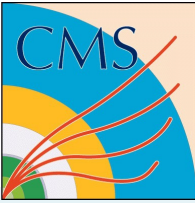




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Measurement of the τ lepton polarization in Z boson decays using CMS detector



Abdollah Mohammadi

Dec 5th 2023

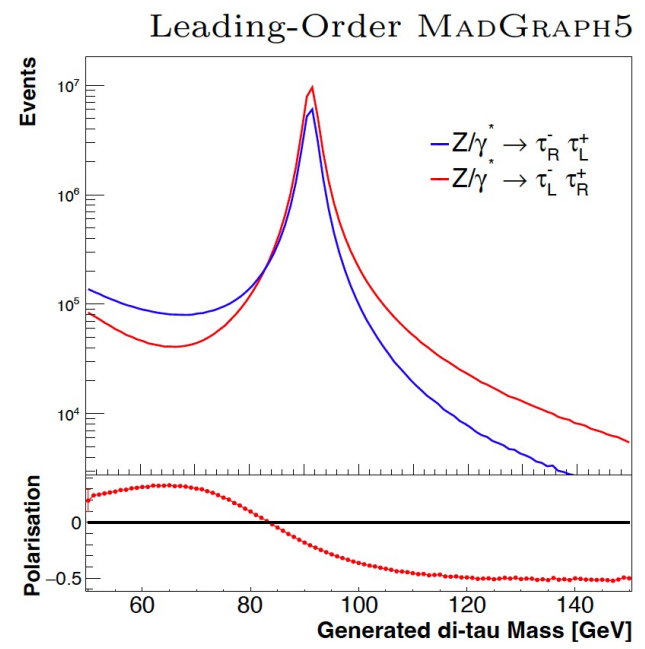
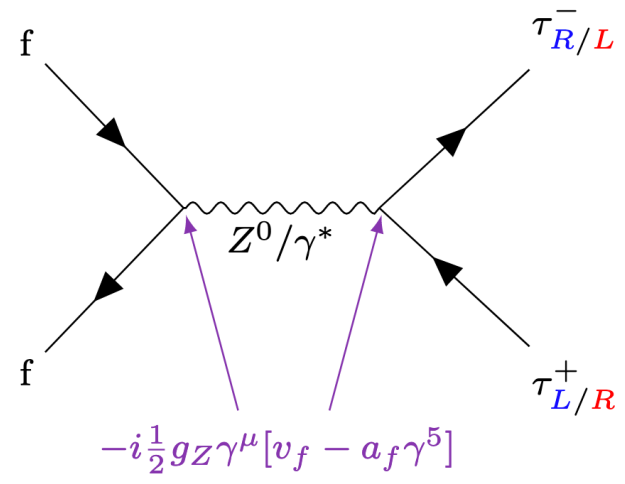
Tau 2023 conference, Louisville, KY

Motivation

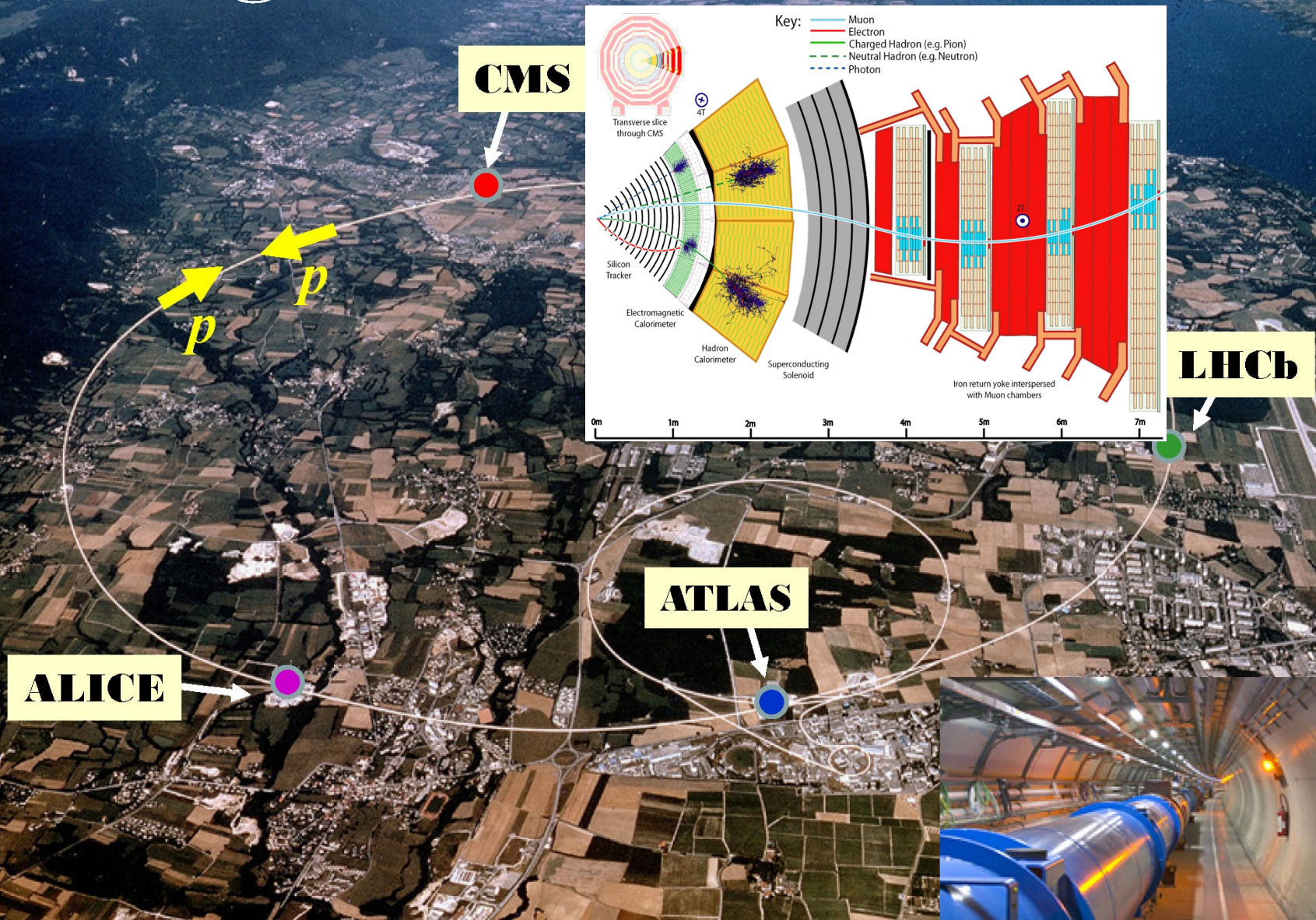
- Electroweak mixing angle, $\sin^2\theta_w$, is related to the effective vector and axial-vector couplings of the fermions to the Z boson
 - Such a mixing angle leads to different couplings for right- and left-handed fermions in weak neutral currents
- The polarization measures the ratio of vector to axial-vector neutral current couplings of the τ lepton
- Aim of this analysis:
 - Measure average polarisation of leptons in Z/γ events:

$$\langle \mathcal{P}_\tau \rangle = \frac{N(pp \rightarrow Z/\gamma \rightarrow \tau_R^- \tau_L^+) - N(pp \rightarrow Z/\gamma \rightarrow \tau_L^- \tau_R^+)}{N(pp \rightarrow Z/\gamma \rightarrow \tau_R^- \tau_L^+) + N(pp \rightarrow Z/\gamma \rightarrow \tau_L^- \tau_R^+)}$$

- Convert polarisation into effective weak mixing angle $\sin^2\theta_w$
- Any deviation from SM reveals a new physics beyond SM!



