



DPF Meeting
Brown University
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Indiana University Center for Spacetime Symmetries

Three-Parameter Lorentz-Violating Model for Neutrino Oscillations

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Indiana University

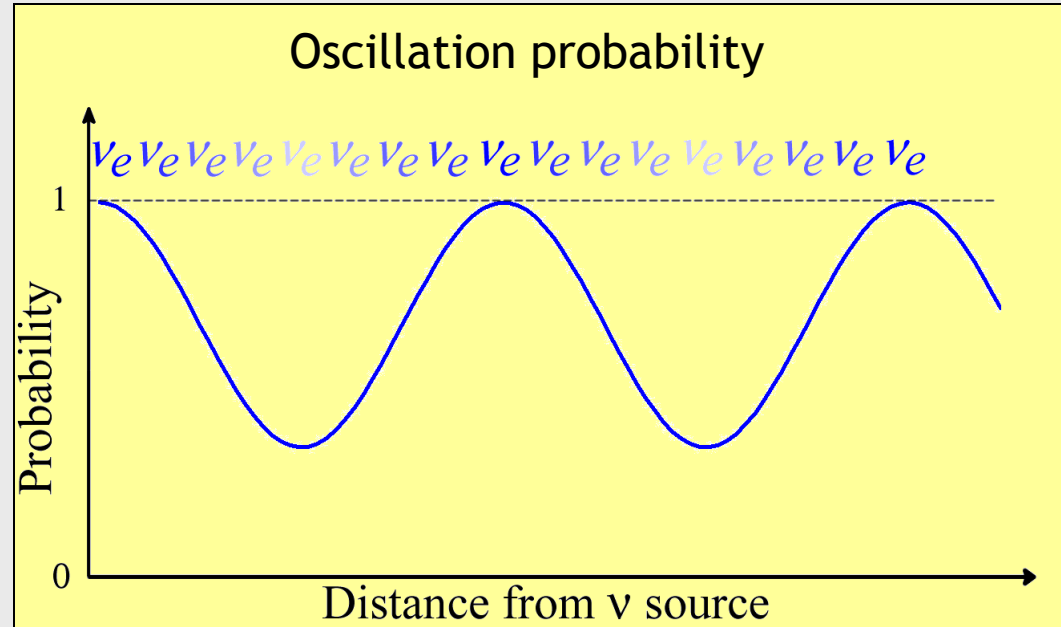
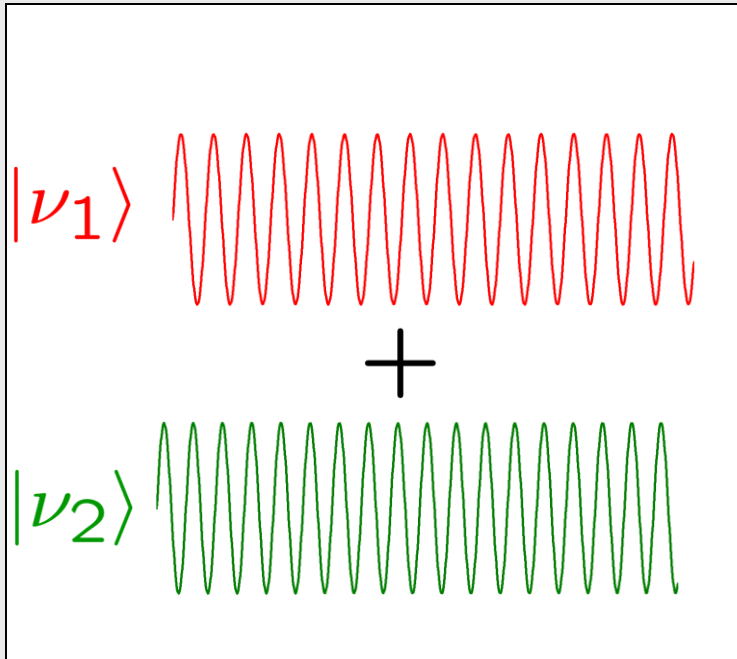
based on

JSD and V.A. Kostelecký, Phys. Lett. B 700, 25 (2011)
JSD and V.A. Kostelecký, arXiv:1108.1799

Outline

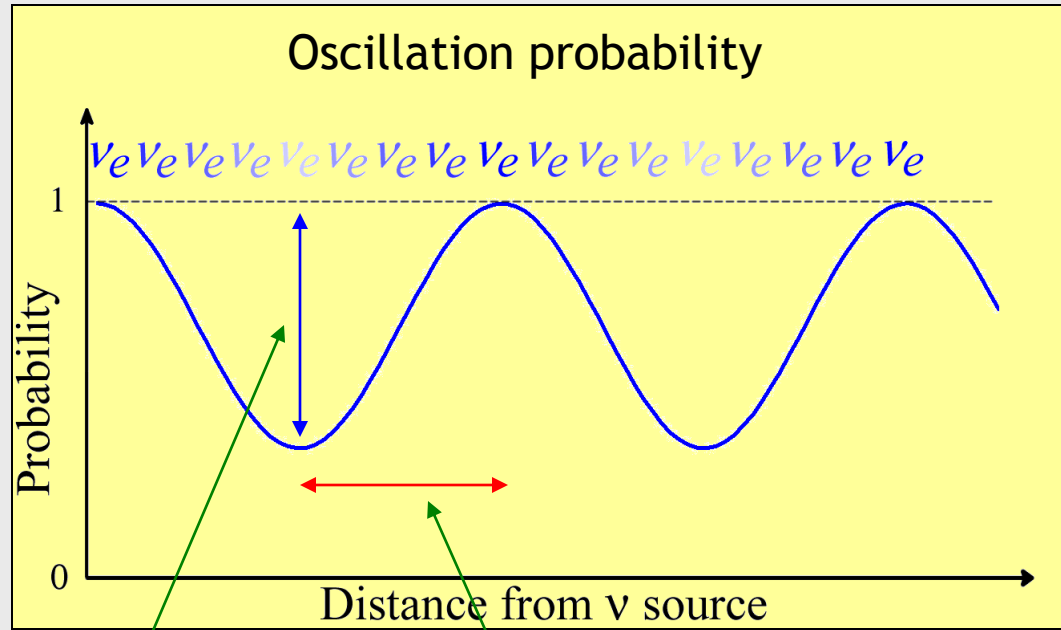
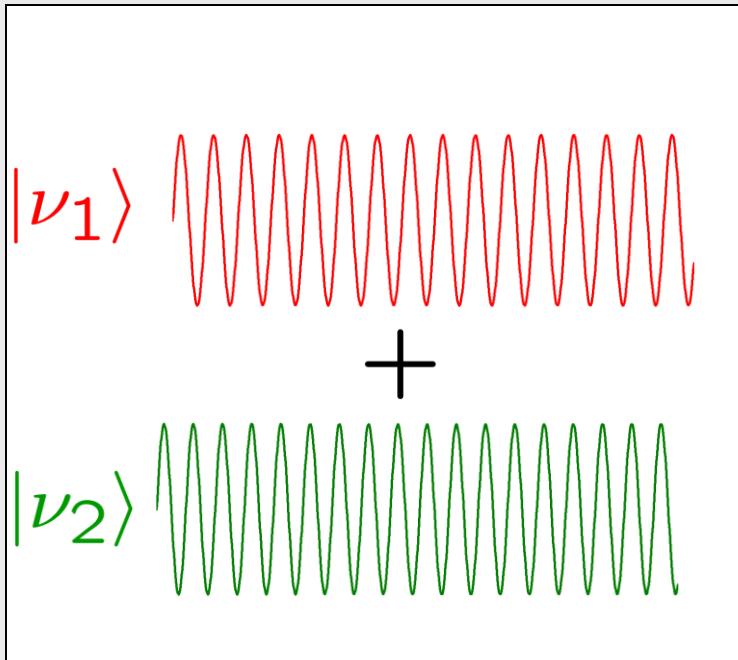
- Neutrino oscillations
 - Established evidence
 - Conventional Lorentz-invariant model
- Lorentz and CPT violation
 - Motivation and framework: the Standard-Model Extension (SME)
- Lorentz-violating model for neutrino oscillations
 - Theory
 - Experimental data and predictions
- Summary

Neutrino Oscillations



$$P_{\nu_a \rightarrow \nu_b}(L) = \sum_{jk} A_{jk}(U) \sin^2(\Delta_{jk}L/2)$$

Neutrino Oscillations



$$P_{\nu_a \rightarrow \nu_b}(L) = \sum_{jk} A_{jk}(U) \sin^2(\Delta_{jk}L/2)$$

Matrix that diagonalizes the hamiltonian

$$\Delta_{jk} = \lambda_j - \lambda_k \quad \text{eigenvalues of the hamiltonian}$$

Neutrino Oscillations: massive model (3ν SM)

Effective hamiltonian

$$h_{\text{eff}} = \frac{1}{2E} U^\dagger \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{\odot}^2 & 0 \\ 0 & 0 & \Delta m_{\text{atm}}^2 \end{pmatrix} U$$

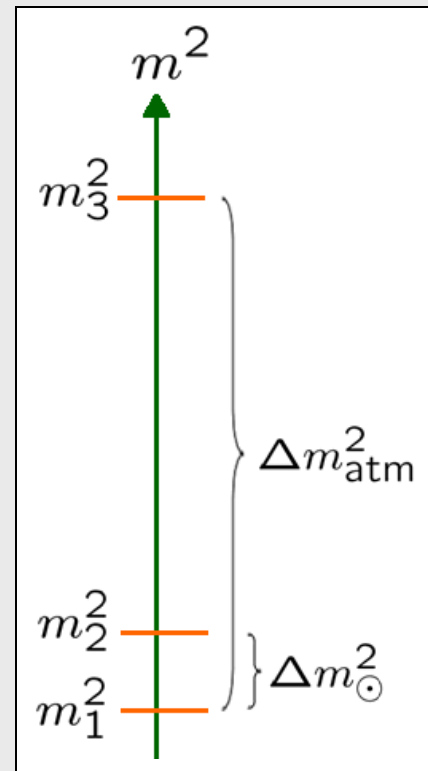
Properties:

- Lorentz and CPT invariant
- 3 massive neutrinos
- 5 parameters
- Energy-independent mixing

$$U = \begin{pmatrix} c_{12} & -s_{12} & 0 \\ s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} c_{13} & 0 & -s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & -s_{23} \\ 0 & s_{23} & c_{23} \end{pmatrix}$$

This model properly describes all the compelling results for neutrino oscillations

- atmospheric-neutrino disappearance (SK, K2K, MINOS, T2K)
- reactor-antineutrino disappearance (KamLAND)
- solar-neutrino deficit (SK, SNO, Borexino)

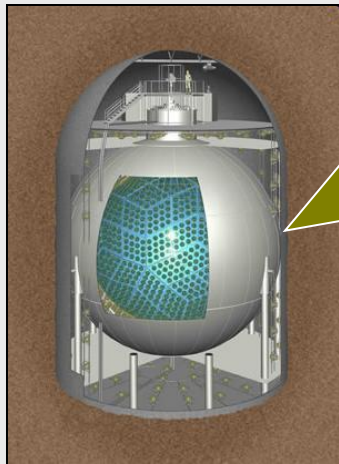


Neutrino Oscillations: massive model (3ν SM)

