

# Development and implementation of new Geant4 QMD model and its validation

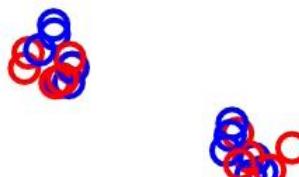
**Yoshihide Sato,**  
Graduate School of Health Science,  
Tokushima University

# | Quantum Molecular Dynamics (QMD)

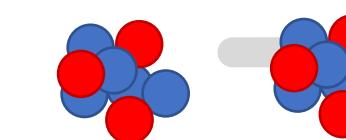
## Introduction

The QMD model is a quantum extension of the classical molecular-dynamics model and can describe hadronic processes, especially **inelastic processes**, in Geant4.

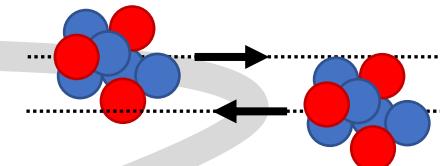
Collision between  $^{12}\text{C}$



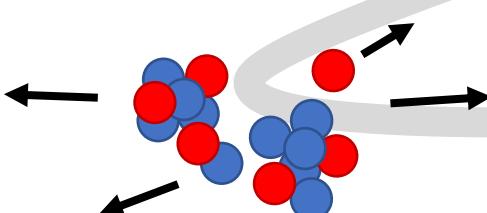
1. Making nuclei



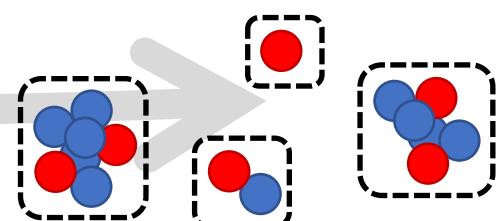
2. Setting



3. Propagation



4. Clustering



→ Decay model

# Development of more accurate QMD model for hadron therapy

## Introduction

IOP Publishing

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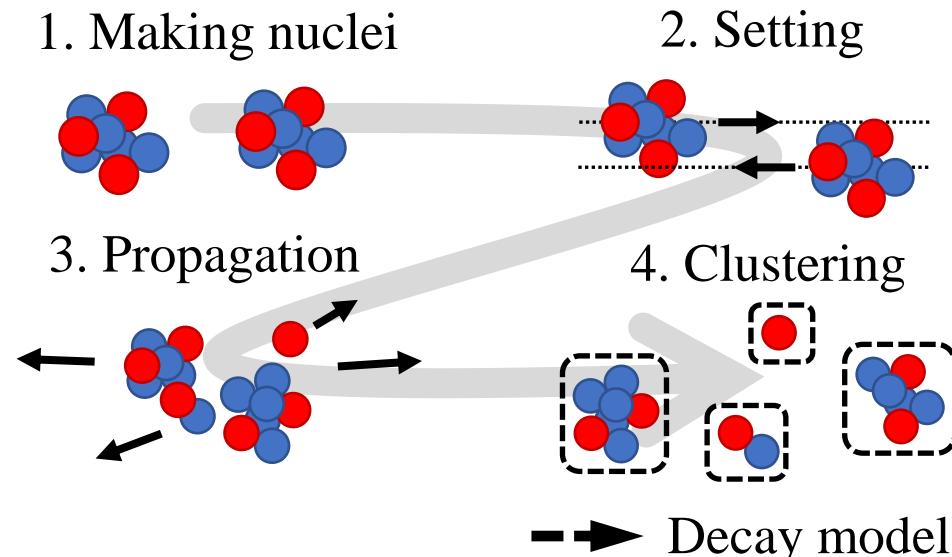
PAPER

### Development of a more accurate Geant4 quantum molecular dynamics model for hadron therapy

Yoshi-hide Sato<sup>1</sup>, Dousatsu Sakata<sup>2,3\*</sup>, David Bolst<sup>4</sup>, Edward C Simpson<sup>5</sup> , Susanna Guatelli<sup>4</sup> , and Akihiro Haga<sup>1,\*</sup>

Sato, Y.-H. et al. Development of a more accurate Geant4 quantum molecular dynamics model for hadron therapy. *Phys. Med. Biol.* **67**, (2022)

### Flow of Geant4 QMD

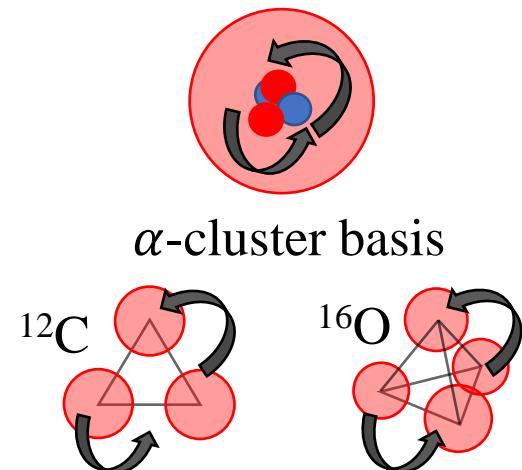


## Three improvements

### 1. Modern interaction

	JQMD <sup>b</sup> (G4QMD)	SLy4 <sup>c</sup>	SkM * <sup>c</sup>	SIII <sup>c</sup>
$A$ [MeV]	-219.4	-297.82	-318	-122.921
$B$ [MeV]	165.3	219.21	249.5	55.343
$g_0$ [MeV fm <sup>2</sup> ]	—	24.569	21.86	18.286
$g_T$ [MeV]	—	9.70	5.9357	6.439
$C_s$ [MeV]	25	32	32	32
$\kappa_s$ [fm <sup>2</sup> ]	—	0.08	0.08	0.08
$\gamma$	4/3	7/6	7/6	2
$\eta^a$	—	5/3	5/3	5/3
$\rho_0$ [fm <sup>-3</sup> ] <sup>a</sup>	0.168	0.160	0.165	0.1452
BE [MeV] <sup>a</sup>	-16.00	-15.97	-15.77	-15.83
$K_0$ [MeV] <sup>a</sup>	237.8	230.2	216.8	355.9

### 2. $\alpha$ -cluster structure



### 3. QMD model Parameter optimization

$$\varphi_i(\mathbf{r}) \equiv \frac{1}{(2\pi L)^{3/4}} \exp \left( -\frac{(\mathbf{r} - \mathbf{r}_i)^2}{4L} + \frac{i}{\hbar} \mathbf{r} \cdot \mathbf{p}_i \right)$$

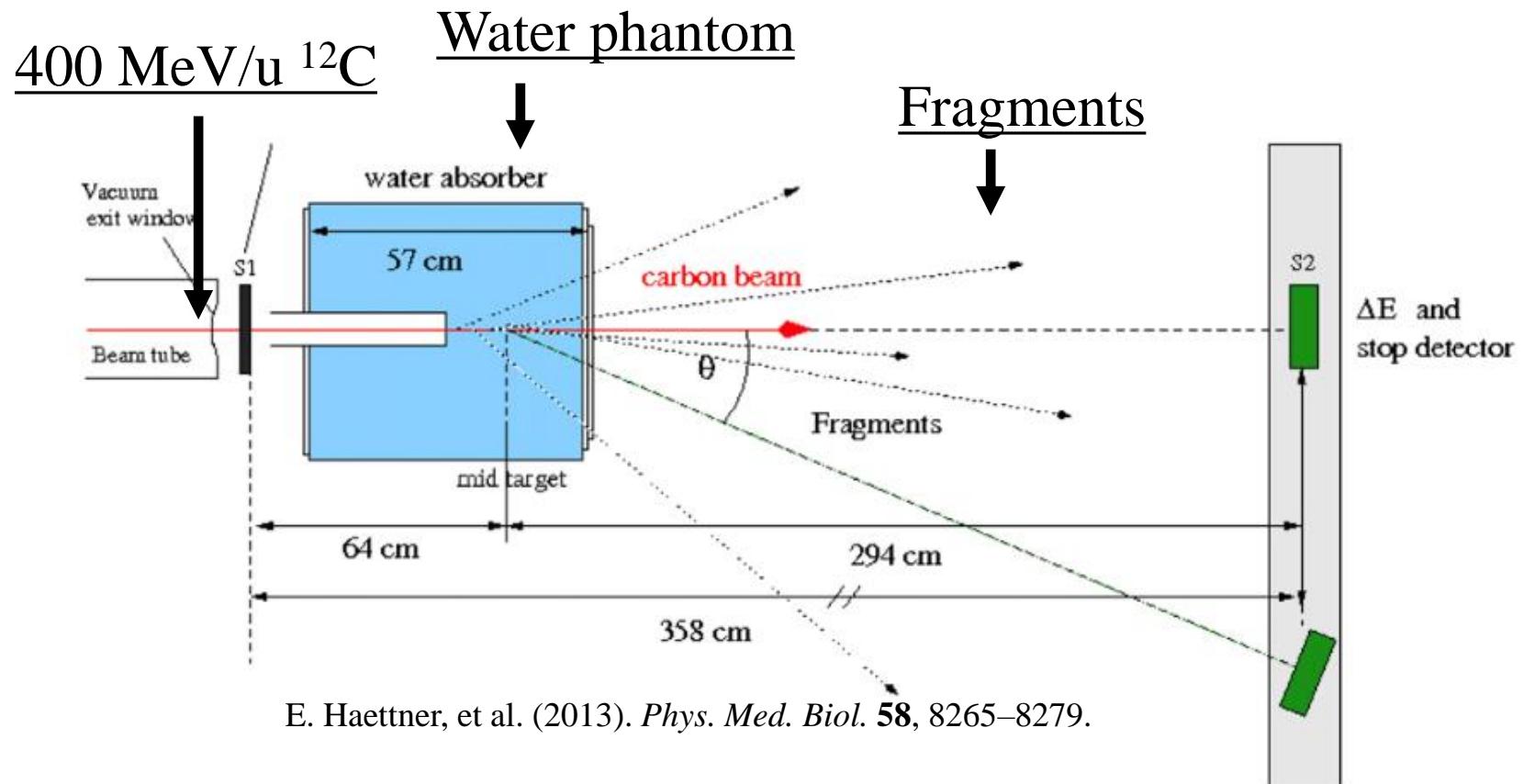
A schematic diagram shows a wavy line representing a particle's trajectory, with a small circle at the end labeled  $\mathbf{r}_{ij}^2$ .

$$|\mathbf{r}_{ij}^2| \leq R^2$$

A schematic diagram shows two gray spheres within a dashed square, representing a cluster. An arrow points from the text  $|\mathbf{r}_{ij}^2| \leq R^2$  to this cluster.

