

**MATTER**

Roni Koitermaa<sup>1, 2 a</sup>  
 Marzhan Toktaganova<sup>1</sup>  
 Flyura Djurabekova<sup>1</sup>  
 Andreas Kyritsakis<sup>1, 2</sup>  
 Tauno Tiirats<sup>2</sup>  
 Veronika Zadin<sup>2</sup>

<sup>1</sup>University of Helsinki

<sup>2</sup>University of Tartu

<sup>a</sup>roni.koitermaa@helsinki.fi

# DEPENDENCE OF VACUUM ARC INITIATION DYNAMICS ON THE APPLICATION OF A STATIC MAGNETIC FIELD

## INTRODUCTION

Vacuum arcing presents technical challenges in applications where high electric fields are used, such as electron sources, particle accelerators and vacuum interrupters. New accelerator technologies such as the proposed **muon collider** can give rise to different arcing behavior compared to what has been observed previously.

The presence of a **magnetic field** can cause **focusing** of electron beams, which can lead to **heating** (figure 1). The ratio of the beam radius  $r$  and beam radius without magnetic field  $r_0$  can be obtained from theory:

$$\frac{r}{r_0} = \rho |\sin(\rho^{-1})|, \quad \rho = \frac{a}{B} \sqrt{\frac{E}{y}},$$

where  $a = 3.39 \times 10^{-3} \text{ V T}^{-1} \text{ nm}^{-1}$ ,  $E$  is electric field,  $B$  is magnetic field and  $y$  is position. By assuming the emitter shape, we can get an estimate for the beam radius  $r_0 = \sqrt{4\eta hy}$ , where  $h$  is the height of the emitter and  $\eta$  is the spreading factor. In figures 2a and 2b, we show the predicted beam radius and anode heat flux.

