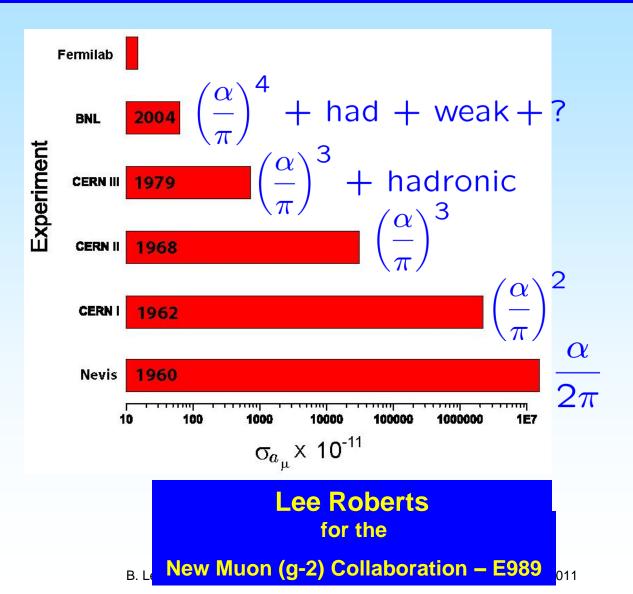
# The Fermilab Muon (g-2) Experiment



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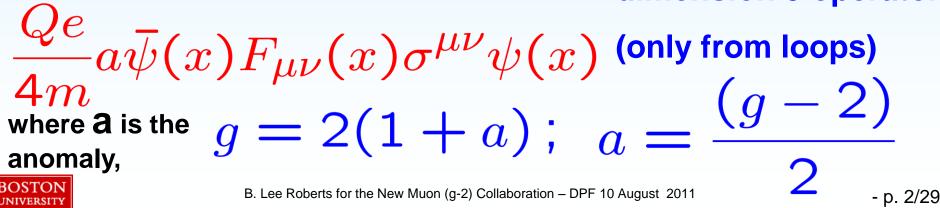
# In the beginning there was Dirac

$$i(\partial_{\mu} - ieA_{\mu}(x))\gamma^{\mu}\psi(x) = m\psi(x)$$

predicted electron magnetic moment

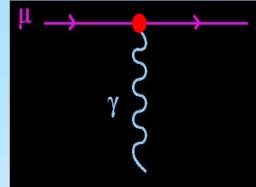
$$\vec{\mu} = g\left(\frac{Qe}{2m}\right)\vec{s}, \quad e > 0$$
$$g \equiv 2$$

However, experimentally **g** > 2; need to add a Pauli term dimension 5 operator



### **Magnetic and Electric Dipole Interactions**

$$\Gamma_{\beta} = eF_1 \bar{\psi}_R \gamma_{\beta} \psi_R + \frac{ie}{2m} F_2 \bar{\psi}_R \sigma_{\beta\delta} q^{\delta} \psi_L$$
$$+ HC$$



• Muon Magnetic Dipole Momoment  $a_{\mu}$  chiral changing

$$\overline{u}_{\mu}[eF_1(q^2)\gamma_{\beta} + \frac{ie}{2m_{\mu}}F_2(q^2)\sigma_{\beta\delta}q^{\delta}]u_{\mu}$$
$$F_1(0) = 1 \quad F_2(0) = a_{\mu}$$

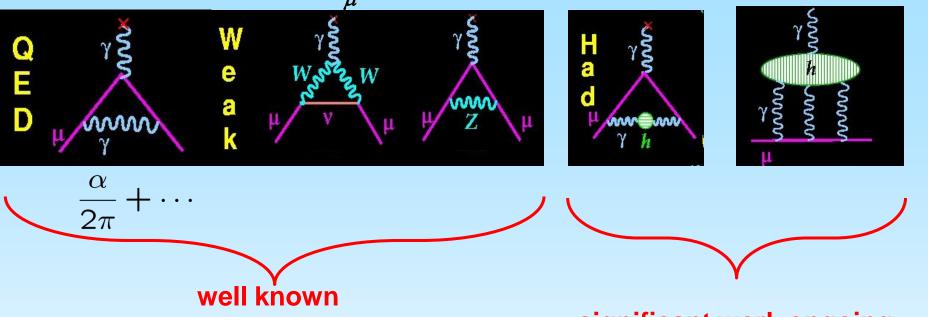
• Muon EDM

$$\overline{u}_{\mu} \begin{bmatrix} \frac{ie}{2m_{\mu}} F_2(q^2) - F_3(q^2)\gamma_5 \end{bmatrix} \sigma_{\beta\delta} q^{\delta} u_{\mu}$$
$$F_2(0) = a_{\mu} \quad F_3(0) = d_{\mu}; \text{ EDM}$$



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#### The SM Value for a<sub>µ</sub>



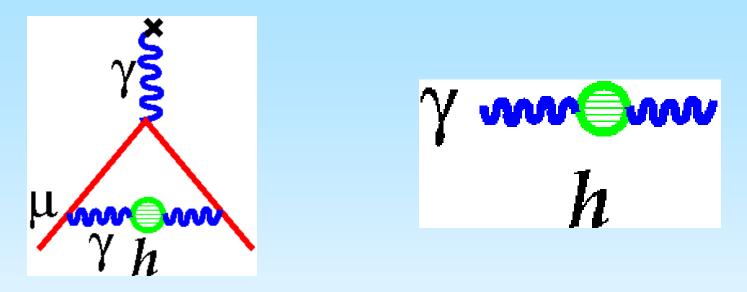
• QED calculated to  $\alpha^5$ 

significant work ongoing

- Weak calculated through 2 loops
  - 2-loop contribution reduced the contribution by 20%
  - 3-loop leading logs estimated to be small

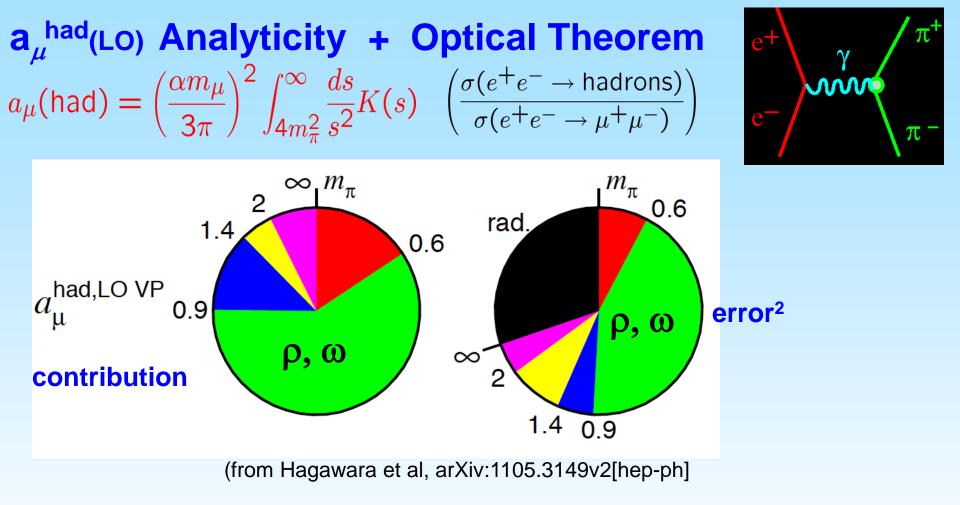


The Lowest-order Hadronic Contribution  $\Pi^{\mu\nu}$ Photon self-energy diagram



