

Measurement of the anomalous like-sign
dimuon charge asymmetry with 9 fb^{-1} of
p \bar{p} collisions

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representing the

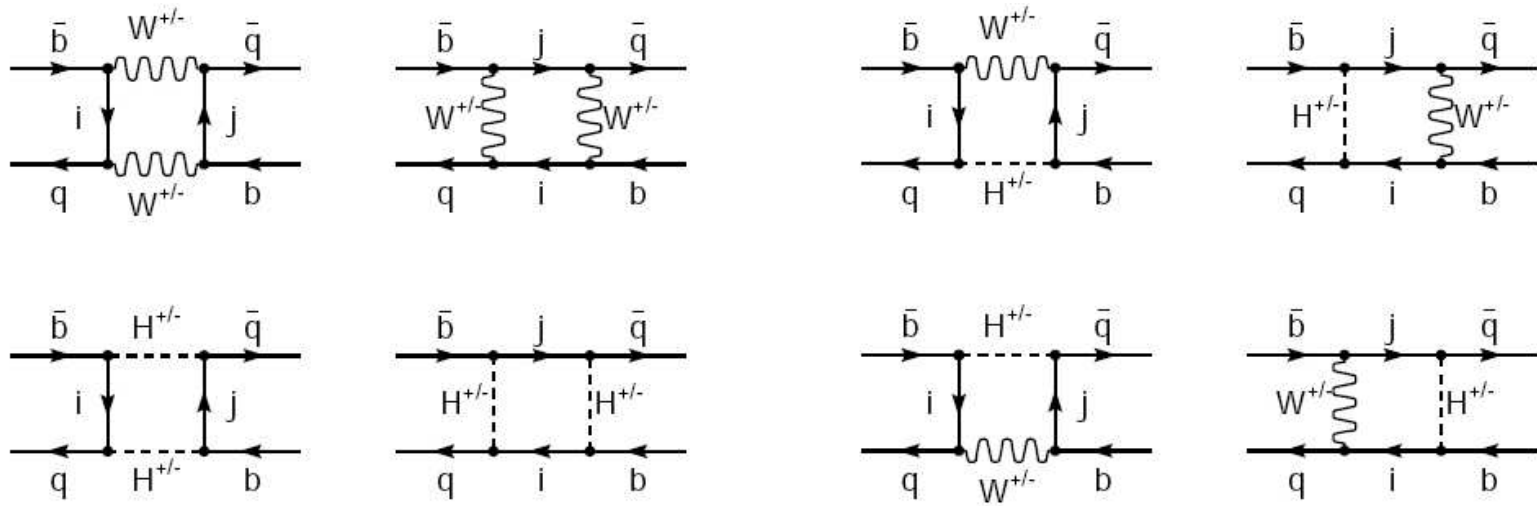
DØ Collaboration

DPF, August 2011

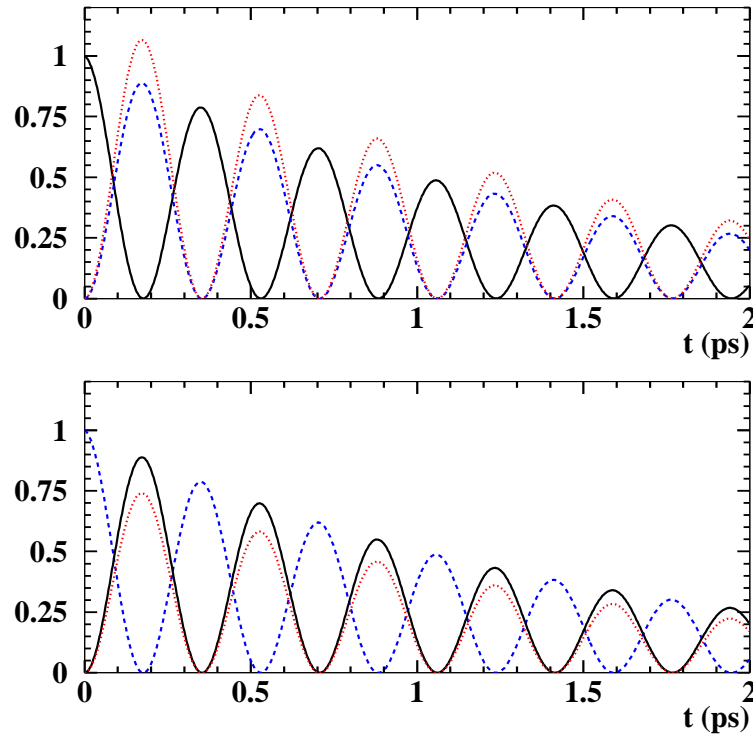
Outline

1. What do we measure, why and how?
2. Results with 9.0 fb^{-1}
3. Cross-checks
4. Dependence on the impact parameter
5. Conclusions

1. What do we measure, why and how?



$B_q^0 \leftrightarrow \bar{B}_q^0$ mixing is sensitive to new physics. $q = d, s$.



Top: Histogram of proper time of decays $B_s^0(s\bar{b}) \rightarrow \mu^+ X$ (continuous line), $B_s^0 \rightarrow \bar{B}_s^0 \rightarrow \mu^- X$ (dashed blue line if no CP violation, dotted red line if CP violation). Bottom: The same for \bar{B}_s^0 at $t = 0$.

At the Tevatron, b quarks are mostly created as $b\bar{b}$ pairs. To obtain a like-sign dimuon from semi-leptonic decay, one b hadron must decay to a “right sign” muon (i.e. a muon of the same sign as the original b quark), and the other b hadron must be a B_d^0 or B_s^0 that oscillates and decays to a “wrong sign” muon. For example

$$B^-(b\bar{u}) \rightarrow \mu^- X, \quad B_s^0(s\bar{b}) \rightarrow \bar{B}_s^0 \rightarrow \mu^- X.$$

We measure the like-sign dimuon charge asymmetry of direct semileptonic B decays in $p\bar{p}$ collisions:

$$A_{\text{Sl}}^b \equiv \frac{N_{b\bar{b}}^{++} - N_{b\bar{b}}^{--}}{N_{b\bar{b}}^{++} + N_{b\bar{b}}^{--}},$$

$$A_{\text{Sl}}^b = C_d a_{\text{Sl}}^d + C_s a_{\text{Sl}}^s,$$

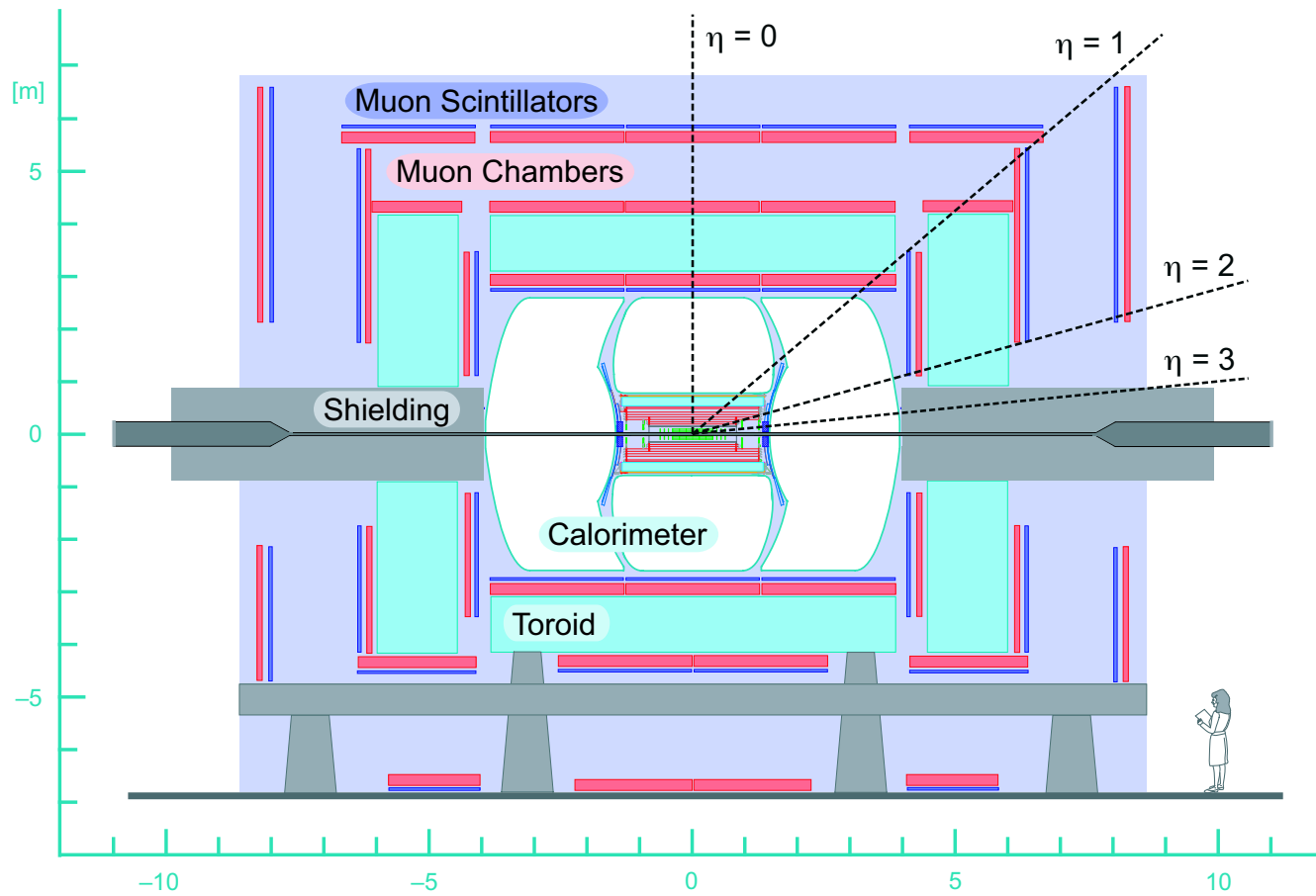
$$a_{\text{Sl}}^q = \frac{\Delta\Gamma_q}{\Delta M_q} \tan \phi_q, \text{ with } q = d, s.$$

