An aerial photograph of the LHCb experiment site at CERN. The image shows a large circular tunnel structure overlaid on a landscape of green fields and some buildings. The text is overlaid on a semi-transparent blue box at the top.

Search for the rare decays  
 $B_s \rightarrow \mu^+ \mu^-$  and  $B^0 \rightarrow \mu^+ \mu^-$   
with the LHCb Experiment

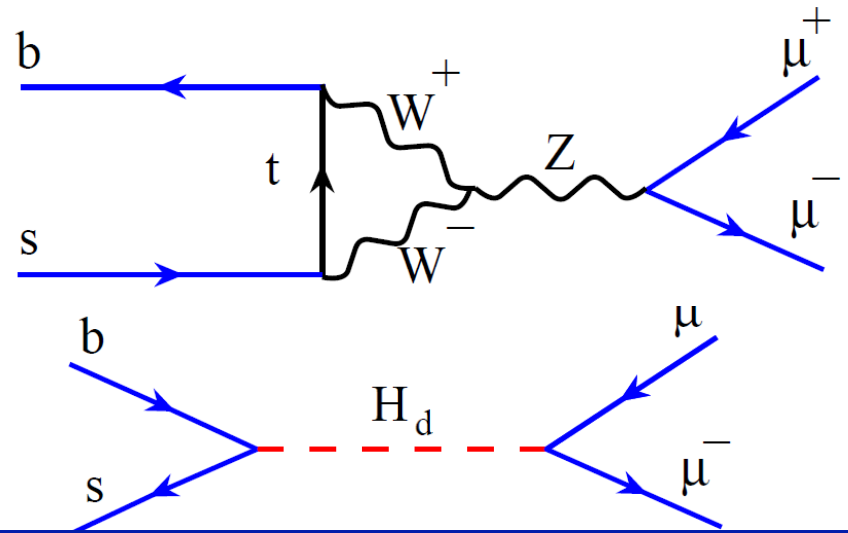
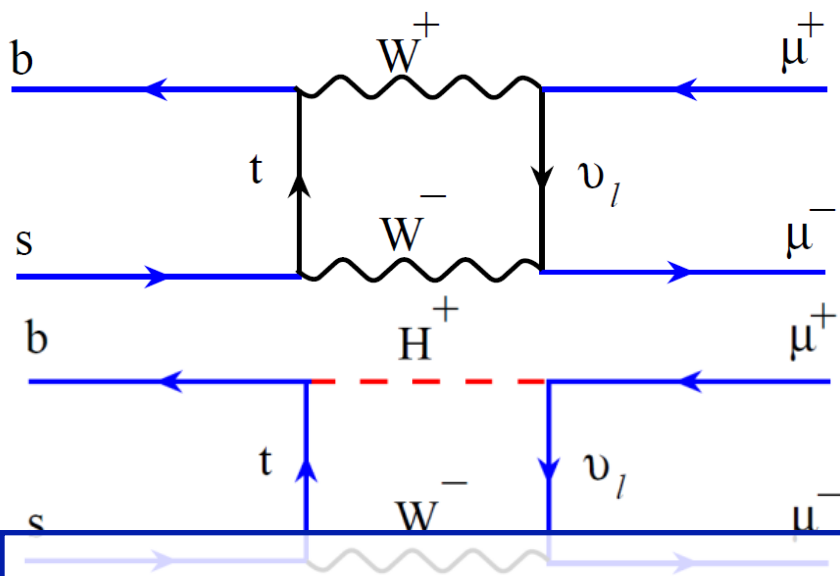
Johannes Albrecht (CERN)  
for the LHCb Collaboration



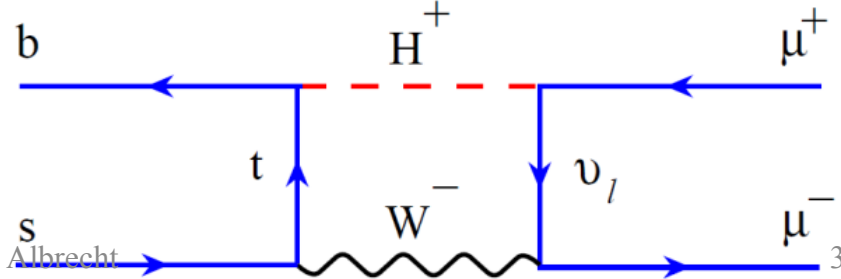
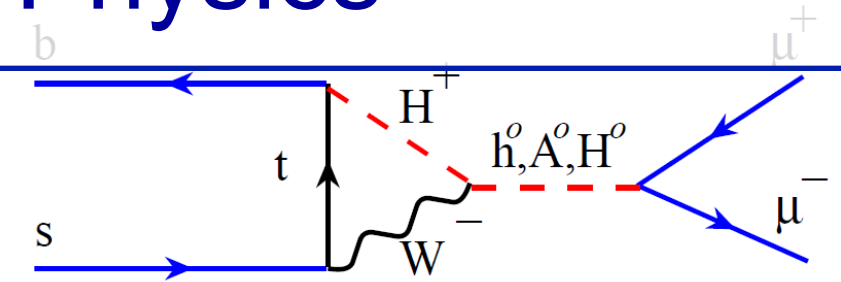
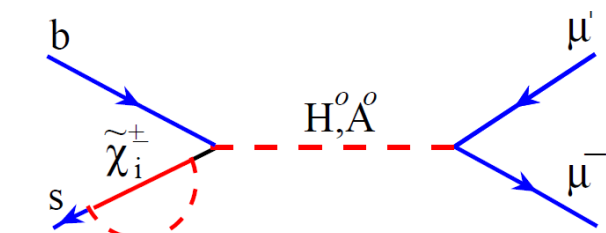
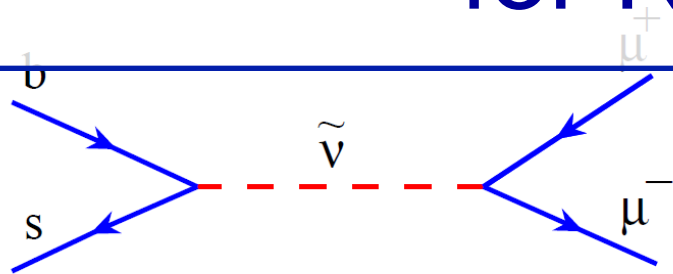
Joint EP/PP/LPCC seminar, 22.March 2011



- Introduction:  $B_{s,d} \rightarrow \mu^+ \mu^-$  as probe for New Physics
- The LHCb experiment
  - Overview of the experiment and performance
- Search for  $B_{s,d} \rightarrow \mu^+ \mu^-$  decays
  - Selection
  - Signal and background likelihoods
  - Normalization
  - Extraction of the limit
- Summary & Outlook



# Introduction: $B_{s,d} \rightarrow \mu^+ \mu^-$ as probe for New Physics



► Flavour physics in the LHC era

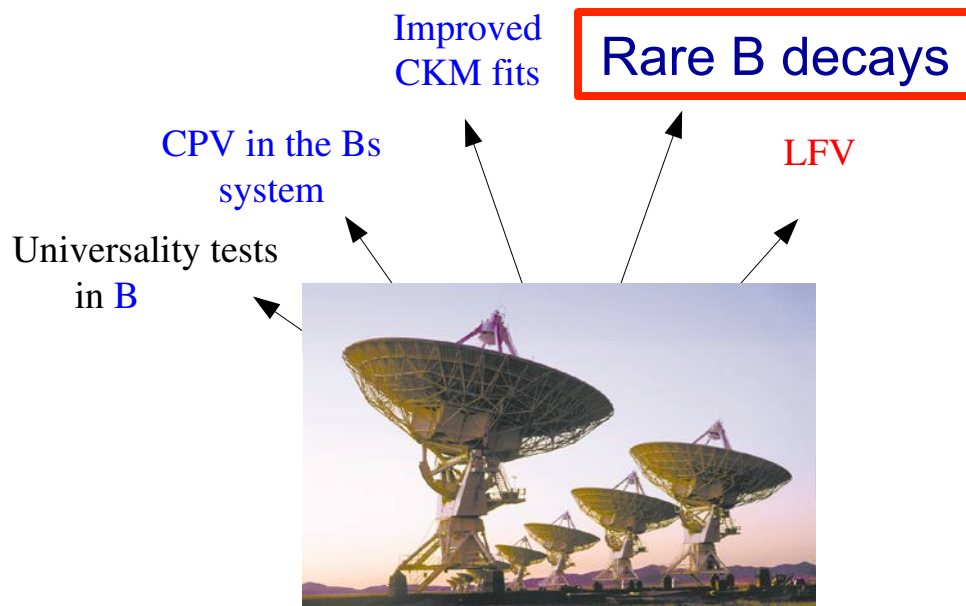
## ATLAS / CMS

*A unique effort toward the high-energy frontier*



Courtesy of G. Isidori, LP07

## LHCb





# $B_{s,d} \rightarrow \mu^+ \mu^-$ in the Standard Model

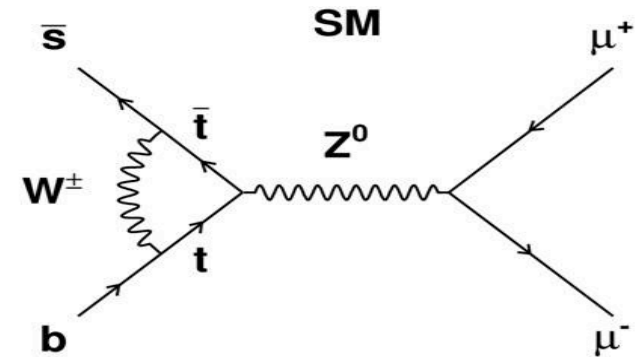
Double suppressed decay: **FCNC process** and **helicity suppressed**:

→ **very small in the Standard Model but well predicted:**

Mode	SM
$B_s \rightarrow \mu^+ \mu^-$	$3.2 \pm 0.2 \cdot 10^{-9}$
$B^0 \rightarrow \mu^+ \mu^-$	$0.10 \pm 0.01 \cdot 10^{-9}$

A.J.Buras: arXiv:1012.1447

E. Gamiz et al: Phys.Rev.D 80 (2009) 014503



BR expressed Wilson coefficients:

$$BR(B_q \rightarrow l^+ l^-) \approx \frac{G_F^2 \alpha^2 M_{B_q}^3 f_{B_q}^2 \tau_{B_q}}{64 \pi^3 \sin^4 \theta_W} |V_{tb} V_{tq}^*|^2 \sqrt{1 - \frac{4m_l^2}{M_{B_q}^2}} \left\{ M_{B_q}^2 \left( 1 - \frac{4m_l^2}{M_{B_q}^2} \right) c_S^2 + \left[ M_{B_q} c_P + \frac{2m_l}{M_{B_q}} (c_A - c'_A) \right]^2 \right\}.$$

→ sensitive to contributions in the **scalar/pseudo-scalar sector**

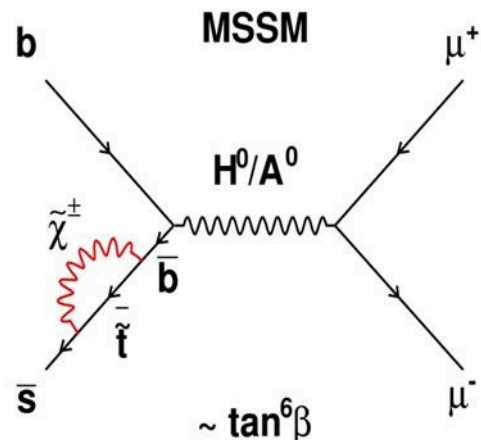
→ highly interesting to probe **extended Higgs** models

# $B_{s,d} \rightarrow \mu^+ \mu^-$ as probe for New Physics

- Example: MSSM  
(with R-parity conservation)

$$BR(B_s \rightarrow \mu^+ \mu^-) \propto \frac{\tan^6 \beta}{m_A^4}$$

→ limit or measurement of  $B_{s,d} \rightarrow \mu\mu$   
will strongly constrain  $\tan\beta$  vs  $M_A$  plane



- NUHM1

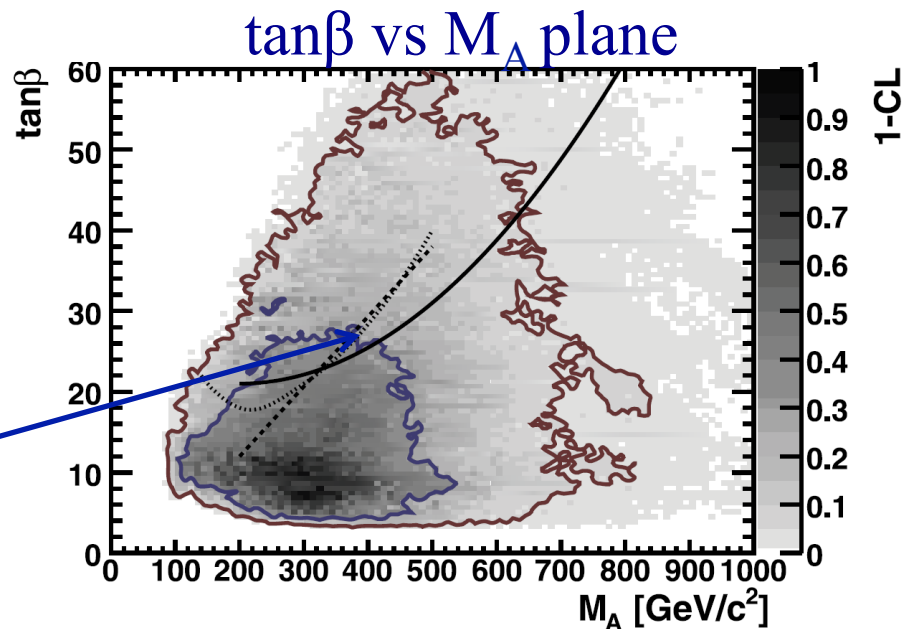
Best fit contours in  $\tan\beta$  vs  $M_A$   
plane in the NUHM1 model

[O. Buchmuller et al, arxiv:0907.5568]

CMS direct search 30-60fb<sup>-1</sup>:

5 $\sigma$  discovery  $H/A \rightarrow \tau\tau$

(2007 analysis: arXiv:0704.0619)

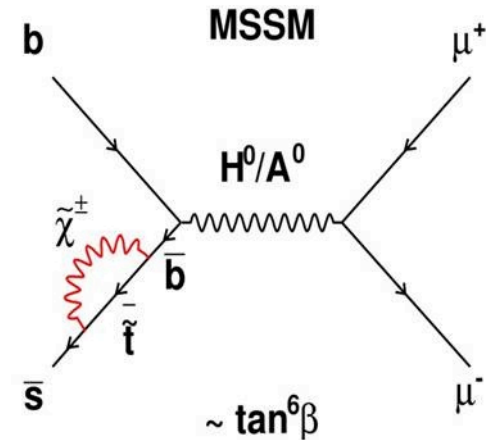


# $B_{s,d} \rightarrow \mu^+ \mu^-$ as probe for New Physics

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Best fit contours in  $\tan\beta$  vs  $M_A$  plane in the NUHM1 model

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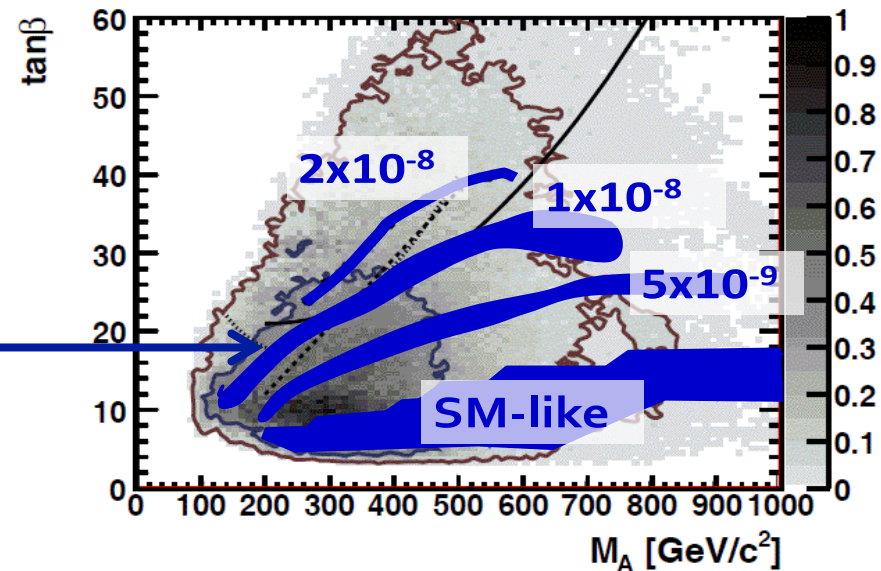
Regions compatible with

$BR(B_s \rightarrow \mu\mu) = 2 \times 10^{-8}, 1 \times 10^{-8}, 5 \times 10^{-9}$  and SM

LHCb calculation using

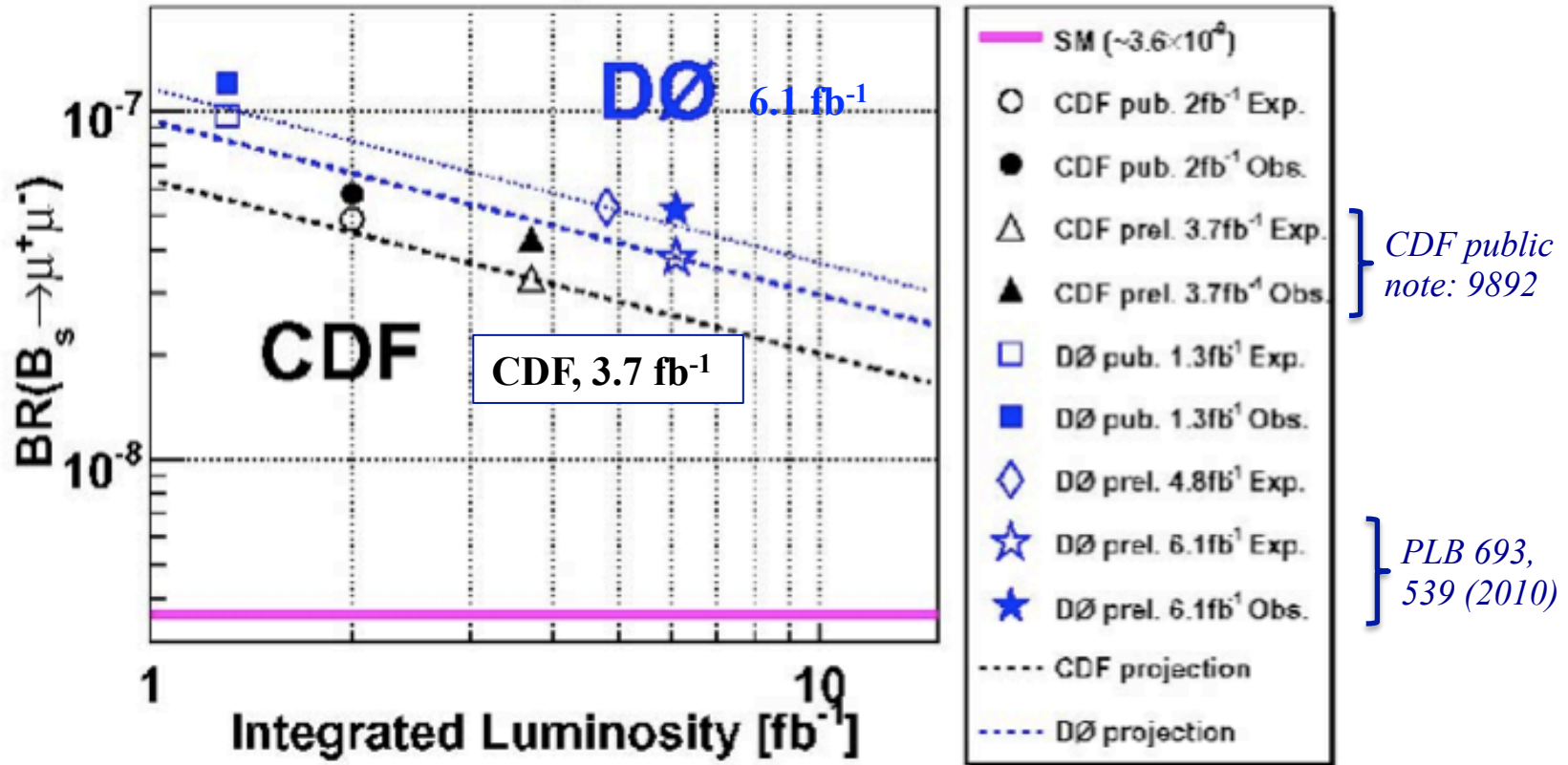
F. Mahmoudi, SuperIso, arXiv: 08083144

$\tan\beta$  vs  $M_A$  plane





## Upper Limits on $BR(B_s \rightarrow \mu^+ \mu^-)$ at 95% C.L. at Tevatron



Limits from Tevatron @ 95% CL:

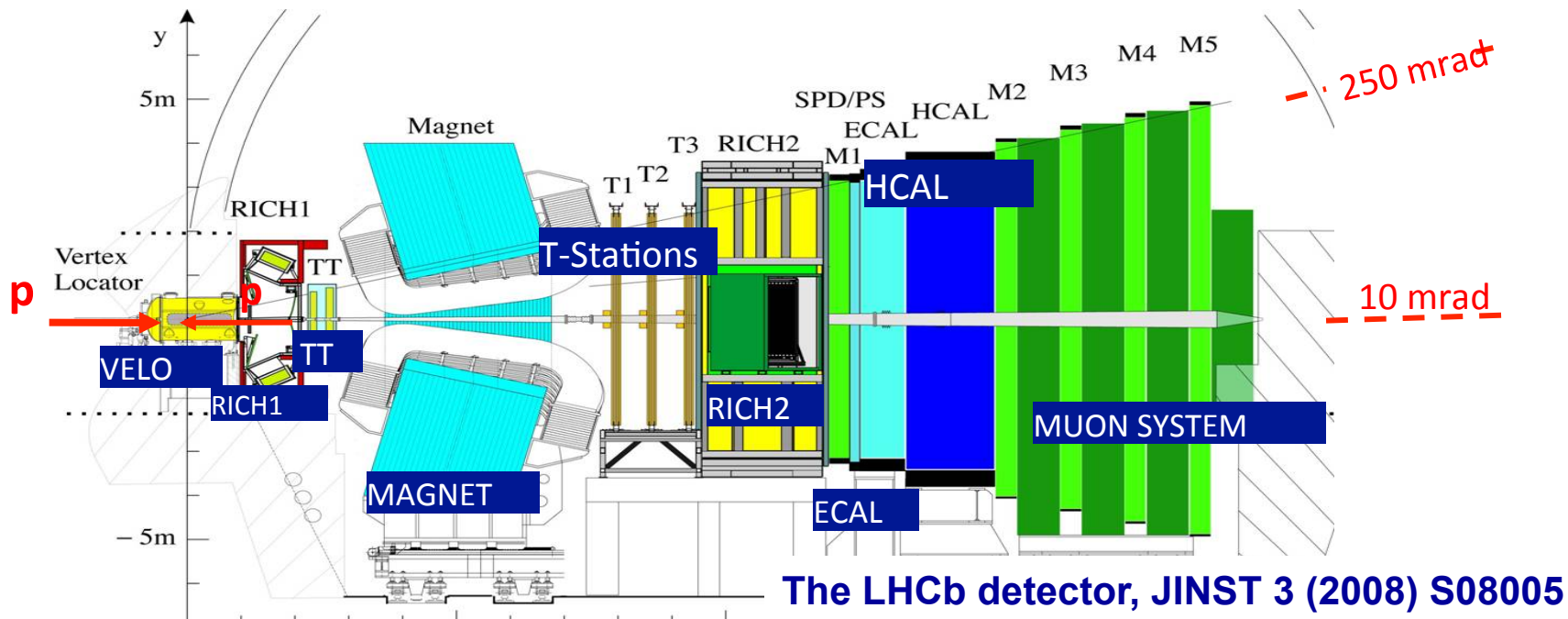
- CDF ( $\sim 3.7 \text{ fb}^{-1}$ ):  $B_S (B_d) \rightarrow \mu\mu < 43 (7.6) \times 10^{-9}$  **factor  $\sim 13$  from SM**
- D0 ( $\sim 6.1 \text{ fb}^{-1}$ ):  $B_S \rightarrow \mu\mu < 51 \times 10^{-9}$

# The LHCb Experiment: Overview of the experiment and performance





# The LHCb detector



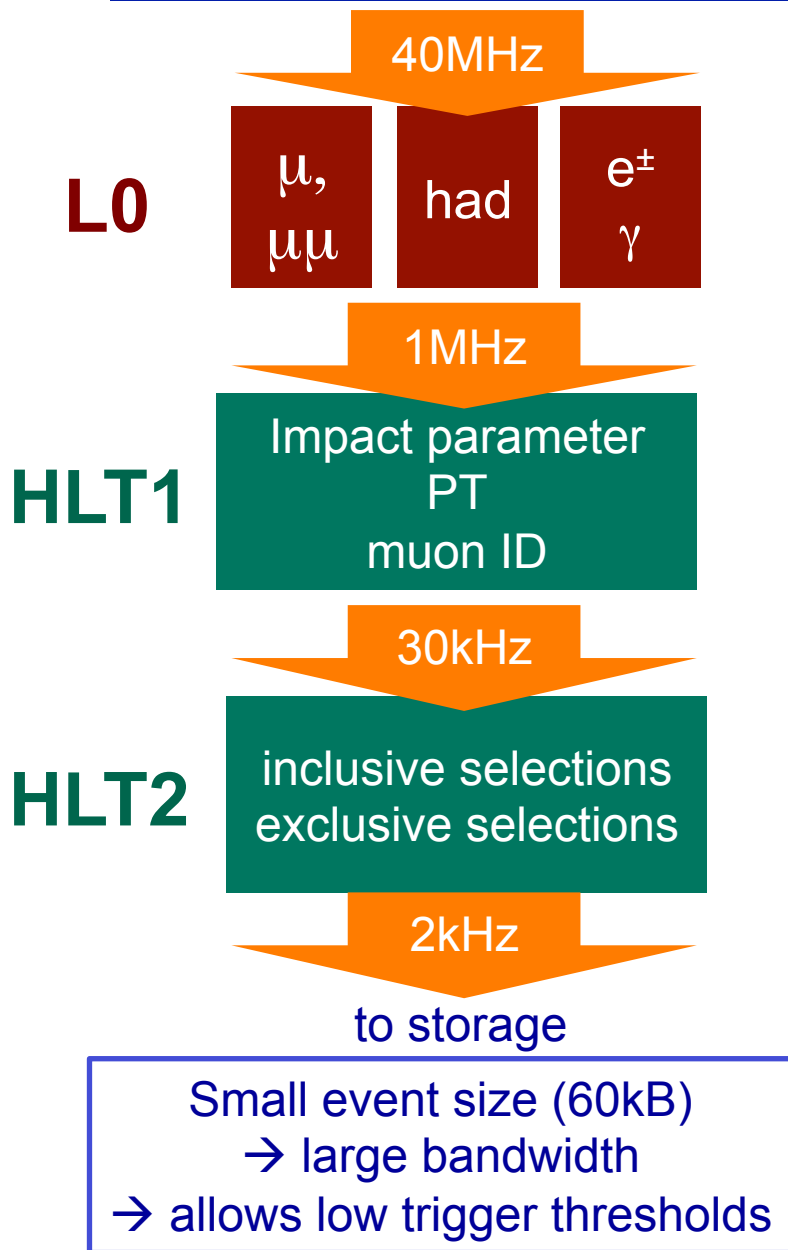
- Huge cross sections:  $\sigma(pp \rightarrow bbX) @ 7 \text{ TeV} \sim 300 \mu\text{b}^*$ 
  - But only 1/200 events contain b quark  $\rightarrow$  Trigger
- Large acceptance  $1.9 < \eta < 4.9$
- Large boost:
  - average flight distance of B mesons  $\sim 10\text{mm}$

**$\rightarrow$  A huge amount of very displaced b's**

(\*) LHCb, Phys.Lett.B 694 (2010) 209



# Keys for b-physics I: Trigger



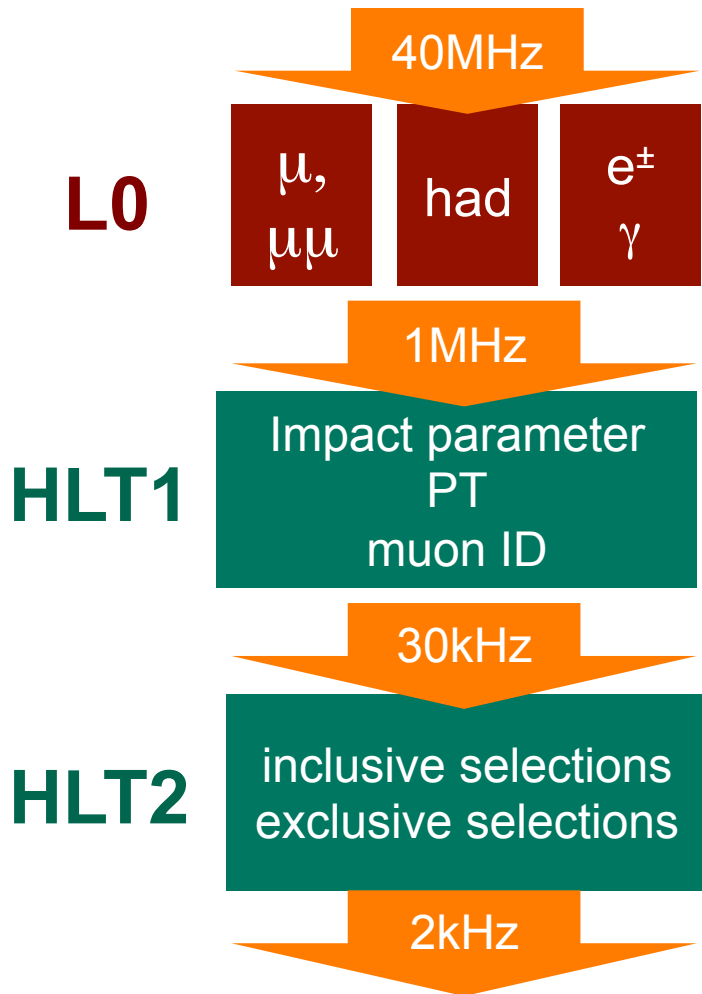
L0 hardware	“high $p_T$ ” signals in calorimeter and muon systems
HLT1 software	Partial reconstruction selection based on one or two tracks (dimuon) displaced in the VELO, muon ID (offline like)
HLT2 software	Global reconstruction (very close to offline) dominantly inclusive signatures

+ Global event cuts rejecting busy events

	Charm	Hadr. B	Lept. B
Global efficiency	~10%	~40%	75-90%

# Keys for b-physics I: Muon trigger

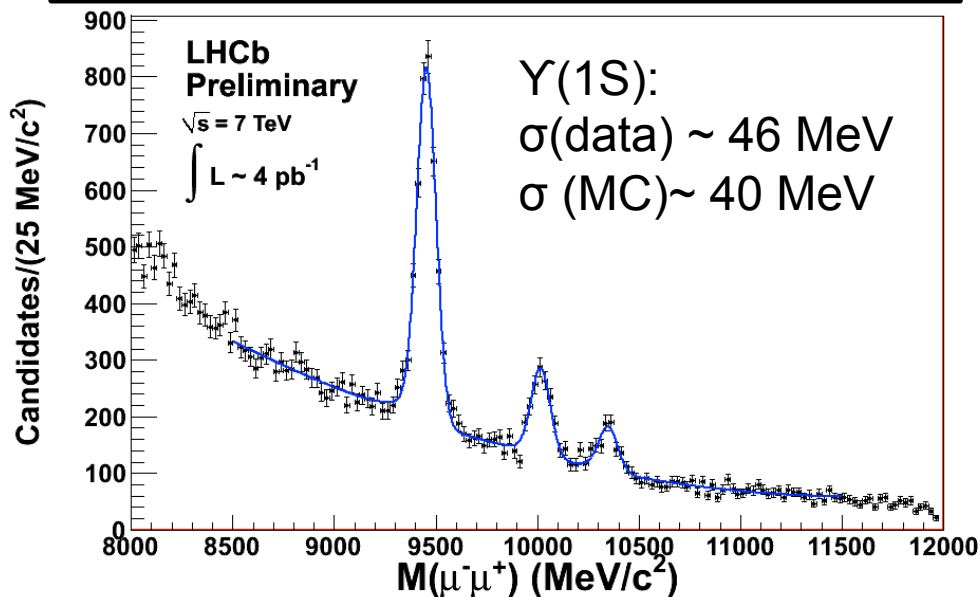
Half of the bandwidth ( $\sim 1$  kHz) given to the muon lines  
 $p_T$  cuts on muon lines kept very low  $\rightarrow$  trigger efficiency very high  
 Trigger rather stable during the whole period (despite L increased by  $\sim 10^5$ )



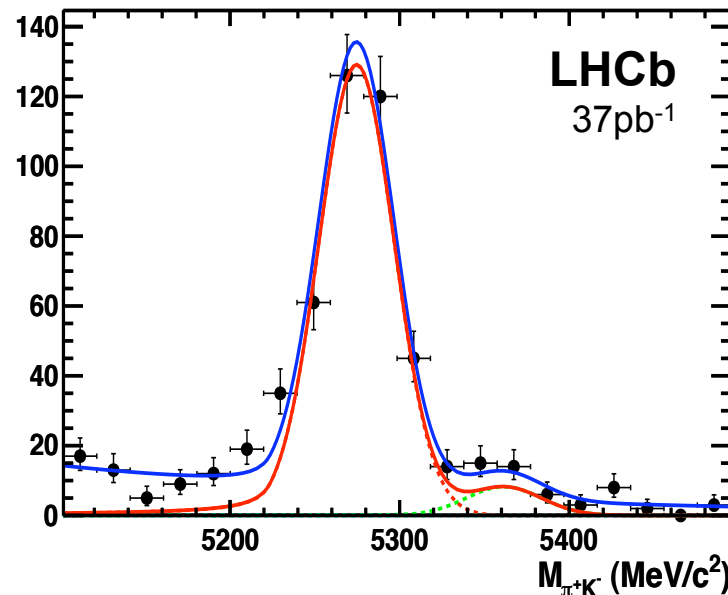
## Muon lines:

<b>L0 hardware</b>	<b>Single-<math>\mu</math>:</b> $p_T > 1.4 \text{ GeV}/c$ <b>Di-<math>\mu</math>:</b> 2 clean muons $p_{T1} > 0.56 \text{ GeV}/c$ $p_{T2} > 0.48 \text{ GeV}/c$
HLT1 software	Single- $\mu$ : $p_T > 0.8 \text{ GeV}/c$ $IP > 0.11 \text{ mm}, IPS > 5$ Single- $\mu$ : $p_T > 1.8 \text{ GeV}/c$ (no IP)
HLT2 software	Dimuon: $M_{\mu\mu} > 4.7 \text{ GeV}/c^2$ $\Delta m(J/\psi) < 120 \text{ MeV}/c^2$  Several lines with $p_T$ and vertex displacement cuts

## $\Upsilon(1S), \Upsilon(2S), \Upsilon(3S)$



## $B^0 \rightarrow K^\pm \pi^\pm$



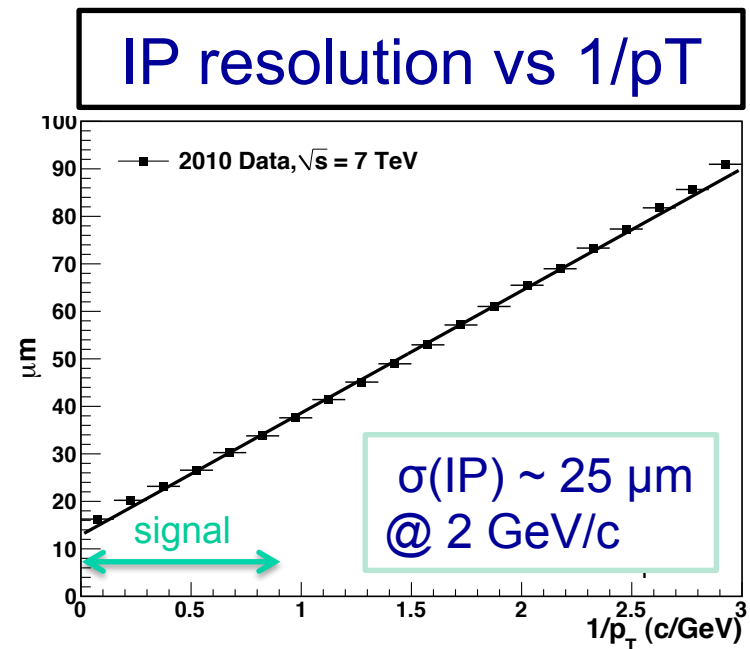
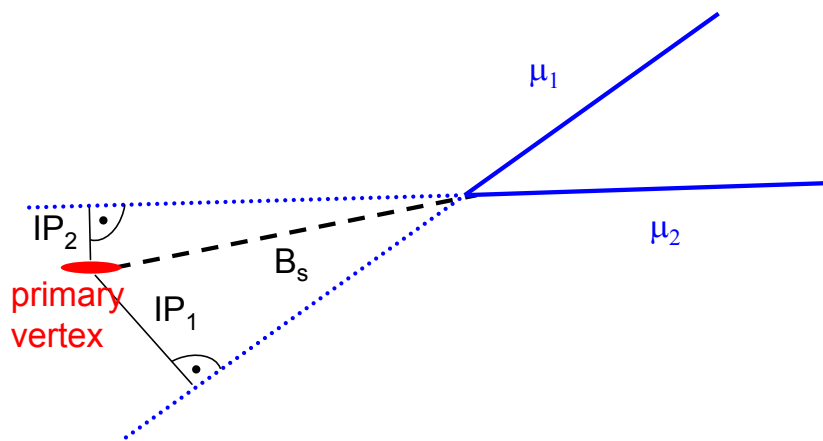
	momentum resolution	mass resolution $J/\psi \rightarrow \mu\mu$
LHCb	$\delta p/p = 0.4-0.6 \%$	13 MeV
CMS	$\delta p_t/p_t = 1-3 \%$	40 MeV
ATLAS	$\delta p_t/p_t = 5-6 \%$	71 MeV



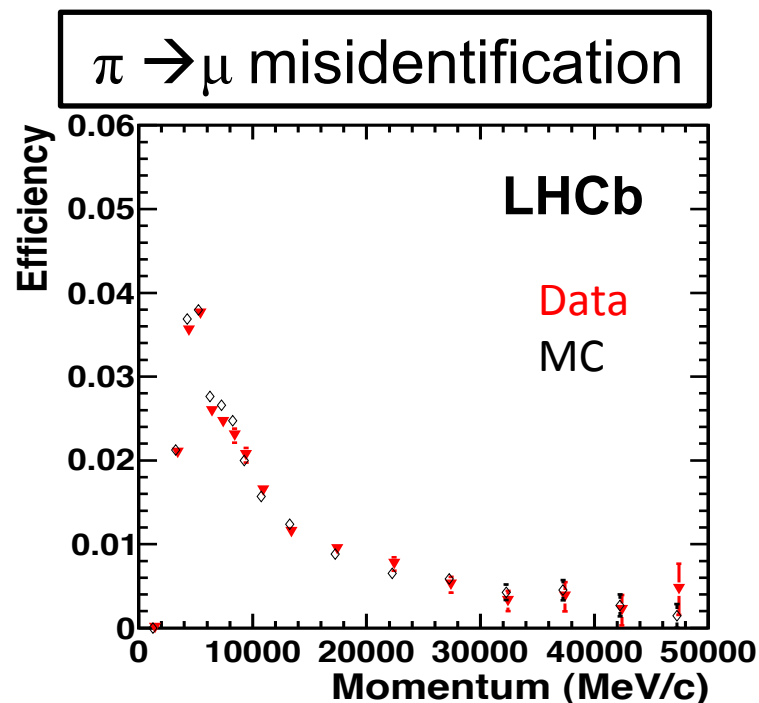
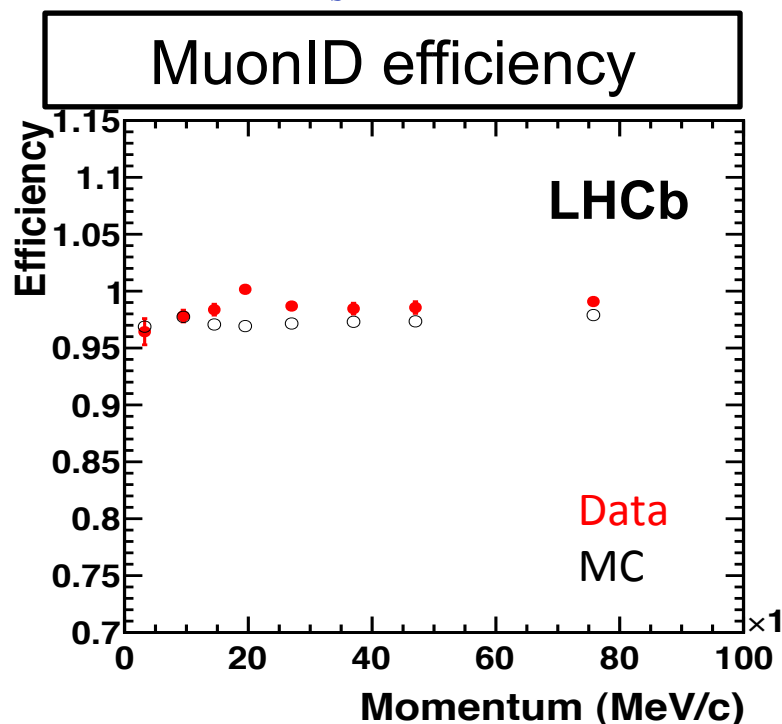
## Primary vertex resolutions ( 25 tracks):

