

Quantum Computing

Lecture 2



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“The history of the universe is, in effect, a huge and ongoing quantum computation. The universe is a quantum computer.”

-Seth Lloyd



Mathematical aside 2 – Matrix Operations

- Quantum theory is **unitary**, a unitary matrix U is such that $U^\dagger U = I_n$, where I_n is the identity matrix and n represents the dimension of the square matrix U \dagger = Hermitian conjugate

$$e.g. I_2 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

- U^\dagger (U -dagger) is the transposed, complex-conjugated version of the matrix U

- Let $U = \begin{pmatrix} U_{00} & U_{01} \\ U_{10} & U_{11} \end{pmatrix}$, $U^\dagger = \begin{pmatrix} U_{00}^* & U_{10}^* \\ U_{01}^* & U_{11}^* \end{pmatrix}$ ($a = 2 - 3i \rightarrow a^* = 2 + 3i$)

- Can express U in Dirac notation as follows:

$$U = \begin{pmatrix} U_{00} & U_{01} \\ U_{10} & U_{11} \end{pmatrix} = U_{00}|0\rangle\langle 0| + U_{01}|0\rangle\langle 1| + U_{10}|1\rangle\langle 0| + U_{11}|1\rangle\langle 1|$$

$$e.g. U = \begin{pmatrix} 5 & 6 \\ 7 & 8 \end{pmatrix} = 5|0\rangle\langle 0| + 6|0\rangle\langle 1| + 7|1\rangle\langle 0| + 8|1\rangle\langle 1|$$

Matrix Operations - continued

- Recap on how to multiply two 2x2 matrix with a 2x1 matrix (2D-vector):

- $A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$ $B = \begin{pmatrix} 5 \\ 6 \end{pmatrix}$

- $AB = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} \begin{pmatrix} 5 \\ 6 \end{pmatrix}$

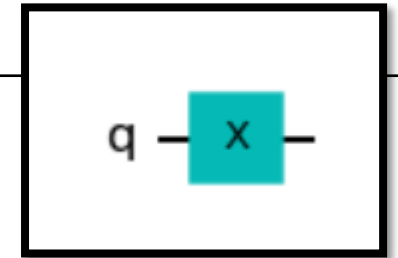
$$= \begin{pmatrix} 1.5 + 2.6 \\ 3.5 + 4.6 \end{pmatrix}$$

$$= \begin{pmatrix} 17 \\ 39 \end{pmatrix}$$



Gates

Quantum Logic Gates (qubit gates)



- Quantum computing relies on **quantum circuits**
- A quantum circuit is a sequence of blocks or gates that carry out computations (input-output)
- A quantum gate is represented by unitary matrices ($U^\dagger U = I_n$)

• **Pauli (spin) matrices (gates):** $\sigma_x, \sigma_y, \sigma_z$

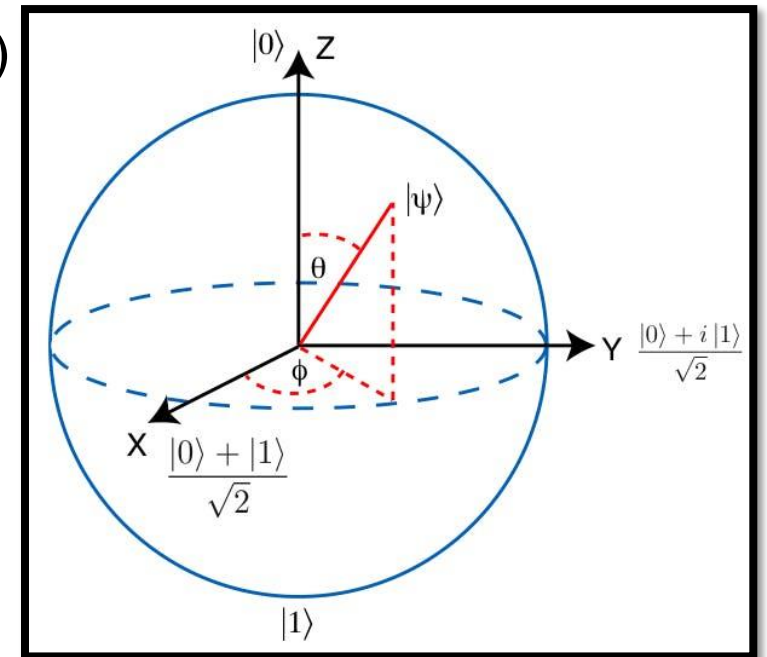
$$\sigma_x = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} = |0\rangle\langle 1| + |1\rangle\langle 0|$$

$$\sigma_x |0\rangle = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \end{pmatrix} = |1\rangle$$

$$\sigma_x |1\rangle = (|0\rangle\langle 1| + |1\rangle\langle 0|) \cdot |1\rangle = |0\rangle\langle 1|1\rangle + |1\rangle\langle 0|1\rangle = |0\rangle$$



Bit flip (rotation about x-axis by π) (analogous to classic NOT gate)



Quantum Logic Gates (qubit gates) - continued

- $\sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} = |0\rangle\langle 0| - |1\rangle\langle 1|$

- $\sigma_z |+\rangle = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -1 \end{pmatrix} = |-\rangle$ ($|+\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$)

- $\sigma_z |-\rangle = (|0\rangle\langle 0| - |1\rangle\langle 1|) \cdot \left(\frac{1}{\sqrt{2}}|0\rangle - |1\rangle\right) = \frac{1}{\sqrt{2}}|0\rangle + |1\rangle = |+\rangle$



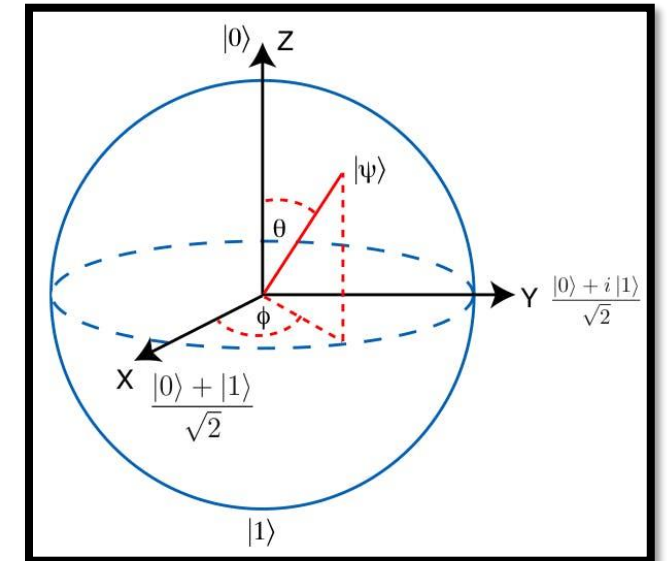
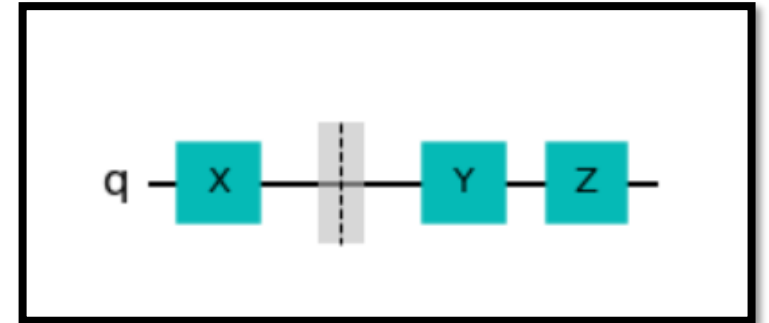
Phase flip (rotation about z-axis by π)

