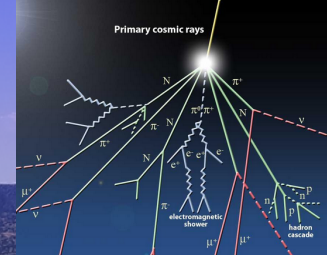




# XIII International Conference on New Frontiers in Physics

26 Aug - 4 Sep 2024, OAC, Kolymbari, Crete, Greece



## Tests and modifications of hadronic interactions in cosmic-ray showers

Jakub Vícha \*, Jiri Blazek, Nikolas Denner, Jan Ebr, Tanguy Pierog, Eva Santos, Petr Travnicek

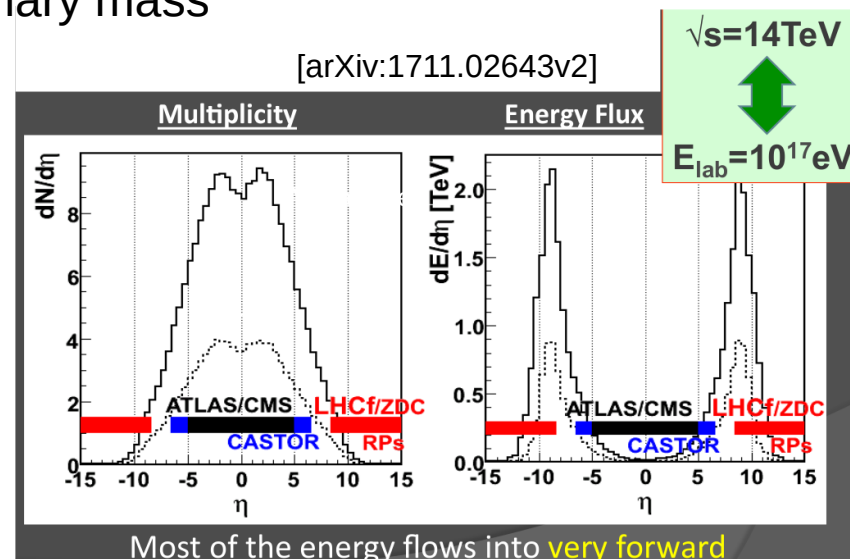
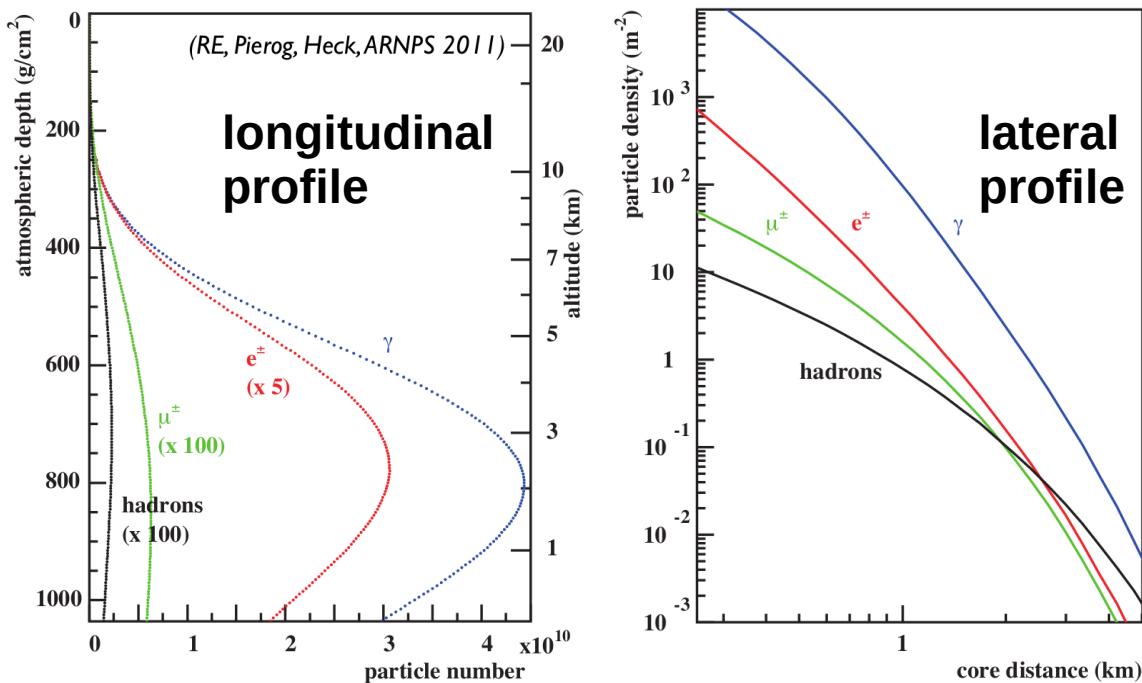
FZU - Institute of Physics of the Czech Academy of Sciences, Prague

\* vicha@fzu.cz



# Hadronic interactions in air showers

- Extrapolated to higher energies and different kinematic regions than accessible
    - systematic uncertainty on interpreted mass composition
  - Depth of shower maximum ( $X_{\max}$ )
  - Number of muons (decays of  $\pi^\pm$ )
- } sensitive to primary mass



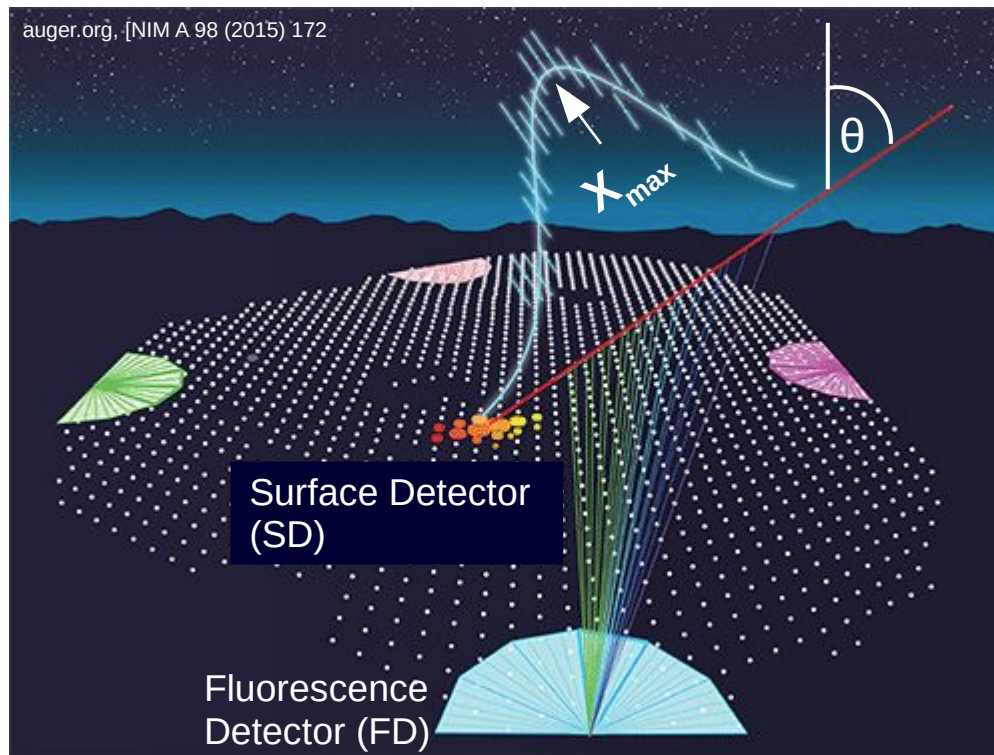
**Current models of hadronic interactions:**  
*EPOS-LHC, QGSJet II-04, Sibyll 2.3d*

# Observables relevant to hadronic interaction models

The Pierre Auger Observatory - *the best instrument to study HI in UHECR*

## SD signal

- **muon content**
  - from buried scintillators,  $\theta < 60^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$   
[Phys. Rev. D 91 (2015), 032003]
- **muon production depth**
  - for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$   
[Phys. Rev. D 90 (2014) 012012]
- **muon energy spectrum**
  - from attenuation with  $\theta$  and  $r$



## FD longitudinal profile

- estimation of **primary masses from  $X_{\max}$  fits**  
[PRD 90 (2014) 122006, PoS ICRC2023 (2023) 438]
- interpretation of  **$X_{\max}$  moments using  $\ln A$**   
[JCAP 02 (2013) 026, PoS (ICRC2023) 365]
- **p-air cross-section** from tail of  $X_{\max}$  distribution  
[Phys. Rev. Lett. 109 (2012) 062002, PoS ICRC2023 (2023) 438]
- **average shape** of longitudinal profiles  
[JCAP 03 (2019) 018]
- frequency of **anomalous showers**  
[EPJ Web of Conferences 144 (2017) 01009]

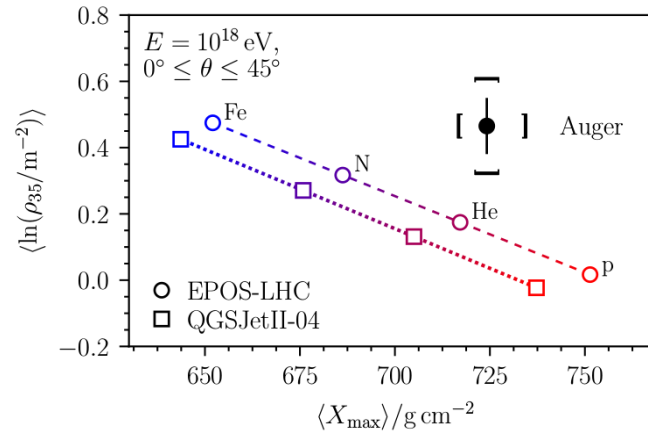
See talks of Tobias Schulz and Vitor de Souza for more detail

# Observables relevant to hadronic interaction models

## SD signal

- muon content
  - from buried scintillators,  $\theta < 60^\circ$
  - from  $N_{19}$ ,  $\theta > 65^\circ$
- muon production depth
  - for core distance  $r > 1500\text{m}$ ,  $\theta > 65^\circ$
- muon energy spectrum
  - from attenuation with  $\theta$  and  $r$

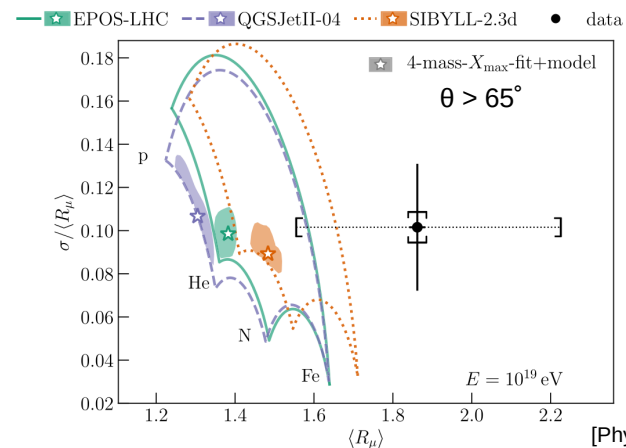
[Eur. Phys. J. C 80 (2020) 751]



## FD Longitudinal profile

- estimation of primary masses from  $X_{\text{max}}$  fits

- Problem to describe the size of the muon content - **factor ~1.3-1.6 !**
- Muon fluctuations consistent with data (no obvious problem in the first interaction)



[Phys. Rev. Lett. 126 (2021) 152002]

- longitudinal profiles
- frequency of anomalous showers



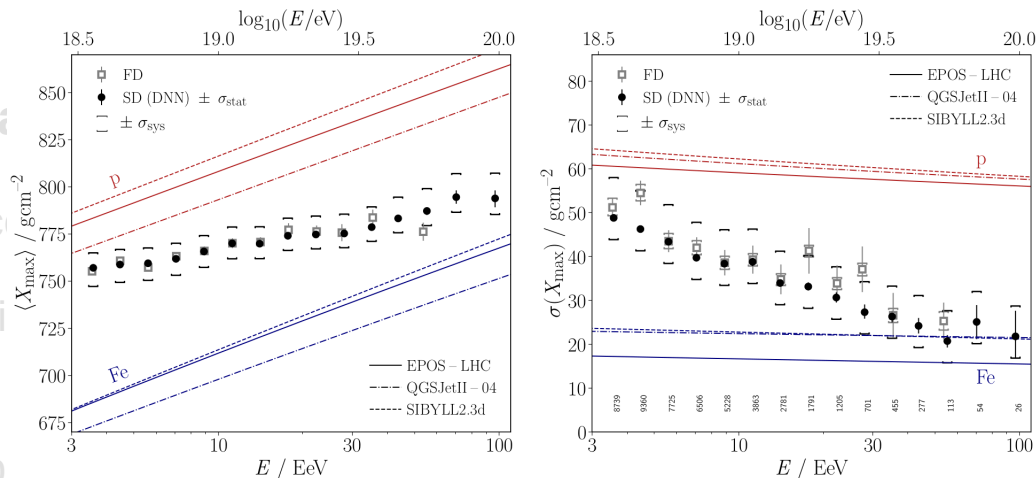
# Observables relevant to hadronic interaction models

SD signa

- muon c
- from sci
- from

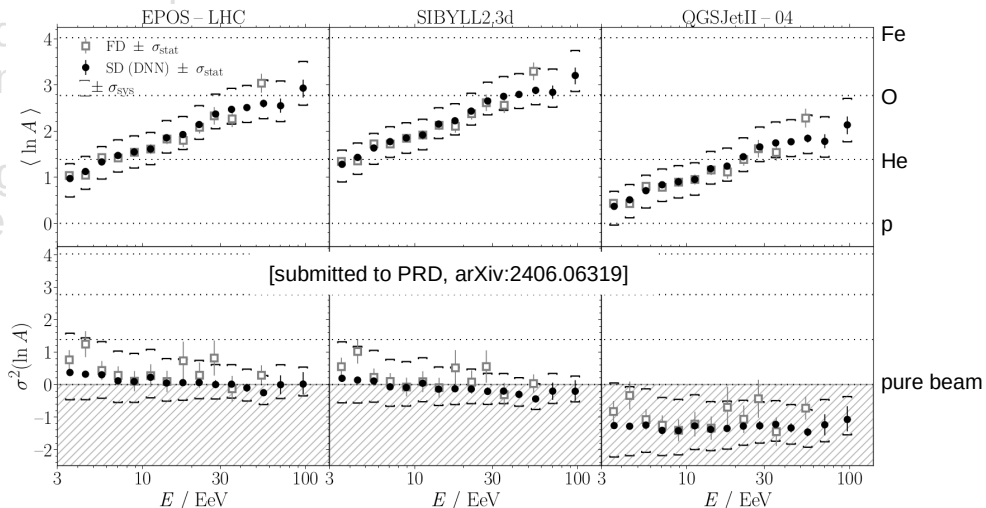
- muon p
- for core c
- r > 1500r

- muon ener
- from atte
- θ and r



## FD longitudinal profile

- estimation of primary masses from  $X_{\max}$  fits
- interpretation of  $X_{\max}$  moments using  $\ln A$



$$\langle \ln A \rangle = \frac{\langle X_{\max} \rangle - \langle X_{\max} \rangle_p}{f_E}$$

$$\sigma_{\ln A}^2 = \frac{\sigma^2(X_{\max}) - \sigma_{\text{sh}}^2(\langle \ln A \rangle)}{b \sigma_p^2 + f_E^2}$$

[JCAP 02 (2013) 026]

