

# Accelerator Physics

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## A Short Introduction ... LOL

*In the end and after all ... : We try to explain the structure of  
“hadronic matter” in the universe.*

*In short words: “What is going on, up there ???”*

*Eine der wichtigsten Fragen in der Physik  
des 20ten Jahrhunderts:*

*Woraus besteht Goldfolie ?*



*naja, a bissi mehr wissenschaftlich:*

*woraus besteht Materie ??*

*oder noch besser ...*

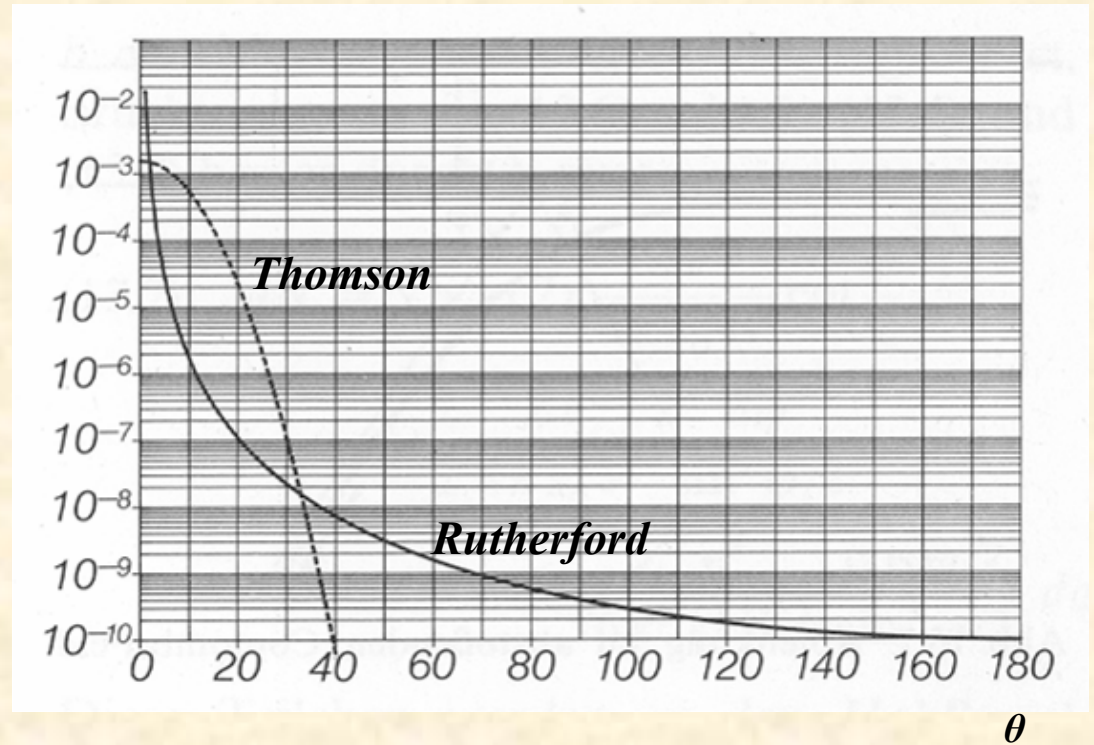
*wie sind positive und negative Ladungen  
in der Materie verteilt ???*



$$N(\theta) = \frac{N_i n t Z^2 e^4}{(\delta \pi \epsilon_0)^2 r^2 K^2} * \frac{1}{\sin^4(\theta / 2)}$$

**Rutherford Scattering, 1911**  
Using radioactive particle sources:  
 $\alpha$ -particles of some MeV energy

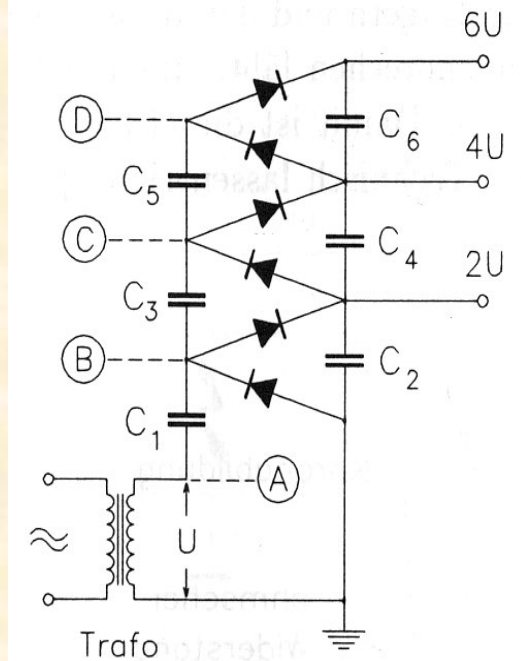
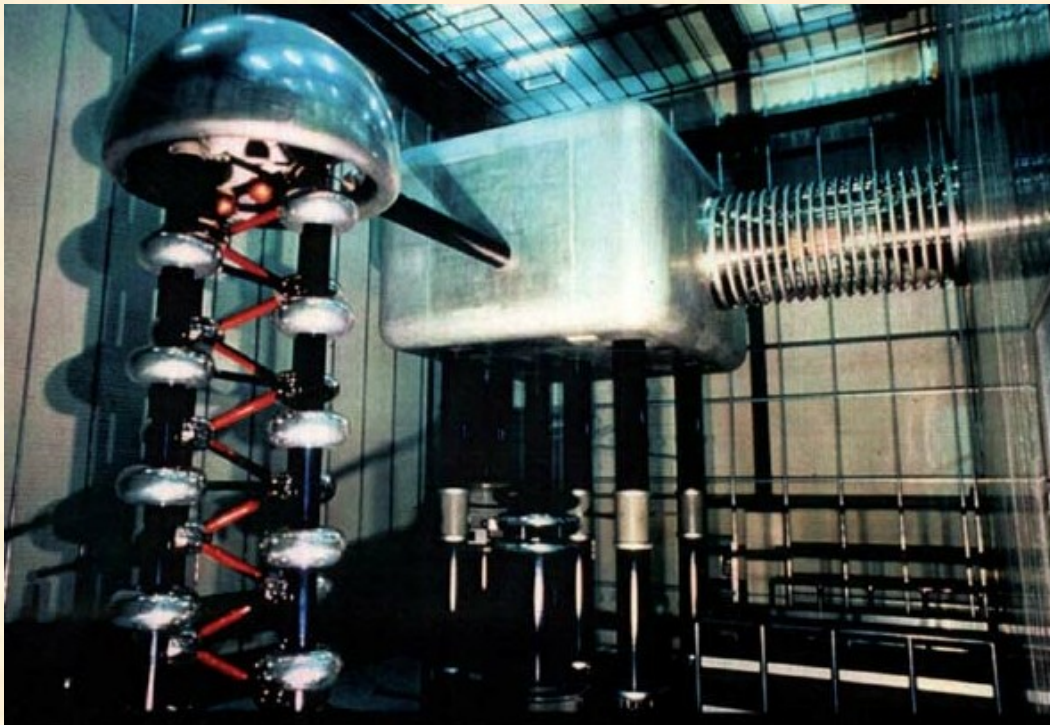
$N(\theta)$



# 1.) Electrostatic Machines: The Cockcroft-Walton Generator

**1928:** Encouraged by Rutherford Cockcroft and Walton start the design & construction of a high voltage generator to accelerate a proton beam

**1932:** First particle beam (protons) produced for nuclear reactions: splitting of Li-nuclei with a proton beam of 400 keV



**Particle source:** Hydrogen discharge tube on 400 kV level

**Accelerator:** evacuated glass tube

**Target:** Li-Foil on earth potential

**Technically:** rectifier circuit, built of capacitors and diodes (Greinacher)

**Problem:**

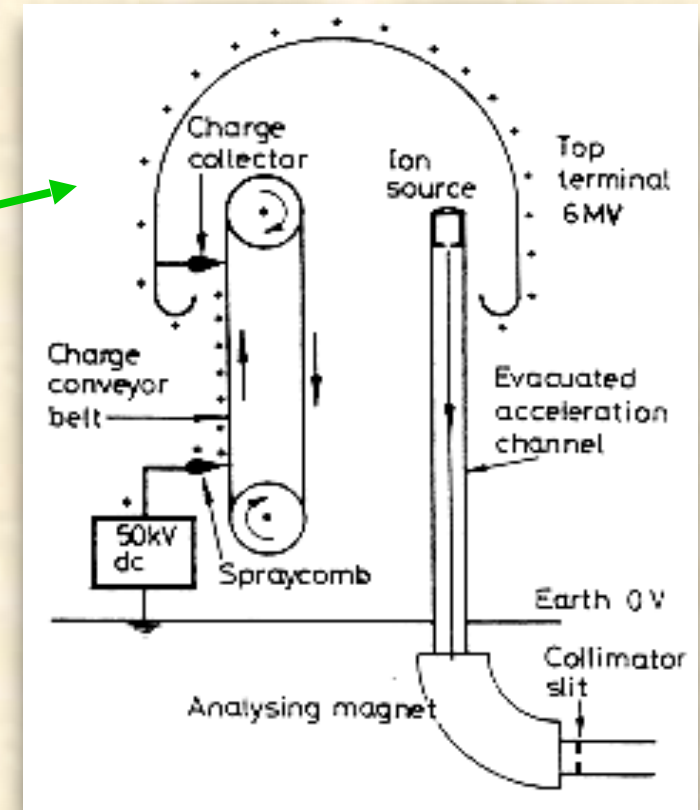
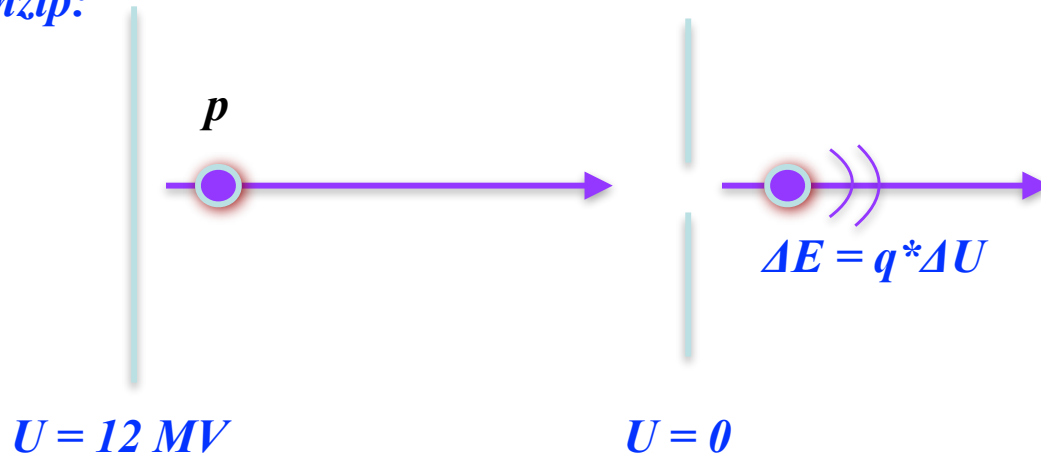
**DC Voltage can only be used once**

## 2.) Electrostatic Machines: van de Graaff Accelerator (1930 ...)

*creating high voltages by mechanical transport of charges*

\* **Terminal Potential:**  $U \approx 12 \dots 28 \text{ MV}$   
*using high pressure gas to suppress discharge ( $\text{SF}_6$ )*

**Das Prinzip:**



**Energie=Ladung \* Spannung  
(Differenz)**

**Problems:** \* Particle energy limited by high voltage discharges  
\* high voltage **can only be applied once per particle ...**  
**... or twice ?**

*The „Tandem principle“: Apply the accelerating voltage twice ...  
... by working with **negative ions (e.g. H<sup>-</sup>)** and  
**stripping the electrons** in the centre of the structure*

*Example for such a „steam engine“: 12 MV-Tandem van de Graaff  
Accelerator at MPI Heidelberg*



*Gretchen Frage (J.W. Goethe, Faust)*

*Fallen die Dinger eigentlich runter ?*

$$l_{vdG} = 30m$$

$$v \approx 10\% c \approx 3 \cdot 10^7 \text{ m/s}$$

$$\Delta t = 1\mu s$$

*Free Fall in Vacuum:*

$$s = \frac{1}{2}gt^2$$

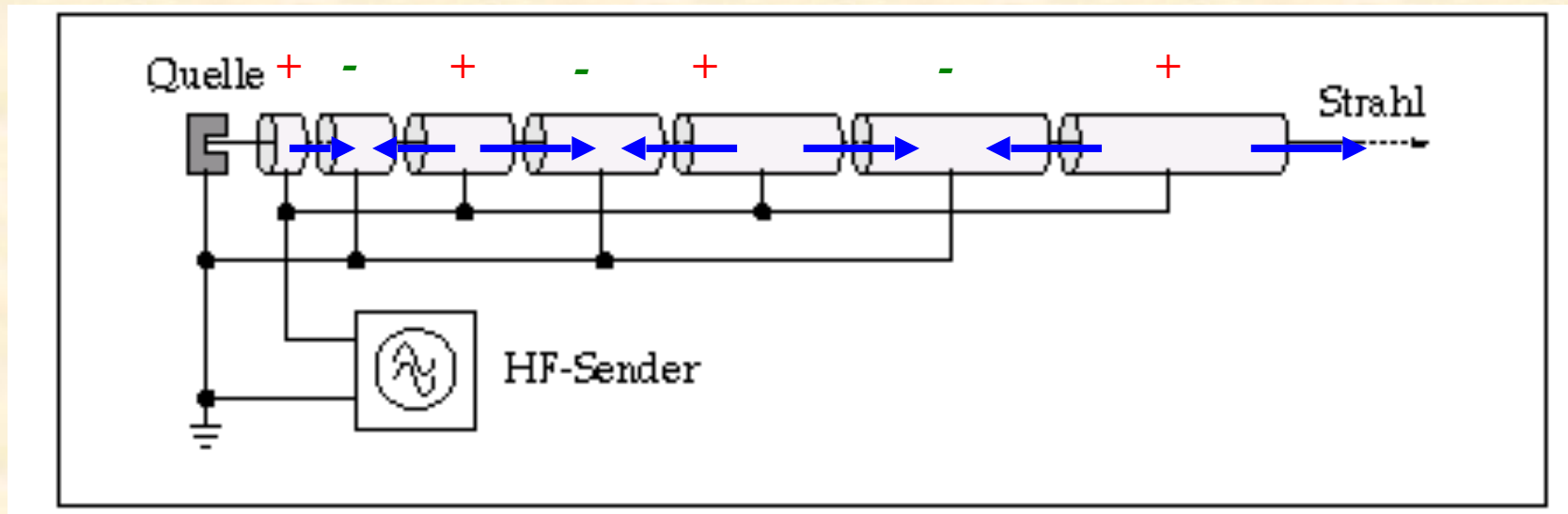
$$s = \frac{1}{2} \cdot 10 \frac{m}{s^2} \cdot (1\mu s)^2$$

$$s = 5 \cdot 10^{-12}m = 5pm$$

### 3.) The first RF-Accelerator: „Linac“

**1928, Wideroe:** how can the acceleration voltage be applied several times to the particle beam

*schematic Layout:*



*Energy gained after  $n$  acceleration gaps*

$$E_n = n \cdot q \cdot U_0 \cdot \sin \psi_s$$

$n$  number of gaps between the drift tubes

$q$  charge of the particle

$U_0$  Peak voltage of the RF System

$\Psi_s$  synchronous phase of the particle

\* acceleration of the proton in the first gap

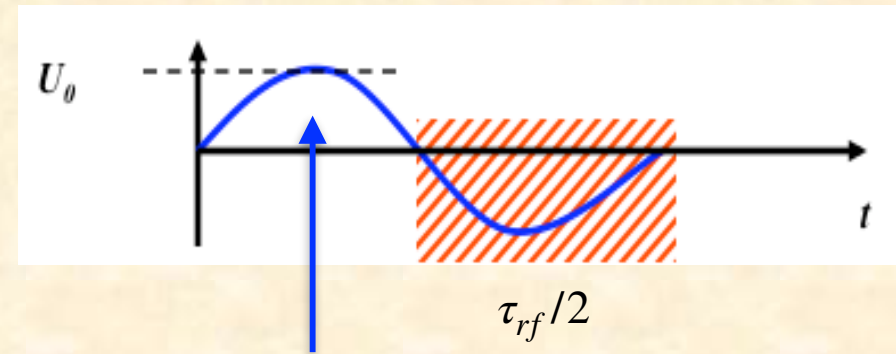
\* voltage has to be „flipped“ to get the right sign in the second gap  $\rightarrow$  RF voltage