- $\sigma_y = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} = -i|0\rangle\langle 1| + i|1\rangle\langle 0| = i\sigma_x \cdot \sigma_z$



Bit and phase flip (rotation about y-axis by π)

- $\sigma_i^2 = I_2 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$, i.e. applying the same Pauli gate twice does nothing to a state



Quantum Logic Gates (qubit gates) - continued

Hadamard gate:

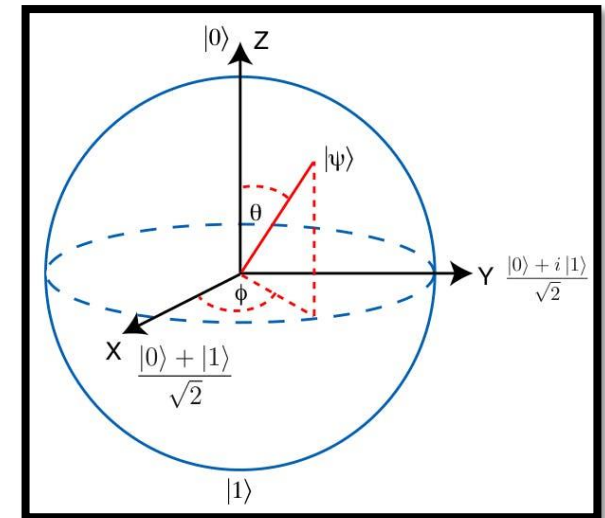
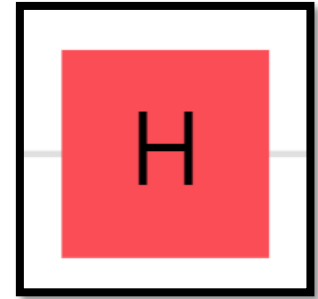
- Can be found in (almost) every quantum circuit

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{\sqrt{2}} (|0\rangle\langle 0| + |0\rangle\langle 1| + |1\rangle\langle 0| - |1\rangle\langle 1|)$$

$$\text{➤ } H|0\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix} = |+\rangle$$

$$\text{➤ } H|1\rangle = \frac{1}{\sqrt{2}} (|0\rangle\langle 0| + |0\rangle\langle 1| + |1\rangle\langle 0| - |1\rangle\langle 1|) \cdot |1\rangle = \frac{1}{\sqrt{2}} (|0\rangle - |1\rangle) = |-\rangle$$

$$\text{➤ } H|+\rangle = |0\rangle \qquad H|-\rangle = |1\rangle$$



Creates and destroys superposition (switch between z and x bases)

Quantum Logic Gates (qubit gates) - continued

S gate:

- $S = \begin{pmatrix} 1 & 0 \\ 0 & i \end{pmatrix} = |0\rangle\langle 0| + i|1\rangle\langle 1|$

➤ $S|+\rangle = |i\rangle$

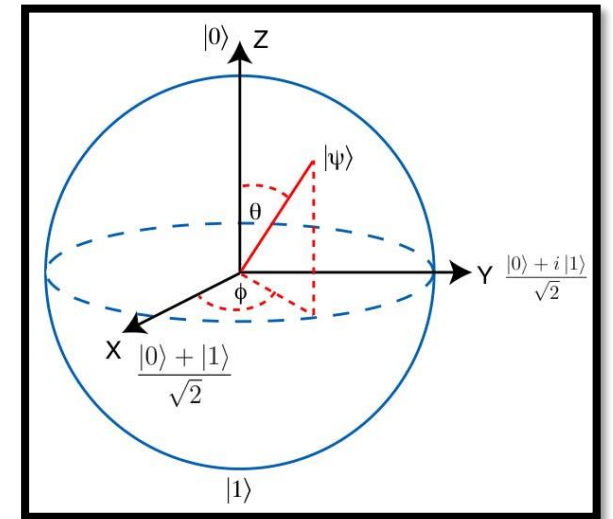
$S|-\rangle = |-i\rangle$



➡ Adds $\frac{\pi}{2}$ (90°) to the phase φ (switch between x and y bases)

- **S.H** allows us to **switch between z and y bases**

<https://javafxpert.github.io/grok-bloch/>



Two qubits and tensor products

$$|00\rangle = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$$|01\rangle = \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix}$$

$$|10\rangle = \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix}$$

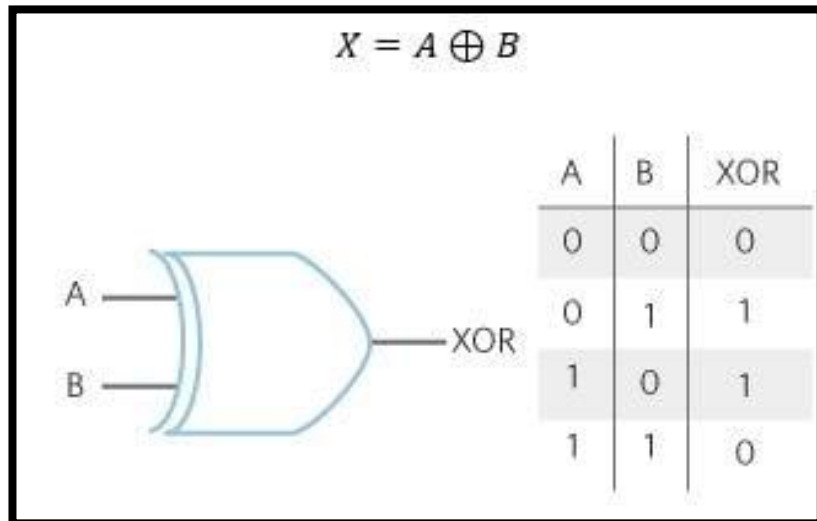
$$|11\rangle = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}$$

