

Wishlist for g-2 at Tau 2025

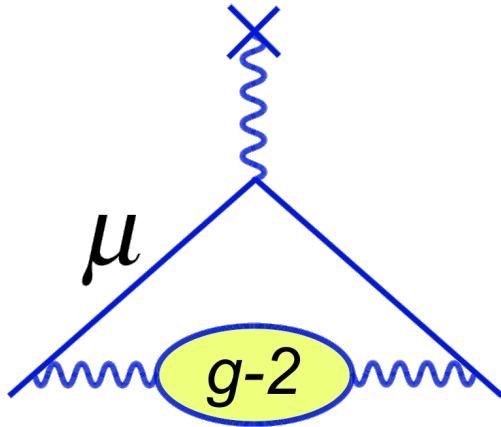
Brendan Kiburg

Fermi National Accelerator Laboratory

Technical Publication Number: FERMILAB-SLIDES-23-407-PPD

Tau 2023, Dec 4-8, Louisville Kentucky

Wishlist for $g-2$ at Tau 2025 Outline



- Tau $g-2$
- Muon $g-2$ Status
 - Experimental Status
 - Recent Results
 - Future Outlook
 - Theoretical Prediction
 - Dispersive Calculation
 - Prospects for Data Improvement
 - Tau Data
 - Lattice QCD

- Where Else to Look
 - Additional Analyses within Fermilab Muon $g-2$ (EDM, CPT/LV, DM)
 - JPARC $g-2$
 - MUonE
 - And beyond...
- Summary

Legend:

Content inside
red boxes
featured at
Tau2023

g-2 Motivation (Tau)

Magnetic and Electric Tau Dipole Moments Revisited

1. Tau lepton DM

Why are we interested in Tau dipole moments?

- $m = 1777 \text{ MeV}$
- Lifetime = $290 \times 10^{-15} \text{ sec}$
- Tau lepton decays into hadrons
- Lepton universality
- Sensitivity to NP $(m_\tau/\Lambda)^n$
- $\left(\frac{m_\tau}{m_e}\right)^2 \approx 10^7$; $\left(\frac{m_\tau}{m_\mu}\right)^2 \approx 3 \cdot 10^2$

G.González- Sprinberg

Louisville, 17th TAU 2023

3

- New Physics (NP) can show up in the anomalous magnetic moment, a_τ
- m^2 enhancement
- Possible additional enhancements in Lepton non-universality models

Magnetic and Electric Tau Dipole Moments Revisited

Monday

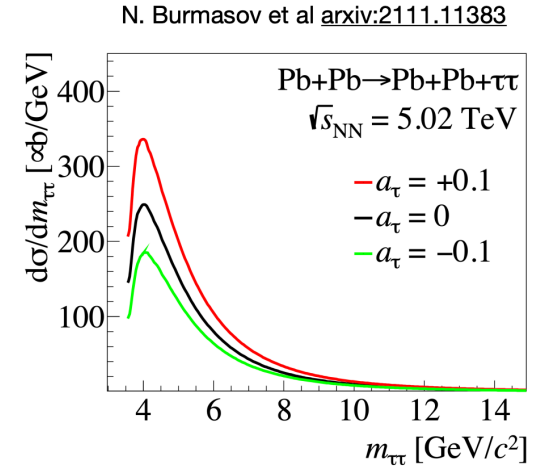
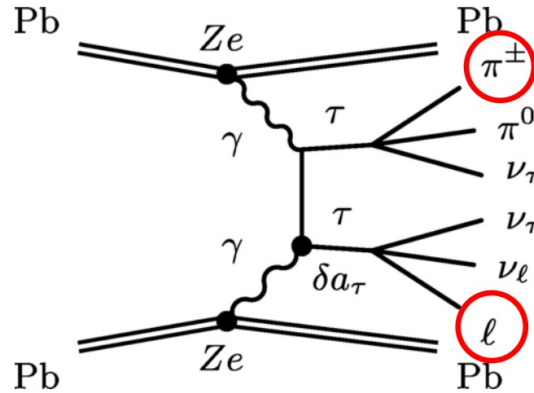
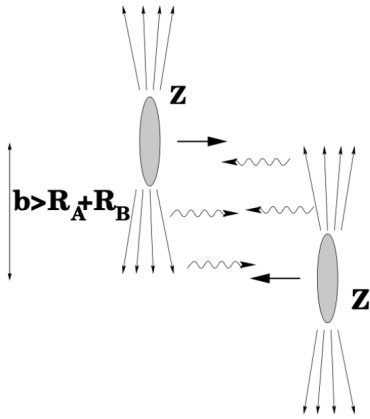
Prof. Gabriel González-Sprinberg



11:40 - 12:05

g-2 Tau Techniques

- Lifetime too short to store / track
- Instead, examining ultra peripheral Pb-Pb collisions, **coupling sensitive to a_τ**



Measurement of the tau-lepton pair production from photons and tau g-2

Wednesday

Quentin Buat

14:50 - 15:10

Measurement of the anomalous magnetic moment in ultraperipheral collisions with ALICE at the LHC

Paul Alois Buhler

Wednesday

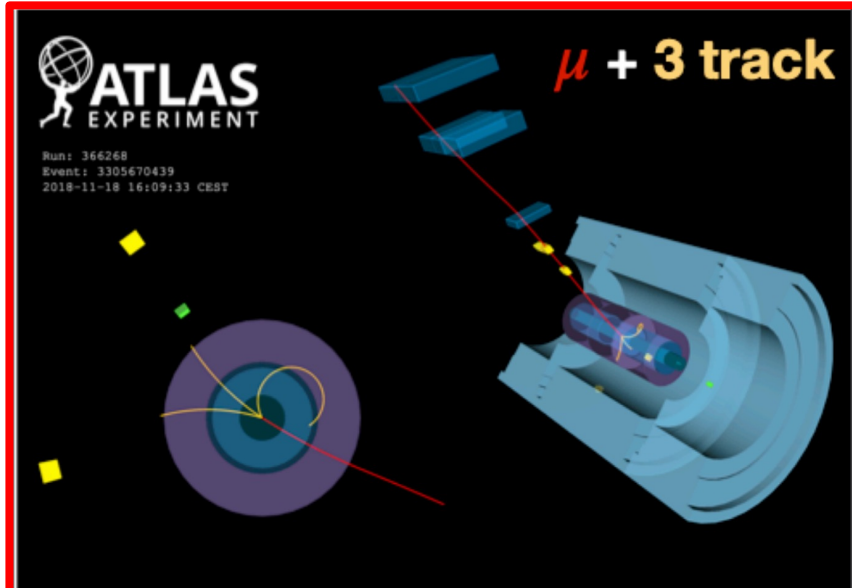
15:10 - 15:30



Event selection

- ATLAS: Focus on events with muon in final state $\mu + 1$ track or $\mu + 3$ track

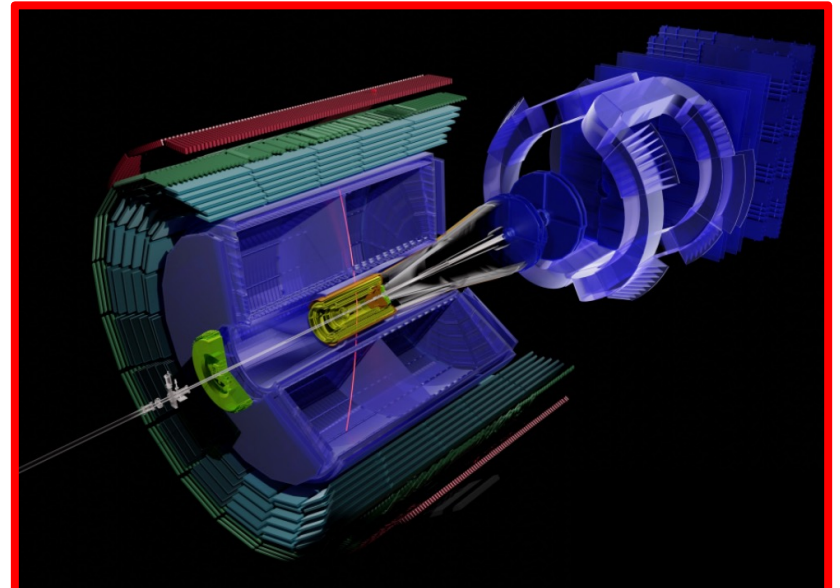
- ALICE: electron or muon and charged particle track
- Particle-ID capabilities \rightarrow enhanced sensitivity



Measurement of the tau-lepton pair production from photons and tau g-2

Quentin Buat

14:50 - 15:10



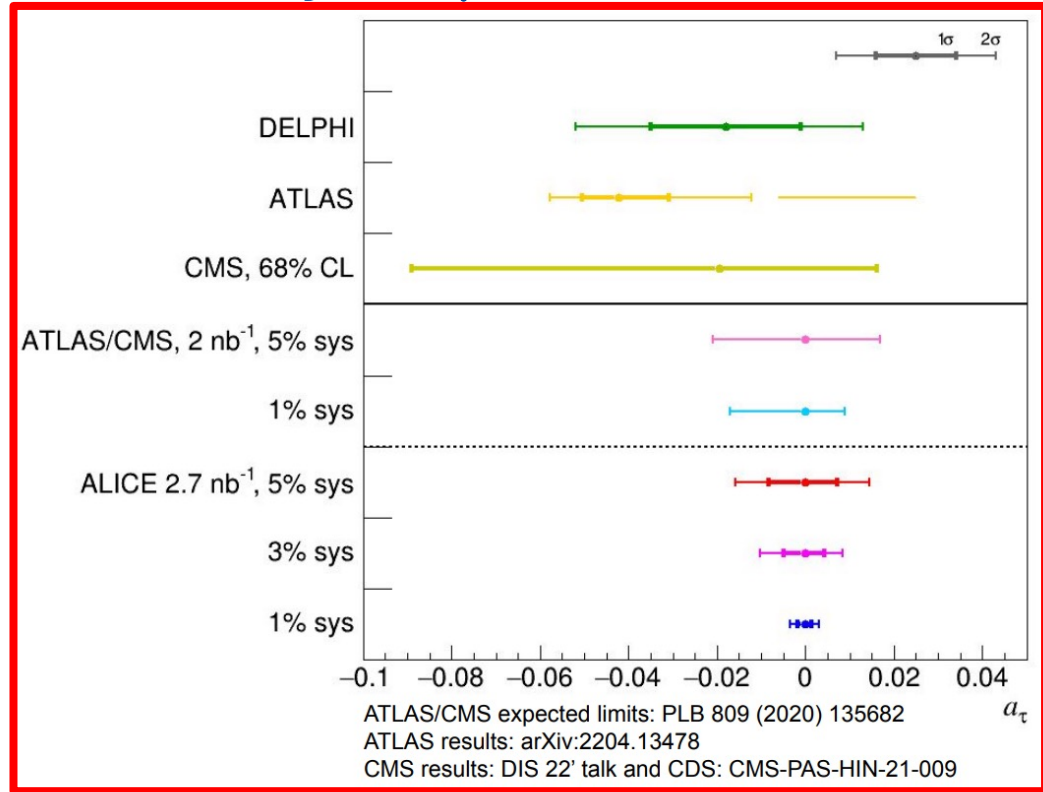
Measurement of the anomalous magnetic moment in ultraperipheral collisions with ALICE at the LHC

Paul Alois Buhler

15:10 - 15:30

LHC Run 3 will improve sensitivity to a_τ

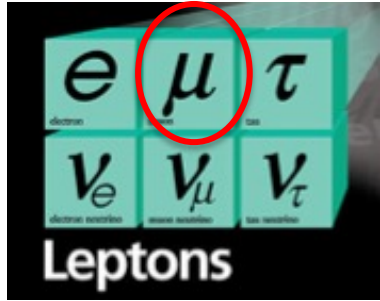
- Current results competitive with LEP
- Significant improvements coming in Run 3 analyses
- From this morning (Chiral Belle Upgrades – M. Roney) “Approaches the precision regime in tau that starts to be sensitive to Minimal Flavour Violation equivalent of muon $g-2$ anomaly”



Measurement of the anomalous magnetic moment in ultraperipheral collisions with ALICE at the LHC Paul Alois Bühler

Wednesday 15:10 - 15:30

The muon

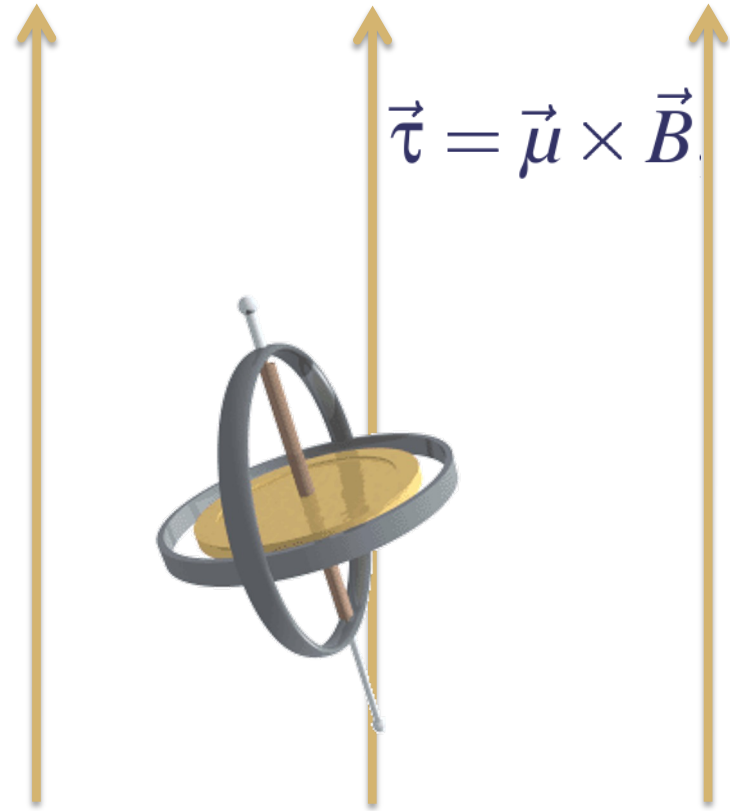


- Spin $\frac{1}{2}$, encodes information about spin in its decay

$$\vec{\mu} = g \frac{q}{2m} \vec{S}$$

- $g = 2$ + contributions from virtual particles

Magnetic Field



The muon

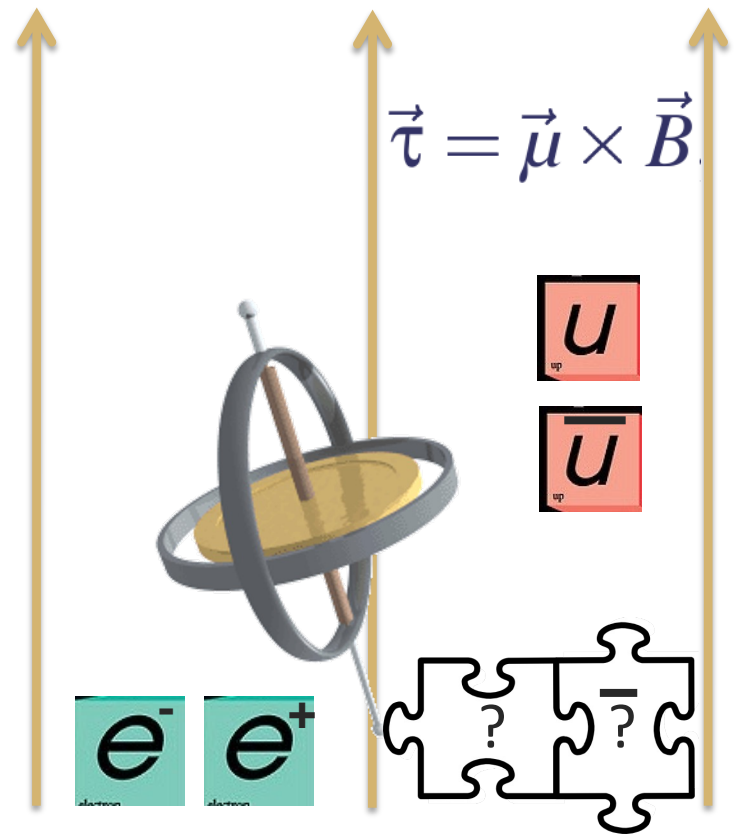


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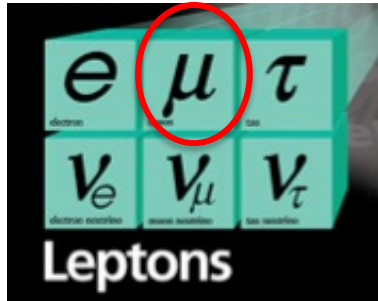
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Magnetic Field



