



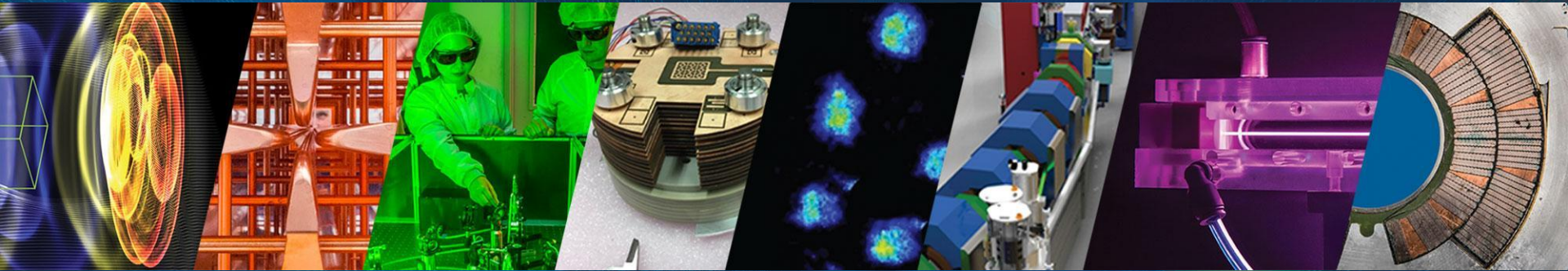
New simulation tools for beam-beam collisions at the interaction point

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FCC Week 2024
San Francisco, 13th June

ACCELERATOR TECHNOLOGY &
APPLIED PHYSICS DIVISION



U.S. DEPARTMENT OF
ENERGY

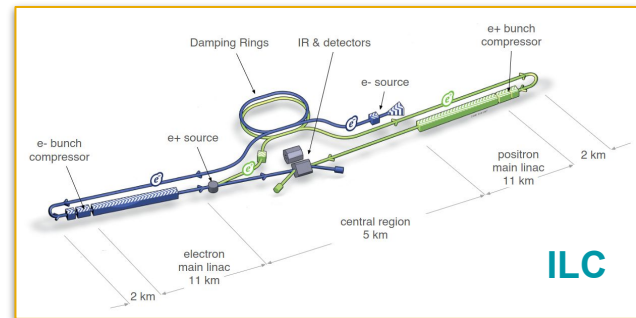
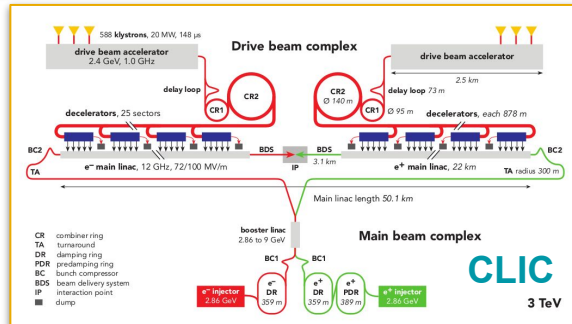
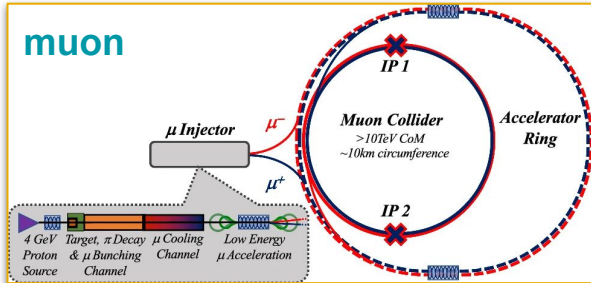
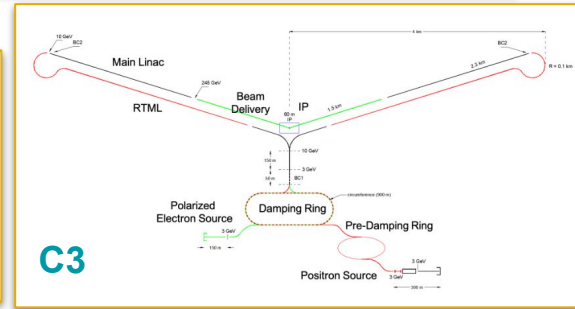
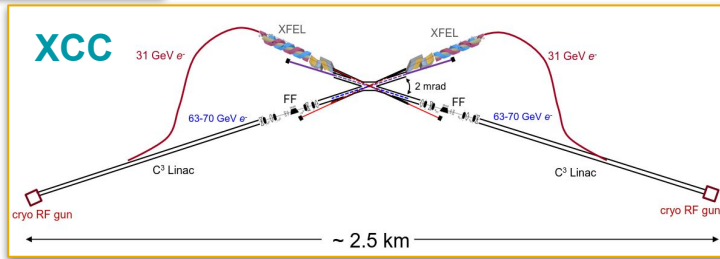
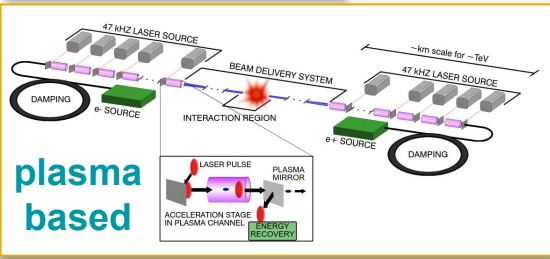
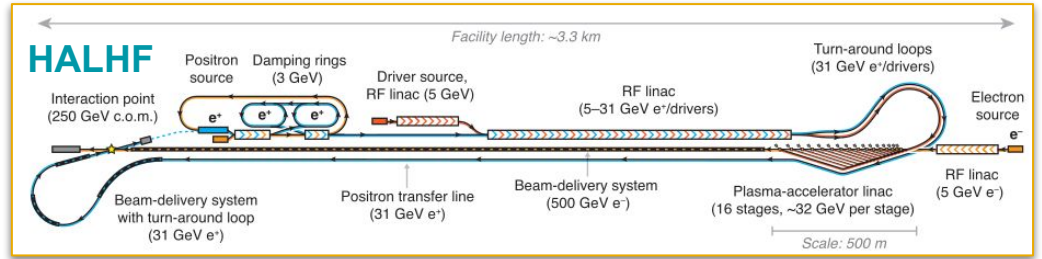
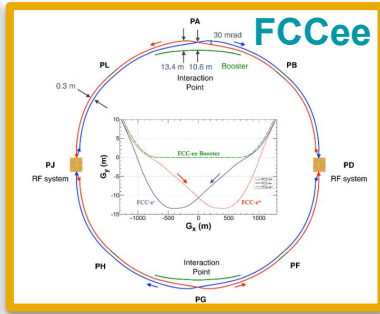
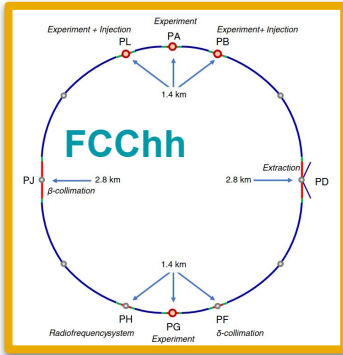
Office of
Science



