

(Update on) Higgs self-coupling determination at the FCC-hh

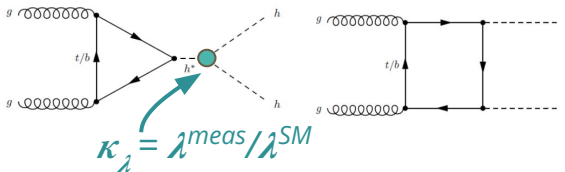
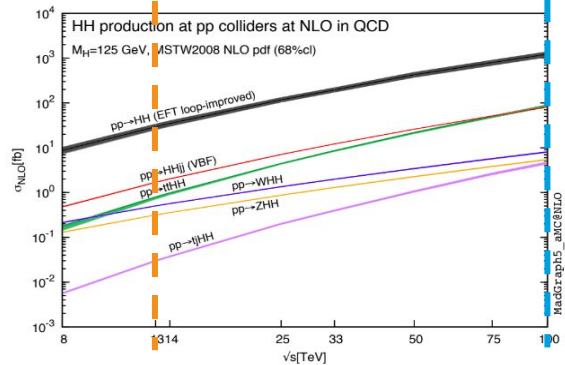
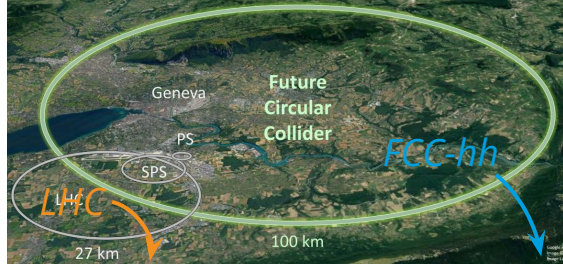
Angela Taliercio, Birgit Stapf

Elisabetta Gallo, Kerstin Tackmann, Paola Mastrapasqua, Michele Selvaggi,
Christophe Grojean

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Higgs self-coupling @ FCC-hh: What & why?

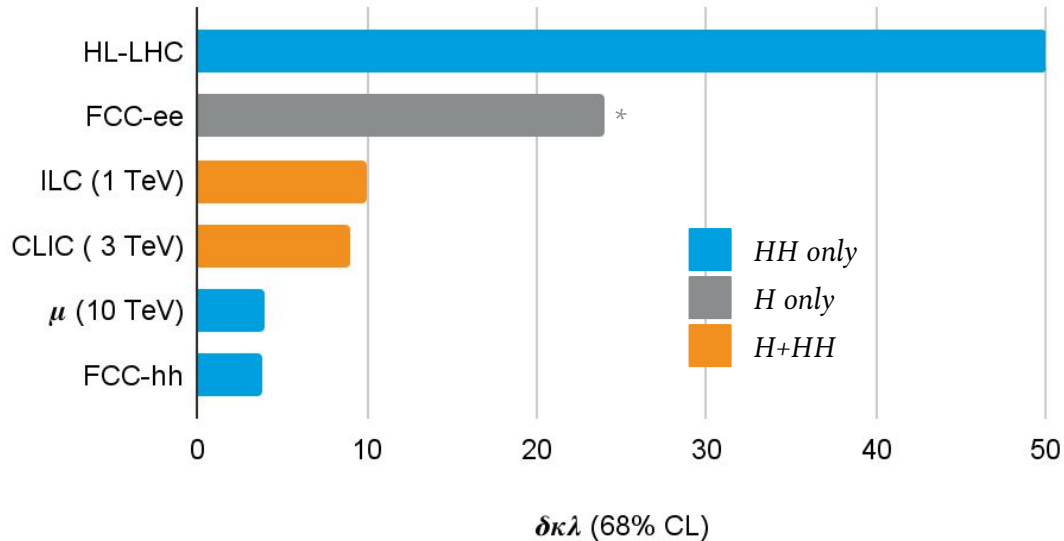


- Measuring the Higgs self-coupling allows us to gain insight into the nature of the Higgs potential and electroweak symmetry breaking
- **FCC-hh**: pp -collisions at 100 TeV, 30 ab^{-1} in ~ 25 years
- Measuring the **Higgs self-coupling via di-Higgs production** is key benchmark for FCC-hh
 - SM: $\sigma(ggHH) \sim O(1000)$ smaller than $\sigma(ggH)$
 - Large cross-section and data-set at FCC-hh
 - 20 x precision of HL-LHC

Overview of Higgs self-coupling limits & prospects

- At LHC we set limits: $-0.4 < \kappa_\lambda < 6.3$ (ATLAS-HDBS-2022-03)
- Only at future colliders we will reach a precision measurement

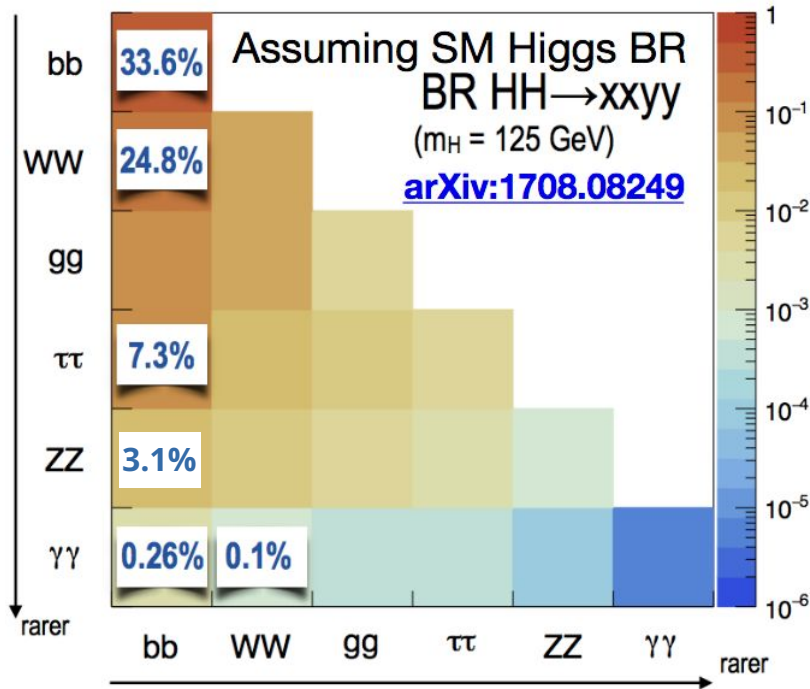
$\delta\kappa\lambda$ (68% CL): Best case scenarios



Details & references in back-up

** For FCC-ee the Higgs self-coupling is measured indirectly via one loop-effect in the ZH process*

Di-Higgs final states

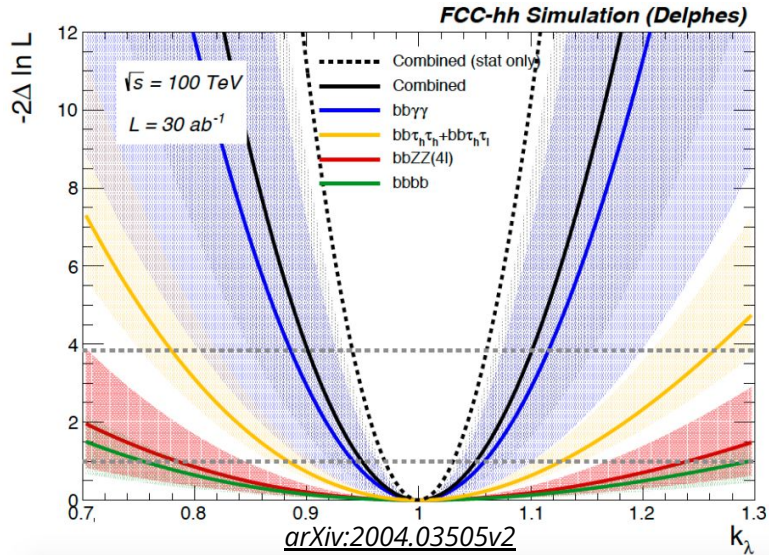


HH measurements:

- Very low cross section
- Challenging final state
- Trade off between purity and high branching ratio

Higgs self-coupling projections for FCC-hh

M. Mangano, G. Ortona, M. Selvaggi

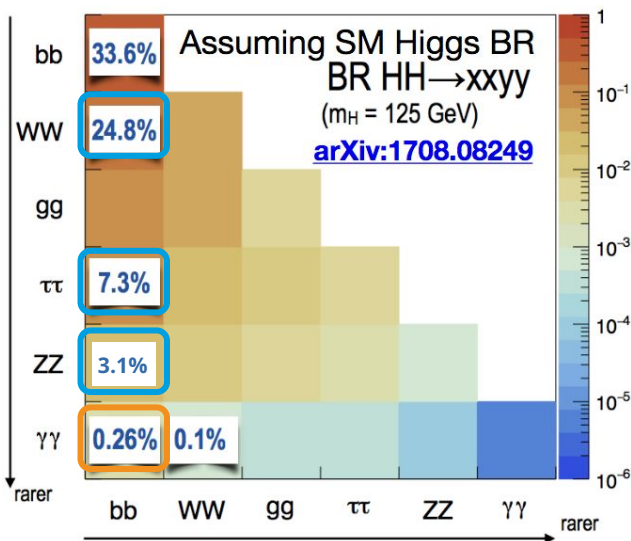


- Previously published prospect studies combined **$bbyy$, $bb\tau\tau(hh+lh)$, $4b$ and $bbZZ(4l)$** final states
- Considered three **different scenarios for detector performance** and systematic uncertainties by reweighting from main, detector scenario **based on LHC performance & FCC-hh CDR**

	Combined precision
$\delta\kappa_\lambda$ (68% CL)	3.4% - 7.8%

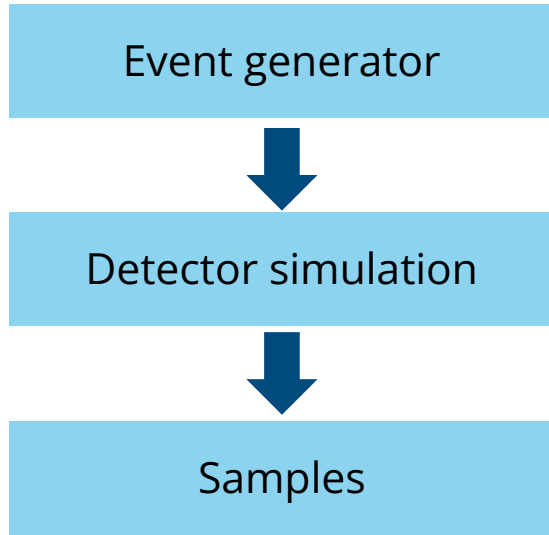
Our work: Update of $\bar{b}b\gamma\gamma$ and adding $\bar{b}bll+E_T^{miss}$

- Studying only ggF HH production mode (so far)



Final state	$BR(HH \rightarrow X)$	Description
$\bar{b}b\gamma\gamma$	0.26%	<ul style="list-style-type: none"> Rare, but high precision DNN-based analysis What is the ultimate precision that can be reached?
$\bar{b}bll+E_T^{miss}$	3.24%	<ul style="list-style-type: none"> Summing contributions from $\bar{b}bWW(l\nu l\nu) + \bar{b}b\tau\tau(ll\nu l\nu) + \bar{b}bZZ(ll\nu\nu)$ Larger BR, but more background contaminated, limited precision Cut-based analysis New for FCC-hh

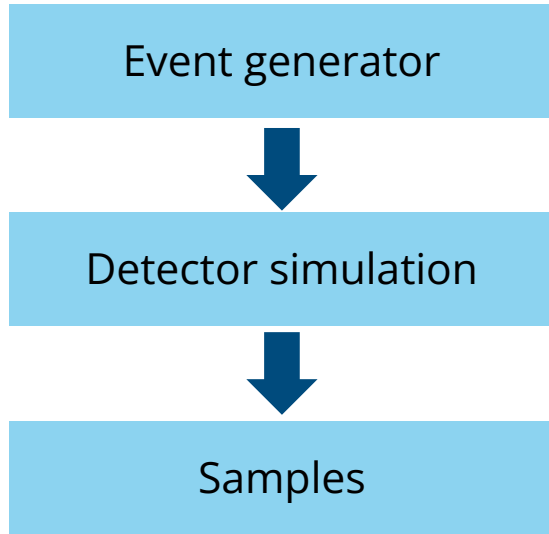
Common software stack for future facilities



All part of key4hep project: Consistent software stack for all future projects

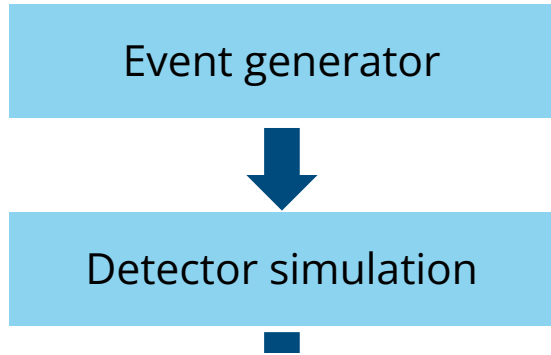
- Fast, parametrized simulation in Delphes
- Using EventProducer framework (fork)
- Samples in EDM4HEP format

Common software stack for future facilities

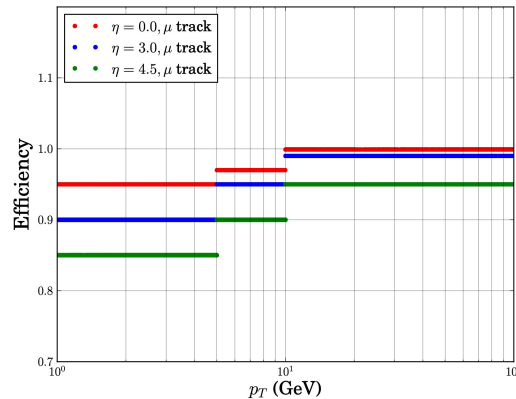
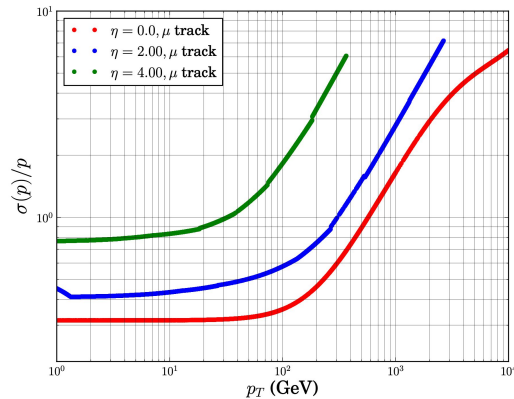


