

# Measuring mass of long-lived particles with inner detector timing

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# Introduction

In e+e- collider with CMS energy  $E_{CM}$  produce long-lived neutral H recoiling against particle of known mass M  
H decays at distance  $d_H$  from the interaction point, with a delay from the time of the interaction  $t_H$ .

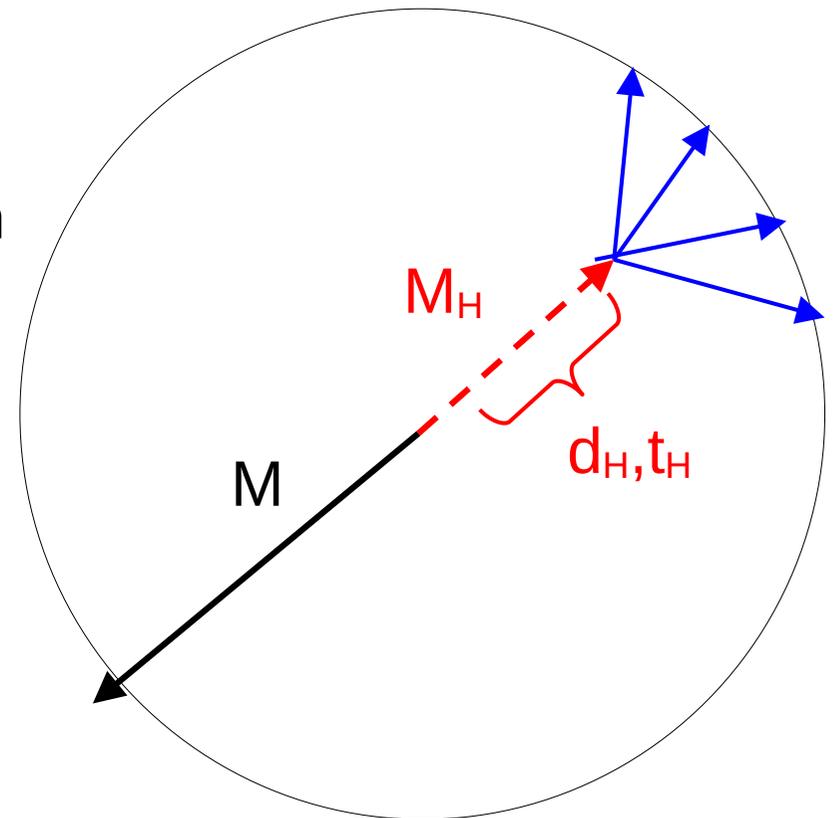
$$p_H = \frac{\sqrt{(E_{CM}^2 - (M_H + M)^2)(E_{CM}^2 - (M_H - M)^2)}}{2E_{CM}}$$

$$p_H = M_H \gamma \beta$$

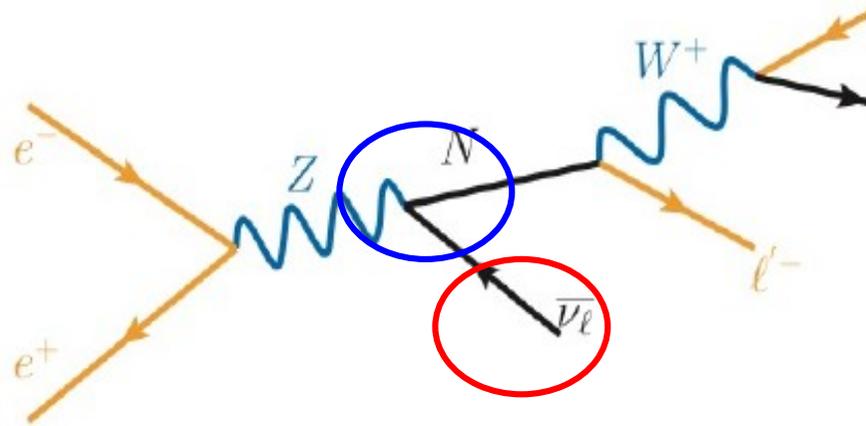
$$\beta = d_H / t_H / c,$$

Solve for  $M_H$ ,  $\rightarrow M_H = f(E_{CM}, M, \beta)$ , all known or measurable quantities.

What precision on  $M_H$  in plausible BSM model for realistic FCC-ee detector?



# Example: HNL decay in IDEA



Mass of recoiling particle=0  $\rightarrow$  no uncertainty

Interaction point undetected  $\rightarrow$  uncertainty on time and position of interaction

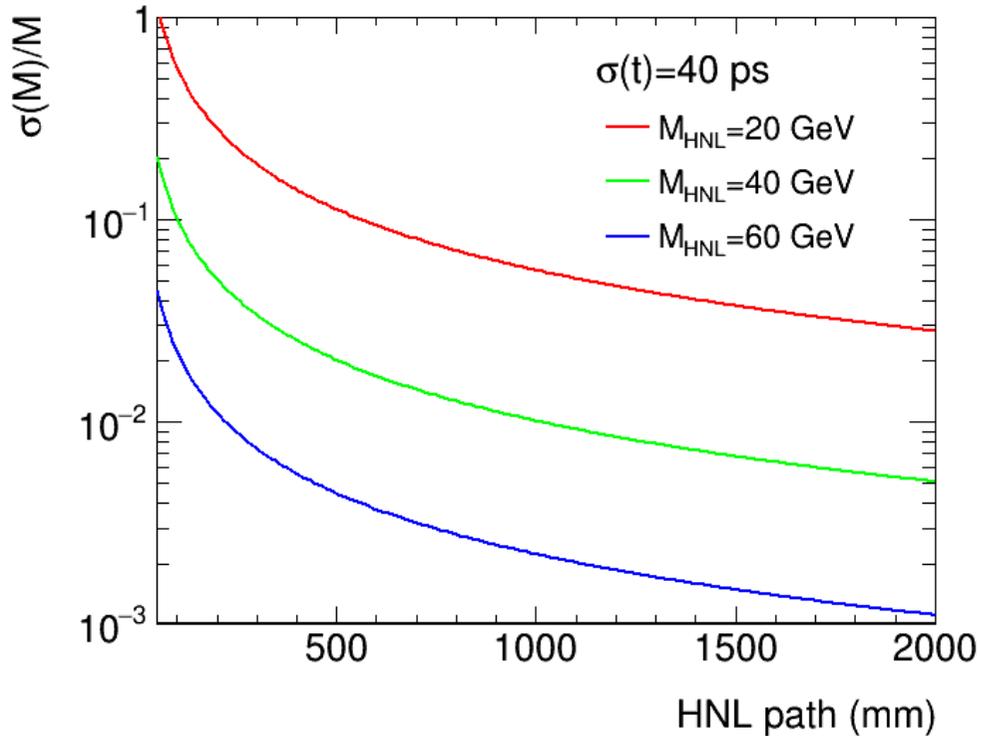
$$m_H = E_{CM} \sqrt{\frac{1-\beta}{1+\beta}} \equiv E_{CM} F(\beta)$$

$$\sigma(M_H) = E_{CM} \frac{1}{\sqrt{\frac{1-\beta}{1+\beta}} (1+\beta)^2} \sigma(\beta) \equiv E_{CM} F'(\beta) \sigma(\beta)$$