- Options
  - Use experimental data and dispersion relations
  - Use low energy effective Lagrangians:
    - hadronic models that contain the features of QCD
  - non-pertubative calculations in lattice QCD



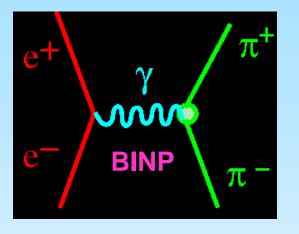


 Future efforts should reduce errors

 CMD3 at VEPP2000, up to 2.0 GeV (next 5 years), Mainz, BES and perhaps Belle

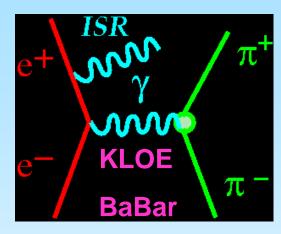


# Energy Scan (Novosibirsk); ISR KLOE and BaBar



scan e<sup>+</sup>e<sup>-</sup> beam energy

- KLOE: on or near φ
  - the  $\gamma$  is soft
    - goes down the beam pipe, (2008)
    - at large angle and is detected(2010); normalize to Bhabha, use theory to calculate  $\sigma_{\mu\mu}$
  - measure R(s) directly (2008 data), presented 2011.



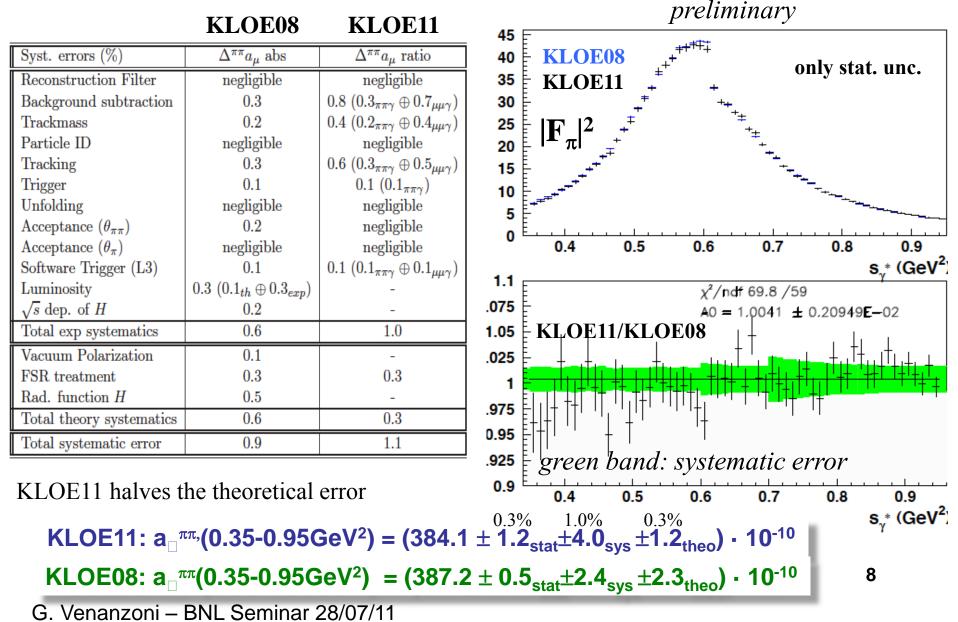
#### use ISR to lower collision energy

- BaBar: on the Y 4s
  - the  $\gamma$  is hard, and is detected
  - excellent particle ID with  $\mu$ - $\pi$  separation
  - measures R (s) directly

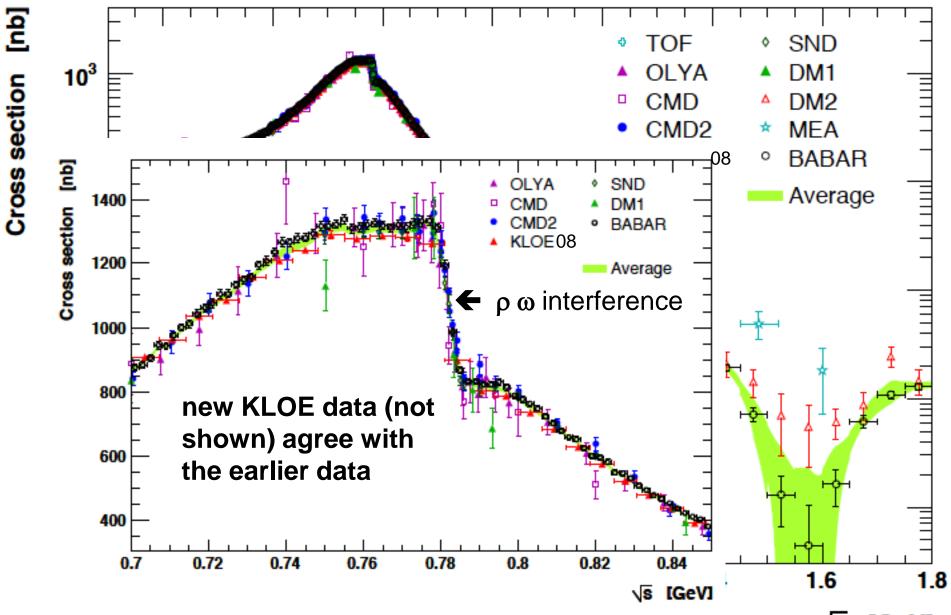


# KLOE11 result on $|F_{\pi}|^2$ and comp. with KLOE08





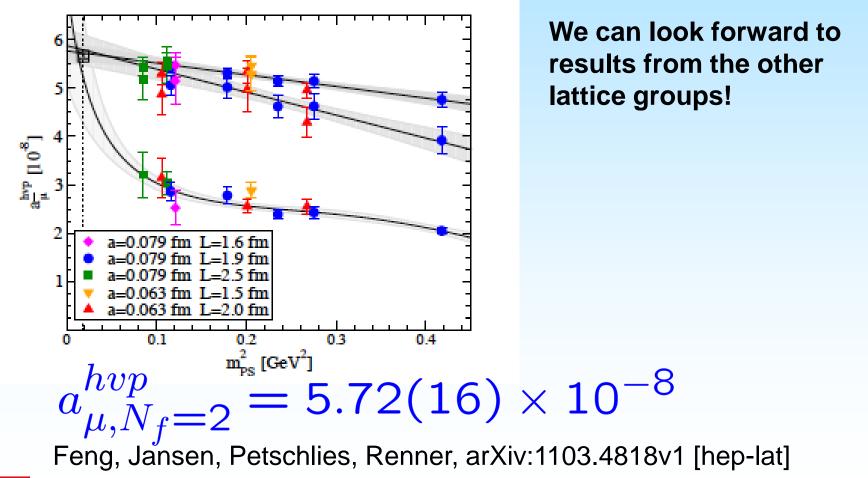
### **Measured Cross section for** $e^+e^- \rightarrow \pi^+\pi^-$



