



# A Search for Heavy Neutral Leptons in tau decays at *BABAR*

Tau2023  
(Louisville, KY)



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on behalf of the *BABAR* Collaboration

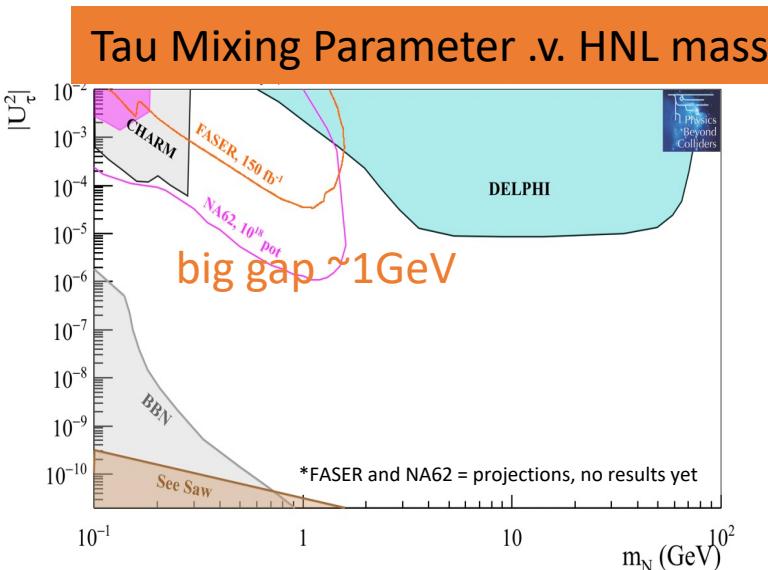
December 2023

# Motivations

Heavy Neutral Leptons (HNLs) are additional neutrino states. They have mass but are neutral in all respects.

- HNLs are proposed by several beyond Standard Model (BSM) theories to explain three major observational phenomena:
  - Neutrino oscillations and origins of their mass via seesaw models etc. (Phys. Rev. D 23,165);**
  - Baryonic asymmetry of Universe (Phys. Rev. Lett. 81, 1359);**
  - Dark matter candidate (Phys. Lett. B 631, 151–156).**
- $\nu$ -MSM proposes three keV-GeV scale HNLs.
- Experiments generally quote results in parameter space of elements  $|U_{ln}|^2$  .v. HNL mass hypothesis.
- Tau sector historically less explored...**

Journal of Physics G: Nuc. & Part.1075 Phys. 47, 010501 (2019)

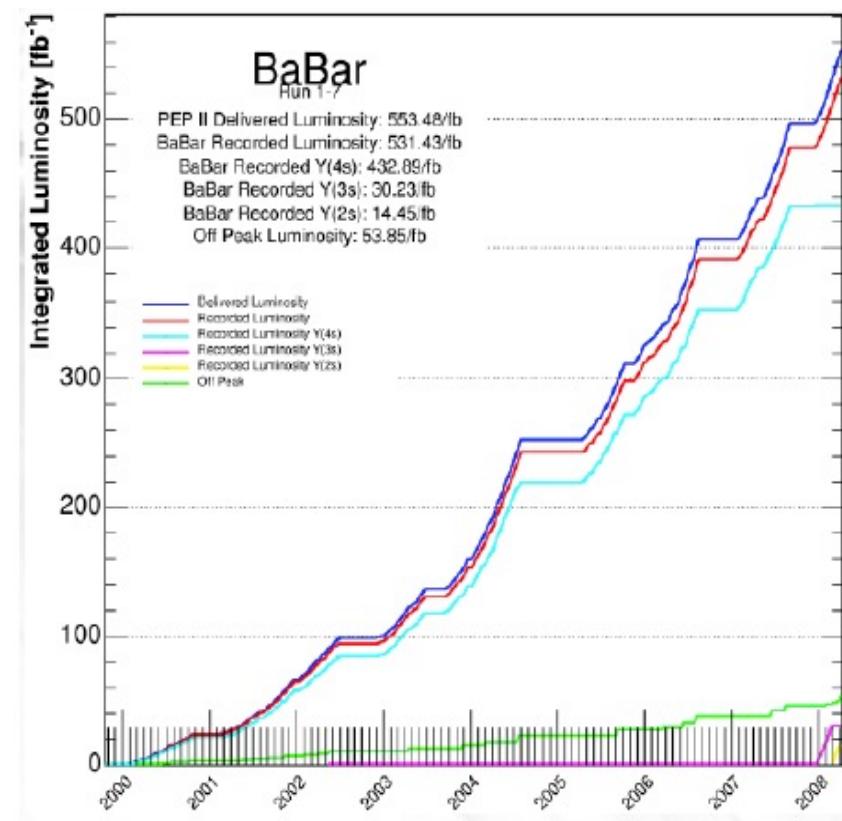
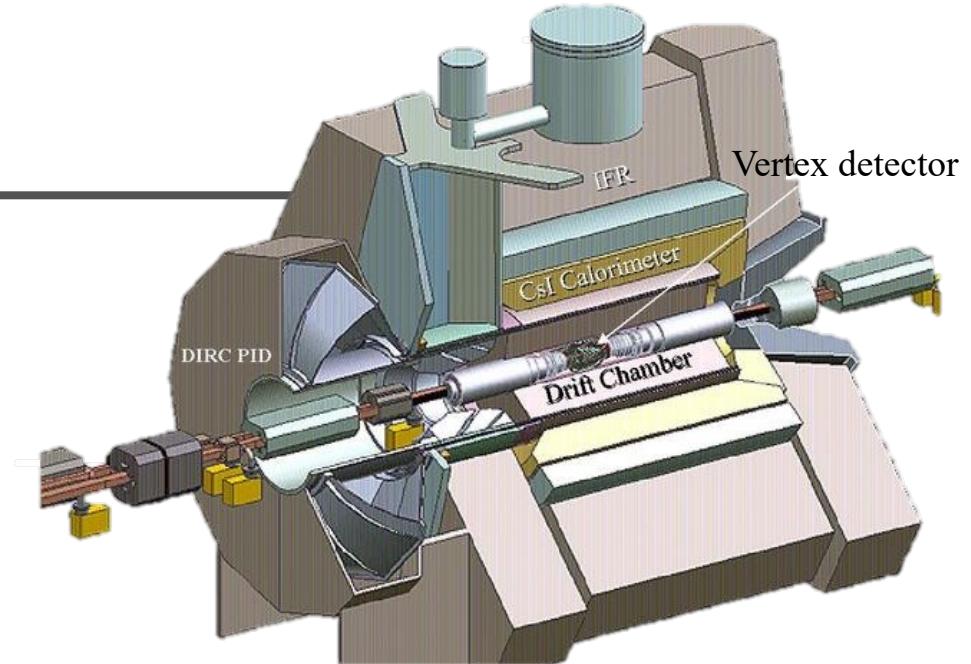


