Astrophysical Probes of Lorentz Violation





LETTERS TO THE EDITORS

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Is there an Æther ?

In the last century, the idea of a universal and all-pervading æther was popular as a foundation on which to build the theory of electromagnetic phenomena. The situation was profoundly influenced in 1905 by Einstein's discovery of the principle of relativity, leading to the requirement of a fourdimensional formulation of all natural laws. It was soon found that the existence of an æther could not be fitted in with relativity, and since relativity was well established, the æther was abandoned.

Physical knowledge has advanced very much since 1905, notably by the arrival of quantum mechanics, and the situation has again changed. If one reexamines the question in the light of present-day knowledge, one finds that the æther is no longer ruled out by relativity, and good reasons can now be advanced for postulating an æther.

Let us consider in its simplest form the old argument for showing that the existence of an ather is incompatible with relativity. Take a region of spacetime which is a perfect vacuum, that is, there is no matter in it and also no fields. According to the principle of relativity, this region must be isotropic in the Lorentz sense-all directions within the lightcone must be equivalent to one another. According to the æther hypothesis, at each point in the region there must be an æther, moving with some velocity, presumably less than the velocity of light. This velocity provides a preferred direction within the light-cone in space-time, which direction should show itself up in suitable experiments. Thus we get a contradiction with the relativistic requirement that all directions within the light-cone are equivalent.

This argument is unassailable from the 1905 point of view, but at the present time it needs modification, because we have to apply quantum mechanics to the æther. The velocity of the æther, like other physical variables, is subject to uncertainty relations. For a particular physical state the velocity of the æther at a certain point of space-time will not usually be a well-defined quantity, but will be distributed over various possible values according to a probability law obtained by taking the square of the modulus of a wave function. We may set up a wave function which makes all values for the velocity of the æther equally probable. Such a wave function may well represent the perfect vacuum state in accordance with the principle of relativity.

One gets an analogous problem by considering the hydrogen atom with neglect of the spins of the electron and proton. From the classical picture it would seem to be impossible for this atom to be in a state of spherical symmetry. We know experimentally that the hydrogen atom can be in a state of spherical symmetry-any spectroscopic S-state is such a state -and the quantum theory provides an explanation by allowing spherically symmetrical wave functions, electron to proton equally probable.

We thus see that the passage from the classical theory to the quantum theory makes drastic alterations in our ideas of symmetry. A thing which cannot be symmetrical in the classical model may very well be symmetrical after quantization.

This provides a means of reconciling the disturbance of Lorentz symmetry in space-time produced by the existence of an æther with the principle of relativity.

There is one respect in which the analogy of the hydrogen atom is imperfect. A state of spherical symmetry of the hydrogen atom is quite a proper state-the wave function representing it can be normalized. This is not so for the state of Lorentz symmetry of the æther.

Let us assume the four components v_{μ} of the velocity of the æther at any point of space-time commute with one another. Then we can set up a representation with the wave functions involving the v's. The four v's can be pictured as defining a point on a three-dimensional hyperboloid in a fourdimensional space, with the equation :

$$v_0^2 - v_1^2 - v_2^2 - v_3^2 = 1$$
 $v_0 > 0.$ (1)

A wave-function which represents a state for which all æther velocities are equally probable must be independent of the v's, so it is a constant over the hyperboloid (1). If we form the square of the modulus of this wave function and integrate over the threedimensional surface (1) in a Lorentz-invariant manner, which means attaching equal weights to elements of the surface which can be transformed into one another by a Lorentz transformation, the result will be infinite. Thus this wave function cannot be normalized.

The states corresponding to wave functions that can be normalized are the only states that can be attained in practice. A state corresponding to a wave function which cannot be normalized should be looked upon as a theoretical idealization, which can never be actually realized, although one can approach indefinitely close to it. Such idealized states are very useful in quantum theory, and we could not do without them. For example, any state for which there is a particle with a specified momentum is of this kind-the wave function cannot be normalized because from the uncertainty principle the particle would have to be distributed over the whole universe -and such states are needed in collision problems.

We can now see that we may very well have an æther, subject to quantum mechanics and conforming to relativity, provided we are willing to consider the perfect vacuum as an idealized state, not attainable in practice. From the experimental point of view, there does not seem to be any objection to this. We must make some profound alterations in our theoretical ideas of the vacuum. It is no longer a trivial state, but needs elaborate mathematics for its description.