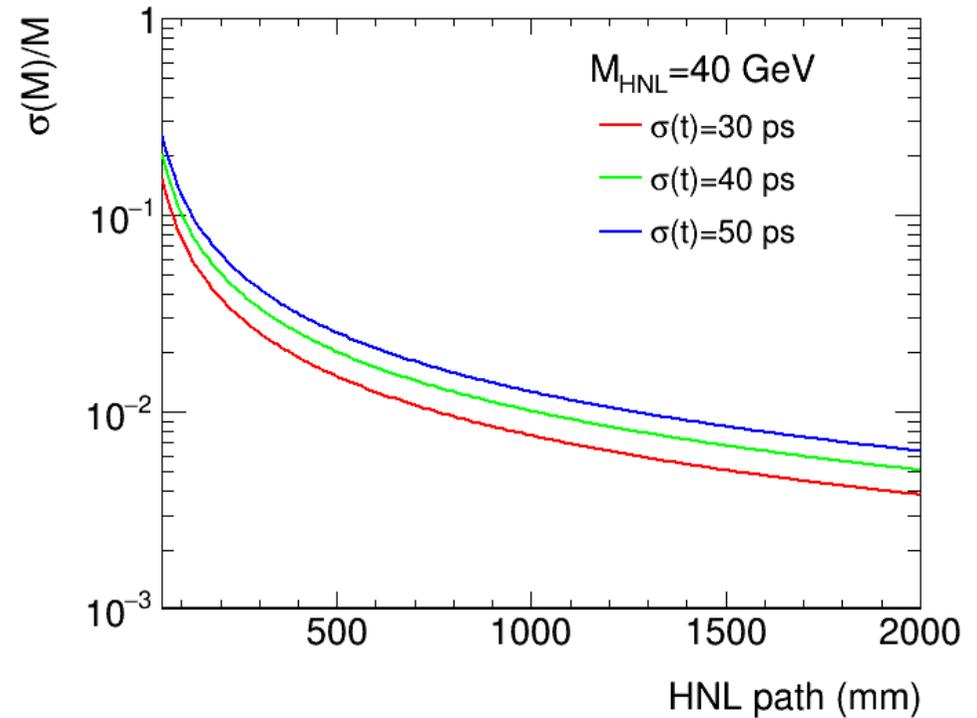
# Analytic formulas

Assuming  $\sigma(t)$  dominant

$$\sigma(M_H) = \frac{E_{CM} \beta^2 F'(\beta) c \sigma(t)}{d_H}$$

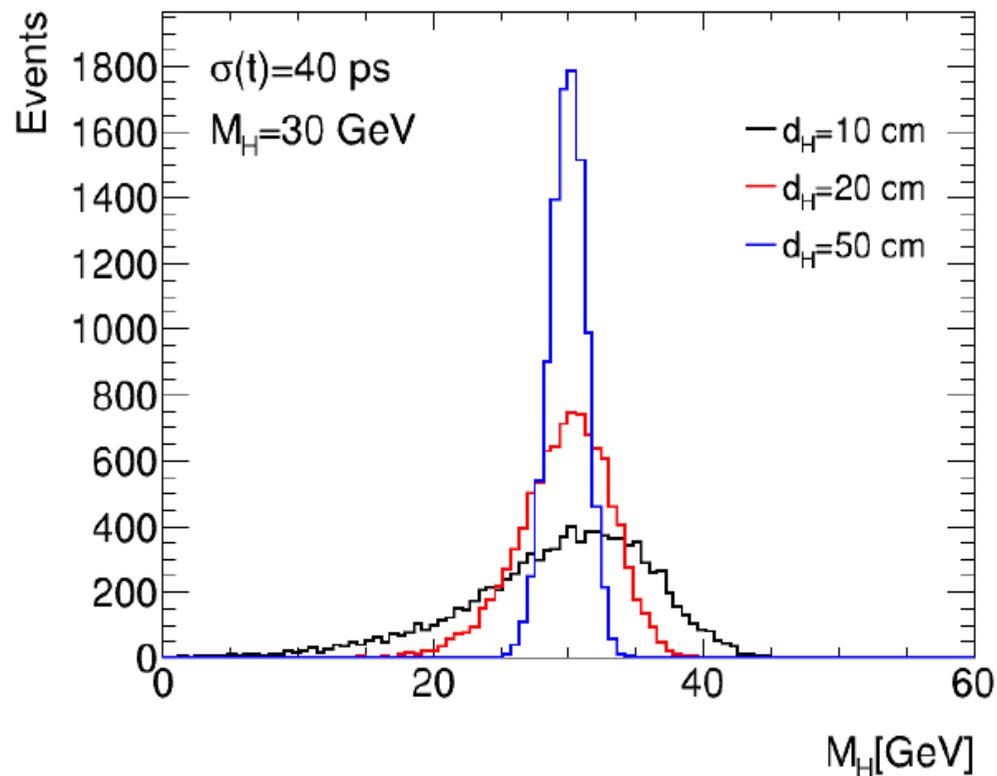


Strong dependence on mass  
 For high masses one can get below percent level

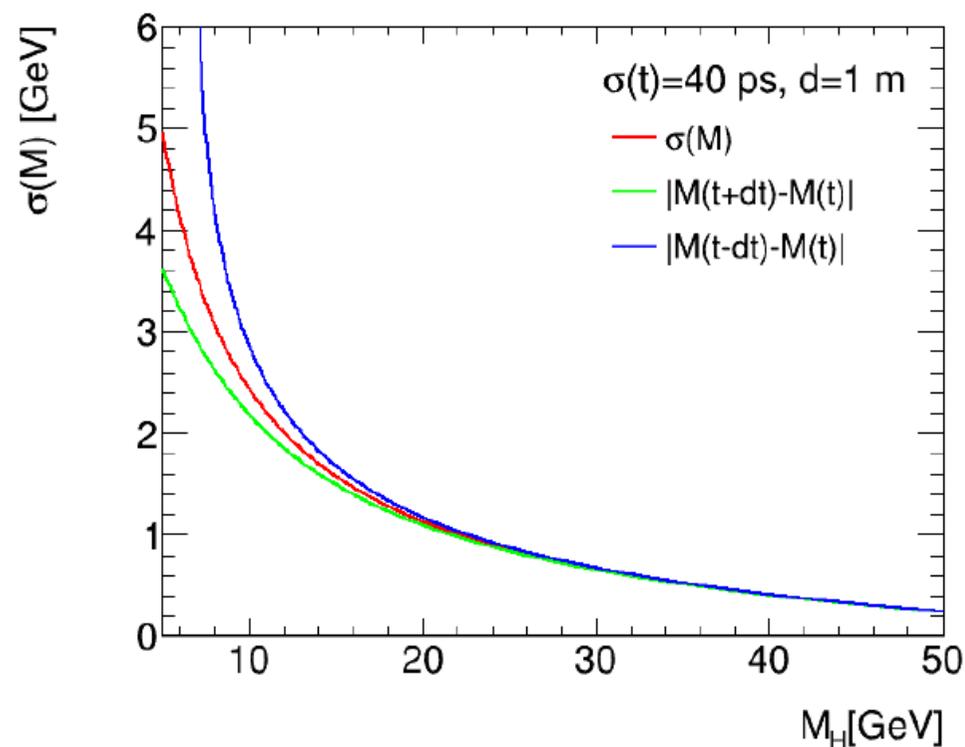


$M=40$  Gev:  
 Few tens of ps timing resolution:  
 mass resolution below 1% for a path  
 between 50 cm and 1 m

# Shape of mass resolution



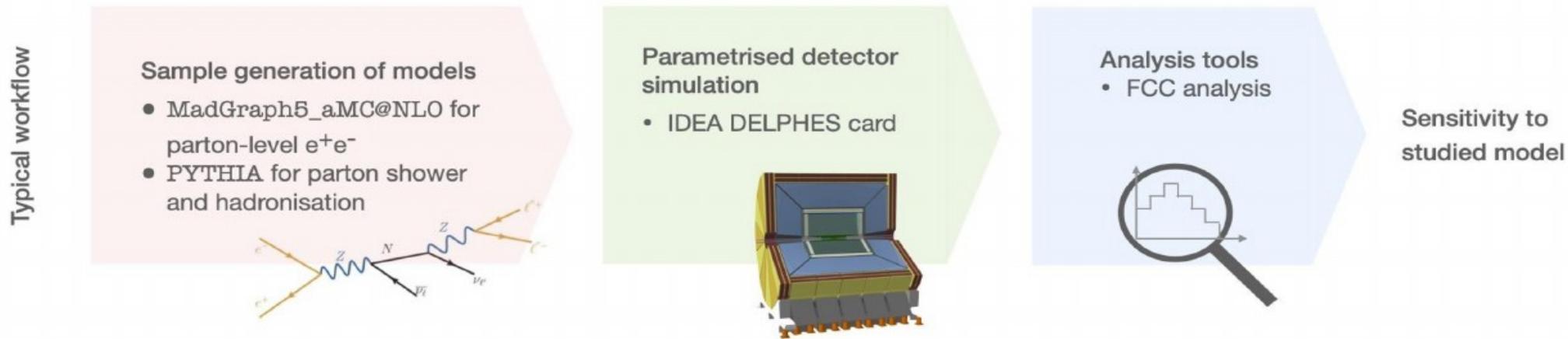
For short decay path  
large low mass tail



For low masses  $\beta$  approaches 1  
and low part tail of resolution explodes

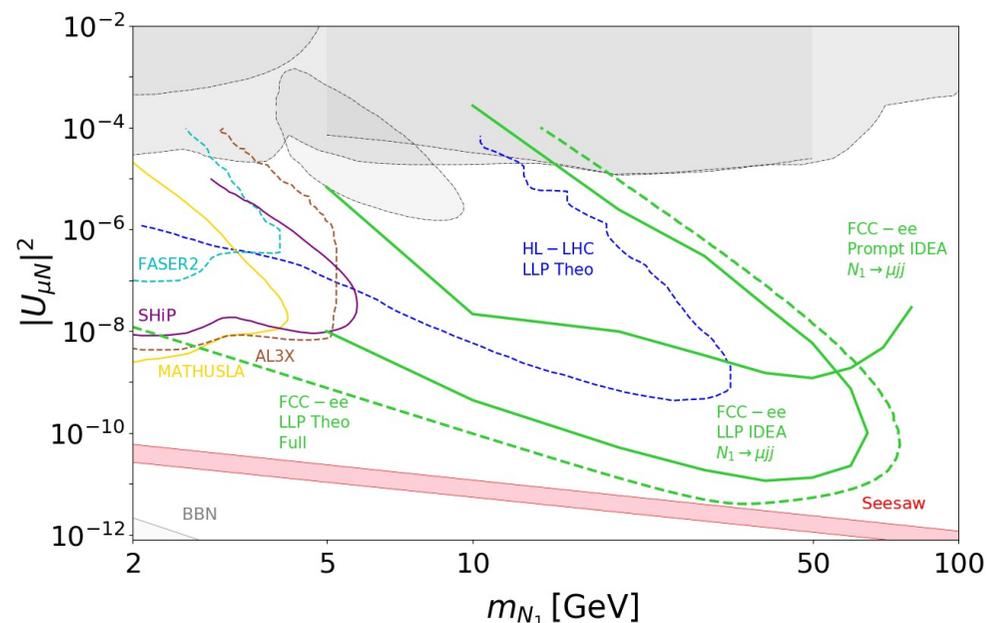
Promising results → go for detailed analysis on simulated samples