$\sigma(e^+e^- \rightarrow \tau^+\tau^-) = 0.919 \pm 0.003 \text{ nb}$   
Integrated luminosity in runs used =  $424 \text{ fb}^{-1}$   
 $\rightarrow N_{\tau\tau} \sim 4 \times 10^8 \text{ events}$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \\ \vdots \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} & \dots \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} & \dots \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} & \dots \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} & \dots \\ \vdots & \vdots & \vdots & \ddots & \vdots \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \\ \nu_4 \\ \vdots \end{pmatrix}.$$

# The BABAR Experiment

- For overview of experiment: **Nucl. Instrum. Meth. A 729, 615 (2013)**.
- Asymmetric  $e^+e^-$  collider with  $\sqrt{s} = 10.58 \text{ GeV}/c^2$  i.e.  $\Upsilon(4S)$  resonance:  
9 GeV electrons collide with 3 GeV positrons.
- **Total luminosity:**  $432 \text{ fb}^{-1}$  ( $4.7 \times 10^8 \bar{B}B$ ) on peak.



## Detectors:

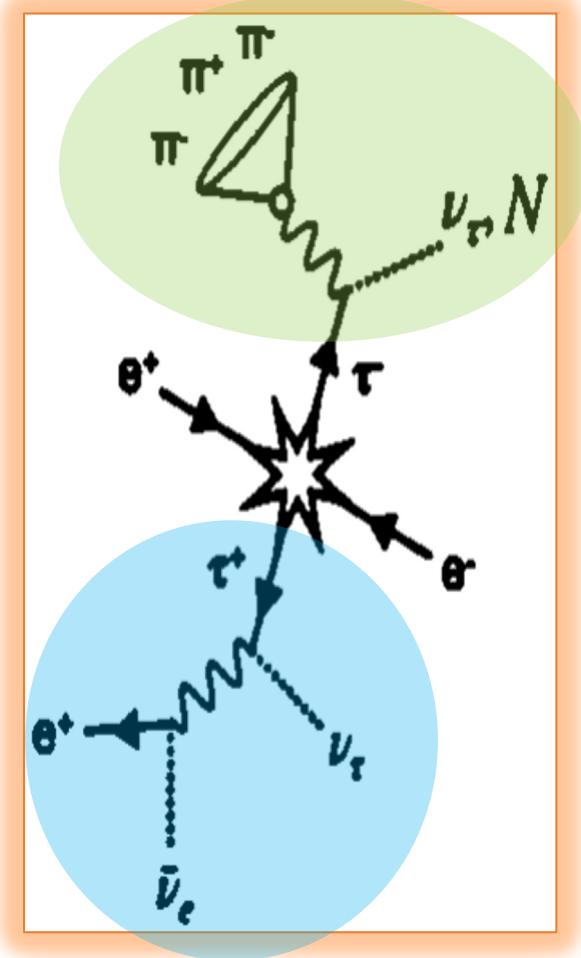
- **Reconstruct tracks:** Silicon Vertex Tracker (SVT) + 40-layer Drift Chamber (DCH), in 1.5-T solenoid.
  - Momentum resolution = 0.47% at 1 GeV/c
- **Measure energy:** Electromagnetic Calorimeter (EMC)
  - Energy resolution = 3% at 1 GeV.
- **PID:**
  - Identify charged pions, kaons and electrons using Ring Imaging Cherenkov detector (DIRC) + ionization loss measurements in the SVT and DCH.
  - Instrumented flux return of solenoid used to identify muons.

