

# Current Status of the $\alpha$ measurement

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LAPP, Annecy-le-vieux



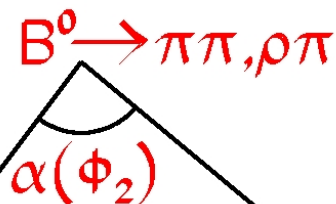
Laboratoire d'Annecy-le-vieux  
de Physique des Particules

*on behalf of BaBar Collaboration*

<http://www.slac.stanford.edu/BF>



CERN Flavour Workshop  
May 17<sup>th</sup> 2006



# $\alpha$ : collecting the ingredients

## $\pi\pi$ and $\rho\rho$ from the diagrams

● considering

only the tree (T):

$$\lambda_{\pi\pi} = e^{2i\alpha}$$

$$C_{\pi\pi} = 0$$

$$S_{\pi\pi} = \sin(2\alpha)$$

● adding the penguins (P):

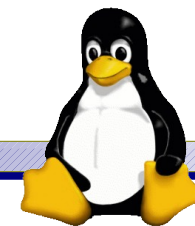
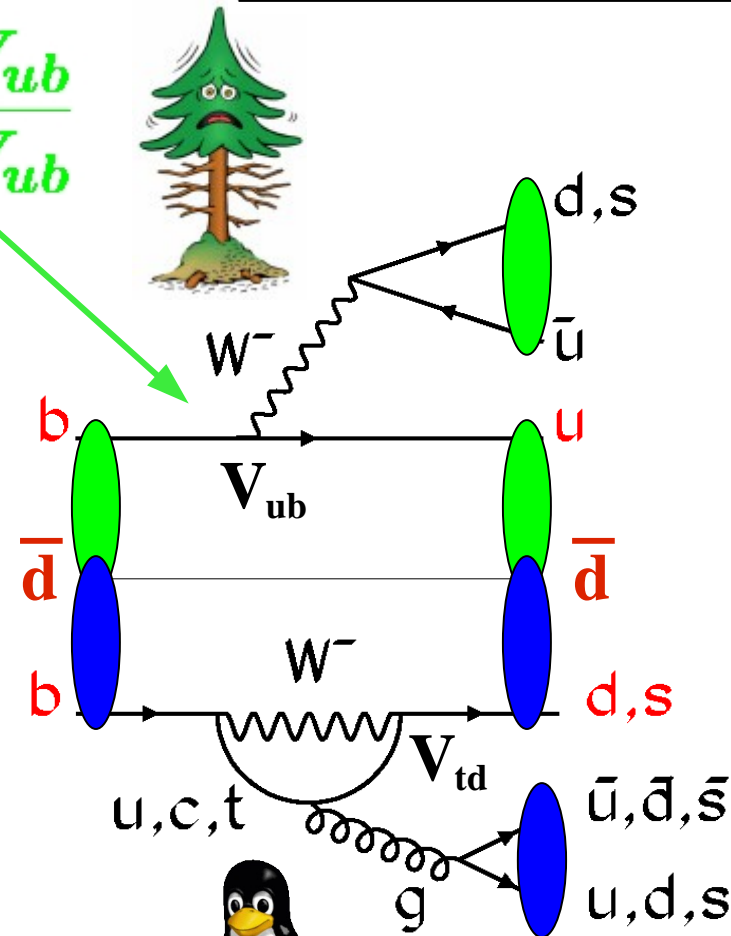
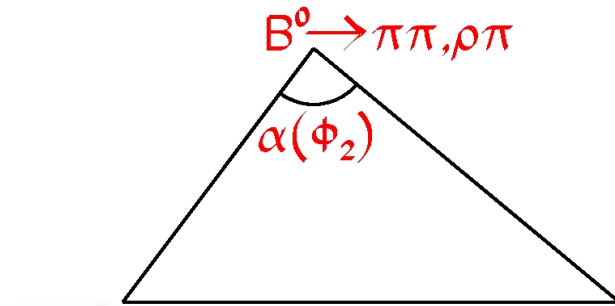
$$\lambda_{\pi\pi} = e^{2i\alpha} \frac{1 + |P/T|e^{i\delta}e^{i\gamma}}{1 + |P/T|e^{i\delta}e^{-i\gamma}}$$

$$C_{\pi\pi} \propto \sin(\delta)$$

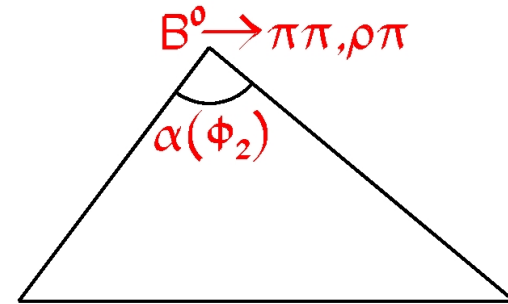
$$S_{\pi\pi} = \sqrt{1 - C_{\pi\pi}^2} \sin(2\alpha_{eff})$$

$$\lambda_{\pi\pi} = \frac{V_{tb}^* V_{td} V_{ud}^* V_{ub}}{V_{tb} V_{td}^* V_{ud} V_{ub}}$$

mixing



# $\alpha$ : collecting the ingredients (II)



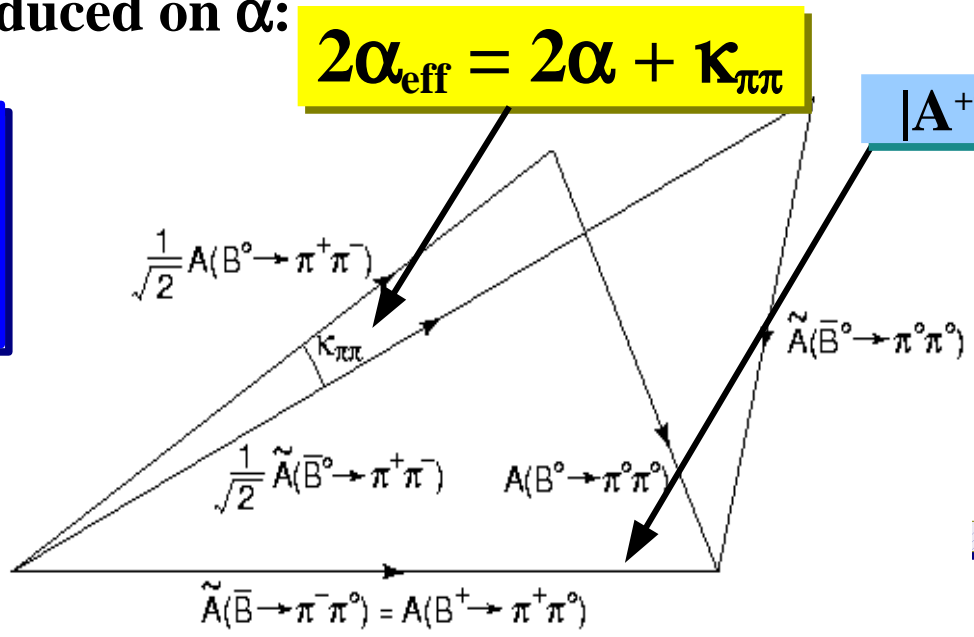
from  $\alpha_{\text{eff}} \rightarrow$  to  $\alpha$ : isospin analysis

- $B \rightarrow \pi^+\pi^-, \pi^+\pi^0, \pi^0\pi^0$  decays are connected from isospin relations
- $\pi\pi$  states can have  $I = 2$  or  $I = 0$ 
  - + the gluonic penguins contribute only to the  $I = 0$  state ( $\Delta I = 1/2$ )
  - +  $\pi^+\pi^0$  is a **pure  $I = 2$**  state ( $\Delta I = 3/2$ ) and it gets contribution only from the **tree diagram**
  - + triangular relations allow for the determination of the phase difference induced on  $\alpha$ :

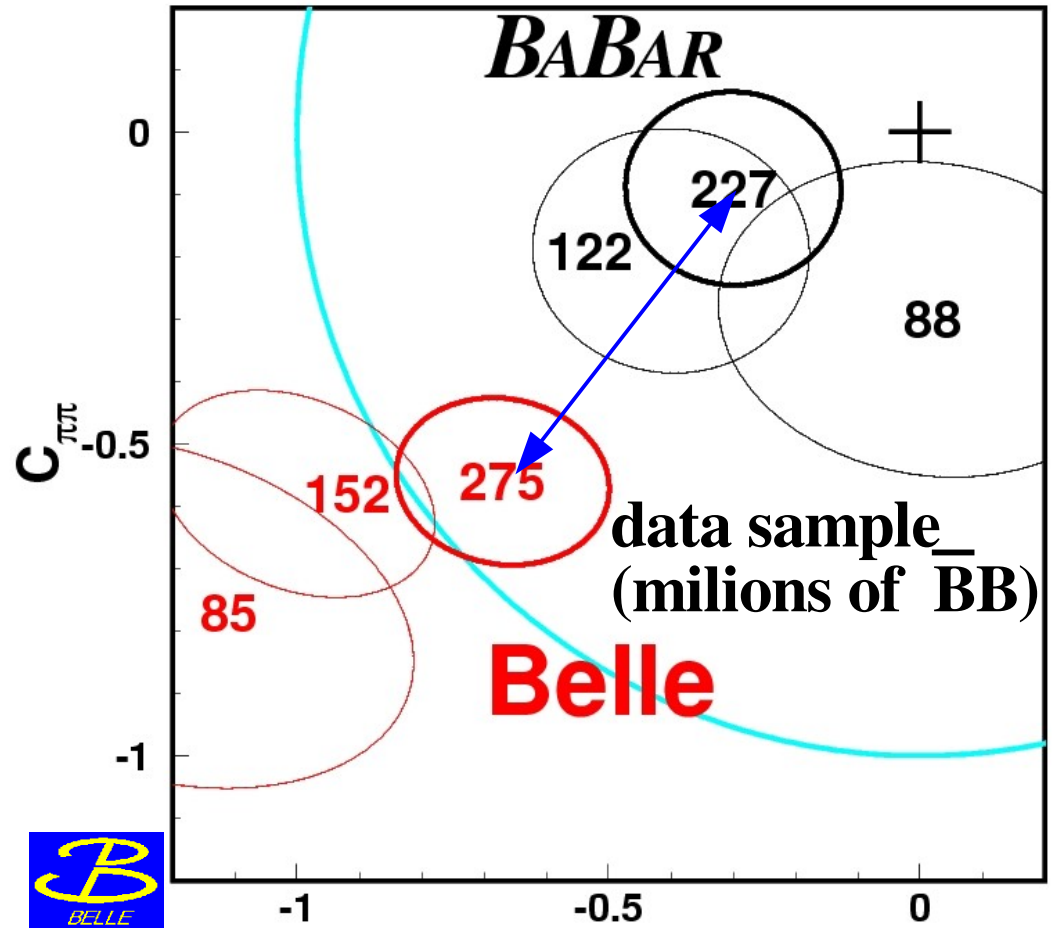
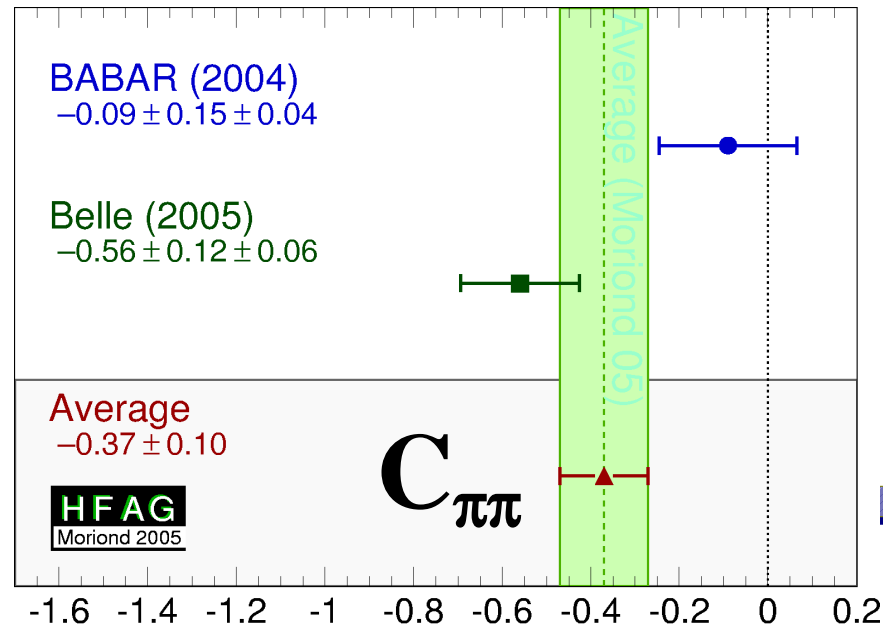
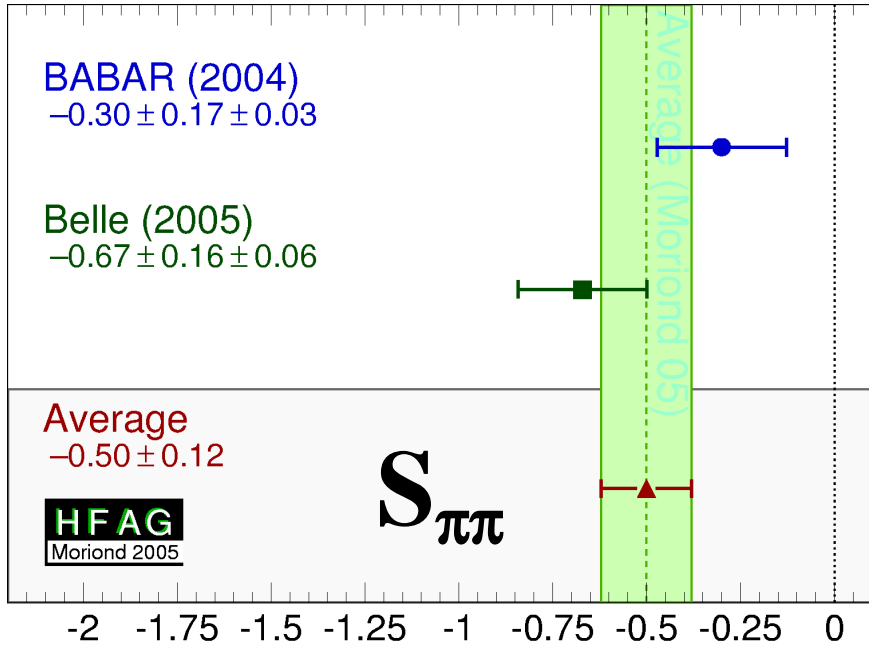
Both  $BR(B^0)$  and  $BR(\bar{B}^0)$  have to be measured in all the  $\pi\pi$  channels