• frequency of anomalous showers

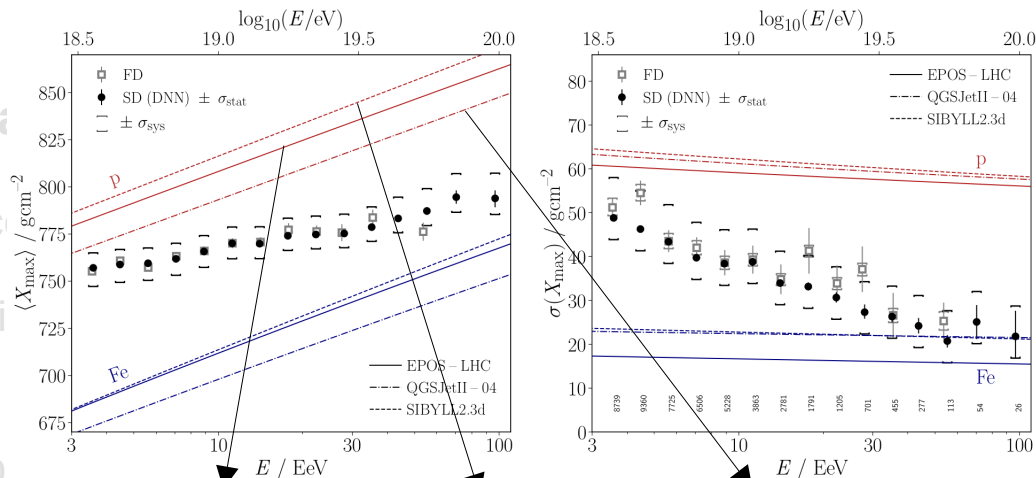
# Observables relevant to hadronic interaction models

SD signa

- muon c
- from sci
- from

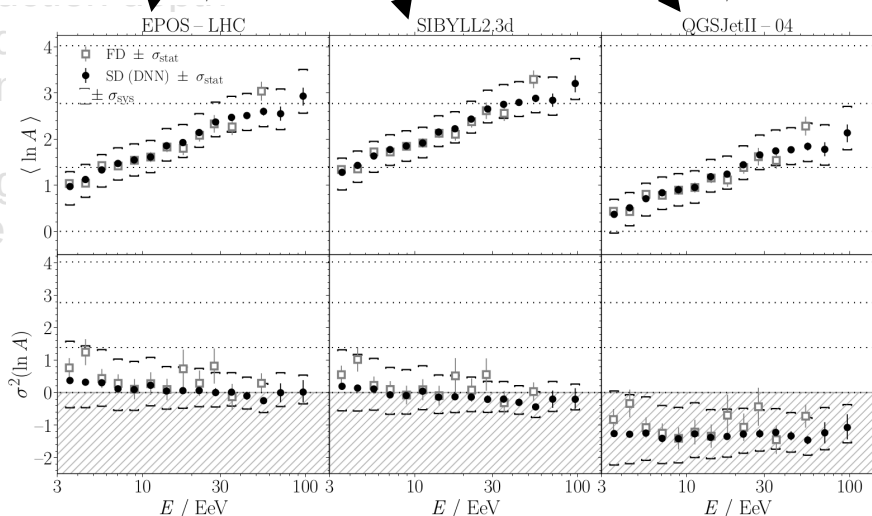
- muon p
- for core c
- r > 1500r

- muon energ
- from atte
- $\theta$  and r



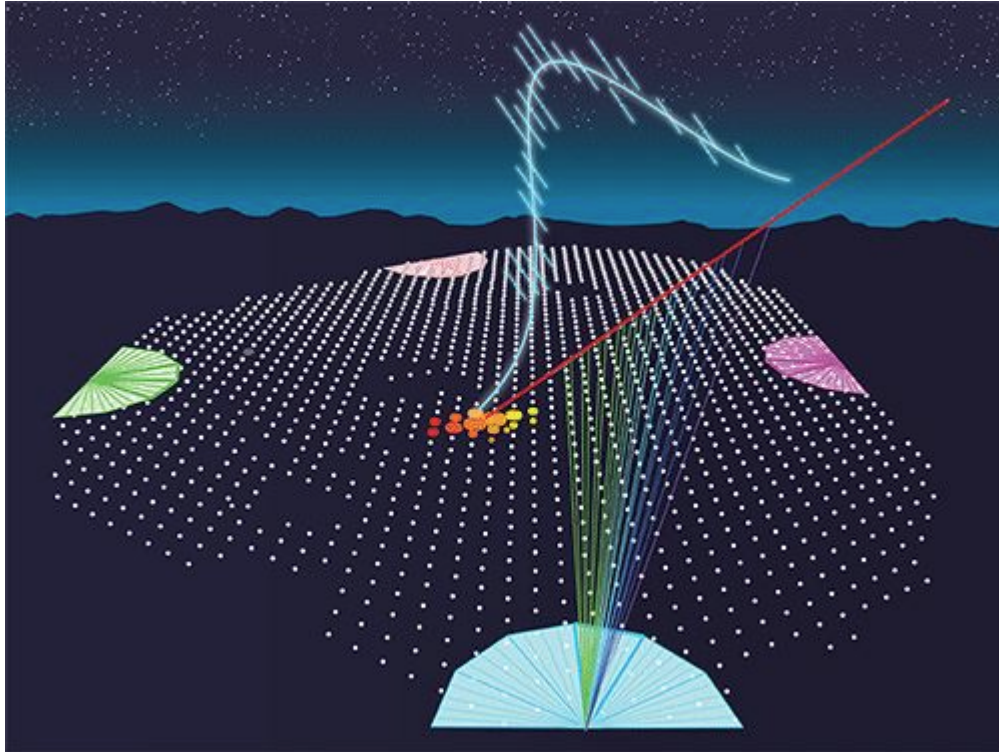
## FD longitudinal profile

- estimation of primary masses from  $X_{\max}$  fits
- interpretation of  $X_{\max}$  moments using  $\ln A$
- p-air cross-section from tail of  $X_{\max}$  distribution



- Strong dependence on the MC  $X_{\max}$  scale
- Indication of too shallow predictions of  $\langle X_{\max} \rangle$  for all three models !

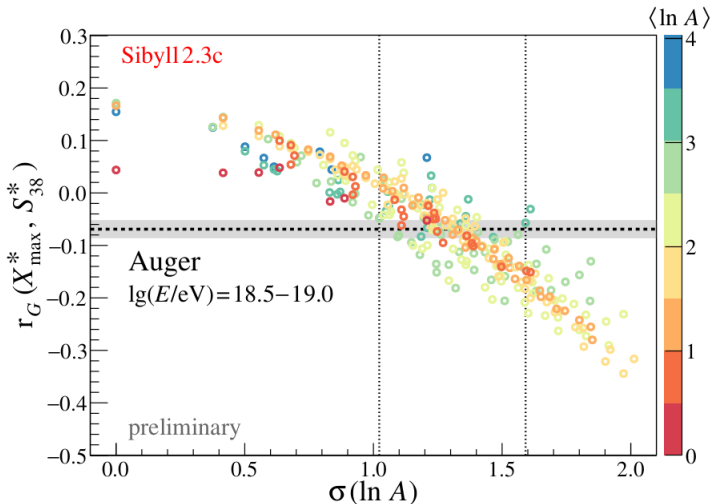
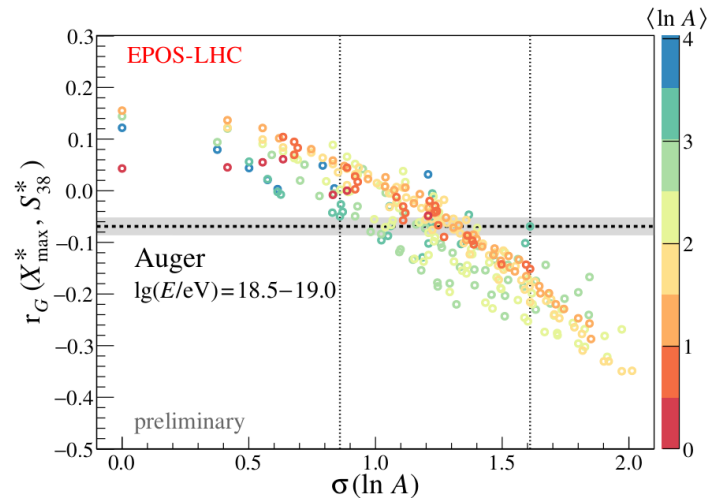
# Combining SD and FD observables



## Ground signal + Longitudinal profile

- correlation between  $X_{\max}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}}$
- applying shower-universality approach  $\rightarrow R_{\text{had}}$
- 2-dim distributions  $[S(1000), X_{\max}] \rightarrow R_{\text{had}}(\theta), \Delta X_{\max}$

# Combining SD and FD observables

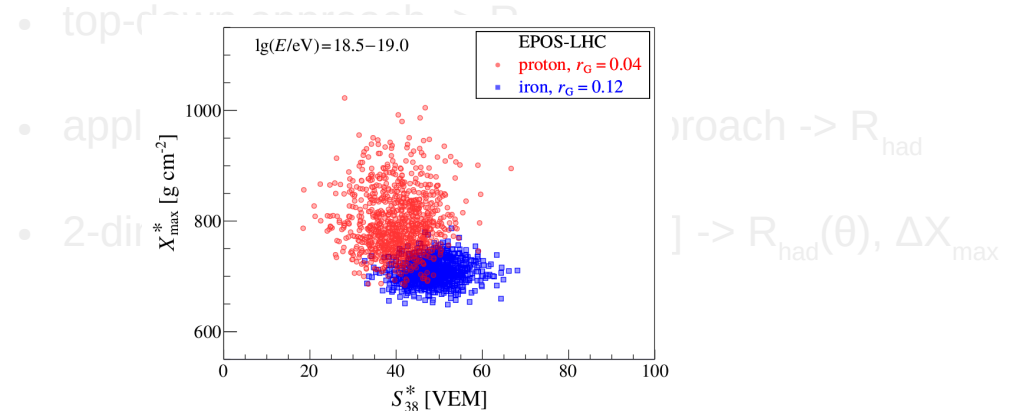


## Ground signal + Longitudinal profile

- correlation between  $X_{\max}$  and  $S(1000)$

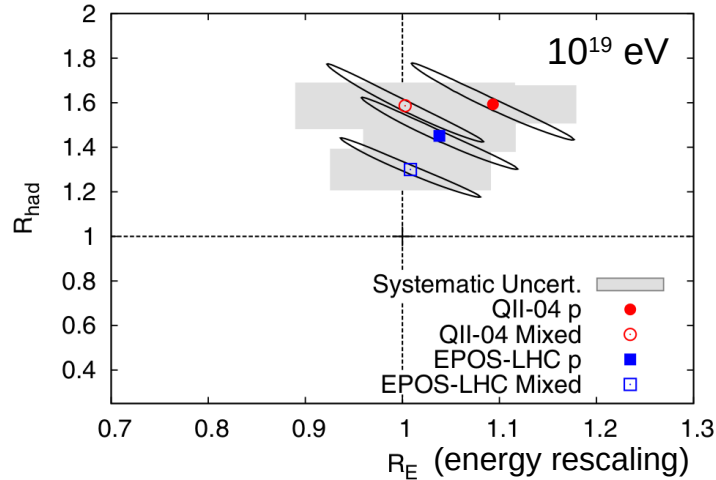
[Phys. Lett. B 762 (2016) 288]

[PoS(ICRC2019)482]

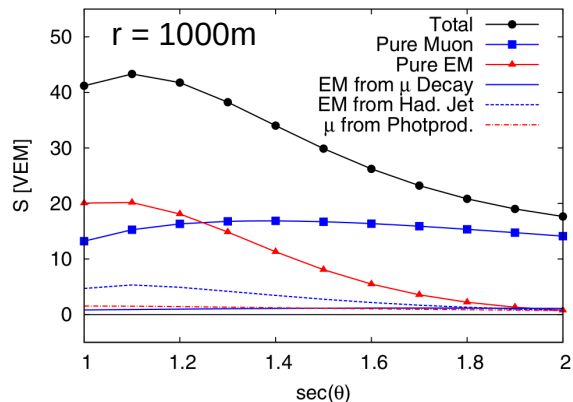


- ~Model-independent estimator of spread of beam masses
- Tension with light masses from  $X_{\max}$  fits for QGSJet II-04 (**too shallow  $X_{\max}$  scale**)

# Combining SD and FD observables



$$S_{\text{resc}}(R_E, R_{\text{had}})_{i,j} \equiv R_E S_{\text{EM},i,j} + R_{\text{had}} R_E^\alpha S_{\text{had},i,j}$$



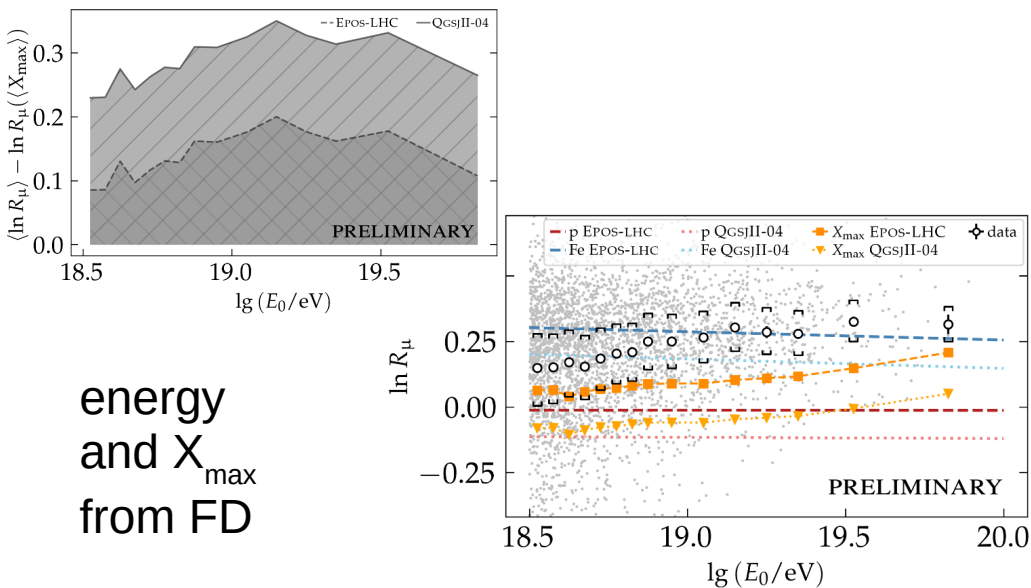
## Ground signal + Longitudinal profile

- correlation between  $X_{\text{max}}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}} \sim \mathbf{1.3 - 1.6 !}$   
[Phys. Rev. Lett. 117 (2016) 192001]
- applying shower-universality approach  $\rightarrow R_{\text{had}}$
- 2-dim distributions  $[S(1000), X_{\text{max}}] \rightarrow R_{\text{had}}(\theta), \Delta X_{\text{max}}$

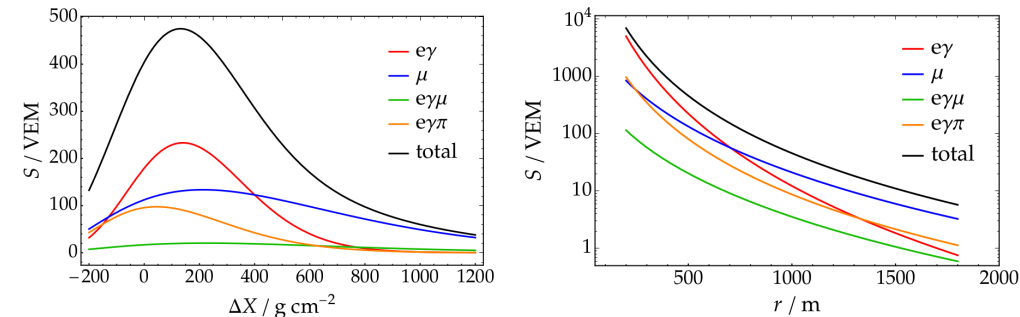
- Mass from measured  $X_{\text{max}}$  - depends on MC  $X_{\text{max}}$  scale
- Strong dependence on energy scale