- $\langle e|d\rangle = \langle ed\rangle$ – inner product
- $|d\rangle\langle e| = |de\rangle$ – outer product
- $|d\rangle|e\rangle = |d\rangle\otimes|e\rangle = |de\rangle$ – tensor product

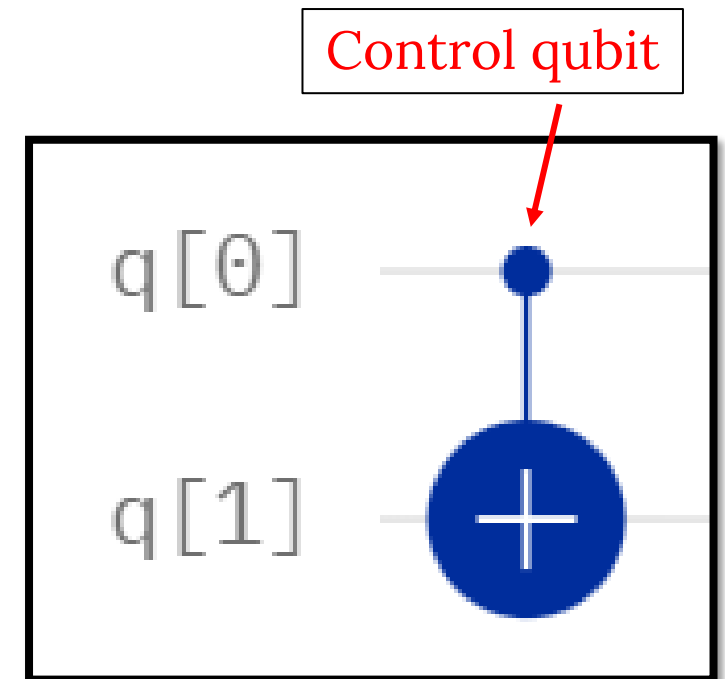
e.g. $|0\rangle_1|0\rangle_2 = |0\rangle_1\otimes|0\rangle_2 = |0_10_2\rangle$

Two qubit gates

CNOT gate (CX):



Input		Output	
x	y	x	$x \oplus y$
0	0	0	0
0	1	0	1
1	0	1	1
1	1	1	0



- Note that a classical XOR gate is non-reversible
- However, since all quantum gates are unitary, they are, in fact, **reversible**
- CNOT stands for Controlled-NOT. The qubit in control does not change by the gate

Two qubit gates - continued

CNOT gate:

$$\bullet \text{CNOT} = \begin{matrix} & 00 & 01 & 10 & 11 \\ \begin{matrix} 00 \\ 01 \\ 10 \\ 11 \end{matrix} & \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} & = & |00\rangle\langle 00| + |01\rangle\langle 01| + |10\rangle\langle 11| + |11\rangle\langle 10| \end{matrix}$$

$$\text{➤ } \text{CNOT}|00\rangle = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} = |00\rangle$$

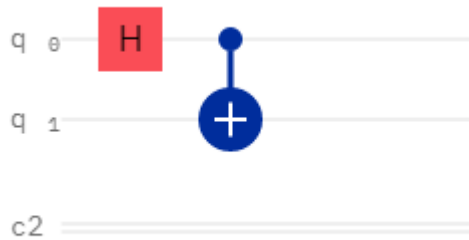
$$\text{➤ } \text{CNOT}|10\rangle = (|00\rangle\langle 00| + |01\rangle\langle 01| + |10\rangle\langle 11| + |11\rangle\langle 10|) \cdot |10\rangle$$

$$\begin{matrix} \nearrow & & \nearrow & & \nearrow \\ |00\rangle\langle 00|10\rangle + |01\rangle\langle 01|10\rangle + |10\rangle\langle 11|10\rangle + |11\rangle\langle 10|10\rangle \\ & & & & \\ & & & & = |11\rangle \end{matrix}$$

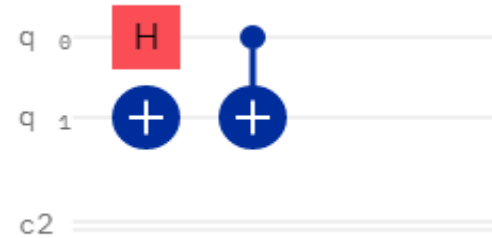
Bell states

- 4 states (2 qubits) that are **maximally-entangled** and build an **orthonormal basis**

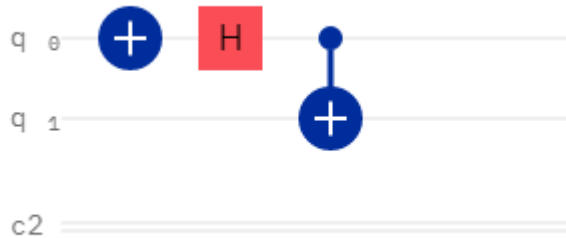
$$|\psi^{00}\rangle = \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle)$$



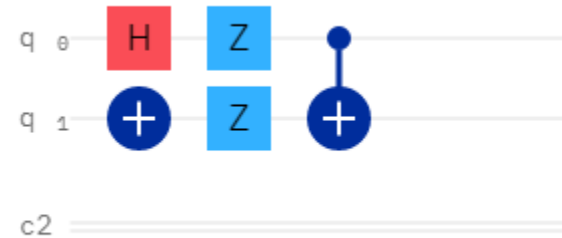
$$|\psi^{01}\rangle = \frac{1}{\sqrt{2}} (|01\rangle + |10\rangle)$$



$$|\psi^{10}\rangle = \frac{1}{\sqrt{2}} (|00\rangle - |11\rangle)$$



$$|\psi^{11}\rangle = \frac{1}{\sqrt{2}} (|01\rangle - |10\rangle)$$



More entanglement

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|00\rangle + |11\rangle)$$

Global state

$$|\psi_1\rangle = \alpha_1|0\rangle + \beta_1|1\rangle \quad \text{local state} \quad |\psi_2\rangle = \alpha_2|0\rangle + \beta_2|1\rangle$$

Given the global state, what are the local states?

$$|\psi_1\rangle \otimes |\psi_2\rangle = |\psi_1\psi_2\rangle = \alpha_1\alpha_2|00\rangle + \alpha_1\beta_2|01\rangle + \beta_1\alpha_2|10\rangle + \beta_1\beta_2|11\rangle$$

Therefore, require:

\otimes – tensor product

- $\alpha_1\beta_2 = \beta_1\alpha_2 = 0$
- $\alpha_1\alpha_2 = \beta_1\beta_2 = \frac{1}{\sqrt{2}}$



$$\alpha_1 = 0 \text{ or } \beta_2 = 0$$

Contradiction!