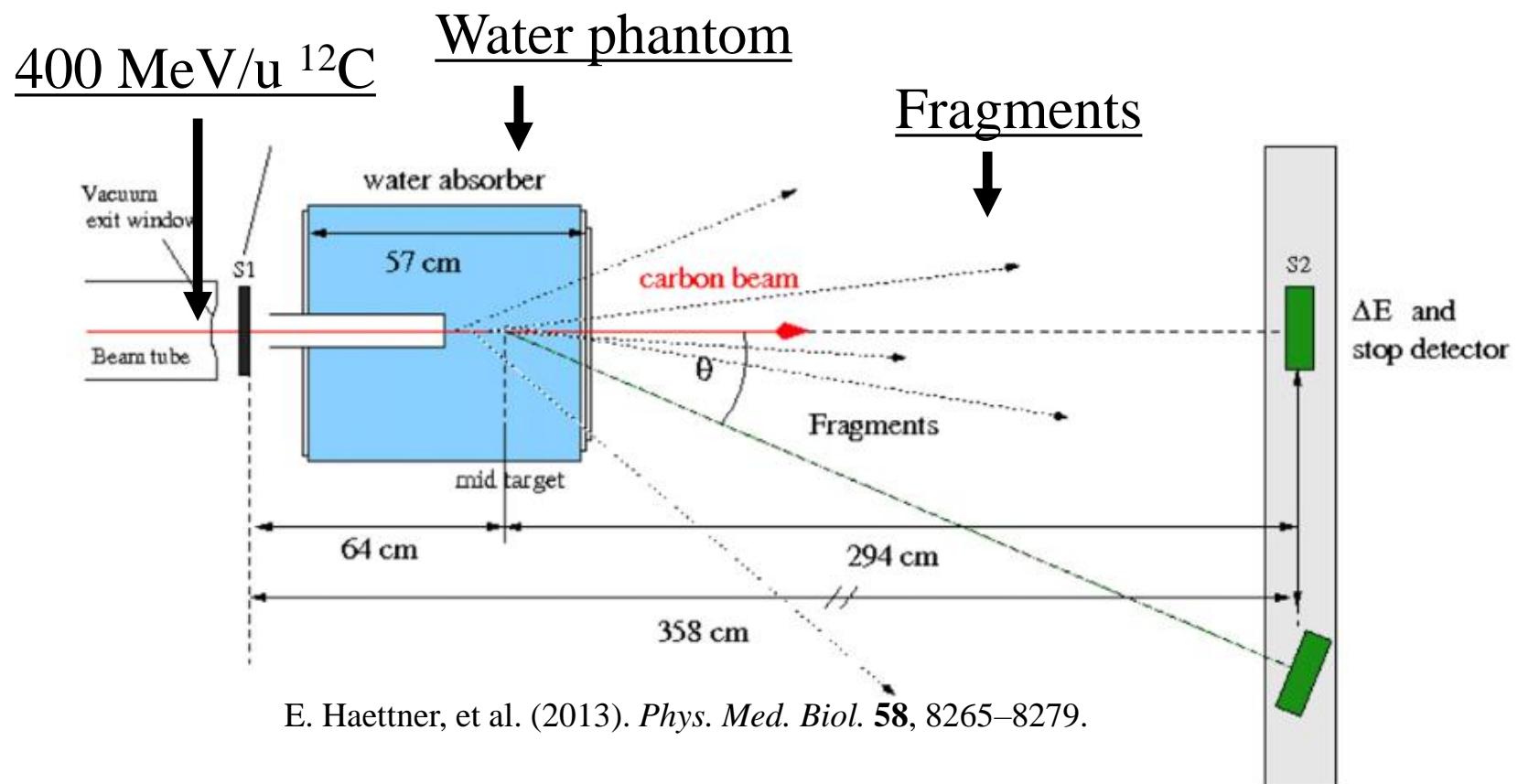
# Water Phantom

## Materials and Methods



# Water Phantom

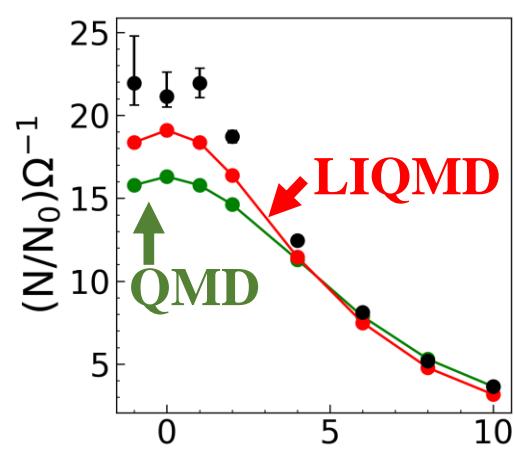
## Materials and Methods



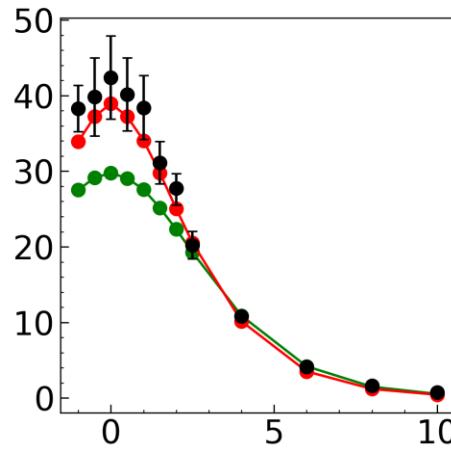
Light Ion QMD (LIQMD)

# Fragment

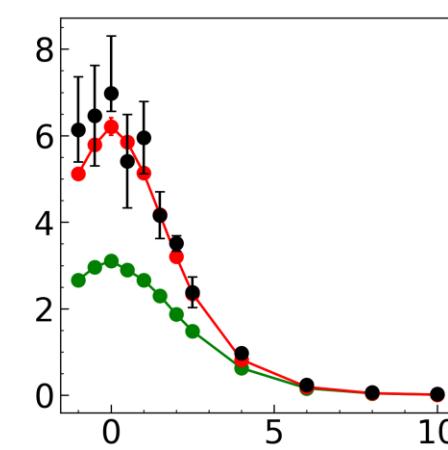
**H**



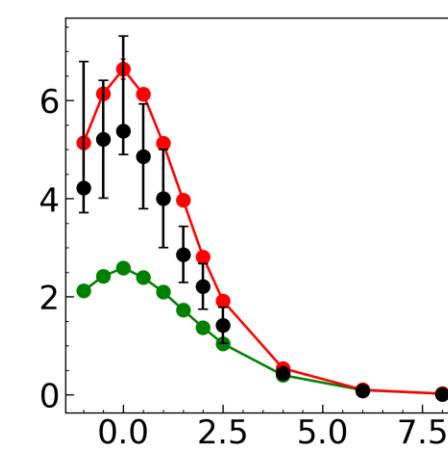
**He**



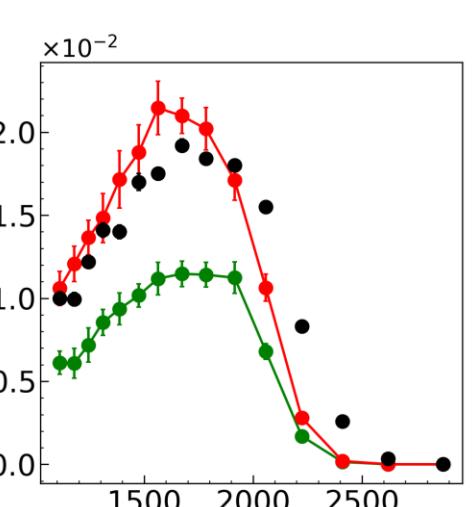
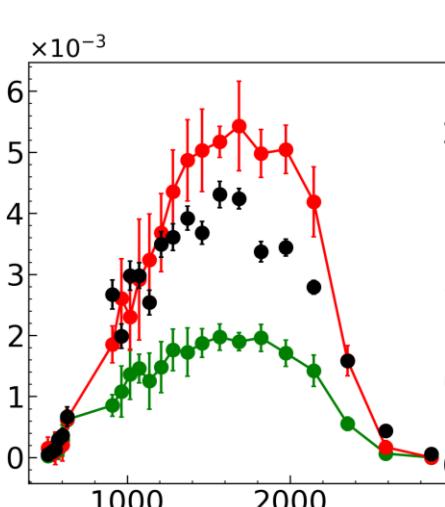
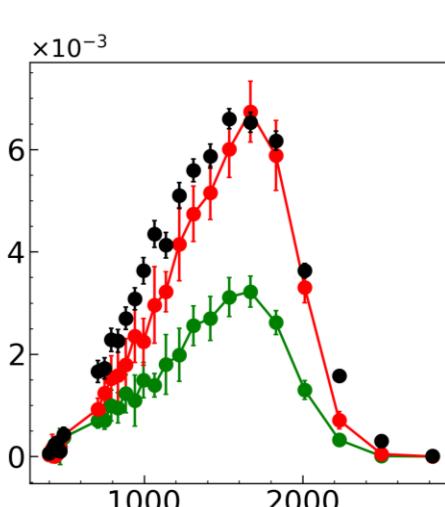
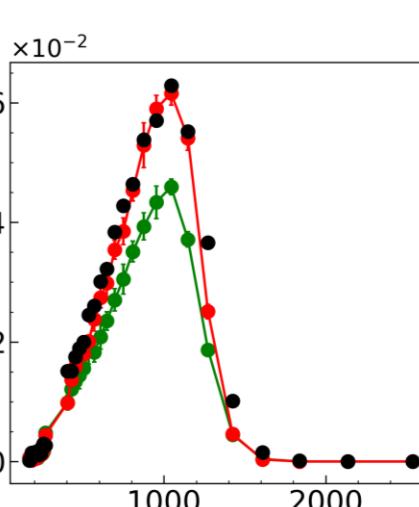
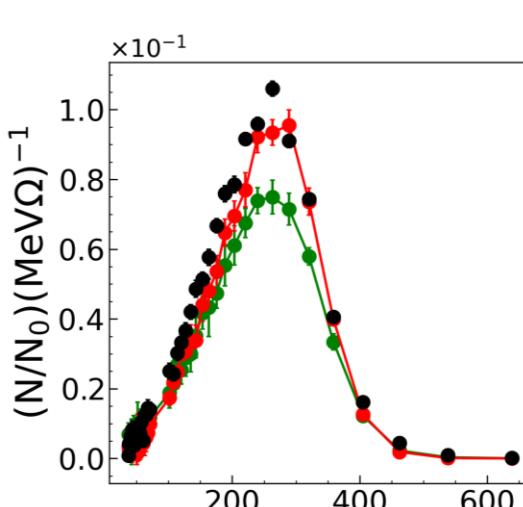
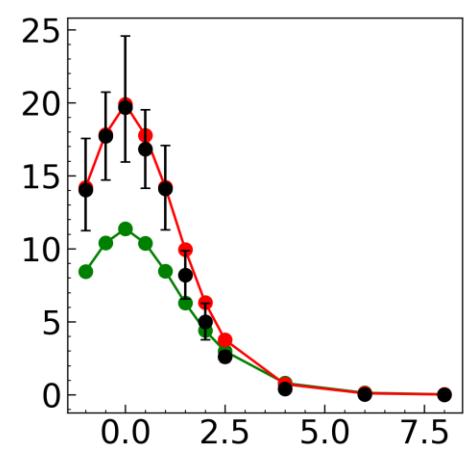
**Li**