I have recently¹ put forward a new theory of electrodynamics in which the potentials A_{μ} are restricted by :

$$A_{\mu} A_{\mu} = k^2,$$

where k is a universal constant. From the continuity of A_0 we see that it must always have the same sign and we may take it positive. We can then put

$$k^{-1}A_{\mu} = v_{\mu}$$
 (2)

and get v's satisfying (1). These v's define a velocity. each of which makes all directions for the line joining . Its physical significance in the theory is that if there is any electric charge it must flow with this velocity, and in regions where there is no charge it is the velocity with which a small charge would have to flow if it were introduced.

We have now the velocity (2) at all points of space-time, playing a fundamental part in electro-

Lorentz Invariance is not Sacred

Dirac, 1951

Quantum-Gravitational Space-Time Foam

ANNALS OF PHYSICS: 2, 604-614 (1957)

On the Nature of Quantum Geometrodynamics

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Classical gravitation, electromagnetism, charge, and mass are described in a preceding article in terms of curved empty space and nothing more. In advance of the detailed quantization of this pure Einstein-Maxwell geometrodynamics, an attempt is made here (1) to bring to light some of the most important properties to be expected for quantized geometrodynamics and (2) to assess whether this theory, without addition of any inventive elements, can contribute anything to the understanding of the elementary particle problem. Gravitational field fluctuations are concluded to have qualitatively new consequences at distances of the order of $(\hbar G/c^3)^{1/2} = 1.6 \times 10^{-33}$ cm. They lead one to expect the virtual creation and annihilation throughout all space of pairs with electric charges of the order $\sim (\hbar c)^{1/2}$ and energies of the order $(\hbar c^5/G)^{1/2} = (2.18 \times 10^{-5} \text{ g})c^2 = 2.4 \times 10^{22} mc^2$.



Nature of Quantum-Gravitational Vacuum

- Expect quantum fluctuations in fabric of space-time
- In natural Planckian units: $\Delta E, \Delta x, \Delta t, \Delta \chi \sim 1$
- Fluctuations in energy, space, time, topology of order unity
- Space-time foam
- Manifestations?
- Lorentz violation?
- Equivalence violation?

(Modification of Quantum Mechanics?)



Modification of Lorentz Invariance?

Small boats slower than big ships in rough seas Higher frequencies travel < c? Violation of principle of equivalence?

Sand entropy in the second second second

Amelino-Camelia, JE, Mavromatos, Nanopoulos & Sarkar, astro-ph/9712103, Nature 393 (1998) 7

Space-Time Foam as a Dynamical Medium

- Expect large intrinsic fluctuations at small scales
- Expect back-reaction due to energetic particles
- Non-trivial refractive index
- Effect on propagation that increases with energy:

$$c^{2}\mathbf{p}^{2} = E^{2}\left[1 + \xi E/E_{\rm QG} + \mathcal{O}(E^{2}/E_{\rm QG}^{2})\right]$$

$$v = \frac{\partial E}{\partial p} \sim c \left(1 - \xi \frac{E}{E_{\rm QG}} \right)$$

- Non-critical string model: $\xi = -1$
- $(\xi = -1 \text{ needed to avoid Čerenkov radiation in vacuo})$
- Expect: $E_{QG} = O(M_P)$?
- Related to string scale in non-critical string model

letters to nature

Tests of quantum gravity from observations of γ -ray bursts

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The recent confirmation that at least some γ -ray bursts originate at cosmological distances¹⁻⁴ suggests that the radiation from them could be used to probe some of the fundamental laws of physics. Here we show that γ -ray bursts will be sensitive to an energy dispersion predicted by some approaches to quantum gravity. Many of the bursts have structure on relatively rapid timescales⁵, which means that in principle it is possible to look for energydependent dispersion of the radiation, manifested in the arrival times of the photons, if several different energy bands are observed simultaneously. A simple estimate indicates that, because of their high energies and distant origin, observations of these bursts should be sensitive to a dispersion scale that is comparable to the Planck energy scale (~10¹⁹ GeV), which is sufficient to test theories of quantum gravity. Such observations are already possible using existing γ -ray burst detectors. photon energies, any analogous quantum-gravity effect could be distinguished by its different energy dependence: the quantum-gravity effect would increase with energy, whereas conventional medium effects decrease with energy in the range of interest⁶.