More entanglement - continued

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|00\rangle + |10\rangle) = \frac{1}{\sqrt{2}}(|0\rangle \otimes |0\rangle + |1\rangle \otimes |0\rangle) = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \otimes |0\rangle$$

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|10\rangle + |01\rangle) = \frac{1}{\sqrt{2}}(|1\rangle \otimes |0\rangle + |0\rangle \otimes |1\rangle) = ?$$

We have full knowledge of the global state,
but no knowledge of the local states.







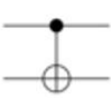


Entanglement!



Gates summary

- Pauli (spin) matrices (gates) cause spins around x,y, or z axes of a Bloch sphere (bit or phase flip)
- Hadamard gates create and destroy superposition
- S gate(also in combination with H gate) switches between bases
- CNOT gates (2 qubit gate) help us achieve entanglement
- Bell states (4 of them – 2 qubits) are maximally-entangled and build an orthonormal bases
→ help you get a Nobel prize

Operator	Gate(s)	Matrix
Pauli-X (X)	 \oplus	$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$
Pauli-Y (Y)		$\begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$
Pauli-Z (Z)		$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$
Hadamard (H)		$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$
Phase (S, P)		$\begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$
$\pi/8$ (T)		$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix}$
Controlled Not (CNOT, CX)		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$

Algorithms

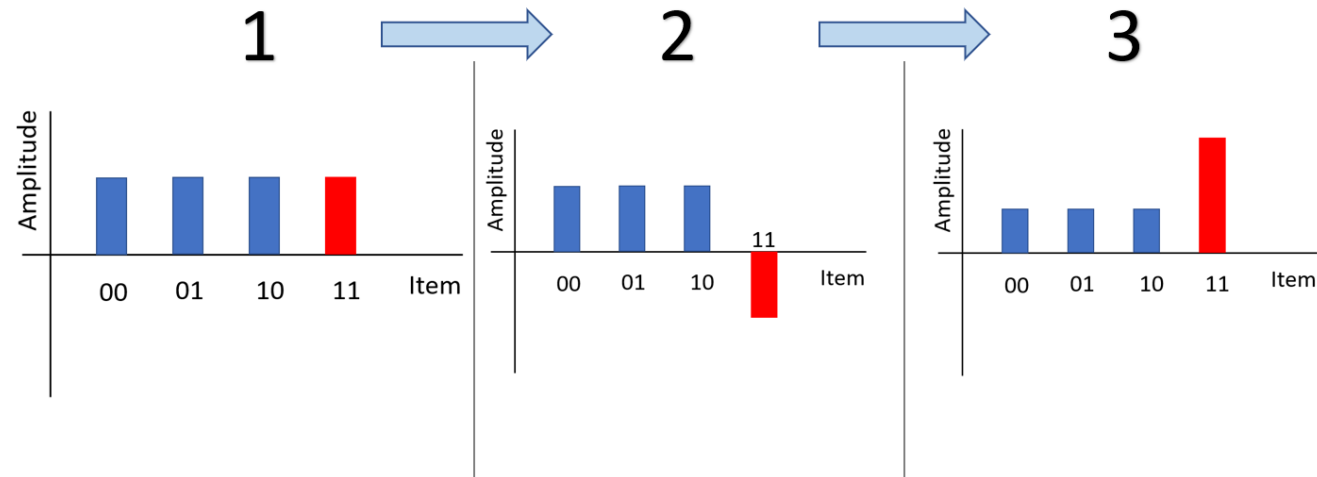
Grover's Algorithm

- An (quantum) algorithm used to search and locate a specific element in an unordered list/unordered database
- Imagine you have a list of 2 columns: **name** and **phone number**
- You have a **phone number**, and you want to find the corresponding **name** using this list
- Using a classical computer, you would need to use brute-forcing or some other method (not highly efficient)
- With Grover's algorithm and the superposition principle, one can exponentially decrease the time needed to find the phone number
- This process happens with the help of two sub-functions called the **oracle function** and the **amplification function**
- Other fun examples is solving a **sudoku puzzle** or **polynomial root** finding problems

Grover's Algorithm - continued

- Suppose you have 2 qubits, corresponding to 4 possibilities: 00, 01, 10, and 11
- All possible states can be described using this equation:
$$a|00\rangle + b|01\rangle + c|10\rangle + d|11\rangle,$$
where a , b , c , and d correspond to the amplitudes of the states (remember, probability of the state is the amplitude-squared)
- Assume for example that our phone number is associated with the state $|11\rangle$
- This means the associated amplitude of interest is " d "

Grover's Algorithm - continued



- The oracle function **flips** the corresponding amplitude " d " so that it becomes " $-d$ "; a **unique amplitude**
- The amplification function **amplifies** the difference between the amplitude corresponding to the number we're looking and the other amplitudes
- This makes the probability of locating the number much higher
- **Repeat** as many times as one pleases to further increase the probability

Grover's Algorithm - demo

More details/explanations can be found [here](#) (Qiskit Textbook)

Cryptography

- Protecting information and communications using codes
- RSA cryptography utilizes **prime numbers** to securely encrypt data. It is fundamental for the operation of internet protocols
- Need to have the factors of a number to be able to decrypt data
- E.g. given the number a number $n = pq = 226,579$, try to find p, q , given that they are prime numbers (answer: $p = 419, q = 541$)
- Nowadays, we use **RSA-2048** which utilized a 2048 bit key (an integer on the order of 2^{2048})
- Estimated it would take a classical computer around **300 trillion years** to break an RSA-2048-bit encryption key

Example of an RSA-2048 integer

2519590847565789349402718324004839857142928212620403202777713783604366202070
7595556264018525880784406918290641249515082189298559149176184502808489120072
8449926873928072877767359714183472702618963750149718246911650776133798590957
0009733045974880842840179742910064245869181719511874612151517265463228221686
9987549182422433637259085141865462043576798423387184774447920739934236584823
8242811981638150106748104516603773060562016196762561338441436038339044149526
3443219011465754445417842402092461651572335077870774981712577246796292638635
6373289912154831438167899885040445364023527381951378636564391212010397122822
120720357

RSA Cryptosystem: *exists*

Quantum Computers:



(very basic) introduction to Shor's Algorithm

- By no means a proper explanation to how Shor's Algorithm works – actual explanation could take more than one lecture
- Using a perfect quantum computer, finding the factors of an RSA-2048-bit integer could take mere **seconds**
- The basic premise is that you setup a **special periodic function** (modulo function), with a period “ r ”, which you try to obtain. This then leads you to obtaining the factors of the big number
- With **superposition**, you can test many values for the period simultaneously
- You use **interference** to zero-in on the correct value of the period (constructive interference) and reduce the probability of landing on the incorrect value (destructive interference)
- To find the period of this modulo function, you use “**Quantum Fourier Transform**” – a very useful tool in quantum computing