The muon



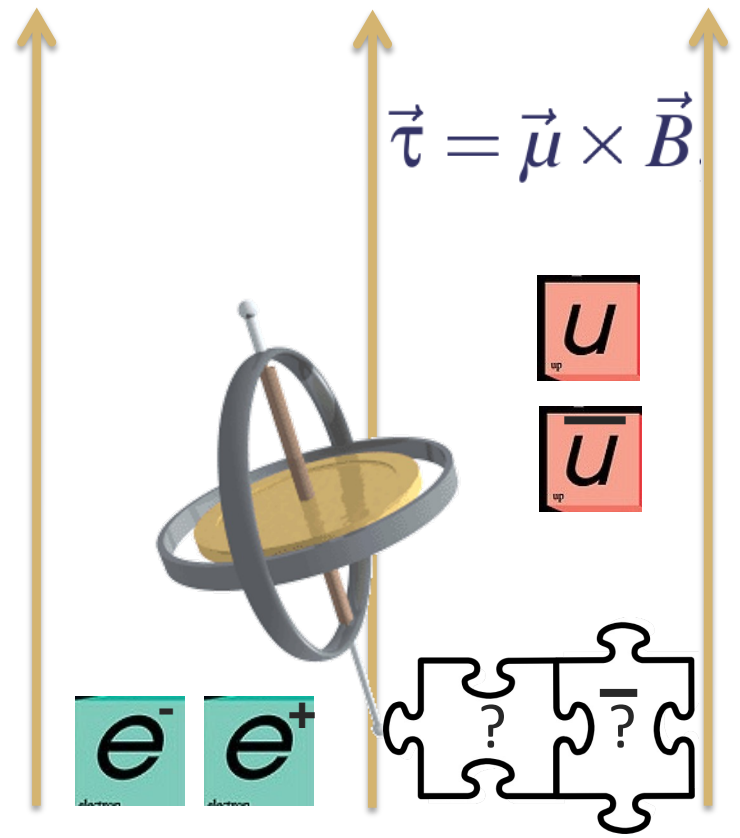
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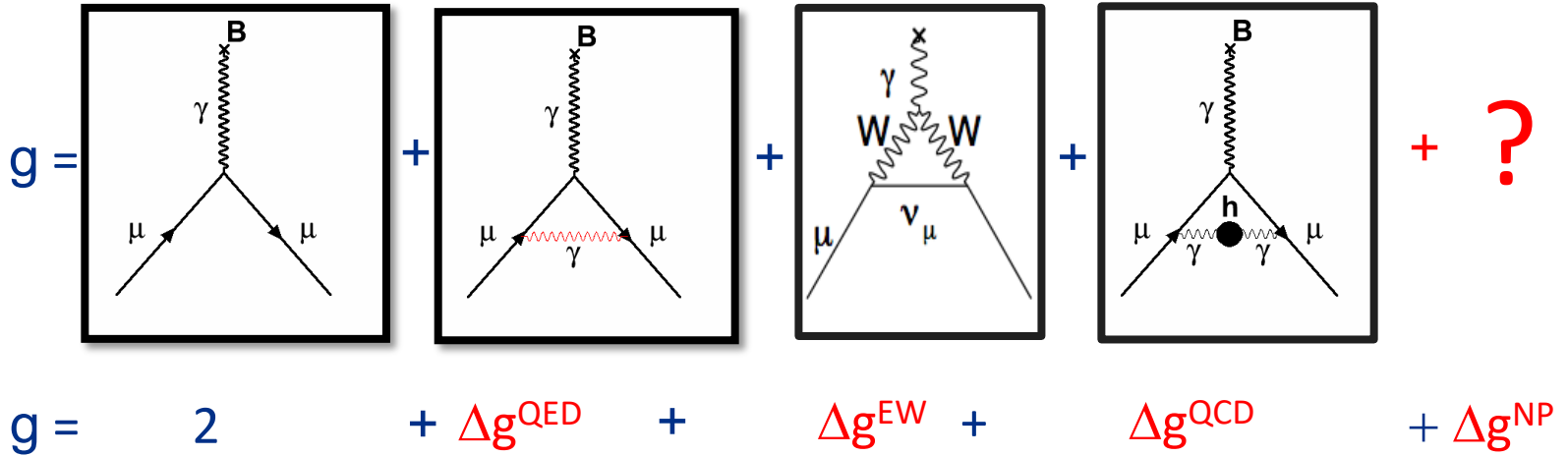
$m_{\mu} \sim 207 m_e$; $m_{\mu} \sim 0.06 m_{\tau}$
 $2.2 \mu\text{s}$ $\tau_{\mu} \sim 8 \times 10^6 \tau_{\tau}$
Goldilocks mass and lifetime to have sensitivity and store

Magnetic Field



Muon g-2: Motivation

$$\vec{\mu} = g \frac{q}{2m} \vec{S}$$



- a_μ is the **anomalous magnetic moment** (i.e the part that differs from 2)

$$a_\mu^{\text{SM}} = (g_\mu^{\text{SM}} - 2)/2 = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{QCD}} + a_\mu^{\text{NP}}$$

Determining a_μ from experiment

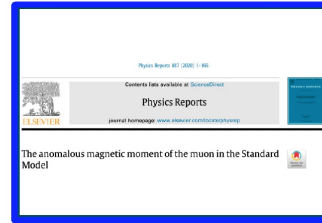
$$a_\mu^{exp} = \frac{m\omega_a}{eB}$$

Storage ring experiment

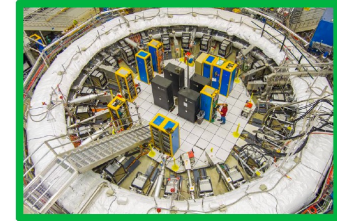
- Uniform, precisely measured B-field
- Measure muon precession in that field
- Weight by how muons sample that field in space and time

Outline

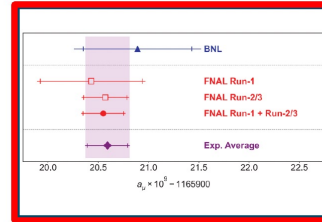
Theory Initiative White Paper 2020



2021 Run-1 results at Fermilab



Run-2/3 upgrades and 2023 results



Puzzles, prospects and outlook



LORENZO COTROZZI

12/05/2023 – TAU2023 – MUON $g - 2$

3



Measurement of the Muon Magnetic anomaly to 0.20 ppm by the Muon $g-2$ experiment at Fermilab

Lorenzo Cotrozzi

Tuesday

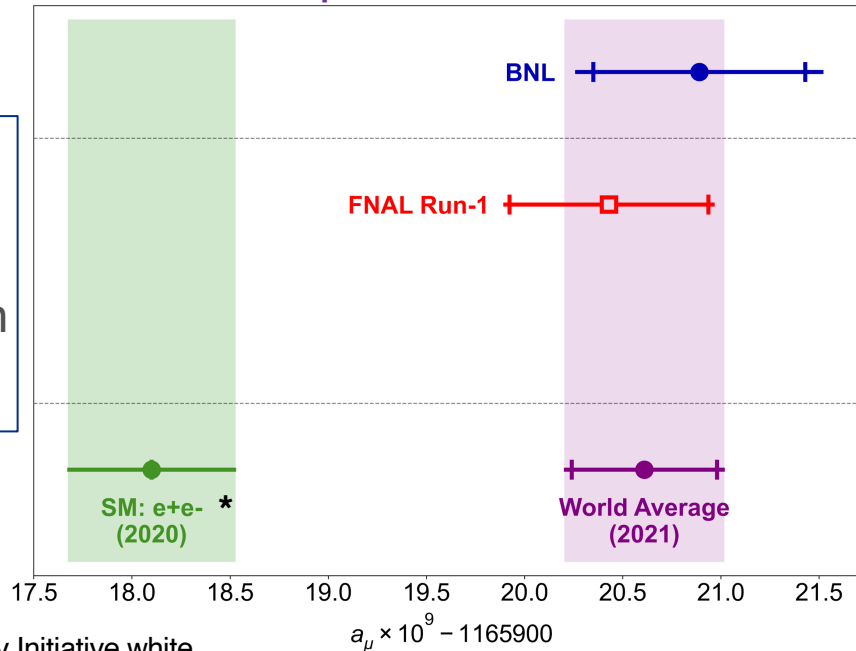
09:05 - 09:30

Starting Point: Run-1 Result

$$a_\mu(\text{FNAL; Run-1}) = 0.00\ 116\ 592\ 040(54) [463\ \text{ppb}]$$

$$a_\mu(\text{Exp}) = 0.00\ 116\ 592\ 061(41) [350\ \text{ppb}]$$

Complex theory situation → interpretation details later



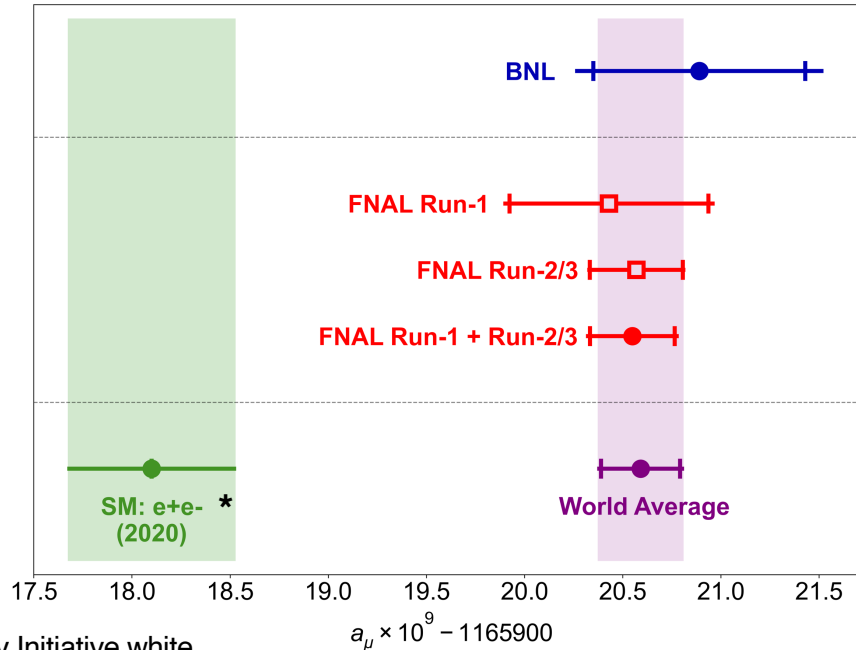
- 3.7σ discrepancy between BNL and WP 2020
- 4.2σ discrepancy between World Average 2021 and WP 2020

* Muon $g - 2$ Theory Initiative white paper (WP) value

<https://doi.org/10.1016/j.physrep.2020.07.006>

Run-2/3 Result: FNAL + BNL Combination

$$a_\mu(\text{FNAL}) = 0.00\ 116\ 592\ 055(24) [203\ \text{ppb}]$$



- FNAL combination: **203 ppb** uncertainty
- Both FNAL and BNL dominated by statistical error
- Combined world average **dominated by FNAL** values.

* Muon $g - 2$ Theory Initiative white paper (WP) value
<https://doi.org/10.1016/j.physrep.2020.07.006>

$$a_\mu(\text{Exp}) = 0.00\ 116\ 592\ 059(22) [190\ \text{ppb}]$$

Run-2/3 a_μ Uncertainties: Final Values

- Total uncertainty is **215 ppb**

[ppb]	Run-1	Run-2/3	Ratio
Stat.	434	201	2.2
Syst.	157	70	2.2

- Systematics of 70 ppb surpasses proposal goal (100 ppb)
- No dominant uncertainties to attack
- Modest improvements to field & beam dynamics possible

Quantity	Correction [ppb]	Uncertainty [ppb]
ω_a^m (statistical)	–	201
ω_a^m (systematic)	–	25
C_e	451	32
C_p	170	10
C_{pa}	-27	13
C_{dd}	-15	17
C_{ml}	0	3
$f_{\text{calib}} \langle \omega_p'(\vec{r}) \times M(\vec{r}) \rangle$	–	46
B_k	-21	13
B_q	-21	20
$\mu_p'(34.7^\circ)/\mu_e$	–	11
m_μ/m_e	–	22
$g_e/2$	–	0
Total systematic	–	70
Total external parameters	–	25
Totals	622	215

Wishlist : No surprises that cause systematic evaluation to increase

We can rewrite a_μ : our observables plus external measurements

Quantities FNAL
g-2 measures

$$a_\mu = \frac{\omega_a}{\tilde{\omega}'_p(T_r)} \frac{\mu'_p(T_r)}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}$$


Determined externally to 25 ppb,
Largest term is

$\frac{m_\mu}{m_e}$ Known to 22 ppb from muonium hyperfine splitting
Phys. Rev. Lett. **82**, 711 (1999)