√s [GeV]

# What about the lattice?

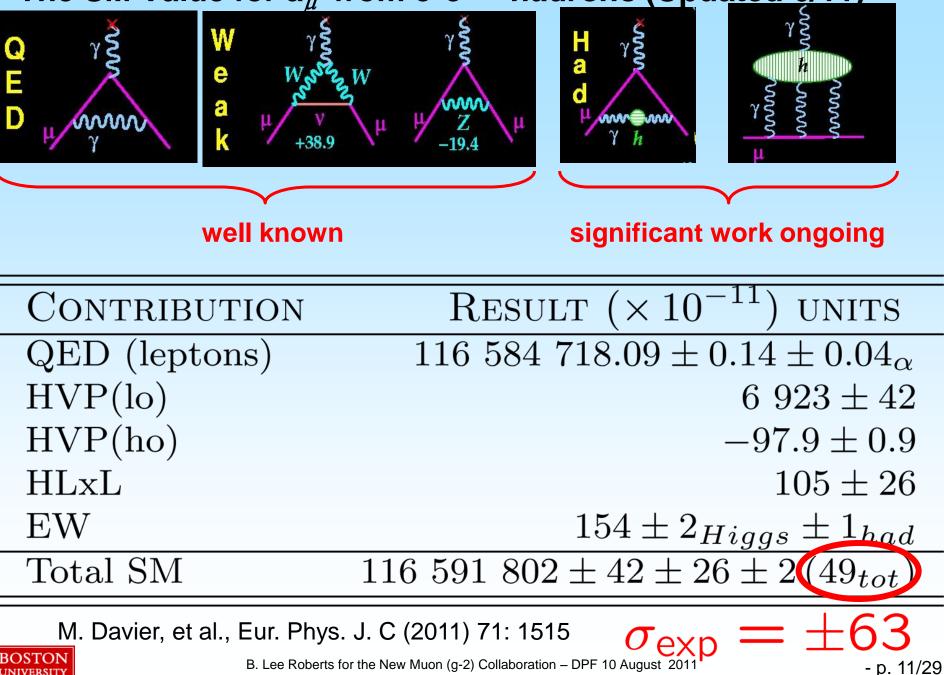
 At the INT Workshop on the Hadronic Light-by-Light contribution in February, Karl Jansen presented a new 2-3% lattice result for the <u>lowest-order</u> hadronic contribution:



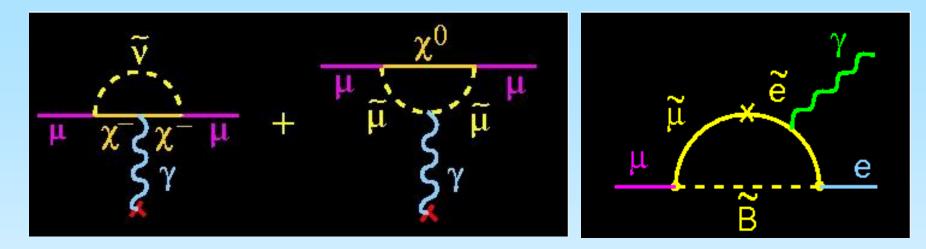


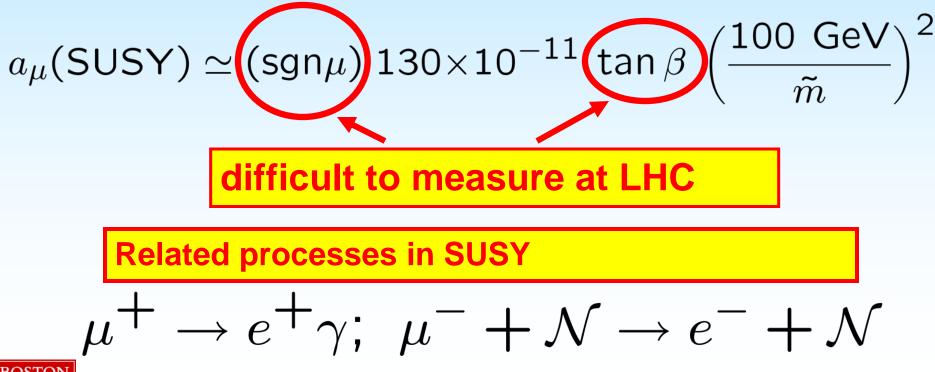
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#### The SM Value for $a_{\mu}$ from $e^+e^- \rightarrow hadrons$ (Updated 6/11)