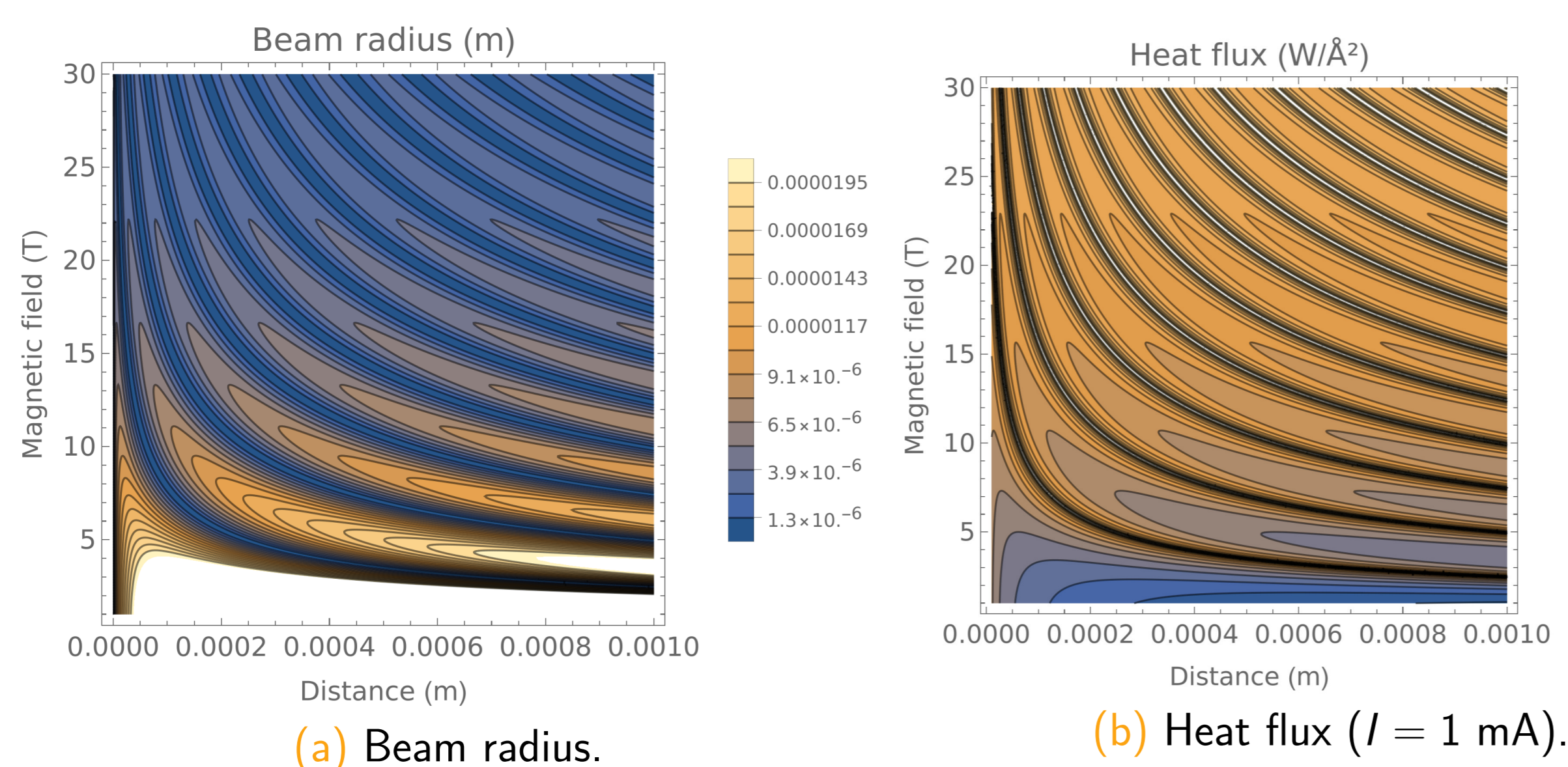


Figure 2: Theory predictions as a function of distance  $y$  and magnetic field  $B$ .

## METHODS

We use the *particle-in-cell* method to calculate trajectories of emitted electrons while including electron-electron interactions. The electrons experience acceleration due to the *Lorentz force*  $F = q_e(E + v \times B)$ . We use the FEMOCS code to perform these simulations in 3D. The applied voltage between the Cu cathode and anode is  $V_0 = 16 \text{ kV}$ , with a gap distance of  $300 \mu\text{m}$ . The macroscopic field is  $53 \text{ MV/m}$ , while the local field is  $9 \text{ GV/m}$ .

Current density at the anode is used to calculate heating, performed using COMSOL. In this model, we calculate a heat rate in the anode as  $P = V_0 j / z_d$ , where  $j$  is current density,  $V_0$  is the applied voltage and  $z_d$  is the electron CSDA depth in Cu. The top of the anode is assumed to be at a temperature of  $T_0 = 300 \text{ K}$ .