# Combining SD and FD observables



$$S_{\text{tot}} \simeq S_{e\gamma} + R_{\mu} (S_{\mu} + S_{e\gamma(\mu)} + S_{e\gamma(\pi)})$$



## Ground signal + Longitudinal profile

- correlation between  $X_{\max}$  and  $S(1000)$
- top-down approach  $\rightarrow R_{\text{had}}$
- applying shower-universality approach  $\rightarrow R_{\text{had}} \sim \mathbf{1.1 - 1.3}$  [PoS(ICRC2023)339, arXiv:2405.03494]
- 2-dim distributions  $[S(1000), X_{\max}] \rightarrow R_{\text{had}}(\theta), \Delta X_{\max}$

- $R_{\text{had}}$  smaller than in top-down approach
- $\sim$  Insensitive to the MC  $X_{\max}$  scale

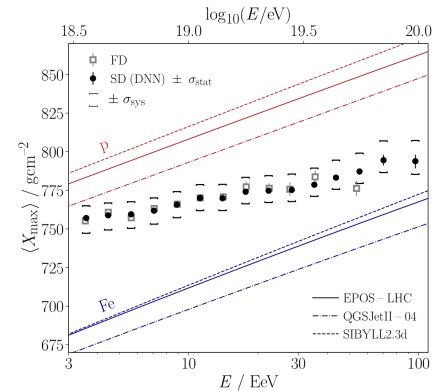
# Mass composition & tests of hadronic interactions

[submitted to PRD, arXiv:2406.06319]

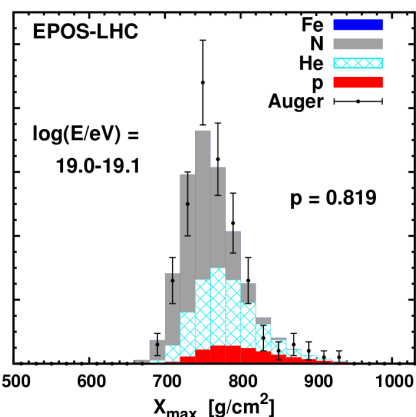
[Phys. Rev. D 90 (2014) 122006]

[Phys. Rev. Lett. 117 (2016) 192001]

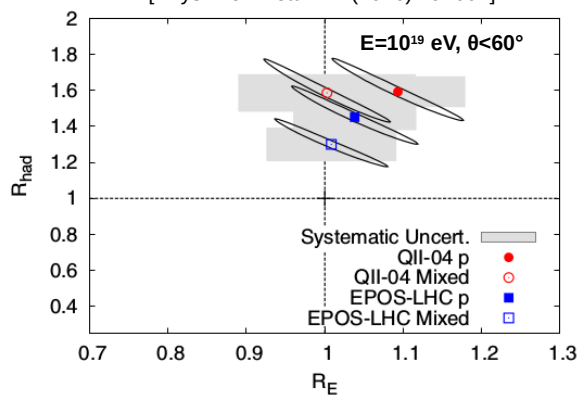
[Phys. Lett. B 762 (2016) 288]



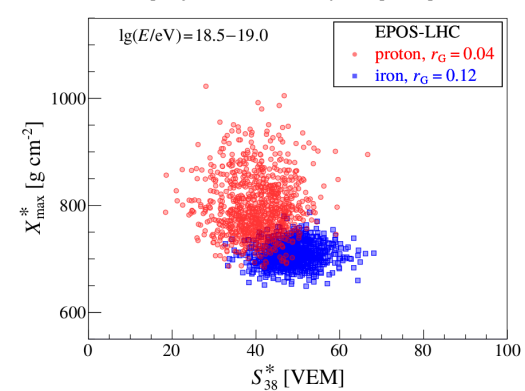
MC  $X_{\max}$  scale ?



Prim. fraction fit



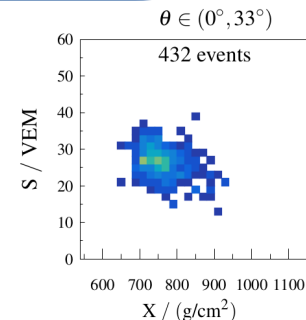
Deficit in MC hadronic signal



~ model-independent estimation of beam mixing from  $[X_{\max}, S(1000)]$  correlation

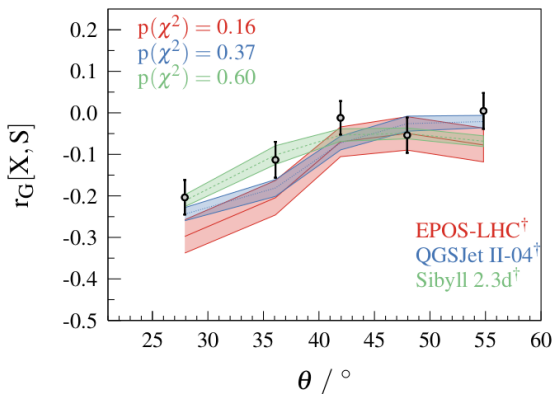
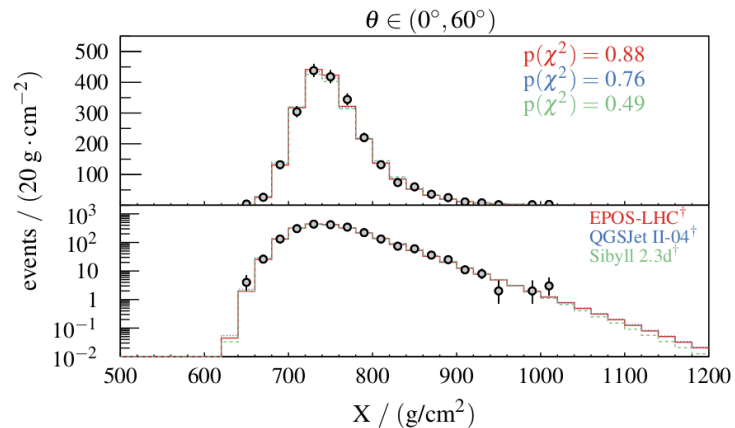
[Phys. Rev. D 109 (2024) 102001]

Mass composition fit of observed  $[X_{\max}, S(1000)](\theta)$  distributions with free modification of MC predictions **not only of hadronic signal but also of  $X_{\max}$**



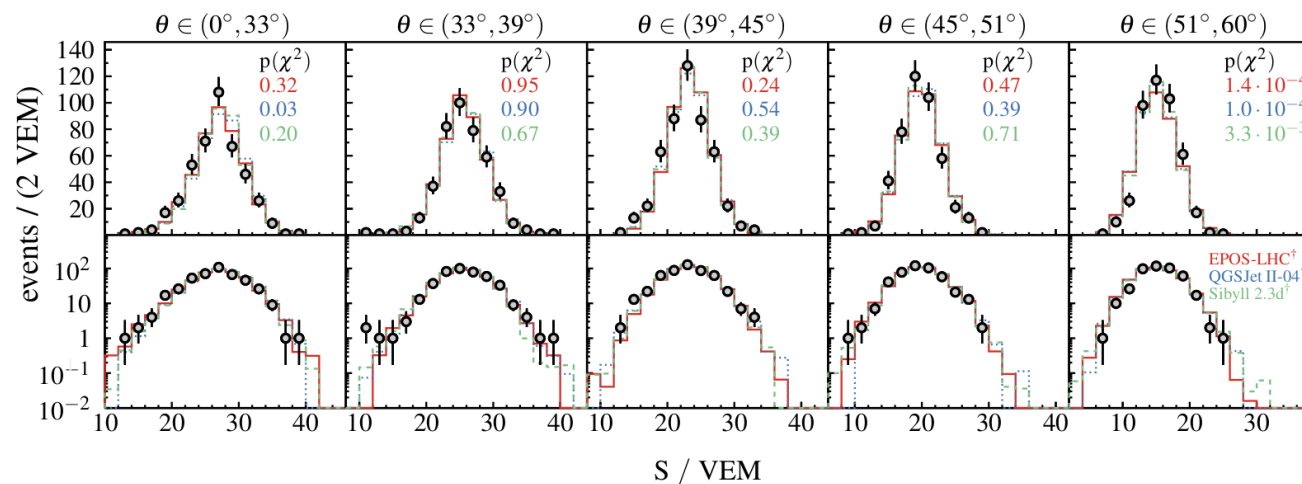
# Improvement in data description

[Phys. Rev. D 109 (2024) 102001]



*p-values of fits from MC-MC tests > 10% for all three models*

$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
none	2022.9	4508.0	2496.5
$\Delta X_{\max}$	738.6	1674.8	1015.7
$R_{\text{had}} = \text{const.}$	489.2	684.4	521.6
$R_{\text{had}}(\theta)$	489.2	673.9	517.6
$R_{\text{had}} = \text{const. and } \Delta X_{\max}$	452.2	486.7	454.2
$R_{\text{had}}(\theta)$ and $\Delta X_{\max}$	451.9	476.3	451.6



Significant improvement  $>5\sigma$  using  $R_{\text{had}}$  and  $\Delta X_{\max}$  (Likelihood ratio tests for nested model using Wilks' theorem)

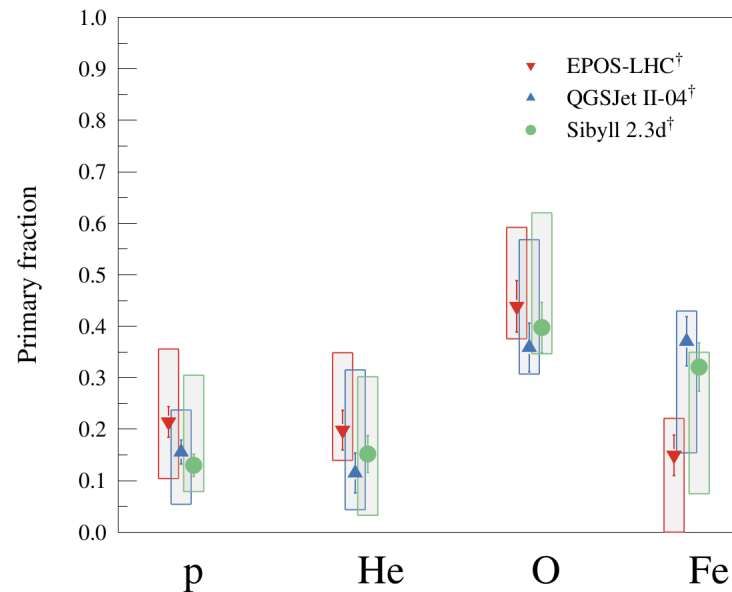
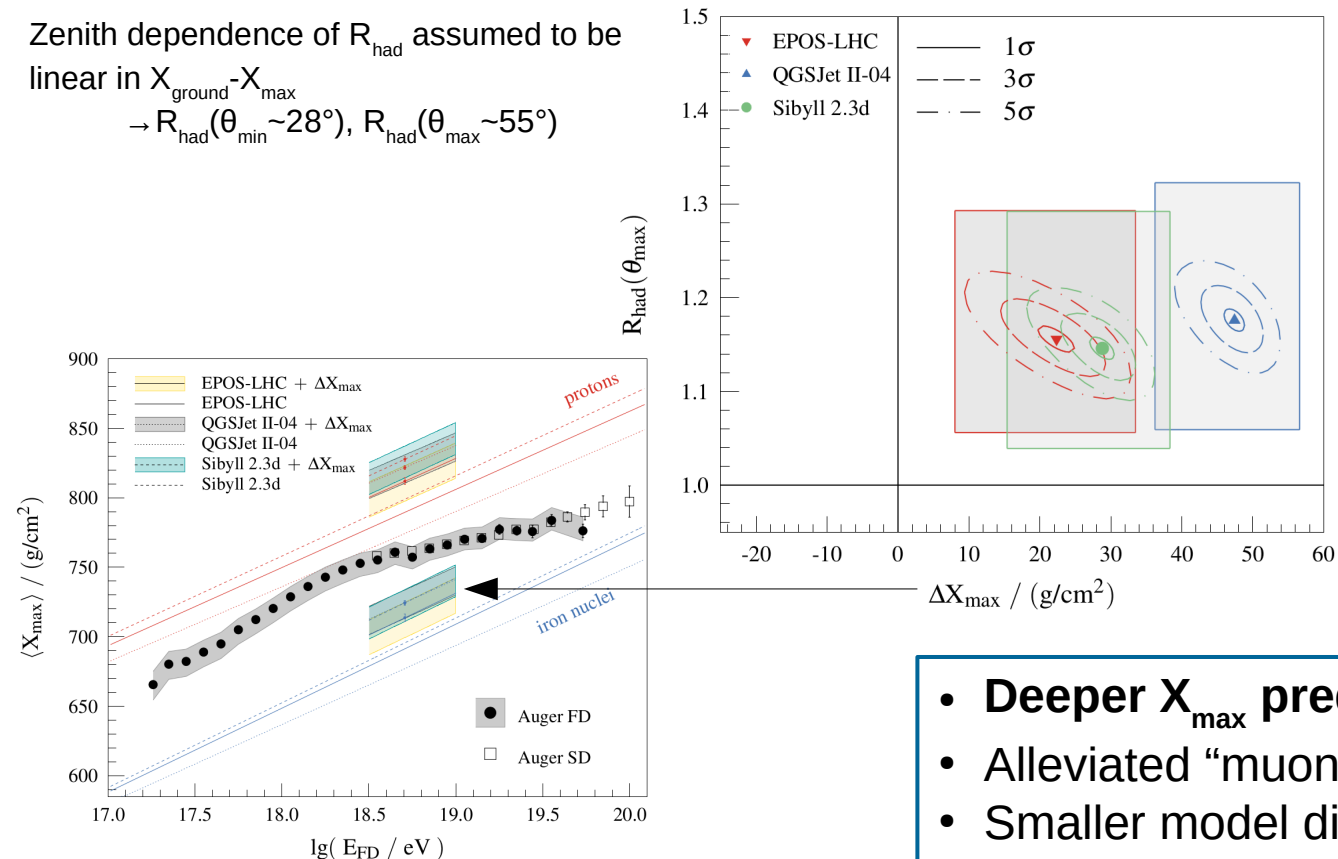
# Fitted parameters

[Phys. Rev. D 109 (2024) 102001]

Zenith dependence of  $R_{\text{had}}$  assumed to be

linear in  $X_{\text{ground}} - X_{\text{max}}$

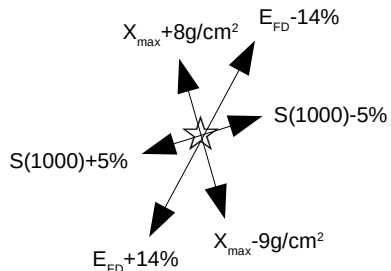
$$\rightarrow R_{\text{had}}(\theta_{\text{min}} \sim 28^\circ), R_{\text{had}}(\theta_{\text{max}} \sim 55^\circ)$$



- **Deeper  $X_{\text{max}}$  predictions for all models !**
- Alleviated “muon problem“ to ~15-25%
- Smaller model differences in mass composition

