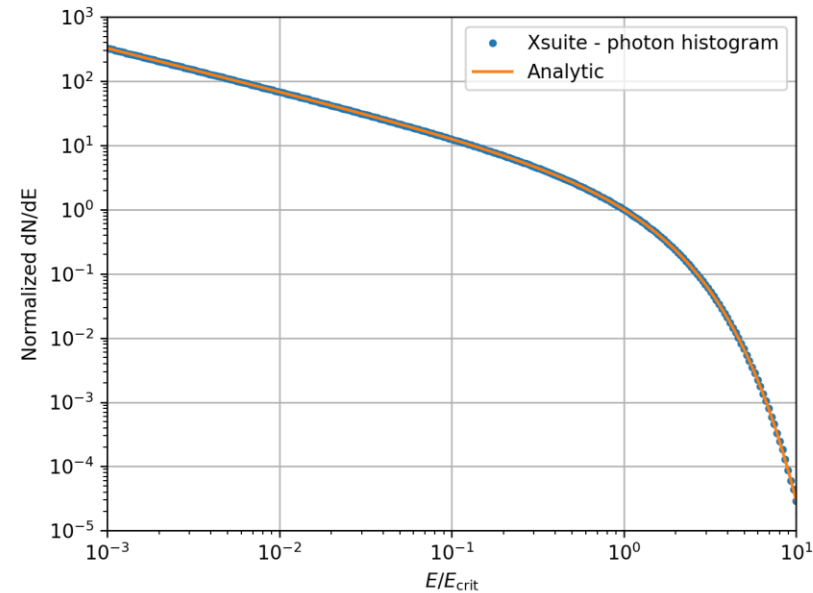
Localization of lost particles along a beam pipe with changing cross section



The effect of **synchrotron radiation** can be included in Xsuite tracking simulations. Two models available:

- The **“mean” model**, for which the energy loss from the radiation is applied particle by particle without accounting for quantum fluctuations;
- The **“quantum” model** for which the actual photon emission is simulated⁽¹⁾.

Validation against analytical photon spectrum



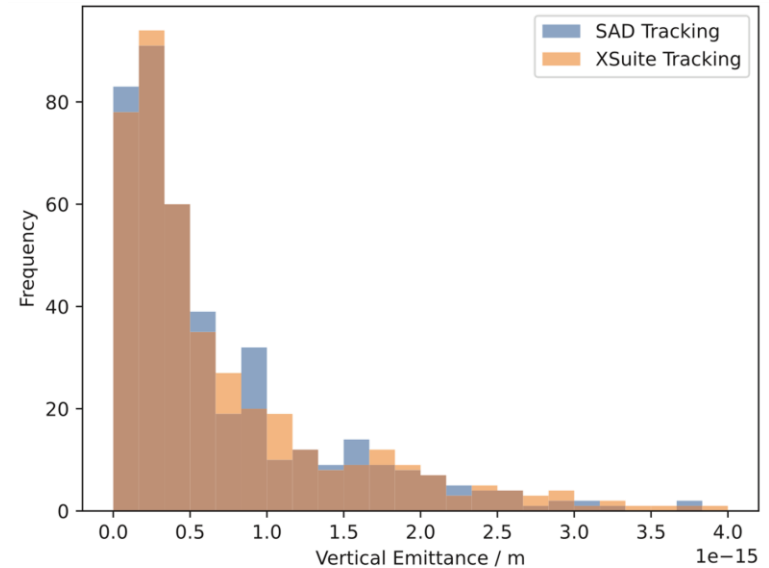
⁽¹⁾ Based on H. Burkhardt, “Monte Carlo generator for synchrotron radiation”, 1990. Implementation ported from PLACET (A. Latina)

⁽²⁾ E. Forest, From tracking code to analysis: generalised Courant-Snyder theory for any accelerator model. Springer, 2016

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Benchmark of equilibrium emittances from tracking (with lattice errors)



