

Event shapes in Higgs decays

and measurements of hadronic Higgs branching ratios

Daniel Reichelt, 31 January 2024

This Talk...

Part I:

alternative ideas for Measurements of Higgs Boson Branching ratios based on event shapes [[Knobbe, Krauss, DR, Schumann '23](#)]

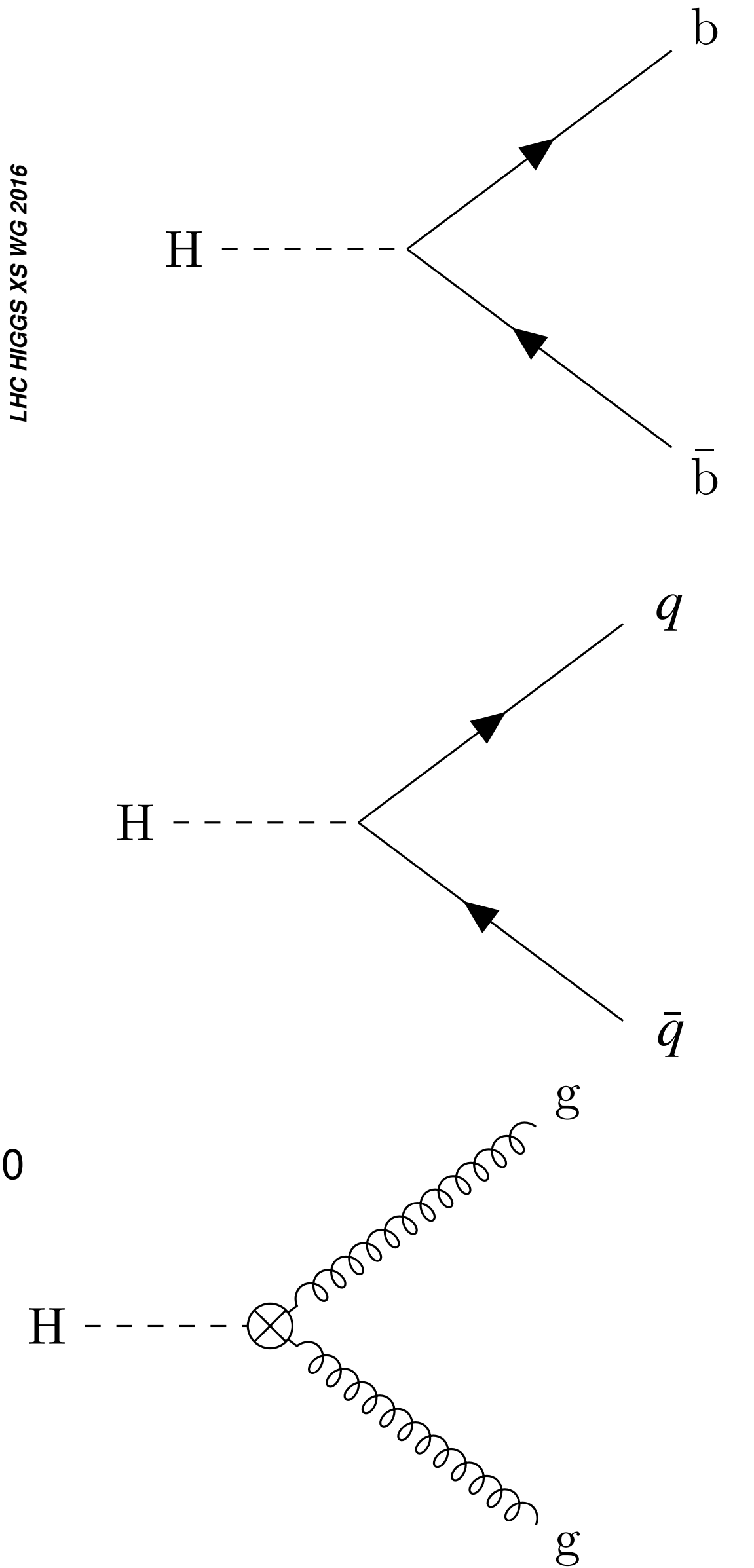
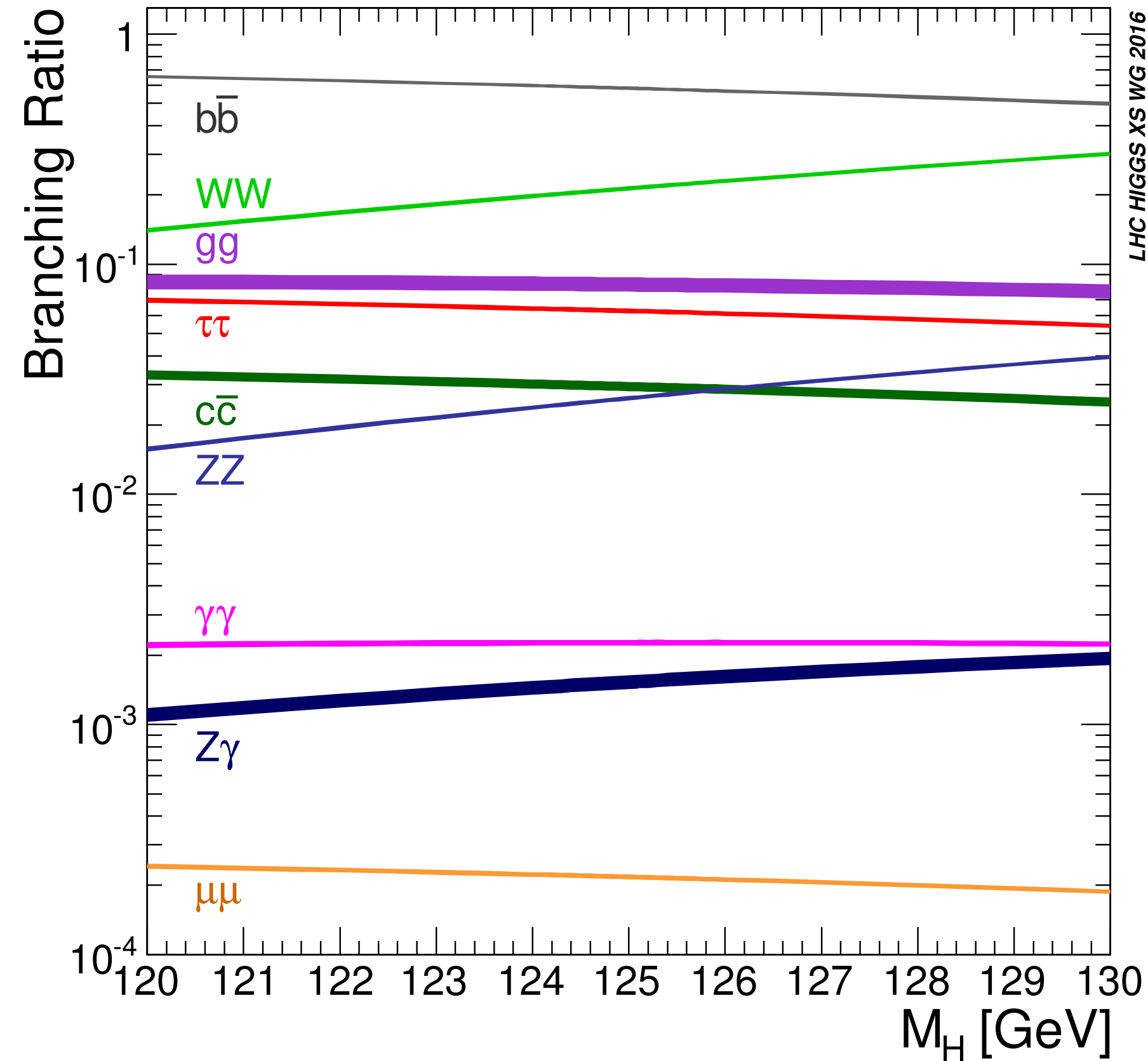
make use of clean environment in FCC-ee setting

Part II:

precision calculations for event shapes in Higgs decays with EERAD [[Coloretti, Gehrmann-de Ridder, Preuss '22](#)] [[Gehrmann-de Ridder, Preuss, Williams '23](#)] and resummation in Sherpa-CAESAR framework [[Gehrmann-de Ridder, Preuss, DR, Schumann WIP](#)]