**Be**



**B**



# Validation

- Water phantom with 400 MeV/u  $^{12}\text{C}$  beam [1]
- Thin target with 95 MeV/u  $^{12}\text{C}$  beam [2]
- Dose-Depth curve of water phantom [3]
- Positron-emitting nucleus yield [3]

[1] E. Haettner, et al. (2013). *Phys. Med. Biol.* **58**, 8265–8279.

[2] Dudouet, J. et al. (2013). *Physical Review C*, 88(2), 024606.

[3] A. Chacon, et. al.(2019), *Phys. Med. Biol.* **64**, 155014.

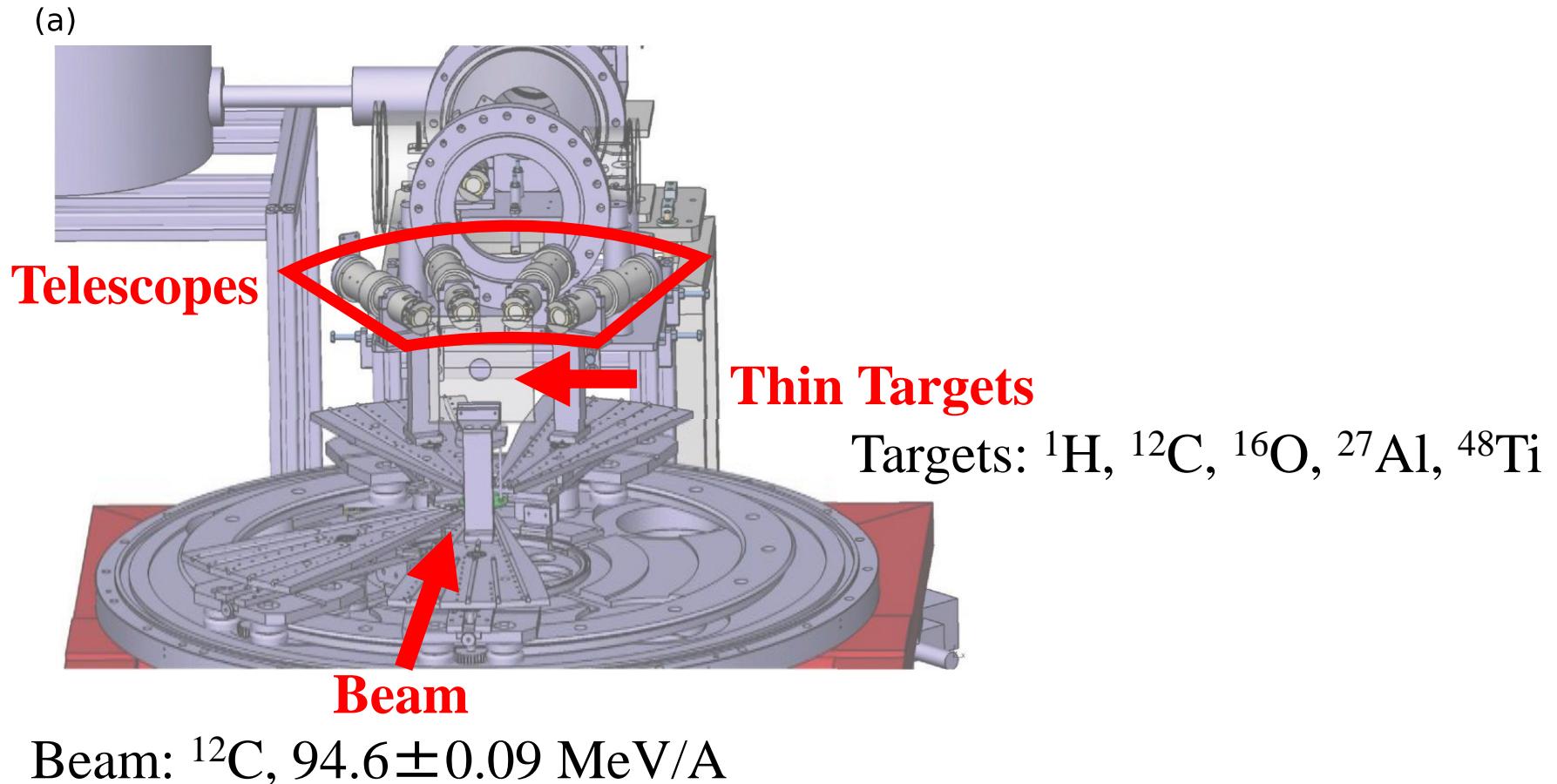
# Validation

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- Thin target with 95 MeV/u  $^{12}\text{C}$  beam
- Dose-Depth curve of water phantom
- Positron-emitting nucleus yield

# Thin Target

## Materials and Methods

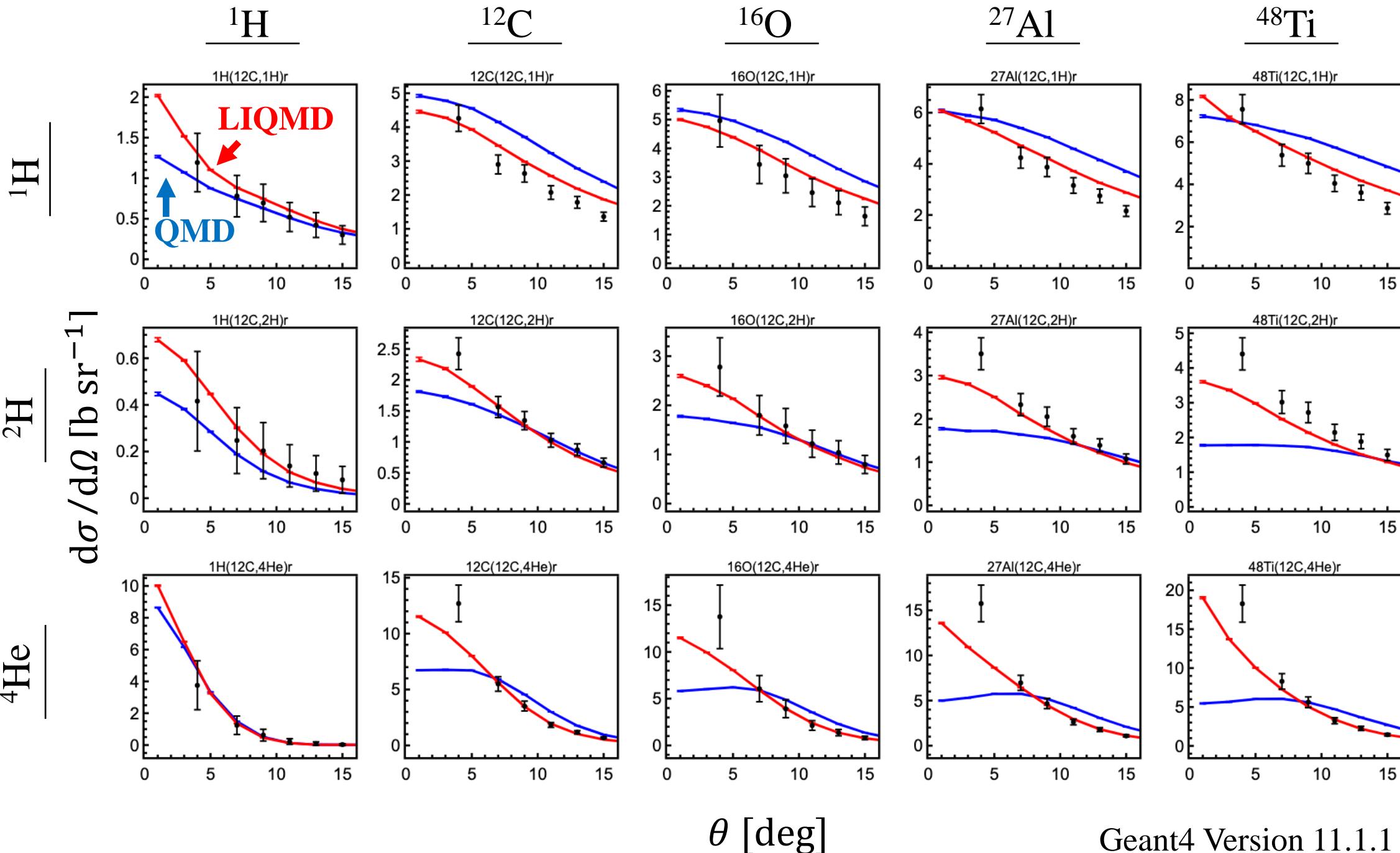
Fragments:  $^{1,2,3}\text{H}$ ,  $^{3,4,6}\text{He}$ ,  $^{6,7}\text{Li}$ ,  $^{7,9,10}\text{Be}$ ,  $^{8,10,11}\text{B}$ ,  $^{10,11,12}\text{C}$