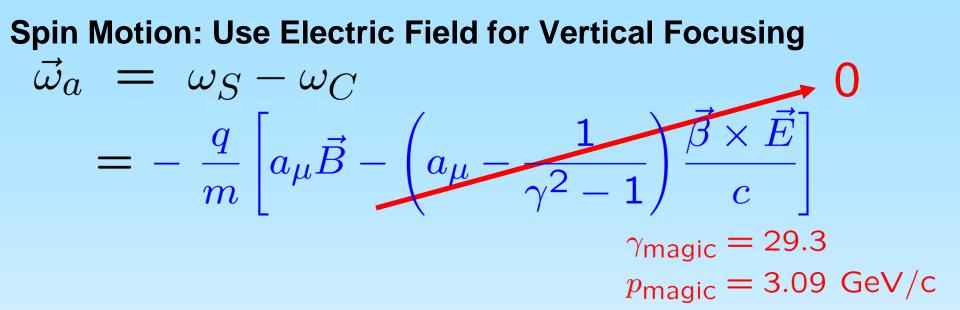


#### $a_{\mu}$ is sensitive to a wide range of new physics, e.g.SUSY

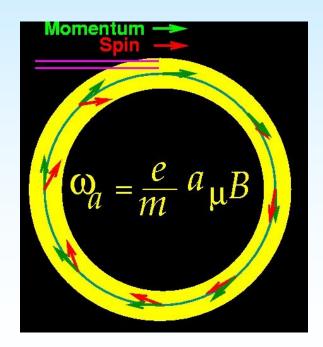




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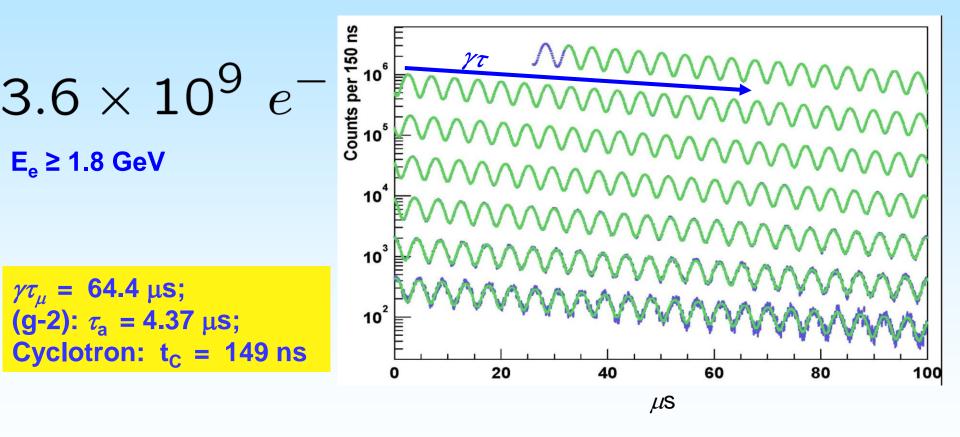
# Electrostatic quadrupoles cover 43% of ring Small (< 1ppm) correction for muons not at the magic γ.





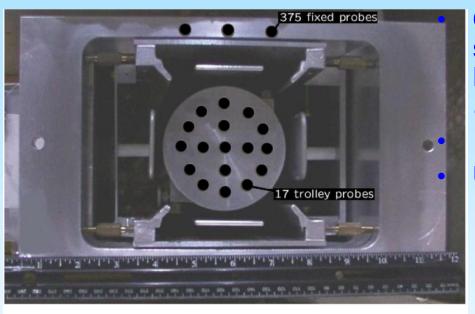
# The arrival time spectrum of high-energy $e^{-\omega_a}$

$$f(t) \simeq N_0 e^{-\lambda t} [1 + A \cos \omega_a t + \phi)]$$

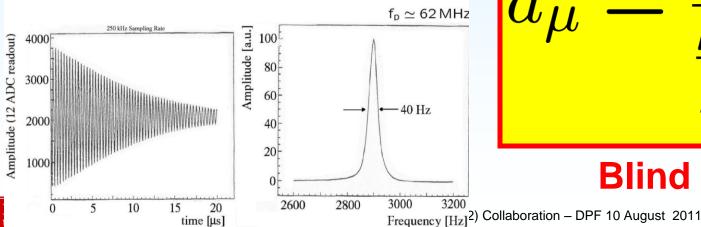




# The magnetic field is measured and controlled using pulsed NMR and the free-induction decay.

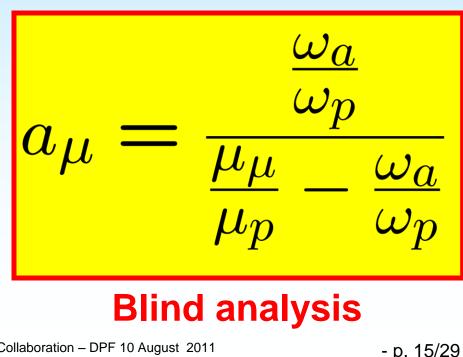


Free induction decay signals:



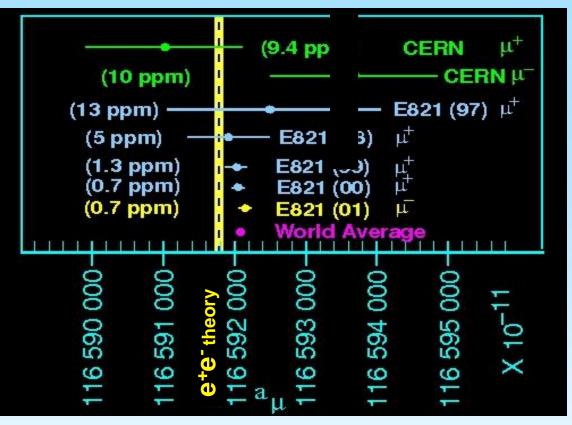
Calibration to a spherical water sample that ties the field to the Larmor frequency of the <u>free</u> proton  $\omega_p$ . We measure  $\omega_a$  and  $\omega_p$  independently Use  $\lambda = \mu_\mu / \mu_p$  as the "fundamental constant"

 $\mathcal{D}_{\mathbf{a}}$ 



E821 achieved 0.54 ppm;  $e^+e^-$  based theory 0.49 ppm Hint is 3.2 – 3.6  $\sigma$ 

Theory: Davier, et al., Eur. Phys. J. C (2011) 71: 1515

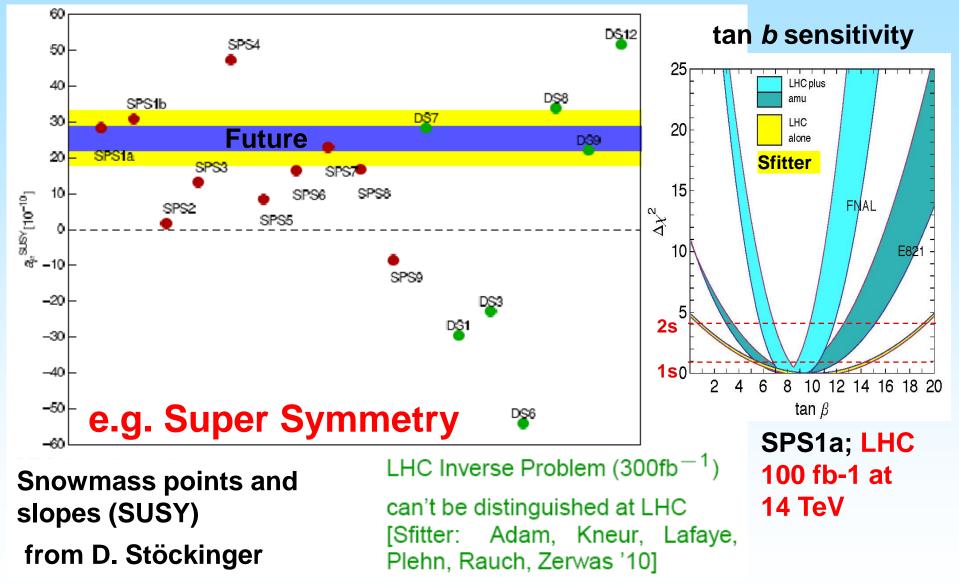


 $\begin{aligned} a_{\mu}^{SM} &= 116\,591\,802 \pm 49 \,\,(0.42\,\text{ppm}) \\ a_{\mu}^{E821} &= 116\,592\,089(54)_{stat}(33)_{sys}(63)_{tot} \times 10^{-11} \\ \Delta a_{\mu}^{(\text{today})} &= (287 \pm 80) \times 10^{-11} \\ a_{\mu}^{EW} &= 154(1)(2) \times 10^{-11} \end{aligned}$ 



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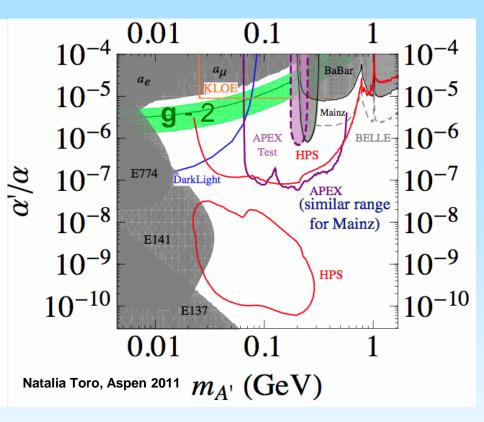
# Muon g-2 is a powerful discriminator between models; chiral-changing, flavor and CP conserving interaction.