# Realistic exercise



Samples used for study of reach of  $HNL \rightarrow \mu jj$  search at the Z pole (see talk by N. Valle)

- Generate grid in  $(U, m)$  space with MG5aMC@NLO
- DELPHES with IDEA card
- Detailed parametrisation of IDEA tracking performance and well developed vertexing code used for the analysis



# Measurement of $t_H$

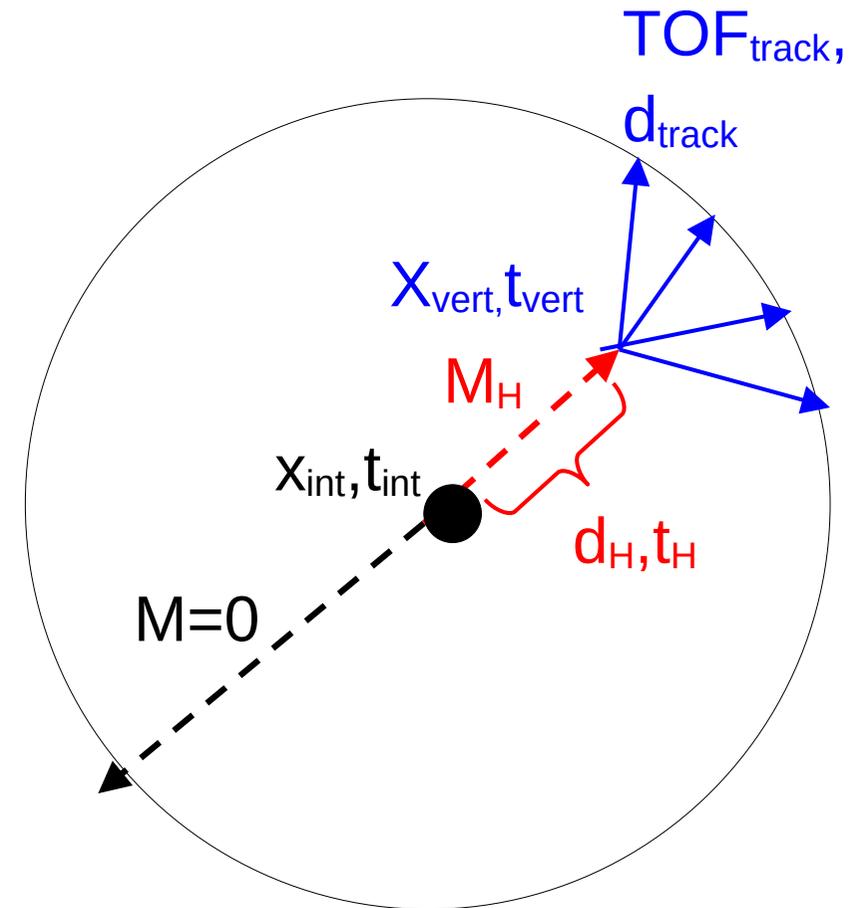
Assume timing layer just outside of tracker  
(Radius=2m)

Two invisible particles in primary interaction:  
time and position of interaction

$(x_{int}, t_{int})$  unknown

Distribution known from beam parameters

Ebeam (GeV)	45.6
$\sigma_x$ ( $\mu\text{m}$ )	8.4
$\sigma_y$ (nm)	33.7
$\sigma_z$ (mm)	15.4
Vertex $\sigma_x$ ( $\mu\text{m}$ )	5.96
Vertex $\sigma_y$ (nm)	23.8
Vertex $\sigma_z$ (mm)	0.397
Vertex $\sigma_t$ (ps)	36.3

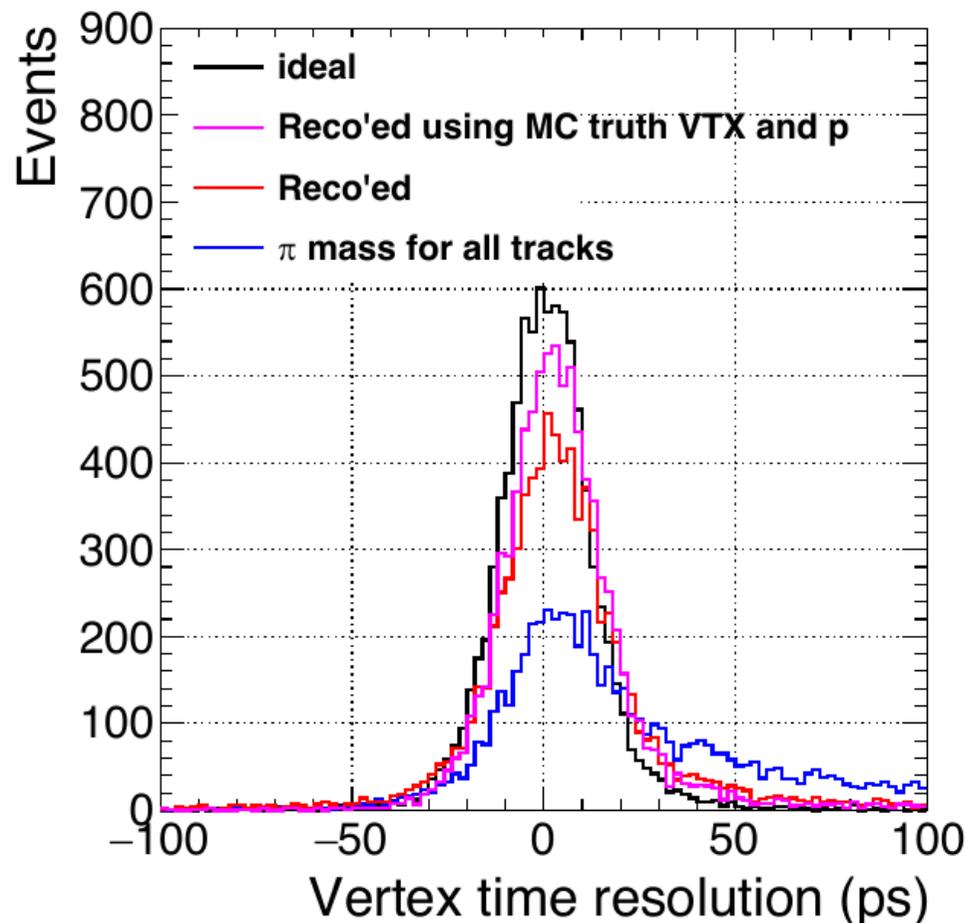


## Time of decay vertex:

- Measure TOF wrt nominal interaction time for each decay track
- For each track, momentum and distance between decay vertex and timing layer measured
- If mass of particle known  $t_{vert}$  can be measured

# Timing resolution on vertex

40 GeV HNL with  $c\tau = 1\text{m}$   
Resolution timing layer 30 ps  
Prim. vtx algo in FCCsw. Require  
 $\chi^2_{\text{vert}} \neq 0$  &  $\chi^2_{\text{vert}} < 10$



To calculate  $t_{\text{vert}}$  for each track need mass of particle. In principle gain of factor  $1/\sqrt{N}$  on resolution, with  $N$ =number tracks from vtx

Two possibilities:

- One of the tracks is a muon: use muon, mass fixed, but only one track
- Apply iterative algorithm on all non-muon tracks starting from pion hypothesis, and modifying id hypothesis for track with worst compatibility with average

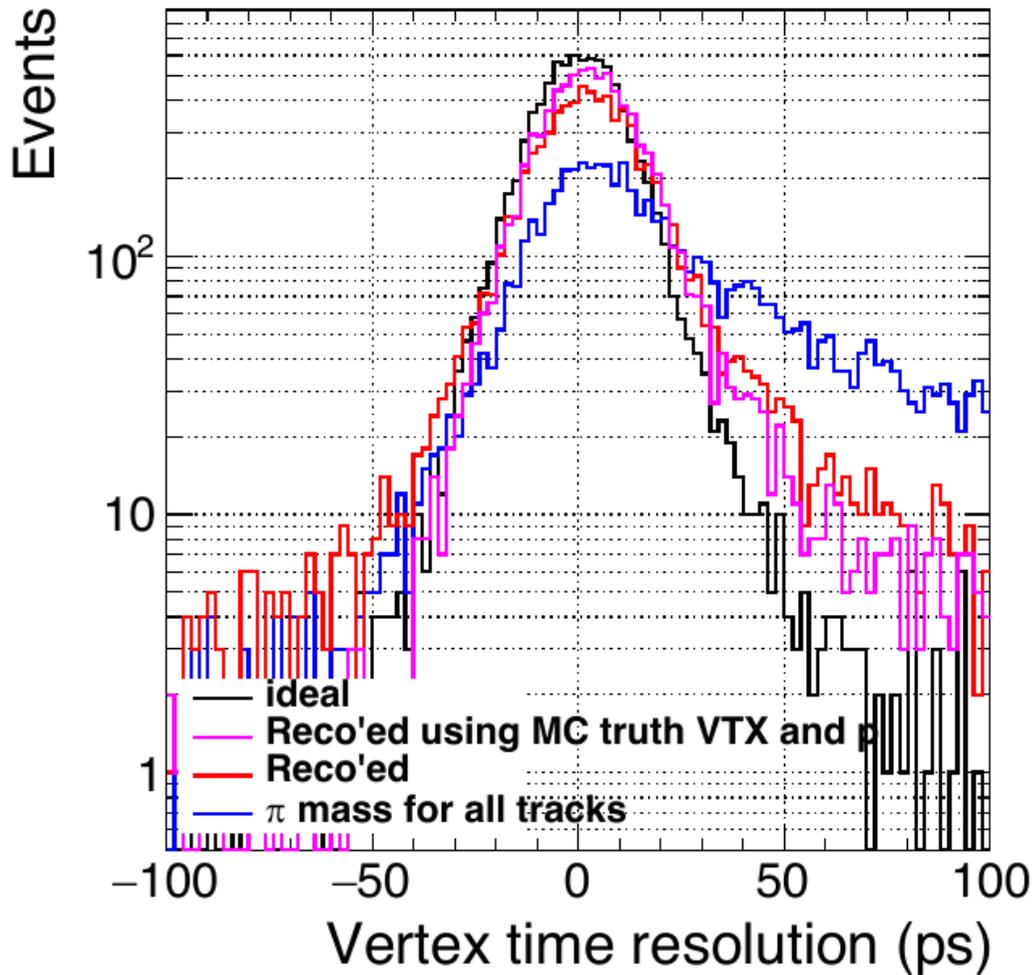
Ideal case gaussian with  $\sigma(t) \sim 30 \text{ ps}/\sqrt{N}$

