

# Hadron-quark crossover phase transition in hybrid compact stars

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## Abstract

Lattice simulation of QCD at small net baryon densities and high temperature have revealed that the transition to hadronic phase to the deconfined quark-gluon plasma is a crossover. Recently, the structure of neutron stars have been studied with a crossover equation of state by means of a switching function to model a smooth transition from a pure neutron matter to massless quarks [1]. The switch function parameter was constrained in order to reproduce neutron stars up to about two solar masses. Afterwards, such a study has been extended by considering the relevance of color superconducting quarks in the cold dense matter [2]. In this contribution, we investigate the crossover phase transition into an hybrid compact stars by means of an equation of state which incorporates hadronic matter, composed by nucleons, hyperons and  $\Delta$ -isobars degrees of freedom, and a quark phase with massive strange quarks. In this framework, we analyze the role of the strangeness content related to the bulk properties of the compact stars.

## Crossover Equation of State

We are going to study the crossover transition from hadronic nuclear matter (H) to quark matter (Q) by imposing  $\beta$ -stability and charge neutrality conditions. Following Ref. [1], the crossover feature is mimic by

$$P_{HQ}(\mu_B, \mu_C) = [1 - S(\mu_B)] P_H(\mu_B, \mu_C) + S(\mu_B) P_Q(\mu_B, \mu_C), \quad (1)$$

where the switch function is defined as [1,2]

$$S(\mu_B) = \exp[-(\mu_0/\mu_B)^r], \quad (2)$$

(in this investigation we neglect possible dependence on the electric charge chemical potential  $\mu_C$  and/or on the isospin chemical potential  $\mu_I$ ).

$P_H$  is the hadronic pressure obtained from the scheme of the SFHo relativistic mean-field (RMF) model [3] by including the full octet of the lightest baryons:  $p$ ,  $n$ ,  $\Lambda$ ,  $\Sigma^+$ ,  $\Sigma^0$ ,  $\Sigma^-$ ,  $\Xi^0$ ,  $\Xi^-$  and the  $\Delta(1232)$ -isobar degrees of freedom.  $P_Q$  is the quark pressure in an extended Bag model including first-order  $\alpha_s = \pi/2(1 - a_4)$  strong nonperturbative interaction and massive strange quark ( $m_s = 100$  MeV) [4].

The thermodynamic description of the system is obtained from the relations for the baryon density

$$\rho_B(\mu_B, \mu_C) = \left. \frac{\partial P}{\partial \mu_B} \right|_{\mu_C} = (1 - S) \rho_B^H + S \rho_B^Q + (P_Q - P_H) \frac{\partial S}{\partial \mu_B}, \quad (3)$$

the charge density

$$\rho_C(\mu_B, \mu_C) = \left. \frac{\partial P}{\partial \mu_C} \right|_{\mu_B} = (1 - S) \rho_C^H + S \rho_C^Q + (P_Q - P_H) \frac{\partial S}{\partial \mu_C}, \quad (4)$$

and the energy density

$$\epsilon_{HQ} = -P_{HQ} + \mu_B \rho_B + \mu_C \rho_C. \quad (5)$$

Moreover, we have to require the charge neutrality

$$\rho_C(\mu_B, \mu_C) = \rho_e(\mu_e), \quad (6)$$

and the  $\beta$ -stability condition:  $\mu_C = -\mu_e$ . Finally, we have  $P = P_{HQ} + P_e$  and  $\epsilon = \epsilon_{HQ} + \epsilon_e$ .

The crossover and, as a consequence, the parameters of the switch function  $S$ , are fixed so that the pressure must be convex for all  $\mu_B$  [5]

$$\partial^2 P / \partial \mu_B^2 = \partial \rho_B / \partial \mu_B > 0. \quad (7)$$

In addition, the adiabatic sound velocity

$$c_s = \sqrt{\partial P / \partial \epsilon} = \sqrt{\partial \ln \mu_B / \partial \ln \rho_B}, \quad (8)$$

cannot exceed the speed of light,  $c$ .