# **Other Models**

- Technicolor
  - small  $\Delta a_{\mu}$
- Littlest Higgs with T-parity
  - small  $\Delta a_{\mu}$
- Universal Extra Dimensions
   small ∆a<sub>µ</sub>
- Randall Sundrum
  - could accommodate large  $\Delta a_{\mu}$
- Two Higgs doublets, shadow Higgs
  - small  $\Delta a_{\mu}$
- Additional light bosons that can affect EM interactions (difficult to study at LHC)
  - secluded U(1),etc., could have significant  $\Delta a_{\mu}$





# Fermilab $a_{\mu}$ Experiment:

- E821 at Brookhaven
  - superferric storage ring, magic  $\gamma$ , <B><sub> $\theta$ </sub> ± 1 ppm

 $\sigma_{stat} = \pm 0.46 \text{ ppm} \\ \sigma_{syst} = \pm 0.28 \text{ ppm}$   $\sigma = \pm 0.54 \text{ ppm}$ 

## • E989 at Fermilab

- move the storage ring to Fermilab, improved shimming, new detectors, electronics, DAQ,
- new beam structure that takes advantage of the multiple rings available at Fermilab, more muons per hour, less per fill of the ring

 $\sigma_{stat} = \pm 0.1 \text{ ppm}$  $\sigma_{syst} = \pm 0.1 \text{ ppm}$   $\sigma = \pm 0.14 \text{ ppm}$ 



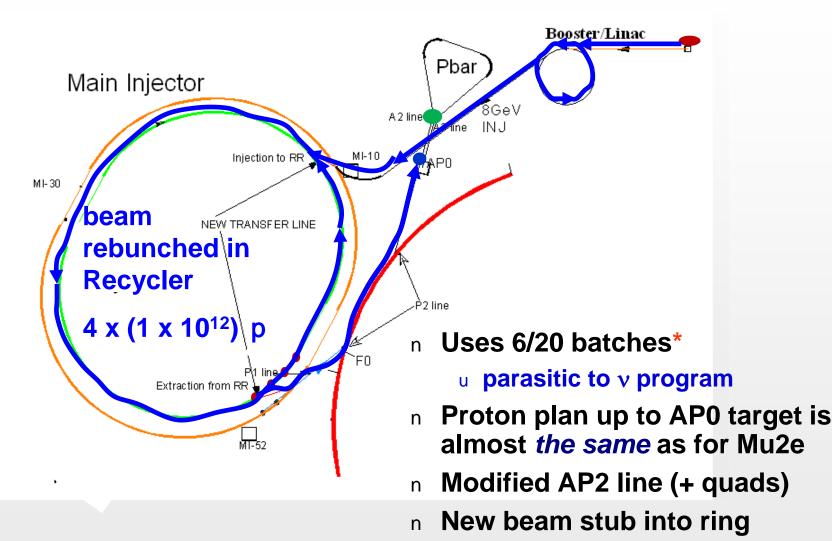
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# Why Fermilab?

- The existence of many storage rings that are interlinked permits us to make the "ideal" beam structure.
  - proton bunch structure:
    - BNL ~5 X 10<sup>12</sup> p/fill: effective rate 4.4 Hz
    - FNAL 10<sup>12</sup> p/fill: effective rate 18 Hz
  - using antiproton rings as an 900m pion decay line
    - 20 times less pion flash at injection than BNL
  - 0° muons
    - ~5-10x increase  $\mu/p$  over BNL
  - Can run parasitic to main injector experiments (e.g. to NOVA) or take all the booster cycles

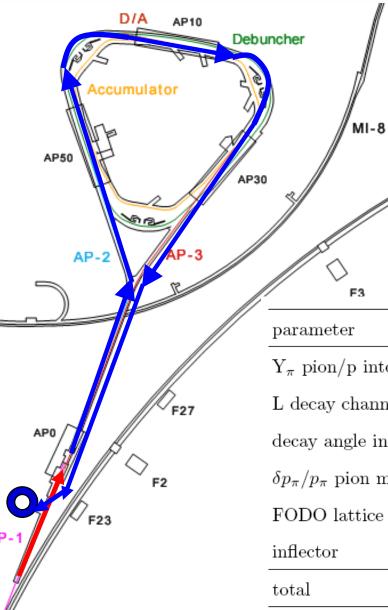


# Polarized muons delivered and stored in the ring at the magic momentum, 3.094 GeV/c



#### \*Can use all 20 if MI program is off

The 900-m long decay beam reduces the pion "flash" by x20 and leads to 6 – 12 times more stored muons per proton (compared to BNL)



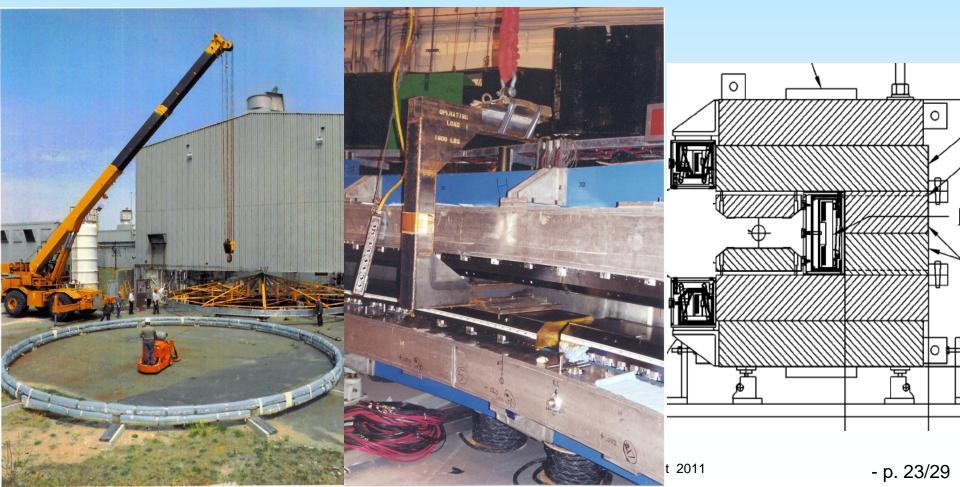
#### Flash compared to BNL

parameter	FNAL/BNL
p / fill	0.25
π/p	0.4
$\pi$ survive to ring	0.01
$\pi$ at magic P	50
Net	0.05