If all tracks assumed  $\pi$ , large tails

Iterative algo yields reasonable result

Peak narrower if truth momentum and vtx position assumed

# Timing resolution on vertex



Timing layer resolution 30 ps.  
Distributions not fully gaussian,  
evaluate resolution as minimum interval  
including 68% of events

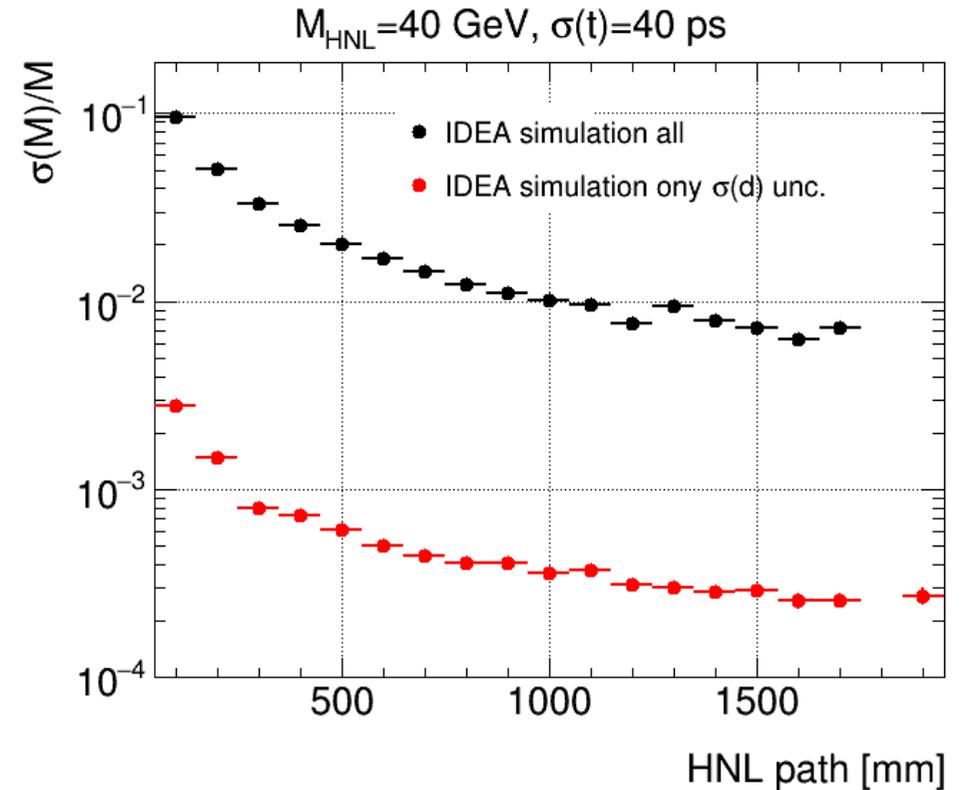
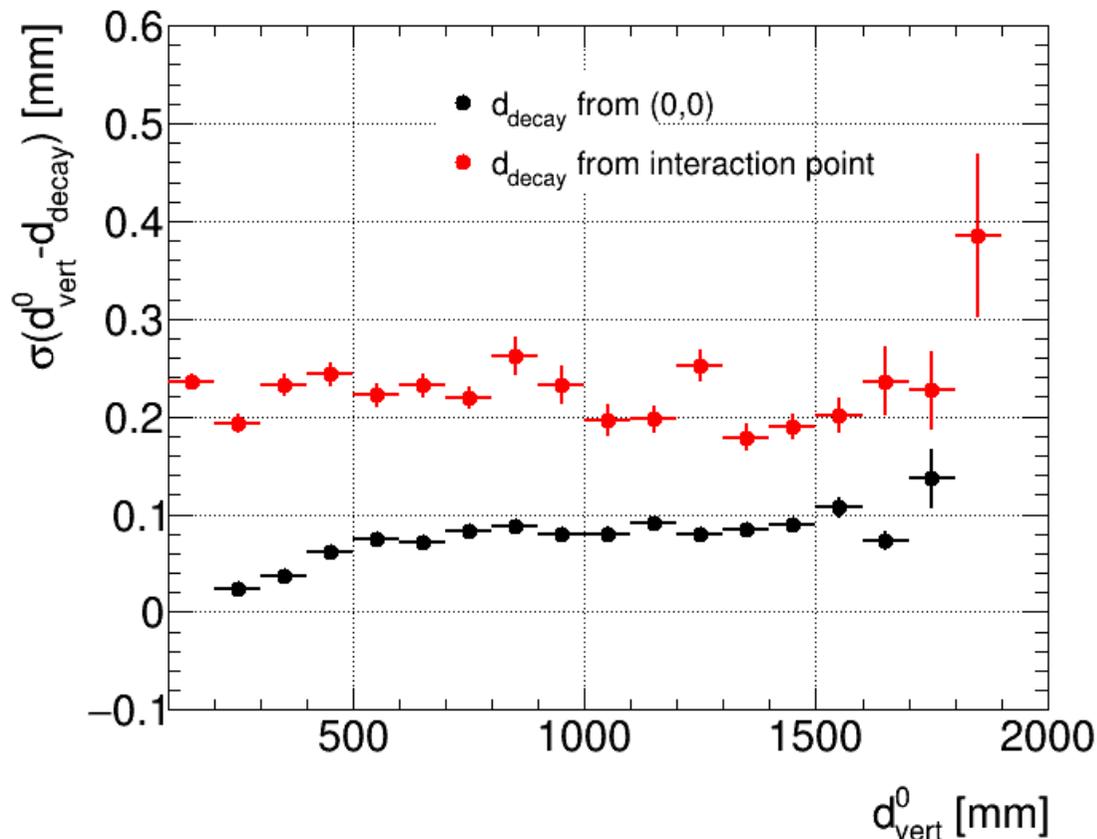
Ideal	12.6 ps
Pion masses	106 ps
Reco'ed	22.8 ps
Reco'ed with MC vtx & p	15 ps

# Impact of position uncertainty of decay vertex

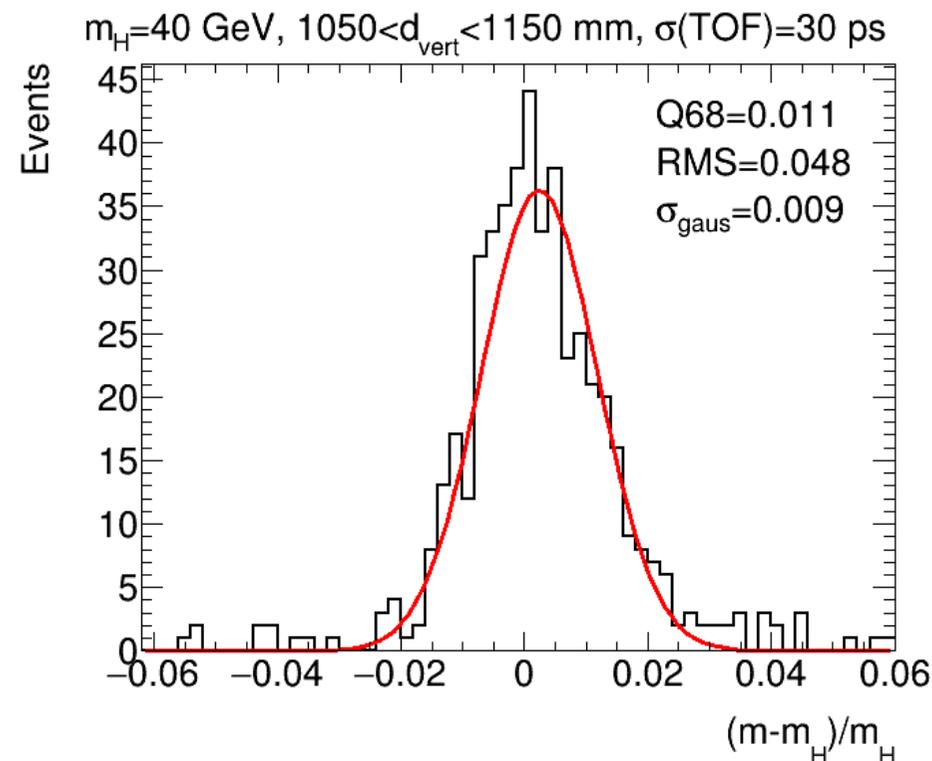
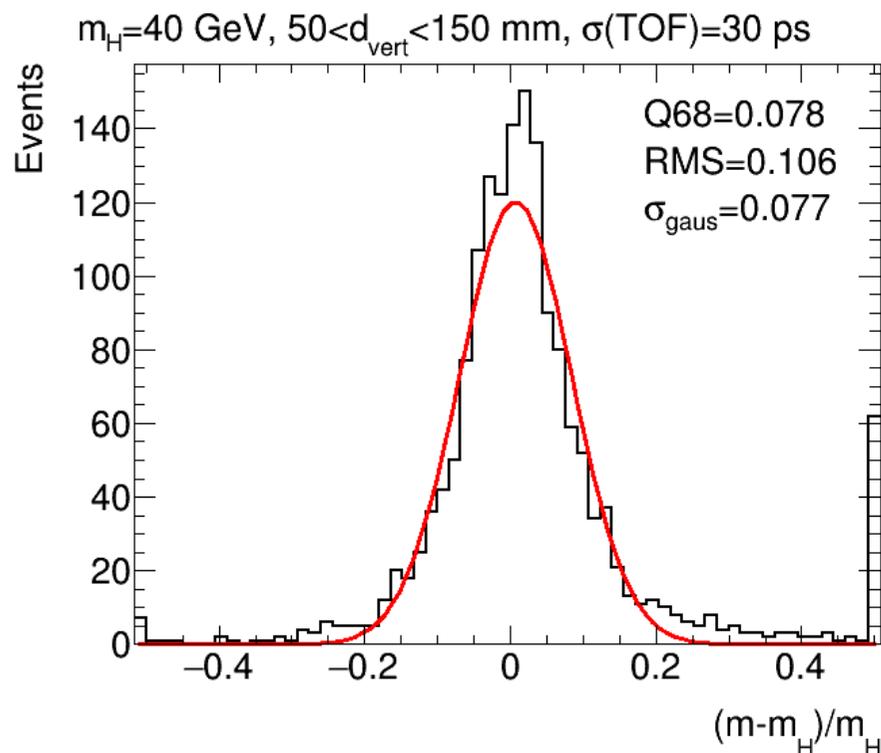
Two components