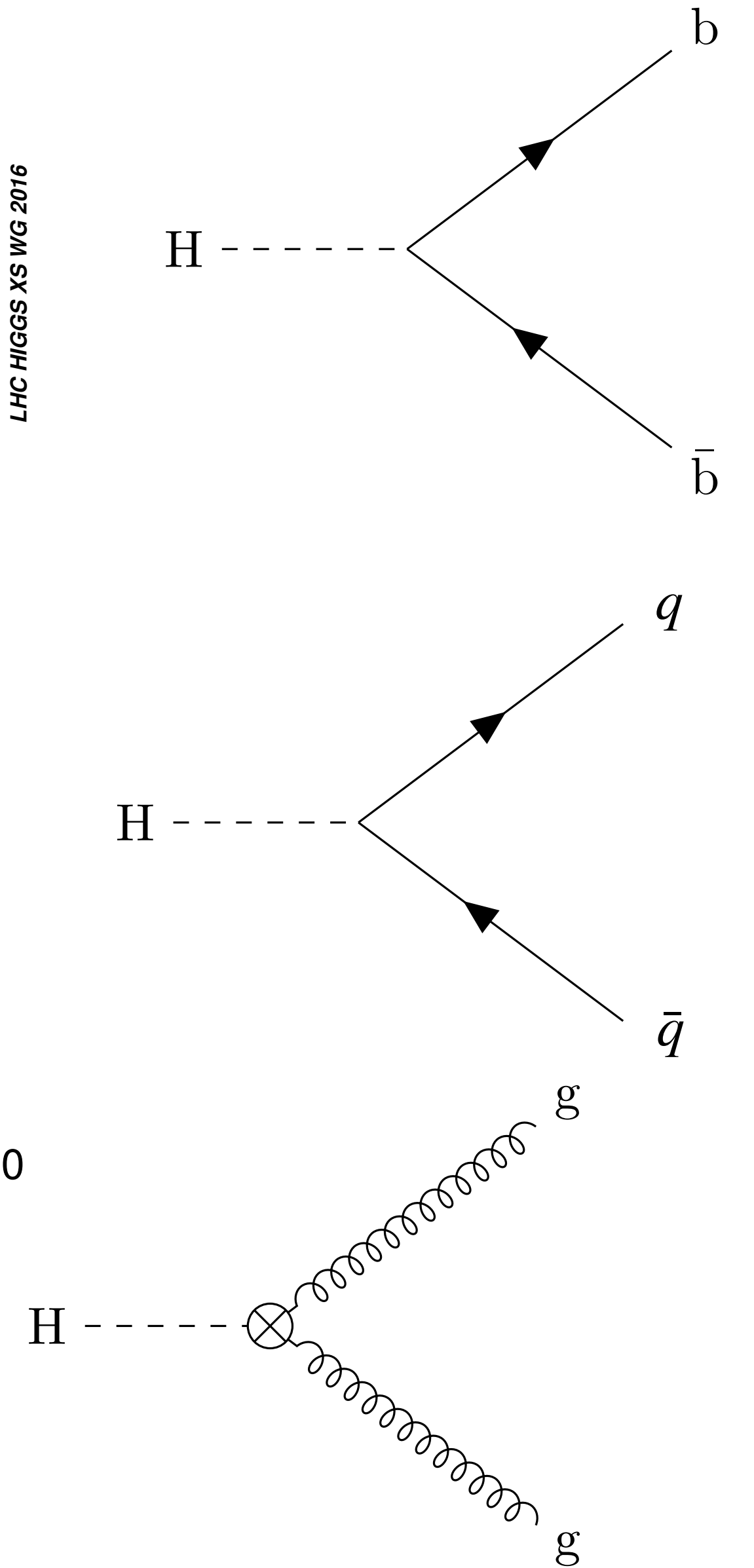
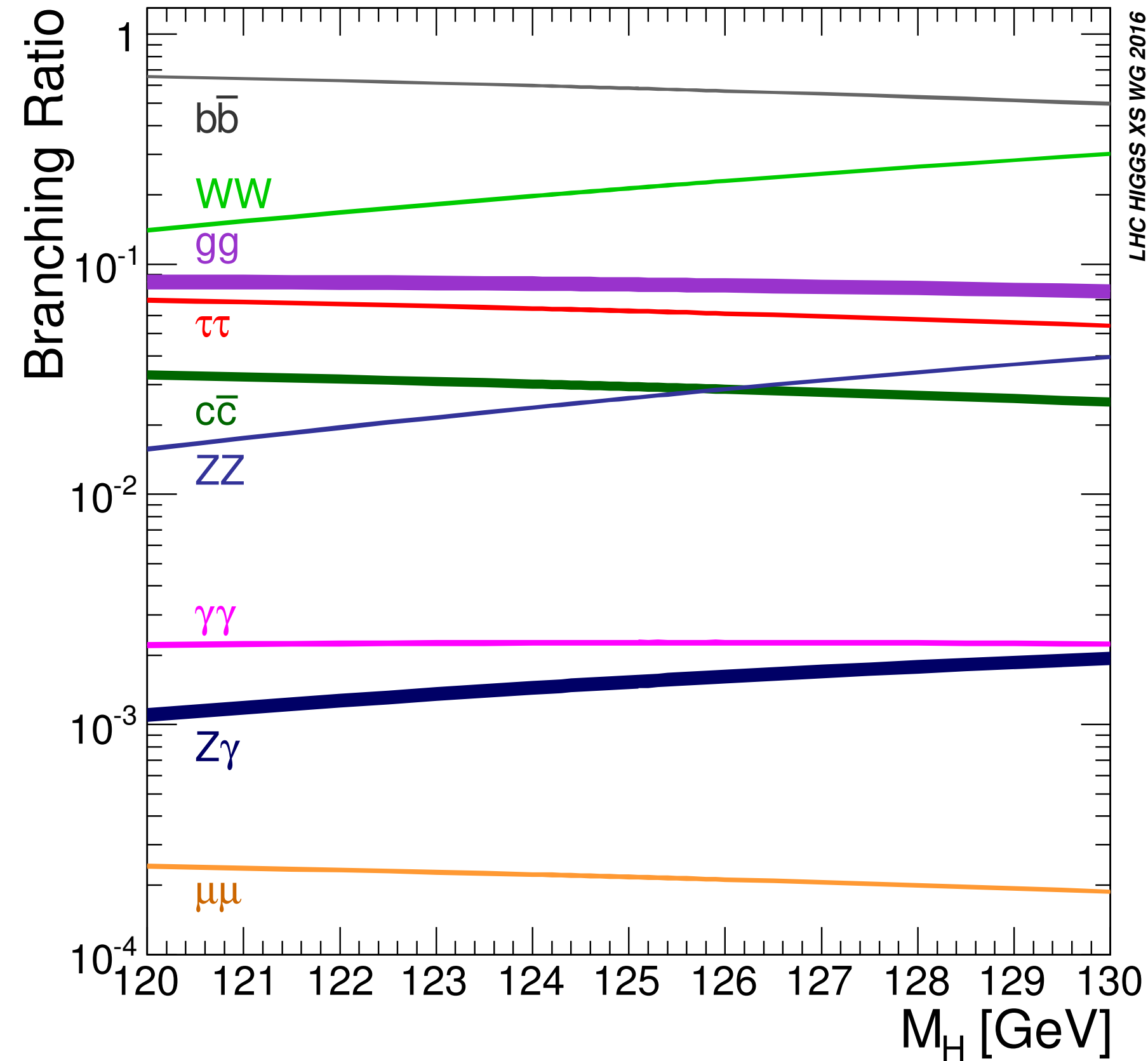
Hadronic Higgs Decays

- Higgs with $m_H = 125$ GeV:
- dominant decay into b-quarks (observed ATLAS/CMS in Run 2)
- tiny c-quark (first limits)
- substantial into gluons
- suppressed light (s-quark) BR



