

# Probing High Scale Physics with Standard Model Parameters

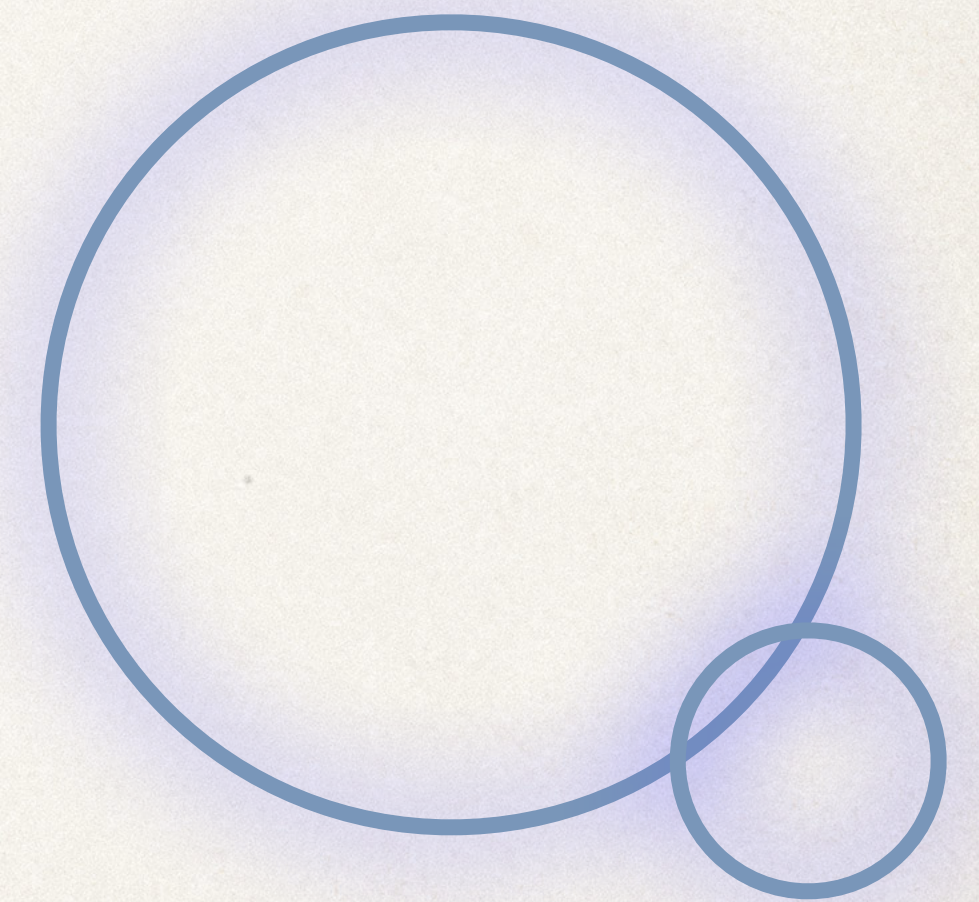
7<sup>th</sup> FCC Workshop • Annecy, France

David Dunsky, Lawrence Hall, Keisuke Harigaya

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01-30-24

[arXiv:1902.07726](https://arxiv.org/abs/1902.07726), [1908.02756](https://arxiv.org/abs/1908.02756), [2007.12711](https://arxiv.org/abs/2007.12711)





# The Higgs Quartic

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$$V(H) = -m^2|H|^2 + \lambda|H|^4$$

❖ 1967:

$$\langle H \rangle = v$$

Weinberg

❖ 2012:

$$m, \lambda$$

ATLAS, CMS



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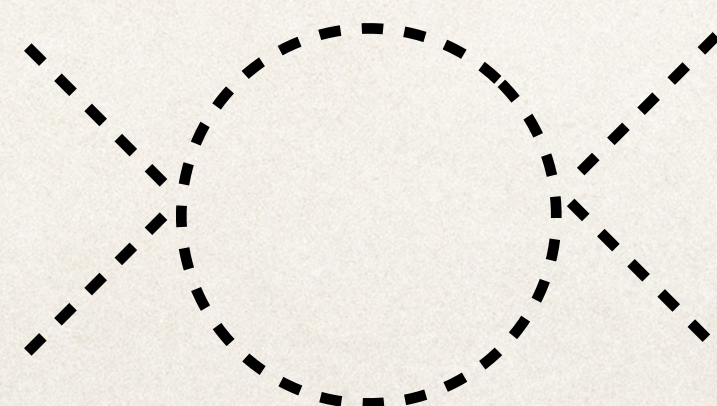
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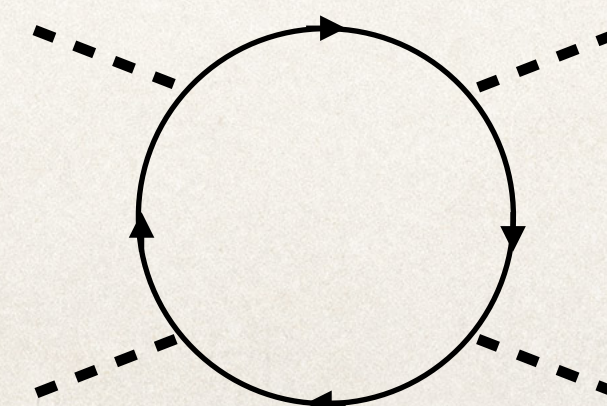
ATLAS, CMS