Large Hadron Collider

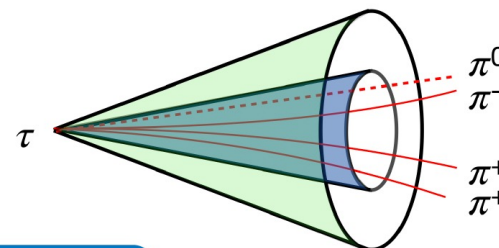


τ CMS reconstruction

[More in Valeria's talk](#)

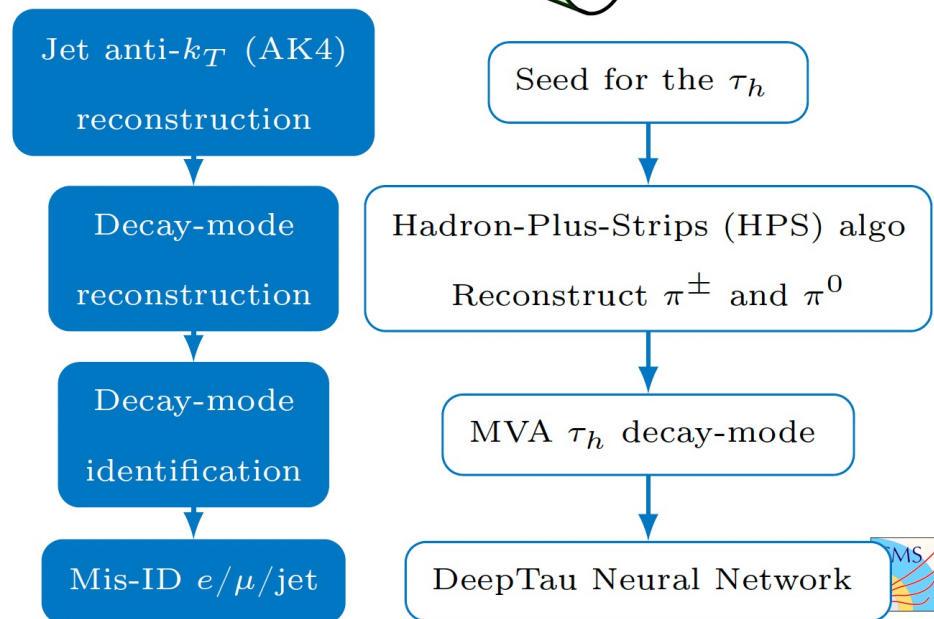
Decay mode	Resonance	$\mathcal{B}(\%)$
Leptonic decays		35.2
$\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau$		17.8
$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$		17.4
Hadronic decays		64.8
$\tau^- \rightarrow h^- \nu_\tau$		11.5
$\tau^- \rightarrow h^- \pi^0 \nu_\tau$	$\rho(770)$	25.9
$\tau^- \rightarrow h^- \pi^0 \pi^0 \nu_\tau$	$a_1(1260)$	9.5
$\tau^- \rightarrow h^- h^+ h^- \nu_\tau$	$a_1(1260)$	9.8
$\tau^- \rightarrow h^- h^+ h^- \pi^0 \nu_\tau$		4.8
Other		3.3

Many decay modes \rightarrow different signatures to be captured by the same algorithm

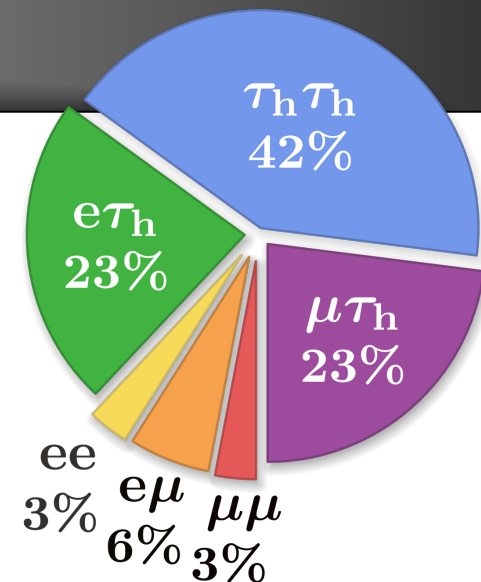


τ_h appear in the detector with :

- 1 or 3 charged hadrons (mainly π^\pm, K^\pm , CMS does not distinguish them)
- 1 or more neutral pions that undergo the decay $\pi^0 \rightarrow \gamma\gamma$
- intermediate resonances in the decay



Event Selection - Summary



$\tau_h \tau_h$ channel

Trigger : *DoubleMediumIsoPFTau35*

Hadronic taus : $p_T(\tau_h) > 40$ GeV and $|\eta(\tau_h)| < 2.1$

$\tau_\mu \tau_h$ channel

Trigger :

- *IsoMu22*
- *IsoMu19_LooseIsoPFTau20*

Muon :

- $p_T(\mu) > 20$ GeV
(> 23 GeV if *IsoMu22*)
- $|\eta(\mu)| < 2.1$

Hadronic tau :

- $p_T(\tau_h) > 30$ GeV
- $|\eta(\tau_h)| < 2.3$

$\tau_e \tau_h$ channel

Trigger :

- *Ele25*

Electron :

- $p_T(e) > 26$ GeV
- $|\eta(e)| < 2.1$

Hadronic tau :

- $p_T(\tau_h) > 30$ GeV
- $|\eta(\tau_h)| < 2.3$

$\tau_e \tau_\mu$ channel

Trigger :

- *Mu8_Ele23*
- *Mu23_Ele12*

Electron :