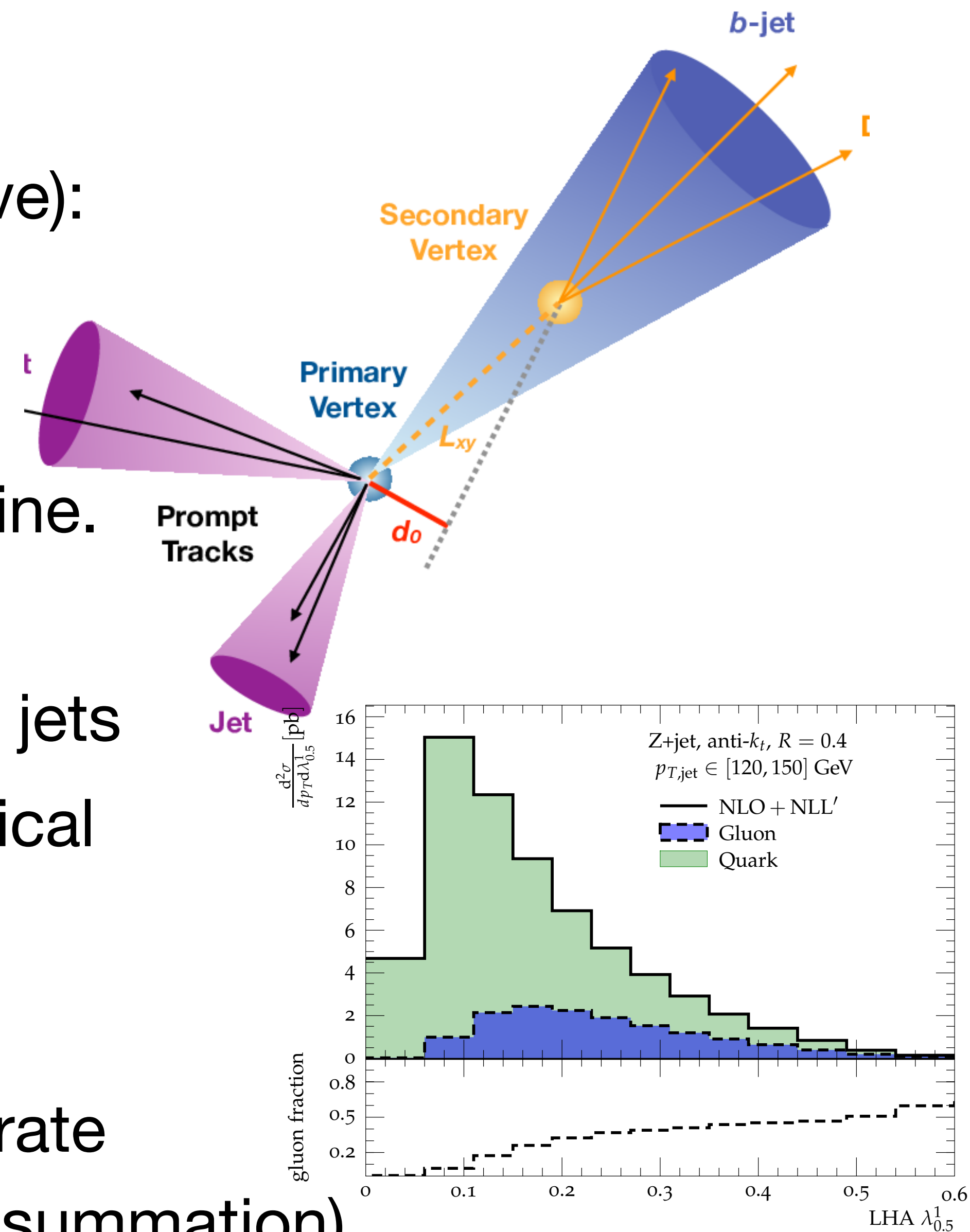
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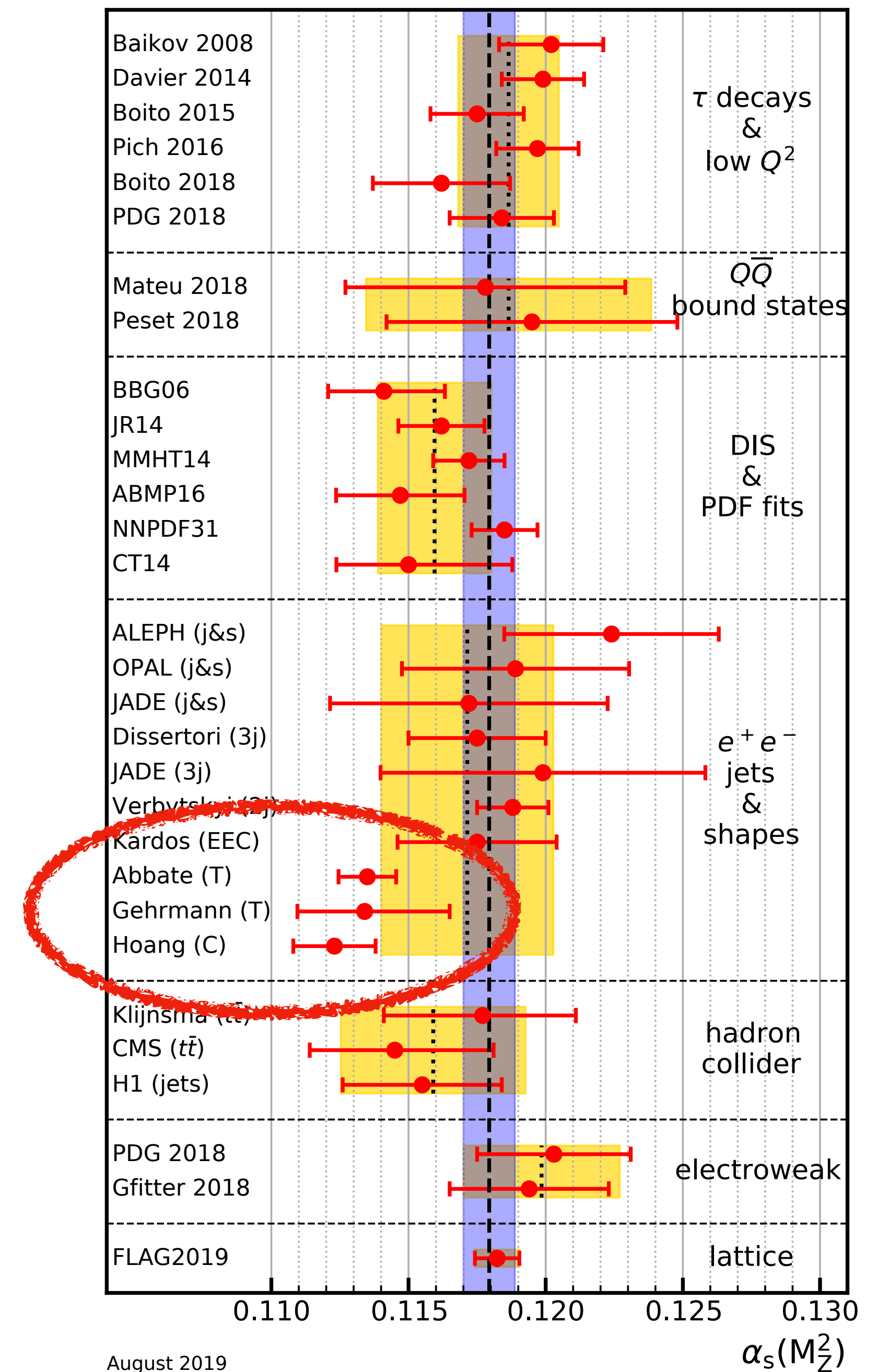
Event/Jet Shapes as taggers

- tagging in experiment (from a theorist's perspective):
 - look for displaced vertex, identify with decaying hadron (\sim heavy parton)
 - improvable with various techniques from machine learning etc.
 - application to H decays \rightarrow just count b tagged jets
- great performance, but often hard to gain theoretical understanding
 - theory study with event or jet shapes \rightarrow not necessarily most performant taggers, but accurate understanding possible (i.e. well defined FO, resummation)
 - can we apply this to H decays (challenge: without any vertex info)?



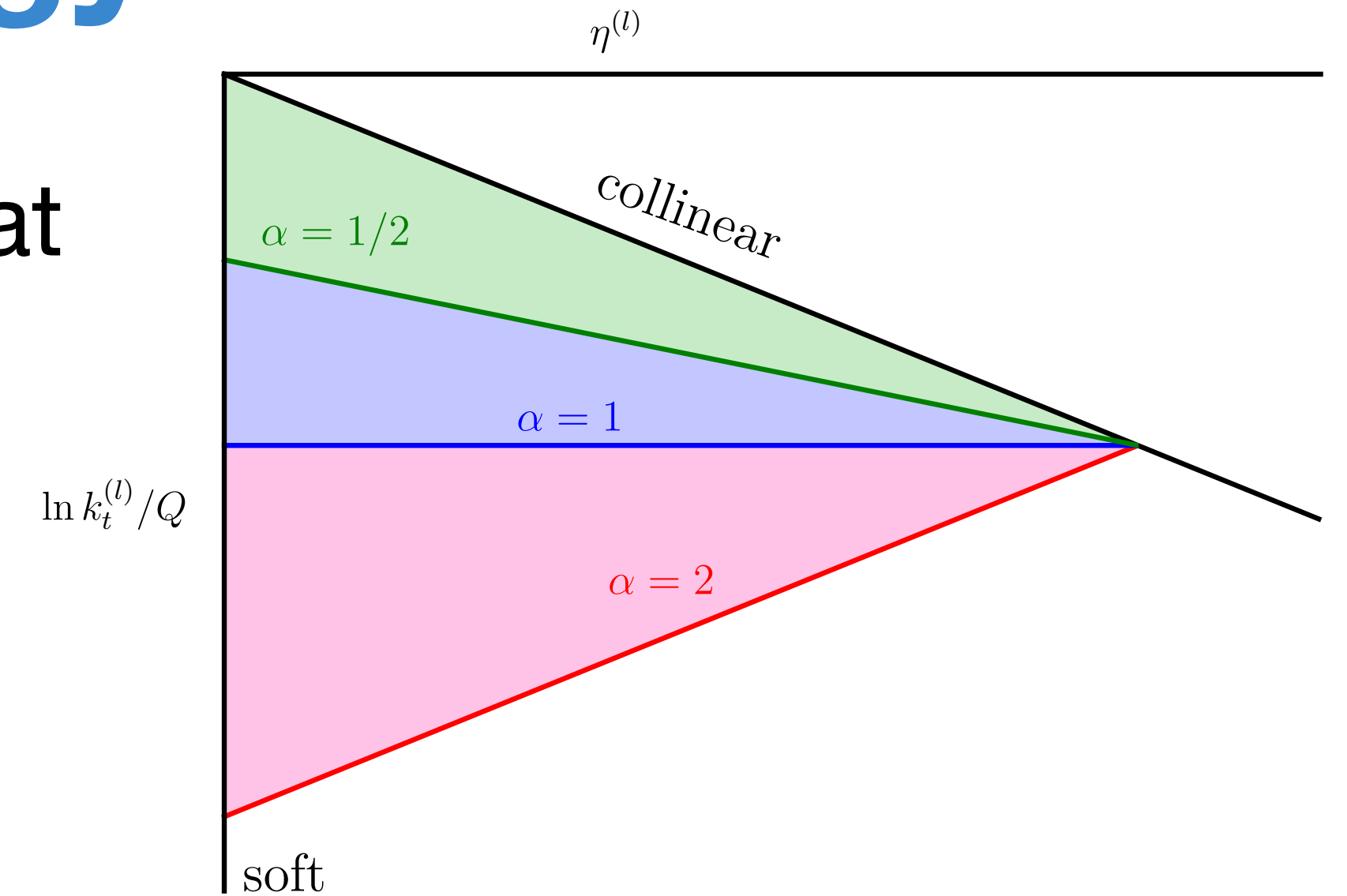
Event Shapes and α_s

- one traditional way to extract strong coupling constant:
- high accuracy (NNLO+NNLL) of event shapes (Thrust, C-Parameter etc.) fitted to LEP data at the Z-pole
- simple 1 or 2 parameter fit, can be pushed by theorists long after experiments are done