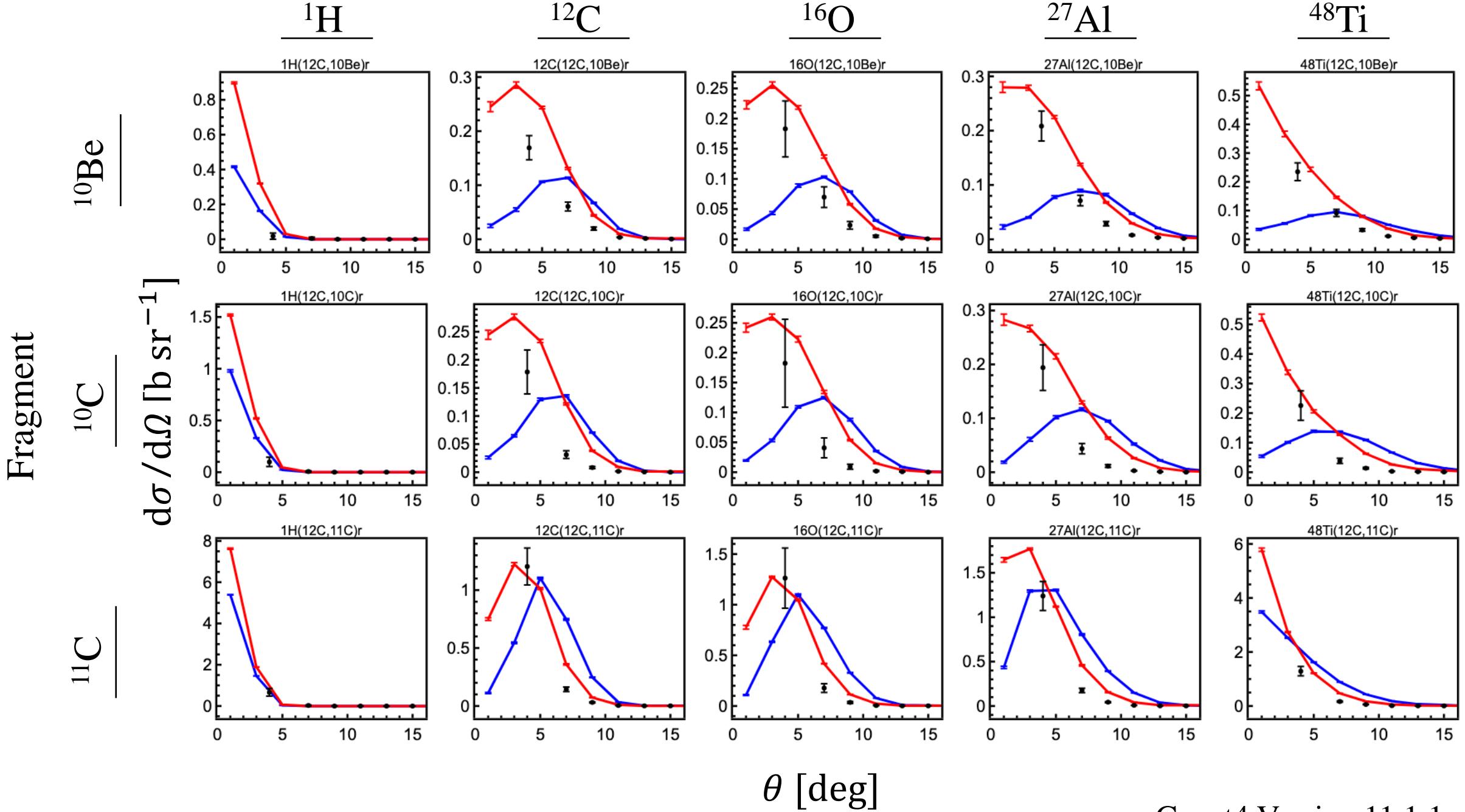


Dudouet, J. et al.. (2013). *Physical Review C*, 88(2), 024606.

E600 experiment at the Grand Accelerateur National d'Ions Lourds (GANIL) facility.

Fragment



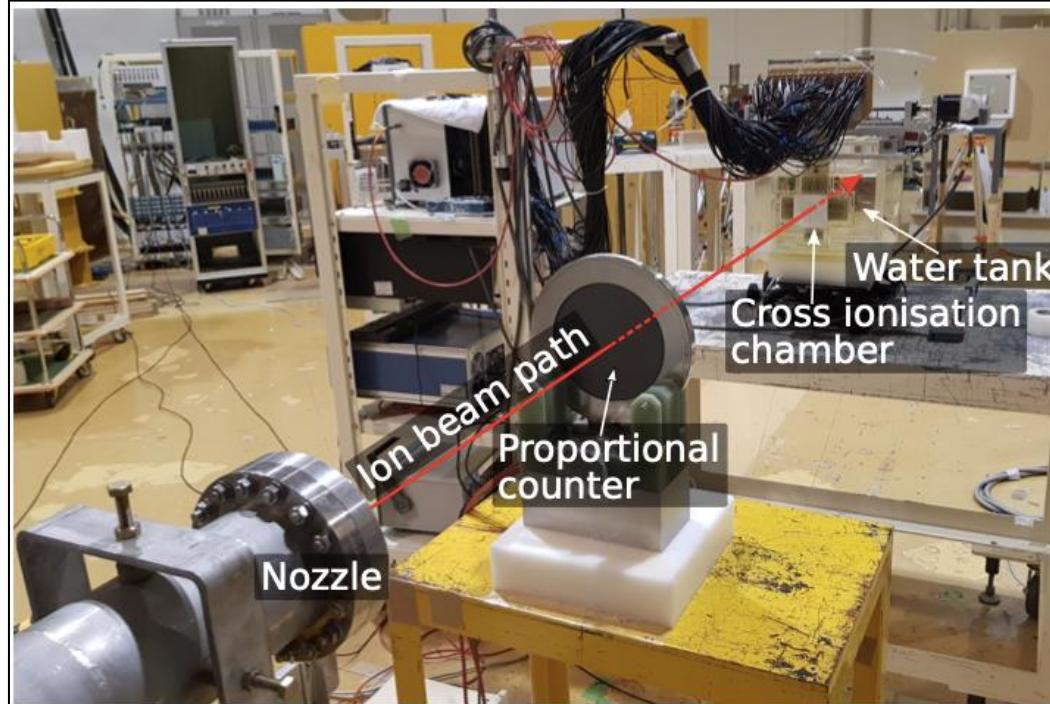


# Validation

- Water phantom with 400 MeV/u  $^{12}\text{C}$  beam
- Thin target with 95 MeV/u  $^{12}\text{C}$  beam
- Dose-Depth curve of water phantom
- Positron-emitting nucleus yield