L. Van van Riesen-Haupt, T. Pieloni, et al., EPFL

⁽¹⁾ Based on H. Burkhardt, “Monte Carlo generator for synchrotron radiation”, 1990. Implementation ported from PLACET (A. Latina)

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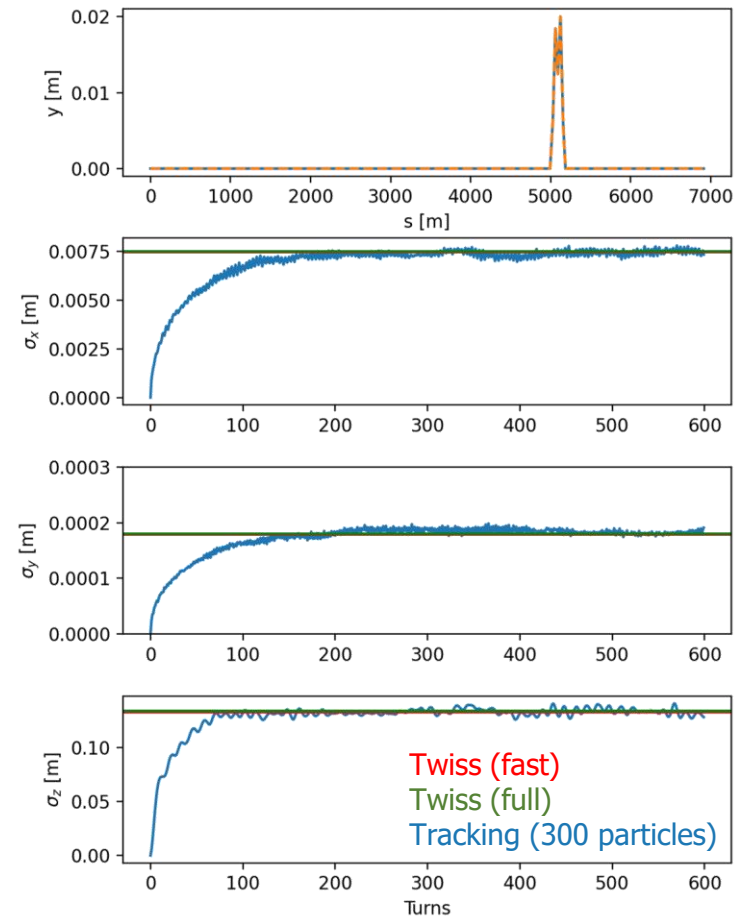
- The **“mean” model**, for which the energy loss from the radiation is applied particle by particle without accounting for quantum fluctuations;
- The **“quantum” model** for which the actual photon emission is simulated⁽¹⁾.

The **Xsuite Twiss** also includes:

- Dedicated algorithm for **non-symplectic one-turn map**⁽²⁾
- Computation of **radiation energy loss, damping times and equilibrium emittances**