# The BABAR Search

$\sigma(e^+e^- \rightarrow \tau^+\tau^-) = 0.919 \pm 0.003 \text{ nb}$   
Integrated luminosity in runs used =  $424 \text{ fb}^{-1}$   
 $\rightarrow N_{\tau\tau} \sim 4 \times 10^8 \text{ events}$

- **BABAR** 2022 analysis used the kinematics of hadronic tau decays based on previous technique (*Phys.Rev.D* 91 (2015) 5, 053006 Kobach and Dobbs).
- Looks only at kinematics, no assumptions on underlying model, except that there must be some small mixing with tau sector:
  - “signal side” : three pronged pionic tau decay ( $\tau^- \rightarrow \pi^-\pi^-\pi^+\nu_\tau$ ) as it allows access to region  $100 < m_4 < 1360 \text{ MeV}/c^2$  where limits were loose.
  - “tag side” : Second tau decay must be leptonic, due to cleaner environment.

CPT assumed to hold, combining + and - signal sides. Branching Fractions:  
1-prong (electron or muon) ~ 34 %  
3-prong (3 pion) ~ 9%



# Method

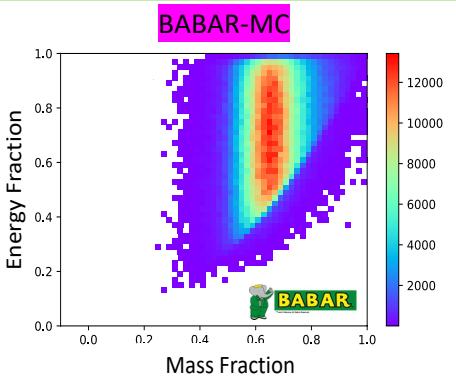
Templates for each mass in the form of 2D plots of  $E_h$ .v.  $m_h$ . Boundary of curved region in this plot characteristic of a massive neutrino.

**SM Tau Decay**

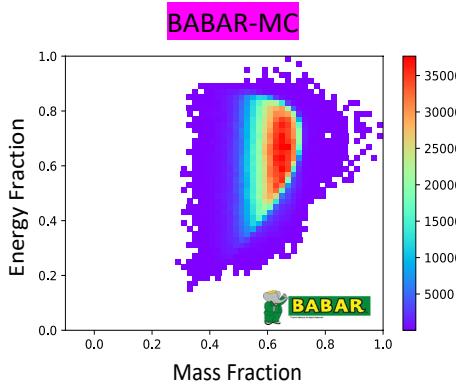
$$\frac{d\Gamma_{\text{tot}}(\tau^- \rightarrow \nu h^-)}{dm_h dE_h} = (1 - |U_{\tau 4}|^2) \frac{d\Gamma(\tau^- \rightarrow \nu h^-)}{dm_h dE_h} \Big|_{m_\nu=0} + |U_{\tau 4}|^2 \frac{d\Gamma(\tau^- \rightarrow \nu h^-)}{dm_h dE_h} \Big|_{m_\nu=m_4}.$$

**BSM Tau Decay**

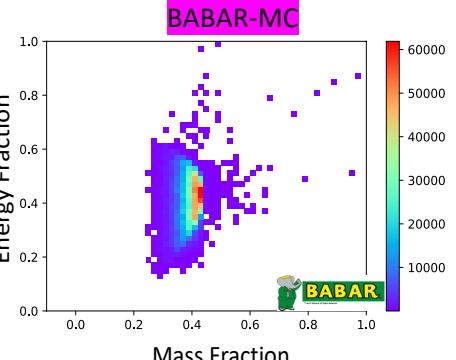
$m_4 = 100 \text{ MeV}/c^2$



$m_4 = 500 \text{ MeV}/c^2$



$m_4 = 1000 \text{ MeV}/c^2$



- Model 3-pronged decay as 2-body with outgoing HNL and hadronic system ( $h$ ).
- Define  $E_h$  as reconstructed energy and  $m_h$  as the invariant mass of the visible, hadronic products.
- $E_\tau = \frac{E_{cms}}{2}$  in the limit of no ISR. The value of  $E_h$  and  $m_h$  can exist, in principle, in the ranges:

$$3m_{\pi^\pm} < m_h < m_\tau - m_4, \quad \text{and}$$

$$E_\tau - \sqrt{m_4^2 + q_+^2} < E_h < E_\tau - \sqrt{m_4^2 + q_-^2},$$

where

$$q_\pm = \frac{m_\tau}{2} \left( \frac{m_h^2 - m_\tau^2 - m_4^2}{m_\tau^2} \right) \sqrt{\frac{E_\tau^2}{m_\tau^2} - 1} \pm \frac{E_\tau}{2} \sqrt{\left(1 - \frac{(m_h + m_4)^2}{m_\tau^2}\right) \left(1 - \frac{(m_h - m_4)^2}{m_\tau^2}\right)};$$

Signal samples made in modified TAUOLA, and passed through G4 + BABAR reco. alg.

# Background and Signal Simulations

- Use MC to estimate expected background contributions
- Detector response modelled using GEANT4, event generator specific to each source
- Three potential sources of non-signal events in data:

1. SM 3 prong decay to 3 charged pions ( $\tau^- \rightarrow \pi^-\pi^-\pi^+\nu_\tau$ )
2. Other SM tau decays accidentally tagged as (1)

## 3. SM non-tau backgrounds:

- $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^+B^-$  and  $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^0\bar{B}^0$
- $e^+e^- \rightarrow \bar{u}u, \bar{d}d, \bar{s}s$  and  $e^+e^- \rightarrow \bar{c}c$
- $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$

- **HNL : characterized by large missing mass** (TAUOLA+KK2F – custom function, mass modified to attribute masses in range 100 – 1300 MeV/c<sup>2</sup>)

TAUOLA: Comp. Phys. Co. 130, 260–325 (2000)  
KK2F: Comp. Phys. Co. 64, 275 (1991)  
EvtGen: Nucl. Instrum. Meth. A 462, 152 (2001)  
JetSet: Comp. Phys. Co. 39, 347 (1986)

# Fit Model

Assume each bin ( i, j ) in 2D plots can be represented by a Poisson sampling function:

$$\mathcal{L} = \prod_{ij} f(n_{ij}; n_{\text{obs}}, \vec{\theta}) = \prod_{ij} \frac{(\nu_{\text{HNL}} + \nu_{\tau-\text{SM}} + \nu_{\text{BKG}})_{ij}^{(n_{\text{obs}})_{ij}} e^{-(\nu_{\text{HNL}} + \nu_{\text{BKG}} + \nu_{\tau-\text{SM}})_{ij}}}{(n_{\text{obs}})_{ij}!} \times \prod_k f(\theta_k, \tilde{\theta}_k),$$

where:

Nuisance parameters

Potential signal events:

$$\hat{\nu}_{\text{HNL},ij} = n_{\text{HNL},ij}^{\text{reco}} = N_{\tau,\text{gen}} \cdot (|U_{\tau 4}|^2) \cdot p_{\text{HNL},ij},$$

Expected tau SM background events:

$$\hat{\nu}_{\tau-\text{SM},ij} = n_{\tau-\text{SM},ij}^{\text{reco}} = N_{\tau,\text{gen}} \cdot (1 - |U_{\tau 4}|^2) \cdot p_{\tau-\text{SM},ij},$$

Expected non-tau SM background events:

$$\hat{\nu}_{\text{BKG},ij} = n_{\text{BKG},ij}^{\text{reco}} = n_{\tau-\text{other},ij}^{\text{reco}} + n_{\text{non}-\tau,ij}^{\text{reco}},$$

Use Wilk's theorem to find limits:

$$q = -2\ln\left(\frac{\mathcal{L}_{H_0}(|U_{\tau 4}|_0^2; \hat{\theta}_0, \text{data})}{\mathcal{L}_{H_1}(|\hat{U}_{\tau 4}|^2; \hat{\theta}, \text{data})}\right) = -2\ln(\Delta \mathcal{L}).$$