## RESULTS

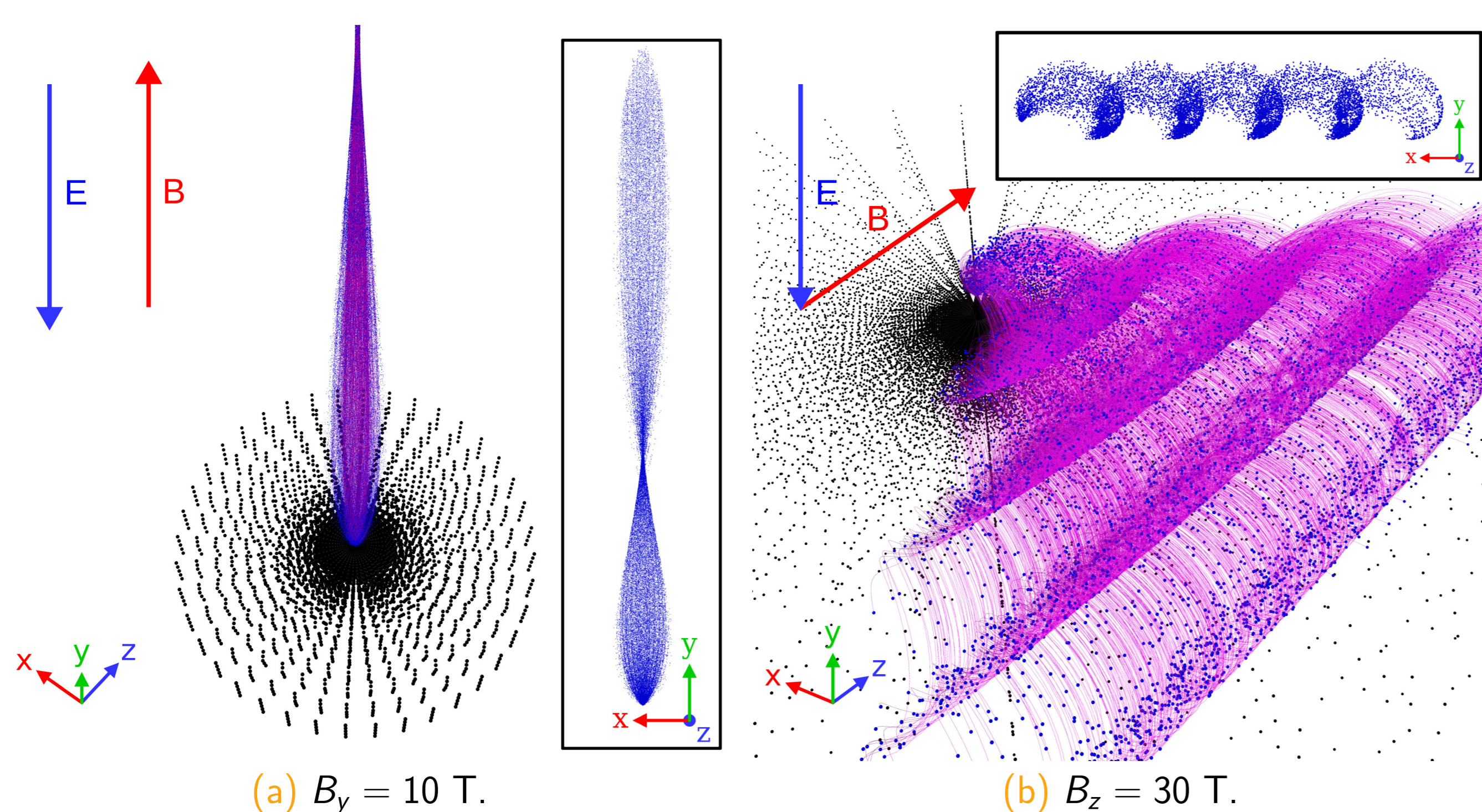
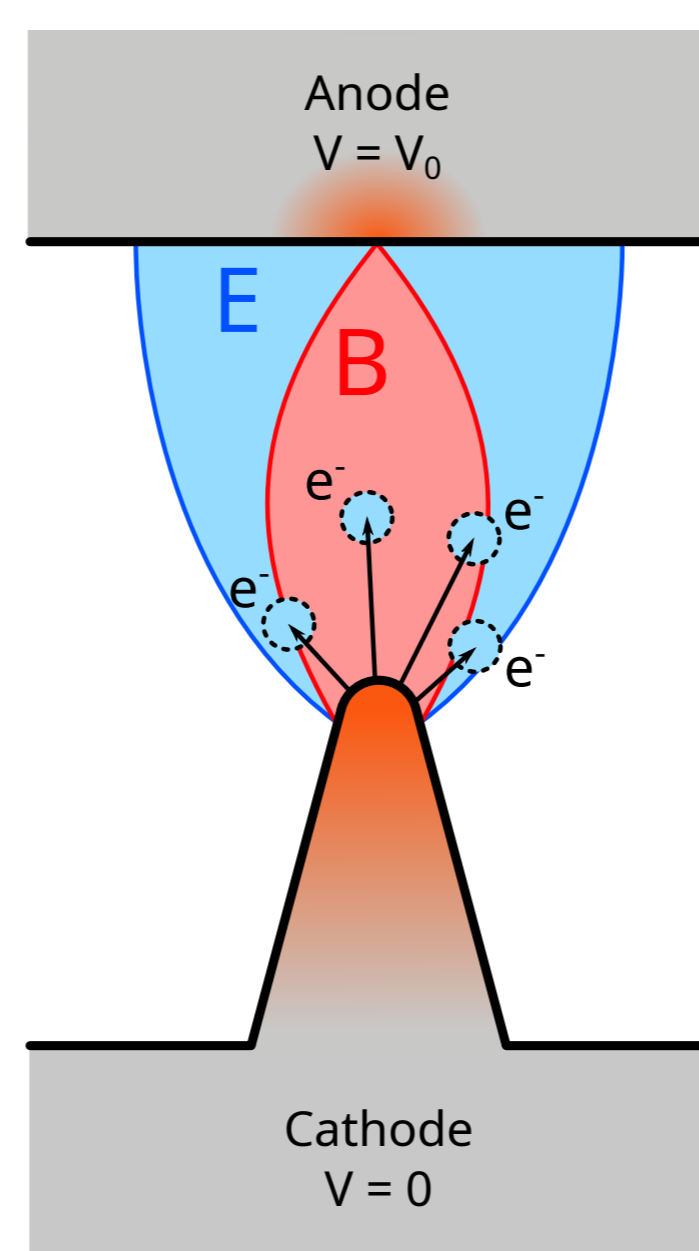


