

# DPF Meeting 2011

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$t\bar{t} + \gamma$  Production  
and the  
Top Quark Electric Charge

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**in collaboration with K. Melnikov and A. Scharf**

[Phys.Rev. D83 (2011) 074013]



# The Tevatron

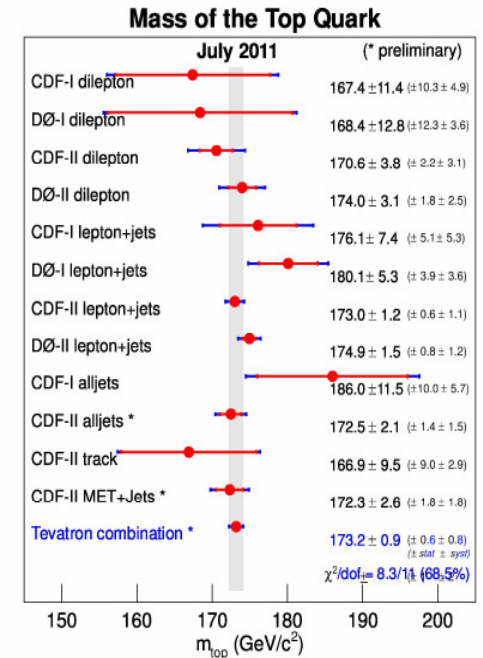
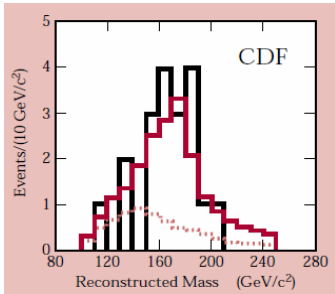
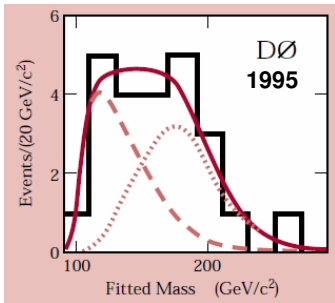
One of Tevatron's greatest legacy:

Discovery of the top quark

Measurement of the cross section

Determination of the mass

Measurement of the FB asymmetry



Plus:

decay width, spin correlations, W helicity fractions,  $|V_{tb}|^2$ , ...

# Electroweak couplings

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## What do we know about top quark electroweak couplings ?

electric charge,                      weak charge,  
magn./electr. dipole mom.,        Yukawa coupl.

# Electroweak couplings

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electric charge,                      weak charge,  
magn./electr. dipole mom.,      Yukawa coupl.

**This is where the LHC takes over:**

$$pp \rightarrow t\bar{t} + \gamma$$

$$pp \rightarrow t\bar{t} + Z$$

$$pp \rightarrow t\bar{t} + \text{Higgs}$$

Studies of  $t\bar{t}Z$  and  $t\bar{t}H$  require at least  $\mathcal{L} = 100 \text{ fb}^{-1}$  (14 TeV)

➔ Let's study  $t\bar{t}\gamma$  first and see what we can do for  $Q_t$ .

# Top quark electric charge

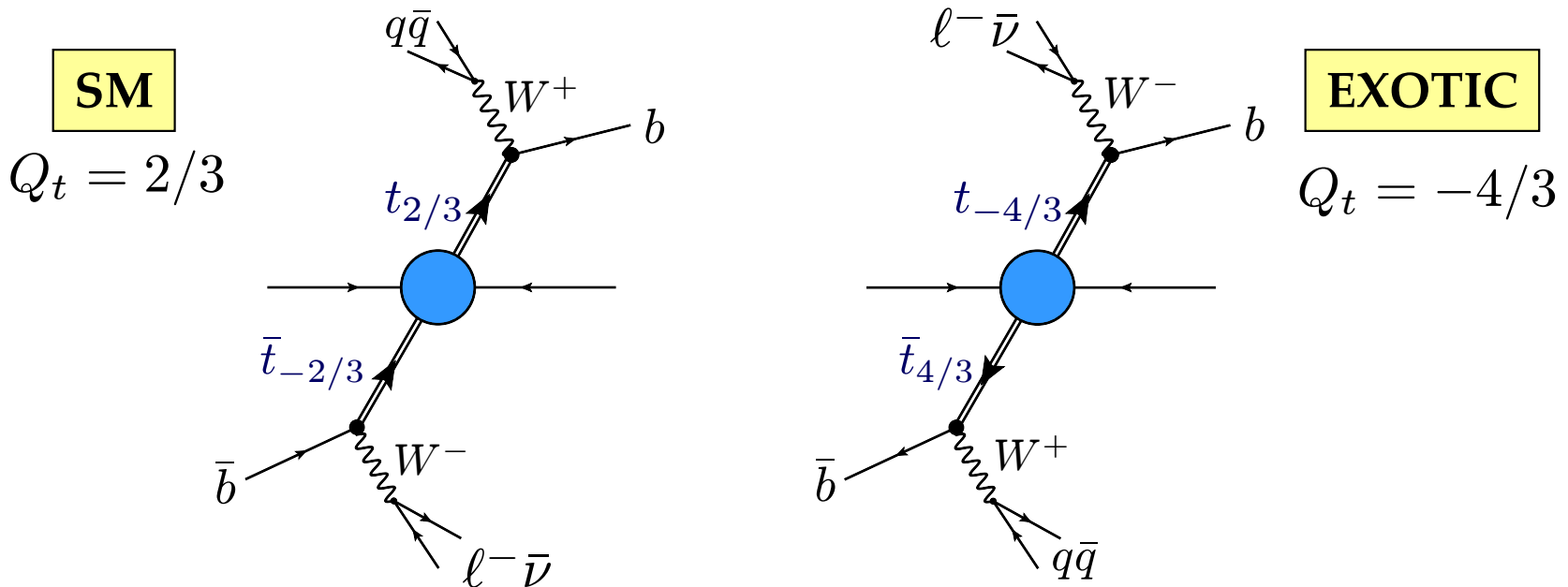
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**What do we know about the  
top quark electric charge ?**

# Top quark electric charge

## What do we know about the top quark electric charge ?

[Chang,Chang,Ma]:  $m_{Q_{4u}} = 172 \text{ GeV}, m_{t_{2/3}} \geq 356 \text{ GeV}$



✓ electroweak precision tests, ✓ Tevatron searches, ✓ LHC searches

# Top quark electric charge

**CDF: 5.6 fb<sup>-1</sup> (2011)**

- 1) identify W-boson charge through lepton charge
- 2) pair b-jet with W-boson (kinem. fits to  $m_{\text{top}}$ ,  $M_W$ )
- 3) measure b-jet charge (JetCharge Algorithm)