	LHCb [ $\mu\text{m}$ ]	ATLAS [ $\mu\text{m}$ ]	CMS [ $\mu\text{m}$ ]
$\sigma(x)$	15.8	60	20-40
$\sigma(y)$	15.2	60	20-40
$\sigma(z)$	76	100	40-60

## Impact parameter (IP):



- Performance measured with pure samples of  $J/\psi \rightarrow \mu\mu$ ,  $K_s \rightarrow \pi\pi$ ,  $\phi \rightarrow KK$ ,  $\Lambda \rightarrow p \pi$



- Performance in the kinematic range of  $B_s \rightarrow \mu\mu$ :

$$\varepsilon(\mu \rightarrow \mu) \sim (97.1 \pm 1.3)\%$$

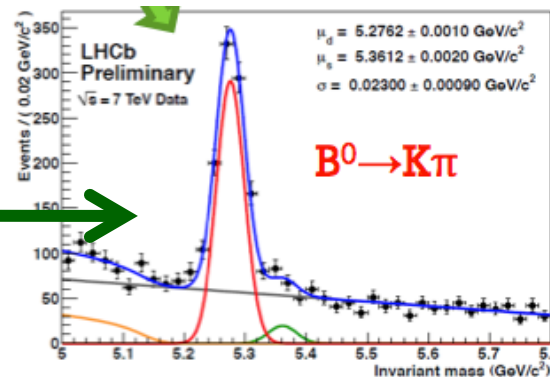
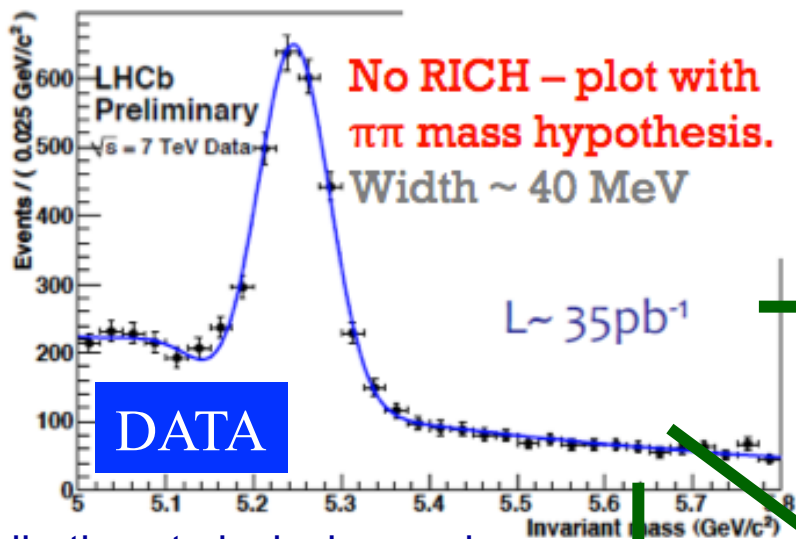
$$\varepsilon(h \rightarrow \mu) \sim (7.1 \pm 0.5) 10^{-3}$$

$$\varepsilon(hh \rightarrow \mu\mu) \sim (3.5 \pm 0.9) 10^{-5}$$

## LHCb capabilities for hadronic physics

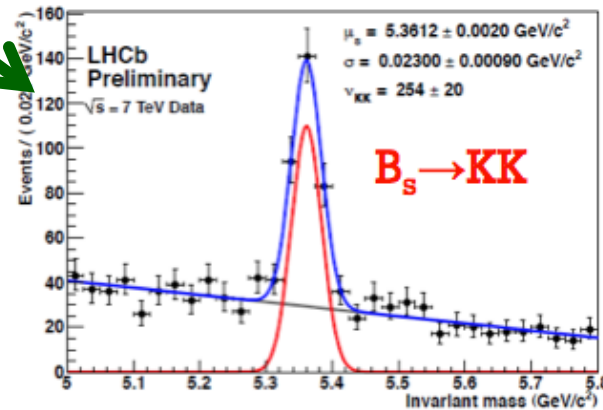
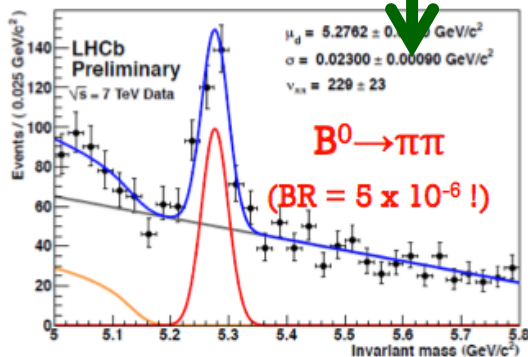
Inclusive  $B_{(s,d)} \rightarrow hh'$

$B_{(s,d)} \rightarrow hh'$  WITH RICH



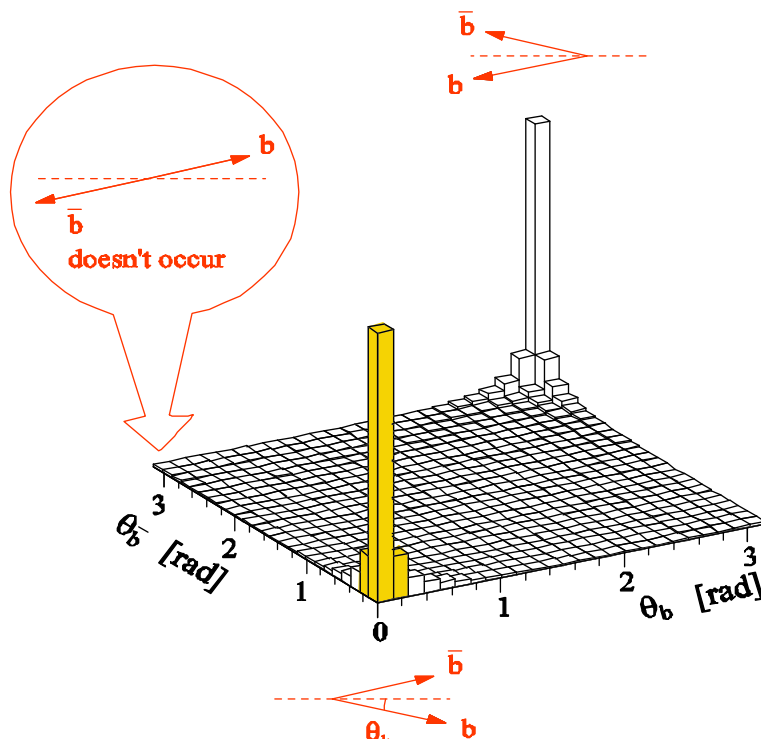
Contributions to inclusive peak:

- $B^0 \rightarrow \pi^+\pi^-$
- $B^0 \rightarrow \pi^+\pi^0$
- $B_s^0 \rightarrow \pi^+\pi^-$
- $B_s^0 \rightarrow \pi^+\pi^0$
- $B_s^0 \rightarrow K^+K^-$
- $B_s^0 \rightarrow K^+K^0$
- $\Lambda_b \rightarrow p\pi^-$
- $\Lambda_b \rightarrow K^+\pi^-$
- $B_s^0 \rightarrow K^+K^-$
- $B_s^0 \rightarrow \pi^+K^-$
- $B_s^0 \rightarrow K^+K^0$
- $\Lambda_b \rightarrow p\pi^-$
- $\Lambda_b \rightarrow K^+\pi^-$

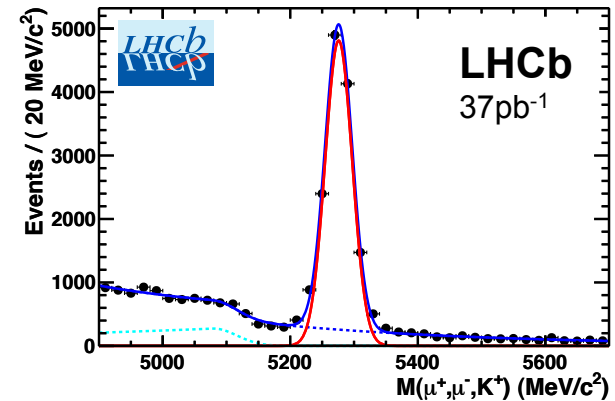




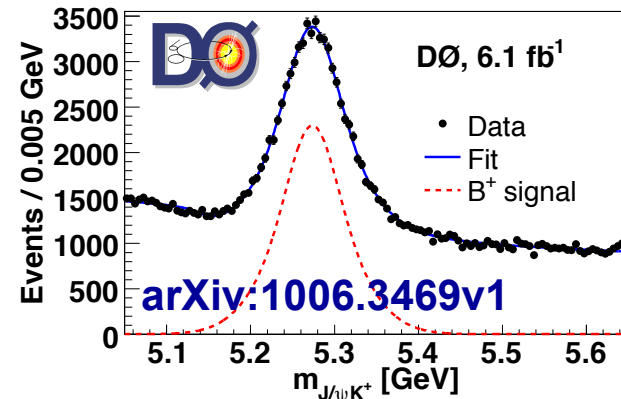
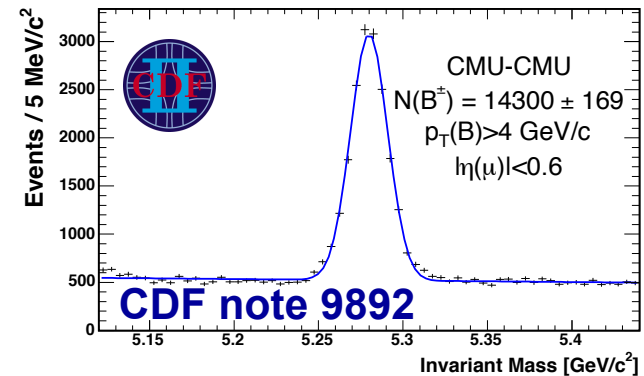
- LHCb: maximize B acceptance @ LHC
  - forward spectrometer,  $1.9 < \eta < 4.9$ 
    - B hadrons produced at low angle
    - B pairs are produced in same forward or backward cone → single arm ok



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CDF II Preliminary 3.7 fb<sup>-1</sup>



Rough estimate for B acceptance:  
compare  $B^\pm \rightarrow J/\psi K^\pm$  yield with CDF / D0

– **LHCb**

$N_{\text{signal}}$ :  $12,366 \pm 403^{\text{stat+syst}}$  (0.037fb<sup>-1</sup>)

– **CDF** (CMU-CM(U+X))

$N_{\text{signal}}$ :  $19,762 \pm 203^{\text{stat+syst}}$  (3.7fb<sup>-1</sup>)

**D0** (RunIIa+b)

$N_{\text{signal}}$ :  $46,803 \pm 1099^{\text{stat+syst}}$  (6.1fb<sup>-1</sup>)

(CDF:  $|\eta| < 1$ ; D0:  $|\eta| < 2$ ; CMS/ATLAS:  $|\eta| < 2.4$ )

- LHCb: maximize B acceptance @ LHC
  - forward spectrometer,  $1.9 < \eta < 4.9$ 
    - B hadrons produced at low angle
    - B pairs are produced in same forward or backward cone → single arm ok

- Rough estimate for B acceptance: compare  $B^\pm \rightarrow J/\psi K^\pm$  yield with CDF / D0

– **LHCb**

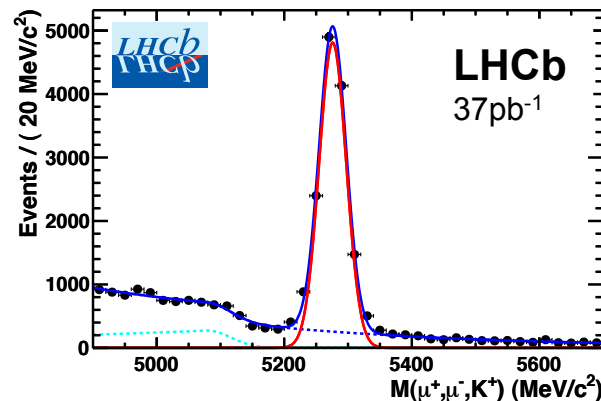
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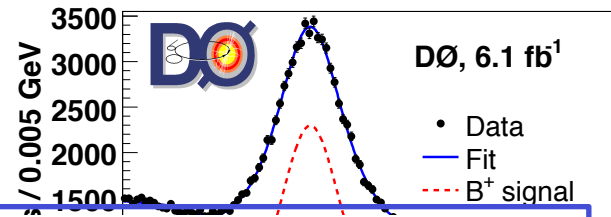
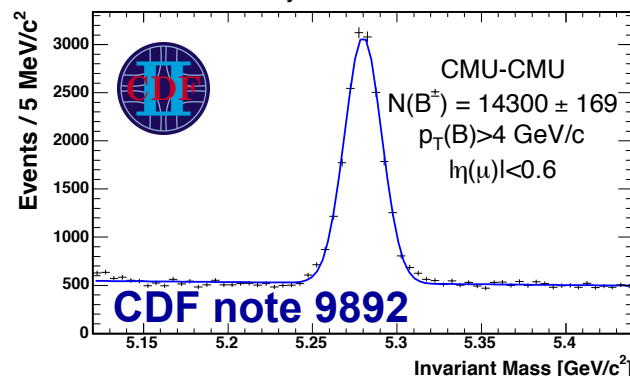
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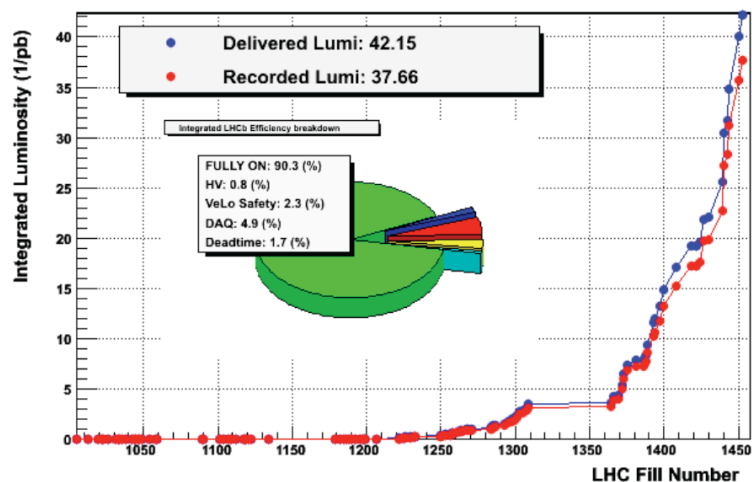


CDF II Preliminary 3.7 fb<sup>-1</sup>



**With 1/100-1/200 of  $\int L dt$ , LHCb records  $1/2$ - $1/4$   $B^\pm$  thanks to acceptance & trigger, cross section, boost**

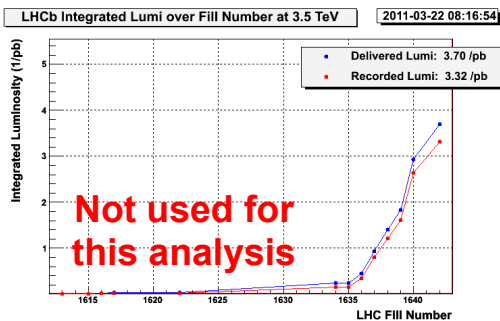
# LHCb operation in 2010



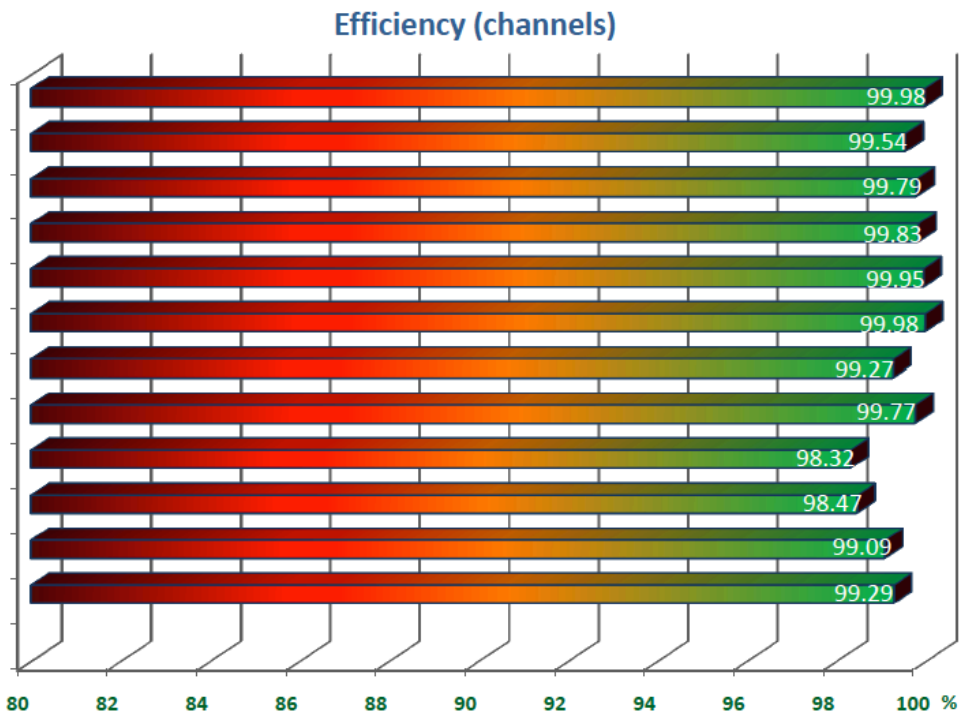
LHCb recorded  $37\text{pb}^{-1}$  of high quality physics data in 2010  
 → dataset for this analysis

Data taking efficiency around 90% over the year

$3.3\text{pb}^{-1}$  recorded in 2011



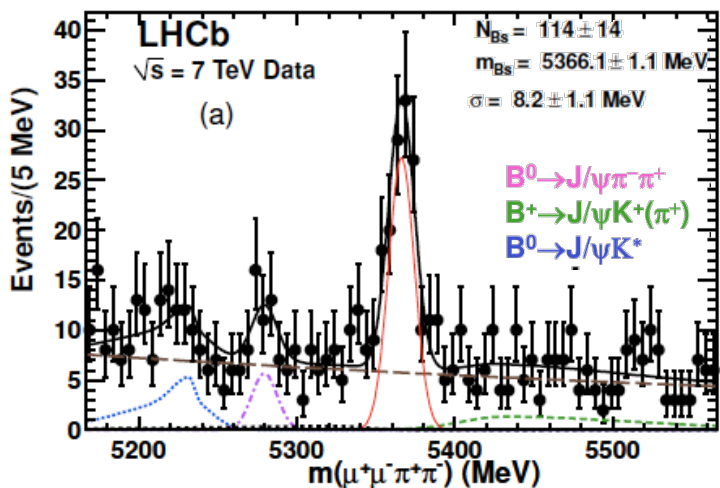
- Muon system 2-5
- Muon station 1
- Hadron Calorimeter
- Electromagnetic Calorimeter
- PreShower
- Scintillator Pad Detector
- RICH 2
- Outer Tracker
- Inner Tracker
- RICH 1
- Tracker Turicensis
- Vertex Locator