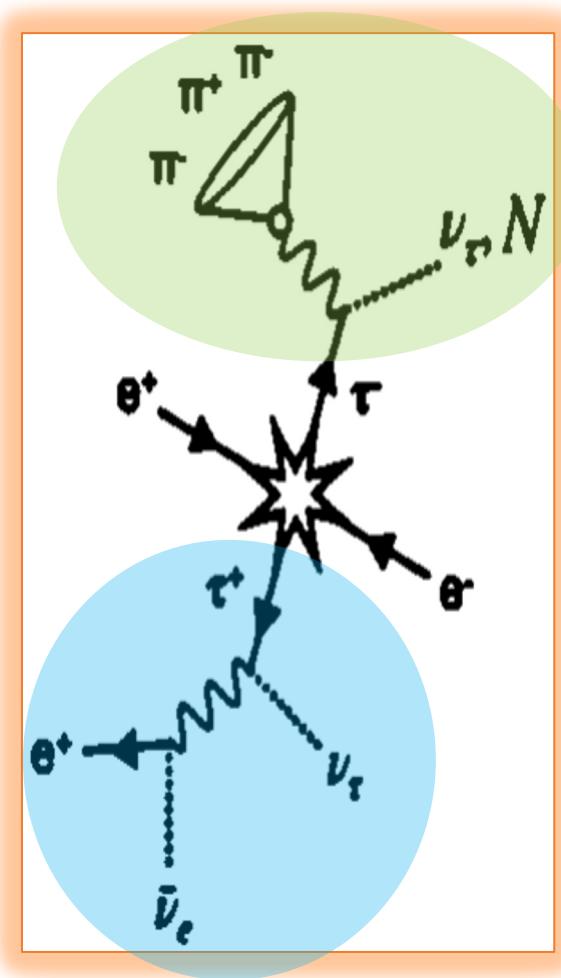
nuisance parameters maximized for a given value of  $|U_{\tau 4}|^2$  i.e. it is the conditional maximum-likelihood.  
Includes background only case

maximized (unconditional) likelihood giving the MLE of  $|U_{\tau 4}|^2$  a vector of nuisance parameters which maximize the likelihood.

# Event Selection

- Selection optimized  $\tau^\pm \rightarrow l^\pm v_l$  (tag) and  $\tau^\mp \rightarrow \pi^\mp \pi^\mp \pi^\pm v_{4?}$  (3h)

| Cut                                       | Purpose                              |
|---|--------------------------------------|
| Number of tracks                          | Ensure 1+3 prong topology            |
| Total charge on all 4 charged tracks is 0 | Charge conservation                  |
| $p_{CM}^{miss} > 0.9\% \sqrt{s}$          | Suppresses non-tau backgrounds       |
| All tracks: $p_{trans} > 250\text{MeV}/c$ | To reach DIRC                        |
| All tracks: $-0.76 < \cos(\theta) < 0.9$  | Acceptance of DIRC                   |
| 1 prong: $\frac{2p}{E} < 0.9\%$           | Consistent with tau decay            |
| PID Requirements                          | Uses Electron and Muon ID algorithms |