❖ Inferred value of  $\lambda$  appears special:



Higgs loop

$\lambda$  ↑



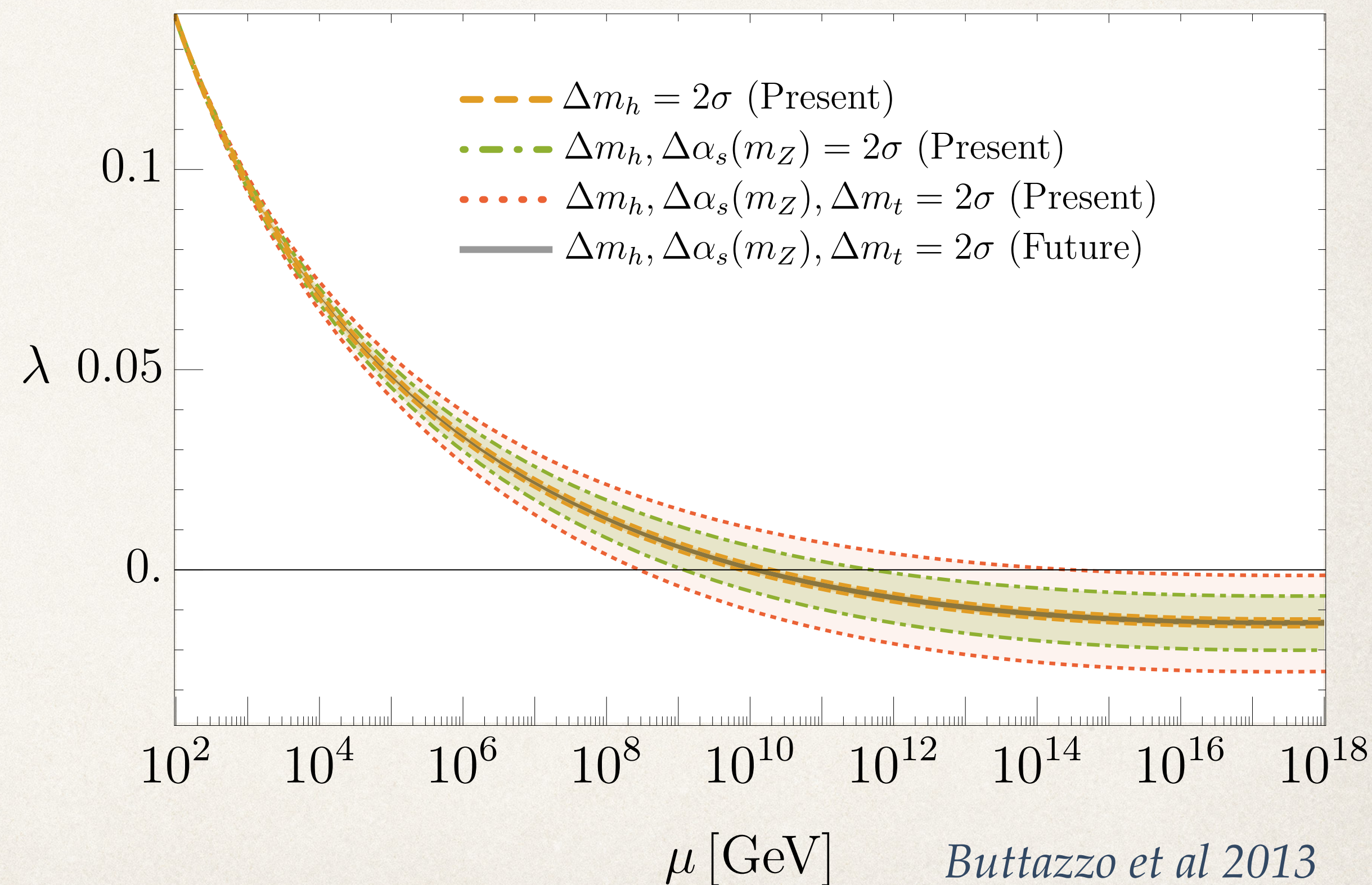
top loop

$\lambda$  ↓



# The Higgs Quartic

- ❖ Why is  $\lambda \sim .01$  above  $10^9$  GeV?
- ❖ Why does  $\lambda$  cross 0 between  $10^9 - 10^{13}$  GeV?
- ❖ Vanishing  $\lambda$  hint of new, high scale physics?





# Vanishing of Higgs Quartic by a $Z_2$

---

❖ Consider a  $Z_2$

$$\begin{aligned} SU(2) &\leftrightarrow SU(2)' \\ H &\leftrightarrow H' \\ (2, 1) &\quad (1, 2) \end{aligned}$$

❖ Most general potential

$$V(H, H') = -m^2(|H|^2 + |H'|^2) + \frac{\lambda}{2}(|H|^2 + |H'|^2)^2 + \lambda'|H|^2|H'|^2$$



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(174 GeV)<sup>2</sup>



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$\uparrow$   
 $(174 \text{ GeV})^2$

