



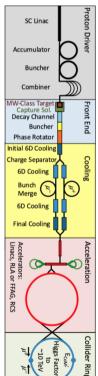
## Muon Collider: MDI – Machine-Detector and Beam Induced Background

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Colliders of Tomorrow: Muon Collider Beam Background

10 Aug 2023





### **Outline**

- Muon collider (MC):
  - Concept and motivations
  - Advantages and radiation challenges
- Machine-Detector Interface (MDI):
  - Geometry of the interaction region
  - Conical nozzle to mitigate the background: nozzle
  - Workflow in IMCC
  - Main aspects under study
- Beam-Induced Background (BIB) from μ-decay at different energies
  - Total number of BIB particles for different machines
  - Effect of the lattice at  $\sqrt{s}$  = 10 TeV
  - Nozzle effect
- Incoherent pair production background
  - Secondary source of background important at high energy
- Halo losses: BIB first assessment
- Long term detector damage
- **Forward muons:** nozzle interference for high η
- Conclusions

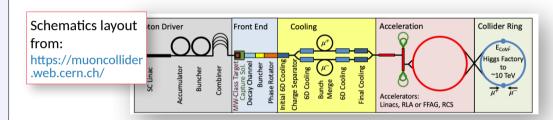


## Muon collider: concept and motivations

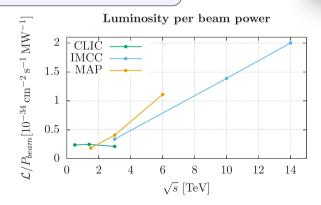
Among various particles accelerated in colliders, muons have already been under consideration for a long time [1]. Very promising results were achieved in the contest of the MAP collaboration [2-3]. The following work is in the context and on behalf of the International Muon Collider Collaboration (IMCC).

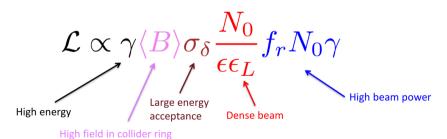
#### Why?

- A multi-TeV muon collider could investigate Higgs properties with an unprecedented precision. [2]
- With  $\sqrt{s}$  = 10 TeV we can explore **new** physics at high energies. [2]



With a muon collider the **luminosity per beam power** increases with the collider energy!





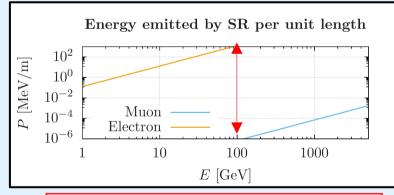


## Muon collider: advantages

#### **Synchrotron radiation\***

 $m_u = 105.7 \text{ MeV/c}^2$ 

 Synchrotron radiation (SR) is not a limiting factor for muon circular colliders.



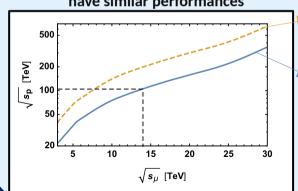
Muons emit  $(m_{\mu}/m_e)^4 = 1.6 \cdot 10^9$  less synchrotron radiation than electrons

\*of the primary muon beam

#### **Lepton collisions**

- Muons are elementary particles, and all the energy is involved in the collision. Instead, in protons, the energy is shared among constituents.
- Same performance of proton colliders, but with much lower center of mass energy! [2]

Energies at which proton/μ-colliders have similar performances



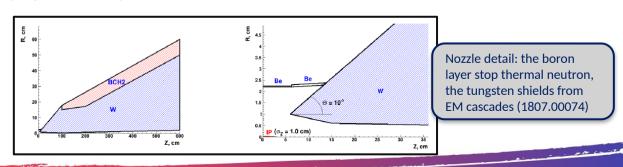
Assuming comparable Feynman amplitudes for muon and proton production processes

Proton production enhanced due to QCD production (factor of 10)



### **Previous studies in MAP**

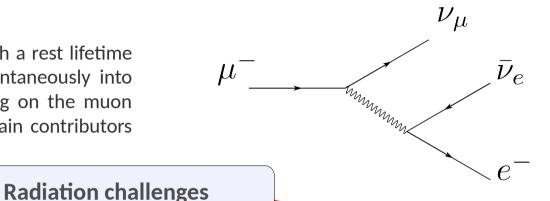
- The renewed efforts in the **International Muon Collider Collaboration (IMCC)** benefit from the previous work done in the **Muon Accelerator Program (MAP)**.
- Extensive work has been done in various field, among which:
  - Design of a muon production target handling ~MW proton sources
  - Exploration studies in the muon cooling
  - Magnet and shielding design to protect coils from decay products
  - Interaction region design to mitigate the background to the detectors
- To mitigate the BIB, particular attention has been devolved to the nozzles. This shielding equipment has been carefully optimized up to √s=1.5 TeV colliders





## Muon collider: radiation challenges

• Muons are unstable particles, with a rest lifetime of  $\tau$  = 2.197  $\mu$ s. They decay spontaneously into electron and positrons (depending on the muon original charge), which are the main contributors to the secondary radiation field.



#### **Superconducting magnets**

Secondary electrons impact on the beam chamber. Their energy induce **heat** and long term radiation **damage** in the **superconducting coils.** 

#### **MDI**

The secondary field is a source of **background** to the experiment and induce radiation **damage** to the **detectors**.

#### **Neutrino radiation**

High energy **neutrinos** from the muon decay interact with the rock delivering **dose** to the **environment**.



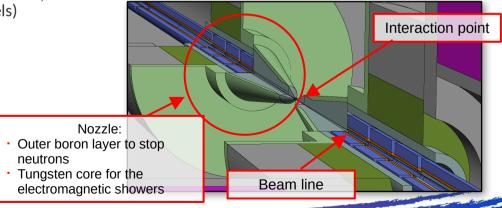
## **Interaction region: MDI**

- MDI is a **difficult challenge** for the muon collider. First studies were done by the MAP collaboration (energies up to 6 TeV). So far, IMCC focused on studies for energies up to 10 TeV.
- Main objectives:
  - Study the beam-induced background (BIB) and identify mitigation strategies for the 3 TeV and 10(+) TeV collider options.
  - Develop a credible interaction region (IR) design that yields background levels compatible with detector operation (1. enabling physics performance reach, 2. reducing radiation damage to acceptable levels)

#### MDI Working Group:

- Formed last year in course of the Muon Collider Community meetings
- Shall bring together expertise from different areas (lattice design, particle-matter interactions, detectors, magnets etc.)
- Meetings every last Friday of a month (<u>Indico</u> <u>event category</u>)