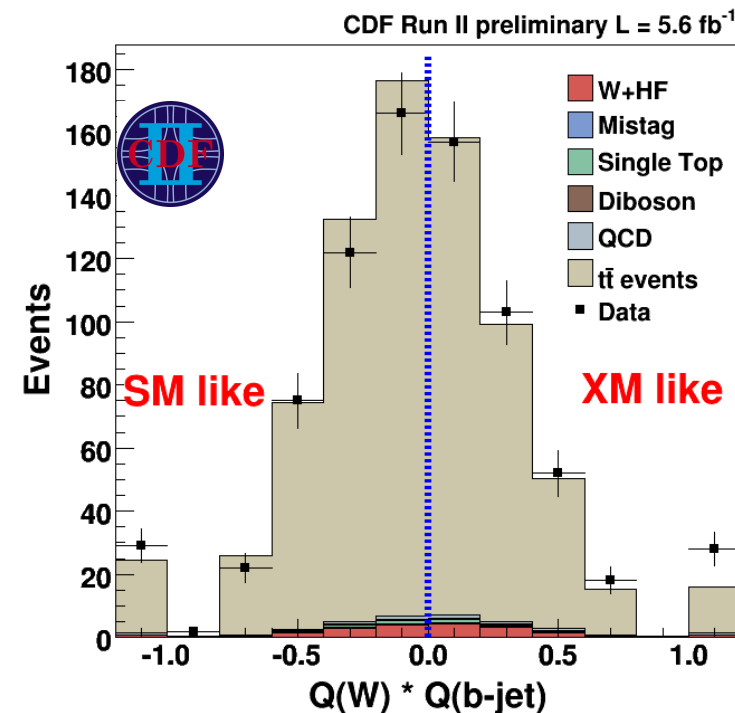
**SM** top quark charge  $\leftrightarrow Q(W) \cdot Q(\text{bjet}) < 0$

**XM** top quark charge  $\leftrightarrow Q(W) \cdot Q(\text{bjet}) > 0$

**result:** 416 SM events vs. 358 XM events

$\Rightarrow$  Exclusion of pure XM hypothesis with 95% C.L.

only 56% signal purity for SM top quarks



## $t\bar{t}$ pairs in association with a photon

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$$pp \rightarrow t\bar{t} + \gamma \text{ at the LHC}$$



# $t\bar{t}$ pairs in association with a photon

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$$pp \rightarrow t\bar{t} + \gamma \text{ at the LHC}$$

We are interested in the correlation  $\sigma_{t\bar{t}\gamma}(Q_{\text{top}}^2)$ .

Charge measurement is mainly a counting experiment.

NLO normalization is important!

LHC: high energy+luminosity  $\longrightarrow$  expect  $\sim 1000$  events from  $10 \text{ fb}^{-1}$

dominance of gluon flux  $\longrightarrow$  few photons from ISR ( $\propto Q_{\text{top}}$ )

**but:** „pollution“ from photon emission off top decay products (FSR)

# $t\bar{t}$ pairs in association with a photon

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[Baur, Juste,  
Rainwater, Orr]:

## Leading-order study

At the LHC with  $10 \text{ fb}^{-1}$  an accuracy of 10% on  $Q_t$  is feasible.  
„If scale uncertainty is reduced to 10%, an improvement in precision by a factor of two seems possible“

[Duan, Ma, Zhang,  
Han, Guo, Wang]:

## Next-to-leading-order QCD calculation

- small/large K-factor at the Tevatron/LHC
- FB asymmetry of -11%
- stable top quarks

# Our calculation

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Hadronic production of  $t\bar{t} + \gamma$  at NLO QCD including decays.

$$pp \rightarrow t\bar{t} + \gamma \rightarrow b\bar{b} \ell\nu jj + \gamma$$

2  $\rightarrow$  7 process is complicated at NLO QCD.

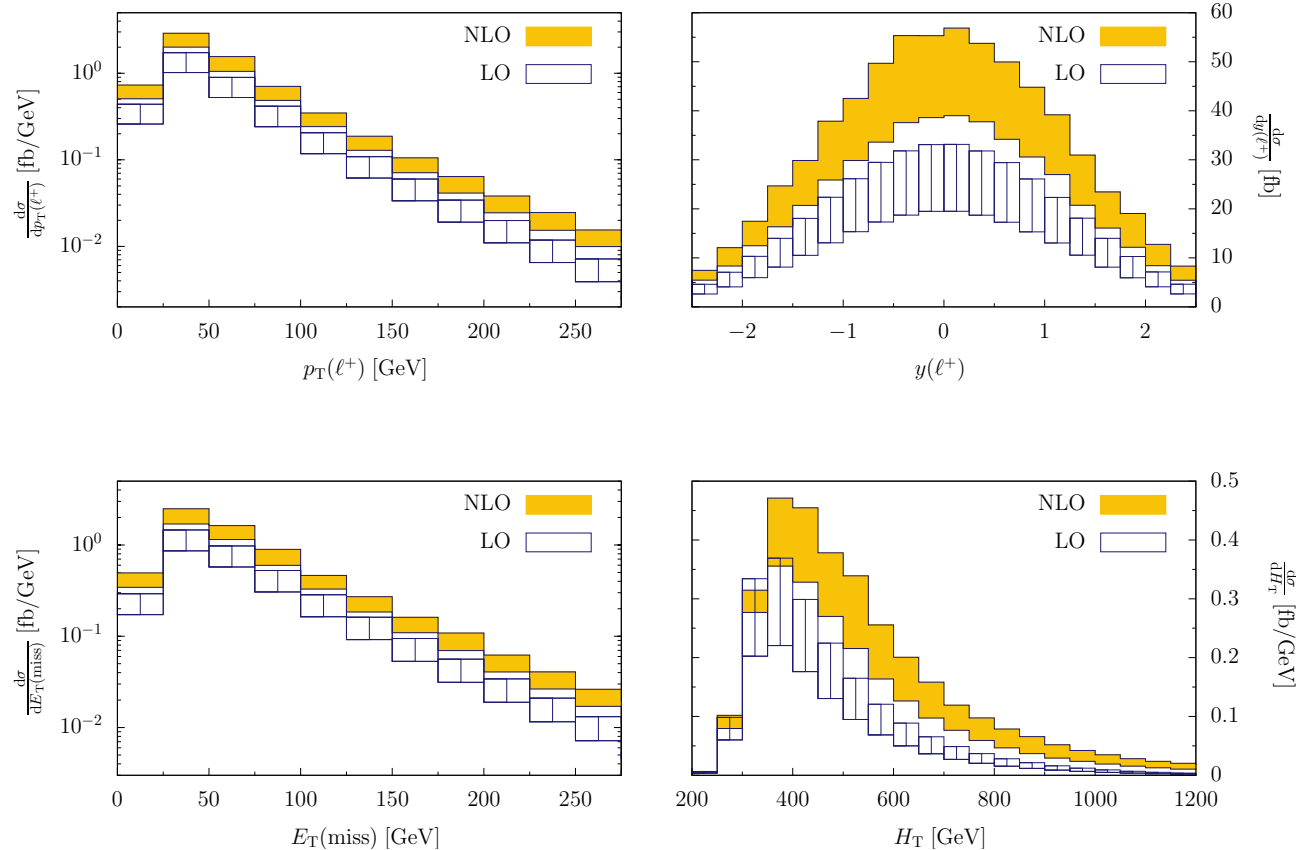
## What is important?