Wishlist for 2025: Maximize precision on
inputs

MuSEUM in J-PARC

- ▶ Muonium Hyperfine splitting measurement

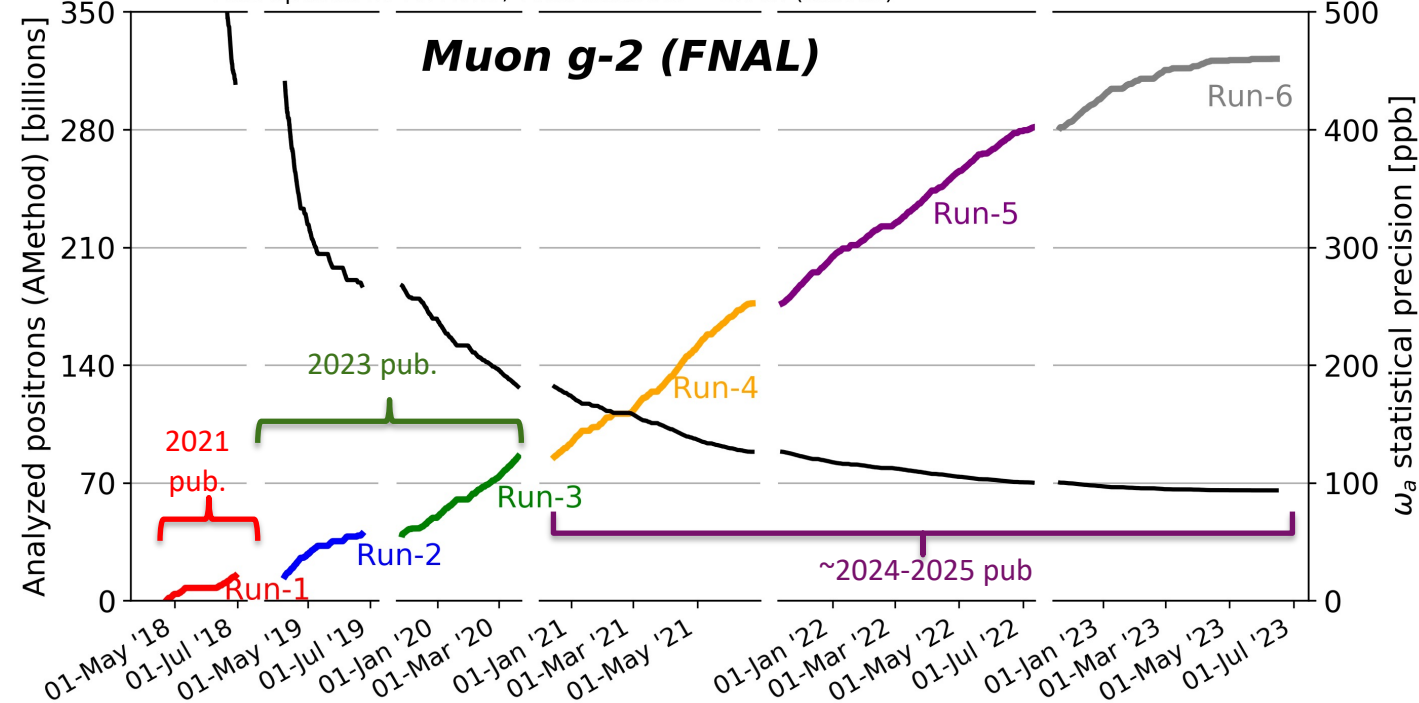


- MRI magnet moved to experimental area
- ▶ Feb. 2024: Shimming
- ▶ Mar. 2024: Beam Run (?)

Ken-ichi Sasaki

FNAL Muon g-2 Data Summary

Last update: 10-11-2023; Total statistics = 322.1 (billions)



- Wishlist for 2025:**
- Publish Run 4-6 analysis
 - Maintain systematic unc. of 70 ppb
 - Reduce total unc. by 35% (190 → 120 ppb)

- Statistical uncertainty should reach <100 ppb, the original proposal goal

Theory Initiative (TI)

Muon $g-2$ Theory Initiative

Sixth Plenary Workshop

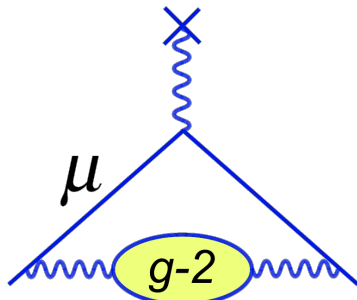
Bern, Switzerland, September 4–8, 2023



Thank you !



Local Organising Committee
Gilberto Colangelo (Chair)
Martin Hoferichter (Chair)
Bai-Long Hoid
Simon Holz
Gurtej Kanwar
Marina Marinković
Letizia Parrato
Peter Stoffer
Jan-Niklas Toelstede
Urs Wenger



On August 9, 2023, in view of the announcement of the new result by the Muon $g-2$ experiment at Fermilab scheduled for August 10, 2023, the Muon $g-2$ Theory Initiative has released the following statement summarizing the status of the Muon $g-2$ Theory in the Standard Model. It was updated on August 10, 2023 at 11:10 AM US CDT to reflect the new experimental average.

STATEMENT

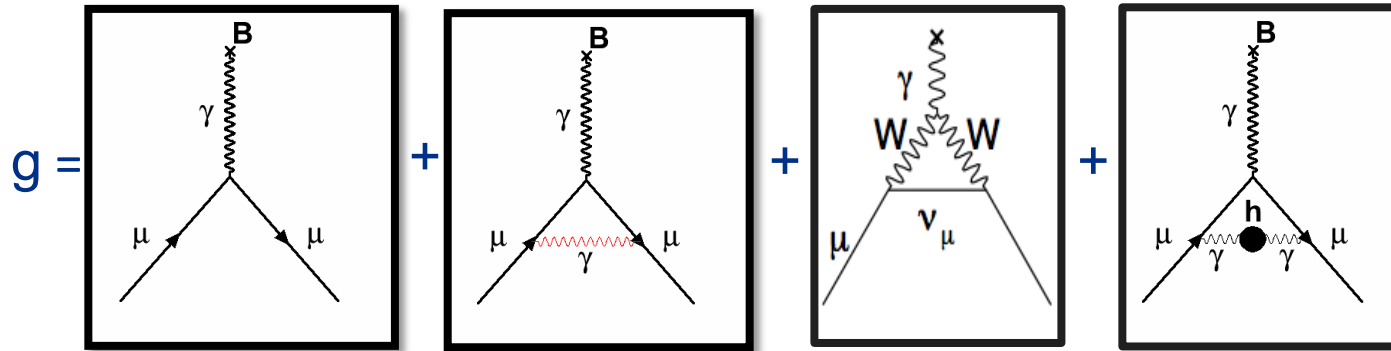
The Status of Muon $g-2$ Theory in the Standard Model

The Muon $g-2$ Theory Initiative

<https://muon-gm2-theory.illinois.edu/>



Muon g-2 calculation

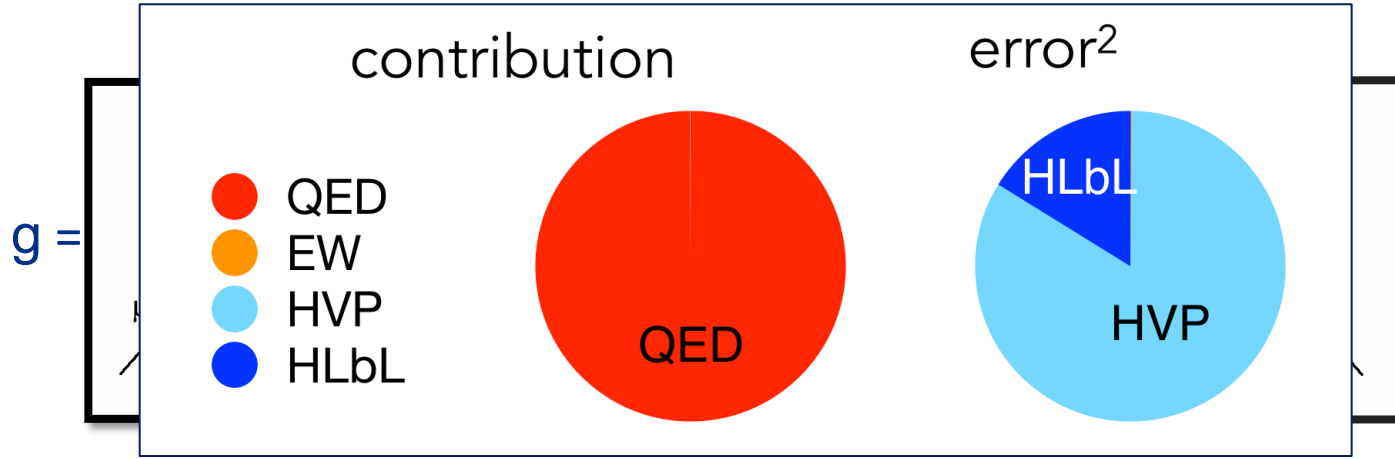


Value $g = 2 + O(10^{-3})_{\text{QED}} + O(10^{-9})_{\text{EW}} + O(10^{-7})_{\text{QCD}}$

Uncertainty (ppm) 0.001 , 0.01 , 0.34 (HVP) & 0.15 (HLBL)

Relative Uncertainty ~1% (HVP) ~20% (HLBL)

Muon g-2 calculation



Value $g = 2 + O(10^{-3})_{\text{QED}} + O(10^{-9})_{\text{EW}} + O(10^{-7})_{\text{QCD}}$

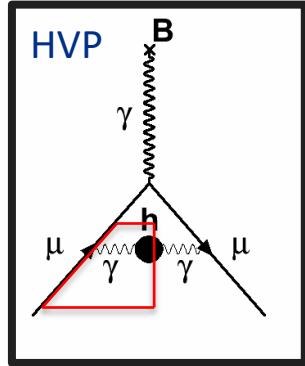
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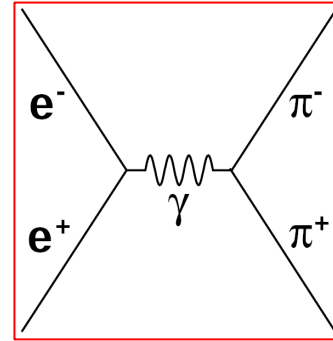
- Dominated by hadronic contributions → study those calculations in more detail

Dispersive Theory Calculation is Driven by Experimental Input

Relates these terms



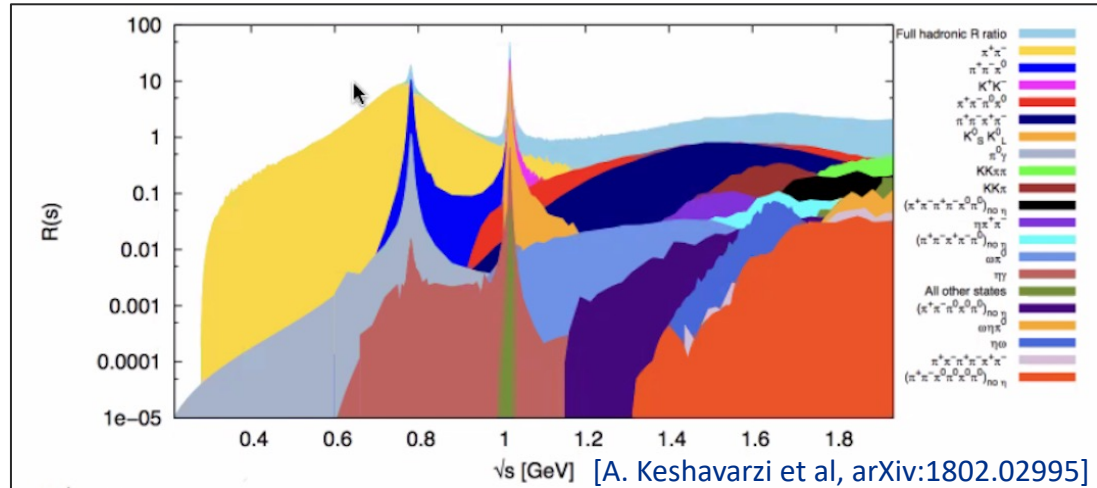
To observable processes like



$$(a_{\mu}^{\text{HAD,LO}}) \propto \int_{4m_{\pi}^2}^{\infty} ds \frac{K(s)}{s} R(s)$$

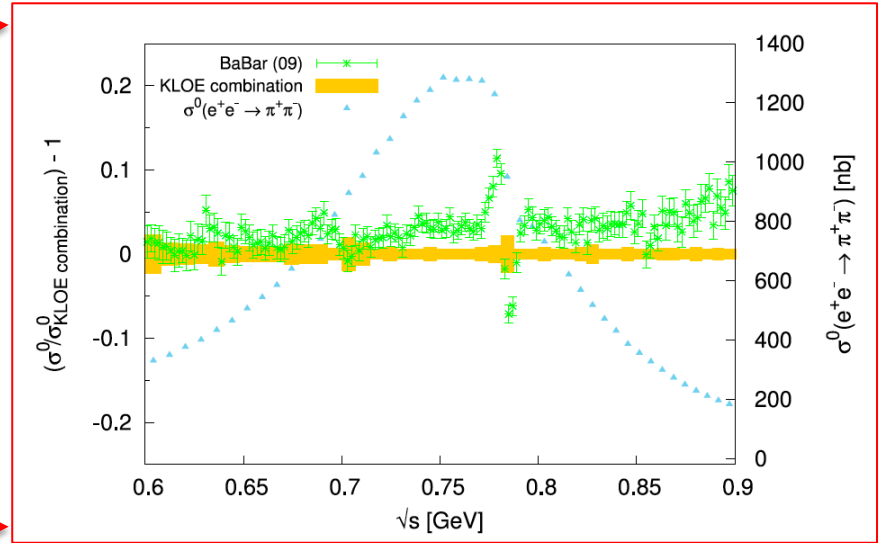
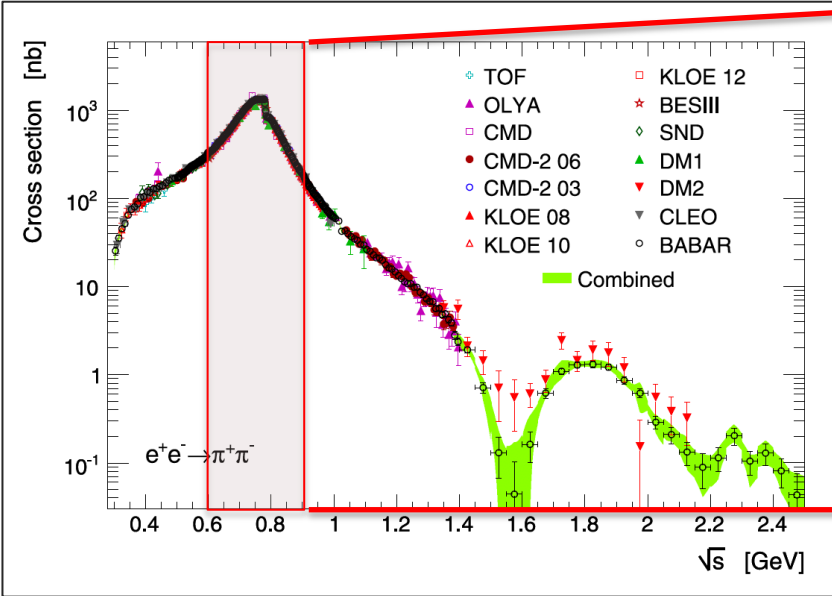
$$R(s) \equiv \frac{\sigma_{\text{tot}}(e^{+}e^{-} \rightarrow \text{hadrons})}{\sigma_{\text{tot}}(e^{+}e^{-} \rightarrow \mu^{+}\mu^{-})}$$