Equation (1) encodes a minute modification for most practical purposes, as E_{QG} is believed to be a very high scale, presumably of the order of the Planck scale $E_{\rm p} \approx 10^{19}$ GeV. Even so, such a deformation could be rather significant for even moderate-energy signals, if they travel over very long distances. According to equation (1), a signal of energy *E* that travels a distance *L* acquires a 'time delay', measured with respect to the ordinary case of an energy-independent speed *c* for metaless paralles:

$$\Delta t \approx \xi \frac{E}{E_{\rm QG}} \frac{L}{c} \tag{2}$$

This is most likely to be observable when E and L are large while the interval δt , over which the signal exhibits time structure, is small. This is the case for GRBs, which is why they offer particularly good prospects for such measurements, as we discuss later.

We first review briefly how modified laws for the propagation of particles have emerged independently in different quantum-gravity approaches. The suggestion that quantum-gravitational fluctuations might modify particle propagation in an observable way can already be found in refs 7 and 9. A phenomenological parametrization of the way this could affect the neutral kaon system^{9–11} has been already tested in laboratory experiments, which have set lower limits on parameters analogous to the E_{QG} introduced above at levels comparable to E_P (ref. 12). In the case of massless particles such as the photon, which interests us here, the first example of a quantumgravitational medium effect with which we are familiar occurred in a string formulation of an expanding Robertson–Walker–Friedman

Astrophysical Probes of Lorentz Violation

• Time delay from distant object: $\Delta t \sim \xi \frac{E}{E_{oc}} \frac{L}{c}$

Amelino-Camelia, JE, Mavromatos, Nanopoulos + Sarkar

- Compare arrivals of photons of different energies from astrophysical source with small intrinsic δt
- Gamma-Ray Bursters, pulsars, active galaxies, ...

• Typical	Source	Distance	E	Δt	Sensitivity to M	
sensitivities.	GRB 920229 ^a	$3000 { m Mpc} (?)$	200 keV	$10^{-2} { m s}$	$0.6\times 10^{16}~{\rm GeV}~(?)$	
	GRB 980425 a	$40 { m Mpc}$	$1.8 { m ~MeV}$	10^{-3} s (?)	$0.7\times 10^{16}~{\rm GeV}~(?)$	
	GRB 920925 c a	$40 { m Mpc} (?)$	$200 { m TeV}$ (?)	$200 \mathrm{~s}$	$0.4\times 10^{19}~{\rm GeV}~(?)$	
	Mrk 421 b	$100 {\rm ~Mpc}$	$2 { m TeV}$	$280 \mathrm{~s}$	$> 7 \times 10^{16}~{ m GeV}$	
	Crab pulsar c	$2.2 \ \mathrm{kpc}$	$2 {\rm GeV}$	$0.35 \mathrm{\ ms}$	$> 1.3 imes 10^{15} { m ~GeV}$.	
	GRB 990123	$5000 { m ~Mpc}$	$4 { m MeV}$	1 s (?)	$2 \times 10^{15} \text{ GeV} (?)$	

Violation of the Equivalence Principle?

- Non-Universality of Lorentz Violation?
- Do all relativistic particles have same velocity?
- Not necessarily, if particle interactions with space-time foam are non-universal
- (Relativistic) departure from Principle of Equivalence
- Consistent with astrophysics: limits on Lorentz violation for electrons >> $m_{\rm P}$
- Expected in non-critical string model of foam

Synchrotron Radiation Constraint from Crab Nebula

- See 0.5 GeV γ : inverse Compton by > 50 TeV *e*
- Consider modified dispersion relations for both electrons eand photons γ : $\omega^2(k) = k^2 + \xi_{\gamma} \frac{k^3}{M_{\rm P}} \quad E^2(p) = m_0^2 + p^2 + \xi_e \frac{p^3}{M_{\rm P}}$
- Lorentz-invariant: $\omega_c^{LI} = \frac{3}{2} \frac{eH}{m_0} \frac{1}{1-\beta^2}$
- QG modification: $\omega_c^{QG} = \frac{3}{\sqrt{2}} \frac{eH}{m_0} \frac{1}{(1+\sqrt{2-1/\eta^2})^{1/2} \left(\frac{m_0^2}{E^2} + (\alpha+1)\left(\frac{E}{M}\right)^{\alpha}\right)}$
- For $\xi = (E/m_P)^{\alpha}$ $data \rightarrow |\xi_e| < \left(\frac{3eH}{m_0}\right)^{\frac{\alpha+2}{2\alpha}} \left(\frac{M_P}{m_0}\right) \left(\frac{2}{\alpha(\alpha+1)}\right)^{1/\alpha} \left(\frac{\alpha}{\alpha+2}\right)^{(\alpha+2)/2\alpha}$
- Lower bound on modification: $\alpha > 1.72$
- If $\alpha = 1$: $m_{QG} > 10^{26} \text{ GeV}$