$\rightarrow$  shield the particle in drift tubes during the negative half wave of the RF voltage



# Wideroe-Structure: the drift tubes

*shielding of the particles during the negative half wave of the RF*



*idealer Zeitpunkt  
90 grad  $\rightarrow \sin(90^\circ)=1$*

*Time span of the negative half wave:*  $\tau_{rf}/2$

*Length of the Drift Tube:*  $l_n = v_n \cdot \frac{\tau_{rf}}{2}$

*Kinetic Energy of the Particles*  $E_n = \frac{1}{2}mv^2 \quad \longrightarrow \quad v_n = \sqrt{2E_n/m}$

*mit der kin. Energie*  $E_n = n \cdot q \cdot U_0 \cdot \sin \psi_s$

*ergibt das*  $v_n = \sqrt{\frac{2 \cdot n \cdot q \cdot U_0 \cdot \sin(\psi_s)}{m}}$

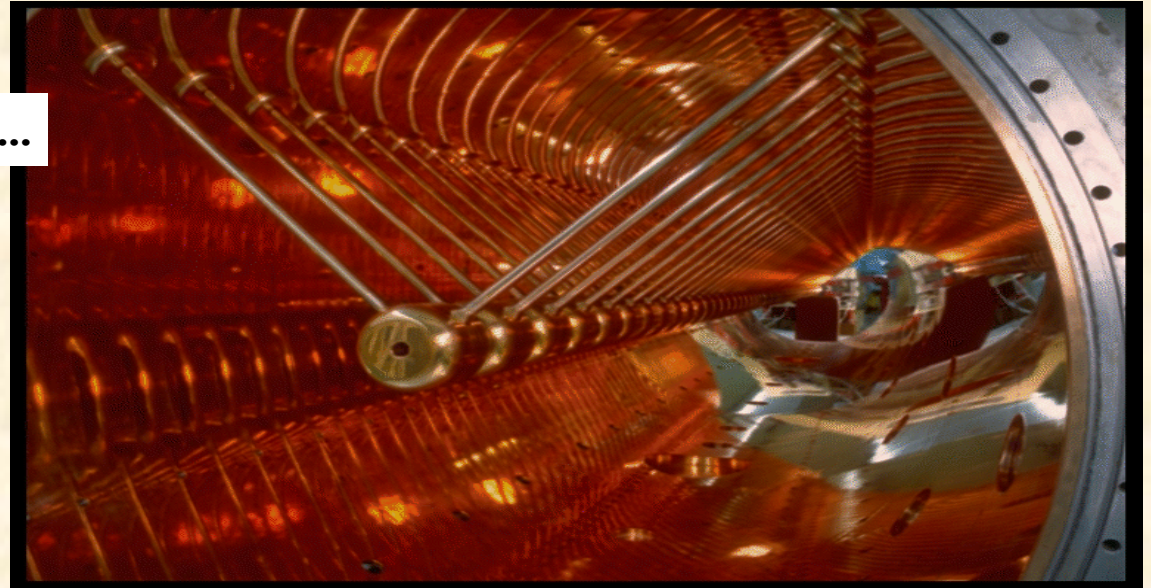
*Bauplan fuer einen Wideroe Beschleuniger:*  $l_n = v_n \cdot \frac{\tau_{rf}}{2} = \frac{1}{f_{rf}} \cdot \sqrt{\frac{n \cdot q \cdot U_0 \cdot \sin \psi_s}{2m}}$

## Und so sieht das innen drinnen aus:

Achtung !!! valid for **non relativistic** particles ...

Energy:  $\approx 20 \text{ MeV per Nucleon}$

$\beta = v/c \approx 0.04 \dots 0.6$ , Particles: Protons/Ions



### Zahlenbeispiel:

total energy  $E_{total} = E_{kin} + m_0c^2$

kinetic energy  $E_{kin} = E_{total} - m_0c^2$

Ruhe-Energie  $E_0 = m_0c^2$

man erinnert sich:  $m \rightarrow \gamma \cdot m_0$

### Linac III:

$$E_{total} = 988 \text{ MeV}$$

$$m_0c^2 = 938 \text{ MeV}$$

$$E_{kin} = 50 \text{ MeV}$$

$$\gamma = \frac{E_{ges}}{E_0} = \frac{988}{938} = 1.05$$

—> im klassischen Bereich

### 3.) The Cyclotron: (Livingston / Lawrence ~1930)

**Problem:**

Linacs werden bei  $v=c$  sehr schnell sehr langgggg.

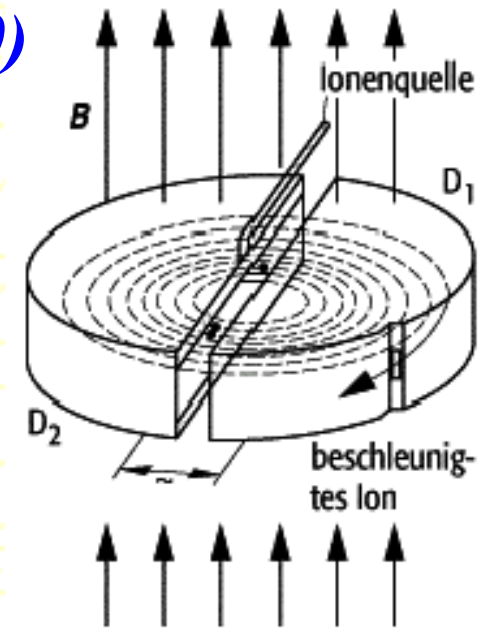
—> Man erhaelt ne kompakte (d.h. billigere) Maschine, wenn man den Orbit der Teilchen aufwickelt.

Idea: Apply a magnetic field:  $B = \text{const}$

**Lorentzforce**

$$F = q \cdot v \cdot B$$

geladene Teilchen in Bewegung werden im Magnetfeld abgelenkt.



**Kreisbahn-Bedingung:**

Zentrifugalkraft wird durch die entgegengesetzte Lorentz-Kraft aufgehoben.

$$F_{\text{Lorentz}} = F_{\text{zentrifugal}}$$

$$q \cdot v \cdot B = \frac{mv^2}{r}$$

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$$B \cdot R = \frac{mv}{q} \longrightarrow B \cdot R = \frac{p}{q}$$

German Teachers

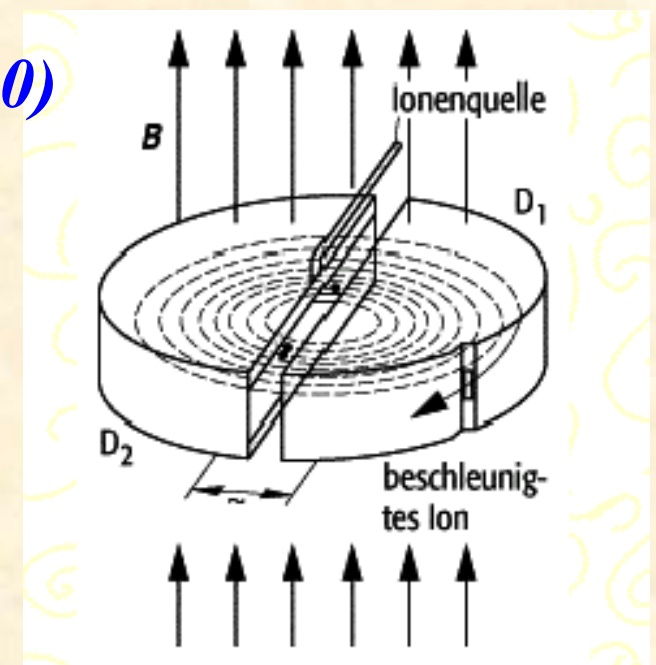
### 3.) The Cyclotron: (Livingston / Lawrence ~1930)

revolution frequency

$$\omega_{\text{revol}} = \frac{v}{r} = \frac{q}{m} \cdot B = \text{const!!!}$$

*Die Umlauf-frequenz im Cyclotron ist konstant.  
Wir lassen eine gleich-grosse konstante RF frequenz  
auf die Teilchen los und die Kiste funktioniert.*

$$\omega_{\text{rf}} = \omega_{\text{revolution}} \quad \text{oder} \quad \omega_{\text{rf}} = h \cdot \omega_{\text{revolution}}$$



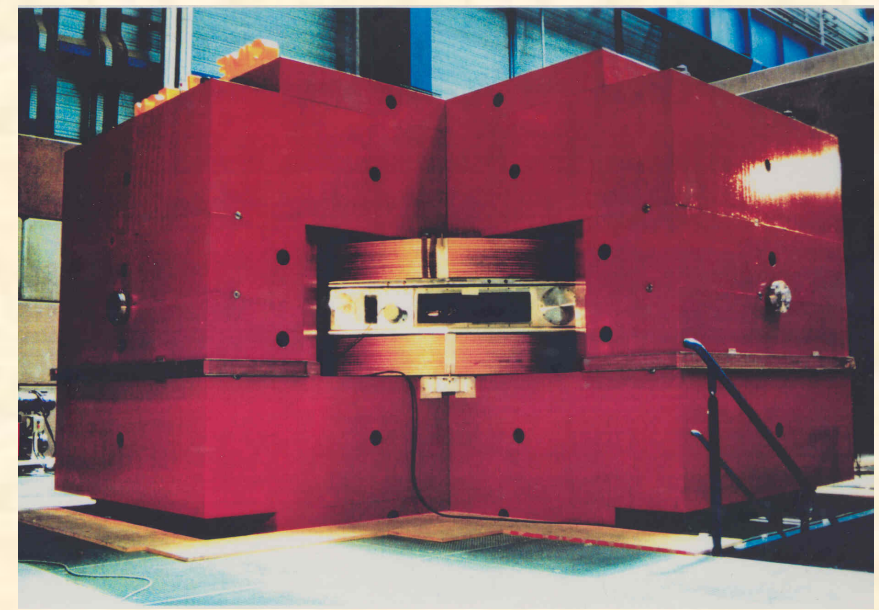
*increasing radius for increasing  
momentum → Spiral Trajectory*

**Problem: Albert !!!**

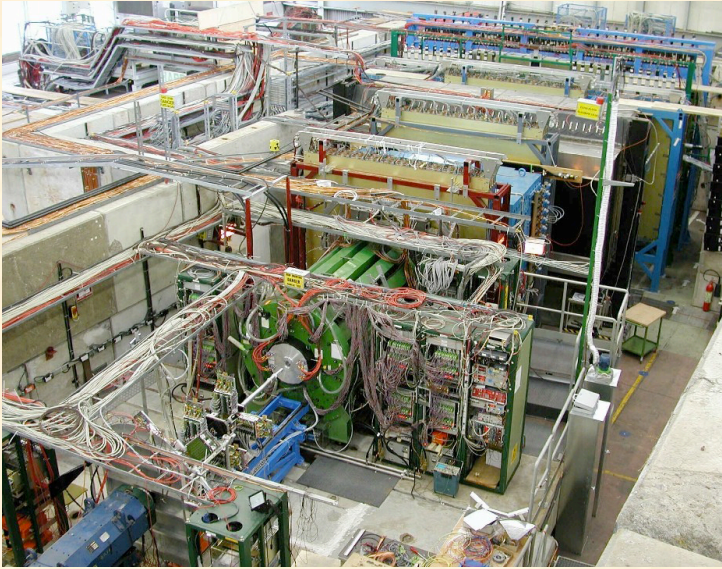
$$m \rightarrow \gamma \cdot m_0$$

$$\omega_{\text{revol}} = \frac{q}{\gamma m} \neq \text{const}$$

*Synchro-Cyclotron  
Korrektur der RF  
Frequenz*

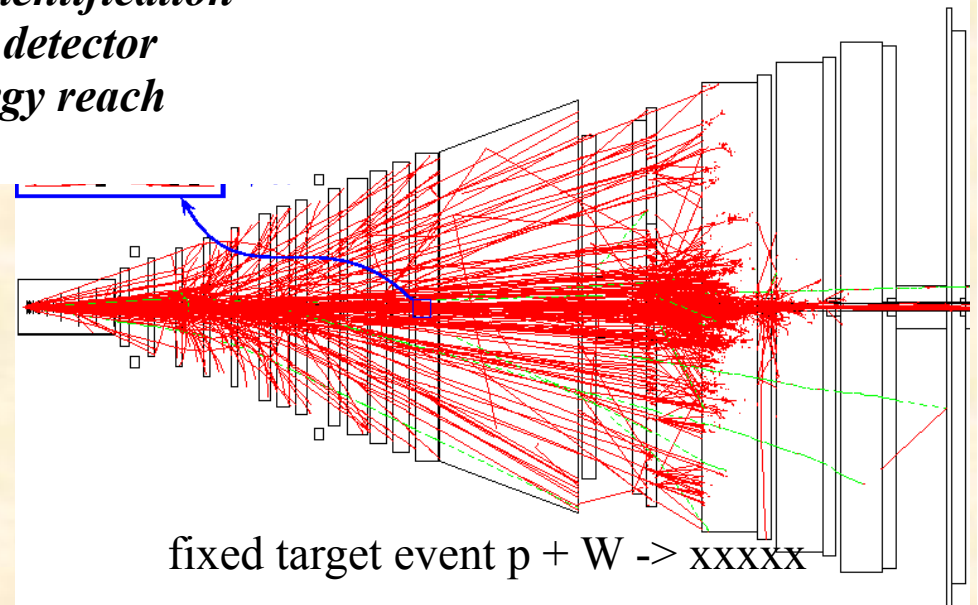


## Fixed target experiments:



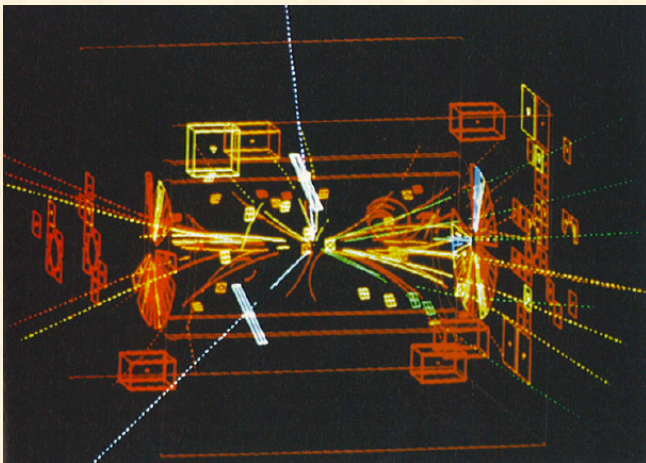
HARP Detector, CERN

*high event rate*  
*easy track identification*  
*asymmetric detector*  
*limited energy reach*

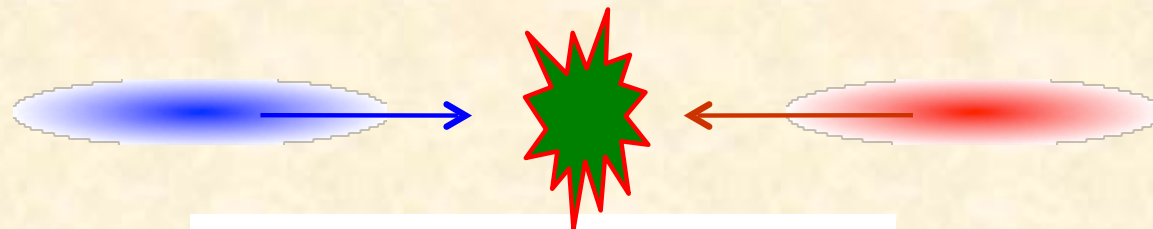


## Collider experiments:

$$E=mc^2$$



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*low event rate (luminosity)*  
*challenging track identification*  
*symmetric detector*

$$E_{lab} = E_{cm}$$

$Z_0$  boson discovery at the UA2 experiment (CERN).

The  $Z_0$  boson decays  
into a  $e^+e^-$  pair, shown as white dashed lines.