Event Shapes - Fractional Energy Correlations

- class of observables, typically normalised such that
 - $FC_x \rightarrow 0 \Rightarrow$ pencil-like event (little radiation),
 - $FC_x \rightarrow FC_x^{\max} < 1 \Rightarrow$ spherical event (a lot of radiation)



$$FC_x \equiv \sum_{i \neq j} \frac{E_i E_j |\sin \theta_{ij}|^x (1 - |\cos \theta_{ij}|)^{1-x}}{(\sum_i E_i)^2} \Theta [(\vec{q}_i \cdot \vec{n}_T)(\vec{q}_j \cdot \vec{n}_T)]$$

- parameter x determines weight of collinear emissions
- analogous to angularities at the LHC ($\alpha \sim 2 - x$)

Event Shapes in Higgs Decays

- naive picture

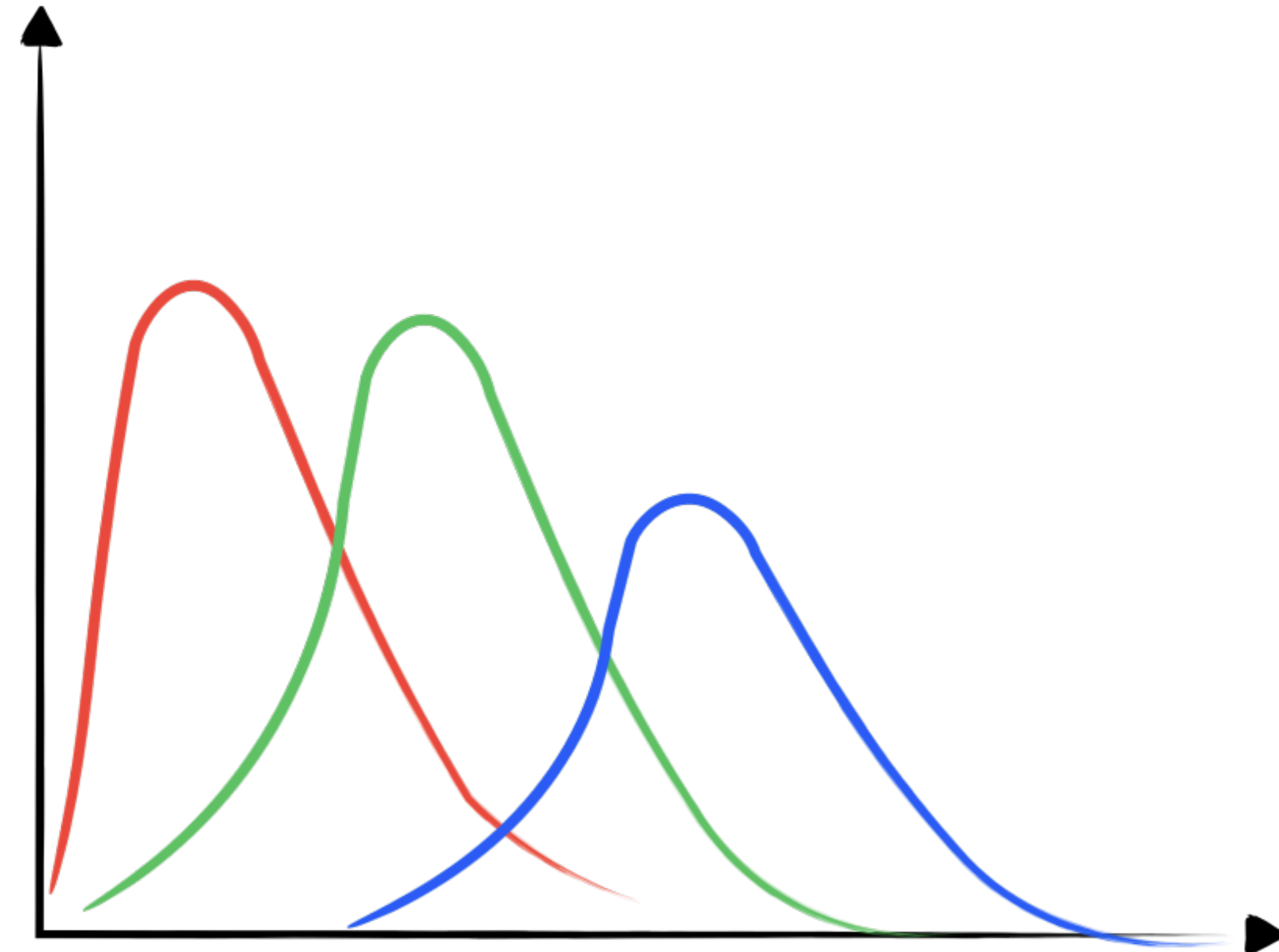
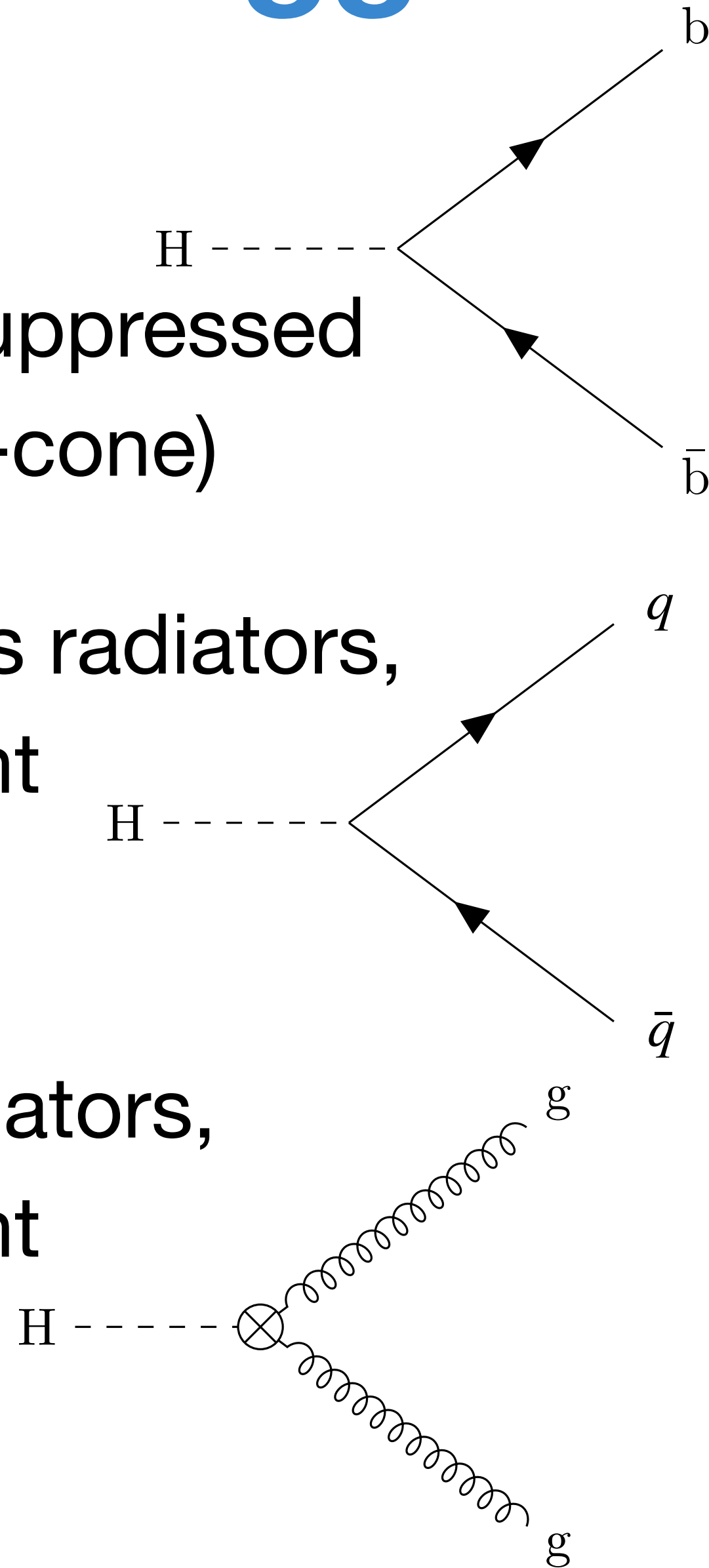
- **b-quarks:** radiation suppressed due to masses (dead-cone)