- spin correlations:  
*acceptances*
- photon radiation in decay:  
*large contribution*
- NLO corrections in production & decay:  
*normalization, scale dependence,  
leading soft/collinear emissions*

## What can be approximated?

- largely off-shell top quarks, W's:  
*neglect non-resonant contributions*  
 $\Rightarrow$  *narrow width approximation*  
*valid up to  $\mathcal{O}(\alpha_s \Gamma/m)$*
- neglect shower effects and  
higher order threshold corrections:  
*observables under consideration*  
*should not be very sensitive*

# Results



**LHC**  
leptons+jets channel  
std. acceptance cuts

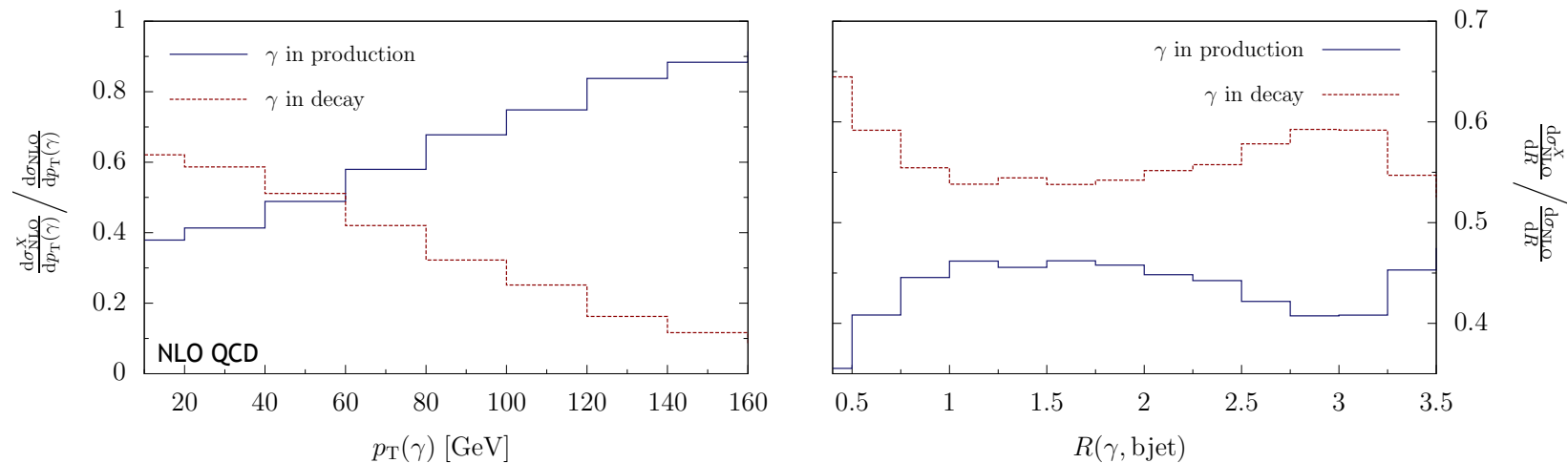
$$\sigma_{t\bar{t}\gamma}^{\text{LO}} = 74.5^{+24.0}_{-16.9} \text{ fb}$$

$$\sigma_{t\bar{t}\gamma}^{\text{NLO}} = 138^{+30}_{-23} \text{ fb}$$

- large K-factor  $\sim 1.9$
- no reduction of scale dependence (opening up of  $q$ - $g$  channel at NLO)

# Results

**Important:**  
**A large fraction of events from radiative top decays**

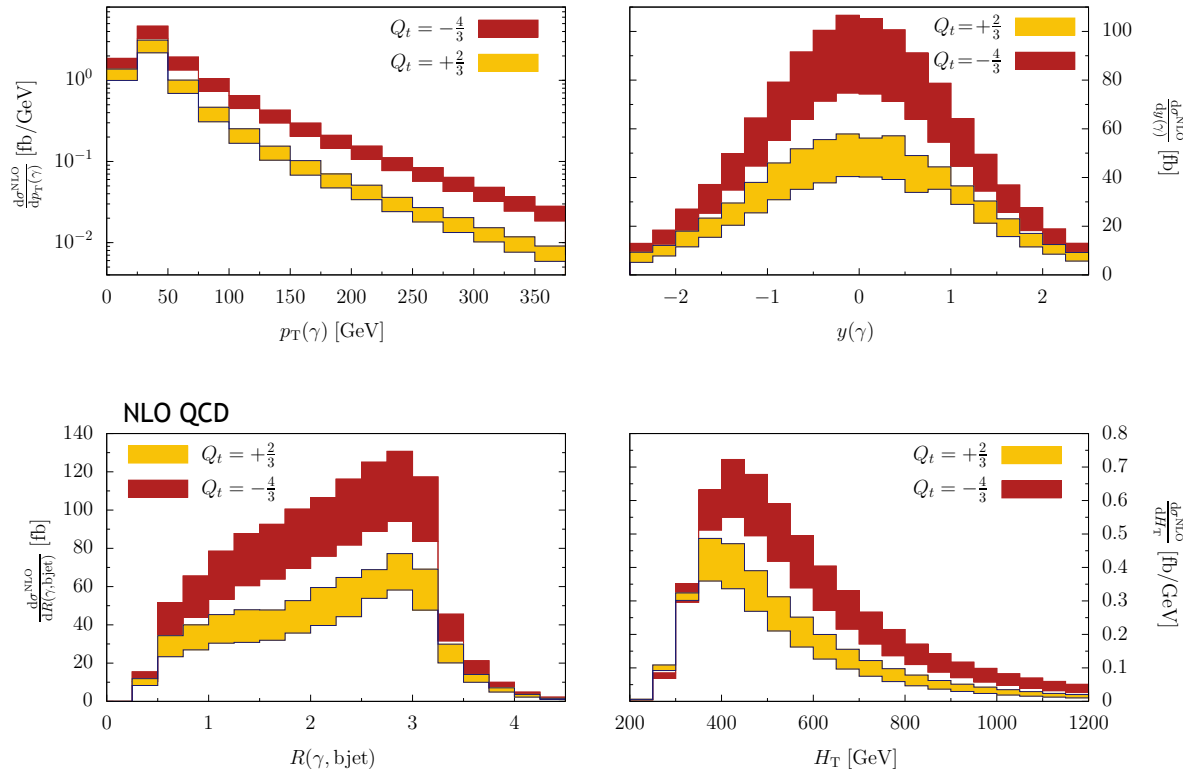


$$\sigma_{t\bar{t}\gamma}^{\text{decay}} = 56\% \sigma_{t\bar{t}\gamma}^{\text{tot}}$$

FSR photons are not very soft and well separated from b quarks.

# Results

## Exotic top quarks



$$\sigma_{t\bar{t}\gamma}^{\text{NLO}} = 138 \text{ fb} \xrightarrow{Q_t = \frac{2}{3} \rightarrow -\frac{4}{3}} \sigma_{t\bar{t}\gamma}^{\text{NLO}} = 243 \text{ fb}$$

Naive expectation of  $Q_t^2$  scaling fails  
because of large contribution from radiative top decay

# Results

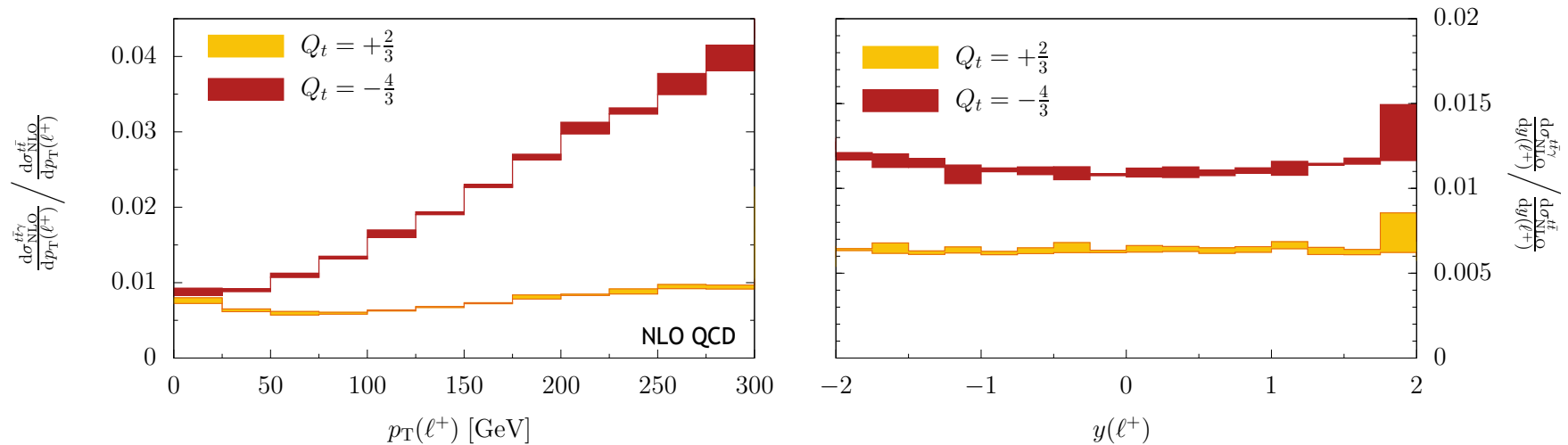
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## Three strategies:

- 1.) measure the total cross section
- 2.) study ratio of cross sections
- 3.) apply cuts to enhance  $Q_t^2$  dependence

# Results

## 2.) Ratio of cross sections $\sigma_{t\bar{t}\gamma} / \sigma_{t\bar{t}}$



$$\frac{\sigma_{t\bar{t}\gamma}^{Q_t=2/3}}{\sigma_{t\bar{t}}} = \begin{cases} 5.66^{+0.03}_{-0.02} \times 10^{-3}, & \text{LO;} \\ 6.33^{+0.26}_{-0.14} \times 10^{-3}, & \text{NLO,} \end{cases} \quad \frac{\sigma_{t\bar{t}\gamma}^{Q_t=-4/3}}{\sigma_{t\bar{t}}} = \begin{cases} 10.4^{+0.2}_{-0.2} \times 10^{-3}, & \text{LO;} \\ 11.2^{+0.3}_{-0.2} \times 10^{-3}, & \text{NLO.} \end{cases}$$

- Ratios are significantly more stable against NLO corrections
- Small scale uncertainties
- Some experimental uncertainties cancel

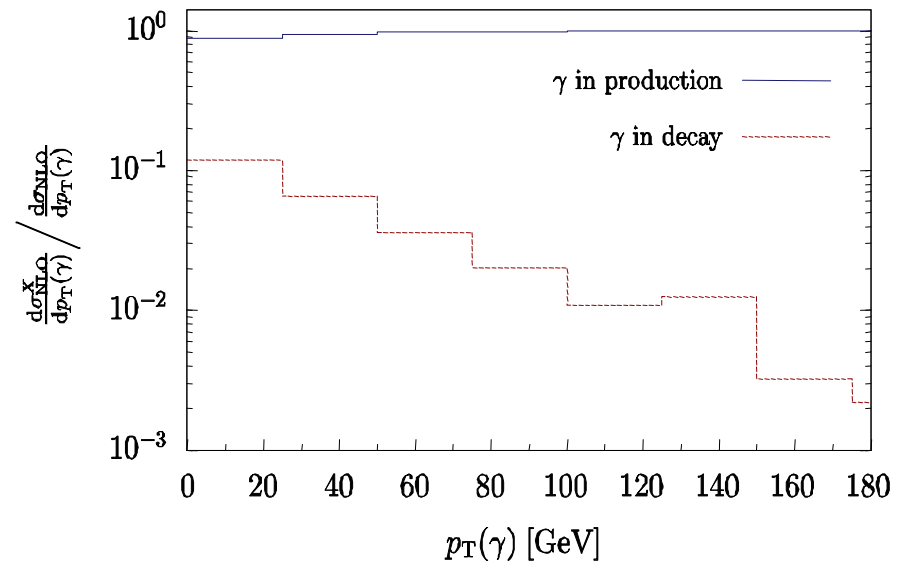
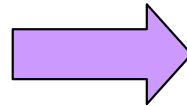
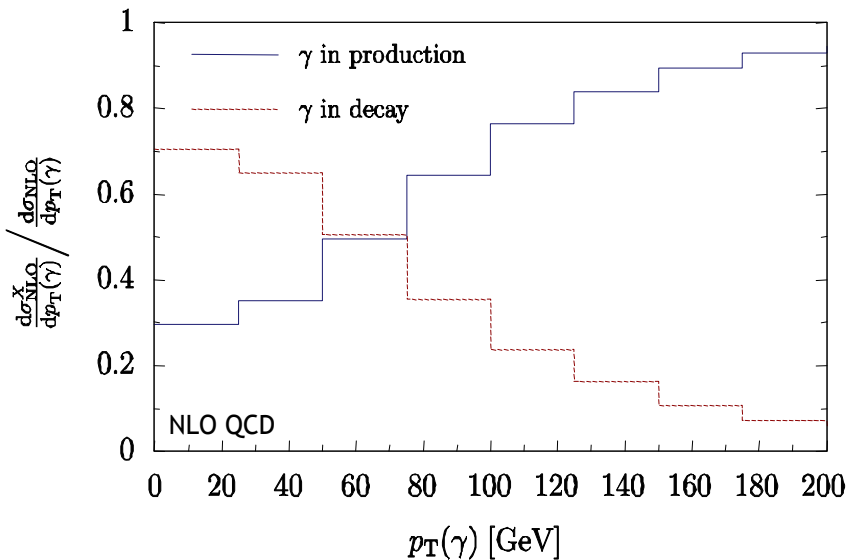


# Results

## 3.) Choose cuts to enhance $Q_t^2$ dependence

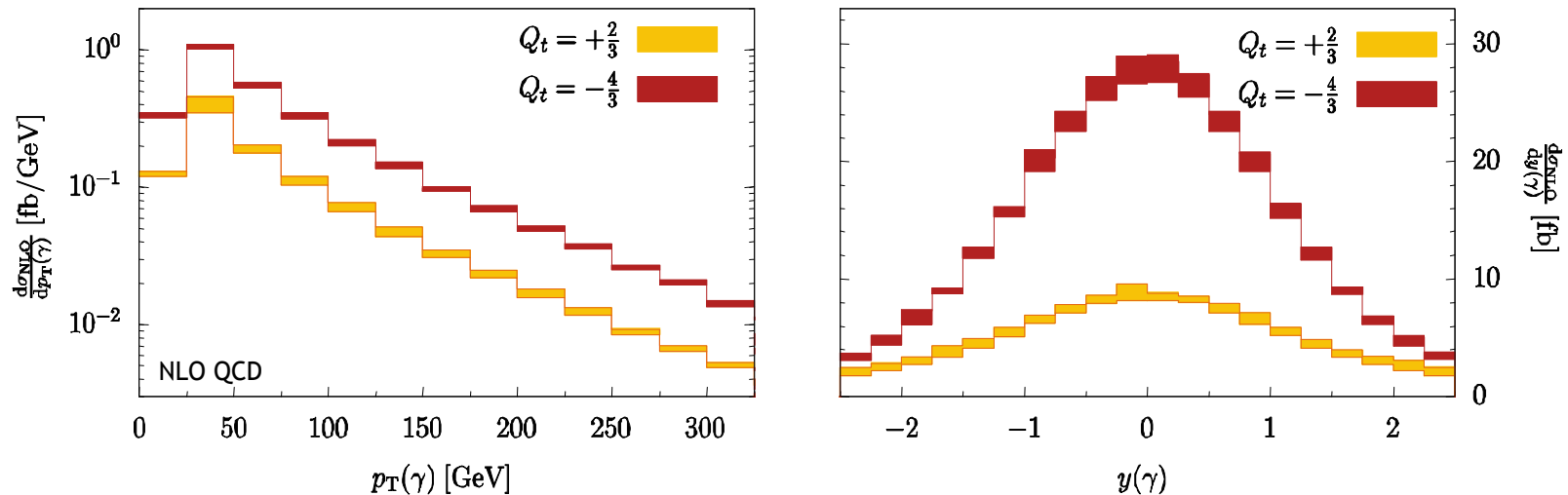
Inspired by U.Baur et.al.: suppress radiative top decays

$$m_T(bl\gamma; E_T^{\text{miss}}) > 180 \text{ GeV}, \quad m_T(l\gamma; E_T^{\text{miss}}) > 90 \text{ GeV}, \\ 160 \text{ GeV} < m(bjj) < 180 \text{ GeV}, \quad 70 \text{ GeV} < m(jj) < 90 \text{ GeV}$$