A_{Sl}^b is obtained from the “raw” charge asymmetries

$$a \equiv \frac{n^+ - n^-}{n^+ + n^-}, \text{ and } A \equiv \frac{N^{++} - N^{--}}{N^{++} + N^{--}}.$$

In the Standard Model $A_{\text{SI}}^b = (-0.028_{-0.006}^{+0.005})\% \approx 0$.

How?



The DØ detector.

Three methods to measure A_{SI}^b : ($a_S \equiv c_b A_{SI}^b$, $A_S \equiv C_b A_{SI}^b$):

Inclusive muon sample (1 μ):

$$a \equiv \frac{n^+ - n^-}{n^+ + n^-} = \sum_{i=0}^5 f_{\mu}^i \{ f_S^i (a_S + \delta_i) + f_K^i a_K^i + f_{\pi}^i a_{\pi}^i + f_p^i a_p^i \}.$$

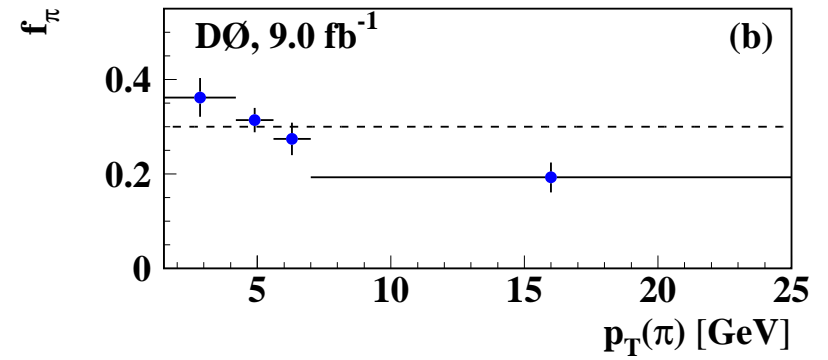
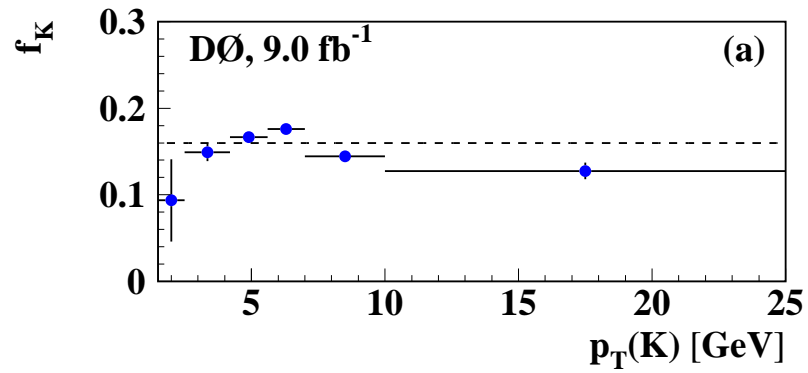
Like-sign dimuon sample (2 μ):

$$\begin{aligned} A &\equiv \frac{N^{++} - N^{--}}{N^{++} + N^{--}} \\ &= F_{SS} A_S + F_{SL} a_S + \sum_{i=0}^5 F_{\mu}^i \{ (2 - F_{\text{bkg}}^i) \delta_i \\ &\quad + F_K^i a_K^i + F_{\pi}^i a_{\pi}^i + F_p^i a_p^i \}. \end{aligned}$$

Combined: $A - \alpha a$. α chosen to minimize total uncertainty.

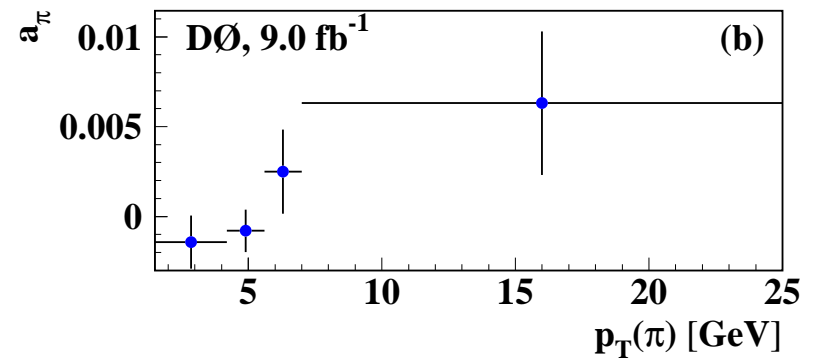
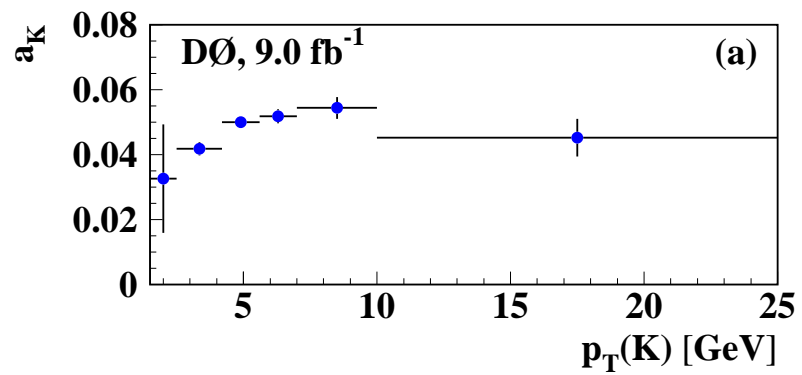
All parameters are measured with data as a function of p_T by reconstructing exclusive decays:

- f_K : $K^{*+} \rightarrow K_S \pi^+$, $K^{*0} \rightarrow \pi^- K^+ \rightarrow \mu^+$ and $K_S \rightarrow \pi^+ \pi^- \rightarrow \mu$.
- f_π : f_K , $K_S \rightarrow \pi^+ \pi^- \rightarrow \mu$, $\phi \rightarrow K^+ K^- \rightarrow \mu$ and n_π/n_K from MC.
- f_p : f_K , $\Lambda \rightarrow \pi^- p^+ \rightarrow \mu$, $\phi \rightarrow K^+ K^- \rightarrow \mu$ and n_p/n_K from MC.
- a_K : $K^{*0} \rightarrow \pi^- K^+ \rightarrow \mu^+$ and $\phi \rightarrow K^+ K^- \rightarrow \mu$.
- a_π : $K_S \rightarrow \pi^+ \pi^- \rightarrow \mu$.
- a_p : $\Lambda \rightarrow \pi^- p \rightarrow \mu$.
- δ : $J/\psi \rightarrow \text{track track} \rightarrow \mu$.
- $R_K \equiv F_K/f_K$: $K^{*0} \rightarrow \pi^- K^+ \rightarrow \mu^+$ (null-fit method) and $K_S \rightarrow \pi^+ \pi^- \rightarrow \mu$.



The fraction of (a) $K \rightarrow \mu$ tracks, and (b) $\pi \rightarrow \mu$ tracks in the inclusive muon sample as a function of the track transverse momentum p_T .

The K^+ has a longer inelastic interaction length in the calorimeter than K^- , and therefore has more time to decay. This results in a **positive charge asymmetry** a_K of the kaon decay background. a_K is measured with the data in two independent channels: $K^{*0} \rightarrow \pi^- K^+ \rightarrow \mu^+$ and $\phi \rightarrow K^+ K^- \rightarrow \mu$.



The asymmetries (a) a_K , and (b) a_π as a function of the kaon or pion p_T .

Contribution of different **background sources** to the observed asymmetry in the inclusive muon and like-sign dimuon samples. Only the statistical uncertainties are given. $a - a_{\text{bkg}} = f_{SC_b} A_{\text{Sl}}^s$, $A - A_{\text{bkg}} = (F_{SS} C_b + F_{SL} C_b) A_{\text{Sl}}^s$.