$$2\alpha_{\text{eff}} = 2\alpha + \kappa_{\pi\pi}$$

$$|A^{+0}| = |A^{-0}|$$



# towards $\alpha$ : time dependent analysis



**Belle: evidence of CP violation**

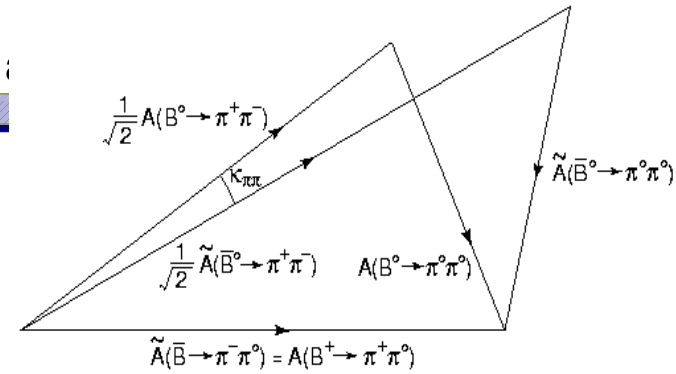
**not confirmed by BaBar**

**2.2 $\sigma$  discrepancy BaBar-Belle**



# towards $\alpha$ : isospin analysis

to complete the isospin analysis



$B \rightarrow \pi^+\pi^0$ :  $BR(\pi^+\pi^0) = (5.8 \pm 0.6 \pm 0.4) \cdot 10^{-6}$

$A(\pi^+\pi^0) = -0.01 \pm 0.10 \pm 0.02$

$B \rightarrow \pi^0\pi^0$ :  $BR(\pi^0\pi^0) = (1.17 \pm 0.32 \pm 0.10) \cdot 10^{-6}$

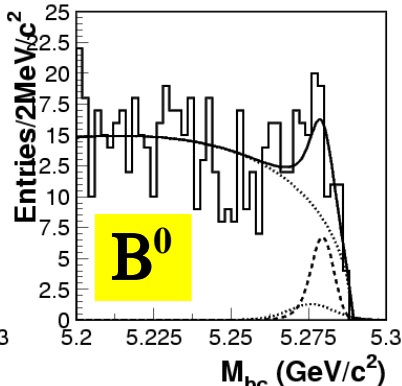
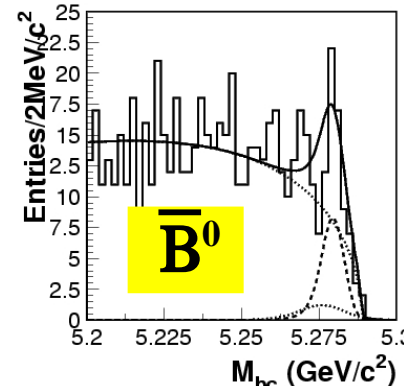
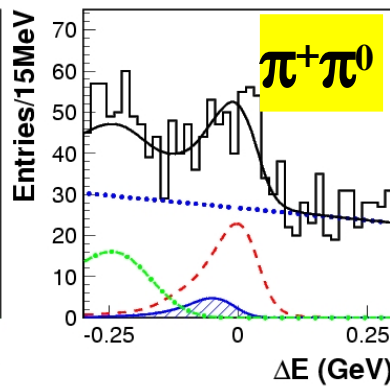
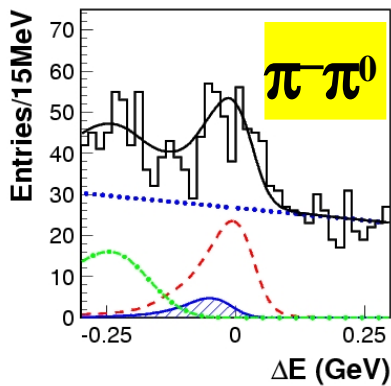
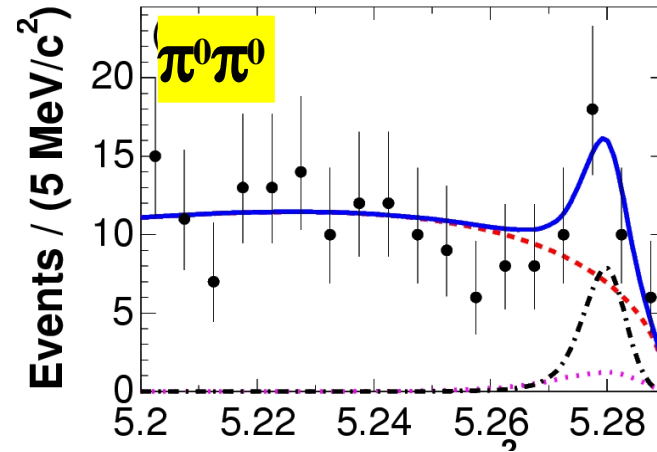
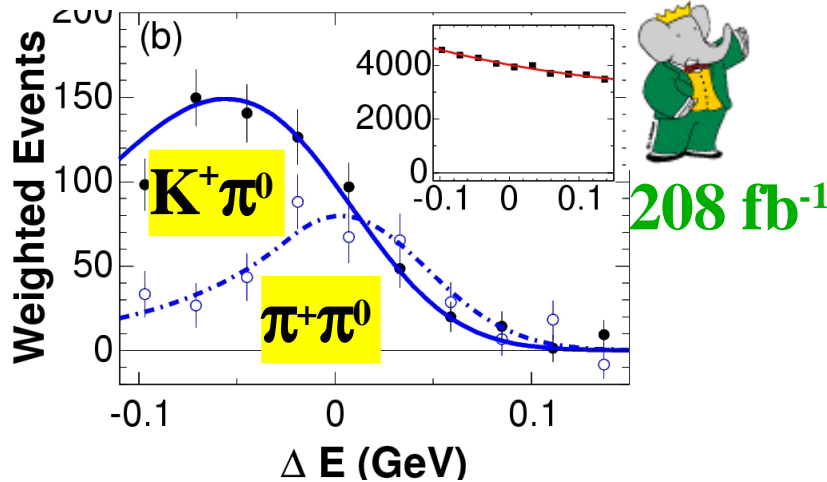
$C(\pi^0\pi^0) = -0.12 \pm 0.56 \pm 0.06$

$BR(\pi^+\pi^0) = (5.0 \pm 1.2 \pm 0.5) \cdot 10^{-6}$

$A(\pi^+\pi^0) = 0.02 \pm 0.08 \pm 0.01$

$BR(\pi^0\pi^0) = (2.3 \pm 0.5 \pm 0.3) \cdot 10^{-6}$

$C(\pi^0\pi^0) = 0.44 \pm 0.53 \pm 0.17$



253 fb<sup>-1</sup>

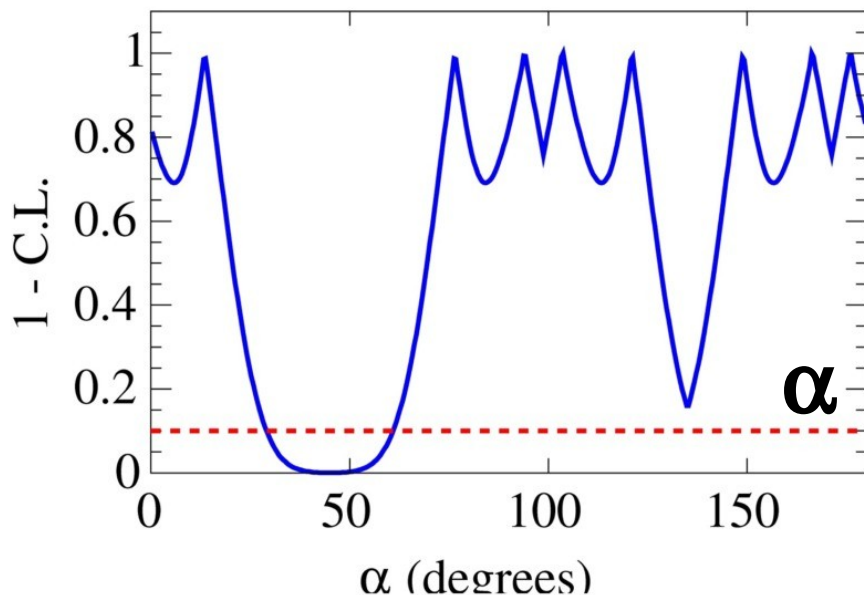


5



$\alpha$ : from  $B \rightarrow \pi\pi$

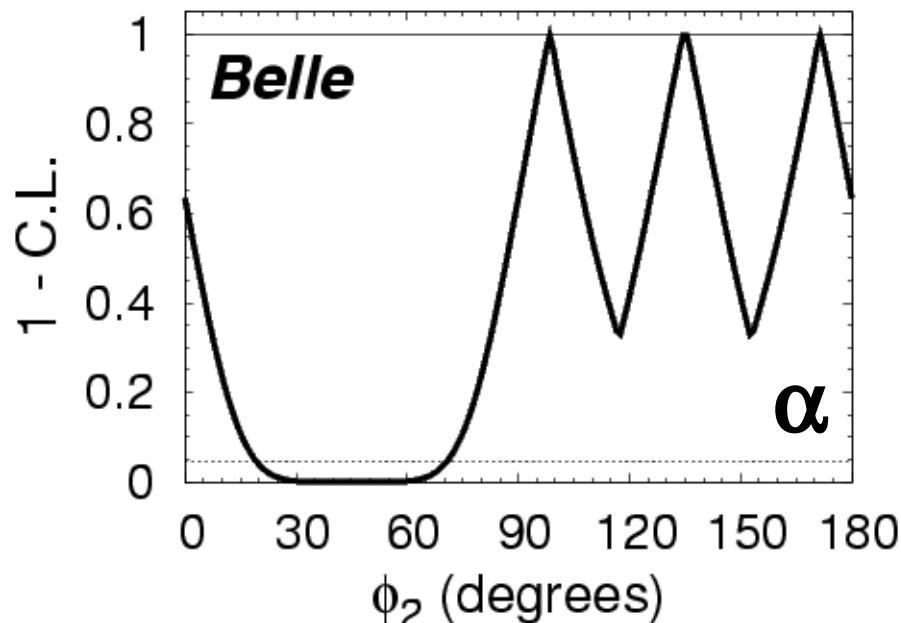
PRL 95, 151803 (2005)



$[29^\circ, 61^\circ]$  excluded @ 90% CL



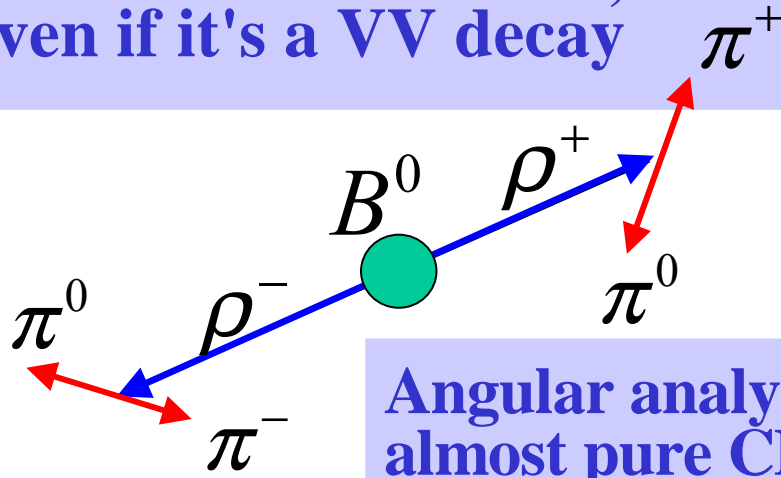
PRL 95, 101801 (2005)



