

Quantum Chromodynamics and the Constituent-Quark Model

Workshop on “Half a Century of QCD”

**13th Int. Conference on New Frontiers in
Physics**

Kolymbari, August 29th, 2024

Willibald Plessas

Institute of Physics, University of Graz

Contents

- ❖ QCD degrees of freedom at low energies
- ❖ Relativistic Hamiltonian dynamics for the constituent quark model
- ❖ Universal RCQM for all baryons
- ❖ Spectroscopy
- ❖ Electroweak structures (form factors) of nucleons, hyperons, ...
including their flavor decompositions
- ❖ Strong vertex form factors πNN , $\pi N\Delta$, $\pi\Delta\Delta$
- ❖ Hadronic resonance decays – failure of $\{QQQ\}$ configurations for resonances
- ❖ Coupled-channels RCQM with explicit meson degrees of freedom
- ❖ Summary and Outlook

Origin of Quantum Chromodynamics (QCD)

Volume 47B, number 4

PHYSICS LETTERS

26 November 1973

ADVANTAGES OF THE COLOR OCTET GLUON PICTURE[☆]

H. FRITZSCH^{*}, M. GELL-MANN and H. LEUTWYLER^{**}

California Institute of Technology, Pasadena, Calif. 91109, USA

Received 1 October 1973

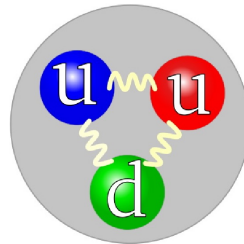
It is pointed out that there are several advantages in abstracting properties of hadrons and their currents from a Yang–Mills gauge model based on colored quarks and color octet gluons.

Phys. Lett. B 47 (1973) 365-368

~ 2600 citations as of today

Low-Energy QCD

- Hadrons consist of **constituent quarks**, e.g. baryons of $\{QQQ\}$, such as the (colorless) proton:

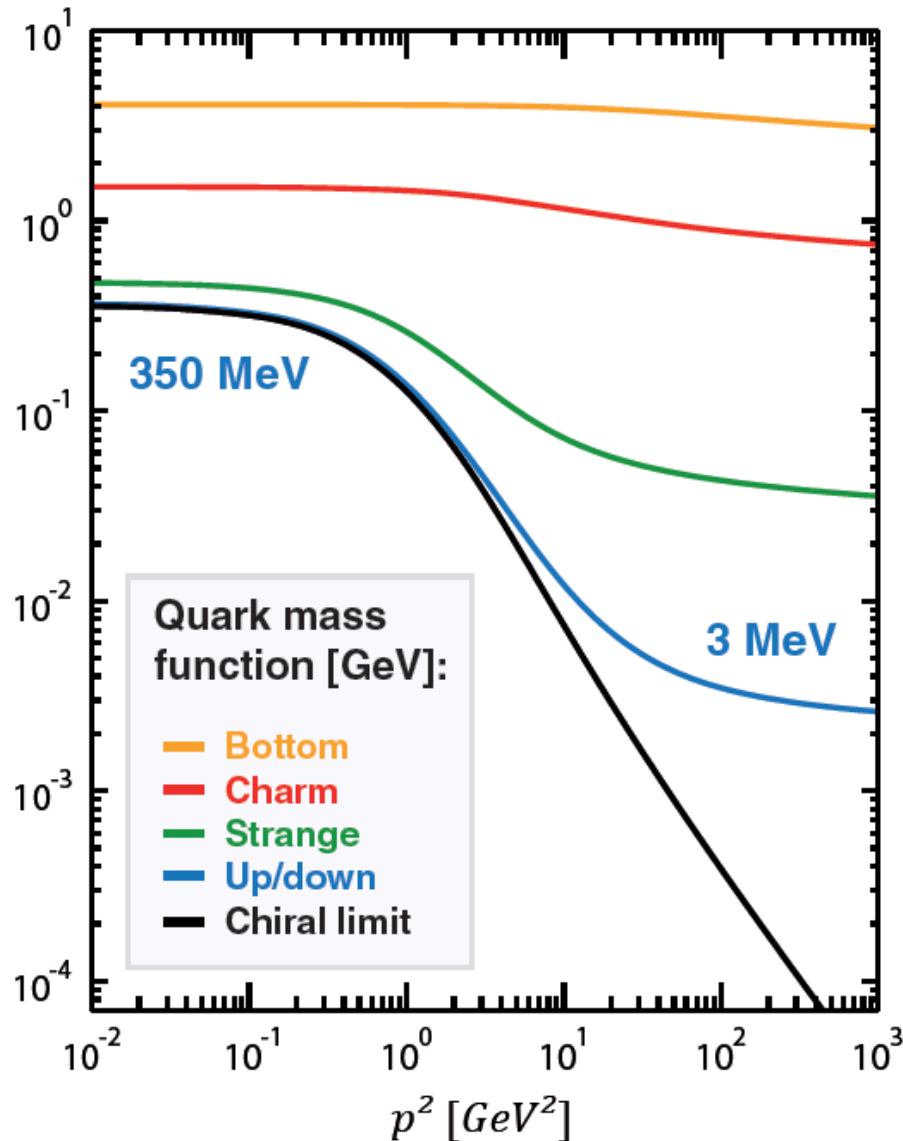


$\{QQQ\}$ are considered as quasiparticles, confined inside hadrons.

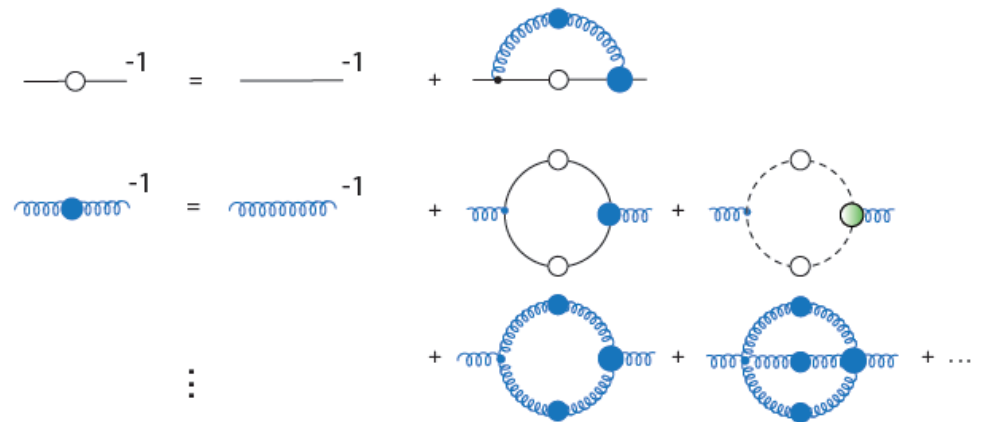
- The $\{Q-Q\}$ interaction is furnished by the low-energy d.o.f. of QCD, resulting from the **spontaneous breaking of chiral symmetry** ($SB\chi S$), i.e. for N_F flavors $SU(N_F)_L \times SU(N_F)_R \rightarrow SU(N_F)_V$, leading to the appearance of Goldstone bosons.
- Construct a **Poincaré-invariant interacting mass operator** based on

$$\mathcal{L}_{\text{int}} \sim ig\bar{\psi}\gamma_5\vec{\lambda}^F \cdot \vec{\phi}\psi$$

Dynamical Mass Generation



Dynamical quark masses generated by Dyson-Schwinger equations (DSE):



Relativistic Quantum Mechanics

Relativistic quantum mechanics (RQM)

i.e. **quantum theory** respecting **Poincaré invariance**

(theory on a Hilbert space \mathcal{H} corresponding to a finite number of particles, not a field theory)

Invariant mass operator

$$\hat{M} = \hat{M}_{free} + \hat{M}_{int}$$

Eigenvalue equations

$$\hat{M} |P, J, \Sigma\rangle = M |P, J, \Sigma\rangle \quad , \quad \hat{M}^2 = \hat{P}^\mu \hat{P}_\mu$$

$$\hat{P}^\mu |P, J, \Sigma\rangle = P^\mu |P, J, \Sigma\rangle \quad , \quad \hat{P}^\mu = \hat{M} \hat{V}^\mu$$

Relativistic Constituent Quark Model (RCQM)

Interacting mass operator

$$\begin{aligned}\hat{M} &= \hat{M}_{free} + \hat{M}_{int} \\ \hat{M}_{free} &= \sqrt{\hat{H}_{free}^2 - \hat{\vec{P}}_{free}^2} \\ \hat{M}_{int}^{rest\ frame} &= \sum_{i<j}^3 \hat{V}_{ij} = \sum_{i<j}^3 [\hat{V}_{ij}^{conf} + \hat{V}_{ij}^{hf}]\end{aligned}$$

fulfilling the **Poincaré algebra**

$$\begin{aligned}[\hat{P}_i, \hat{P}_j] &= 0, & [\hat{J}_i, \hat{H}] &= 0, & [\hat{P}_i, \hat{H}] &= 0, \\ [\hat{K}_i, \hat{H}] &= -i\hat{P}_i, & [\hat{J}_i, \hat{J}_j] &= i\epsilon_{ijk}\hat{J}_k, & [\hat{J}_i, \hat{K}_j] &= i\epsilon_{ijk}\hat{K}_k, \\ [\hat{J}_i, \hat{P}_j] &= i\epsilon_{ijk}\hat{P}_k, & [\hat{K}_i, \hat{K}_j] &= -i\epsilon_{ijk}\hat{J}_k, & [\hat{K}_i, \hat{P}_j] &= -i\delta_{ij}\hat{H}\end{aligned}$$

\hat{H}, \hat{P}_i ... time and space translations,
 \hat{J}_i ... rotations, \hat{K}_i ... Lorentz boosts

Universal Goldstone-Boson-Exchange RCQM

Phenomenologically, baryons with 5 flavors: u, d, s, c, b

$$\Rightarrow H_{free} = \sum_{i=1}^3 \sqrt{m_i^2 + \vec{k}_i^2}$$

$$V^{conf}(\vec{r}_{ij}) = B + C r_{ij}$$

$$V^{hf}(\vec{r}_{ij}) = \left[V_{24}(\vec{r}_{ij}) \sum_{f=1}^{24} \lambda_i^f \lambda_j^f + V_0(\vec{r}_{ij}) \lambda_i^0 \lambda_j^0 \right] \vec{\sigma}_i \cdot \vec{\sigma}_j$$

- ▶ i.e., for $N_f = 5$, we have the exchange of a **24-plet** plus a **singlet** of Goldstone bosons.