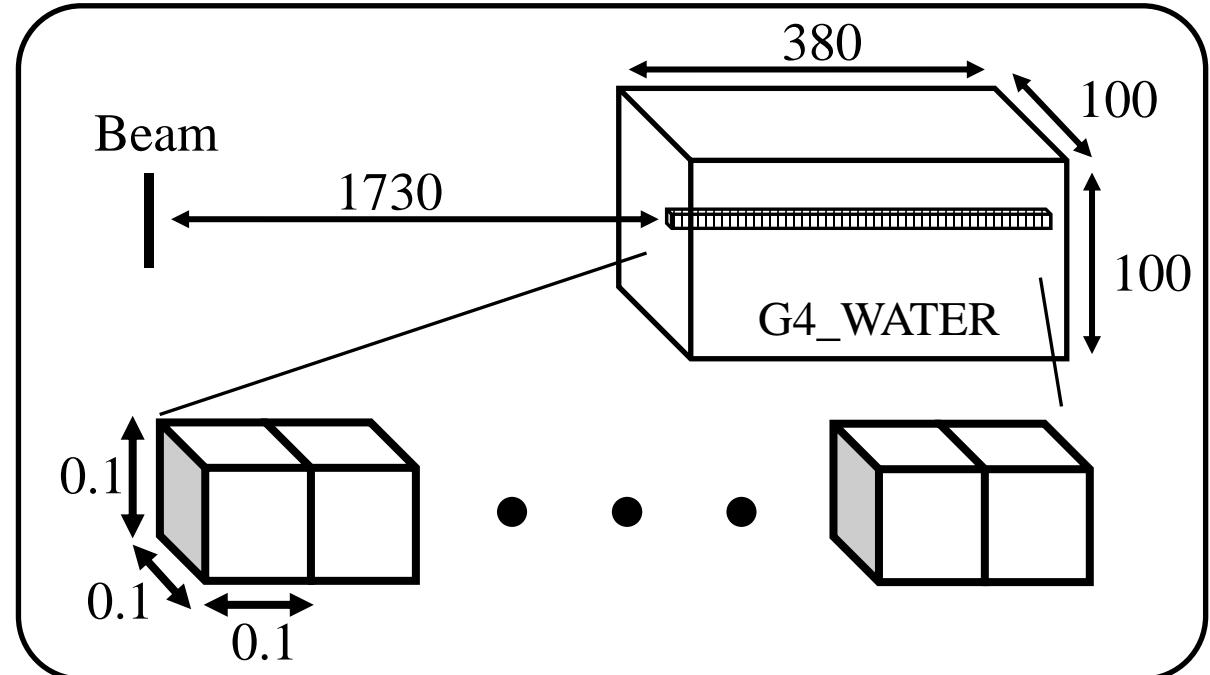
# Depth-Dose Curve

## Materials and Methods

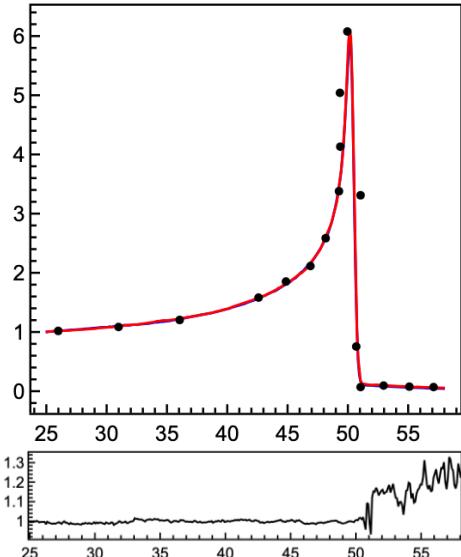
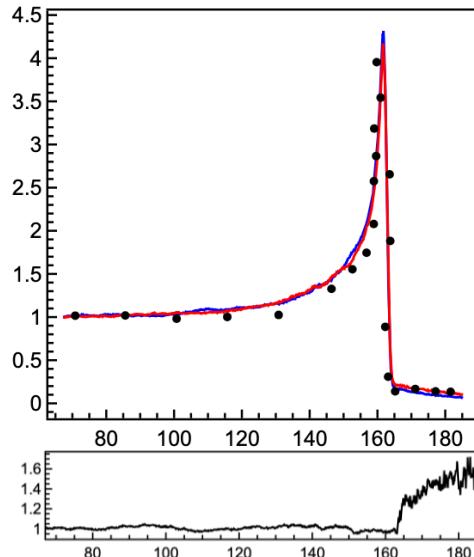
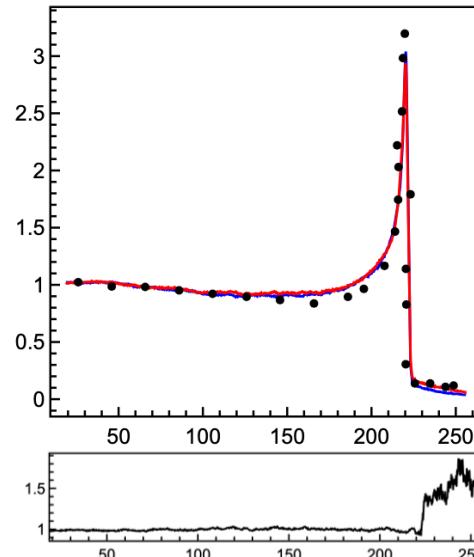
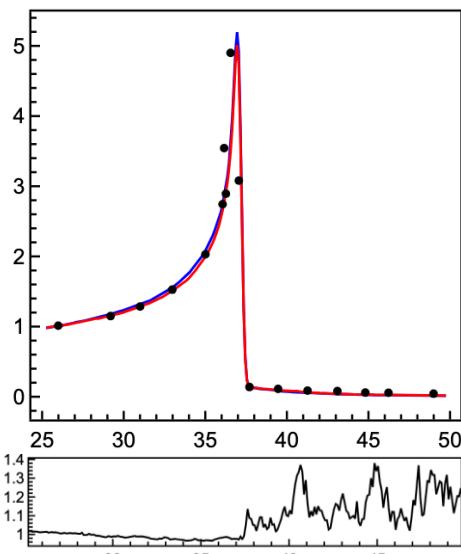
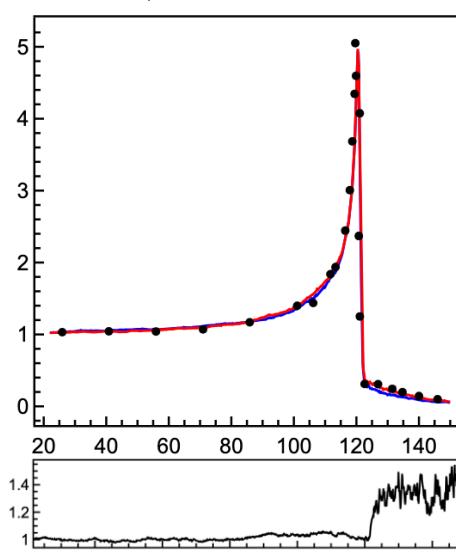


[1] A. Chacon, et. al., *Phys. Med. Biol.* **64**, 155014 (2019).

Simulation geometry (Unit : mm)



- Recording the **energy deposition** to each voxel on the beam axis by Command-based scoring.

$N_0 = 10^8$ Normalized Dose  
&  
Dose Ratio (LIQMD/QMD) $^{12}\text{C}, 148.5 \text{ MeV/u}$  $^{12}\text{C}, 290.5 \text{ MeV/u}$  $^{12}\text{C}, 350 \text{ MeV/u}$  $^{16}\text{O}, 148 \text{ MeV/u}$  $^{16}\text{O}, 290 \text{ MeV/u}$ 

— QMD  
— LIQMD  
● Exp.

Geant4 Version 11.1.1

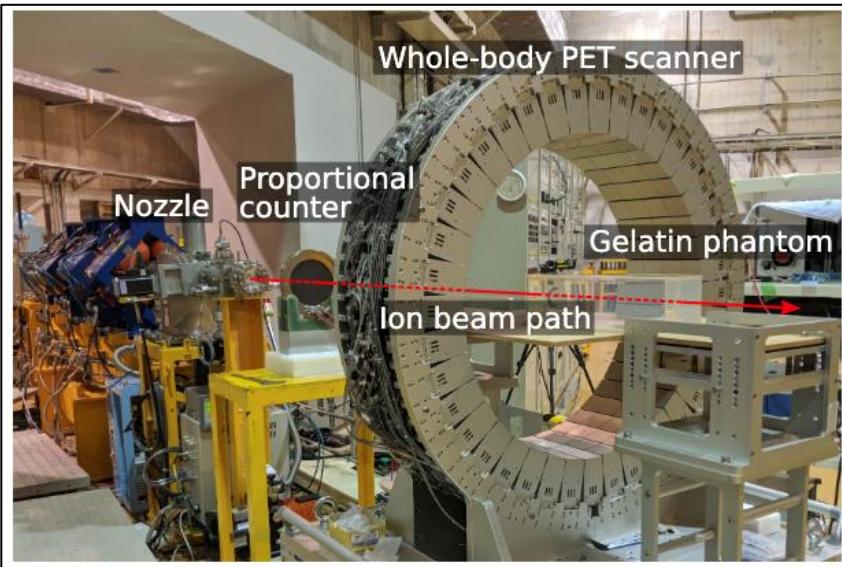
Depth in water [mm]

# Validation

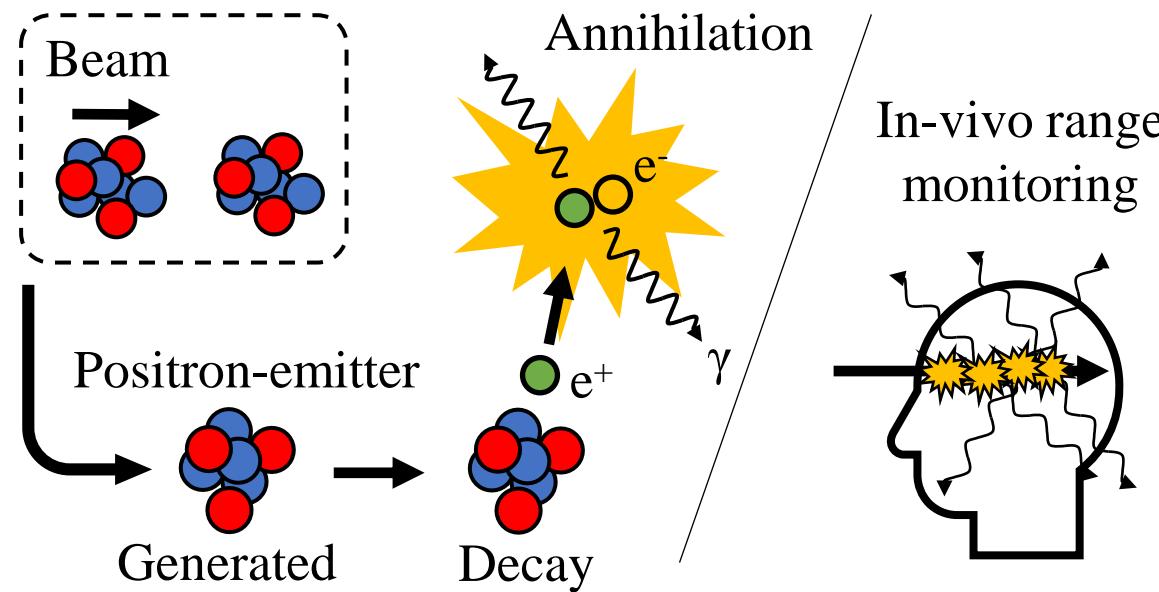
- Water phantom with 400 MeV/u  $^{12}\text{C}$  beam
- Thin target with 95 MeV/u  $^{12}\text{C}$  beam
- Dose-Depth curve of water phantom
- Positron-emitting nucleus yield