Figure 3: Electron paths in magnetic field.

We simulated two cases:

1. Magnetic field **parallel** with electric field  $B \parallel E$  (figure 3a)
2. Magnetic field **perpendicular** to electric field  $B \perp E$  (figure 3b)



(1) Figure 1: Beam with vs. without  $B$ .

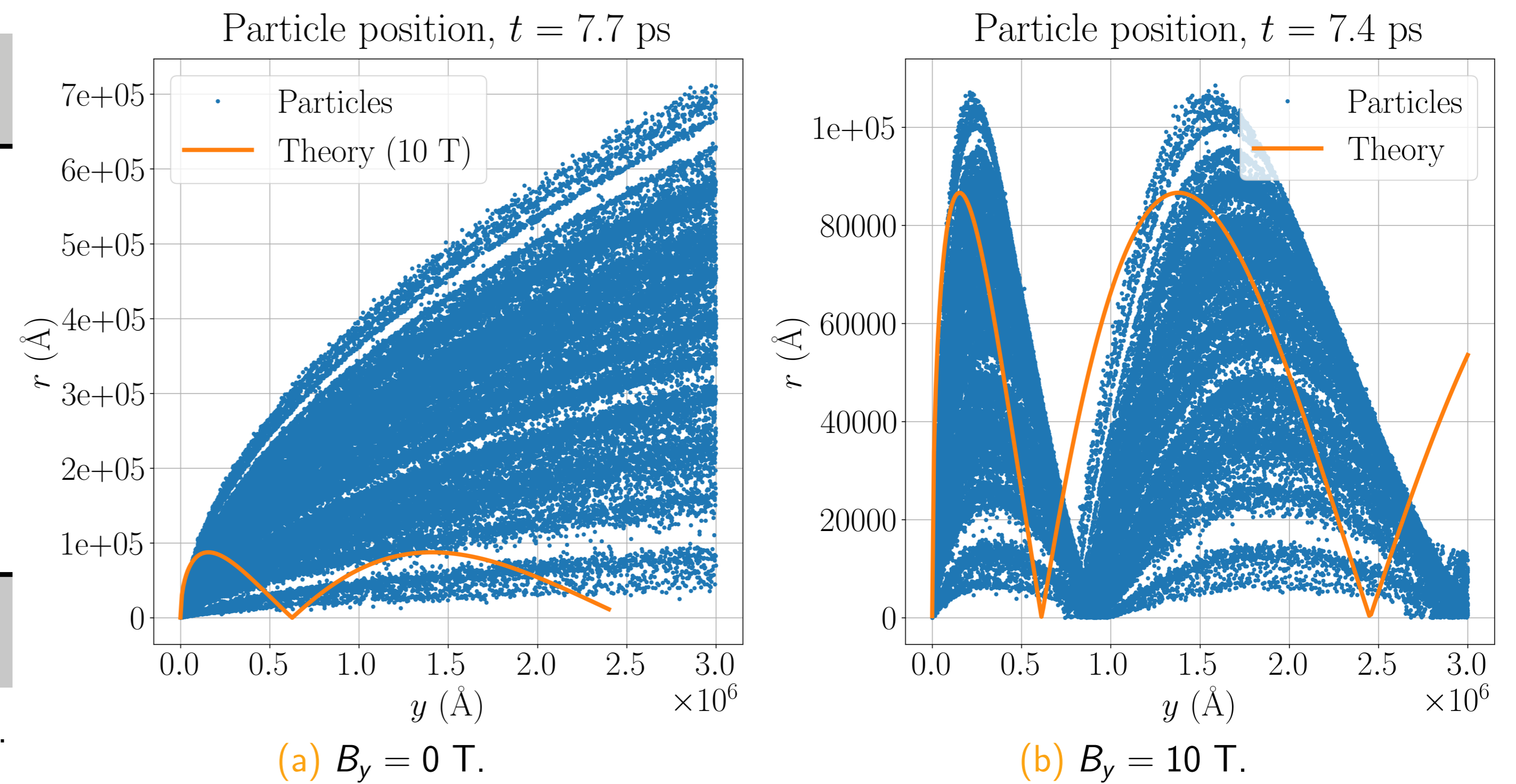


Figure 4: Electron beam shape.