- Low-energy region dominates



Dispersive Theory Calculation is Driven by Experimental Input

Many detailed measurements of $e^+e^- \rightarrow \pi^+\pi^-$

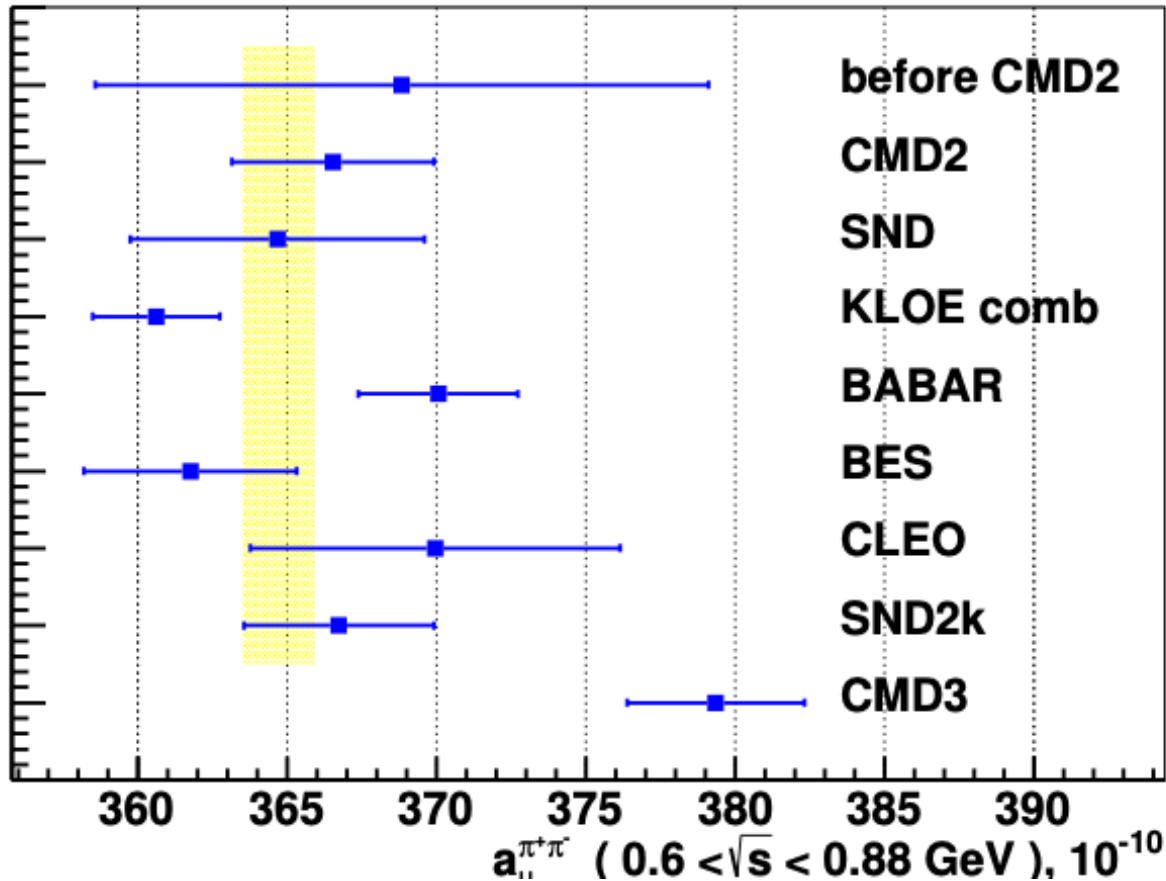


Spectral differences have limited the combination (recall, need percent level precision)

Evaluations inflate uncertainties to account for the tension \rightarrow has limited e^+/e^- prediction

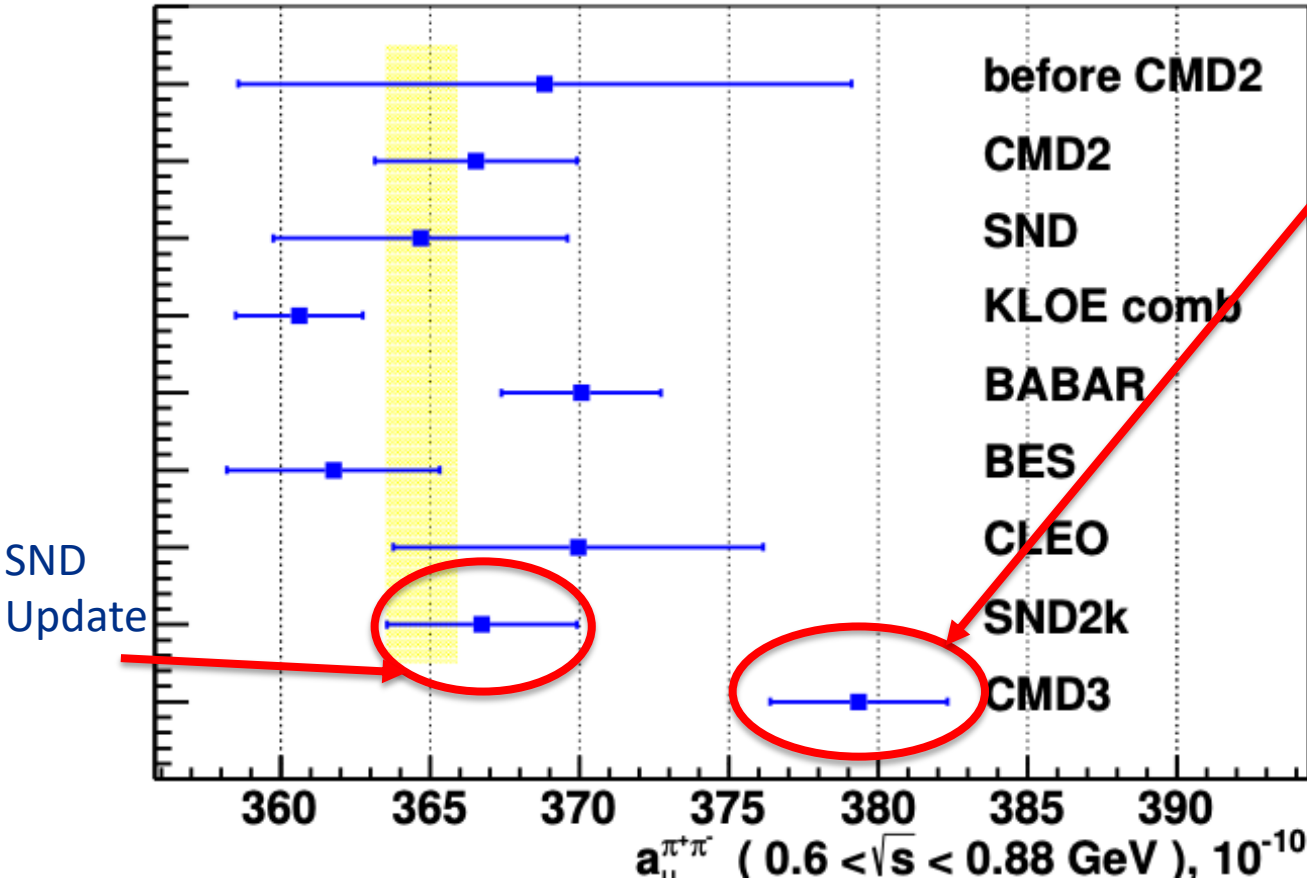
Wishlist for 2025: Understand spectral differences in $e^+e^- \rightarrow \pi^+\pi^-$

Various Evaluations of 2-pion contributions



New data further clouds interpretation

New from CMD-3
[arXiv:2302.08834](https://arxiv.org/abs/2302.08834)



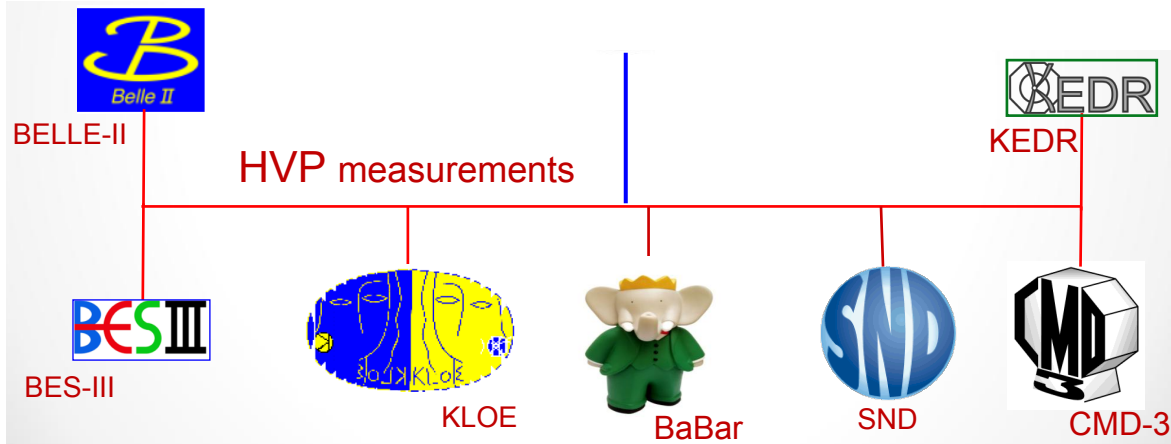
- Disagrees with others by 2.5-5 σ !
- Common facility w/ SND; some detector upgrades
- Analyzer seminar, community panels to investigate \rightarrow No smoking gun

Wishlist for 2025:
Understand why
CMD normalization
so different  Fermilab

Improved e^+e^- Prospects

Many machines/exp pushing to improve to sub % precision

BELLE-II:
362 /fb on
tape →
publish 2025



CMD-3:
continues to
investigate
differences

BESIII:
Pub: 2.9/fb
Data: 17.1 /fb
2024

KLOE: 7x larger
data set on
tape.
Blinded analysis

BaBar:
New analysis,
full data set in
2024

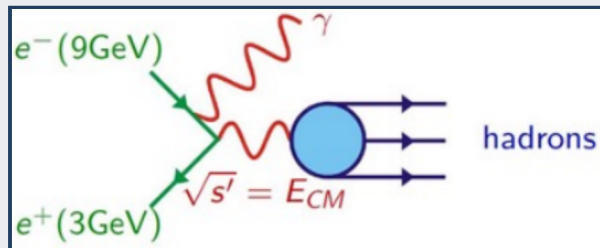
SND:
Pub 10% of data.
Full stats analysis
in prep

Wishlist for 2025: Use larger e^+e^- data sets to study tensions

Understanding NNLO ISR corrections in e⁺/e⁻ data from BaBar

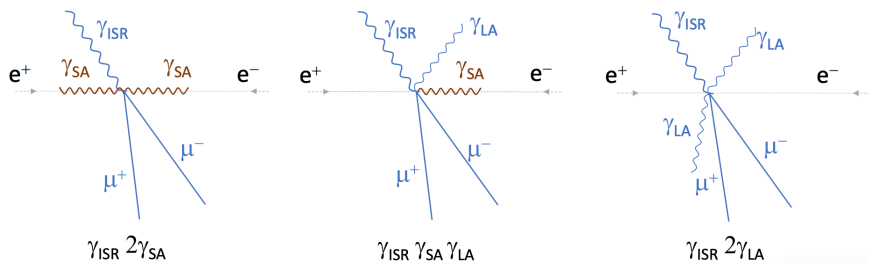
- ▶ *BABAR* measured $\sigma[e^+e^- \rightarrow \pi^+\pi^-(\gamma)]$ in 2009 with ISR technique and is working on $\sigma[e^+e^- \rightarrow \pi^+\pi^-(\gamma)]/\sigma[e^+e^- \rightarrow \mu^+\mu^-(\gamma)]$ with μ/π separation without PID

ISR technique



- ▶ measure $\sigma(e^+e^- \rightarrow \text{hadrons})(s)$ by measuring $\sigma(e^+e^- \rightarrow \gamma_{\text{ISR}} + \text{hadrons})[\Upsilon(4s)]$

NNLO



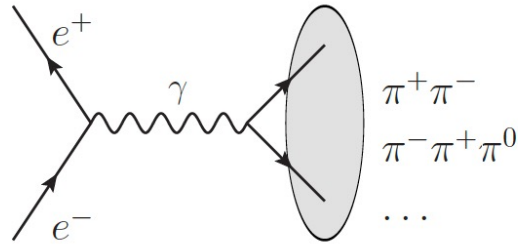
- ▶ NNLO radiation with ISR photon plus two additional radiation photons observed for the first time
fraction = $(3.47 \pm 0.38)\%$ for muons and $(3.36 \pm 0.39)\%$ for pions
- ▶ permits subtracting NNLO feed-through contributions to NLO samples

Study of additional radiation in the initial-state-radiation processes $e^+e^- \rightarrow \mu^+\mu^-\gamma$ and $e^+e^- \rightarrow \pi^+\pi^-\gamma$ in the BABAR experi...

Alberto Lusiani

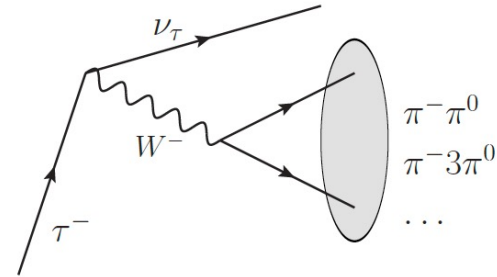
Friday

Tau Data inputs to a_μ^{HVP}



EM current

Final states $I = 0, 1$ neutral



$V - A$ current

Final states $I = 1$ charged

LEP and b-factories provide high-statistic tau decay samples
Can relate $\tau^- \rightarrow \pi^0 \pi^- \nu$ to $e^+e^- \rightarrow \pi^+ \pi^-$ with difficult isospin corrections

Tau Data inputs to a_μ^{HVP}

a_μ^{HVP} in the SM: Our τ -data based prediction

Miranda-Roig'20

$$a_\mu^{\text{HVP,LO}} = \frac{1}{4\pi^3} \int_{s_{thr}}^{\infty} ds K(s) \sigma_{e^-e^+ \rightarrow \text{hadrons}}(s)$$

Both K & σ go as $1/s$ enhancing low-E contributions

(Alemany, Davier, Höcker '97)

Alternative evaluation possible using semileptonic tau decay data, specifically 2π (4π) channel. Requires isospin breaking (IB)

$$\sigma_{\pi\pi}^0 = \left[\frac{K_\sigma(s)}{K_\Gamma(s)} \frac{d\Gamma_{\pi\pi[\gamma]}}{ds} \right] \frac{R_{IB}(s)}{S_{EW}}, \quad \longrightarrow \quad R_{IB}(s) = \frac{FSR(s)}{G_{EM}(s)} \left(\frac{\beta_{\pi^+\pi^-}^3}{\beta_{\pi^+\pi^0}^3} \left(\frac{F_V(s)}{f_+(s)} \right)^2 \right)$$

Kinematics & global cts. Measurement Short-distance EW RadCor

Kinematics (Cirigliano-Ecker-Neufeld '01)

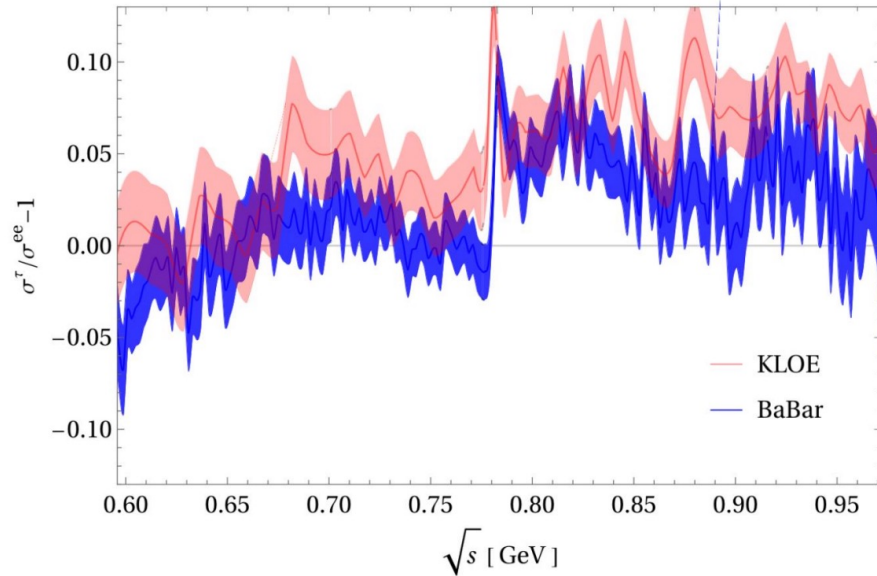
The ratio of neutral to charged current di-pion form factors (F_V/f_+) and the long-distance em RadCor (G_{EM}) are challenging.