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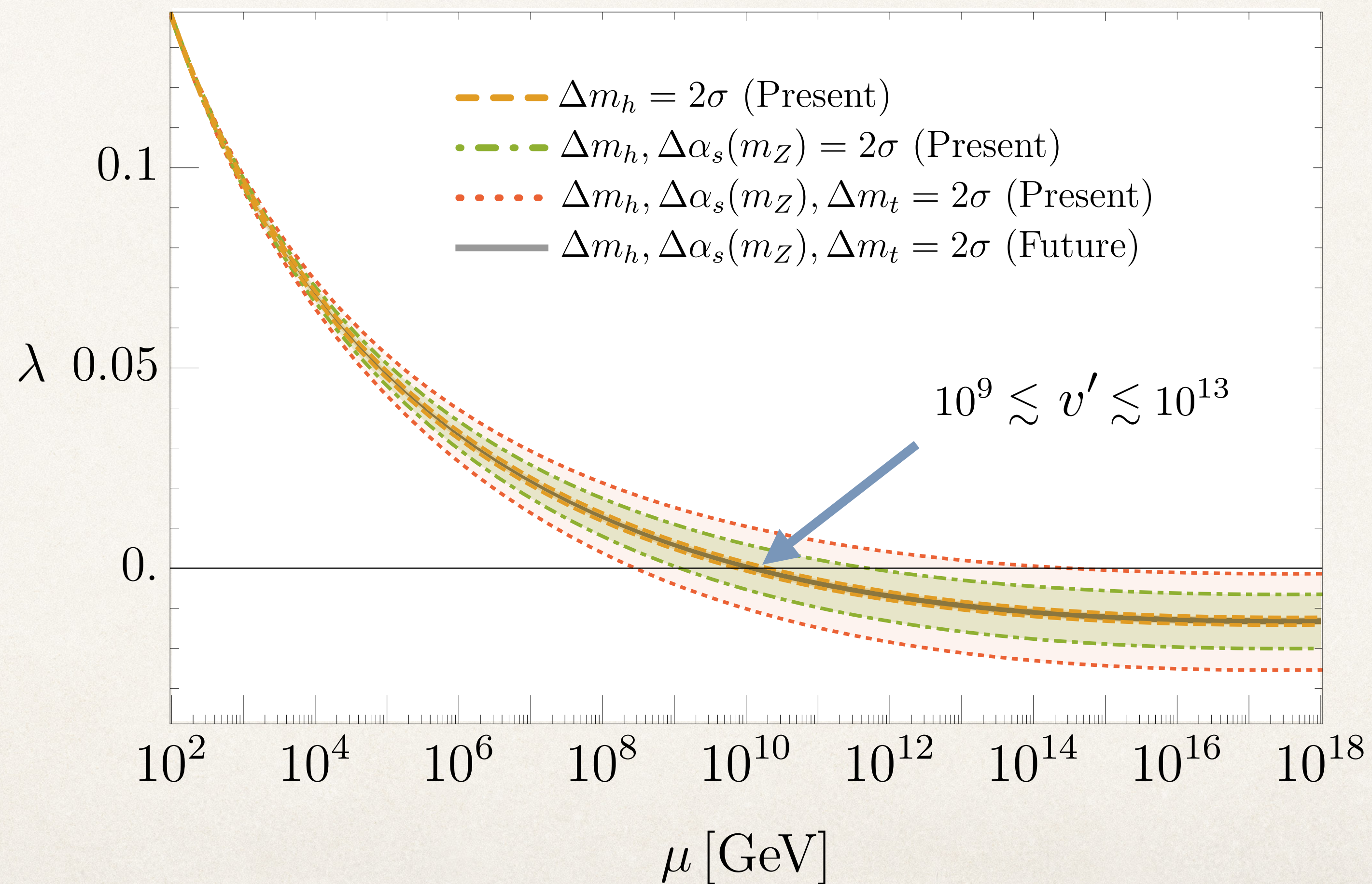
↑  
 $(174 \text{ GeV})^2$

$$V_{\text{LE}}(H) = \underbrace{\lambda' v'^2}_{-m_{\text{SM}}^2} |H|^2 - \underbrace{\lambda' \left(1 + \frac{\lambda'}{2\lambda}\right)}_{\lambda_{\text{SM}}} |H|^4$$

- Requiring  $v \ll v' \longrightarrow \lambda' \ll 1 \longrightarrow \lambda_{\text{SM}} \approx 0$



# Renormalization Running of $\lambda$





# Fine-Tuning

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- ❖ Fine-tuning required, but same as Standard Model

$$\left(\frac{v^2}{m^2}\right) \times \left(\frac{m^2}{\Lambda^2}\right) = \frac{v^2}{\Lambda^2}$$