## *II.)*

### *A Bit of Theory*

### *The big storage rings: „Synchrotrons“*

# 1.) Introduction and Basic Ideas

„ ... in the end and after all it should be a kind of circular machine“  
→ need transverse deflecting force

Lorentz force  $\vec{F} = q * (\cancel{\vec{E}} + \vec{v} \times \vec{B})$

typical velocity in high energy machines:  $v \approx c \approx 3 * 10^8 \text{ m/s}$

Example:

$$B = 1 \text{ T} \quad \rightarrow \quad F = q * 3 * 10^8 \frac{\text{m}}{\text{s}} * 1 \frac{\text{Vs}}{\text{m}^2}$$

$$F = q * 300 \frac{\text{MV}}{\text{m}}$$

equivalent electrical field:

Technical limit for electrical fields:

$$E \leq 1 \frac{\text{MV}}{\text{m}}$$

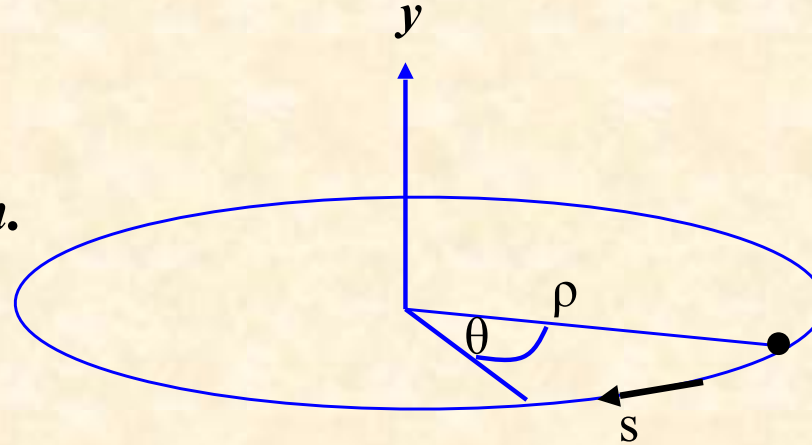


# Ein Speicherring besteht aus Magneten, Magneten und Magneten

und ein wenig Vakuum-Kammern, Strahldiagnose, und RF Systemen

## The ideal circular orbit

... das hatten wir schon.



circular coordinate system

## condition for circular orbit:

Lorentz force

$$F_L = e v B$$

centrifugal force

$$F_{centr} = \frac{\gamma m_0 v^2}{\rho}$$

$$\frac{\cancel{\gamma m_0 v^2}}{\rho} = \cancel{e v B}$$

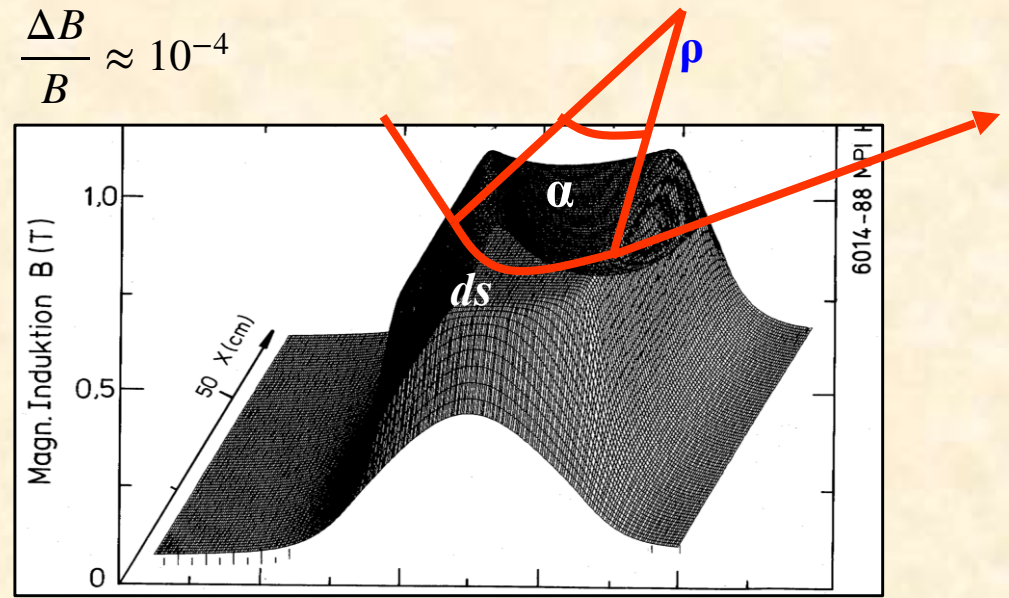
$$\frac{p}{e} = B \rho$$

$B \rho =$  "beam rigidity"  
... und jetzt isses sogar  
relativistisch korrekt.

# The Magnetic Guide Field



$B \approx 1 \dots 8 \text{ T}$



field map of a storage ring dipole magnet

Dipole erzeugen ein konstantes (!) Magnetfeld

Ablenkradius:

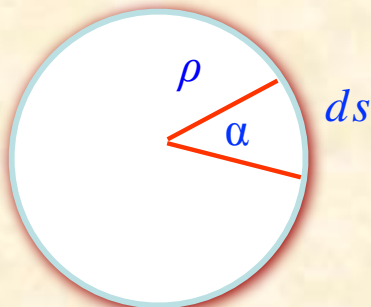
$$\rho = \frac{p}{e B} = \frac{7000 \cdot 10^9 \text{ eV}}{3 \cdot 10^8 \text{ m/s} \cdot 8 \text{ Vs/m}^2}$$

$$\rho = 2.8 \text{ km}$$

nota bene:

fuer ultra relativistische  
Teilchen gilt

$$p \approx \frac{E}{c}$$



Ablenkwinkel eines Dipols:

$$\alpha_{dipol} = \frac{ds}{\rho} = \frac{\int B ds}{B \rho} \approx \frac{B \cdot l_{dipol}}{B \rho}$$

Anzahl Dipol Magnete:

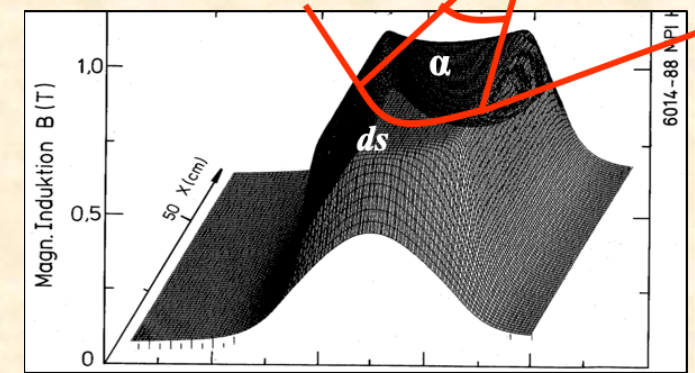
$$N_{dipole} = \frac{2\pi}{\alpha_{dipol}} = 1232 \text{ !!!}$$

Umfang des Speicherrings:

$$C_0 = 2\pi \cdot \rho$$

# Bending Angle

„wieviele Dipole sollen's denn sein ???“



Winkel im Kreis-Segment  $\alpha = \frac{ds}{\rho} = \frac{B \cdot ds}{B \cdot \rho}$

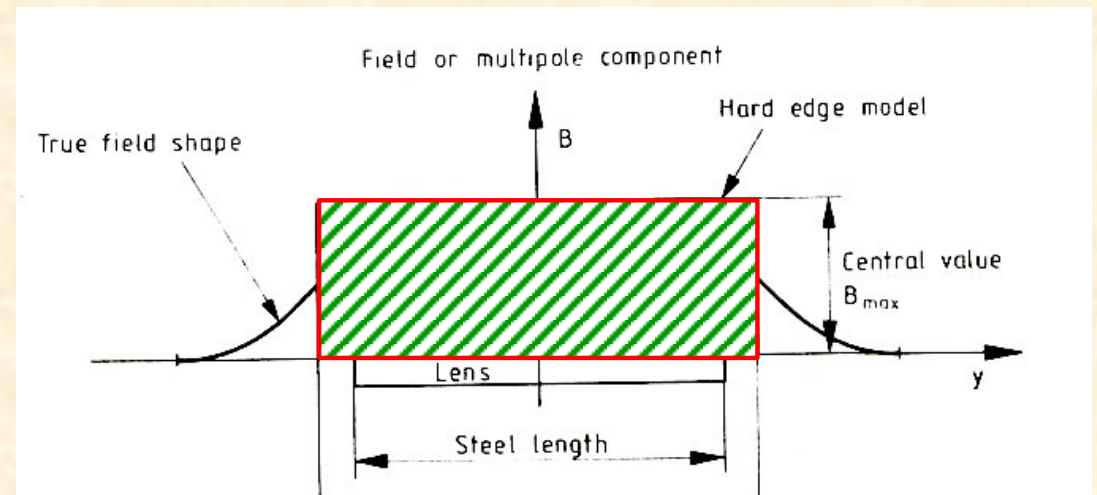
fuer den ganzen Dipol  $B l_{eff} = \int_0^{l_{mag}} B ds$

Und alle Dipole zusammen muessen nen Vollkreis ergeben, also  $2\pi$

$$\alpha = \frac{\int B dl}{B \rho} \approx \frac{n \cdot B \cdot l_{dipol}}{B \rho} = 2\pi$$

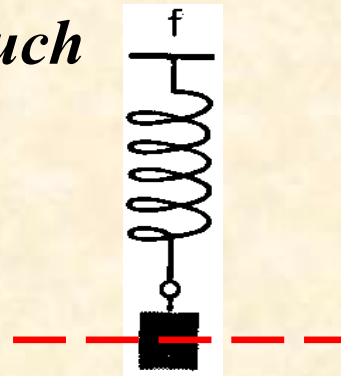
und damit braucht's "n" Dipole mit Feldstaerke "B" und Laenge "l"

$$n \cdot B \cdot l_{dipol} = 2\pi \cdot \frac{p}{q}$$



## 2.) Focusing Forces: Hook's law

*Federpendel im Physik Buch*



there is a **restoring force**, proportional to the elongation  $x$ :

$$F = m * a = - \text{const} * x$$

$$F = m * \frac{d^2 x}{dt^2} = - \text{const} * x$$

**Hook's Federgesetz:**  $F = - k * x$

*Integration liefert uns eine cos- artige Lösung  
oder eine sinus artige*

$$x(t) = A \cdot \cos(\omega t)$$

$$x(t) = B \cdot \sin(\omega t)$$

*oder eine Kombination aus beiden*

$$x_{\text{allg}}(t) = A \cdot \cos(\omega t) + B \cdot \sin(\omega t)$$

**Vorteil:**

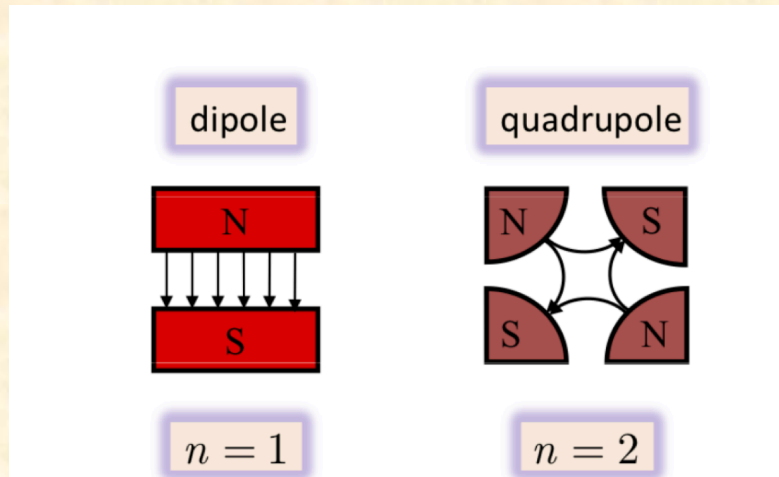
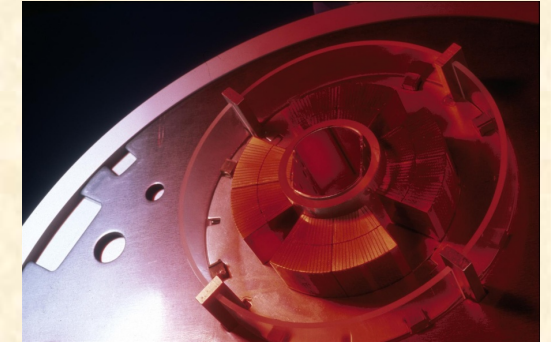
*harmonische Schwingungen **sind sehr (!!)** stabil,  
haben eine wohldefinierte Frequenz  
sind in der Natur (i.e. Physik) weit verbreitet*

## 2.) Focusing Forces: Quadrupole Fields

*Apply this concept to magnetic forces: we need a Lorentz force that rises as a function of the distance to ...*

*... the design orbit*

$$F(x) = q \cdot v \cdot B(x)$$



*Dipoles: Create a constant field*

$$B_y = \text{const}$$

*Quadrupoles: Create a linear increasing magnetic field:*

$$B_y(x) = g \cdot x, \quad B_x(y) = g \cdot y$$

# Focusing forces and particle trajectories:

normalise magnet fields to momentum  
(remember:  $B \cdot \rho = p / q$ )

*Dipole Magnet*

$$\frac{B}{p/q} = \frac{B}{B\rho} = \frac{1}{\rho}$$

*Quadrupole Magnet*

$$k := \frac{g}{p/q}$$

*Achtung:  
um Energie unabhängige  
Gleichungen zu erhalten teilen  
wir die Felder durch "p"*

*„normalised  
bending strength“*

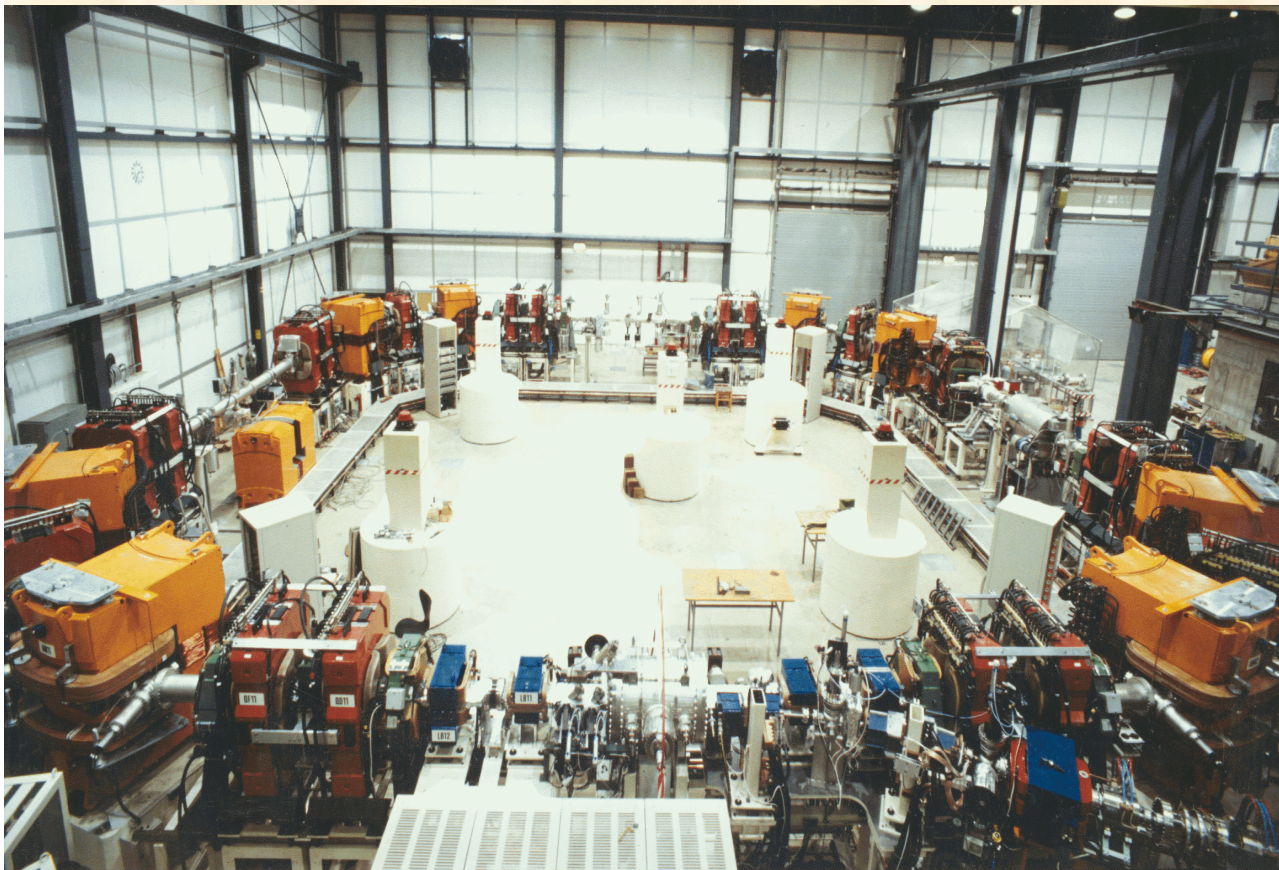
$$1/\rho = \frac{B}{p/e}$$



### 3.) The Equation of Motion:

$$\frac{B(x)}{p/e} = \frac{1}{\rho} + kx + \frac{1}{2!} \cancel{m} x^2 + \frac{1}{3!} \cancel{n} x^3 + \dots$$