Highlighted challenging isospin breaking term

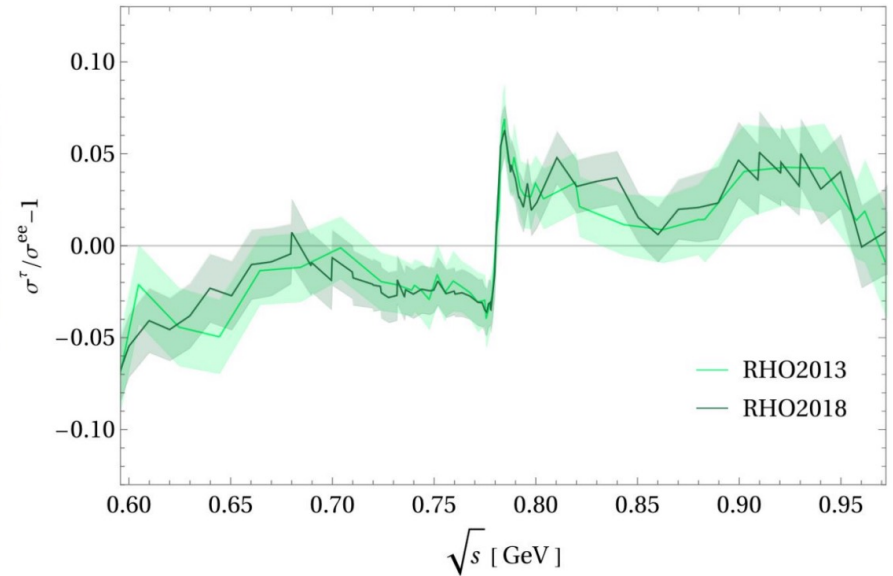
Pablo Roig (Cinvestav, Mexico City)

Spectral ratios of $\sigma^\tau / \sigma^{ee}$ show tension

Ratio $\sigma^\tau / \sigma^{ee}$ KLOE & Babar Masjuan-Miranda-Roig'23



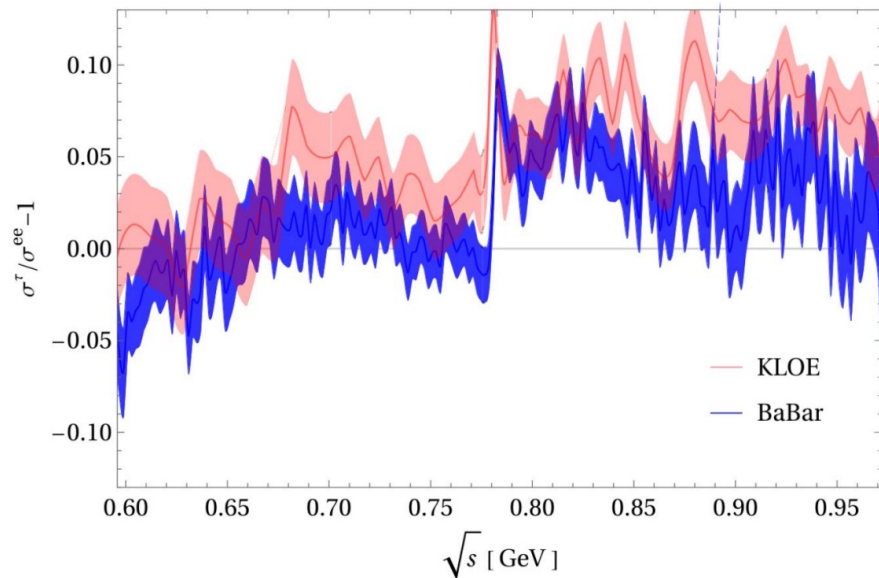
Ratio $\sigma^\tau / \sigma^{ee}$ CMD



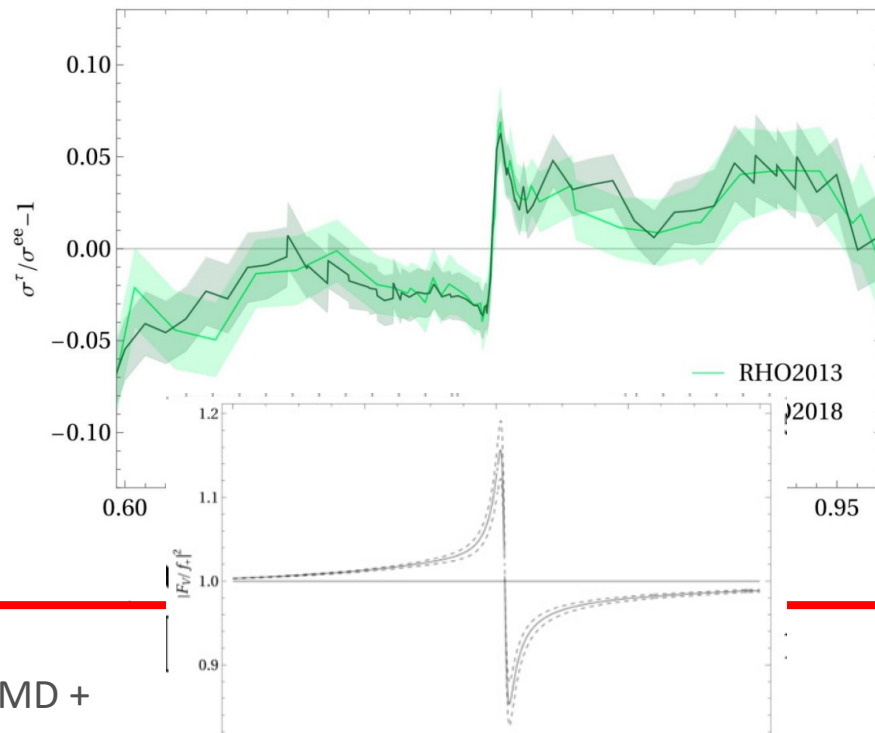
Need to determine integral of these σ to percent-level
Shape of the isospin-breaking correction shows up in CMD +
Babar ratios

Spectral ratios of $\sigma^\tau / \sigma^{ee}$ show tension

Ratio $\sigma^\tau / \sigma^{ee}$ KLOE & Babar Masjuan-Miranda-Roig'23



Ratio $\sigma^\tau / \sigma^{ee}$ CMD

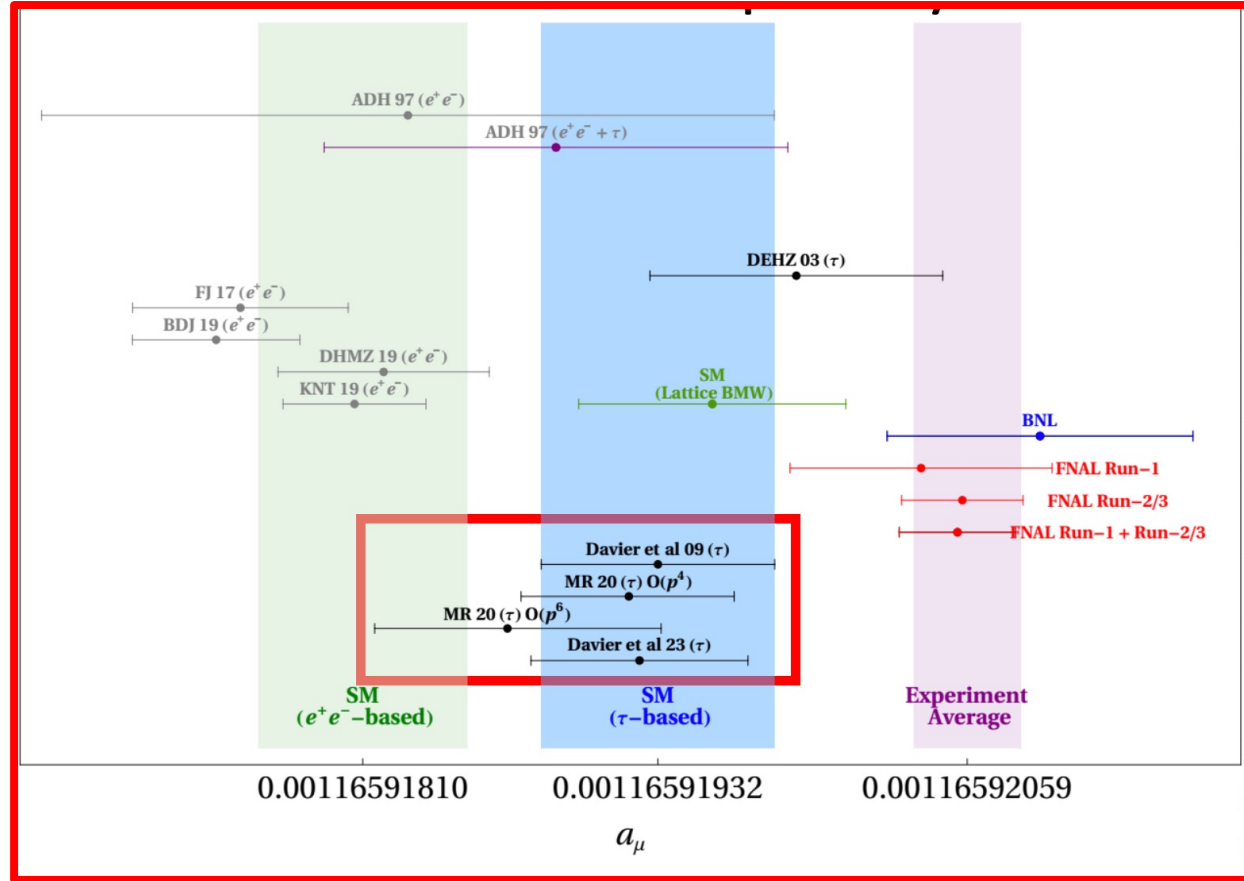


Need to determine integral of these σ to percent-level
Shape of the isospin-breaking correction shows up in CMD +
Babar ratios

Wishlist for 2025: Understand impact of isospin corrections on spectral shape above/below rho-omega mixing ... can Lattice QCD weigh in?

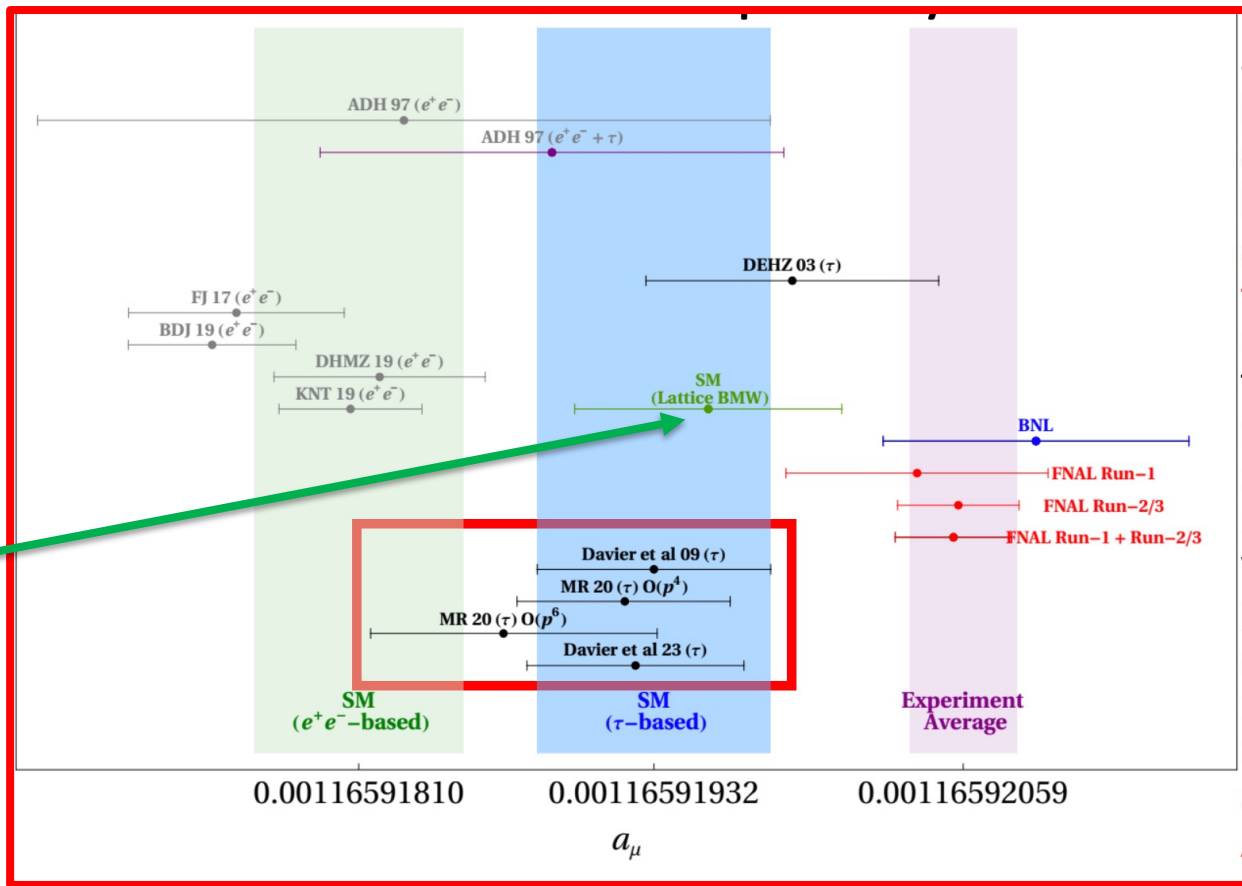
Tau Data inputs to a_μ^{HVP}

- Landscape of a_μ^{HVP} in flux
- Lots to understand in terms of spectral and absolute variations in $e^+ e^-$ and τ data