Source	inclusive muon	like-sign dimuon
$(f_K a_K \text{ or } F_K A_K) \times 10^2$	$+0.776 \pm 0.021$	$+0.633 \pm 0.031$
$(f_\pi a_\pi \text{ or } F_\pi A_\pi) \times 10^2$	$+0.007 \pm 0.027$	-0.002 ± 0.023
$(f_p a_p \text{ or } F_p A_p) \times 10^2$	-0.014 ± 0.022	-0.016 ± 0.019
$[(1 - f_{\text{bkg}})\delta \text{ or } (2 - F_{\text{bkg}})\Delta] \times 10^2$	-0.047 ± 0.012	-0.212 ± 0.030
$(a_{\text{bkg}} \text{ or } A_{\text{bkg}}) \times 10^2$	$+0.722 \pm 0.042$	$+0.402 \pm 0.053$
$(a \text{ or } A) \times 10^2$	$+0.688 \pm 0.002$	$+0.126 \pm 0.041$
$[(a - a_{\text{bkg}}) \text{ or } (A - A_{\text{bkg}})] \times 10^2$	-0.034 ± 0.042	-0.276 ± 0.067

Heavy quark decays. Note: we now take χ_0 from LEP.

	Process	Weight
T_1	$b \rightarrow \mu^- X$	$w_1 \equiv 1.$
T_{1a}	$b \rightarrow \mu^- X$ (nos)	$w_{1a} = (1 - \chi_0)w_1$
T_{1b}	$\bar{b} \rightarrow b \rightarrow \mu^- X$ (osc)	$w_{1b} = \chi_0 w_1$
T_2	$b \rightarrow c \rightarrow \mu^+ X$	$w_2 = 0.096 \pm 0.012$
T_{2a}	$b \rightarrow c \rightarrow \mu^+ X$ (nos)	$w_{2a} = (1 - \chi_0)w_2$
T_{2b}	$\bar{b} \rightarrow b \rightarrow c \rightarrow \mu^+ X$ (osc)	$w_{2b} = \chi_0 w_2$
T_3	$b \rightarrow c\bar{c}q$ with $c \rightarrow \mu^+ X$ or $\bar{c} \rightarrow \mu^- X$	$w_3 = 0.064 \pm 0.006$
T_4	$\eta, \omega, \rho^0, \phi(1020), J/\psi, \psi' \rightarrow \mu^+ \mu^-$	$w_4 = 0.021 \pm 0.002$
T_5	$b\bar{b}c\bar{c}$ with $c \rightarrow \mu^+ X$ or $\bar{c} \rightarrow \mu^- X$	$w_5 = 0.013 \pm 0.002$
T_6	$c\bar{c}$ with $c \rightarrow \mu^+ X$ or $\bar{c} \rightarrow \mu^- X$	$w_6 = 0.675 \pm 0.101$

Dilution factors: $c_b = 0.061 \pm 0.007$, $C_b = 0.474 \pm 0.032$.

2. Results with 9.0 fb^{-1}

- **From 1 μ** (2.041×10^9 muons):
 $A_{\text{SI}}^b = (-1.04 \pm 1.30 \text{ (stat)} \pm 2.31 \text{ (syst)}) \%$.
- **From 2 μ** (6.019×10^6 like-sign dimuons):
 $A_{\text{SI}}^b = (-0.808 \pm 0.202 \text{ (stat)} \pm 0.222 \text{ (syst)}) \%$.
- **Combined** (from $A - \alpha a$ with $\alpha = 0.89$):
 $A_{\text{SI}}^b = (-0.787 \pm 0.172 \text{ (stat)} \pm 0.093 \text{ (syst)}) \%$.

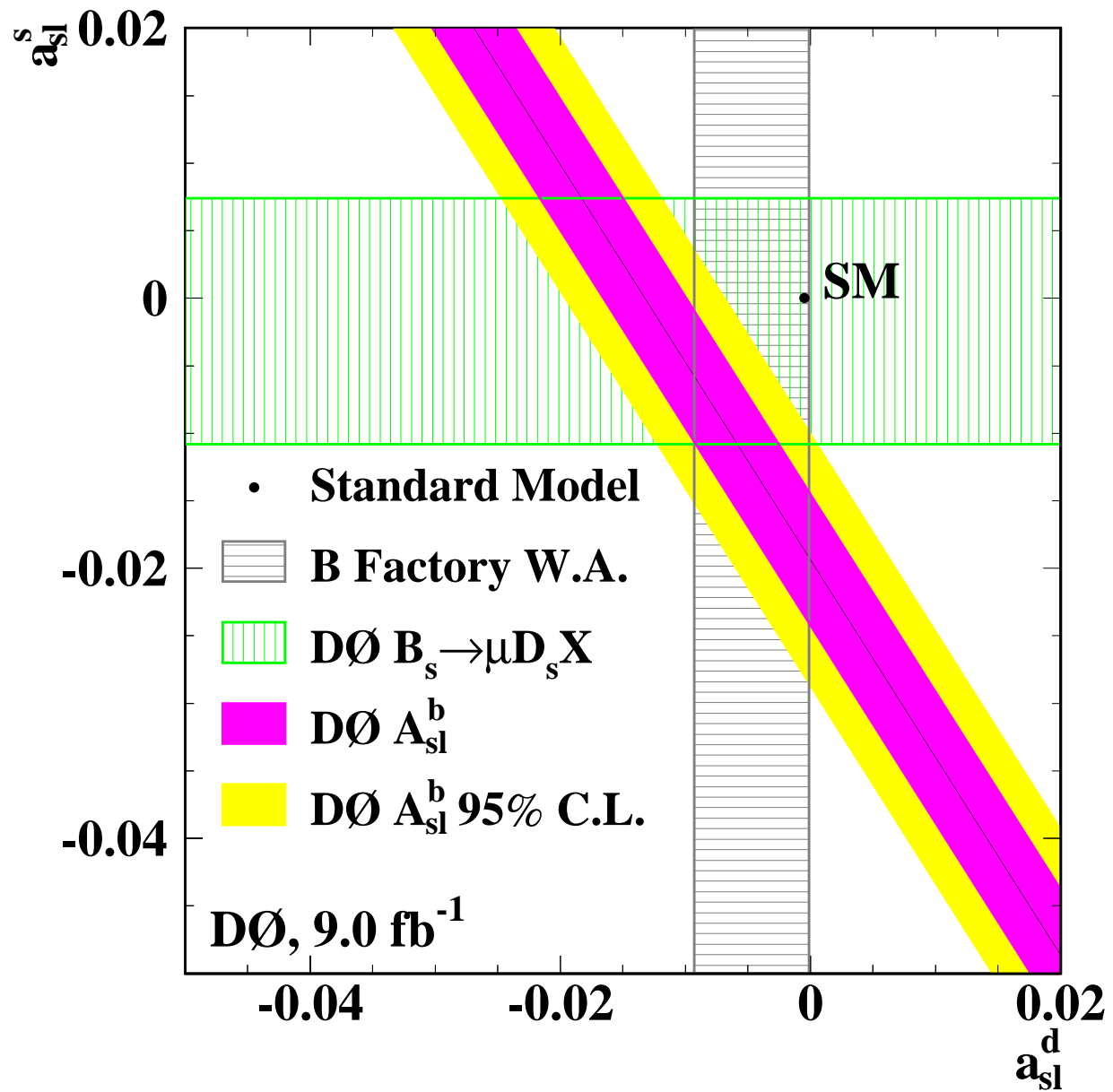
- $A_{\text{SI}}^b = (-0.787 \pm 0.172 \text{ (stat)} \pm 0.093 \text{ (syst)}) \%$.
This measurement disagrees with the prediction of the Standard Model by **3.9 standard deviations**.
- The charge asymmetry of like-sign dimuon events after subtracting all background contributions from the raw charge asymmetry is:

$$\begin{aligned} A_{\text{res}} &\equiv (A - \alpha a) - (A_{\text{bkg}} - \alpha a_{\text{bkg}}) \\ &= (-0.246 \pm 0.052 \text{ (stat)} \pm 0.021 \text{ (syst)})\%. \end{aligned}$$

This quantity does not depend on the interpretation in terms of the charge asymmetry of semileptonic decays of B mesons. This measurement disagrees with the prediction of the Standard Model by **4.2 standard deviations**.

Sources of uncertainty on A_{SI}^b . The first nine rows contain statistical uncertainties, the next four rows contain systematic uncertainties.