**All sub-detectors >99% efficient**

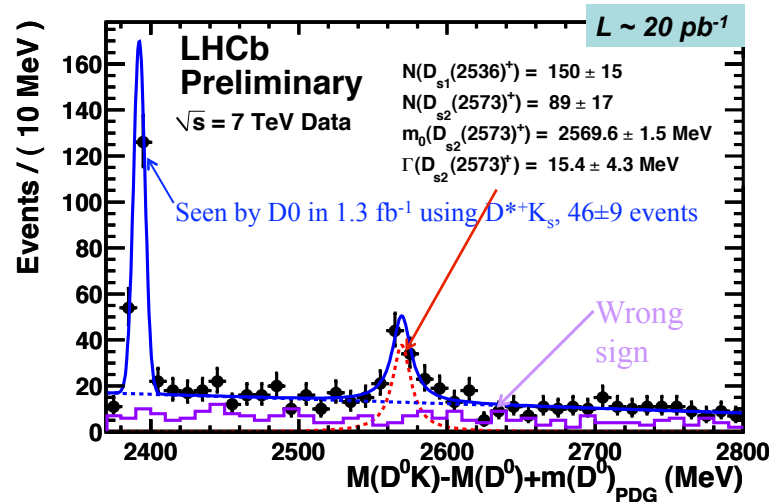


## First observation of $B_s \rightarrow J/\psi f^0(980)$ :



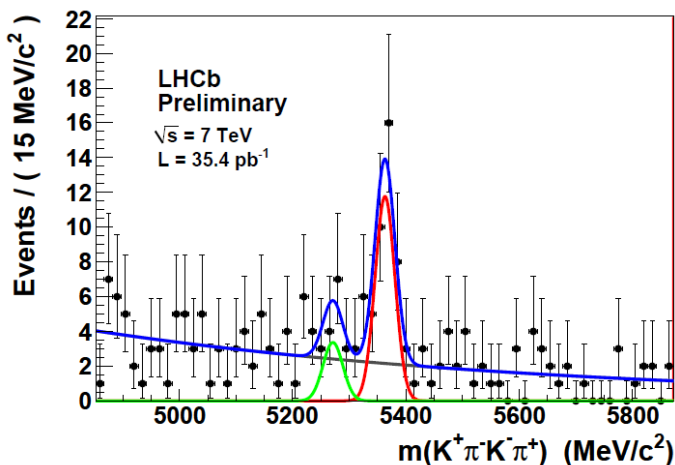
arXiv:1102.0206  
Phys. Lett. B 698 (2011)

## First observation of $B_s \rightarrow D_{s2}^{*+} X_{\mu\nu}$



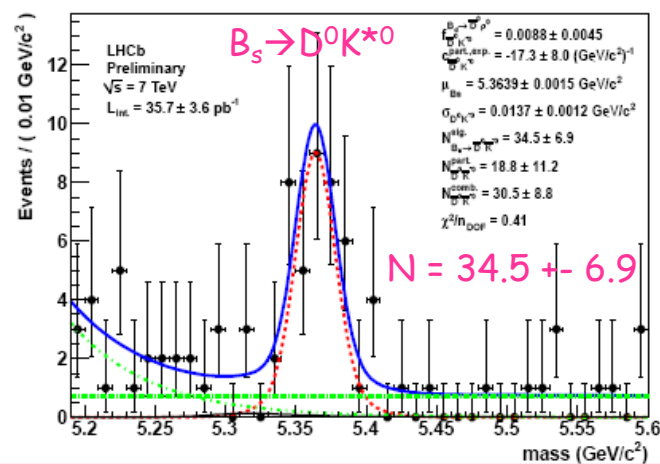
arXiv:1102.0348

## First observation of $B_s \rightarrow K^* K^*$



LHCb-CONF-2011-019

## First observation of $B_s \rightarrow D^0 K^*$

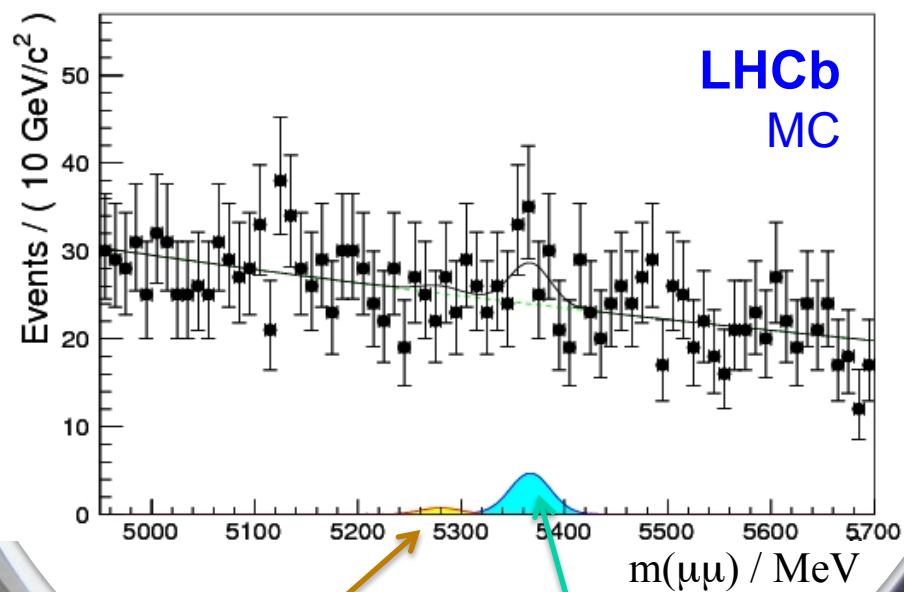


LHCb-CONF-2011-008

# Next observations by LHCb ?

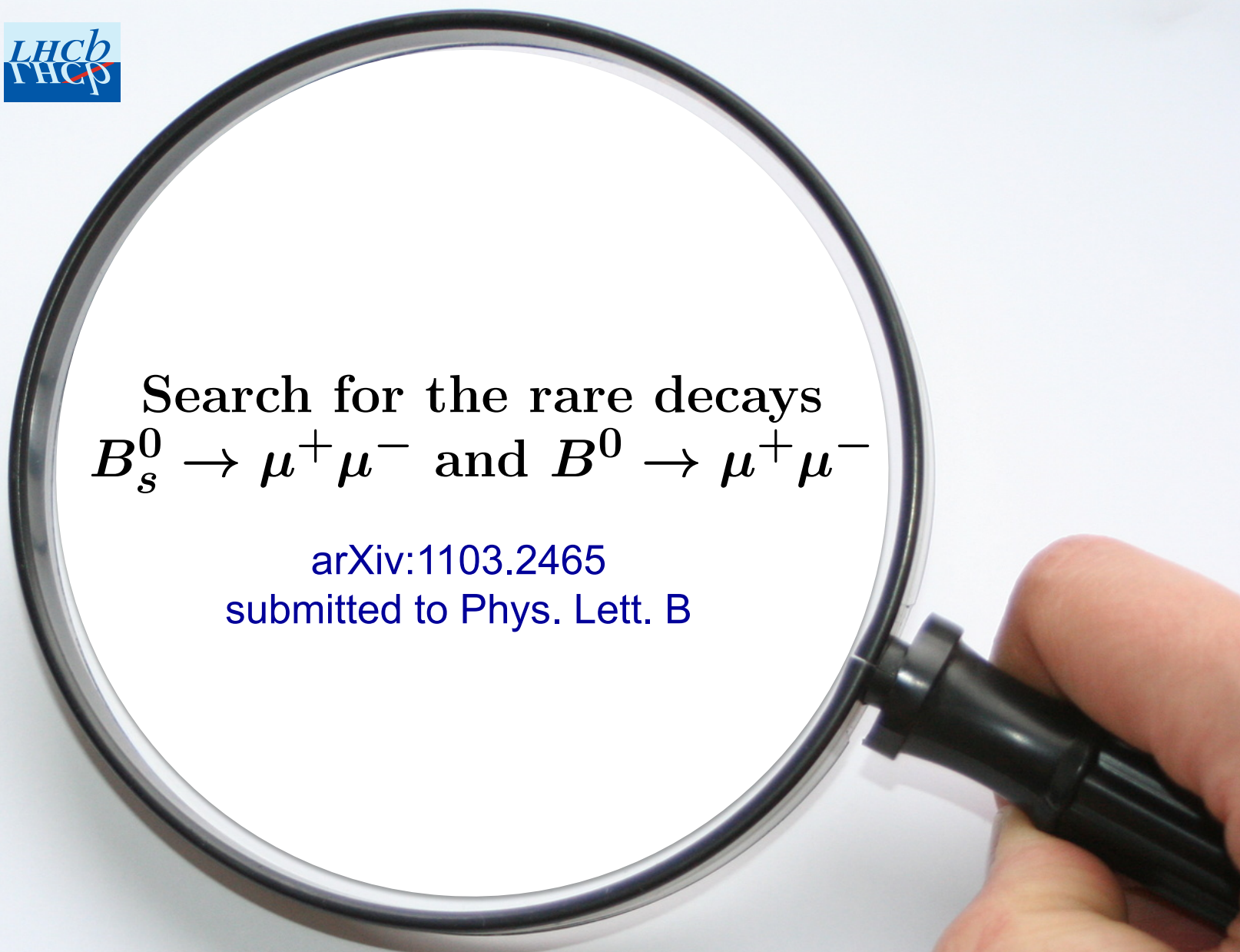
Appetizer with (too) high BR

Dimuon background  
+ 25  $B_s \rightarrow \mu\mu$  events



$B_d \rightarrow \mu\mu$

$B_s \rightarrow \mu\mu$

A hand is holding a magnifying glass over the text. The magnifying glass is positioned over the text, making it larger and clearer. The text is centered within the lens of the magnifying glass.

Search for the rare decays  
 $B_s^0 \rightarrow \mu^+ \mu^-$  and  $B^0 \rightarrow \mu^+ \mu^-$

arXiv:1103.2465  
submitted to Phys. Lett. B

- **Selection**
  - Soft selection to reduce size of dataset
- **Signal and background likelihoods**
  - Geometrical Likelihood (GL)  
Multivariate classifier combining topological and kinematic information
  - Invariant mass
- **Normalization**
  - Convert number of observed events in branching fraction by normalizing with channels of known BR
- **Extraction of the limit**
  - Extract observation / exclusion measurement using the  $CL_S$  method

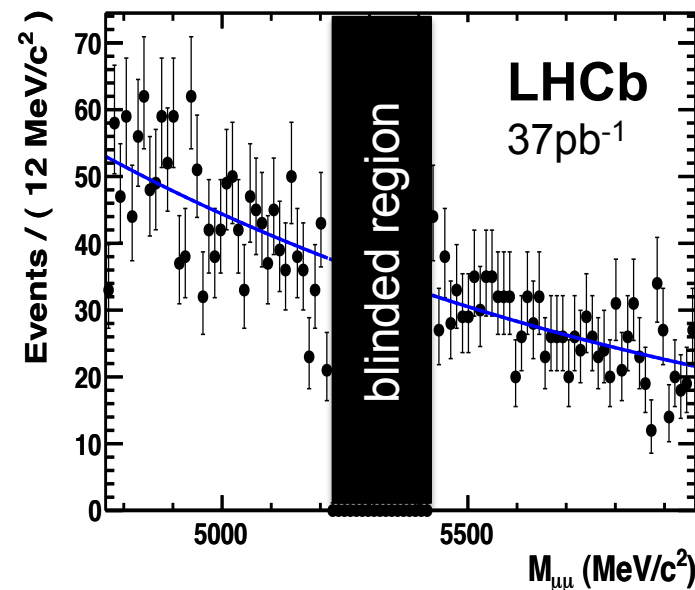


## Search for $B_{d,s} \rightarrow \mu^+ \mu^-$

- Selection
- Signal and background likelihood
- Normalization
  - Extraction of the limit



- Soft selection:
  - pairs of opposite charged muons with high quality tracks, making a common vertex very displaced with respect to the PV and  $M_{\mu\mu} \pm 600 \text{ MeV}/c^2$
- Keeps high signal efficiency:
  - Expected after selection ( $BR=BR^{\text{SM}}$ ):  
 $B_s(B^0) \rightarrow \mu\mu : 0.3 (0.04) \text{ events}$
- Rejects most of the background
  - $\sim 300$  background events in the signal windows  $m(B_{d,s}) \pm 60 \text{ MeV}/c^2$
  - $\sim 3000$  background events ( $M_{\mu\mu} \pm 600 \text{ MeV}/c^2$ )



Signal regions were blinded up to analysis approval

## Background composition after selection:

$bb \rightarrow \mu\mu X$	fake + muon	peaking background
90%	10%	negligible
Double semileptonics and cascade decays	$\sim 0.3\%$ from double fake	<ul style="list-style-type: none"> <li>Double misID from <math>B \rightarrow hh'</math>: <math>&lt; 0.1</math> events in signal region</li> <li>misID well described by MC <math>\epsilon(hh \rightarrow \mu\mu) \sim (3.5 \pm 0.9) 10^{-5}</math></li> </ul>

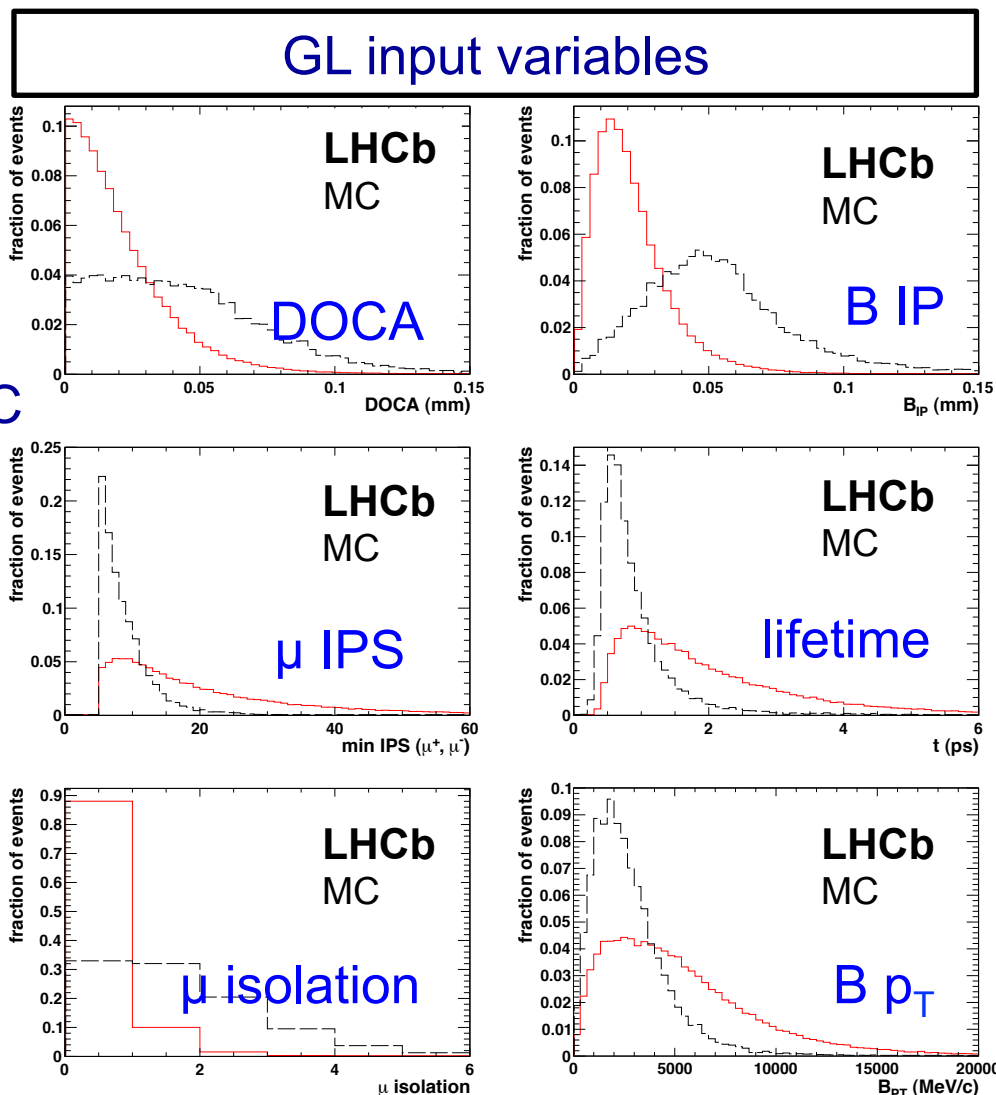
- Remaining background consists of real muons  
 → further signal discrimination from topology of event and invariant mass in likelihoods
- **Remark: precise knowledge of background not necessary for analysis:  
 background estimate taken from sidebands**

## Search for $B_{d,s} \rightarrow \mu^+ \mu^-$

- Selection
- Signal and background likelihoods
- Normalization
  - Extraction of the limit

- After selection:
  - $\sim 0.3 B_s \rightarrow \mu\mu$  signal events expected
  - $\sim 300$  background events
  - Background consists dominantly of real muons
- Create 2D likelihood to classify events:
  - **Geometrical likelihood (GL):**  
combines topological and kinematic information
  - **Invariant mass**
- Geometrical likelihood is *defined* on simulation and *calibrated* on data
  - Analysis does not rely critically on simulation
  - fast analysis possible

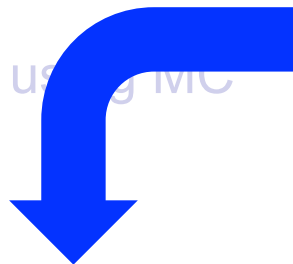
- Combination of kinematic and topological variables
- Variables are decorrelated and a discriminant variable is built
- Optimization and training using MC
  - Signal  $B_s \rightarrow \mu\mu$
  - Background  $bb \rightarrow \mu\mu X$



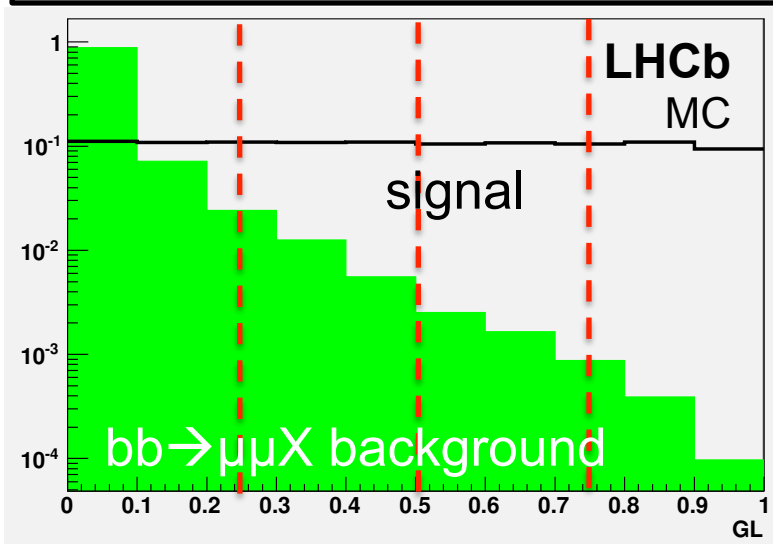
MC  $B_s \rightarrow \mu\mu$   
 MC  $bb \rightarrow \mu\mu X$



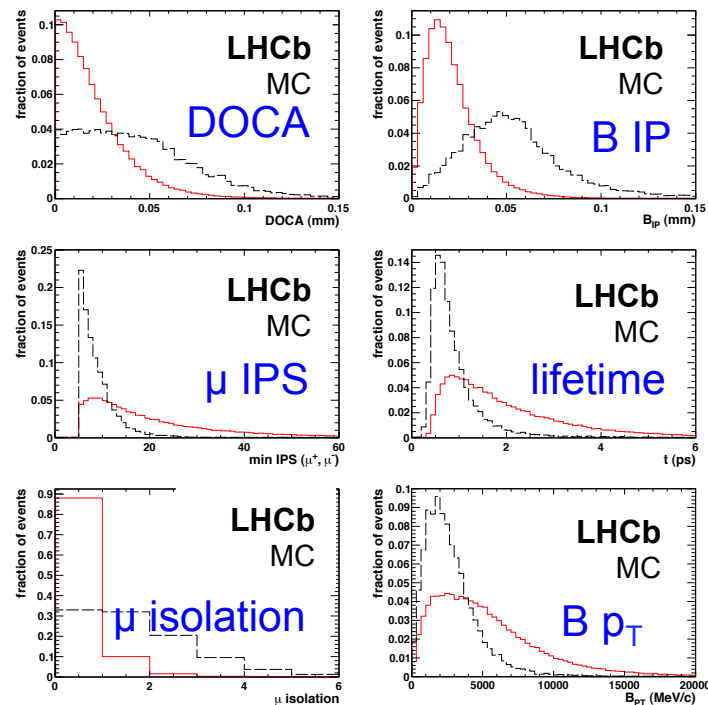
- Combination of kinematic and topological variables
- Variables are decorrelated and a discriminant variable is built
- Optimization and training using MC
  - Signal  $B_s \rightarrow \mu\mu$
  - Background  $bb \rightarrow \mu\mu X$