- Unknown position of interaction vertex
- Uncertainty on vertex reconstruction

$$\beta = d_H / t_H / c,$$

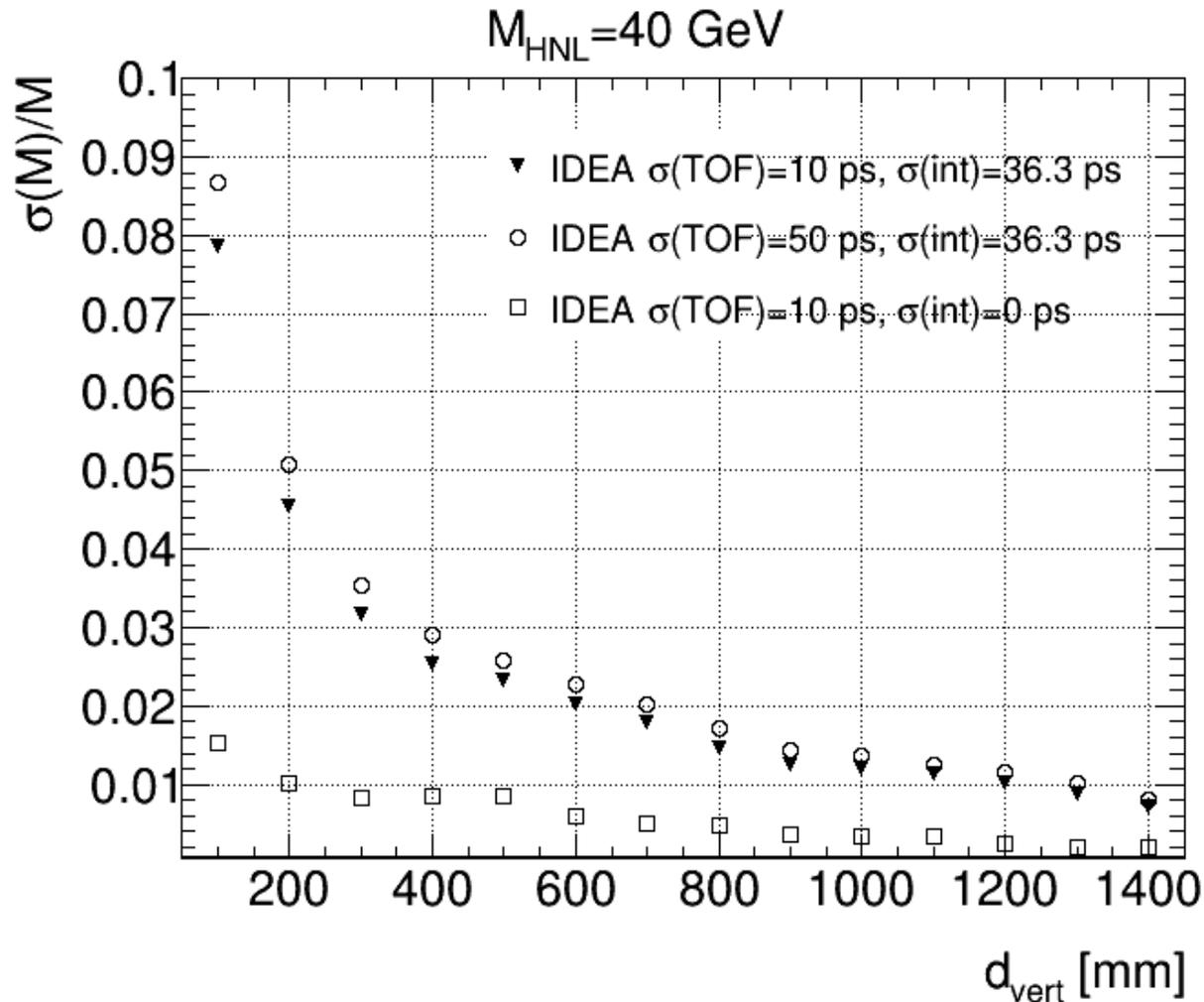


# Measured mass distributions



Based on algorithm for  $t_{\text{vert}}$ , measure mass event-by-event for  $M_H=40$  GeV  
Show result for two bins in measured vertex position  
Distributions mediocrelly fitted by gaussian, with tails on both sides  
Use as resolution value:  $Q68=(\text{Quantile}(0.84)-\text{Quantile}(0.16))/2$

# Path dependence of mass resolution



Mild dependence on TOF resolution because of large uncertainty on time of primary interaction

Use Q68 as estimator of resolution

with  $\sigma(\text{TOF})=50 \text{ ps}$  obtain resolution of order 5% for  $d_{\text{vert}} > 15 \text{ cm}$

comparable to expected PFA measurement from cristal+DR calo

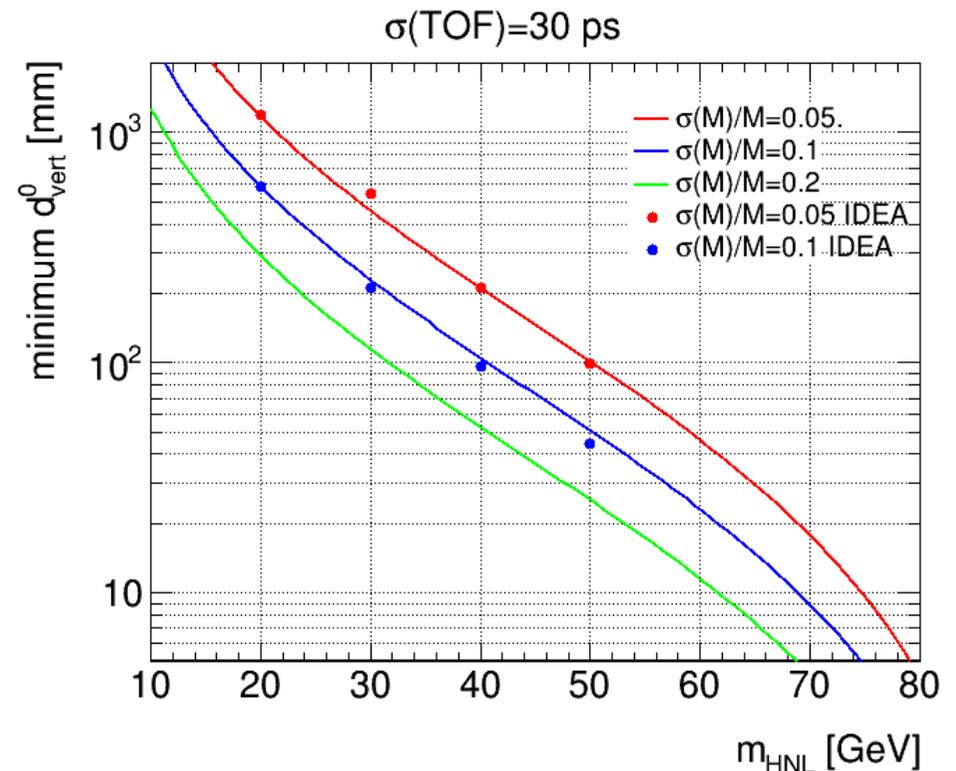
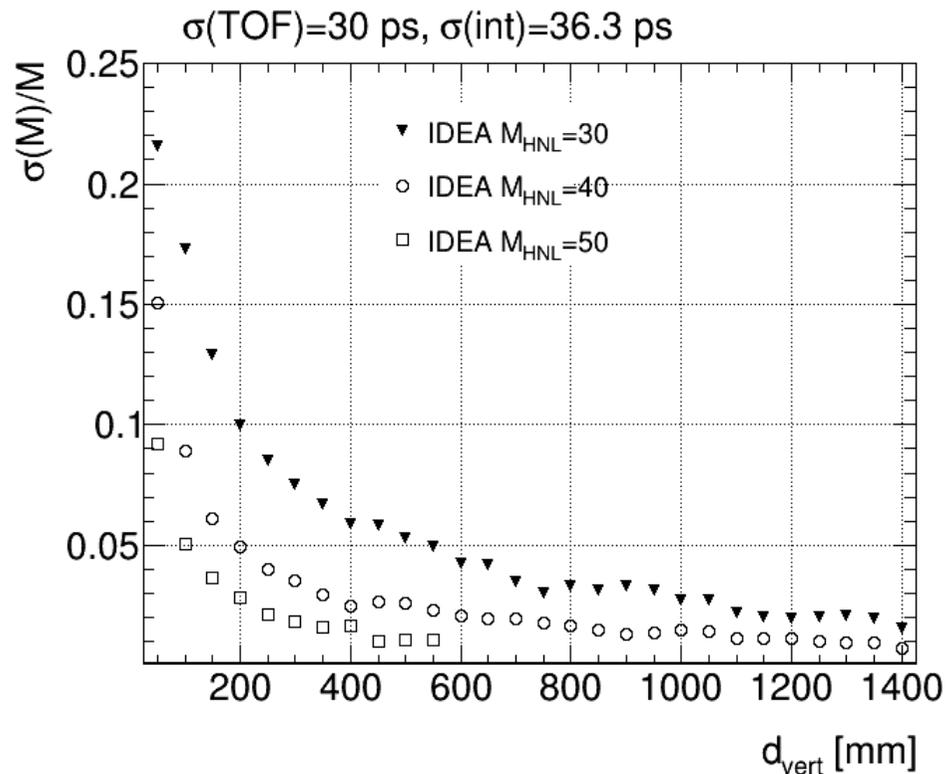
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# Minimum decay length yielding fixed $\sigma(M)/M$