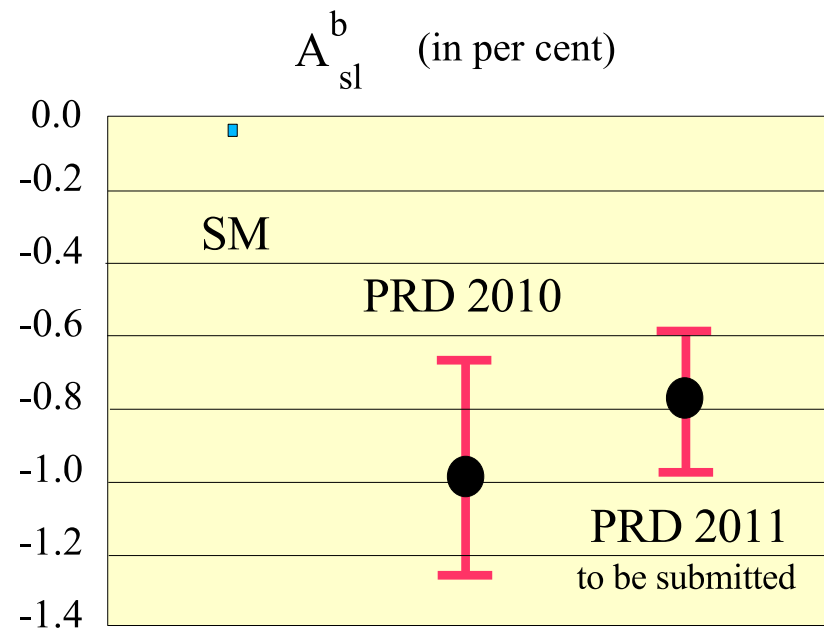
Source	1μ	2μ	combined
A or a (stat)	0.00068	0.00121	0.00132
f_K (stat)	0.00472	0.00064	0.00028
R_K (stat)	N/A	0.00059	0.00065
$P(\pi \rightarrow \mu)/P(K \rightarrow \mu)$	0.00181	0.00023	0.00008
$P(p \rightarrow \mu)/P(K \rightarrow \mu)$	0.00323	0.00026	0.00002
A_K	0.00458	0.00052	0.00037
A_π	0.00802	0.00067	0.00030
A_p	0.00584	0.00050	0.00020
δ or Δ	0.00377	0.00087	0.00067
f_K (syst)	0.02310	0.00204	0.00007
R_K (syst)	N/A	0.00068	0.00072
π, K, p multiplicity	0.00067	0.00019	0.00017
c_b or C_b	0.00121	0.00052	0.00056
Total statistical	0.01304	0.00202	0.00172
Total systematic	0.02313	0.00222	0.00093
Total	0.02656	0.00300	0.00196



History

- Phys. Rev. D 82, 032001, (2010),
Phys. Rev. Lett. 105, 081801 (2010), 6.1 fb⁻¹:
 $A_{\text{SI}}^b = (-0.957 \pm 0.251 \text{ (stat)} \pm 0.146 \text{ (syst)}) \%$, 3.2 σ from SM.
- This measurement (2011) with 9.0 fb⁻¹:
 $A_{\text{SI}}^b = (-0.787 \pm 0.172 \text{ (stat)} \pm 0.093 \text{ (syst)}) \%$, 3.9 σ from SM.

All measurements are consistent.



Comparison of measurements of A_{sl}^b .

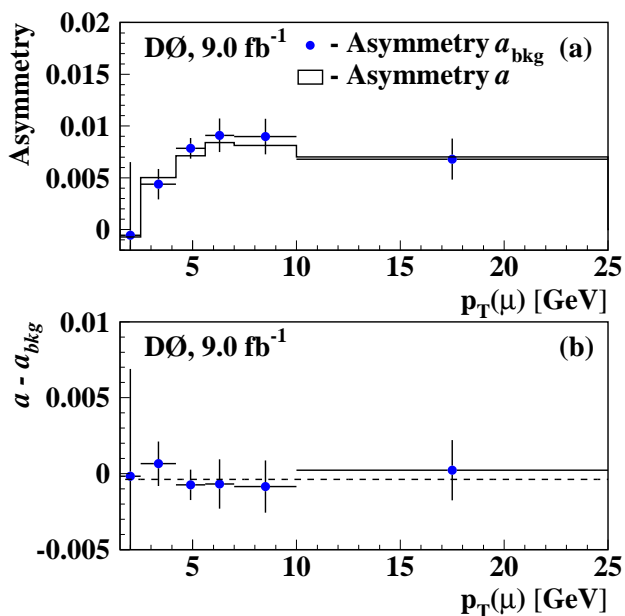
Comparison of directly measured background subtracted asymmetries

(before dividing by the dilution factor which depends on the physics interpretation in terms of $B_q\bar{B}_q$ mixing and semi-leptonic decay):

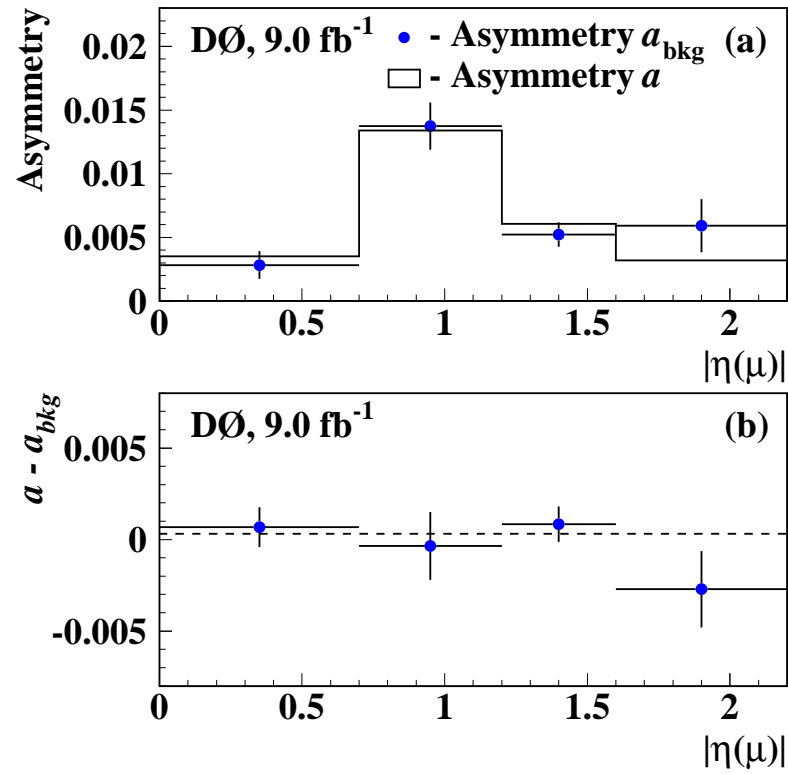
- Phys. Rev. D 74, 092001 (2006), Eq. (11), 1 fb^{-1} :
 $A = (-0.28 \pm 0.13 \text{ (stat)} \pm 0.09 \text{ (syst)})\%$.
- This measurement, (2011), 9.0 fb^{-1} :
 $A_{\text{res}} = (-0.246 \pm 0.052 \text{ (stat)} \pm 0.021 \text{ (syst)})\%$.

All measurements are consistent.

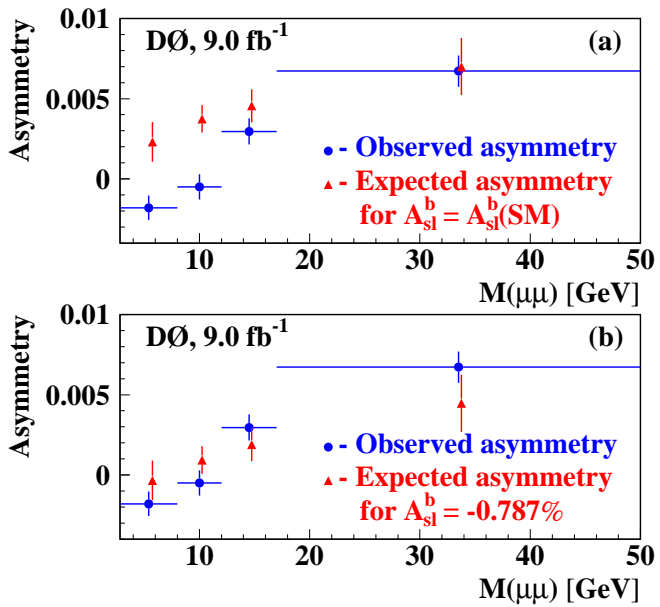
3. Cross-checks



The asymmetry a_{bkg} (points with error bars, total uncertainties are shown), as expected from our measurements of the fractions and asymmetries of the background processes, is compared to the measured asymmetry a of the **inclusive muon sample as a function of p_T** . The asymmetry from CP violation is negligible compared to the background in the inclusive muon sample.



The same, but as a function of the absolute value of muon pseudorapidity $|\eta(\mu)|$.