### **Geometry** of the MDI



## Tentative target parameters Scaled from MAP parameters

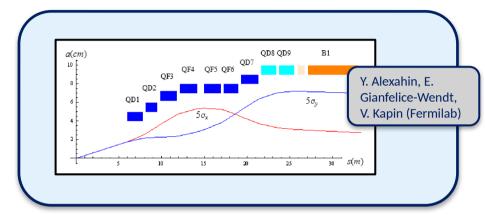
Comparison: CLIC at 3 TeV: 28 MW

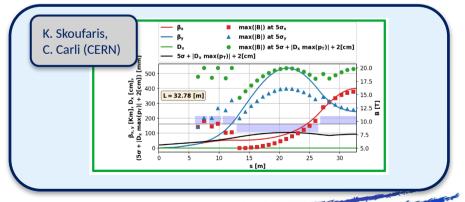
Parameter	Unit	3 TeV	10 TeV	14 TeV
L	10 <sup>34</sup> cm <sup>-2</sup> s <sup>-1</sup>	1.8	20	40
N	1012	2.2	1.8	1.8
f <sub>r</sub>	Hz	5	5	5
P <sub>beam</sub>	MW	5.3	14.4	20
С	km	4.5	10	14



## MDI: lattices used for background studies

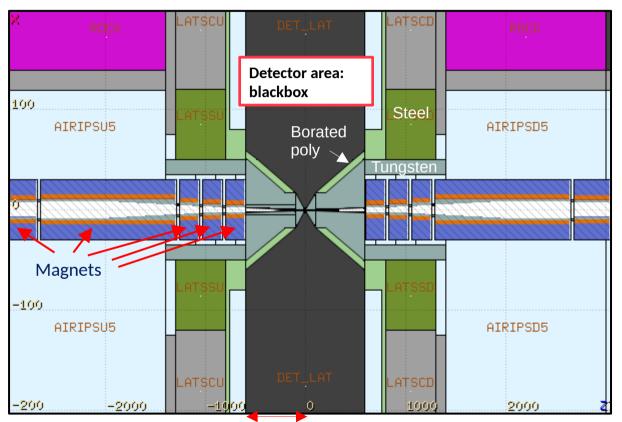
- $\sqrt{s} = 3$  TeV IR lattice taken from US-MAP (Y. Alexahin et al 2018 JINST 13 P11002):
  - L\* = 6 m
  - Quadruplet final focus with combined function magnets (ß\* = 5 mm)
  - Maximum field at inner bore is 12 T
- $\sqrt{s}$  = 10 TeV IR lattice was developed from scratch within IMCC:
  - $L^* = 6 \text{ m}$  as baseline
  - Triplet layout (ß\* = 1.5 mm), optionally with and without dipolar component
  - Max field at inner bore is 20 T







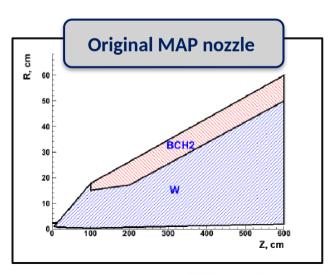
## MDI: geometry of a 10 TeV collider

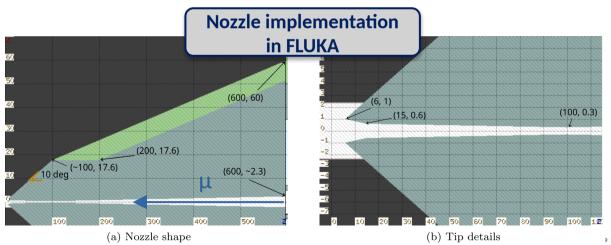




## **MDI:** nozzle geometry

- Our implementation of the nozzle follows the original design from MAP collaboration
- The scope of the solid tungsten layer is to have a dense material to stop electromagnetic cascades
- The **boron polyethylene** layer acts as moderator (the hydrogen atoms), while the boron content is **capturing** the thermalized **neutrons**.







### Workflow in the IMCC

Example of a LB application: LHC IR7

2. FLUKA geometry model

The magnet optics is computed via dedicated codes (e.g. MAD-X).

Via LineBuilder (LB), complex geometries are assembled in a FLUKA input file

The output is a twiss file, containing the machine elements in a sequence

1. Lattice design

3. BIB simulation

With the built geometry, a FLUKA simulation is run.

The position and momentum of the decay muons are sampled from the matched phase-space

Iteration with lattice design experts to mitigate the BIB

BIB data to detector experts

Machine-Detector

Interface: MDI

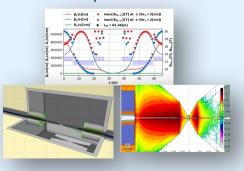
CERN STI/BMI is currently responsible for the geometry built at  $\sqrt{s}$  = 3 and 10 TeV



## MDI: main aspects under study

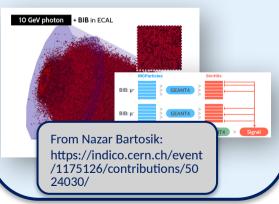
# Background and radiation damage in detector\*

Develop a credible interaction region (IR) design that yields background levels compatible with detector operation



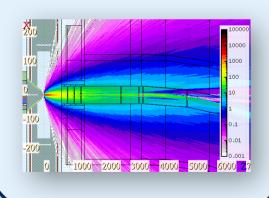
# BIB data handling in collaboration with detector simulation

Establish a coherent framework to share the simulated background for the signal reconstruction



## MDI design for forward muon detection

Incorporate forward muon detection needs in the design choices.