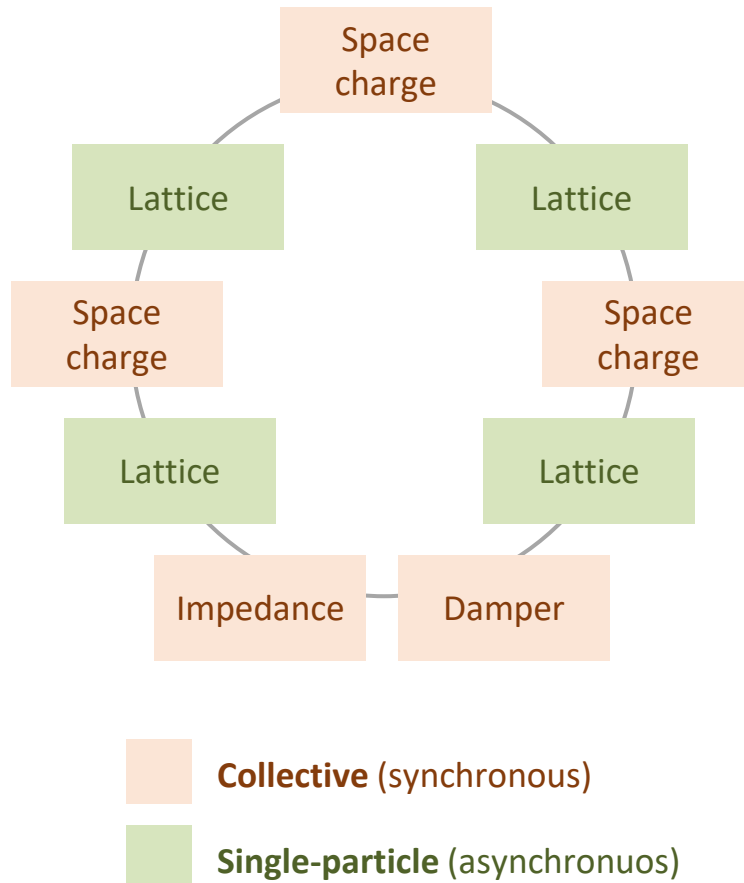
An **automatic tool** is provided for **phasing the RF cavities** and **adjusting magnet strengths** to **compensate the radiation energy loss (“tapering”)**

Equilibrium emittance (twiss vs track)



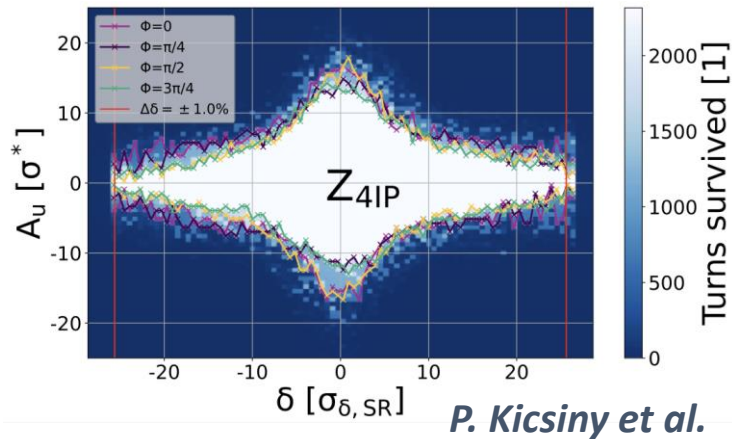
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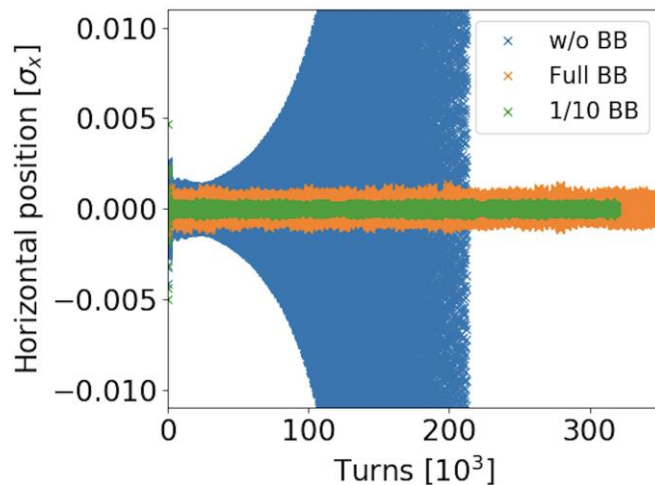


- Xsuite is designed to include **collective effects** in the simulations
- Handling of collective elements is **fully automatic** → The Xtrack module identifies the collective elements and **splits the sequence**:
 - The **non-collective** parts are handled **asynchronously** to **gain speed**
 - The simulation of the **collective effects** is **performed synchronously**
- **Space-charge, beam-beam, e-cloud** (weak-strong) are handled **natively**
- **Impedances** and **feedback systems** are handled through an interface with **PyHEADTAIL**
- An automatic tool for the **computation of stability diagrams** from amplitude detuning is also provided