## Results

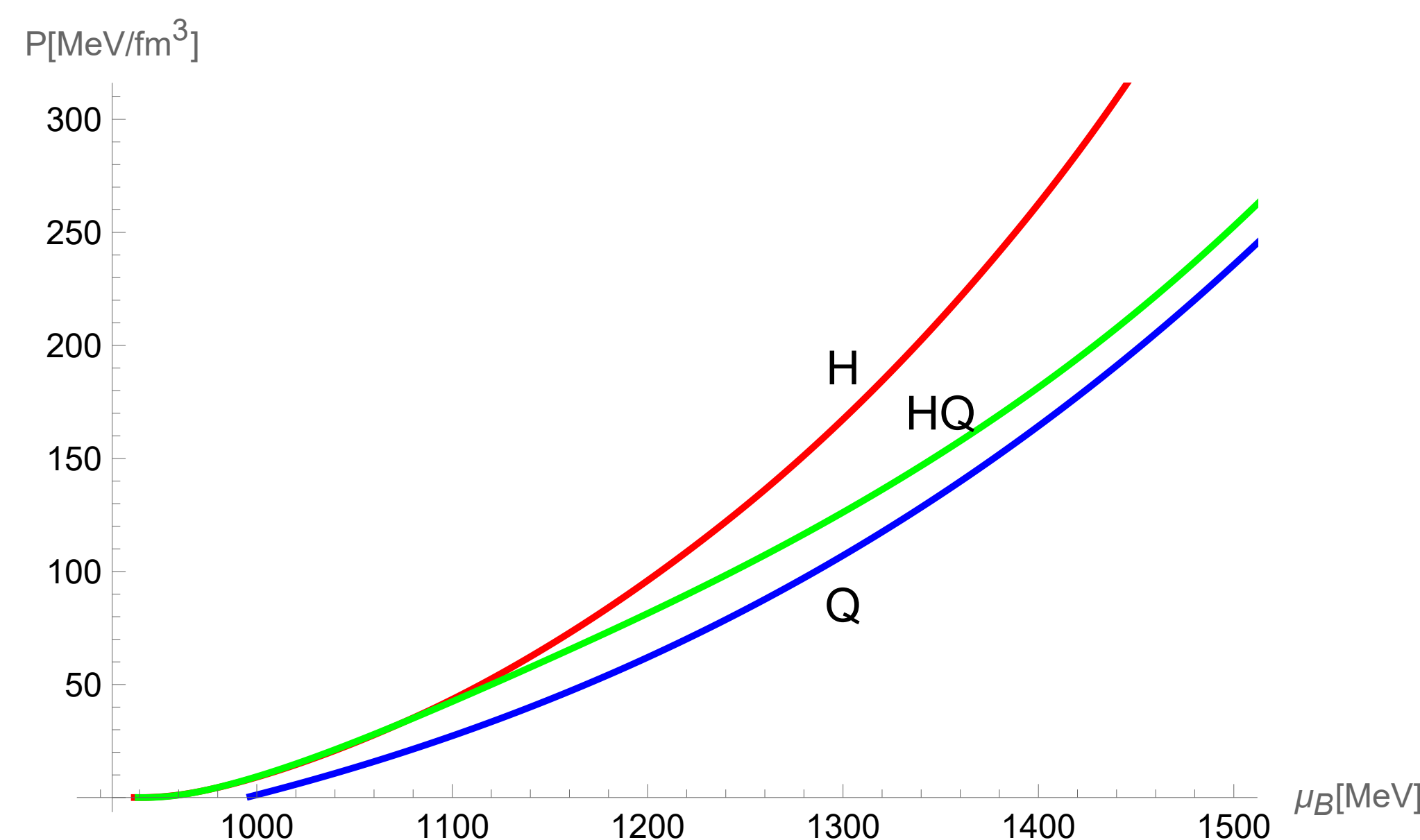


Fig. 1: Pressure as a function of the baryon chemical potential for the hadronic phase H, the pure quark phase Q and the mixed hadron-quark (HQ) crossover EOS