- Our analyses employ two detector scenarios
 - Both implement fixes w.r.t the original FCC-hh Delphes card, e.g. bremsstrahlung for electrons, multiple scattering, resolutions in forward region

Common software stack for future facilities

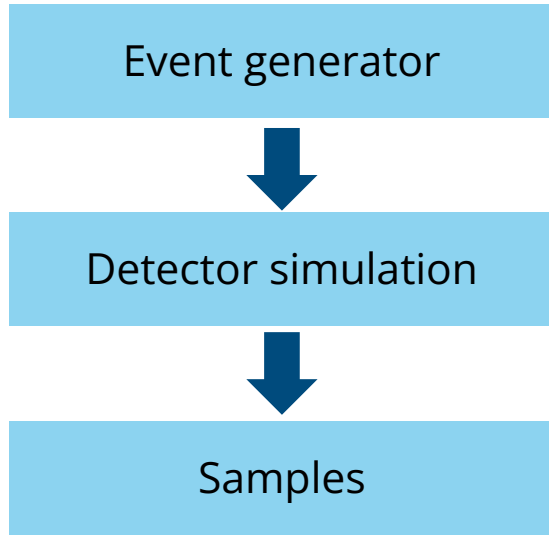


Example parametrization for muons



- Our analyses employ two detector scenarios
 - **Scenario I:** Optimistic case
 - LHC run 2 conditions with e.g. ideal crystal calorimeter, b-tagging (slightly) better than current CMS → This is the scenario to use for ultimate precision in $\bar{b}b_{yy}$

Common software stack for future facilities



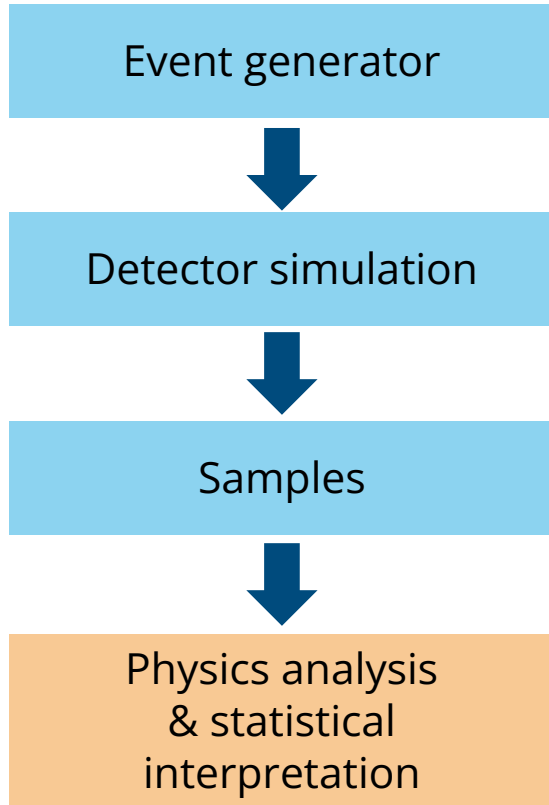
Across all p_T and η bins, up to $|\eta| < 6$

- Our analyses employ two detector scenarios
 - Scenario I: Optimistic case
 - Scenario II: Baseline, more realistic
 - I.e. baseline LaR calorimeter from CDR, lower efficiencies, ...
 - Use for new channel $\bar{b}bll + E_T^{miss}$

Relevant objects

	Relative p resolution		Efficiency	
	Scen I	Scen II	Scen I	Scen II
Electrons	0.4-1%	0.8-3%	76-95%	72-90%
Muons	0.5-3%	1-6%	90-99%	88-97%
Medium b-tagging			80-90%	76-86%

Common software stack for future facilities



All part of key4hep project: Consistent software stack for all future projects

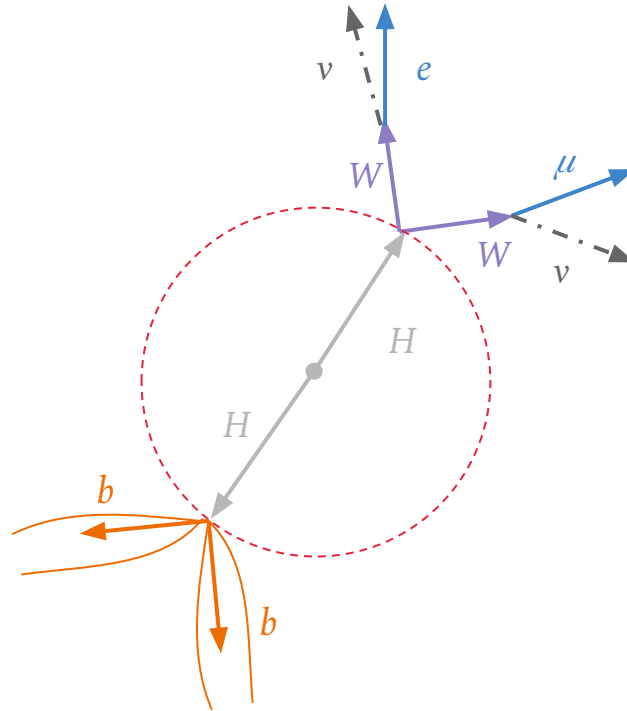
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Analysis with common framework FCCAnalyses

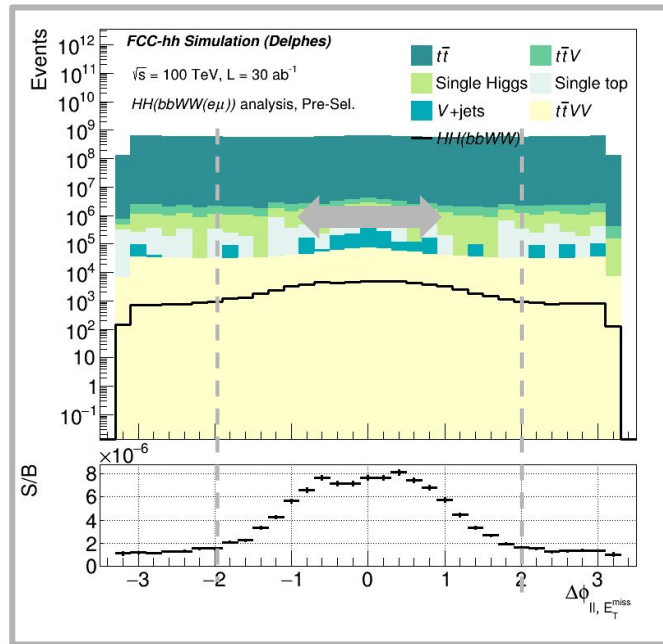
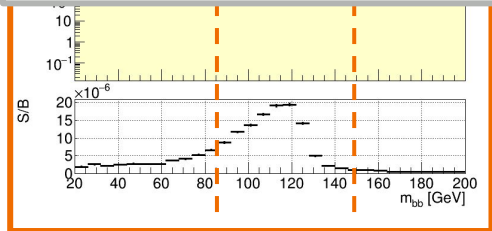
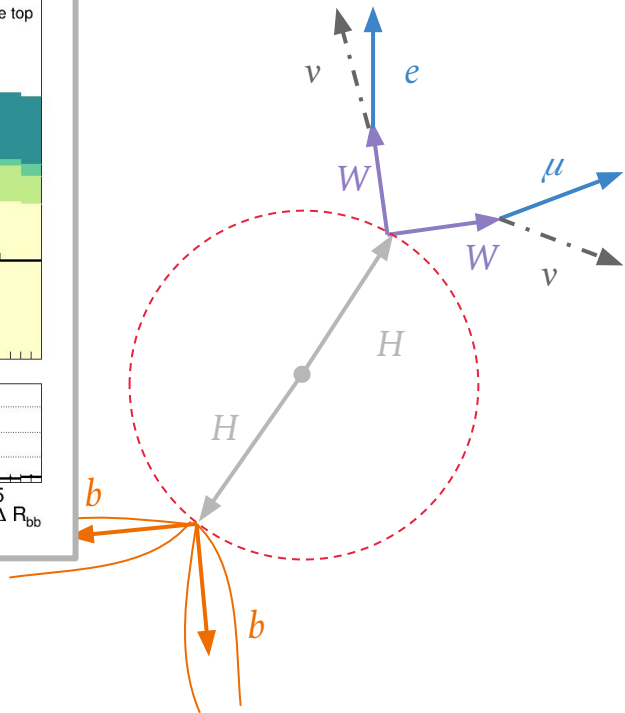
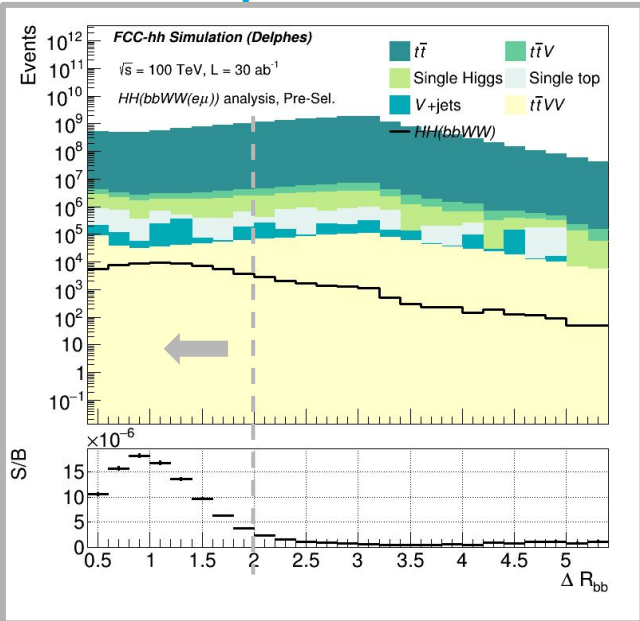
- Currently on fork with some new additions
 - E.g. getting tagged jets from Delphes
- Plan to integrate into main repo

$\bar{b}bl + E_T^{miss}$ analysis

$\bar{b}b\mu + E_T^{miss}$: Event kinematics & selection

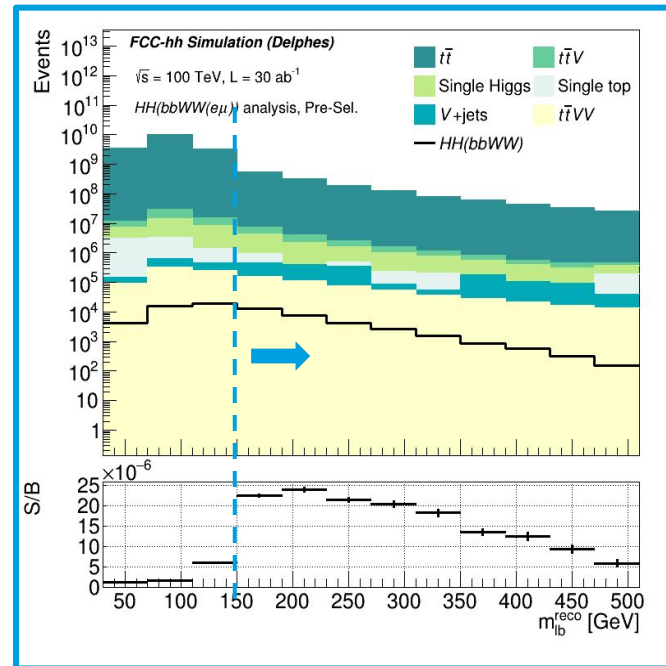
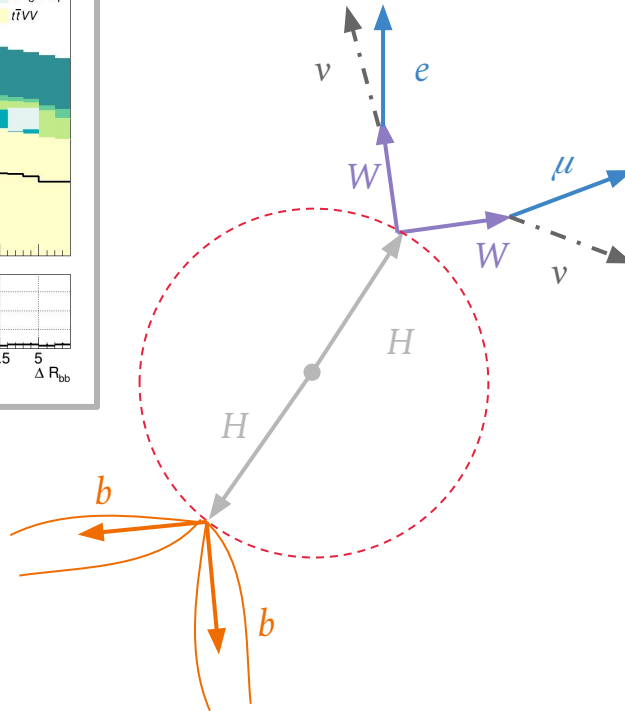
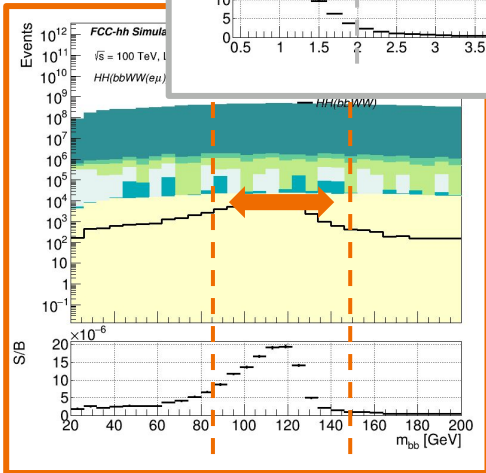
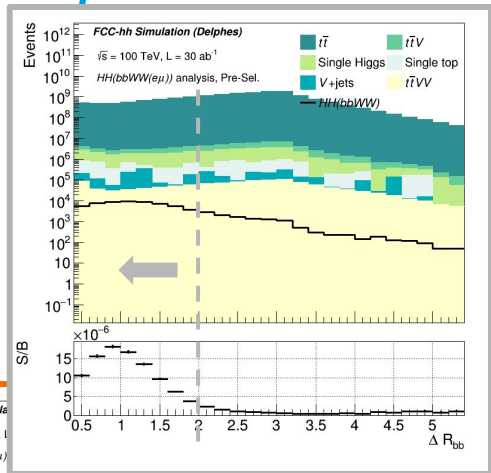


$b\bar{b}ll + E_T^{miss}$: Event kinematics & selection



Higgses recoil against each other \rightarrow Subsequent decays are boosted \rightarrow Exploit angles!