$[19^\circ, 71^\circ]$  excluded @ 95% CL

more on  $\alpha_{\text{eff}}$ : from  $B \rightarrow \rho^+ \rho^-$

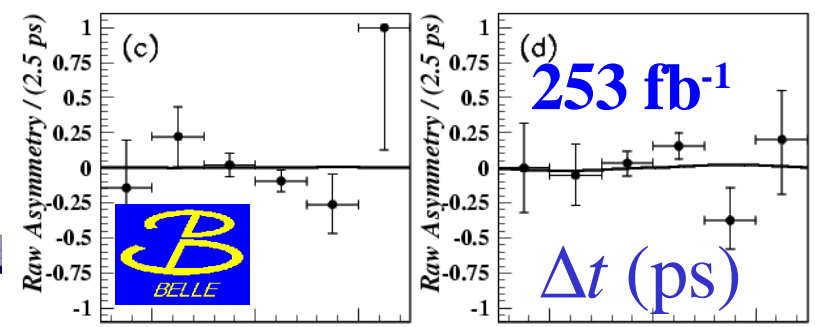
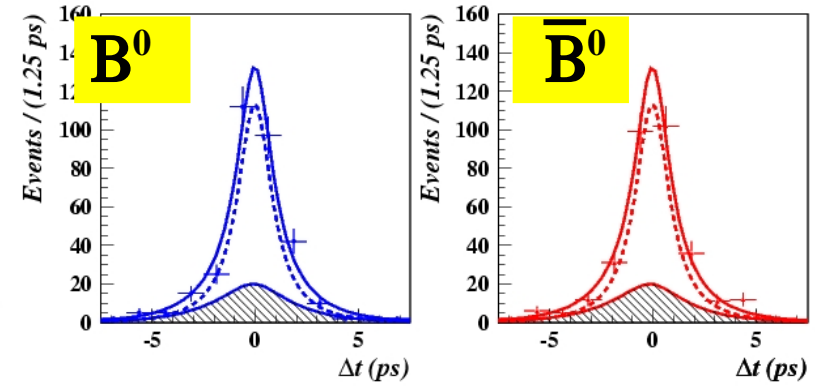
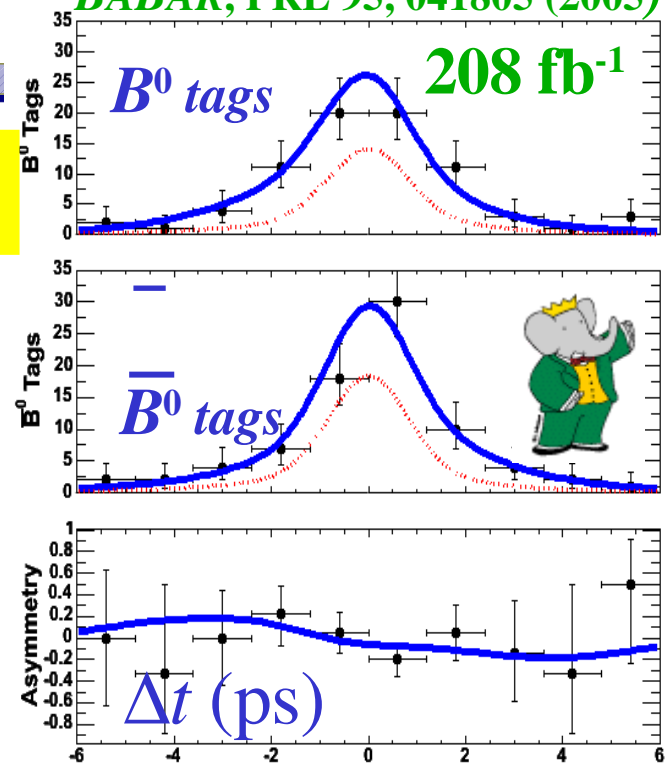
3 polarizations  $\rightarrow$  mixed CP state:  
 but we are lucky  $\rightarrow$  there is just one!  
 no additional dilution,  
 even if it's a VV decay



Angular analysis  $\rightarrow$   
 almost pure CP=+1!

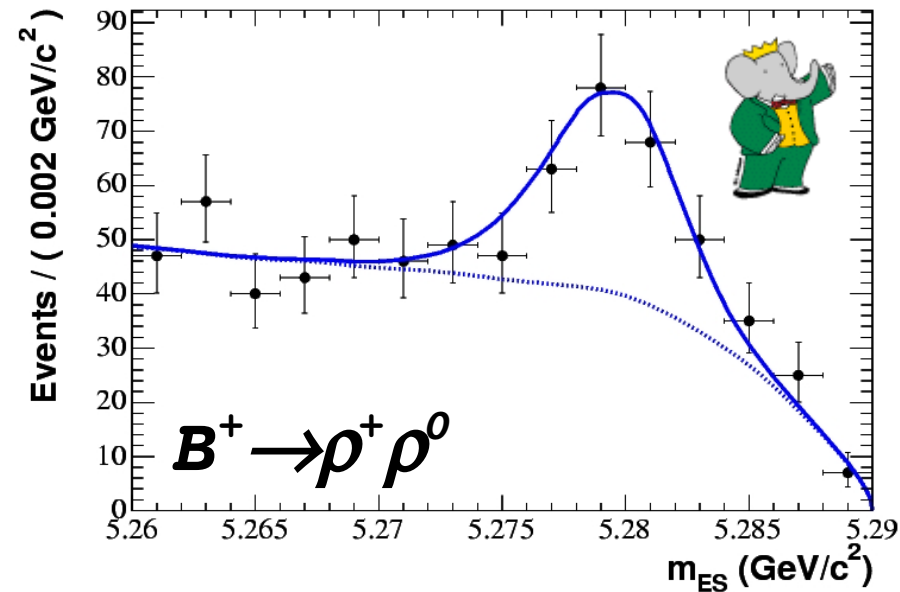
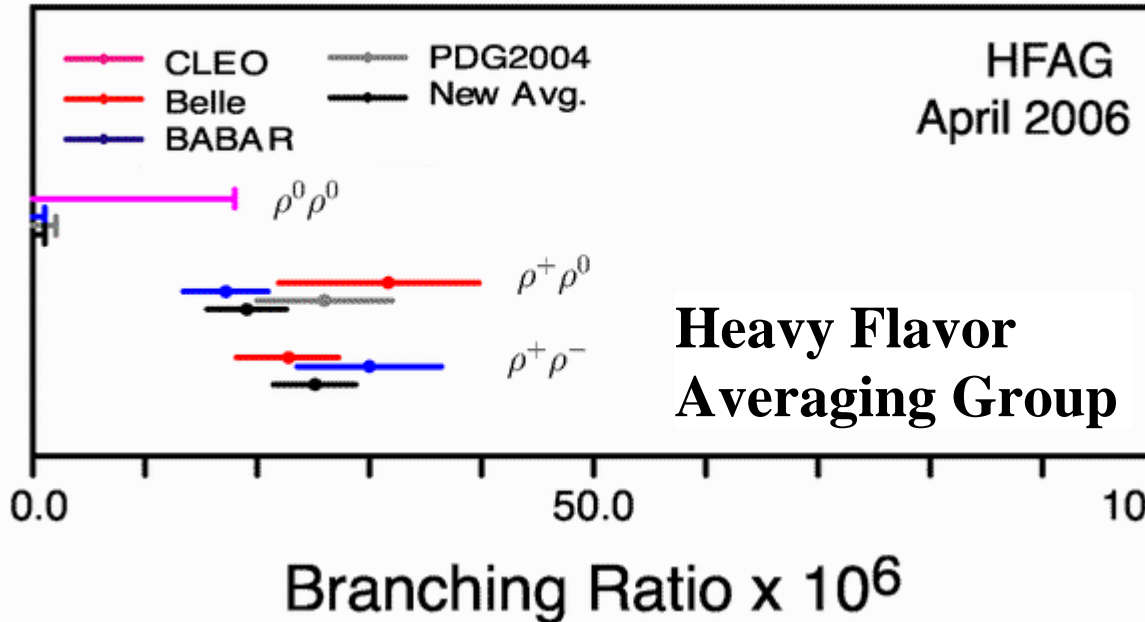


	BABAR	Belle	HFAG
$f_L$	$0.978 \pm 0.014^{+0.021}_{-0.029}$	$0.941^{+0.034}_{-0.040} \pm 0.030$	$0.967^{+0.023}_{-0.028}$
$S_{\rho\rho}$	$-0.33 \pm 0.24^{+0.08}_{-0.14}$	$0.08 \pm 0.41 \pm 0.09$	$-0.21 \pm 0.22$
$C_{\rho\rho}$	$-0.03 \pm 0.18 \pm 0.09$	$0.00 \pm 0.30^{+0.09}_{-0.10}$	$-0.03 \pm 0.17$



# towards $\alpha$ : isospin analysis from $B \rightarrow \rho\rho$

$$\mathcal{B}(B \rightarrow VV)$$



Mode	$B/10^{-6}$ ( <i>BABAR</i> )	$B/10^{-6}$ ( <i>Belle</i> )
$B^0 \rightarrow \rho^0 \rho^0$	$<1.1$ (@90% C.L.) [230 M $\bar{B}B$ ]	—
$B^+ \rightarrow \rho^+ \rho^0$	$17.2 \pm 2.5 \pm 2.8$ [230 M $\bar{B}B$ ]	$31.7 \pm 7.1 \pm 6.7$ [85 M $\bar{B}B$ ]
$B^0 \rightarrow \rho^+ \rho^-$	$30 \pm 4 \pm 5$ [89 M $\bar{B}B$ ]	$22.8 \pm 3.8 \pm 2.6$ [275 M $\bar{B}B$ ]

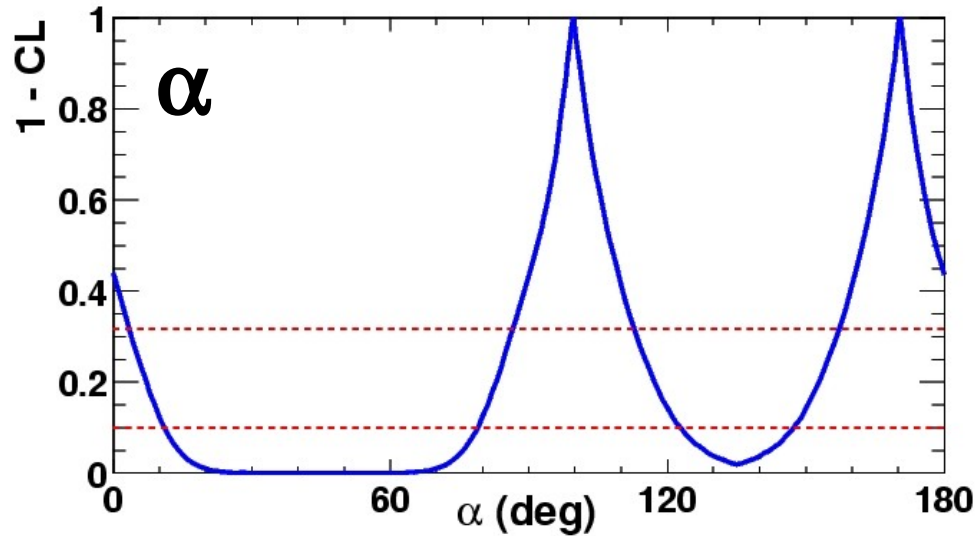
if 00 channel  $\rightarrow 0$   $|\alpha - \alpha_{\text{eff}}| \rightarrow 0$   
 from data:  $|\alpha - \alpha_{\text{eff}}|_{\rho\rho} < |\alpha - \alpha_{\text{eff}}|_{\pi\pi}$



# $\alpha$ : from $B \rightarrow \rho\rho$



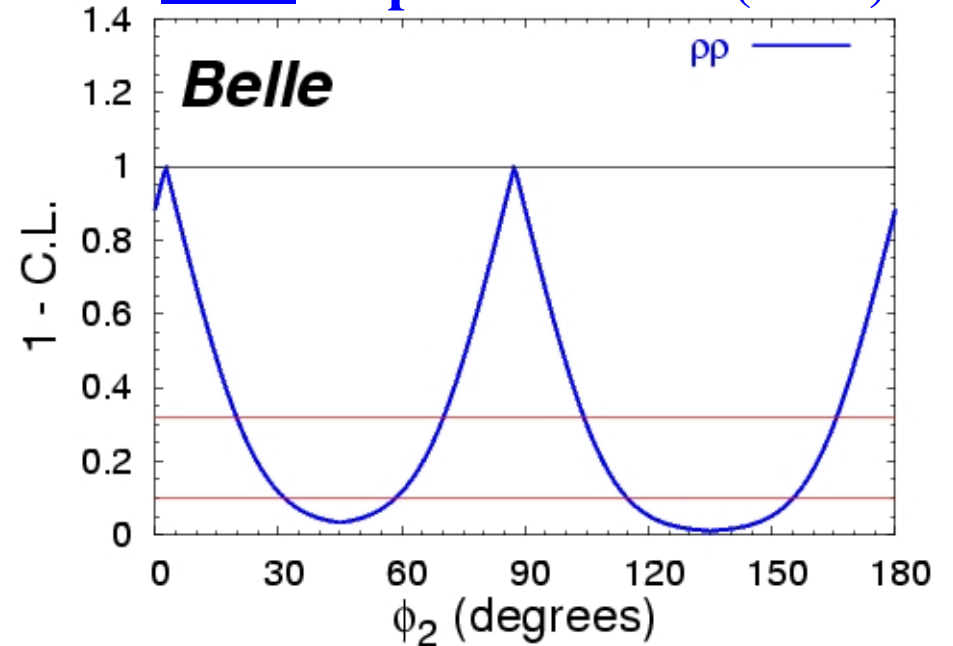
PRL 95, 041805 (2005)



$$\alpha_{SM} = [100 \pm 13]^\circ$$



hep-ex/0601024 (2006)