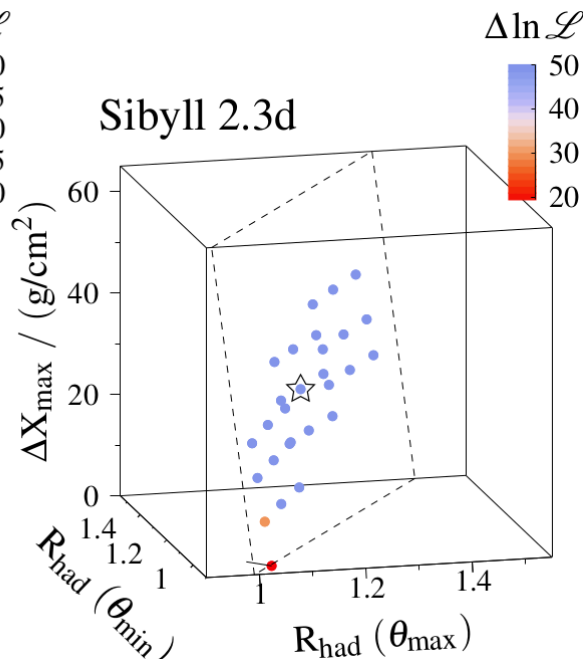
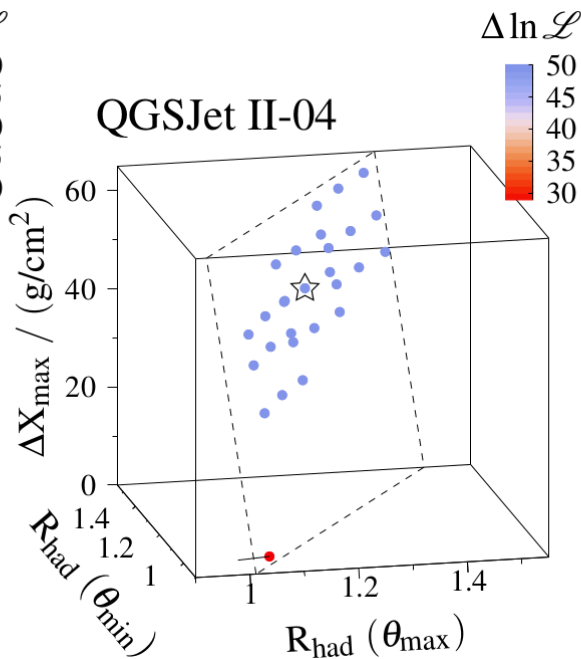
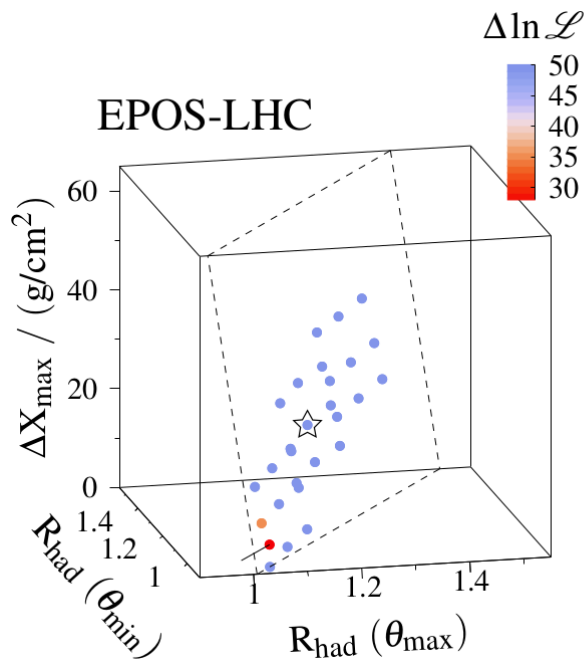
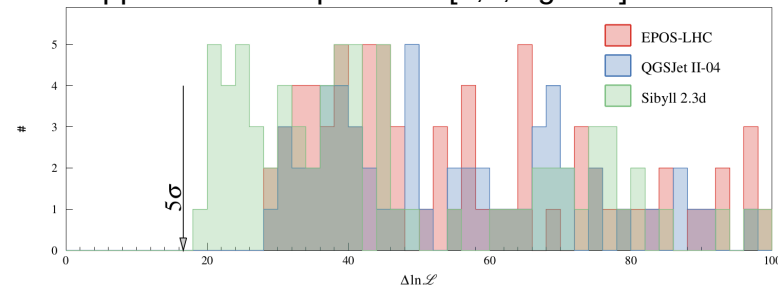
# Scanning in combinations of experimental systematics

[Phys. Rev. D 109 (2024) 102001]



Significance of improvement  
of data description always  
above  $5\sigma$

Denser scan in the region of the closest  
approach of the plane to  $[1,1,0 \text{ g/cm}^2]$





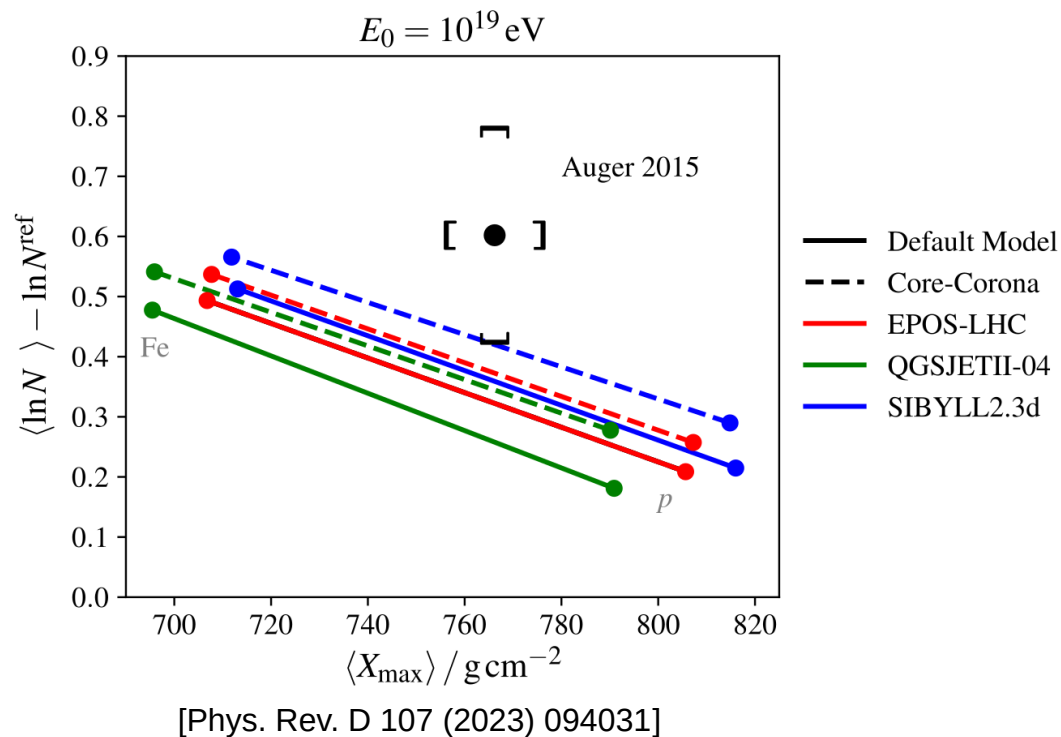
# Summary of tests of models using Auger data

test	energy / EeV	$\theta / ^\circ$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
$X_{\max}$ moments	$\sim 3$ to 50	0 to 80	no tension <span style="color: green;">■</span>	tension <span style="color: red;">■</span>	no tension (2.3c) <span style="color: green;">■</span>
$X_{\max}:S(1000)$ correlation	3 to 10	0 to 60	no tension <span style="color: green;">■</span>	tension <span style="color: red;">■</span>	no tension (2.3c) <span style="color: green;">■</span>
mean muon number	$\sim 10$	$\sim 67$	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>
mean muon number	0.2 to 2	0 to 45	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	—
fluctuation of muon number	4 to 40	$\sim 67$	no tension <span style="color: green;">■</span>	no tension <span style="color: green;">■</span>	no tension <span style="color: green;">■</span>
muon production depth	20 to 70	$\sim 60$	tension <span style="color: red;">■</span>	no tension <span style="color: green;">■</span>	—
$S(1000)$	$\sim 10$	0 to 60	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	—
$[X_{\max}, S(1000)]$	3 to 10	0 to 60	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>	tension <span style="color: red;">■</span>

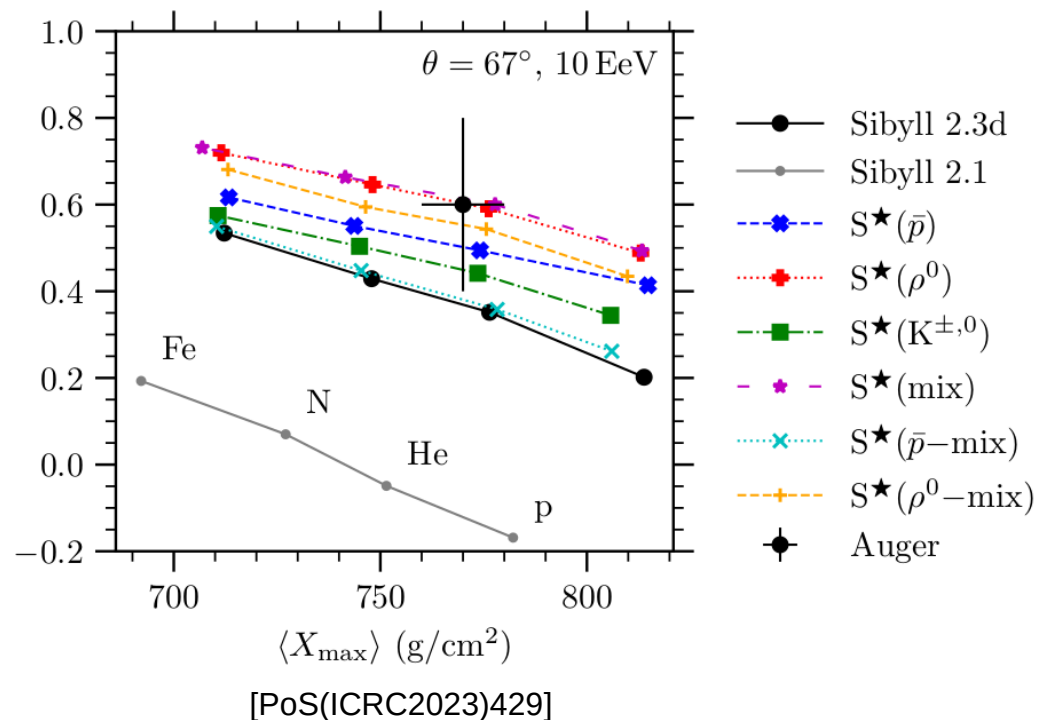
- All models have problems ...
- A need to describe consistently both  $X_{\max}$  and ground signal  
- issue in both observables !

# Adding muons ~ without changing $X_{\max}$

Core-corona model - collective statistical hadronization  $\rightarrow$  EPOS 4

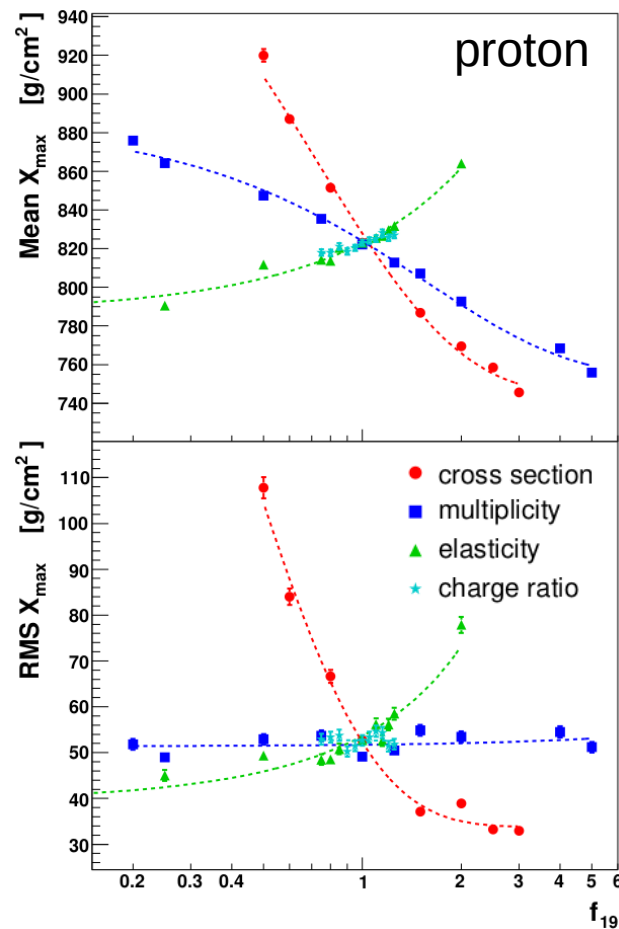


Sibyll \* - artificial enhancement of muons

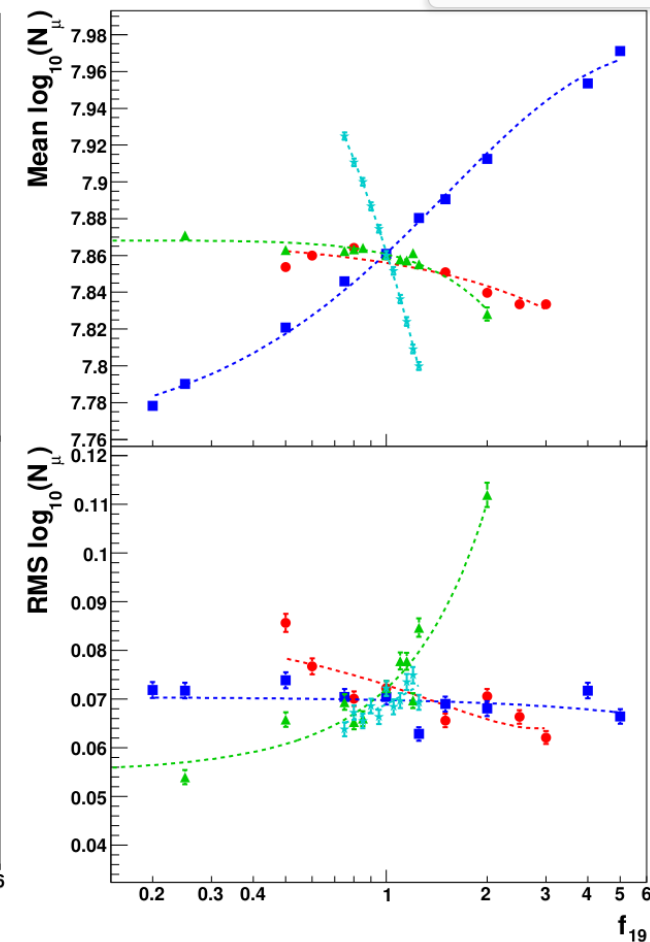


# Modifications of hadronic interactions

- 1D CONEX simulations
- Sibyll 2.1 @  $10^{19.5}$  eV
- Cross-section modification, or resampling of produced particles
- Energy threshold for modifications  $10^{15}$  eV



[Phys. Rev. D 83 (2011) 054026]



# Towards more complex explanation: MOCHI

*MO*modified *C*haracteristics of *H*adronic *I*nteractions

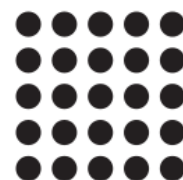
- CONEX in CORSIKA: 3D information
- Modification factors in **cross-section**, **multiplicity** and **elasticity**



0.8

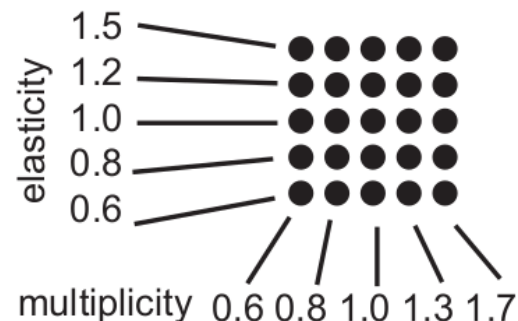


1.0



1.2

cross-section



- **MOCHI library:**

- Sibyll 2.3d
- energy  $10^{18.7}$  eV
- protons and iron nuclei
- 5 zenith angles
- 1000 showers per „bin“
- 750 000 showers (~200 TB, ~250y CPU time)