The electron beam shape is plotted with the theoretical prediction at  $B_y = 10 \text{ T}$  (equation 1) in figures 4a–4b.

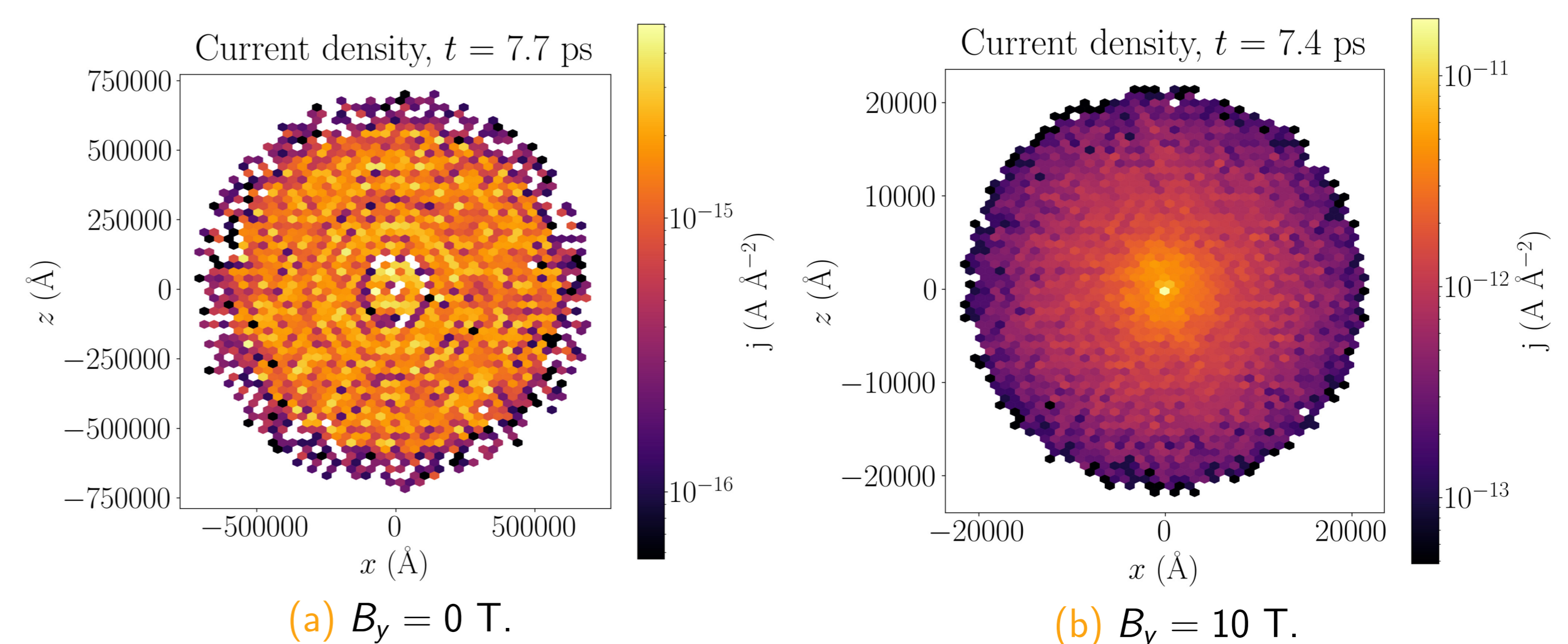


Figure 5: Current density on anode surface.