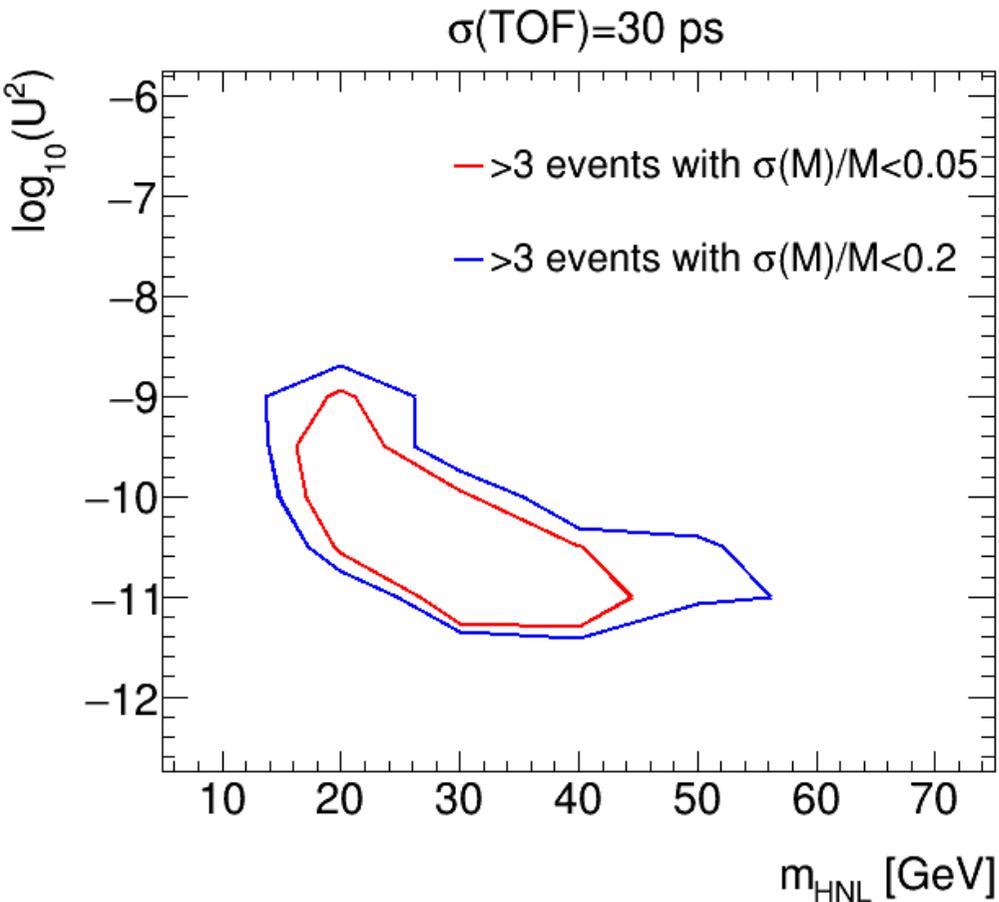
$$\sigma(M_H) = \frac{E_{CM} \beta^2 F'(\beta) c \sigma(t)}{d_H}$$

Can be inverted to evaluate the minimum path yielding a desired mass resolution



Use these values to apply lower limit on position of primary vertex to estimate number of well-measured surviving events

# Parameter space coverage



Require:  $\chi^2$  of primary vertex  $< 10$ ,  
at least 4 tracks in event.

Zero background events for  $d_{\text{vert}} > 50 \text{ mm}$ .

Some mild kinematic cuts for masses  
for which minimum  $d_{\text{vert}} < 50 \text{ mm}$

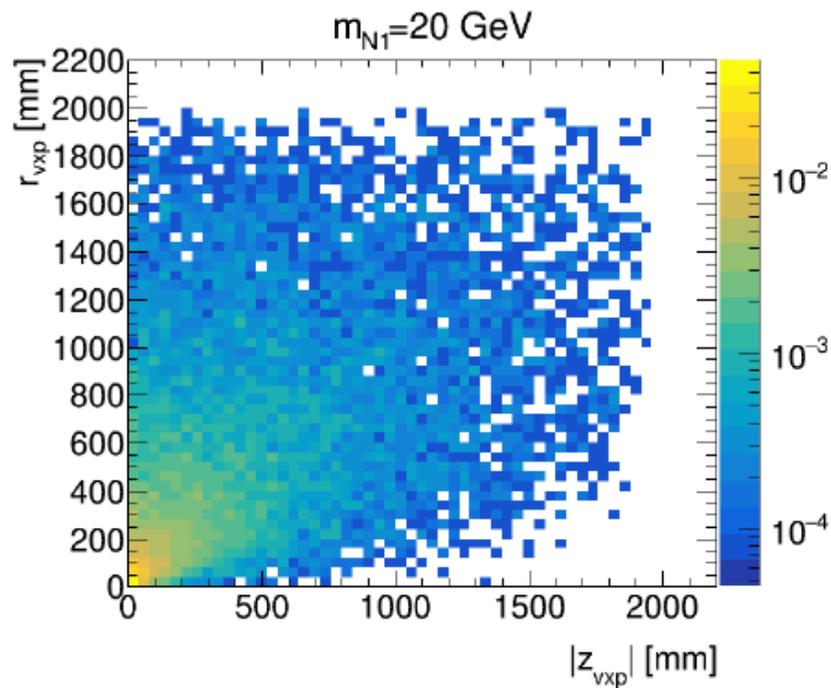
In significant fraction of parameter space  
obtain useful mass measurement  
from timing

# Conclusions

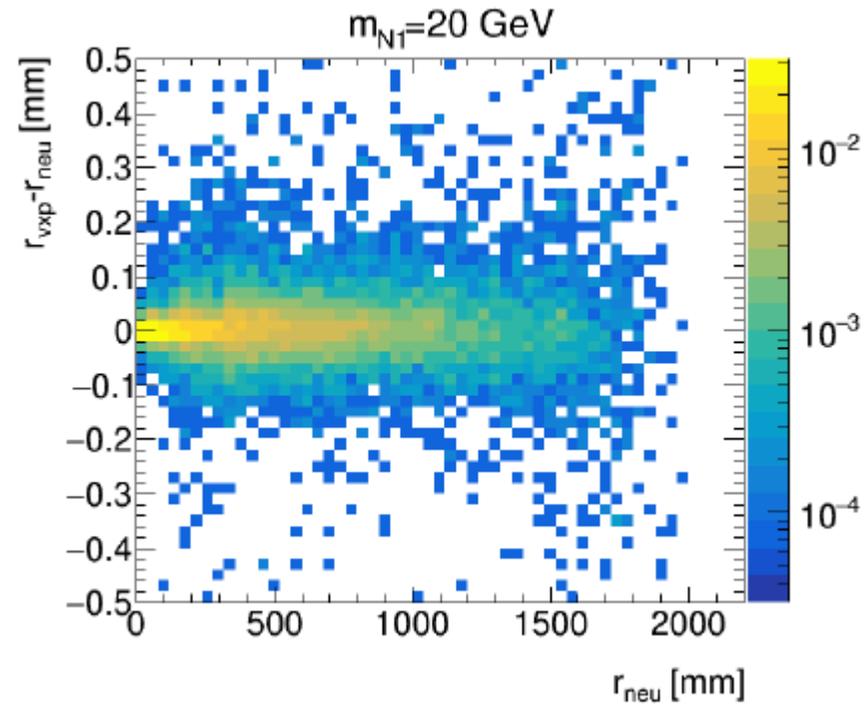
- Detection of decay products of long-lived particles (LLP) may allow measurement of LLP mass based on recoil formula and accurate measurement of position and timing of decay vertex
- Benchmarked on HNL production with  $\text{HNL} \rightarrow \mu jj$
- For a timing layer with  $\sigma(t)$  a few tens of ps, mass resolution at percent level for long enough path and high enough mass
- Timing resolution dominated by unknown time of primary vertex
- Developed algorithm to precisely measure timing of decay vertex based on parametrised simulation of IDEA tracker
- Useful measurement of HNL mass from timing over large part of accessible HNL parameter space