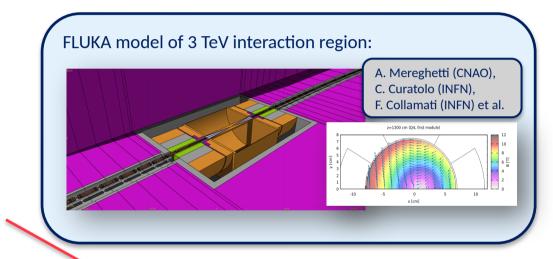


<sup>\*</sup>Most relevant point, and this presentation will focus mostly on this



## Status of the background studies for the √s = 3 TeV collider

- $\sqrt{s} = 3$  TeV BIB studies with FLUKA:
  - The procedure used to verify the beaminduced background at = 1.5 TeV (F. Collamati et al 2021 JINST 16 P11009) is being used to study background at = 3 TeV
  - Nozzle inspired by 1.5 TeV MAP design (N. Mokhov)
  - Particle distributions were used for first detector studies
  - Dose/neutron fluence maps for detector
  - Renewed effort in assessing the background reported in L. Castelli presentation during 2023 IMCC annual meeting

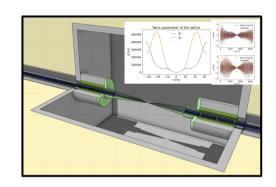


See presentation of D. Lucchesi in the IMCC Accelerator meeting Nov 14, 2022



# Status of the background studies for the √s = 10 TeV collider

- Simulation model (FLUKA):
  - Started with a nozzle inspired by 1.5 TeV MAP design (N. Mokhov)
  - Conical W liners in magnets which follow  $5\sigma$  beam envelope
  - Muon decay sampling → fully matched beam phase space distr.
- Topics addressed so far for the 10 TeV collider:
  - Is the decay-induced background worse than in a 3 TeV collider?
  - Impact of lattice design choices on the decay background
  - Assessment of the nozzle optimization potential for 10 TeV
  - Assessment of the contribution of incoherent electron-positron pair production
  - Estimate of the cumulative radiation damage in the detector
  - First study of forward muons from IP (muon tagging)



See next

slides

Results with MAP-like nozzle yield similar number of particles entering detector for 3 TeV and 10 TeV:

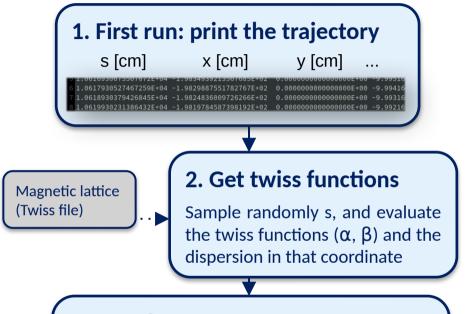
Monte Carlo simulator	FLUKA	FLUKA
Beam energy [GeV]	1500	5000
$\mu$ decay length [m]	$93.5 \cdot 10^{5}$	$311.7 \cdot 10^{5}$
μ decay/m/bunch	$2.1 \cdot 10^{5}$	$0.64 \cdot 10^{5}$
Photons $(E_{\gamma} > 0.1 \text{ MeV})$	$70 \cdot 10^{6}$	$107 \cdot 10^{6}$
Neutrons $(E_n > 1 \text{ MeV})$	$91 \cdot 10^{6}$	$101 \cdot 10^{6}$
Electrons & positrons ( $E_{e^{\pm}} > 0.1 \text{ MeV}$ )	$1.1 \cdot 10^{6}$	$0.92 \cdot 10^{6}$
Charged hadroms ( $E_{h^{\pm}} > 0.1 \text{ MeV}$ )	$0.020 \cdot 10^{6}$	$0.044 \cdot 10^{6}$
Muons $(E_{\mu^{\pm}} > 0.1 \text{ MeV})$	$0.0033 \cdot 10^{6}$	$0.0048 \cdot 10^{6}$

From Snowmass white paper.



## μ decay: sampling procedure

- For an accurate description, I propose to sample the muon decays position and momentum from a matched phase-space distribution.
- Once the position and momentum of the muons are known, the muon decay is forced.
- Results are naturally expressed per muon decay.
- Muons do not need to be tracked in the machine (+ save CPU time & + no tracking inaccuracy)

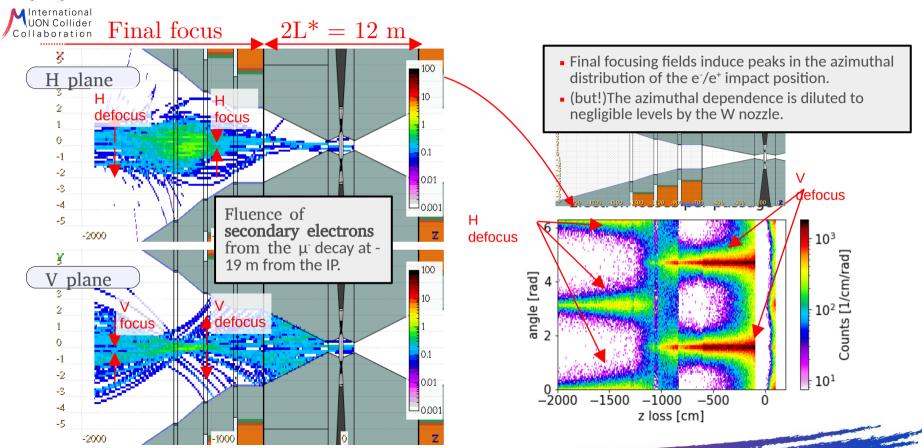


### 3. Sample muon

Given the muon in the ideal trajectory, sample the muon position and momentum from the linear optic corrections (appendix 1).



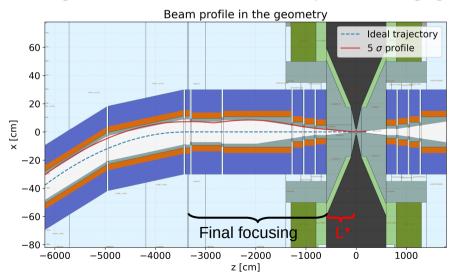
## μ decay: e<sup>+/-</sup> impact on aperture





## μ decay: original lattice

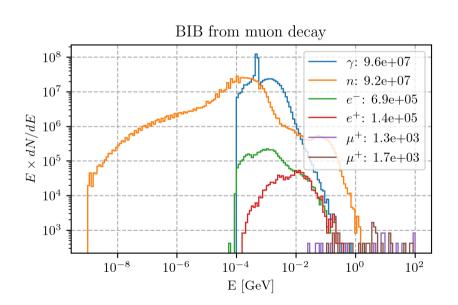
- The original preliminary lattice consisted of a L\* = 6m, followed by the final focusing scheme. This consisted of a straight section containing quadrupoles up to ~35 m from the IP.
- The contribution coming from the bent section is proven negligible





## $\mu$ decay @ $\sqrt{s}$ = 10 TeV: particle spectra

Considering the starting simplified lattice, the BIB particle multiplicity has been evaluated.