Low energy: reactor antineutrinos

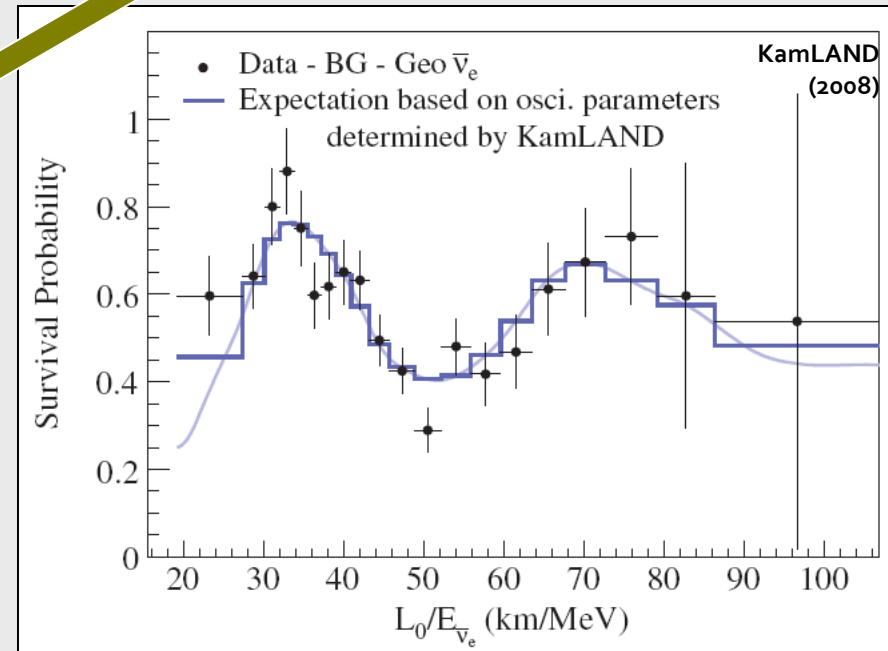
$$h_{\text{eff}} = \frac{1}{2E} U^\dagger \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{\odot}^2 & 0 \\ 0 & 0 & \Delta m_{\text{atm}}^2 \end{pmatrix} U$$

$$P_{\bar{\nu}_e \rightarrow \bar{\nu}_e} \simeq 1 - \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{\odot}^2 L}{4E} \right)$$



KamLAND

$\bar{\nu}_e$

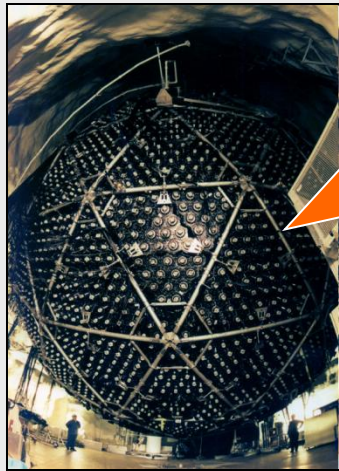
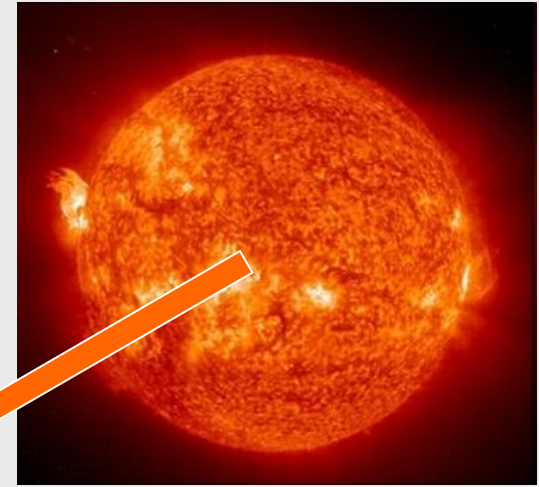


Neutrino Oscillations: massive model (3ν SM)

Low energy: solar neutrinos

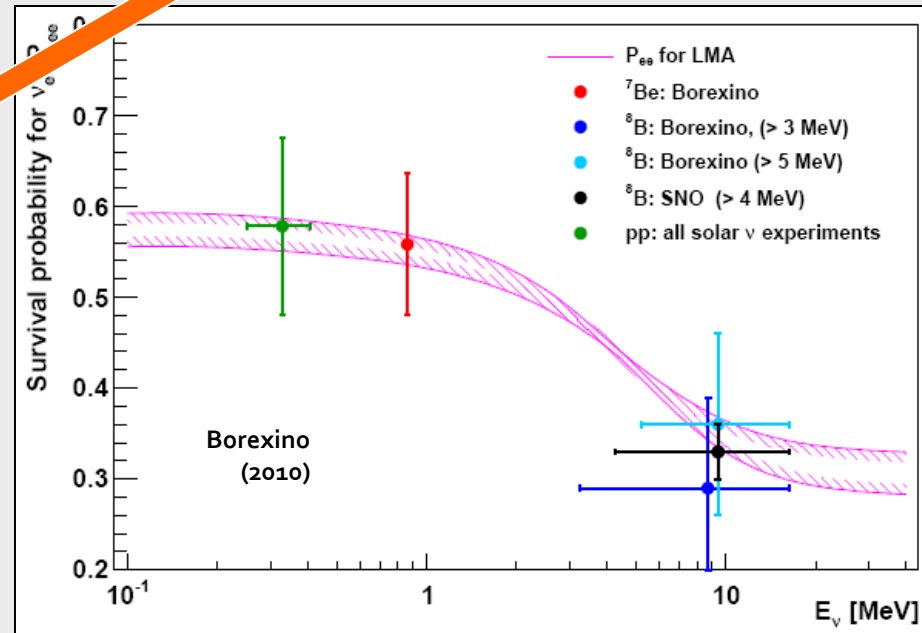
$$h_{\text{eff}} = \frac{1}{2E} U^\dagger \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{\odot}^2 & 0 \\ 0 & 0 & \Delta m_{\text{atm}}^2 \end{pmatrix} U + \begin{pmatrix} V_{\text{CC}} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\langle P_{\nu_e \rightarrow \nu_e} \rangle \simeq \frac{1}{2} + \frac{1}{2} \cos 2\theta_{12} \cos 2\theta_M(\Delta m_{\odot}^2, E, V_{\text{CC}})$$



SNO

ν_e

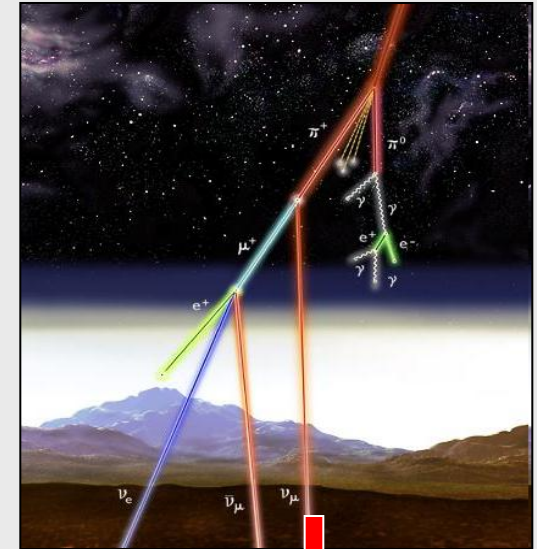


Neutrino Oscillations: massive model (3ν SM)

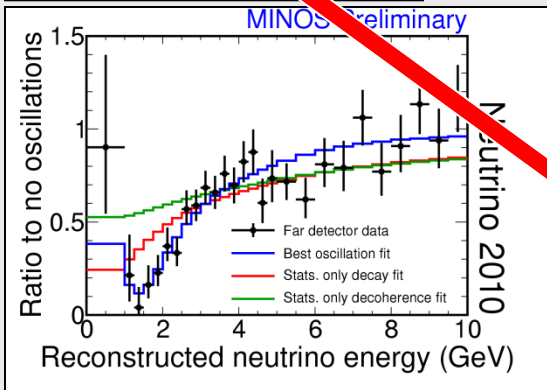
High energy: atmospheric neutrinos

$$h_{\text{eff}} = \frac{1}{2E} U^\dagger \begin{pmatrix} 0 & 0 & 0 \\ 0 & \cancel{\Delta m_{21}^2} & 0 \\ 0 & 0 & \Delta m_{\text{atm}}^2 \end{pmatrix} U$$

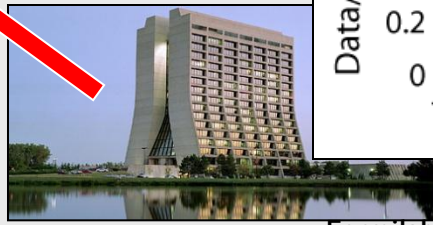
$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \sin^2 2\theta_{23} \sin^2 \left(\frac{\Delta m_{\text{atm}}^2 L}{4E} \right)$$



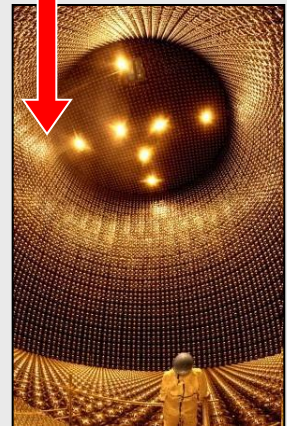
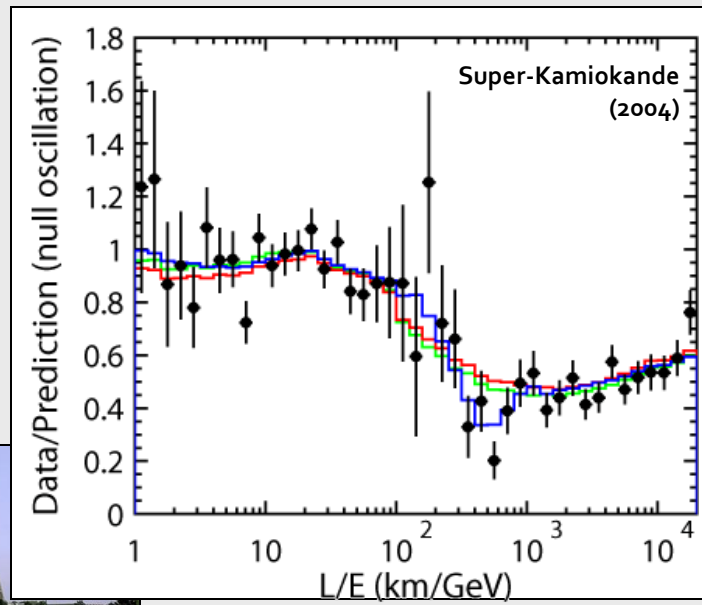
MINOS