# Backup

# Prompt vs Long Lived selection



Primary vertex well reconstructed  
in the volume of the detector



Very good resolution in position  
of HNL reconstructed vertex

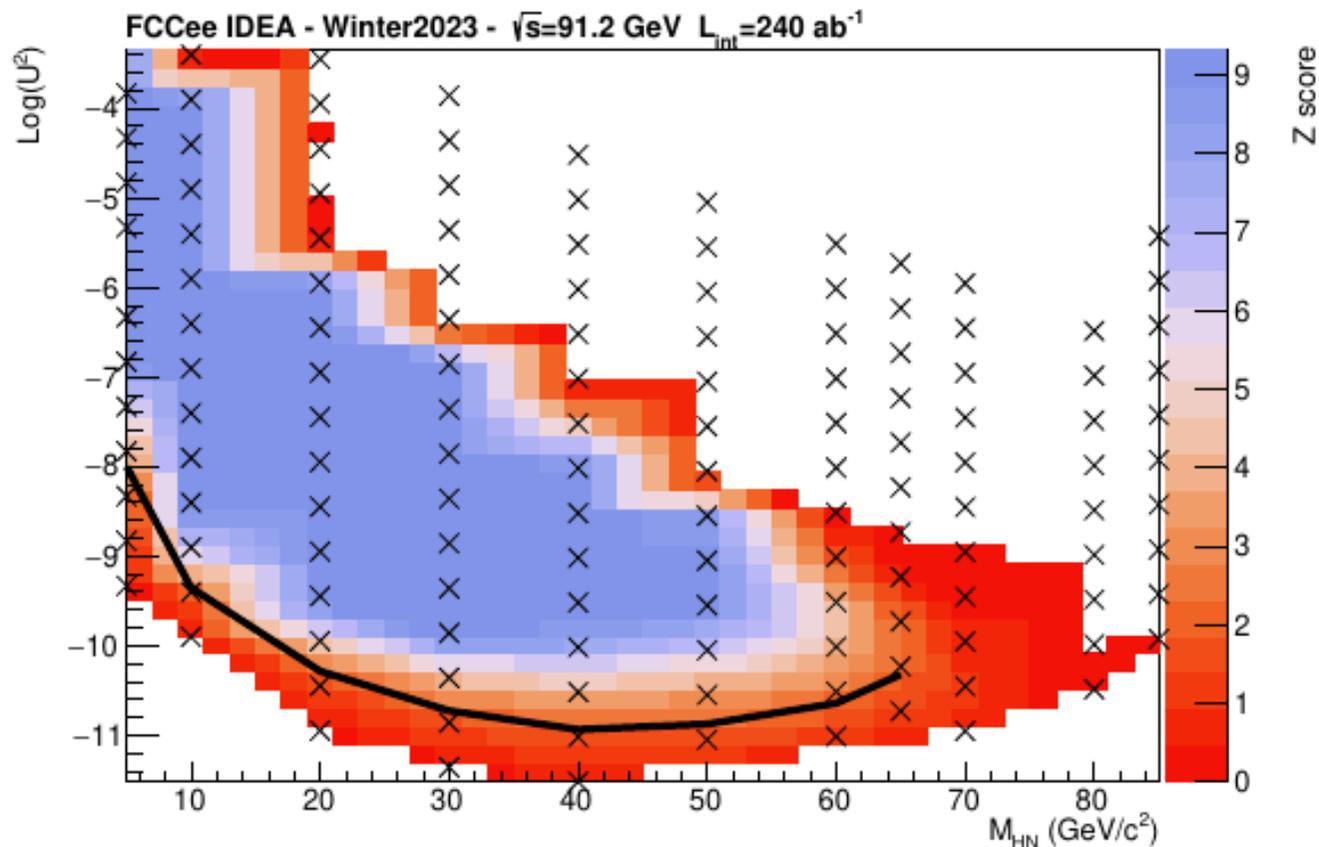
Separation between Prompt and Long Lived to some extent arbitrary, choose transverse position of primary vertex such that backgrounds become zero:

$$r_{vxp} = 0.5 \text{ mm}$$

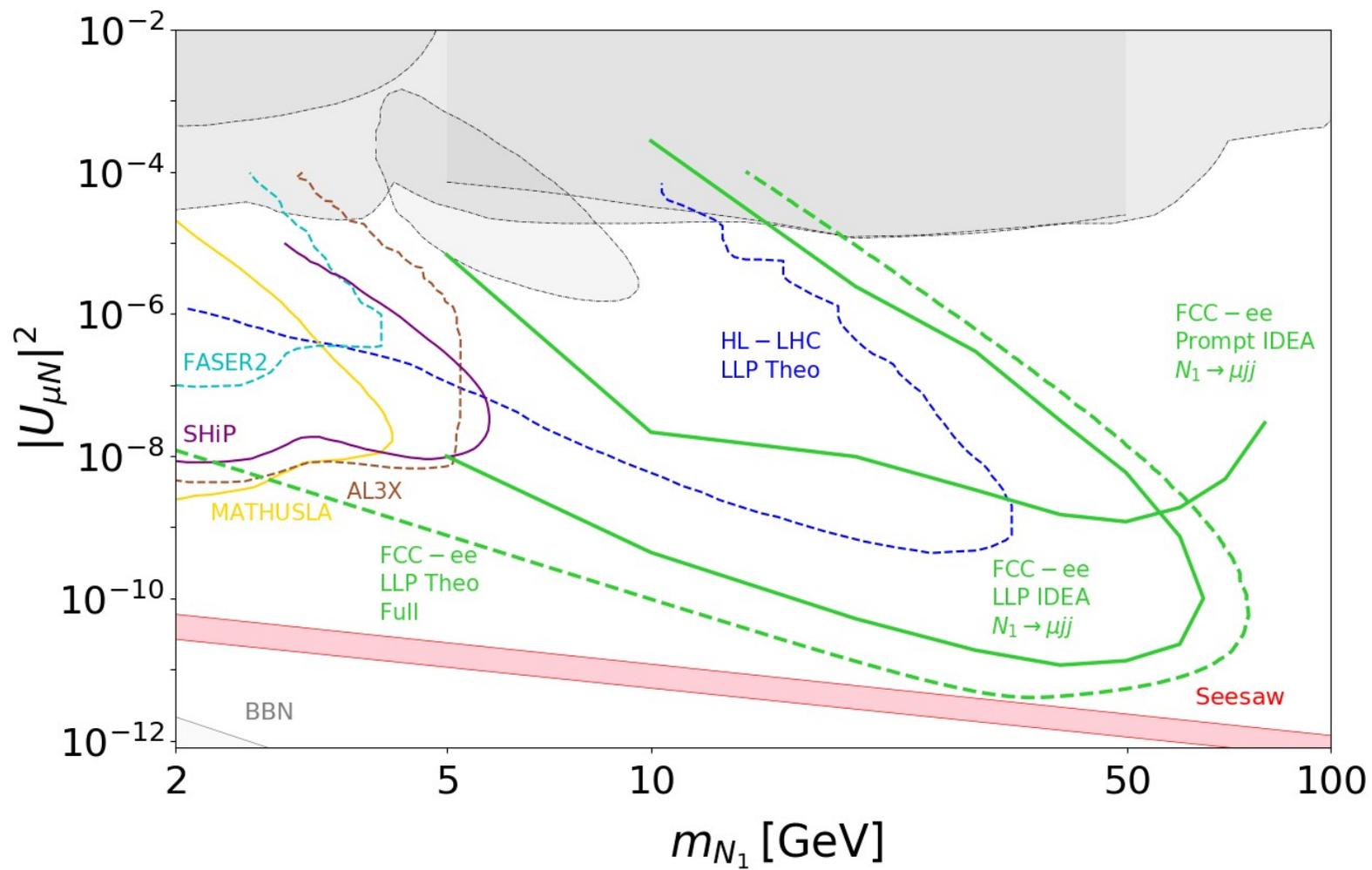
About five times values  $r_{vxp}$  for extreme tails of backgrounds