FCC-ee DA studies (with bb)



Wakefield + beam-beam simulations for HL-LHC (strong-strong modelling)



- Xsuite implementation based on experience from **Sixtrack** and **COMBI**
- Two models are provided:
 - The **“4D” model**, which applies **only transverse** forces **independent on the longitudinal motion**
 - The **“6D” model**, which applies **longitudinal and transverse** forces accounting for the synchrotron motion (method by Hirata et al.)
- Both models can be used either in **“weak-strong” mode** (fixed assigned distribution for the other beam) or in **“strong-strong” mode** (self-consistent two-beam simulation, “soft Gaussian”)
- For the simulation of lepton colliders, the code can also simulate for **beamstrahlung** and **Bhabha scattering** (developed in collaboration with EPFL)
- **Strong-strong simulations** are accelerated by **parallel computing on HPC clusters** (based on MPI)
 - **“Pipeline” algorithm⁽¹⁾** used to optimize workload distribution across the nodes

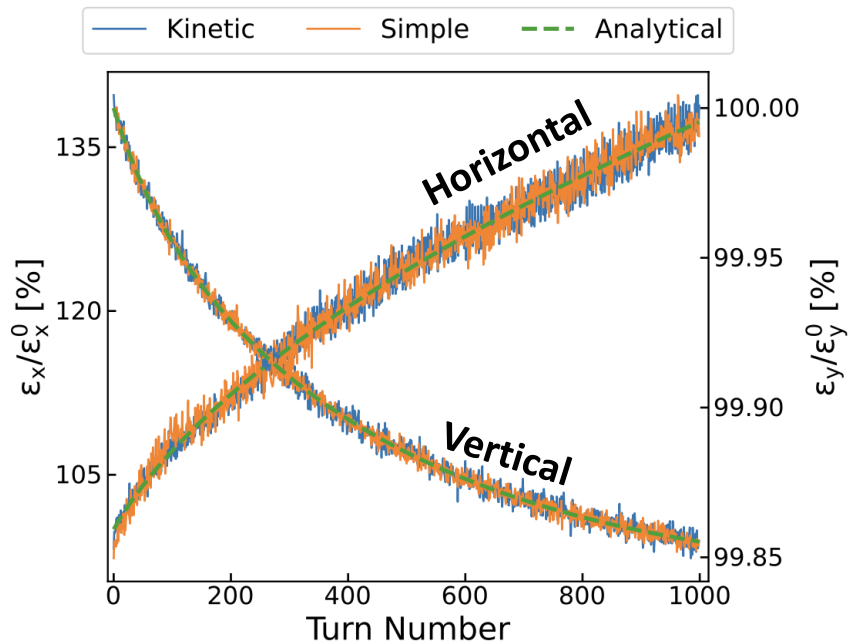
(1) S. Furuseth and X. Buffat, *Comput. Phys. Commun.* 244 (2019)

(2) For more details, see presentation by P. Kicsiny

Intra Beam Scattering (IBS) simulation capabilities have been recently introduced:

- **IBS growth rates computation** from beam parameters and optics. Two methods available:
 - [Nagaitsev](#) (very fast, vertical dispersion neglected)
 - [Bjorken-Mtingwa](#) (slower, D_y correctly accounted)
- Effect of **IBS can be included in multiparticle simulations** in combination with all other effects available in Xsuite. Two methods available:
 - [Effective kick](#)
 - [Kinetic formalism](#)

Benchmark case for the SPS ring (Pb ions)





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After three years the software has grown very rapidly, thanks to many people contributing code and expertise...



and more...