*See [PoS(ICRC2023)245]  
for more detail*

# Range of modifications and thresholds

## Cross-section ( $E_{\text{thr}} = 10^{16}$ eV)

- well constrained for p-p at LHC to a few %
- unc. in conversion to p-A limited by CMS p-Pb measurement

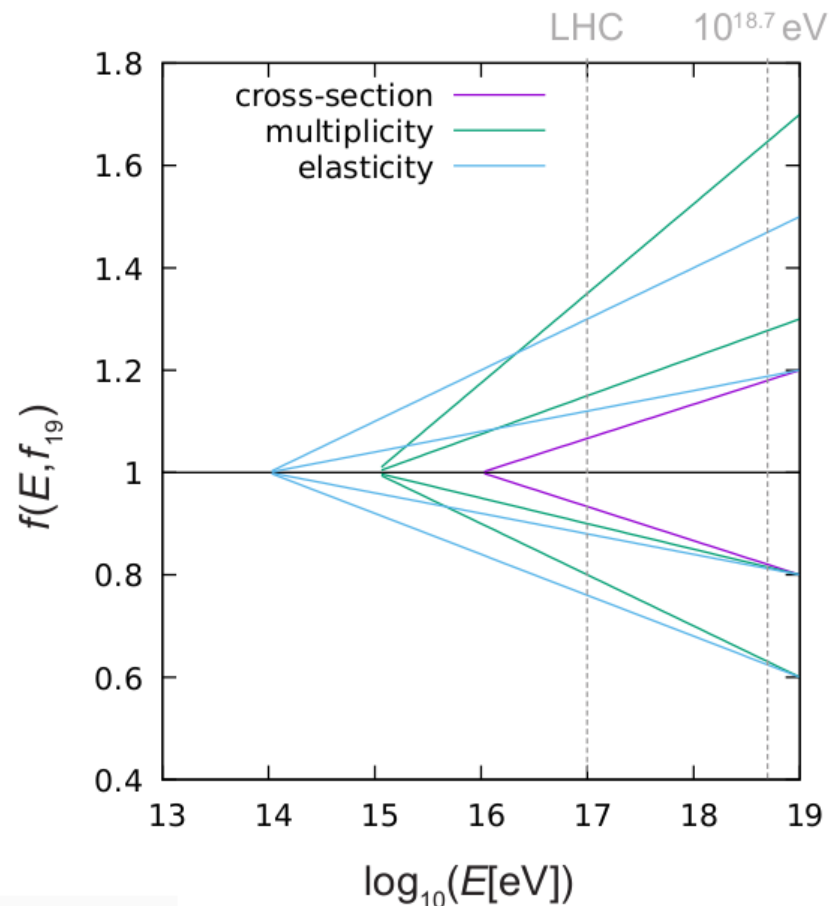
## Multiplicity ( $E_{\text{thr}} = 10^{15}$ eV)

- no p-A data, limited rapidity coverage

## Elasticity ( $E_{\text{thr}} = 10^{14}$ eV)

- difficult at accelerators, limits from nuclear emulsion chambers
- recent LHCf neutron elasticity measurement?
- range of modifications limited by internal consistency

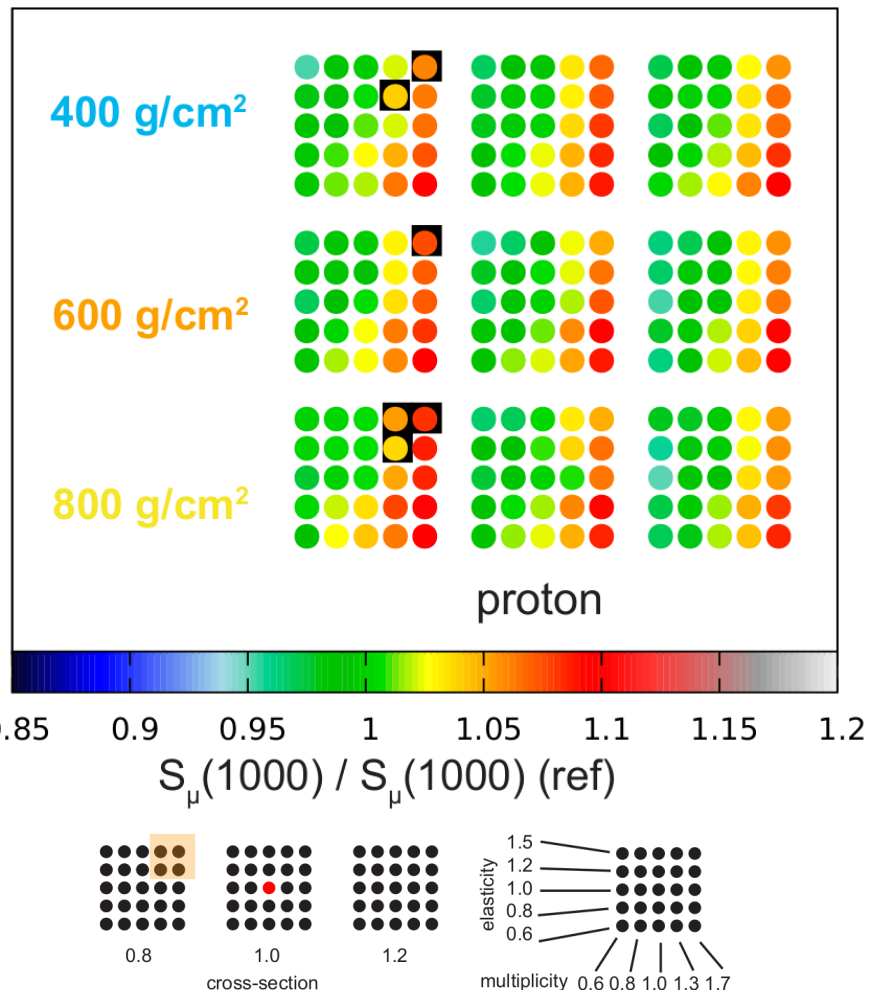
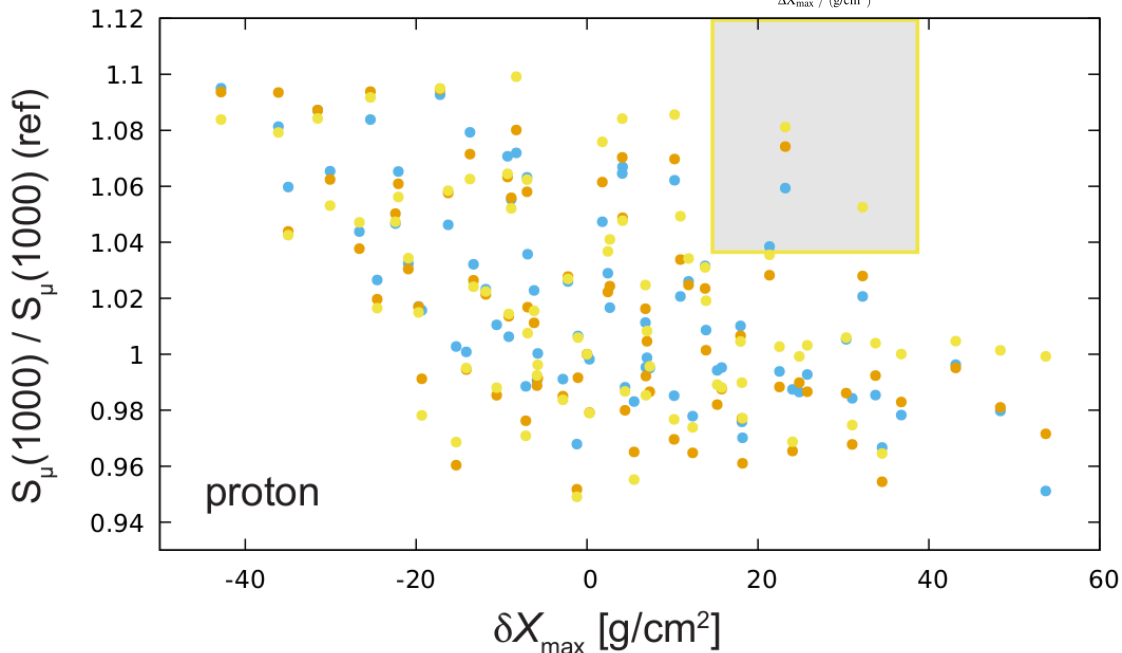
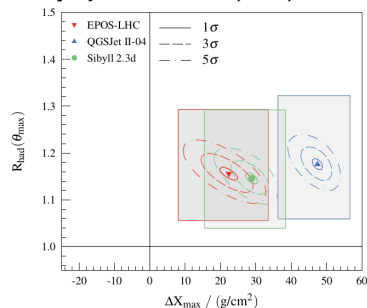
$$f(E, f_{19}) = 1 + (f_{19} - 1) \cdot \frac{\log_{10}(E/E_{\text{thr}})}{\log_{10}(10 \text{ EeV}/E_{\text{thr}})}$$



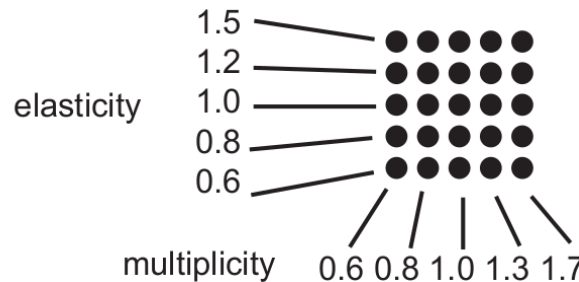
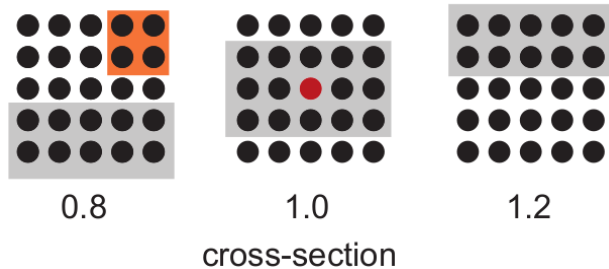
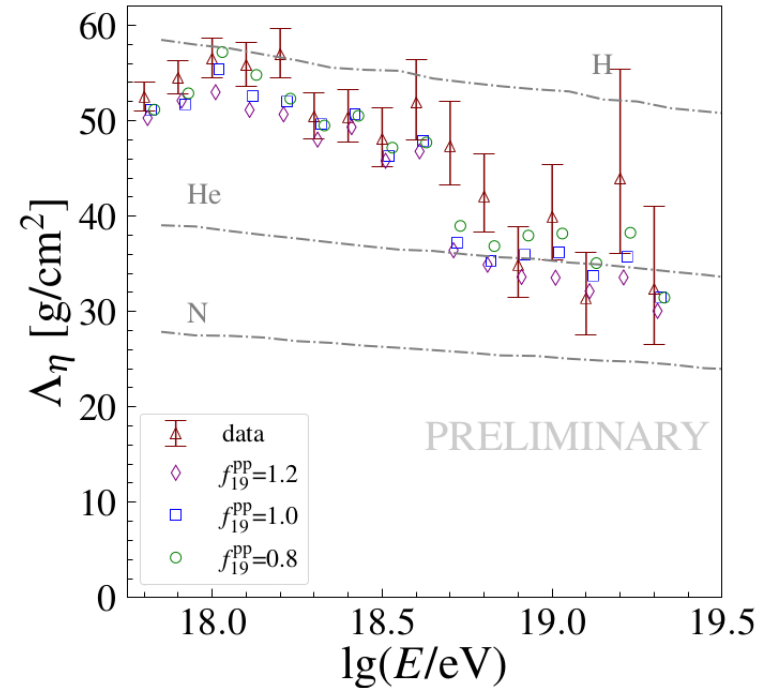
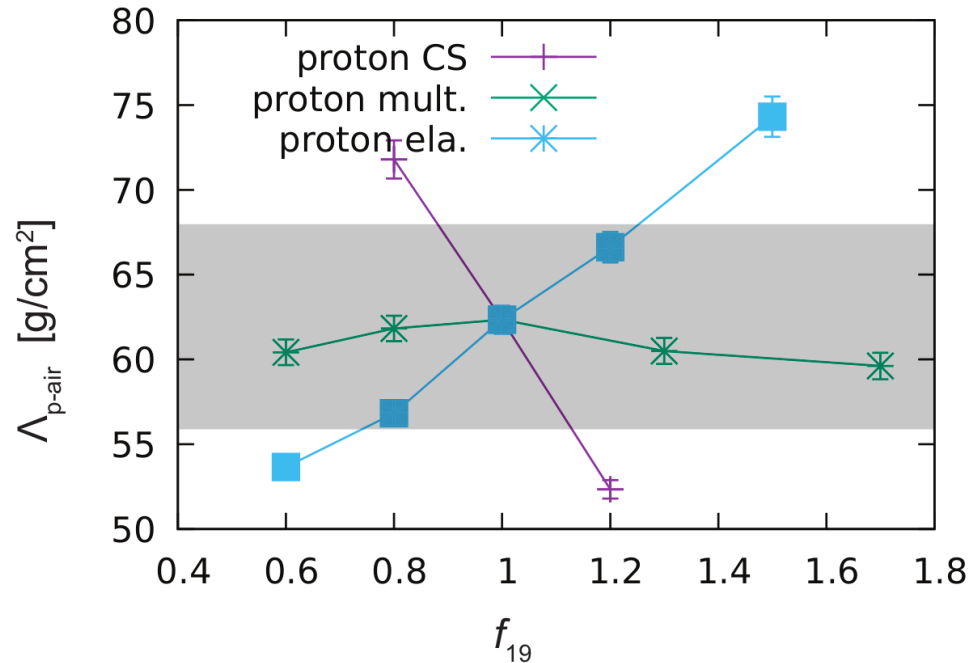


# Comparison with Auger results

[Phys. Rev. D 109 (2024) 102001]