*only terms linear in x, y taken into account* **dipole fields**  
**quadrupole fields**



**Separate Function Machines:**

*Split the magnets and optimise them according to their job:*

*bending, focusing etc*

*Example:  
heavy ion storage ring TSR*

\* *man sieht nur  
dipole und quads → linear*  
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## The Equation of Motion:

\* Equation for the *horizontal motion*:

$$x'' + x \cdot \left( \frac{1}{\rho^2} + k \right) = 0$$

$x$  = *particle amplitude*

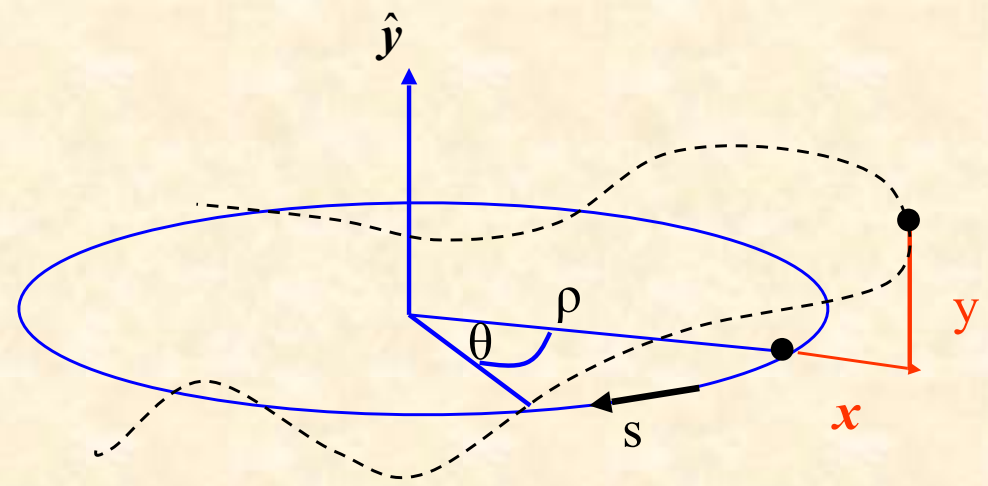
$x'$  = *angle of particle trajectory (wrt ideal path line)*

$$x'' = - x \cdot \underbrace{\left( \frac{1}{\rho^2} + k \right)}$$

$$x'' = - K \cdot x$$

*Hook's Gesetz fuer Speicherringe*

*... es gibt da nur ein kleines Problem:*





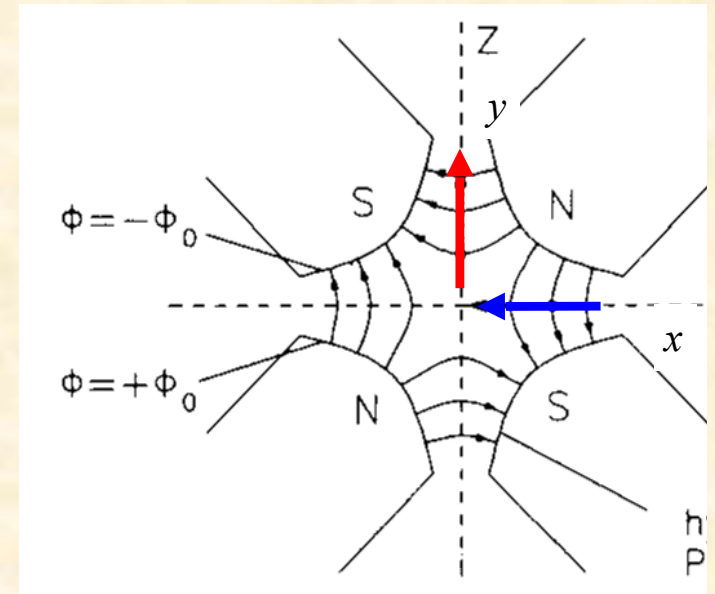
*In der vertikalen Ebene drehen sich die Magnetfeld-Linien um*

\* *Equation for the vertical motion:*

$$\frac{1}{\rho^2} = 0 \quad \text{no dipoles ... in general ...}$$

$$k \leftrightarrow -k \quad \text{quadrupole field changes sign}$$

$$y'' - k \cdot y = 0$$



*... und Teilchen,  
die in der horizontalen Ebene fokussiert werden,  
werden im gleichen Atemzug in der vertikalen Ebene  
aus der Maschine befördert.*



# 4.) Solution of Trajectory Equations

Define ... hor. plane:  $K = 1/\rho^2 + k$

... vert. Plane:  $K = -k$

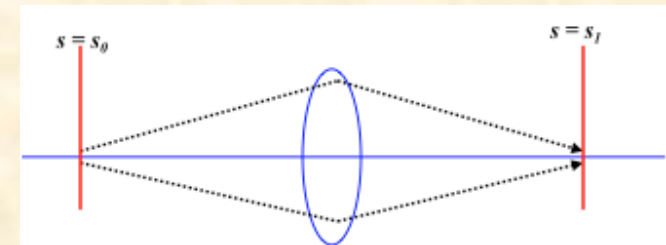
$$x'' + K x = 0$$

Differential Equation of harmonic oscillator ... with spring constant  $K$

Ansatz: **Hor. Focusing Quadrupole  $K > 0$ :**

$$x(s) = x_0 \cdot \cos(\sqrt{|K|}s) + x'_0 \cdot \frac{1}{\sqrt{|K|}} \sin(\sqrt{|K|}s)$$

$$x'(s) = -x_0 \cdot \sqrt{|K|} \cdot \sin(\sqrt{|K|}s) + x'_0 \cdot \cos(\sqrt{|K|}s)$$



... da ist wieder unsere Kuckucksuhr.

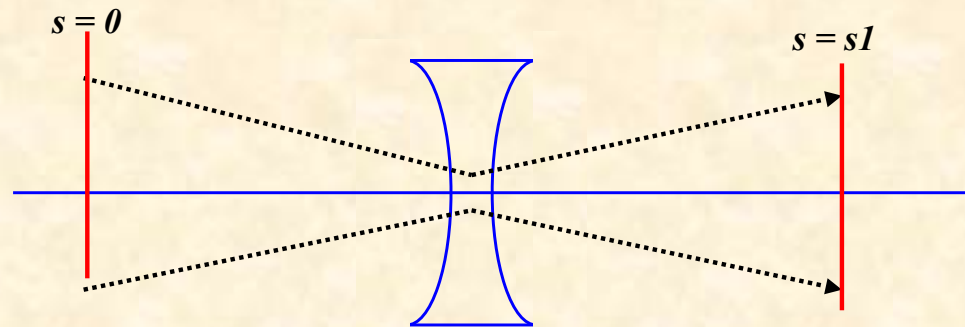
For convenience expressed in matrix formalism:

$$\begin{pmatrix} x \\ x' \end{pmatrix}_{s1} = M_{foc} * \begin{pmatrix} x \\ x' \end{pmatrix}_{s0}$$

$$M_{foc} = \begin{pmatrix} \cos(\sqrt{|K|}l) & \frac{1}{\sqrt{|K|}} \sin(\sqrt{|K|}l) \\ -\sqrt{|K|} \sin(\sqrt{|K|}l) & \cos(\sqrt{|K|}l) \end{pmatrix}$$

*hor. defocusing quadrupole:*

$$x'' - K x = 0$$



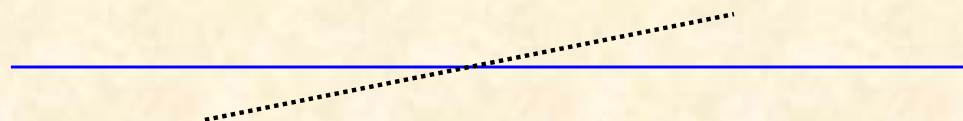
*Ansatz: Remember from school*

$$x(s) = a_1 \cdot \cosh(\omega s) + a_2 \cdot \sinh(\omega s)$$

$$M_{defoc} = \begin{pmatrix} \cosh \sqrt{|K|}l & \frac{1}{\sqrt{|K|}} \sinh \sqrt{|K|}l \\ \sqrt{|K|} \sinh \sqrt{|K|}l & \cosh \sqrt{|K|}l \end{pmatrix}$$

*drift space:*

$$K = 0$$



$$x(s) = x'_0 \cdot s$$

$$M_{drift} = \begin{pmatrix} 1 & l \\ 0 & 1 \end{pmatrix}$$

**! with the assumptions made, the motion in the horizontal and vertical planes are independent „ ... the particle motion in x & y is uncoupled“**

... zur Erinnerung:

*hyperbolische Funktionen führen leicht zu Panik Attacken !*

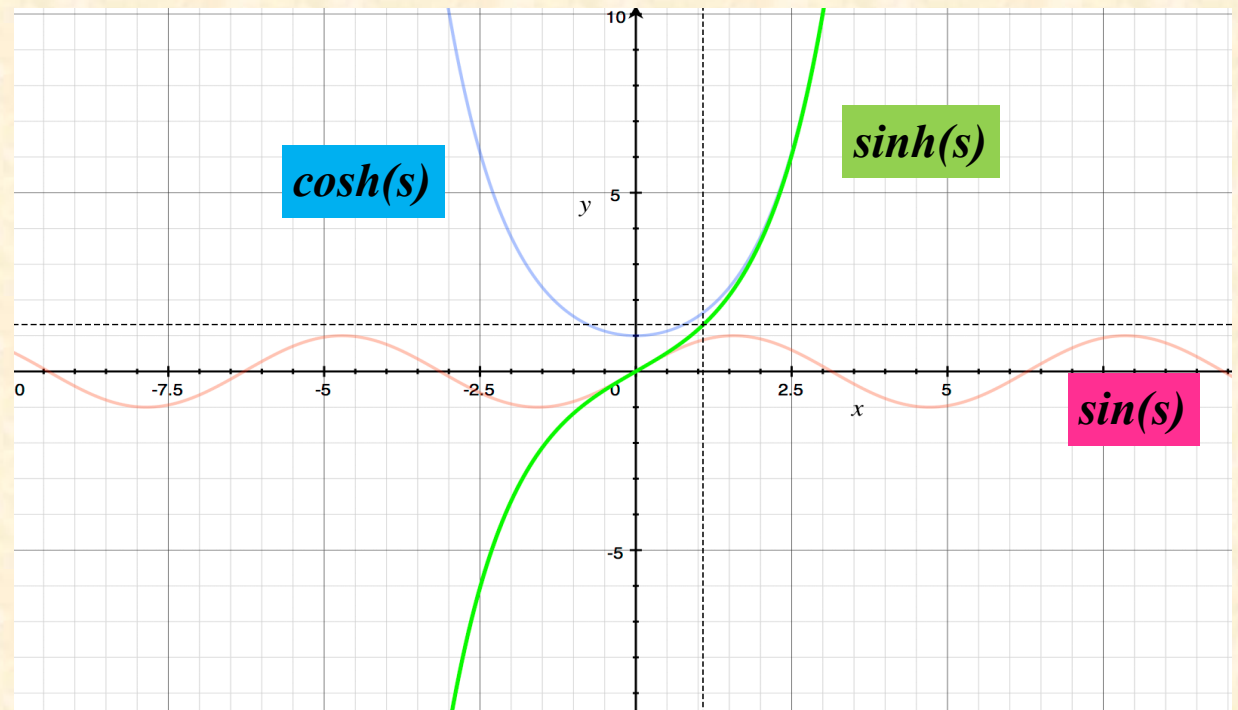
$$M_{defoc} = \begin{pmatrix} \cosh \sqrt{|K|}l & \frac{1}{\sqrt{|K|}} \sinh \sqrt{|K|}l \\ \sqrt{|K|} \sinh \sqrt{|K|}l & \cosh \sqrt{|K|}l \end{pmatrix}$$

$$f(s) = \sin(s) \quad f(s) = \cos(s)$$

$$f(s) = \sinh(s) \quad f(s) = \cosh(s)$$

*Ansatz für die Teilchenbewegung im defokussierenden Fall:*

$$x(s) = a_1 \cdot \cosh(\omega s) + a_2 \cdot \sinh(\omega s)$$

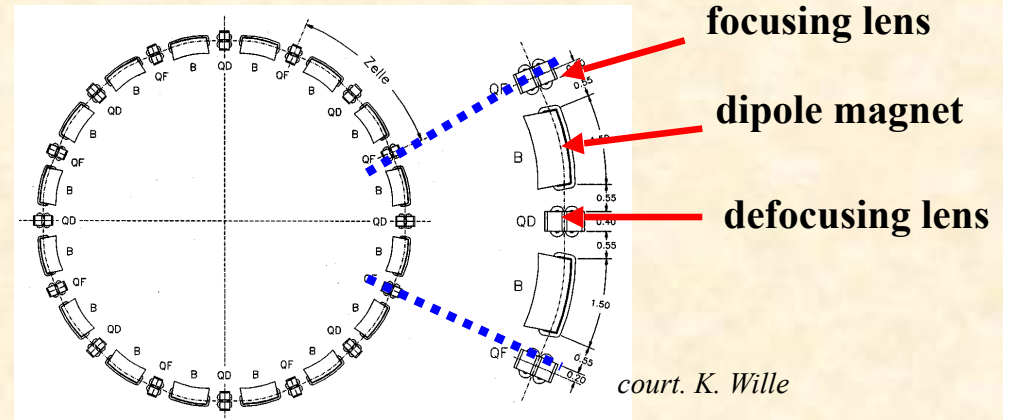


# Transformation through a system of lattice elements

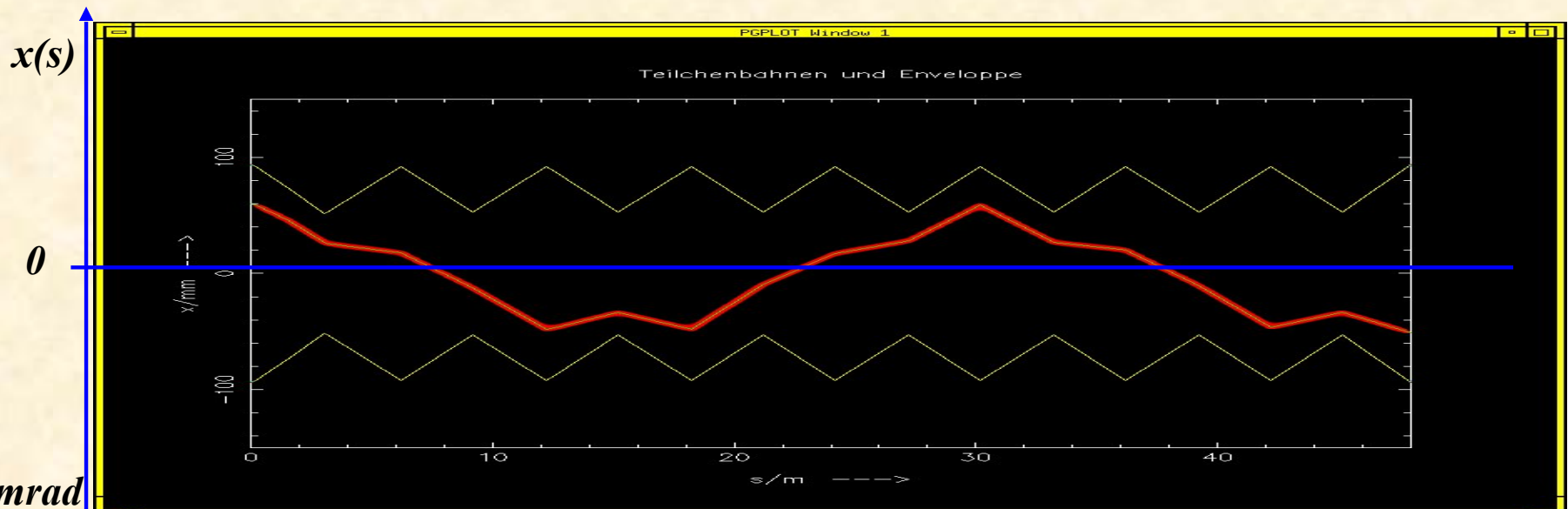
combine the single element solutions by multiplication of the matrices

$$M_{total} = M_{QF} * M_D * M_{QD} * M_{Bend} * M_{D*} * \dots$$

$$\begin{pmatrix} x \\ x' \end{pmatrix}_{s_2} = M(s_2, s_1) \cdot \begin{pmatrix} x \\ x' \end{pmatrix}_{s_1}$$



in each accelerator element the particle trajectory corresponds to the movement of a harmonic oscillator ,,