# Positron-Emitting Nuclide Yield

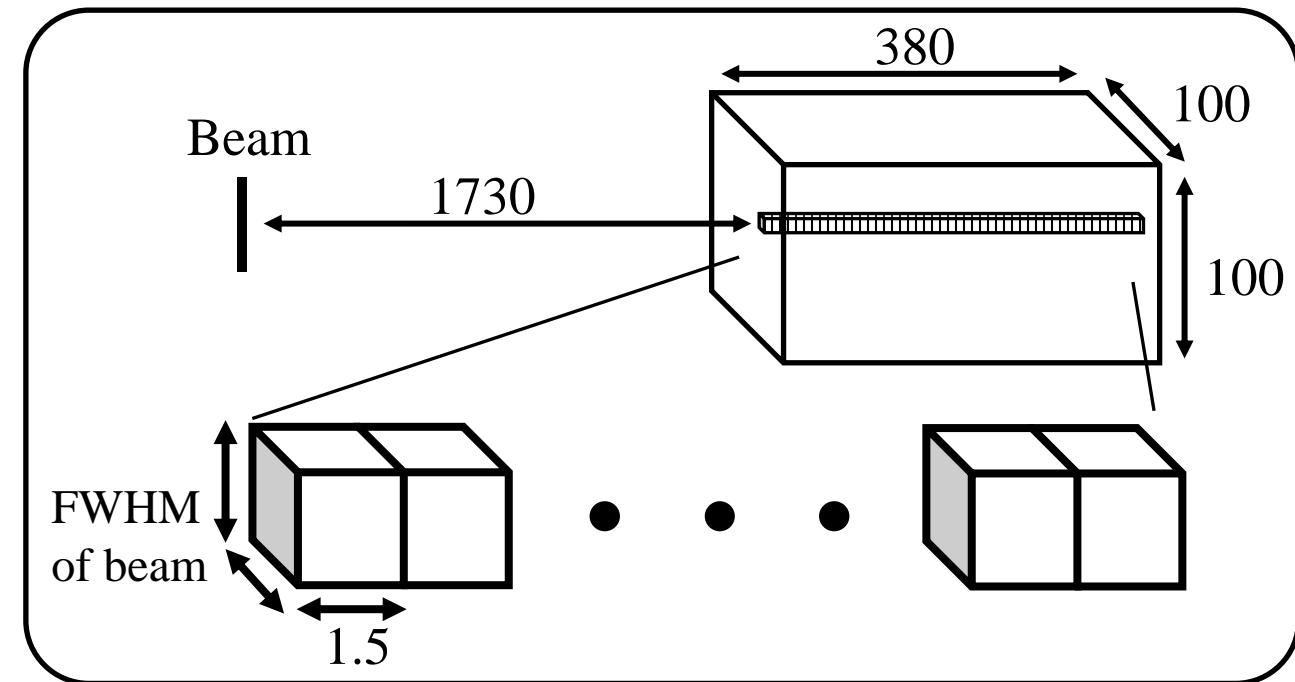
## Materials and Methods



A. Chacon, et. al., *Phys. Med. Biol.* **64**, 155014 (2019).



## Simulation and analysis geometry (Unit : mm)



- Calculating the **number of positron-emitting nuclide** in each voxel on the beam axis at the initial.

— QMD — LIQMD

● Exp.

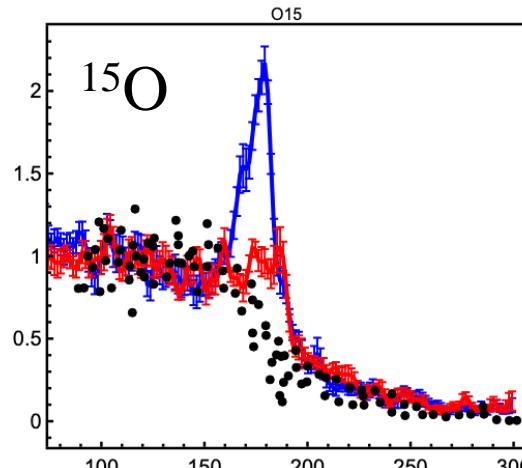
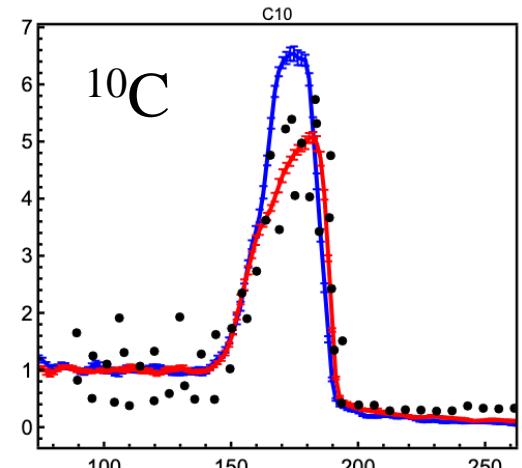
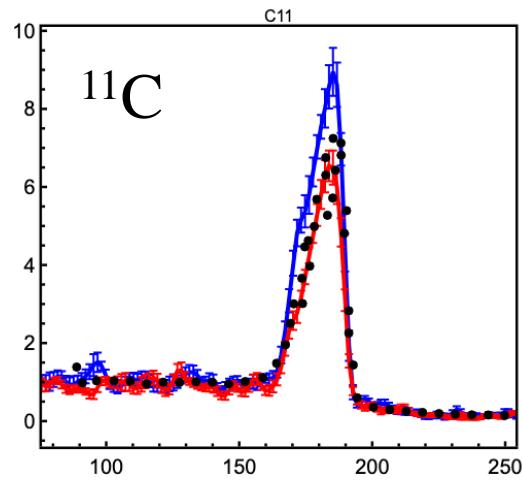
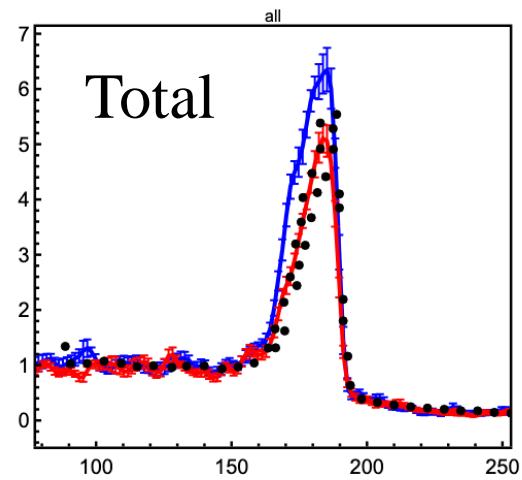
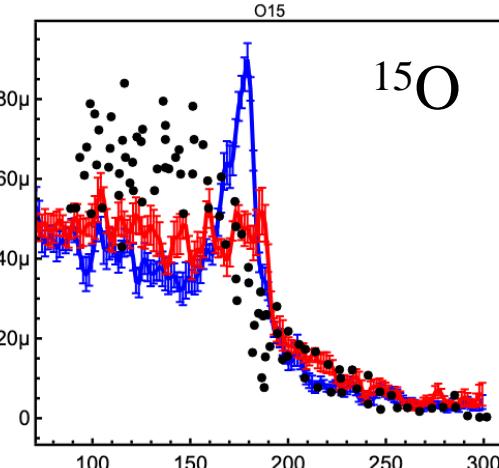
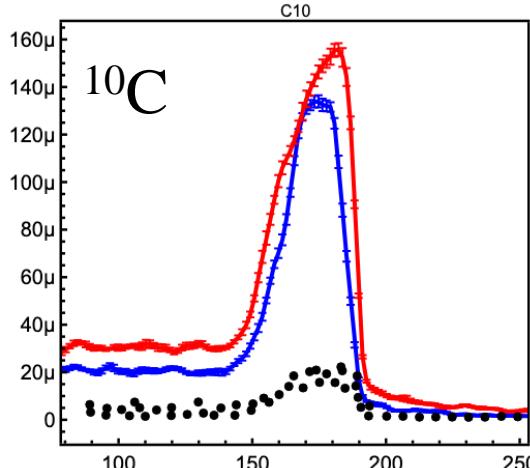
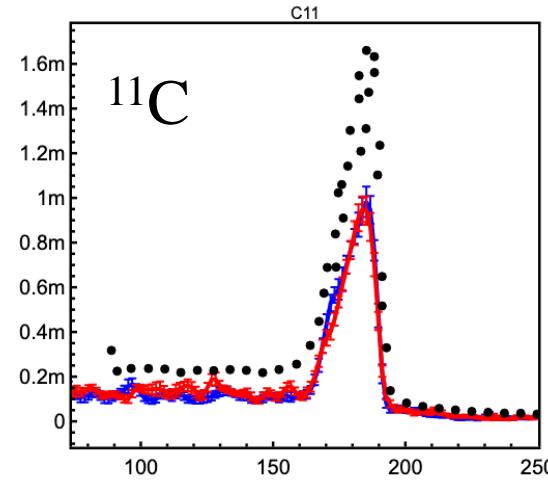
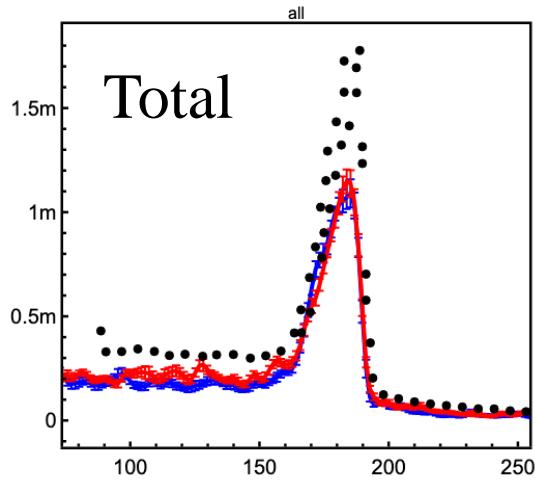
$^{12}\text{C}$ , 350MeV/u, PMMA

$N_0 = 10^8$

10 repetitions

Normalized (Focus on shape)

Yield



Depth in water [mm]

Geant4 Version 11.1.1

17

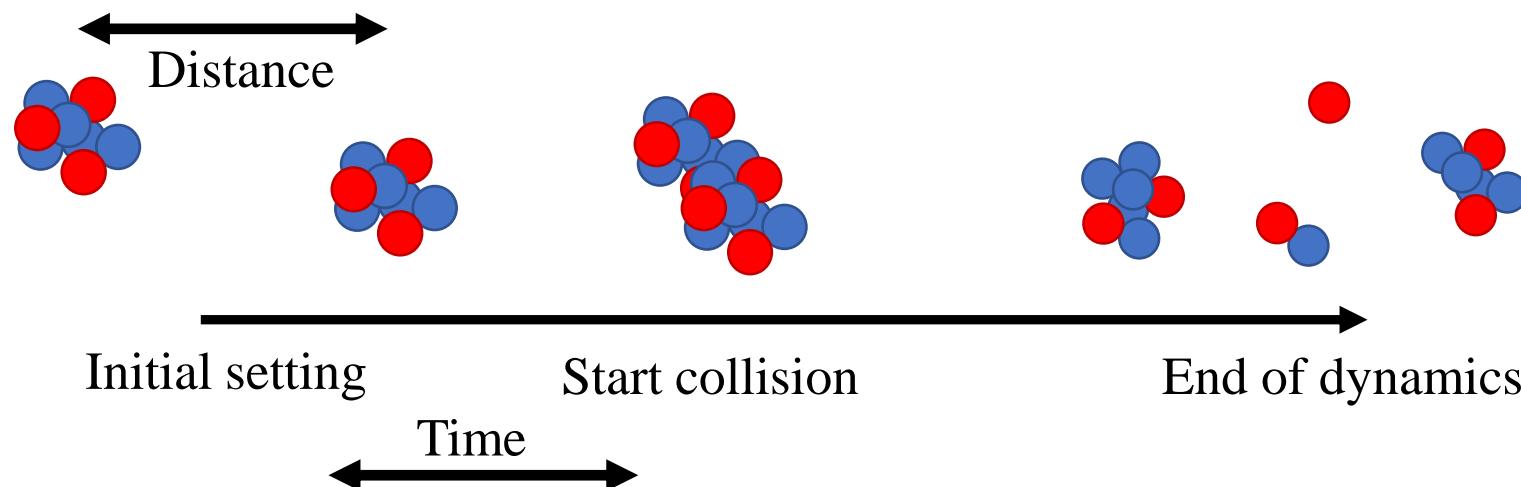
## Limitation in LIQMD

- Energy range
- Mass range

# Energy Range Recommended in LIQMD

## Materials and Methods

Projectile and target should be separated by at least about b-value.