No constraint on LV for photon, none expected for electron

JE, Mavromatos + Nanopoulos







JE, Konoplich, Mavromatos, Nguyen, Sakharov, Sarkisyan-Grinbaum, arXiv:1807.00189

Robust Analysis of Fermi-LAT GRBs



HESS Analysis of Markarian 501



Another Possible Effect of Lorentz Violation

- For effect ~ $(E/E_{QG})^n$
- Time lag:

$$\tau_n = \frac{\Delta t_n}{\Delta E_n} \simeq \pm \frac{n+1}{2} \frac{1}{E_{QG}^n} \int_0^z \frac{(1+z')^n}{H(z')} \mathrm{d}z'$$

 Also: absorption of energetic photons by e⁺e⁻ pair production modified by threshold:
 Kifure, astro-ph/9904164 Proheree & Meyer, astro-ph/9904164

$$\epsilon_{\rm thr} = \frac{m_e^2 c^4}{E_\gamma'} + \frac{1}{4} \frac{E_\gamma'^{n+1}}{E_{\rm QG}^n}$$

• Competitive sensitivities

Possible Effect on y Spectrum

- Expect absorption due to e⁺e⁻ production in collisions with γ background
- Reduced absorption if _ Lorentz violation via modified (E, p) dispersion relation for γ



Interesting for CTA



HESS Analysis of Markarian 501



MAGIC Analysis of GRB 190114C



Analysis of GRB 221009A



Brightest GRB Ever: z = 0.151, E < 7 TeV^(*) Comparison of LV limits with other GRBs (in Planck units) (*) Would be strengthened by ~ 3 if higher-energy events included

GRB	090510^{a}	190114C	221009A
Red Shift	0.903	0.425	0.151
$\Delta E ~[{ m TeV}]$	$10^{-4} - 0.03$	0.3 - 1	0.2 - 7
$\Delta T_{\rm obs}$ [s]	0.15 - 0.217	30 - 60	9 - 14
$\mathcal{E}_{ ext{QG},1}^{(\sigma)}$	$11^- \ 5.2^+$	$0.23^- \ 0.45^+$	$5.9^- \ 6.2^+$
$\mathcal{E}_{\mathrm{QG},2}^{(\sigma)}/10^{-8}$	$0.7^- \ 0.77^+$	$0.46^- \ 0.52^+$	$5.8^- \ 4.6^+$

Piran & Ofengeim, arXiv:2308.03031

Neutrinos?



Early Constraints on Neutrino Lorentz Violation

• First MINOS measurement of neutrino velocity:

 $(v - c)/c > -2.4 \times 10^{-5}$

corresponded to

 $M_1 > 10^5 \text{ GeV}$

• Improved MINOS measurement

 $(v - c)/c > -1 \times 10^{-6}$

MINOS Collaboration, arXiv:0706.0437 [hep-ex]

MINOS Collaboration, arXiv:1507.04328

corresponds to

 $M_1 > 3 \ge 10^6 \text{ GeV}$

• Coincidence between neutrinos from supernova 1987a in Kamioka II, IMB and Baksan experiments:

 $M_1 > 2.7 \times 10^{10} \text{ GeV}$

Ellis, Harries, Meregaglia, Sakharov, & A.Rubbia, arXiv:0805.0253 [hep-ph]

Multimessenger Observations of Blazar TXS 0506+056

IceCube-170922A vs Fermi-LAT (left), MAGIC (right)



IceCube, Fermi-LAT, MAGIC, AGILE, ASAS-SN, HAWC, H.E.S.S, INTEGRAL, Kanata, Kiso, Kapteyn, Liverpool telescope, Subaru, Swift/NuSTAR, VERITAS, and VLA/17B-403 teams arXiv:1807.08816

Electromagnetic Follow-up to IC170922



JE, Mavromatos, Sakharov & Sarkisyan-Grinbaum, arXiv:1807.05155

Earlier Neutrino Flare from TXS 0506+056



Bustamante, JE, Konoplich & Sakharov, in preparation

Analysis of Neutrino Burst from TXS 0506+056

- Compensation of possible Lorentz violation:
 - Kolmogorov-Smirnov, skewness, kurtosis, combination



Bradascio et al, arXiv:2308.16699

Neutrinos from Tidal Disruption Events

- Stars captured by massive black holes disrupted, subject to "spaghettification"
- Squeezing, heating, X-ray emission: neutrinos?