			Opuateu:
Collider energy	1.5 TeV	3 TeV	10 TeV
Photons	7.1E+7	9.6E+7	9.6E+7
Neutron	4.7E+7	5.8E+7	9.2E+7
e+/e-	7.1E+5	9.3E+5	8.3E+5
Ch. hadrons	1.7E+4	2.0E+4	3.0E+4
Muons	3.1E+3	3.3E+3	2.9E+3

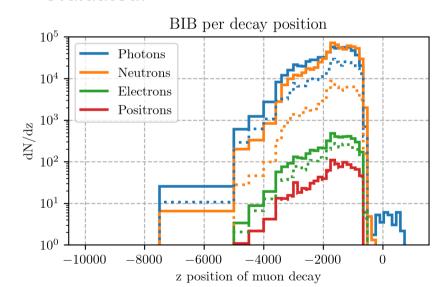
Data from: https://arxiv.org/pdf/2209.01318.pdf

Undated



## $\mu$ decay @ √s = 10 TeV: particle origin

 Considering the starting simplified lattice, the BIB particle multiplicity has been evaluated.



			Updated!
Collider energy	1.5 TeV	3 TeV	10 TeV
Photons	7.1E+7	9.6E+7	9.6E+7
Neutron	4.7E+7	5.8E+7	9.2E+7
e+/e-	7.1E+5	9.3E+5	8.3E+5
Ch. hadrons	1.7E+4	2.0E+4	3.0E+4
Muons	3.1E+3	3.3E+3	2.9E+3

Data from:

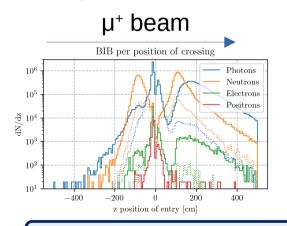
https://arxiv.org/pdf/2209.01318.pdf

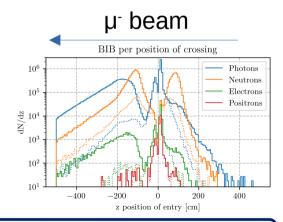
Dashed line for particles arriving in the time window of [-5, 15] ns



# µ decay @ √s = 10 TeV: different beams contribution

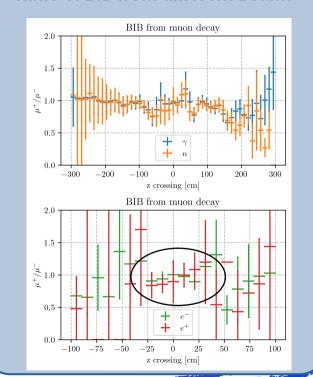
- Most of the 10 TeV simulations are conducted with a  $\mu^+$  beam. To confirm that the contribution from the opposite beam is the same, a comparison has been done.
- The simulations (comparing also energy spectra) do not show any systematic difference!





Dashed line for particles arriving in the time window of [-5, 15] ns

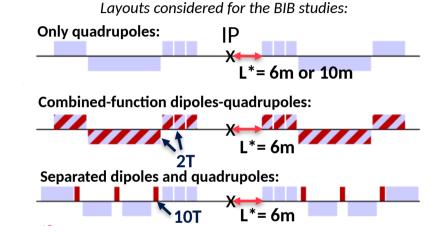
#### Ratio of BIB from different beams





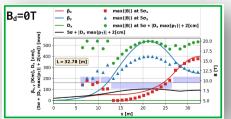
## $\mu$ decay @ $\sqrt{s}$ = 10 TeV: lattice design choices

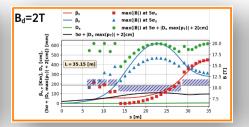
- Can the decay-induced background be reduced by adjusting the lattice design?
- Two key aspects were investigated:
  - Dipolar component in the final focus triplet (combined function magnets or separate dipoles)
  - Distance between IP and final focus magnets (L\*)

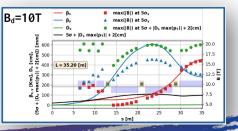


Lattices with and without dipolar component (L\*=6m):

K. Skoufaris



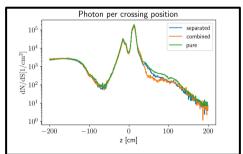


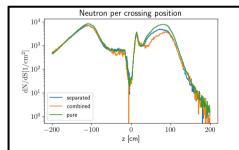




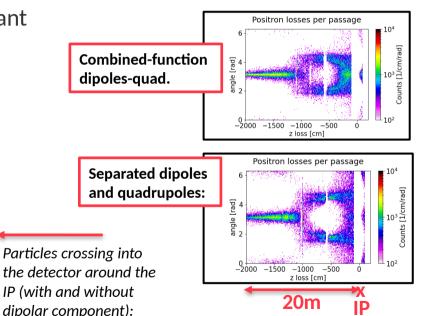
## $\mu$ decay @ $\sqrt{s}$ = 10 TeV: dipolar component

- The presence of a dipolar component changes the loss distribution of decay-e<sup>-</sup>/e<sup>+</sup> on the aperture
- Some reduction of the contribution from distant decays
- However, the overall benefits are limited





Only quadrupoles

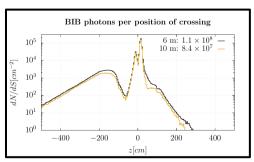


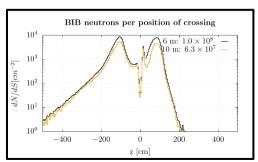
MDI meeting #5, 29/05/2022

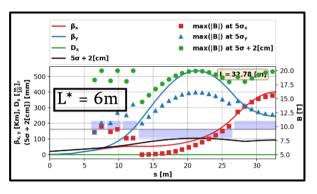


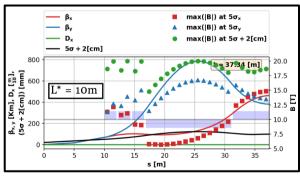
## $\mu$ decay @ $\sqrt{s}$ = 10 TeV: different L\*

- The 10 TeV MDI studies show that μ-decays between IP and first quad contribute little to the BIB – is it beneficial to increase L\*?
- With L\*= 10 m, some reduction of the particle fluence is found around the IP compared to L\*= 6 m
- Nevertheless, the gain is not large enough to justify the increase of L\*







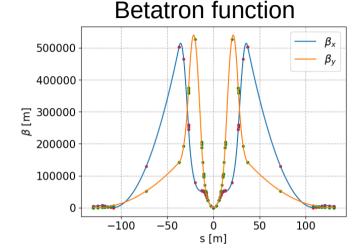


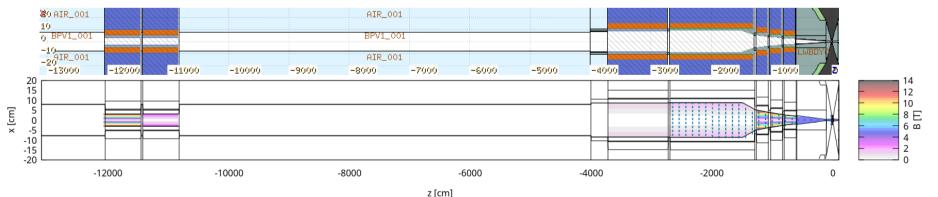
K. Skoufaris



## $\mu$ decay @ $\sqrt{s}$ = 10 TeV: new lattice (v.06)

- For a realistic machine, the final focusing schemes studied so far do not represent a satisfactory scenario.
  - A new lattice was provided by K. Skoufaris containing a very long straight section before the nozzle
  - Electrons produced in the drift section are not overbent or deflected by strong quadrupoles nor dipoles!