↑                      ↑

Tuning of  $\lambda'$       Tuning of  $v'$



# Importance of Precise SM Parameter Measurements

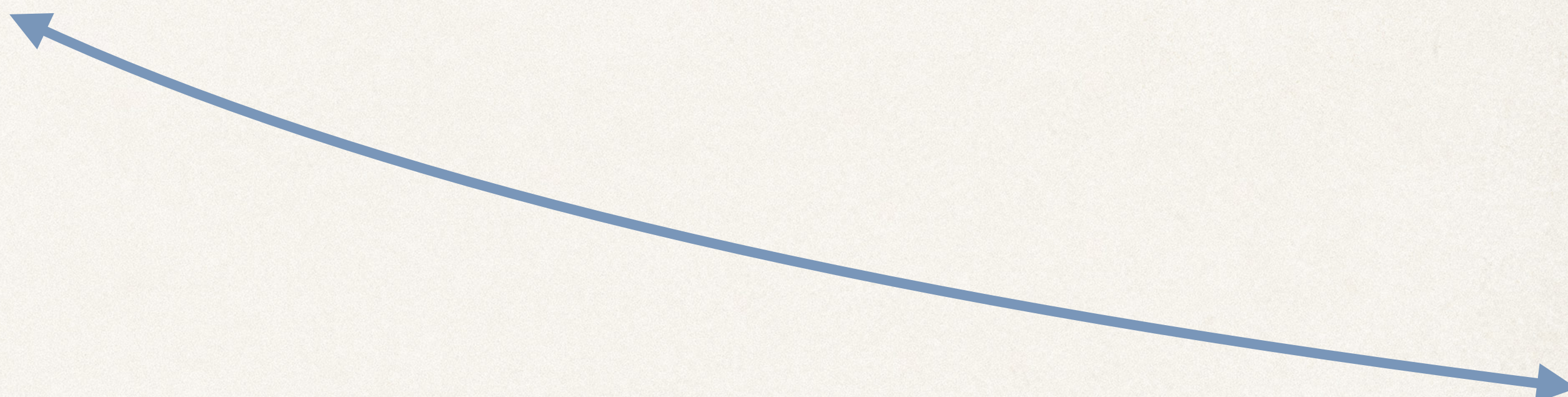
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- ❖ Important to measure  $m_t$ ,  $m_h$ ,  $\alpha_s(m_Z)$  precisely!
- ❖ FCC will be fantastic at this



# Importance of Precise SM Parameter Measurements

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- ❖ Important to measure  $m_t$ ,  $m_h$ ,  $\alpha_s(m_Z)$  precisely!
  - ❖ FCC will be fantastic at this
  - ❖ In phenomenological models, the BSM physics depend only (or mostly) on  $v'$ 
    - ❖ No new free parameters for most new observables!
    - ❖ FCC will provide precise predictions
- 



# Models of Higgs Parity

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- ❖ Can embed  $Z_2$  (“Higgs Parity”) in: *Hall & Harigaya (2018)*



# Models of Higgs Parity

---

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❖ Mirror electroweak sector

[1902.07726](#)

$$(SU(2)_L \times U(1)_Y) \times (SU(2)'_L \times U(1)'_Y)$$



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- ❖ Mirror electroweak sector  $(SU(2)_L \times U(1)_Y) \times (SU(2)'_L \times U(1)'_Y)$   
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- ❖ Mirror Standard Model  $(SU(3)_c \times SU(2)_L \times U(1)_Y) \times (SU(3)'_c \times SU(2)'_L \times U(1)'_Y)$   
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[2007.12711](#)
- ❖ Focus on first one for this talk, will mention interesting signals of others



# The Mirror Electroweak Sector

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- ❖ Extend  $Z_2$  to mirror electroweak sector
- ❖ Identify  $Z_2$  with spacetime parity

$$SU(2) \times U(1) \leftrightarrow SU(2)' \times U(1)'$$

$$\vec{x} \leftrightarrow -\vec{x}$$

$$q, \bar{u}, \bar{d}, l, \bar{e} \leftrightarrow (q', \bar{u}', \bar{d}', l', \bar{e}')^\dagger$$

$$H \leftrightarrow H'$$

- ❖ Implications?



# Solves Strong CP Problem

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- ❖  $SU(3) \times (SU(2) \times U(1)) \times (SU(2)' \times U(1)')$  solves strong CP problem

Babu, Chang, Senjanovic (1991)