L.Ya. Glozman, W. Plessas, K. Varga, and R.F. Wagenbrunn: Phys. Rev. D **58**, 094030 (1998)

J.P. Day, K.-S. Choi, and W. Plessas: arXiv:1205.6918

J.P. Day, K.-S. Choi, and W. Plessas: Few-Body Syst. **54**, 329 (2013)

UGBE RCQM Parametrization

$$V^{conf}(\vec{r}_{ij}) = B + C r_{ij}$$

$$V_{\beta}(\vec{r}_{ij}) = \frac{g_{\beta}^2}{4\pi} \frac{1}{12m_i m_j} \left\{ \mu_{\beta}^2 \frac{e^{-\mu_{\beta} r_{ij}}}{r_{ij}} - 4\pi \delta(\vec{r}_{ij}) \right\}$$
$$= \frac{g_{\beta}^2}{4\pi} \frac{1}{12m_i m_j} \left\{ \mu_{\beta}^2 \frac{e^{-\mu_{\beta} r_{ij}}}{r_{ij}} - \Lambda_{\beta}^2 \frac{e^{-\Lambda_{\beta} r_{ij}}}{r_{ij}} \right\}$$

$$B = -402 \text{ MeV}, \quad C = 2.33 \text{ fm}^{-2}$$

$$\beta = 24 : \quad \frac{g_{24}^2}{4\pi} = 0.7, \quad \mu_{24} = \mu_{\pi} = 139 \text{ MeV}, \quad \Lambda_{24} = 700.5 \text{ MeV}$$

$$\beta = 0 : \quad \left(\frac{g_0}{g_{24}} \right)^2 = 1.5, \quad \mu_0 = \mu_{\eta'} = 958 \text{ MeV}, \quad \Lambda_0 = 1484 \text{ MeV}$$

$$m_u = m_d = 340 \text{ MeV}, \quad m_s = 480 \text{ MeV},$$

$$m_c = 1675 \text{ MeV}, \quad m_b = 5055 \text{ MeV}$$

Solution of Mass-Operator Eigenvalue Problem

$$\begin{aligned}\hat{M}|P, J, \Sigma, F_{abc}\rangle &= M|P, J, \Sigma, F_{abc}\rangle \\ &= M|M, V, J, \Sigma, F_{abc}\rangle\end{aligned}$$

→ baryon wave functions (initially in rest frame)

$$\Psi_{PJ\Sigma F_{abc}}(\vec{\xi}, \vec{\eta}) = \langle \vec{\xi}, \vec{\eta} | P, J, \Sigma, F_{abc} \rangle ,$$

where $\vec{\xi}$ and $\vec{\eta}$ are the usual Jacobi coordinates and

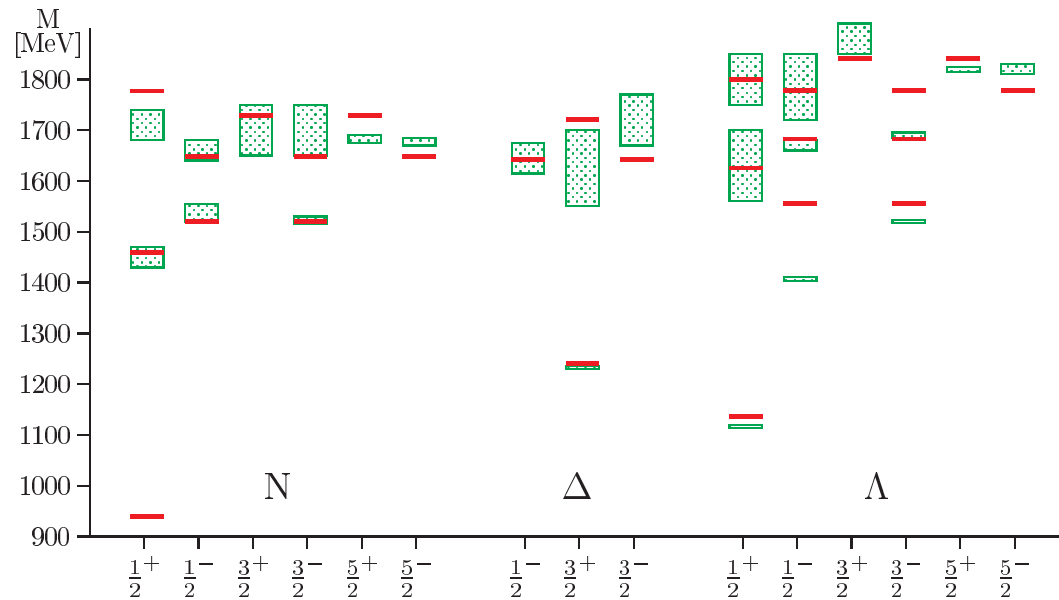
P	momentum eigenvalues
$(M, V$	mass resp. velocity eigenvalues)
J	intrinsic spin $\hat{=}$ total angular momentum)
Σ	z-component of J
F_{abc}	flavor content

Spectroscopy of Baryons

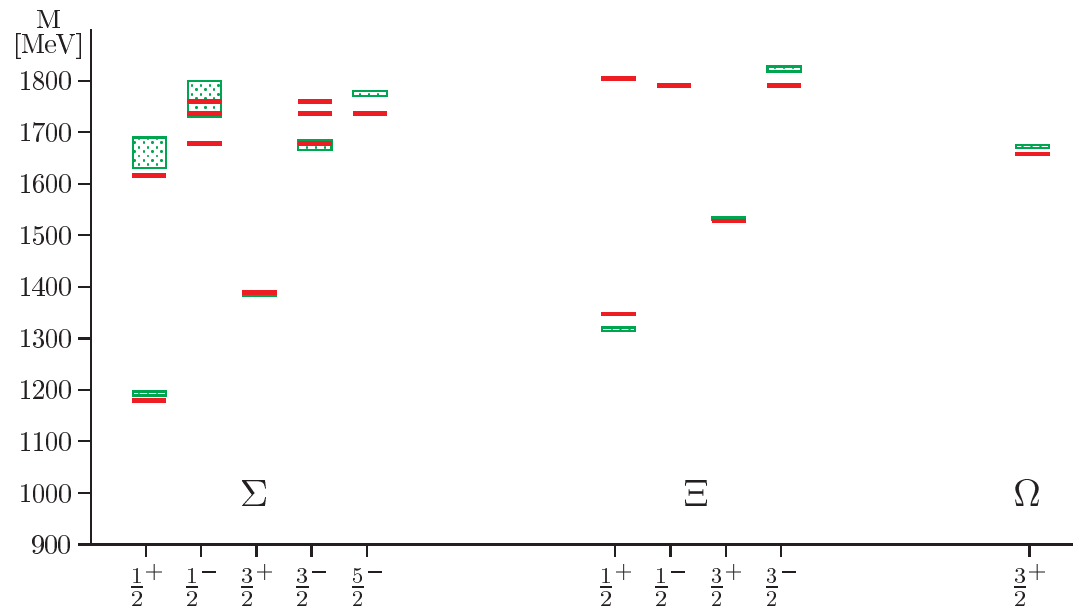
Excitation Spectra
of Baryons with **ALL** Flavors

u, d, s, c, b

Excitation Spectra of Baryons with u, d, s Flavors



red levels = theoretical prediction

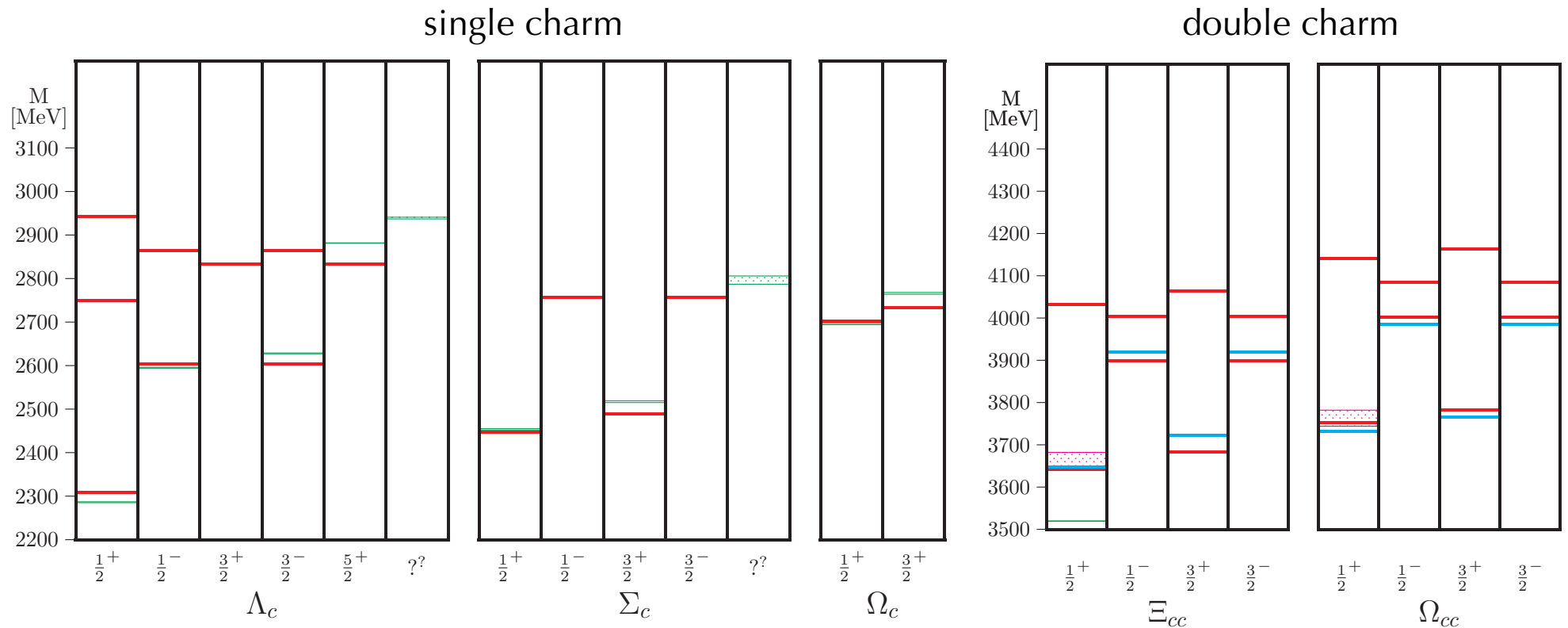


green boxes = exp. data
with uncertainties

L.Ya. Glozman, W. Plessas, K. Varga, and R.F. Wagenbrunn:

Phys. Rev. D 58, 094030 (1999)

Excitation Spectra of Charm Baryons



Left panel – single charm:

- red Universal GBE RCQM prediction
- green PDG 2013 (experiment)

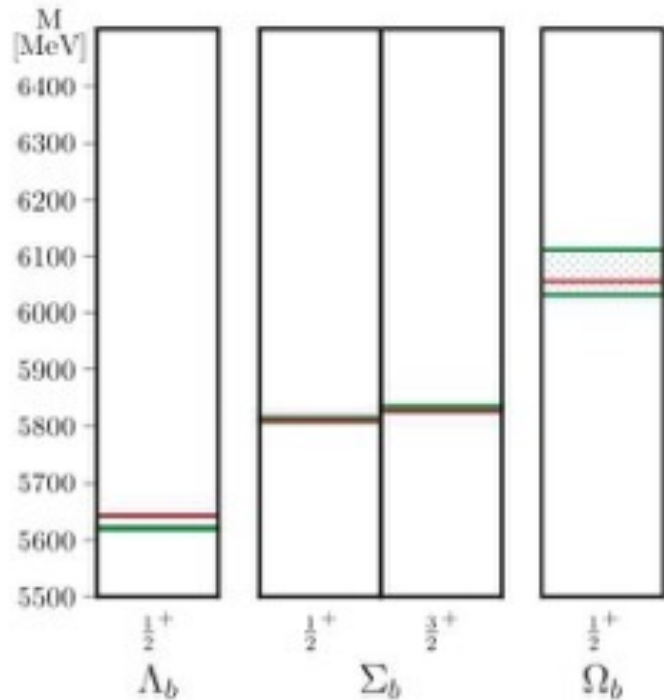
↑ our value $m(\Xi_{cc}) = 3642$ MeV

Right panel – double charm:

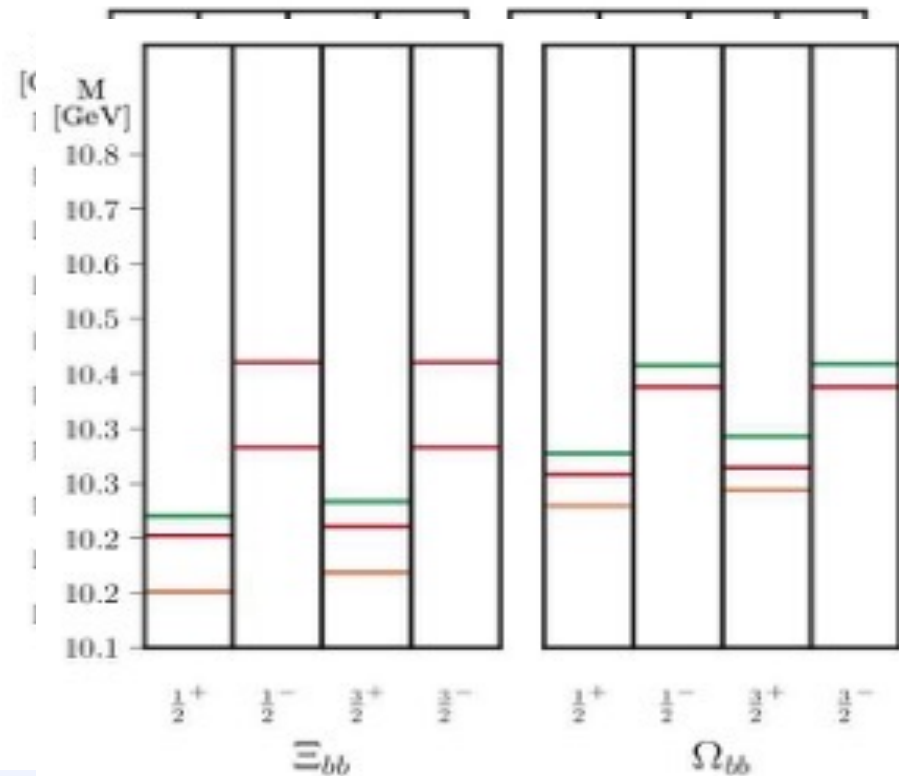
- green M. Mattson et al.: Phys. Rev. Lett. 89 (2002) 112001 (SELEX experiment)
- New datum from LHCb 2017: $m(\Xi_{cc}) = 3621.40 \pm 0.72(\text{stat.}) \pm 0.27(\text{syst.}) \pm 0.14(\Lambda_c)$ MeV
- cyan S. Migura, D. Merten, B. Metsch, and H.-R. Petry: Eur. Phys. J. A 28 (2006) 41 (Bonn RCQM)
- magenta L. Liu et al.: Phys. Rev. D 81 (2010) 094505 (Lattice QCD)

Excitation Spectra of Bottom Baryons

single bottom



double bottom



Left panel – single bottom:

red Universal GBE RCQM prediction

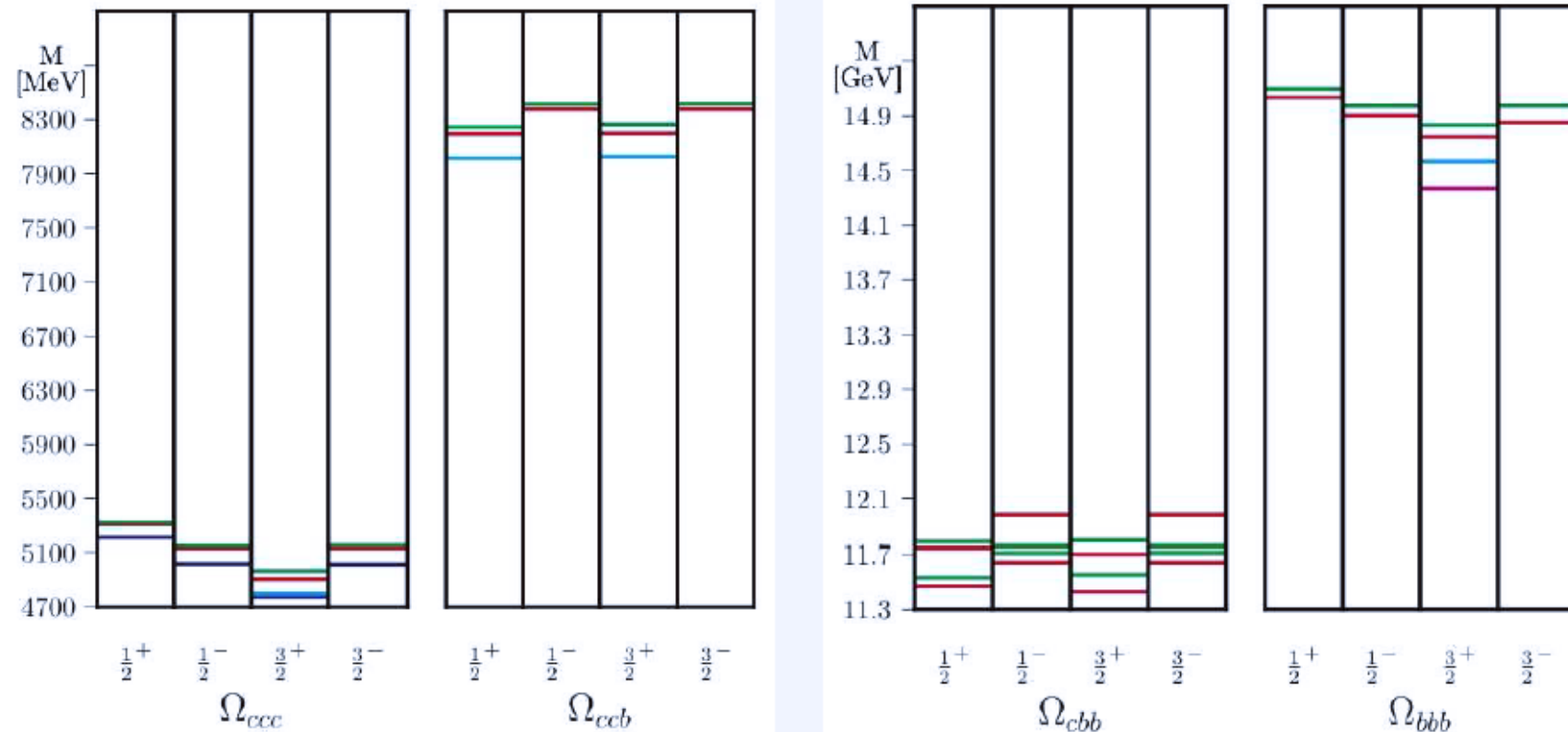
green PDG 2013 (experiment)

Right panel – double bottom:

green W. Roberts and M. Pervin: Int. J. Mod. Phys. A 23 (2008) 2817 (nonrel. one-gluon-exchange CQM)

orange D. Ebert, R.N. Faustov, V.O. Galkin, and A.P. Martynenko: Phys. Rev. D 66 (2002) 014008 (RCQM)

Triple-Heavy Baryon Spectra

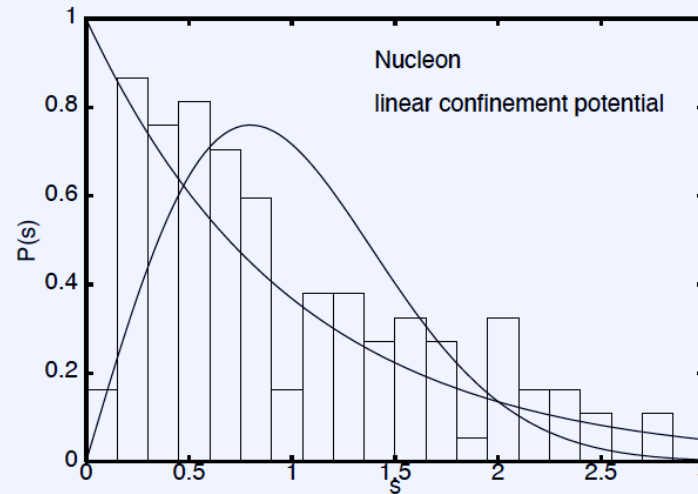


- red** Universal GBE RCQM
- green** W. Roberts and M. Pervin: Int. J. Mod. Phys. A 23 (2008) 2817
(nonrelativistic one-gluon-exchange CQM)
- blue** S. Migura, D. Merten, B. Metsch, and H.-R. Petry: Eur. Phys. J. A 28 (2006) 41 (Bonn RCQM)
- cyan** A.P. Martynenko: Phys. Lett. B 663 (2008) 317 (RCQM)
- magenta** S. Meinel: Phys. Rev. D 82 (2010) 114502 (lattice QCD)

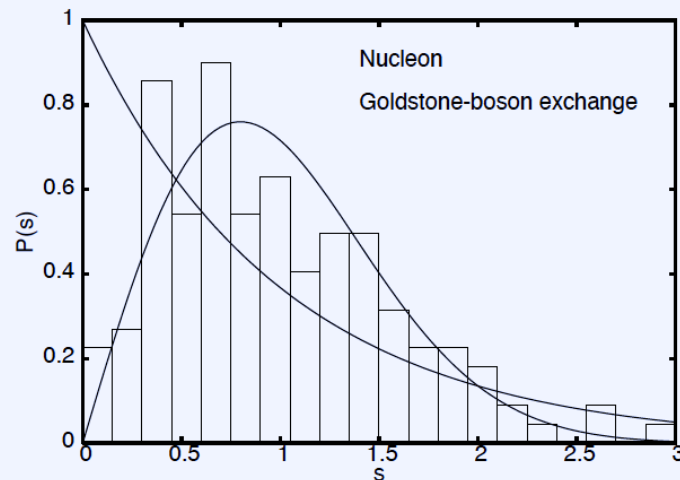
Quantum Chaos in N Spectra

Distribution of nearest-neighbour **nucleon** level spacings:

Only confinement interaction



Confinement + GBE hyperfine interaction



Histogramm of theoretical level spacings in comparison to Poisson and Wigner GOE distributions (solid lines)

Rest-Frame Baryon States

Mass operator eigenstates

$$\hat{M} |P, J, \Sigma, T, M_T\rangle = M |P, J, \Sigma, T, M_T\rangle$$

represented in configuration space

$$\langle \vec{\xi}, \vec{\eta} | P, J, \Sigma, T, M_T \rangle = \Psi_{PJ\Sigma TM_T}(\vec{\xi}, \vec{\eta})$$

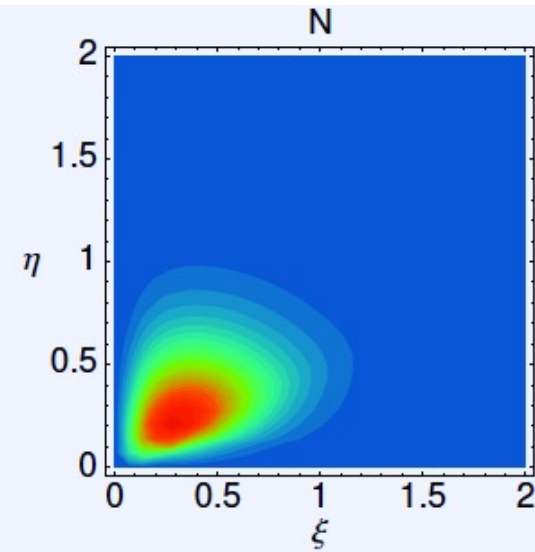
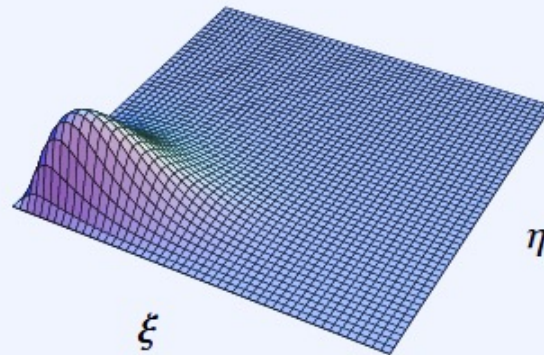
with $\vec{\xi}$ and $\vec{\eta}$ the usual Jacobi coordinates.