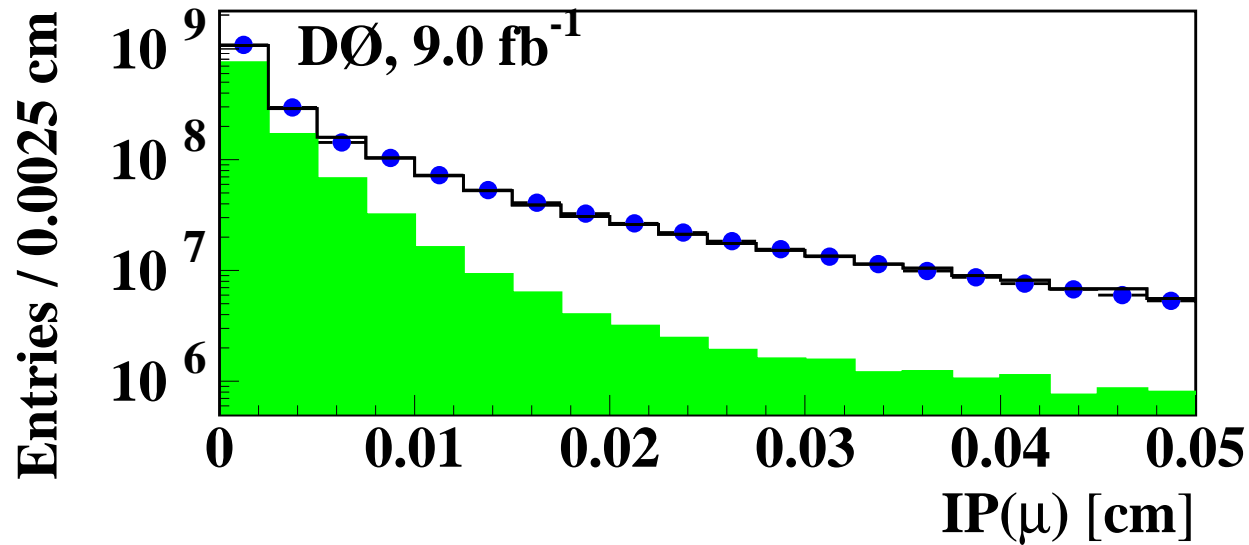
The observed and expected like-sign dimuon charge asymmetries in bins of dimuon invariant mass. The expected asymmetry is shown for (a) $A_{sl}^b = \text{SM value}$, and (b) $A_{sl}^b = -0.787\%$.

4. Dependence on the impact parameter

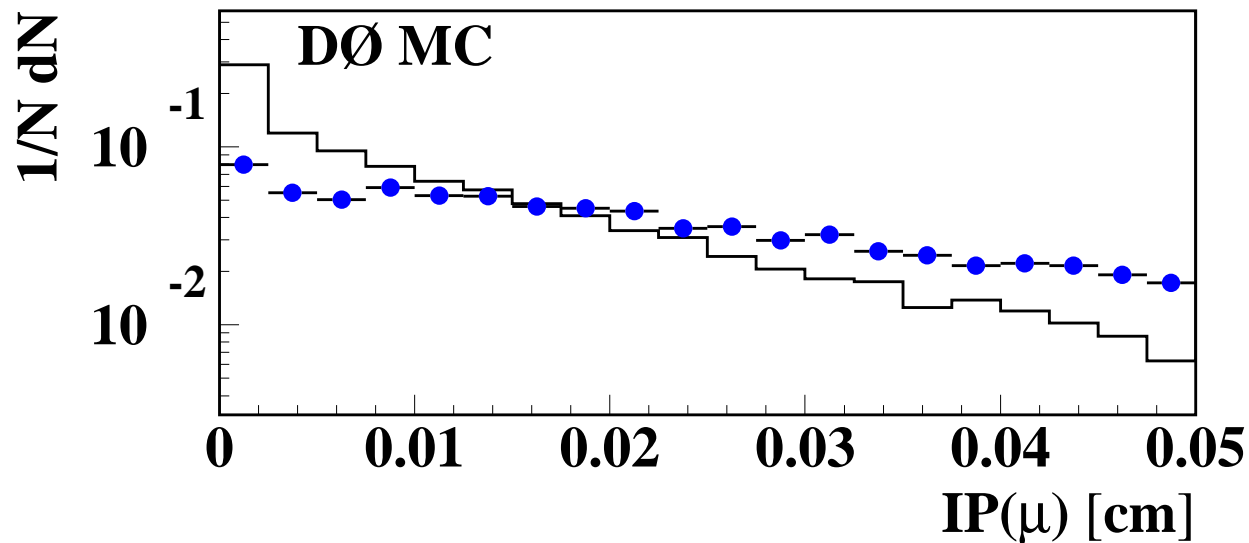
Additional measurements are made applying an impact parameter (IP) cut on **each** muon.

IP is the distance of closest approach of the muon track to the primary vertex projected onto the plane transverse to the $p\bar{p}$ beams.

The dependence of $A_{SI}^b = C_d a_{SI}^d + C_s a_{SI}^s$ on IP can reveal the origin of the asymmetry because C_d and C_s depend on IP .



The muon impact parameter (IP) distribution in the inclusive muon sample (dots). The solid line represents the muon IP distribution in simulation. The shaded histogram is the contribution from K , π and p background muons in simulation.

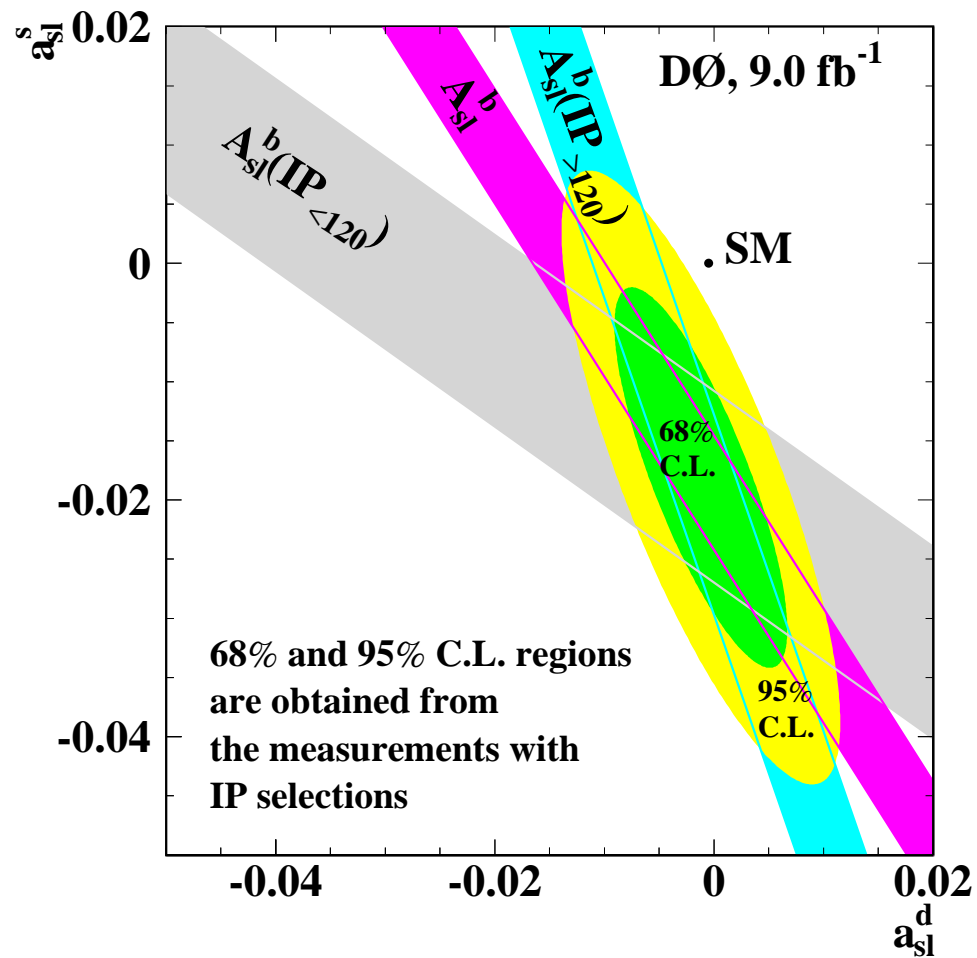


The normalized impact parameter (IP) distribution for muons produced in **oscillating decays** of B_d^0 mesons (dots) and B_s^0 mesons (solid histogram) in simulation.

Input quantities for the measurement of A_{SI}^b using the muons with impact parameter (IP) above and below $120 \mu\text{m}$. Only the statistical uncertainties are given.