- ❖ Parity is a symmetry

- ❖  $\frac{\theta}{32\pi^2} G\tilde{G}$  forbidden

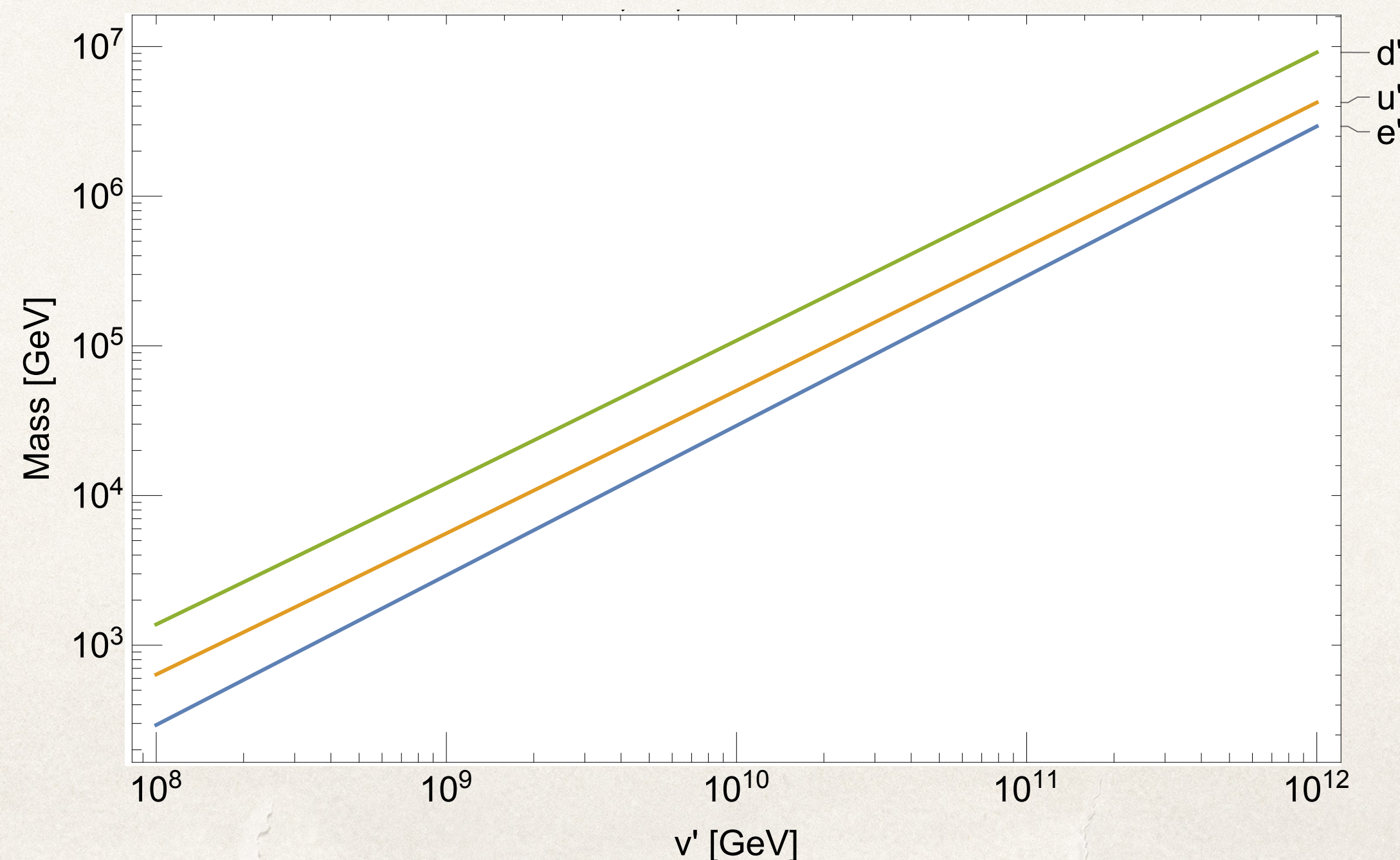
- ❖ No  $\bar{\theta}$  contribution from Yukawa sectors

- ❖  $\arg \det \begin{pmatrix} y_{u,d} & v \\ 0 & y_{u,d}^* v' \end{pmatrix} = 0$



# Mirror Dark Matter

- ❖ Natural DM candidate lightest  $U(1)'_{EM}$  particle,  $e'$
- ❖ DM mass  $m_{e'} = y_{e'} v' = m_e \frac{v'}{v}$  (1-10<sup>4</sup> TeV)





# Signals: Neutron EDM

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- ❖ Higher dimensional operators generate

- ❖  $\mathcal{L}_6 = \frac{C}{M_{Pl}^2} (|H|^2 - |H'|^2) G\tilde{G}$

$$\theta = 32\pi^2 C \left( \frac{v'}{M_{Pl}} \right)^2 = 5 \times 10^{-11} C \left( \frac{v'}{10^{12} \text{ GeV}} \right)^2$$

- ❖ Current neutron EDM limit  $\theta < 10^{-10}$  Baker, et al (2006)

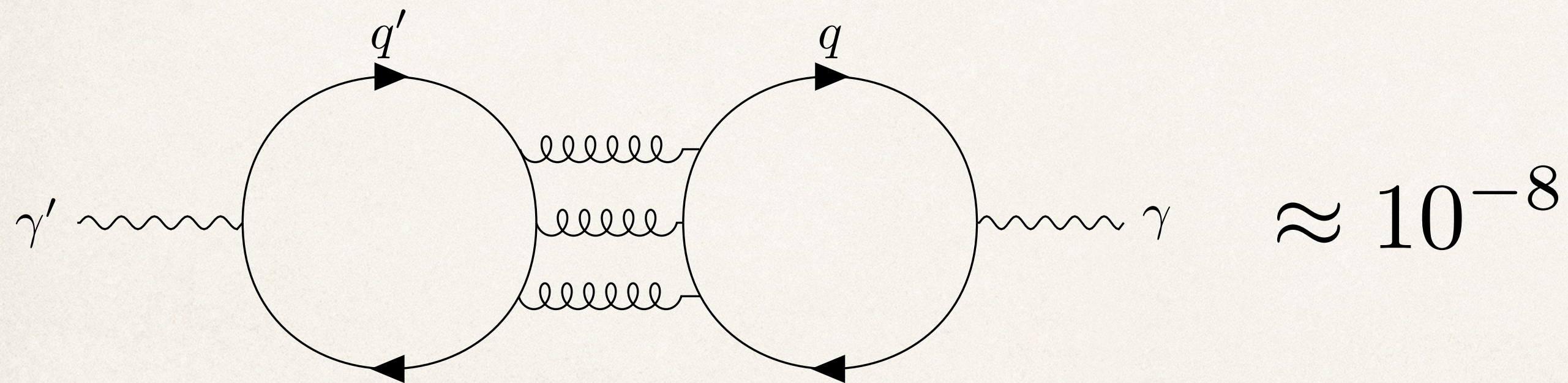


# Signals: Kinetic Mixing

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✦  $\mathcal{L} \supset -\frac{\epsilon_B}{2} B^{\mu\nu} B'_{\mu\nu}$  allowed