## GL shape of signal and bkg



## GL input variables

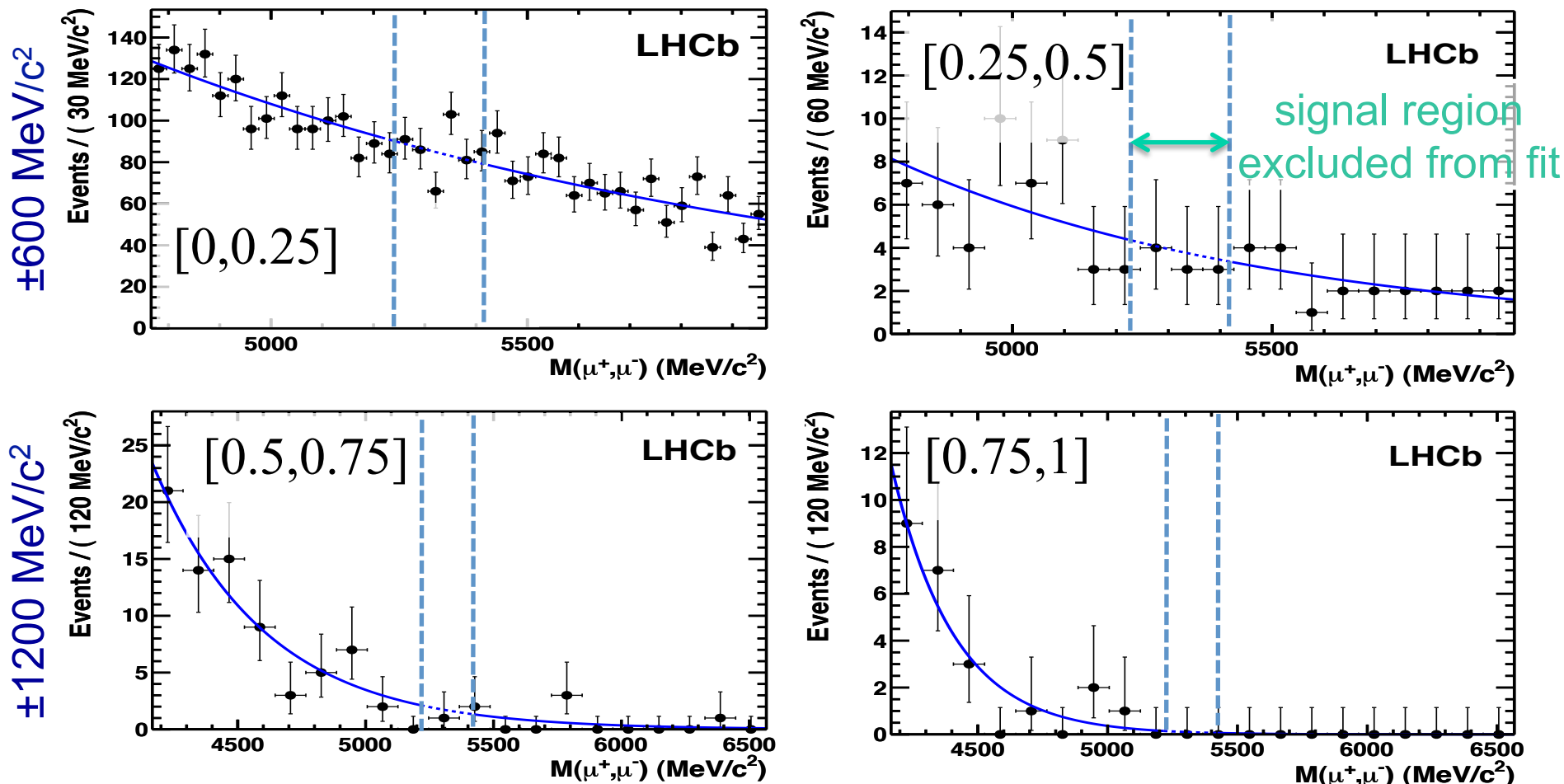


- flat for signal
- peaked at zero for background

Analysis is done in 4 bins of GL

- Calibration of likelihoods from data:
  1. Background
    - Both GL and invariant mass are calibrated simultaneously from mass sidebands
  2. Signal:
    - a) GL calibrated with  $B \rightarrow h^+ h'^-$
    - b) Invariant mass shape from  $B \rightarrow h^+ h'^-$  and dimuon resonances

Expected background in signal region is extracted from a fit to mass sidebands divided in GL bins

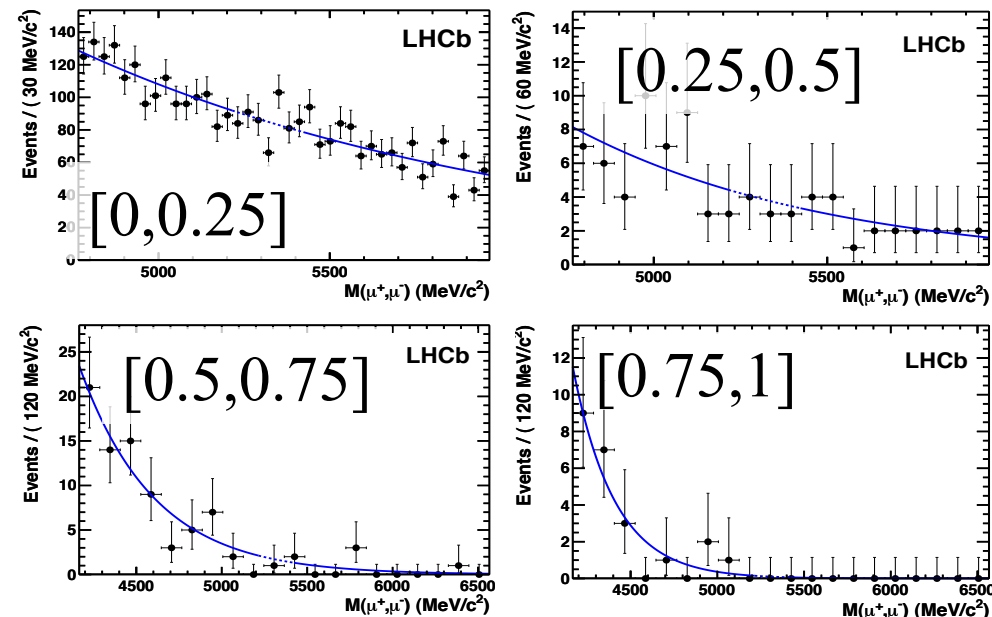


Very low background in regions of high sensitivity

Expected background in signal region is extracted from a fit to mass sidebands divided in GL bins

Invariant mass in GL bins

Expected background events in  $B_{s,d}$  mass regions

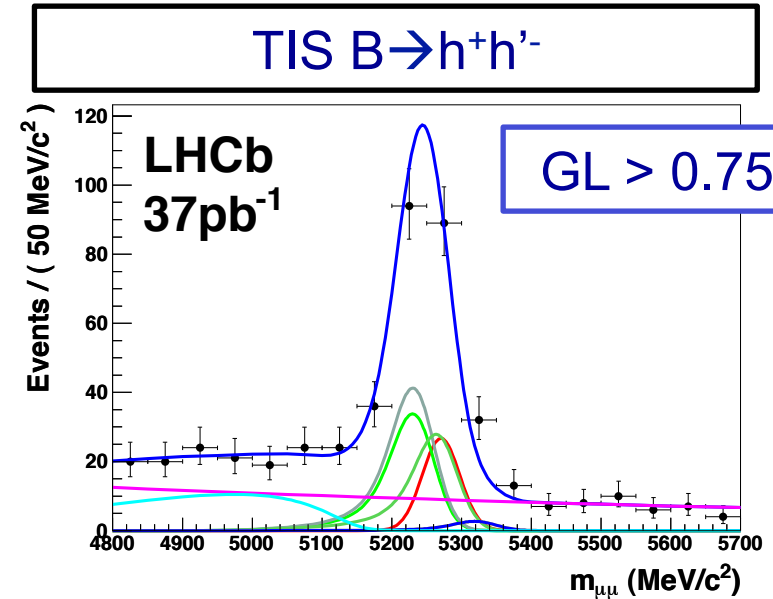


GL	$B_s \rightarrow \mu\mu$	$B^0 \rightarrow \mu\mu$
$[0, 0.25]$	$329.1 \pm 6.4$	$351.6 \pm 6.6$
$[0.25, 0.5]$	$7.4 \pm 1$	$8.3^{+1.1}_{-1.0}$
$[0.5, 0.75]$	$1.51^{+0.41}_{-0.35}$	$1.85^{+0.45}_{-0.39}$
$[0.75, 1]$	$0.08^{+0.10}_{-0.05}$	$0.13^{+0.13}_{-0.07}$

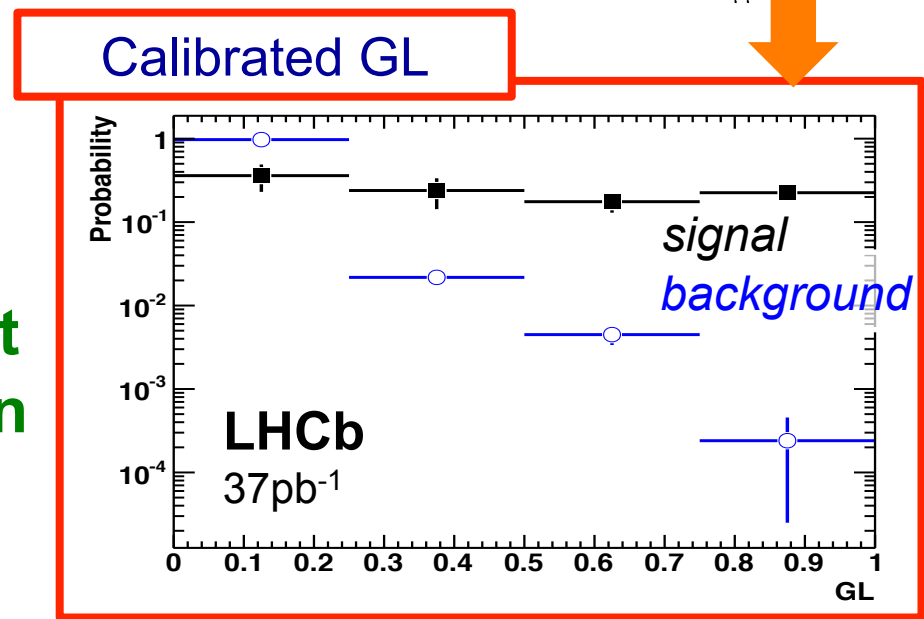
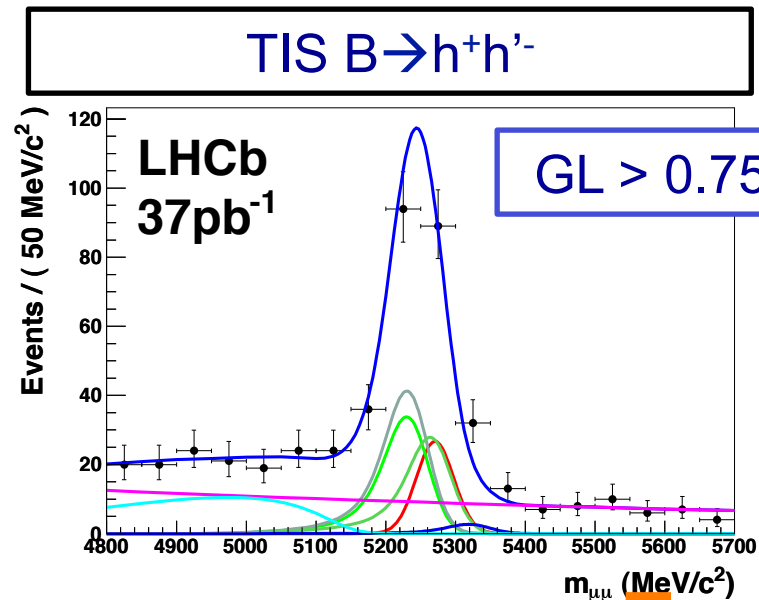
Very low background in sensitive region



- $B \rightarrow h^+ h'^-$  ideal sample for GL calibration
  - Identical decay topology
  - Use events triggered independent of signal (TIS) to avoid trigger bias
- Inclusive  $B \rightarrow h^+ h'^-$  fit
  - Fit all  $B \rightarrow h^+ h'^-$  channels simultaneously
  - uses constrained BR (PDG)



- $B \rightarrow h^+ h'^-$  ideal sample for GL calibration
  - Identical decay topology
  - Use events triggered independent of signal (TIS) to avoid trigger bias
- Inclusive  $B \rightarrow h^+ h'^-$  fit
  - Fit all  $B \rightarrow h^+ h'^-$  channels simultaneously
  - uses constrained BR (PDG)
- **Signal distribution in GL flat as expected from simulation**



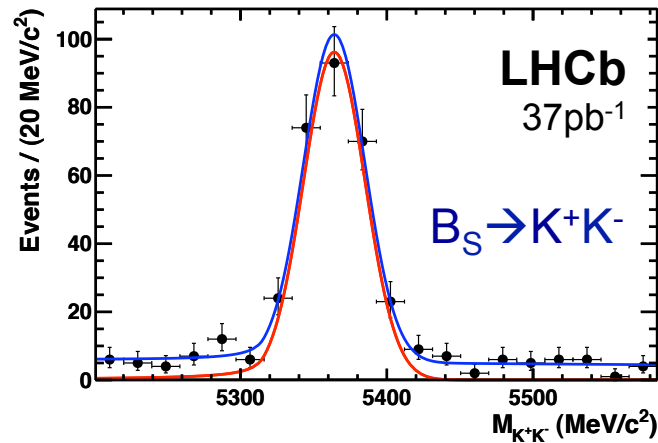
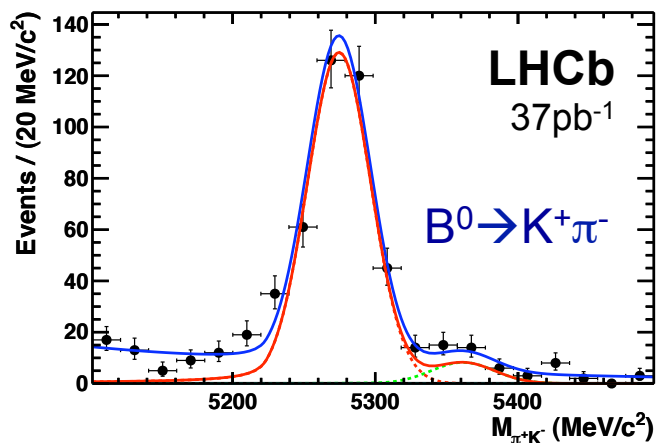
- Parameters of crystal ball (mean, resolution) from data
  - **Central value:** fit to exclusive  $B^0$  and  $B_s$  decays
  - **Resolution:** average from
    - Inclusive  $B \rightarrow hh'$  (identical topology)
    - dimuon resonances

# Signal invariant mass calibration: Mean

- Parameters of crystal ball (mean, resolution) from data
  - **Central value:** fit to exclusive  $B^0$  and  $B_s$  decays
  - **Resolution:** average from
    - Inclusive  $B \rightarrow hh'$  (identical topology)
    - dimuon resonances

## Central value of invariant mass:

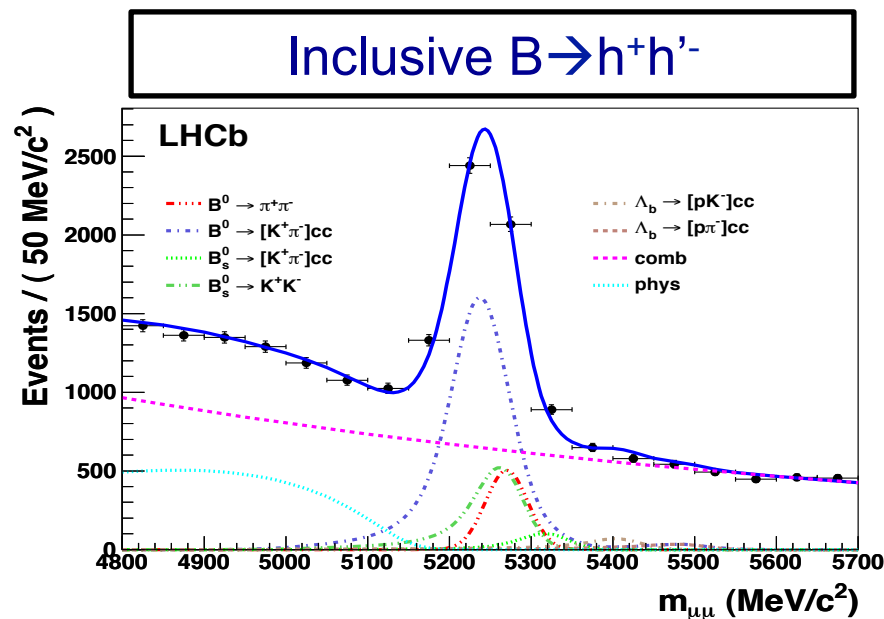
Select exclusive  $B^0 \rightarrow K^+\pi^-$  and  $B_s \rightarrow K^+K^-$  by using RICH particle ID



$$m(B^0) = 5275.0 \pm 1.0 \text{ MeV}/c^2$$

$$m(B_s) = 5363.1 \pm 1.5 \text{ MeV}/c^2$$

- Mass resolution from  $B \rightarrow h^+ h'^-$ 
  - No use of PID info
    - would bias  $\sigma$
  - BR fixed to PDG values
- Signal resolution from  $B \rightarrow h^+ h'^-$ :  
 $\sigma = 25.8 \pm 1.0^{\text{stat}} \pm 2.7^{\text{syst}} \text{ MeV}/c^2$





- Mass resolution of resonances depends linearly on the mass
  - interpolate between  $J/\psi$ ,  $\psi(2S)$  and  $\Upsilon(1S)$ ,  $\Upsilon(2S)$ ,  $\Upsilon(3S)$
  - momentum spectrum of resonances reweighted to the  $B_s \rightarrow \mu\mu$  one

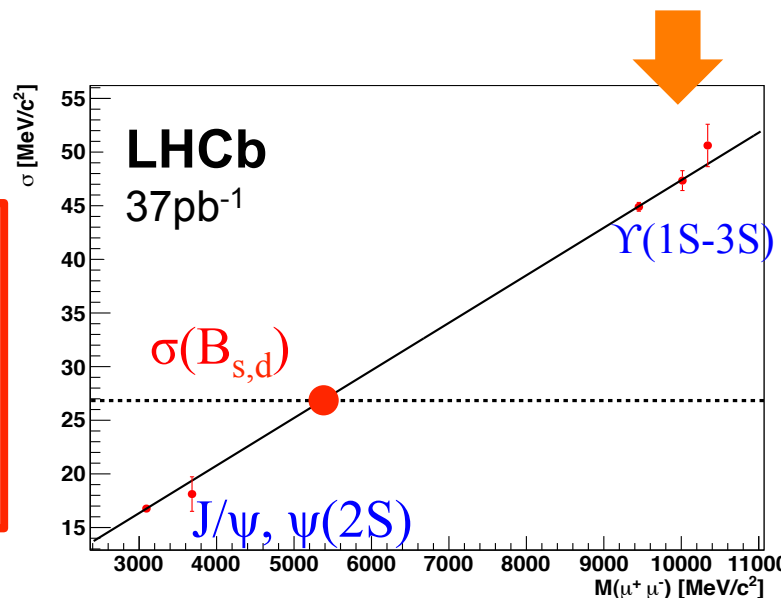
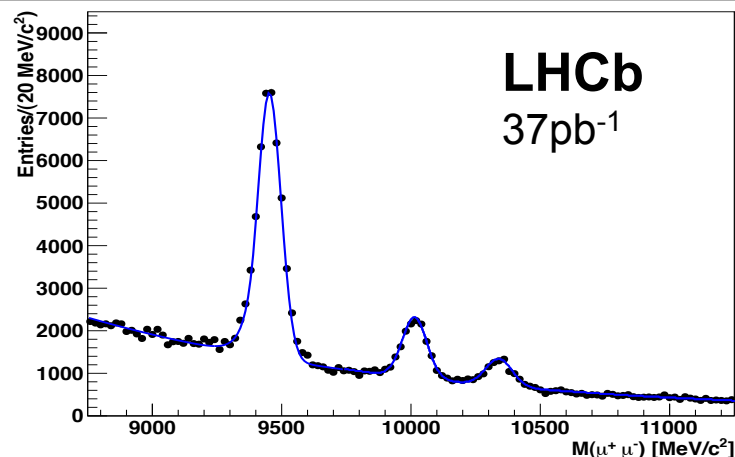
- Resolution from interpolation:  
 $\sigma(B_{S,d}) = 26.8 \pm 0.1^{\text{stat}} \pm 1^{\text{syst}} \text{ MeV}/c^2$