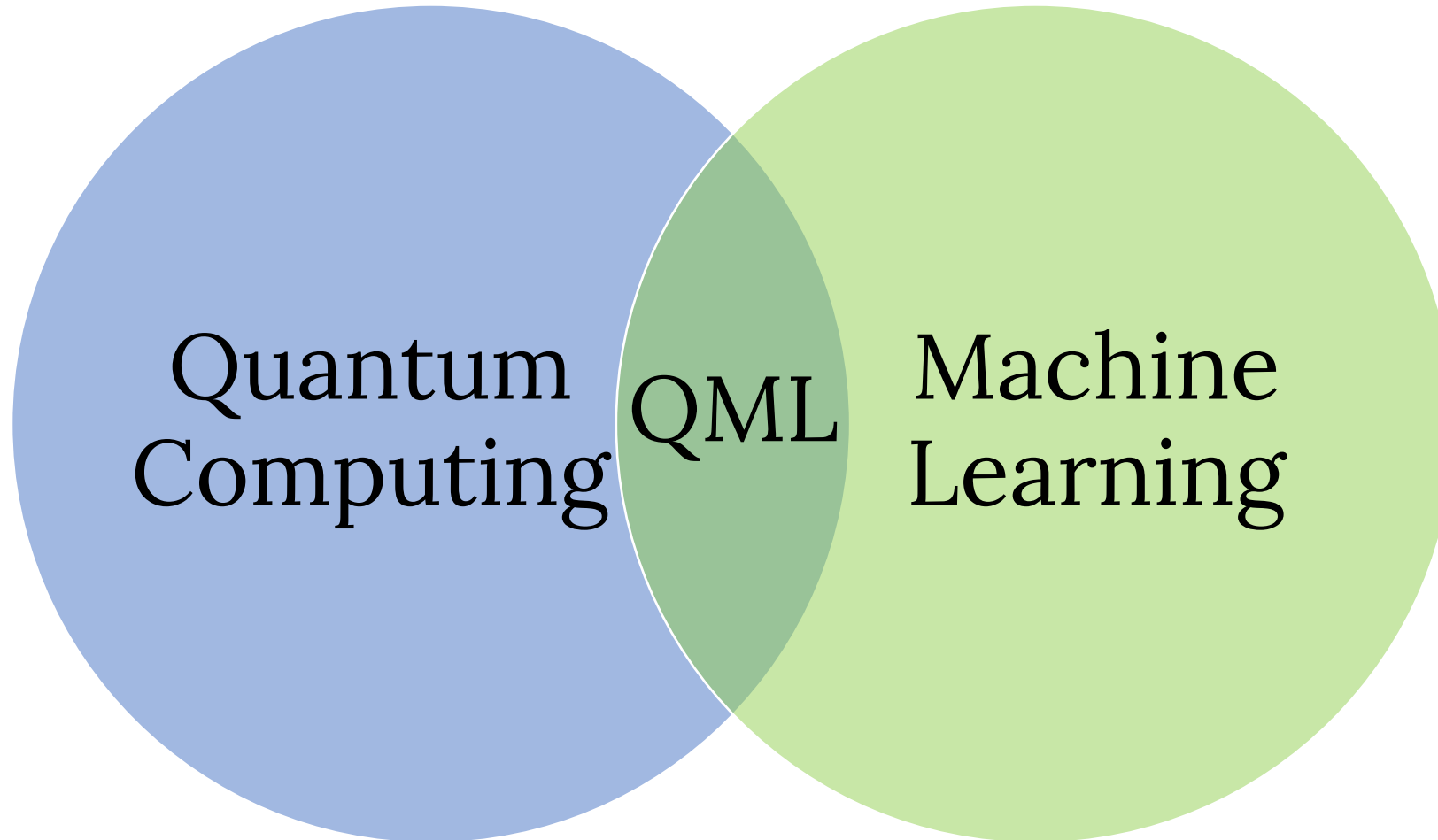
Quantum-safe cryptography

- RSA encryption is the basis of a lot of encryption schemes used to protect many assets
- Shor's algorithm poses a threat to these kind of commonly used encryption methods
- Need to have a quantum computer with **millions** of physical qubits to be able to do that (due to decoherence and noise)
- Quantum-safe algorithms which typically rely on mathematical problems that can't be solved easily by both classical and quantum computers already available
- Algorithms that rely on geometric problems based on lattices such as [CRYSTALS-Kyber](#) and [CRYSTALS-Dilithium](#) are now recommended by [NIST](#)
- Expected that industries will transition over to quantum-safe cryptographic algorithms as soon as **2024**. Therefore, there is (almost) no reason to worry about quantum computers destroying the world



Current applications of quantum computing

Quantum Machine Learning (QML)



Quantum Machine Learning (QML) - continued

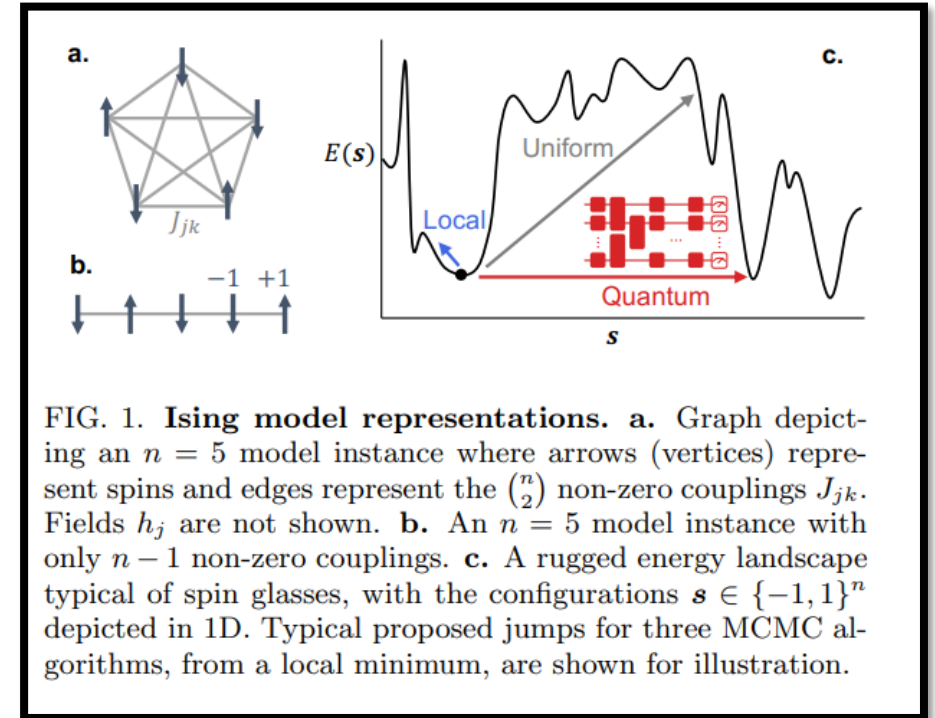
- Machine Learning is linear algebra, and quantum computing heavily relies on linear algebra → excellent match up
- QML can be used to solve Fourier Transformation, finding eigenvectors and eigenvalues, and solving linear sets of equations with an **exponential speedup**
- **Quantum Support Vector Machines (QSVM)** are also one of the more popular QML techniques.
 - Classical SVMs can be performed only up to a certain number of dimensions while QSVMs do not suffer from these restrictions
- **Quantum Optimization:** try to produce best possible output by using the least possible resources.
 - Superposition, entanglement and interference