# LLP results

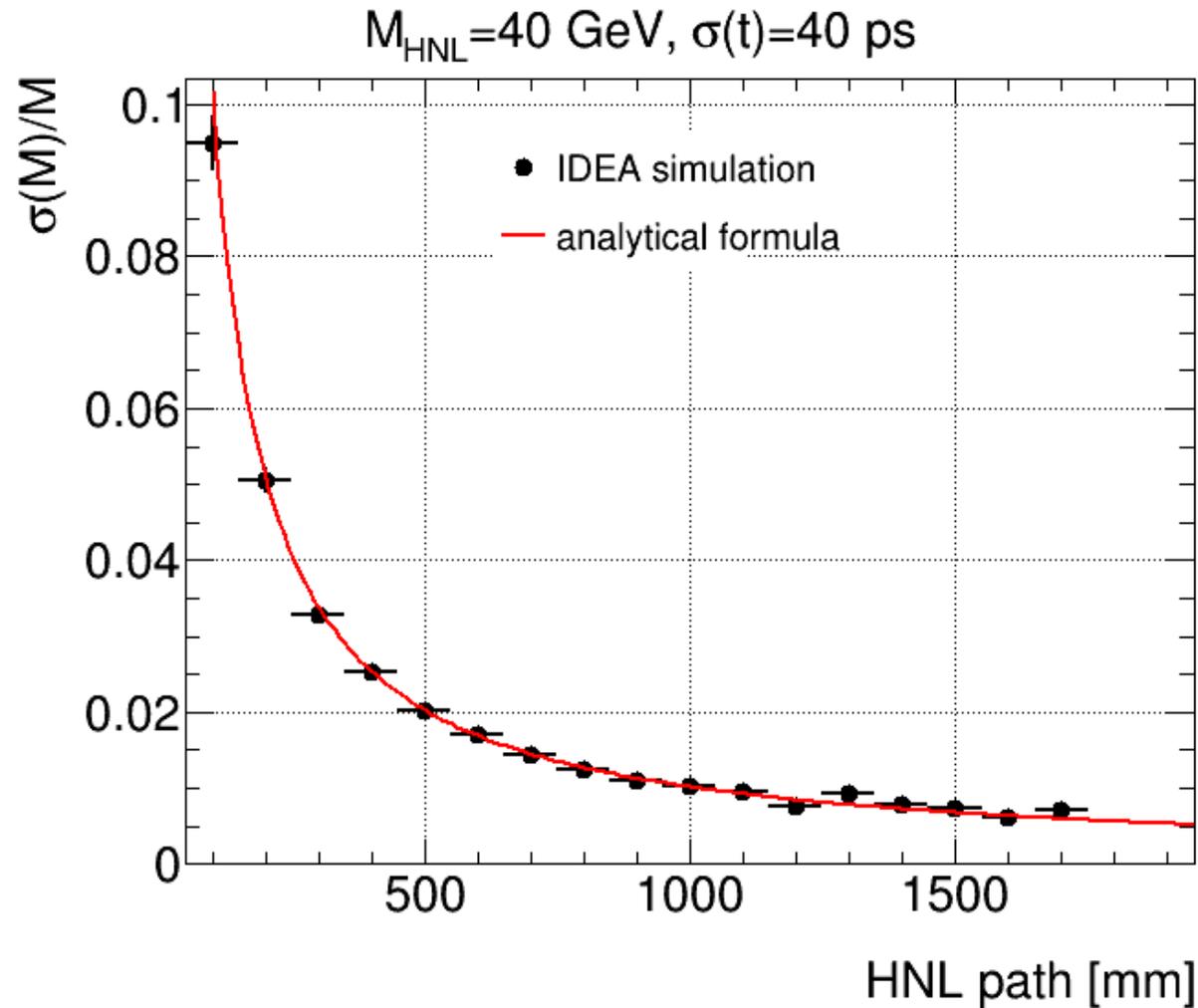
Backgrounds=0: sensitivity curve defined as points in parameter space where 3 events are expected after cuts



# Final result



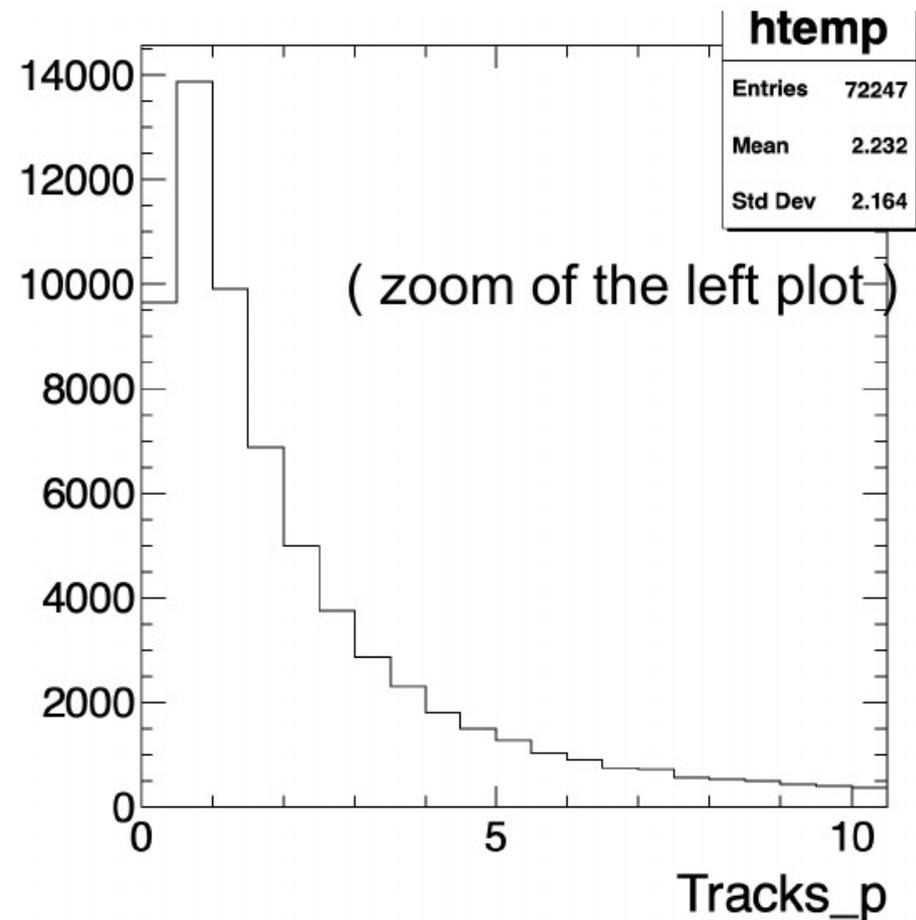
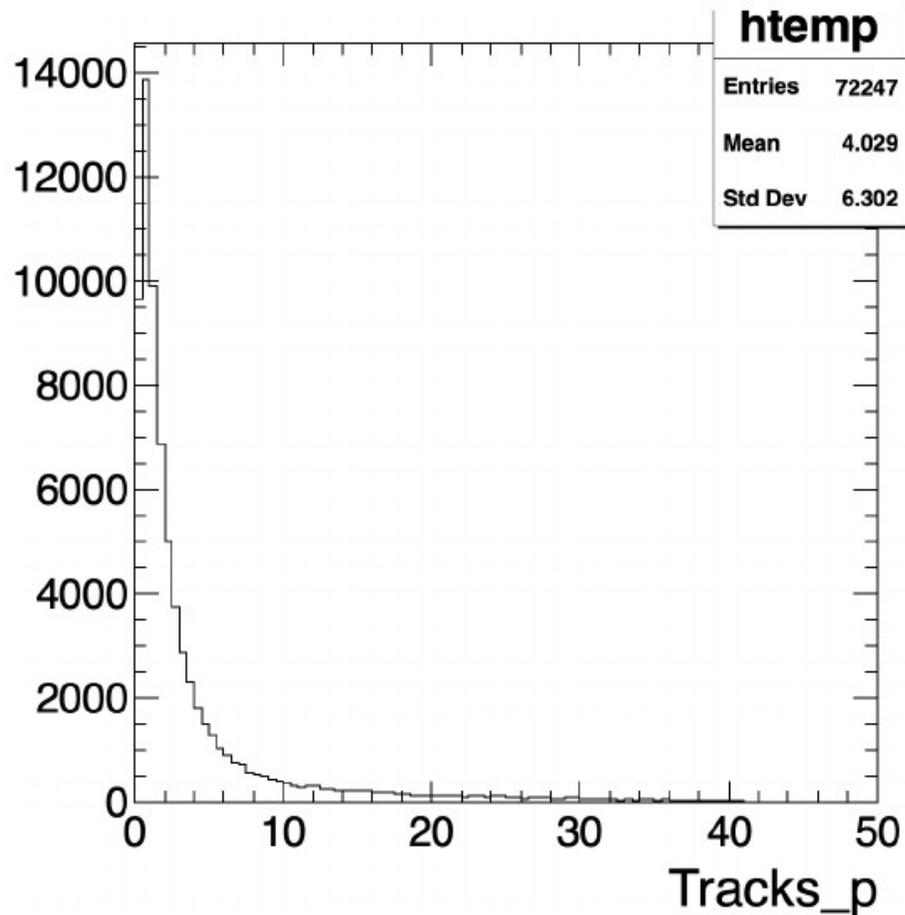
# Analytic formulas vs. simulation



Consider decay  
 $\text{HNL} \rightarrow \mu j$

Compare analytic formulas to DELPHES simulation of IDEA detector with detailed parametrisation of the performance of the tracker

# Possible gain from dE/dx PID



Momentum of the tracks: peak at  $\sim 1$  GeV where  $dN/dx$  is blind.  
But average  $\sim 4$  GeV, so some improvement expected although the resolution is expected to be  $\sim \sqrt{2}$  worse than for prompt tracks.