**Weighted average of signal resolution:**

$$\sigma(B_{S,d}) = 26.7 \pm 0.9^{\text{stat+syst}} \text{ MeV}/c^2$$

CDF (D0) :  $\sigma(M) \sim 24 (120) \text{ MeV}/c^2$

The  $\Upsilon$  family:  $\Upsilon(1S)$ ,  $\Upsilon(2S)$ ,  $\Upsilon(3S)$



## Search for $B_{d,s} \rightarrow \mu^+ \mu^-$

- Selection
- Signal and background likelihoods
- **Normalization**
  - Extraction of the limit

Normalize measured events to a channel with known BR

→ many uncertainties cancel

→ no knowledge of luminosity or cross section needed

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

# Normalization channels

Normalize measured events to a channel with known BR

→ many uncertainties cancel

→ no knowledge of luminosity or cross section needed

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

Three independent normalization channels used:

$B^\pm \rightarrow J/\psi(\mu\mu) K^\pm$	$B_s \rightarrow J/\psi(\mu\mu) \phi(KK)$	$B^0 \rightarrow K^+ \pi^-$
BR = $5.98 \times 10^{-5}$ ( $\pm 3.7\%$ )	BR = $3.35 \times 10^{-5}$ ( $\pm 26\%$ )	BR = $1.94 \times 10^{-5}$ ( $\pm 3.1\%$ )
<ul style="list-style-type: none"> <li>• Similar trigger and PID</li> <li>• Tracking efficiency (+1track) dominates error on efficiency ratio</li> <li>• <math>f_d/f_s</math> dominates overall uncertainty</li> </ul>	<ul style="list-style-type: none"> <li>• Similar trigger and PID</li> <li>• Tracking efficiency (+2tracks) dominates error on efficiency ratio</li> <li>• BR dominates overall uncertainty</li> </ul>	<ul style="list-style-type: none"> <li>• Different trigger → <b>use events triggered independent of signal</b></li> <li>• Identical topology</li> <li>• Uncertainty from <math>f_d/f_s</math>, trigger, mass fit</li> </ul>

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

Currently use HFAG average of LEP/Tevatron value:  $f_d/f_s = 3.71 \pm 0.47$

## LHCb already provides (preliminary) results

- Measure  $f_d/f_s$  in the relative yields of  $B^0 \rightarrow D^\pm K^\pm$  or  $B^0 \rightarrow D^\pm \pi^\pm$  to  $B_s \rightarrow D_s^\pm \pi^\pm$

Fleischer et al, Phys.Rev.D83,014017 (2011)

**NEW:** with  $35\text{pb}^{-1}$  LHCb measures

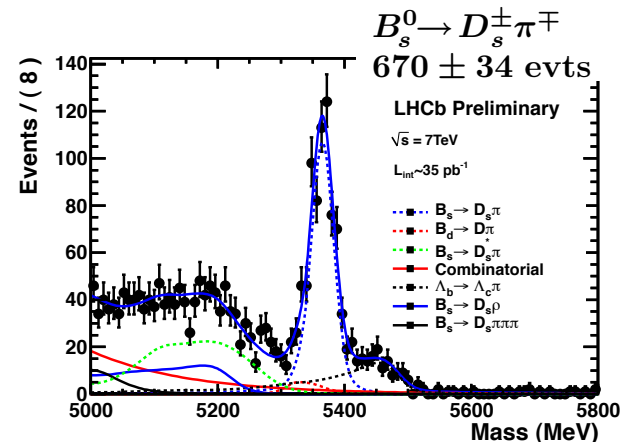
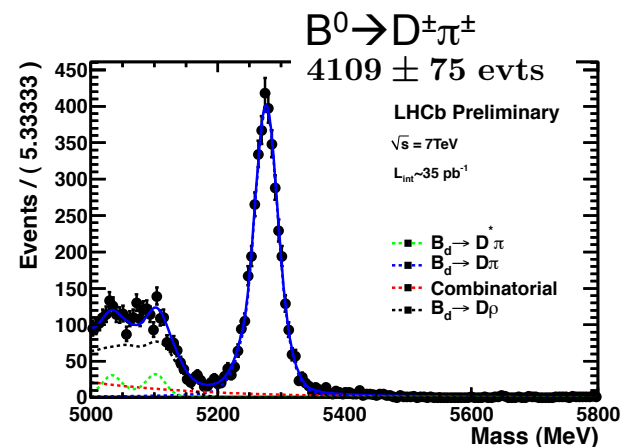
$$\frac{f_{B_d^0}}{f_{B_s}} = 4.02 \pm 0.52$$

(using  $B^0 \rightarrow D^\pm \pi^\pm$ )

LHCb-CONF-2011-013

- Also preliminary result from semileptonics:

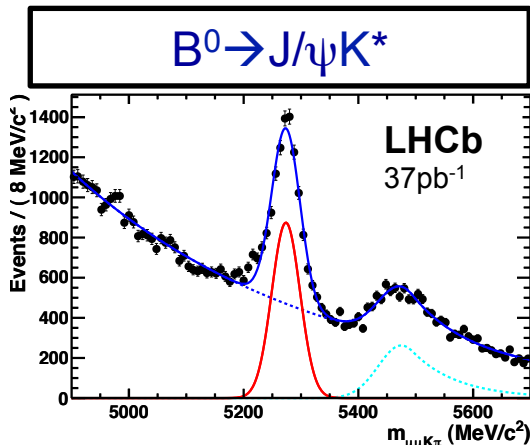
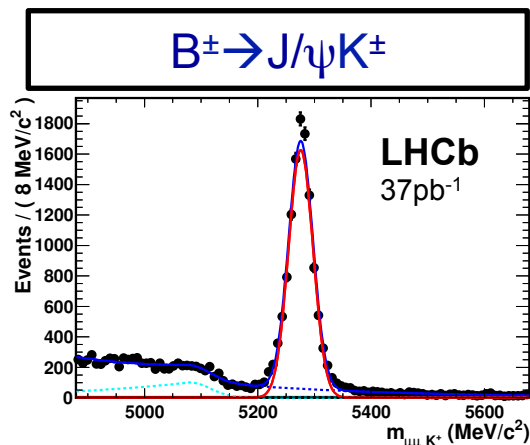
$$\frac{f_{B_d^0}}{f_{B_s}} = 3.84 \pm 0.34 \text{ preliminary}$$





$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

- Ratio of reconstruction / acceptance and selection efficiencies from simulation, dominated by
  - $B^\pm \rightarrow J/\psi K^\pm$ ,  $B_s \rightarrow J/\psi \phi$ : acceptance and cuts for extra track(s)
  - $B \rightarrow hh'$ : material interactions, no muon ID
- X-check: Yield ratio 4-body / 3-body B decays in data
  - Gives reconstruction efficiency / acceptance for extra track



$$\frac{\epsilon_{B^0 \rightarrow J/\psi K^*}^{Rec}}{\epsilon_{B^\pm \rightarrow J/\psi K^\pm}^{Rec}} \propto \frac{\epsilon_{B^\pm \rightarrow J/\psi K^\pm}^{Rec}}{\epsilon_{B_s \rightarrow \mu\mu}^{Rec}}$$

Good data / MC agreement

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

- Ratio of reconstruction / acceptance and selection efficiencies from simulation, dominated by
  - $B^\pm \rightarrow J/\psi K^\pm$ ,  $B_s \rightarrow J/\psi \phi$ : acceptance and cuts for extra track(s)
  - $B \rightarrow hh'$ : material interactions, no muon ID

Ratio of reconstruction, selection efficiencies & acceptance:

$B^\pm \rightarrow J/\psi K^\pm$	$B_s \rightarrow J/\psi \phi$	$B \rightarrow hh'$
$0.49 \pm 0.02$	$0.25 \pm 0.02$	$0.82 \pm 0.06$

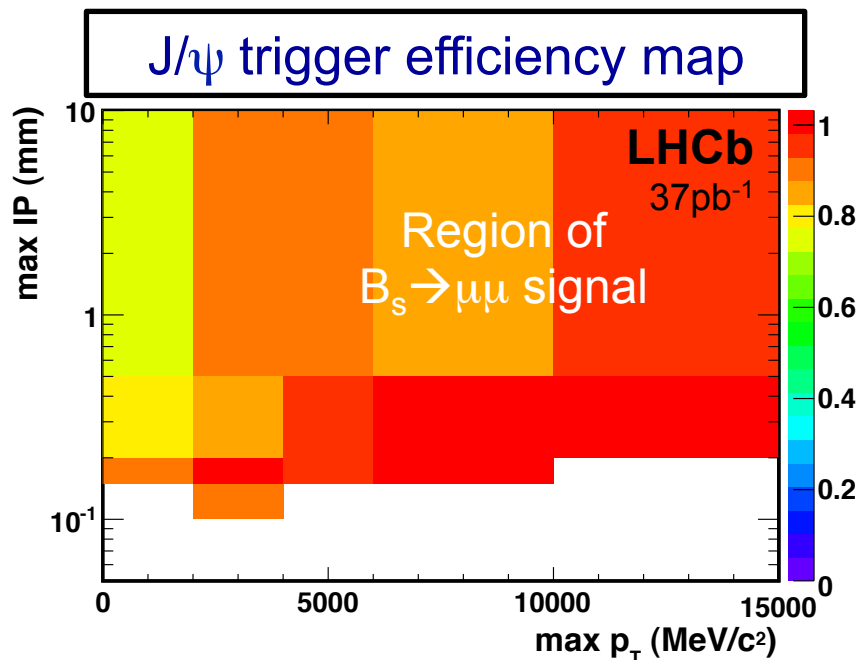
# Trigger efficiency ratio: $J/\psi$ channels

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

- Trigger efficiency determined purely from data
  - use independent trigger decisions to measure efficiency
- Efficiency for  $B_s \rightarrow \mu\mu$  signal:
  - parameterize trigger efficiency with inclusive detached  $J/\psi$  sample
  - apply harder  $B_s \rightarrow \mu\mu$  spectra:  
trigger efficiency:  $\epsilon^{B_s \rightarrow \mu\mu} = 90 \pm 4\%$

Ratio of trigger efficiencies:

$B_{S,d} \rightarrow J/\psi X$
$0.96 \pm 0.05$



$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

- $B^0 \rightarrow K^+ \pi^-$ : normalize to trigger independent sample (TIS)
- Efficiency to trigger independent of the signal is **independent of the signal**
  - Measure from  $B^\pm \rightarrow J/\psi K^\pm$  candidates
    - higher yield allows more precise efficiency determination

Ratio of trigger efficiencies:

**$B \rightarrow hh'$  (TIS)**

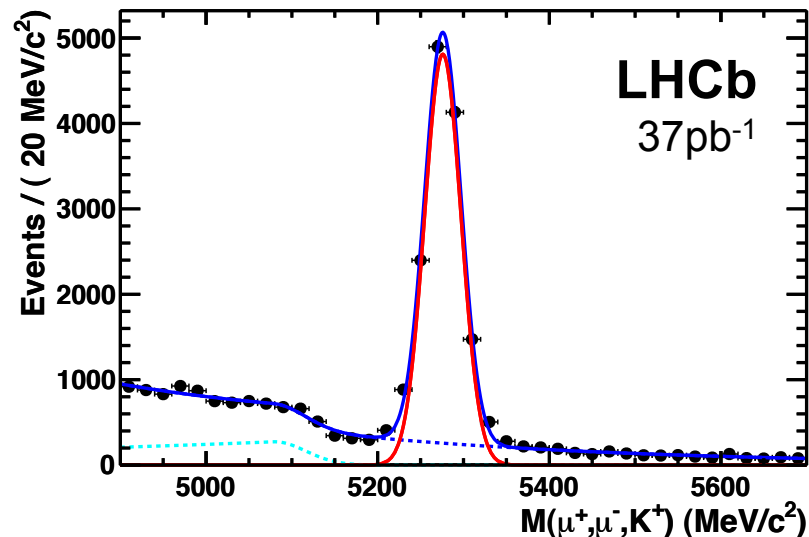
$7.2 \pm 1.0$  %

# First normalization factor : $B^\pm \rightarrow J/\psi K^\pm$

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

- $B^\pm \rightarrow J/\psi K^\pm$ :  $12,366 \pm 403^{\text{stat+syst}}$ 
  - 3% systematics from fit model and duplicated candidates
  - No RICH PID used
- Normalization factor:**
  - $\alpha(B_s \rightarrow \mu\mu) = 8.4 \pm 1.3 \times 10^{-9}$
  - $\alpha(B^0 \rightarrow \mu\mu) = 2.27 \pm 0.18 \times 10^{-9}$

$B^\pm \rightarrow J/\psi K^\pm$  normalization



## Summary of uncertainties

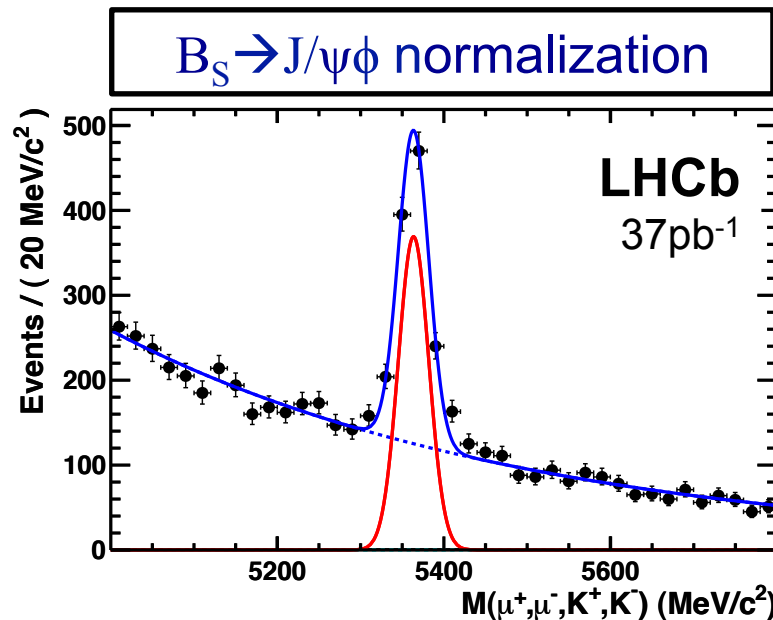
	BR	sel* rec	Trigger	$f_d/f_s$	N	total $B_s$	total $B^0$
$B^\pm \rightarrow J/\psi K^\pm$	4%	4%	5%	13%/-	3%	15%	8%



# Second normalization factor: $B_s \rightarrow J/\psi\phi$

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{N_{cal}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

- $B_s \rightarrow J/\psi\phi$ :  $760 \pm 71^{\text{stat+syst}}$ 
  - 9% systematics from fit model and duplicated candidates
  - No RICH PID used
- **Normalization factor:**  
 $\alpha(B_s \rightarrow \mu\mu) = 10.5 \pm 2.9 \times 10^{-9}$   
 $\alpha(B^0 \rightarrow \mu\mu) = 2.83 \pm 0.86 \times 10^{-9}$



## Summary of uncertainties:

	BR	sel* rec	Trigger	$f_d/f_s$	N	total $B_s$	total $B^0$
$B_s \rightarrow J/\psi\phi$	26%*	8%	5%	-/13%	9%	28%	30%

(\*) from Belle @  $\Upsilon(5S)$ : arXiv:0905.4345

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{f_{K\pi} \cdot N_{B \rightarrow hh}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

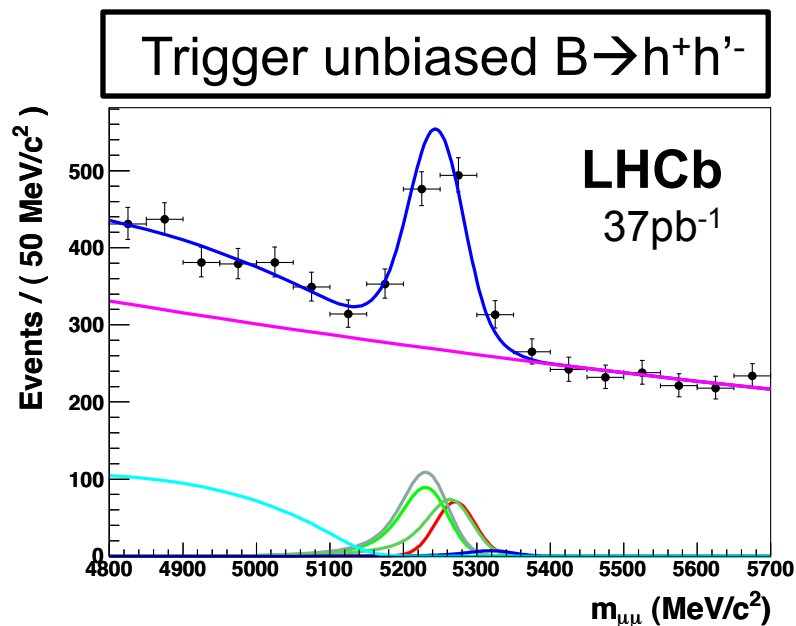
- Strategy: measure yield from inclusive  $B \rightarrow hh'$  sample
  - $B_s$  modes in  $B \rightarrow hh'$  have poorly known BR
  - Calibration of absolute PID efficiency non-trivial
  - determine fraction of  $B^0 \rightarrow K^+ \pi^-$  directly from data:

$$f_{B^0 \rightarrow K^+ \pi^-} = 0.605 \pm 0.027 \quad \text{without relying on absolute PID efficiencies}$$

# Third Normalization factor: $B^0 \rightarrow K^+ \pi^-$

$$BR = BR_{cal} \cdot \frac{f_{cal}}{f_{B_s}} \cdot \frac{\epsilon_{cal}^{Rec} \cdot \epsilon_{cal}^{Sel} \cdot \epsilon_{cal}^{Trig}}{\epsilon_{B_s}^{Rec} \cdot \epsilon_{B_s}^{Sel} \cdot \epsilon_{B_s}^{Trig}} \cdot \frac{N_{B \rightarrow \mu\mu}}{f_{K\pi} \cdot N_{B \rightarrow hh}} = \alpha \cdot N_{B \rightarrow \mu\mu}$$

- $B^0 \rightarrow K^+ \pi^-$ :  $578 \pm 74^{\text{stat+syst}}$ 
  - 8% systematics from fit model
  - 4% from  $B^0 \rightarrow K^+ \pi^-$  fraction
- **Normalization factor:**
  - $\alpha(B_s \rightarrow \mu\mu) = 7.3 \pm 1.8 \times 10^{-9}$
  - $\alpha(B^0 \rightarrow \mu\mu) = 1.99 \pm 0.40 \times 10^{-9}$



## Summary of uncertainties:

	BR	sel* rec	Trigger	$f_d/f_s$	N	total $B_s$	total $B^0$
$B^0 \rightarrow K^+ \pi^-$	3%	7%	14%	13%/-	13%	25%	20%

# Summary of normalization factors

- Normalization factors from three channels consistent  
 → take the **weighted average**

$$\alpha_{B_s \rightarrow \mu\mu} = 8.6 \pm 1.1 \times 10^{-9}$$

$$\alpha_{B^0 \rightarrow \mu\mu} = 2.24 \pm 0.16 \times 10^{-9}$$

(dominated by  $B^\pm \rightarrow J/\psi K^\pm$ )

- The three normalization channels bring very different systematic uncertainties

	BR $10^{-5}$	sel * rec	Trigger	$N_{\text{cal}}$	$\alpha(B_s \rightarrow \mu\mu)$ $10^{-9}$	$\alpha(B^0 \rightarrow \mu\mu)$ $10^{-9}$
$B^\pm \rightarrow J/\psi K^\pm$	$5.98 \pm 0.22$	$0.49 \pm 0.02$	$0.96 \pm 0.05$	$12,366 \pm 403$	$8.4 \pm 1.3$	$2.27 \pm 0.18$
$B_s \rightarrow J/\psi \phi$	$3.4 \pm 0.9$	$0.25 \pm 0.02$	$0.96 \pm 0.05$	$760 \pm 71$	$10.5 \pm 2.9$	$2.83 \pm 0.86$
$B^0 \rightarrow K^+ \pi^-$	$1.94 \pm 0.06$	$0.82 \pm 0.06$	$0.072 \pm 0.01^*$	$578 \pm 74^*$	$7.3 \pm 1.8$	$1.99 \pm 0.40$

(\*) trigger independent  $B \rightarrow hh'$  sample used

## Search for $B_{d,s} \rightarrow \mu^+ \mu^-$

- Selection
- Signal and background likelihoods
- Normalization
  - Extraction of the limit