F3 Stored Muons / POT							
neter	BNL	FNAL	gain factor $\mathrm{FNAL}/\mathrm{BNL}$				
ion/p into channel acceptance	$\approx$ 2.7 E-5	$\approx 1.1\text{E-5}$	0.4				
cay channel length	88 m	$900 \mathrm{~m}$	2				
v angle in lab system	$3.8\pm0.5~\mathrm{mr}$	forward	3				
$p_{\pi}$ pion momentum band	$\pm 0.5\%$	$\pm 2\%$	1.33				
O lattice spacing	$6.2 \mathrm{m}$	$3.25~{ m m}$	1.8				
tor	closed end	open end	2				
			11.5				

# **Ring relocation to Fermilab**

- Heavy-lift helicopters bring coils to a barge
- Rest of magnet is a "kit" that can be trucked to and from the barge







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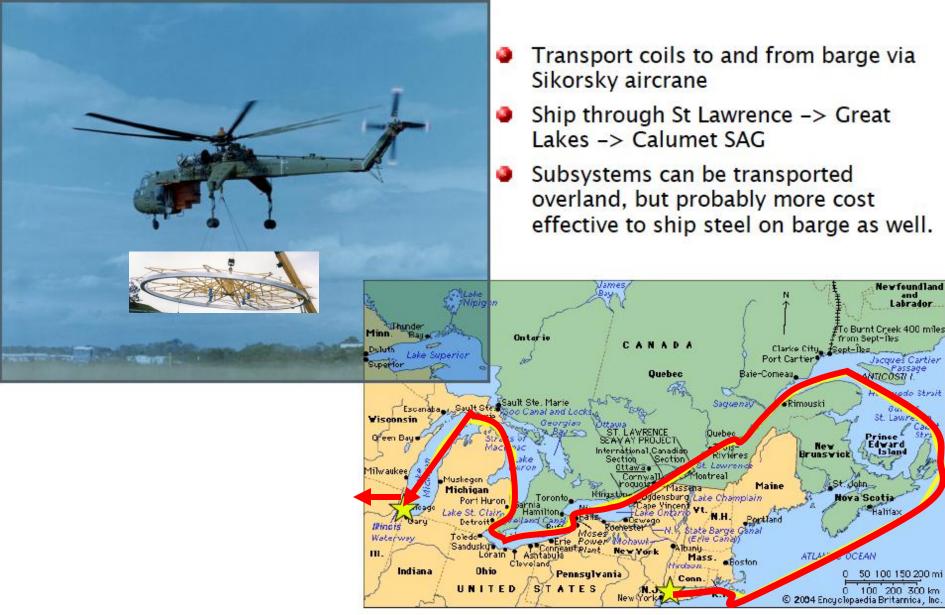
### Yoke fully assembled



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#### Sikorsky S64F 12.5 T hook weight (Outer coil 8T)



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# Goal is to be ready for data in 2015 - 2016 Subject to funding availability

- Total project cost ~\$4XM
  - CD0 expected this fall
  - Conceptual Design Report being prepared
- FY2011 Funding began this June
- FY12 and beyond is being discussed between DOE and Fermilab



# Summary:

- The measurements of e  $\pm$  and  $\mu^{\pm}$  magnetic dipole moments have been important benchmarks for the development of QED and the Standard Model.
- At present there appears to be a > 3  $\sigma$  difference between a<sub>u</sub> and the SM prediction.
  - if confirmed it would fit well with SUSY expectations, but LHC data will play a role in the interpretation.
- A worldwide effort continues to improve the SM value.
- The Fermilab experiment, E989, will improve the error on a<sub>µ</sub> by a factor of ≥4.
- The muon EDM limit could be improved by  $\approx 10^2$
- First results could be available around 2017



Thank you!

# THE END



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# The error budget for a new experiment represents a continuation of improvements already made during E821

Systematic uncertainty (ppm)	1998	1999	2000	2001	E821 final	P989 Goal
Magnetic field – w <sub>p</sub>	0.5	0.4	0.24	0.17		0.07
Anomalous precession – w <sub>a</sub>	0.8	0.3	0.31	0.21		0.07
Statistical uncertainty (ppm)	4.9	1.3	0.62	0.66	0.46	0.1
Systematic uncertainty (ppm)	0.9	0.5	0.39	0.28	0.28	0.1
Total Uncertainty (ppm)	5.0	1.3	0.73	0.72	0.54	0.14



# Systematic errors on $\omega_a$ (ppm)

σ <sub>systematic</sub>	1999	2000	2001	Future
Pile-up	0.13	0.13	0.08	0.04
AGS Background	0.10	0.10	0.015*	
Lost Muons	0.10	0.10	0.09	0.02
Timing Shifts	0.10	0.02	0.02	
E-Field, Pitch	0.08	0.03	0.06*	0.03
Fitting/Binning	0.07	0.06	0.06*	
СВО	0.05	0.21	0.07	0.04
Beam Debunching	0.04	0.04	0.04*	
Gain Change	0.02	0.13	0.13	0.02
total	0.3	0.31	0.21	~0.07



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# **The Precision Field: Systematic errors**

• Why is the error 0.11 ppm?

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- That's with existing knowledge and experience
  - with R&D defined in proposal, it will get better

Source of Uncertainty	1998	999	2000	2001	Next _ (g-2)	
Absolute Calibration	0.05	0.05	0.05	0.05	0.05	
Calibration of Trolley	0.3	0.20	0.15	0.09	0.06	
Trolley Measurements of B0	0.1	0.10	0.10	0.05	0.02	
Interpolation with the fixed probes	0.3	0.15	0.10	0.07	0.06	
Inflector fringe field	0.2	0.20	-	-		
uncertainty from muon distribution	0.1	0.12	0.03	0.03	0.02	
Other*		0.15	0.10	0.10	0.05	
Total	0.5	0.4	0.24	0.17	0.11	p. 34/29

# **Hadronic Light-by-Light Contribution**

#### see: http://www.int.washington.edu/PROGRAMS/11-47w/

#### Organizers:

Thomas Blum University of Connecticut tblum@phys.uconn.edu

Eduardo de Rafael Marseille EdeR@cpt.univ-mrs.fr

David Hertzog University of Washington hertzog@uw.edu

Fred Jegerlehner DESY Zeuten fjeger@physik.hu-berlin.de

Lee Roberts Boston University roberts@bu.edu

Arkady Vainshtein University of Minnesota vainshte@umn.edu

Program Coordinator: Inge Dolan inge@phys.washington.edu (206) 685-4286

Schedule

Talks online

Application form

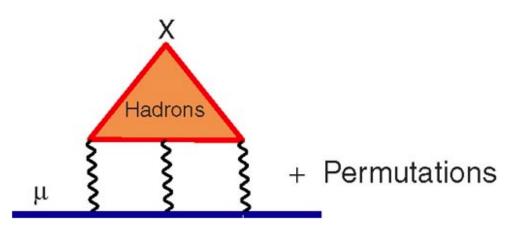
Friends of the INT

Obtain an INT preprint number

INT homepage

INT Workshop on The Hadronic Light-by-Light Contribution to the Muon Anomaly

February 28 - March 4, 2011



There is a registration fee of \$80 to attend this workshop to cover the expenses for catering and a workshop dinner.