- **light quarks:** massless radiators, collinear enhancement

$$\propto C_F = 4/3$$

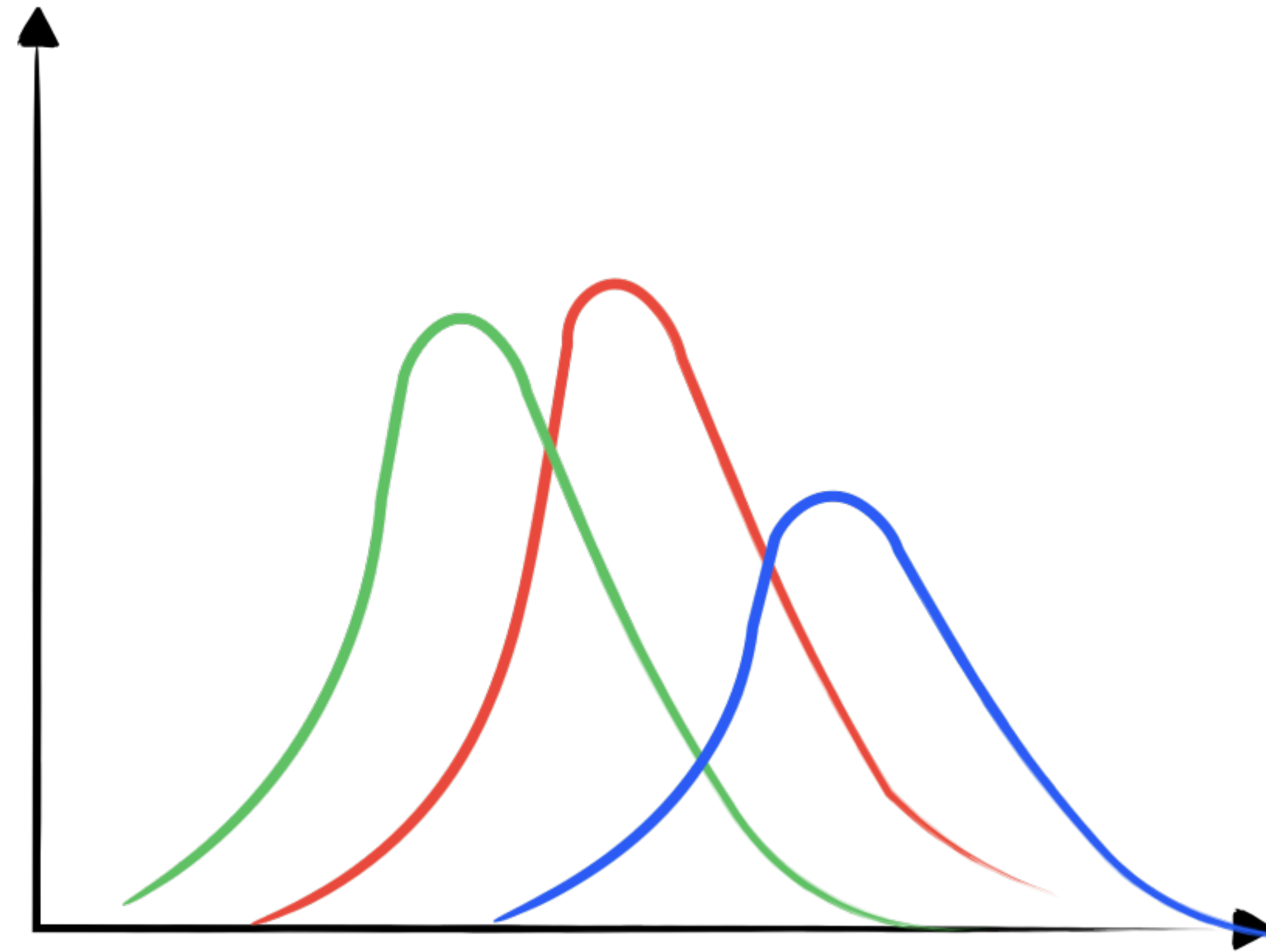
- **gluons:** massless radiators, collinear enhancement

$$\propto C_A > C_F$$



Event Shapes in Higgs Decays

- naive picture, at hadron level
- **b-quarks**: radiation suppressed due to masses (dead-cone), **high mass decay**
- **light quarks**: massless radiators, collinear enhancement
 $\propto C_F = 4/3$
- **gluons**: massless radiators, collinear enhancement
 $\propto C_A > C_F$



Effect of Yukawa couplings

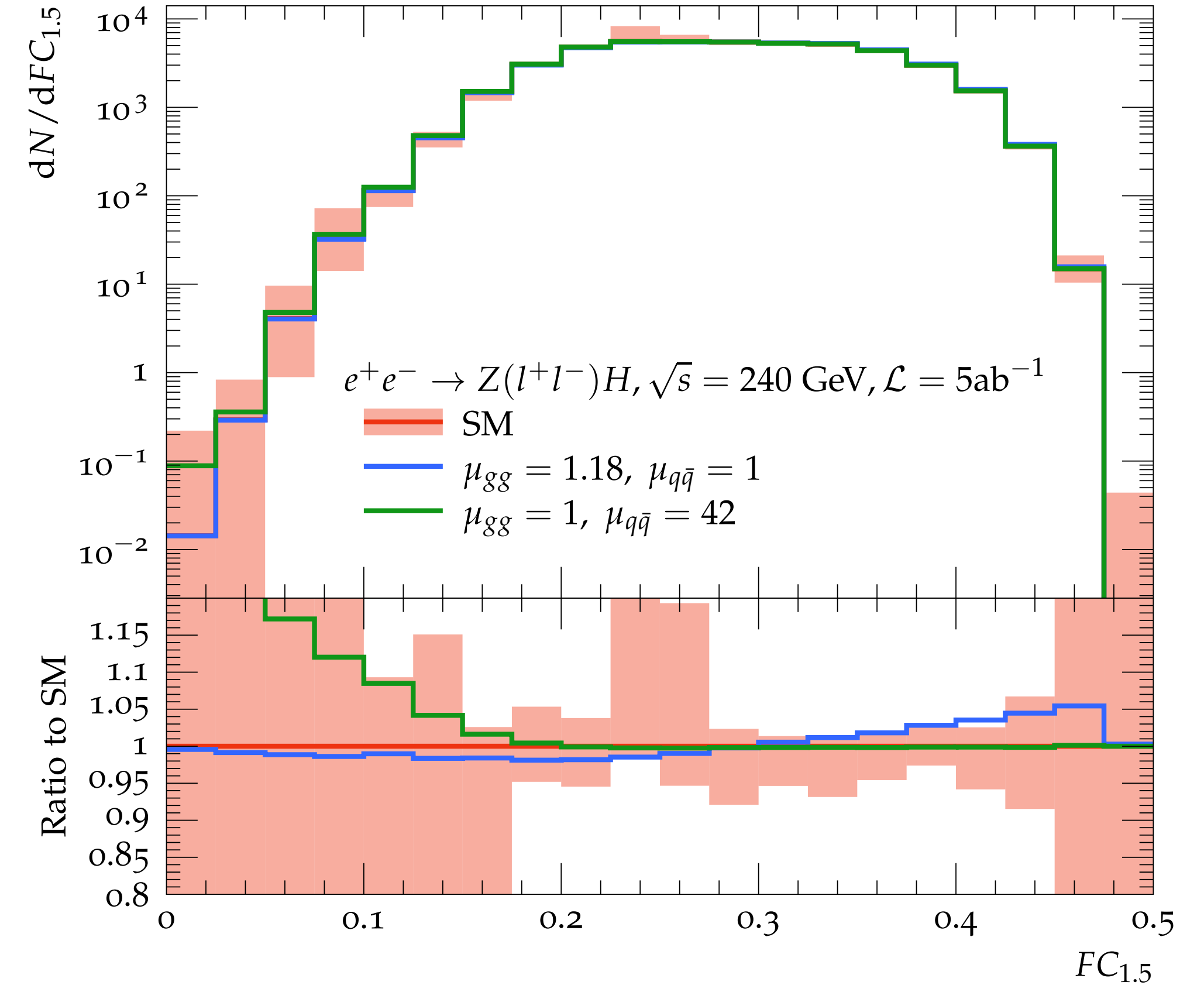
- overall distribution is sum over hadronic decay channels

$$\frac{d\sigma}{dv} = \sum_{i \in \{q\bar{q}, c\bar{c}, b\bar{b}, gg, WW, ZZ\}} \mu_i \frac{d\sigma_i}{dv} + \frac{d\sigma_{ZZ}}{dv}$$