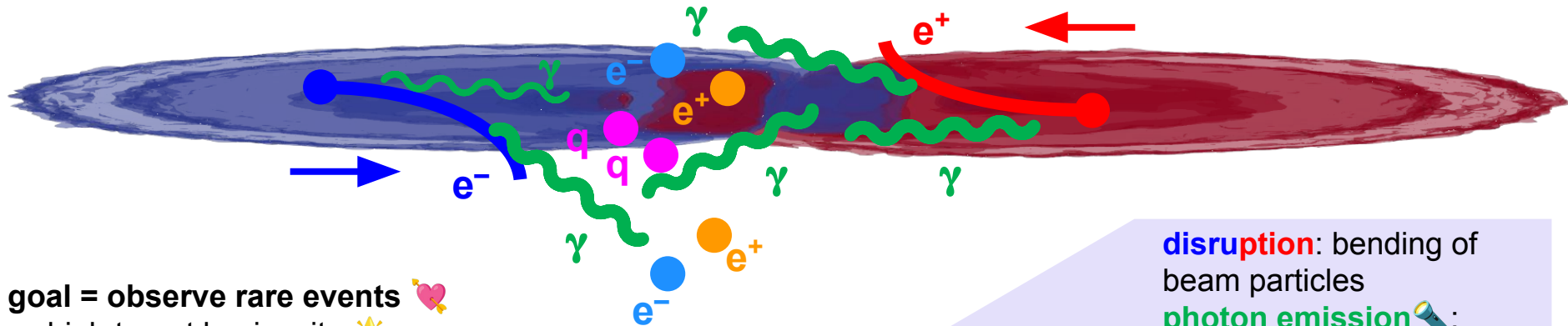
NATIONAL
ACCELERATOR
LABORATORY



There are many designs & ideas for future Higgs factories and 10 TeV colliders



A key challenge is mitigating or embracing beam-beam effects



goal = observe rare events 🍷

- high target luminosity 🌟
- need to squeeze the beams 🍊
- very high EM fields 😱
- **beam-beam effects** 😡: incoherent & collective
- **luminosity different from target value** 🤔

disruption: bending of beam particles

photon emission 🔦:

- beamstrahlung
- bremsstrahlung

pair creation 🐱🐱:

- nonlinear Breit-Wheeler
- linear Breit-Wheeler
- Bethe-Heitler
- Landau-Lifshitz

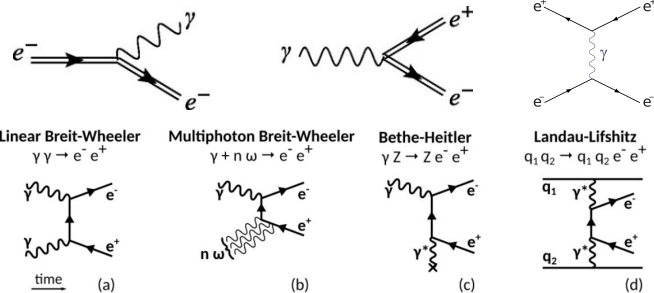
scattering

- Compton
- Bhabha

hadron photoproduction

...

💡 **accurate modeling to control these effects!** 🎯 🐘



Linear Breit-Wheeler
 $\gamma\gamma \rightarrow e^-e^+$

Multiphoton Breit-Wheeler
 $\gamma + n\omega \rightarrow e^-e^+$

Bethe-Heitler
 $\gamma Z \rightarrow Z e^-e^+$

Landau-Lifshitz
 $q_1 q_2 \rightarrow q_1 q_2 e^-e^+$

time (a) (b) (c) (d)

Particle-In-Cell + Monte Carlo simulations are the main modeling tools

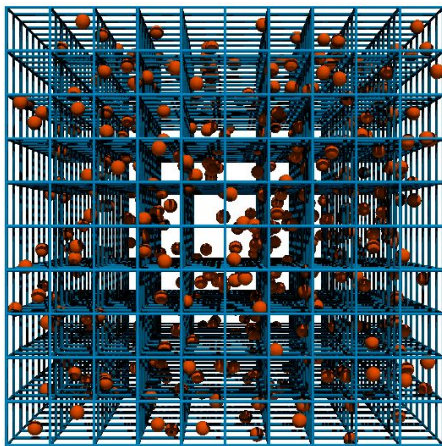
ab initio approach

fields on a grid

$$\begin{cases} \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \times \mathbf{B} = \frac{1}{c^2} \frac{\partial \mathbf{E}}{\partial t} + \mu_0 \mathbf{J} \end{cases}$$

interpolate fields at particles' positions
 $\mathbf{E}, \mathbf{B} \rightarrow \mathbf{E}_p, \mathbf{B}_p$

QED, ionization,
collisions, reactions, ...



project current densities on the grid
 $\mathbf{x}_p, \mathbf{p}_p \rightarrow \mathbf{J}$

macroparticles motion

$$\begin{cases} \frac{d\mathbf{x}_p}{dt} = \mathbf{v}_p \\ \frac{d\mathbf{p}_p}{dt} = q(\mathbf{E}_p + \mathbf{v}_p \times \mathbf{B}_p) \end{cases}$$