✦ Generated by



(Calculable from 4-loop QCD beta function)

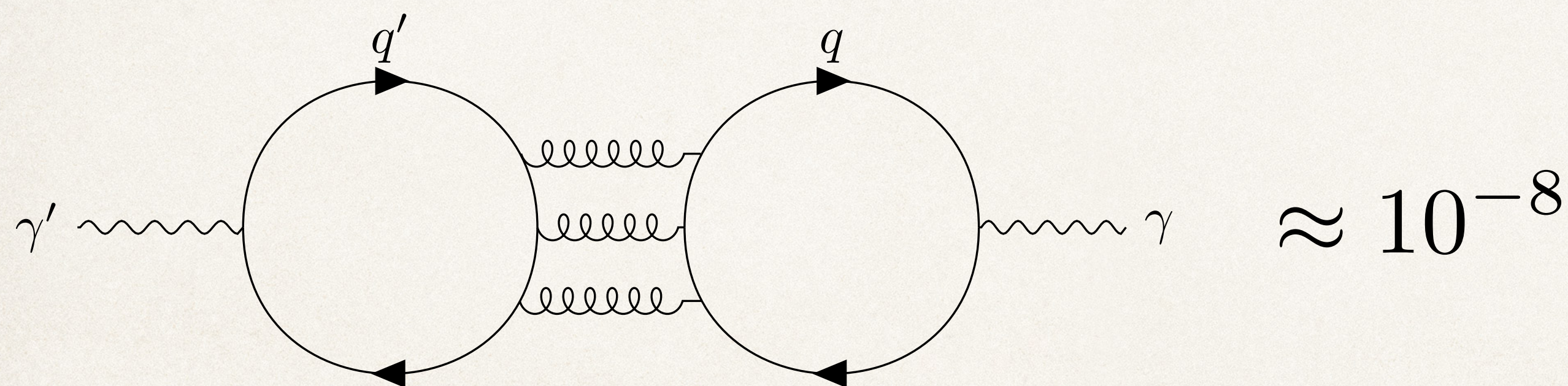
van Ritbergen, Vermaseren, Larin (1997)