$\bar{b}b\mu + E_T^{\text{miss}}$: Event kinematics & selection



$$m_{lb}^{\text{reco}} = \min \left(\frac{m_{l_1 b_1} + m_{l_2 b_2}}{2}, \frac{m_{l_2 b_1} + m_{l_1 b_2}}{2} \right)$$

Targeted $t\bar{t}$ suppression

$\bar{b}bll + E_T^{miss}$: Fit inputs

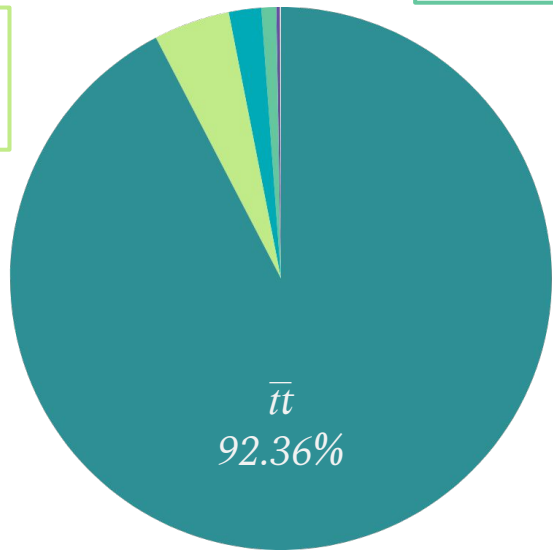
V+jets
1.94%

$\bar{t}tVV$
0.89%

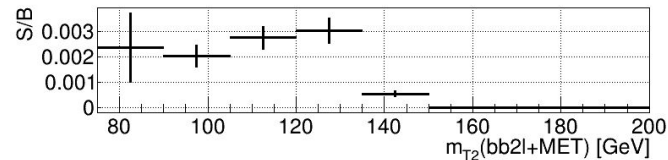
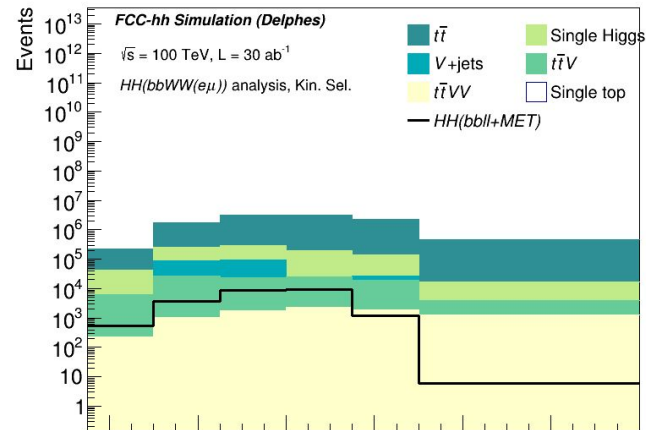
$\bar{t}tV$
0.07%

$S/\sqrt{B} \sim 7$

H
4.54%



Signal
0.21%



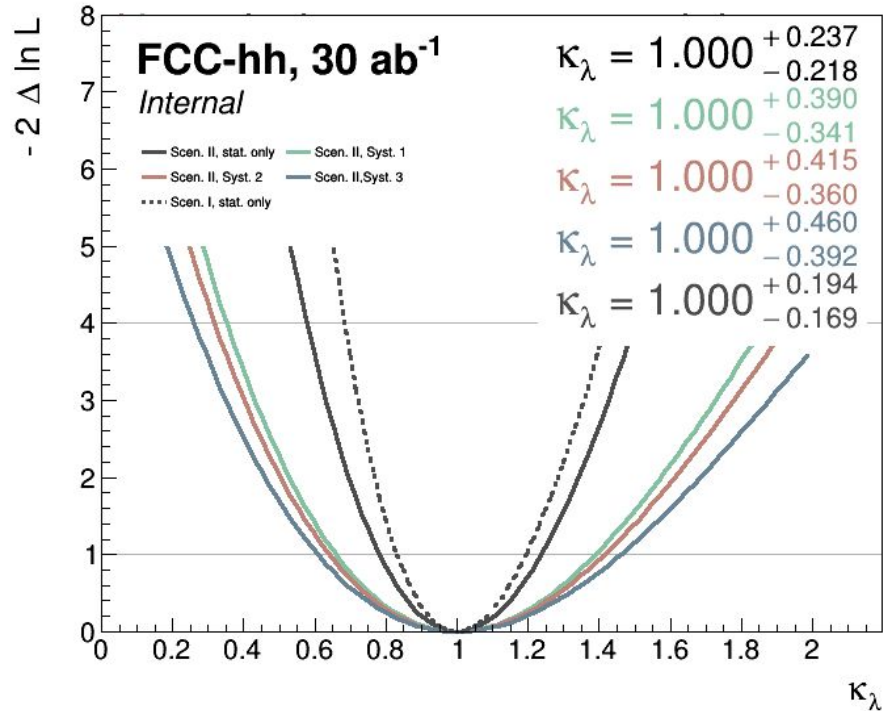
- Transverse mass m_{T2} predicts invisible mass contribution
 - Capture the full HH decay

Results: Systematic uncertainties

Source of uncertainty	Syst. 1	Syst. 2	Syst. 3	Applies to	Correlated
Common systematics					
b-jet ID / b-jet	0.5%	1%	2%	Signals, MC bkgs.	✓
Luminosity	0.5%	1%	2%	Signals, MC bkgs.	✓
Signal cross-section	0.5%	1%	1.5%	Signals, MC bkgs.	✓
<i>bb̄γγ</i> systematics					
γ ID / γ	0.5%	1%	2%	Signals, MC bkgs.	✗
<i>bb̄ll + E_T^{miss}</i> systematics					
Lepton ID / lepton	0.5%	1%	2%	Signals, MC bkgs.	✗
Data-driven bkg. est.	-	1%	1%	V + jets	✗
Data-driven bkg. est.	-	-	1%	t \bar{t}	✗

- Following previous di-Higgs studies@FCC-hh
- Applied as rate systematics only, no shape effect

$\bar{b}bll + E_T^{miss}$: Results

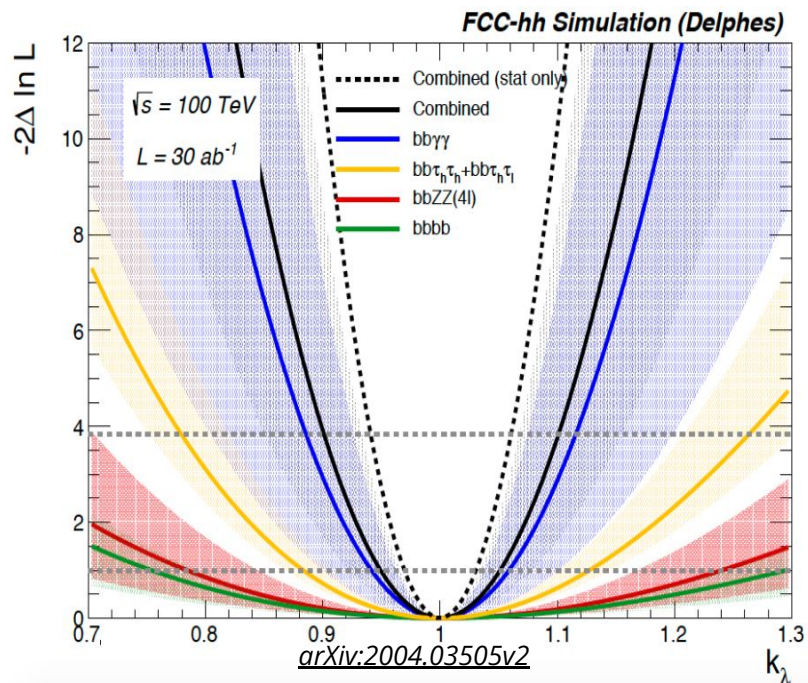


- Higgs self-coupling modifier κ_λ interpretation
 - Parametrized dependence of $\sigma(ggHH)$ on κ_λ
 - Inputs: $\kappa_\lambda = 1.0, 2.4, 3.0$
 - All other couplings fixed to SM
 - NLO cross-sections at 100 TeV, with k -factor independent of κ_λ
 - No Higgs BR dependence on κ_λ and uncertainties or other additional theory uncertainties
- Preliminary results for scenario II $\bar{b}bll + E_T^{miss}$
 - Neglecting V+jets and single top backgrounds

bbyy analysis

$\bar{b}b\gamma\gamma$ analysis: Introduction

M. Mangano, G. Ortona, M. Selvaggi



- The $\bar{b}b\gamma\gamma$ channel is the most sensitive one and it was already studied by previous paper achieving at best 3.8% (3.4% stat only) precision on the self coupling

$\bar{b}b\gamma\gamma$ analysis: Introduction

M. Mangano, G. Ortona, M. Selvaggi



**Is this the ultimate precision that we can reach on the self coupling?
Can we improve this result? If yes how?**

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$\bar{b}b\gamma\gamma$ analysis: Introduction

Is this the ultimate precision that we can reach on the self coupling?
Can we improve this result? If yes how?

- **New detector simulation**
 - **First time that we simulate an 'ideal' detector, in the previous studies it was reweighted from the main FCC-hh scenario**

*b*byy analysis: Introduction

Is this the ultimate precision that we can reach on the self coupling?
Can we improve this result? If yes how?

- **New detector simulation**
- **New analysis strategy**
 - **We tried 2 main analysis strategy and compared the results**

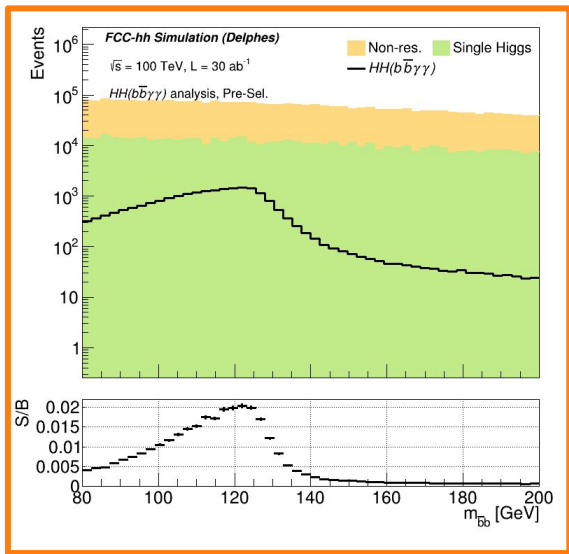
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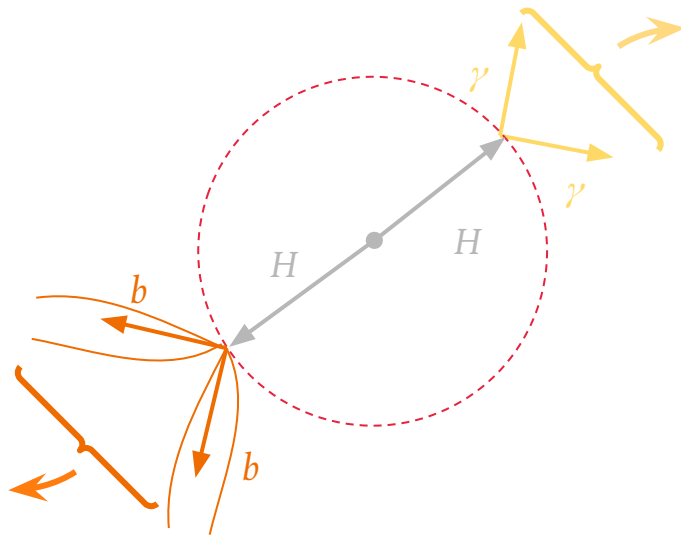
- **New detector simulation**
- **New analysis strategy**
- **Check which is the most sensitivity observable and try to improve it**
 - **Different assumptions on $m_{\bar{b}b}$ resolution**

$b\bar{b}\gamma\gamma$ analysis: Strategy overview

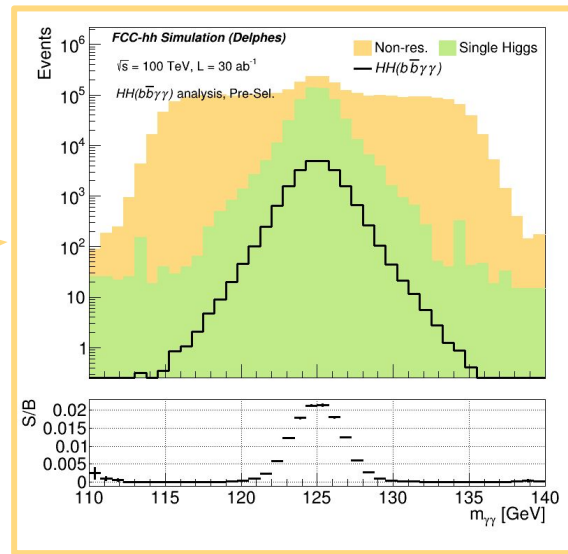
Pre-selected events



Signal signature



- 2 b -jets & 2 photons with invariant masses near m_H



- Backgrounds:

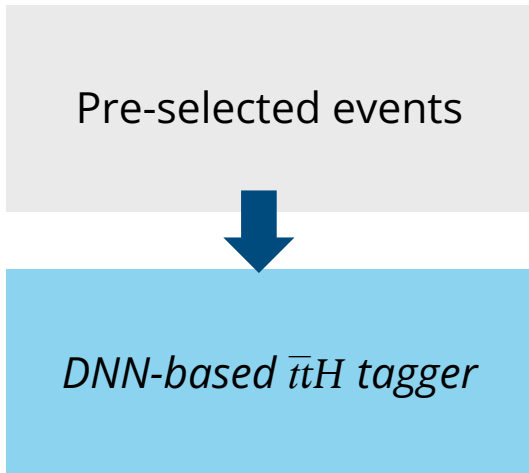
- Non-resonant QCD: $\gamma\gamma$ +jets and γ +jets
- Single Higgs production

$\bar{b}b\gamma\gamma$ analysis: Strategy 1 (Run2 like analysis)

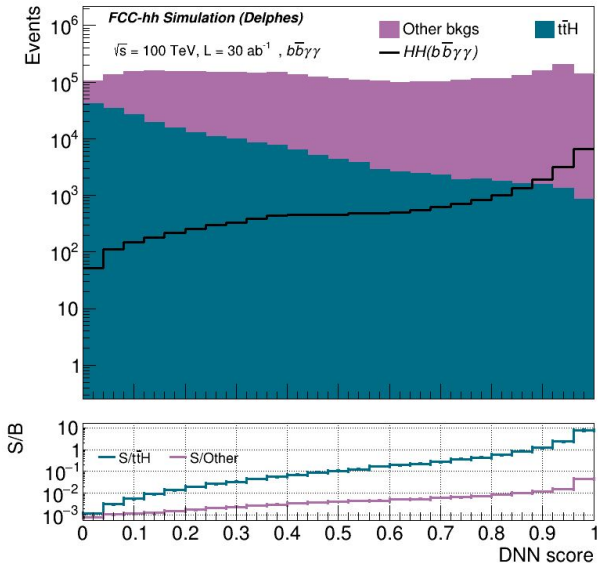
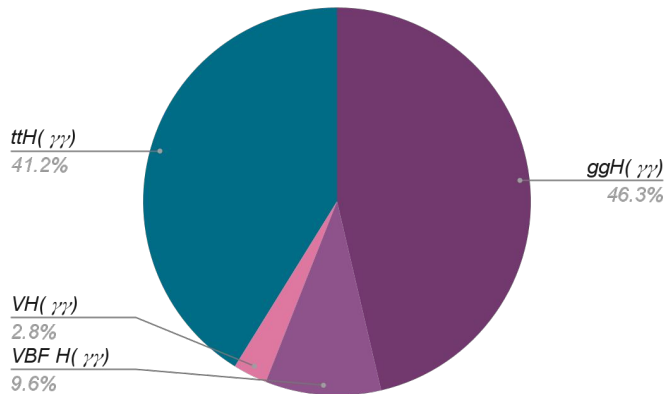
3DNNs as for the baseline analysis:

- 'ttH-killer' trained signal vs ttH background (93% AUC)

$b\bar{b}\gamma\gamma$ analysis: Strategy 1 (Run2 like analysis)



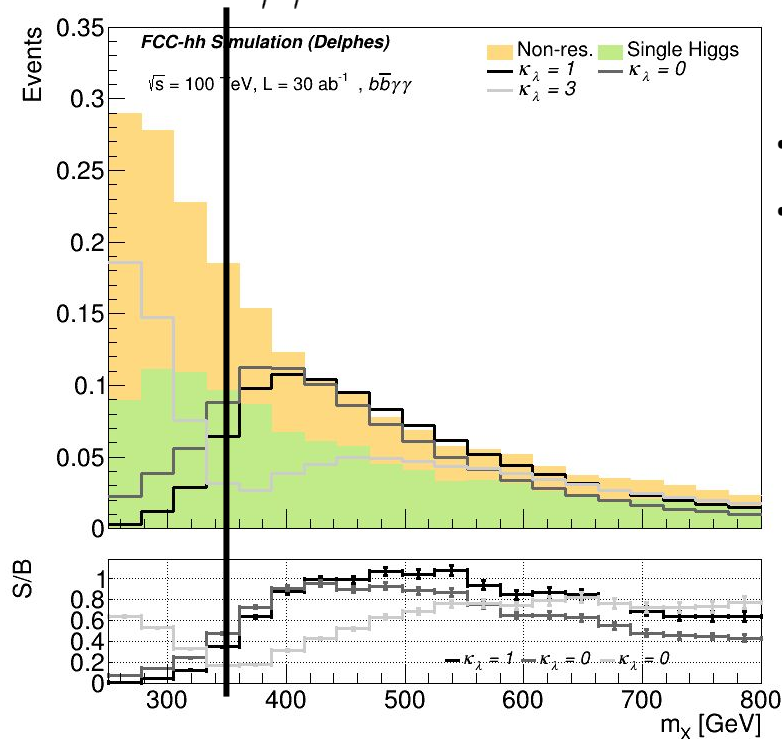
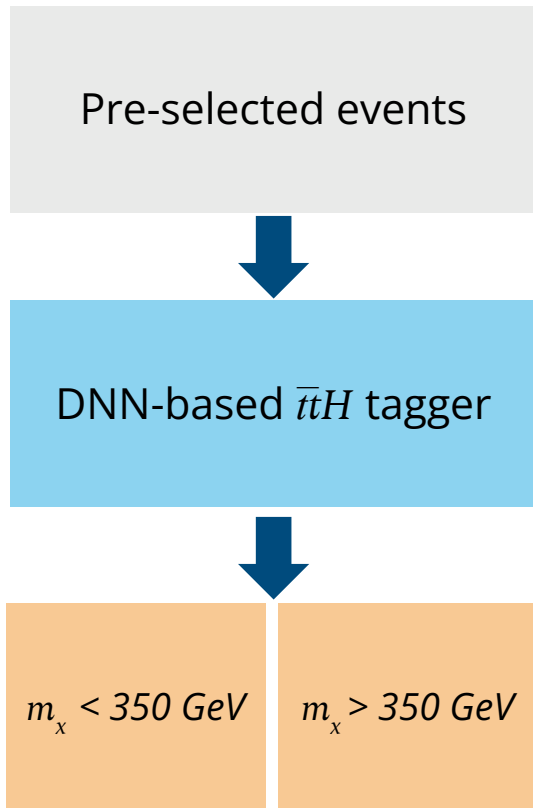
Single Higgs bkg composition



- $t\bar{t}H$ enhanced - same final state as signal signature
 - $\sigma(t\bar{t}H \rightarrow \gamma\gamma) \sim 3 \sigma(ggHH \rightarrow b\bar{b}\gamma\gamma)$
- Exploit expected differences in kinematics:
 - $t\bar{t}H$ more jets, but less energetic
 - $t\bar{t}H$ can contain high p_T leptons

$\bar{b}b\gamma\gamma$ analysis: Strategy 1 (Run2 like analysis)

$$m_x = m_{\bar{b}b\gamma\gamma} - m_{\bar{b}b} - m_{\gamma\gamma} + 250\text{GeV}$$



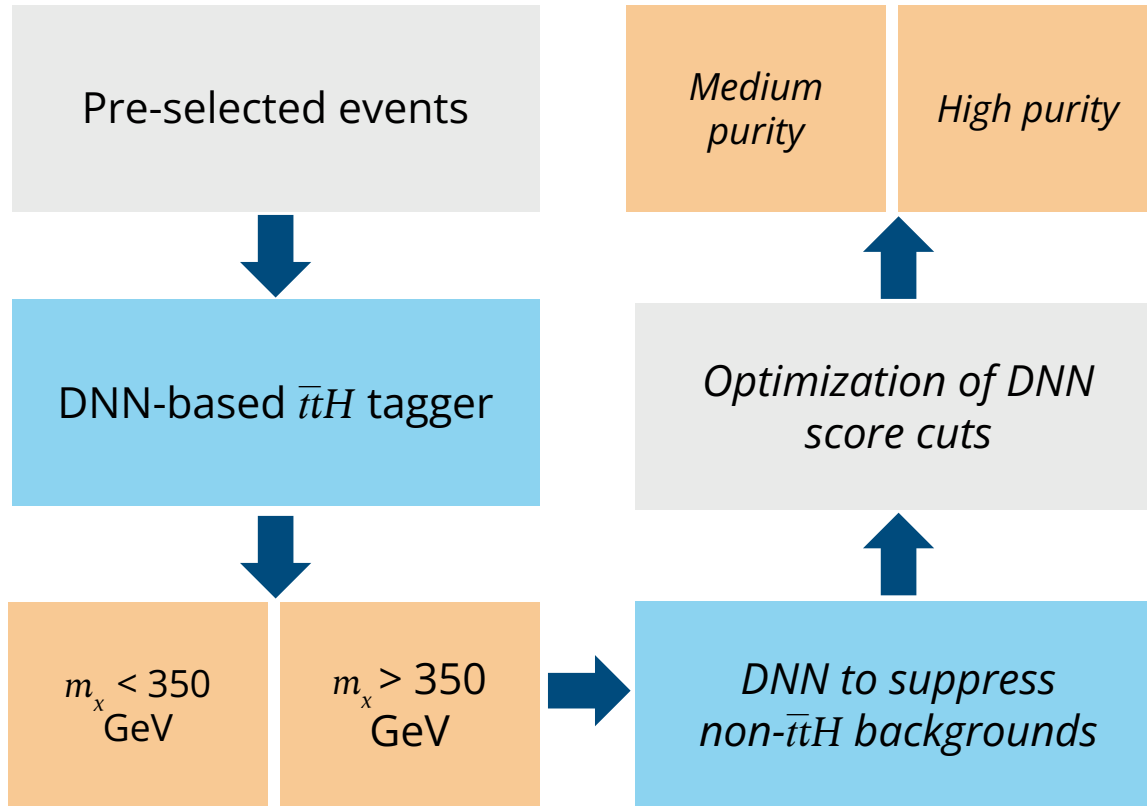
- Shape depends on κ_λ
- Region $m_x < 350\text{ GeV}$ has low S/B for $\kappa_\lambda = 1$ (SM), but contributions from $\kappa_\lambda \neq 1$ (BSM) signals

$\bar{b}b\gamma\gamma$ analysis: Strategy 1 (Run2 like analysis)

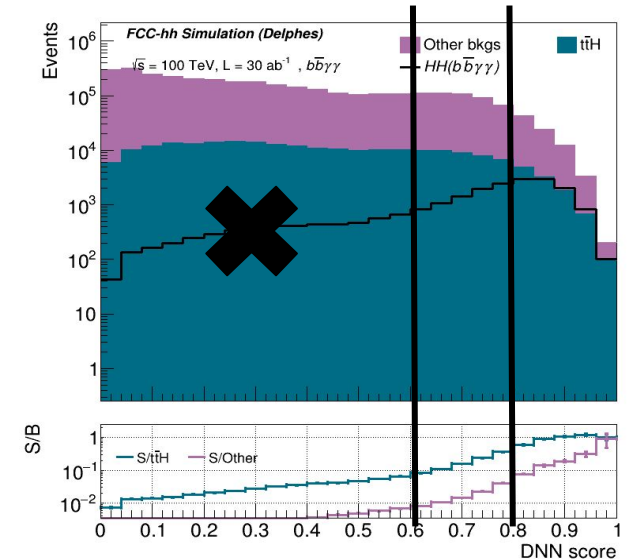
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- 'ttH-killer' trained signal vs ttH background (93% AUC)
- 'High Mx region DNN' trained signal vs all background but ttH (82% AUC)
- 'Low Mx region DNN' trained signal vs all background but ttH (74% AUC)

$b\bar{b}\gamma\gamma$ analysis: Strategy 1 (Run2 like analysis)



- Separate DNNs for suppressing non- background, using same input variables as $\bar{t}tH$ tagger
- Optimization of cuts based on significance



$\bar{b}b$ analysis: Strategy 1 (Run2 like analysis)