# Results

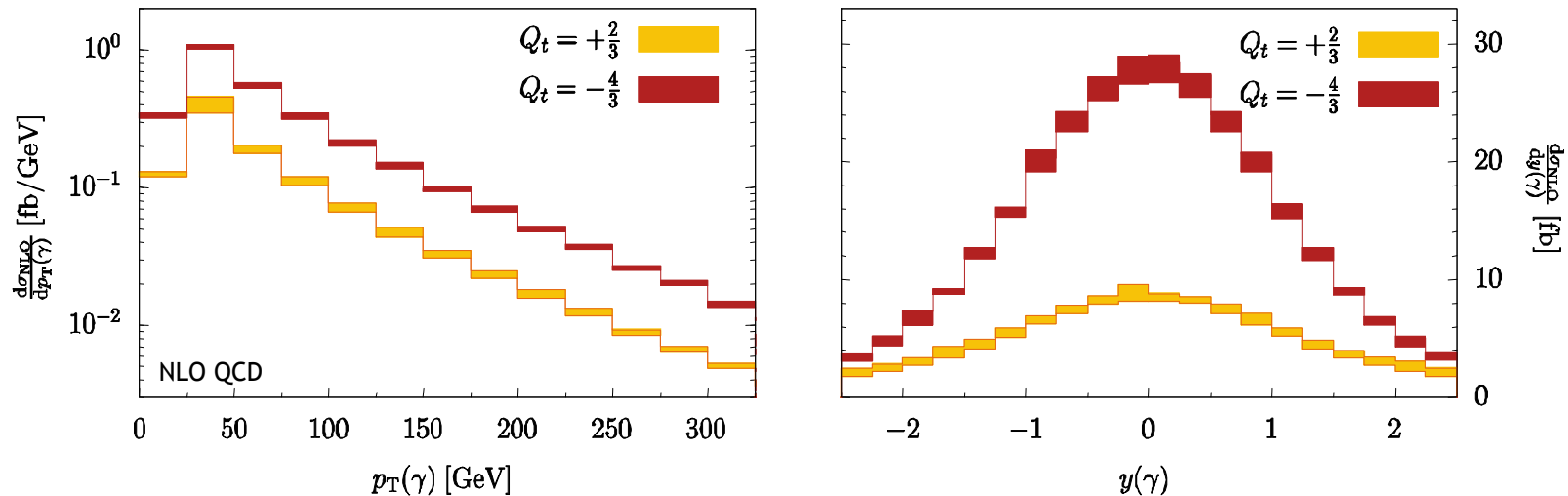
## 3.) Choose cuts to enhance $Q_t^2$ dependence



- strong reduction of scale dependence  
smaller K-factor
- enhanced  $Q_t$  dependence

# Results

## 3.) Choose cuts to enhance $Q_t^2$ dependence



- strong reduction of scale dependence  
smaller K-factor
- enhanced  $Q_t$  dependence

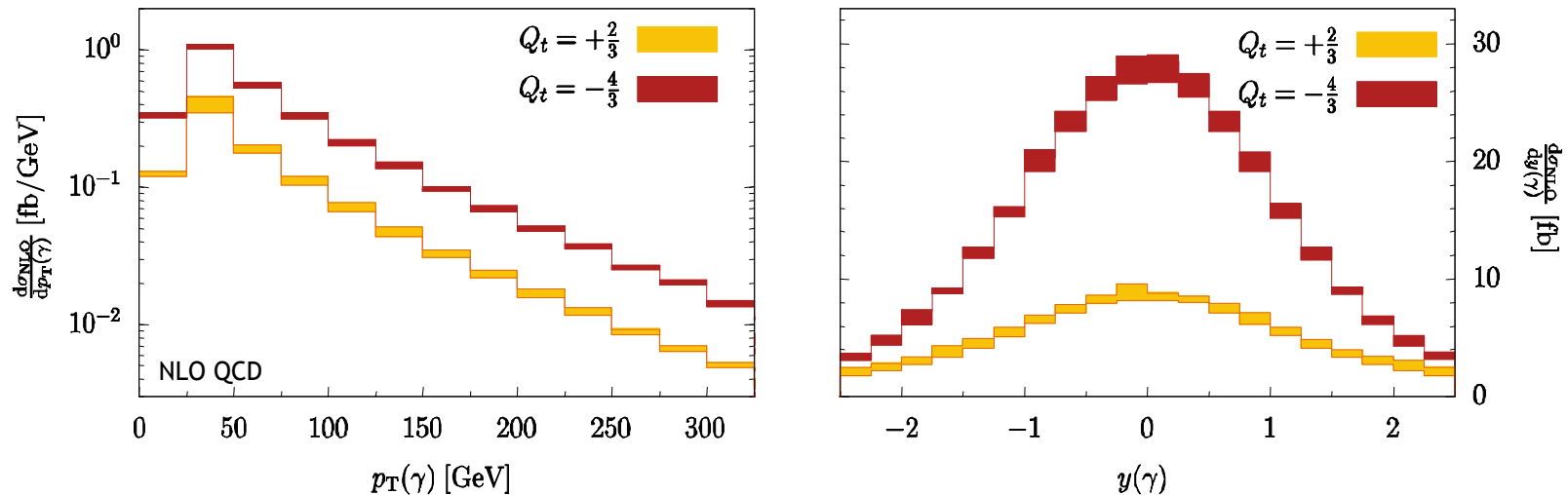
**However:**

- much smaller cross section

$$\sigma_{\text{SM } t\bar{t}\gamma}^{\text{nocuts}} = 138 \text{ fb} \quad \longrightarrow \quad \sigma_{\text{SM } t\bar{t}\gamma}^{\text{cuts}} = 26 \text{ fb}$$

# Results

## 3.) Choose cuts to enhance $Q_t^2$ dependence



luminosity  $\mathcal{L}$  to separate SM and XM hypothesis at  $3\sigma$  C.L.:

$$\frac{\mathcal{L}_{\text{no cuts}}}{\mathcal{L}_{\text{cuts}}} = \begin{cases} 1.98 \pm 0.02, & \text{LO;} \\ 1.12 \pm 0.08, & \text{NLO;} \end{cases}$$

100% gain at LO is reduced to 10% gain at NLO

# SUMMARY

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- $t\bar{t} + \gamma$  is an interesting LHC signal that can be studied soon
- we provide NLO QCD predictions for realistic observables
- large fraction of events from radiative top decays
- measurement of the top quark electric charge at the LHC is the first step towards studies of other electroweak couplings