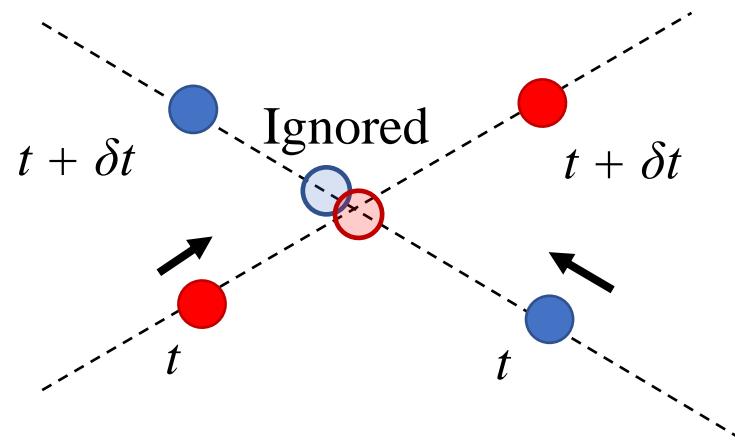
If the speed is slow (Low kinetic energy per nucleon), it will take a long time to collide, leaving not enough time for simulation after the collision.

It is better to have at least about 30 MeV/u.

# Energy Range Recommended in LIQMD

## Materials and Methods

Too high energy



500 MeV/u gives 1.5 fm gap in time step  $\delta t = 2$  fm/c.

Due to this large gap, collisions that should occur may be ignored.

Energies below about 500 MeV/u are recommended.

# Mass Range Recommended in LIQMD

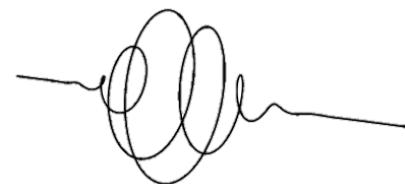
## Materials and Methods

### Wave function of nucleon

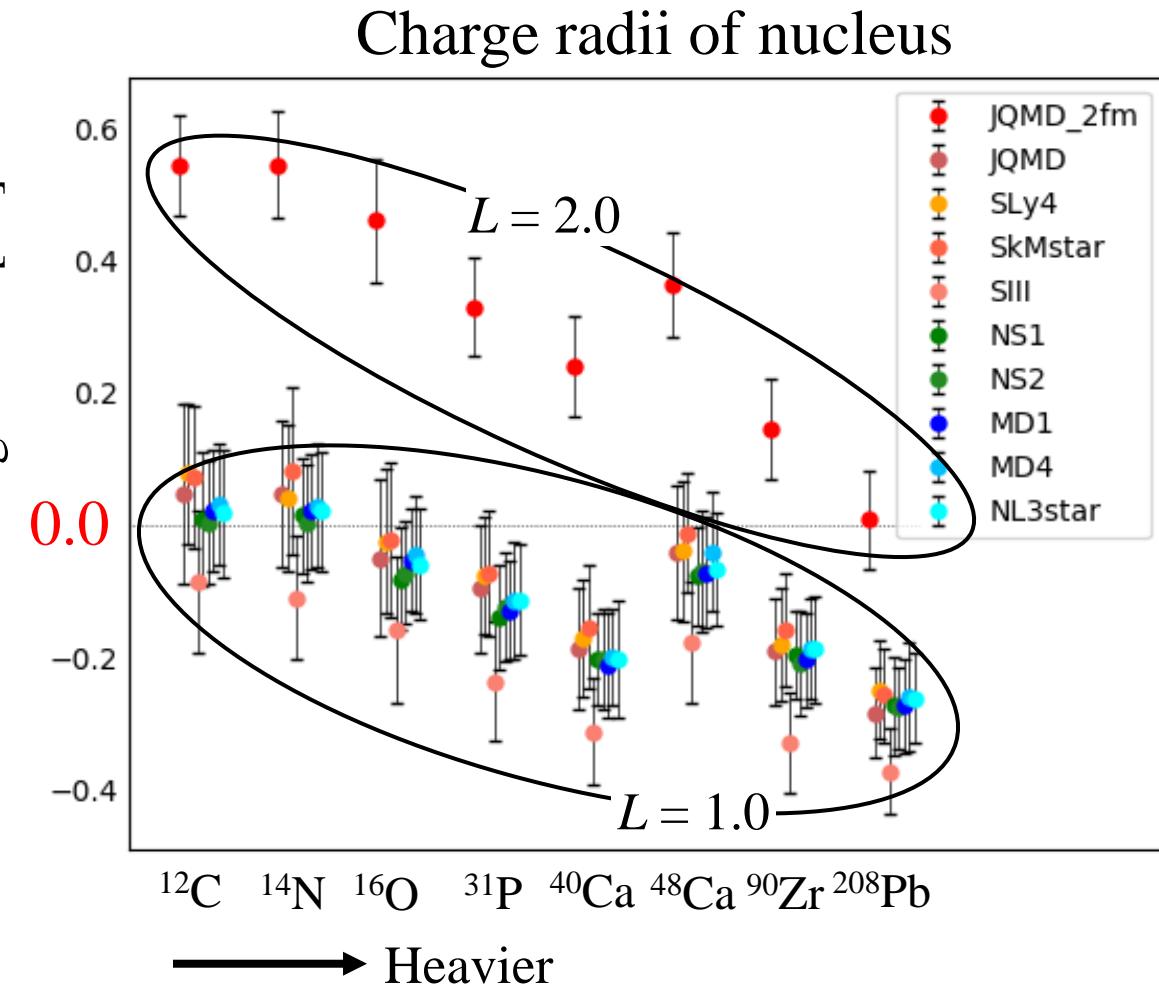
$$\varphi_i(\mathbf{r}) \equiv \frac{1}{(2\pi L)^{3/4}} \exp\left(-\frac{(\mathbf{r} - \mathbf{r}_i)^2}{4L} + \frac{i}{\hbar} \mathbf{r} \cdot \mathbf{p}_i\right)$$

$L = 2.0$  [fm] for QMD

$L = 1.26$  [fm] for LIQMD



Difference from experimental value of the charge radii<sup>†</sup> [fm]



<sup>†</sup>: I. Angeli, K.P. Marinova, Atomic Data and Nuclear Data Tables, 99, 2013, 69-95.

# Mass Range Recommended in LIQMD

## Materials and Methods

### Wave function of nucleon

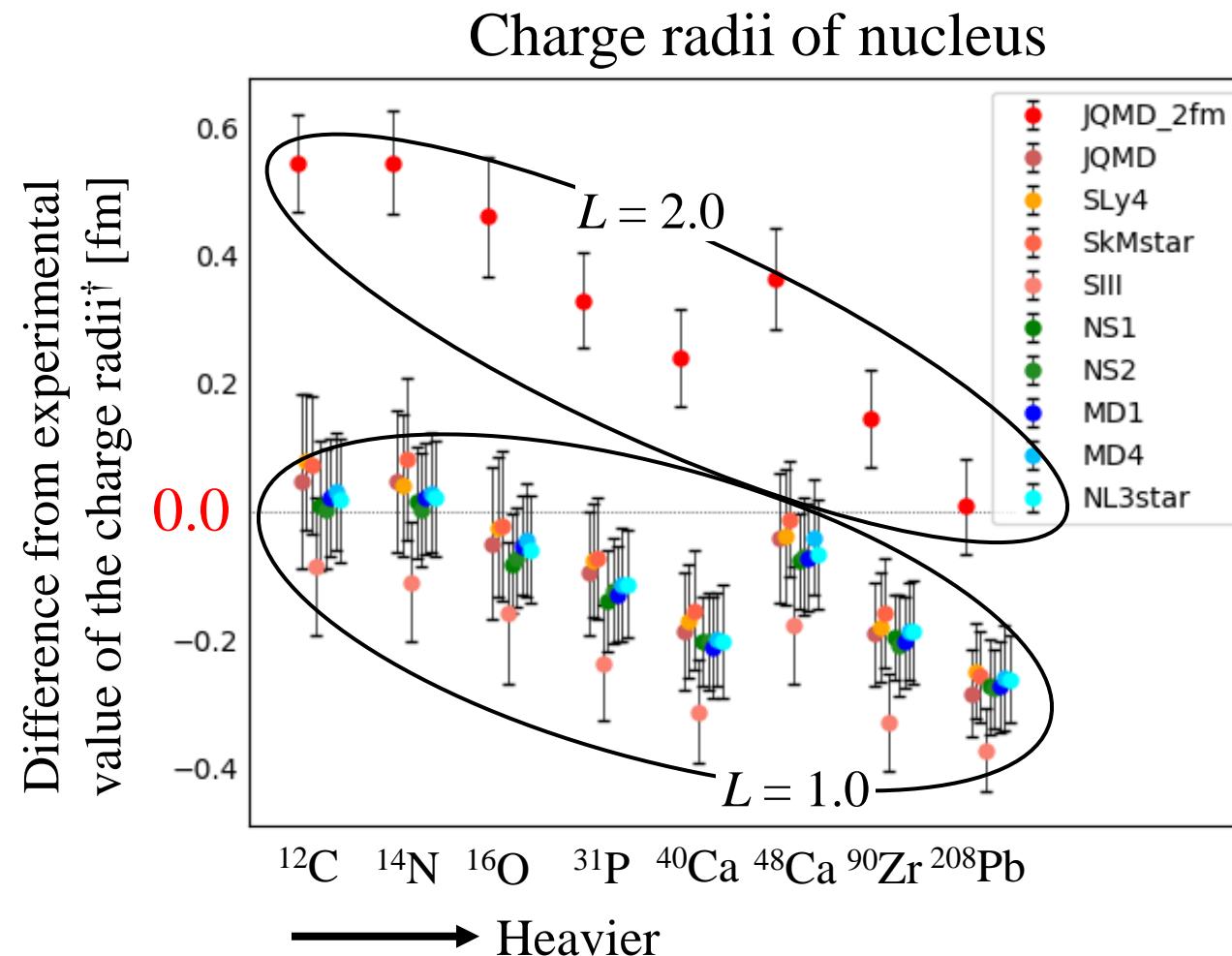
$$\varphi_i(\mathbf{r}) \equiv \frac{1}{(2\pi L)^{3/4}} \exp\left(-\frac{(\mathbf{r} - \mathbf{r}_i)^2}{4L} + \frac{i}{\hbar} \mathbf{r} \cdot \mathbf{p}_i\right)$$

$L = 2.0$  [fm] for QMD

$L = 1.26$  [fm] for LIQMD



For heavier nuclei, the difference from the experimental values is larger with small  $L$ . For this reason, at best, mass number  $A \leq 64$  is recommended.