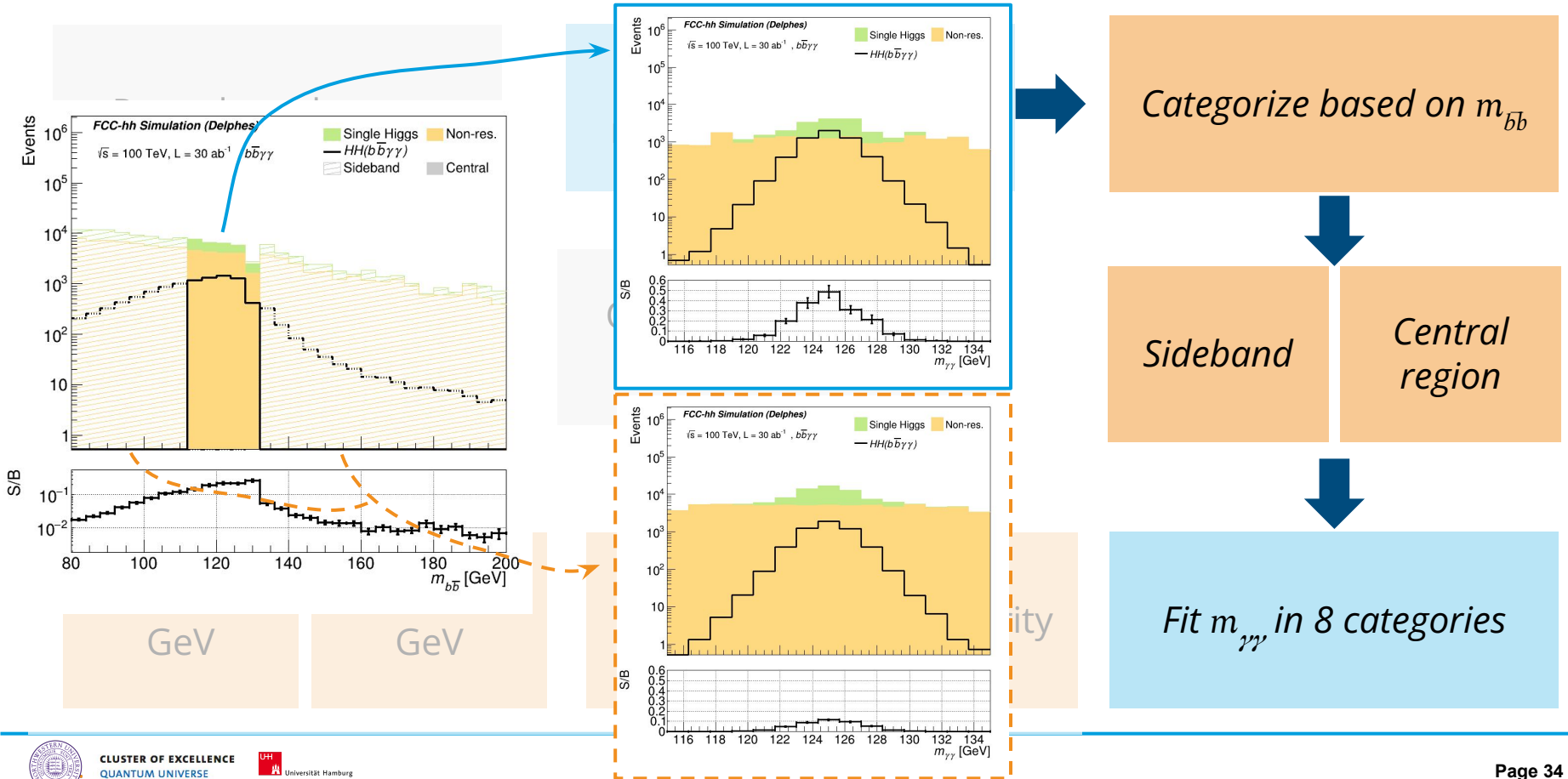
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$m_{\bar{b}b}$ splitting:

- 1 $m_{\bar{b}b}$ bin ($m_{\bar{b}b}$ distribution not used)
- 2 $m_{\bar{b}b}$ bins (sideband + central region)
- optimal mbb binning ($m_{\bar{b}b}$ in bins that are determined by the significance)

$b\bar{b}\gamma\gamma$ analysis: Strategy 1 (Run2 like analysis 2 $m_{b\bar{b}}$ bins)



$b\bar{b}$ analysis: Strategy 2

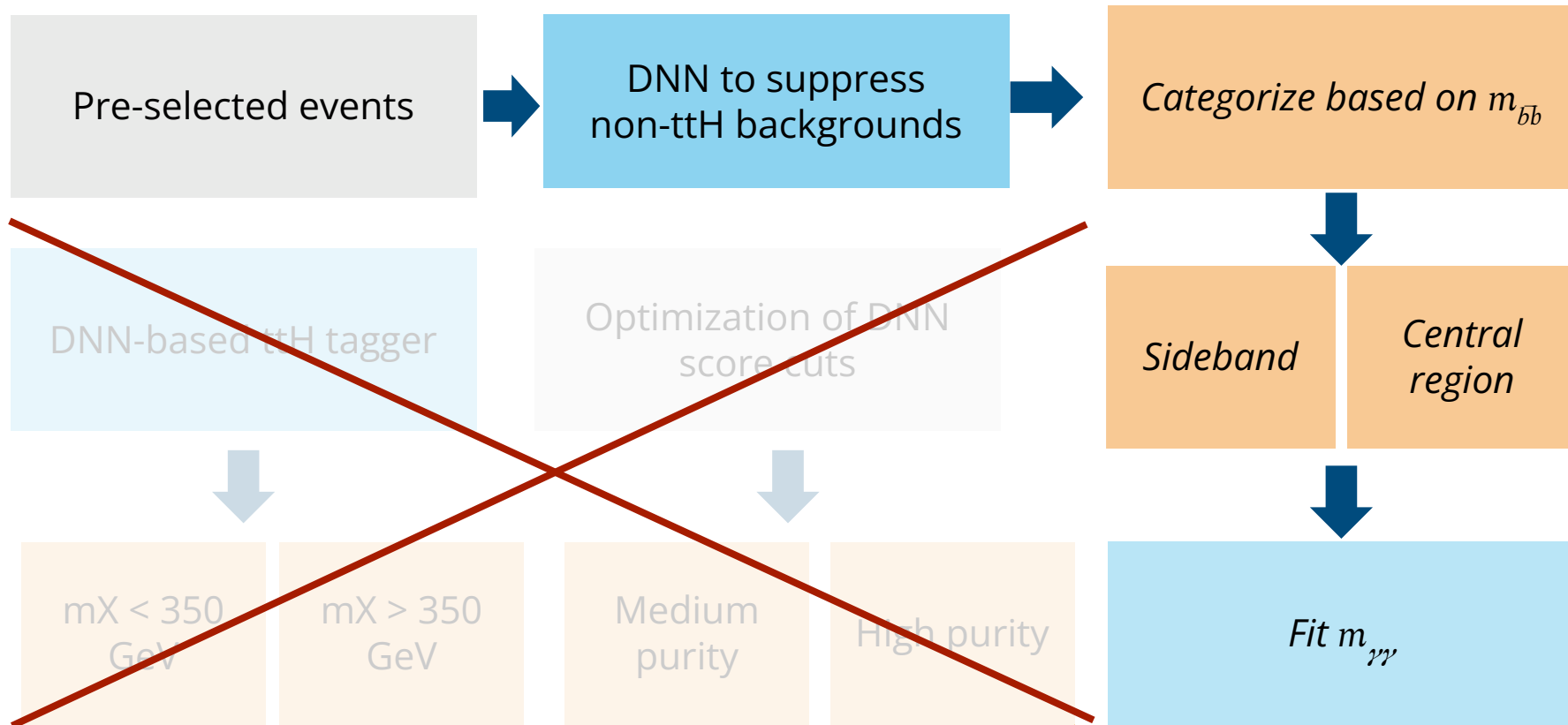
1DNN with all the backgrounds in (87% AUC)

- AUC is compatible with the mean of the AUCs used in strategy 1 → the sensitivity at the end should be the same

$m_{b\bar{b}}$ splitting:

- 1 $m_{b\bar{b}}$ bin ($m_{b\bar{b}}$ distribution not used)
- 2 $m_{b\bar{b}}$ bins (sideband + central region)
- optimal mbb binning ($m_{b\bar{b}}$ in bins that are determined by the significance)

$\bar{b}b\gamma\gamma$ analysis: Strategy 2 overview (2 $m_{\bar{b}b}$ bins splitting)



$\bar{b}b$ analysis: Strategies comparison and results

Strategy 1 and strategy 2 gave the same results:

- Improve the DNN splitting doesn't really optimize the analysis

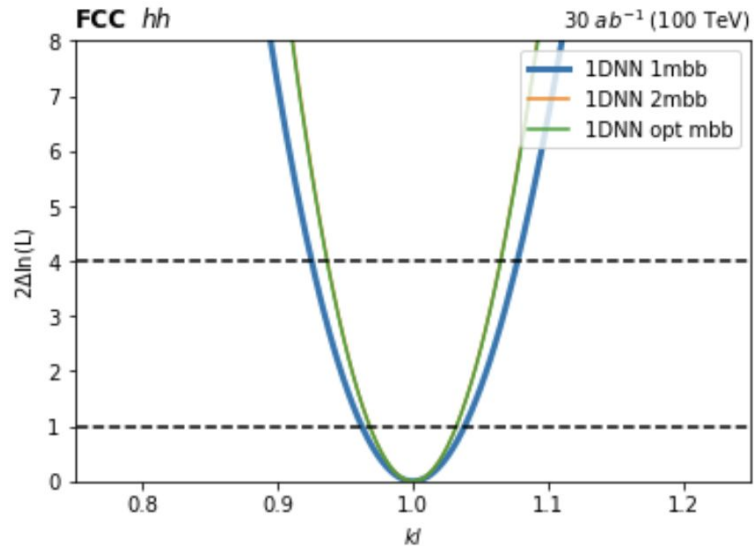
Does the $m_{\bar{b}b}$ splitting optimize the sensitivity?

$\bar{b}b\gamma\gamma$ analysis: Strategies comparison and results

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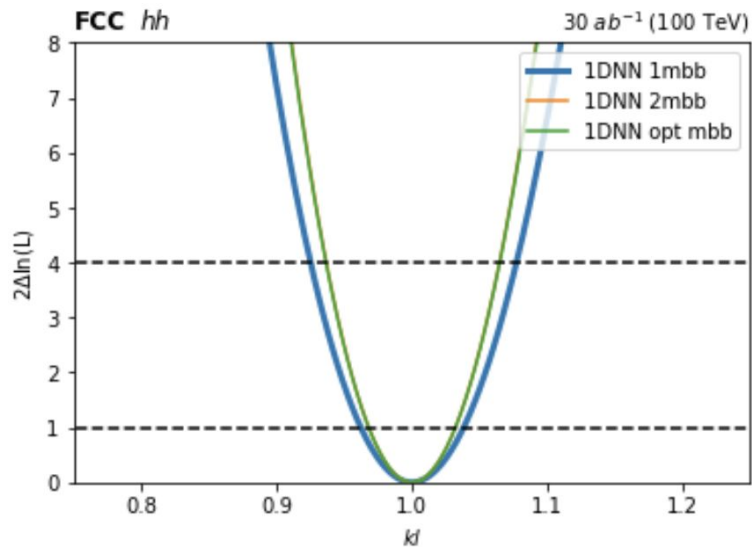
Does the $m_{\bar{b}b}$ splitting optimize the sensitivity?



	$1 m_{\bar{b}b}$
Stat only	3.8%
Syst I	4.4%

$\bar{b}b\gamma\gamma$ analysis: Strategies comparison and results

Does the $m_{\bar{b}b}$ splitting optimize the sensitivity?



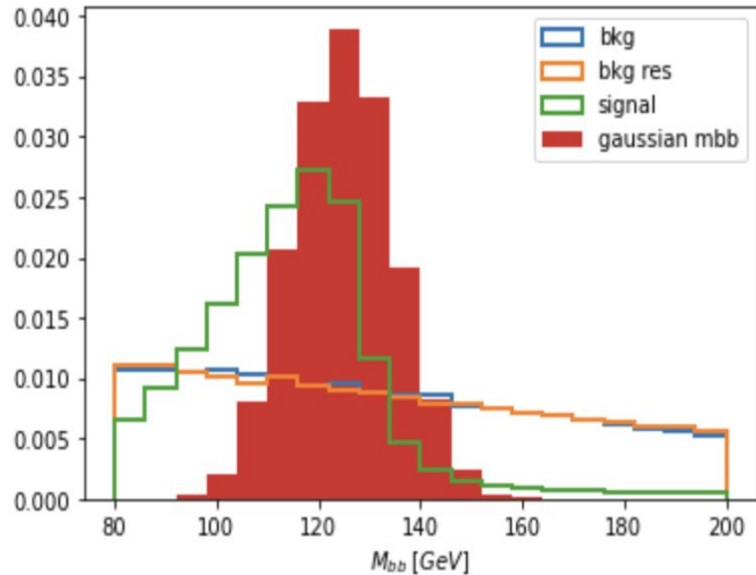
Why the solution with 2 $m_{\bar{b}b}$ binning or a $m_{\bar{b}b}$ optimize binning lead to the same precision on κ_I ?

	1 $m_{\bar{b}b}$	2 $m_{\bar{b}b}$	$m_{\bar{b}b}$ optBin
Stat only	3.8%	3.2%	3.2%
Syst I	4.4%	3.6%	3.6%

It's time to investigate properly the $m_{\bar{b}b}$ distribution

$\bar{b}b\gamma\gamma$ analysis: the road to 1% precision on self coupling

We assume a gaussian resolution of 10 GeV for the $m_{\bar{b}b}$ of the signal



	$m_{\bar{b}b}$ optBin	Old result
Stat only	2.5%	3.4%
Syst I	2.7%	3.8%

1.5x improvement versus the older results

Seems that the resolution on $m_{\bar{b}b}$ is the key to achieve better precision on k_λ

$\bar{b}b\gamma\gamma$ analysis: the road to 1% precision on self coupling

What happens if we assume better resolution for the $m_{\bar{b}b}$ mass?

	Stat only	Syst 1
No assumption on $m_{\bar{b}b}$ resolution	3.2%	3.6%
10 GeV $m_{\bar{b}b}$ res	2.5%	2.7%



Already better
than what
quoted in the
documentation
(3.8% syst 1)

$\bar{b}b\gamma\gamma$ analysis: the road to 1% precision on self coupling

What happens if we assume better resolution for the $m_{\bar{b}b}$ mass?

	Stat only	Syst 1
No assumption on $m_{\bar{b}b}$ resolution	3.2%	3.6%
10 GeV $m_{\bar{b}b}$ res	2.5%	2.7%
5 GeV $m_{\bar{b}b}$ res	2.0%	2.3%
3 GeV $m_{\bar{b}b}$ res	1.8%	2.0%



Already better than what quoted in the documentation (3.8% syst 1)

Conclusion

We restarted the effort of FCC-hh Higgs self-coupling studies:

- Common software tools, working on integration of our developments into the main repositories

$b\bar{b}l+l+E_T^{miss}$

- Cut-based analysis showing first estimates of precision 20-40% stand-alone
- Finalizing the analysis with realistic detector scenario II
- Potential further optimization/studies: Improve lepton isolation efficiencies, impact of higher levels of pile-up, MVA ...