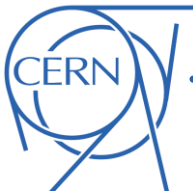


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Response went well beyond our expectation:

- **>30 colleagues from CERN and other labs contributed by developing new features and debugging issues**
 - Leveraging their python skills and the short tool-specific learning curve
- **Xsuite was adopted by a large and diverse user community (>100 users!!!)**
 - **Very lively community** providing mutual support, advice, lots of feedback to developers (very precious!)
 - For first time at CERN we are using the same software tool for **optics, dynamic aperture studies, collimation, beam-beam, space-charge, instabilities, lepton machines, extraction and beam transfer studies and more...**
 - **Already profited from lots of synergies**
 - Adopted for **many FCC studies** (counted ~10 talks in this workshop presenting work based on Xsuite)

and more...



Xsuite simulations have been already used for **studies covering a variety of rings:**

- | | | | |
|--|---|---|--|
| CERN <ul style="list-style-type: none">• ELENA• LEIR• PSB• PS• SPS, TI2, TI8• LHC• FCC-ee, FCC-hh• Muon collider• LEP | GSI <ul style="list-style-type: none">• SIS-18• SIS-100 Medical facilities <ul style="list-style-type: none">• HIT (Heidelberg)• MEDAUSTRON• PIMMS• NIMMS | BNL <ul style="list-style-type: none">• RHIC• Booster• EIC Fermilab <ul style="list-style-type: none">• Main injector• Recycler• Booster• IOTA | Light sources and damping rings: <ul style="list-style-type: none">• PETRA• DESY injector ring• ELETTRA• BESSY III• CLIC-DR ... and more |
|--|---|---|--|

Each of these taught us something and contributed to extend and improve the software!



- CERN Accelerator and Beam Physics group is **committed to maintain Xsuite and support its users for the years to come**
 - For other legacy tools (e.g. MAD-X, PyHEADTAIL) we will keep present level of functionality and support for as long as needed, while focusing resources on the development of this stack.
- **Xsuite development continues:**
 - Next items on our plate include **3D PIC for beam-beam, spin tracking, insertion devices, quadrupole fringes, and more...**
- The code is **publicly available** on GitHub and can be installed through pip
 - You are **vey welcome to give it a try** for your use case
 - **Installation instructions and many examples** available in the [documentation pages](#)
 - We are very interested in getting your **feedback** (don't hesitate to contact us for issues, questions, suggestions)
- Code is **open-source** and is open to **developments from the community**
 - Get in touch if you are interested in contributing to the development



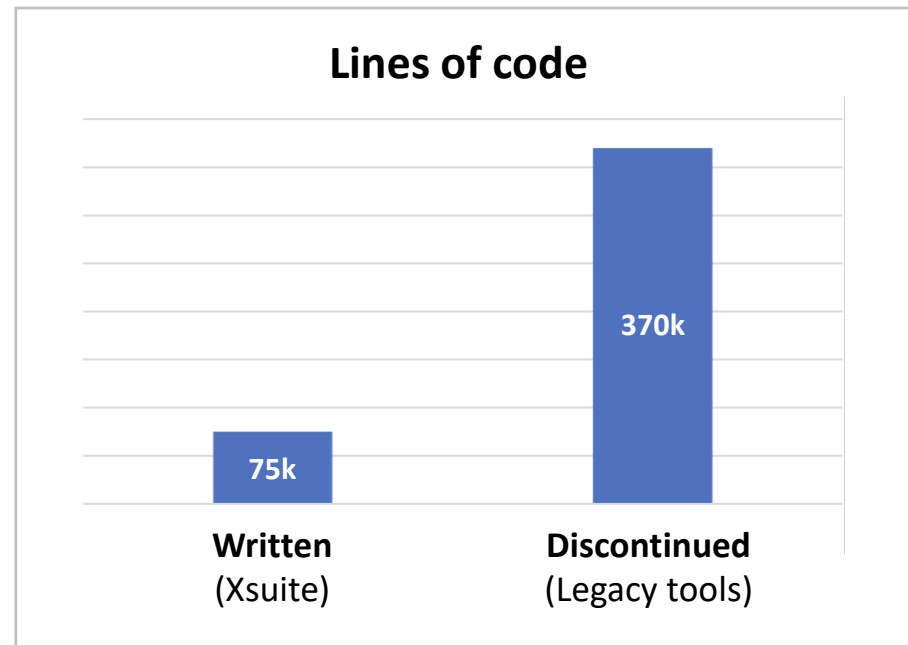
Thanks for your attention!