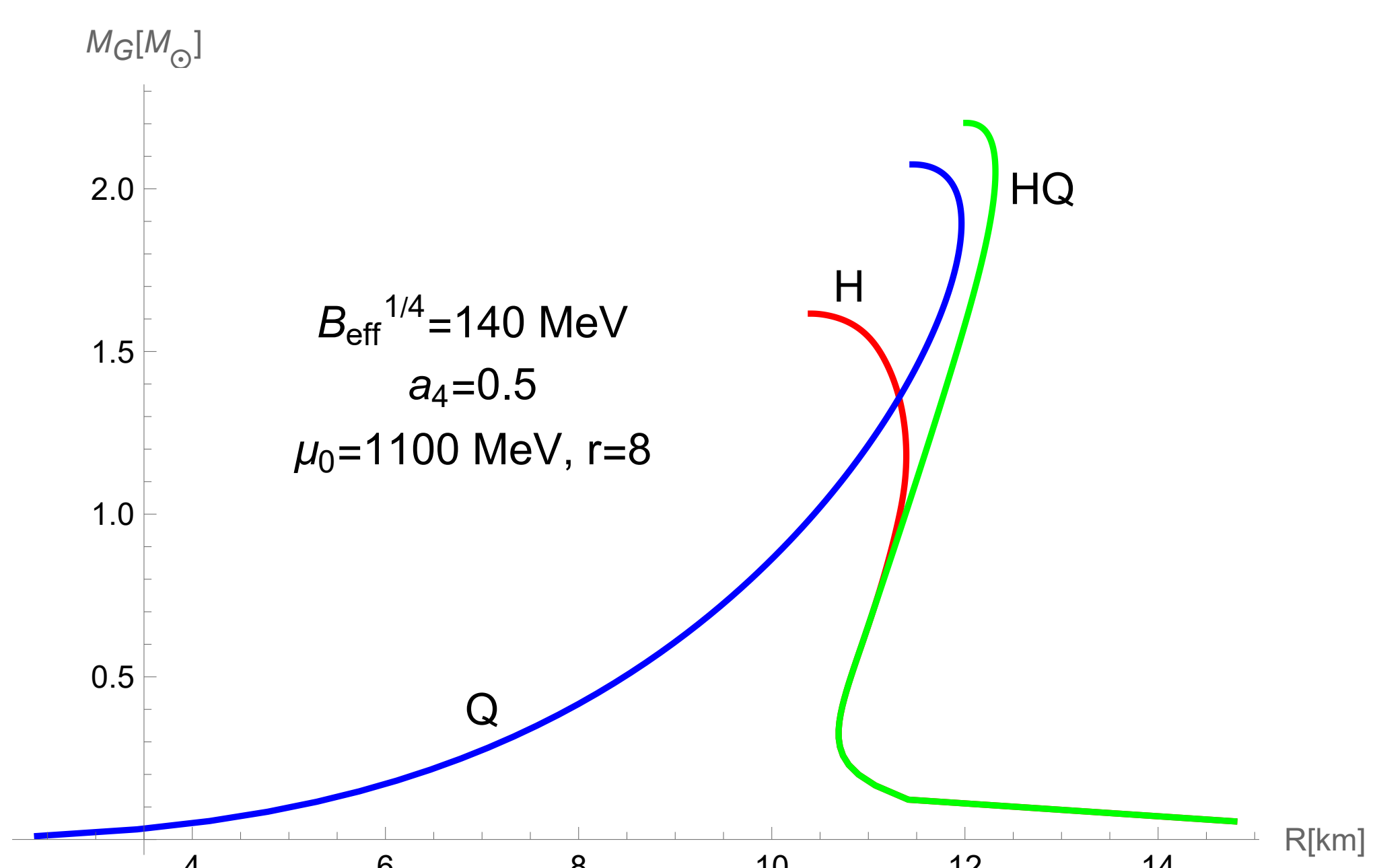


Fig. 2: Mass vs. radius for the hadronic phase H, the pure quark phase Q and the mixed hadron-quark (HQ)