Conclusion

We restarted the effort of FCC-hh Higgs self-coupling studies:

- Common software tools, working on integration of our developments into the main repositories

$b\bar{b}y\bar{y}$

- We studied several analysis configuration to test the stability of our results and the precision to which we are able to measure the self coupling
 - Not much difference in applying 3 or 1 DNN, but very sensitive to the $m_{\bar{b}b}$ resolution/splitting
- Reaching $\sim 1\%$ precision on κ_λ seems possible only if we are able to build a detector that can have a $m_{\bar{b}b}$ resolution of 3GeV
- We are happy to study different center of mass energy scenarios:
 - 80 TeV and 120 TeV

Bonus

Overview of Higgs self-coupling limits & prospects

Experiment	95% CL limit	Reference
ATLAS - HH - $H+HH$	$-0.6 < \kappa_\lambda < 6.6$ $-0.4 < \kappa_\lambda < 6.3$	ATLAS-HDBS-2022-03
CMS - HH	$-1.2 < \kappa_\lambda < 6.5$	Nature 607 (2022) 60
	$\delta\kappa_\lambda$ (68% CL)	
HL-LHC	$\sim 50\%$	e.g. ATL-PHYS-PUB-2022-005

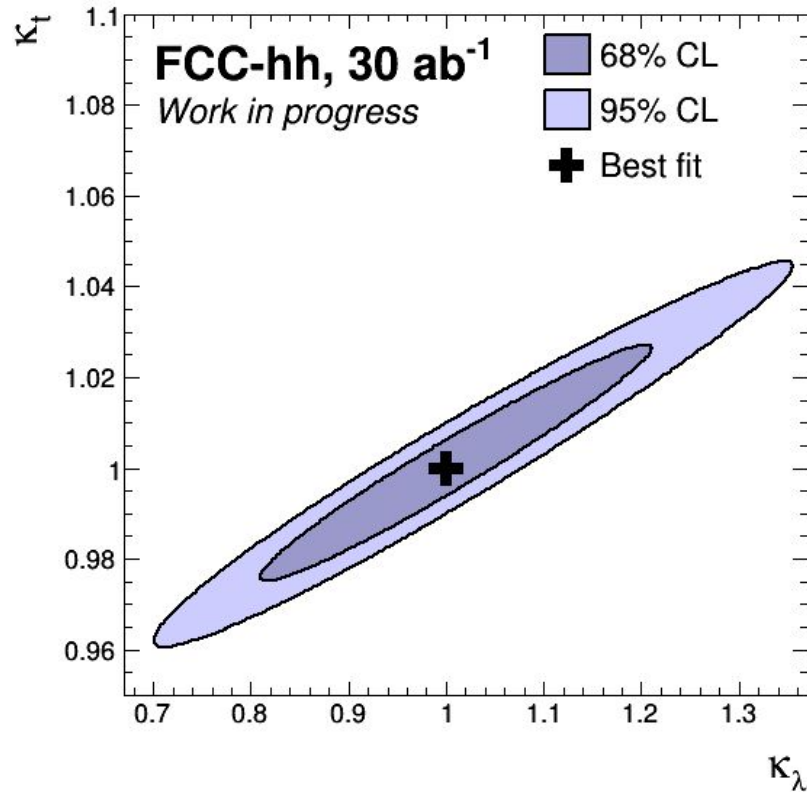
Best case scenarios for Future Colliders		
Experiment	$\delta\kappa_\lambda$ (68% CL)	Reference
ILC (1 TeV)	10%	arXiv:2203.07622 v2
CLIC (3 TeV)	9%	arXiv:1812.01644 v1
FCC-ee	24%	JHEP01(2020)139
μ (10 TeV)	$\sim 3.5\%$	arXiv:2203.07261 v2
FCC-hh	3.4%	arXiv:2004.03505v2

$H+HH$

H only

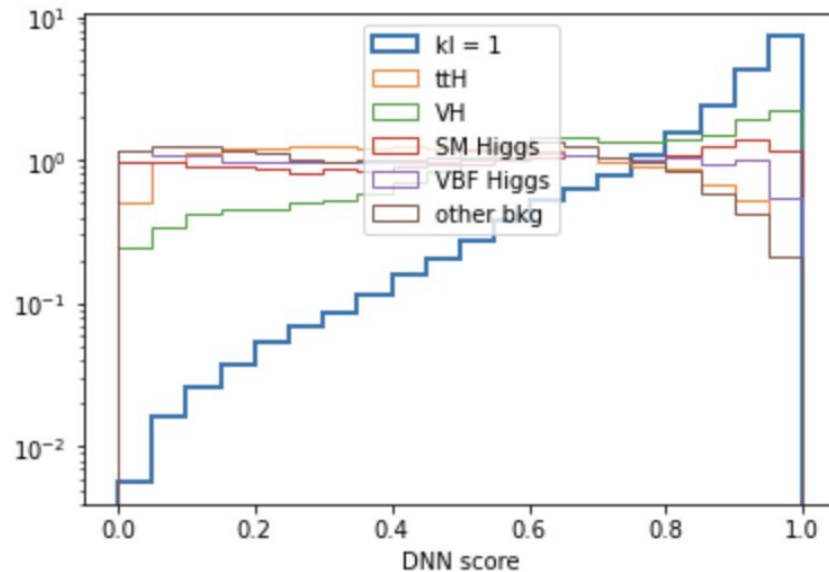
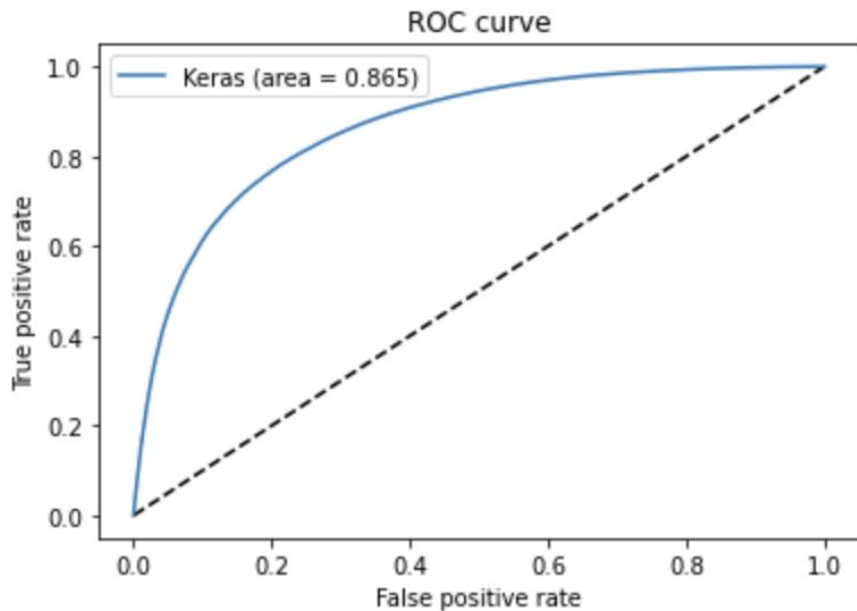
HH

Results: Self-coupling precision



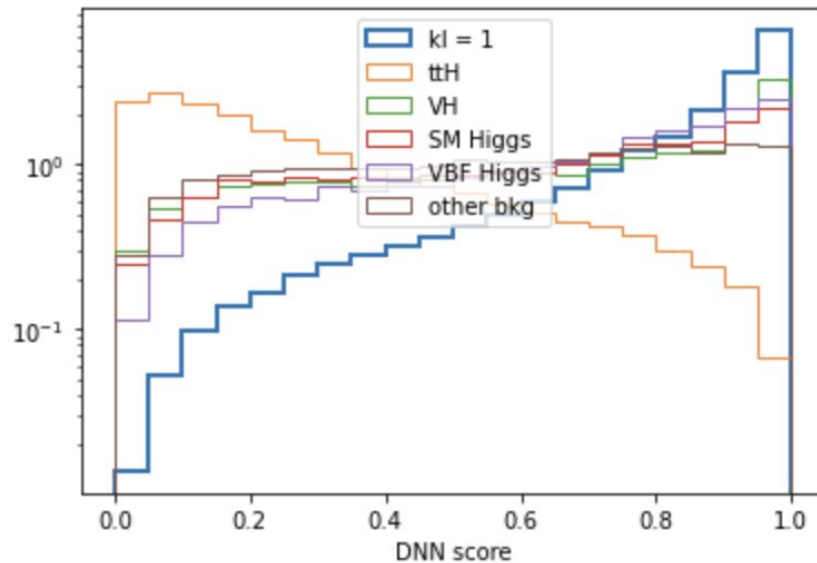
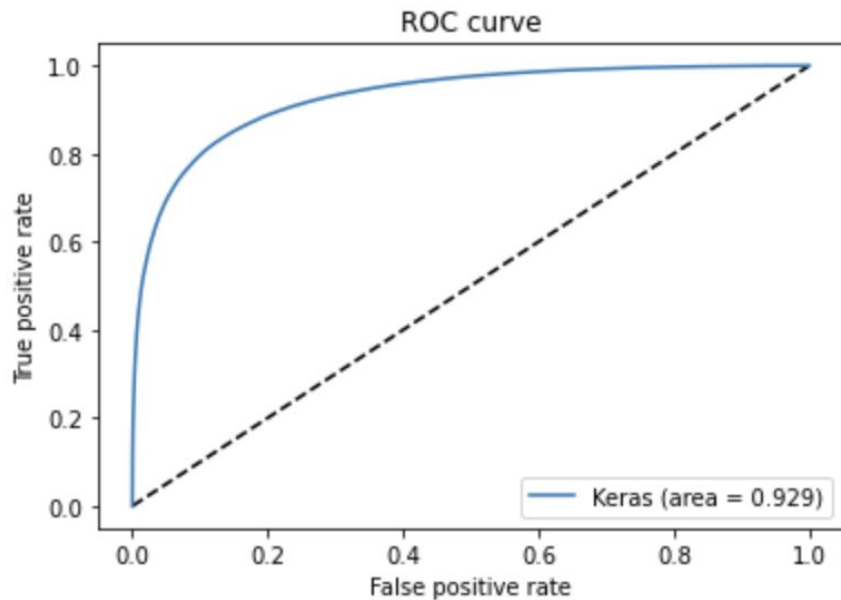
$b\bar{b}yy$ analysis: Strategy optimization

1 DNN performance



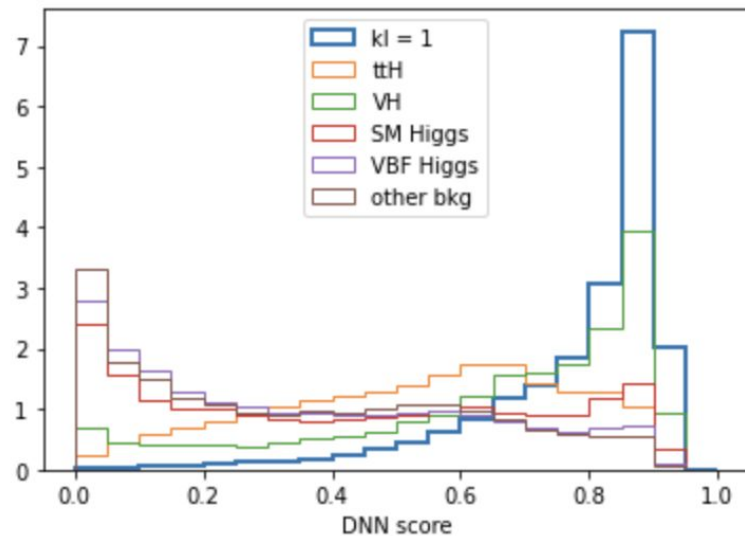
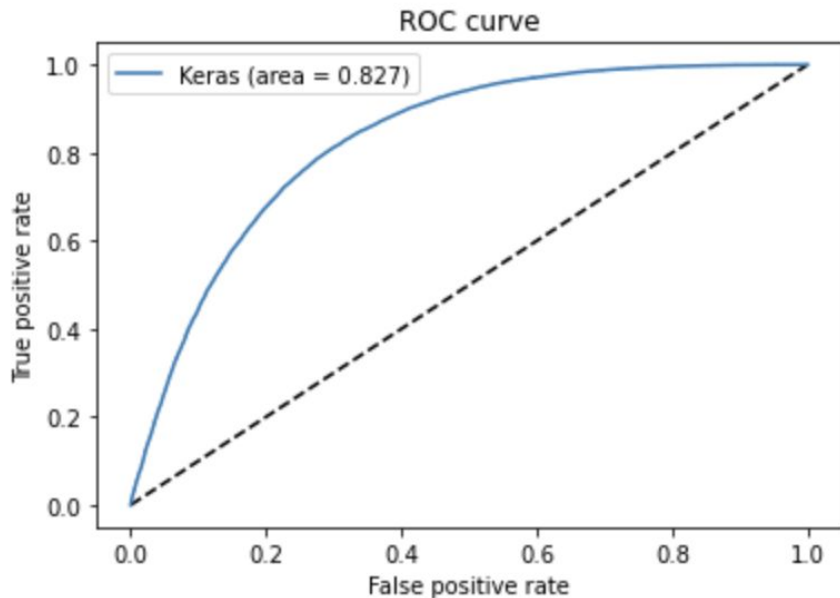
$b\bar{b}$ analysis: Strategy optimization