In 2022-23 we have **essentially discontinued** the development and, to a very large extent, the usage of the following tools:

- Sixtrack
- Sixdesk
- Sixtracklib
- COMBI
- PySSD
- DistLib

This led to a **massive simplification** of our code base.



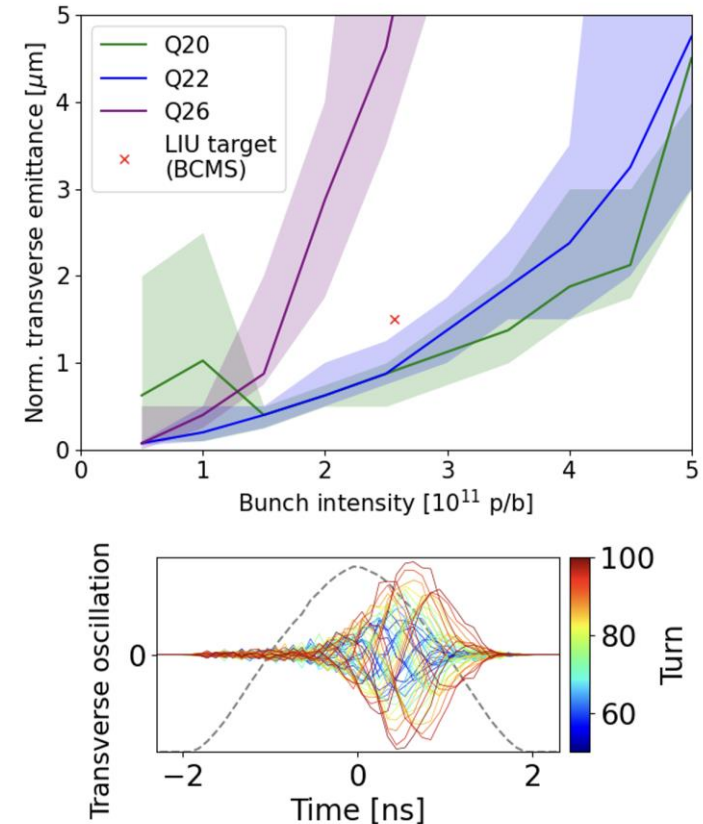
The implementation is largely based on

PyHEADTAIL-PyPIC

Different **space-charge models** are implemented:

- The **“frozen” model**, in which particles interact with fixed charge distributions
- The **“quasi frozen” model**, in which the **beam intensity and beam sizes are recomputed at each interaction**
- The **“Particle In Cell (PIC)” model**:
 - Charge of tracked particles distributed on a **rectangular grid**
 - **Fast Poisson solver** based on **FFT** method with Integrated Green Functions
- Space charge simulations **strongly profiting from GPU acceleration**

Simulation campaign for the CERN SPS including full non-linear lattice, space charge and wakefields