Current applications of quantum computing

- **Condensed matter physics** has important implications for our understanding of nature and the development of new technologies
- It is also one of the main building blocks behind building computers, both classical and quantum
- One of the most popular models of ferromagnetism in statistical mechanics is called the “**Ising model**”
- Utilizes spins as its variables, and its coefficients comprise couplings and fields
- Each spin configuration is assigned an energy and a corresponding Boltzmann probability
- The connectivity of qubits allows researchers to simulate the dynamics of spin lattices

Current applications of quantum computing - continued

- One of many research papers on this subject include this one from [IBM Quantum](#)
- They perform Markov chain Monte Carlo (MCMC), a popular iterative sampling technique, to sample from the Boltzmann distribution of classical Ising models
- A new quantum algorithm that with many current applications including ones in machine learning (Boltzmann Machines) and statistical physics (thermal averages)
- Uses relatively simple quantum circuits using current hardware
- Many similar efforts trying to create solutions for optimization, statistical, and machine learning problems



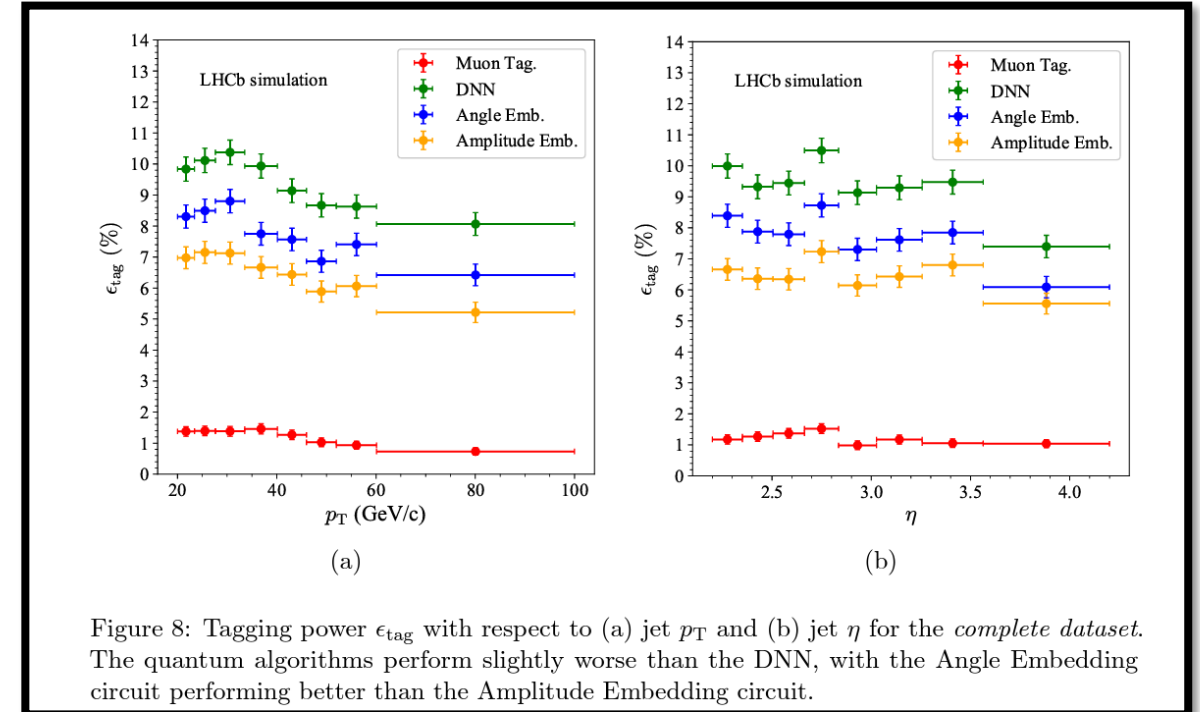
[arXiv:2203.12497]

Current applications of quantum computing - HEP

- Many applications in HEP, focusing on things like track reconstruction, Lattice Electrodynamics, signal versus background separation, and finding rare processes with QML
- The field of quantum computing in HEP is super recent → lots of opportunities to explore!
- I am going to be biased and focus on one [recent paper](#) published by my current experiment, LHCb
- Main premise is utilizing QML to identify the **charge of the b hadron-jets**
- Proponents utilize a Variational Quantum Classifier (VQC) on LHCb data and compare it against a Deep Neural Network (DNN) model

Current applications of quantum computing – HEP – continued

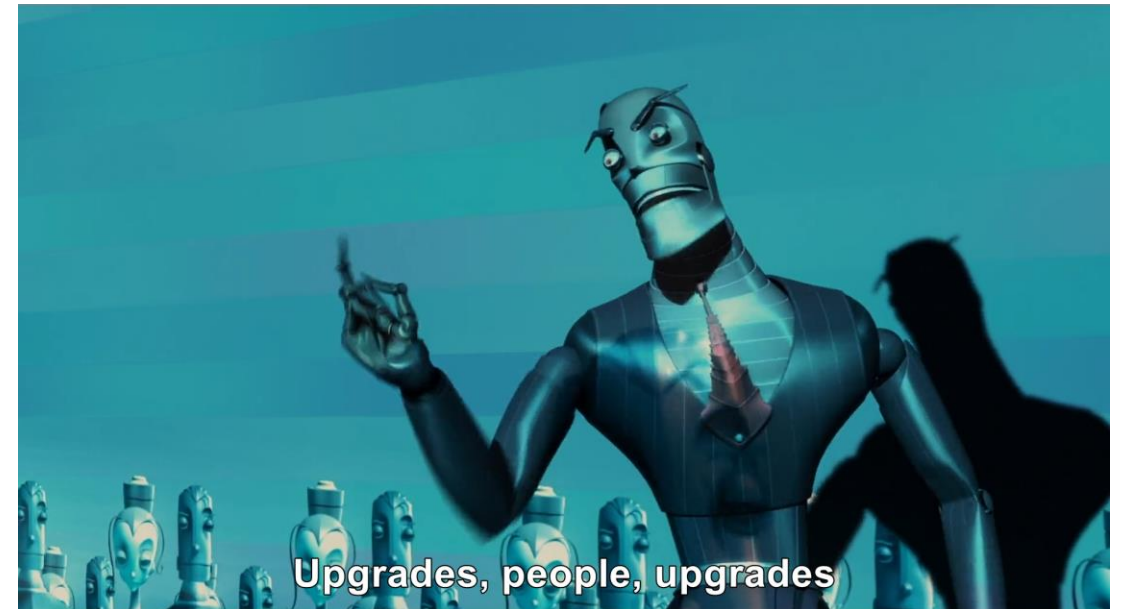
- Measurements mapped to probabilities for different labels
- Probabilities used to estimate a cost function
- Cost function optimized using a classical optimizer
- QML algorithms achieve performance consistent with classical methods like the DNN with low-complexity circuits and a smaller number of training events
- Room for improvement, especially when using a larger number of features and utilizing better hardware