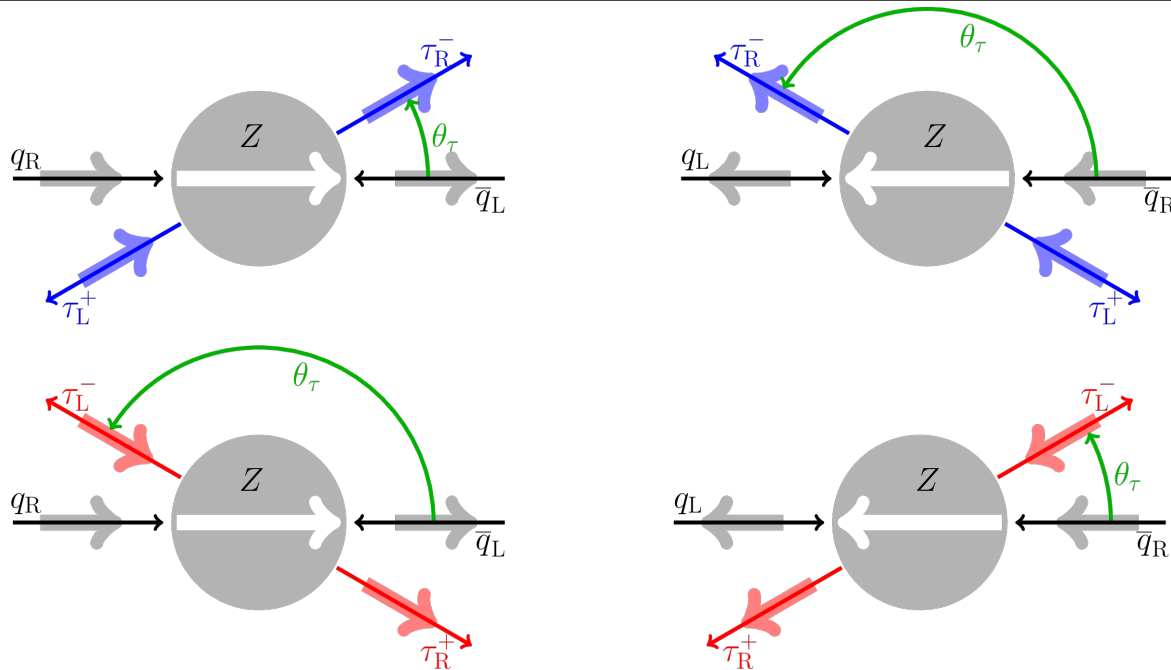
- $p_T(e) > 15$ GeV
(> 24 GeV if *Mu8_Ele23*)
- $|\eta(e)| < 2.4$

Muon :

- $p_T(\mu) > 15$ GeV
(> 24 GeV if *Mu23_Ele12*)
- $|\eta(\mu)| < 2.4$



Helicity states of incoming quarks and outgoing τ leptons.

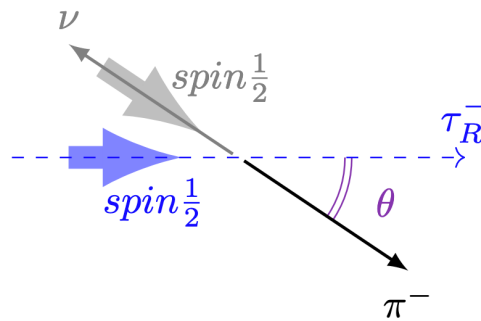
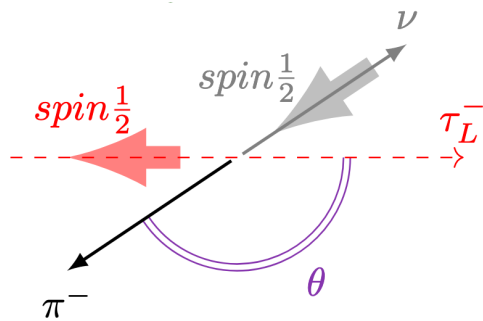


- The angle θ_τ is the scattering angle of the τ -lepton with respect to the quark momentum in the rest frame of the Z boson

$$\frac{d\sigma}{d\cos\theta_\tau} = F_0(\hat{s})(1 + \cos^2\theta_\tau) + 2F_1(\hat{s})\cos\theta_\tau - \lambda_\tau[F_2(\hat{s})(1 + \cos^2\theta_\tau) + 2F_3(\hat{s})\cos\theta_\tau].$$

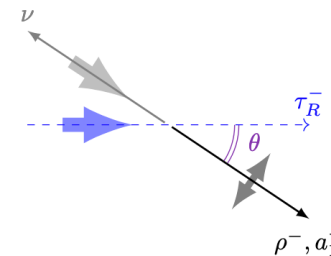
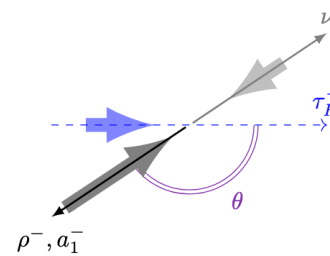
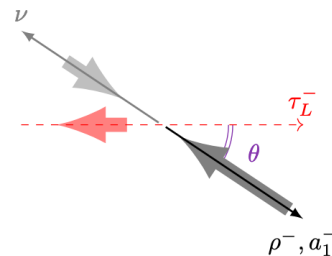
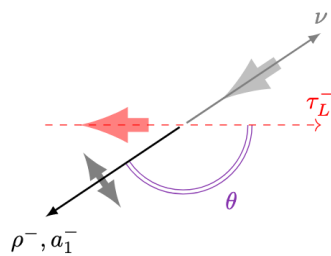
- The helicity of τ leptons from Z boson decays can be measured from energy and angular distributions of the τ lepton decay products.

Helicity of τ leptons - Angle θ in τ rest frame



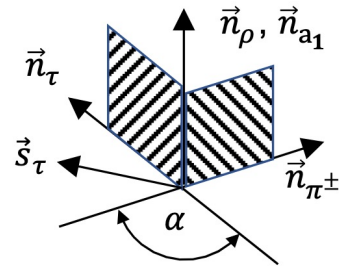
$$\cos \theta = \vec{n}_\tau \cdot \vec{n}_{h^\pm} = 2 \frac{E(h^\pm)}{E(\tau^\pm)} - 1$$

Intermediate spin-0 resonance (π^-) \Rightarrow angle θ contains full helicity information

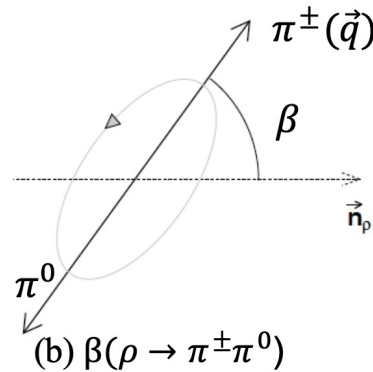


Intermediate spin-1 resonances (ρ^-, a_1^-) \Rightarrow angle θ depends on the polarisation of the resonance. Not sensitive enough to analyse by itself the τ - polarisation. Need more discriminative variables

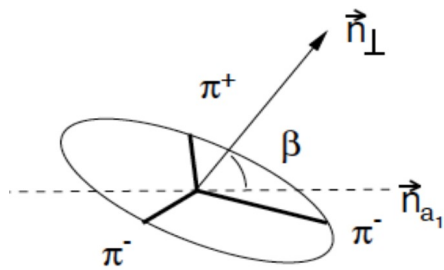
Helicity of τ leptons - Angles β , α and γ