- can determine relative contribution of each channel (here 2 parameters, $\mu_{gg}, \mu_{q\bar{q}}$)

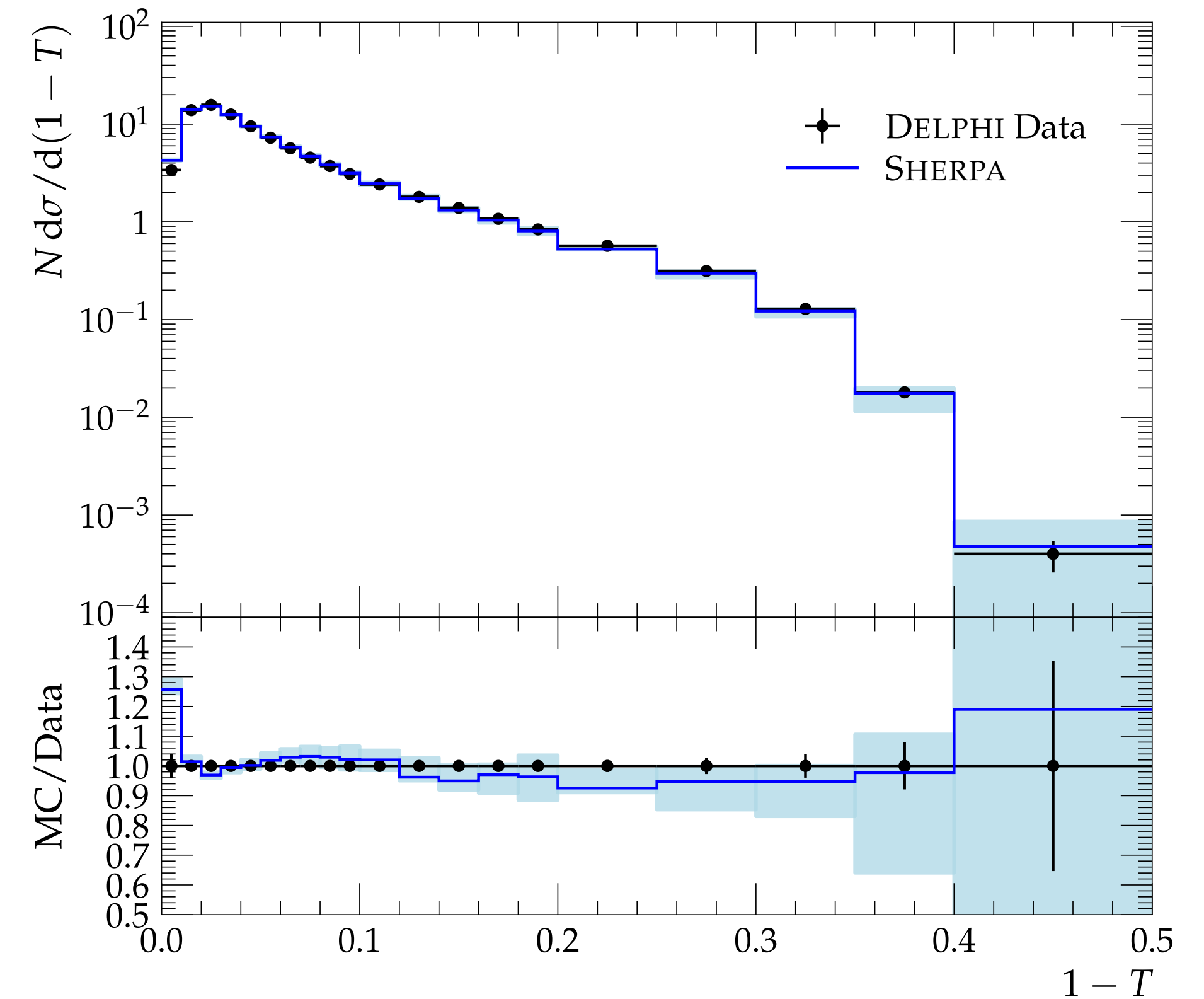
- boundary condition

$$\mu_{b\bar{b}} = 1 - (\mu_{gg} - 1) \frac{\sigma_{gg}}{\sigma_{b\bar{b}}} - (\mu_{q\bar{q}} - 1) \frac{\sigma_{q\bar{q}}}{\sigma_{b\bar{b}}}$$



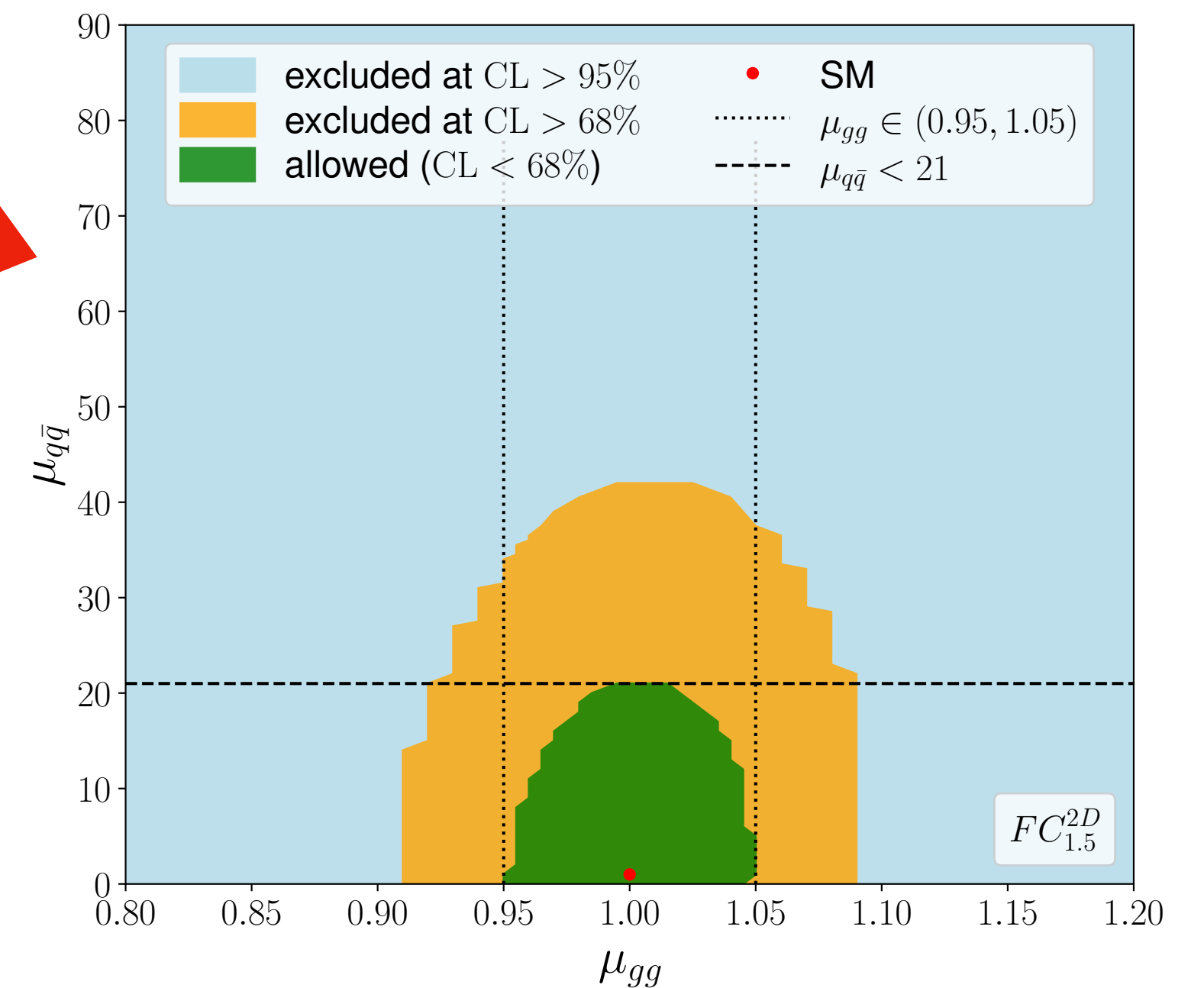
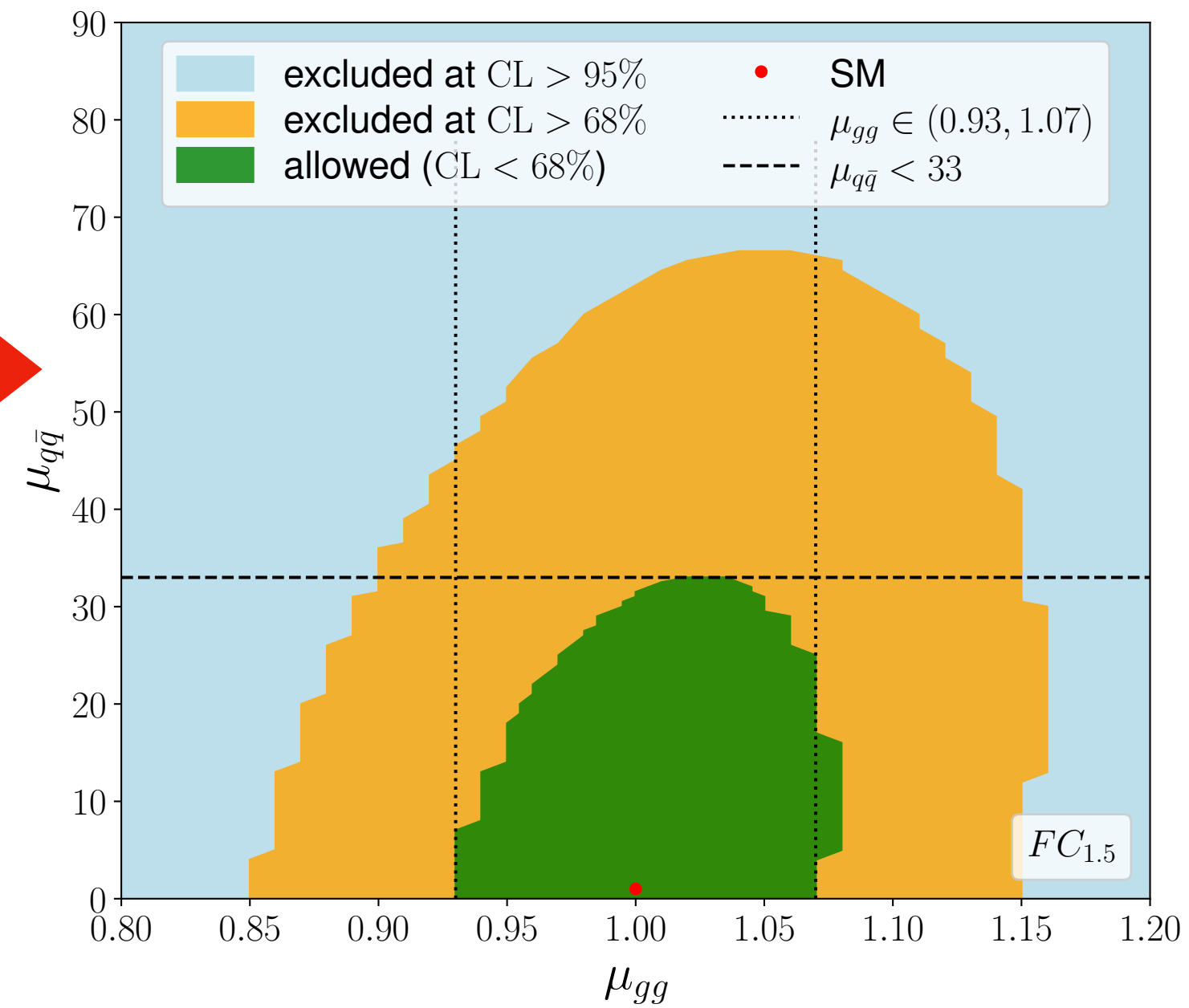
Study Setup