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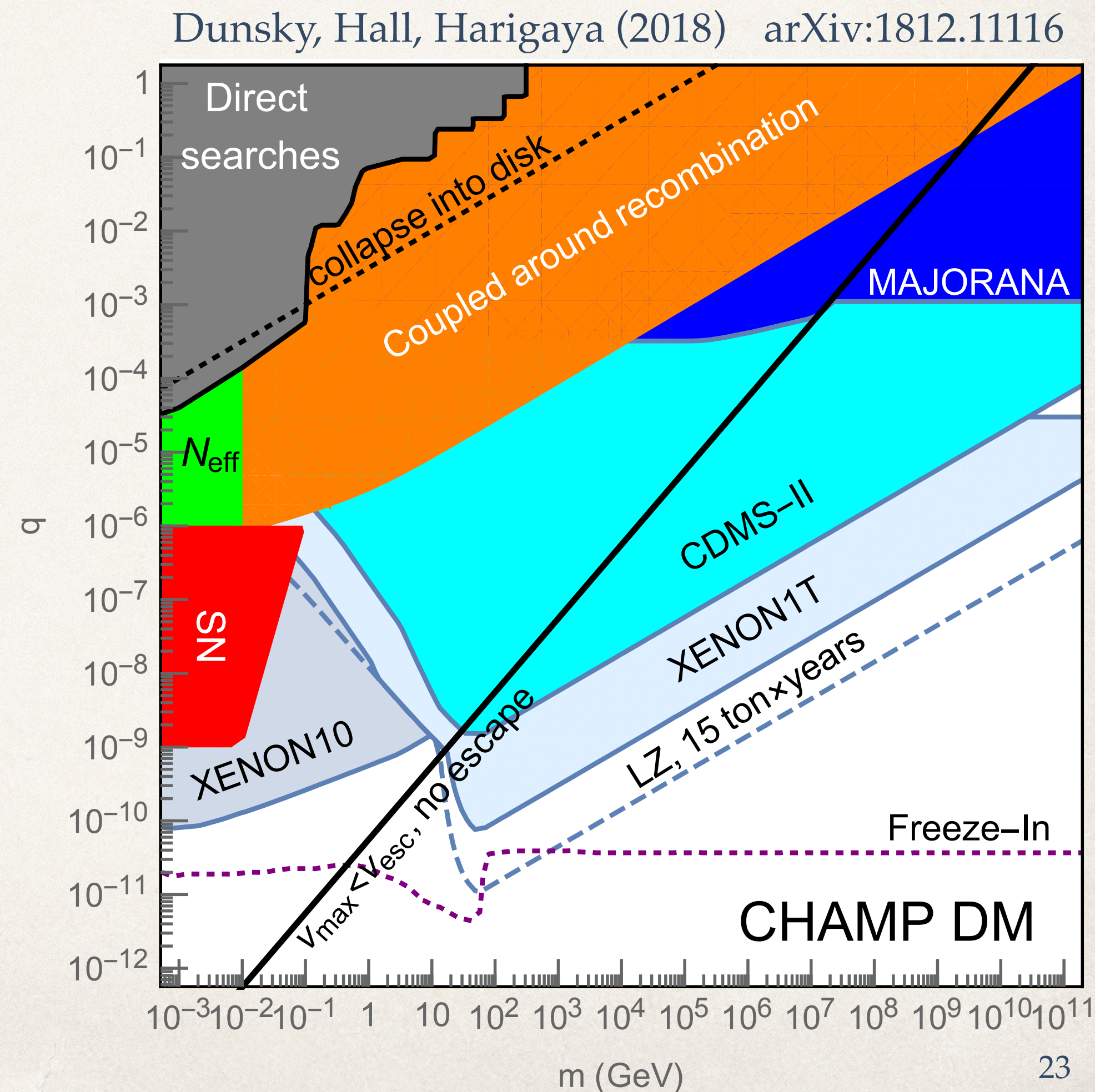
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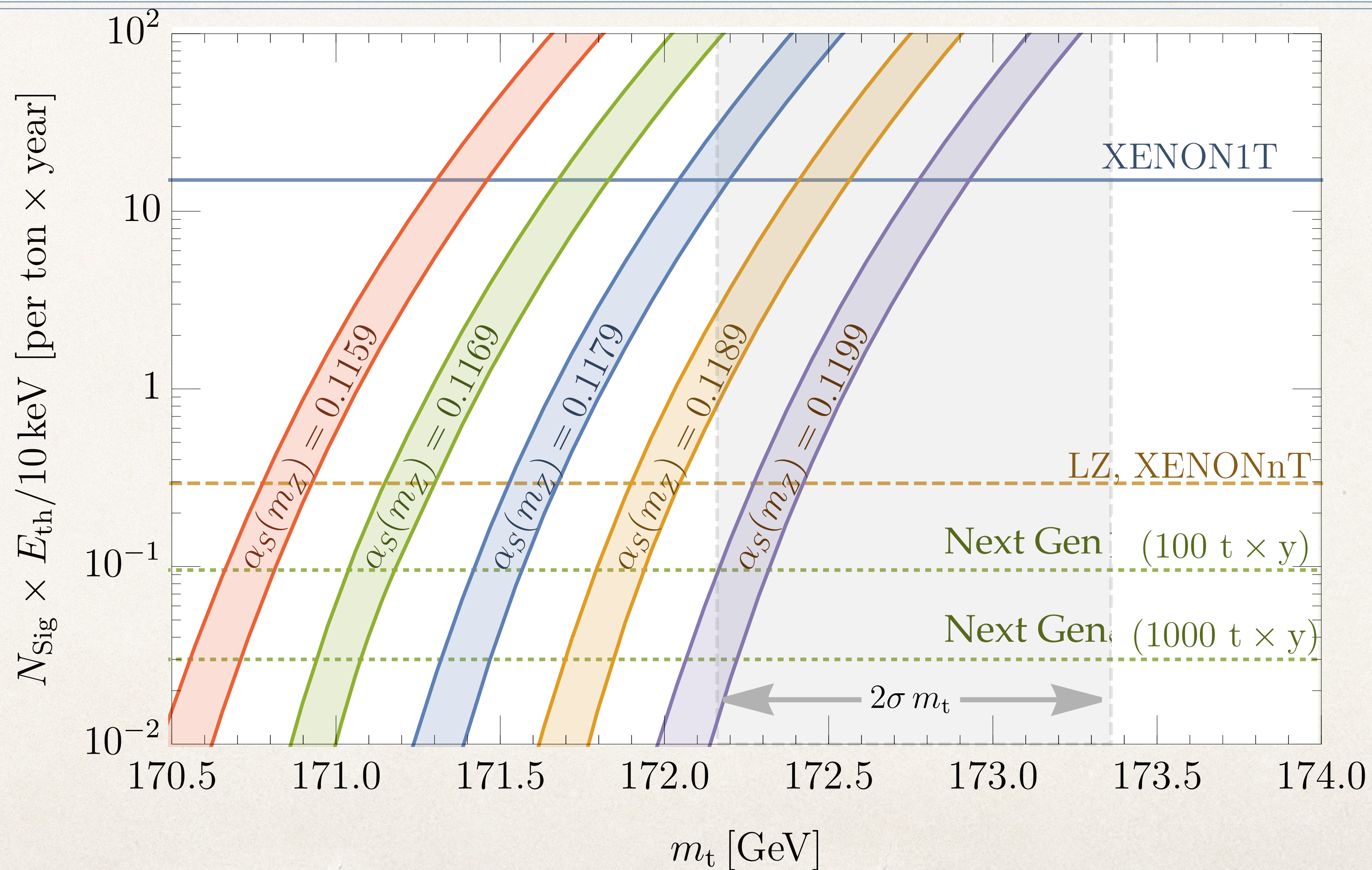
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# Signals: Kinetic Mixing