ν_μ



Fermilab



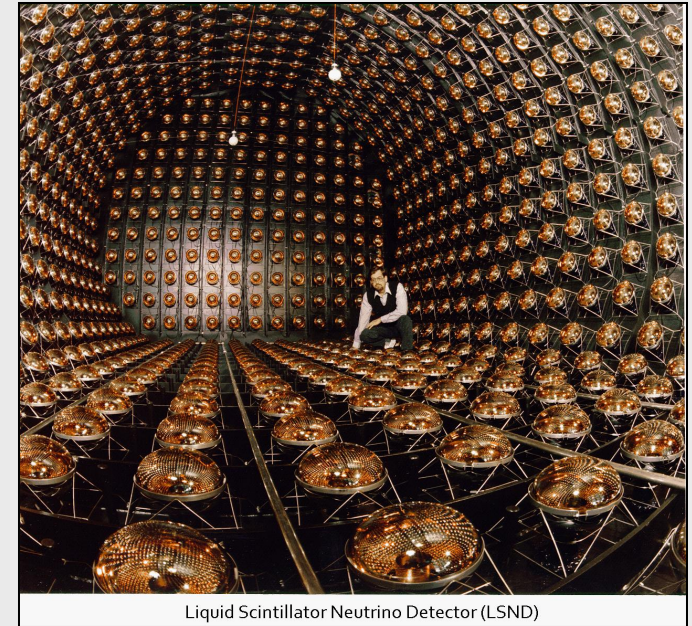
SK

ν_μ

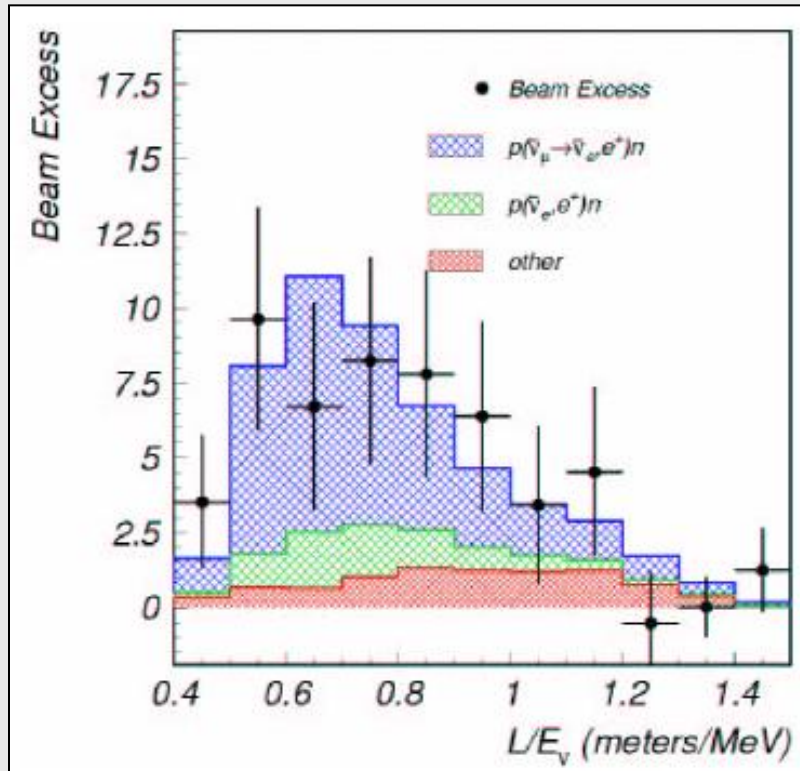
Neutrino Oscillations: anomalies

LSND (2001)

3.8 σ evidence of oscillations $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$



DNP



LSND 2001

If excess is due to oscillations then extra neutrino flavors are needed (sterile neutrinos)

$$\Delta m_{\text{LSND}}^2 \gg \Delta m_{\text{atm}}^2, \Delta m_{\odot}^2$$

Neutrino Oscillations: anomalies

MiniBooNE (2007,2010)

$$\nu_{\mu} \rightarrow \nu_e$$

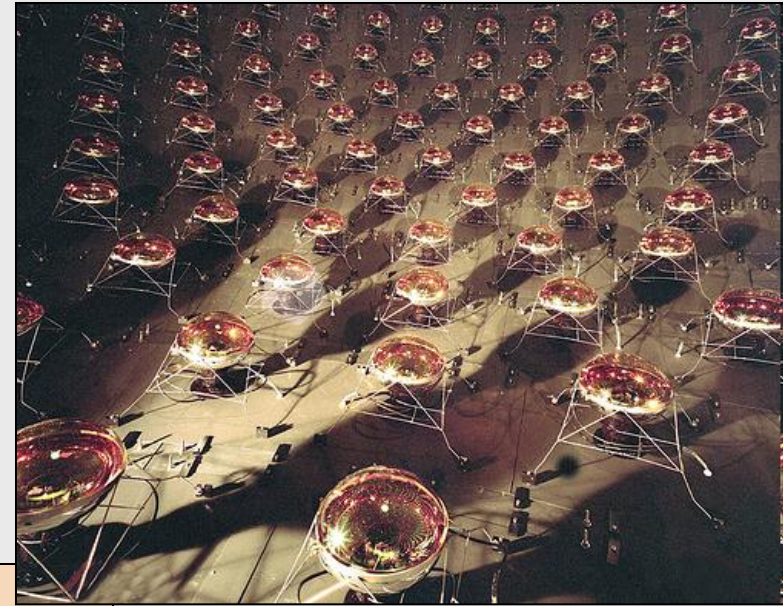
Neutrinos (2007):

- $E < 475$ MeV: unexplained 3.0σ excess
- $E > 475$ MeV: no signals of oscillations

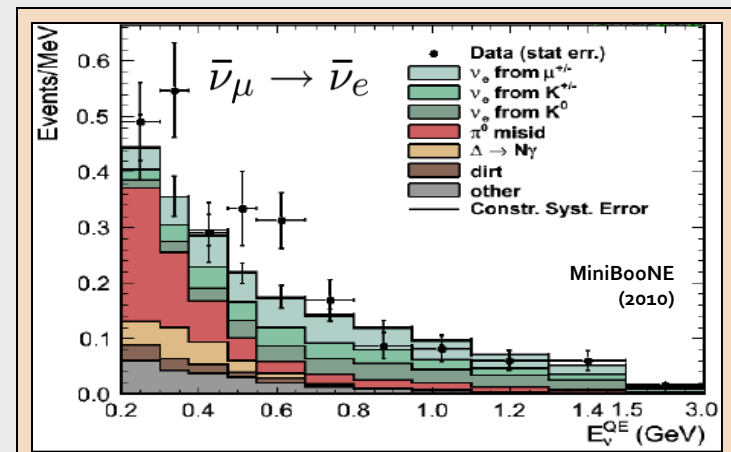
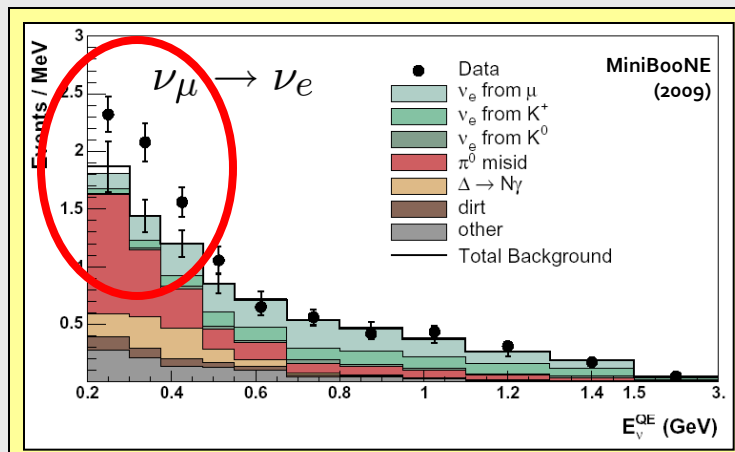
$$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$$

Antineutrinos (2010):

- $E < 475$ MeV: 1.3σ excess
- $E > 475$ MeV: signal consistent with LSND (99.4%CL)



MiniBooNE



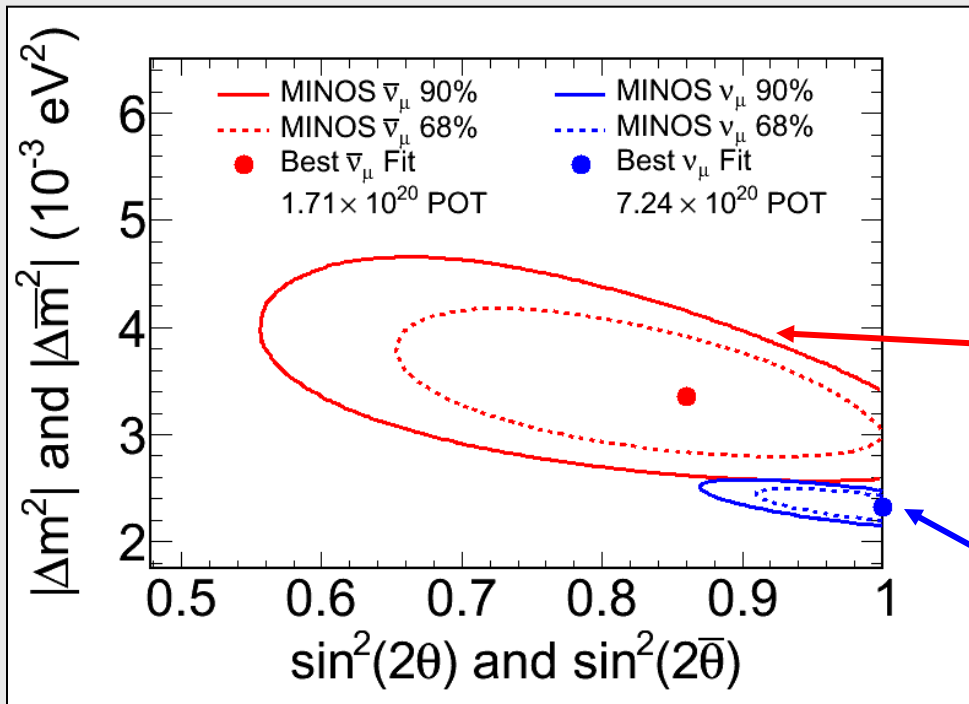
Neutrino Oscillations: anomalies

MINOS (2010)

Preliminary data is inconsistent with the 3ν SM: oscillation parameters for neutrinos and antineutrinos must be equal.



MINOS



antineutrinos




neutrinos

MINOS (2011)





Neutrino Oscillations: results summary

Established data

3ν SM

Atmospheric neutrinos	L/E oscillation signature	
Reactor antineutrinos	L/E oscillation signature	
Solar neutrinos	MSW-LMA signature (matter effects)	

Anomalies

LSND	Oscillation signal	
MiniBooNE 2007	Low-energy excess	
MiniBooNE 2010	Behavior $\nu \neq \bar{\nu}$	
MINOS	Behavior $\nu \neq \bar{\nu}$	

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Lorentz violation

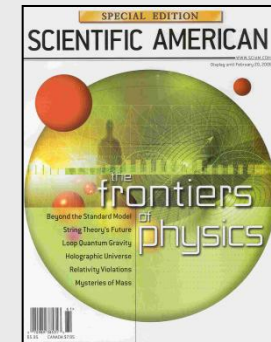
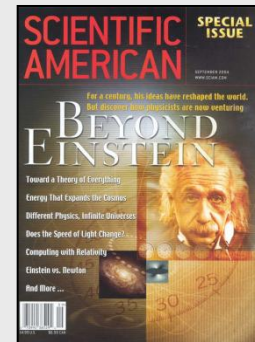
Last 20 years, growing interest in the possibility that Lorentz symmetry may not be exact.