- run $e^+e^- \rightarrow HZ(\rightarrow l^+l^-)$ at $\sqrt{s} = 240$ GeV with Sherpa (3.0.alpha)
- assume luminosity of 5ab^{-1}
- follow cuts from [\[Azzi, Bernet, Botta, et. al. '12\]](#)
- fragmentation: tune to LEP data
- replica tunes: well defined variations of fragmentation parameters, allow systematic study of uncertainties



Results

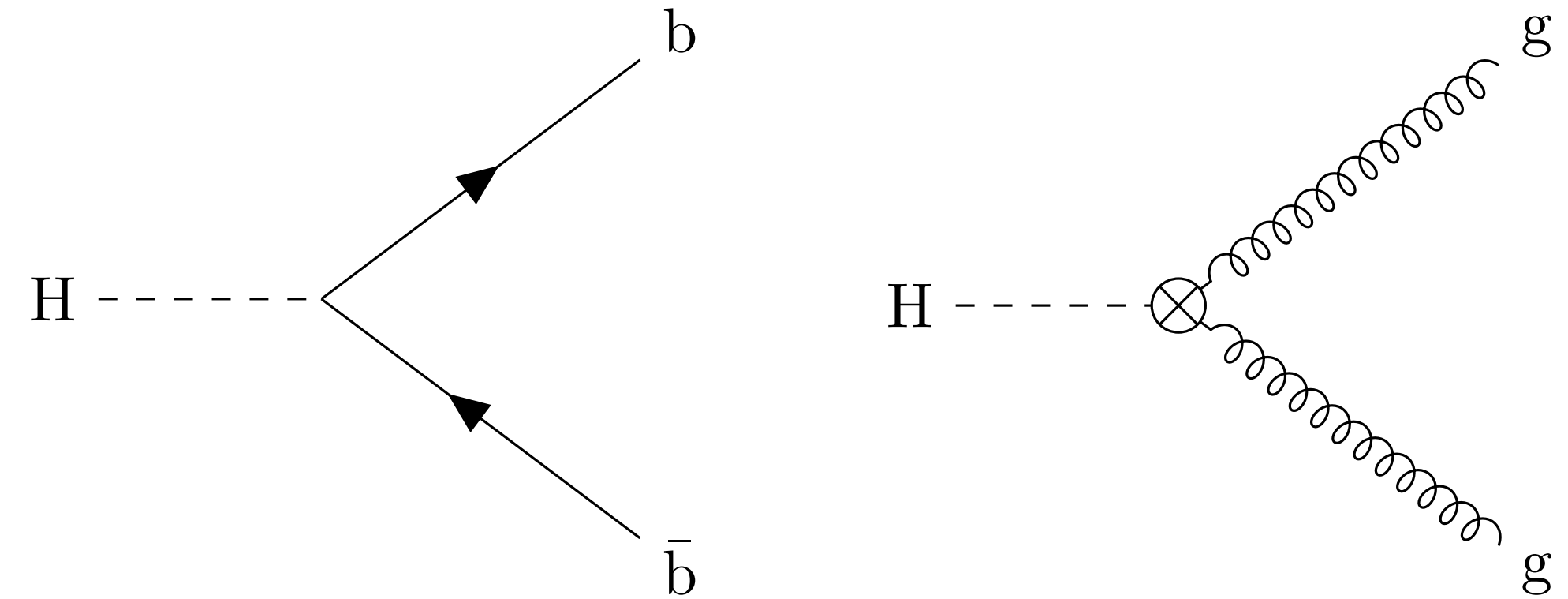
- generally best limit from $FC_{1.5}$ (higher weight on collinear emissions)
- slight improvement from taking into account correlated distribution in each jet
- limit of the same orders as tagging techniques, though not quite competitive (but provides independent methodology)



Part II - precision calculations for event shapes

Precision calculations - Fixed Order

- From [Coloretti, Gehrmann-de Ridder, Preuss '22]: two types of Higgs decays, to (massless) quarks and gluons via effective vertex, implemented in EERAD3



- produces coefficients A , B for IR safe event shape O :

$$\frac{1}{\Gamma^n(s, \mu_R)} \frac{d\Gamma(s, \mu_R, O)}{dO} = \frac{\Gamma^0(\mu_R)}{\Gamma^n(s, \mu_R)} \left(\frac{\alpha_s(\mu_R)}{2\pi} \right) \frac{dA(s)}{dO} + \frac{\Gamma^0(\mu_R)}{\Gamma^n(s, \mu_R)} \left(\frac{\alpha_s(\mu_R)}{2\pi} \right)^2 \frac{dB(s, \mu_R)}{dO}$$

- needs addition of all orders (resummed) calculation

Resummation - CAESAR in Sherpa

- CAESAR formalism for soft gluon resummation at NLL [Banfi, Salam, Zanderighi '04]
- available as implementation in Sherpa [Gerwick, Höche, Marzani, Schumann '15]
[Baberuxki, Preuss, DR, Schumann '19]
- multiplicative matching (\Rightarrow NLL' accurate)
- necessary extensions for jet observables... :
 - modified wide angle behaviour [Dasgupta, Khelifa-Kerfa, Marzani, Spannowski '12]
[Caletti, Fedkevych, Marzani, DR, Schumann, Soyez, Theeuwes '21]
[DR, Caletti, Fedkevych, Marzani, Schumann, Soyez '22]
 - non-global logs [Dasgupta, Salam '01]
- ... and for soft drop grooming [Larkoski, Marzani, Soyez, Thaler '14]
- CEASAR style formulas available [Baron, DR, Schumann, Schwanemann, Theeuwes '20]

Precision Calculations - Resummation with CAESAR

- master formula for rIRC safe observable: [Banfi, Salam, Zanderighi '04]

$$\Sigma_{\text{res}}^{\delta}(v) = \int d\mathcal{B}_{\delta} \frac{d\sigma_{\delta}}{d\mathcal{B}_{\delta}} \exp \left[- \sum_{l \in \delta} R_l^{\mathcal{B}_{\delta}}(L) \right] \mathcal{P}^{\mathcal{B}_{\delta}}(L) \mathcal{S}^{\mathcal{B}_{\delta}}(L) \mathcal{F}^{\mathcal{B}_{\delta}}(L) \mathcal{H}^{\delta}(\mathcal{B}_{\delta})$$