Quantity	$IP_{>120}$	$IP_{<120}$
$f_K \times 10^2$	5.19 ± 0.37	17.64 ± 0.27
$f_\pi \times 10^2$	5.65 ± 0.40	34.72 ± 1.86
$f_p \times 10^2$	0.05 ± 0.03	0.45 ± 0.20
$F_K \times 10^2$	4.48 ± 4.05	21.49 ± 0.62
$F_\pi \times 10^2$	4.43 ± 3.95	40.47 ± 2.26
$F_p \times 10^2$	0.03 ± 0.05	0.59 ± 0.23
$f_S \times 10^2$	89.11 ± 0.88	47.18 ± 2.03
$F_{\text{bkg}} \times 10^2$	8.94 ± 8.26	62.56 ± 3.07
$F_{SS} \times 10^2$	91.79 ± 7.65	53.66 ± 2.68
$a \times 10^2$	-0.014 ± 0.005	$+0.835 \pm 0.002$
$a_{\text{bkg}} \times 10^2$	$+0.027 \pm 0.023$	$+0.864 \pm 0.049$
$A \times 10^2$	-0.529 ± 0.120	$+0.555 \pm 0.060$
$A_{\text{bkg}} \times 10^2$	-0.127 ± 0.093	$+0.829 \pm 0.077$

Selection	Sample	A_{SI}^b $\times 10^2$	Uncertainty $\times 10^2$	
			statistical	systematic
All events	1μ	-1.042	1.304	2.314
	2μ	-0.808	0.202	0.222
	comb.	-0.787	0.172	0.093
$IP < 50\mu\text{m}$	1μ	-3.244	4.101	7.466
	2μ	-2.837	0.776	1.221
	comb.	-2.779	0.674	0.694
$IP > 50\mu\text{m}$	1μ	-0.171	0.343	0.311
	2μ	-0.593	0.257	0.074
	comb.	-0.533	0.239	0.100
$IP < 80\mu\text{m}$	1μ	-1.293	3.282	5.841
	2μ	-1.481	0.541	0.810
	comb.	-1.521	0.458	0.501
$IP > 80\mu\text{m}$	1μ	-0.388	0.280	0.179
	2μ	-0.529	0.285	0.048
	comb.	-0.742	0.226	0.091
$IP < 120\mu\text{m}$	1μ	-1.654	2.774	4.962
	2μ	-1.175	0.439	0.590
	comb.	-1.138	0.366	0.323
$IP > 120\mu\text{m}$	1μ	-0.422	0.240	0.121
	2μ	-0.818	0.342	0.067
	comb.	-0.579	0.210	0.094



Measurements of A_{sl}^b with $IP > 120\mu\text{m}$ and $IP < 120\mu\text{m}$, and corresponding 68% and 95% confidence level regions in the (a_{sl}^d, a_{sl}^s) plane. Also shown is the measurement with no IP cut.

From $IP > 120\mu\text{m}$ and $IP < 120\mu\text{m}$ we measure

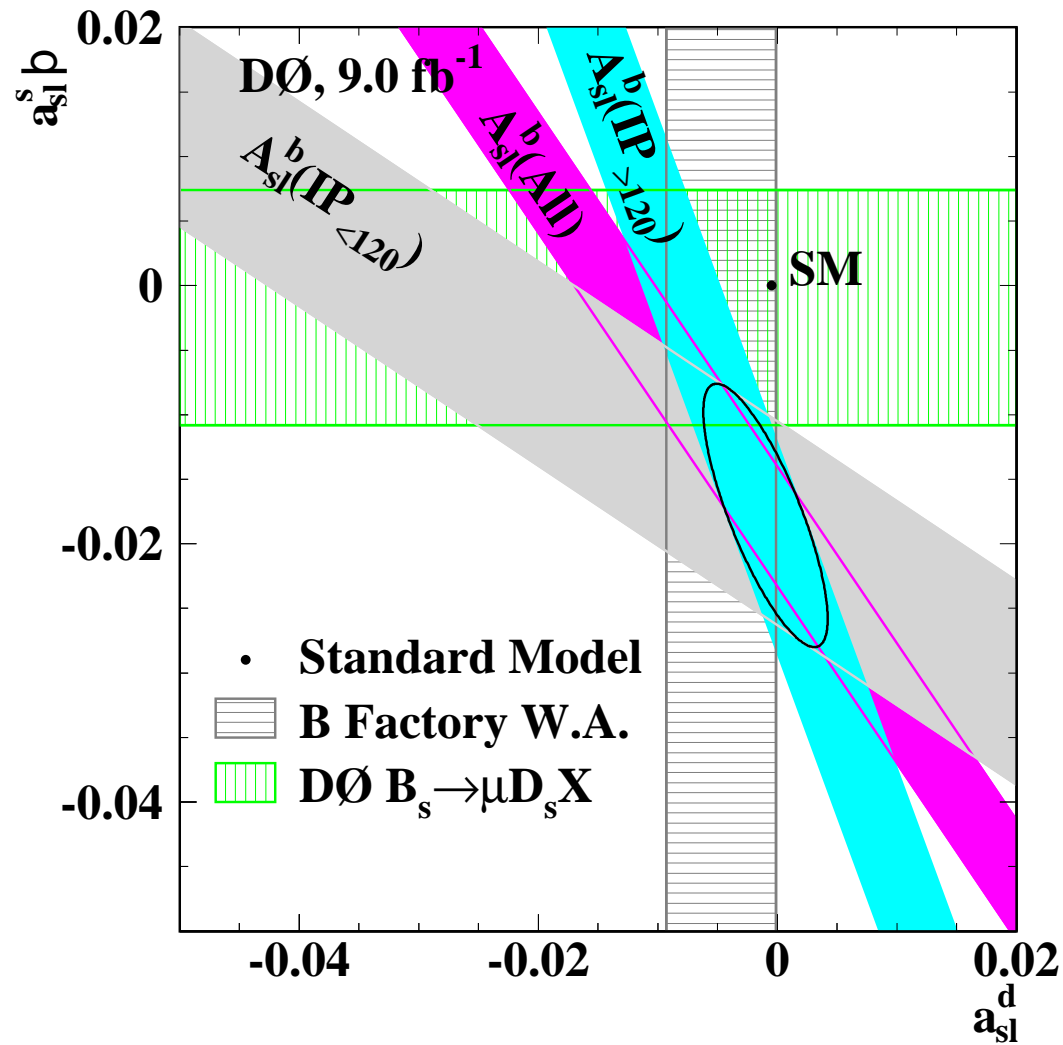
$$a_{\text{SI}}^d = -0.0012 \pm 0.0051,$$

$$a_{\text{SI}}^s = -0.0181 \pm 0.0104,$$

with correlation $\rho_{ds} = -0.782$.

5. Conclusions

- We have completed a new measurement of the like-sign dimuon charge asymmetry, with improvements in the data selection and analysis techniques, and a larger data set of 9.0 fb^{-1} .
- We obtain
 $A_{\text{sl}}^b = (-0.787 \pm 0.172 \text{ (stat)} \pm 0.093 \text{ (syst)}) \%$.
This measurement disagrees with the prediction of the standard model by **3.9 standard deviations**.
- The dependence of A_{sl}^b on IP is consistent with the hypothesis of a **new source of CP violation in the mixing of B_d^0 and B_s^0 mesons**.



Ellipse for 1D 1σ ($\Delta\chi^2 = 1.0$) from $IP > 120\mu\text{m}$ and $IP < 120\mu\text{m}$ only.

Appendix: Theory

If CPT is a symmetry,

$$i\frac{d}{dt} \begin{pmatrix} B_s(t) \\ \bar{B}_s(t) \end{pmatrix} = \left(\begin{bmatrix} m & M_{12}^s \\ M_{12}^{s*} & m \end{bmatrix} - \frac{i}{2} \begin{bmatrix} \Gamma & \Gamma_{12}^s \\ \Gamma_{12}^{s*} & \Gamma \end{bmatrix} \right) \begin{pmatrix} B_s(t) \\ \bar{B}_s(t) \end{pmatrix}.$$

The eigenvalues are

$$M_s + \frac{1}{2}\Delta M_s - \frac{i}{2}(\Gamma_s - \frac{1}{2}\Delta\Gamma_s),$$

$$M_s - \frac{1}{2}\Delta M_s - \frac{i}{2}(\Gamma_s + \frac{1}{2}\Delta\Gamma_s),$$

where $\Delta M_s > 0$ by definition.

The CP-violating phase is

$$\phi_s \equiv \arg \left(-\frac{M_{12}^s}{\Gamma_{12}^s} \right).$$

The observables are M_s , Γ_s , ϕ_s ,

$$\Delta M_s = 2 |M_{12}^s|, \quad \Delta \Gamma_s = 2 |\Gamma_{12}^s| \cos \phi_s,$$

$$a_{\text{sl}}^s = \Im \frac{\Gamma_{12}^s}{M_{12}^s} = \frac{|\Gamma_{12}^s|}{|M_{12}^s|} \sin \phi_s = \frac{\Delta \Gamma_s}{\Delta M_s} \tan \phi_s.$$

The semileptonic charge asymmetry is

$$a_{\text{sl}}^s \equiv \frac{N(\bar{B}_s \rightarrow f) - N(B_s \rightarrow \bar{f})}{N(\bar{B}_s \rightarrow f) + N(B_s \rightarrow \bar{f})},$$

where f is a flavor specific final state to which only B_s can decay.

$$A \equiv \frac{N^{++} - N^{--}}{N^{++} + N^{--}}$$

$$A_{\text{sl}}^b = \frac{f_d \chi_d a_{\text{sl}}^d + f_s \chi_s a_{\text{sl}}^s}{f_d \chi_d + f_s \chi_s} = (0.506 \pm 0.043) a_{\text{sl}}^d + (0.494 \pm 0.043) a_{\text{sl}}^s.$$

New Physics may change the Standard Model $M_{12}^{SM,s}$ to:

$$M_{12}^s \equiv M_{12}^{SM,s} \cdot \Delta_s = M_{12}^{SM,s} \cdot |\Delta_s| e^{i\phi_s^\Delta}.$$

$$\phi_s = \phi_s^{SM} + \phi_s^\Delta = 0.0042 \pm 0.0014 + \phi_s^\Delta,$$

$$\Delta M_s = \Delta M_s^{SM} \cdot |\Delta_s| = (19.30 \pm 6.74) \text{ ps}^{-1} \cdot |\Delta_s|$$

$$\Delta \Gamma_s = 2 |\Gamma_{12}^s| \cos \phi_s = (0.096 \pm 0.039) \text{ ps}^{-1} \cdot \cos \phi_s,$$

$$\frac{\Delta \Gamma_s}{\Delta M_s} = \frac{|\Gamma_{12}^s|}{|M_{12}^{SM,s}|} \cdot \frac{\cos \phi_s}{|\Delta_s|} = (4.97 \pm 0.94) \cdot 10^{-3} \cdot \frac{\cos \phi_s}{|\Delta_s|},$$

$$a_{\text{SI}}^s = \frac{|\Gamma_{12}^s|}{|M_{12}^{SM,s}|} \cdot \frac{\sin \phi_s}{|\Delta_s|} = (4.97 \pm 0.94) \cdot 10^{-3} \cdot \frac{\sin \phi_s}{|\Delta_s|}.$$

From Alexander Lenz and Ulrich Nierste, hep-ph/0612167, November 2007.