Neutrinos from Tidal Disruption Events

• Tidal disruption events accompanied by neutrinos:



- AT2019dsg: 200 TeV neutrino, time-lag $\frac{1}{2}$ yr, z = 0.051
- AT2019fdr: 80 TeV neutrino, time-lag 1 yr, z = 0.267
- AT2019aacl: 170 TeV neutrino, time-lag 0.4 yr, z = 0.036
- Sensitivities to $M_1 \sim 3 \times 10^{14} \text{ GeV}$

IceCube Constraints on Lorentz Violation

• From energetic extragalactic neutrinos:										
	Source	Redshift	Remark	Tele	elescope $\nu = E_{\nu}$ [TeV	E_{ν} [TeV]	Δt [days]	Significance	Lower limit on LV scale [GeV	
						_p[101]			Linear, M_1	Quadratic, M_2
	PKS B1424-418	1.522	Single ν/γ	HESE-35		2000	160	5%	1.1×10^{17}	$7.6 imes10^{11}$
	TXS $0506 + 056$	0.3365	Single ν/γ	IC170922A		200	10	0.3%	$3.7 imes 10^{16}$	$1.1 imes 10^{11}$
	TXS $0506+056$	0.3365	Multiple ν	Several IC		~ 100	~ 100	0.8%	$4.0 imes 10^{14}$	$6.7 imes 10^8$
	GB6 J1040+0617	≥ 0.7351	Single ν/γ	IC1	41209A	100	100	30%	(4.2×10^{15})	(2.9×10^{10})
	PKS $0735 + 178$	≥ 0.424	$4 u/\gamma$	IC2	11208A	170	10	See text	$(3.0 imes 10^{16})$	(1.1×10^{10})
	PKS $1123 + 264$	2.341	Single ν/γ	IC120523A		> 200	10	See text	(2.6×10^{17})	(4.1×10^{11})
	TXS $0506+056$	0.3365	Single $\nu/{\rm radio}$	GVD210418CA		220	200	See text	$(\sim 2.0\times 10^{15})$	$(\sim 2.6 \times 10^{10})$
	PKS 0625-35	0.055	Three ν	IceCube		63 - 302	1	3.56σ	$(\sim 10^{16})?$	$(\sim 10^{10})?$
	AT2019dsg	0.051	Single ν/γ	IC191001A		200	150	TDE events	$3.5 imes 10^{14}$	1.0×10^{10}
	AT2019fdr	0.267	Single ν/γ	IC200530A		80	393	combined	$3.0 imes10^{14}$	$6.3 imes10^9$
	AT2019aacl	0.036	Single ν/γ	IC191119A		170	148	6×10^{-4}	2.1×10^{14}	7.4×10^9
•	• For comparison.									
		P ••• ••			$M \sim$	$1 \sim 10$	5 CaV			
	• Accelerator neutrinos:				$M_1 >$	1 X 10	Gev			
					$N_{\rm c}$	$l_2 > 60$	$0 { m GeV}$			
	• SN1097A.				$M_1 > 2.7 \times 10^{10} \text{ GeV}$					
- SIN170/A.					1.01	$a^4 \alpha v$				
					$M_2 >$	4.0×10	J⁻ GeV			







- Graviton mass $< 10^{-27} \times \text{mass of electron}$
- Waves of different frequencies have similar speeds

Constrain Lorentz violation JE, Mavromatos & Nanopoulos, arXiv:1602.04764

Observations of Neutron Star Merger



AION Collaboration

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Network with MAGIS project in US

MAGIS Collaboration (Abe et al): arXiv:2104.02835





Oxford

Boulby? CERN?

AION: Proposed Programme

- AION-10: Stage 1 [year 1 to 3]
- 1 & 10 m Interferometers & site investigation for 100m baseline
 Initial funding from UK STFC
- AION-100: Stage 2 [year 3 to 6]
- 100m Construction & commissioning
- AION-KM: Stage 3 [> year 6]
- Operating AION-100 and planning for 1 km & beyond
- AION-SPACE (AEDGE): Stage 4
- Space-based version



Principle of Atom Interferometry

Mach-Zehnder Laser Interferometer

Atom Interferometer



Laser excitation gives momentum kick to excited atom, which follows separated space-time path

Interference between atoms following different paths





JE & Vaskonen: arXiv:2003.13480

Subir: The Face that Launched 1309 Lorentz-Violating Papers (so far)