# SUMMARY

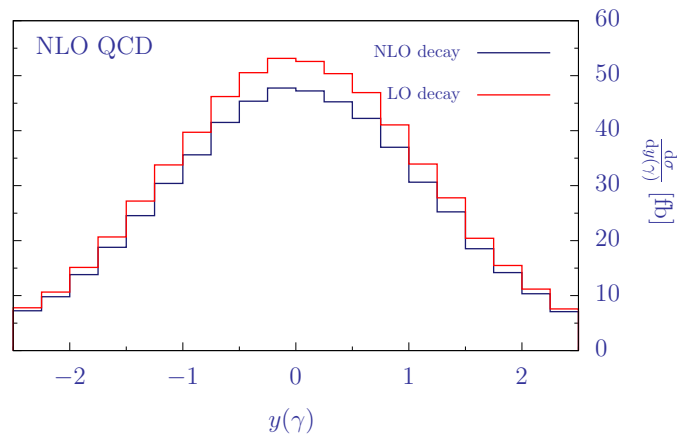
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- $t\bar{t} + \gamma$  is an interesting LHC signal that can be studied soon
- we provide NLO QCD predictions for realistic observables
- large fraction of events from radiative top decays
- measurement of the top quark electric charge at the LHC is the first step towards studies of other electroweak couplings
- what I left out:
  - we use unitarity methods to calculate virtual corrections
  - $t\bar{t} + \gamma$  measurement at the Tevatron (New Physics search)
  - FB asymmetry

# Extras

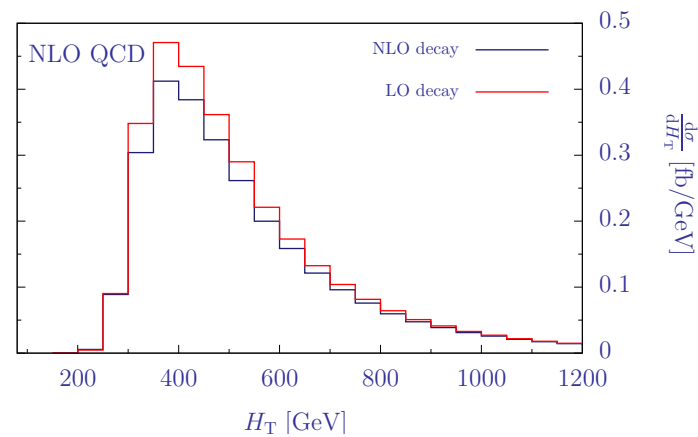
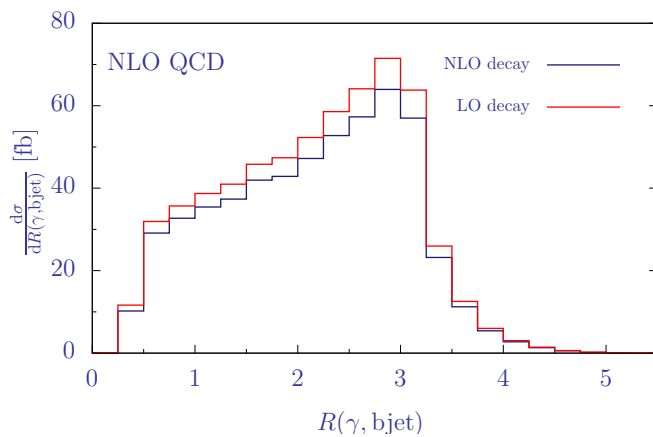
# Extras

## Impact of NLO corrections in the decay



LHC (7TeV)  
semi-lept. channel  
std. accept. cuts

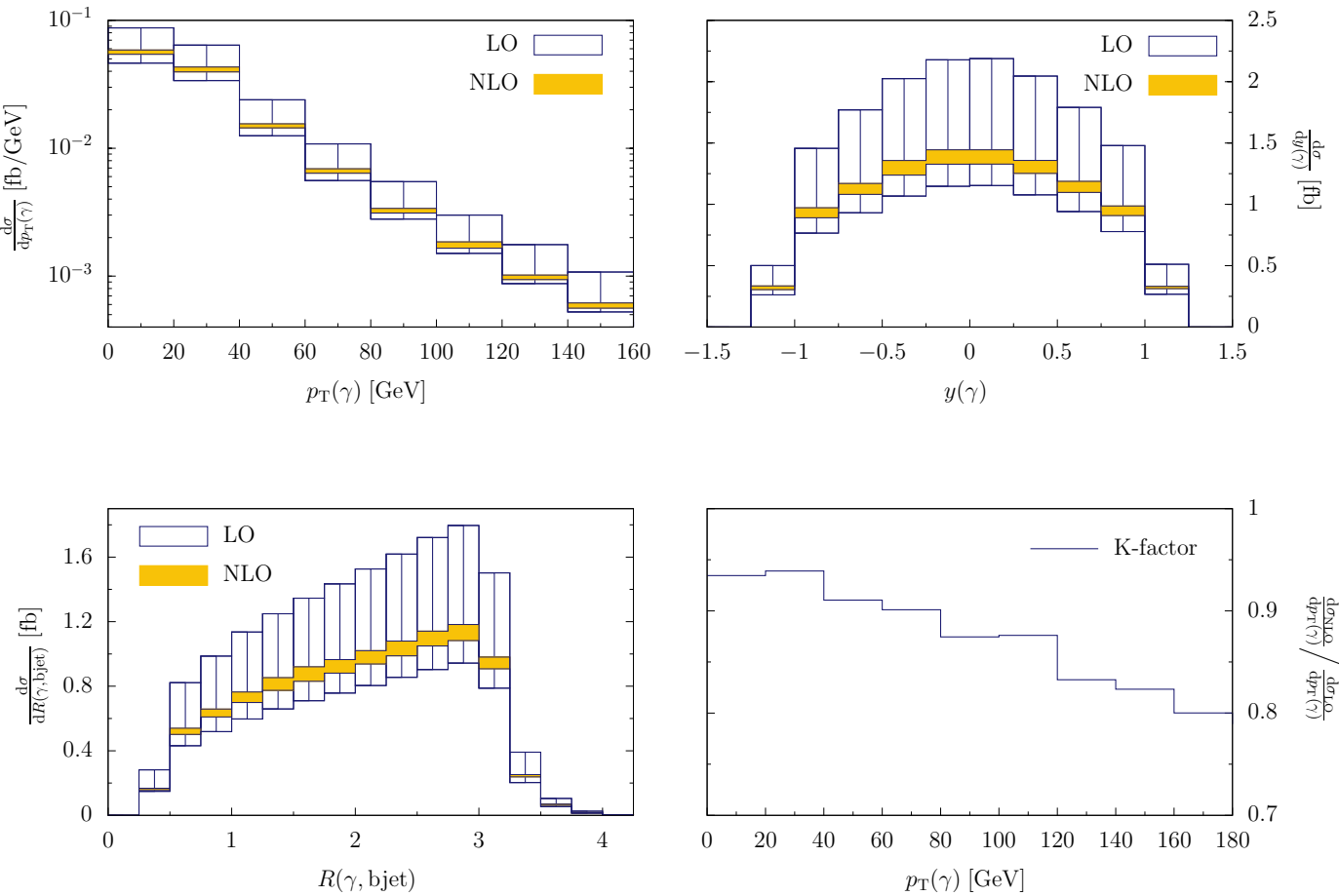
-13% to total cross section





# Extras

## Tevatron results



$$\sigma_{t\bar{t}\gamma}^{\text{LO}} = 2.85_{-0.75}^{+1.14} \text{ fb}$$

$$\sigma_{t\bar{t}\gamma}^{\text{NLO}} = 2.64_{-0.03}^{+0.21} \text{ fb}$$

$$\sigma_{t\bar{t}\gamma}^{\text{NLO}} = 2.64 \text{ fb}$$

$$\xrightarrow[\times \text{efficiencies} \times 4]{\mathcal{L}_{\text{int}} = 6.0 \text{ fb}^{-1}}$$