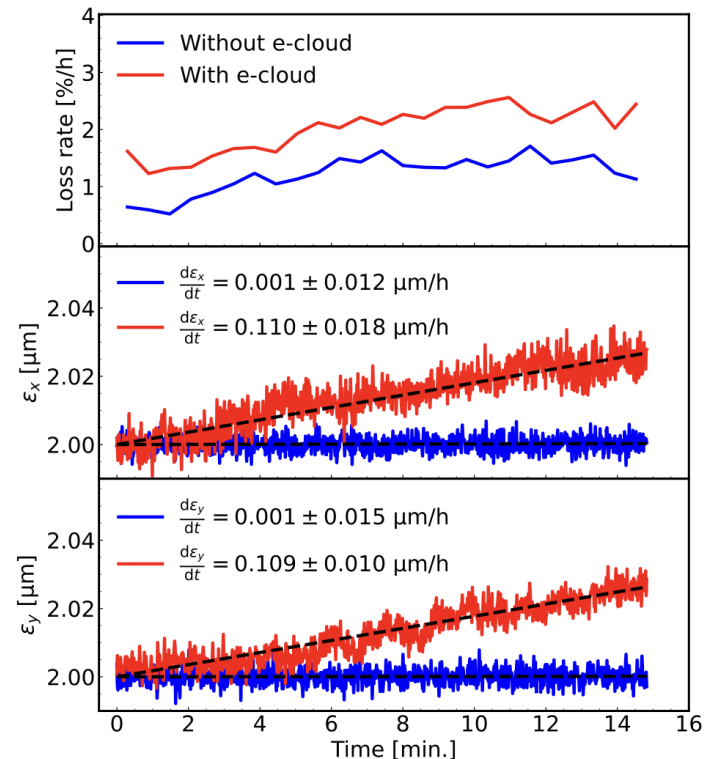
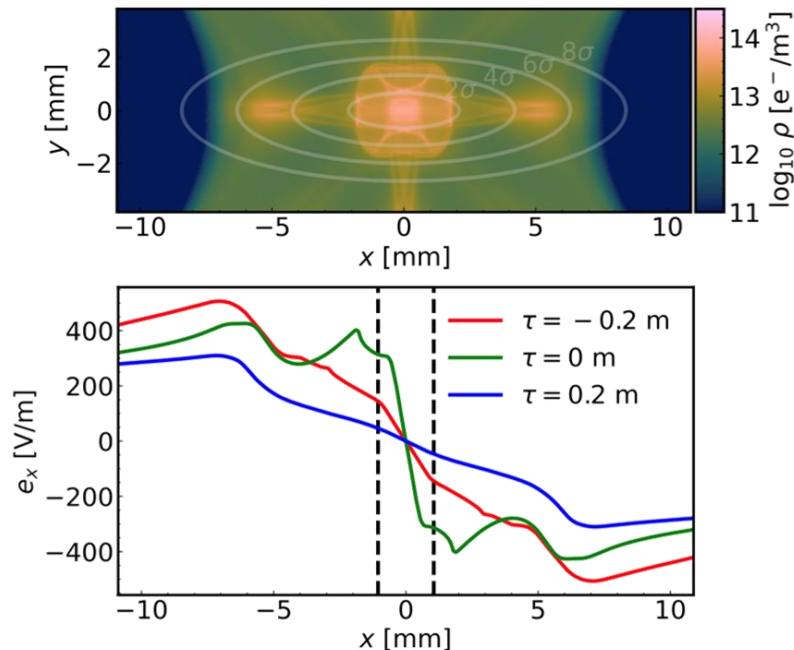


| | |
|--------------------------------------|-------------|
| N. simulations | 400 |
| Number of PIC calculations per turn | 540 |
| Number of turns per simulation | 40'000 |
| Computing time per sim. (GPU) | ~3 days |
| Computing time per sim. (CPU serial) | > 12 months |

Courtesy X. Buffat

Xsuite has been exploited to study the **effect of electron cloud on slow beam degradation** (emittance growth, lifetime degradation).

- Done by applying a **high-order interpolation scheme** to the **e-cloud potential imported** from a dedicated multipacting simulator.
 - Scheme designed to **preserve the symplecticity of the resulting map** by ensuring the global continuity of the potential and required derivatives.
- **Use of GPUs is mandatory** to simulate the required long time scales ($>10^6$ turns).