The community needs new tools that can provide long term support and vision

PIC codes specific to strong-strong beam-beam collisions

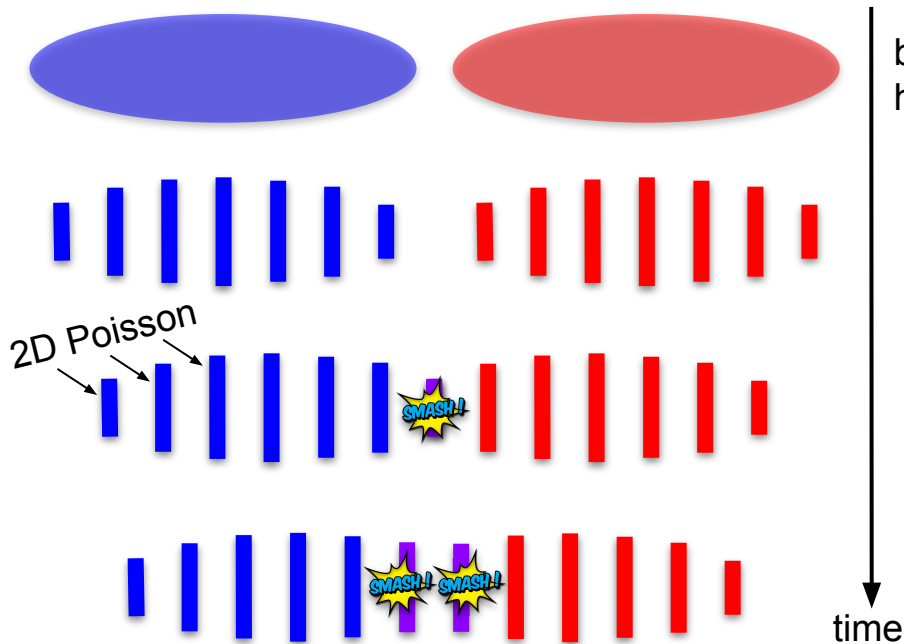
GUINEA-PIG

CAIN

<https://gitlab.cern.ch/clic-software/guinea-pig>

<https://github.com/slaclab/CAIN>

beams are sliced along z
the slices interact subsequently



both codes are well-established in the collider community, however:

- serial
- poorly maintained: no active developer
- poorly adaptable: algorithms, initial condition
- limited diagnostics
- **lack of self-consistency** (pair plasmas @ 10 TeV)
- **corrections will be required** (rates of QED at $\chi > 50$)

WarpX, part of the BLAST toolkit, is a promising candidate for beam-beam studies

<https://ecp-warpX.github.io/>

open-source

OS portable: Linux, MacOS, Windows,

GPU portable: NVIDIA, AMD, Intel

multi-platform: multi-CPU/GPUs

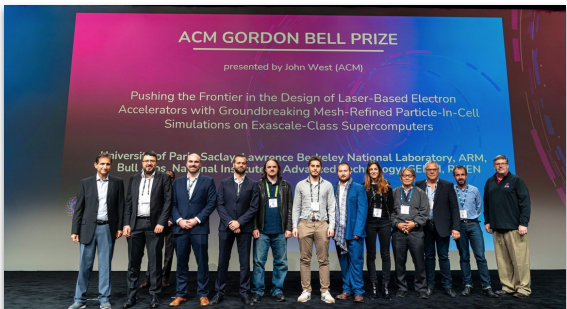
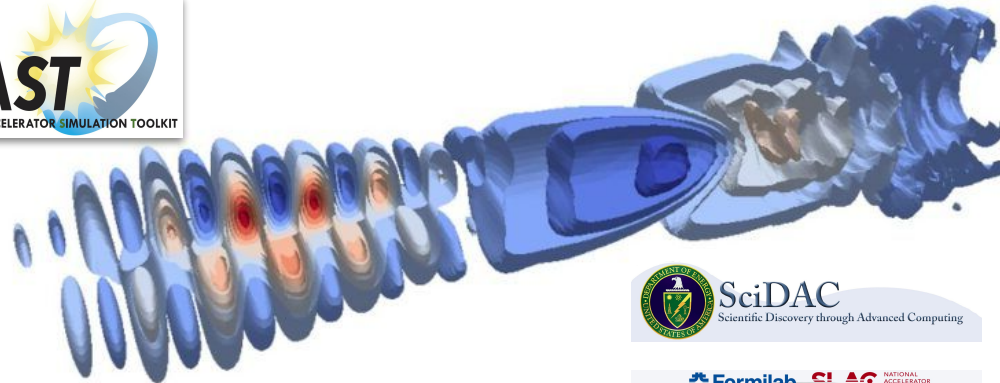
flexible:

- different geometries: 1D, 2D, RZ, 3D
- many algorithms
- many diagnostics
- electromagnetic, electrostatic, magnetostatic

versatile:

- plasma-based accelerators
- RF accelerators
- fusion devices
- laser-plasma interactions
- astrophysics
- ...

international, cross-disciplinary & active community!
WELL DOCUMENTED!!!!!!



We have a poster about BLAST this evening!