#### The Workshop Plan:

The workshop will bring together both theorists and experimentalists to focus on one of the outstanding theoretical issues in interpreting the muon anomalous magnetic moment:

- Can agreement be reached on the individual and combined theoretical contributions to the hadronic light-by-light (HLbL) contribution to the muon anomalous magnetic moment, a<sub>µ</sub>, based on QCD-inspired models?
- 2. Can the lattice approach lead to a result having sufficient precision to check the models or to independently establish the HLbL value?
- 3. Which data that can be obtained at Frascati, and at other facilities, are essential to constrain the theoretical calculations and what theoretical developments are required to connect data to model predictions?

Hadronic Light–by–Light Scattering Contribution to the Muon Anomalous Magnetic Moment arXiv:0901.0306v1

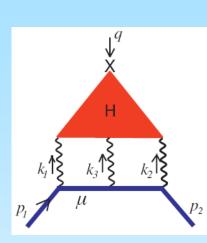
Joaquim Prades<sup>*a*</sup>, Eduardo de Rafael<sup>*b*</sup> and Arkady Vainshtein<sup>*c*</sup>

 $a^{\mathrm{HLbL}}(\pi,\eta,\eta') = (11.4 \pm 1.3) \times 10^{-10}$ 

 $a^{\text{HLbL}}(\text{scalars}) = -(0.7 \pm 0.7) \times 10^{-10}$ 

$$a^{\mathrm{HLbL}}(\pi - \mathrm{dressed\ loop}) = -(1.9 \pm 1.9) \times 10^{-10}$$

$$a^{\text{HLbL}}(\text{pseudovectors}) = (1.5 \pm 1) \times 10^{-10}$$



# Dynamical models with QCD behavior

$$a_{\mu}^{\mathsf{HLBL}} = 105 \ (26) \times 10^{-11}$$

Note, with  $\Delta a_{\mu} = 295 \times 10^{-11} \dots$  If HLBL is the source of the difference with SM, it would need to increase by 11  $\sigma$  ....



# The $\pi^0$ (Goldstone) contribution fixes sign of the contribution From $\chi pt$ and large N<sub>c</sub> QCD

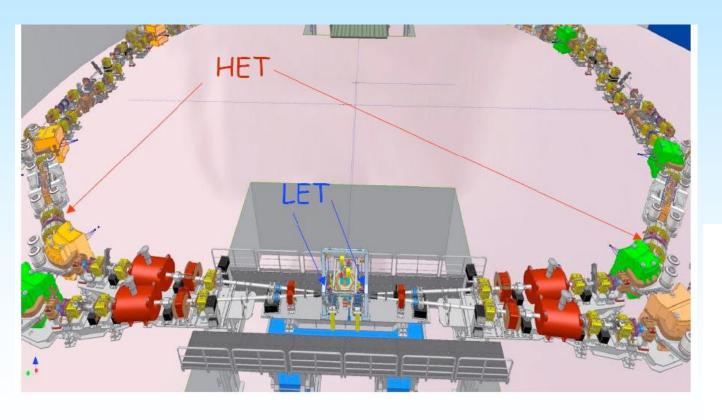
$$a_{\mu}^{[\chi pt]} \underbrace{\left(\frac{\alpha}{\pi}\right)^{3}}_{e} \underbrace{\left(\frac{N_{c}^{2}}{48\pi^{2}} \frac{m_{\mu}^{2}}{F_{\pi}^{2}} \ln^{2}\left(\frac{\mu}{m}\right) + \mathcal{O}\left[\ln\left(\frac{\mu}{m}\right) + \kappa(\mu)\right]}_{e} \right\}_{i=1}^{i=1} \underbrace{\left(\frac{\alpha}{m}\right)^{3}}_{i=1} \underbrace{\left(\frac{\alpha}{m}\right)^{3}}_{i=1} \underbrace{\left(\frac{\mu}{m}\right)^{2}}_{i=1} + \mathcal{O}\left[\ln\left(\frac{\mu}{m}\right) + \kappa(\mu)\right]}_{i=1} \right]_{i=1}^{i=1} \underbrace{\left(\frac{\mu}{m}\right)^{2}}_{i=1} + \frac{\mu}{\mu} \underbrace{\left(\frac{\mu}{m}\right$$

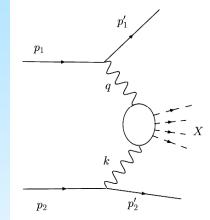
- The magnitude of the HLBL is about the same as the magnitude of the 3-loop HVP which can be calculated from the dispersion relation.
- It's hard to believe that the HLBL would be huge compared to the other 3-loop contributions. B. Lee Roberts for the New Muon (g-2) Collaboration – DPF 10 August 2011

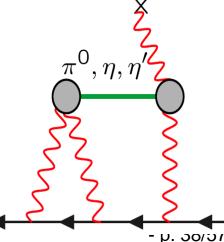
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#### **KLOE** to measure $\gamma * \gamma * \rightarrow hadrons$ to constrain HLBL

Constrain the off-shell amplitudes and remove a significant portion of the theoretical uncertainty on the HLBL









## EDMs in Storage Rings: E821@ BNL

$$\vec{\omega} = -\frac{e}{m} \left[ a_{\mu}\vec{B} - \left(a_{\mu} - \frac{1}{\gamma^{2} - 1}\right) \frac{\vec{\beta} \times \vec{E}}{c} \right] + \frac{e}{2m} \left[ \eta \left(\frac{\vec{E}}{c} + \vec{\beta} \times \vec{B}\right) \right]$$

$$= \frac{e}{2m} \left\{ a\vec{B} + \frac{\eta}{2} (\vec{\beta} \times \vec{B}) \right\}$$

$$\vec{d} = \eta \left(\frac{Qe}{2mc}\right) \vec{s}$$

$$\vec{d} = \eta \left(\frac{Qe}{2mc}\right) \vec{s}$$

$$\tan \theta = \frac{\omega_{edm}}{\omega_{a}}$$

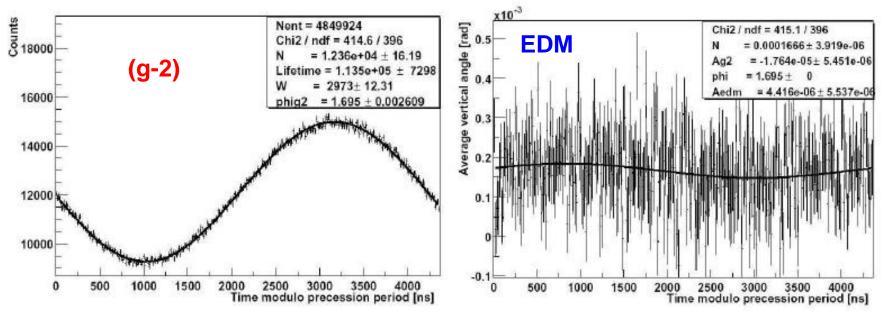
$$\Theta_{edm} < < < < \infty_{a}$$



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# Muon EDM in the BNL E821 Storage Ring