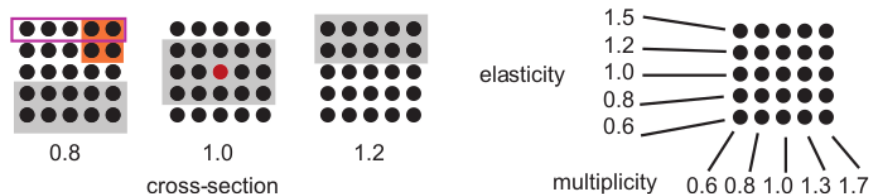
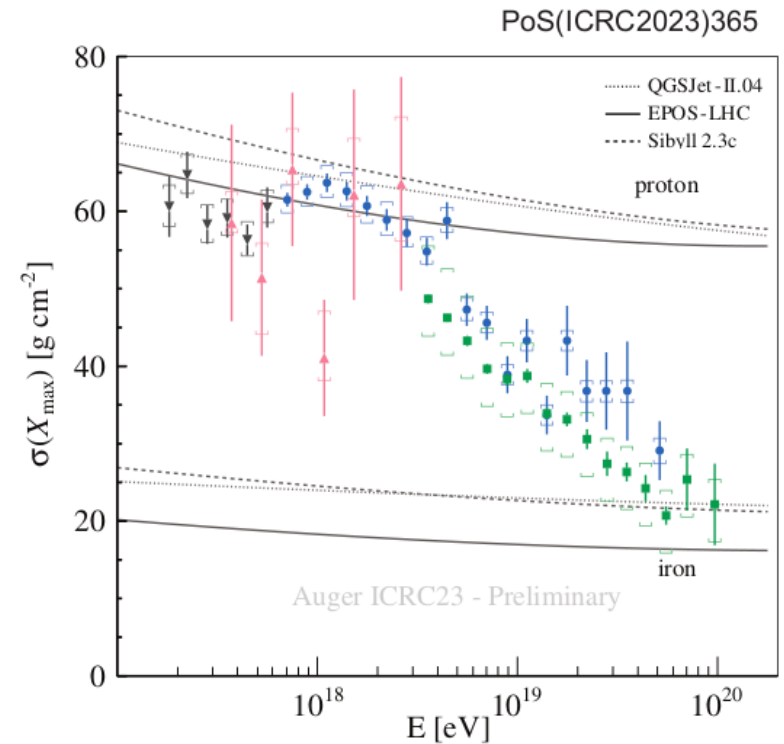
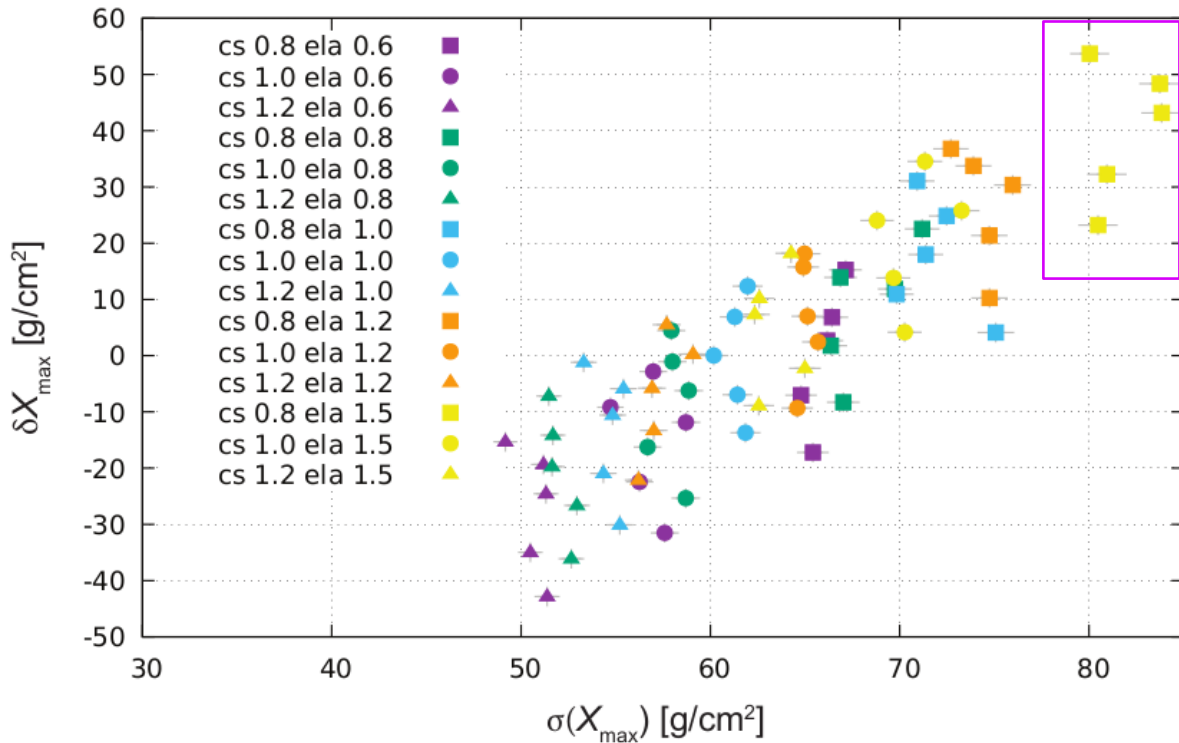


# Effect on tail of $X_{\max}$ distribution



Slope of  $X_{\max}$  tail distribution for protons too constrained by Auger data

# Effect on $X_{\max}$ fluctuations



Lower cross-section and high elasticity leads to very high  $X_{\max}$  fluctuations that may be difficult to reconcile with data

# Conclusions

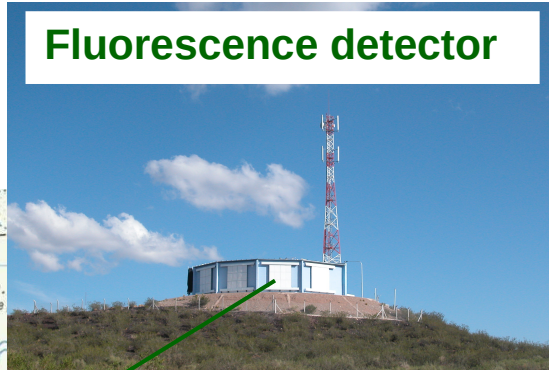
- We are facing **change of mass-composition paradigm** → we should start seriously consider “disappointing“ heavy scenario of ultra-high energy cosmic rays
- Models of hadronic interactions proven to fail to describe air-shower data  $> 5\sigma$ 
  - possible underestimation of experimental systematics ruled out
- Modifications of macro-parameters (cross-section, multiplicity, elasticity) of hadronic interactions does not seem (preliminary) to be enough
  - different approach is needed: modifying micro parameters (production rates and energy spectra of secondary particles) or (not exclusively!) revisions of models of hadronic interactions (EPOS 4, QGSJet III?, ...)
- **p + O run** at LHC is extremely important for decrease of systematic uncertainties on mass composition of UHECR
- **AugerPrime** (2024-2035) will be the best test facility so far for hadronic interactions at  $\sqrt{s} \sim 100$  TeV

# Backup slides

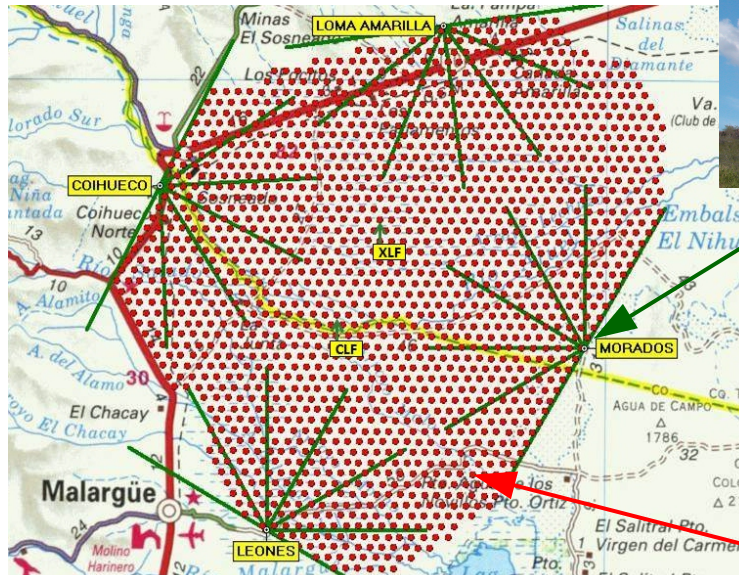


# Hybrid detection at the Pierre Auger Observatory

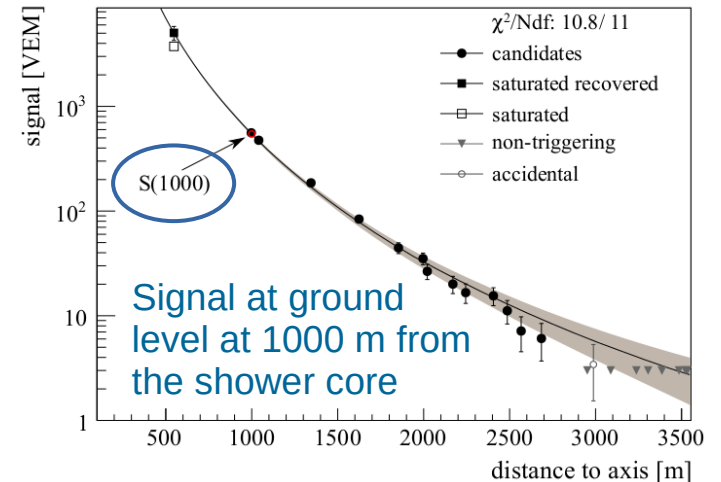
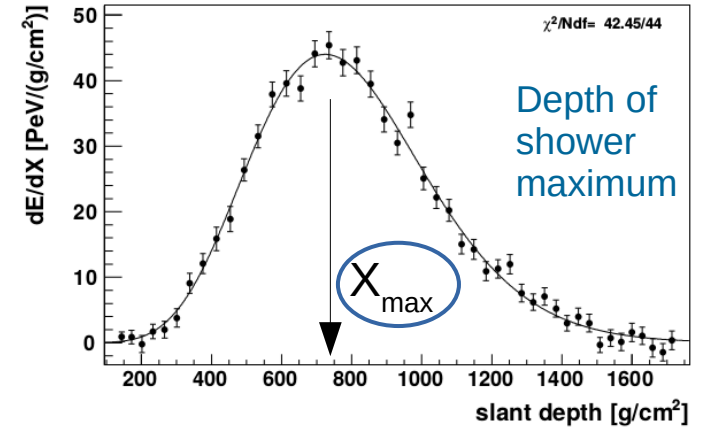
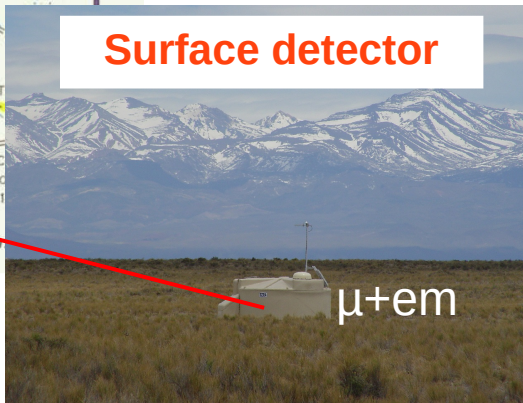
Fluorescence detector



[Nucl. Instrum. Meth. A 798 (2015) 172]



Surface detector



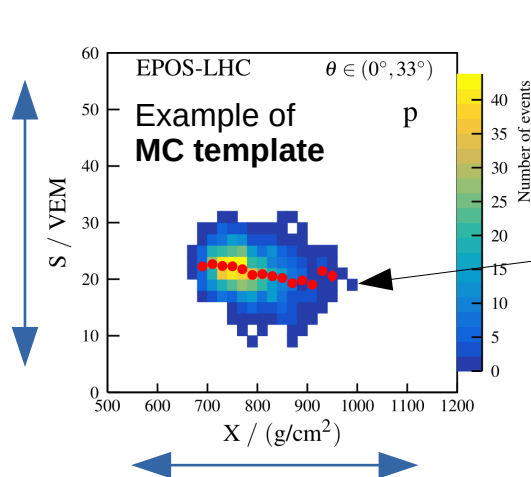
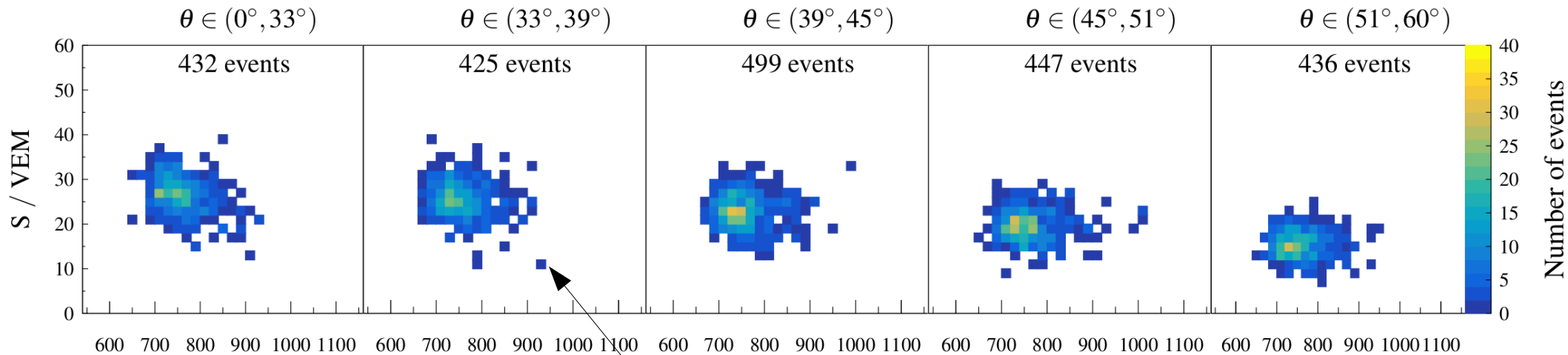
Auger data:  
2239 HQ events for  $10^{18.5-19.0}$  eV

# Method

$$S = S(1000) \left( \frac{E^{\text{ref}}}{E_{\text{FD}}} \right)^{1/B}$$

$$X = X_{\text{max}} + D \lg \left( \frac{E^{\text{ref}}}{E_{\text{FD}}} \right)$$

$E^{\text{ref}} = 10^{18.7}$  eV



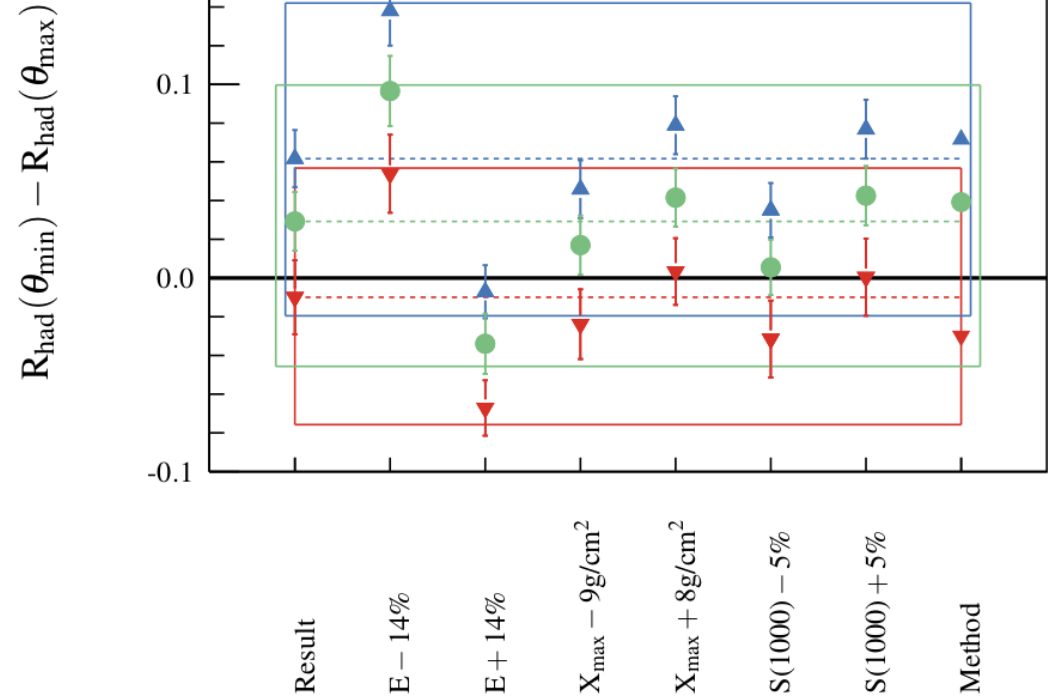
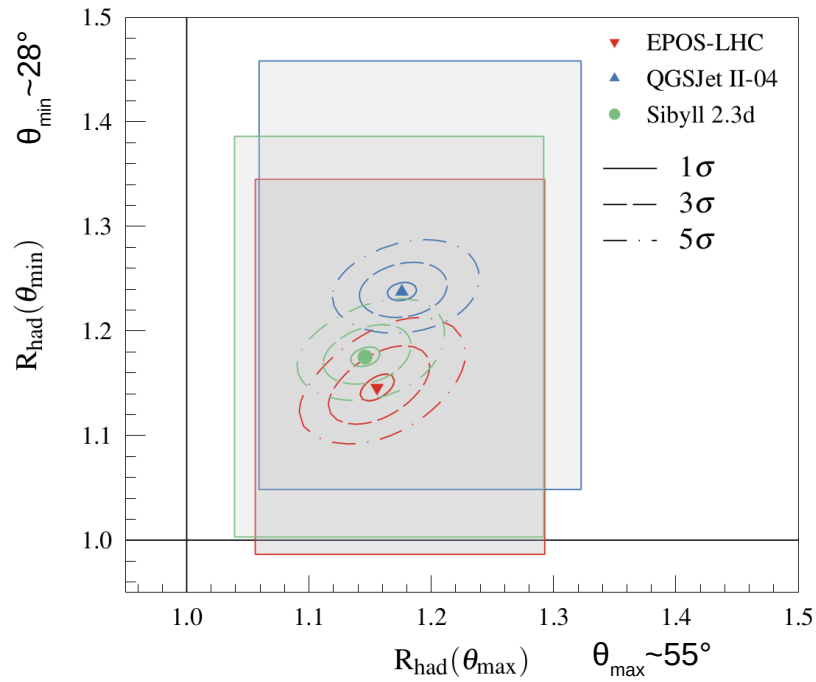
$$\ln \mathcal{L} = \begin{cases} \sum_k \sum_j (C_{jk} - n_{jk} + n_{jk} \ln \frac{n_{jk}}{C_{jk}}), & n_{jk} > 0 \\ \sum_k \sum_j C_{jk}, & n_{jk} = 0 \end{cases}$$