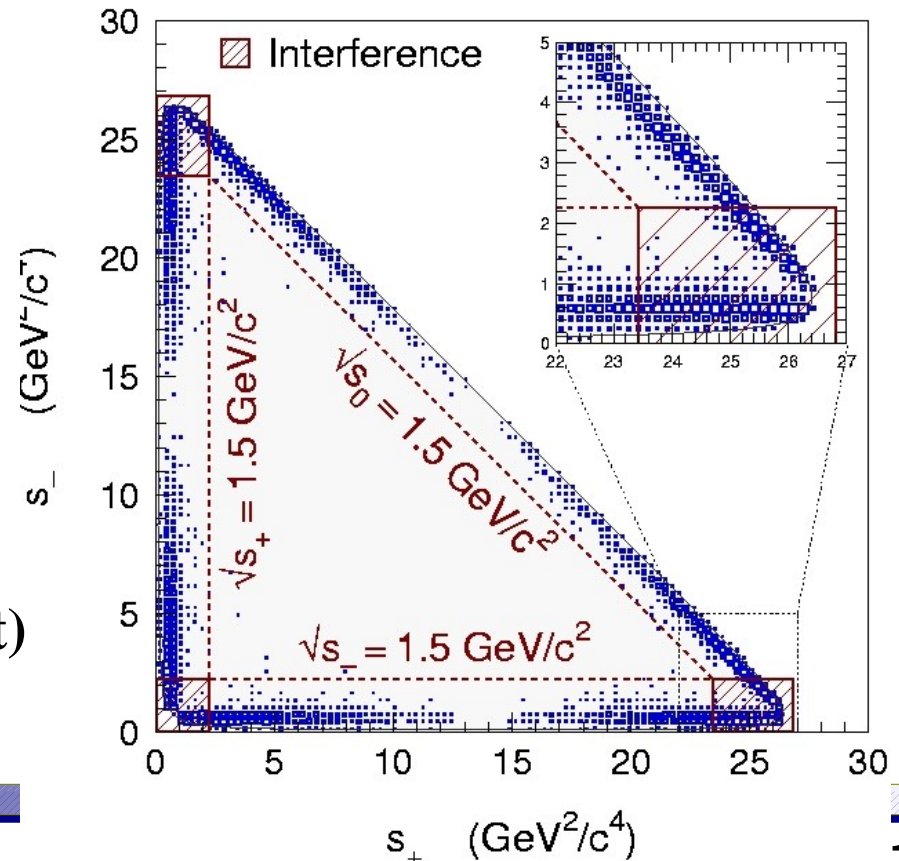
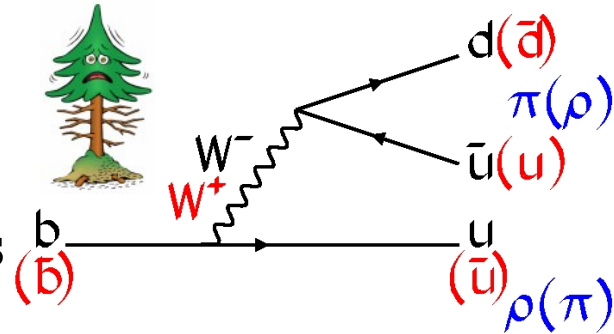


$$\alpha_{SM} = [88 \pm 17]^\circ$$

dominant contribution to the error:  
 $11^\circ$  from the Grossman-Quinn bound  
 with the  $\rho^0\rho^0$  limit

# Still $\alpha$ : time-dependent analysis $B^0 \rightarrow (\rho\pi)^0$

- method Snyder-Quinn
  - *Phys. Rev. D48 2139 (1993)*
- $\alpha$  extraction together with the strong phases exploiting the amplitude interference
- the amplitude  $A_{3\pi}$  is dominated by  $\rho^+\pi^-$ ,  $\rho^-\pi^+$ ,  $\rho^0\pi^0$  and by the radial component
  - $A_{3\pi} = f_+ A^{+-} + f_- A^{-+} + f_0 A^{00}$
  - $A^k = T^k e^{-i\alpha} + P^k$
- with this one can define time-dependent coefficients as functions of  $\cos(\Delta m_d \Delta t)$  and  $\sin(\Delta m_d \Delta t)$



# $B^0 \rightarrow (\rho\pi)^0$ results

● direct asymmetry measurement:

⊕  $A^{+-} = -0.21 \pm 0.11 \pm 0.04$

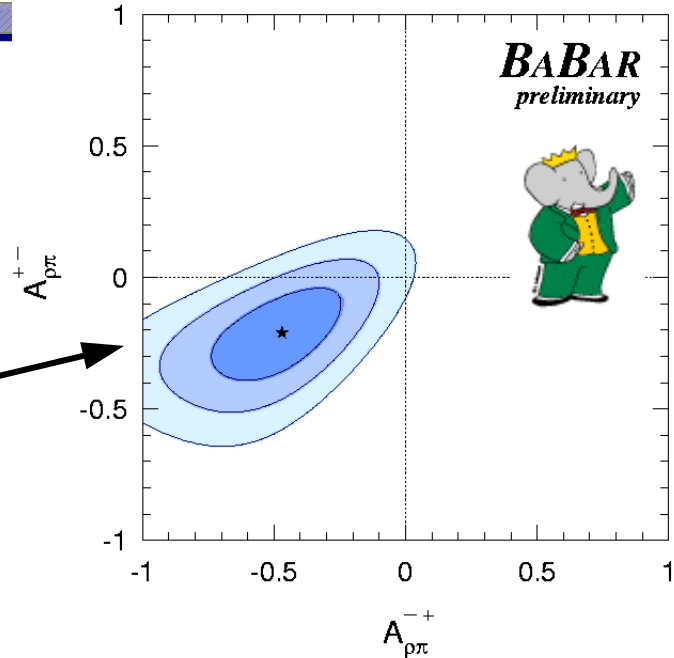
⊕  $A^{-+} = -0.47 \pm 0.15 \pm 0.06$

● defining  $\delta_{+-} = \arg(A^{+*}A^-)$

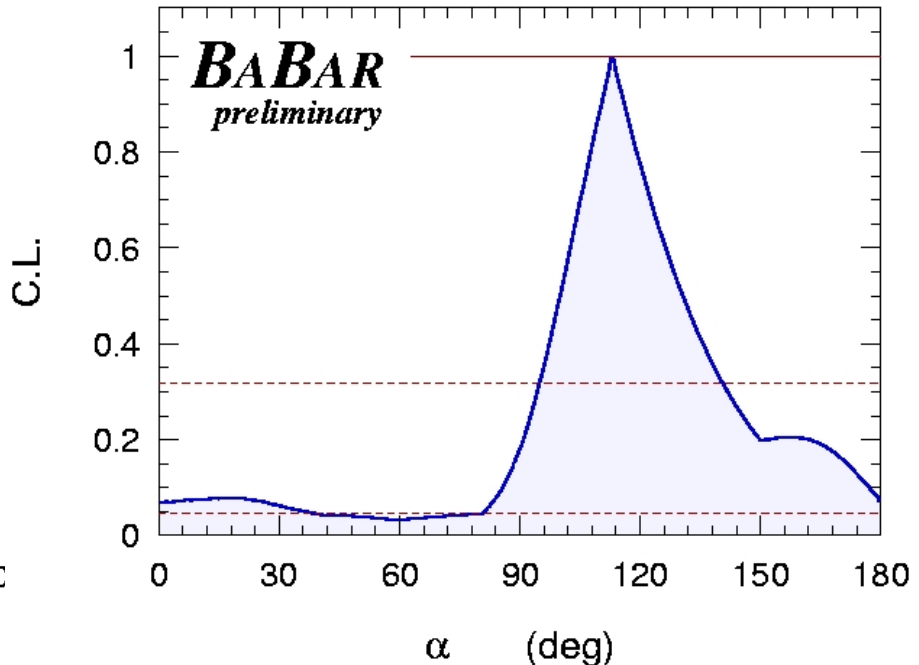
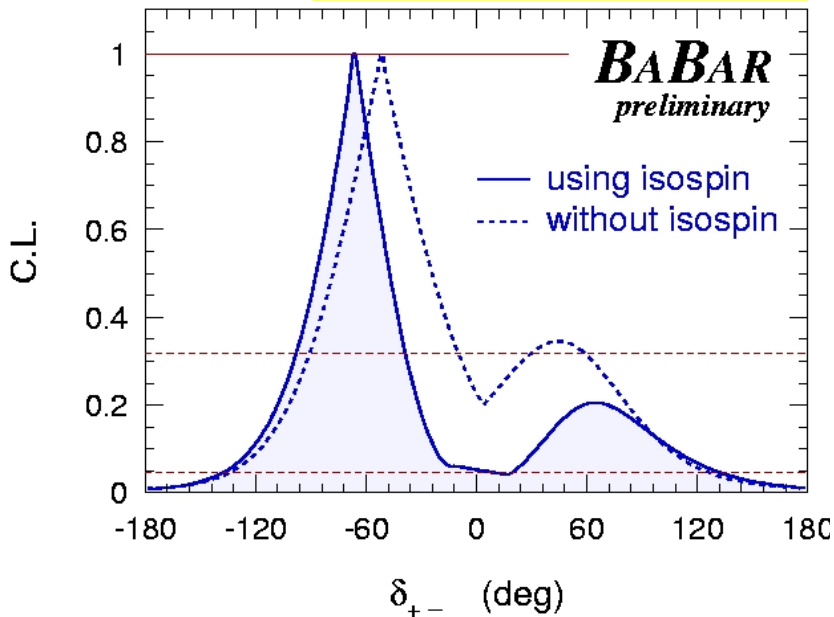
and using SU(2) relation in  $P^0 = -(P^{++}+P^{--})/2$

⊕ one can extract

**2.9 $\sigma$**



**$\alpha = (113^{+27}_{-17} \pm 6)^\circ$**



# $\alpha$ from isospin analysis: $\pi\pi$ , $\rho\rho$ , $\rho\pi$

Starting from the SU(2) amplitudes ( $\pi\pi$ ,  $\rho\rho$ ):

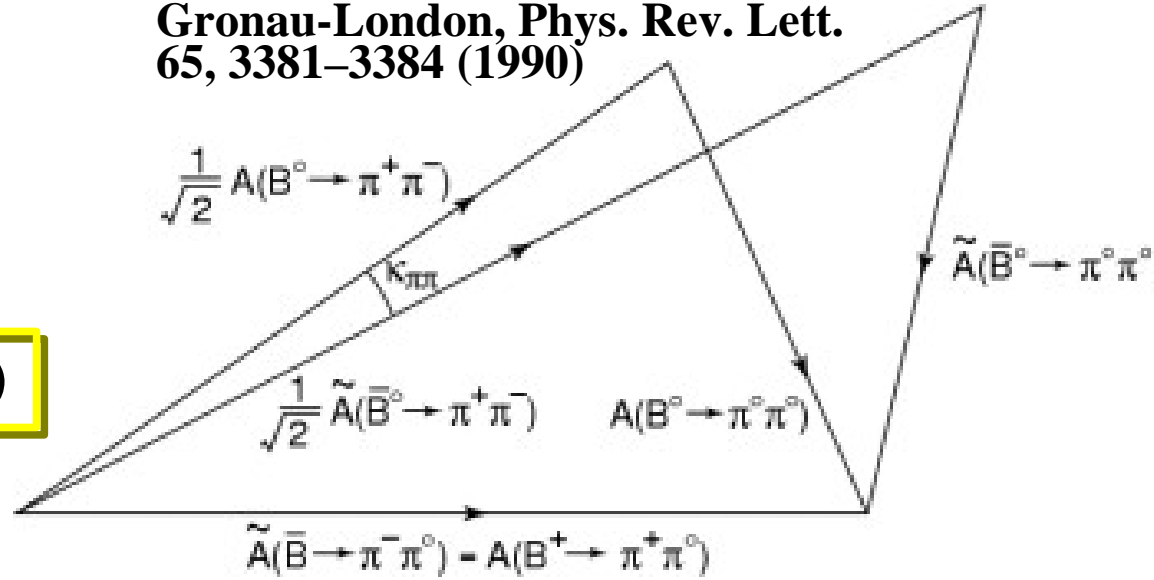
$$A^{+-} = -T e^{-i\alpha} + P e^{i\delta_P}$$

$$A^{+0} = -1/\sqrt{2} e^{-i\alpha} (T + T_C e^{i\delta_C})$$

$$A^{00} = -1/\sqrt{2} (T_C e^{i\delta_C} e^{-i\alpha} + P e^{i\delta_P})$$

unknowns:  $T, P, T_C, \delta_P, \delta_{T_C}, \alpha$   
 observable:  $3x$  BR,  $C_{+-}, S_{+-}, C_{00}$

Gronau-London, Phys. Rev. Lett. 65, 3381–3384 (1990)