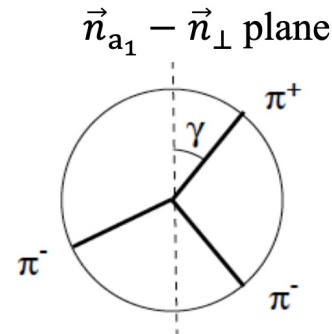
(a) $\alpha(\tau \rightarrow \nu_\tau + \rho, a_1)$



(b) $\beta(\rho \rightarrow \pi^\pm \pi^0)$



(c) $\beta(a_1 \rightarrow \pi^- \pi^+ \pi^-)$



(d) $\gamma(a_1 \rightarrow \pi^- \pi^+ \pi^-)$

Angular kinematics of τ decays are fully described by 1-4 angles :

- $\tau^\pm \rightarrow \pi^\pm \nu : \theta$
- $\tau^\pm \rightarrow a_1^\pm \nu \rightarrow 3\pi^\pm \nu : \theta, \beta, \alpha, \gamma$
- $\tau^\pm \rightarrow \rho^\pm \nu \rightarrow \pi^\pm \pi^0 \nu : \theta, \beta, \alpha$ (β can be reconstructed from four-momenta of pions)

Discriminant Observables (optimal variables)

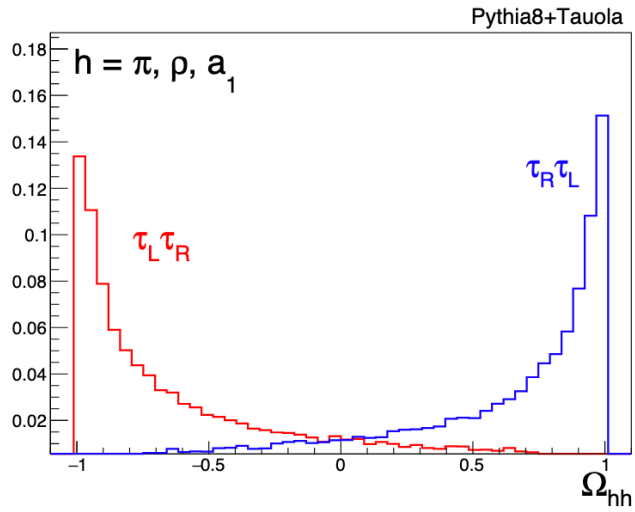
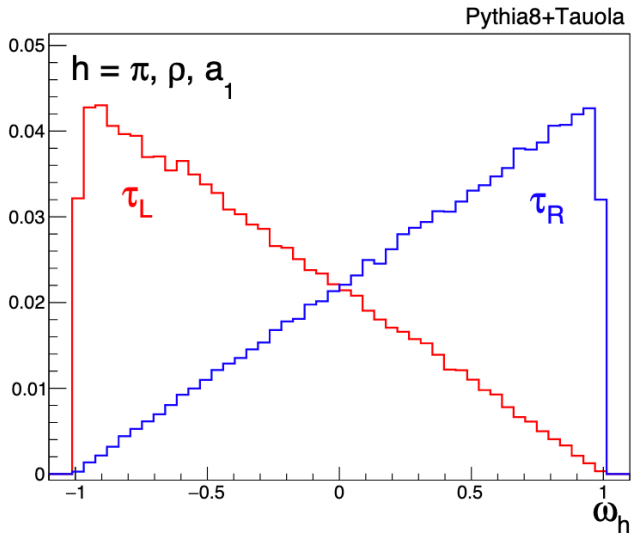
Definition : ratio of matrix elements (number of considered angles depends on decay mode)

$$\omega(\tau = \theta, \beta, \alpha, \gamma) = \frac{|M(\theta, \beta, \alpha, \gamma|\tau_R)|^2 - |M(\theta, \beta, \alpha, \gamma|\tau_L)|^2}{|M(\theta, \beta, \alpha, \gamma|\tau_R)|^2 + |M(\theta, \beta, \alpha, \gamma|\tau_L)|^2}$$

$\theta, \beta, \alpha, \gamma$: angles approximately estimated from the decay data

Combination : helicity information from both taus is 100% anti-correlated (on generator level)

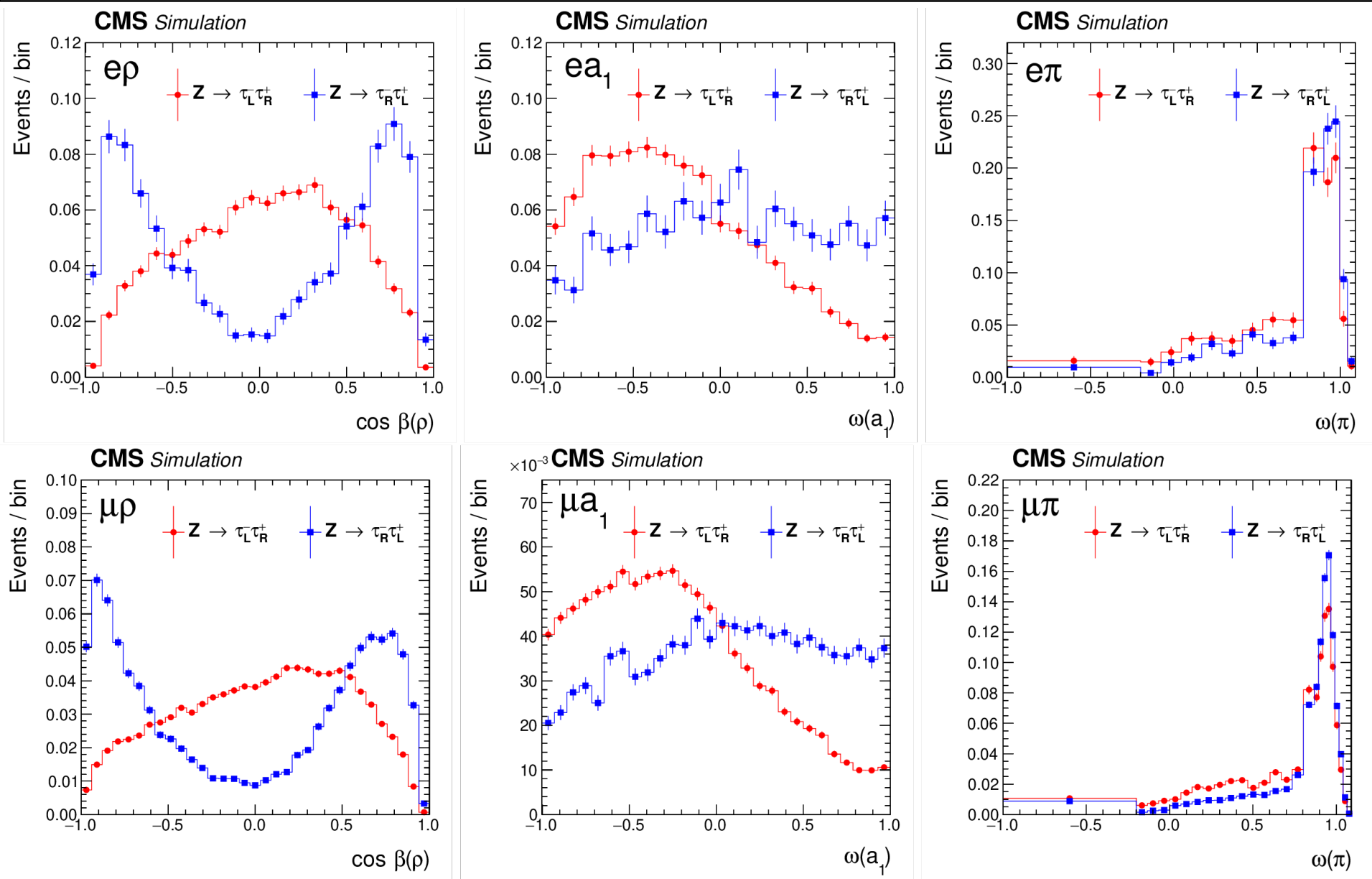
$$\Omega(\tau^-, \tau^+) = \frac{\omega(\tau^-) + \omega(\tau^+)}{1 + \omega(\tau^-) \cdot \omega(\tau^+)}$$