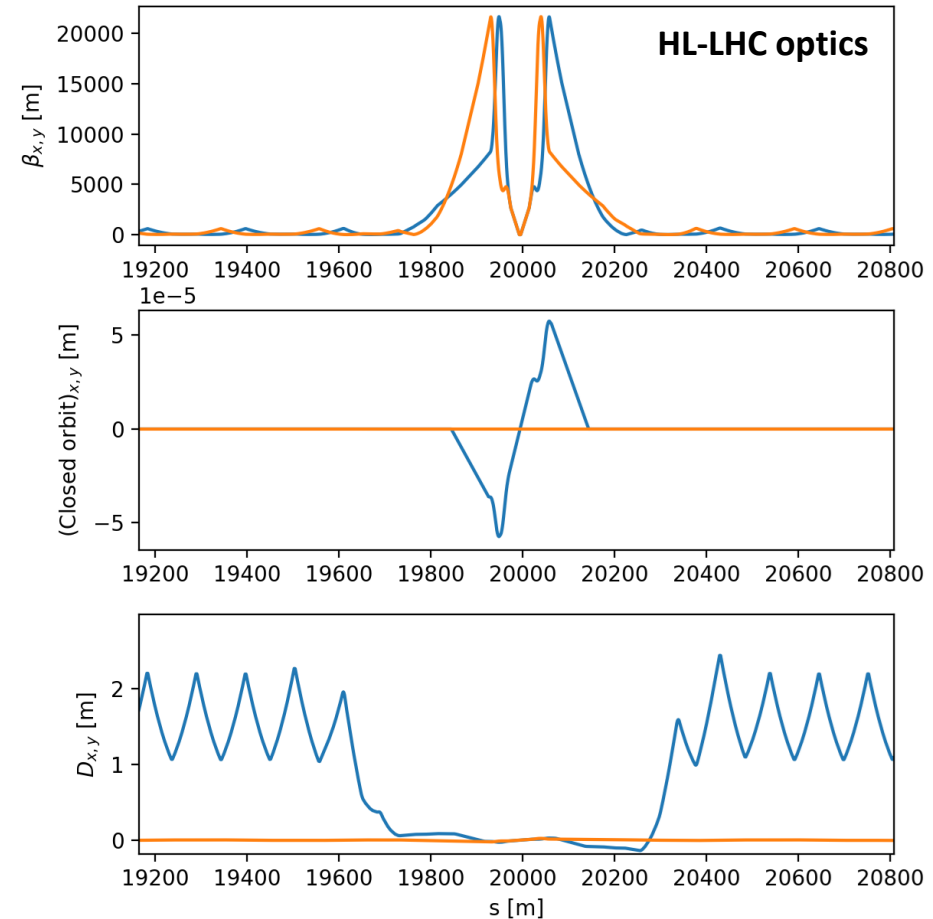


$$q_x = 0.31000 \quad q_y = 0.32000$$

$$Q'_x = 2.00 \quad Q'_y = 2.00 \quad \gamma_{tr} = 53.57$$

Computation of **Twiss parameters based on the tracking** has **two main advantages**:

- Any **physical model included in the tracking** is **automatically usable in Twiss**
 - Without additional development effort
- Twiss becomes a **powerful diagnostics tool** on the built **tracking model**
 - Allows **measuring directly on the tracking model** tunes, chromaticities, closed orbit, beta functions, etc.
 - Can be done **effortlessly** and **without exporting or manipulating the model**.
 - **Used daily** to for validating simulation models, catching mistakes, investigating issues



Accuracy compared to MAD-X: $\Delta\beta / \beta \ll 10^{-4}$
Computation time is very similar

```
In [37]: tw.bety[0] # xsuite
Out[37]: 149.4305507849305

In [38]: mad.table.twiss.bety[0] # madx
Out[38]: 149.43055000962505

In [39]: t_mad_ms
Out[39]: 202.0

In [40]: t_xsuite_ms
Out[40]: 185.0
```

Example