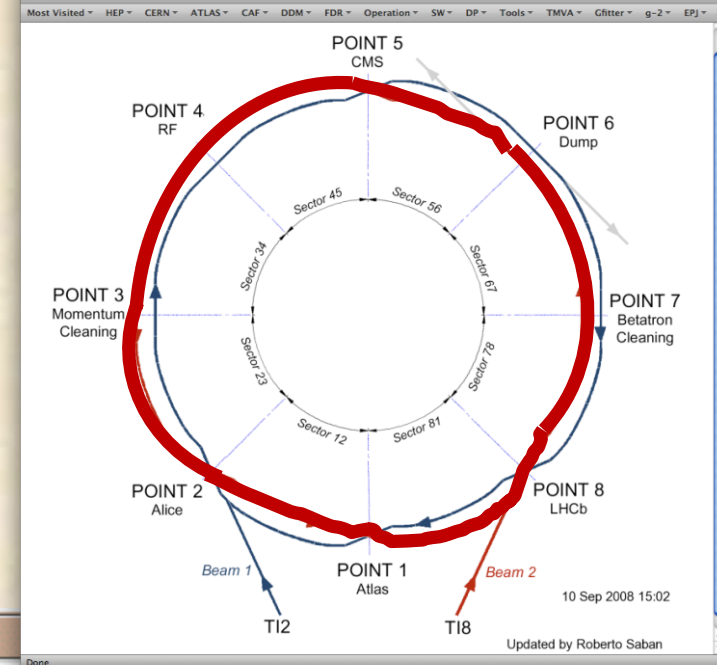


typical values  
in a strong  
foc. machine:  
 $x \approx \text{mm}$ ,  $x' \leq \text{mrad}$

# LHC Operation: Beam Commissioning

The transverse focusing fields create a harmonic oscillation of the particles with a well defined “Eigenfrequency” which is called **tune**

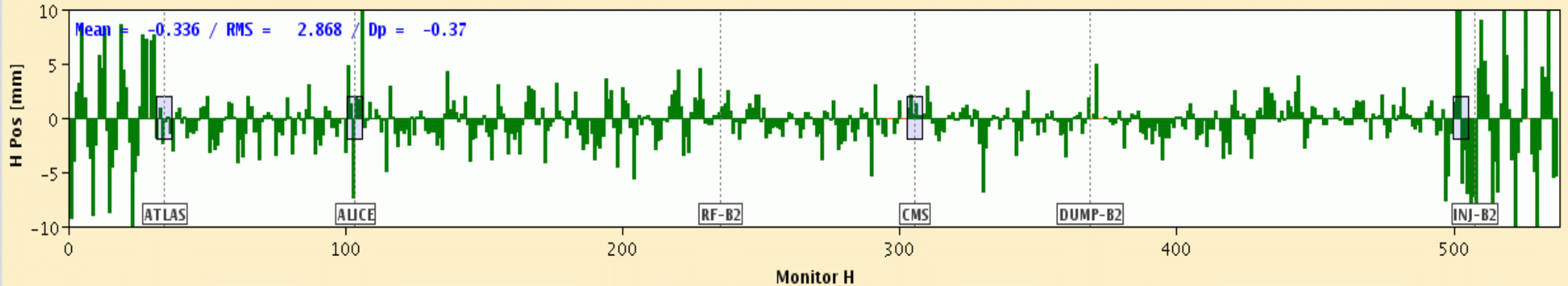
First turn steering "by sector:"



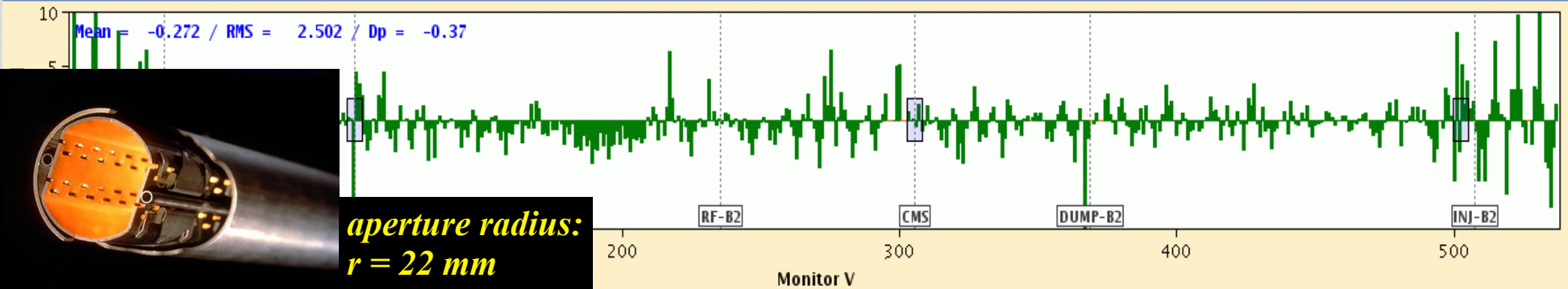
YASP DV LHCRING / INJ-TEST-NB / beam 2

Views [Icons] More [Icon]

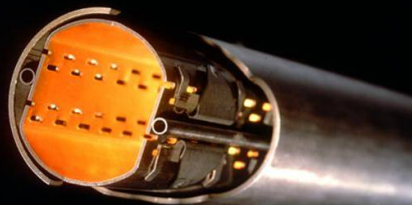
FT - P 450.12 GeV/c - Fill # 830 INJPROT - 10/09/08 15-01-58



FT - P 450.12 GeV/c - Fill # 830 INJPROT - 10/09/08 15-01-58



aperture radius:  
 $r = 22 \text{ mm}$



*“Once more unto the breach, dear friends, once more”  
(W. Shakespeare, Henry 5)*

*“Do they actually drop ?”*

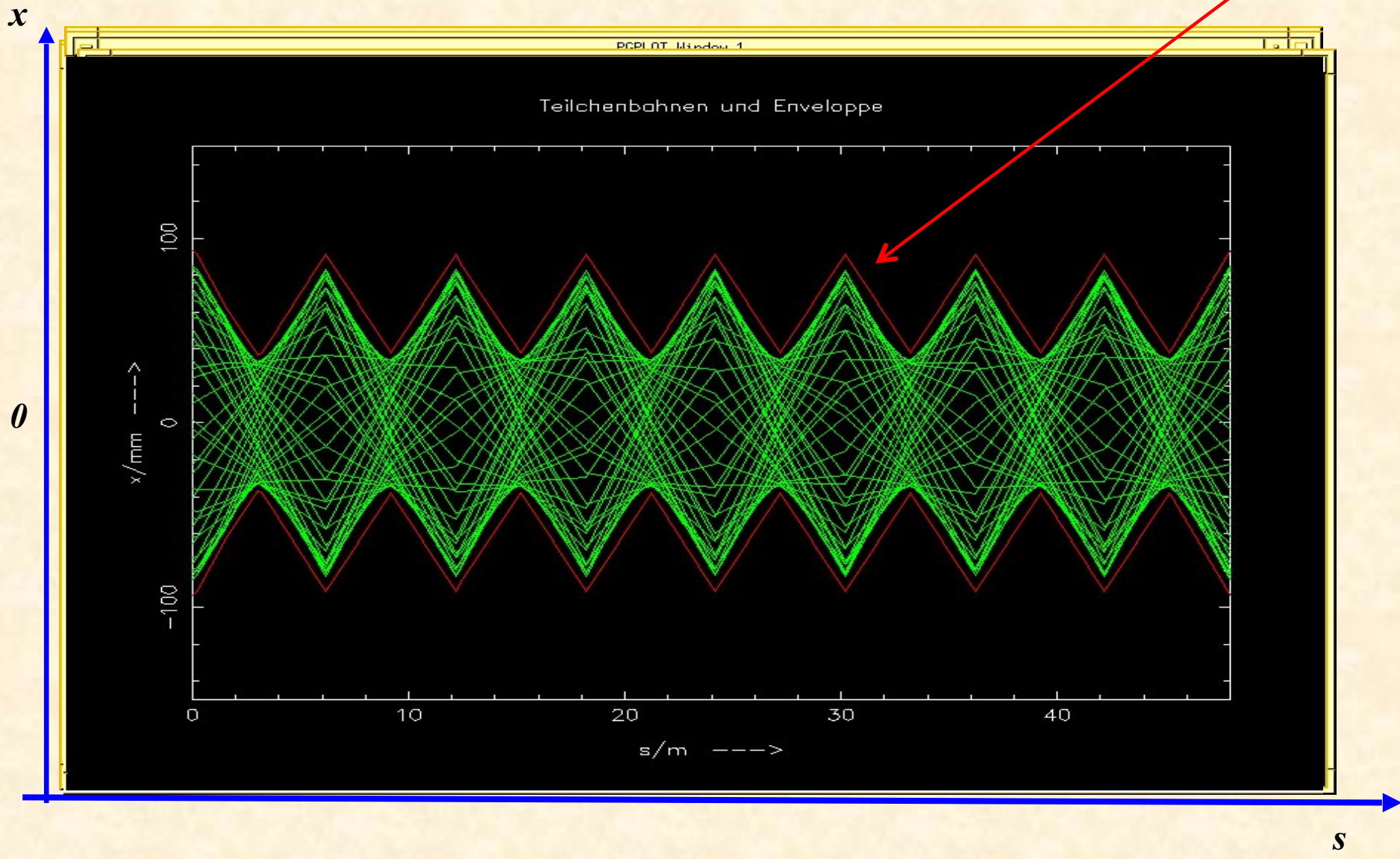
*Answer: No*



**Question: what will happen, if the particle performs a second turn ?**

*... or a third one or ...  $10^{10}$  turns*

$$\sigma = \sqrt{\epsilon\beta}$$



# *Collisions*

*Die zwei wichtigsten Formeln fuer uns ...*

$$E = mc^2$$

*die Energie unserer Strahlen kann in **Masse** neuer **Teilchen** umgewandelt werden.*

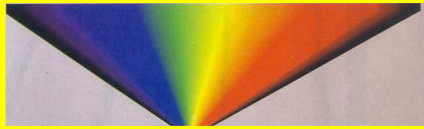
$$\lambda = \frac{h}{p}$$

***Teilchen** verhalten sich wie **Wellen** mit einer wohl definierten Wellenlaenge;  $h = 4.1 \cdot 10^{-21} \text{ MeV s}$*

# Collisions

*Lichtspektrum:*

$$\lambda = 400 \dots 800 \text{ nm}$$



*Lichtmikroskope haben damit eine Auflösung von etwas besser als  $\mu\text{m}$*



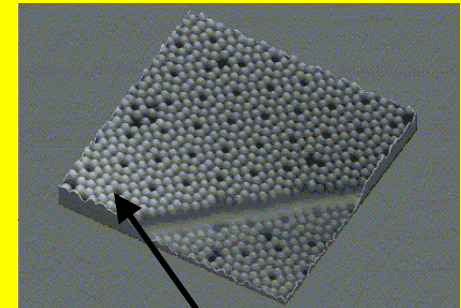
$\longleftrightarrow$  250  $\mu\text{m}$

*LHC:*

$$E = p \cdot c \quad \rightarrow \quad p = \frac{E}{c} \quad p = \frac{7 \cdot 10^{12} \text{ eV}}{3 \cdot 10^8 \text{ m/s}}$$

$$\lambda = \frac{h}{p} = 4.1 \cdot 10^{-21} \text{ MeVs} \cdot \frac{3 \cdot 10^8 \text{ m/s}}{7 \cdot 10^{12} \text{ eV}}$$

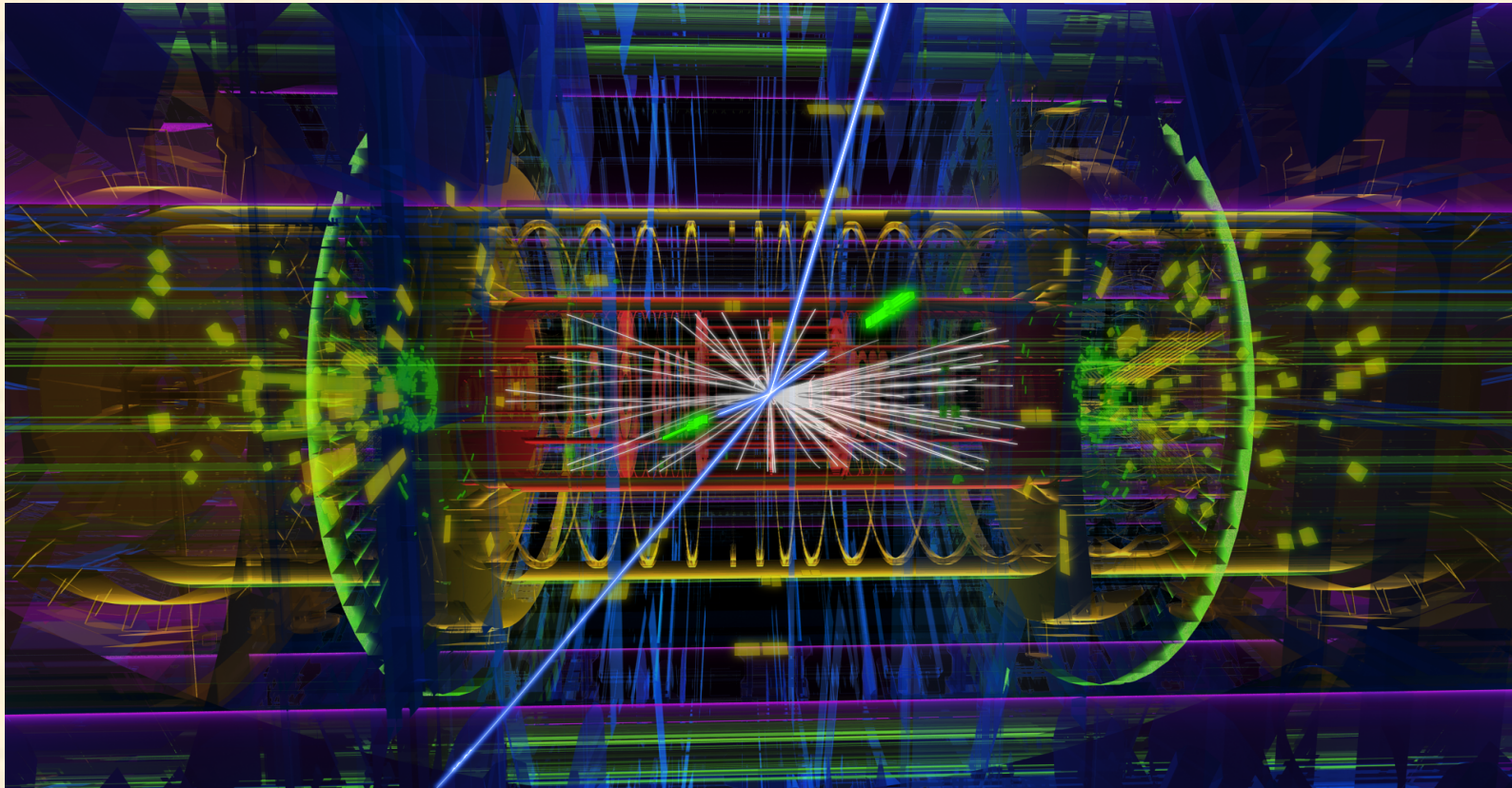
$$\lambda \approx 2 \cdot 10^{-19} \text{ m}$$



*Atome:*  $\approx 10^{-10} \text{ m}$

*Kerne:*  $\approx 10^{-15} \text{ m}$

# *Collisions*



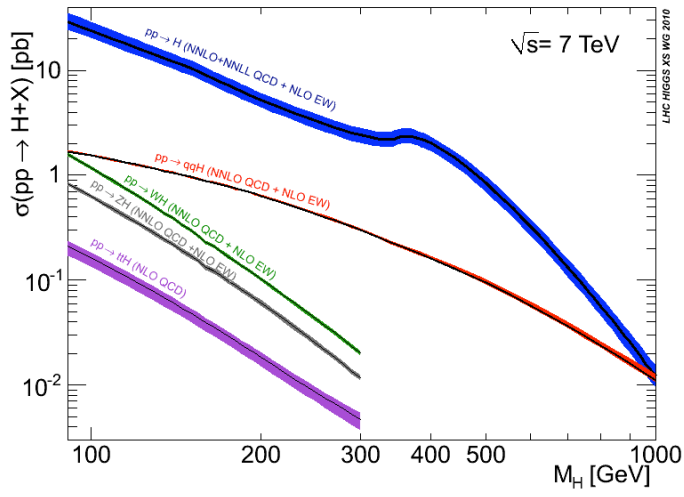
*ATLAS event display: Higgs => two electrons & two muons*

$$E = m_0c^2 = m_{e1} + m_{e2} + m_{\mu1} + m_{\mu2} = 125.4 \text{ GeV}$$

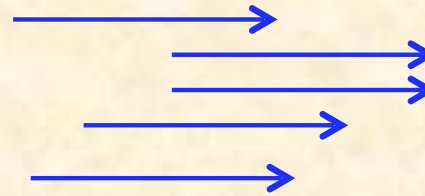
# Problem: Our particles are *VERY* small !!