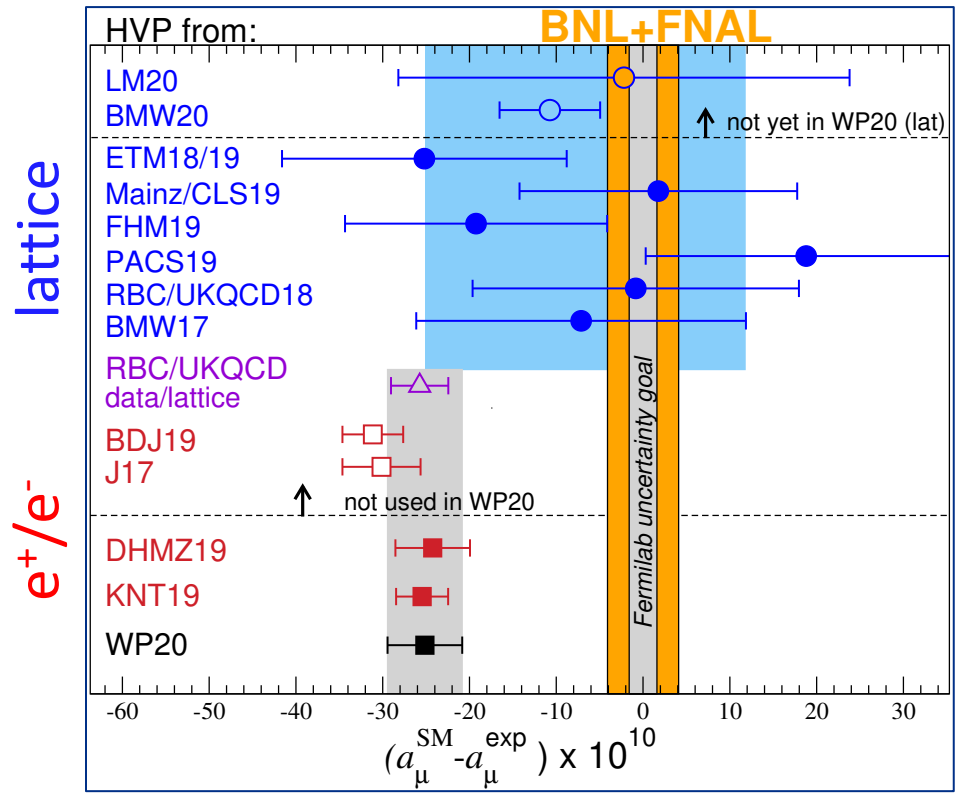
Tau Data inputs to a_μ^{HVP}

- Landscape of a_μ^{HVP} in flux
- Lots to understand in terms of spectral and absolute variations in $e^+ e^-$ and τ data ... as well as lattice...



a_μ^{SM} determined using HVP from lattice QCD or **dispersive calc**

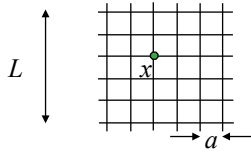
- In 2020 the first high-precision lattice QCD result came out: **BMW**
- Showed significant tension with **e^+/e^- evaluation**, much closer to experiment



Lattice QCD Introduction

- Provides alternative method of calculating hadronic contributions
- Maps Minkowski spacetime \leftrightarrow Euclidean space

• Direct calculation using Euclidean Lattice QCD



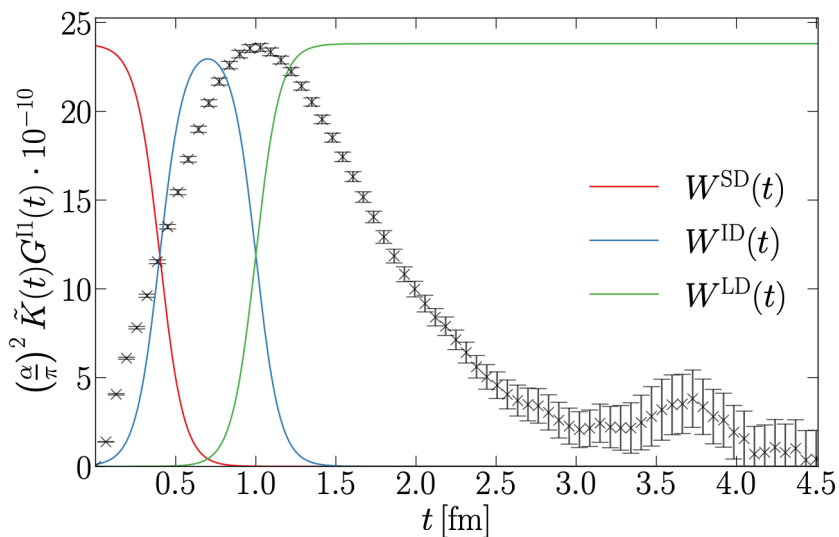
Approximations:
discrete space-time (spacing a)
finite spatial volume (L), and time extent (T)
...

Integrals are evaluated numerically using Monte Carlo methods.

Extrapolate:

- Lattice spacing $a \rightarrow 0$
- Finite volume, time: $L \rightarrow \infty$, $T > L$
- Quark masses, $m \rightarrow$ physical masses

Different windows in Euclidean time are sensitive to different systematics



- Enables comparisons between groups in each window
- Short Distance (SD) $t: 0 \rightarrow t_0$
- Intermediate (W) $t: t_0 \rightarrow t_1$
- Long Distance (LD) $t: t_1 \rightarrow \infty$

- Systematics vary for different windows
 - SD \rightarrow discretization
 - LD \rightarrow finite volume / stats

Hadronic vacuum polarization contribution to the muon $g-2$ from lattice QCD

Friday

Simon Kuberski

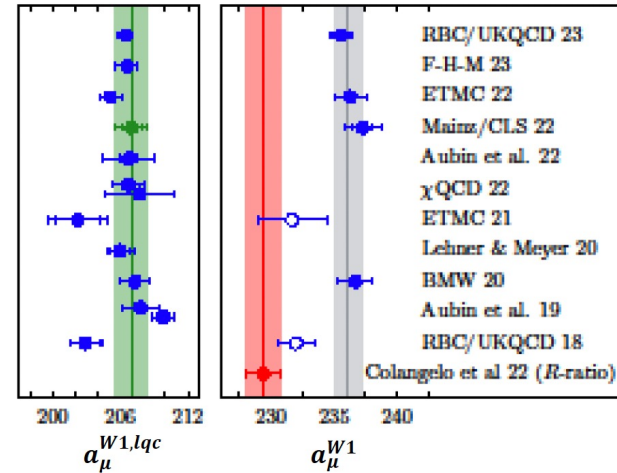
10:50 - 11:15

Intermediate Window Benchmark

- **Contributes 1/3** of the LO HVP contribution
- Systematic uncertainties are smaller
- Dispersive data can be mapped to the Euclidean space

- The full intermediate window a_μ^{W1}

H. Wittig, EW Moriond 2306.04165

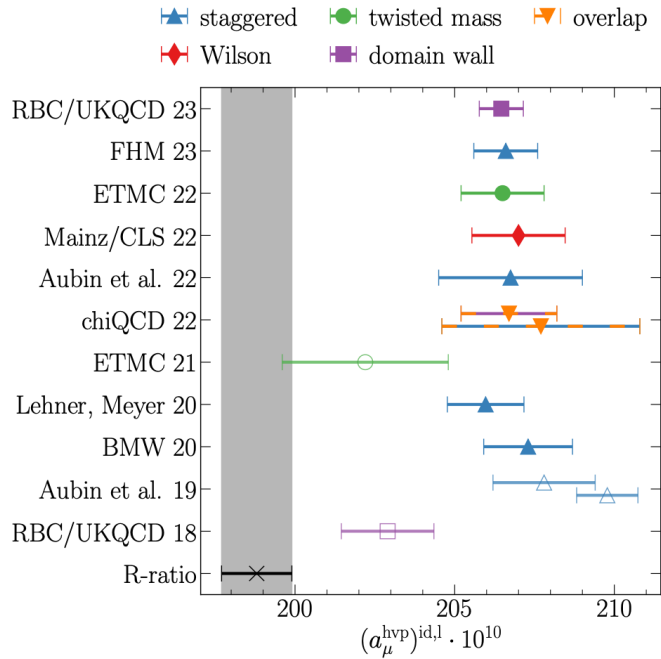


Data-driven determinations of light-quark-connected and strange-plus-disconnected window contributions to a_μ
Kim Maltman

Tuesday

Status Intermediate window 2023

THE INTERMEDIATE-DISTANCE WINDOW



- BY 2023, many groups have results in this window with $<1\%$ precision
- Several groups include sub-leading contributions to a_μ^{HVP} , all in good agreement
- $\sim 4\sigma$ discrepancy with the r-ratio data
- Explains about 50% of the overall discrepancy between BMW and dispersive data
- In this window, where the lattice systematics are well-controlled, lattice QCD predicts significantly larger quark contribution to a_μ than the e+/e- data

Lattice Wishlist for Tau 2025

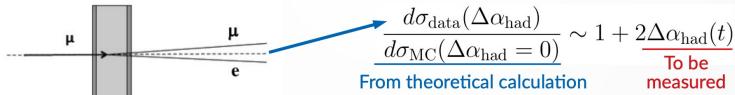
- Understand the 4σ discrepancy in the intermediate window between lattice QCD & $e^+e^- \rightarrow \pi^+ \pi^-$ r-ratio evaluation
- Develop multiple comparisons in the long-distance window
 - LD window contributes 2/3 of the total HVP
 - Has trickier finite-volume systematics
 - Statistically limited
- Achieve multiple, full evaluations of a_μ^{HVP}

Additional Experimental handle on HVP: MUonE at CERN

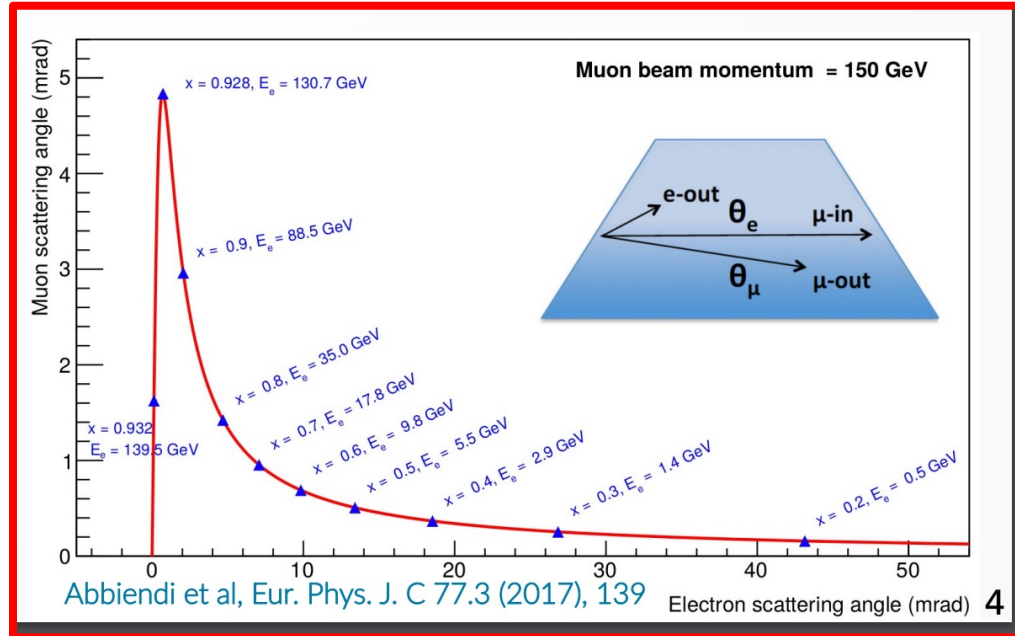
- A novel approach to determine the leading hadronic contribution via a high-precision shape measurement of the differential cross section of μe elastic scattering

$$a_{\mu}^{HLO} = \frac{\alpha_0}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{had}[t(x)]$$

Extraction of $\Delta\alpha_{had}(t)$ from the **shape** of the $\mu e \rightarrow \mu e$ differential cross section



- Precision tracking off of target via silicon strip detectors
- Correlation between muon and electron angle
- Compute a_{μ}^{HLO} from 1 experiment
- Final Goal: 3 years of running \rightarrow 0.3% precision on a_{μ}^{HLO}



An alternative evaluation of the leading-order hadronic contribution to the muon g-2 with MUonE

Riccardo Pilato

Tuesday

09:55 - 10:20

MUonE

- 3 weeks Test Run 2023: proof of concept of the experimental proposal. Data analysis ongoing. Request for a longer commissioning run in 2025 instrumenting more tracking stations.
- Full apparatus (40 stations) after CERN Long Shutdown 3 (2026-28) to achieve the target precision ($\sim 0.3\%$ stat and similar syst).
- Alternative method to calculate a_μ^{HLO} with MUonE data: less sensitive to the parameterization chosen to model $\Delta\alpha_{\text{had}}(t)$ in the MUonE kinematic range. Comparable uncertainty to the space-like integral method.

23

Wishlist for Tau2025

- Full proposal developed
- Commissioning run (2025) with scaled down detector

An alternative evaluation of the leading-order hadronic contribution to the muon g-2 with MUonE

Riccardo Pilato



Tuesday

09:55 - 10:20

JPARC Muon g-2 & EDM

Novel g-2 approach

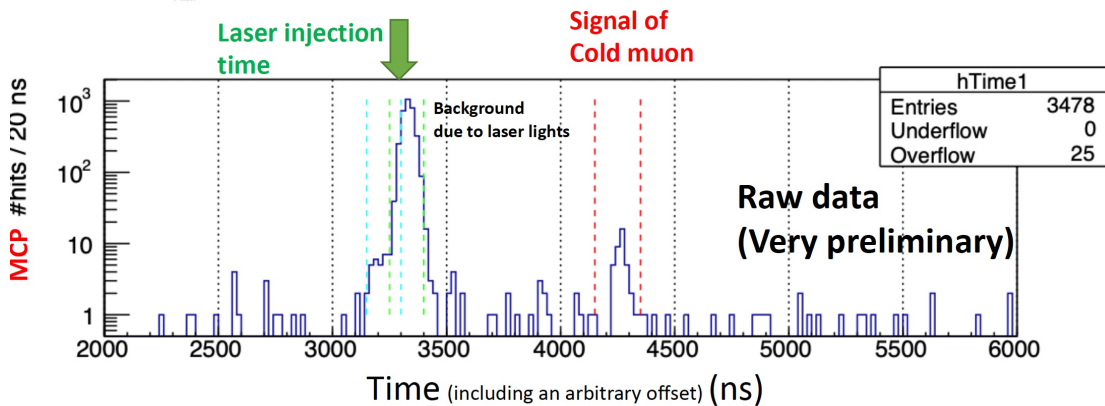
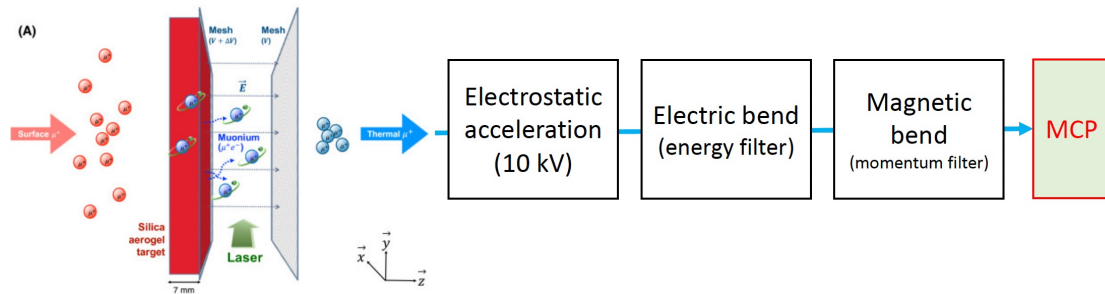
Ideal for pushing Muon EDM limits