$14 \pm 1$  events vs. **CDF**:  $14 \pm 3$  events  
(LO:  $16 \pm 5$  events)

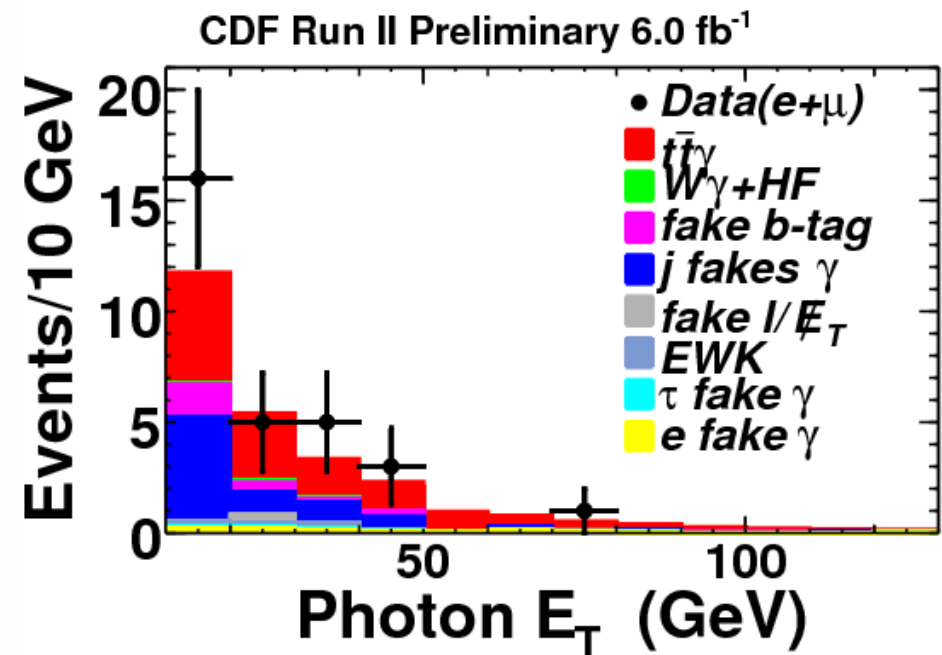
# Extras

## Tevatron results

CDF Run II, 6.0 fb<sup>-1</sup>

$t\bar{t}\gamma$ , Isolated Leptons, Tight Chi2 on Photons

Standard Model Source	$e\gamma b\cancel{E}_T$	$\mu\gamma b\cancel{E}_T$	$(e + \mu)\gamma b\cancel{E}_T$
$t\bar{t}\gamma(\text{semileptonic})$	$5.98 \pm 1.10$	$5.21 \pm 0.97$	$11.19 \pm 2.04$
$t\bar{t}\gamma(\text{dileptonic})$	$1.47 \pm 0.27$	$1.27 \pm 0.24$	$2.74 \pm 0.50$
$W^\pm e\gamma$	$0 \pm 0.07$	$0 \pm 0.07$	$0 \pm 0.09$
$W^\pm c\bar{c}\gamma$	$0 \pm 0.05$	$0.05 \pm 0.05$	$0.05 \pm 0.07$
$W^\pm b\bar{b}\gamma$	$0.15 \pm 0.07$	$0.06 \pm 0.05$	$0.21 \pm 0.08$
$WZ$	$0.05 \pm 0.05$	$0.05 \pm 0.05$	$0.09 \pm 0.06$
$WW$	$0.06 \pm 0.03$	$0.06 \pm 0.03$	$0.11 \pm 0.03$
Single Top (s-chan)	$0.09 \pm 0.10$	$0 \pm 0.10$	$0.09 \pm 0.13$
Single Top (t-chan)	$0.14 \pm 0.14$	$0.13 \pm 0.14$	$0.27 \pm 0.19$
$\tau \rightarrow \gamma$ fake	$0.20 \pm 0.08$	$0.10 \pm 0.05$	$0.29 \pm 0.09$
Jet faking $\gamma$ ( $e j \cancel{E}_T b, j \rightarrow \gamma$ )	$5.75 \pm 1.76$	$1.79 \pm 1.56$	$7.54 \pm 2.53$
Mistags	$1.47 \pm 0.37$	$1.02 \pm 0.32$	$2.50 \pm 0.51$
QCD(Jets faking $\ell$ and $\cancel{E}_T$ )	$0.38 \pm 0.38$	$0.02 \pm 0.020$	$0.40 \pm 0.38$
$ee\cancel{E}_T b, e \rightarrow \gamma$	$0.94 \pm 0.19$	-	$0.94 \pm 0.19$
$\mu e\cancel{E}_T b, e \rightarrow \gamma$	-	$0.49 \pm 0.11$	$0.49 \pm 0.11$
Total SM Prediction	$16.7 \pm 2.2(\text{tot})$	$10.3 \pm 1.9(\text{tot})$	$26.9 \pm 3.4(\text{tot})$
Observed in Data	17	13	30



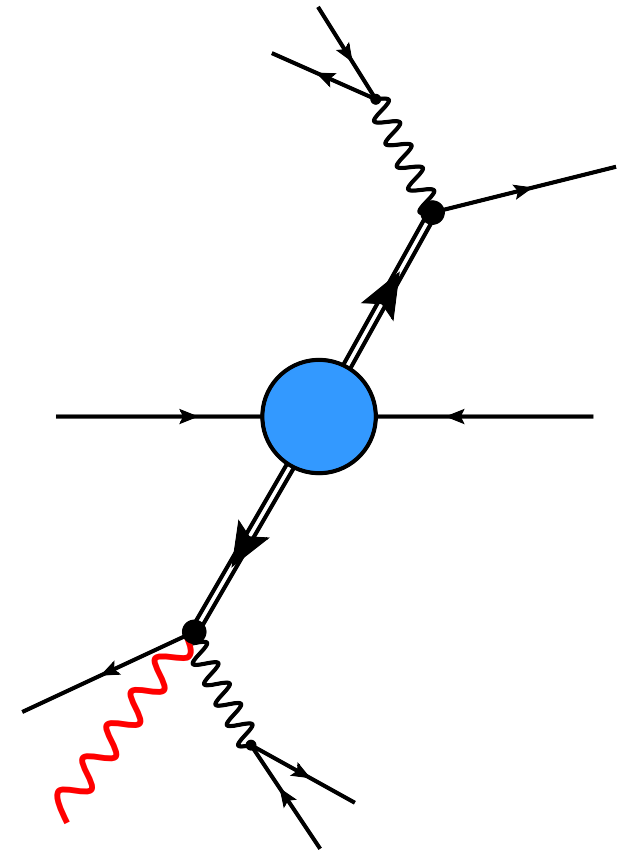
# Extras

## Coupling the photon at NLO

Master formula:  $d\sigma \stackrel{\text{NWA}}{=} d\sigma_{t\bar{t}\gamma} d\mathcal{B}_t d\mathcal{B}_{\bar{t}} + d\sigma_{t\bar{t}} (d\mathcal{B}_{t\gamma} d\mathcal{B}_{\bar{t}} + d\mathcal{B}_t d\mathcal{B}_{\bar{t}\gamma})$

expand in  $\alpha_s$ :