*man trifft nicht so häufig.*

## Overall cross section of the Higgs:



$$\Sigma_{react} \approx 1pb$$

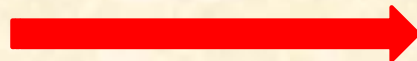
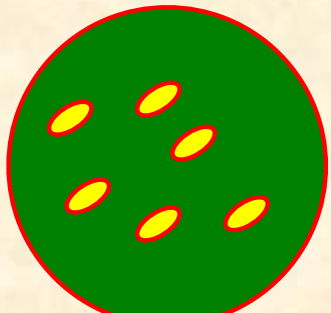


$$1b = 10^{-24} cm^2 = \frac{1}{mio} \cdot \frac{1}{mio} \cdot \frac{1}{mio} \cdot \frac{1}{10000} mm^2$$

$$1pb = 10^{-12}b \approx ZERO$$

*The particles are “very small”*

*The only chance we have:  
compress the transverse beam size ... at the IP*

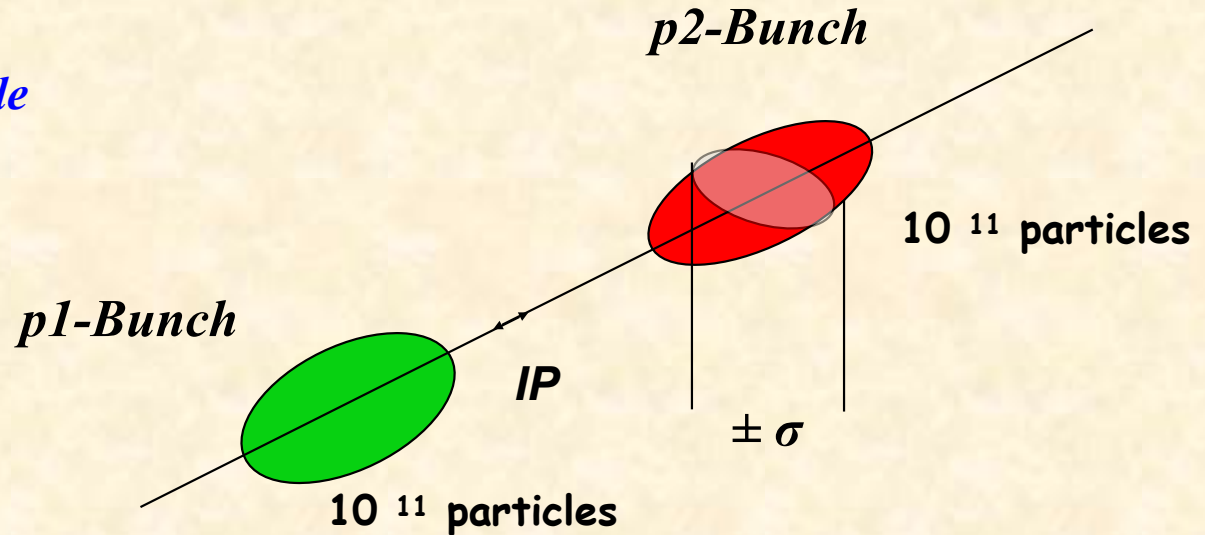


*LHC typical → 16 μm*

# 5.) Luminosity

Ereignis Rate: "Physik" pro Sekunde

$$R = L \cdot \Sigma_{react}$$



Example: Luminosity run at LHC

$$\sigma_x = \sigma_y = 16 \mu m$$

Strahlgröße am IP

$$f_0 = 11.245 \text{ kHz}$$

Umlaufs-Frequenz

$$n_b = 2808$$

Zahl der Bunche

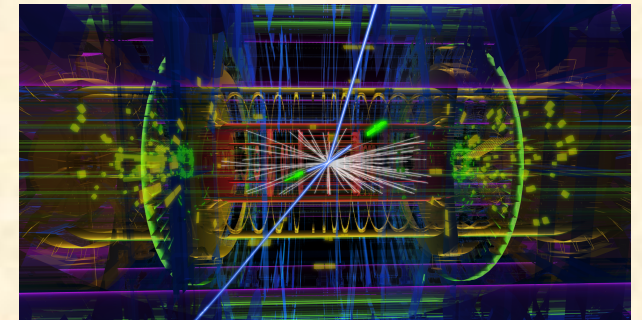
$$N_p = 1.2 \cdot 10^{11}$$

Teilchen in einem Bunch

$$I_p = 584 \text{ mA}$$

Strahlstrom

$$L = \frac{1}{4\pi} \cdot N_{p1} \cdot \frac{N_{p2}}{\sigma_x \sigma_y} \cdot (n_b \cdot f_0)$$

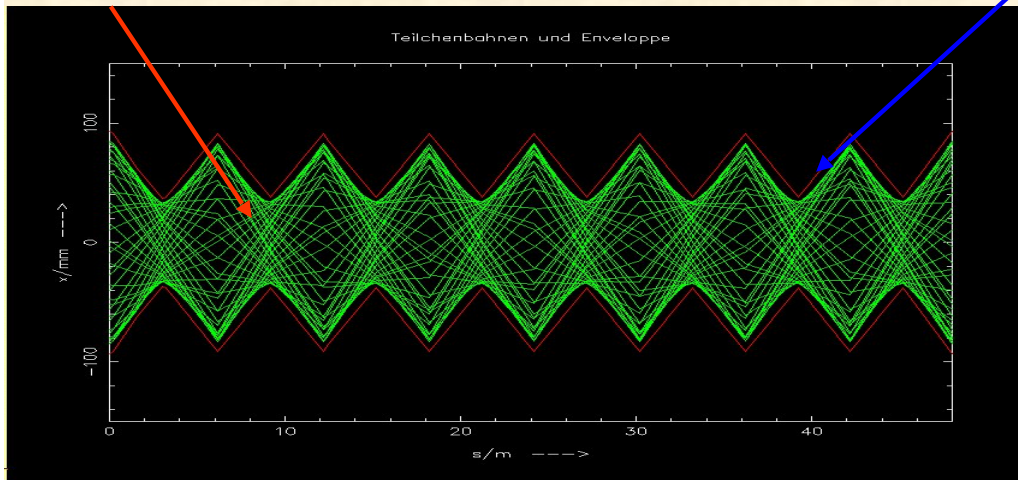


$$L = 1.0 * 10^{34} \frac{1}{\text{cm}^2 \text{ s}}$$

# Emittance of the Particle Ensemble:

$$x(s) = \sqrt{\varepsilon} \sqrt{\beta(s)} \cdot \cos(\Psi(s) + \phi)$$

$$\hat{x}(s) = \sqrt{\varepsilon} \sqrt{\beta(s)}$$



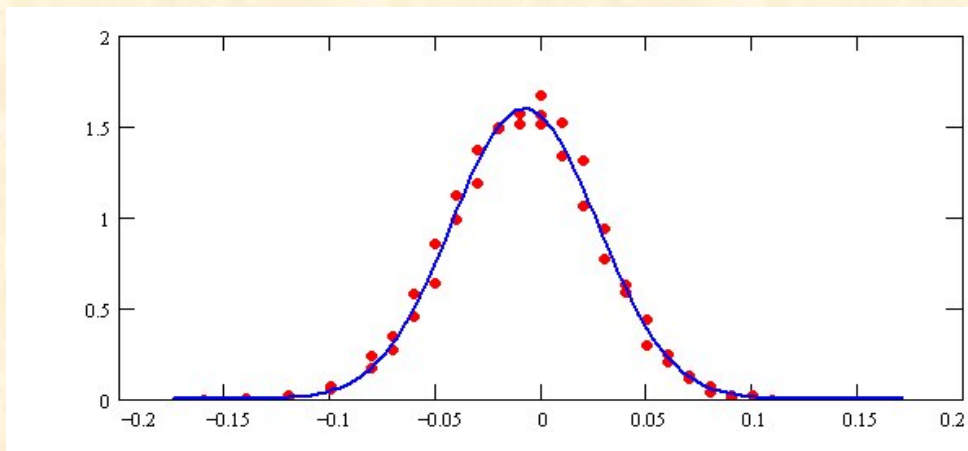
single particle trajectories,  $N \approx 10^{11}$  per bunch

**Gauß Particle Distribution:**

$$\rho(x) = \frac{N \cdot e}{\sqrt{2\pi} \sigma_x} \cdot e^{-\frac{1}{2} \frac{x^2}{\sigma_x^2}}$$

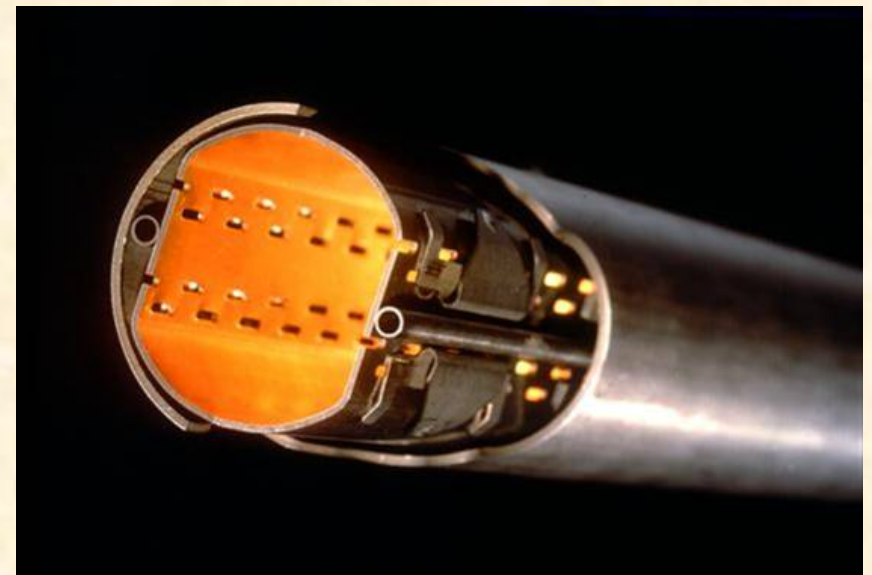
particle at distance  $1 \sigma$  from centre  
 $\leftrightarrow$  68.3 % of all beam particles

**LHC: Strahlgrösse =  $\sigma \approx 0.3$  mm**



B. J. Holzer, CERN

German Teachers



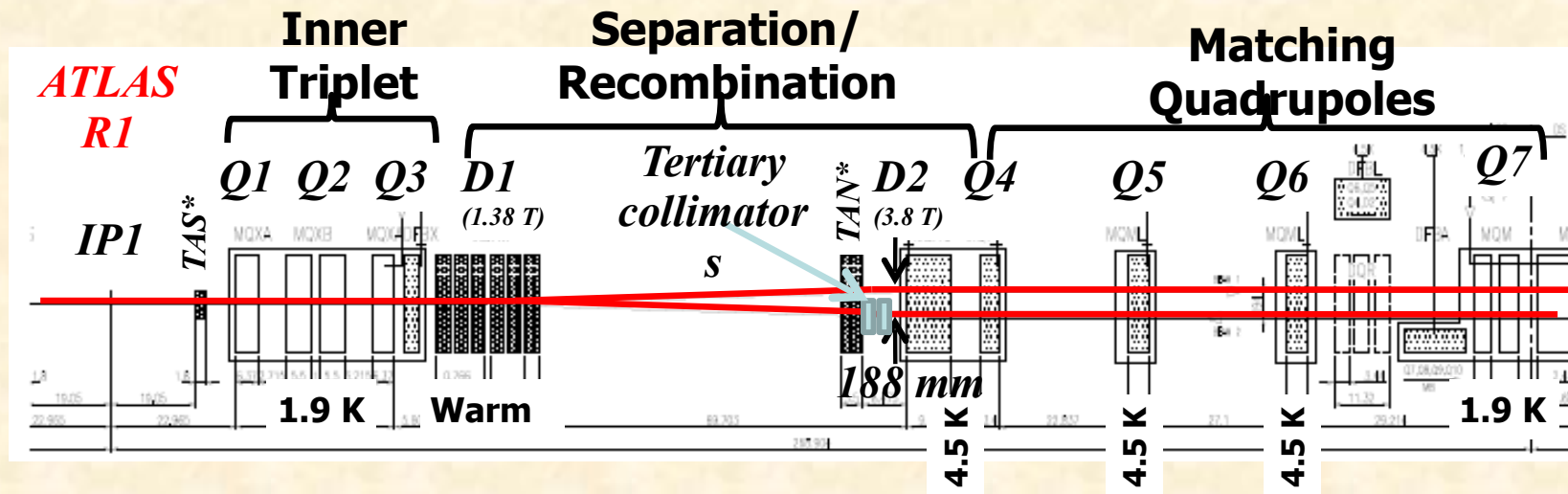
aperture requirements:  $r_0 = 17 * \sigma$



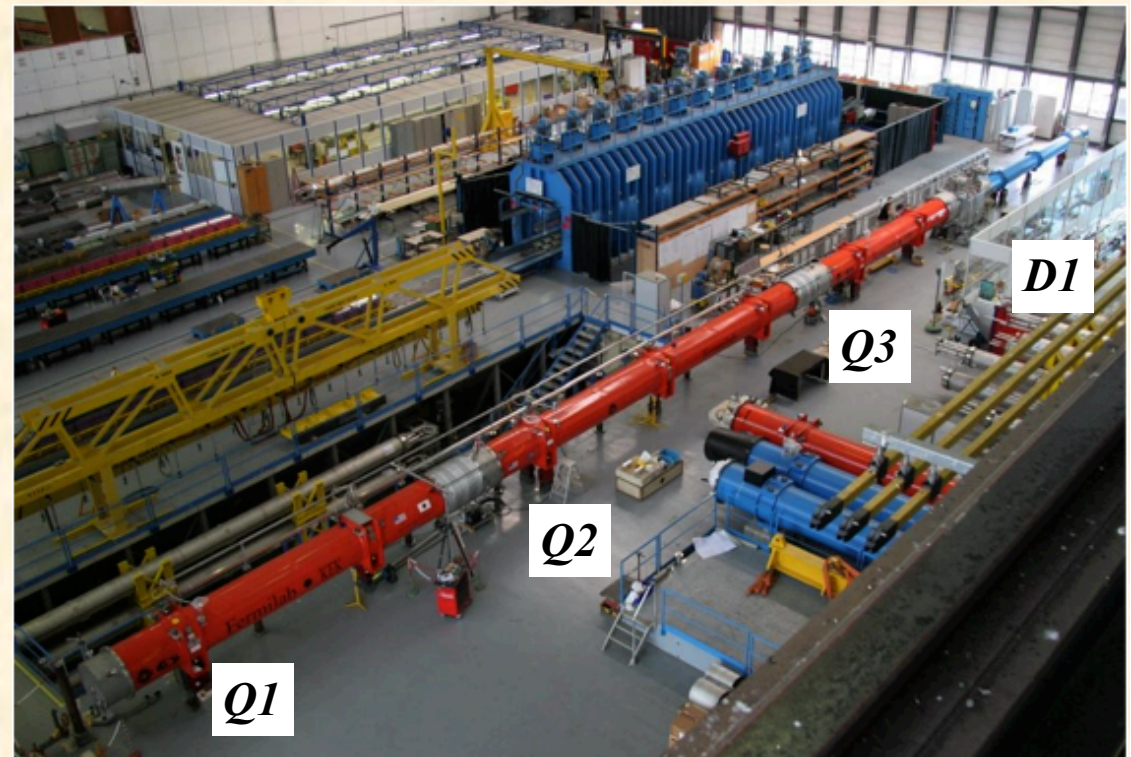
*beam sizes in the order of my cat's hair !!*  
B. J. Holzer, CERN  
German Teachers