Experiment adopts new method (different systematics):

- Low-emittance beam (cooling+ acceleration)
- Compact storage ring
- Very weak magnetic focusing

Muon cooling test (since Feb 2023)

17



Measurement of muon g-2 and EDM at J-PARC

Tuesday

Tsutomu Mibe

09:30 - 09:55



JPARC Muon g-2 & EDM

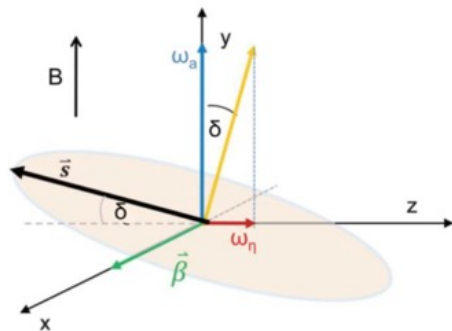
JFY	2022	2023	2024	2025	2026	2027	2028 and beyond	
KEK Budget								
Surface muon	✓ Beam at H1 area				★ Beam at H2 area			
Bldg. and facility				★ Final design				★ Completion
Muon source	✓ Ionization test @S2					★ Ionization test at H2		
LINAC			★ 80keV acceleration @S2			★ 4.3 MeV @ H2	★ fabrication complete	
Injection and storage			★ Completion of electron injection test				★ 210 MeV muon injection	
Storage magnet				★ B-field probe ready				★ Install ★ Shimming done
Detector			★ Quater vane prototype			★ Mass production ready	★ Installation	
DAQ and computing			★ grid service open ★ common computing resource usage start			★ small DAQ system operation test	★ Ready	
Analysis						★ Tracking software ready	★ Analysis software ready	

Commissioning
Data taking

Wishlist for Tau2025:

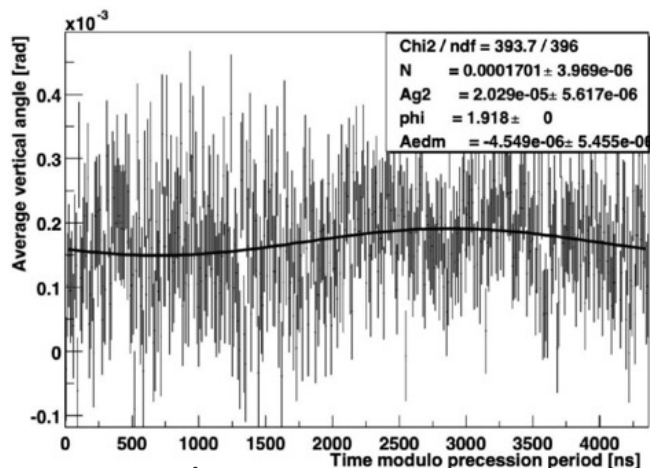
- Continued ramp up of JPARC support
- Progress on the muon source, cooling, accelerator and detectors!

Searching for NP within Fermilab Muon g-2 (Muon EDM)



- Presence of a muon EDM would tilt precession plane

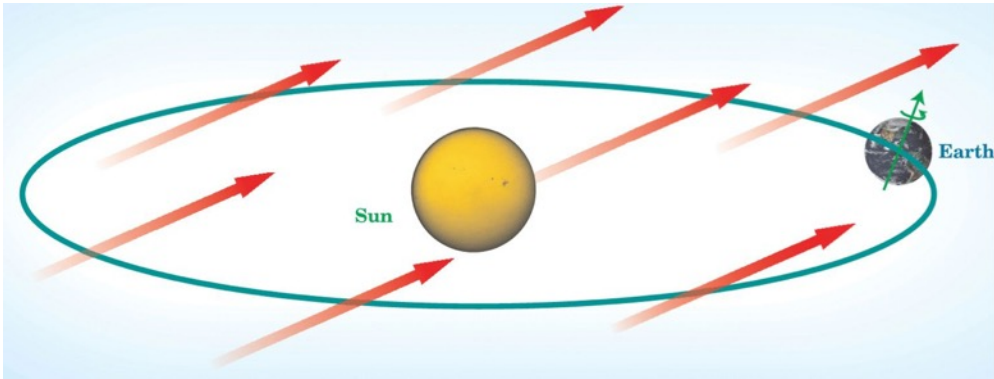
$$\vec{\omega}_{a\eta} = a_\mu \frac{e}{m} \vec{B} + \eta \frac{e}{2m} \left[\frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} \right]$$



BNL data

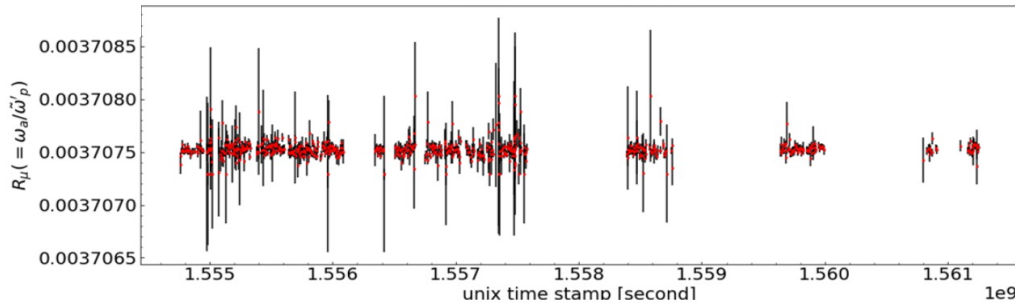
- Look for a rotation of muon precession out of the plane, oscillating out of phase with the g-2 wiggle. Requires:
 - precision pitch angle of decay electron
 - Tracker alignment and acceptance
 - Knowledge of vector components of the magnetic field
- **Run 1/2/3 analysis nearing completion (still blind)**
 - Statistical error dominated
 - Anticipated sensitivity $|d_\mu| \sim 5 \times 10^{-20} \text{ e}\cdot\text{cm}$
 - $\sim 4x$ better than current BNL limit of $|d_\mu| < 1.9 \times 10^{-20} \text{ e}\cdot\text{cm}$
- At least 4x statistics on tape $\rightarrow \sim 2 \times 10^{-20} \text{ e}\cdot\text{cm}$ ultimate limit

Searching for NP within Fermilab Muon g-2 data (CPT/LV)



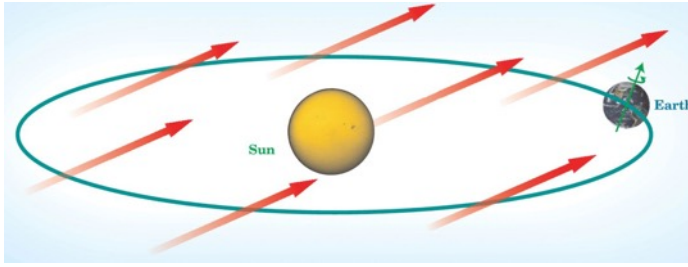
$$\mathcal{L}' = -a_\kappa \bar{\psi} \gamma^\kappa \psi - \underbrace{b_\kappa}_{\text{CPT/LV}} \bar{\psi} \gamma_5 \gamma^\kappa \psi - \frac{1}{2} H_{\kappa\lambda} \bar{\psi} \sigma^{\kappa\lambda} \psi + \frac{1}{2} i c_{\kappa\lambda} \bar{\psi} \gamma^\kappa \overleftrightarrow{D}^\lambda \psi + \frac{1}{2} i d_{\kappa\lambda} \bar{\psi} \gamma_5 \gamma^\kappa \overleftrightarrow{D}^\lambda \psi$$

Run 2 Data



- Lorentz-violating extensions (e.g. [Kostelecký et al.](#)) to the SM include terms with CPT/Lorentz violating signatures for our data
- Signals
 - Sidereal oscillation in ω_a ($T = 23\text{hr } 56\text{min}$)
 - $a(\mu^+) - a(\mu^-)$
 - Global fits to BNL/FNAL
- Improvements/complementarity to BNL
 - >20 x statistics w/ reduced systematics
 - Longer lever arm (ran for ~ 36 mos over 6 years compared to ~ 9 mos over 3 at BNL)
 - Different latitude
- Expecting > 4x improvement

Searching for NP within Fermilab Muon g-2 data (Dark Matter)

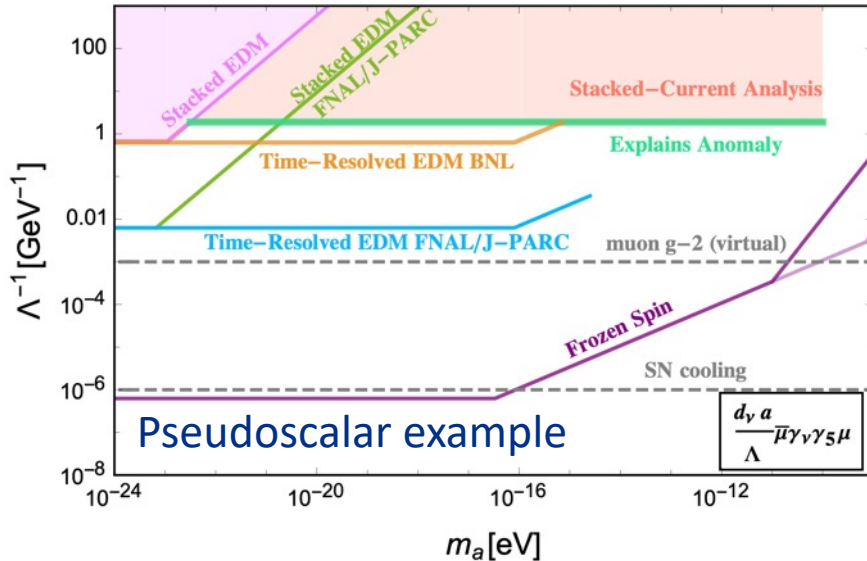


- Coherent DM interactions can exert a spin torque and cause an oscillation in a_μ or the EDM signal
- Similar to sidereal variation analysis but the period now depends on the m_{DM}

$$\vec{\omega}_a(t) = \omega_{\text{sm}} \hat{z} + \vec{\omega}_{\text{dm}}(t) \quad \vec{\omega}_{\text{dm}} \approx -\frac{a_0}{\Lambda} m_a \vec{v} \sin(m_{\text{dm}} t)$$

- Stacked plots are sensitive to overall shift in ω_a , but time-resolved analysis needed for ultimate sensitivity

- Precision analyses underway of a_μ vs time ($t=100\text{ms} \rightarrow 5 \text{ years}$)



Ryan Janish, Harikrishnan Ramani
PRD 102, 115018 (2020)

Wishlist Summary for Tau 2025

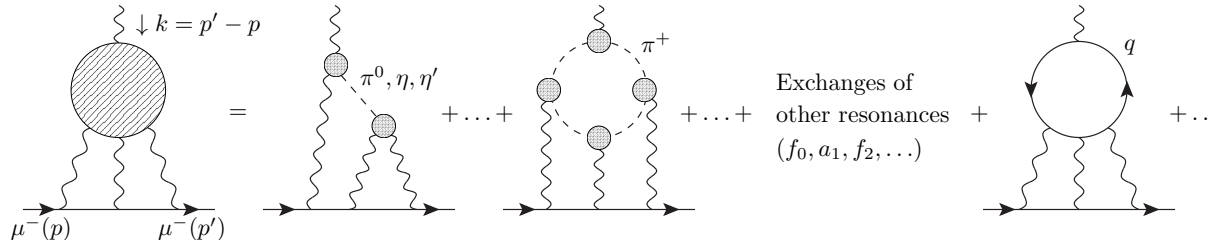
- **Muon g-2 Experiment**
 - Publish Run 4-6 analysis
 - Maintain systematic uncertainty of 70 ppb (No surprises!)
 - Reduce total uncertainty on a_μ^{exp} by 35% (190 ppb \rightarrow 120 ppb)
 - Publish companion EDM + CPT/LV & DM searches
- **MUonE**
 - Complete a fully developed proposal for physics run after long shutdown
 - Achieve first commissioning run (2025) w/ scaled down detector
- **JPARC g-2 / EDM effort**
 - Develop novel experimental method to determine a_μ with different systematic effects
 - Achieved demonstration of mature muon source, cooling, acceleration with launch of detector production

Wishlist Summary for Tau 2025

- Theory

- Understand spectral differences in $e^+e^- \rightarrow \pi^+ \pi^-$
- Understand why CMD-3 normalization so different from KLOE/BaBar/CMD-2
- Update results from KLOE, BABAR, BELLE-II, CMD,... and the corresponding dispersive evaluations
- Understand impact of isospin corrections on spectral shape of τ data above and below the rho-omega mixing: Can lattice QCD weigh in and provide model-independent calculations for the isospin corrections?
- Understand the 4σ discrepancy in the intermediate window between lattice QCD & $e^+e^- \rightarrow \pi^+ \pi^-$ r-ratio evaluation
- Develop multiple comparisons in the long-distance window, which contributes 2/3 of the total HVP, as well as full evaluations
- Utilize blinding methods whenever possible to reduce unintentional biases

Hadronic Light by Light



- This difficult problem previously caused quite some stress!
- HLBL has smaller contribution than HVP, but relative uncertainty is larger
- After some excellent work in the last 5 years, multiple current HLbL lattice results and dispersive approaches are compatible with uncertainties $\sim 20\%$.
- Corresponds to 0.15 ppm uncertainty on a_μ
- TI Outlook: **We expect that ongoing work on both approaches will yield reduced uncertainties in 2024-2025, down to the 10% level.**

Wishlist: Converge on HLbL calc. with $\sim 10\%$ rel uncertainty

Recent publication

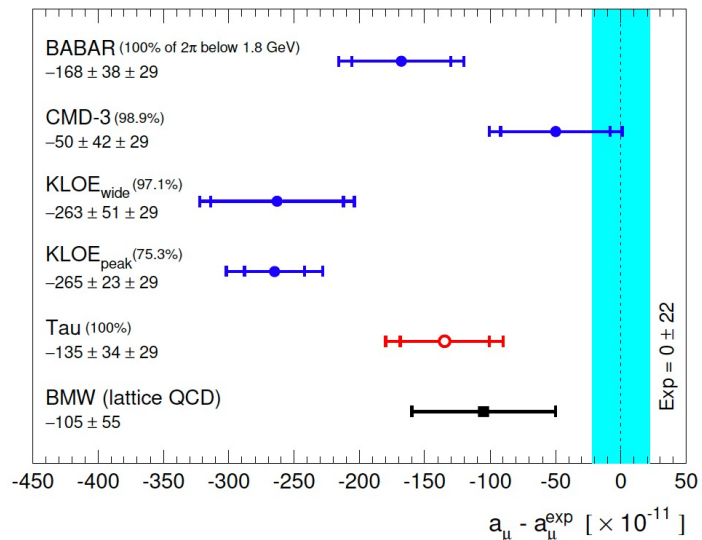


Fig. 11. Compilation of a_μ predictions subtracted by the central value of the experimental world average [2]. The

Note: Similar plots for the intermediate window

Davier et al: [arXiv:2312.02053](https://arxiv.org/abs/2312.02053)