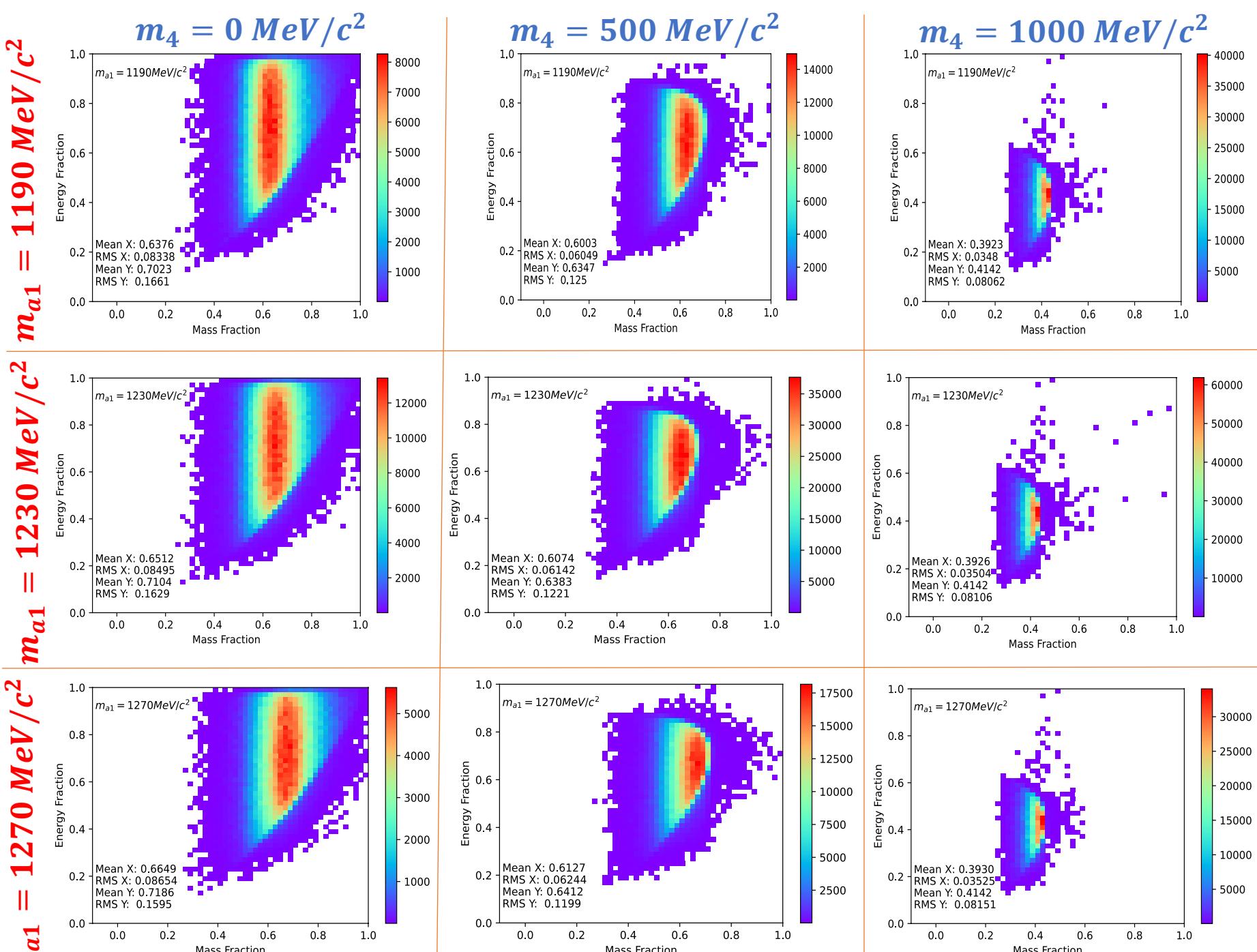


# Normalization Uncertainties

- Normalization uncertainties affect all bins uniformly.
- Have small effect on overall yield.
- They will be characterized as Gaussian nuisance parameters in the likelihood.

| Uncertainty                              | Contribution  |
|--|---|
| Luminosity                               | 0.44 % [ <i>BABAR</i> ]                                       |
| Cross-section                            | 0.31% [Data]  |
| Branching fraction of 1-prong tau decays | Electron : 0.23 % [PDG]<br>Muon: 0.23% [PDG]                  |
| Branching fraction of 3-prong tau decays | 3 pions : 0.57 % [PDG]  |
| PID Efficiency                           | Electron : 2 % [ <i>BABAR</i> ]<br>Muons : 1 %<br>Pions : 3 % |
| $q\bar{q}$ and Bhabha Contamination      | 0.3 % [Control region analysis]                               |
| Bin Size                                 | < 1% [Alter bins, check results]                              |
| Tracking Efficiency                      | N/A   |
| Detector Modelling                       | N/A   |
| Tau Mass uncertainty                     | N/A   |
| Tau Energy                               | N/A   |

# Systematic Shape Uncertainties



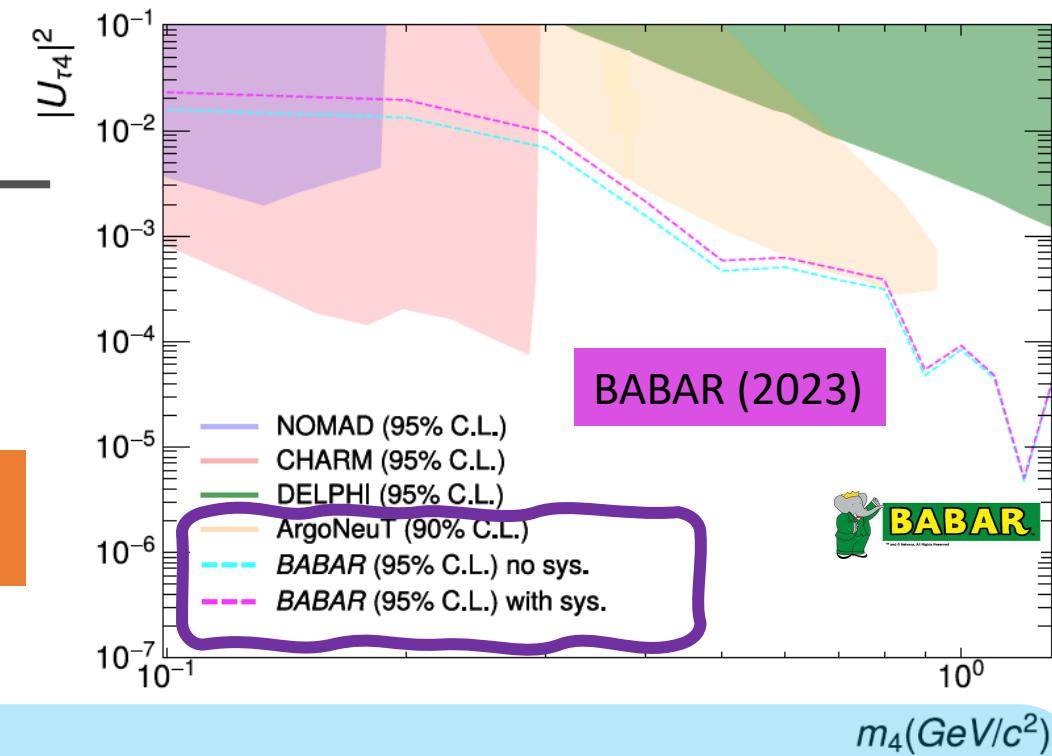
- $\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_\tau$  is mediated by the  $a_1$  resonance 97% of the time.
- Dominant shape systematic in signal and tau backgrounds are from modelling of the hadronic tau decays in TAUOLA.
- Experimental (PDG) uncertainties large:
  - $m_{a1} = 1230 \pm 40 \text{ MeV}/c^2$
  - $\Gamma_{a1} = 420 \pm 35 \text{ MeV}/c^2$  (we use PDG estimates 250 – 600  $\text{MeV}/c^2$ )
- To account for this looked at templates with mass and width varied to these extremes and re-calculated the likelihood
- $\Gamma_{a1}$  error has largest effect:
  - Shift in RMS of ~ 6 – 7% in  $m_h$  and ~ 1 – 3% in  $E_h$ .
  - Shift in mean values for  $E_h$  and  $m_h$  shift by only ~ 1 – 2%.