Picture the baryon wave functions through
spatial probability density distributions

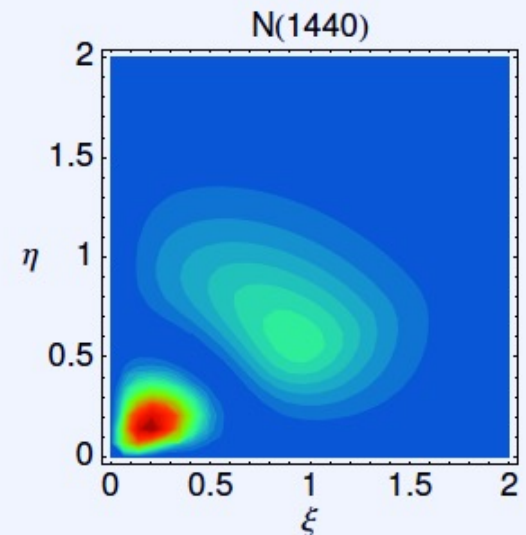
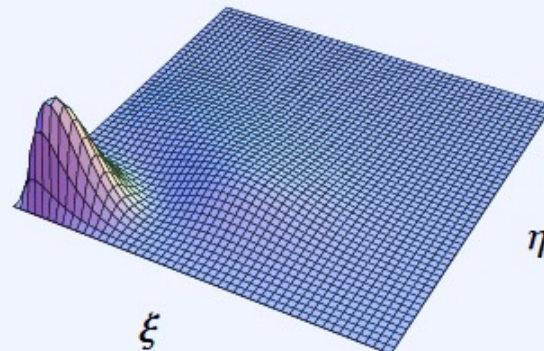
$$\rho(\xi, \eta) = \xi^2 \eta^2 \int d\Omega_\xi d\Omega_\eta \Psi_{PJ\Sigma TM_T}^*(\xi, \Omega_\xi, \eta, \Omega_\eta) \Psi_{PJ\Sigma TM_T}(\xi, \Omega_\xi, \eta, \Omega_\eta)$$

Spatial Probability Density Distributions

N GBE CQM

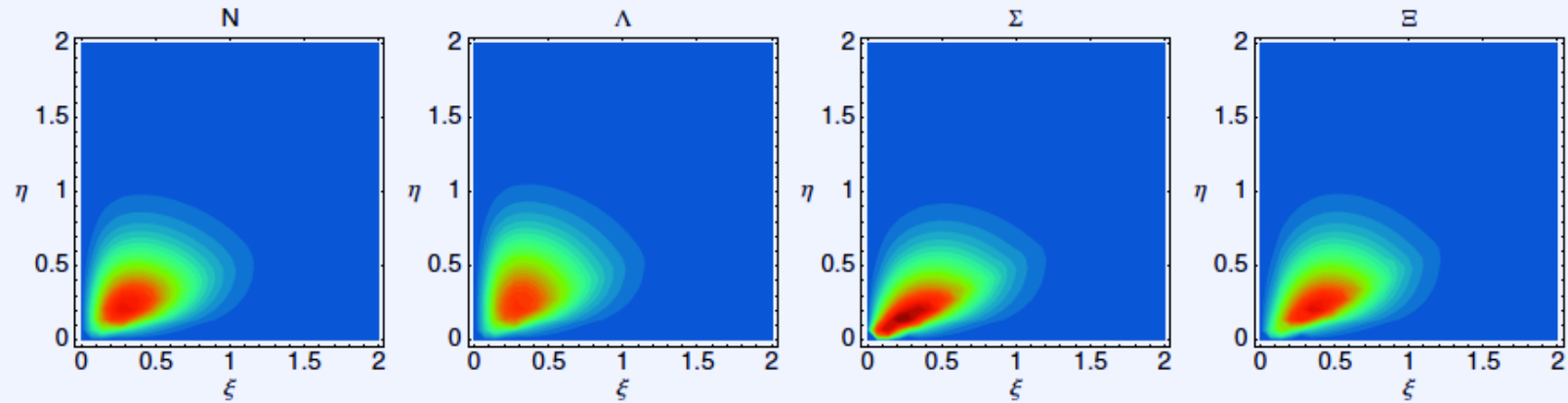


N(1440) GBE CQM

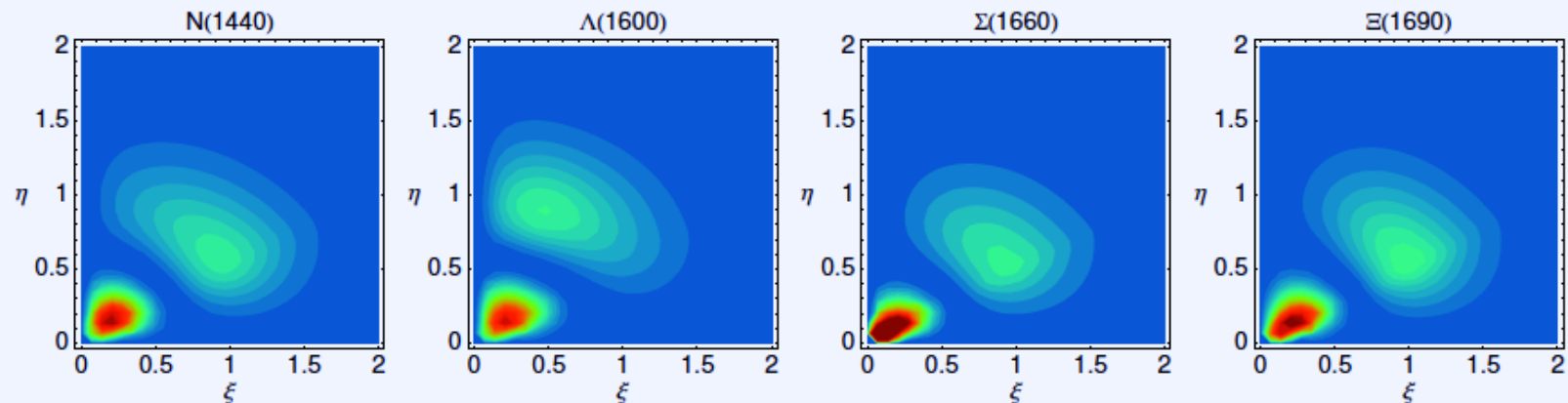


Spatial Probability Density Distributions

$\rho(\xi, \eta)$ for the $\frac{1}{2}^+$ octet baryon ground states $N(939)$, $\Lambda(1116)$, $\Sigma(1193)$, $\Xi(1318)$:

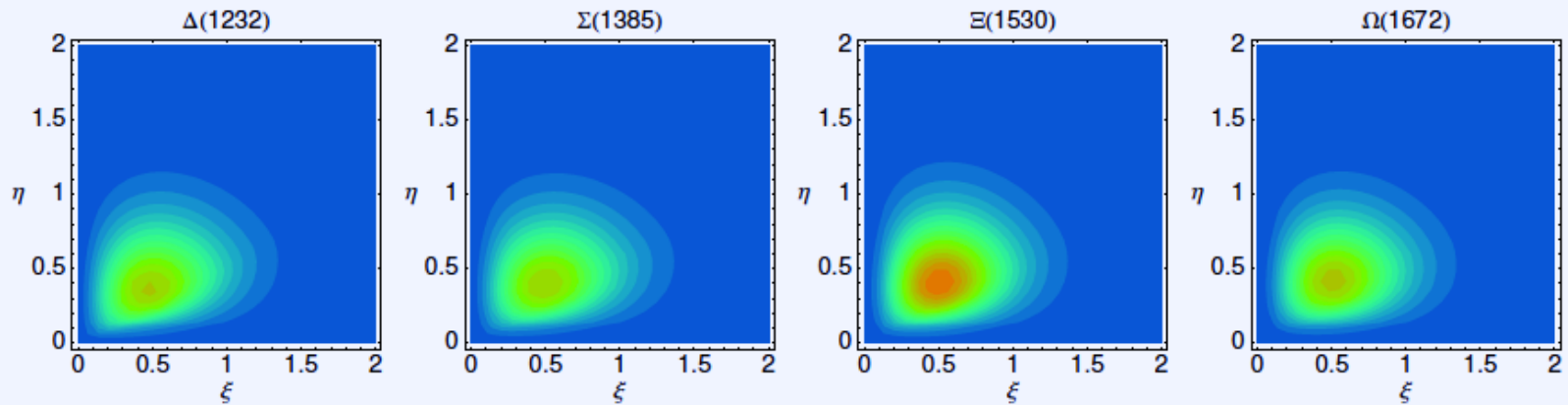


$\rho(\xi, \eta)$ for the $\frac{1}{2}^+$ octet baryon states $N(1440)$, $\Lambda(1600)$, $\Sigma(1660)$, $\Xi(1690)$:

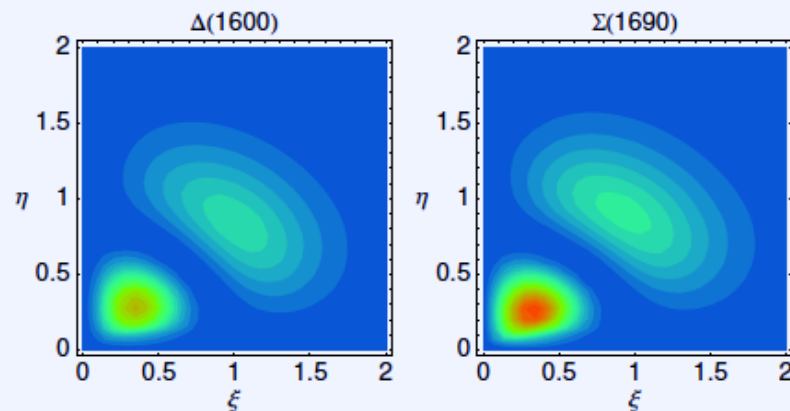


Spatial Probability Density Distributions

$\rho(\xi, \eta)$ for the $\frac{3}{2}^+$ decuplet baryon states $\Delta(1232)$, $\Sigma(1385)$, $\Xi(1530)$, $\Omega(1672)$:



$\rho(\xi, \eta)$ for the $\frac{3}{2}^+$ decuplet baryon states $\Delta(1600)$, $\Sigma(1690)$:



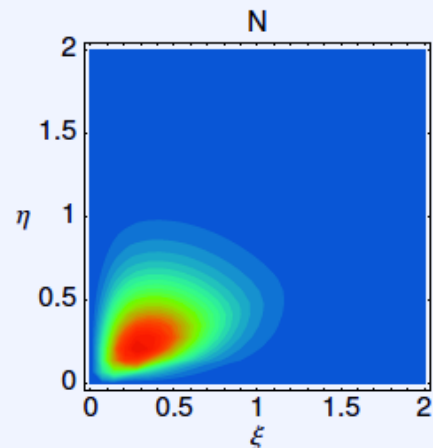
Electric Radii vs. Root-Mean-Square Radii

The **root-mean-square radius** (in the rest frame):

$$r_{\text{rms}} = \sqrt{\langle r_i^2 \rangle} = \left(\int d^3 r_i \langle P = 0, J, \Sigma | \hat{r}_i^2 | P = 0, J, \Sigma \rangle \right)^{\frac{1}{2}}$$

Is NOT an **observable**! Is NOT **relativistically invariant**!