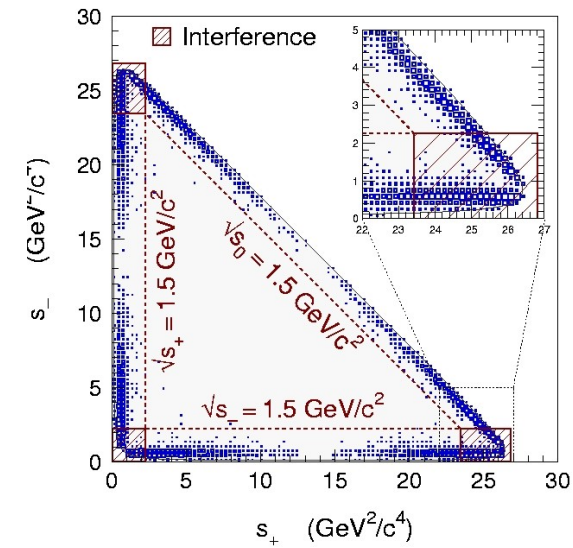


Similar analysis for  $(\rho\pi)^0$  on the Dalitz plane

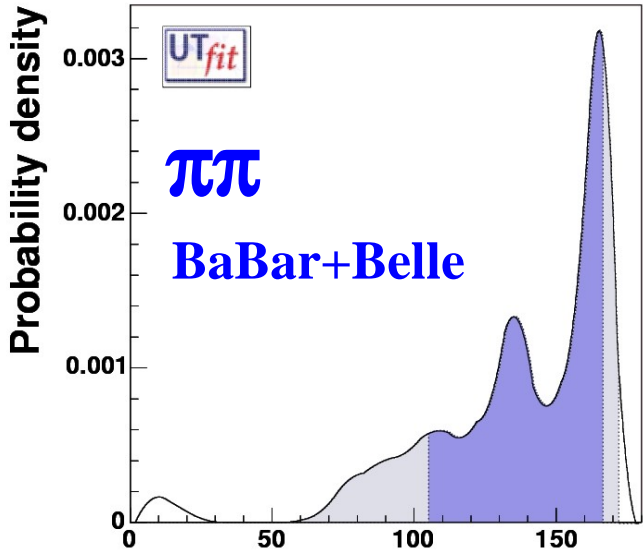
$$A^k = T^k e^{-i\alpha} + P^k$$

$$\bar{A}^k = T^{\bar{k}} e^{i\alpha} + P^{\bar{k}}$$

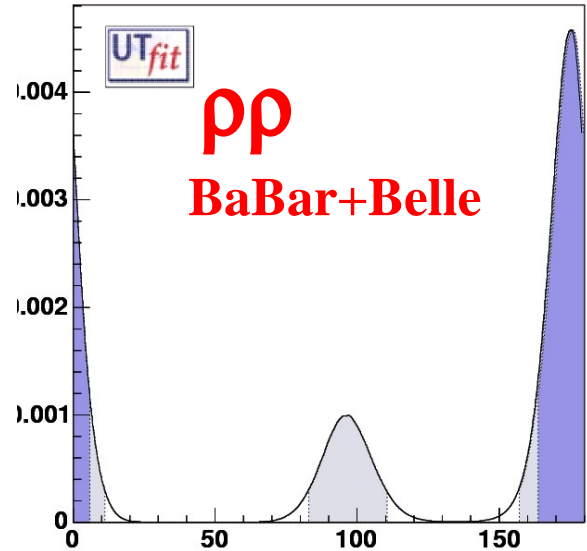
with  $k=+-$  for  $\rho^+\pi^-$ ,  $-+$  for  $\rho^-\pi^+$ ,  
 $e$  00 for  $\rho^0\pi^0$



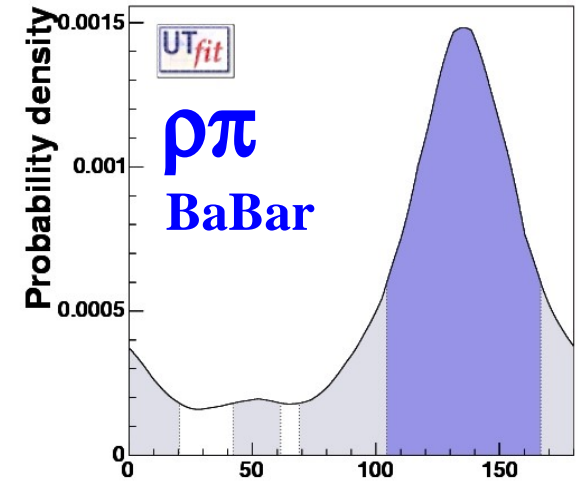
# $\alpha$ from isospin analysis: $\rho\rho$ , $\pi\pi$ and $\rho\pi$



$\alpha \in [76, 173]^\circ$



$\alpha \in [83, 111]^\circ \cup [157, 191]^\circ$



$\alpha = (136 \pm 31)^\circ$

$$C_{\pi\pi} = -0.37 \pm 0.10$$

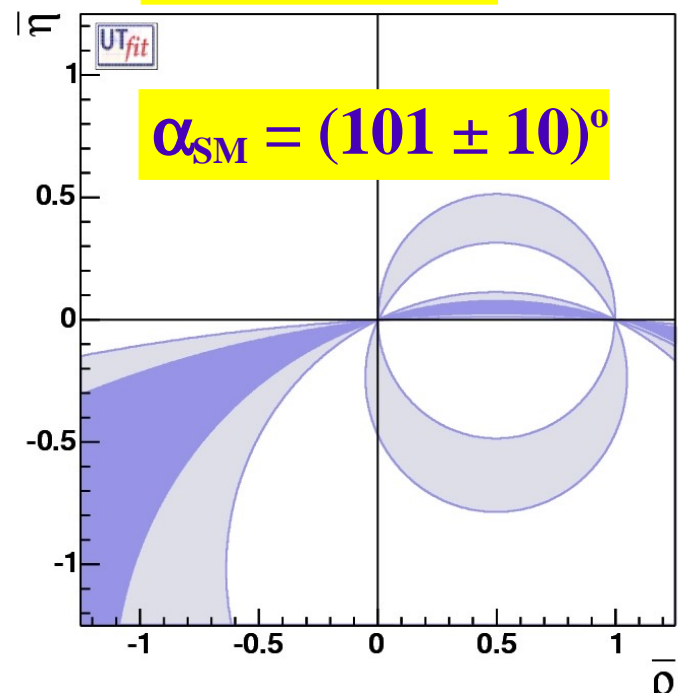
$$S_{\pi\pi} = -0.50 \pm 0.12$$

$C_{\pi\pi}$  and  $S_{\pi\pi}$  equal to 0 are excluded

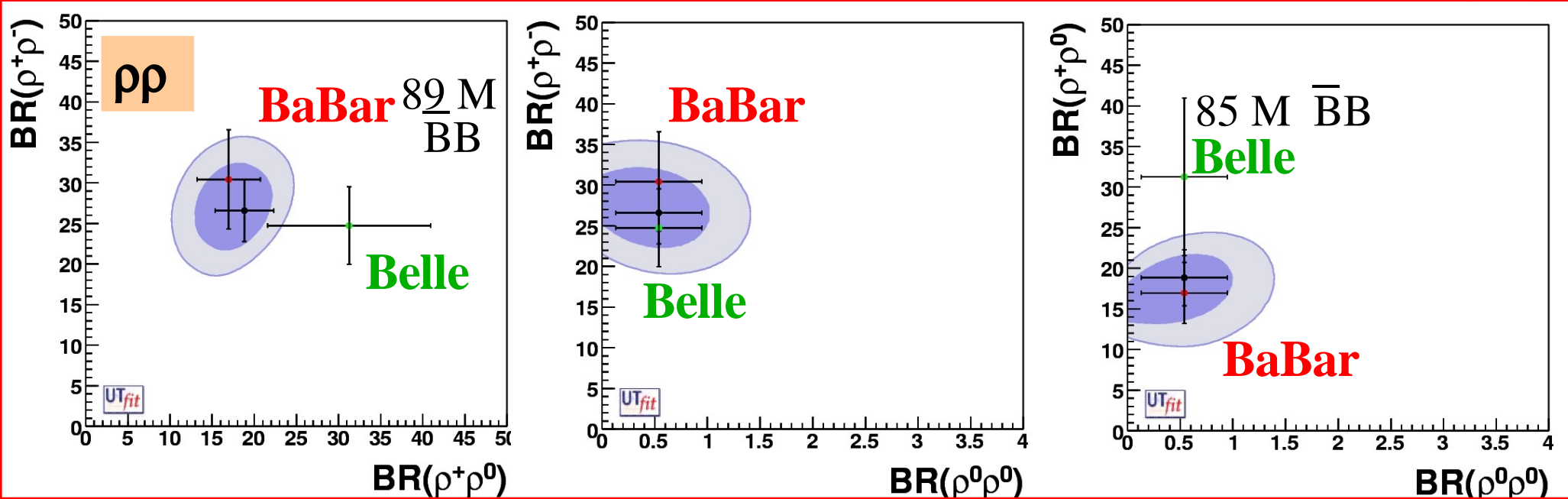
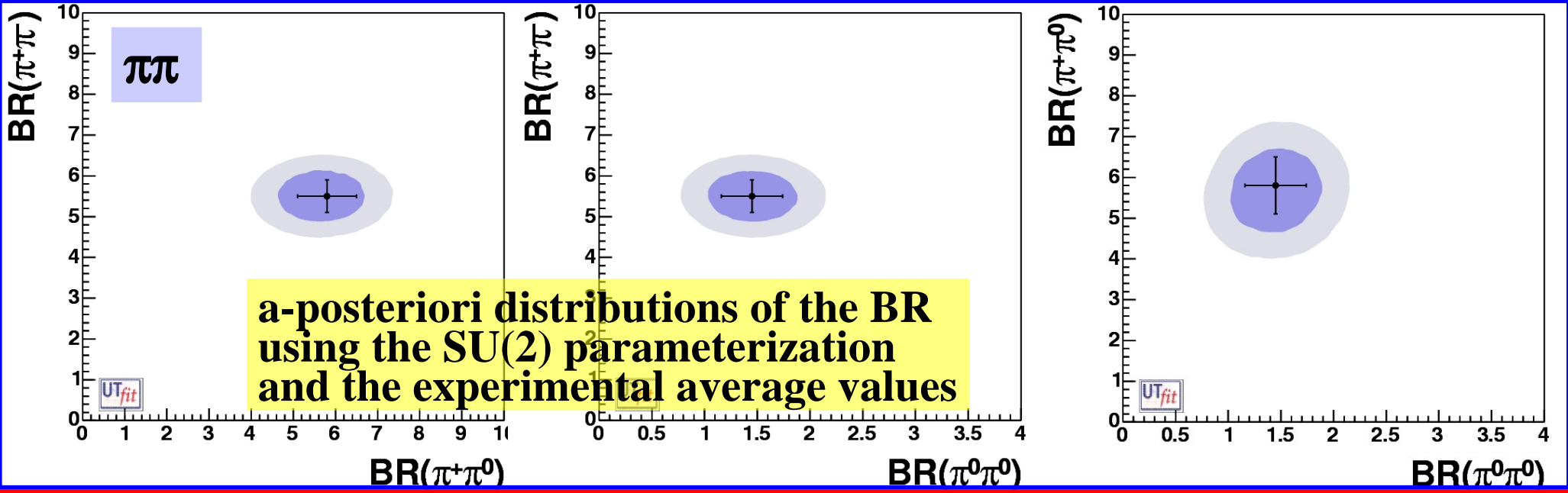
$$C_{\rho\rho} = -0.03 \pm 0.17$$