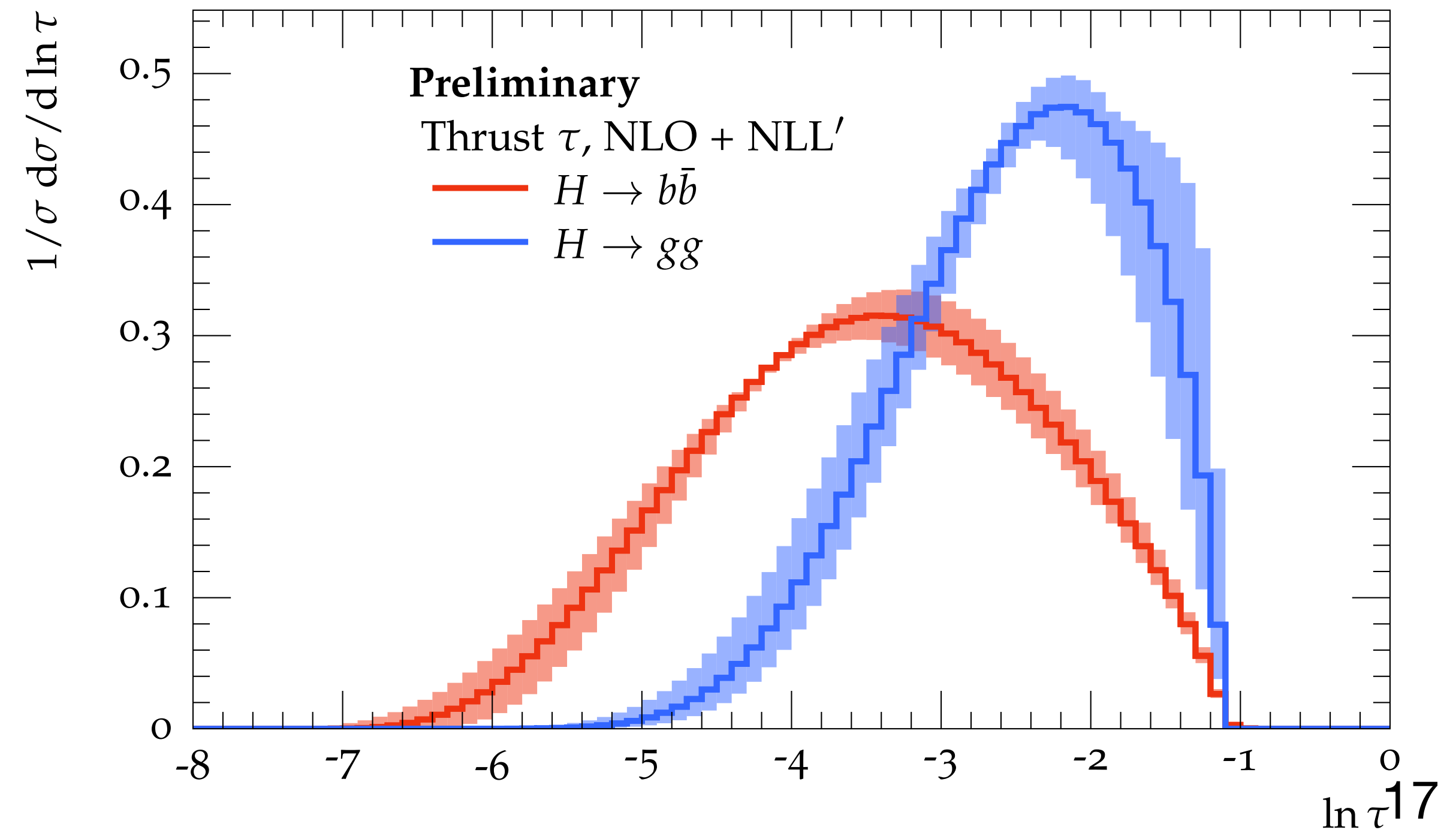
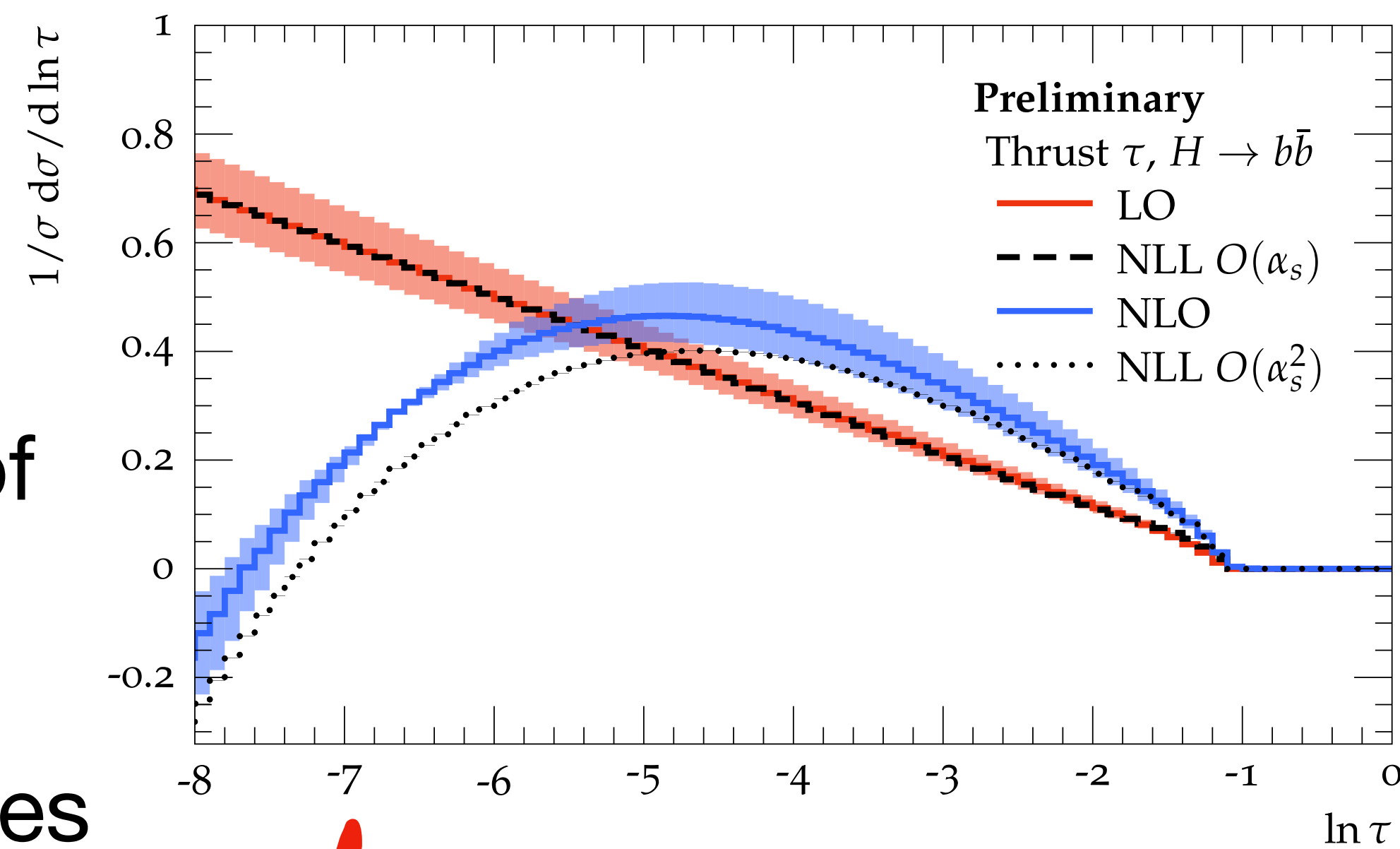
- ingredients known analytically in our cases

- matching:
$$\Sigma_{\text{matched}} = \Sigma_{\text{res}} \left(1 + \frac{\Sigma_{\text{fo}}^{(1)} - \Sigma_{\text{res}}^{(1)}}{\sigma^{(0)}} + \frac{\Sigma_{\text{fo}}^{(2)} - \Sigma_{\text{res}}^{(2)}}{\sigma^{(0)}} - \frac{\Sigma_{\text{res}}^{(1)}}{\sigma^{(0)}} \frac{\Sigma_{\text{fo}}^{(1)} - \Sigma_{\text{res}}^{(1)}}{\sigma^{(0)}} \right)$$

- here for the first time, handle external (to Sherpa) fixed order calculation, given in terms of A, B distributions for matching

First Results

- calculation in rest frame of decaying Higgs boson
- confirm expansion captures logarithms up to NLL
- prepare matched predictions
- confirm general behaviour of MC simulation



Summary

- Event shapes as theoretically well controllable taggers
 - applicable to hadronic Higgs decays
 - enables measurement with minimal (possibly without) modelling input
 - strongest limits for $FC_{1.5}$ observable, in particular 2D version
- accompanied by precision calculation of event shapes
 - NLO+NLL' almost trivially available
 - NNLO+NNLL \rightarrow probably all ingredients known, need to be put together