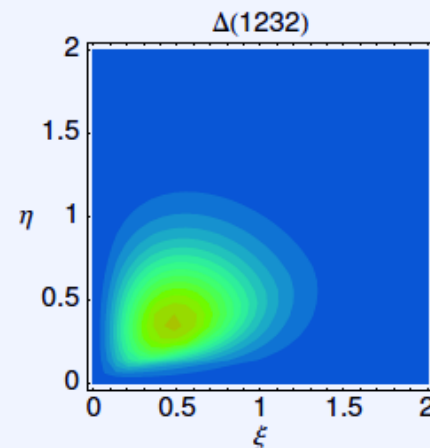
→ Idea about the **spatial distribution** of constituent quarks.



$$r_{\text{rms}}^N = 0.304 \text{ fm}$$

Exp.: $r_E^p \sim 0.88 \text{ fm}$

$(r_E^n)^2 \sim -0.12 \text{ fm}^2$



$$r_{\text{rms}}^\Delta = 0.390 \text{ fm}$$

$r_E^{\Delta^{++}} = r_E^{\Delta^+} = r_E^{\Delta^-} = 0.656 \text{ fm}$

$r_E^{\Delta^0} = 0 \text{ fm}$

Calculation of Covariant Observables

Matrix elements of a transition operator \hat{O} between baryon eigenstates $|P, J, \Sigma, T, T_3, Y\rangle$

$$\langle P', J', \Sigma', T', T'_3, Y' | \hat{O} | P, J, \Sigma, T, T_3, Y \rangle$$

- $\hat{O} \dots \hat{J}_{\text{em}}^\mu \rightarrow$ electromagnetic FF's
- $\dots \hat{A}_{\text{axial}}^\mu \rightarrow$ axial FF's
- $\dots \hat{S} \rightarrow$ scalar FF
- $\dots \hat{\Theta}^{\mu\nu} \rightarrow$ gravitational/tensor FF's
- $\dots \hat{D}_\lambda^\mu \rightarrow$ hadronic decays

To be calculated from microscopic three-quark ME's

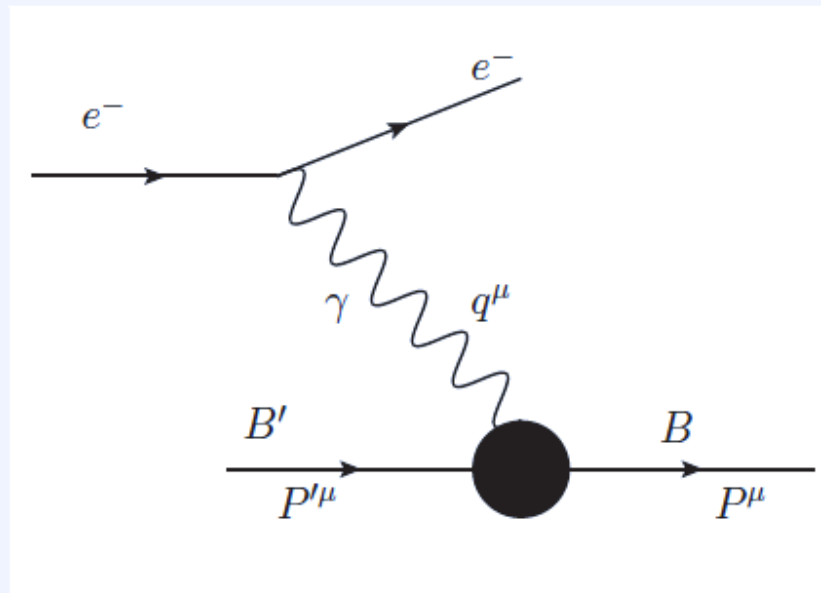
$$\langle p'_1, p'_2, p'_3; \sigma'_1, \sigma'_2, \sigma'_3; f'_{i_1}, f'_{i_2}, f'_{i_3} | \hat{O} | p_1, p_2, p_3; \sigma_1, \sigma_2, \sigma_3; f_{i_1}, f_{i_2}, f_{i_3} \rangle$$

↑↑
boosted 3-body states

↑↑
boosted 3-body states

e^- Scattering – Electromagnetic Form Factors

Elastic electron scattering:

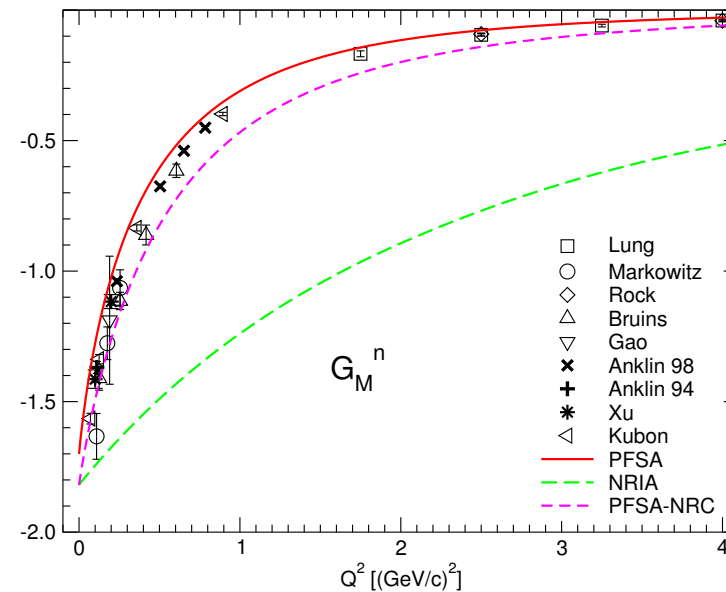
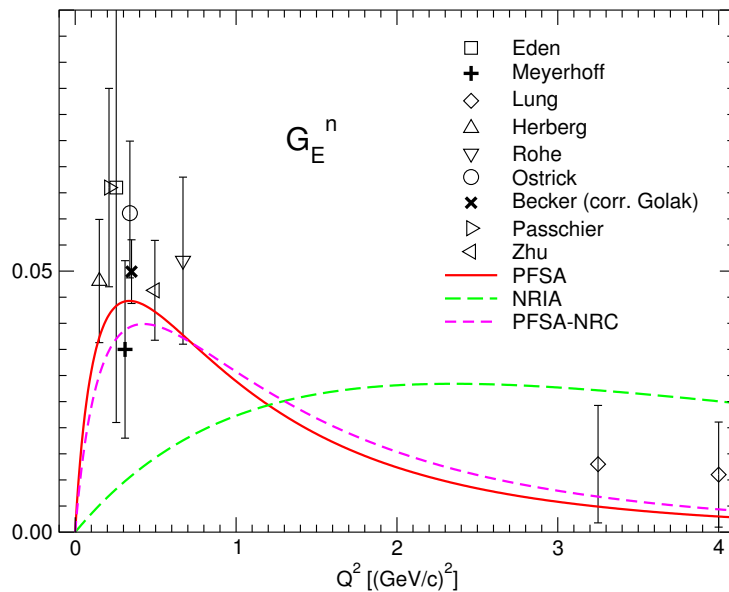
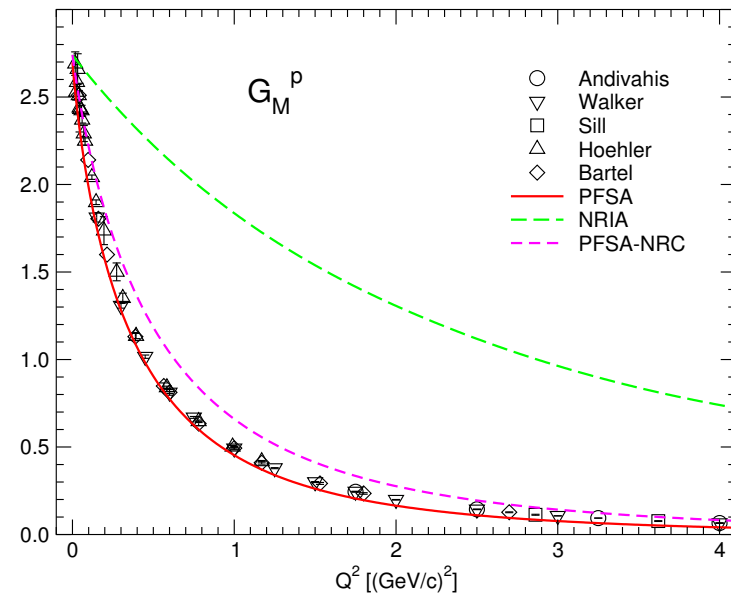
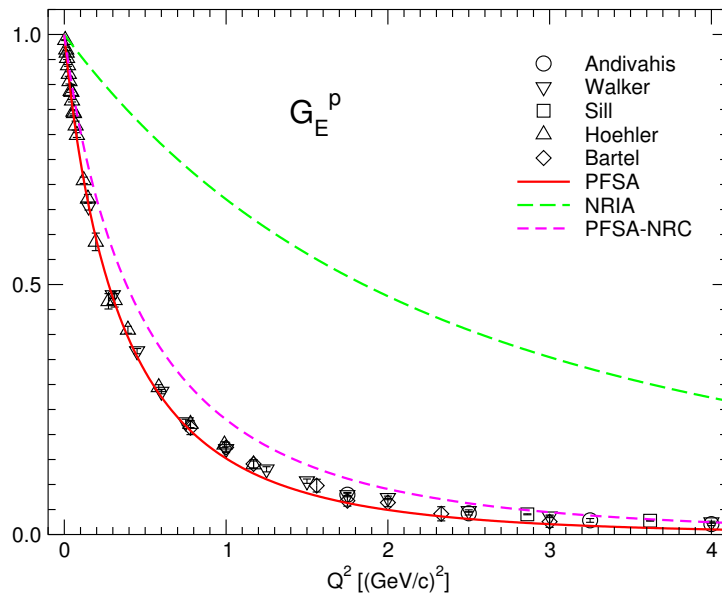


Invariant form factors:

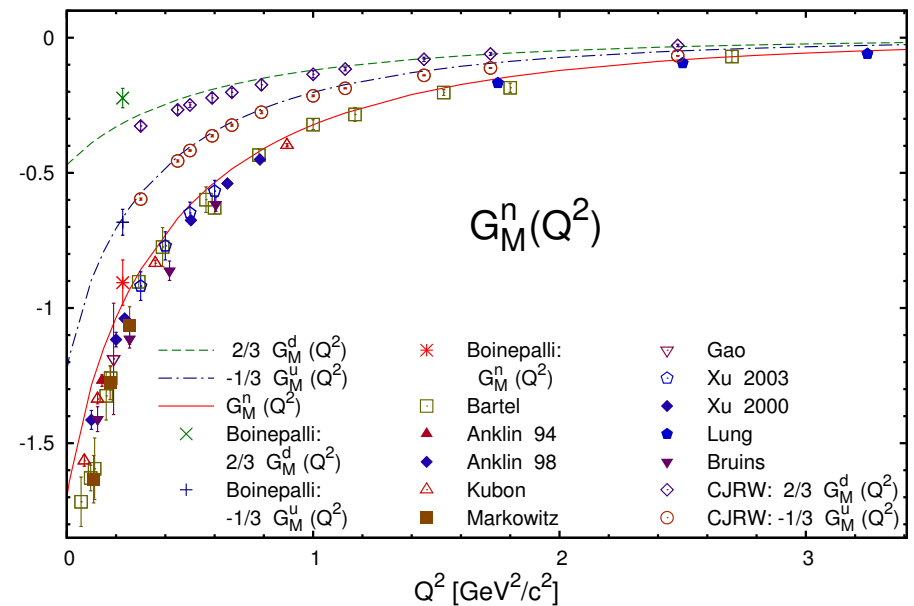
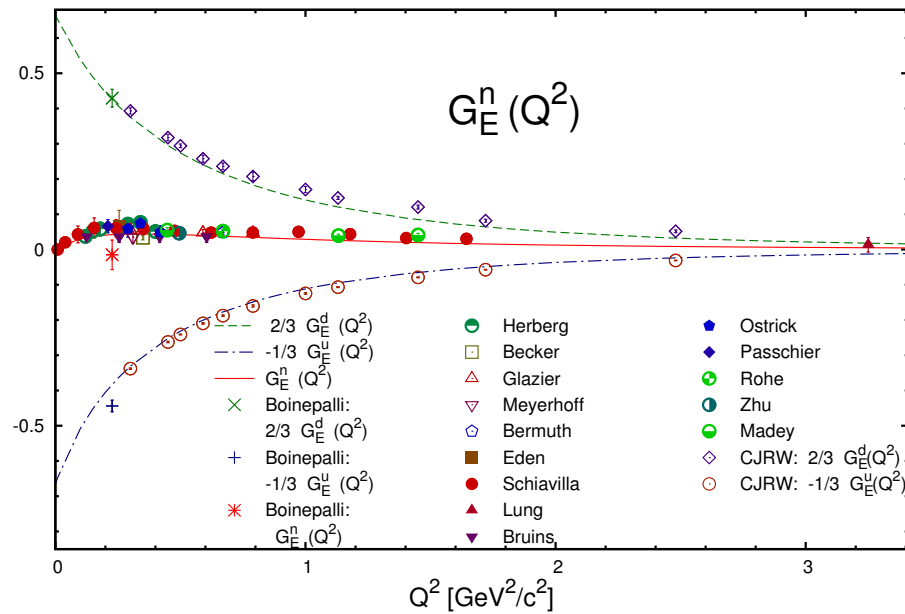
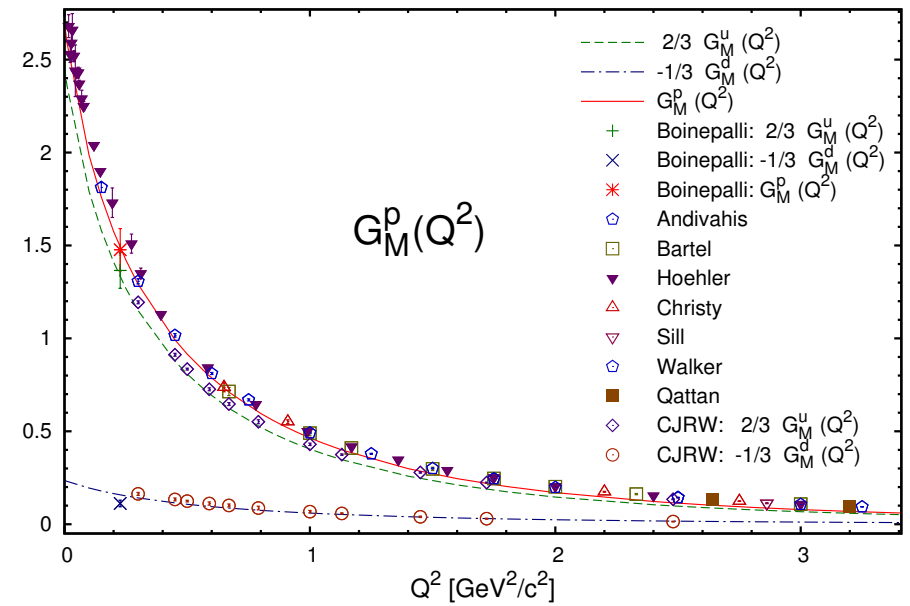
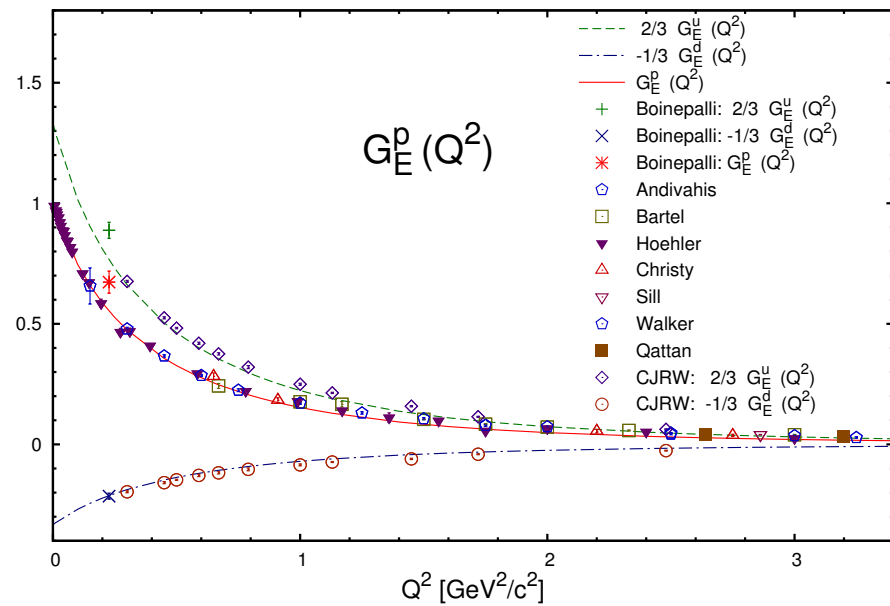
$$F_{\Sigma'\Sigma}^\nu(Q^2) = \langle P', J, \Sigma', T, M_T | \hat{J}_{\text{em}}^\nu | P, J, \Sigma, T, M_T \rangle$$

$$\text{with } Q^2 = -q^2; \quad q^\mu = P^\mu - P'^\mu$$

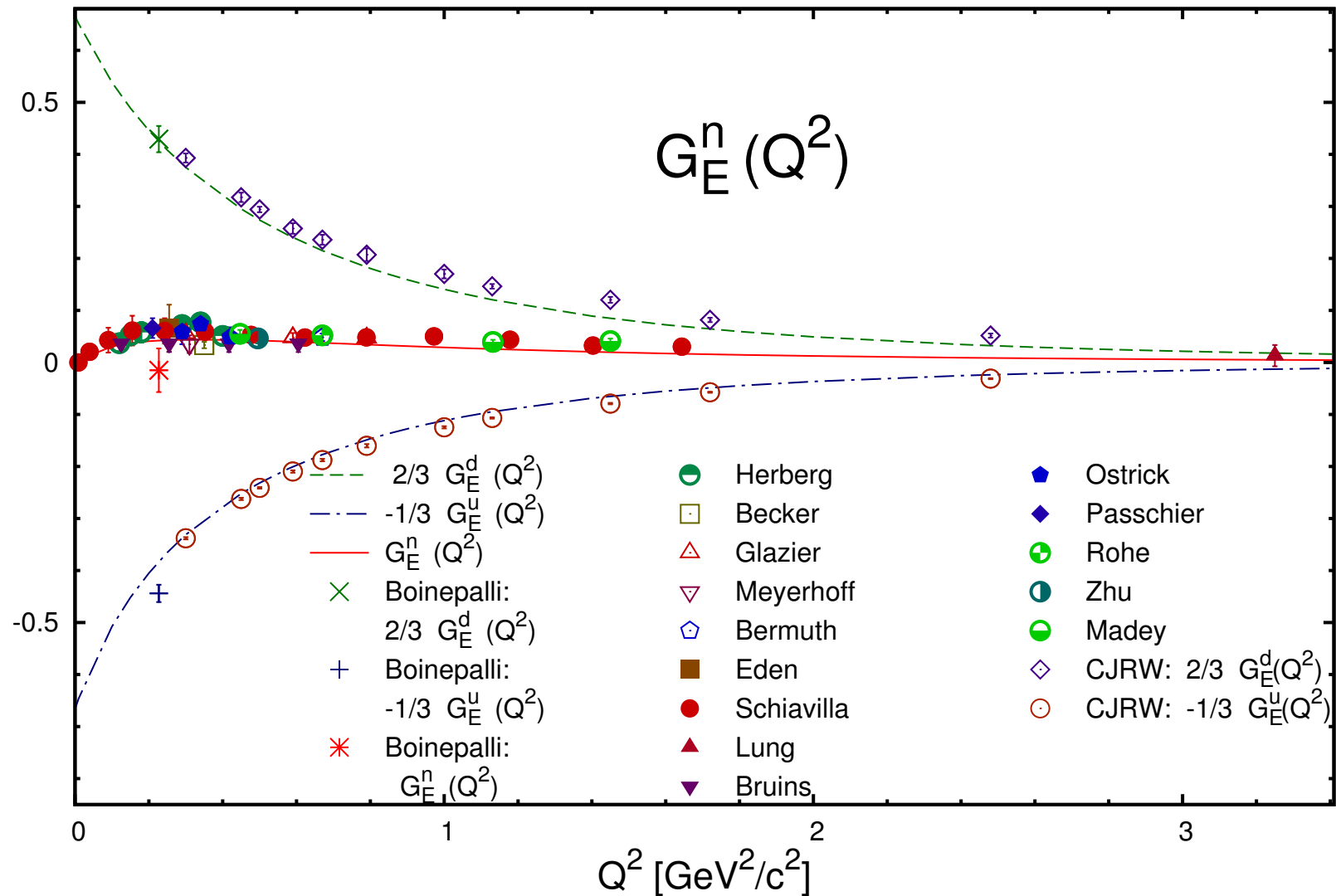
Electromagnetic Nucleon Form Factors



Flavor Decomposition of Nucleon Form Factors



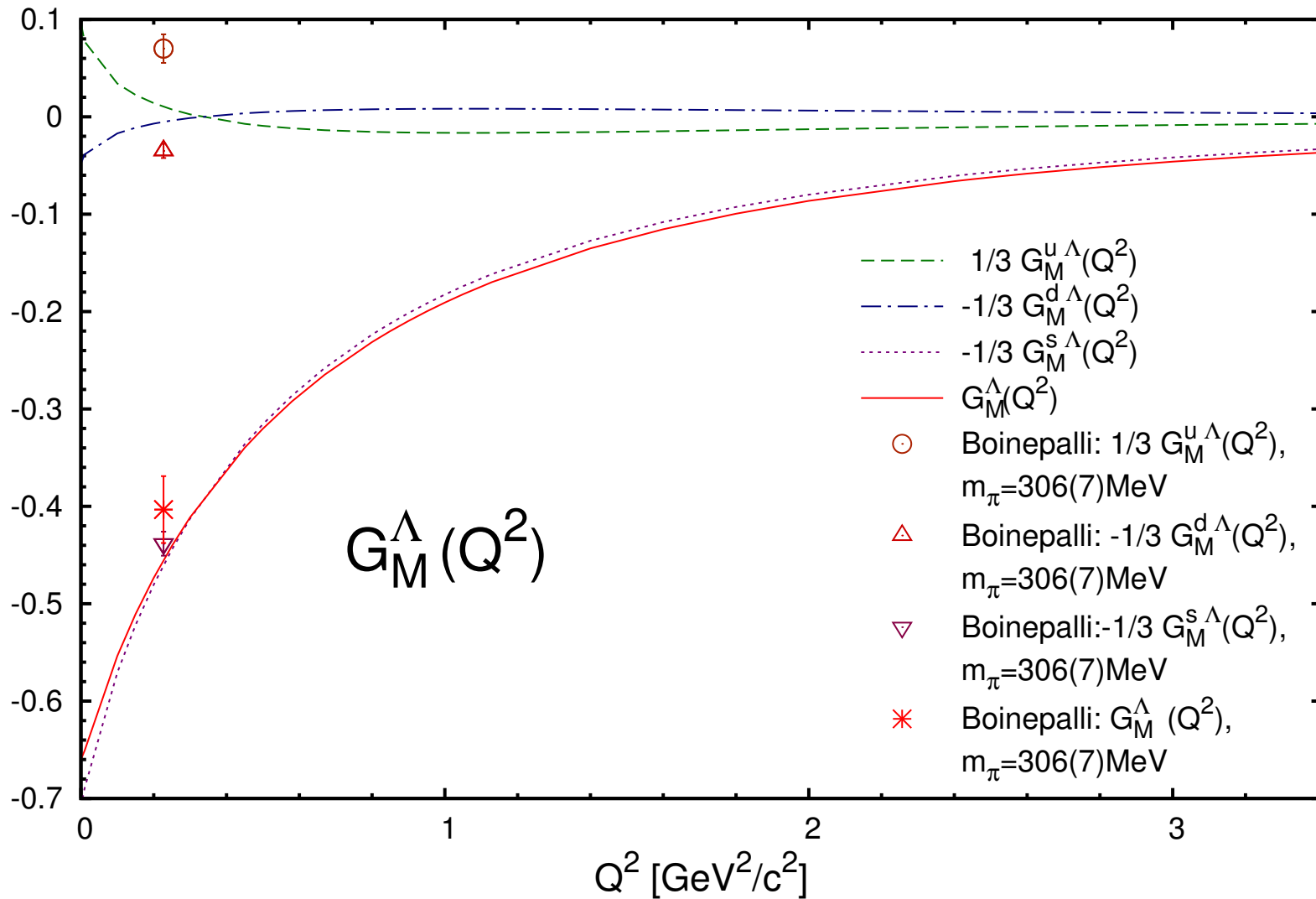
Flavor Decomposition of Neutron $G_E(Q^2)$