- Quantum gravity candidates involve the breaking of Lorentz symmetry

Kostelecký & Samuel, PRD 1989

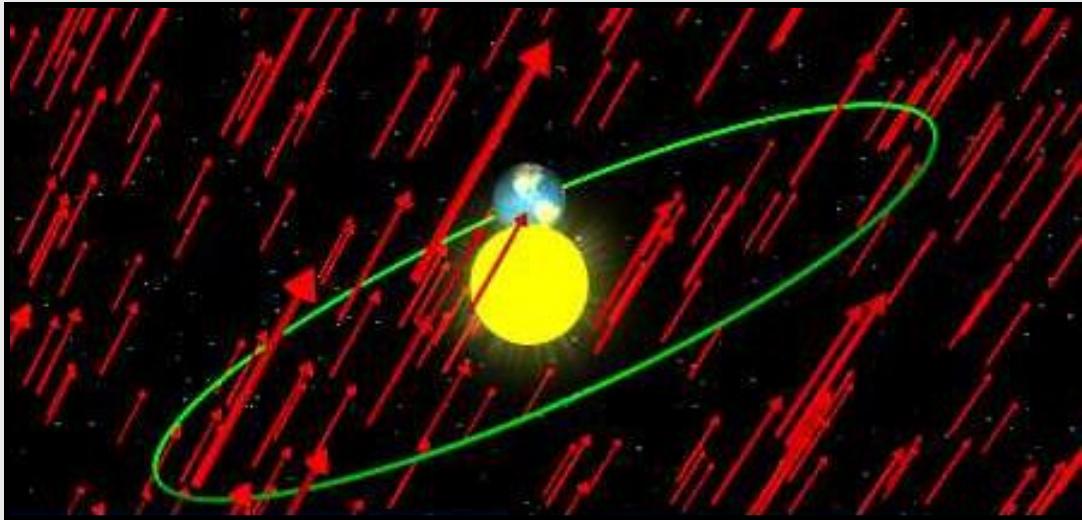
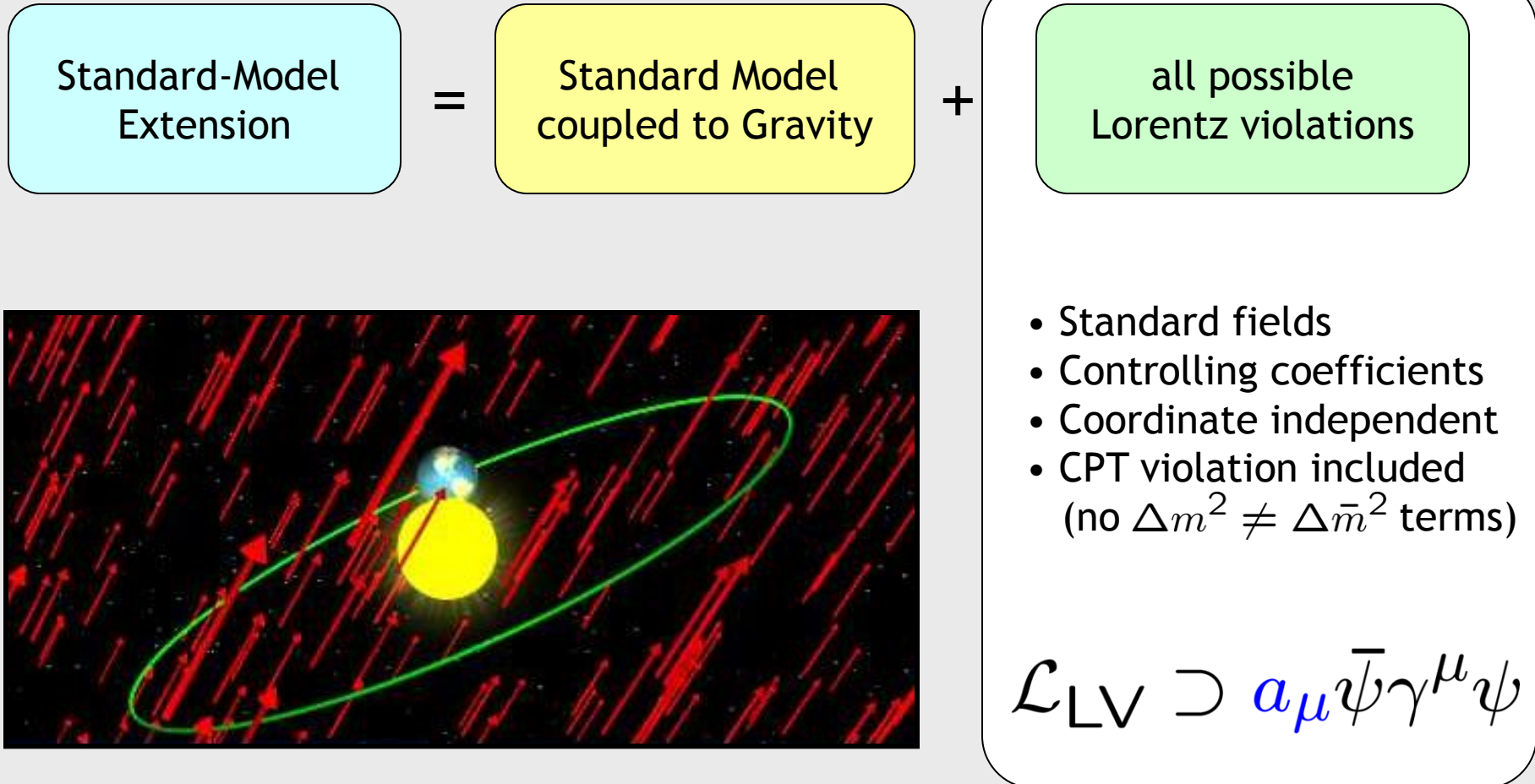
Kostelecký & Potting, NPB 1991

- Lorentz symmetry is a basic building block of both General Relativity (GR) and the Standard Model (SM). Anything this fundamental should be tested.



Standard-Model Extension

Colladay & Kostelecký, PRD 1997
Colladay & Kostelecký, PRD 1998
Kostelecký, PRD 2004



SME: worldwide searches

[K⁰-K⁰ oscillations](#)

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[D⁰-D⁰ oscillations](#)

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[Neutrino oscillations](#)

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SME: the neutrino sector

Kostelecký & Mewes (PRD 2004a)
Kostelecký & Mewes (in preparation)

Effective hamiltonian for neutrinos (3x3 matrix) ← three left-handed neutrinos

$$(h_{\text{eff}})_{ab} = \frac{1}{2E} (\tilde{m}^2)_{ab} + \underbrace{(a_L)_{ab}^\alpha \hat{p}_\alpha}_{\text{Lorentz invariant}} - \underbrace{(c_L)_{ab}^{\alpha\beta} p_\alpha \hat{p}_\beta}_{\text{Lorentz violating}}$$

$a, b = e, \mu, \tau$

CPT odd **CPT even**

Models based on this general effective hamiltonian

- bicycle model (Kostelecký et al., 2004)
- tandem model (Katori et al., 2006)
- BMW model (Barger et al., 2007)
- puma model (JSD et al., 2010) rest of this talk
- isotropic bicycle model (Barger et al., 2011) ← talk by K. Whisnant
- many others...

Search for key signals of Lorentz violation

- sidereal variations: LSND, MiniBooNE, MINOS (2), IceCube

Lorentz-violating Neutrino Oscillations: puma model

JSD & V.A. Kostelecký
PLB 2011
& arXiv:1108.1799



- Isotropic (no direction dependence)
- Includes nonrenormalizable terms
- Three real parameters

Puma model

$$h_{\text{eff}} = A \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} + B \begin{pmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} + C \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$A = m^2/2E, \quad B = aE^2, \quad C = cE^5$$

“[the model] was discovered by a systematic hunt through the jungle of possible SME-based models.”

Lorentz-violating Neutrino Oscillations: puma model

JSD & V.A. Kostelecký
PLB 2011
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Low energy

$$h_{\text{eff}} = A \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} + B \begin{pmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} + C \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$A = m^2/2E,$$

$$B = aE^2,$$

$$C = cE^5$$

- mass term dominates
- L/E oscillation signature
- symmetries: Lorentz, CPT, S_3
- tri-bimaximal mixing
- consistent with KamLAND data
- consistent with solar data

$$\Delta m_{\odot}^2 \rightarrow m^2$$

$$\theta_{12} \rightarrow \text{given by texture}$$

Lorentz-violating Neutrino Oscillations: puma model

JSD & V.A. Kostelecký
 PLB 2011
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Low energy

$$h_{\text{eff}} = A \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} + B \begin{pmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} + C \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\begin{aligned} A &= m^2/2E, \\ B &= aE^2, \\ C &= cE^5 \end{aligned}$$

- mass term dominates
- L/E oscillation signature
- symmetries: Lorentz, CPT, S_3
- tri-bimaximal mixing
- consistent with KamLAND data
- consistent with solar data

$$U \simeq \begin{pmatrix} \frac{2}{\sqrt{6}} & \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{6}} \\ \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} \\ 0 & -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

$$\Delta m_{\odot}^2 \rightarrow m^2$$

$$\theta_{12} \rightarrow \text{given by texture}$$

Lorentz-violating Neutrino Oscillations: puma model

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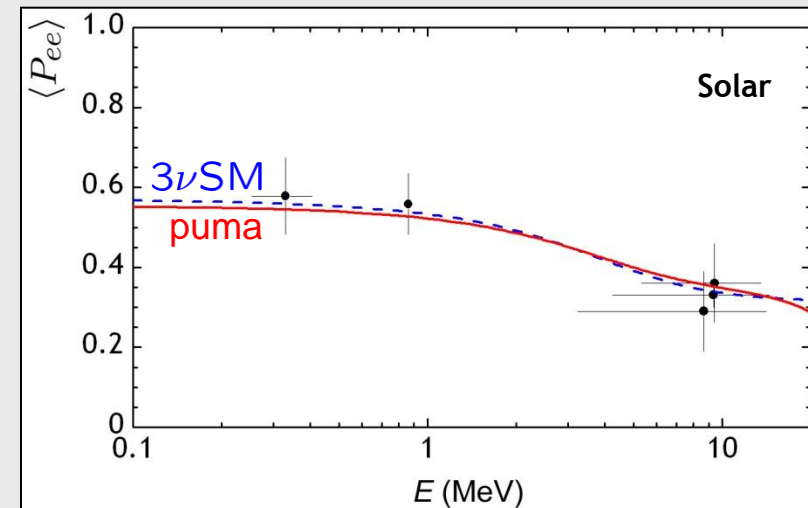
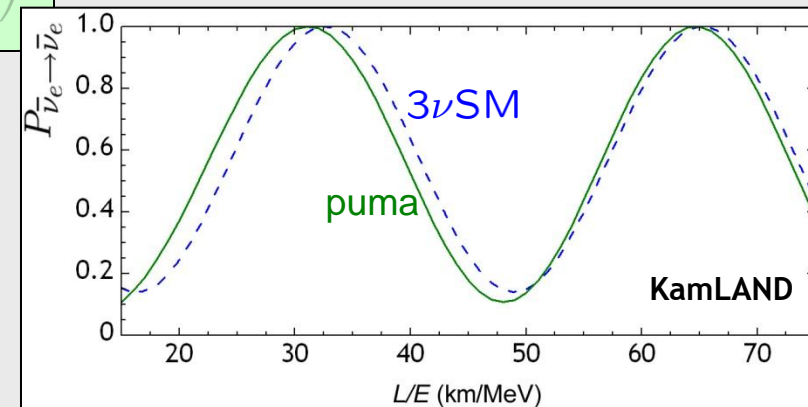
Low energy

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$$\begin{aligned} A &= m^2/2E, \\ B &= aE^2, \\ C &= cE^5 \end{aligned}$$