# The LHC Mini-Beta-Insertions

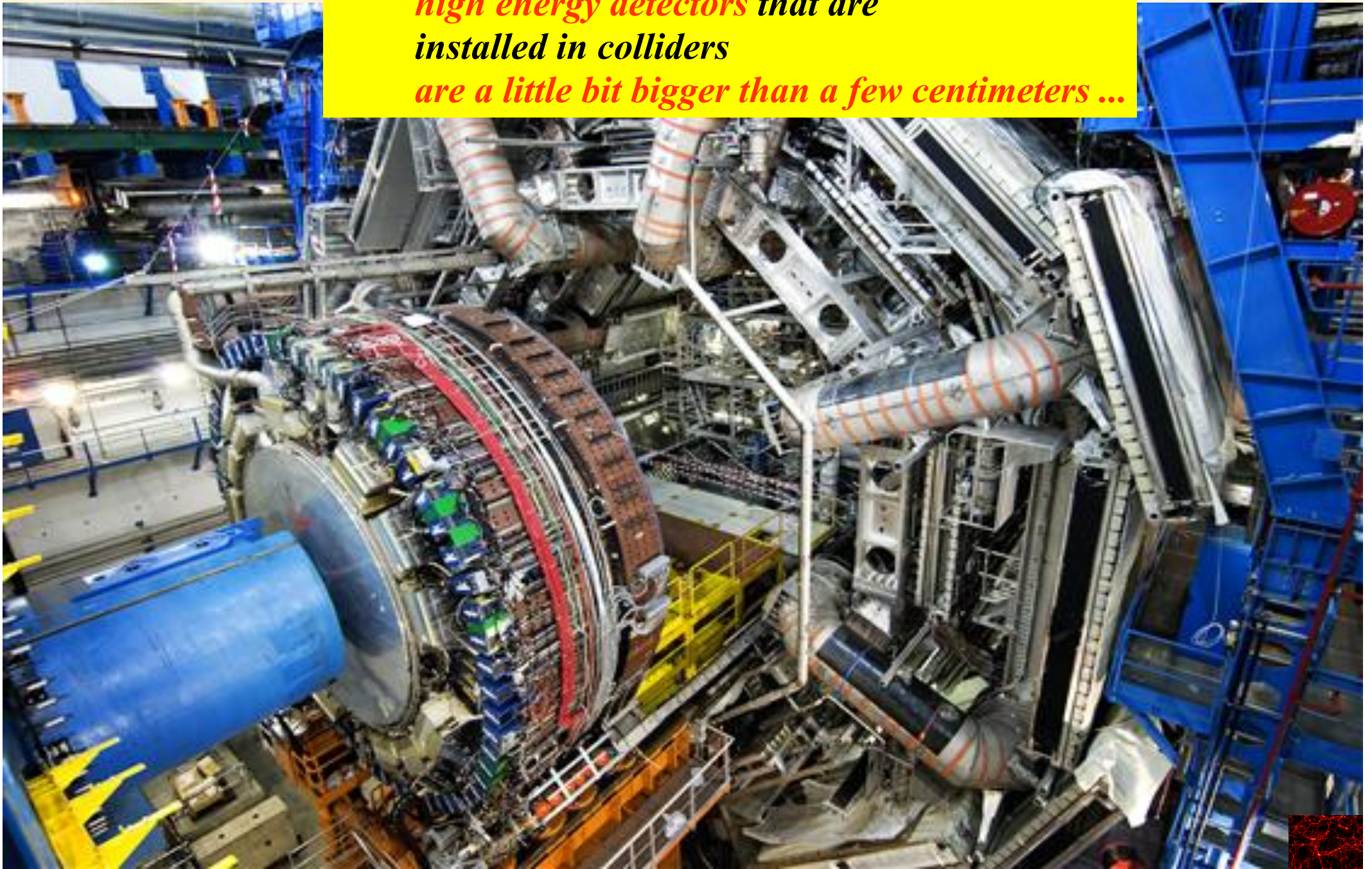


*Extrem starke Fokussierung  
(in beiden Ebenen) für beide Strahlen, um  
die Trajektorien der  $10^{11}$  Teilchen auf  
micro Meter zu komprimieren.*



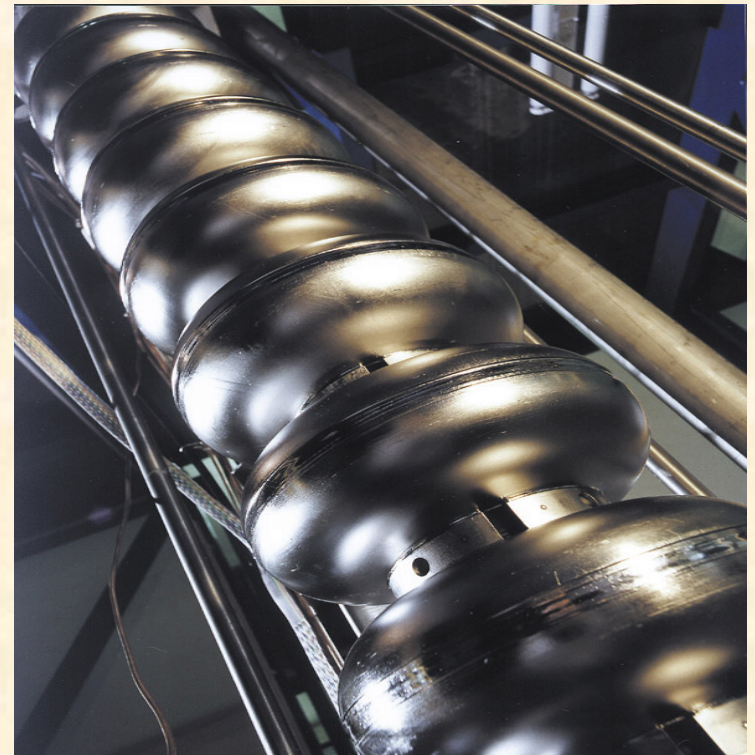
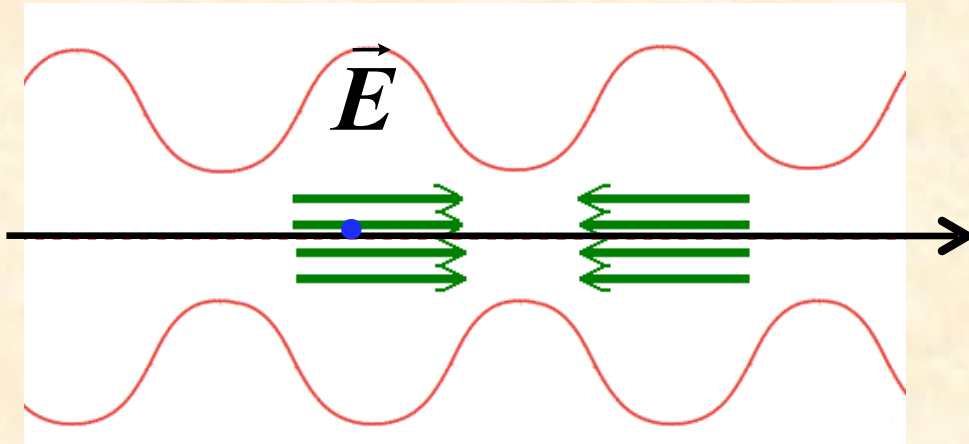
... clearly there is another problem !!!

... unfortunately ... in general  
*high energy detectors* that are  
*installed in colliders*  
*are a little bit bigger than a few centimeters ...*



# The Acceleration

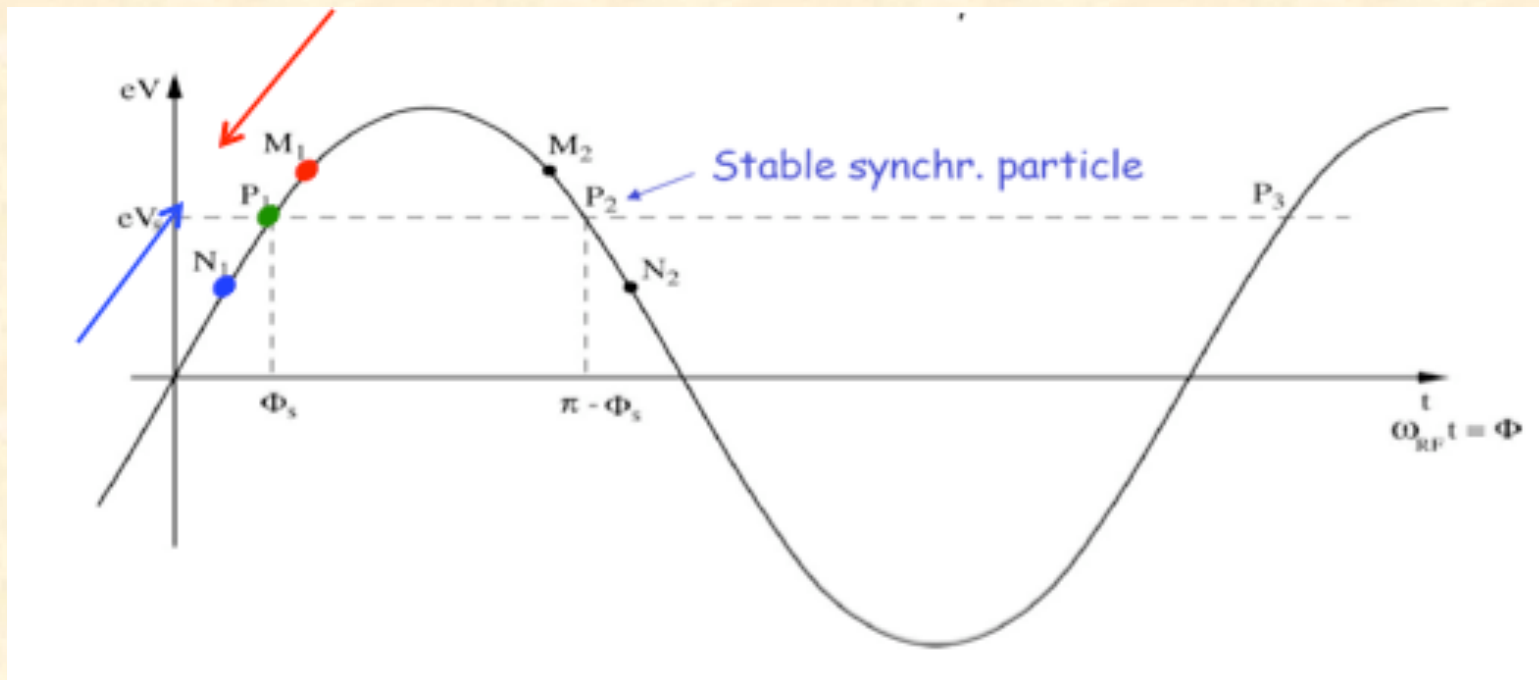
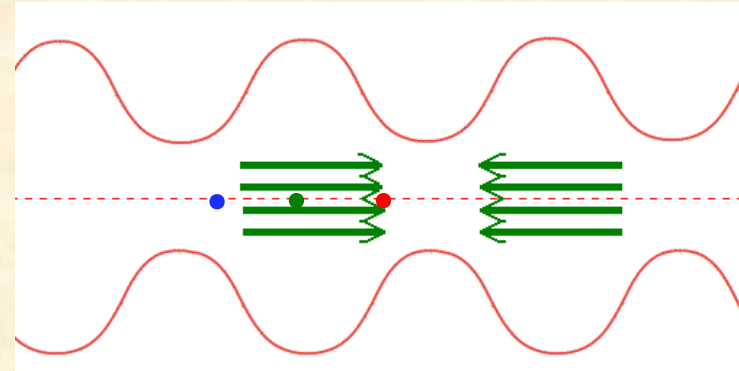
Install an RF accelerating structure in the ring:



# The Acceleration & "Phase Focusing"

$\Delta p/p \neq 0$  below transition

- ideal particle* •
- particle with  $\Delta p/p > 0$*  • *faster*
- particle with  $\Delta p/p < 0$*  • *slower*



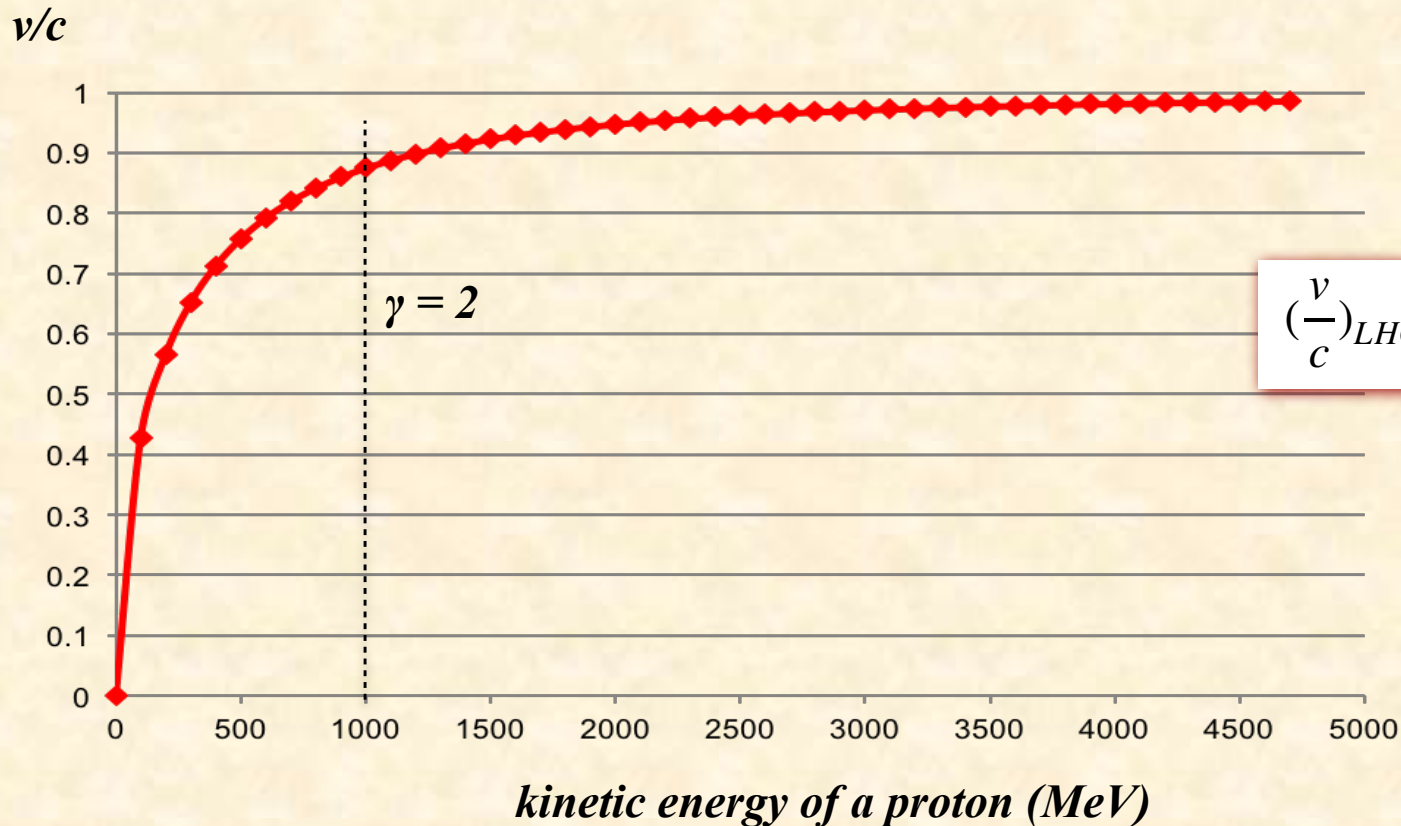
*Focussing effect in the longitudinal direction keeping the particles close together ... forming a "bunch"*

*... so sorry, here we need help from Albert:*

*was passiert, wenn wir die Teilchen immer "schneller" machen ?*

$$\gamma = \frac{E_{total}}{m_0 c^2} = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \quad \longrightarrow \quad \frac{v}{c} = \sqrt{1 - \frac{m c^2}{E_{total}^2}}$$