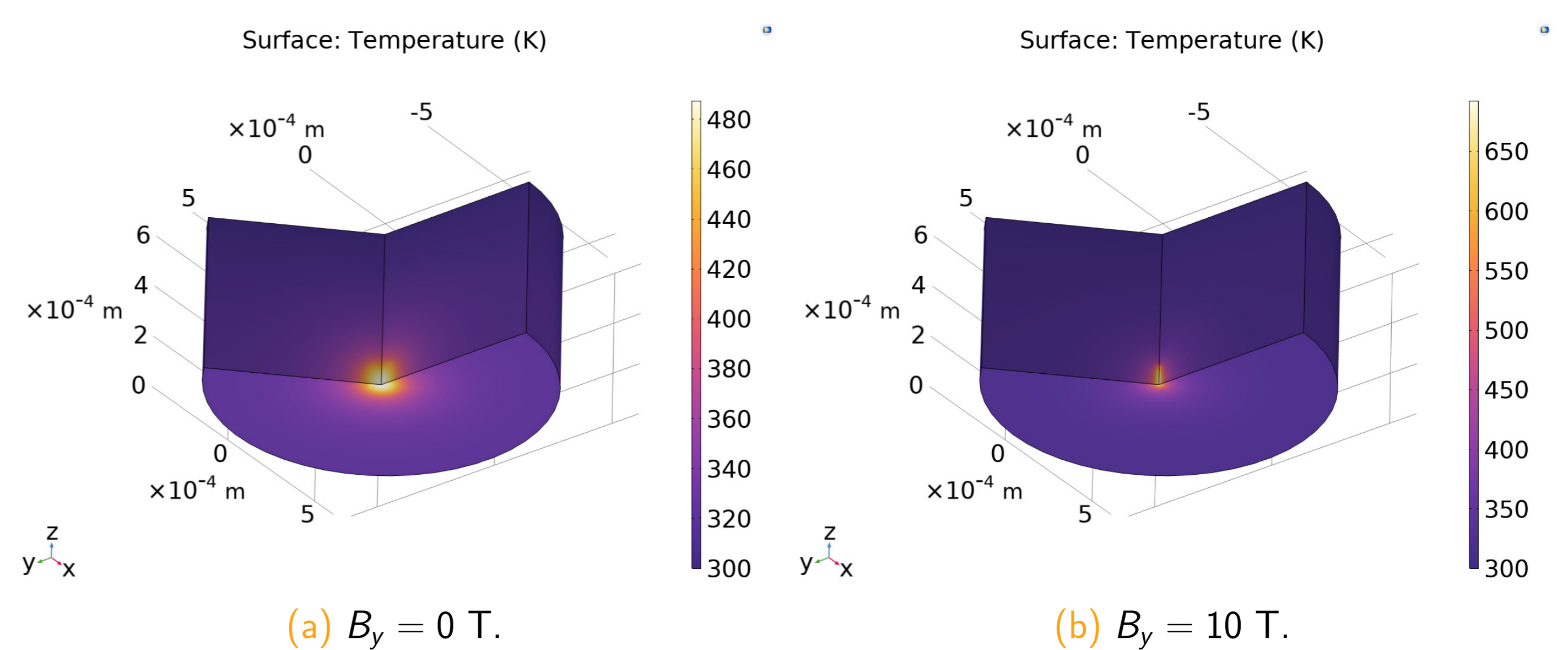


Figure 6: Anode temperature.

Based on the simulated current density (figures 5a–5b), we calculate the steady-state temperature distribution in the anode. This is done for the  $0 \text{ T}$  (figure 6a) and  $10 \text{ T}$  (figure 6b) cases.

We run additional simulations with varying anode spot size assuming a current of  $1 \text{ mA}$ . In figure 7, we can see that the average temperature at the anode spot reaches over  $1000 \text{ K}$  for a spot size of  $10 \mu\text{m}$ .