- mass term dominates
- L/E oscillation signature
- symmetries: Lorentz, CPT, S_3
- tri-bimaximal mixing
- consistent with KamLAND data
- consistent with solar data

$$\begin{aligned} \Delta m_{\odot}^2 &\rightarrow m^2 \\ \theta_{12} &\rightarrow \text{given by texture} \end{aligned}$$



Lorentz-violating Neutrino Oscillations: puma model

JSD & V.A. Kostelecký
PLB 2011
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High energy

$$h_{\text{eff}} = A \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} + B \begin{pmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} + C \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$A = m^2/2E,$$

$$B = aE^2,$$

$$C = cE^5$$

- no masses
- Lorentz-violating see-saw mechanism
- L/E oscillation signature
- symmetries: S_2
- maximal mixing
- consistent with SK, K2K, MINOS, T2K

Lorentz-violating see-saw mechanism

$$\lambda_1 = \frac{1}{2} \left(B + C - \sqrt{(B + C)^2 + 8B^2} \right) \\ \approx -\frac{2B^2}{C} = -\frac{2a^2}{cE}$$

$$\Delta m_{\text{atm}}^2 \rightarrow a^2/c$$

Lorentz-violating Neutrino Oscillations: puma model

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 PLB 2011
 & arXiv:1108.1799



High energy

$$h_{\text{eff}} = A \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} + B \begin{pmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} + C \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\begin{aligned} A &= m^2/2E, \\ B &= aE^2, \\ C &= cE^5 \end{aligned}$$

- no masses
- Lorentz-violating see-saw mechanism
- L/E oscillation signature
- symmetries: S_2
- maximal mixing
- consistent with SK, K2K, MINOS, T2K

Lorentz-violating seesaw mechanism

$$\begin{aligned} \lambda_1 &= \frac{1}{2} \left(B + C - \sqrt{(B + C)^2 + 8B^2} \right) \\ &\approx -\frac{2B^2}{C} = -\frac{2a^2}{cE} \end{aligned}$$

$$h_{\text{eff}} \approx B \begin{pmatrix} e & \mu & \tau \\ 1 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} + C \begin{pmatrix} e & \mu & \tau \\ 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$\mu\tau$ symmetry produces maximal mixing

$$\begin{aligned} \Delta m_{\text{atm}}^2 &\rightarrow a^2/c \\ \theta_{23} &\rightarrow \text{given by texture} \end{aligned}$$

Lorentz-violating Neutrino Oscillations: puma model

JSD & V.A. Kostelecký
 PLB 2011
 & arXiv:1108.1799



High energy

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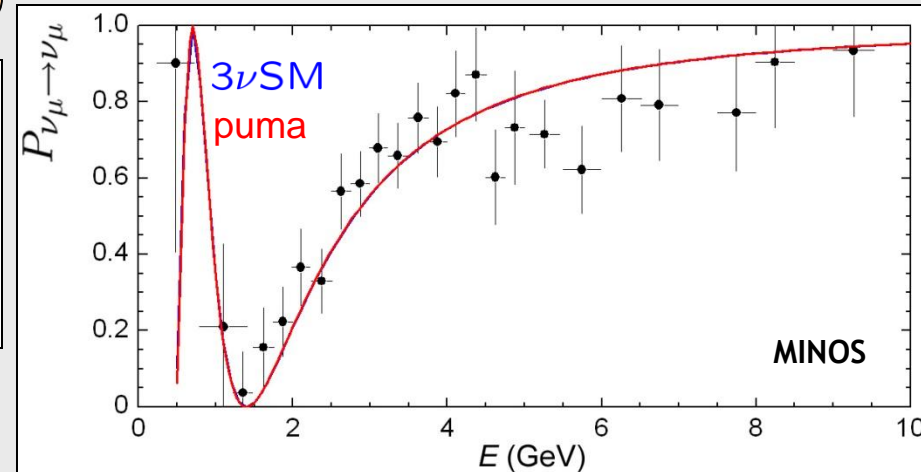
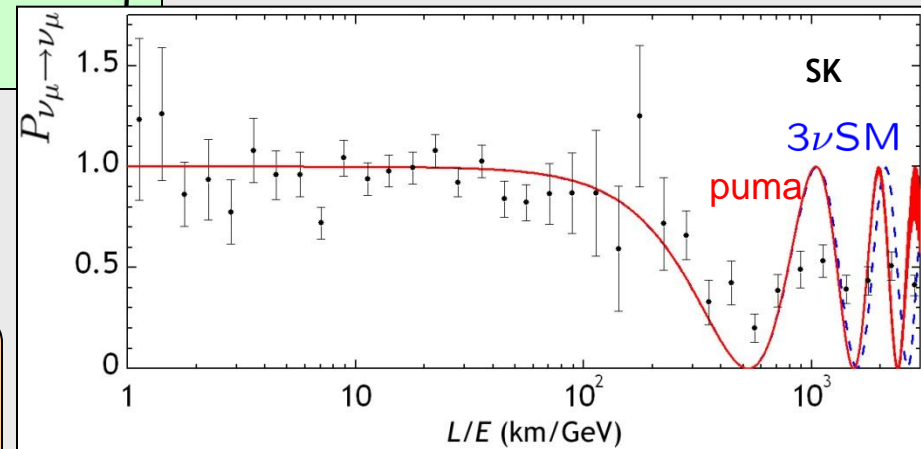
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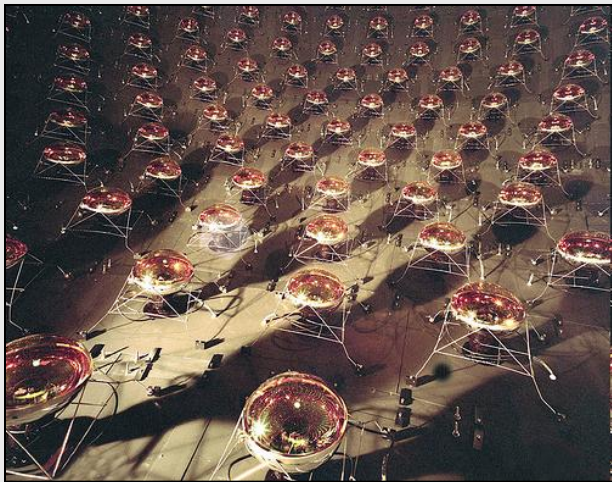


Remarkable natural feature:

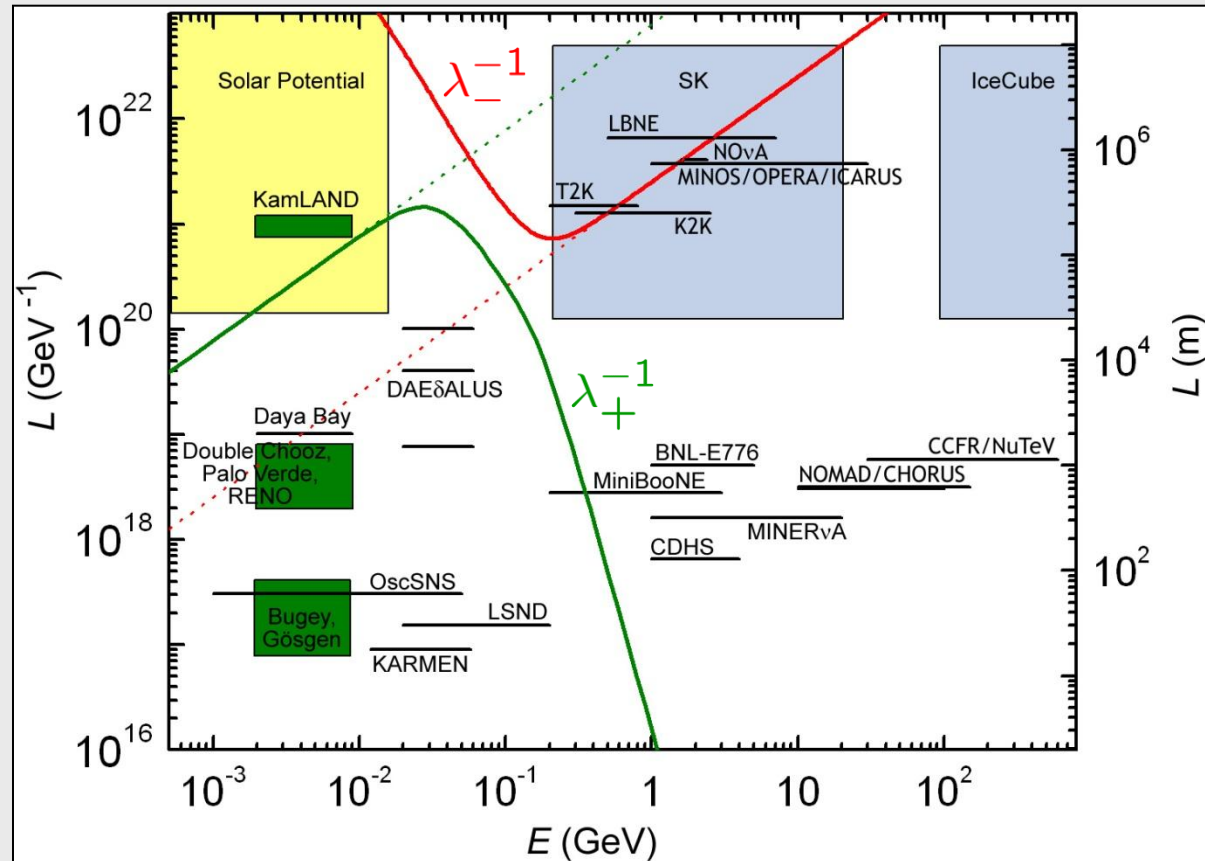
Low-energy signal in MiniBooNE

$$P_{\nu_{\mu} \rightarrow \nu_e} \simeq A_{21}(U) \sin^2(\lambda_+ L/2)$$

Kostelecký & Mewes, PRD 2004



MiniBooNE



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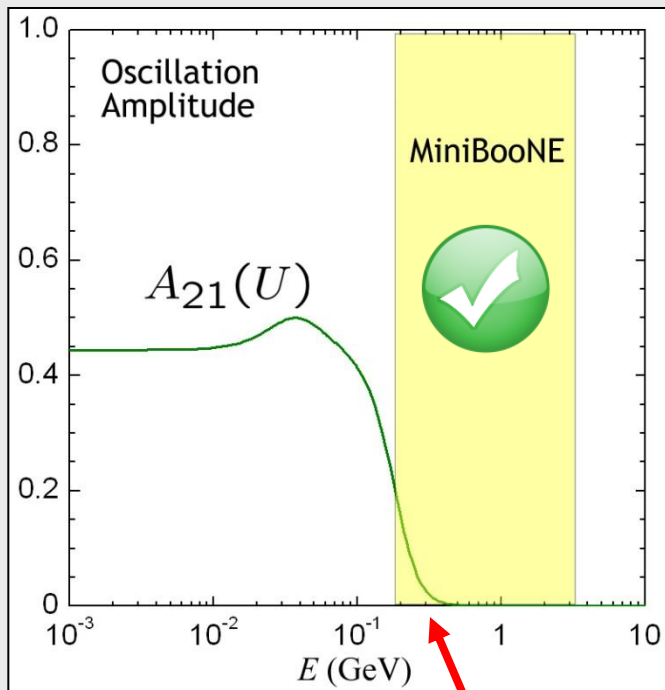


Remarkable natural feature:

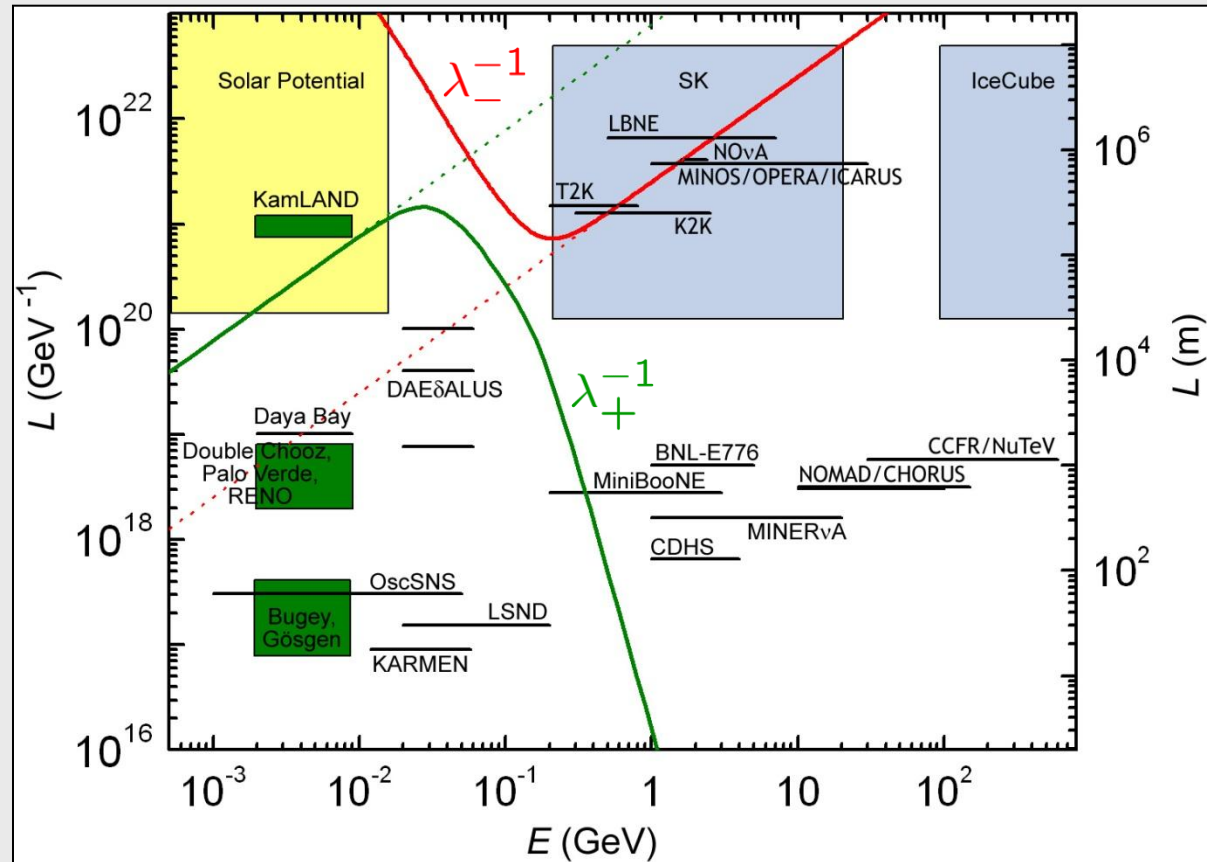
Low-energy signal in MiniBooNE

$$P_{\nu_{\mu} \rightarrow \nu_e} \simeq A_{21}(U) \sin^2(\lambda_+ L/2)$$

Kostelecký & Mewes, PRD 2004



signal at low energy only



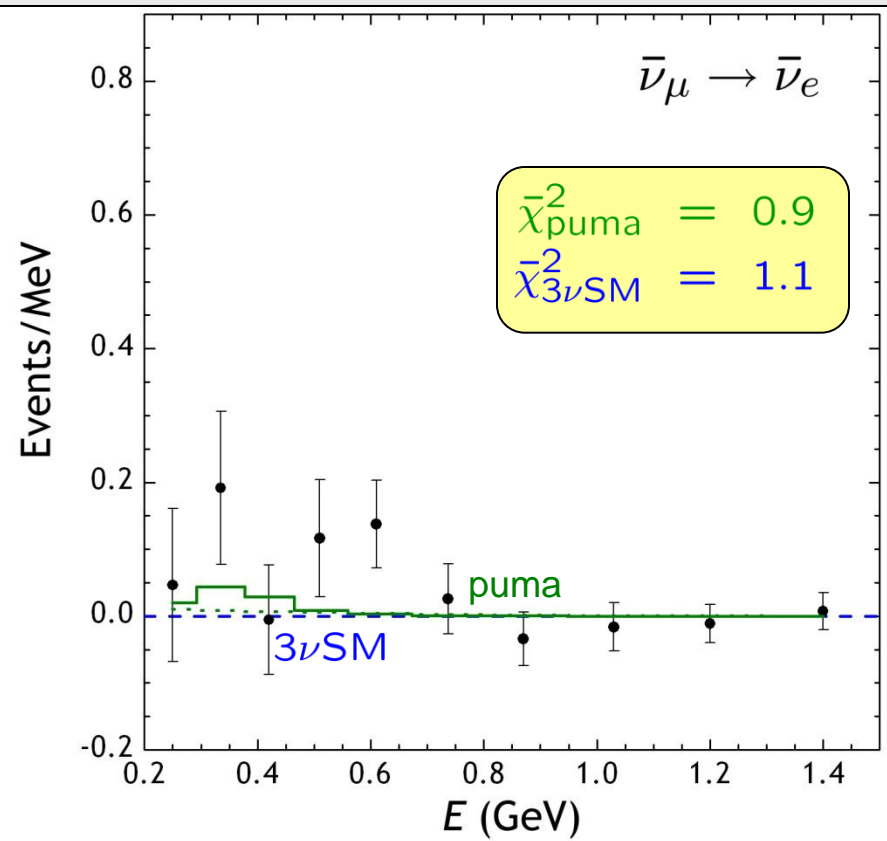
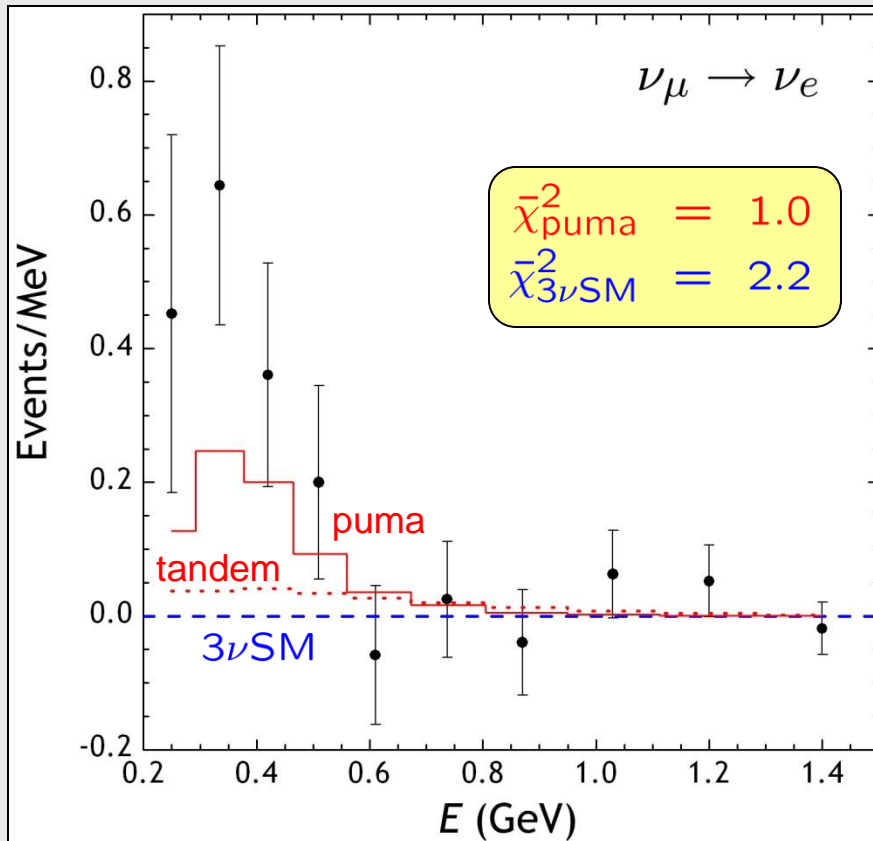
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Remarkable natural feature:

Low-energy signal in MiniBooNE



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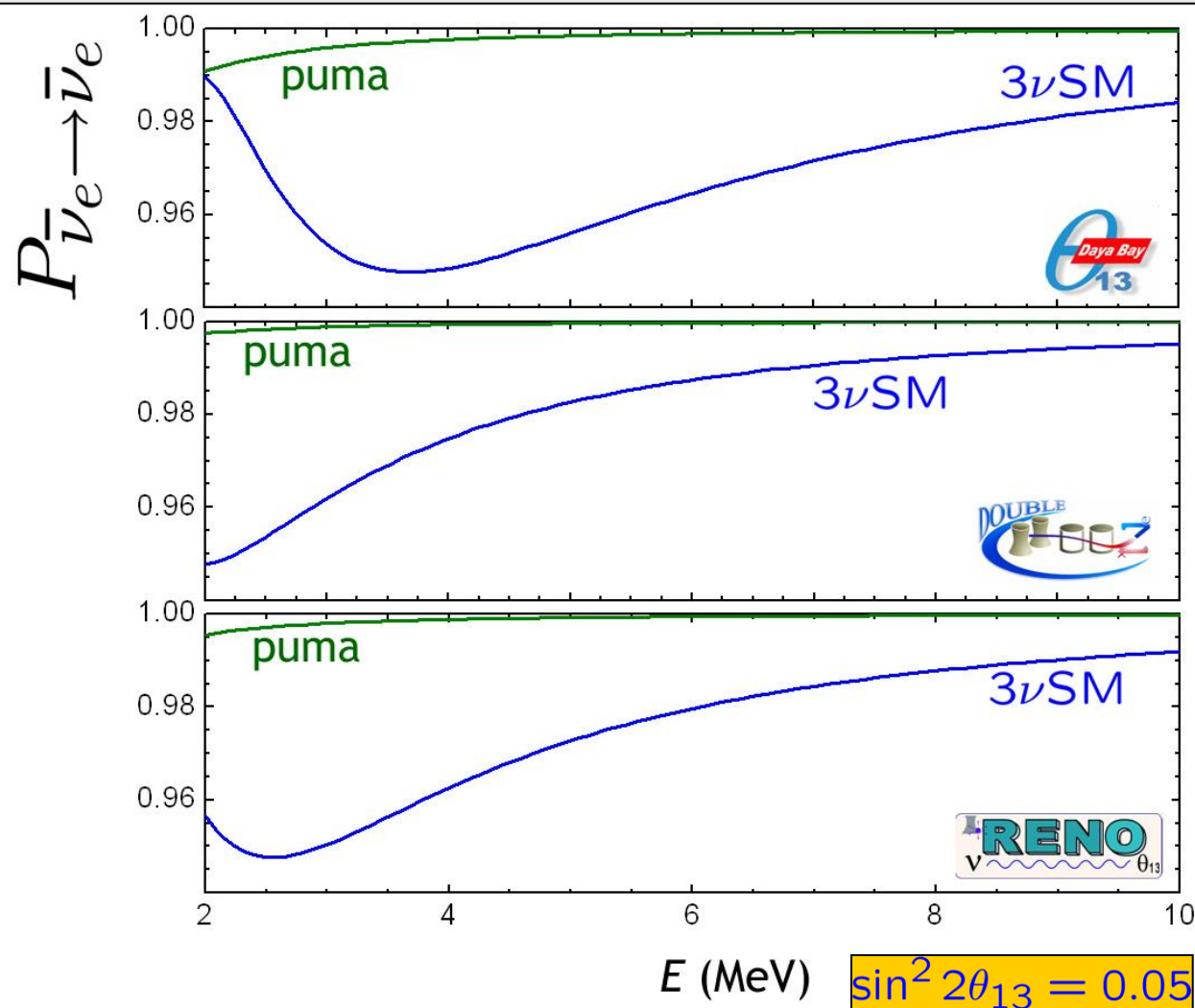
Predictions: new reactor experiments