Our main goal: establish WarpX as a next-gen tool in the collider community

OUTLINE

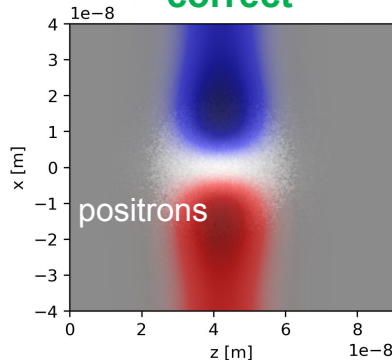
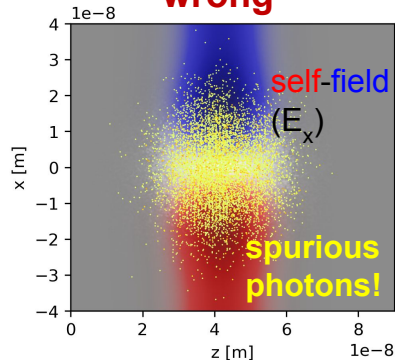
- numerical challenges 🏔️
- benchmarks ✅
- performances 🏃
- preliminary results
- conclusions & next steps 🏁

The numerical algorithms and resolution matter

single spherical bunch of left-propagating positrons

wrong[†]

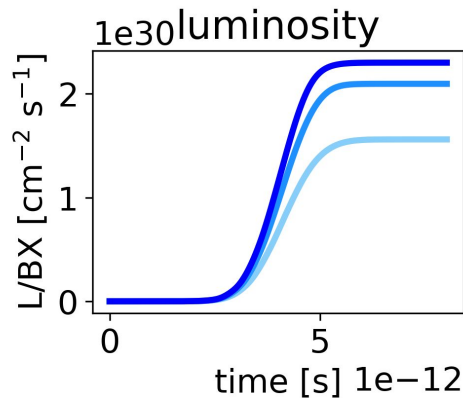
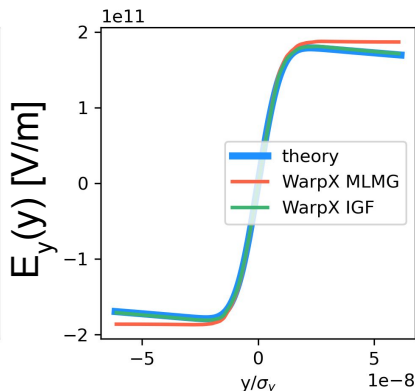
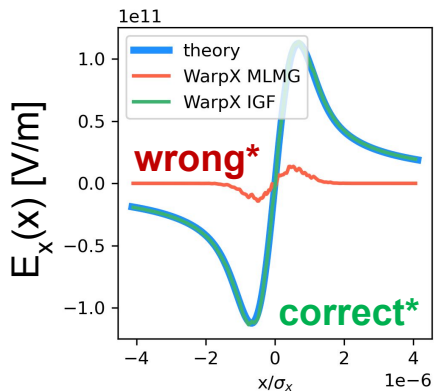
correct[†]



[†] Yee solver with PEC BCs

[†] iterative nodal solver with PEC BCs

self-field of a flat beam



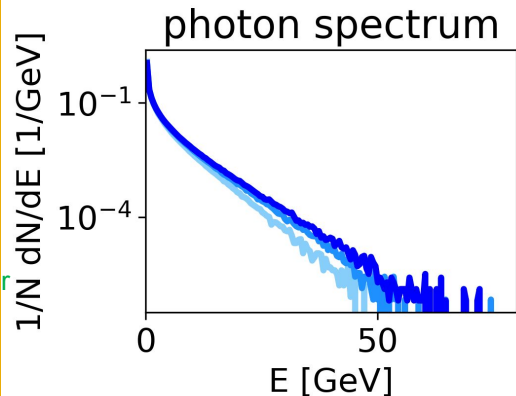
higher res

256 x 256 x 512

128 x 128 x 256

64 x 64 x 128

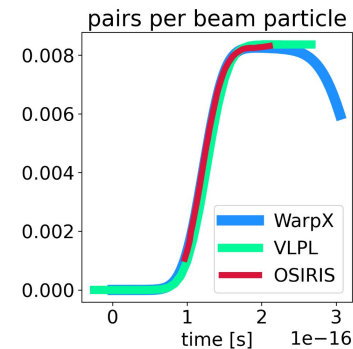
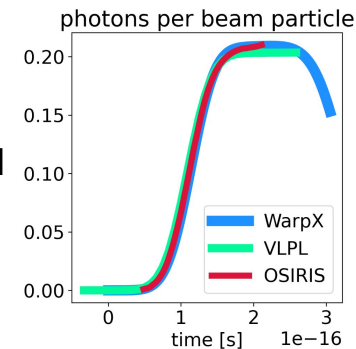
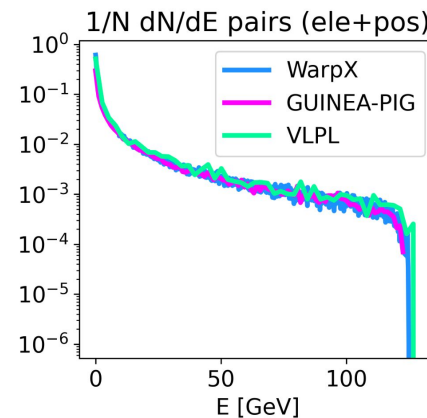
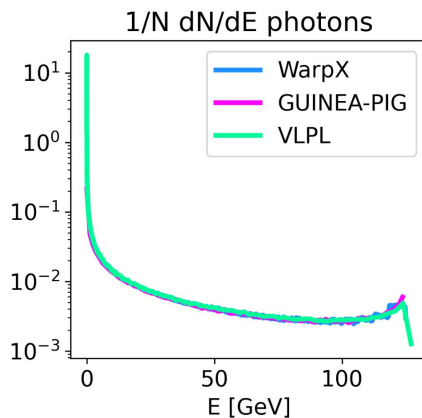
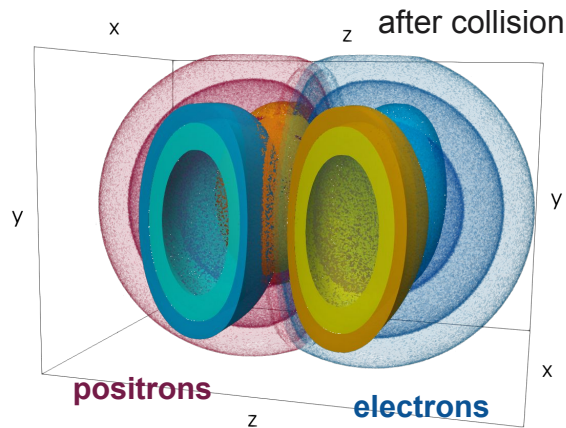
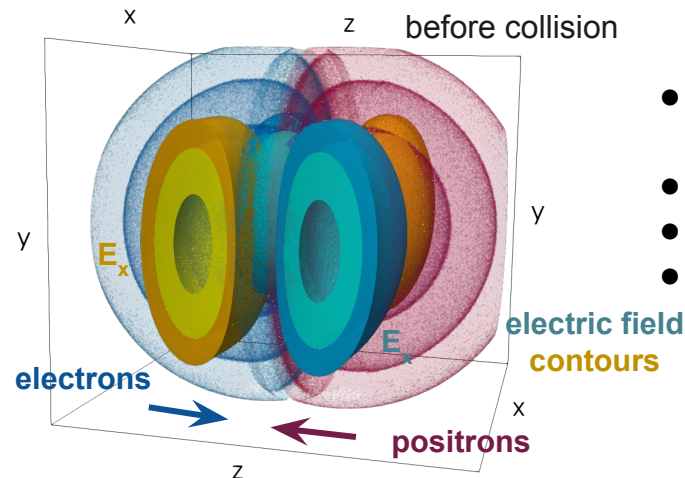
lower res