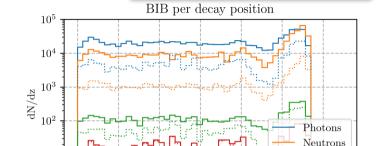






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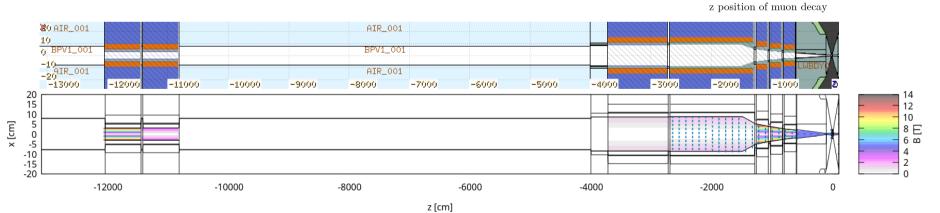
-6000

-4000

-8000

-12000 -10000

Dashed line: with time cut

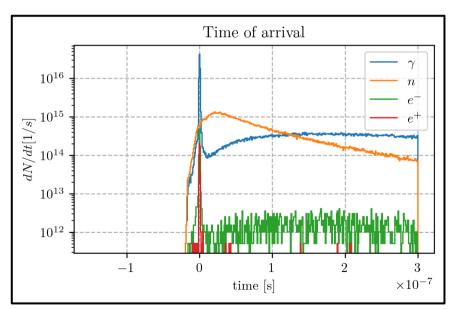


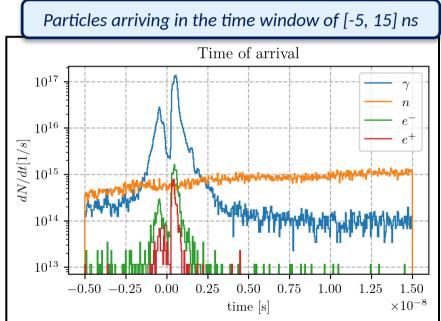
Electrons
Positrons



# µ decay @ √s = 10 TeV: new lattice (v.06) time distribution

Part of the BIB arrives with delayed times in comparison with the bunch crossing. Applying a time cut
offers the possibility to strongly reduce this background.

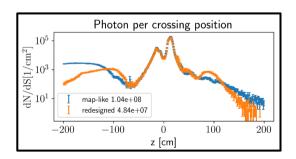


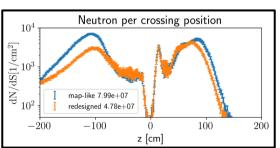


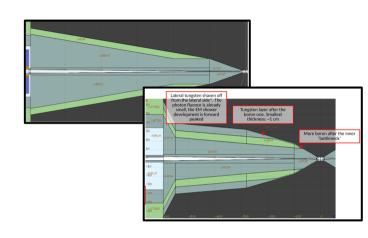


## $\mu$ decay @ $\sqrt{s}$ = 10 TeV: nozzle optimization (1)

- So far, a proof of concept for the nozzle optimization has been conducted.
- The next step will be to start from scratches and perform a nozzle optimization for the 10 TeV machine, having in mind the detector performance
- Room for improvement!







MDI meeting #6, 29/06/2022

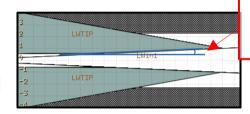


## $\mu$ decay @ $\sqrt{s}$ = 10 TeV: nozzle optimization (2)

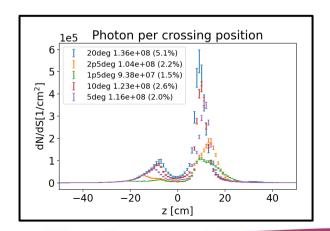
- So far, a proof of concept for the nozzle optimization has been conducted.
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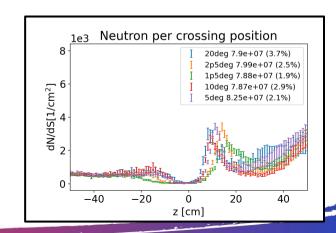
the detector performance

Room for improvement!



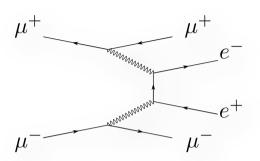
Starting from 2.5 deg, we modify this angle.



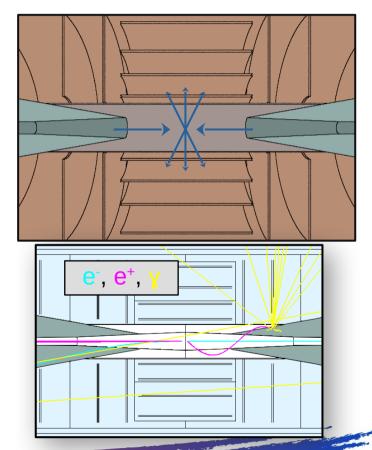




### Incoherent pair production: phenomenon



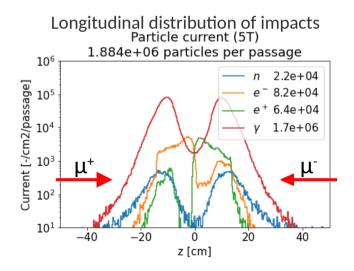
- At very high beam energies, beam-beam effects are not negligible. The most important phenomenon is due to the incoherent beam-beam pair production μ+μ-→μ+μ-e+e-.
  - The incoherent pair production e⁺/e⁻ are provided by D. Schulte and are obtained by a **Guinea-Pig simulation**
- The total number of crossing is much lower than the muon decay case.
- The produced electrons are energetic and they impact directly on the detectors, since are generated in the IP, hence they might be dangerous despite the low total number.