- Events are classified in 2D plane: invariant mass, GL

- Evaluate the compatibility of measurement with

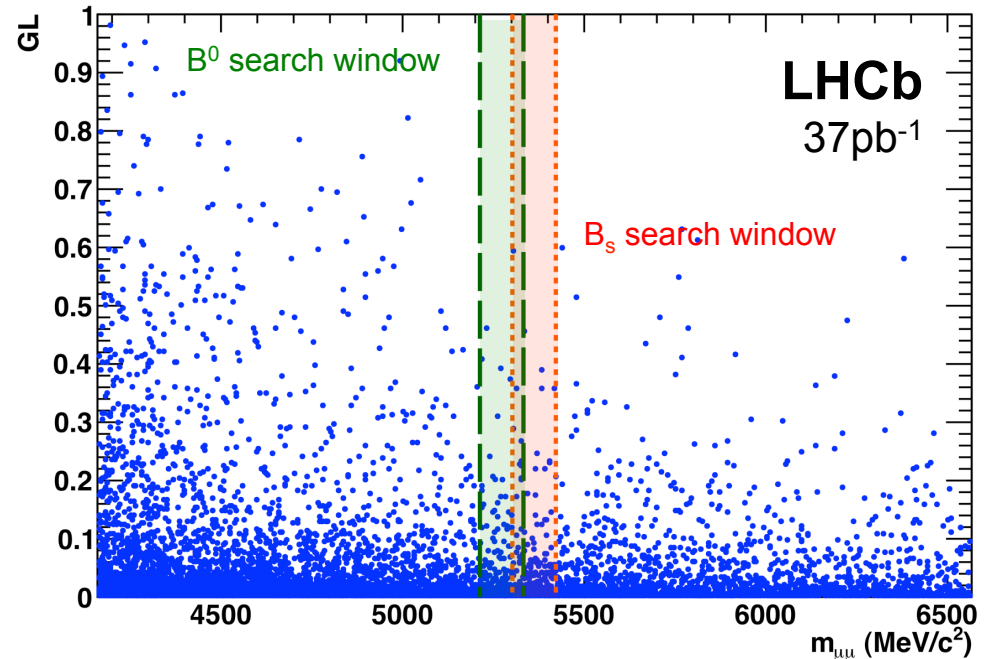
- B only hypothesis [ $CL_B$ ]

- quote observation

- S+B hypothesis

- [ $CL_S = CL_{S+B} / CL_B$ ]

- quote **exclusion limit**



- Calculate **expected limit** using toy MC techniques

- Shows reach of the measurement, independent of stat. fluctuations

- Errors of normalization factors and PDF parameters are included as nuisance parameters in limit calculation

- Use pattern of events to calculate **observed limit**



## Expected number of background (signal) events

Invariant mass ( $\Delta m$ , MeV/c<sup>2</sup>)

$\Delta m \setminus GL$	[0-0.25]	[0.25-0.5]	[0.5-0.75]	[0.75-1]
<b>[-60, -40]</b>	57 (0.01)	1.3 (0.01)	0.3 (0.00)	0.0 (0.00)
<b>[-40,-20]</b>	56 (0.02)	1.3 (0.01)	0.3 (0.01)	0.0 (0.01)
<b>[-20,0]</b>	55 (0.04)	1.2 (0.03)	0.3 (0.02)	0.0 (0.02)
<b>[0,20]</b>	54 (0.04)	1.2 (0.03)	0.3 (0.03)	0.0 (0.02)
<b>[20,40]</b>	54 (0.02)	1.2 (0.01)	0.2 (0.01)	0.0 (0.01)
<b>[40,60]</b>	53 (0.01)	1.1 (0.01)	0.2 (0.00)	0.0 (0.00)
<i>(bkgexp.)</i>	329	7.36	1.51	0.081

# $B_s \rightarrow \mu^+ \mu^-$ : Expected Limit

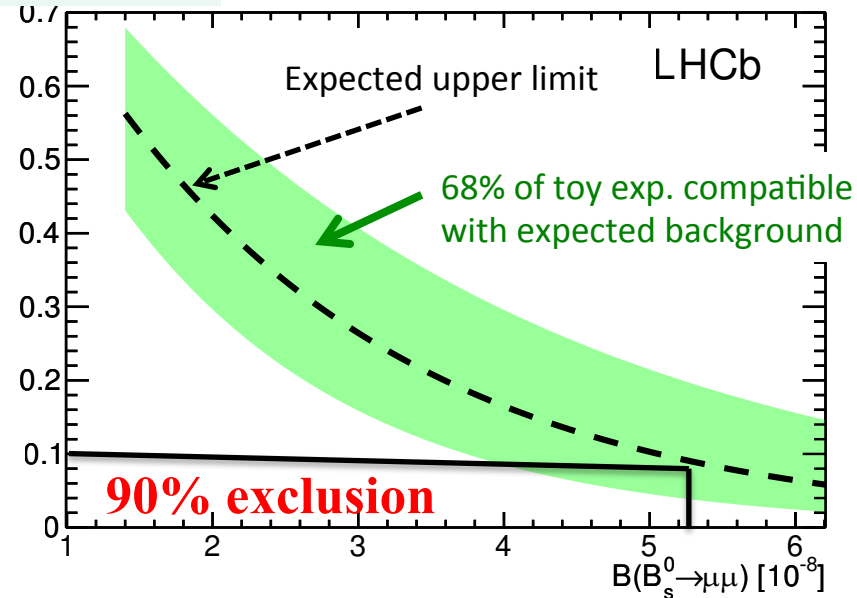
## Expected number of background (signal) events

Invariant mass ( $\Delta m$ , MeV/c<sup>2</sup>)

$\Delta m \setminus GL$	[0-0.25]	[0.25-0.5]	[0.5-0.75]	[0.75-1]
[-60, -40]	57 (0.01)	1.3 (0.01)	0.3 (0.00)	0.0 (0.00)
[-40,-20]	56 (0.02)	1.3 (0.01)	0.3 (0.01)	0.0 (0.01)
[-20,0]	55 (0.04)	1.2 (0.03)	0.3 (0.02)	0.0 (0.02)
[0,20]	54 (0.04)	1.2 (0.03)	0.3 (0.03)	0.0 (0.02)
[20,40]	54 (0.02)	1.2 (0.01)	0.2 (0.01)	0.0 (0.01)
[40,60]	53 (0.01)	1.1 (0.01)	0.2 (0.00)	0.0 (0.00)
( <i>bkgexp.</i> )	329	7.36	1.51	

CLs

### CL<sub>s</sub> vs BR( $B_s \rightarrow \mu\mu$ )



### Expected limit:

$$BR(B_s \rightarrow \mu\mu) < 5.1 \text{ (6.5)} \cdot 10^{-8} \\ @ 90 \text{ (95\%)} \text{ CL}$$

## Observed number of events

Invariant mass ( $\Delta m$ , MeV/c<sup>2</sup>)

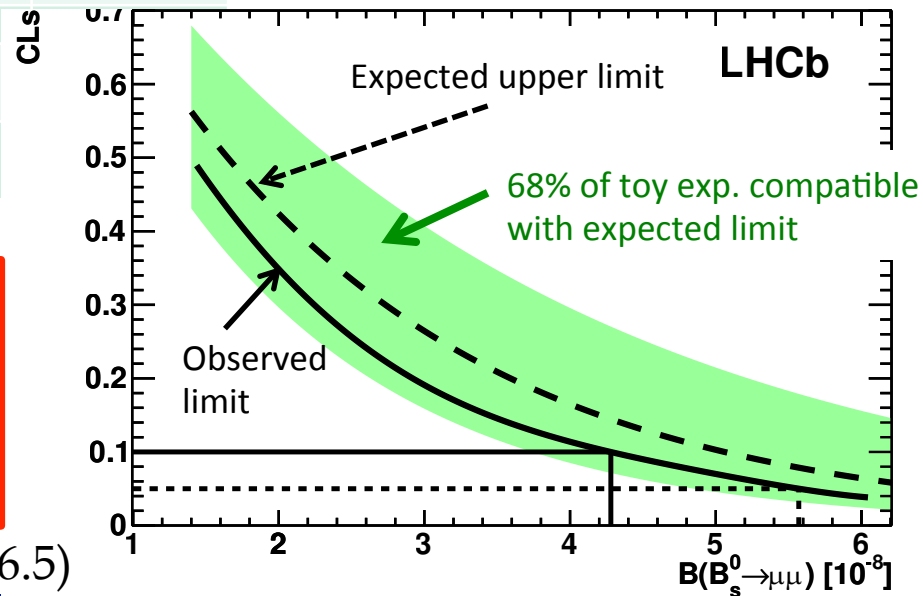
$\Delta m \setminus GL$	[0-0.25]	[0.25-0.5]	[0.5-0.75]	[0.75-1]
[-60, -40]	39	2	1	0
[-40,-20]	55	2	0	0
[-20,0]	73	0	0	0
[0,20]	60	0	0	0
[20,40]	53	2	0	0
[40,60]	55	1	0	0
(TOTAL)	335	7	1	0
(bkg exp.)	329	7.36	1.51	0.081

## Observed number of events

Invariant mass ( $\Delta m$ , MeV/c<sup>2</sup>)

$\Delta m \setminus GL$	[0-0.25]	[0.25-0.5]	[0.5-0.75]	[0.75-1]
[-60, -40]	39	2	1	0
[-40,-20]	55	2	0	0
[-20,0]	73	0	0	0
[0,20]	60	0	0	0
[20,40]	53	2	0	0
[40,60]	55	1	0	0
(TOTAL)	335	7	1	
(bkg exp.)	329	7.36	1.51	

## CL<sub>s</sub> vs BR( $B_s \rightarrow \mu\mu$ )



### Observed limit:

$$BR(B_s \rightarrow \mu\mu) < 4.3 \text{ (5.6)} \cdot 10^{-8} \\ @ 90 \text{ (95\%)} \text{ CL}$$

Expected are: 5.1 (6.5)

## Observed number of events

Invariant mass ( $\Delta m$ , MeV/c<sup>2</sup>)

$\Delta m \setminus GL$	[0-0.25]	[0.25-0.5]	[0.5-0.75]	[0.75-1]
[-60, -40]	59	2	0	0
[-40,-20]	67	0	0	0
[-20,0]	56	2	0	0
[0,20]	60	0	0	0
[20,40]	42	2	1	0
[40,60]	49	2	0	0
(TOTAL)	333	8	1	0
( <i>bkgexp.</i> )	352	8.29	1.85	0.118

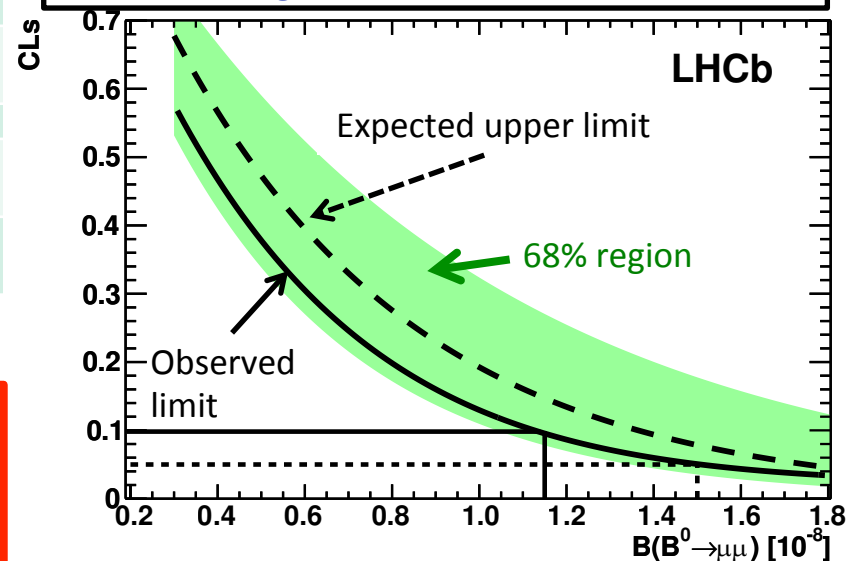


## Observed number of events

Invariant mass ( $\Delta m$ , MeV/c<sup>2</sup>)

$\Delta m \setminus GL$	[0-0.25]	[0.25-0.5]	[0.5-0.75]	[0.75-1]
[-60, -40]	59	2	0	0
[-40,-20]	67	0	0	0
[-20,0]	56	2	0	0
[0,20]	60	0	0	0
[20,40]	42	2	1	0
[40,60]	49	2	0	0
(TOTAL)	333	8	1	0
( <i>bkgexp.</i> )	352	8.29	1.85	0.

**CL<sub>s</sub> vs BR( $B^0 \rightarrow \mu\mu$ )**



### Observed limit:

$$BR(B^0 \rightarrow \mu^+ \mu^-) < 1.2 \text{ (1.5)} \cdot 10^{-8} \\ @ 90 \text{ (95\% CL)}$$

Expected are: 1.4 (1.8)

- First LHCb result (0.037 fb<sup>-1</sup>)

$$\mathbf{BR(B_s \rightarrow \mu^+ \mu^-) < 4.3 (5.6) 10^{-8} @ 90 (95\% CL)}$$

$$\mathbf{BR(B^0 \rightarrow \mu^+ \mu^-) < 1.2 (1.5) 10^{-8} @ 90 (95\% CL)}$$

*arXiv 1103.2465, submitted to Phys. Lett. B*

- Already now competitive to worlds best limit (not published, CDF 3.7 fb<sup>-1</sup>):

$$\mathbf{BR(B_s \rightarrow \mu^+ \mu^-) < 3.6 (4.3) 10^{-8} @ 90 (95\% CL)}$$

$$\mathbf{BR(B^0 \rightarrow \mu^+ \mu^-) < 0.76 (0.91) 10^{-8} @ 90 (95\% CL)}$$

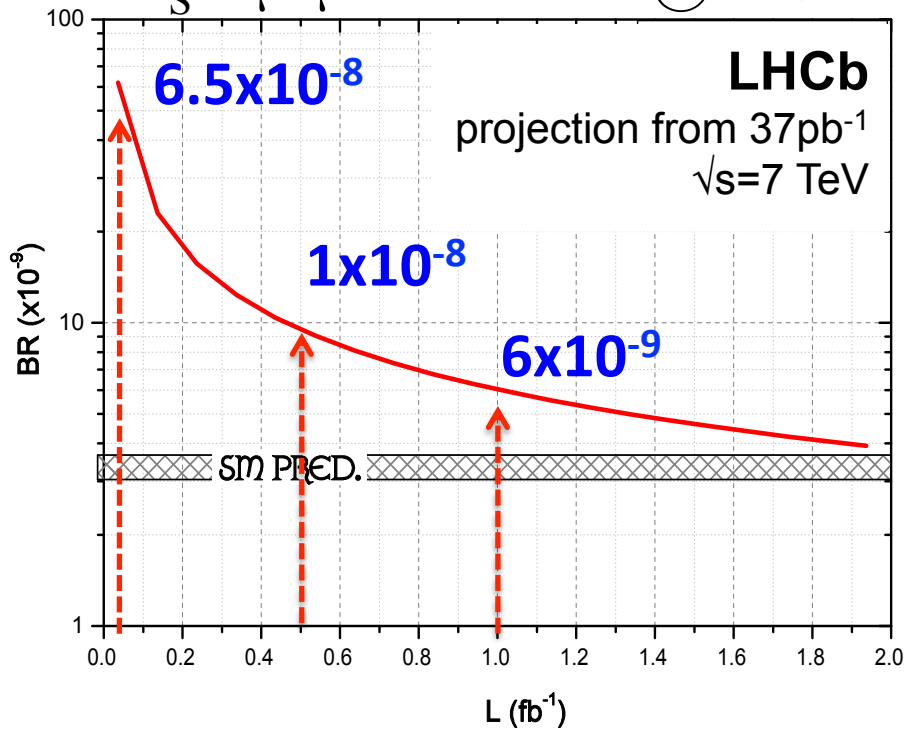
Public CDF note 9892

- And to worlds best published (D0 6.1 fb<sup>-1</sup>):

$$\mathbf{BR(B_s \rightarrow \mu\mu) < 5.1 \times 10^{-8} @ 95\% CL}$$

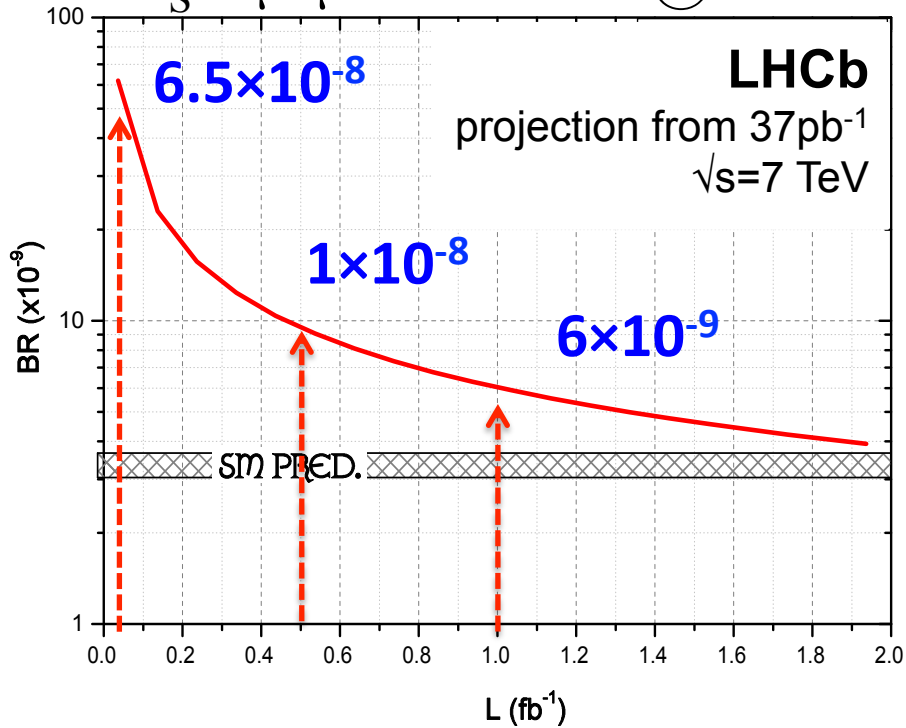
Phys. Lett B 693, 593 (2010)

## $B_s \rightarrow \mu^+ \mu^-$ exclusion @ 95% CL



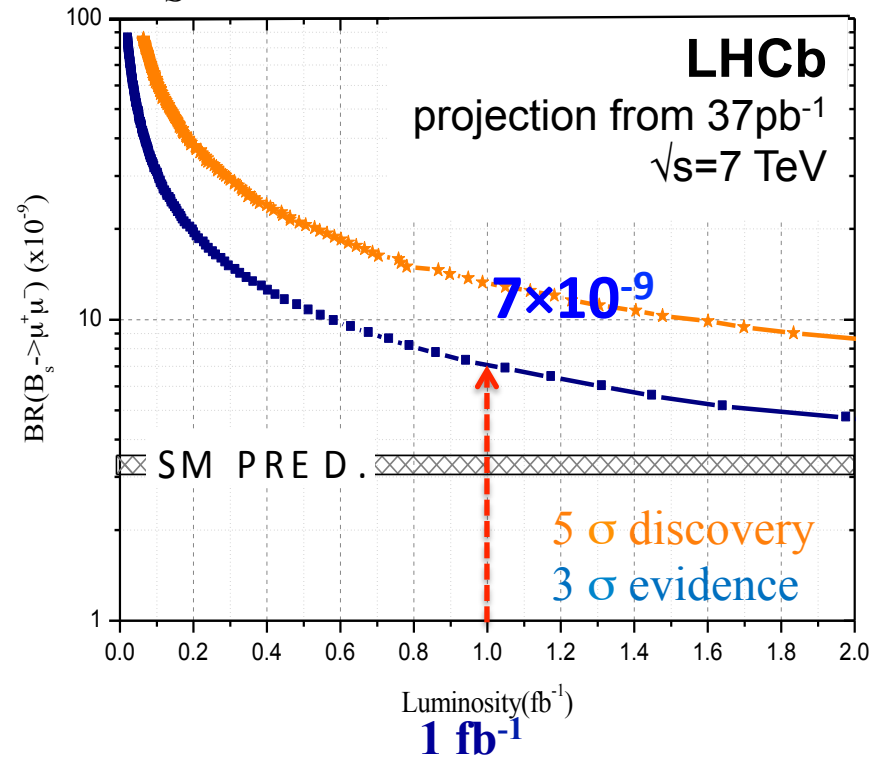
$37 \text{ pb}^{-1}$      $500 \text{ pb}^{-1}$      $1 \text{ fb}^{-1}$

## $B_s \rightarrow \mu^+ \mu^-$ exclusion @ 95% CL



$37\text{ pb}^{-1}$      $500\text{ pb}^{-1}$      $1\text{ fb}^{-1}$

## $B_s \rightarrow \mu^+ \mu^-$ observation



With the data collected in 2011 we will be able to explore the region  $\text{BR} \sim 6-10 \times 10^{-9}$

- With only  $37\text{pb}^{-1}$  LHCb showed its amazing potential to search for New Physics in rare B decays
- The LHCb results...