E821 Data



Vertical Oscillation out of phase with  $\omega_a$ 

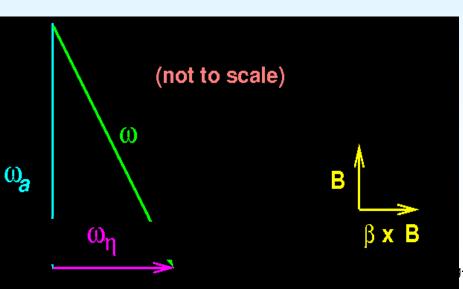
$$N^{\pm}(t) \propto 1 + A_{\mu} \cos(\omega t + \phi) \mp A_{EDM} \sin(\omega t + \phi)$$
  
 $d_{\mu} < 1.8 \times 10^{-19}$  (95% CL)



## How do we get rid of the (g - 2) signal?

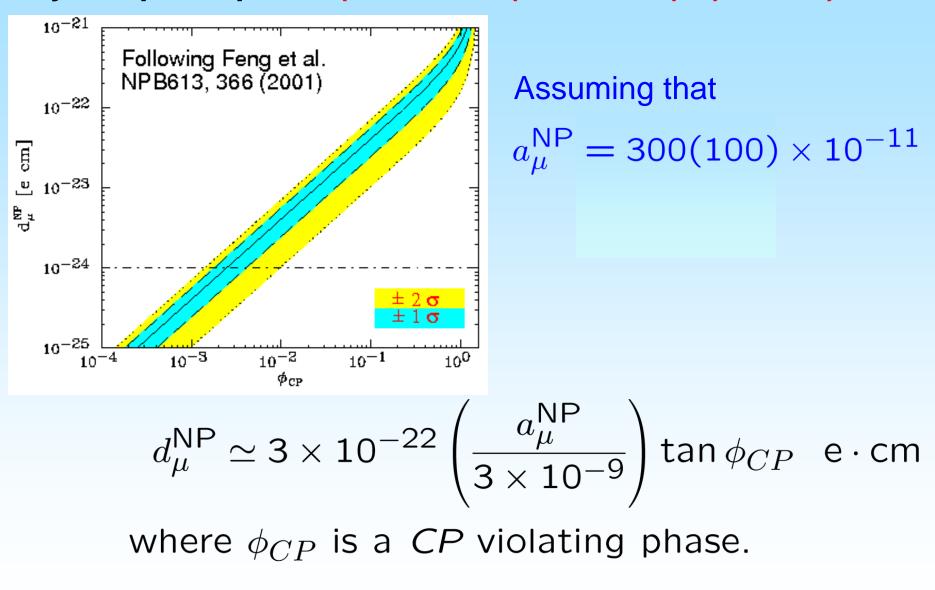
Y. Semertzidis idea of the "frozen spin"
 Use a radial E field to turn off the *w*<sub>a</sub> precession

$$\vec{\omega} = -\frac{e}{m} \left[ a_{\mu} \vec{B} - \left( a_{\mu} - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]^{0}$$



$$+ \frac{e}{m} \left[ \frac{\eta}{2} \left( \frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} \right) \right]$$

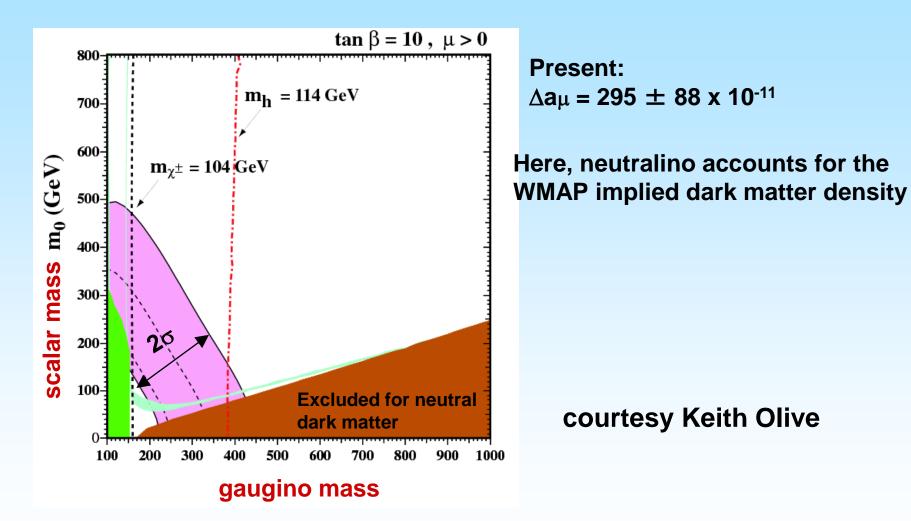
 $a_{\mu}$  implications for the muon EDM assuming same New Physics participates (recall that (∆today=255(80) X10<sup>-11</sup>)



Either  $d_{\mu}$  is of order 10<sup>-22</sup> e cm, or the CP phase is strongly suppressed! - μ. <del>4</del>2/57 UNIVERSIT

BO

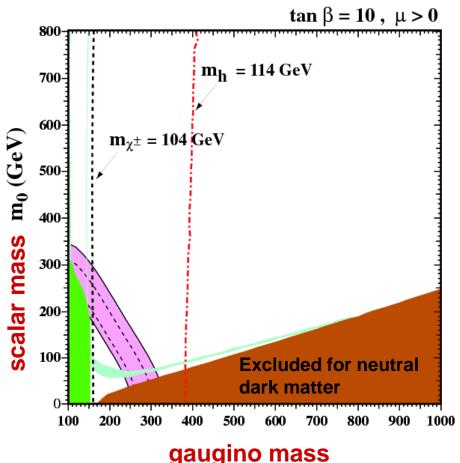
#### Typical CMSSM 2D space showing g-2 effect (note: NOT an exclusion plot)



This CMSSM calculation: Ellis, Olive, Santoso, Spanos. Plot update: K. Olive



# Typical CMSSM 2D space showing g-2 effect (note: NOT an exclusion plot)



Future  $\Delta a_{\mu} = 295 \pm 34 \times 10^{-11}$ 

Here, neutralino accounts for the WMAP implied dark matter density

Historically muon (g-2) has played an important role in restricting models of new physics.

It provides constraints that are independent and complementary to high-energy experiments.

This CMSSM calculation: Ellis, Olive, Santoso, Spanos. Plot update: K. Olive

#### With new experimental and theoretical precision and same $\Delta a_{\mu}$

#### **courtesy Keith Olive**



B. Lee Roberts for the New Muon (g-2) Collaboration – DPF 10 August 2011

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