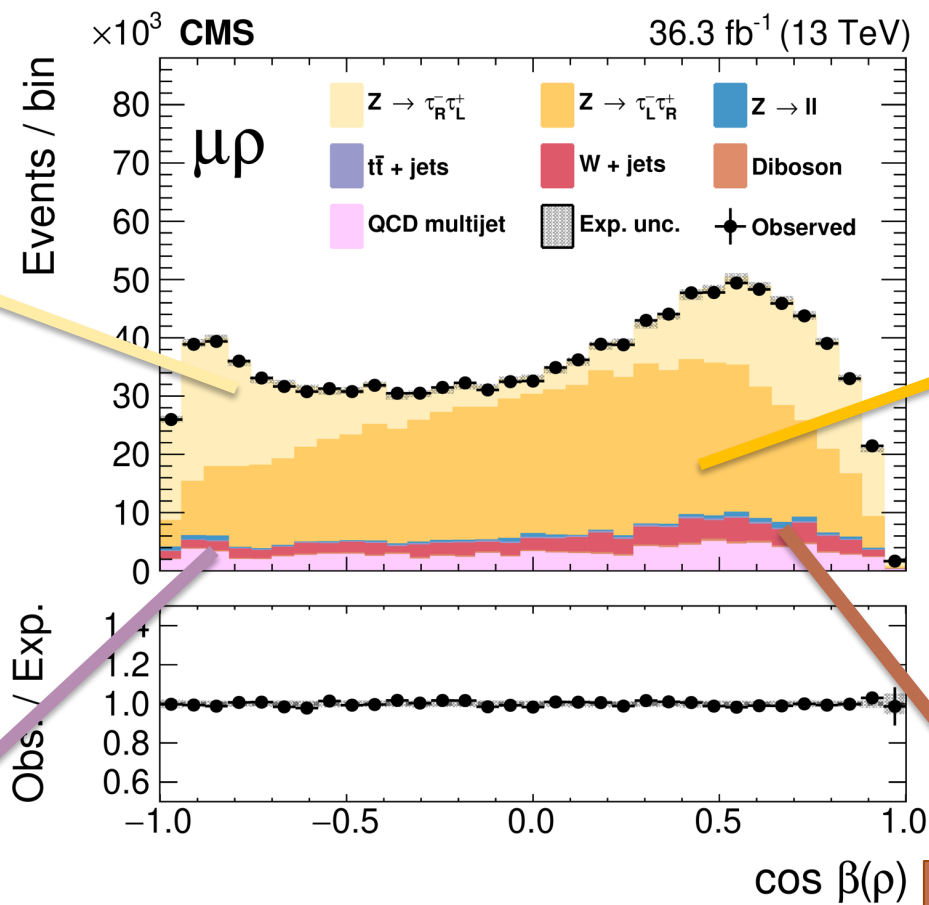
Final Choice of Discriminators

Channel	Category	Discriminator	
$\tau_e \tau_\mu$	$e + \mu$	$m_{\text{vis}}(e, \mu)$	visible mass
$\tau_e \tau_h$	$e + a_1$	$\omega(a_1)$	optimal observable with SVfit
	$e + \rho$	$\cos\beta(\rho)$	visible optimal observable
	$e + \pi$	$\omega(\pi)$	optimal observable with SVfit
$\tau_\mu \tau_h$	$\mu + a_1$	$\omega(a_1)$	optimal observable with SVfit
	$\mu + \rho$	$\cos\beta(\rho)$	visible optimal observable
	$\mu + \pi$	$\omega(\pi)$	optimal observable with SVfit
$\tau_h \tau_h$	$a_1 + a_1$	$m_{\text{vis}}(a_1, a_1)$	visible mass
	$a_1 + \pi$	$\Omega(a_1, \pi)$	combined optimal observable with SVfit
	$\rho + \tau_h$	$\cos\beta(\rho)$	visible optimal observable (for leading ρ)
	$\pi + \pi$	$m_{\text{vis}}(\pi, \pi)$	visible mass