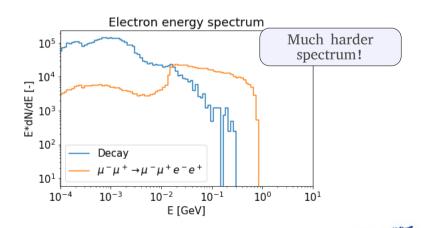




## Incoherent pair production: space distribution

- The trajectory of the pairs is curved by the solenoidal 5 T magnetic field.
- Most of the particles enter in the detector area as photons produced in the nozzle

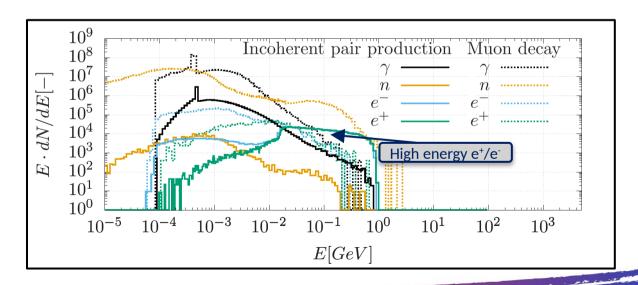






## Incoherent pair production: spectra

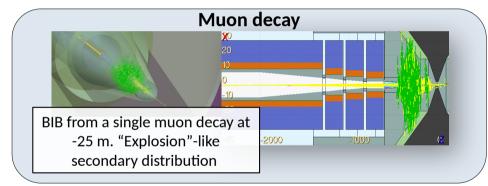
- The total BIB multiplicity is much smaller than the one coming from the muon decay
- However, the spectrum is significantly harder, and the BIB is in time with the signal

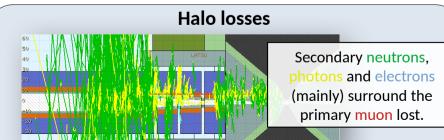




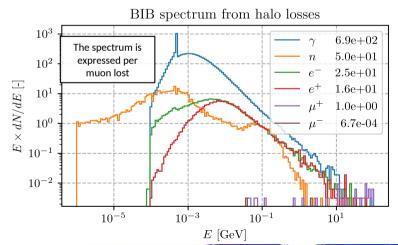
## Halo losses: spectra

- The halo losses gives a significantly different contribution to the BIB: the particles are generated close to the IP due to the muon interaction with the nozzle.
- As a preliminary simulation, we considered a muon beam going in the magnet at 0 degrees with the z axis



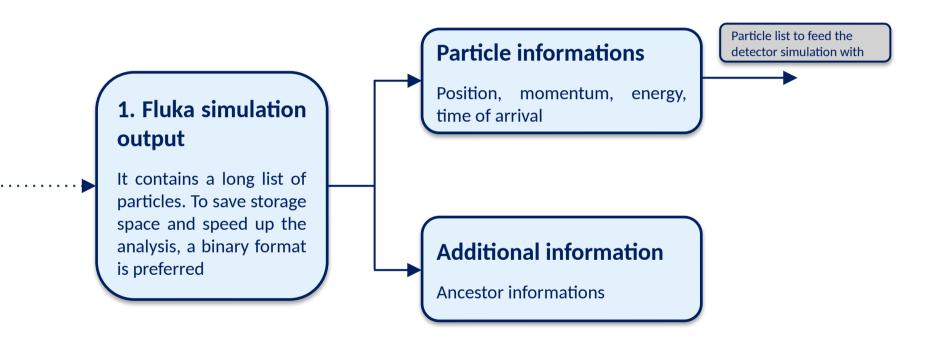


 In terms of n and γ, the muon decay produces ~10<sup>8</sup> particle per bunch crossing. To have the same contribution here, we would need to lose ~2E5 muons in the final focusing.





## How to read BIB data: FLUKA output





### How to read BIB data: data format

Question: are these variables descriptive (and sufficient) to understand the BIB

sources? Suggestions are well accepted

variables for the detector studies?

//y/z p<sub>x</sub>/p<sub>y</sub>/p<sub>z</sub> Time at

What is a "parent"? Are there any insightful

Id particle	ld parent	Energy	x/y/z	$p_x/p_y/p_z$	Time of crossing	x/y/z sampling	x/y/z parent	p <sub>x</sub> /p <sub>y</sub> /p <sub>z</sub> parent	Time at generation
Integer	Integer	Double	Double (x 3)	Double (x 3)	Double	Double (x 3)	Double (x 3)	Double (x 3)	Double

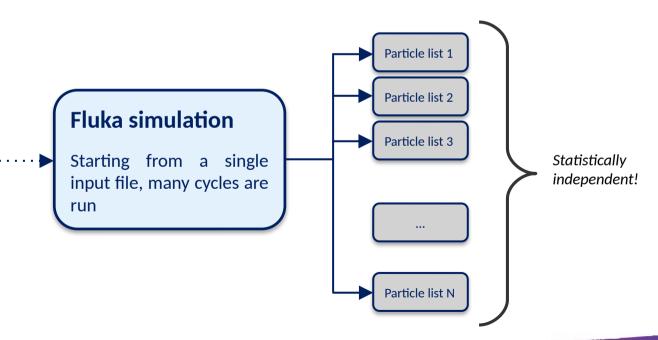
00000000: 0700 0000 0000 0000 fbb2 9397 b9db 353f 00000010: 0a7e 778f 357b f4bf 72da e775 b03d 0040 000000020: a467 dd2a 1c5c 27c0 0f5f a698 d8de e8bf Little endian 930: b001 93bf 6ed9 d83f d0c7 8226 ffb0 dfbf 000000050: e06b 1731 2ea7 d03f 5a23 1df7 850b 01c0

Example: a photon (particle id = 7), with energy 0.710383952 GeV, is crossing in the detector area in (-1.91, 2.00, -2.61)



## How to read BIB data: data organization

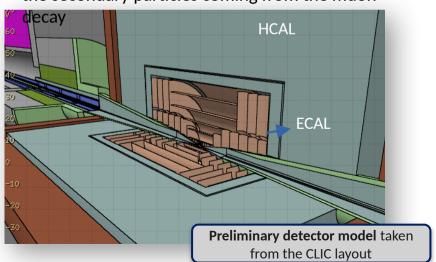
 Each simulation is run in parallel in many cycles. To estimate the uncertainty, I do a batch statistical analysis.