*die Teilchen werden irgendwann nicht mehr schneller !*



*... some when the particles do not get faster anymore*

*.... but heavier !*

# The Acceleration above transition

*ideal particle*

•

*particle with  $\Delta p/p > 0$*

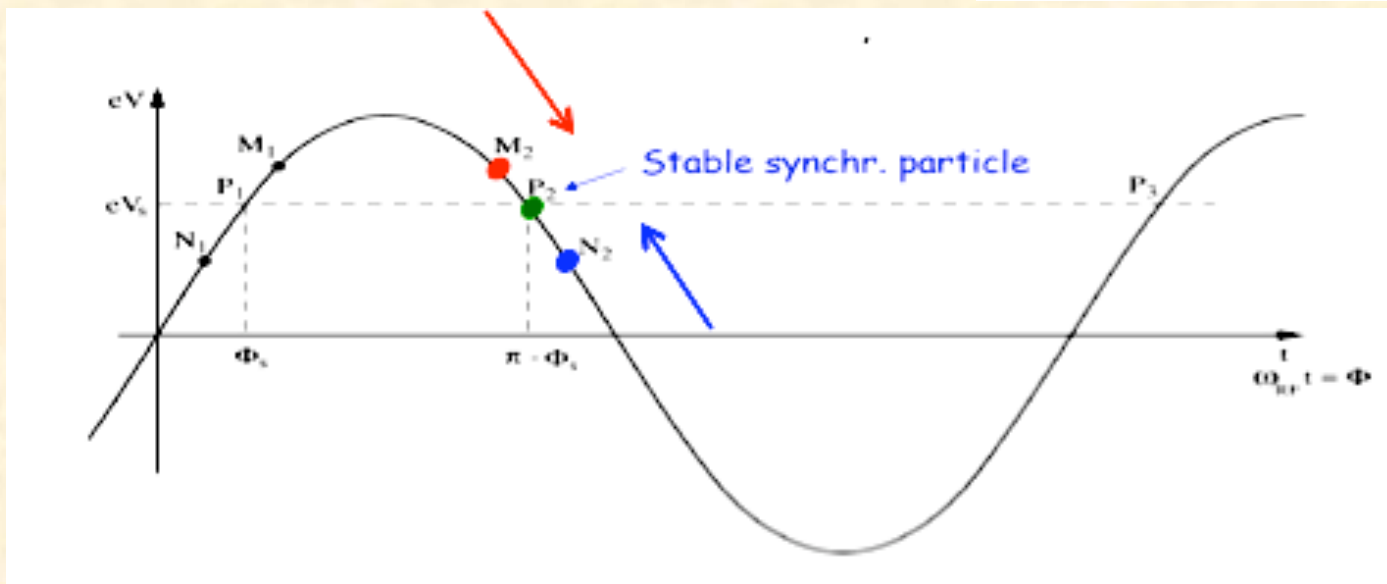
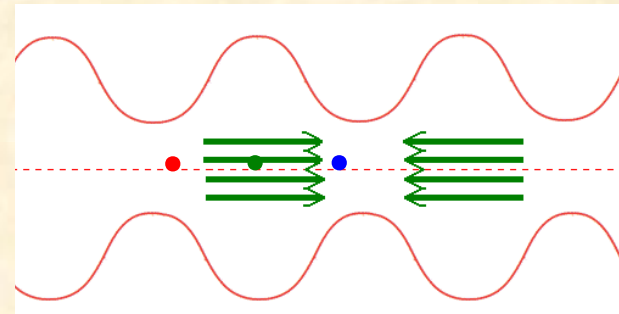
•

*heavier*

*particle with  $\Delta p/p < 0$*

•

*lighter*



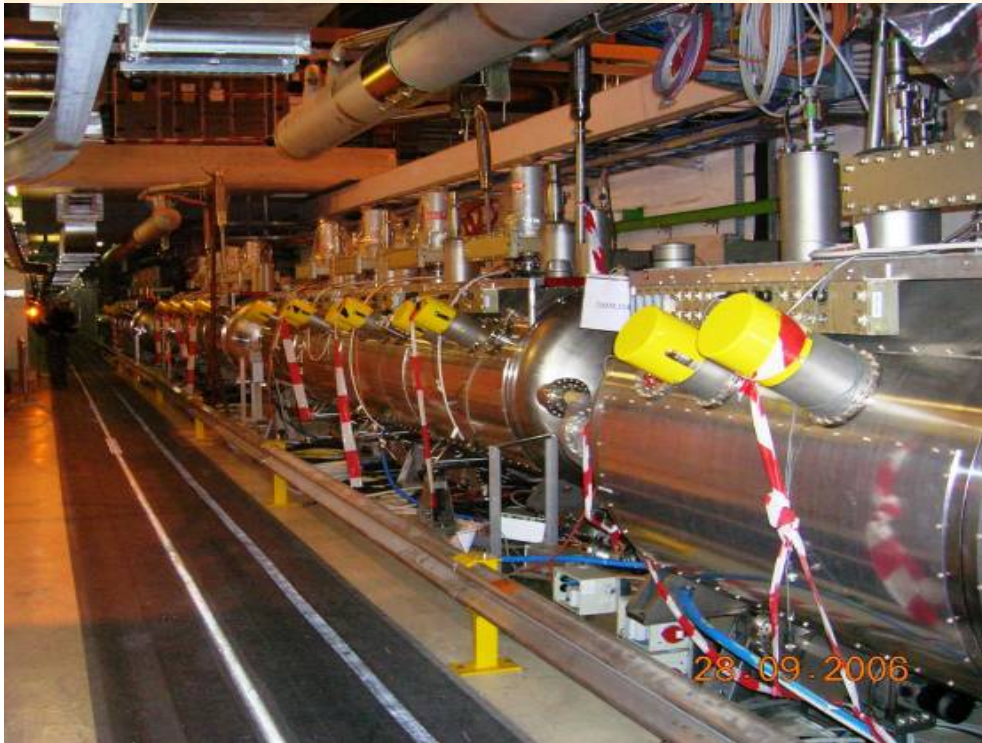
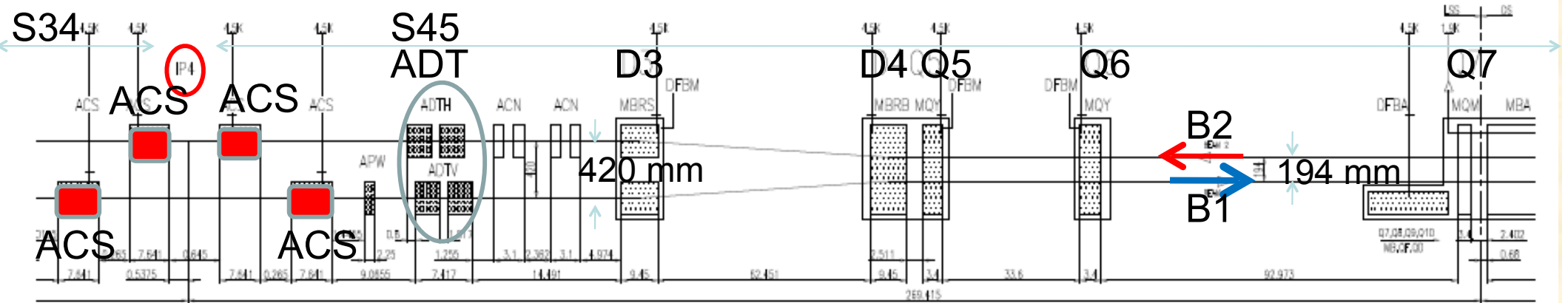
*Focussing effect in the longitudinal direction*

*keeping the particles close together ... forming a “bunch”*

*... and how do we accelerate now ???*

*with the dipole magnets !*

# The RF system: IR4



*Nb on Cu cavities @4.5 K (=LEP2)  
Beam pipe diam.=300mm*

Bunch length ( $4\sigma$ )	ns	1.06
Energy spread ( $2\sigma$ )	$10^{-3}$	0.22
Synchr. rad. loss/turn	keV	7
Synchr. rad. power	kW	3.6
RF frequency	MHz	400
Harmonic number		35640
RF voltage/beam	MV	16
Energy gain/turn	keV	485
Synchrotron frequency	Hz	23.0

## *1.) Where are we ?*

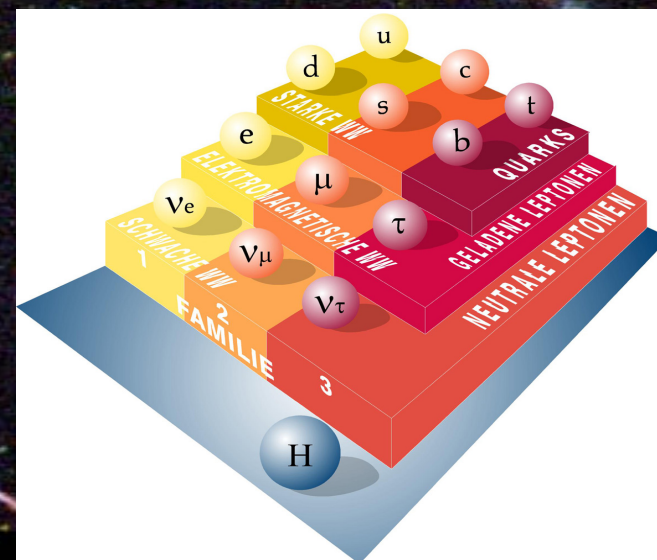
- \* Standard Model of HEP*
- \* Higgs discovery*



*What's next ???*

*Dark Matter & Dark Energy*

*Physics beyond the Standard Model*



**Hubble Deep Field**

PRC96-01a · ST ScI OPO · January 15, 1996 · R. Williams (ST ScI), NASA

HST · WFPC2

# What's next ???

## Dark Matter

*The outer region of galaxies rotate faster than expected from visible matter*

$$\frac{m \cdot v^2}{r} = \frac{m_1 \cdot M_2 \cdot G}{r^2}$$

$$v_{\text{circ}} = \sqrt{\frac{M_2(r) \cdot G}{r}}$$

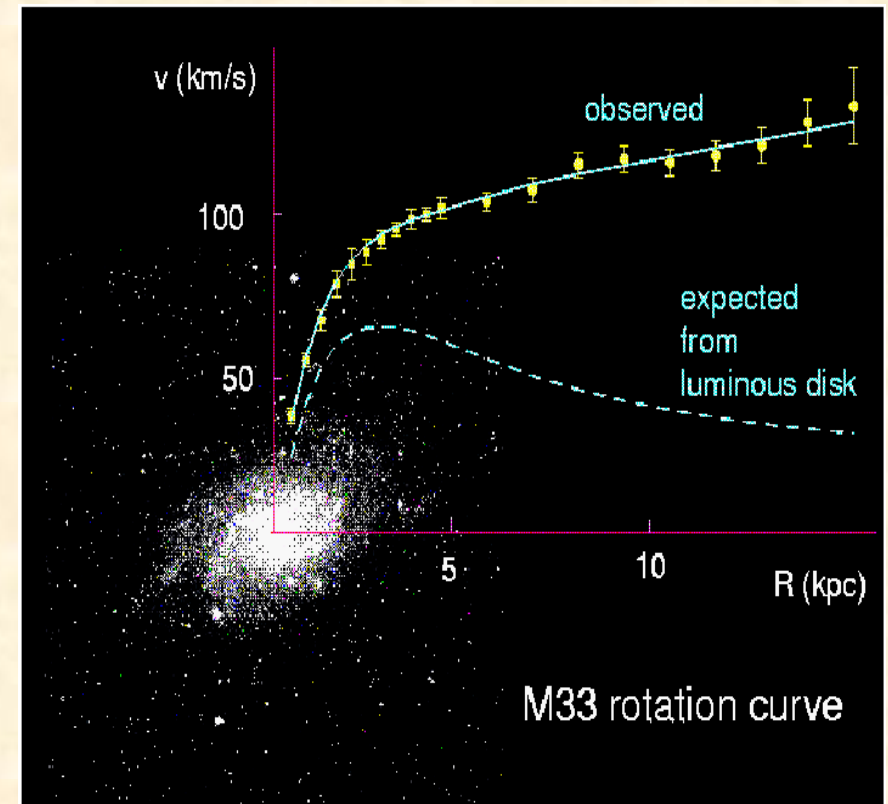
*Dark matter would explain this*

*Other observations exist ... (grav. lens effects)  
but all through gravity*

*What is it?*

*( One explanation is super-symmetry )*

Corbelli & Salucci (2000);  
Bergstrom (2000)





*Reconstruction of Dark Matter distribution based on observations*

*Budget:    Dark Matter: 26 %  
              Dark Energy: 70 %  
              Anything else (including us) 4 %*

court. Michael S. Turner  
Kavli Institute for Cosmological Physics  
The University of Chicago

# *Considered Future High Energy Frontier Colliders*

## *Circular colliders:*

*FCC (Future Circular Collider ... Euro-Circol)*

***FCC-hh**: 100 TeV proton-proton cm energy*

***FCC-ee**: Potential intermediate step 90-350 GeV lepton collider*

## *Linear colliders*

***ILC** (International Linear Collider):  $e^+e^-$ , 500 GeV cms energy,  
Japan considers hosting project*

***CLIC** (Compact Linear Collider):  $e^+e^-$ , 380GeV - 3TeV cms energy,  
CERN hosts collaboration*

## *Others*

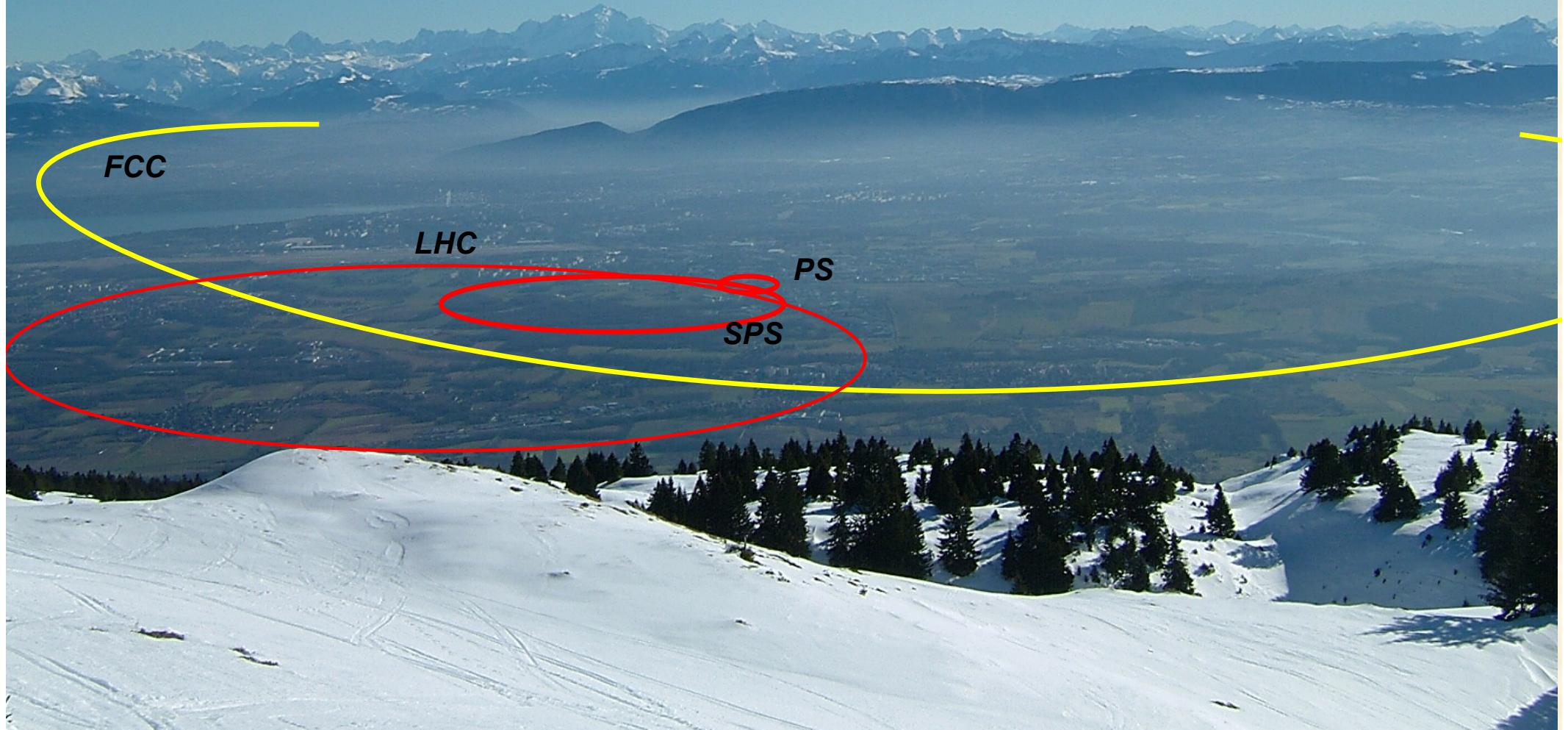
***Plasma acceleration***

*Muon collider, has been supported in the US but effort has stopped*

*Photon-photon collider*



# *The Next Generation Ring Collider*



**FCC**

**LHC**

**PS**

**SPS**