Discriminant Observables



Signal and background definition



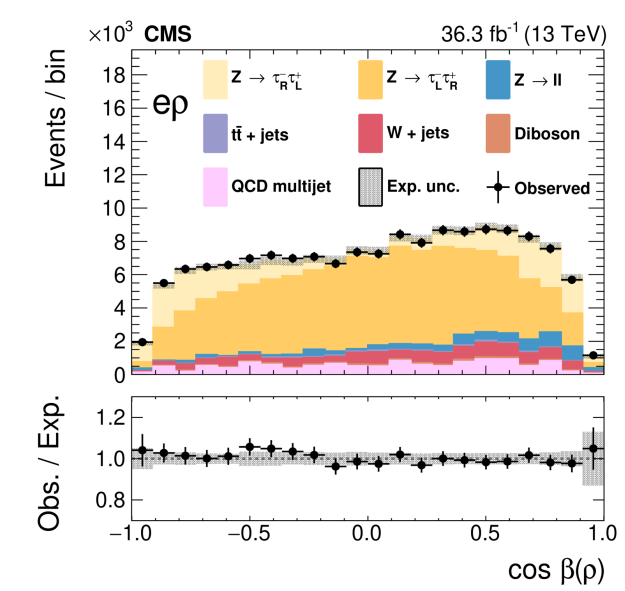
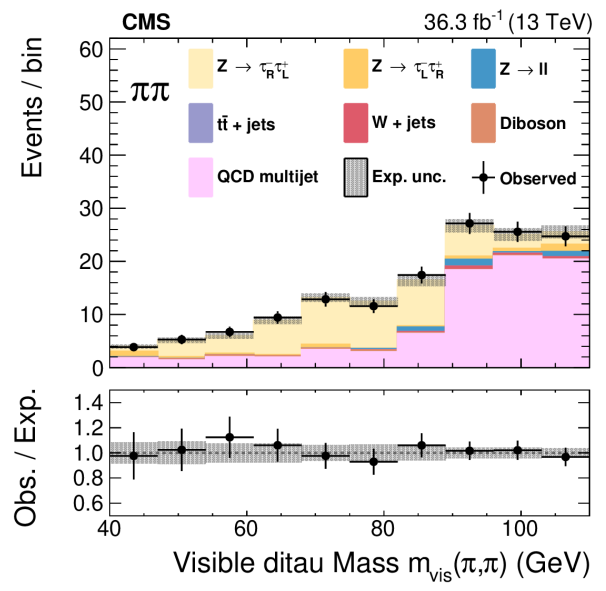
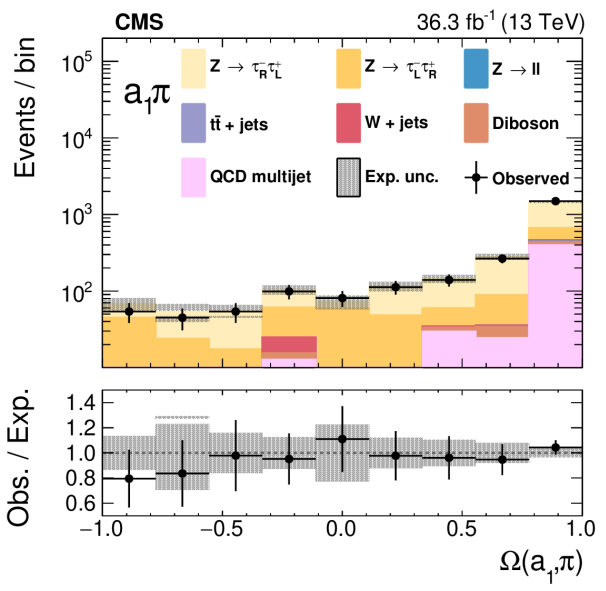
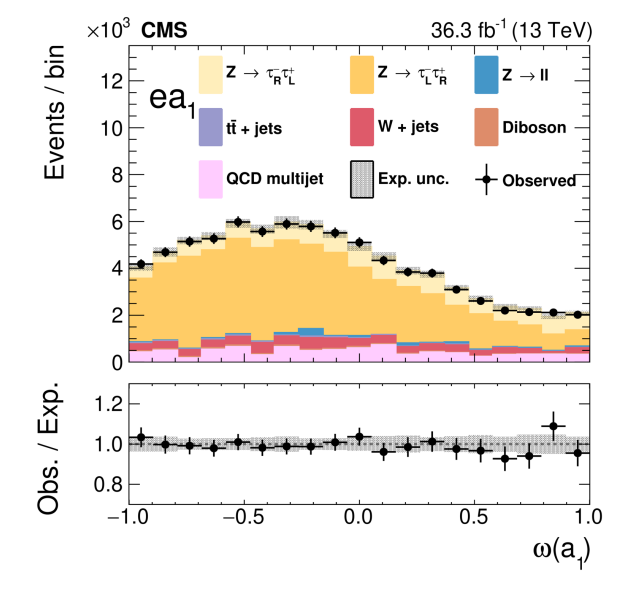
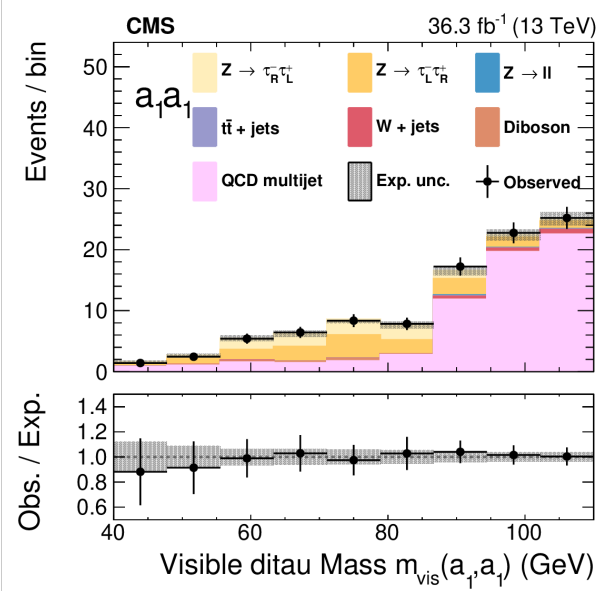
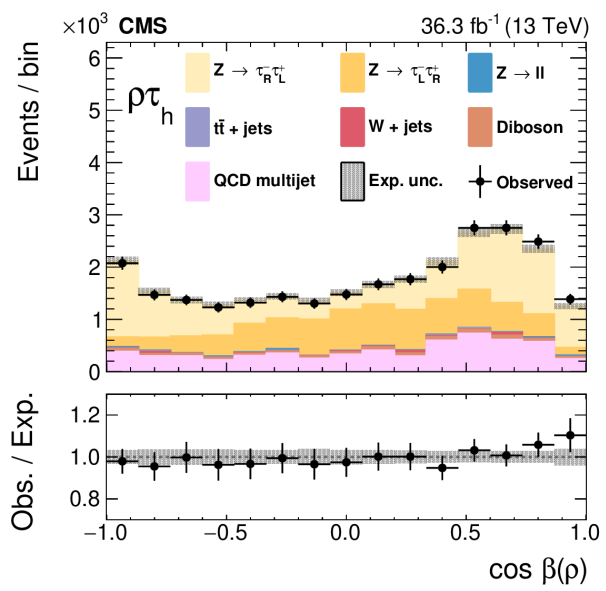
Right-helicity
Signal split at
generator level

Left-helicity
Signal split at
generator level

QCD multijet events
estimated from data using
jet to tau fake rate

W+jet background
normalization estimated
from data from high MT
control region

Final Observables



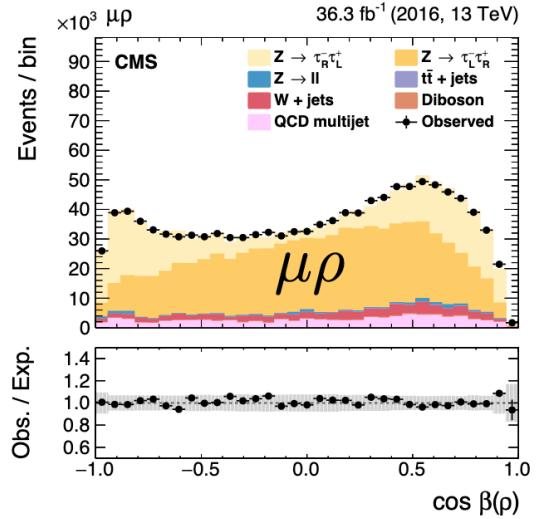
Extraction of Polarisation by Template Fit