$$S_{\rho\rho} = -0.21 \pm 0.22$$

$C_{\rho\rho}$  and  $S_{\rho\rho}$  equal to 0 are preferred

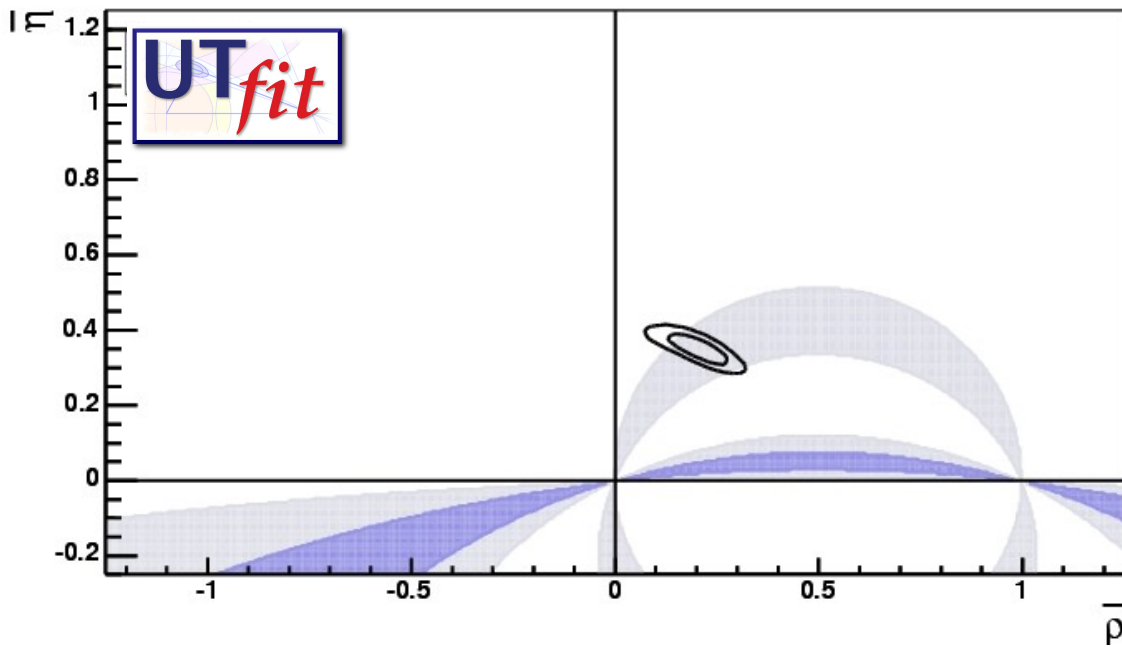


# Test of the isospin assumption in $\pi\pi$ and $\rho\rho$

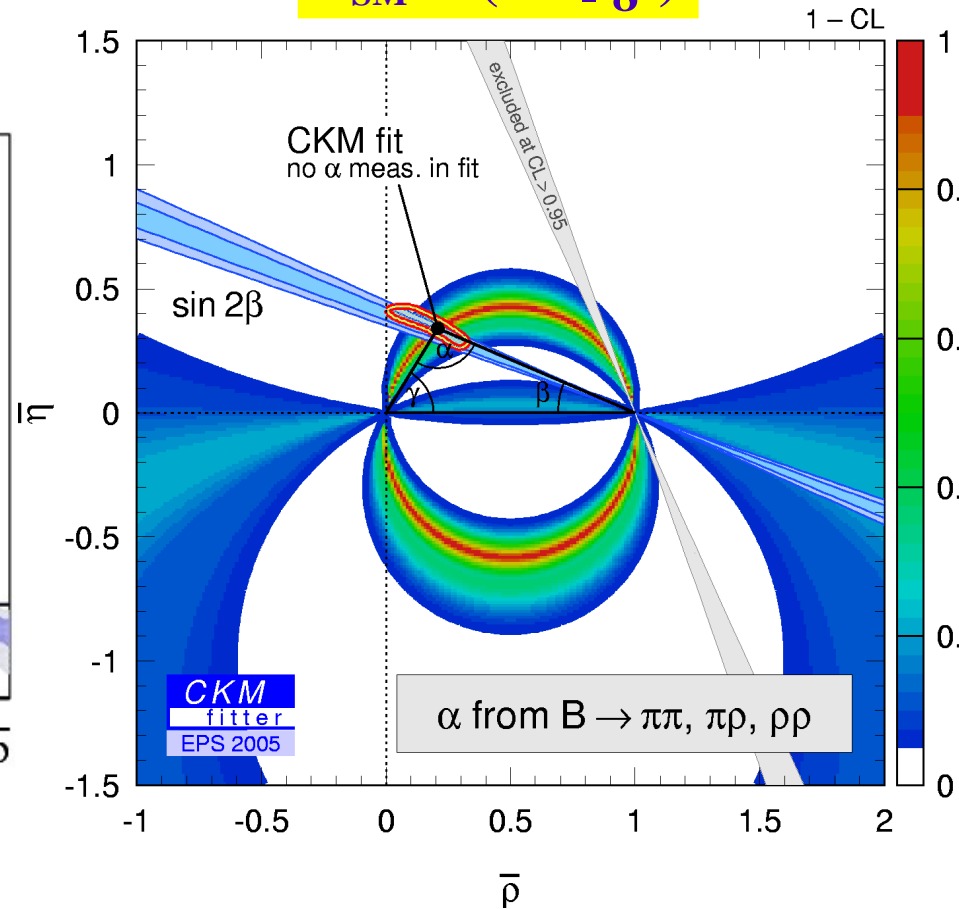


# $\alpha$ from isospin analysis: summary

$\alpha_{SM} = (101 \pm 10)^\circ$

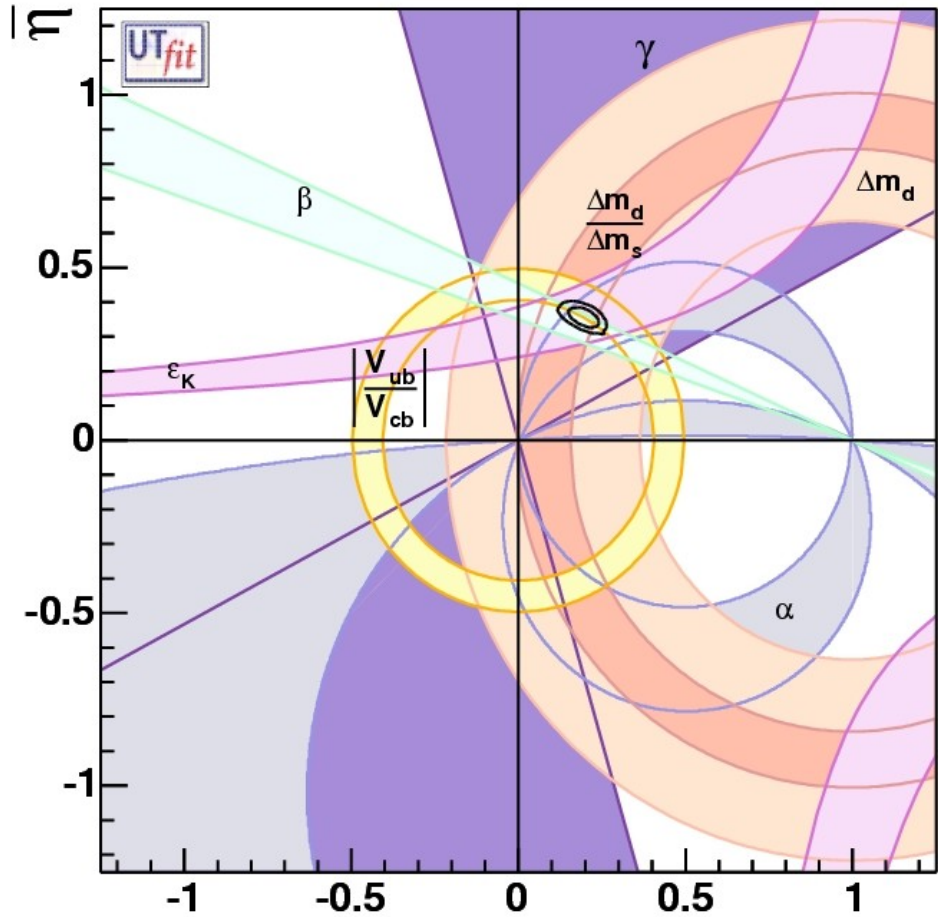
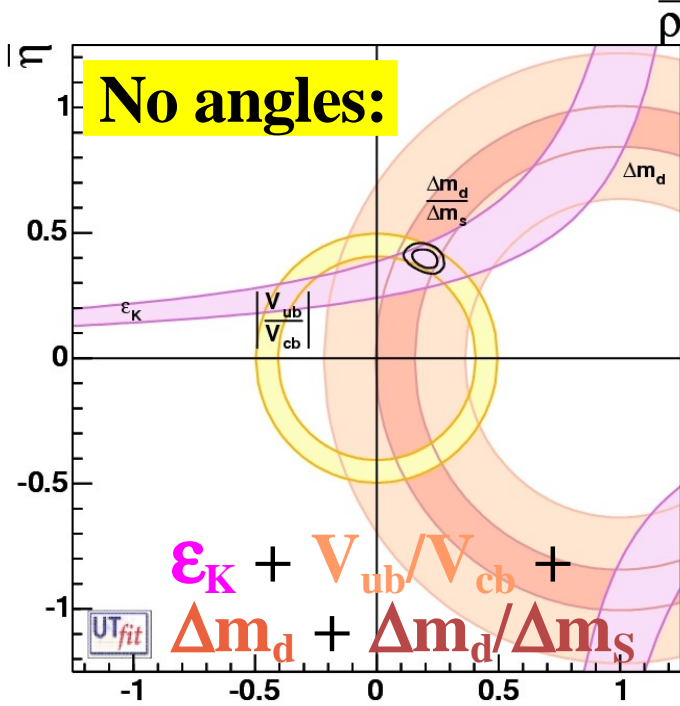
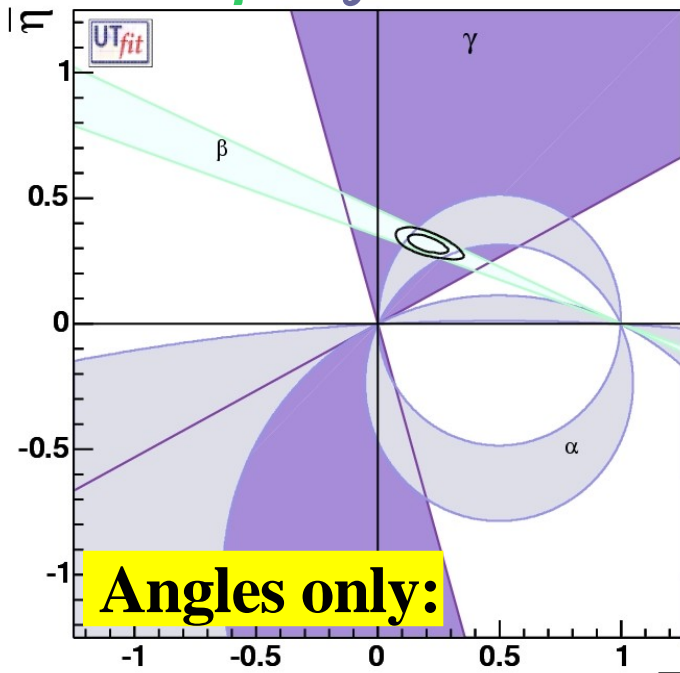


$\alpha_{SM} = (99^{+13}_{-8})^\circ$



$\beta + \gamma + \alpha$

**Including all the constraints**



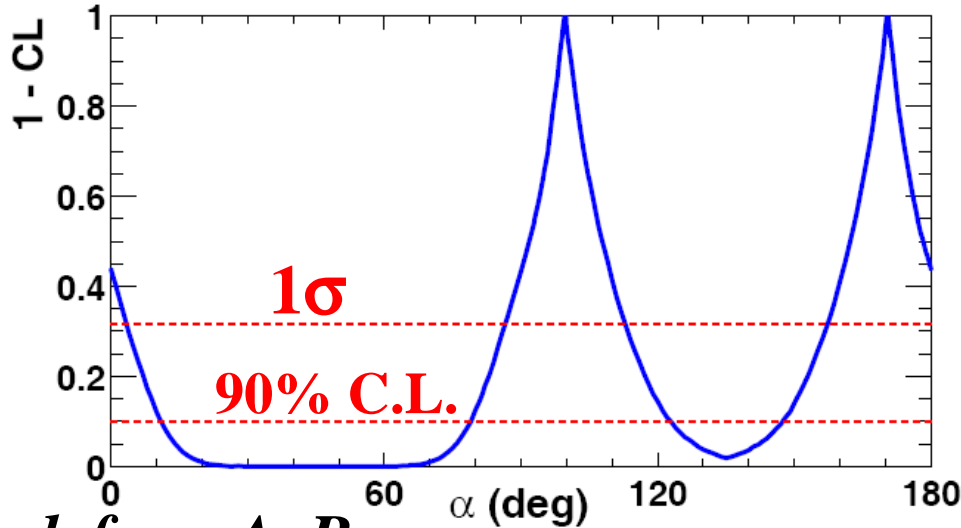
$\bar{\rho} = 0.193 \pm 0.029$   
 [0.133, 0.248] @ 95% Prob.

$\bar{\eta} = 0.355 \pm 0.019$   
 [0.318, 0.393] @ 95% Prob.

UT fit



# Physics Reach with $1 \text{ ab}^{-1}$ scenario

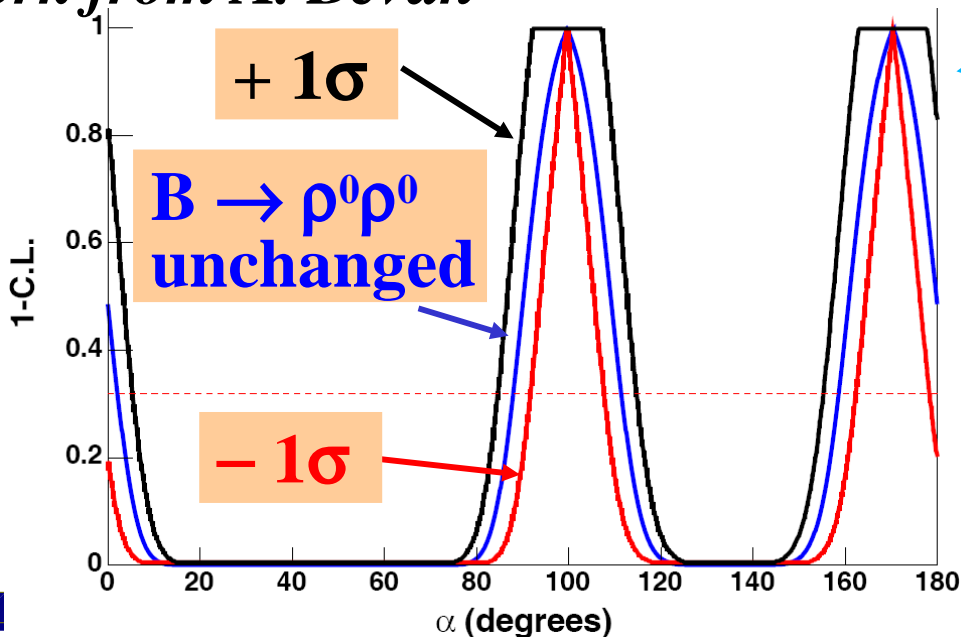


Current  $\alpha$  measurement from  $B \rightarrow \rho\rho$ :

multiple unresolved solutions within each peak

Projected  $\alpha$  measurement from  $B \rightarrow \rho\rho$  for  $1 \text{ ab}^{-1}$

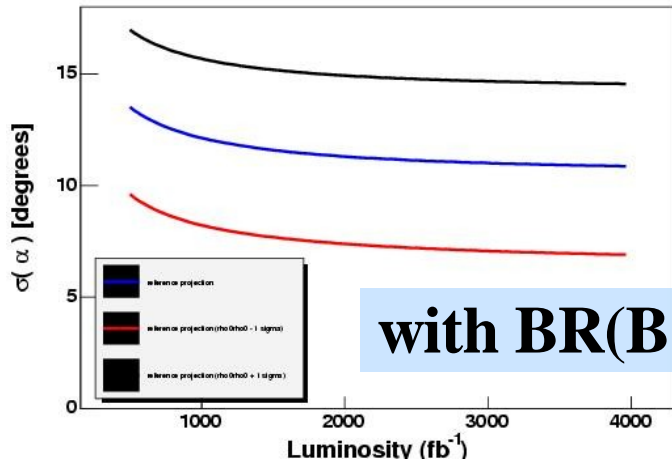
work from A. Bevan



the uncertainty on  $\alpha$  depends critically on  $\text{BR}(B \rightarrow \rho^0\rho^0)$   
 Scenarios:

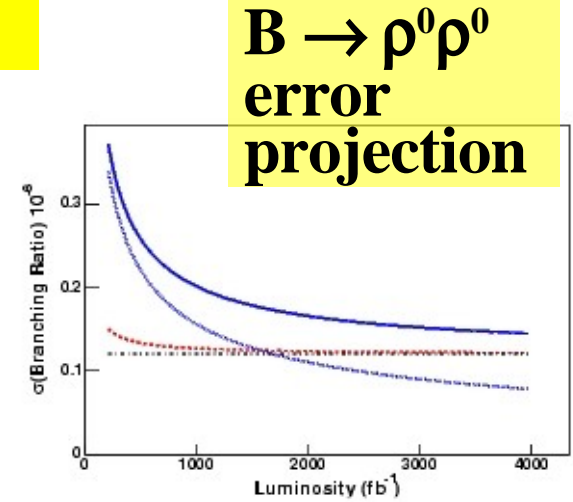
- use the current value
- $+ 1\sigma$
- $- 1\sigma$

# Physics Reach with $1 \text{ ab}^{-1}$ scenario

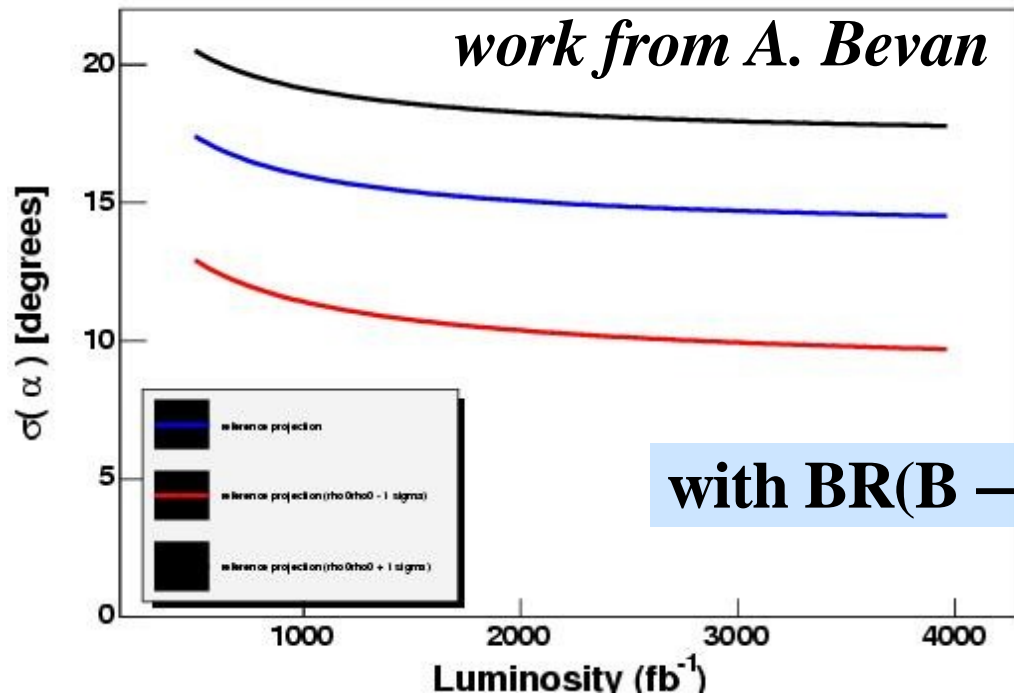


critical issue:  $B \rightarrow \rho^0\rho^0$   
but also  $B \rightarrow \rho^+\rho^0$

with  $\text{BR}(B \rightarrow \rho^+\rho^0) \sim 26.4 \cdot 10^{-6}$

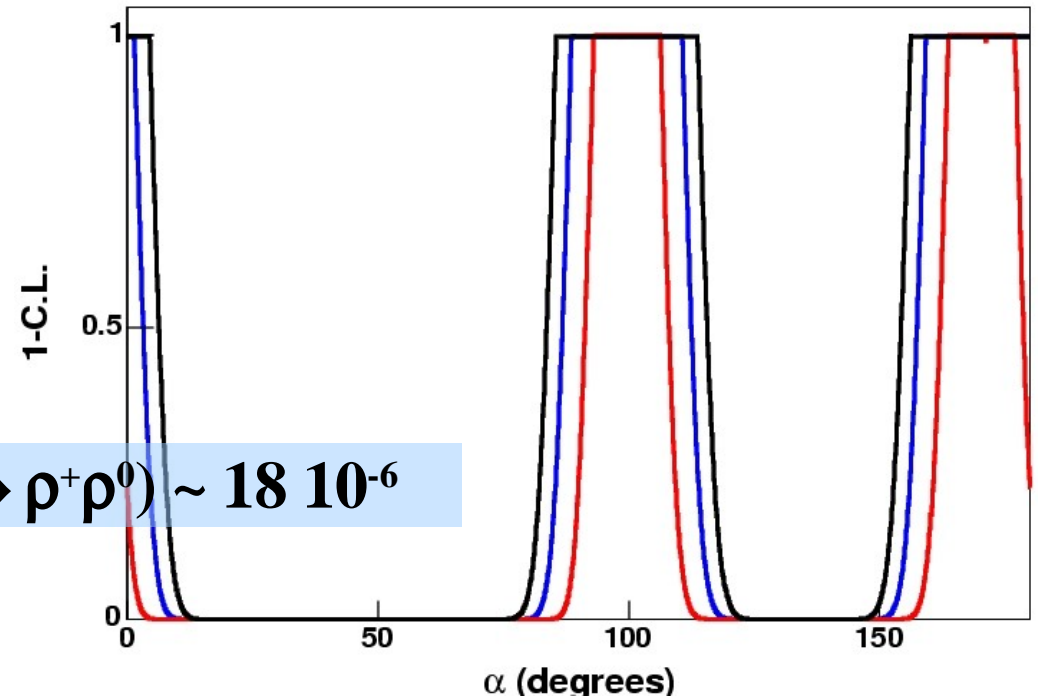


$B \rightarrow \rho^0\rho^0$   
error  
projection



*work from A. Bevan*

with  $\text{BR}(B \rightarrow \rho^+\rho^0) \sim 18 \cdot 10^{-6}$



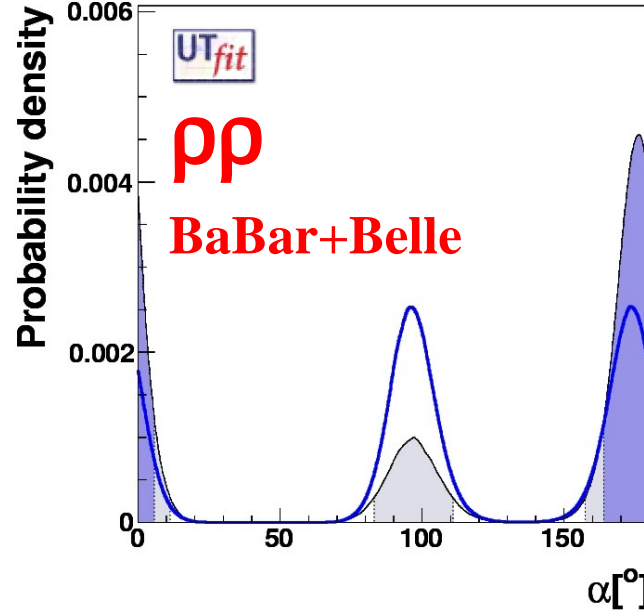
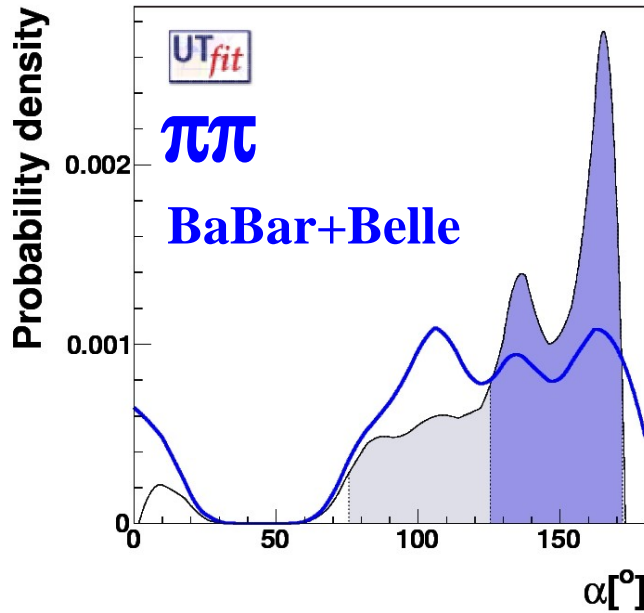
## Conclusions:

**$\alpha$  is still a land open for discussion even if the SM solution already reaches the  $10^0$  precision**

**I keep the conclusions short this time!**

# Back up slides

# $\alpha$ from isospin analysis (III): $\pi\pi$ and $\rho\rho$



$C_{\pi\pi}$  and  $S_{\pi\pi}$  equal to 0 are excluded

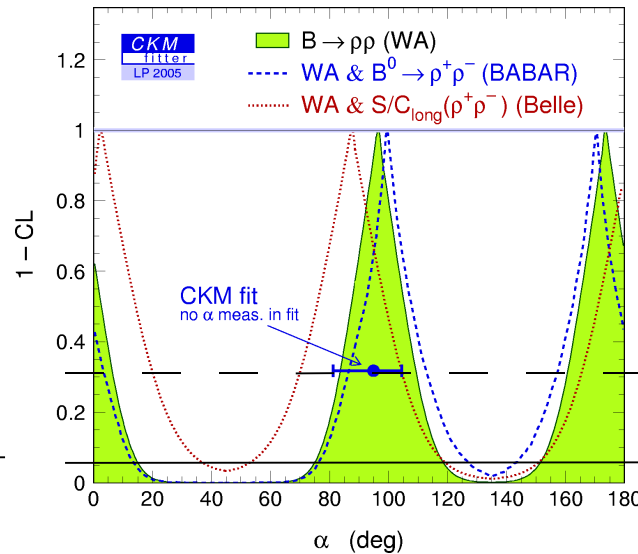
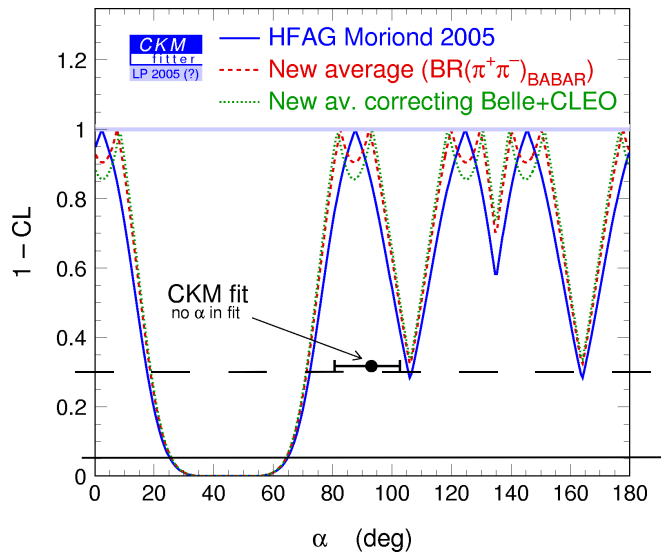
$$C_{\pi\pi} = -0.37 \pm 0.10$$