The ϕ_s obtained from fits to $B_s \rightarrow J/\psi\phi$ is slightly different:

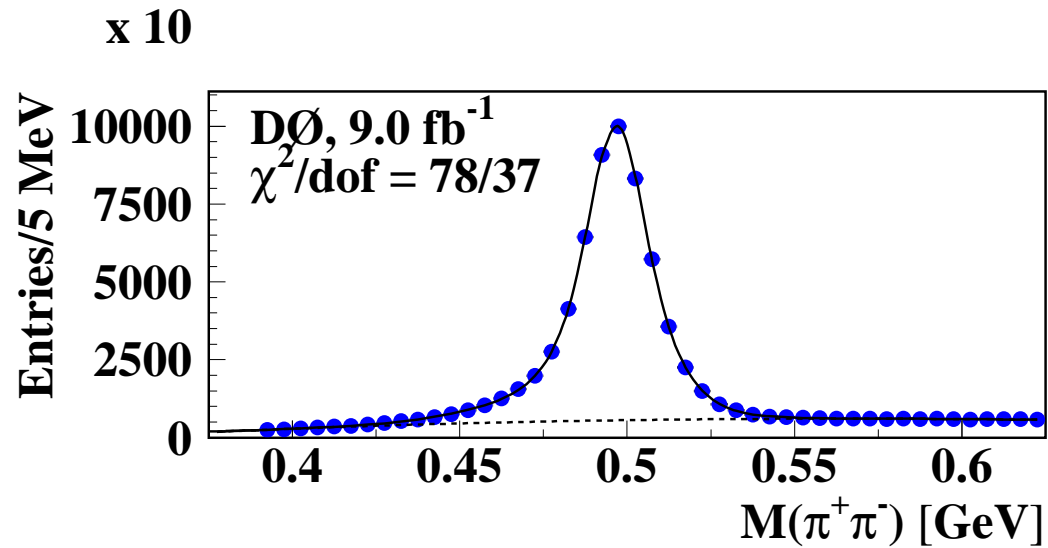
$$\phi_s = -2\beta_s^{SM} + \phi_s^\Delta,$$

where

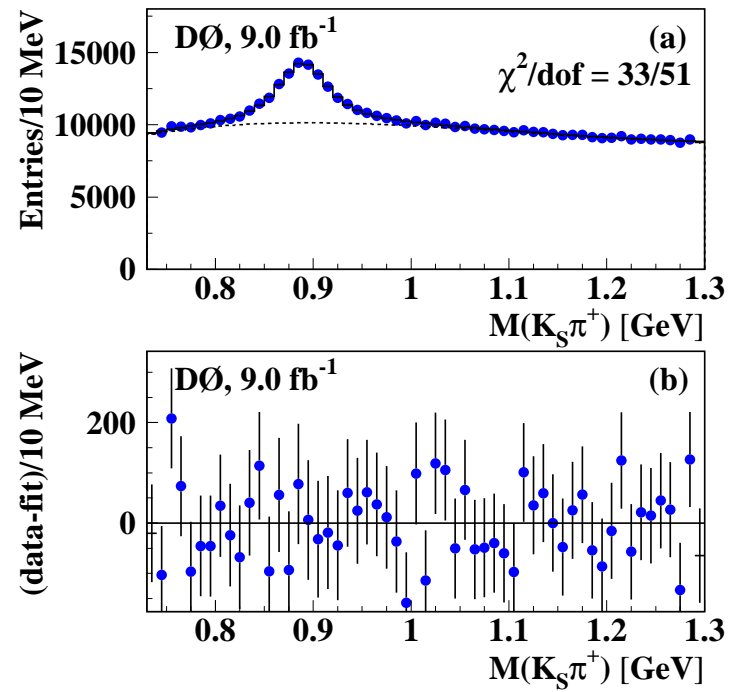
$$\beta_s^{SM} \equiv \arg \frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*} = 0.019 \pm 0.001.$$

Backup slides

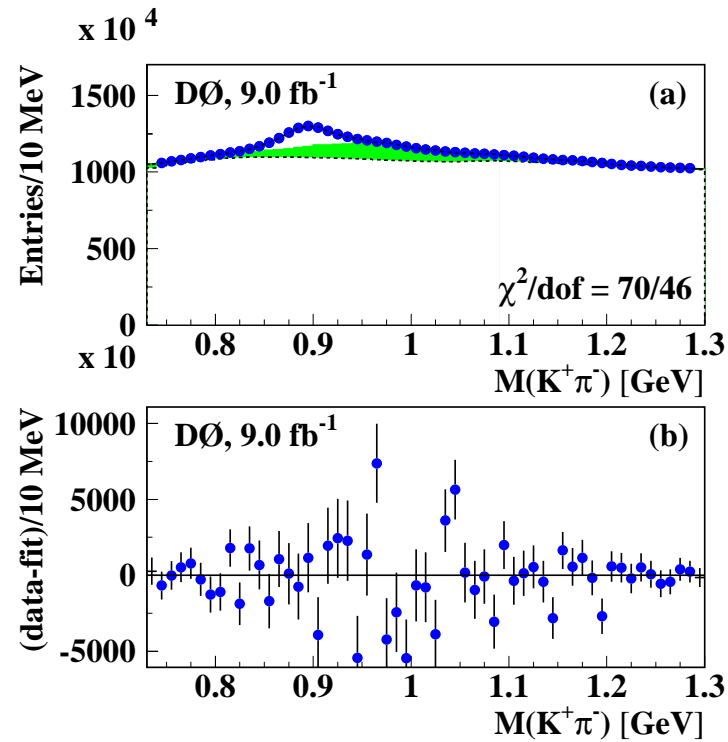
Example: fits to obtain f_K



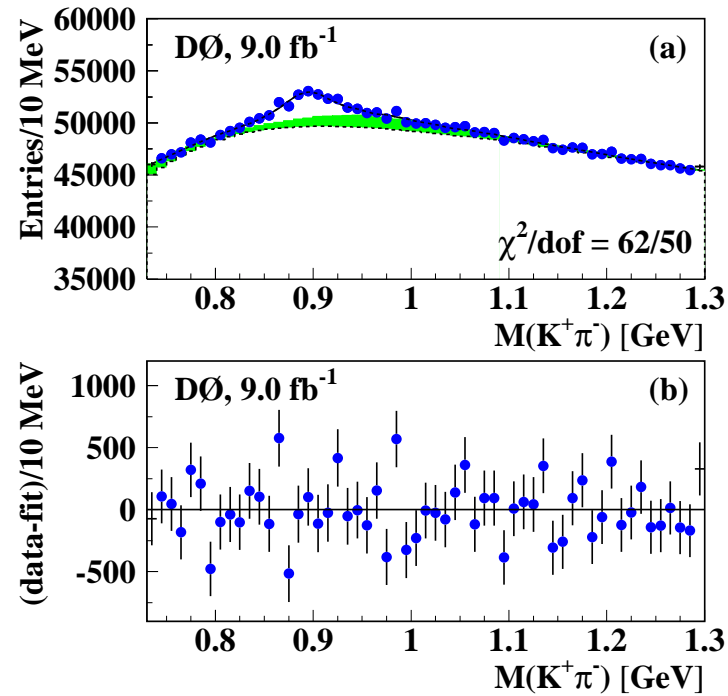
$K_S \rightarrow \pi^+\pi^- \rightarrow \mu$ candidates with $4.2 < p_T(K_S) < 5.6$ GeV in the inclusive muon sample.



$K^{*+} \rightarrow \pi^+ K_S \rightarrow \pi\pi \rightarrow \mu$ candidates with $4.2 < p_T(K_S) < 5.6$ GeV in the inclusive muon sample.