Excellent agreement between several codes with spherical ultra-tight beams

Yakimenko et al. PRL 2019

- main parameters:
 $E_{\text{COM}} = 250 \text{ GeV} \mid N = 8.7 \cdot 10^8 \mid \sigma_z = \sigma_x = \sigma_y = 10 \text{ nm}$
- significant generation of coherent pairs
- low disruption $D = 0.001$
- spherical beams \rightarrow “convenient” for “traditional” PIC simulations since the domain is not stretched (as in flat beams)



Excellent agreement with flat ILC beams

main parameters

[The International Linear Collider:
Report to Snowmass 2021](#)

- $E_{\text{COM}} = 250 \text{ GeV}$
- $N = 2 \cdot 10^{10}$
- $\sigma_z^* = 300 \text{ }\mu\text{m}$
- $\sigma_x^* = 516 \text{ nm}$
- $\sigma_y^* = 7.7 \text{ nm}$
- $\epsilon_x = 5 \text{ }\mu\text{m}$
- $\epsilon_y = 35 \text{ nm}$

magnetic field
streamlines

electron
density

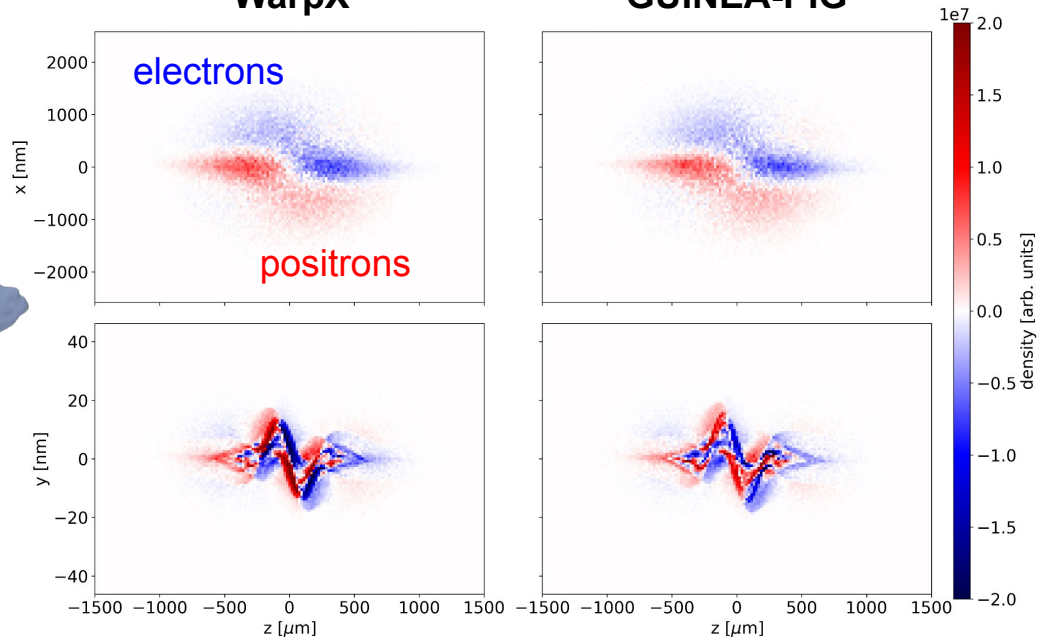
positron
density

- flat beams
- significant disruption $D_x = 0.30$, $D_y = 24.39$
- negligible coherent pairs

snapshot of the beams' **density integrated along the missing coordinate** during collision

WarpX

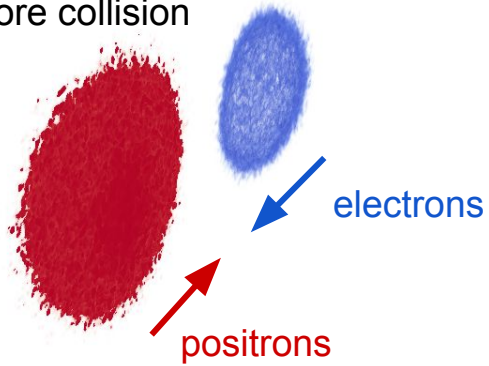
GUINEA-PIG



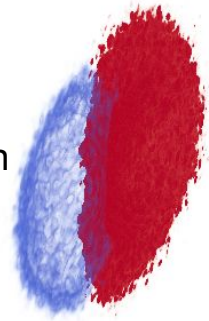
offsets along x and $y \sim \sigma_{x,y}/10$ to induce the kink instability and mitigate stochastic discrepancies