# The BABAR Result

| Mass [MeV] | No Sys.               | With Sys.             |
|------------|-----------------------|-----------------------|
| 100        | $1.58 \times 10^{-2}$ | $2.31 \times 10^{-2}$ |
| 200        | $1.33 \times 10^{-2}$ | $1.95 \times 10^{-2}$ |
| 300        | $6.91 \times 10^{-3}$ | $9.67 \times 10^{-3}$ |
| 400        | $1.57 \times 10^{-3}$ | $2.14 \times 10^{-3}$ |
| 500        | $4.65 \times 10^{-4}$ | $5.85 \times 10^{-4}$ |
| 600        | $5.06 \times 10^{-4}$ | $6.22 \times 10^{-4}$ |
| 700        | $3.82 \times 10^{-4}$ | $4.85 \times 10^{-4}$ |
| 800        | $3.12 \times 10^{-4}$ | $3.58 \times 10^{-4}$ |
| 900        | $4.70 \times 10^{-5}$ | $5.28 \times 10^{-5}$ |
| 1000       | $8.34 \times 10^{-5}$ | $9.11 \times 10^{-5}$ |
| 1100       | $4.49 \times 10^{-5}$ | $4.78 \times 10^{-5}$ |
| 1200       | $4.70 \times 10^{-6}$ | $5.04 \times 10^{-6}$ |
| 1300       | $3.85 \times 10^{-5}$ | $4.09 \times 10^{-5}$ |

At 95 % C.L

BABAR (2023):  
*Phys.Rev.D 107 5, 052009*



$m_4(\text{GeV}/\text{c}^2)$

- Binned likelihood fit incorporating nuisance parameters.
- Dominant systematic from modelling uncertainties in hadronic tau decays.
- Presents new upper limits on  $|U_{\tau 4}|^2$  at 95 % C.L. between 100 MeV/c<sup>2</sup> – 1300 MeV/c<sup>2</sup> :
  - **World-leading constraints at time of acceptance for publication.**
- In 2021-2023 there have also been new results in this region from:
  - ArgoNEUT: *Phys. Rev. Lett.*, 127, 121801 (shown)
  - Boiarska et al.: *Phys. Rev. D* 104, 095019 (indirect use of CHARM electron and muon result)
  - Barouki et al. : *SciPost Phys.*, 13:118, 2022. (BEBC reanalysis)