[arXiv:2202.13943]

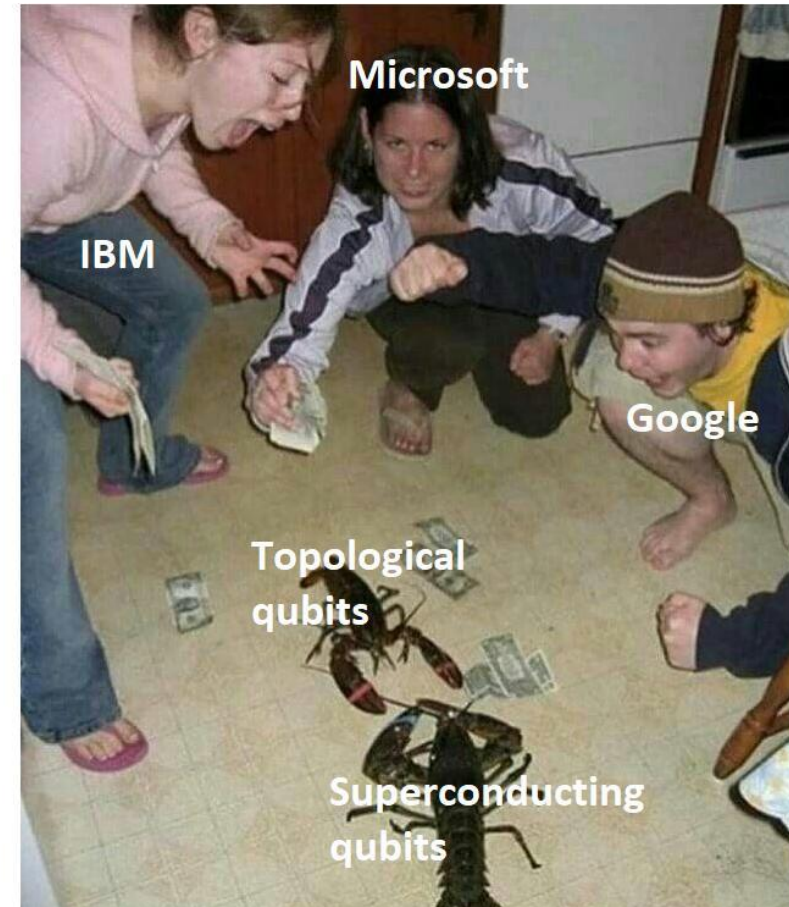
Prospects and future applications

- High Energy Physics
- Complex Manufacturing and Industrial Design
- Logistics
- Finance and financial modelling
- Chemical and biological Engineering
- Pharmacy and drug development
- Artificial Intelligence
- Cybersecurity
- Material Science
- ... and many more!



Future Predictions

- IBM currently have 433 qubits – expect to reach 1,000,000 qubits in **2027**
- Google has 53 qubits – expect to reach 1,000,000 qubits in **2029**
- Google announced their first error correcting, logical qubit in February 2023
- Many others are joining “the race”
- When do you think quantum computers will become “useful”?
- **Do you think it would happen at all?**





How can I participate?

CERN Quantum Technology Initiative

- First [workshop](#) on Quantum Computing in HEP at CERN in 2018
- [Conference](#) on Quantum Technologies in HEP last November
- Established a comprehensive R&D, academic and knowledge-sharing initiative for quantum technologies
- Currently focusing on:
 - Quantum computing and algorithms
 - Quantum theory and simulation
 - Quantum sensing, metrology and materials
 - Quantum communications and networks
- Collaborating with universities and institutions all over the world with a lot of them being in Europe
- In 2021, CERN became a quantum hub in partnership with the [IBM Q-Network](#)
- Quantum Technology Initiative Journal Club – [meeting](#) on Thursdays
- <https://quantum.cern/>