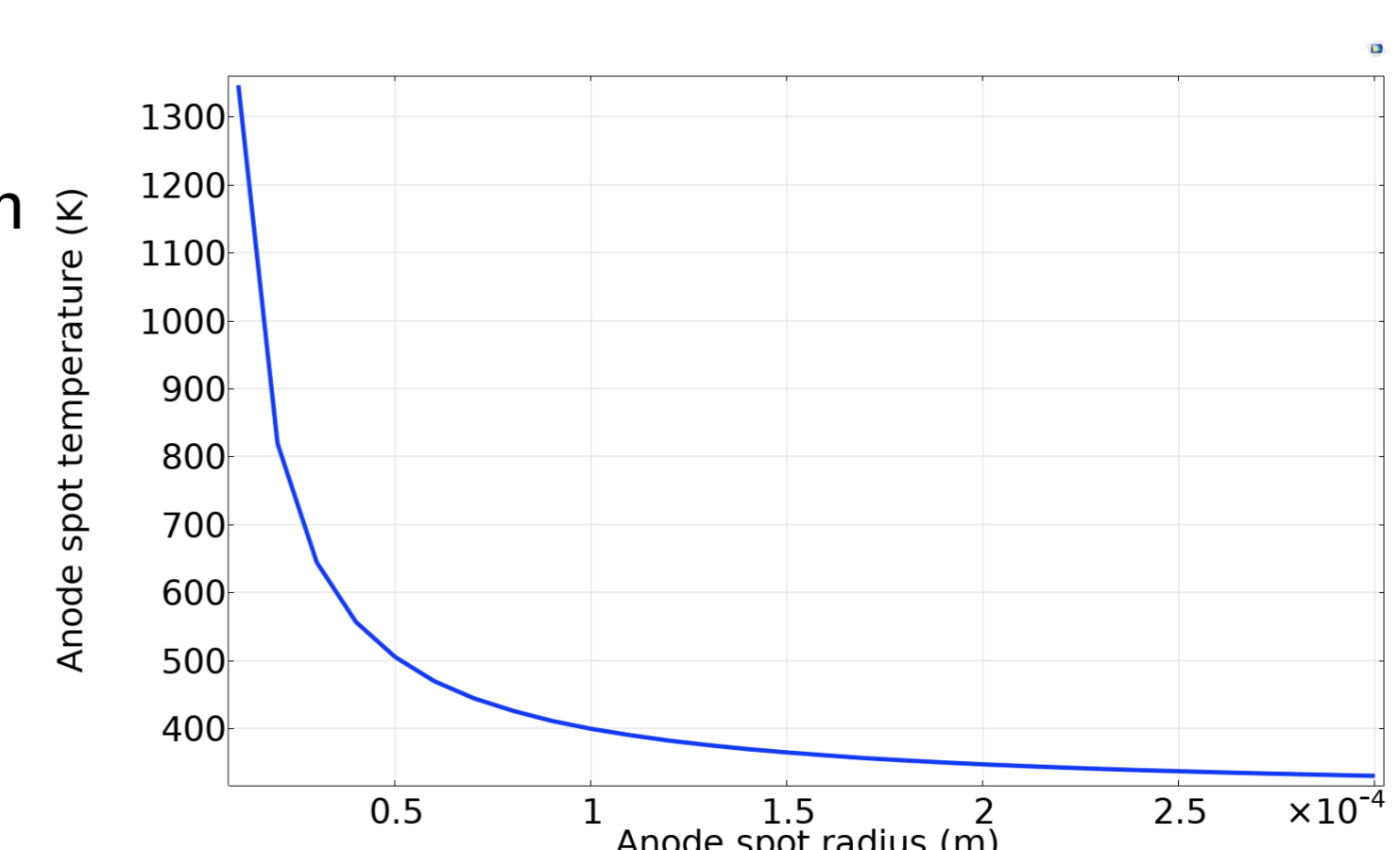


Figure 7: Dependence of anode temperature on heat spot radius,  $I = 1 \text{ mA}$ .

## CONCLUSIONS

The presence of **magnetic fields** ( $10 \text{ T}$ – $30 \text{ T}$ ) can significantly **focus** emitted electron beams and lead to **heating**. The temperature at the anode can reach as high as  $1000 \text{ K}$  or more, depending on the **current density** and **voltage**. This opens the possibility for anode-initiated vacuum arcs, as plasma could start forming on the anode side.

## ACKNOWLEDGEMENTS

RK, AK, TT and VZ are supported by the European Union's Horizon 2020 research and innovation program, under Grant Agreement No. 856705 (ERA Chair "MATTER") and by the Estonian Research Council's project RVT3 "CERN Science Consortium of Estonia". TT is supported by the Estonian Research Council Grant No. SJD61. RK is supported by the doctoral program MATRENA of the University of Helsinki.