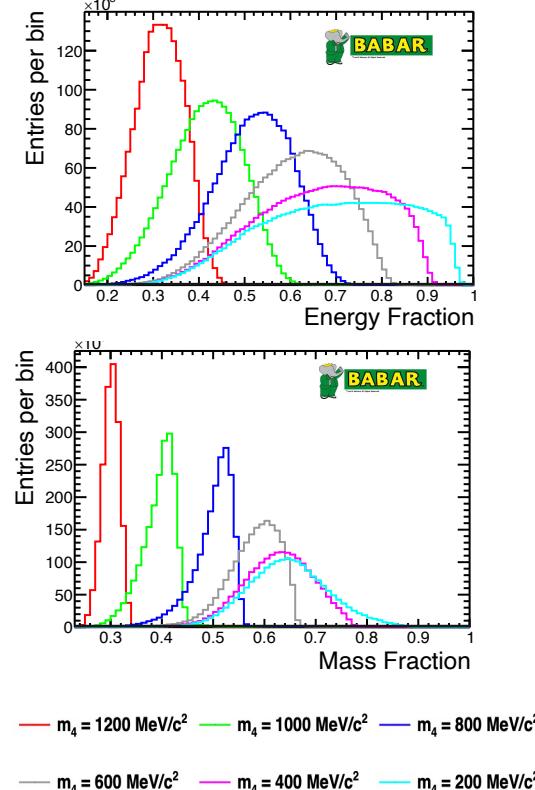
# Summary

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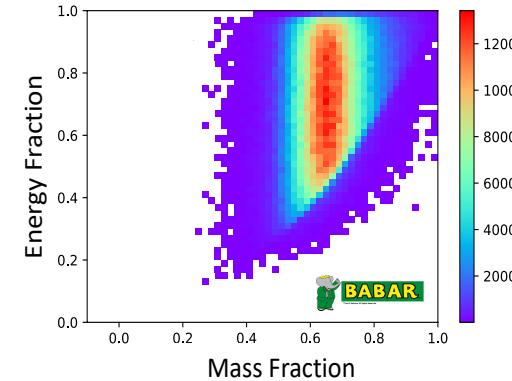
- Heavy Neutral Leptons offer ways of explaining several observational phenomena.
- The possible masses of the additional neutrino state is model dependent and can range from eV/c<sup>2</sup> up to very heavy masses.
- In the last few years, several new results have been published including results from collider-based experiments and neutrino experiments.
- Constraints in tau sector now comparable to those in the electron and muon sector.
- Many of these results are not from new experiments, they are in fact new studies using old data.
- This talk has given details on the latest analysis from **BABAR** which presents new upper limits on  $|U_{\tau 4}|^2$  at 95 % C.L. between 100 MeV/c<sup>2</sup> – 1300 MeV/c<sup>2</sup> in the range  $10^{-6} < |U_{\tau 4}|^2 < 10^{-2}$ .

# Example Signal Simulations

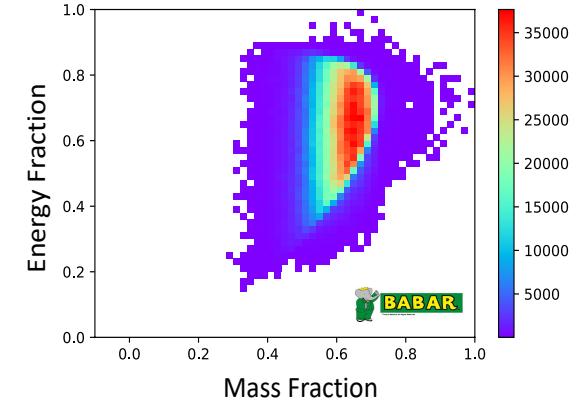
*largest sensitivity for large masses*



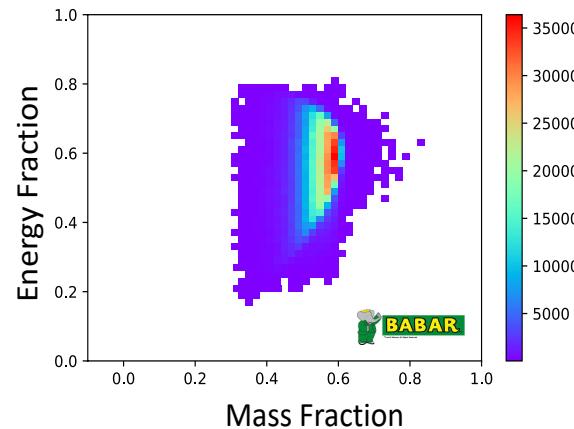
$m_4 = 100 \text{ MeV}/c^2$



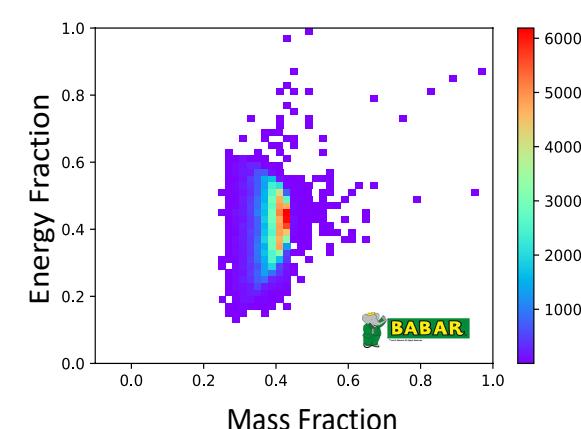
$m_4 = 500 \text{ MeV}/c^2$



$m_4 = 700 \text{ MeV}/c^2$



$m_4 = 1000 \text{ MeV}/c^2$



- Plots illustrate in 1D projections and final 2D templates for  $\tau^- \rightarrow \pi^- \pi^- \pi^+ \nu_X$
- Phase space changes with HNL mass

# Example 2D Plots

Data Total = 1273291  
MC Total = 1283654