Excellent agreement with flat asymmetric HALHF beams

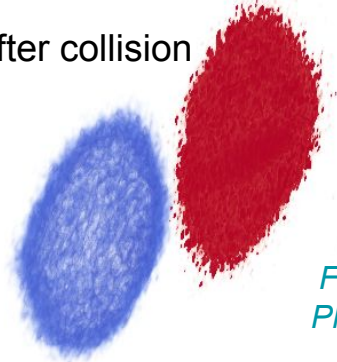
before collision



during collision



after collision



Foster et al. New Journal of Physics 25.9 (2023): 093037

electrons

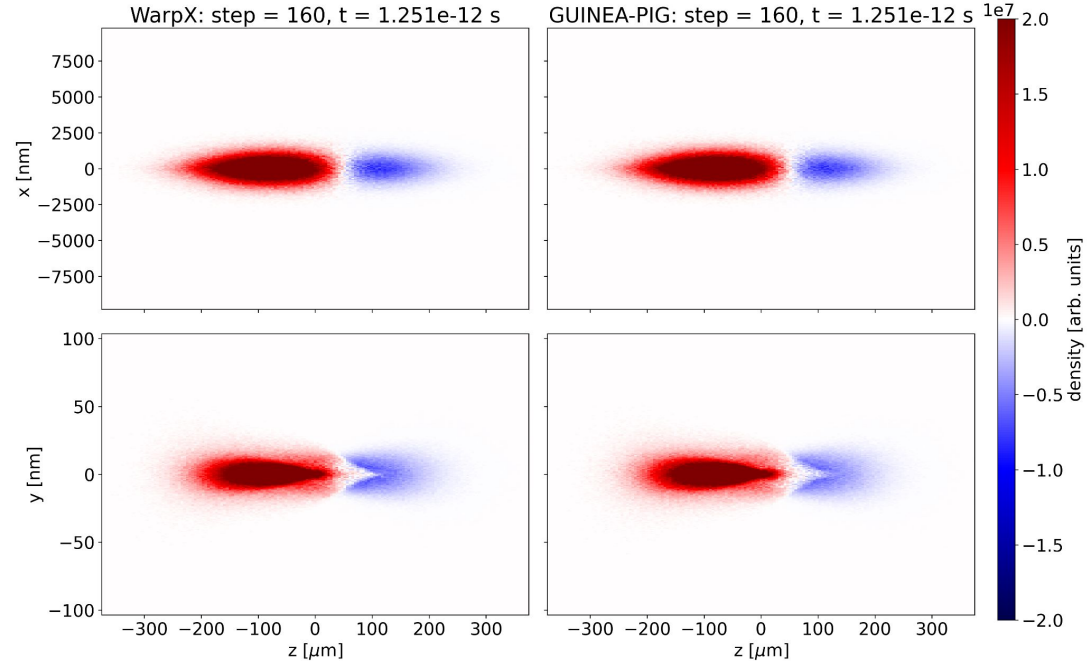
- $E = 500 \text{ GeV}$
- $N = 10^{10}$
- $\epsilon_x = 160 \text{ } \mu\text{m}$
- $\epsilon_y = 560 \text{ nm}$

positrons

- $E = 31.25 \text{ GeV}$
- $N = 4 \times 10^{10}$
- $\epsilon_x = 10 \text{ } \mu\text{m}$
- $\epsilon_y = 35 \text{ nm}$

both

- $E_{\text{COM}} = 250 \text{ GeV}$
- $\sigma_z^* = 75 \text{ } \mu\text{m}$
- $\sigma_x^* = 729 \text{ nm}$
- $\sigma_y^* = 7.7 \text{ nm}$



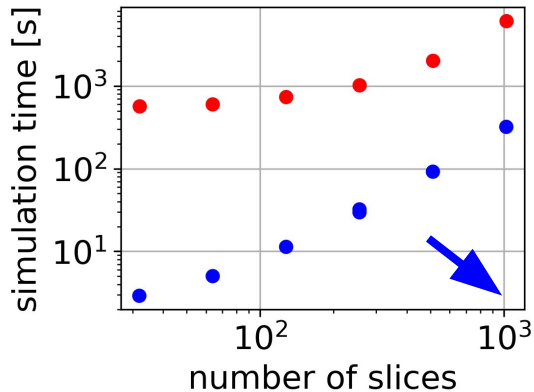
WarpX can be faster and/or go to higher resolution and statistics

GUINEA-PIG
(serial!!)