Oscillation signals in
 Daya Bay, Double
 Chooz, and RENO
 driven by the solar
 mass term

Tribimaximal mixing
 at low energy

$$U \simeq \begin{pmatrix} 2 & 1 & 1 \\ -\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{6}} \\ 1 & 1 & 1 \\ \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} \\ 0 & 1 & 1 \\ -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

$\sin \theta_{13}$



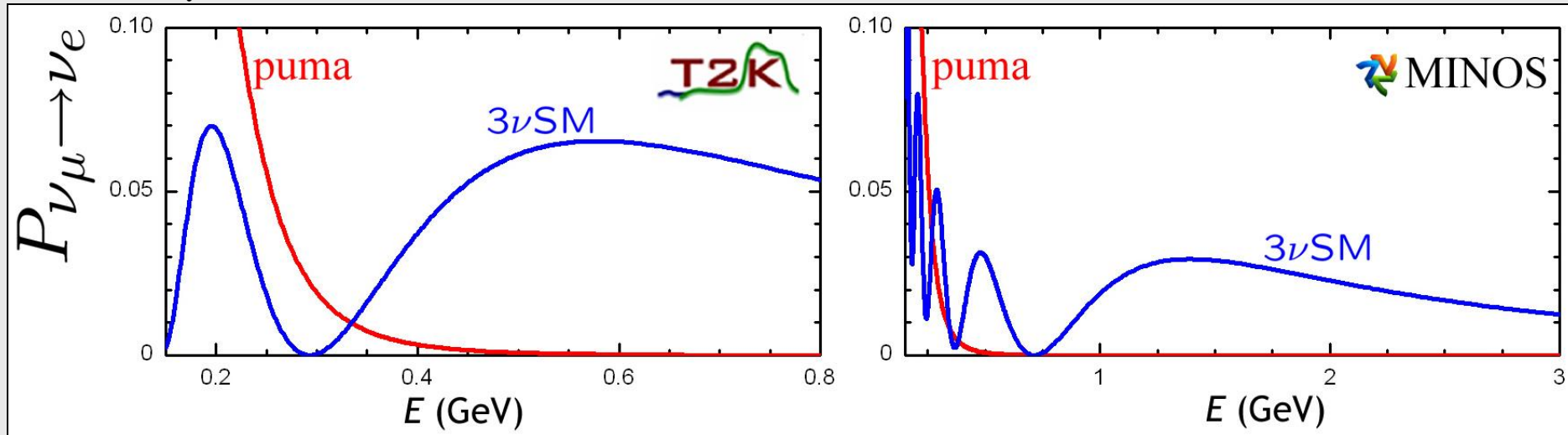
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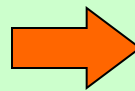


Predictions: long-baseline experiments

$$\nu_{\mu} \rightarrow \nu_e$$



Appearance signal
decreases with energy



$\sin^2 2\theta_{13}$ will be smaller in
MINOS compared to T2K

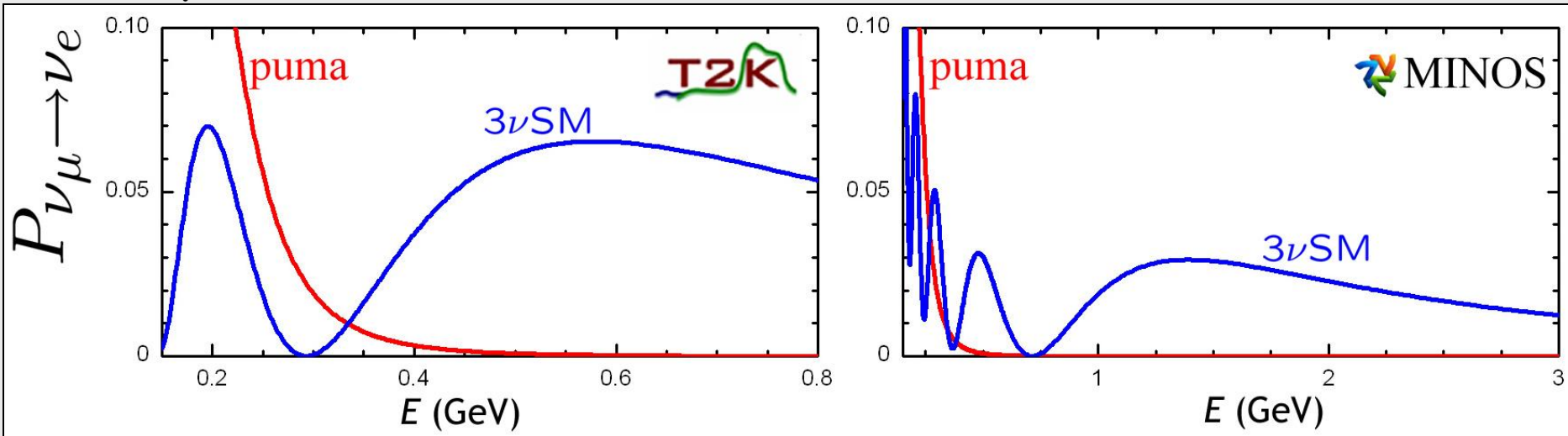
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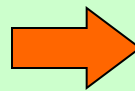


Predictions: long-baseline experiments

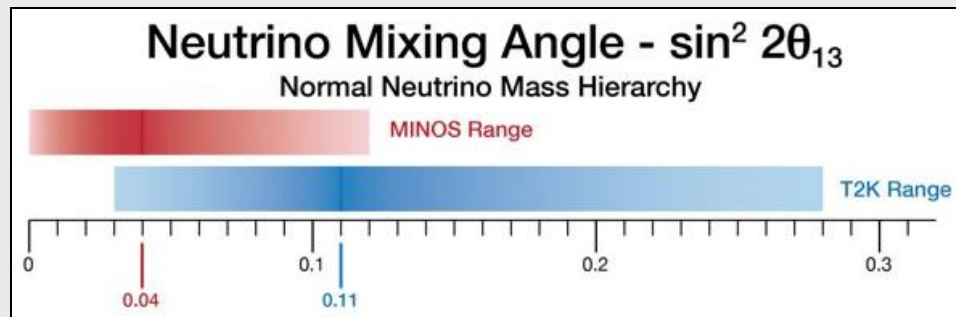
$$\nu_\mu \rightarrow \nu_e$$



Appearance signal decreases with energy



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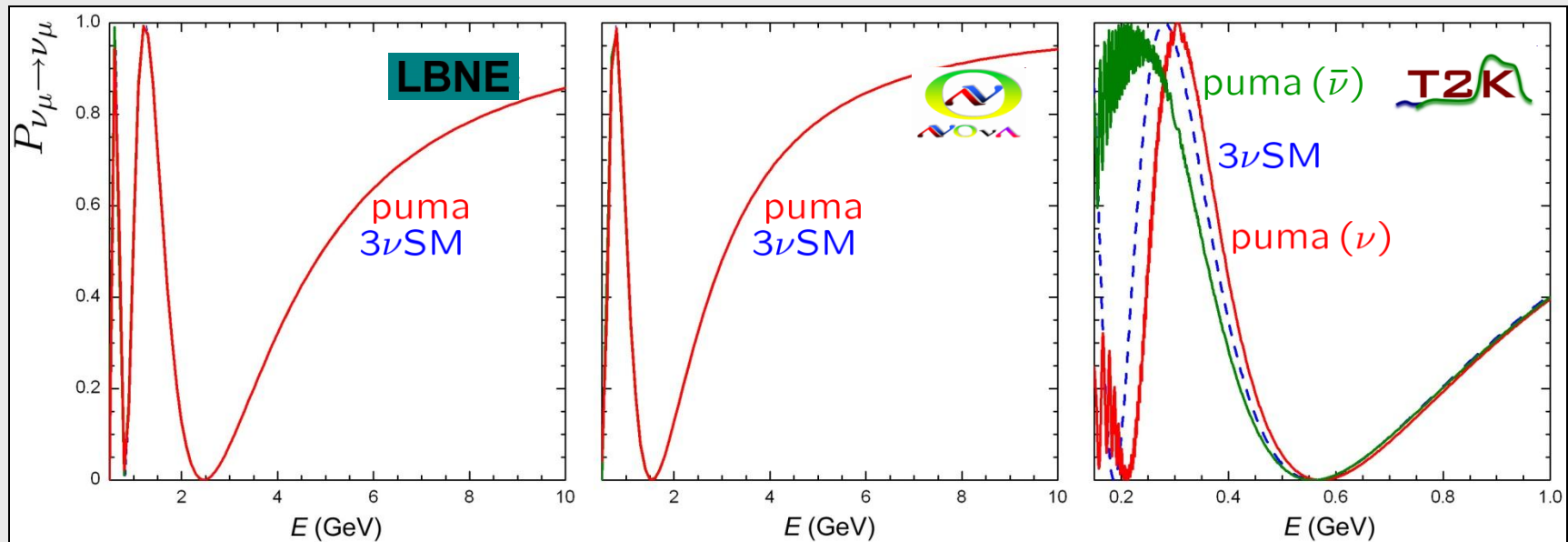
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Predictions: new long-baseline experiments

$$\nu_{\mu} \rightarrow \nu_{\mu}$$



Conventional signal

Conventional signal

Unconventional signal

LSND: enhanced puma

JSD & V.A. Kostelecký
PLB 2011
& arXiv:1108.1799



- Our model does not include LSND
- We should explore possible extensions

$$h_{\text{eff}}^{\bar{\nu}} = A \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} + \bar{B} \begin{pmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} + \bar{C} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\bar{f}(E) = \alpha e^{-\beta(E-E_0)^2}$$