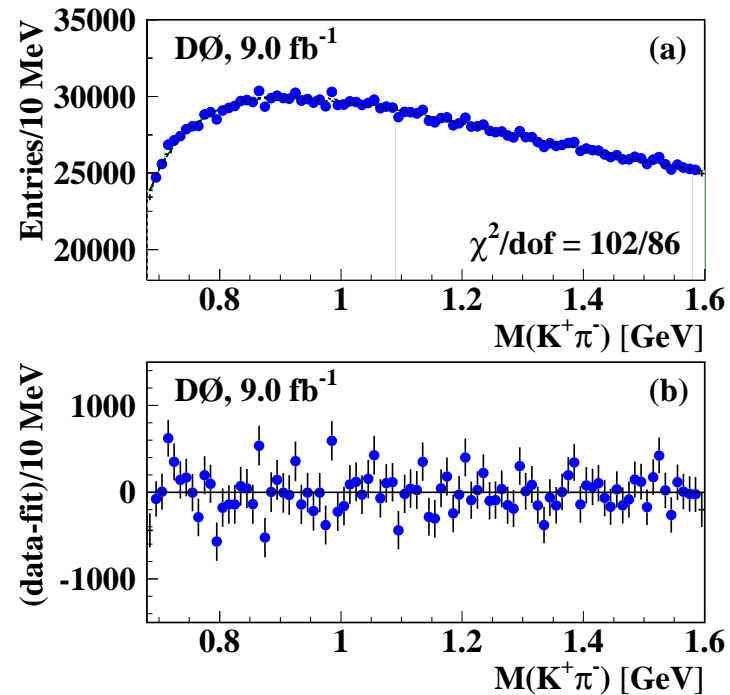


$K^{*0} \rightarrow \pi^- K^+ \rightarrow \mu^+$ candidates with $4.2 < p_T(K^+) < 5.6$ GeV in the inclusive muon sample. Green: $\rho^0 \rightarrow \pi^+\pi^-$ events.



$K^{*0} \rightarrow \pi^- K^+ \rightarrow \mu^+$ candidates with $4.2 < p_T(K^+) < 5.6$ GeV in the like-sign dimuon sample. Green: $\rho^0 \rightarrow \pi^+ \pi^-$ events.

Null-fit to obtain $R_K = F_K/f_K$



$K^+\pi^-$ invariant mass distribution of a weighted difference of histograms for inclusive muons and like-sign dimuons for $4.2 < p_T(K^+) < 5.6 \text{ GeV}$.

Improvements (since Phys. Rev. D 82, 032001, (2010))

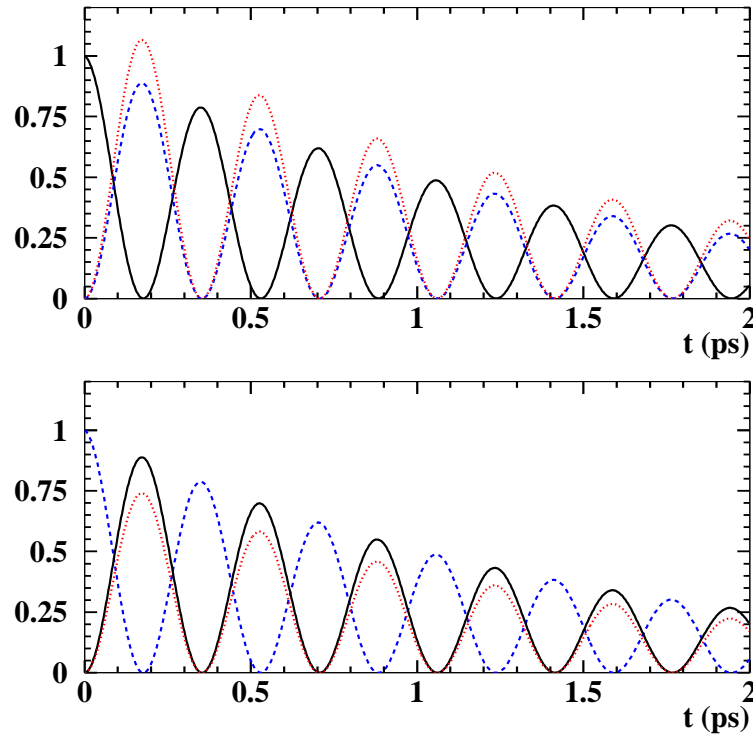
- To increase the number of events, the $|p_z|$ cut is lowered from 6.4 GeV to 5.4 GeV.
- To lower the $K \rightarrow \mu$ and $\pi \rightarrow \mu$ backgrounds, the χ^2 of the match of track parameters obtained with the central detector and outer muon system is reduced from 40 to 12 (with 4 d.o.f.).
- The measurement of f_K is improved: $K_S \rightarrow \pi\pi \rightarrow \mu$ (muon required for same sample composition as $K \rightarrow \mu$).

- The measurement of $R_K \equiv F_K/f_K$ is done in two independent channels: $K^{*0} \rightarrow \pi^- K^+ \rightarrow \mu^+ X$ (with the null-fit method), and the new channel $K_S \rightarrow \pi\pi \rightarrow \mu$.
- The data set is increased from 6.1 fb^{-1} to 9.0 fb^{-1} .

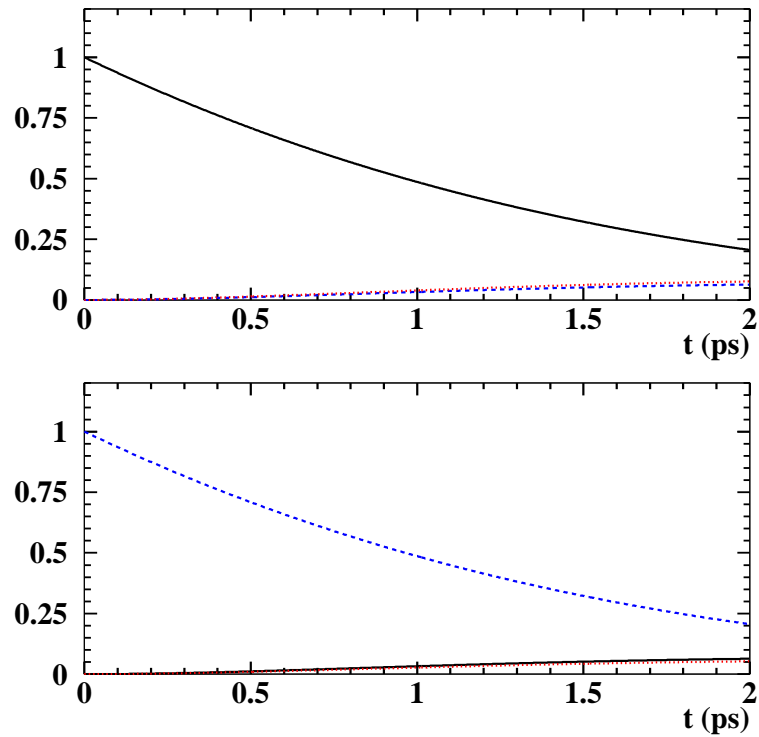
More cross-checks (see paper for numerical details):

- Different running periods
- Tighter muon selection
- Lower background (by tightening χ^2 match between central detector and outer muon system track parameters).
- Lower impact parameter cut from 0.300 to 0.012 cm.
- Only low luminosity events.

- Invariant mass of the 2 muons greater than 12 GeV (instead of 2.8 GeV).
- Only muons with $p_T > 4.2$ GeV.
- Only muons with $p_T < 7.0$ GeV.
- Only muons in part of the ϕ range.
- Only muons in part of the η range (several tests).
- Tests with different trigger requirements.



Top: Histogram of proper time of decays $B_s^0 \rightarrow \mu^+ X$ (continuous line), $B_s^0 \rightarrow \bar{B}_s^0 \rightarrow \mu^- X$ (dashed line if no CP violation, dotted red line if CP violation).
 Bottom: The same for \bar{B}_s^0 at $t = 0$.



Same for B_d^0 (top) and \bar{B}_d^0 (bottom) at $t = 0$. Applying an IP cut can enrich the sample in oscillating B_d^0 's (shown in red).

Mixing probability χ_d obtained in simulation and the coefficients C_d and C_s for different muon selections.

Selection	$\chi_d(MC)$	C_d	C_s
all	0.186 ± 0.002	0.594 ± 0.022	0.406 ± 0.022
$IP < 50\mu\text{m}$	0.059 ± 0.002	0.316 ± 0.021	0.684 ± 0.021
$IP < 80\mu\text{m}$	0.069 ± 0.002	0.351 ± 0.022	0.649 ± 0.022
$IP < 120\mu\text{m}$	0.084 ± 0.002	0.397 ± 0.022	0.603 ± 0.022
$IP > 50\mu\text{m}$	0.264 ± 0.004	0.674 ± 0.020	0.326 ± 0.020
$IP > 80\mu\text{m}$	0.299 ± 0.004	0.701 ± 0.019	0.299 ± 0.019
$IP > 120\mu\text{m}$	0.342 ± 0.004	0.728 ± 0.018	0.272 ± 0.018