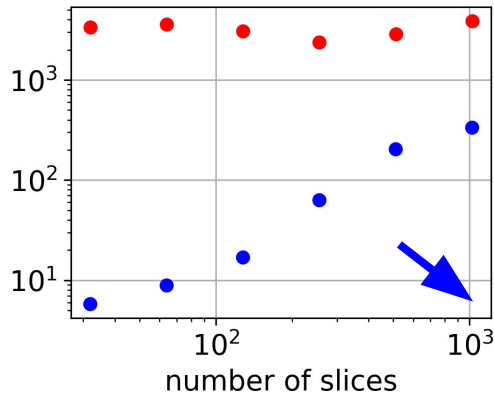


WarpX
on 1 GPU

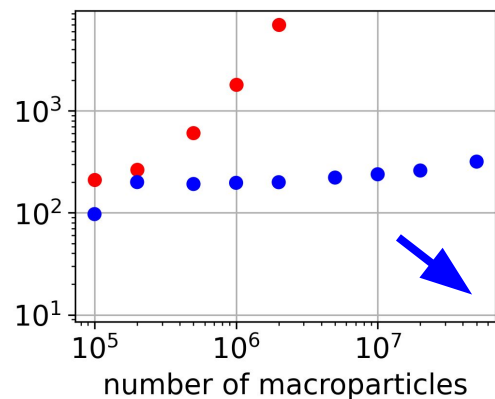
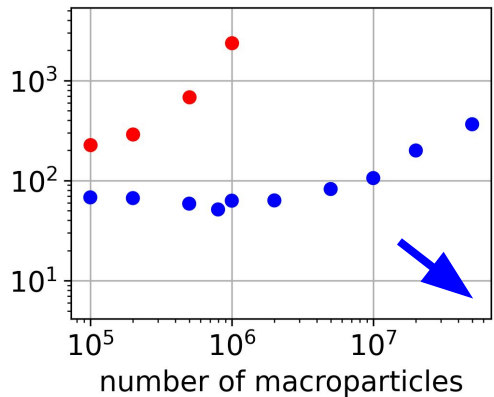
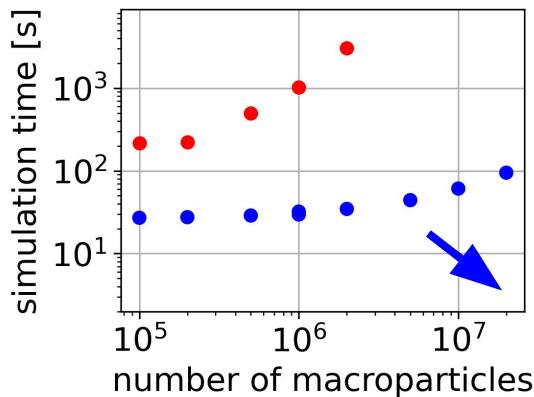
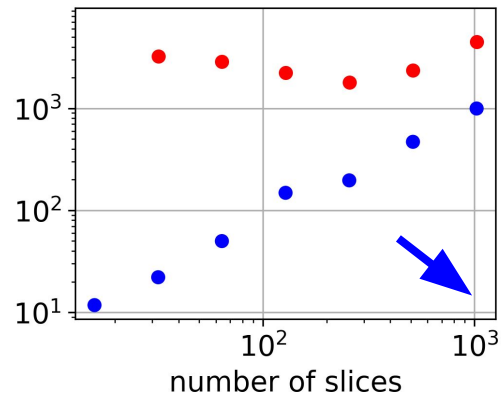
spherical ultra-tight



flat ILC

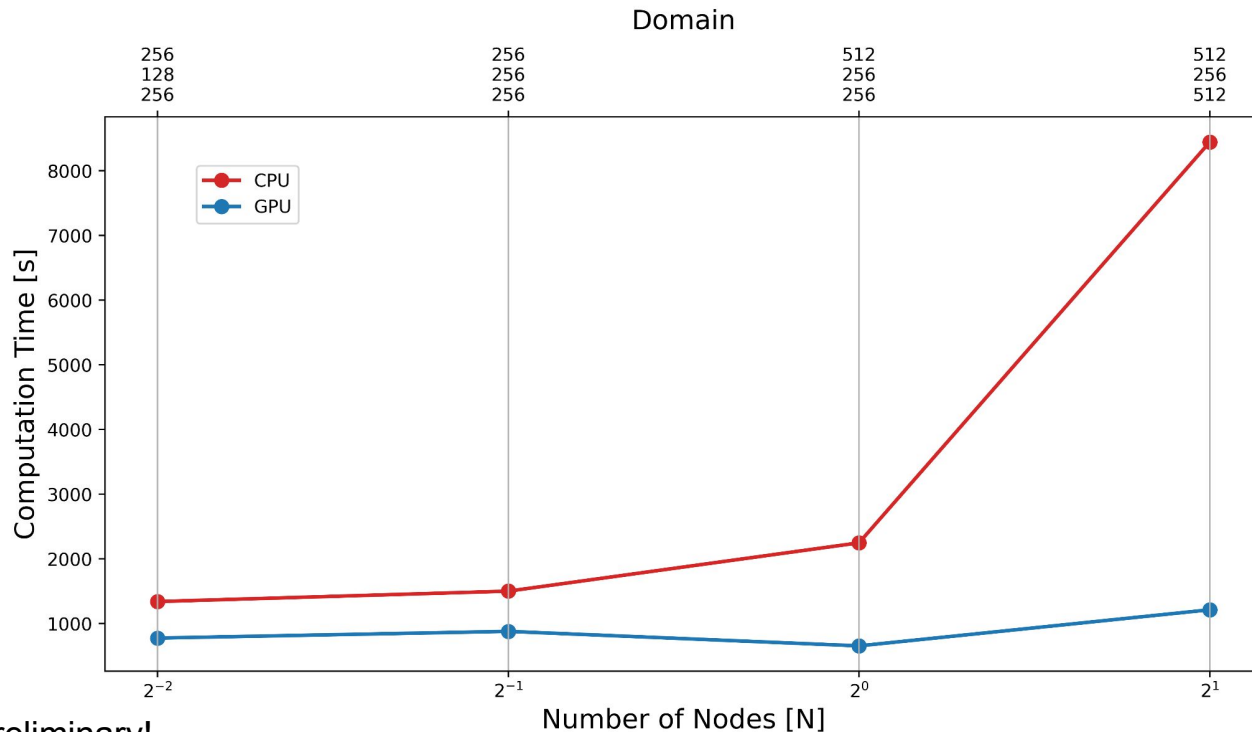


asymmetric HALHF



We are working to guarantee good performances on multiple GPUs

flat ILC beams on Perlmutter @ NERSC



preliminary!

1 CPU node = 128
cores AMD Milan

1 GPU node =
4 NVIDIA A100



National Energy Research
Scientific Computing Center

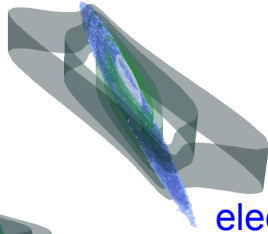
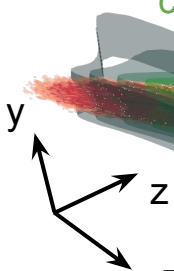
heFFTe

Highly Efficient FFTs
for Exascale

Preliminary simulations with FCC-ee Z beams & 10 TeV plasma-based beams

before collision

magnetic field contours

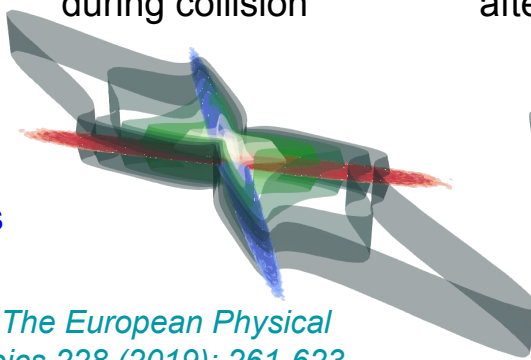


electrons

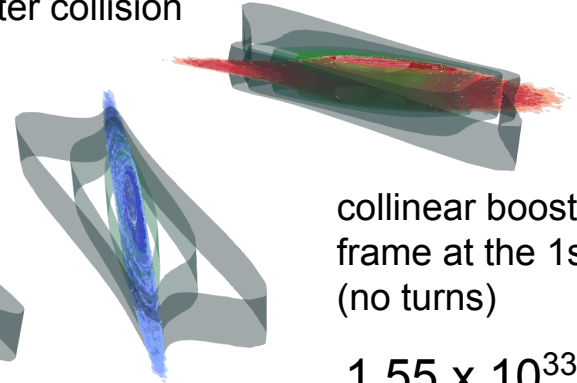
positrons

FCC collaboration, *The European Physical Journal Special Topics* 228 (2019): 261-623.