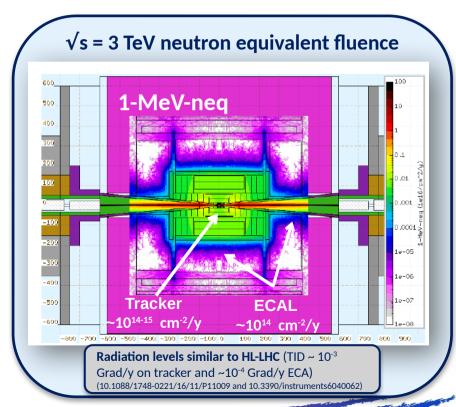




# Long term detector damage: FLUKA detector implementation

- The first detector FLUKA implementation follows the CLIC models.
- In the context of BIB studies, the detector damage is studied.
- The only source of detector damage considered are the secondary particles coming from the muon

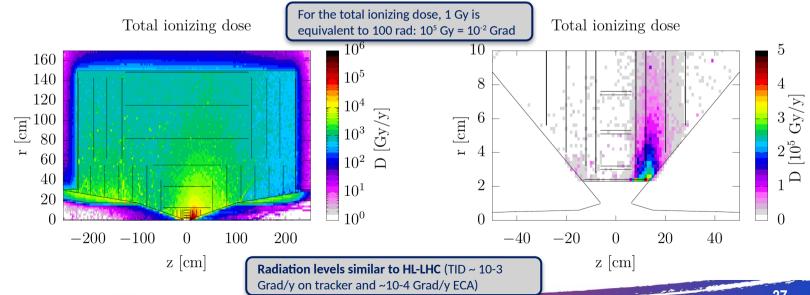






## Long term detector damage: √s = 10 TeV total ionizing dose

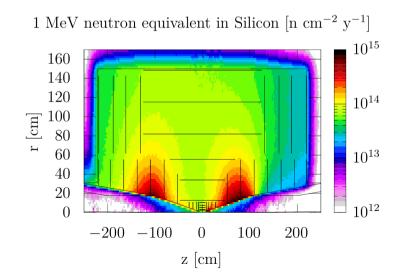
- As operational lifetime, we assume to work for 5 years. Each year, we assume to work for 1.2E7 seconds (139) days). In comparison with the nominal luminosity and the target integrated luminosity, we have a 20% safety factor.
- In the plots, the effects of one beam (left to right) are shown

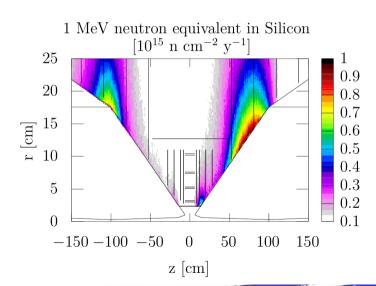




# Long term detector damage: √s = 10 TeV total displacement damage

- As operational lifetime, we assume to work for 5 years. Each year, we assume to work for 1.2E7 seconds (139 days). In comparison with the nominal luminosity and the target integrated luminosity, we have a 20% safety factor.
- In the plots, the effects of one beam (left to right) are shown







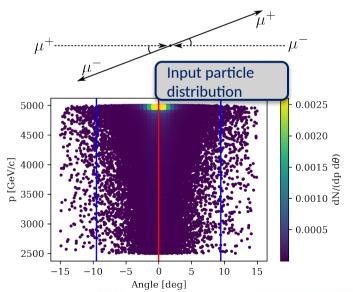
#### Forward muon detection: introduction

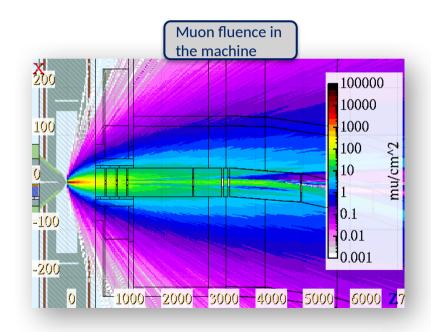
- During the annual meeting, Maximilian Ruhdorfer clearly shown the physics interest in tagging forward directed muons (this talk). 'Coverage of very forward muons is crucial'.
- For a full coverage,  $\eta$  above 6. At  $\eta$  = 2.44 ( $\vartheta$  = 10°), all the signal is removed.
- The muon collider requires thick nozzles to mitigate the enormous BIB to the detectors generated by the decaying beams.
- The a part of the forward muons crosses the shielding and machine components before it can be detected.
- In this study, I simulated the **propagation of very forward muons** in the machine. We want to understand *if*, *how* and *where* these muons can be detected.
- All results here are preliminary



#### Forward muon detection: first test case

 Matthew Forslund generated and Massimo Casarsa provided us a muon list containing both μ<sup>+</sup> and μ<sup>-</sup> in case of a VBF possible process.

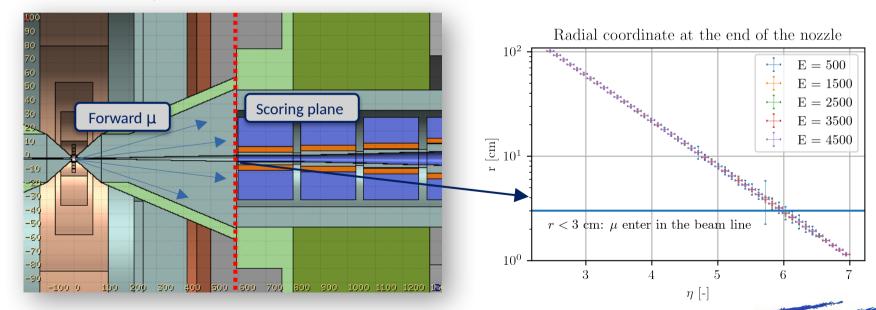






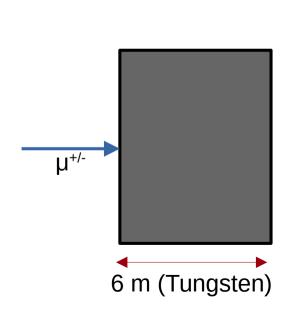
• Assuming isotropy in the  $\phi$  angle, I made some simulation for the forward muons emitted at various energies and angles in the interaction point.

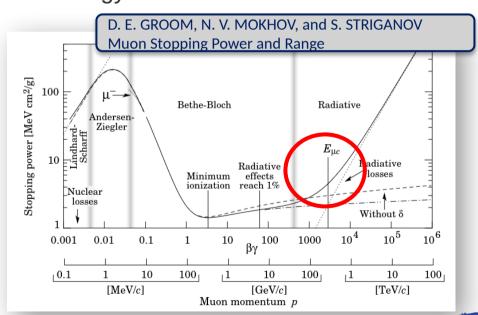
$$\eta \equiv -\ln\!\left[ an\!\left(rac{ heta}{2}
ight)
ight]$$





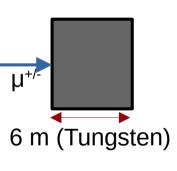
Within a large pseudo-rapidity range, muons will cross a large portion of the tungsten nozzle. They lose energy in it!