$\theta$  bins  
 $\theta \in (33^\circ, 39^\circ)$   
 2D bins

- Freedom in  $X_{\text{max}}$  ( $\Delta X_{\text{max}}$ ) and  $S(1000)$  ( $R_{\text{had}}(\theta)$ ) and primary fractions
- Change of  $S_{\text{had}}$  and  $S_{\text{em}}$  due to  $\Delta X_{\text{max}}$  incorporated

Simultaneous log-likelihood ratio fit of **two-dimensional distributions** of  $X_{\text{max}}$  and  $S(1000)$  in 5 zenith-angle bins with **MC templates** for combinations of four primary nuclei (p, He, O, Fe)

# Attenuation of hadronic signal with $\theta$



Indication of harder muon spectra in QGSJet II-04 than in data

# Motivations for modifications of MC predictions

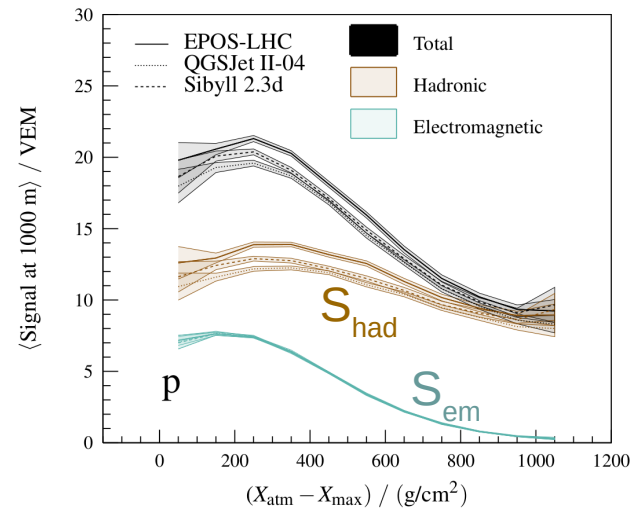
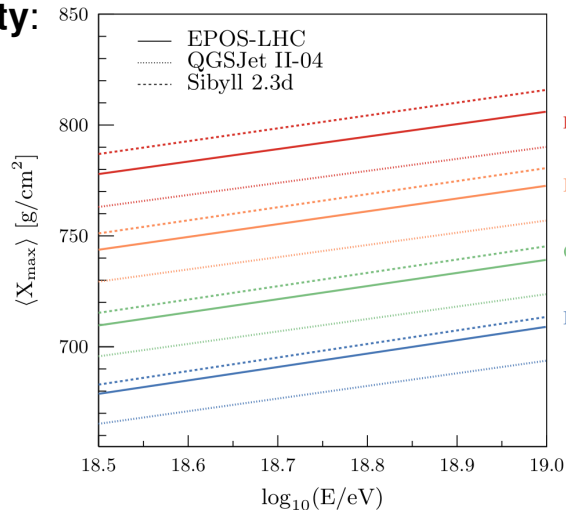
- Properties of **4-component shower universality**:

[Astropart. Phys. 87 (2017) 23, Astropart. Phys. 88 (2017) 46]

- $S(1000) = S_{had} + S_{em}$
- $S_{em}$  very universal

- **Main differences** between model predictions:

- Scale of  $\langle X_{max} \rangle$  and  $\langle S_{had} \rangle(\theta)$  are **approx. primary and energy independent**



$$X_{atm} = 880 / \cos \theta \text{ g/cm}^2$$

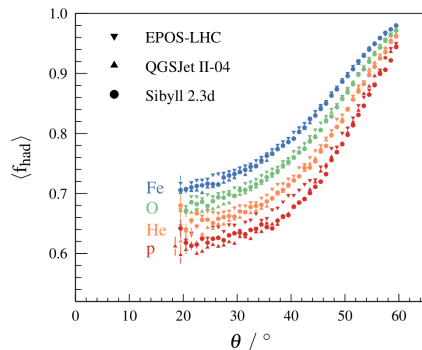
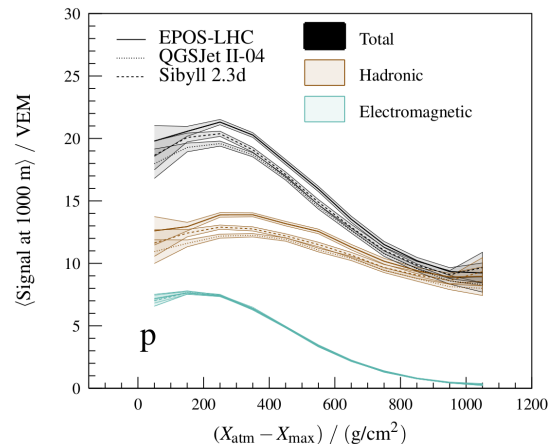
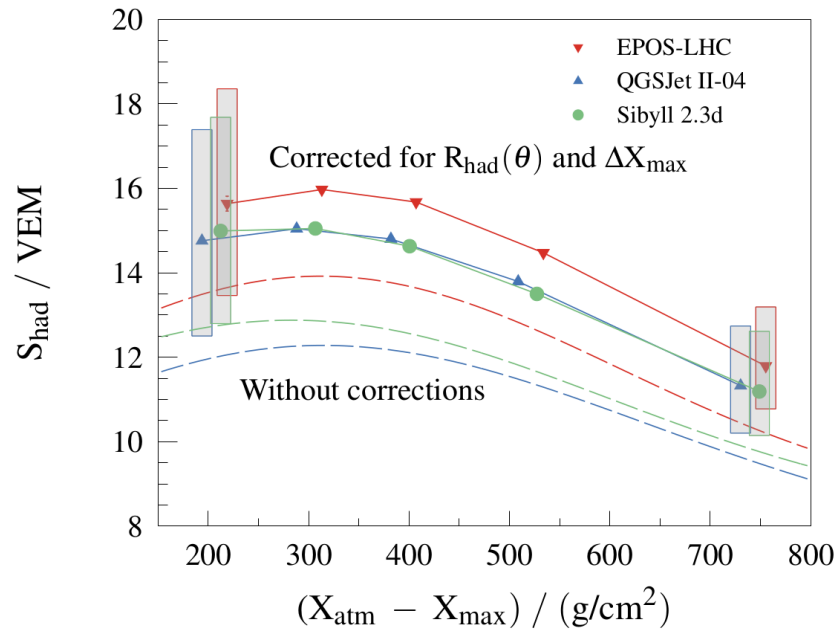
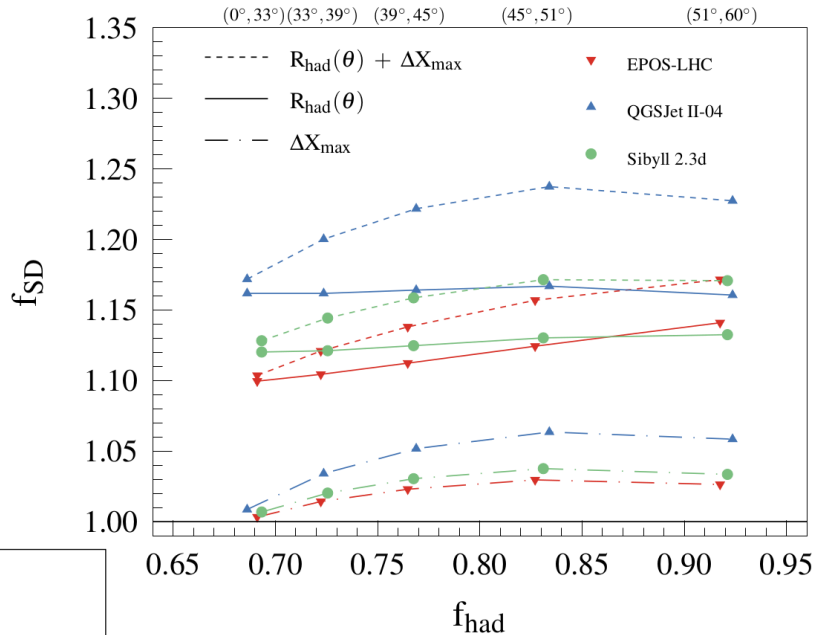
**Caveat:** no modifications in fluctuations or mass-dependencies etc. considered

## ad-hoc modifications

$$X_{max} \rightarrow X_{max} + \Delta X_{max}$$

$$S_{had}(\theta) \rightarrow S_{had}(\theta) \cdot R_{had}(\theta)$$

# Effect of modified $X_{\max}$ on the ground signal



# Assumption on primary species

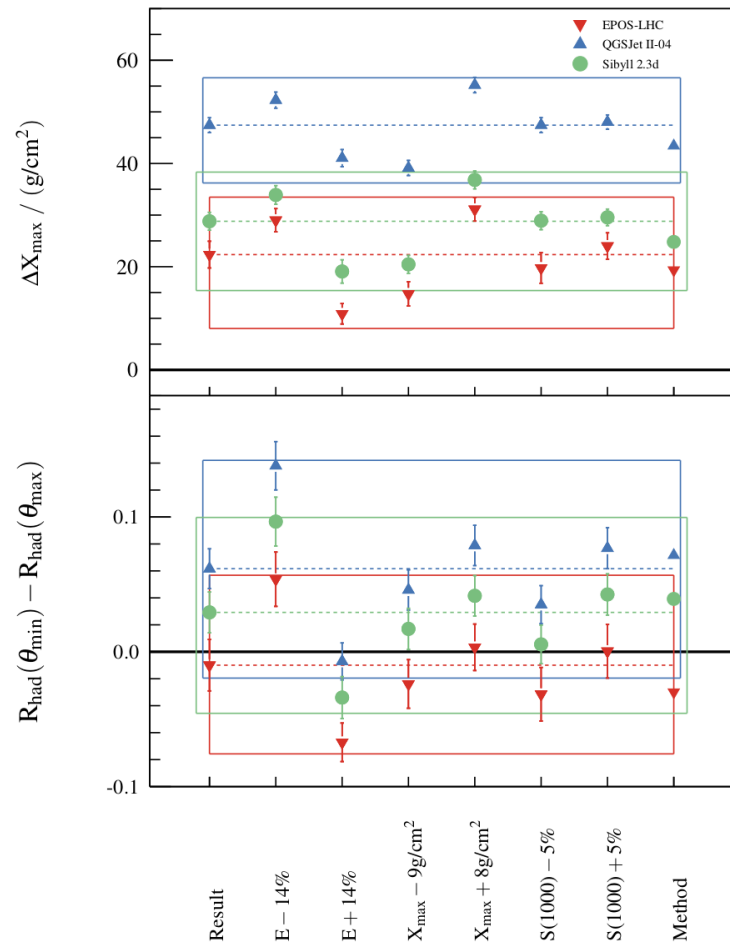
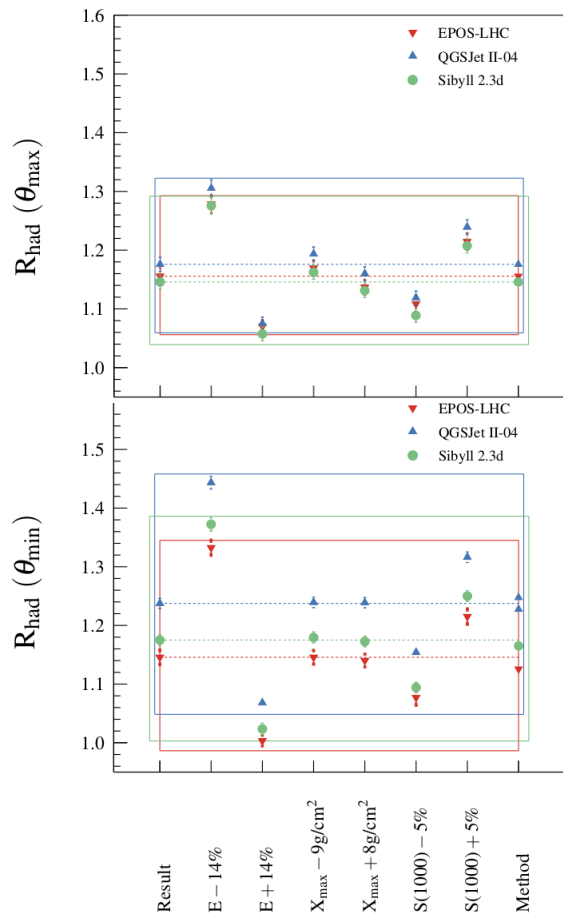
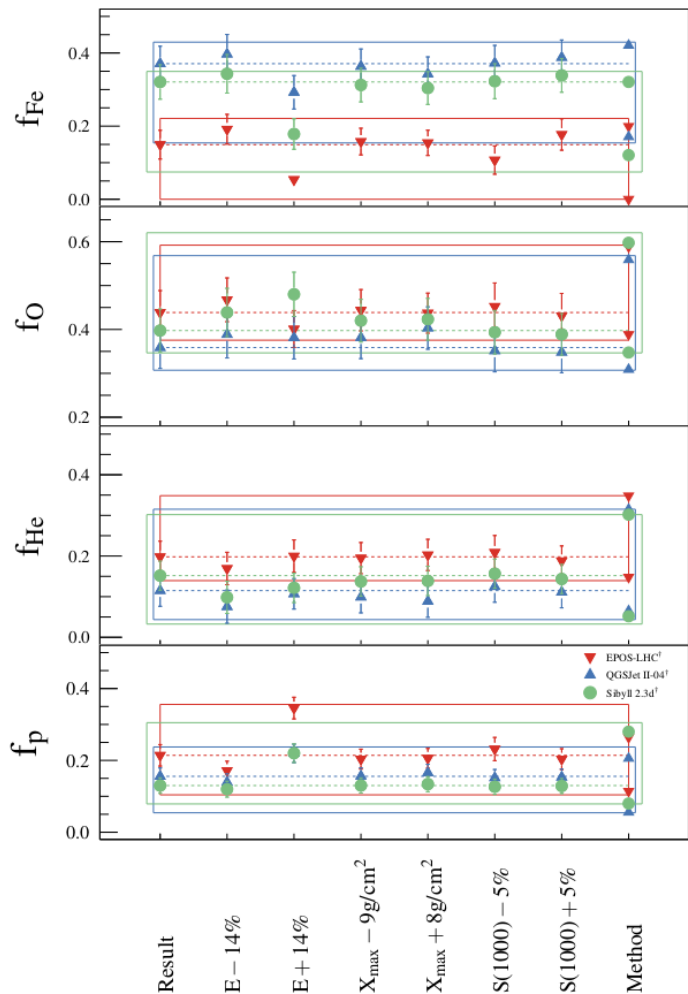
- $\Delta X_{\max}$  decreases by about 5-7, 10-17 and 30-40 g/cm<sup>2</sup> and  $R_{\text{had}}(\theta)$  increases by about 2-5%, 4-9% and 15-20% when the heaviest primary Fe is replaced by Si, O and He, respectively