# Other Higgs Parity Models:

$$G_{\text{SM}} \times G_{\text{SM}'}$$

- ❖ Unlike Standard Model, mirror quark masses  $> \Lambda_{\text{QCD}'}$

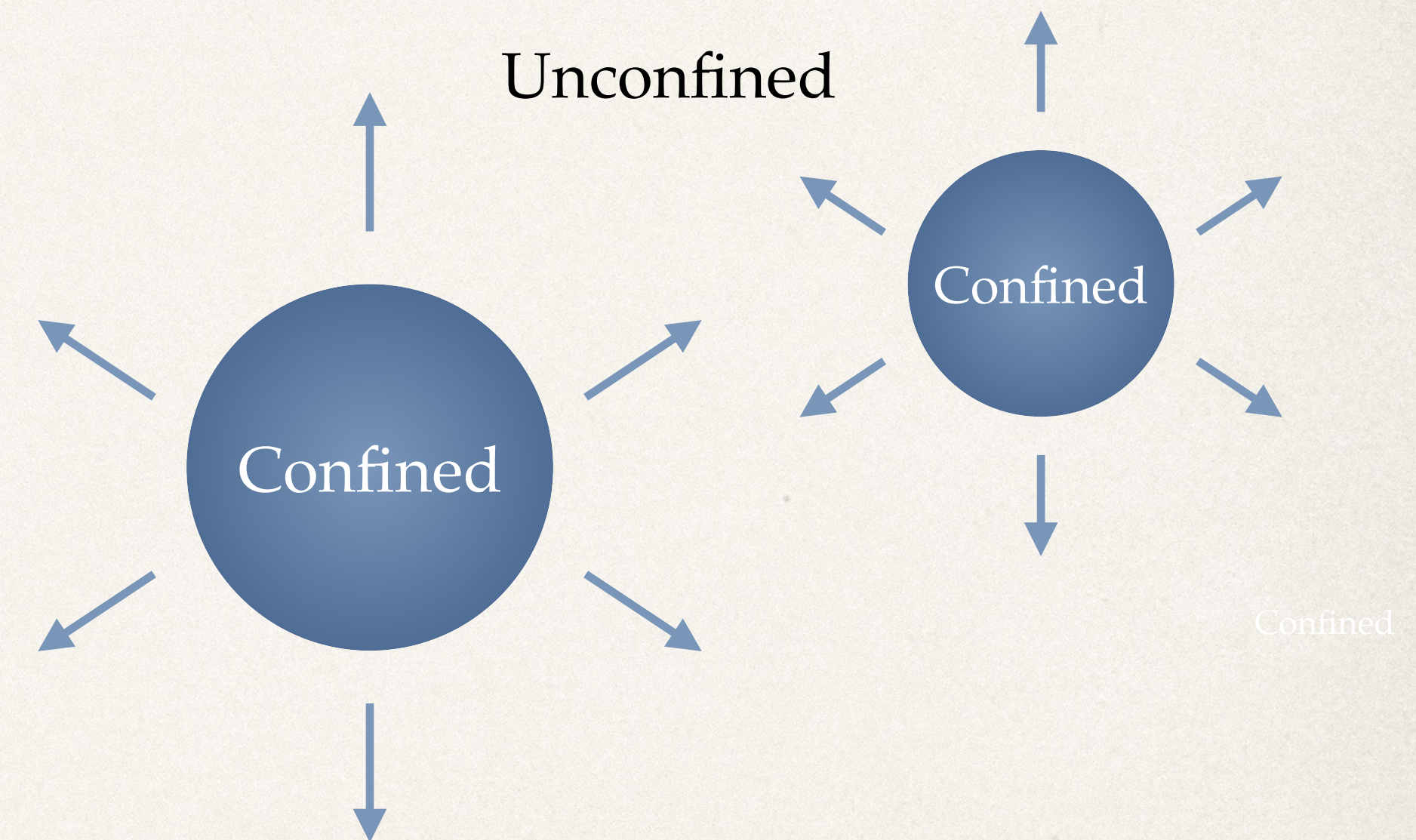


- ❖ QCD' phase transition is 1st order

*Yaffe & Svetitsky 1982 & 1983*

- ❖ Gives rise to expanding bubbles

- ❖ Gravitational Waves from bubble collisions and interactions with plasma. Signal depends on  $v'$



*Witten 1982*



# Other Higgs Parity Models: $SU(2)_L \times SU(2)_R$

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- ❖ Necessarily predicts right-handed neutrinos  $\begin{pmatrix} \nu \\ e \end{pmatrix}_L \leftrightarrow \begin{pmatrix} N \\ e \end{pmatrix}_R$
- ❖  $N$  SM gauge singlets. If long-lived,  $N_1$  can be dark matter
- ❖ *Three Weinberg operators*  $-\mathcal{L}_{LR} \supset f_{ij} \frac{1}{\Lambda} (\ell_i \bar{\ell}_j) H_L H_R + f'_{ij} \frac{1}{\Lambda} (\ell_i \ell_j) H_L^2 + f'^{(*)}_{ij} \frac{1}{\Lambda} (\bar{\ell}_i \bar{\ell}_j) H_R^2 + \text{h.c.}$

$$\downarrow \\ M_N \simeq m_\nu (v_R/v)^2$$

- ❖ Interesting phenomenology.  $N_1$  DM mass and  $N_{2,3}$  leptogenesis depend on  $v_R$



# Summary

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- ❖ Observed Higgs mass imply next symmetry breaking scale of nature?
- ❖ Motivated by Strong CP  $\longrightarrow$  Higgs Parity, no QCD'
- ❖ Motivated by DM  $\longrightarrow$  mirror electroweak (also Left-Right)
- ❖ Same number of parameters as SM below  $v'$
- ❖ Future measurements of  $m_t, m_h, \alpha_s(m_Z)$  by FCC will hone in on  $v'$
- ❖ Entire parameter space will be probed / corroborated by future detectors