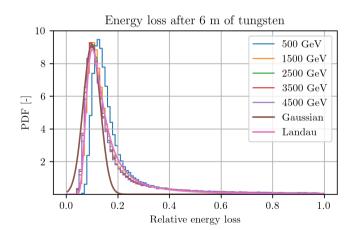


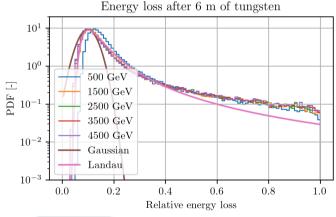




 The energy loss distribution depends on the interaction mechanism (energy straggling). The energy loss follows the Landau distribution.



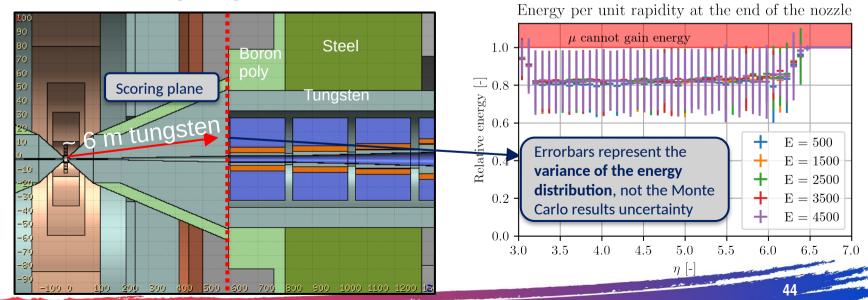




$$p(x;\mu,c) = rac{1}{\pi c} \int_0^\infty e^{-t} \cos\!\left(t\left(rac{x-\mu}{c}
ight) + rac{2t}{\pi} \log\!\left(rac{t}{c}
ight)
ight) dt$$

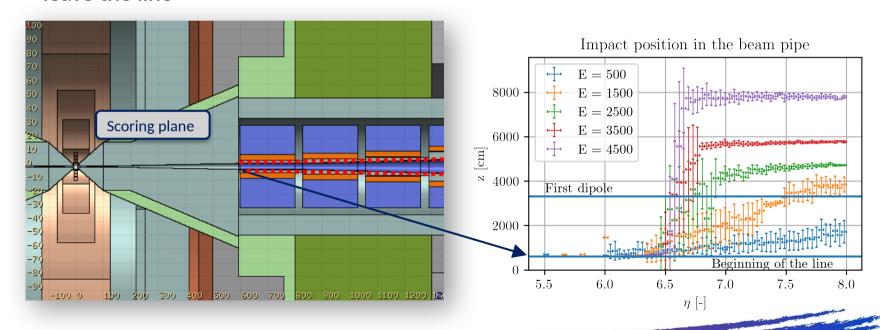


- As expected, the energy loss distibution is similar for all the  $\eta$  values.
- Behind the nozzle there are machine elements ( $\eta > 3.7$ ) and further lateral shielding ( $\eta < 3.7$ )  $\rightarrow$  potentially higher energy straggling
- Forward muons were not a primary MDI requirement. We can include them in future shielding design.





 When the pseudorapidity is large enough (~6.5) the muons do not touch the tungsten and go directly in the beam pipe. There, they cross the magnet and leave the line





#### **Conclusions**

- **BIB from muon decay** has been assessed with various configuration:
  - A dipolar component offers only a slight beneficial contribution to the BIB mitigation
  - The new lattice with a long drift increases the BIB multiplicity of a factor 2
- The negative muon beam and the positive one have the same effect for what concerns the BIB from muon decay
- Incoherent pair production is a non negligible background at high energies. This should be included with the BIB from muon decay in the detector design
- The halo losses could pose a threat only if a large fraction of the beam is lost at the final focusing. A tracking study could be necessary to better assess this contribution
- The nozzle still remains the most important element in the MDI. A systematic optimization is necessary, once an agreement is reached for the final focusing lattice
- The long term radiation damage has been assessed. From preliminary simulation, the damage is comparable with the Hi-Lumi LHC upgrade
- Tracking and measuring forward muons can be challenging. Nevertheless, we should keep these in thought during the MDI design process





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## Particle sampling in linear optics

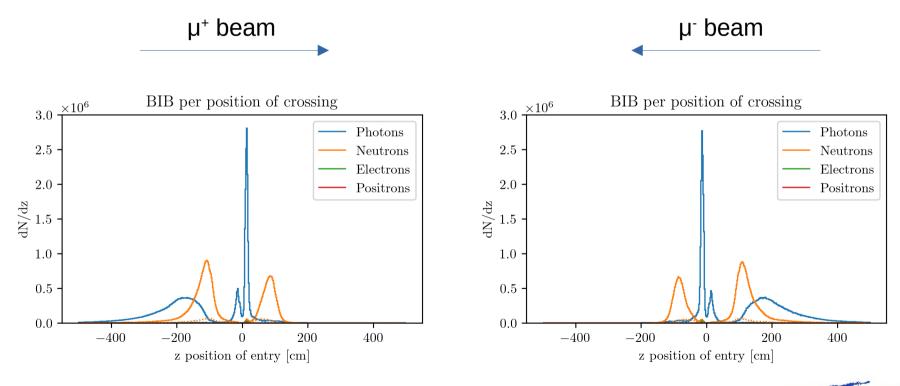
- Sample the s-coordinate (curvilinear arc length) uniformly across the particle trajectory.
- Sample the beam energy from a gaussian distribution
- Sample from the matched phase-space the correction to the ideal trajectory (this formula is applied performing the Cholensky matrix decomposition for the beam matrix)

$$\begin{cases} \Delta_x = \operatorname{Rand}_x \cdot \sqrt{\epsilon_x \beta_x} \\ \Delta_{x'} = (\operatorname{Rand}_{x'} - \operatorname{Rand}_x \cdot \alpha_x) \sqrt{\epsilon_x / \beta_x} \end{cases}$$

$$\begin{cases} \Delta_x = D_x \delta_p \\ \Delta_{x'} = D_{x'} \delta_p \end{cases}$$



## 10 TeV muon collider: position of crossing





# 10 TeV muon collider: new and original lattice