†: I. Angeli, K.P. Marinova, Atomic Data and Nuclear Data Tables, 99, 2013, 69-95.

# Implementation

# Implementation of LIQMD

## Materials and Methods

qmd

Source code

source/processes/hadronic/models/

light\_ion\_qmd

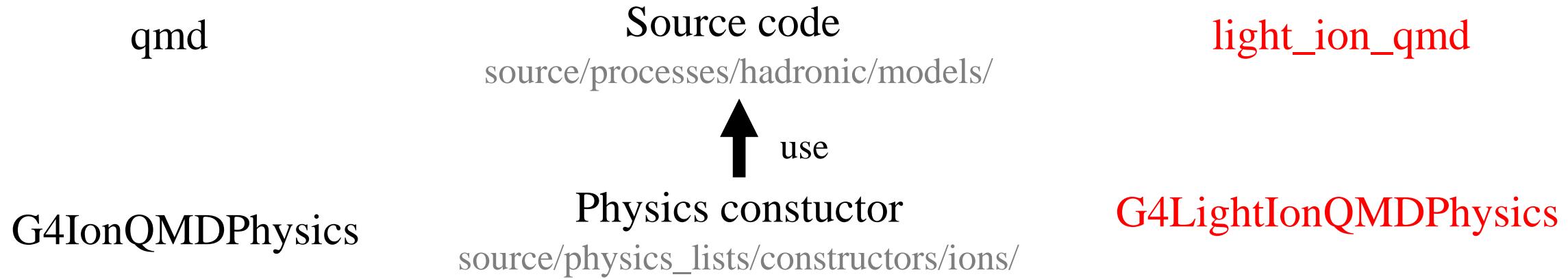
- G4QMReaction
- G4QMDMeanField
- G4QMDCollision
- G4QMDParameters
- G4QMDNucleus
- G4QMDGroundStateNucleus
- G4QMDSystem
- G4QMDParticipant

- G4LightIonQMReaction
- G4LightIonQMDMeanField
- G4LightIonQMDCollision
- G4LightIonQMDParameters
- G4LightIonQMDNucleus
- G4LightIonQMDGroundStateNucleus
- G4LightIonQMDSystem
- G4LightIonQMDParticipant

I might put these files in the qmd folder.

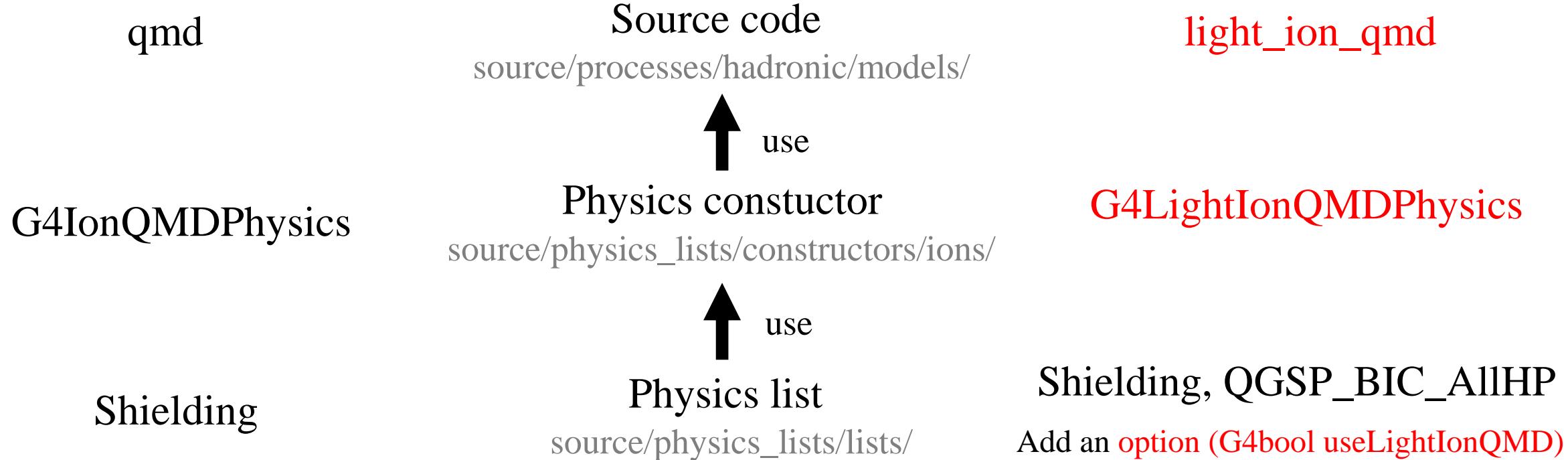
# Implementation of LIQMD

## Materials and Methods



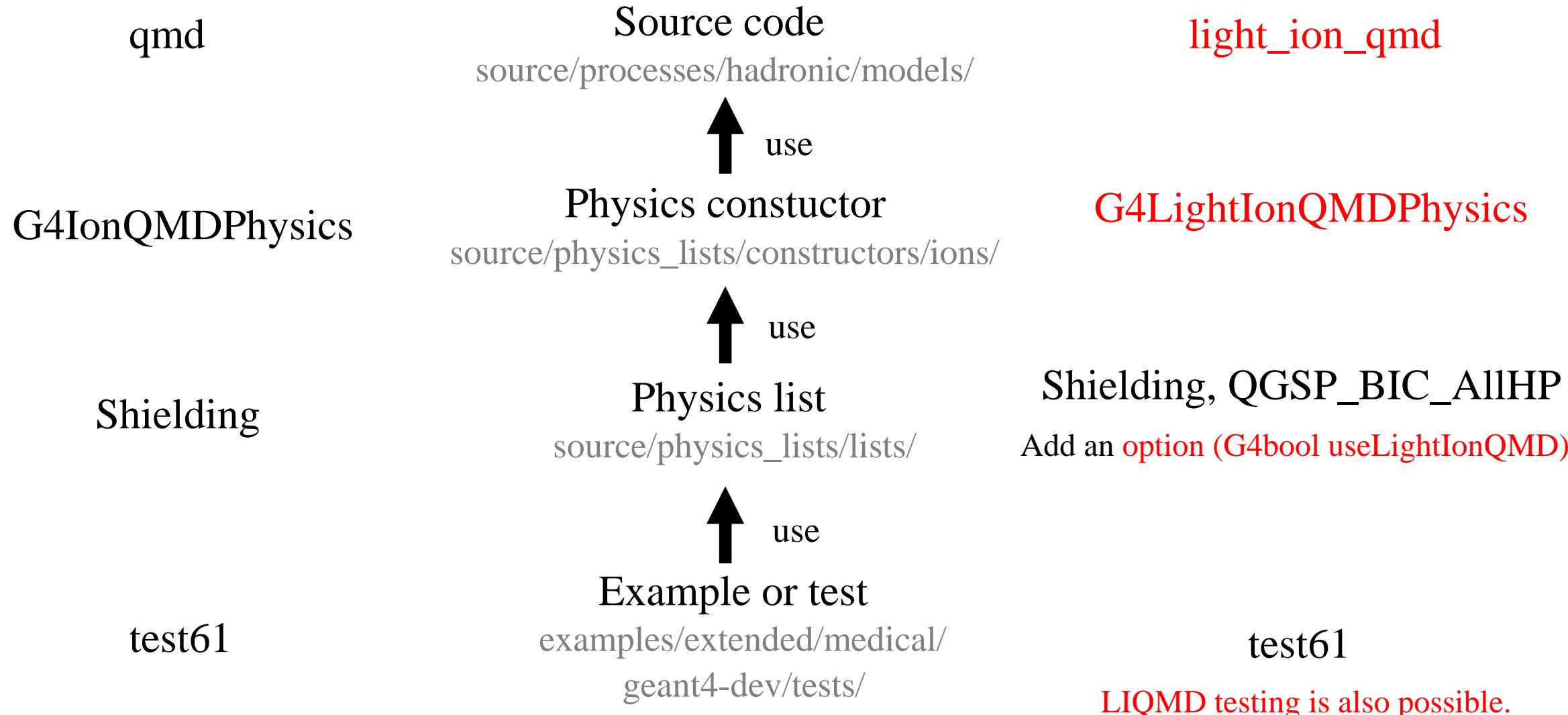
# Implementation of LIQMD

## Materials and Methods



# Implementation of LIQMD

## Materials and Methods



# |Summary and Future plan

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- We have improved the QMD especially for hadron therapy using light ions and are considering to implement it as “Light Ion QMD” in Geant4.
- We have verified the performance of Light Ion QMD with various experimental data and confirmed that it is as good as or better than the conventional QMD model, at least in light ion beams and targets.
- Currently, the merge request is underway.

Thank you for listening