Fitting data distributions of optimal observables with templates for $Z \rightarrow \tau\tau$ signal and background :

$$\mathcal{T}(data) \stackrel{fit}{=} \mathcal{T}(sig, \langle \mathcal{P}_\tau \rangle, r) + \mathcal{T}(bkg)$$

Two parameters of interest :

- average tau polarisation $\langle \mathcal{P}_\tau \rangle$
- signal strength r



Signal templates :

$$\mathcal{T}(sig, \langle \mathcal{P}_\tau \rangle, r) = r \cdot \left[\frac{1 + \langle \mathcal{P}_\tau \rangle}{2} \cdot \mathcal{T}(Z \rightarrow \tau_R^- \tau_L^+) + \frac{1 - \langle \mathcal{P}_\tau \rangle}{2} \cdot \mathcal{T}(Z \rightarrow \tau_L^- \tau_R^+) \right]$$

templates for **right-** and **left-handed** τ
(splitting is done with MADGRAPH5 spin flag)

Background processes :

$Z^0/\gamma^* \rightarrow e^-e^+/\mu^-\mu^+$, $t\bar{t} + jets$, di-boson, W + jets (normalisation from data) and QCD (normalisation and shape from data)

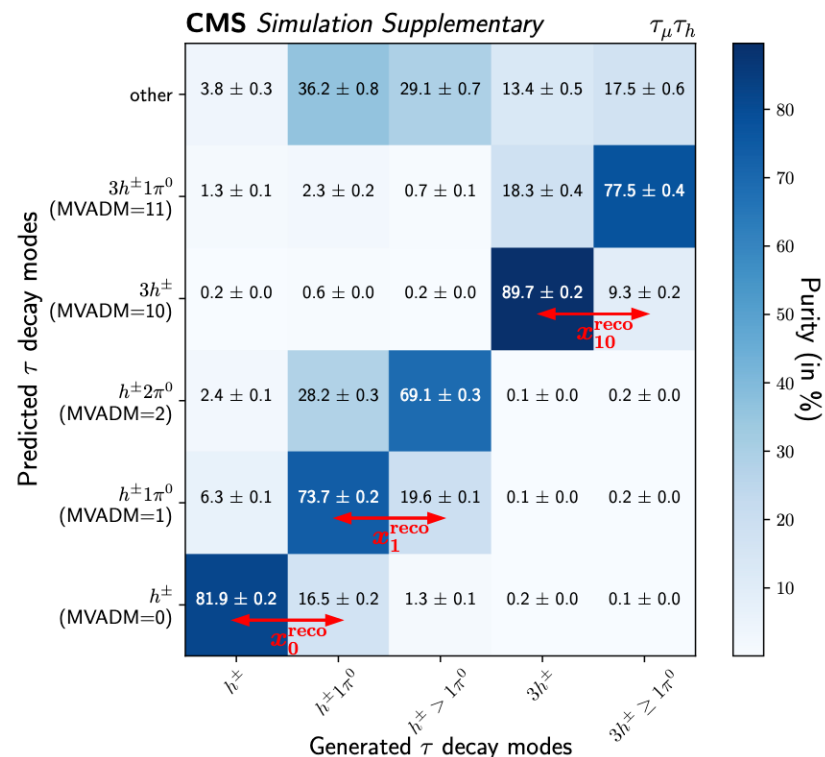
Closure test : The average polarisation of MC MADGRAPH5 is found back by extracting polarisation with templates



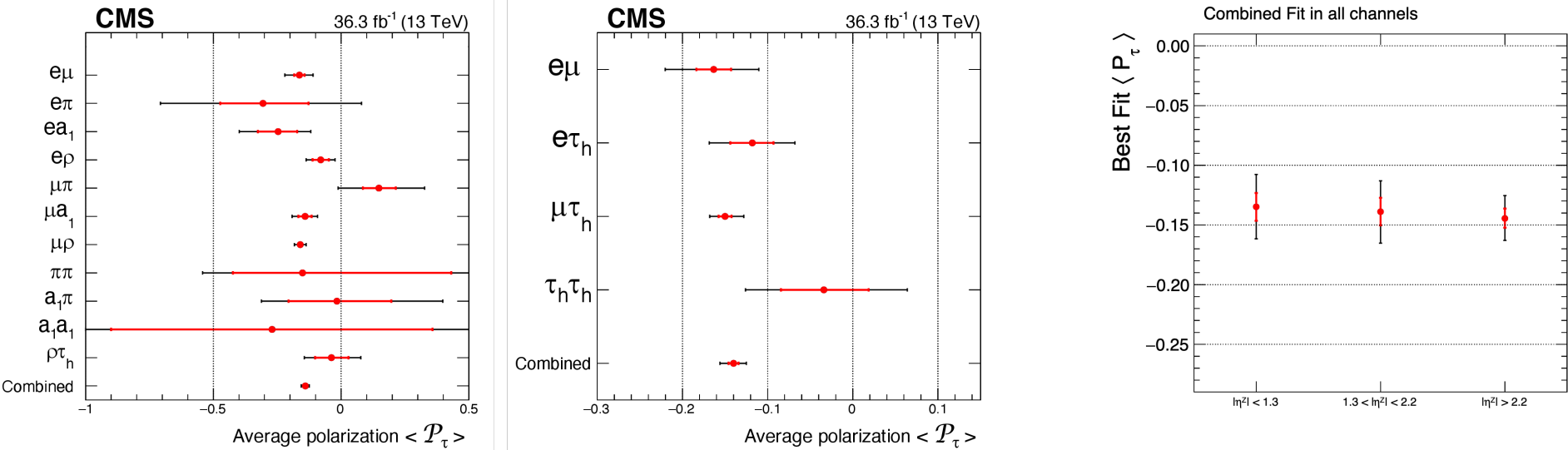
Systematic Source - τ DM Migrations

- Does MC simulation describes decay-mode reconstruction in data well?
- Variations of migrations have strong impact on polarisation measurement :
 - Problem of normalisation inside categories
 - Discriminant variables are optimised for a given τ decay-mode
- Define 3 most important migrations :
 - $x_0^{\text{reco}} \equiv x^{\text{reco}}(h^\pm \leftrightarrow h^\pm \pi^0)$
 - $x_1^{\text{reco}} \equiv x^{\text{reco}}(h^\pm \pi^0 \leftrightarrow h^\pm \pi^0 \pi^0)$
 - $x_{10}^{\text{reco}} \equiv x^{\text{reco}}(3h^\pm \leftrightarrow 3h^\pm \pi^0)$

Parameters x_i^{reco} quantify the fraction of all events in a given reconstructed DM i that migrate differently in data compared to MC.