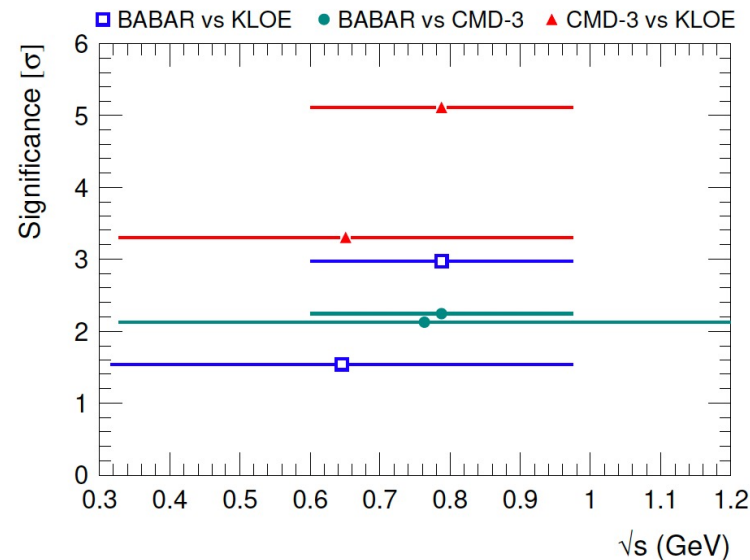
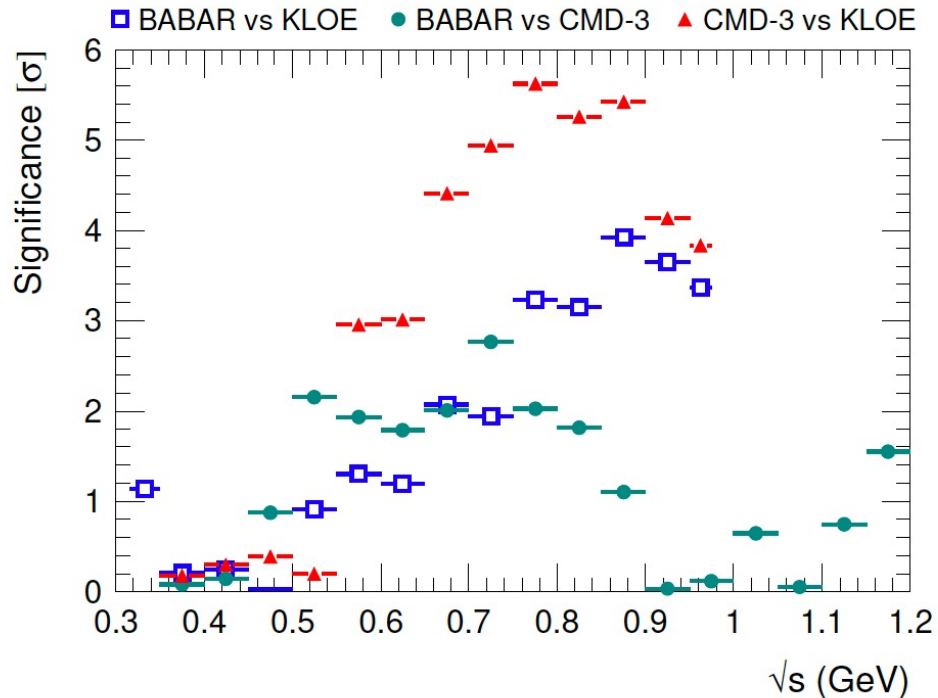


Fig. 5. Significance of the difference between pairs of the three most precise $e^+e^- \rightarrow \pi^+\pi^-$ experiments for narrow energy intervals of 50 MeV or less (top) and larger energy intervals (bottom) indicated by the horizontal lines.

Lepton Universality connections

If anomaly persists, potential explanation include things like $U(1)_{L_\mu-L_\tau}$ extension of the SM

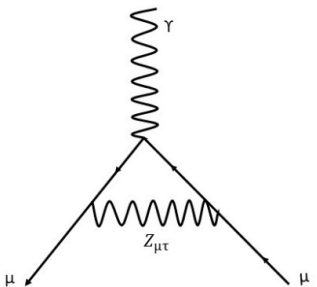
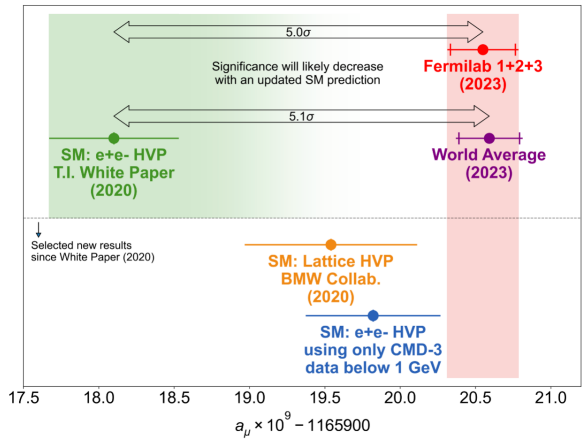


Figure 2: One loop contribution to muon ($g-2$) mediated by neutral gauge boson $Z_{\mu\tau}$.

Muon $g-2$ (Lepton Universality)



Anyway, muon $g-2$ gives us some hint to violate the lepton universality. For example, $L_\mu-L_\tau$ model explains this discrepancy. So, muon $g-2$ may indicate deep relation between τ and μ . We may need to consider tau $g-2$ more seriously.

04/Dec/2023 TAU2023 2

Overview of Tau Physics

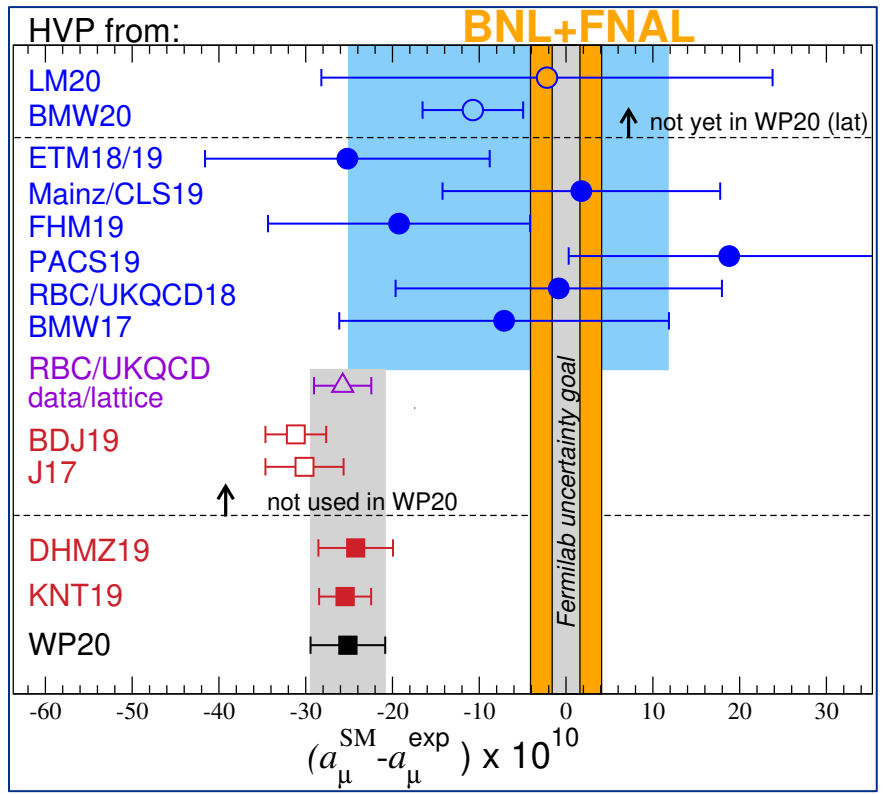
Kiyoshi Hayasaka

Monday

09:15 - 09:55

Summary: New Precise Lattice Calculations are in tension with Dispersive Calculations for a_μ

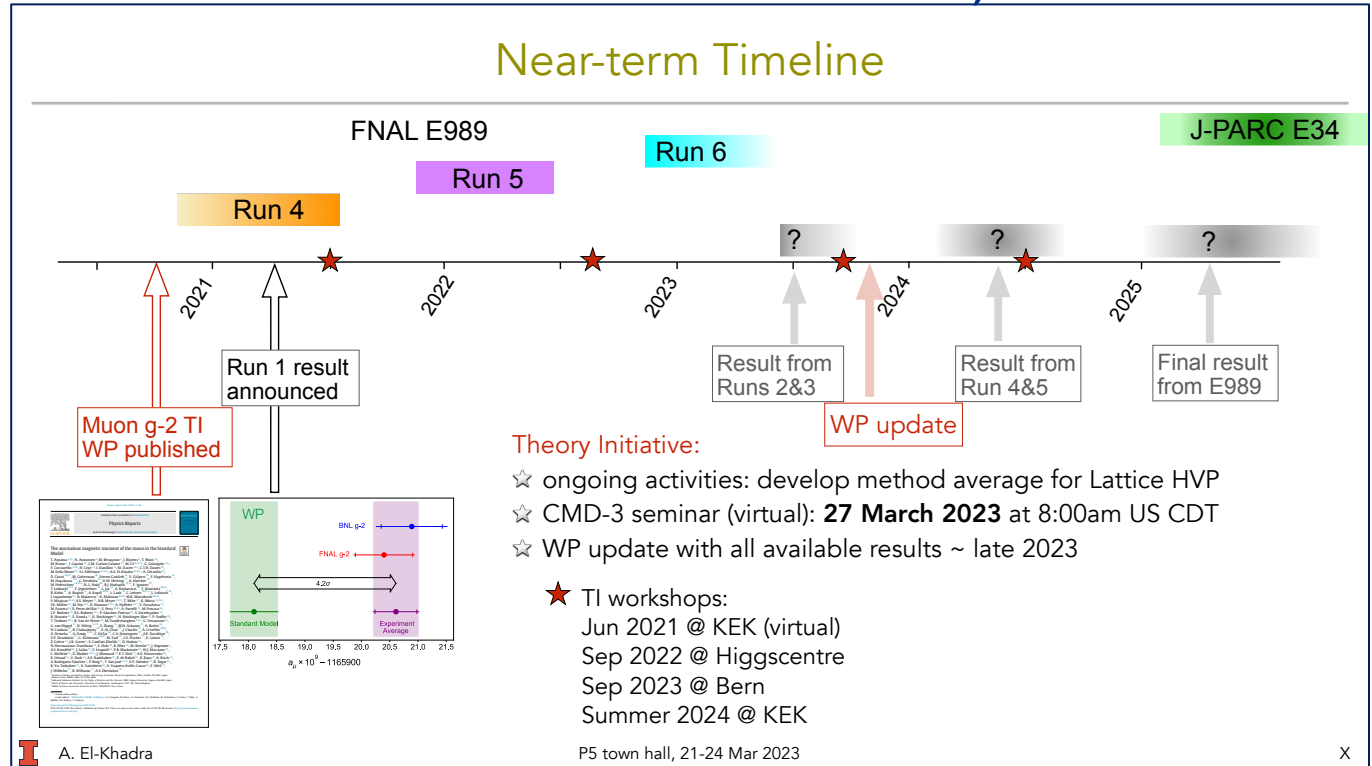
- Important to see how story evolves
 - Will need to see how other windows compares
 - There are several tensions within the dispersive calculations, within lattice and between dispersive and lattice contributions for HVP
- **Critical** to support efforts to understand these discrepancies and develop a firm theoretical calculation

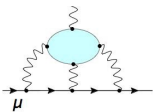


Overall Timeline & Summary

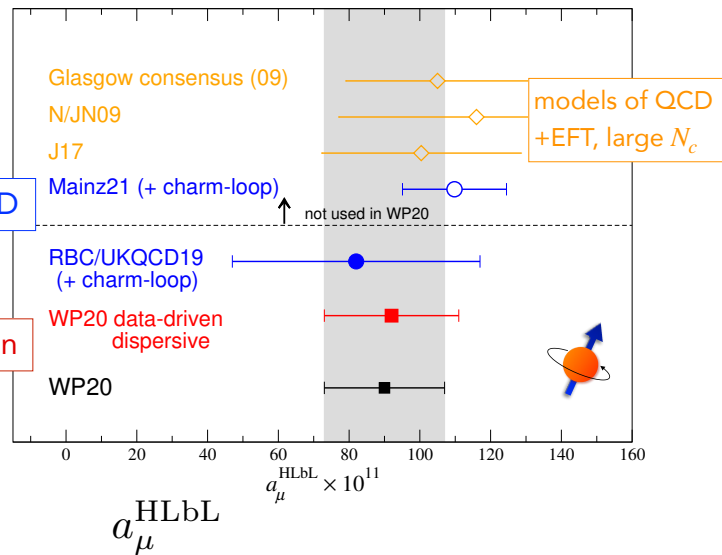
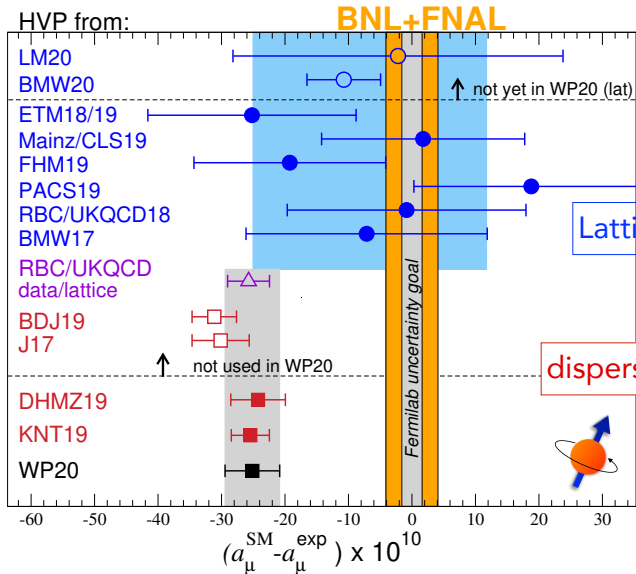
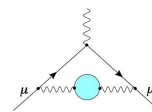
- Major exp & theory updates planned in 2023
- Both exp & theory planning significant updates by 2025
- Open questions on theory-theory & theory-exp anomalies will be addressed on this timeline

A. El-Khadra's talk at P5 town hall, March 2023





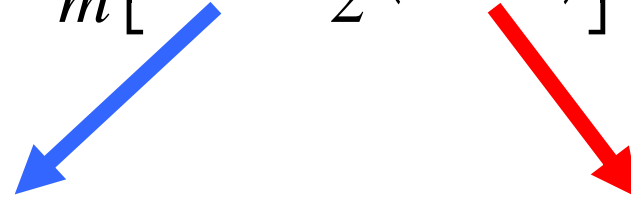
Hadronic Corrections: Comparisons



$$a_\mu^{\text{SM}} = a_\mu^{\text{HVP}} + [a_\mu^{\text{QED}} + a_\mu^{\text{Weak}} + a_\mu^{\text{HLbL}}]$$

Simultaneous measurements: g-2, EDM

$$\vec{\omega} = -\frac{e}{m} \left[a_\mu \vec{B} + \frac{\eta}{2} (\vec{\beta} \times \vec{B}) \right]$$



Expected time spectrum of e⁺ in μ → e⁺νν decay