$$\begin{aligned}
 d\sigma^{\delta\text{NLO}} = & d\sigma_{t\bar{t}\gamma}^{\delta\text{NLO}} d\mathcal{B}_t^{\text{LO}} d\mathcal{B}_{\bar{t}}^{\text{LO}} \\
 & + d\sigma_{t\bar{t}\gamma}^{\text{LO}} (d\mathcal{B}_t^{\delta\text{NLO}} d\mathcal{B}_{\bar{t}}^{\text{LO}} + d\mathcal{B}_t^{\text{LO}} d\mathcal{B}_{\bar{t}}^{\delta\text{NLO}}) \\
 & + d\sigma_{t\bar{t}}^{\delta\text{NLO}} (d\mathcal{B}_{t\gamma}^{\text{LO}} d\mathcal{B}_{\bar{t}}^{\text{LO}} + d\mathcal{B}_t^{\text{LO}} d\mathcal{B}_{\bar{t}\gamma}^{\text{LO}}) \\
 & + d\sigma_{t\bar{t}}^{\text{LO}} (d\mathcal{B}_{t\gamma}^{\delta\text{NLO}} d\mathcal{B}_{\bar{t}}^{\text{LO}} + d\mathcal{B}_t^{\text{LO}} d\mathcal{B}_{\bar{t}\gamma}^{\delta\text{NLO}} \\
 & \quad + d\mathcal{B}_{t\gamma}^{\text{LO}} d\mathcal{B}_{\bar{t}}^{\delta\text{NLO}} + d\mathcal{B}_t^{\delta\text{NLO}} d\mathcal{B}_{\bar{t}\gamma}^{\text{LO}})
 \end{aligned}$$



# Extras

## FB asymmetry in $t\bar{t}$ +photon

$$A_{\text{FB}} = \frac{N(y_t > 0) - N(y_t < 0)}{N(y_t > 0) + N(y_t < 0)}$$

- $t\bar{t}$  asymmetry appears only at NLO QCD

[Kühn,Rodrigo]

Theory prediction  $A_{\text{FB}}(t\bar{t}) = 5\%$  in tension with measurement ( $2\sigma$ )

Complete NNLO correction unknown, but indications for robustness

- $t\bar{t} + \gamma$  asymmetry appears already at LO

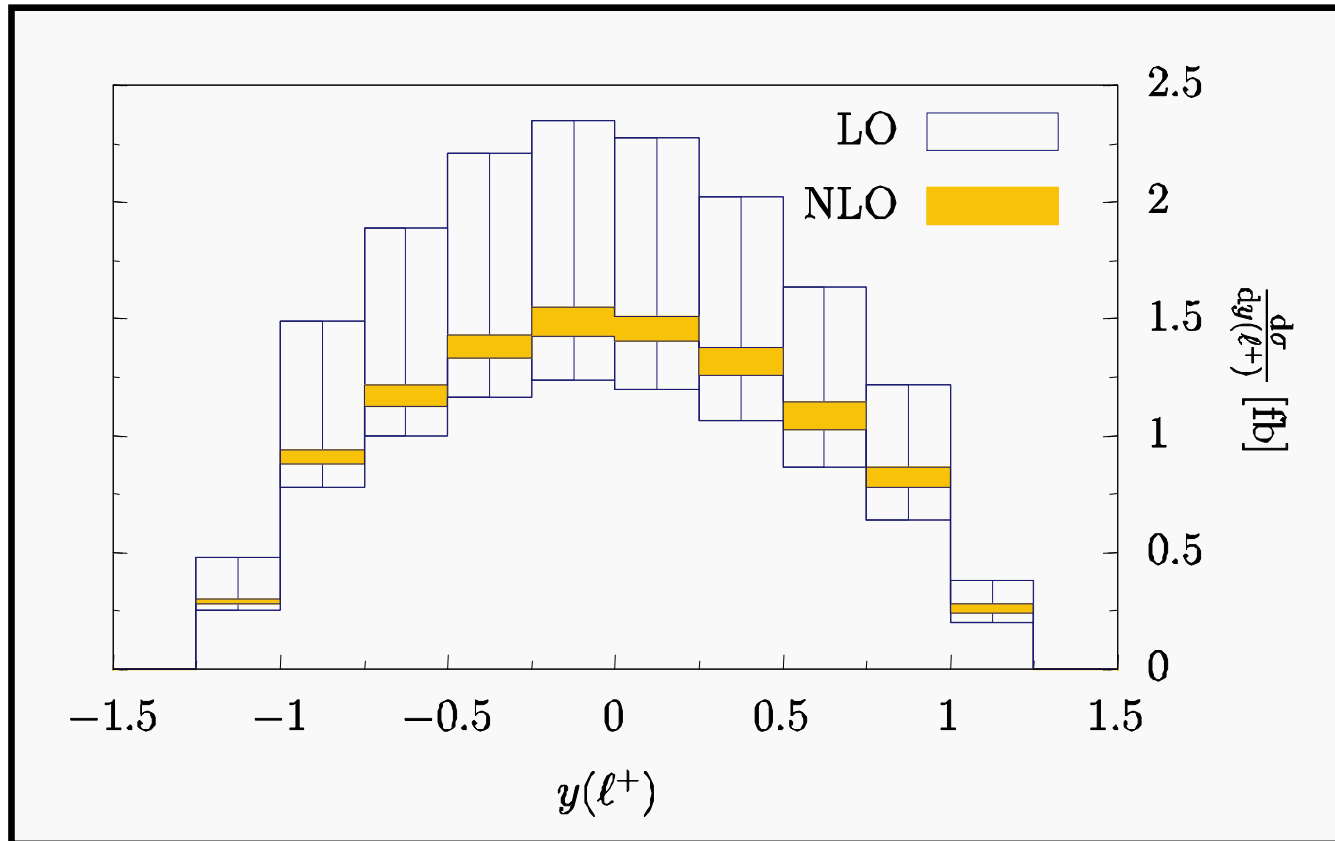
$$A_{\text{FB}}^{\text{LO}}(t\bar{t}\gamma) = -17\%, \quad A_{\text{FB}}^{\text{NLO}}(t\bar{t}\gamma) = -12\%$$

The 5% reduction at NLO can be understood. [Melnikov,MS :  $t\bar{t} + \text{jet}$ ]

Similar effect for  $t\bar{t} + \text{jet}$  :  $A_{\text{FB}}^{\text{LO}}(t\bar{t}\text{jet}) = -8\%$ ,  $A_{\text{FB}}^{\text{NLO}}(t\bar{t}\text{jet}) = -2\%$

# Extras

## FB asymmetry in $t\bar{t}$ +photon



# Extras

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## Extraction of total cross section

Measure  $\sigma_{b\bar{b}l\nu jj\gamma}^{\text{meas.}}$  and extract  $\sigma_{t\bar{t}\gamma}$  through dividing by branchings

$$\sigma_{t\bar{t}\gamma} = \sigma_{b\bar{b}l\nu jj\gamma}^{\text{meas.}} \times \mathcal{B}(t \rightarrow bl\nu)^{-1} \times \mathcal{B}(\bar{t} \rightarrow \bar{b}jj)^{-1} \quad \text{is wrong.}$$

Instead, the radiative top decays have to be treated as „background“,

$$\sigma_{t\bar{t}\gamma} = \left( \sigma_{b\bar{b}l\nu jj\gamma}^{\text{meas.}} - \sigma_{b\bar{b}l\nu jj\gamma}^{\text{decay}} \right) \times \mathcal{B}(t \rightarrow bl\nu)^{-1} \times \mathcal{B}(\bar{t} \rightarrow \bar{b}jj)^{-1} .$$