Results of the Average τ Polarisation



$$\langle P_\tau \rangle_{75-120 \text{ GeV}} = -0.140 \pm 0.006 \text{ (stat)} \pm 0.014 \text{ (syst)} = -0.140 \pm 0.015.$$

$$P_\tau(Z) = -0.144 \pm 0.015$$

$$P_\tau = -A_\tau = -\frac{2v_\tau a_\tau}{v_\tau^2 + a_\tau^2} \approx -2\frac{v_\tau}{a_\tau} = -2(1 - 4\sin^2 \theta_W^{\text{eff}}).$$

$$\sin^2 \theta_W^{\text{eff}} = 0.2319 \pm 0.0008 \text{ (stat)} \pm 0.0018 \text{ (syst)} = 0.2319 \pm 0.0019.$$

- Sensitivity is mostly driven by $\mu\tau$ channel following by $e\tau$, $e\mu$, and $\tau\tau$.
- No dependence on the pseudo-rapidity of the Z_0 boson

Summary

- Polarization of τ^- leptons in the decay of Z bosons produced in pp collisions using CMS detector is presented to an integrated luminosity of 36.3 fb^{-1} .
- The measured τ^- lepton polarization, $\mathcal{P}_\tau(Z) = -0.144 \pm 0.015$, is in good agreement with the SLD, LEP and ATLAS results.
- The measured polarization constrains the effective couplings of τ^- leptons to the Z boson and determines the effective weak mixing angle to be $\sin^2 \theta_w^{\text{eff}} = 0.2319 \pm 0.0019$
- No deviation from SM! Improving the sensitivity requires both more data and more importantly, better understanding/reducing the systematics.

CMS (13 TeV)
 36.3 fb^{-1}

ATLAS (8 TeV)
Eur. Phys. J. C 78
(2018) 163

LEP-SLD (PDG)
Prog. Theor. Exp. Phys.
083 C 01 (2022)

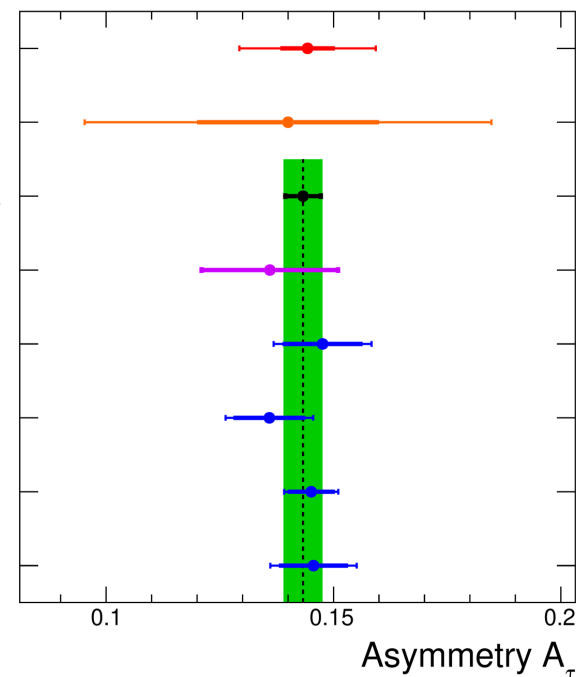
SLD
Phys. Rev. Lett. 86
(2001) 1162

L3
Phys. Lett. B 429
(1998) 387

DELPHI
Eur. Phys. J. C 14
(2000) 585

ALEPH
Eur. Phys. J. C 20
(2001) 401

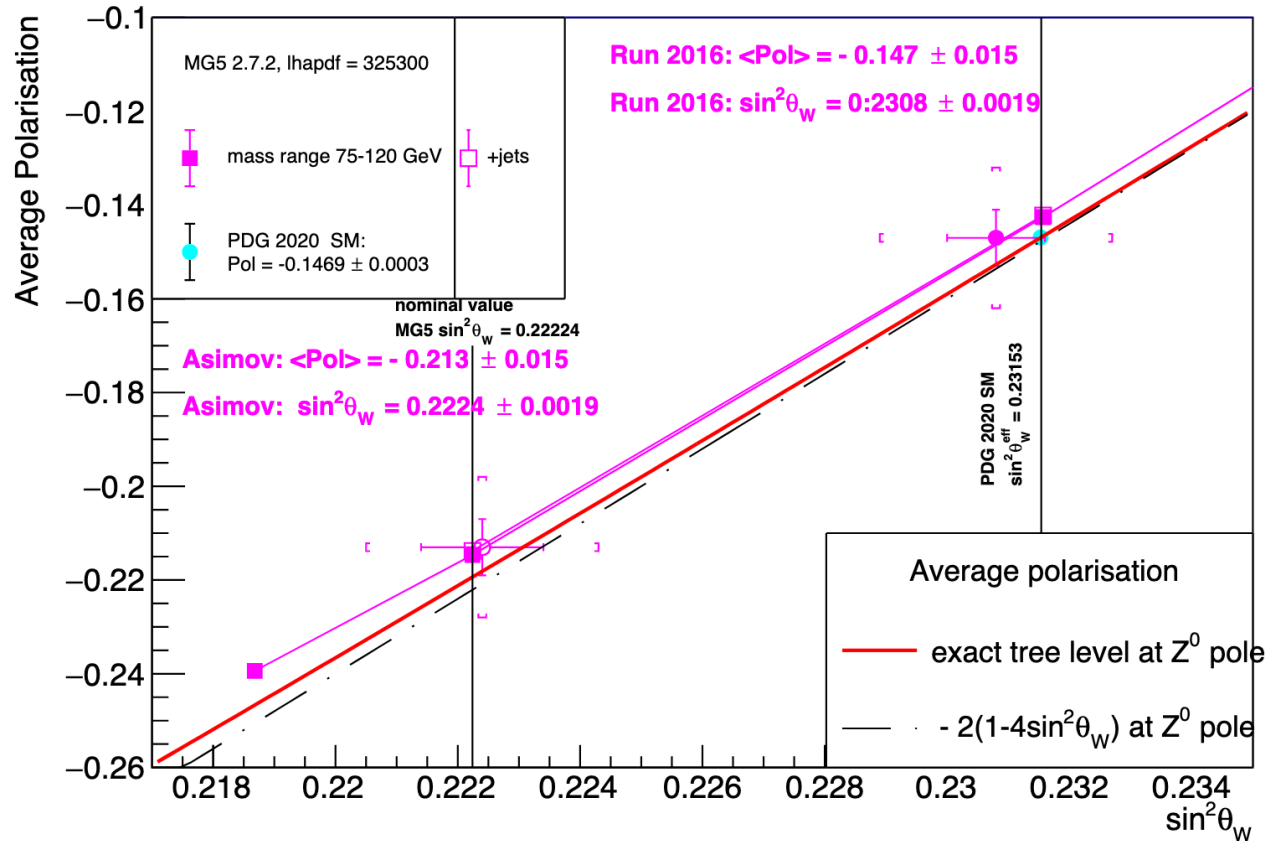
OPAL
Eur. Phys. J. C 21
(2001) 1



Backup

Polarization curve

Polarisation curve



$$\mathcal{P}_\tau = -A_\tau = -\frac{2v_\tau a_\tau}{v_\tau^2 + a_\tau^2} \approx -2\frac{v_\tau}{a_\tau} = -2(1 - 4\sin^2 \theta_W^{\text{eff}}).$$