$$S_{\pi\pi} = -0.50 \pm 0.12$$

$$C_{\rho\rho} = -0.03 \pm 0.17$$

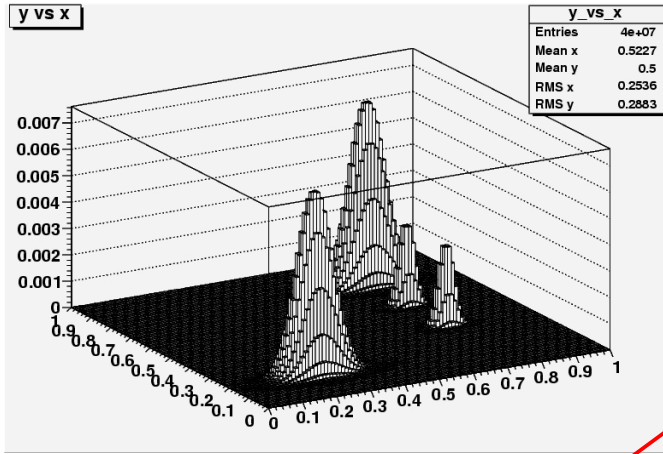
$$S_{\rho\rho} = -0.21 \pm 0.22$$

$C_{\rho\rho}$  and  $S_{\rho\rho}$  equal to 0 are preferred

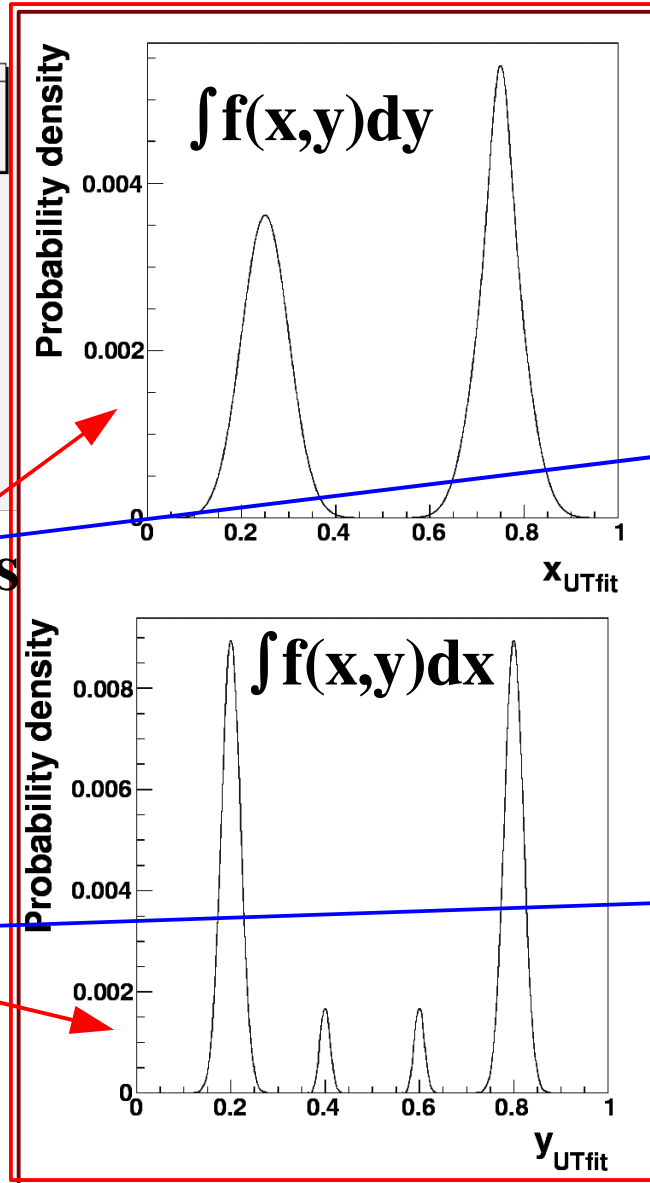


# $\alpha$ from isospin analysis (IV): toy

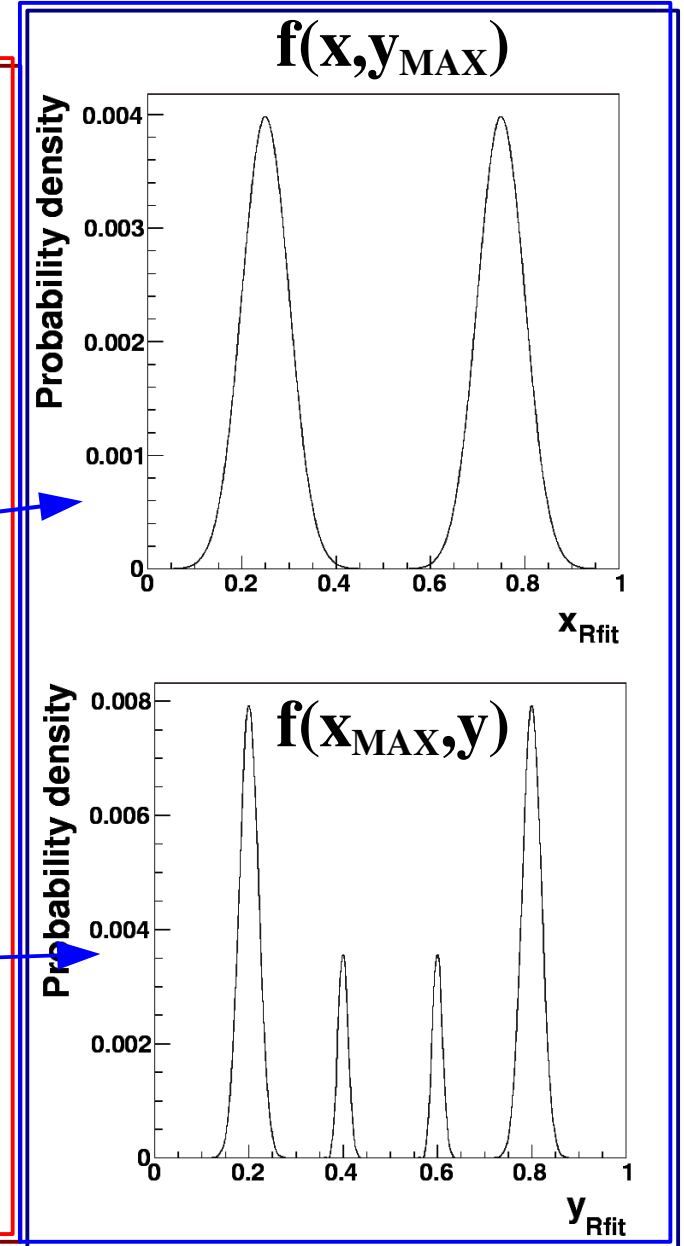
what does the difference in peak height mean?



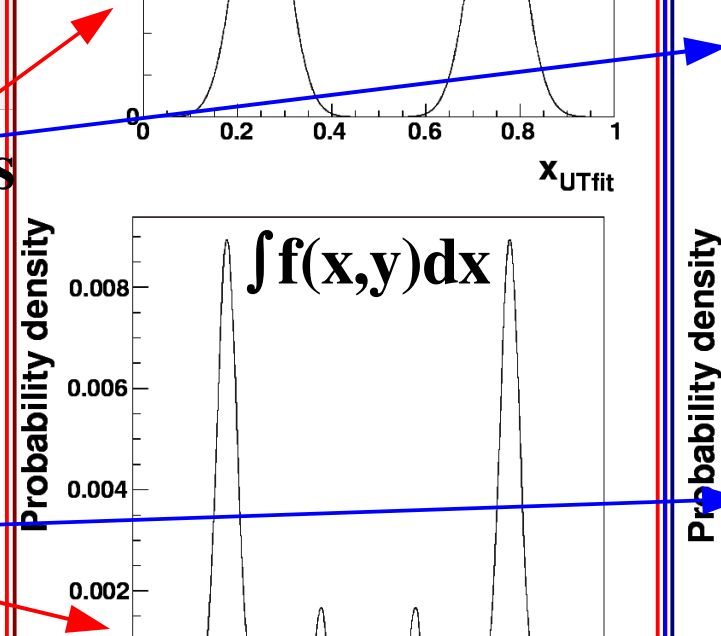
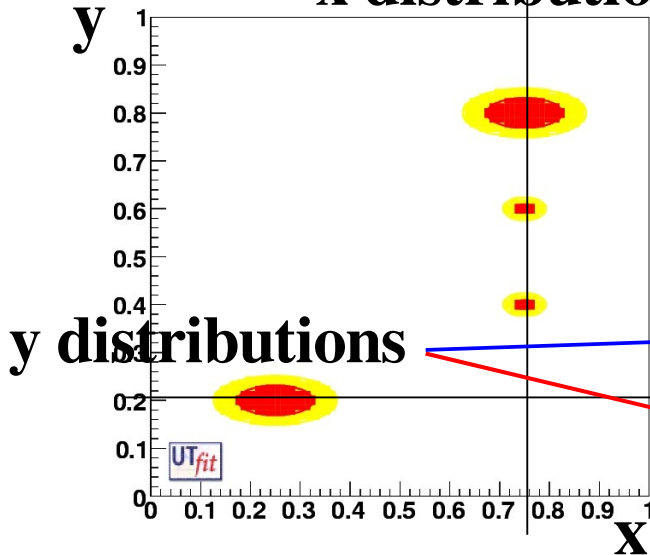
**UTfit**



**Rfit**

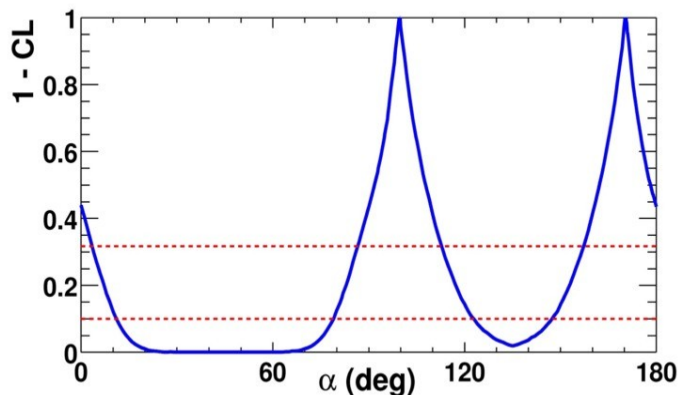


**x distributions**

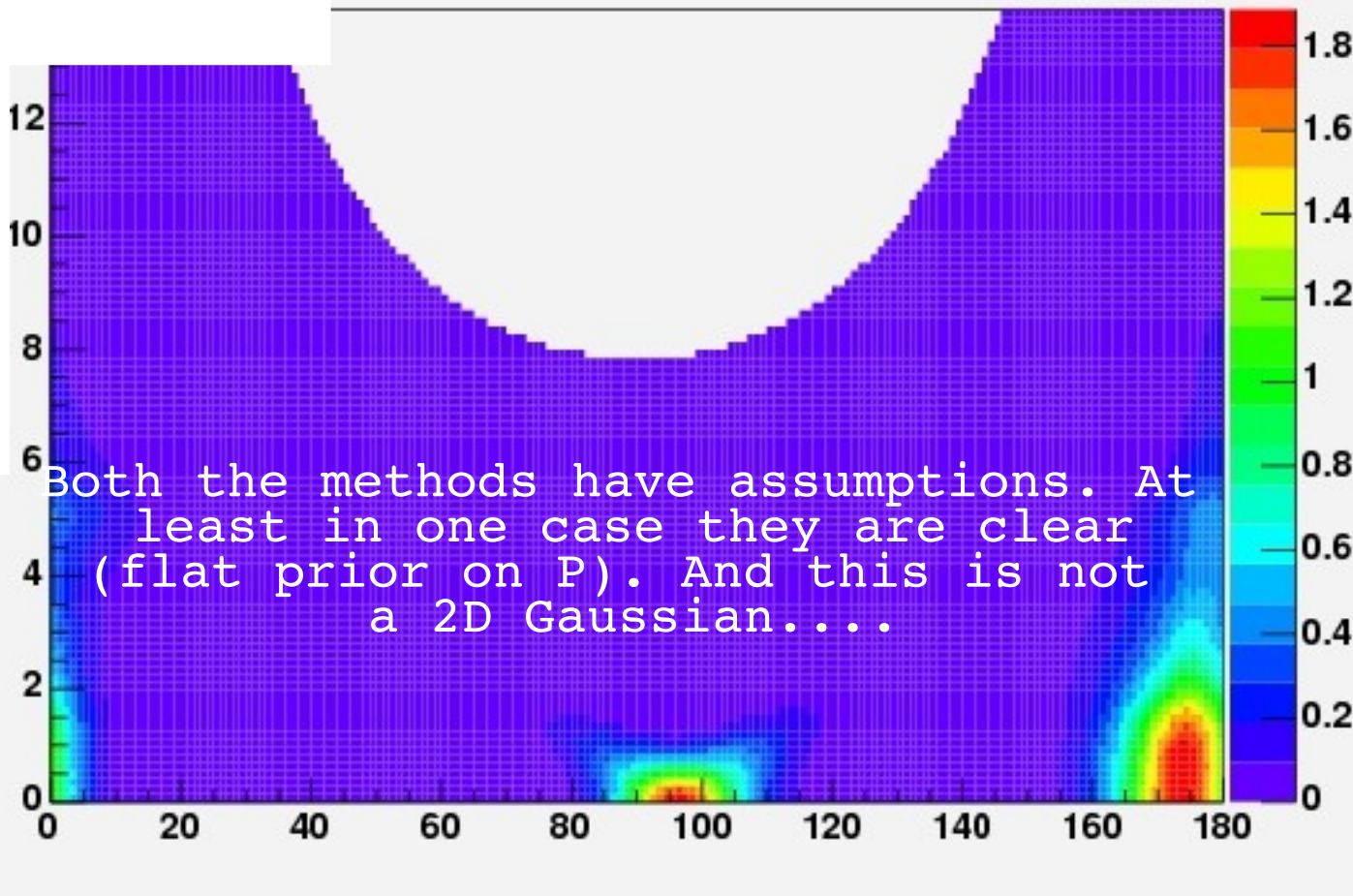
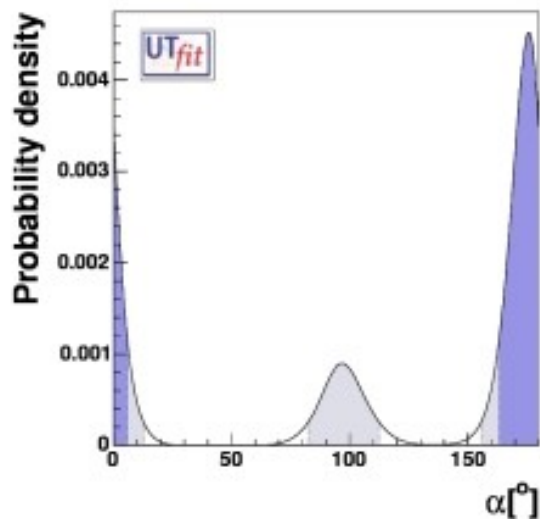


rho rho alpha vs P

Taking the maximum



Integrating



Both the methods have assumptions. At least in one case they are clear (flat prior on P). And this is not a 2D Gaussian....