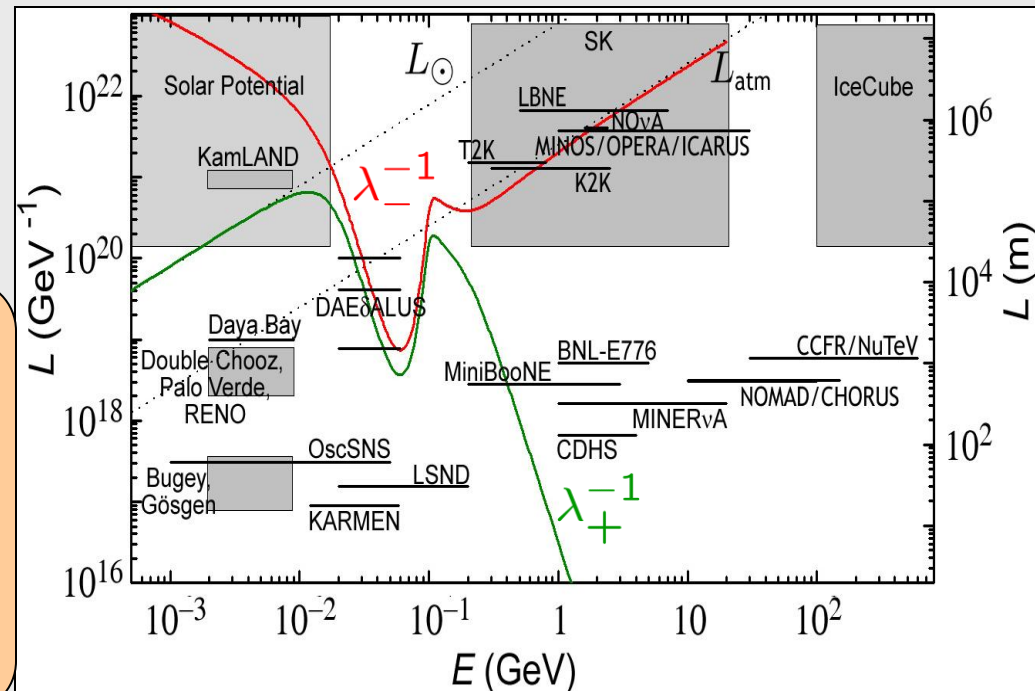
$$A = m^2/2E,$$

$$\bar{B} = -aE^2 + c'E + \bar{f}(E),$$

$$\bar{C} = cE^5 - c'E - \bar{f}(E).$$

Properties

- model fits LSND data better than $3\nu\text{SM}$
- requires three new parameters
- clear oscillation signals in future experiments:
 - OscSNS
 - DAESALUS

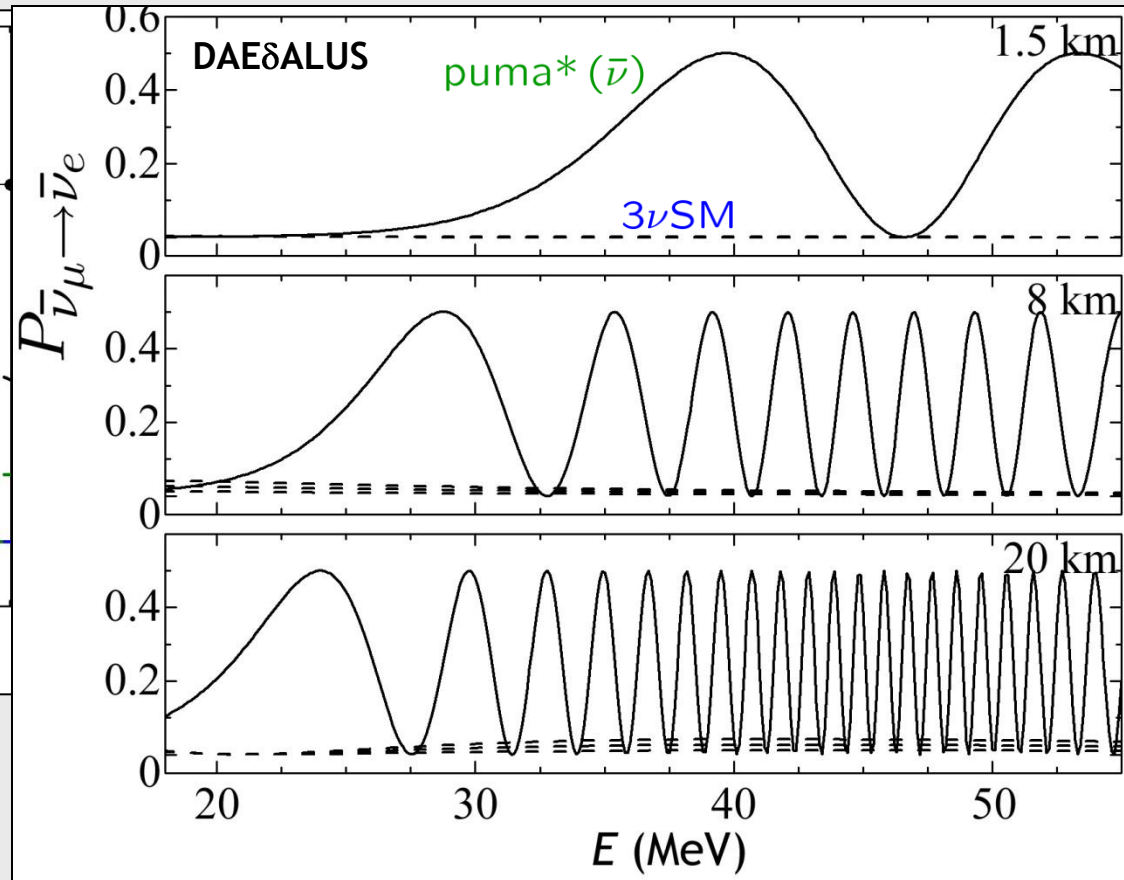
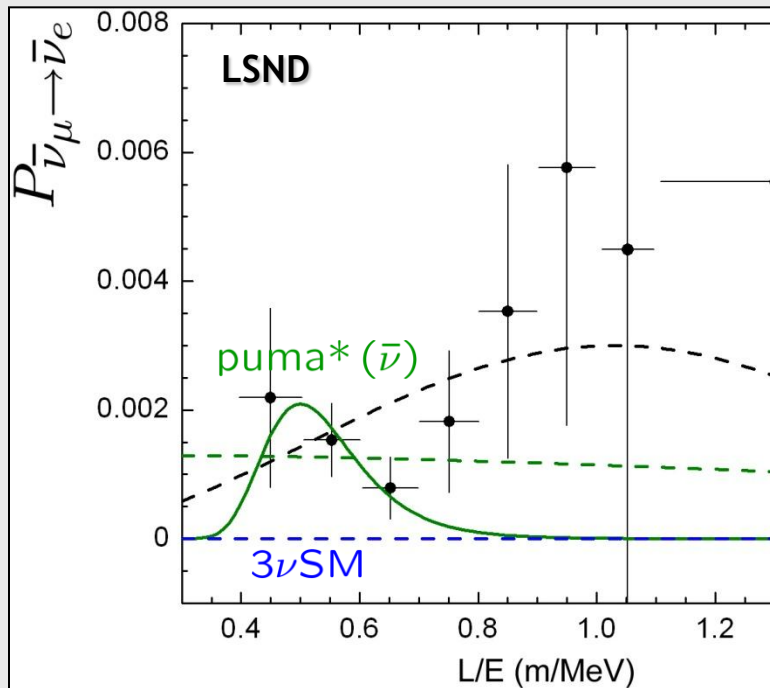


LSND: enhanced puma

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extension could be tested in future experiments



Possible extension of the puma model

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Addition of one more coefficient preserving the texture

Puma* model

$$h_{\text{eff}} = A \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} + B \begin{pmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} + C \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$A = m^2/2E, \quad B = aE^2 + c'E, \quad C = cE^5 - c'E$$

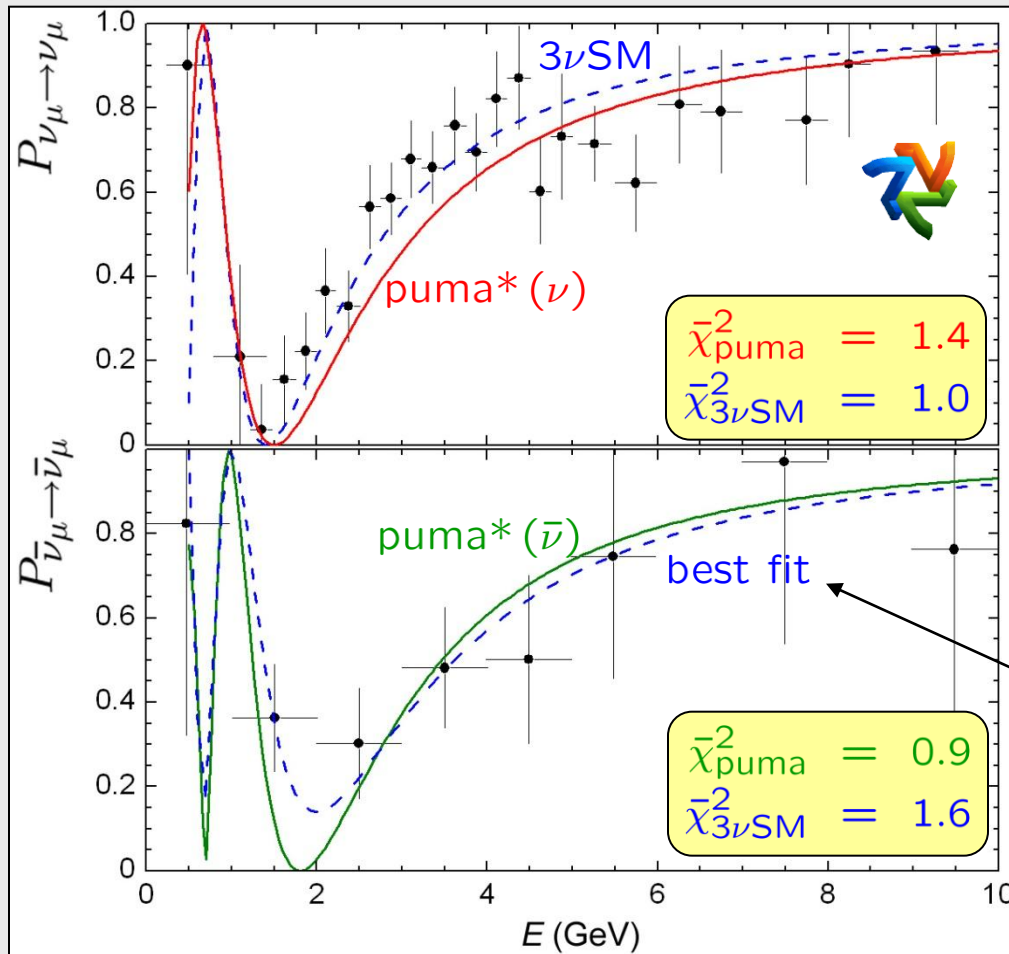
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New features: $\nu \neq \bar{\nu}$ at high energies

MINOS





Neutrino-antineutrino difference is produced by a CPT-odd coefficient.

There are no masses at high energies.

best fit $\neq 3\nu$ SM

Description of anomalies: parameters

$3\nu\text{SM}$	puma*
5	7
It does not explain - MiniBooNE 2007 - MiniBooNE 2010 - MINOS - LSND 	 consistent with everything

(*): extension

To my knowledge no other existing model is consistent with all compelling data and all the anomalies with 7 parameters. The puma is an economical model...

Summary

Puma model

- based on Lorentz and CPT violation;
- uses a total of 3 parameters (instead of 5 as the $3\nu\text{SM}$);
- consistent with all established data (atmospheric, reactor, and solar neutrinos);
- naturally reproduces the two MiniBooNE anomalies;
- simple extensions produce signals of the LSND and MINOS type;
- predictions for $\nu_\mu \rightarrow \nu_e$ in agreement with recent results from MINOS and T2K;
- realistic possible solution to some anomalies without extra particles or interactions;
- more details can be found in arXiv:1108.1799.