$\ln \mathcal{L}_{\min}$	EPOS-LHC	QGSJET-II-04	SIBYLL 2.3d
p He	518.3	633.5	563.5
p He O	467.5	523.3	486.6
p He O Fe	451.9	476.3	451.6



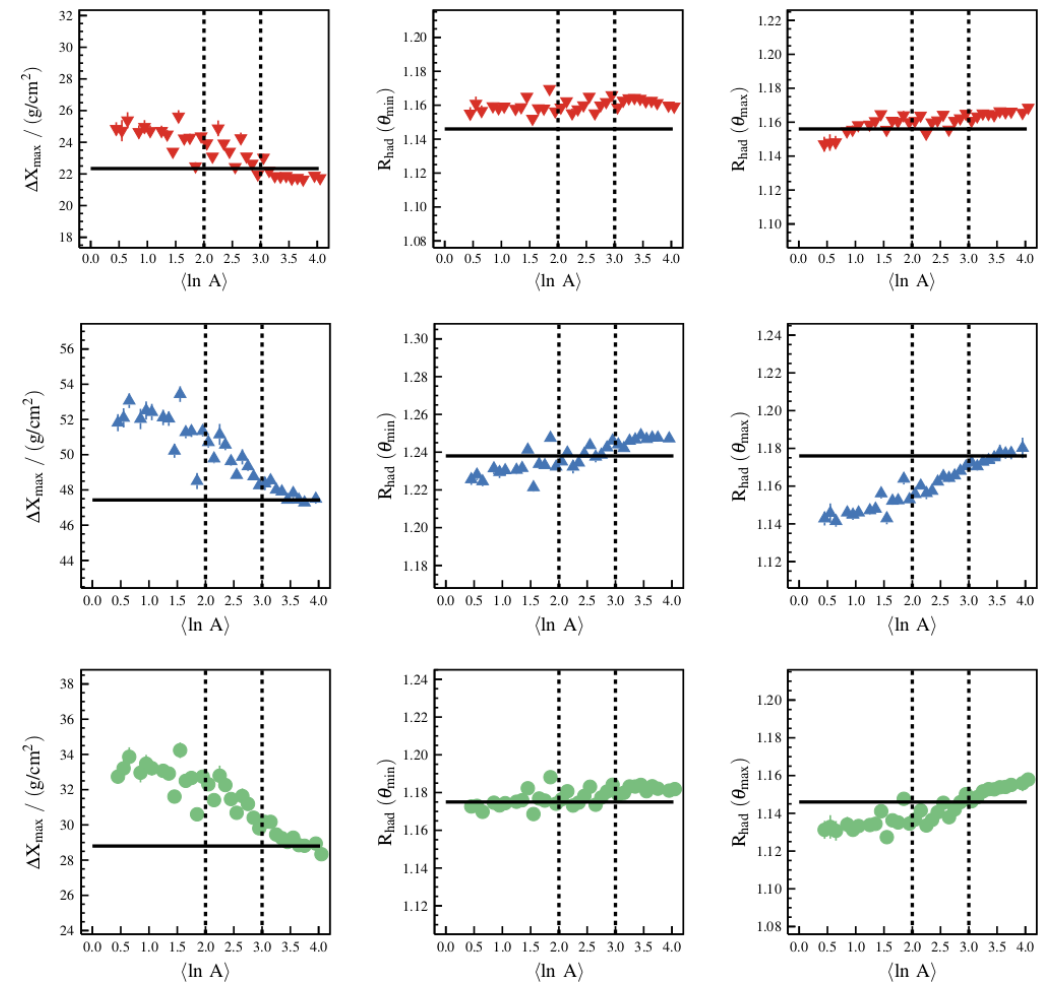
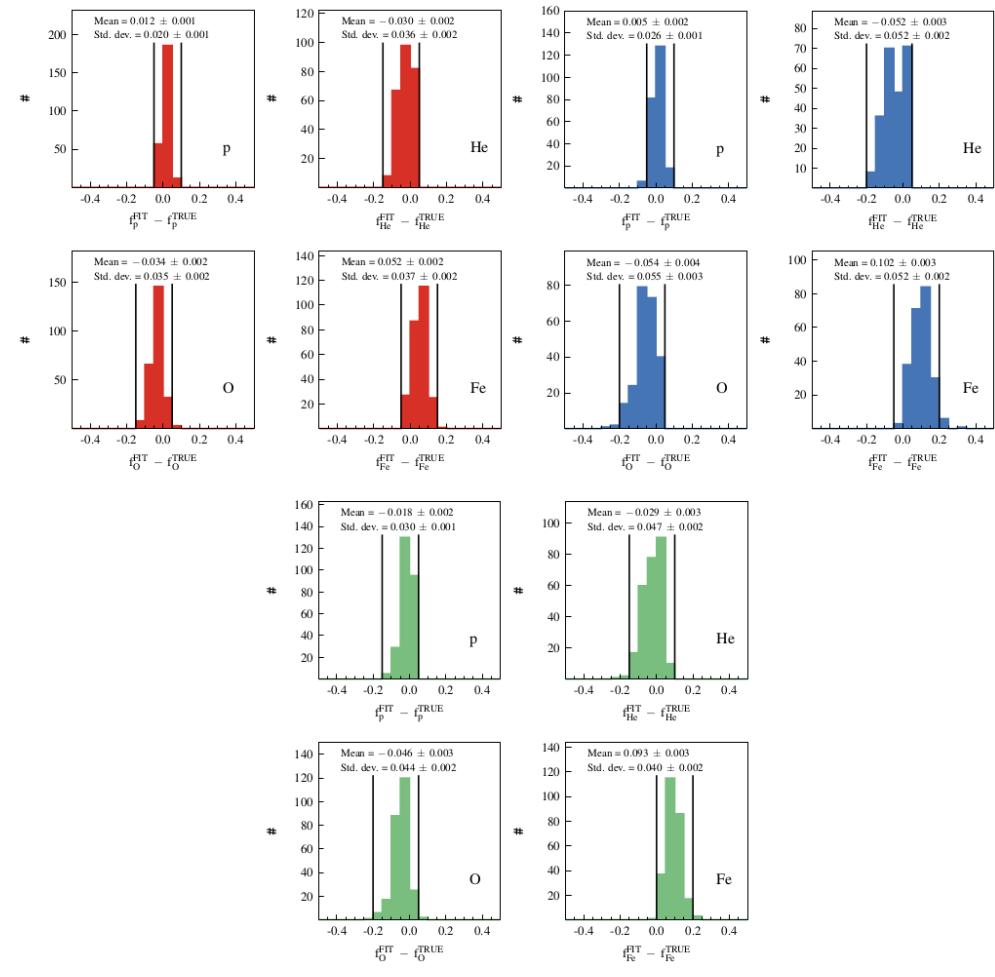
Significance of improvement of data description above  $5\sigma$

# Systematic uncertainties





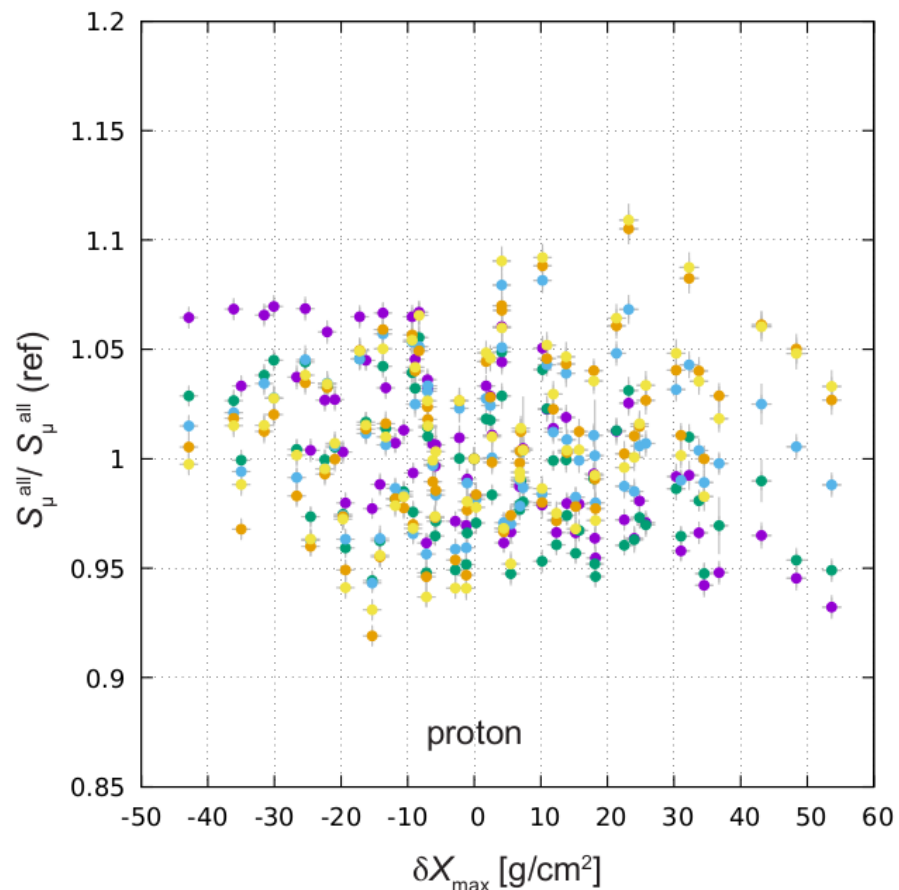
# MC-MC tests



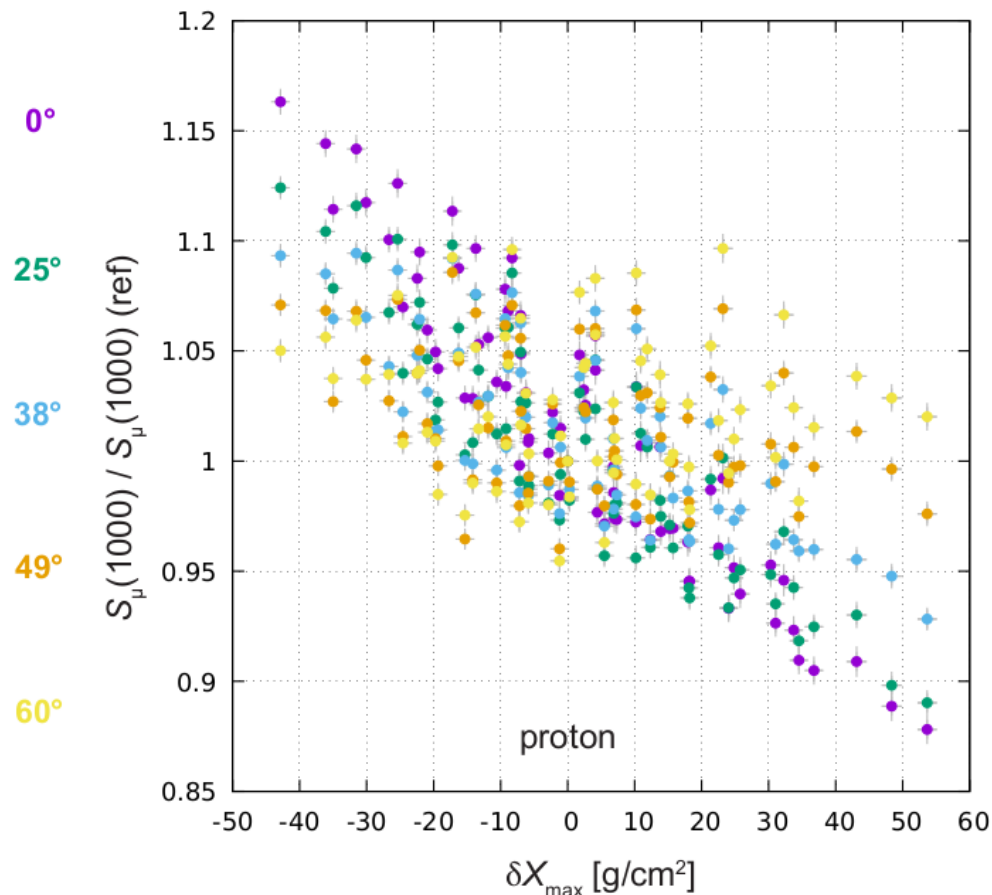


# Importance of 3D simulation

## All muons

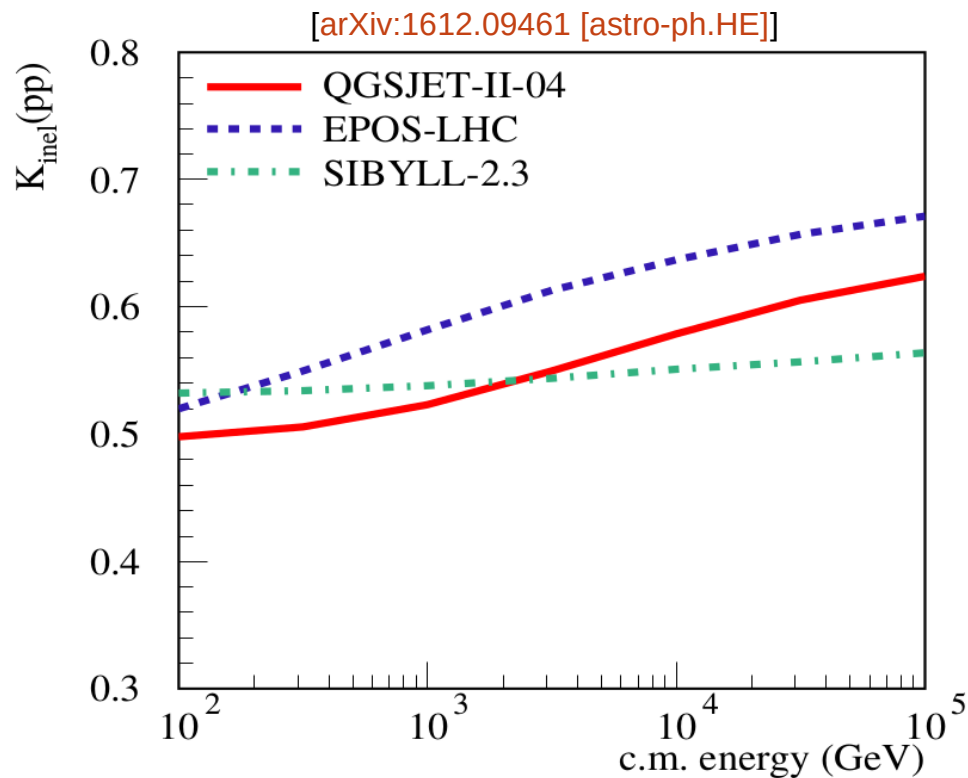


## Muons around 1000m



# Possible mass-(in)dependence of $X_{\max}$ shift

“changing the normalization of energy dependence”  $\rightarrow$  mass independent modifications



multiplicity:  $N \propto N_0 \cdot E^\alpha$   
 inelasticity:  $\kappa \propto \kappa_0 \cdot E^{-\omega}$

$$X_{\max}^A = X_1^A + X_0 \ln \frac{\kappa E}{A \cdot 2N \xi_C^\pi} =$$

$$X_1^A + (1 - \alpha - \omega) \cdot \left( X_0 \ln \frac{E}{A \cdot \xi_C^\pi} \right) + X_0 \cdot (\ln \kappa_0 - \ln N_0)$$

$$\begin{matrix} \kappa_0 \rightarrow f_\kappa \kappa_0 \\ N_0 \rightarrow f_N N_0 \end{matrix} \Rightarrow X_{\max}^A ' = X_{\max}^A + X_0 (\ln(f_\kappa) - \ln(f_N))$$

“changing the shape of energy dependence” → mass-dependent modifications