M. Rohrmoser, K.-S. Choi, and W. Plessas: *Few-Body Syst.* 58 (2017) 83

Lattice QCD: S. Boinelli et al.: *Phys. Rev. D* 74 (2006) 093005

Flavor Components in $\Lambda(1116)$ Magnetic FF $G_M(Q^2)$



M. Rohrmoser, K.-S. Choi, and W. Plessas: *Few-Body Syst.* 58 (2017) 83

Lattice QCD: S. Boinepalli et al.: *Phys. Rev. D* 74 (2006) 093005

Electric Radii and Magnetic Moments

Electric radii r_E^2 [fm²]

Baryon	GBE PFSM	Experiment
p	0.82	0.7692 ± 0.0123 ¹⁾ 0.70870 ± 0.00113 ²⁾
n	-0.13	-0.1161 ± 0.0022

¹⁾ CODATA value (PDG)

²⁾ Pohl et al.: Nature **466** (2010) 213

Magnetic moments μ [n.m.]

Baryon	GBE PFSM	Experiment
p	2.70	2.792847356
n	-1.70	-1.9130427

Electric Radii and Magnetic Moments – Nonrelativistic !!

Electric radii r_E^2 [fm²]

Baryon	GBE PFSM	GBE NRIA	Experiment
p	0.82	0.10	0.7692 ± 0.0123 ¹⁾ 0.70870 ± 0.00113 ²⁾
n	-0.13	-0.01	-0.1161 ± 0.0022

¹⁾ CODATA value (PDG)

²⁾ Pohl et al.: Nature **466** (2010) 213

Magnetic moments μ [n.m.]

Baryon	GBE PFSM	GBE NRIA	Experiment
p	2.70	2.74	2.792847356
n	-1.70	-1.82	-1.9130427

Baryon Electric Radii and Magnetic Moments

Electric radii r_E^2 [fm²]

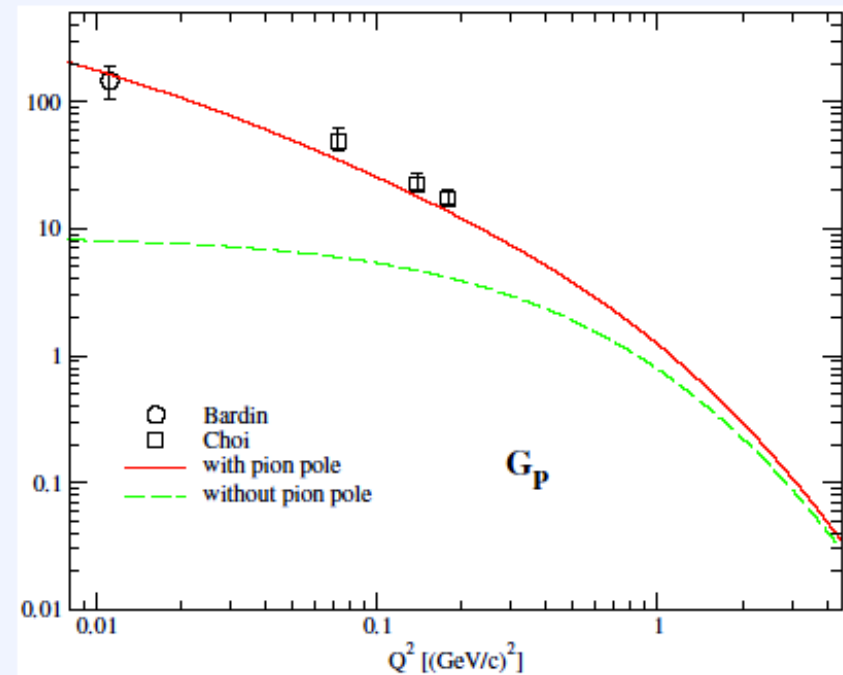
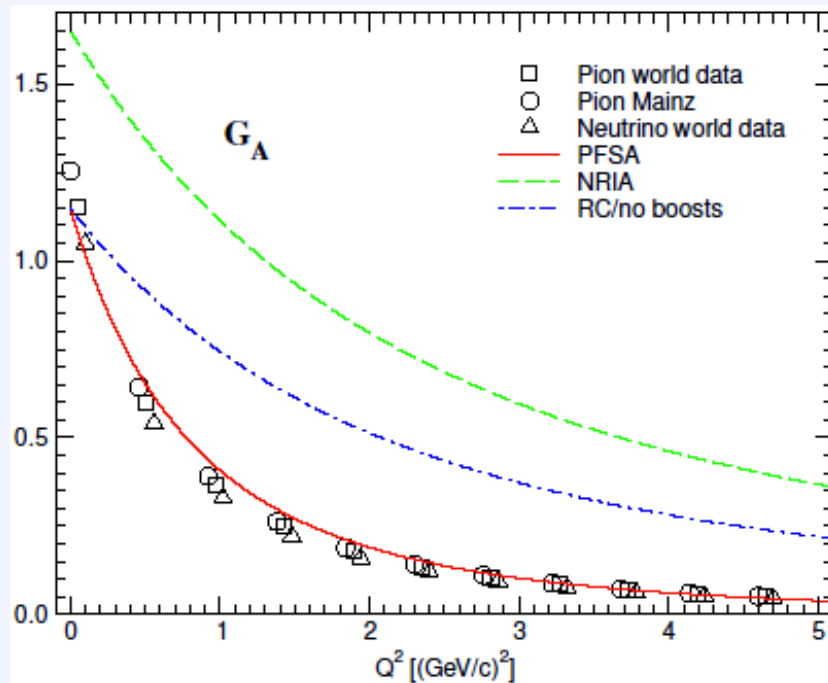
Baryon	GBE PFSM	Experiment
p	0.82	0.7692 ± 0.0123
n	-0.13	-0.1161 ± 0.0022
Σ^-	0.72	$0.61 \pm 0.12 \pm 0.09$

Magnetic moments μ [n.m.]

Baryon	GBE PFSM	Experiment
p	2.70	2.792847356
n	-1.70	-1.9130427
Λ	-0.64	-0.613 ± 0.004
Σ^+	2.38	2.458 ± 0.010
Σ^-	-0.93	-1.160 ± 0.025
Ξ^0	-1.25	-1.250 ± 0.014
Ξ^-	-0.70	-0.6507 ± 0.0025
Δ^+	2.08	$2.7_{-1.3}^{+1.0} \pm 1.5 \pm 3$
Δ^{++}	4.17	3.7 - 7.5
Ω^-	-1.59	-2.020 ± 0.05

Axial Nucleon Form Factors

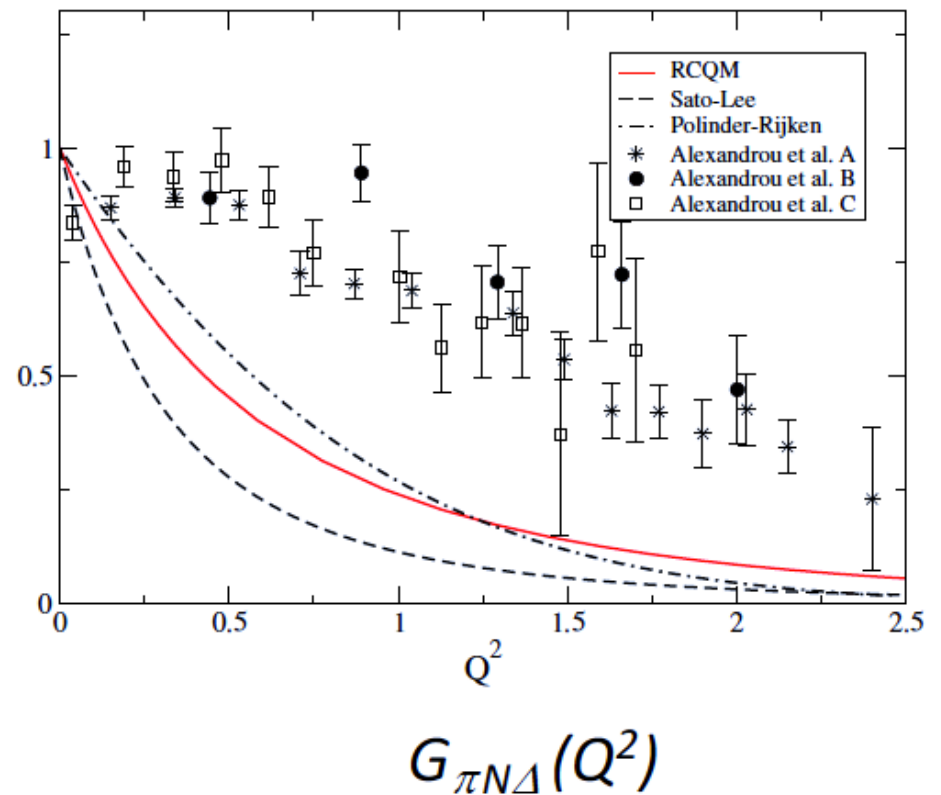
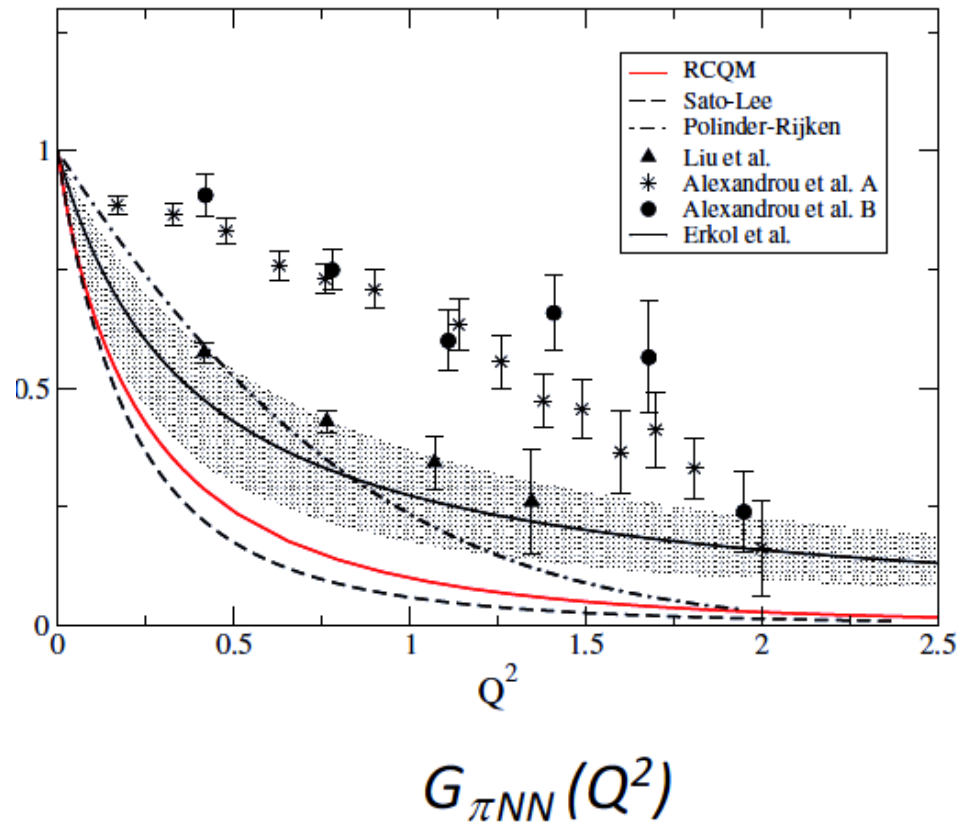
Covariant predictions of the GBE RCQM:



$$g_A^{GBE} = 1.15 \quad \text{vs.}$$

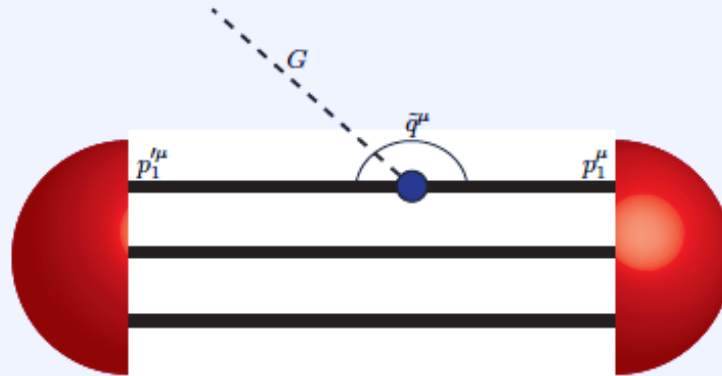
$$g_A^{exp} = 1.2695 \pm 0.0029$$

Meson-Baryon Vertices – Strong FFs



First genuine microscopic predictions of the πNN and $\pi N\Delta$ strong-interaction vertices from the relativistic Goldstone-boson-exchange constituent quark model

Gravitational Nucleon Form Factors

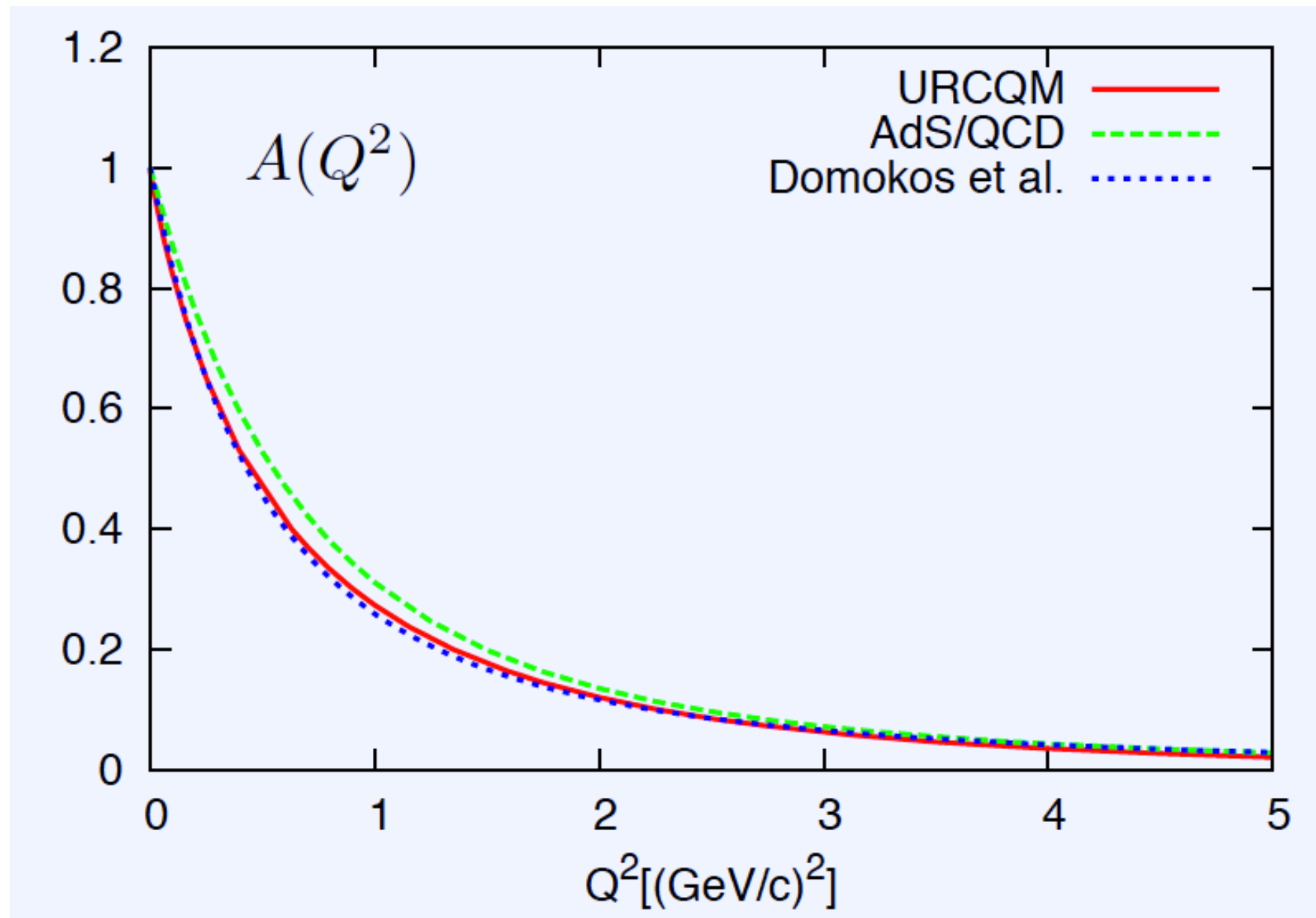


Invariant ME of **energy-momentum tensor** $\hat{\Theta}^{\mu\nu}$:

$$\langle P' J \Sigma' | \hat{\Theta}^{\mu\nu} | P J \Sigma \rangle = \bar{U}(P') \left[\gamma^{(\mu} \bar{P}^{\nu)} A(Q^2) + \frac{i}{2M} \bar{P}^{(\mu} \sigma^{\nu)} B(Q^2) + \frac{q^\mu q^\nu - q^2 g^{\mu\nu}}{M} C(Q^2) \right] U(P)$$

$$A(Q^2) \sim \langle P' J \Sigma' | \Theta^{00} | P J \Sigma \rangle$$

Gravitational Nucleon Form Factor $A(Q^2)$



Hadronic Resonance Decays

N^*, Δ^* $\rightarrow N\pi$	Experiment [MeV]	Relativistic		Nonrel. EEM	
		GBE	OGE	GBE	OGE
$N(1440)$	$(227 \pm 18)_{-59}^{+70}$	30	59	7	27
$N(1520)$	$(66 \pm 6)_{-5}^{+9}$	21	23	38	37
$N(1535)$	$(67 \pm 15)_{-17}^{+28}$	25	39	559	1183
$N(1650)$	$(109 \pm 26)_{-3}^{+36}$	6.3	9.9	157	352
$N(1675)$	$(68 \pm 8)_{-4}^{+14}$	8.4	10.4	13	16
$N(1700)$	$(10 \pm 5)_{-3}^{+3}$	1.0	1.3	2.2	2.7
$N(1710)$	$(15 \pm 5)_{-5}^{+30}$	19	21	8	6

$N \rightarrow N\eta$	Experiment [MeV]	Relativistic		Nonrel. EEM	
		GBE	OGE	GBE	OGE
$N(1520)$	$(0.28 \pm 0.05)_{-0.01}^{+0.03}$	0.1	0.1	0.04	0.04
$N(1535)$	$(64 \pm 19)_{-28}^{+28}$	27	35	127	236
$N(1650)$	$(10 \pm 5)_{-1}^{+4}$	50	74	283	623
$N(1675)$	$(0 \pm 1.5)_{-0.1}^{+0.3}$	1.5	2.4	1.1	1.8
$N(1700)$	$(0 \pm 1)_{-0.5}^{+0.5}$	0.5	0.9	0.2	0.3
$N(1710)$	$(6 \pm 1)_{-4}^{+11}$	0.02	0.06	2.9	9.3

With theoretical masses

Coupled-Channels RCQM with Explicit Mesons

Coupled-channels mass-operator eigenvalue equation

for π -dressing of a given bare $\{\widetilde{QQQ}\}$ cluster state

$$\begin{pmatrix} M_{\widetilde{QQQ}} & K_{\pi\widetilde{QQQ}} \\ K_{\pi\widetilde{QQQ}}^\dagger & M_{\widetilde{QQQ}+\pi} \end{pmatrix} \begin{pmatrix} |\psi_{QQQ}\rangle \\ |\psi_{QQQ+\pi}\rangle \end{pmatrix} = m \begin{pmatrix} |\psi_{QQQ}\rangle \\ |\psi_{QQQ+\pi}\rangle \end{pmatrix},$$

where $M_{\widetilde{QQQ}}$ is the $\{\widetilde{QQQ}\}$ mass operator with confinement.

After Feshbach elimination of the $|\psi_{QQQ+\pi}\rangle$ channel:

$$\underbrace{[M_{\widetilde{QQQ}} + K_{\pi\widetilde{QQQ}}(m - M_{\widetilde{QQQ}+\pi})^{-1}K_{\pi\widetilde{QQQ}}^\dagger]}_{V_{opt}} |\psi_{QQQ}\rangle = m|\psi_{QQQ}\rangle.$$

It is an exact eigenvalue equation for $|\psi_{QQQ}\rangle$, yielding in general a complex eigenvalue m of the π -dressed $\{QQQ\}$ system.

π -Dressing Effects on N and Δ

Predictions of the **CC RCQM**

	CC	RCQM	SL	KNLS	PR Gauss	PR Multipole
$\frac{f^2}{4\pi} \frac{\pi \tilde{N} \tilde{N}}{\pi}$	0.071	0.0691	0.08	0.08	0.013	0.013
m_N	939	939	939	939	939	939
$m_{\tilde{N}}$	1096	1067	1031	1037	1025	1051
$m_N - m_{\tilde{N}}$	-157	-128	-92	-98	-86	-112

	CC	RCQM	SL	KNLS	PR Gauss	PR Multipole
$\frac{f^2}{4\pi} \frac{\pi \tilde{N} \tilde{\Delta}}{\pi}$	0.239	0.188	0.334	0.126	0.167	0.167
m_N	939	939	939	939	939	939
$Re[m_\Delta]$	1232	1232	1232	1232	1232	1232
$m_{\tilde{\Delta}}$	1327	1309	1288	1261	1329	1347
$Re[m_\Delta] - m_{\tilde{\Delta}}$	-95	-77	-56	-29	-96	-115
$2 Im[m_\Delta] = \Gamma$	67	47	64	27	52	52
$\Gamma_{exp}(\Delta \rightarrow \pi N)$			~ 117			

(all values in MeV)

Summary and Some Open Problems

- ❖ **Baryon spectroscopy of ALL flavors** can be consistently described in a universal relativistic constituent quark model (URCQM), especially with respect to ground states
- ❖ The **nonrelativistic constituent quark model** must be discarded
- ❖ The **covariant structures of the baryon ground states** (N , Δ , Λ , Ξ , ... form factors) at low momentum transfers result in agreement with experimental observables
- ❖ Beyond that the results agree with (reliable) lattice QCD data
- ❖ **Strong baryon resonance** decays fail with $\{QQQ\}$ d.o.f. only
- ❖ A **realistic description of hadron resonances** still represents a formidable challenge (for all QCD-based approaches)
- ❖ **Inclusion of explicit meson d.o.f.** can be achieved in a coupled-channels relativistic constituent quark model
- ❖ Calculation of **baryon properties in a medium** will be an interesting task

The End

Thank you very much for your attention!