3 DNNs performances: ttH killer



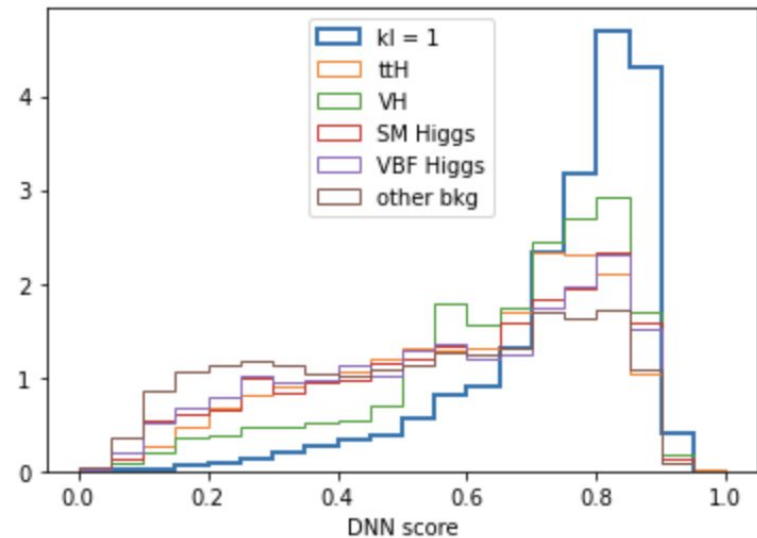
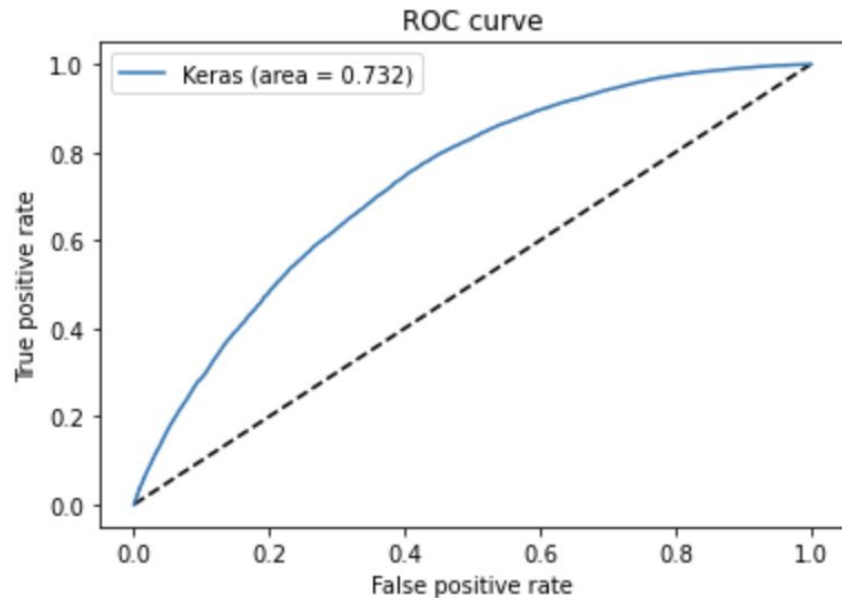
bbyy analysis: Strategy optimization

3 DNNs performances: $Mx > 350$



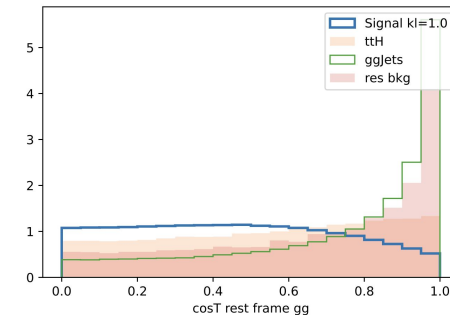
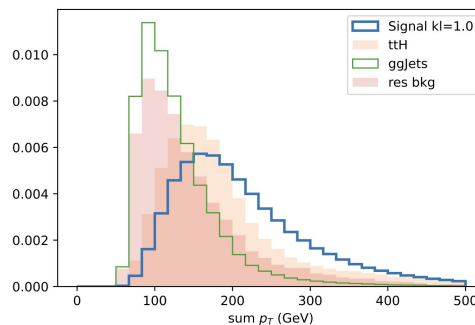
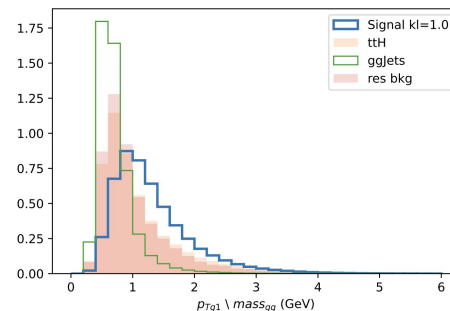
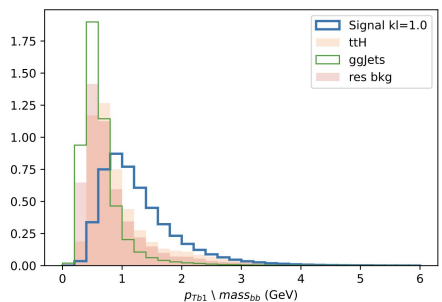
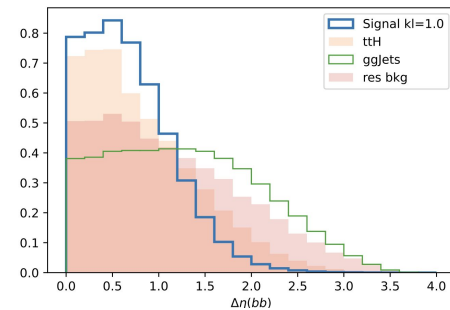
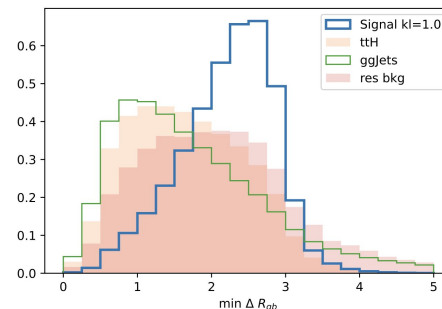
$b\bar{b}yy$ analysis: Strategy optimization

3 DNNs performances: $M_x < 350$



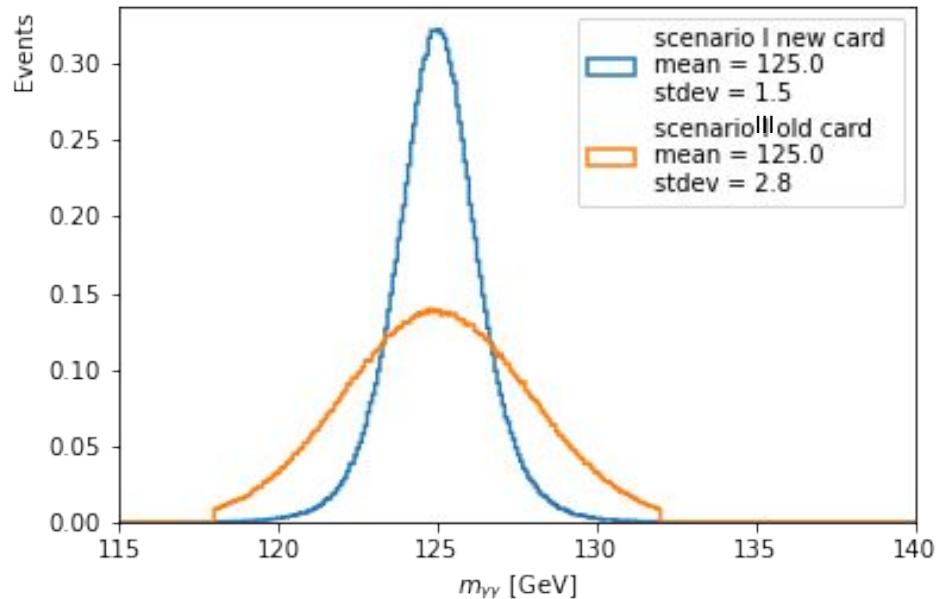
$b\bar{b}yy$ analysis: DNN input variables

- The number of jets (with no b tag requirement)
- The b tag of the leading and subleading jet;
- $p_T(j)/m(jj)$ of the leading and subleading jet.
- $p_T(jj)/m(jj)$ of the dijet object;
- $p_T(\gamma)/m(\gamma\gamma)$ of the leading and subleading photon;
- $p_T(\gamma\gamma)/m(\gamma\gamma)$ of the diphoton object;
- The scalar sum of the jet p_T ;
- The ΔR between the closest photon-jet pair;
- The ΔR between the other photon-jet pair;
- The $\Delta\phi$ and $\Delta\eta$ between the leading and subleading photon;
- The $\Delta\phi$ and $\Delta\eta$ between the leading and subleading jet;
- The $\Delta\phi$ and $\Delta\eta$ between the diphoton and the dijet object;
- The angle between the diphoton object and the beam axis in the dijet rest frame;
- The angle between the leading jet and the beam axis in the dijet rest frame;
- The angle between the leading photon and the beam axis in the diphoton rest frame;
- Number of leptons, i.e. muons and electrons
- p_T of muons and electrons



Delphes parametrization update: m_{yy} resolution

Reco level resolution obtained using $HH \rightarrow b\bar{b}yy$ sample



- More aggressive resolution for m_{yy} compared to the baseline scenario

Delphes parametrization update: b-tagging

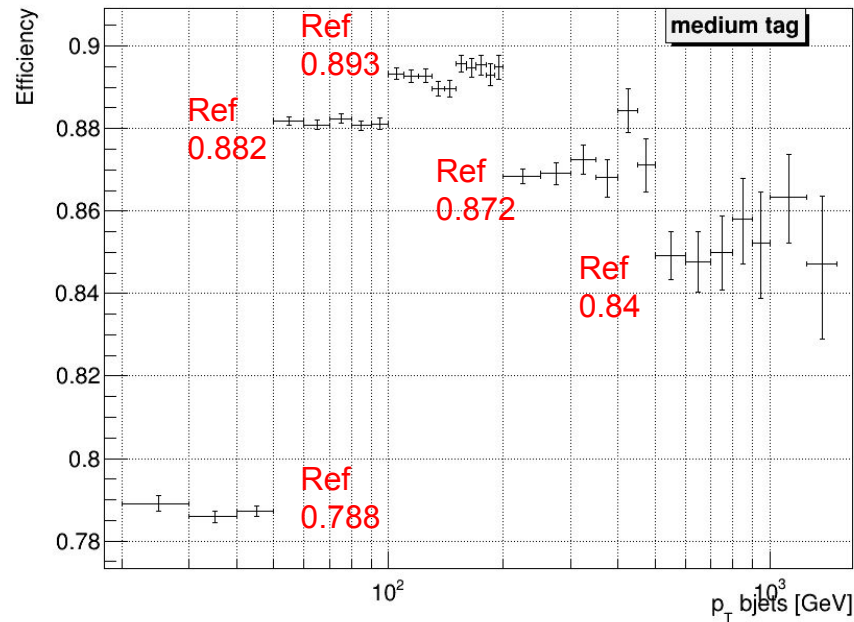
Checks were performed using 600k of $HH \rightarrow \bar{b}b\tau\tau$ events

eff. = $\frac{\text{pT reco-bjets medium, matched with a B had.}}{\text{pT reco-jet matched with a B had.}}$

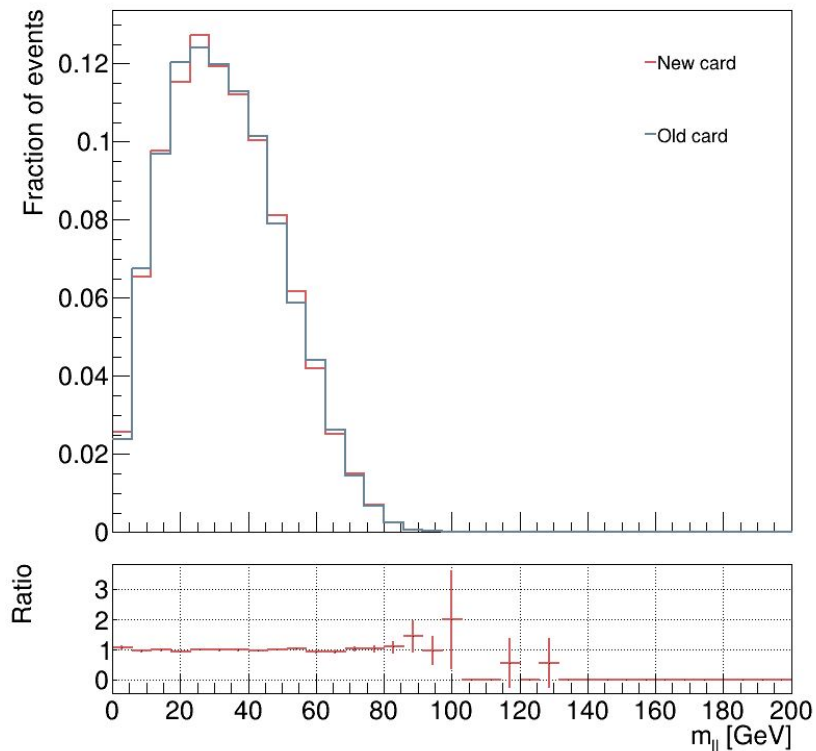
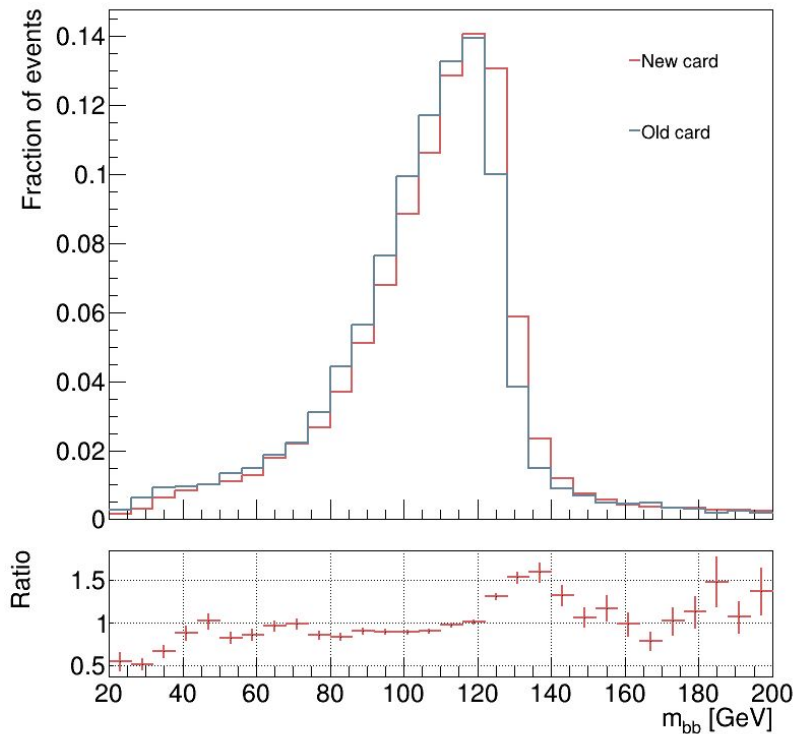
From Delphes card:

```

1.05 * (
  (pt <= 20.0) * (0.00) +
  (abs(eta) < 4.0) * (pt > 20.0 && pt < 50) * (0.88) +
  (abs(eta) < 4.0) * (pt > 50.0 && pt < 100) * (0.92) +
  (abs(eta) < 4.0) * (pt > 100.0 && pt < 200) * (0.93) +
  (abs(eta) < 4.0) * (pt > 200.0 && pt < 500) * (0.90) +
  (abs(eta) < 4.0) * (pt > 500.0 && pt < 1000) * (0.87) +
  (abs(eta) < 4.0) * (pt > 1000.0) * (0.85) +
  (abs(eta) >= 4.0) * (0.00)
)
    
```