during collision



after collision



collinear boosted frame at the 1st IP (no turns)

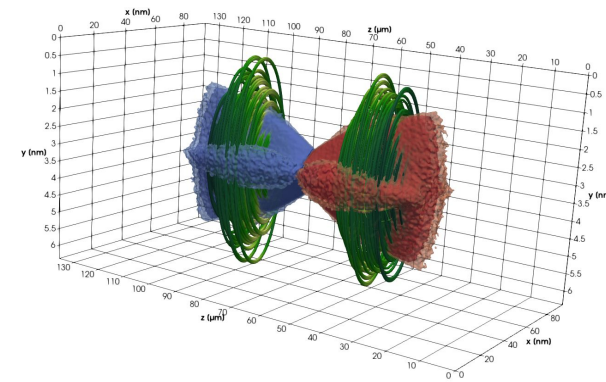
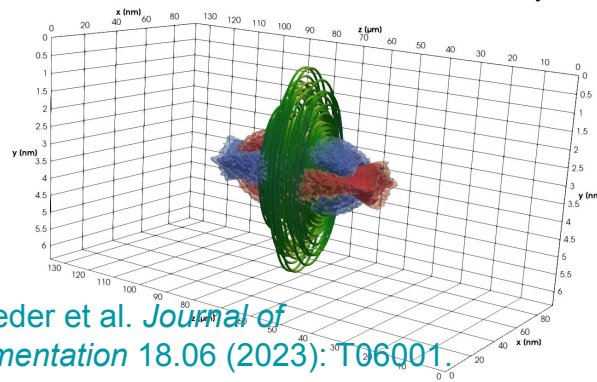
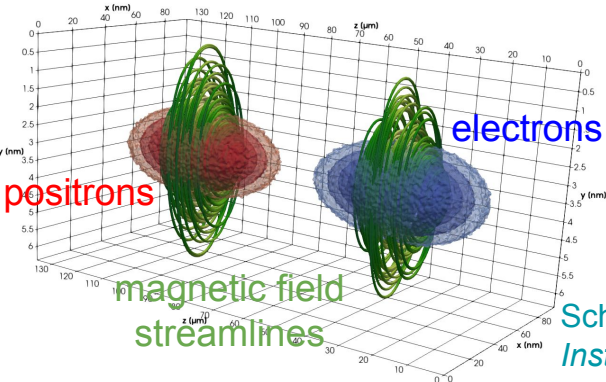
$$E_{\text{COM}} = 45.6 \text{ GeV} \mid N = 1.7 \cdot 10^{11} \mid \sigma_z = 3.5 \text{ mm} \mid \sigma_x^* = 6.36 \text{ } \mu\text{m} \mid \sigma_y^* = 28.3 \text{ nm}$$

$$E_{\text{COM}} = 10 \text{ TeV} \mid N = 1.2 \cdot 10^9 \mid \sigma_z = 8.5 \text{ mm} \mid \sigma_x^* = 6 \text{ nm} \mid \sigma_y^* = 0.4 \text{ nm}$$

L/BX

$$1.55 \cdot 10^{33} \text{ m}^{-2}$$

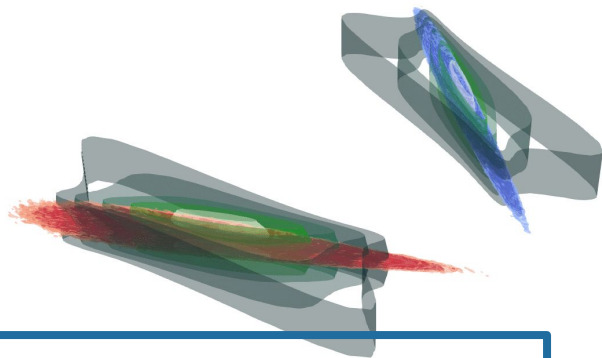
$$8.84 \cdot 10^{34} \text{ m}^{-2}$$



Schroeder et al. *Journal of Instrumentation* 18.06 (2023): T06Q01.

Conclusions and next steps




We are working to make WarpX a next-gen code for next-gen colliders




Goal

establish WarpX as a modern high-performance tool in the extended collider community

Outline




- numerical challenges 
- benchmarks 
- performances 
- preliminary results

Two main takeaways

 WarpX agrees well with GUINEA-PIG under very different parameters

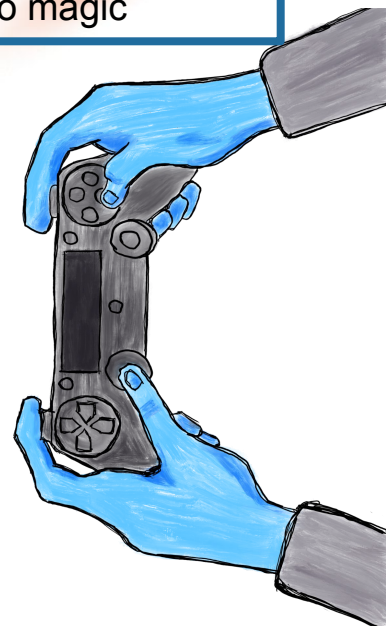
 WarpX can be much faster than GUINEA-PIG

Next steps

add missing physics
 more benchmarks
  do magic

Open discussions

- what are the modeling needs of the FCC & other communities?
- how can we work synergistically with/on different tools?



Thank you for your time :)