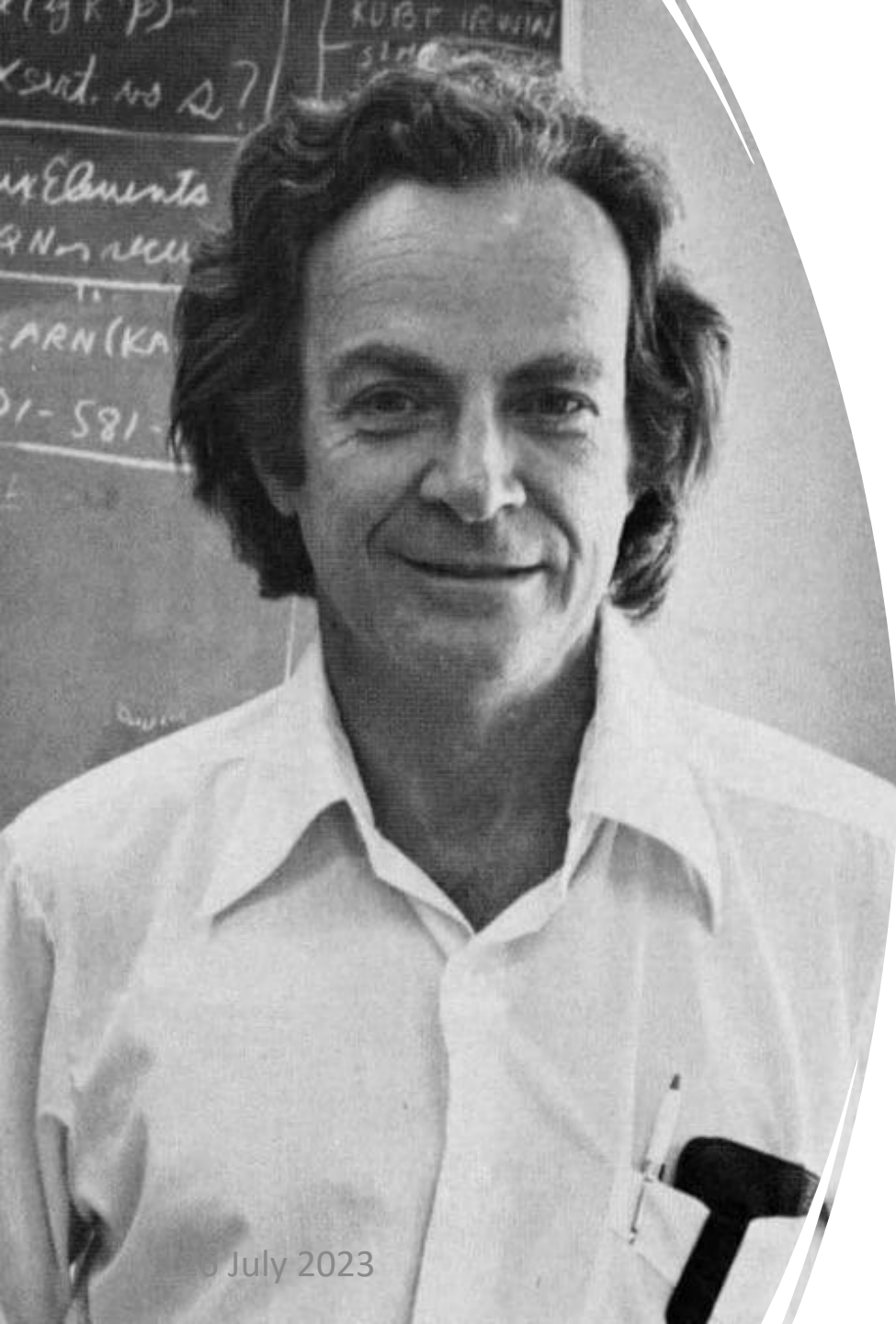
Qiskit Quantum Developer Certificate

- Certification awarded for learning quantum computation using Qiskit
- Demonstrates you having fundamental knowledge of quantum computing concepts
- Demonstrates you being able to create and execute quantum computing programs on IBM Quantum computers and simulators
- Defining, executing, and visualizing results of quantum circuits with different gates, etc.
- Useful if you want to demonstrate your ability in quantum computing
- <https://www.ibm.com/training/certification/C0010300>



Takeaways

- Quantum computing is an emerging field that's still far away from being useful in solving real life problems at an exponential rate
- Quantum computing is basically linear algebra and complex variables (unless you're working on developing the hardware)
- Current main problems revolve around error correction and increasing number of useful qubits
- When people first created the classical computer, they did not imagine how it would evolve. They probably never imagined the Internet and the horrors you can now find there
- Prospects are looking **okay** for the time being – just need to be cautiously optimistic and not blindly follow the hype train
- There are many ways you can get involved in quantum computing today!



“Nature isn't classical, dammit, and if you want to make a simulation of nature, you'd better make it quantum mechanical, and by golly it's a wonderful problem, because it doesn't look so easy.”

-Richard Feynman

Blooket

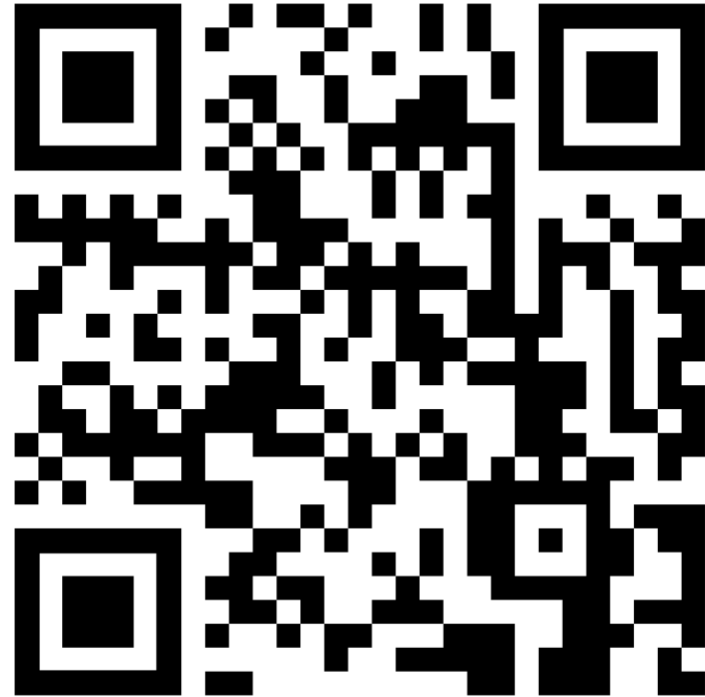


<https://play.blooket.com>

More resources

- [Introduction to Quantum Computing and Quantum Hardware \(Qiskit on YouTube\)](#)
- [Qiskit textbook](#)
- [Xanadu textbook](#)
- [Quantum Machine Learning demonstrations \(Pennylane\)](#)
- [A course on Quantum Machine Learning \(Github – Pennylane\)](#)
- [1 Minute Qiskit \(Qiskit on YouTube\)](#)
- [Why Did Quantum Entanglement Win the Nobel Prize in Physics? \(PBS Spacetime on YouTube\)](#)
- [What is Quantum Safe \(IBM Technology on YouTube\)](#)

Thank you for your attention!



<https://forms.gle/5NoXyLmBANAWA88d9>

Bonus!

Quantum lingo cheat sheet

- **Noisy Intermediate-Scale Quantum (NISQ) era:** era with intermediate number of qubits (~100) that still have problems with noise/decoherence – era we are currently in
- **Fault tolerant computer:** Less affected by noise/decoherence
- **Fidelity:** a measure of how close the final quantum state of the real-life qubits is to the ideal case. The threshold for fault-tolerant quantum computing is over 99%
- **Quantum volume:** a metric that measures the capabilities and error rates of a quantum computer based on the size of the successfully running circuits. It was invented by IBM
- **Coherence time:** the length of time a quantum superposition state can survive
- **Transmon:** a superconducting loop-shaped qubit that can be created at extremely low temperatures

Cracking RSA encryption with a quantum computer

- Chinese scientists released a [paper](#) in Dec 2022 claiming to have cracked low-level RSA encryption using a hybrid of a quantum and classical computer
- 48-bit numbers using a 10-qubit quantum computer
- They combine classical lattice reduction factoring techniques (Schnorr's algorithm – not be confused with Shor's algorithm) with a quantum approximate optimization algorithm
- They calculated that it's possible to scale their algorithm for use with 2048-bit keys using a quantum computer with only **372 qubits!**
- IBM already has a [433-qubit quantum computer](#)...
- Experts are saying these claims don't add up and shouldn't be scalable to higher qubit computer. Expect IBM to do some tests soon