$\bar{b}bll + E_T^{miss}$: Mass resolution comparisons old and new Delphes card

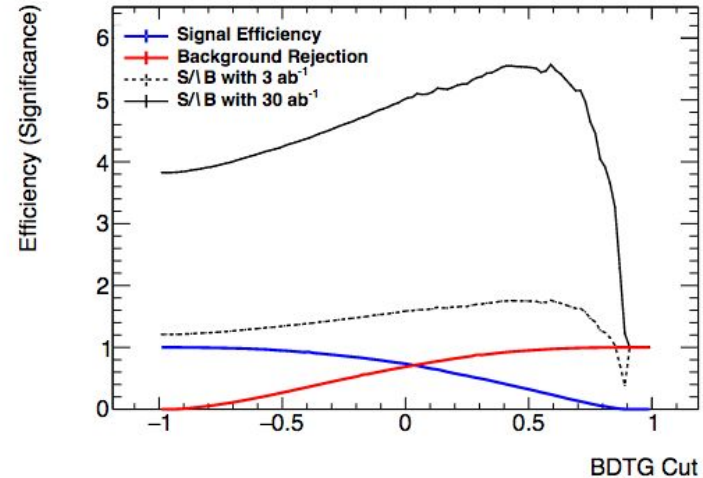
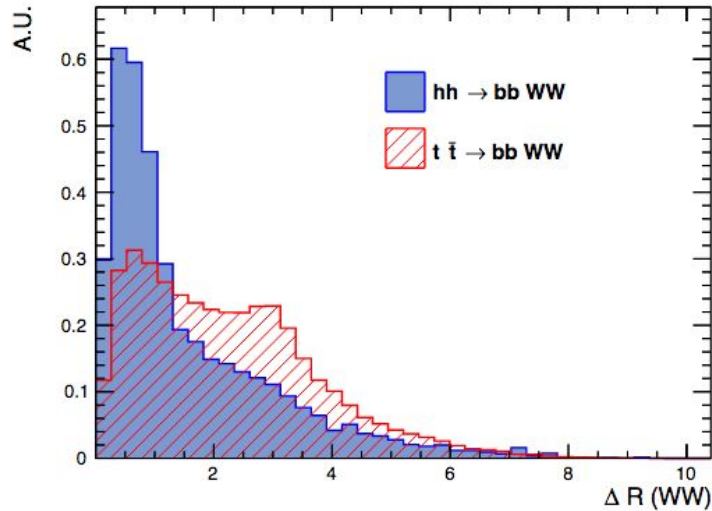


$\bar{b}bll + E_T^{\text{miss}}$: Event selection & categorization

	Analysis category		
	DFOS	SFOS, no Z-peak	SFOS, on Z-peak
Main signals	$\bar{b}bWW^*, \bar{b}b\tau\tau$	$\bar{b}bWW^*, \bar{b}b\tau\tau$	$\bar{b}bZZ^*, \bar{b}b\tau\tau$
Selection variable	Criterion		
Lepton pair	$e\mu$	ee or $\mu\mu$	ee or $\mu\mu$
Number of b-jets		≥ 2	
m_{bb}		85 - 105 GeV	
ΔR_{bb}		< 2	
$\Delta R_{\ell\ell}$		< 1.8	
H_{T2}^{ratio}		> 0.8	
m_{lb}^{reco}		> 150 GeV	
$\Delta\phi(\ell\ell, E_T^{\text{miss}})$		< 2	< 1.2
$m_{\ell\ell}$		10 - 80 GeV	81 - 101 GeV
$\Delta\phi(\ell\ell, E_T^{\text{miss}})$ -categories	< 1.2 ("low") and $1.2 - 2.0$ ("high")		-

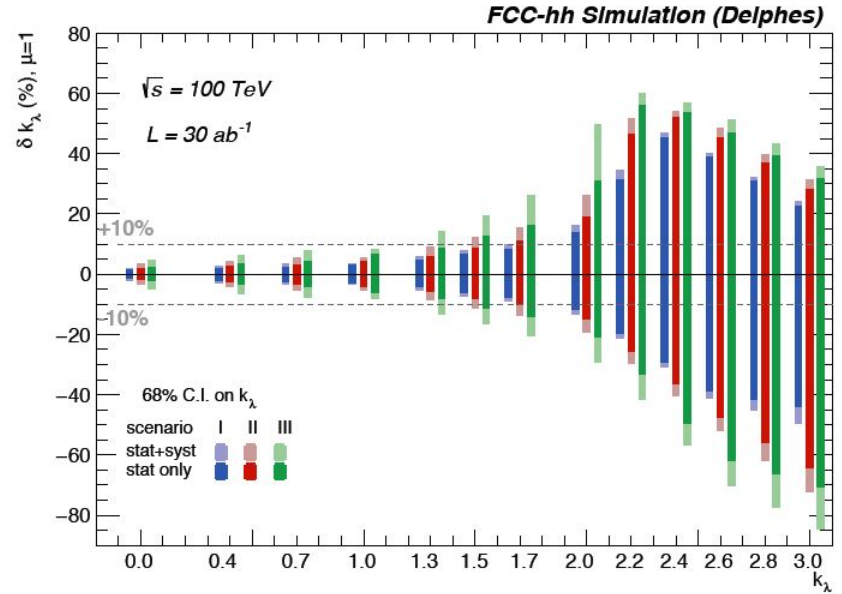
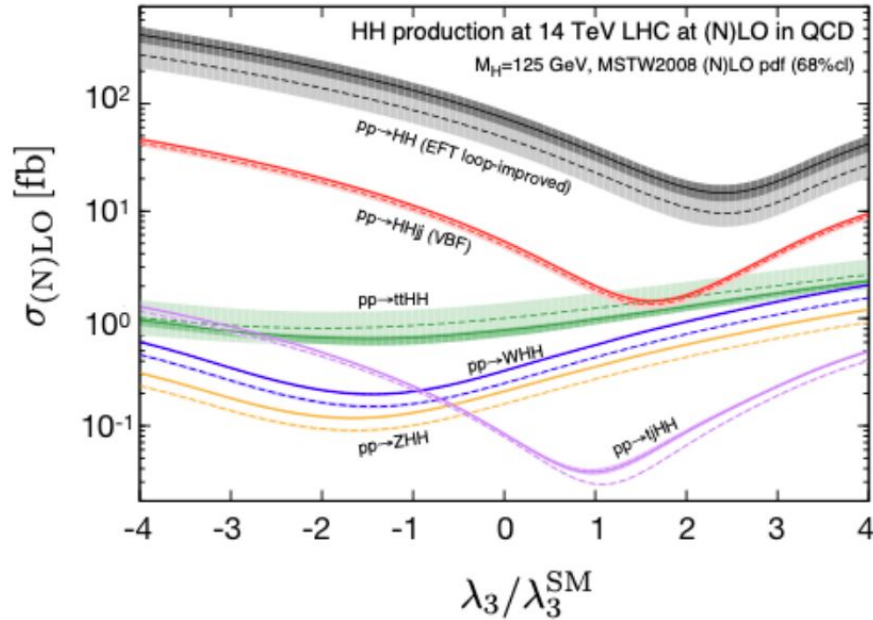
Table 3.25.: Overview of the harmonized event selection and categorization.

Previous projections for $\bar{b}b WW$ @ FCC-hh



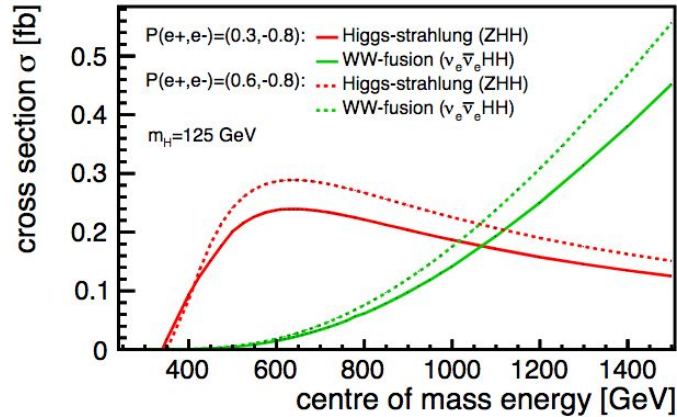
- $bbWW(2jlv)$ studied using BDT, with similar input variables as used here
- Achieved 40% precision (@68% CL) on κ

Di-Higgs cross-section dependence on κ_λ in pp -collisions

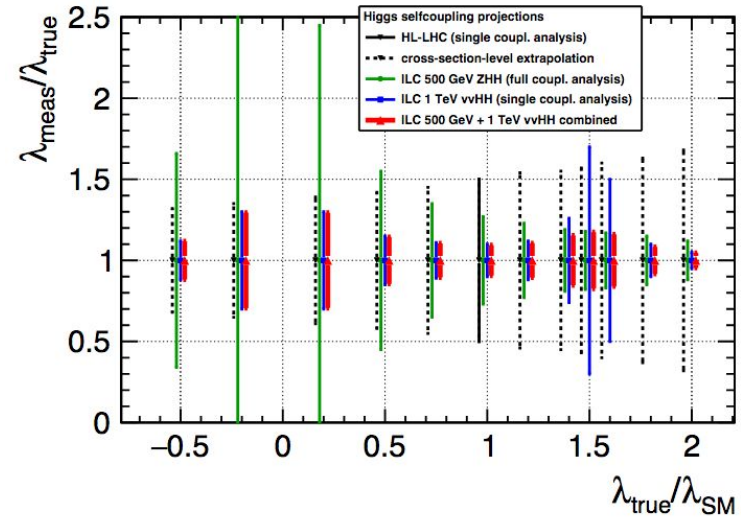


[arXiv:2004.03505v2](https://arxiv.org/abs/2004.03505v2)

Higgs self-coupling @ ILC



- Two production modes:
 - Higgsstrahlung, peaks ~ 500 GeV
 - WW-fusion, above ~ 1 TeV
 - \rightarrow need runs at both energies for maximum κ_λ precision



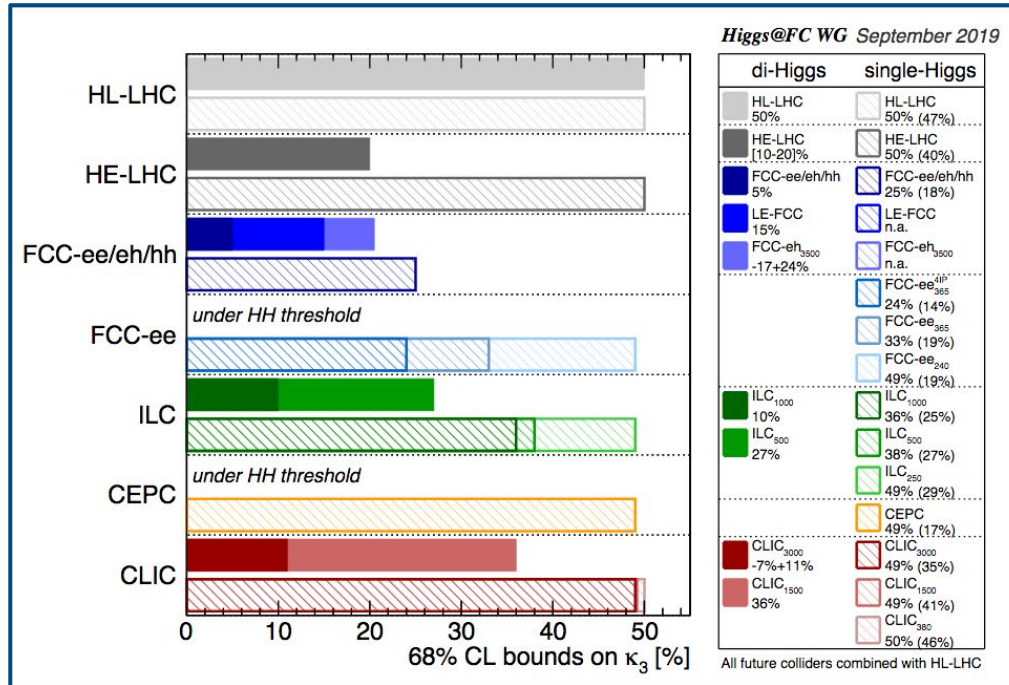
- Studied dominant channels $4b$ and $bbWW$
- Advantage of ee -collider: ZHH cross-section increases with κ_λ , hence better constraints at values $\kappa_\lambda > 1$ than pp -colliders

Higgs self-coupling @ muon collider

- Only $4b$

	3 TeV μ -coll. $L \approx 1 \text{ ab}^{-1}$	10 TeV μ -coll. $L = 10 \text{ ab}^{-1}$	14 TeV μ -coll. $L \approx 20 \text{ ab}^{-1}$	30 TeV μ -coll. $L = 90 \text{ ab}^{-1}$
	68% prob. interval			
$\delta\kappa_\lambda$	$[-0.27, 0.35] \cup [0.85, 0.94]$	$[-0.035, 0.037]$	$[-0.024, 0.025]$	$[-0.011, 0.012]$
	$\rightarrow [-0.15, 0.16] (2 \times L)$			

Why di-Higgs at FCC-hh?



[arXiv:1905.03764v2]

FCC-hh is the only perspective for a Higgs self-coupling precision measurement



Higgs self-coupling measurement is a clear benchmark channel for the FCC-hh