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) < 4.3 \text{ (5.6)} \times 10^{-8} \text{ @ 90 (95\% CL)}$$

$$\text{BR}(B^0 \rightarrow \mu^+ \mu^-) < 1.2 \text{ (1.5)} \times 10^{-8} \text{ @ 90 (95\% CL)}$$

*arXiv 1103.2465, submitted to Phys. Lett. B*

... are very close to the worlds best results from Tevatron with  $\sim 100$  (CDF) to  $\sim 200$  (D0) less luminosity

- The 2011-12 LHC run will allow LHCb to explore the range of BR down to  $4 \times 10^{-9}$  and possibly discover New Physics





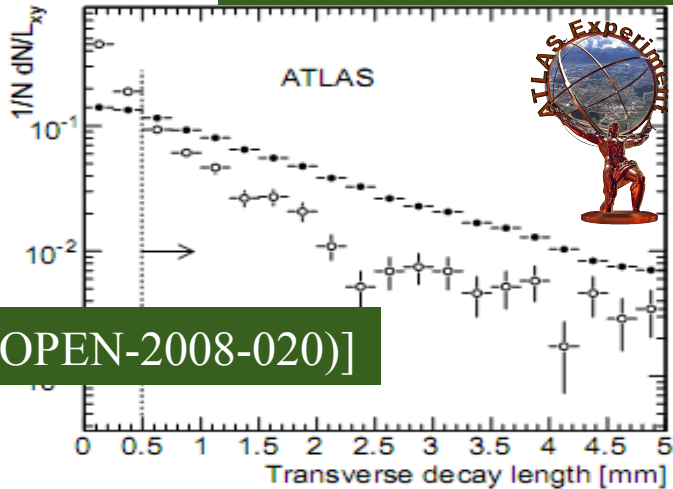
	LHCb	CDF	D0
Luminosity	$0.037\text{fb}^{-1}$	$3.7\text{fb}^{-1}$	$6.1\text{fb}^{-1}$
$B^+ \rightarrow J/\psi K^+$	12366	19762	46803
Expected limit @ 95% CL	$6.5 \cdot 10^{-8}$	$3.3 \cdot 10^{-8}$	$4.0 \cdot 10^{-8}$
Observed limit @ 95% CL	$5.6 \cdot 10^{-8}$	$4.3 \cdot 10^{-8}$	$5.1 \cdot 10^{-8}$

LHCb / CDF:

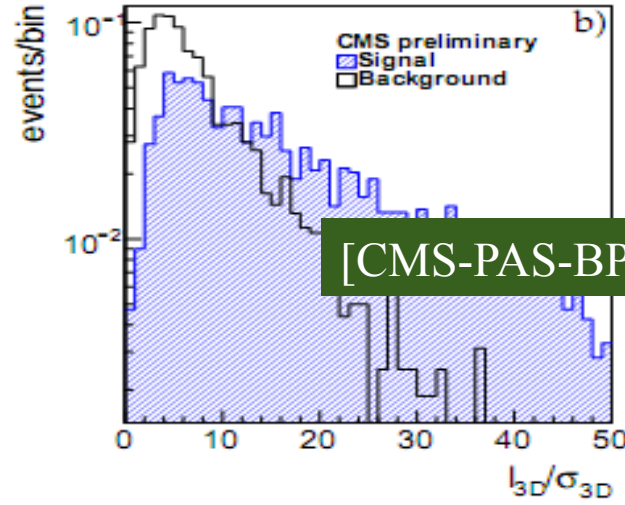
L : 1/100  
 $n_{B^+}$ : 0.63  
 expected limit: 1.97

Cut based analysis: separate signal from background by using highly discriminant variables such as pointing, isolation and secondary vertex displacement:

Eg: Distance of flight and distance of flight significance:



[CERN-OPEN-2008-020]

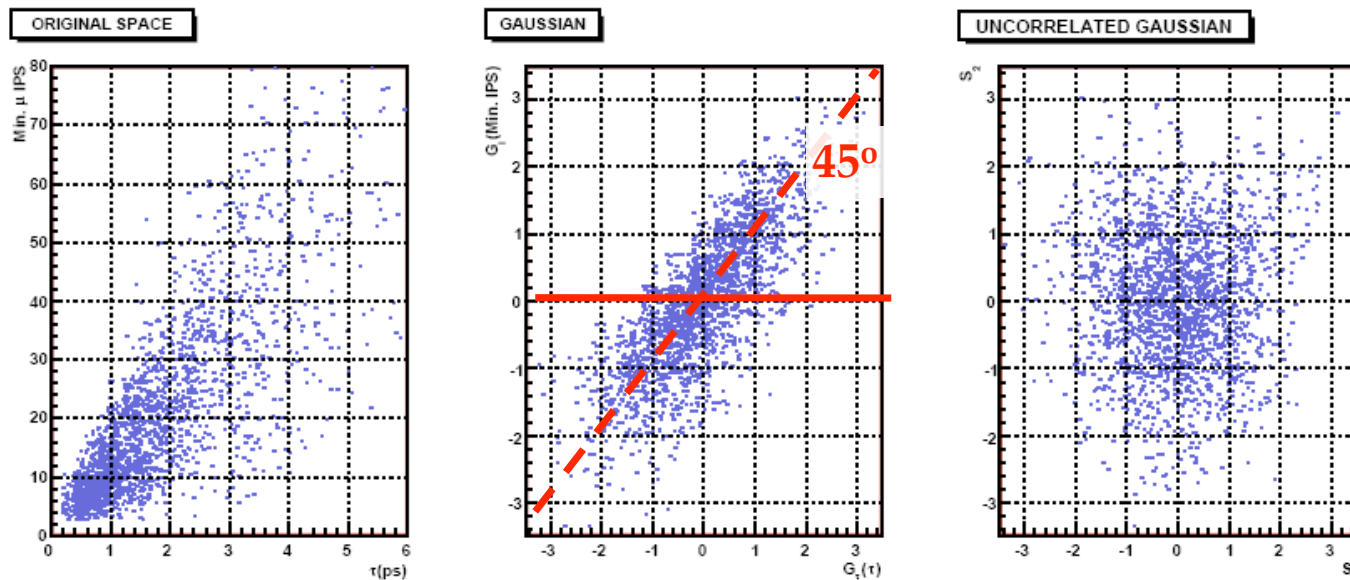


[CMS-PAS-BPH-07-001 (2009)]

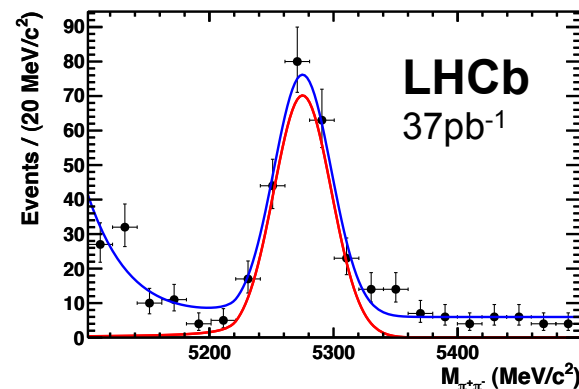
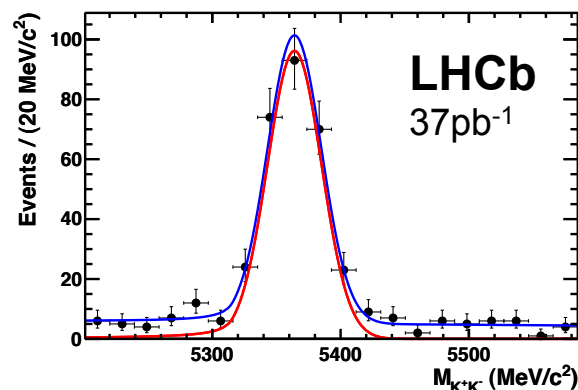
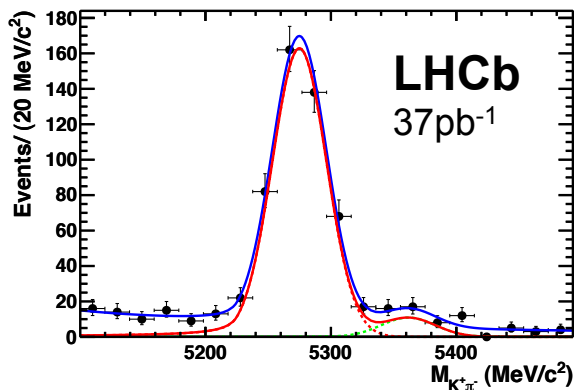
Experiment	N sig	N bkg	90% CL limit in absence of signal
ATLAS ( $10 \text{ fb}^{-1}$ ) $\sigma(\text{bb})=500 \text{ ub}$	5.6 events	$14^{+13}_{-10}$ events (only $\text{bb} \rightarrow \mu\mu$ )	-----
CMS ( $1 \text{ fb}^{-1}$ ) $\sigma(\text{bb})=500 \text{ ub}$	2.36 events	6.53 events ( $2.5 \text{ bb} \rightarrow \mu\mu$ )	$< 1.6 \times 10^{-8}$

# GL build procedure

- The geometrical likelihood built from input variables, takes into account properly the correlations among the variables
  1. the input variables are transformed to Gaussian through cumulative and inverse error function
  2. **In such space correlations are more linear-like** → a rotation matrix, [inverse of correlation matrix] is applied and the 1st step is repeated
  3. Transformations under **signal hyp.** →  $\chi^2_S$ , under **bkg.** →  $\chi^2_B$ .
  4. Discriminating variable is  $\chi^2_S - \chi^2_B$



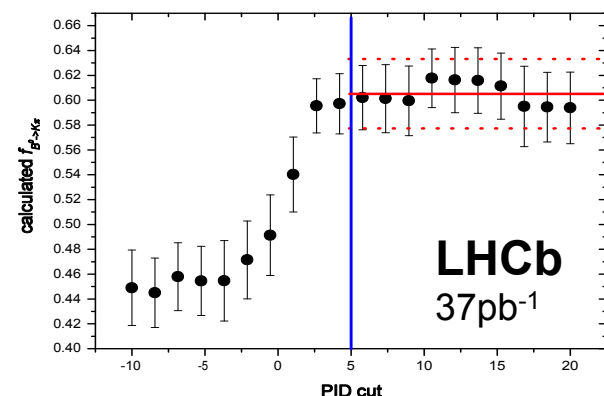
- Fraction of  $B \rightarrow K\pi$  events in inclusive  $B \rightarrow hh'$  from data
  - use RICH PID and fit exclusive peaks
    - RICH efficiency cancels if well known  $BR(B_d \rightarrow K\pi)/BR(B_d \rightarrow \pi\pi)$  are constrained
    - For clean selections,  $f_{B \rightarrow K\pi}$  is independent of PID cut



$f_{B \rightarrow K\pi}$  as function of PID cut, plateau value:

$$f_{B \rightarrow K\pi} = 0.605 \pm 0.027$$

(in agreement but more precise than PDG)



→ For each bin (i) we need to know:

- Number of expected signal events [for a given BR & L] :  $s_i$
- Number of expected background events [for a given L] :  $b_i$
- The number of observed events from data [after unblinding!]:  $d_i$

$$X_i = \frac{\text{Poisson}(d_i, < d_i \geq s_i + b_i)}{\text{Poisson}(d_i, < d_i \geq b_i)}$$

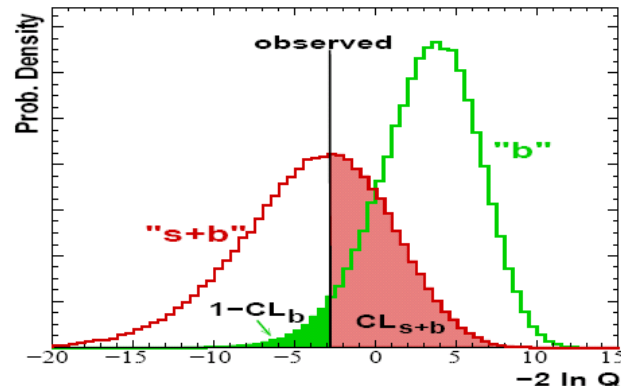
$$X = \prod_i^N X_i$$

$$CL_{s+b} = P_{s+b}(X \leq X^{\text{OBSERVED}})$$

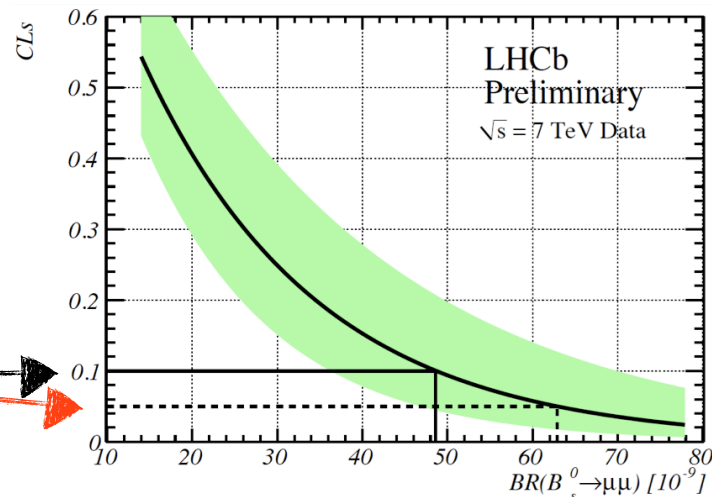
$$CL_b = P_b(X \leq X^{\text{OBSERVED}})$$

Compute CL<sub>s</sub> as  $CL_{s+b}/CL_b$   
and evaluate the limits at

90 (95) % CL



← "s + b"                      "b" →



# Geometrical Likelihood Bins

$B_s \rightarrow \mu\mu$  search window

Invariant Mass bins ( $\text{MeV}/c^2$ )

		[0, 0.25]	[0.25, 0.5]	[0.5, 0.75]	[0.75, 1]	
[−60, −40]	Exp. bkg.	$56.9^{+1.1}_{-1.1}$	$1.31^{+0.19}_{-0.17}$	$0.282^{+0.076}_{-0.065}$	$0.016^{+0.021}_{-0.010}$	
	Exp. sig.	$0.0076^{+0.0034}_{-0.0030}$	$0.0050^{+0.0027}_{-0.0020}$	$0.0037^{+0.0015}_{-0.0011}$	$0.0047^{+0.0015}_{-0.0010}$	
	Observed	39	2	1	0	
	[−40, −20]	Exp. bkg.	$56.1^{+1.1}_{-1.1}$	$1.28^{+0.18}_{-0.17}$	$0.269^{+0.072}_{-0.062}$	$0.015^{+0.020}_{-0.009}$
		Exp. sig.	$0.0220^{+0.0084}_{-0.0079}$	$0.0146^{+0.0066}_{-0.0053}$	$0.0107^{+0.0036}_{-0.0026}$	$0.0138^{+0.0034}_{-0.0024}$
		Observed	55	2	0	0
[−20, 0]	Exp. bkg.	$55.3^{+1.1}_{-1.1}$	$1.24^{+0.17}_{-0.16}$	$0.257^{+0.069}_{-0.059}$	$0.014^{+0.018}_{-0.009}$	
	Exp. sig.	$0.038^{+0.015}_{-0.014}$	$0.025^{+0.012}_{-0.010}$	$0.0183^{+0.0063}_{-0.0047}$	$0.0235^{+0.0059}_{-0.0042}$	
	Observed	73	0	0	0	
[0, 20]	Exp. bkg.	$54.4^{+1.1}_{-1.1}$	$1.21^{+0.17}_{-0.16}$	$0.246^{+0.066}_{-0.057}$	$0.013^{+0.017}_{-0.008}$	
	Exp. sig.	$0.03761^{+0.015}_{-0.015}$	$0.025^{+0.012}_{-0.010}$	$0.0183^{+0.0063}_{-0.0047}$	$0.0235^{+0.0060}_{-0.0044}$	
	Observed	60	0	0	0	
[20, 40]	Exp. bkg.	$53.6^{+1.1}_{-1.0}$	$1.18^{+0.17}_{-0.15}$	$0.235^{+0.063}_{-0.054}$	$0.012^{+0.015}_{-0.007}$	
	Exp. sig.	$0.0220^{+0.0084}_{-0.0081}$	$0.0146^{+0.0067}_{-0.0054}$	$0.0107^{+0.0036}_{-0.0027}$	$0.0138^{+0.0035}_{-0.0025}$	
	Observed	53	2	0	0	
[40, 60]	Exp. bkg.	$52.8^{+1.0}_{-1.0}$	$1.15^{+0.16}_{-0.15}$	$0.224^{+0.060}_{-0.052}$	$0.011^{+0.014}_{-0.007}$	
	Exp. sig.	$0.0076^{+0.0031}_{-0.0027}$	$0.0050^{+0.0025}_{-0.0019}$	$0.0037^{+0.0013}_{-0.0010}$	$0.0047^{+0.0013}_{-0.0010}$	
	Observed	55	1	0	0	



$B_d \rightarrow \mu\mu$  search window

# Geometrical Likelihood Bins

Invariant Mass bins ( $\text{MeV}/c^2$ )

[0, 0.25]      [0.25, 0.5]      [0.5, 0.75]      [0.75, 1]

[−60, −40]	Exp. bkg.	$60.8^{+1.2}_{-1.1}$	$1.48^{+0.19}_{-0.18}$	$0.345^{+0.084}_{-0.073}$	$0.024^{+0.027}_{-0.014}$	
	Exp. sig.	$0.0009^{+0.0004}_{-0.0003}$	$0.0006^{+0.0003}_{-0.0002}$	$0.0004^{+0.0002}_{-0.0001}$	$0.0006^{+0.0002}_{-0.0001}$	
	Observed	59	2	0	0	
	[−40, −20]	Exp. bkg.	$59.9^{+1.1}_{-1.1}$	$1.44^{+0.19}_{-0.17}$	$0.329^{+0.080}_{-0.070}$	$0.022^{+0.024}_{-0.013}$
		Exp. sig.	$0.0026^{+0.0009}_{-0.0009}$	$0.0017^{+0.0008}_{-0.0006}$	$0.0013^{+0.0004}_{-0.0003}$	$0.0016^{+0.0004}_{-0.0002}$
		Observed	67	0	0	0
[−20, 0]	Exp. bkg.	$59.0^{+1.1}_{-1.1}$	$1.40^{+0.18}_{-0.17}$	$0.315^{+0.077}_{-0.067}$	$0.020^{+0.022}_{-0.012}$	
	Exp. sig.	$0.0045^{+0.0017}_{-0.0017}$	$0.0030^{+0.0014}_{-0.0011}$	$0.00219^{+0.00067}_{-0.00054}$	$0.00280^{+0.00060}_{-0.00045}$	
	Observed	56	2	0	0	
[0, 20]	Exp. bkg.	$58.1^{+1.1}_{-1.1}$	$1.36^{+0.18}_{-0.16}$	$0.300^{+0.073}_{-0.064}$	$0.019^{+0.021}_{-0.011}$	
	Exp. sig.	$0.0045^{+0.0017}_{-0.0017}$	$0.0030^{+0.0014}_{-0.0011}$	$0.00219^{+0.00067}_{-0.00054}$	$0.00280^{+0.00060}_{-0.00045}$	
	Observed	60	0	0	0	
[20, 40]	Exp. bkg.	$57.3^{+1.1}_{-1.1}$	$1.33^{+0.17}_{-0.16}$	$0.287^{+0.070}_{-0.061}$	$0.017^{+0.019}_{-0.010}$	
	Exp. sig.	$0.0026^{+0.0009}_{-0.0009}$	$0.0017^{+0.0008}_{-0.0006}$	$0.0013^{+0.0004}_{-0.0003}$	$0.0016^{+0.0004}_{-0.0002}$	
	Observed	42	2	1	0	
[40, 60]	Exp. bkg.	$56.4^{+1.1}_{-1.1}$	$1.29^{+0.17}_{-0.16}$	$0.274^{+0.067}_{-0.058}$	$0.016^{+0.018}_{-0.009}$	
	Exp. sig.	$0.0009^{+0.0003}_{-0.0003}$	$0.0006^{+0.0003}_{-0.0002}$	$0.0004^{+0.0001}_{-0.0001}$	$0.0006^{+0.0002}_{-0.0001}$	
	Observed	49	2	0	0	