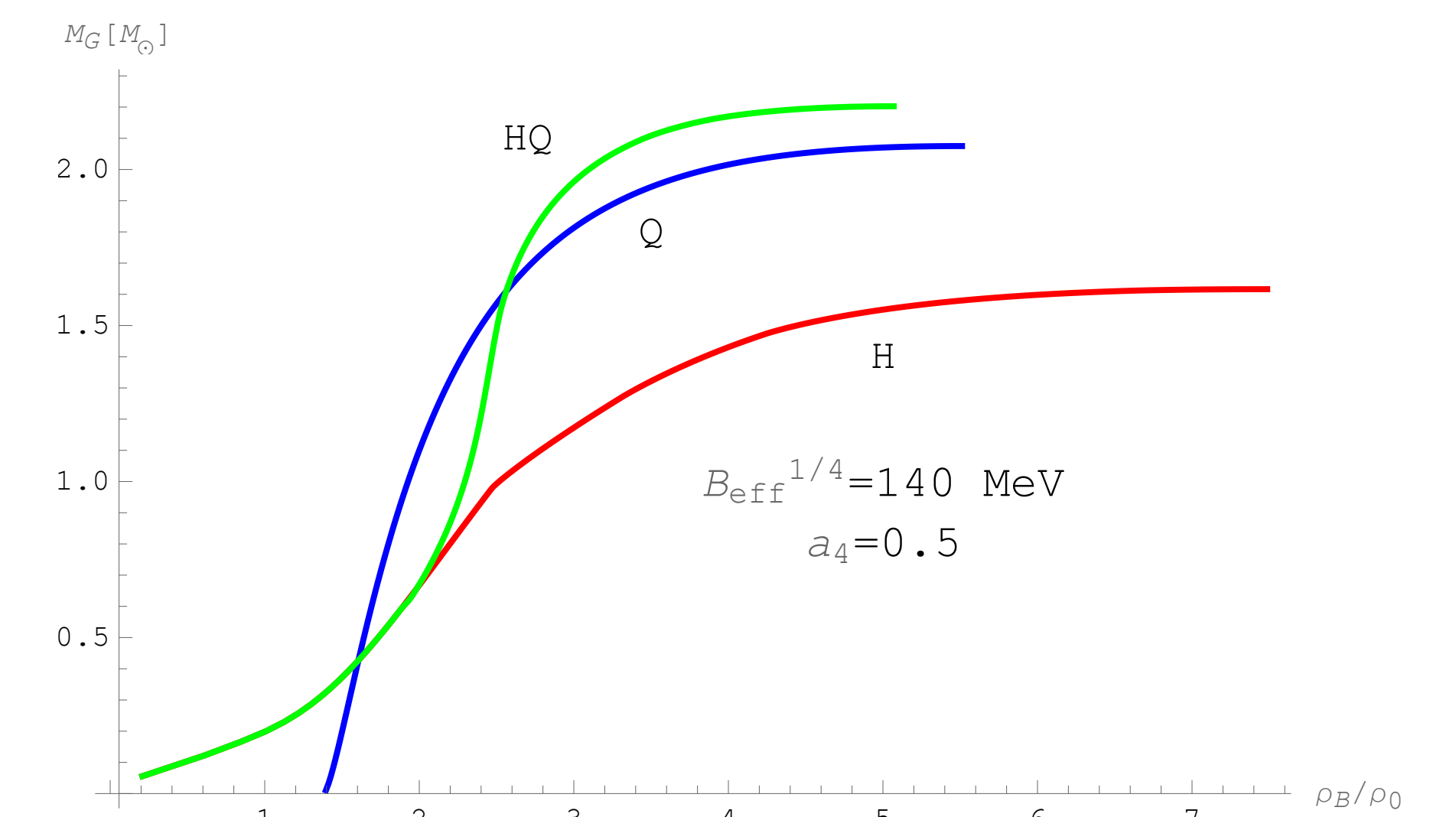


Fig. 3: Mass as a function of the central baryon density for the hadronic phase H, the pure quark phase Q and the mixed hadron-quark (HQ)

## Remarks

We have studied the crossover EOS of hybrid compact stars, composed by nucleons, hyperons,  $\Delta$ -isobars and quarks with nonperturbative effects. It is well known that adding degrees of freedom softens the equation of state, this makes it difficult to make massive neutron stars in presence of hyperons and  $\Delta$ -isobars [7]. As discussed in Ref. [8], this problem could be overcome in the scenario of two coexisting families of compact stars: hadronic stars, whose EOS is soft, can be very compact with small radii and with maximum masses of about  $1.5 M_\odot$ , while massive strange quark stars, whose EOS is stiff, with masses greater than  $2 M_\odot$ . We have seen that massive compact stars configurations can be realized for a particular crossover EOS in presence of strong nonperturbative effects. In this context, let us remember that we are considering a system with two conserved charges, in this case the dynamics of the phase transition is more complex with respect to the one (baryon) conserved charge (related to the crossing of the hadron and quark curves in the  $P - \mu_B$  plane).

We are planning to extend this preliminary investigation by taking into account color superconducting quarks effects and the role of isospin asymmetry in the crossover switch function.

## References

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